



Parameterization of downward longwave radiation based on long-term baseline surface radiation measurements in China

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Abstract. Downward longwave radiation (DLR) affects energy exchange between the land surface and the atmosphere, and plays an important role in weather forecasting, agricultural activities, and the development of climate models. Because DLR is seldom observed at conventional radiation stations, numerous empirical parameterizations have been presented to estimate DLR from screen-level meteorological variables. The reliability and representativeness of parameterization depend on the coefficients regressed from the simultaneous observations of DLR and meteorological variables. Only a few previous studies have attempted to build parameterizations over regions in China such as the Tibetan Plateau and East China. In this study, a long-term (2011–2022) hourly dataset of DLR and meteorological elements, obtained from seven stations of the China Baseline Surface Radiation Network, was used to recalculate the coefficients of the Brunt and Weng models, and to develop a new model. Results showed that the mean bias error (MBE) and relative MBE (rMBE) between the measured clear-sky DLR and that estimated using the Brunt, Weng, and new models were -4.3 , -5.1 , and 3.7 W m^{-2} and -1.5% , -1.8% , and 1.3% , respectively. The root mean squared errors (RMSEs) were in the range of 13.8 – 14.3 W m^{-2} and the relative RMSEs (rRMSEs) were approximately 5.0% . The MBEs (rMBEs) of the Brunt, Weng, and new models under all-sky conditions were -2.8 W m^{-2} (-1.0%), -6.1 W m^{-2} (-2.1%), and -1.5 W m^{-2} (-0.5%), respectively. The RMSE (rRMSE) of the parameterization models in retrieving all-sky DLR was $\sim 17.5 \text{ W m}^{-2}$ ($\sim 6.1 \%$). Therefore, the models are considered suitable for retrieval of DLR over China.

1 Introduction

Downward longwave radiation (DLR) on the ground is one of the fluxes involved in the exchange of energy between Earth's surface and the atmosphere (Konzelmann et al., 1994; Gabathuler et al., 2001; Sridhar and Elliot, 2002). Consequently, DLR plays a vital role in weather forecasting, agricultural production (e.g., prediction of frost and crop temperature), climate



simulations, and water cycle modeling (Crawford and Duchon, 1999; Bilbao and De Miguel, 2007; Li et al., 2017; Liu et al., 2020).

In comparison with other radiation components, DLR is seldom observed at conventional radiation stations (Iziomon et al., 2003; Stephens et al., 2012). Therefore, considerable effort has been made to develop simple parameterization methods to calculate DLR from easily measured meteorological variables (Duarte et al., 2006). As identified by Ångström (1915), clear-sky DLR can be determined from the emissivity and effective temperature of the atmosphere. Under clear-sky conditions, as much as 60 % (90 %) of atmospheric emission is derived from the atmosphere within the first 100 m (1 km). When the sky is overcast, more than 90 % originates from within first 1-km layer between the ground and the bottom of the cloud (Ohmura, 2001). Following the pioneering work of Ångström, numerous investigators have presented empirical relationships between effective atmospheric emissivity (hereinafter refer to emissivity) under clear-sky conditions and meteorological elements such as vapor pressure (e) (Brunt, 1932; Weng et al., 1993; Niemelä et al., 2001), screen-level temperature (T_a) (Swinbank, 1963; Idso and Jackson, 1969), dewpoint temperature (T_d) (Berdahl and Fromberg, 1982), e and T_a (Brutsaert, 1975; Satterlund, 1979; Idso, 1981; Iziomon et al., 2003), and relative humidity (ϕ) and T_a (Carmona et al., 2014). Under all-sky conditions, the presence of cloud can increase emissivity and atmospheric radiation. Clouds generally consist of water vapor, water droplets, or ice crystals. They absorb thermal radiation very strongly and radiate similar to a black body in the infrared range (Heitor et al., 1991). Many studies have demonstrated that all-sky emissivity can be well predicted from clear-sky emissivity with correction for cloud effects (Crawford and Duchon, 1999; Bilbao and De Miguel, 2007; Wang and Liang, 2009; Alados, et al., 2012; Li et al., 2017; Liu et al., 2020).

Because the regression coefficients of empirical parameterization models exhibit spatial dependence (Goss and Brooks, 1956; Brutsaert, 1975; Marthews et al., 2012; Liu et al., 2020), they should be recalculated on the basis of observations over wider regions to ensure their accuracy and representativeness in estimating DLR. For instance, Wang and Liang (2009) assessed the performance of clear-sky DLR parameterization models presented by Brunt (1932) and Brutsaert (1975) at 36 global sites. However, owing to the shortage of high-quality DLR measurements in China, most previous works focused on retrieval of DLR over only a few regions, e.g., the Tibetan Plateau (Weng et al., 1993; Zhu et al., 2017; Liu et al., 2020) and East China (Wang and Liang, 2009). Therefore, these models might not represent optimal parameterizations suited to retrieval of DLR over other areas of China. Fortunately, the China Meteorological Administration has established the China Baseline Surface Radiation Network (CBSRN) in 2007 (Li et al., 2013), which currently comprises seven stations (Mohe, Xilinhot, Yanqi, Shangdianzi, Xuchang, Wenjiang, and Dali). Nine radiometric components including DLR are measured at 1-min intervals at CBSRN stations. The purpose of this study was to recalculate the coefficients of the Brunt (1932) model and the Weng (1993) model, and to develop a new parametric formula in terms of a long-term (2011–2022) hourly dataset obtained from the CBSRN stations. This study represents an advance in comparison with previous work in terms of the following aspects: 1) it not only recalculated the regression coefficients of the Brunt and Weng models, but also developed a new parametric formula suited to estimation of DLR over China; 2) the hourly cloud fraction (CF) measured by a HY-WP1A Intelligent Weather Observation System was incorporated to considerably improve the handling of cloud effects in DLR



65 retrieval under all-sky conditions; and 3) the spatial representativeness of the parameterization models over China was
improved through use of measurements from the seven CBSRN stations in China.

2 Site, instruments, and data

2.1 Site description

Figure 1 shows the geographical locations of the seven CBSRN stations: Mohe (MH; 52.97 °N, 122.52 °E; 438.5 m a.s.l.),
70 Xilinhot (XL; 44.13 °N, 116.33 °E; 1003.0 m a.s.l.), Yanqi (YQ; 42.05 °N, 86.61 °E; 1056.5 m a.s.l.), Shangdianzi (SDZ;
40.65 °N, 117.12 °E; 293.3 m a.s.l.), Xuchang (XC; 34.07 °N, 113.93 °E; 67.2 m a.s.l.), Wenjiang (WJ; 30.75 °N, 103.86 °E;
547.7 m a.s.l.), and Dali (DL; 25.71 °N, 100.18 °E; 1990.5 m a.s.l.). It can be seen from Table 1 that these stations are
distributed in seven representative climatic zones, i.e., the cold temperate zone (MH), middle temperate semiarid zone (XL),
middle temperate arid zone (YQ), warm temperature semihumid zone (SDZ), northern subtropical humid zone (XC), middle
75 subtropical humid zone (WJ), and subtropical humid zone (DL). Additionally, the elevation of three stations (i.e., XC, SDZ,
and MH) is <500 m a.s.l., one station (WJ) has medium elevation (547.7 m a.s.l.), and the other three stations (i.e., XL, YQ,
and DL) have elevation >1000 m a.s.l. (Table 1).

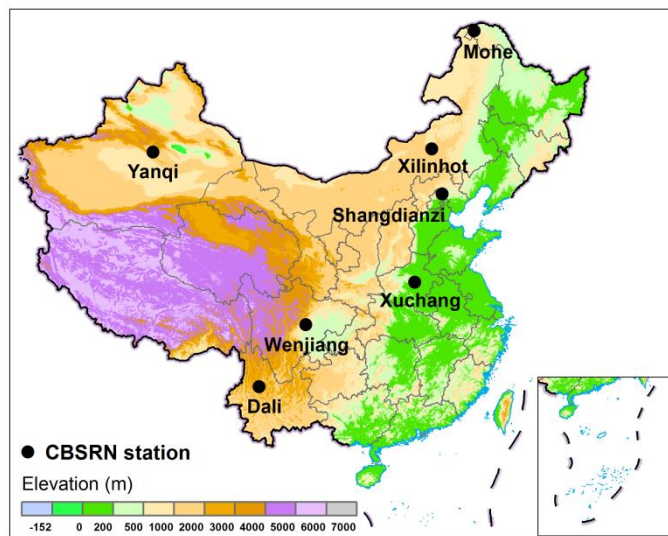


Figure 1. Geographical locations of seven CBSRN stations in China. Terrain data represent GTOP30 digital
elevation model (<ftp://edcftp.cr.usgs.gov/data/gtopo30/global/>).

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Table 1. Basic descriptions of CBSRN stations in China.

Station name	Station ID	Latitude(° N)	Longitude(° E)	Altitude(m)	Climatic zones
Mohe	50136	52.97	122.52	438.5	Cold temperate zone
Xilinhot	54102	44.13	116.33	1107.0	Middle temperate semiarid zone
Yanqi	51567	42.05	86.61	1056.5	Middle temperate arid zone
Shangdianzi	54421	40.65	117.12	293.3	Warm temperate semihumid zone
Xuchang	57089	34.07	113.93	67.2	Northern subtropical humid zone
Wenjiang	56187	30.75	103.86	547.7	Middle subtropical humid zone
Dali	56751	25.71	100.18	1990.5	Subtropical humid zone

2.2 Instruments and data

The CBSRN stations use IR02 pyrgeometers (Huksflux, the Netherlands) to measure DLR. The spectral range of the IR02 instrument is 4.5–42 μm , which covers most of spectral range of atmospheric longwave radiation, making it a suitable instrument for measuring DLR in most cases. Moreover, to avoid influencing from solar radiation, the IR02 is shaded by a ball mounted on a FS-ST22 automatic solar tracker (Jiangsu Radio Science Research Institute Co. Ltd., China) during observation. Its temperature dependence is within $\pm 3\%$ (-10 to $40\text{ }^\circ\text{C}$), and a ventilation/heating system is installed to reduce the influence of environmental temperature and to prevent dew/dust fall on its window. Note that the field of view (FOV) of the IR02 instrument is 150° rather than the desired 180° , which means its price is attractive, while the accuracy loss is relatively minor (Hukseflux, 2022). The IR02 sampling frequency is 1 Hz and the 1-min averaged data are stored using a WUSH-BR data logger (Jiangsu Radio Science Research Institute Co. Ltd., China). The IR02 pyrgeometers are carefully maintained and regularly calibrated by the manufactures to guarantee that the observations meet the standards specified by the China National Centre for Meteorological Metrology (Huo et al., 2017).

A fisheye camera, mounted on top of the HY-WP1A Intelligent Weather Observation System (Huayun Sounding Meteorological Technology Inc., China), is used to automatically record CF data. Full-sky photographs with a FOV of 180° are acquired at 1-min intervals. The photographs are then processed using artificial intelligence image detecting technology to yield hourly CF data with uncertain $<10\%$ (Hua et al., 2021).

Meteorological elements (i.e., T_a , e , and ϕ) are observed by an automatic weather station (AWS) at 1-min intervals and the data are stored using a HY3000 data logger (Huayun Sounding Meteorological Technology Inc., China).

The data used in this study, which were downloaded from the China Meteorological Administration Data Service (<http://idata.cma/cmadaas/>), undergo strictly quality controlled by meteorological experts and trained engineers of the National Meteorological Information Centre of China. Note that the DLR data measured by the IR02 instruments at high-elevation stations (i.e., MH and YQ) under extremely dry and cold synoptic conditions, in which irrational DLR



110 measurements might be produced due to the high temperature dependency of the IR02 pyrgeometer (Hukseflux, 2022), were not involved in this study.

3 Methods

3.1 Emissivity calculation

Effective atmospheric emissivity (ϵ) is defined as the ratio of incoming long-wave radiation to blackbody radiation at screen-level air temperature (Monteith, 1961; Rodgers, 1967; Prata, 1996):

$$115 \quad \epsilon = \frac{\text{DLR}}{\sigma T_a^4}, \quad (1)$$

where DLR is the downward hemispheric longwave irradiance (W m^{-2}) at the ground, which can be observed directly by a pyrgeometer; T_a is the screen air temperature (K) measured by the AWS; and σ is the Stefan–Boltzmann constant ($5.6697 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$).

3.2 Statistical methods

120 This study used the nonlinear curve fitting method, orthogonal distance regression (ODR) iteration algorithm and Levenberg–Marquardt iteration algorithm to regress the coefficients of the parameterization models. Parameterizations were assessed by means of statistical parameters such as mean bias error (MBE), relative MBE (rMBE), root mean squared error (RMSE), relative RMSE (rRMSE), and the correlation coefficient (r). The MBE is an indicator adopted to denote whether predictions from the parameterization are overestimates (positive values) or underestimates (negative values) in comparison
125 with the measurements. The RMSE accounts for the average magnitude of the errors but it does not provide an indication of the direction of the errors. The correlation coefficient r reflects the linear agreement between the observed parameter and the estimated variable (Gubler et al., 2012; Zhou et al., 2021).

4 Results

4.1 Clear-sky emissivity parameterization

130 In this study, the coefficients of the Brunt model and the Weng model were calibrated using the nonlinear curve fitting method with 12,368 clear-sky hourly data pairs (DLR and e) observed at seven CBSRN stations between January 2011 and December 2017. Note that both the Brunt model and the Weng model are single-parameter parameterization models because only one parameter (e) is adopted as input in these models. The Brunt model is a power function of e with an exponent of 1/2, whereas the Weng model is a natural logarithm function of e . A two-parameter model such as the Brutsaert (1975) model, in
135 which e and T_a are both used as input parameters, is recognized to be more reasonable than a single-parameter model in terms of the physical mechanism, especially under warm and wet conditions (Culf and Gash, 1993; Prata, 1996). In this



study, we developed a two-parameter parametric formula (hereinafter refer to the parametric formula) that is similar to the Brutsaert model except the exponent of the function is set to 1/3 rather than 1/7. The coefficients of the parametric formulae were computed on the basis of the clear-sky hourly dataset (DLR, e , and T_a) using the nonlinear curve fitting method together with the ODR iteration algorithm.

The formulae of the parameterization models for retrieving clear-sky emissivity can be expressed as follows:

$$\epsilon_{clr,B} = 0.599 + 0.053\sqrt{e}, \quad (2)$$

$$\epsilon_{clr,W} = 0.590 + 0.075\ln(1+e), \quad (3)$$

$$\epsilon_{clr,Y} = 0.532 + 0.808\sqrt[3]{e/T_a}, \quad (4)$$

where $\epsilon_{clr,B}$, $\epsilon_{clr,W}$, and $\epsilon_{clr,Y}$ represent the clear-sky emissivity retrieved from the Brunt model, Weng model, and new model developed in this study, respectively, e (hPa) is vapor pressure, and T_a (K) is screen-level air temperature. The coefficients of determination (R^2) of Eqs. (2)–(4) were 0.999, 0.999, and 0.930, respectively.

The Brunt model (denoted by the black thick curve in Fig. 2a) can well fit all data pairs under most cases ($0 < e \leq 45$ hPa), especially those data pairs observed at low-elevation (<1000 m) stations such as XC (67.2 m a.s.l.) and SDZ (293.3 m a.s.l.), whereas the Weng model (denoted by the red thick curve in Fig. 2a) appears to fit the data pairs better than the Brunt model under dry conditions ($e \leq 17.5$ hPa). Note that the Weng model was proposed in terms of radiation data observed over the Tibetan Plateau, where the atmospheric vapor pressure is lower than that in other regions in China. Therefore, it can be inferred that the Weng model is suitable for estimating clear-sky emissivity over arid regions. The parametric formula developed in this study (denoted by the red thick curve in Fig. 2b) fitted the data pairs reasonably and was considered to have basis in physics because it uses both e and T_a as input.

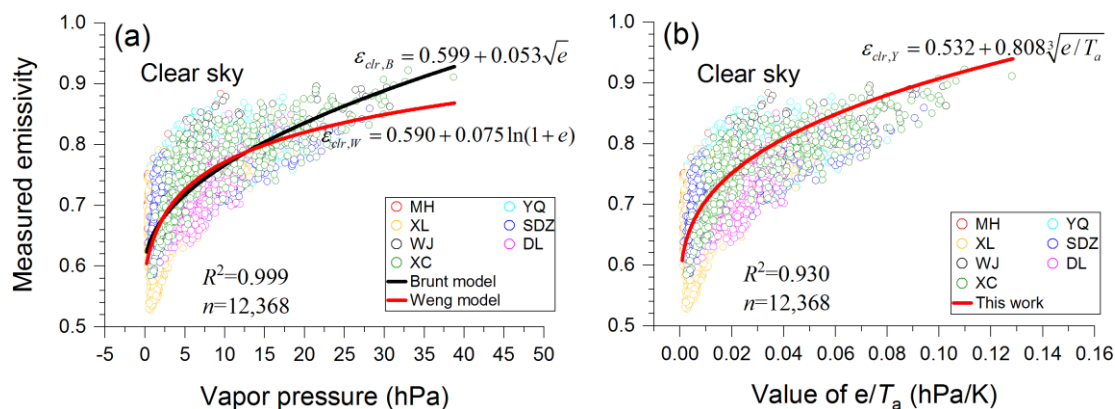


Figure 2. Scatter plots of measured clear-sky emissivity versus coincident measurements of (a) vapor pressure and (b) the ratio of vapor pressure to screen-level air temperature. Circles represent data pairs observed at seven CBSRN stations. Black and red thick curves in (a) denote the Brunt model (Eq. 2) and the Weng model (Eq. 3), respectively. Red thick curve in (b) denotes the parametric formula developed in this study (Eq. 4).



The values of coefficients a and b of the well-known Brunt model reported by previous authors as well as those derived in this study are listed in Table 2. The values of coefficients a (0.599) and b (0.053) derived in this study are in consistent with those presented both by Li et al. (2017) and by Wang and Liang (2009), but differ from those provided by other investigators. Discrepancies in the coefficients might result from different atmospheric conditions (e.g., water vapor content, CF, and temperature profiles) and the temporal resolution (hourly, daily, or monthly) of the data used in establishing the parameterization models. The greater the values of coefficient b , the larger the dependences of the parameterization formula on water vapor (Iziomon et al., 2003). Note that the value of coefficients b was > 0.05 in the Brunt model, Monteith (1961) model, Iziomon model, Berdahl and Martin (1984) model, Li model, and the model developed in this study, which means that these models have greater sensitivity to water vapor in comparison with other models.

Table 2. Coefficients of the Brunt model reported by previous investigators as well as those derived in this study. The temporal resolution of the data used to derive the coefficients and the details of network/sites at which the observations were performed are also listed.

Reference	Network/Site	Number of Sites	Elevation(m)	a	b	Resolution	Country
Brunt [1932]	Benson	1	6	0.520	0.065	Monthly	UK
Anderson [1954]	Laker Hefner	1	369	0.680	0.036	Monthly	USA
Goss and Brooks [1956]	Davis	1	14	0.660	0.039	Monthly	USA
DeCoster and Schuepp [1957]	Kinshasa	1	321	0.645	0.048	Daily	Zaire
Monteith [1961]	Kew	1	-	0.530	0.065	Hourly	England
Swinbank [1963]	Aspendale, Kerang	2	-	0.640	0.037	Hourly	Australia
Berger et al. [1984]	Carpentras	1	-	0.660	0.040	Hourly	France
Berdahl and Martin [1984]	Tucson, Gaithersburg, San Antonio, Boulder St. Louis, West palm beach	6	-	0.564	0.059	Hourly	USA
Heitor et al. [1991]	Sacavem	1	-	0.590	0.044	Hourly	Portugal
Iziomon et al.[2003]	Bremgarten, Feldberg	2	212, 1489	0.600	0.064	Hourly	Germany
Wang and Liang [2009]	SURFRAD AsiaFlux FLUXNET AmeriFlux GAME AAN	36	98–4700	0.605	0.048	Hourly	USA Indonesia Japan China Thailand Australia Botswana Canada Germany
Li et al. [2017]	SURFRAD	7	98–1689	0.598	0.057	Hourly	USA
Liu et al. [2020]	Naqu, Nyingchi, Ali	3	2290–4507	0.560	0.070	Minute	China



This work	CBSRN	7	67–1991	0.599	0.053	Hourly	China
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4.2 All-sky emissivity parameterization

All-sky emissivity can be derived from clear-sky emissivity with correction for clouds and other meteorological elements. In this study, the parameterizations of all-sky emissivity were derived using the dataset of observations recorded at seven CBSRN stations between January 2011 and December 2020. The dataset comprises 71,204 hourly measurements of DLR, e ,
185 T_a , CF, and ϕ under all-sky conditions. The formulae derived for all-sky emissivity are as follows:

$$\varepsilon_{all,B} = \varepsilon_{clr,B}(1 - 0.178CF^{0.339}) + 0.075CF^{0.395}\phi^{0.253}, \quad (5)$$

$$\varepsilon_{all,W} = \varepsilon_{clr,W}(1 + 0.186CF^{0.499}) - 0.298CF^{0.424}\phi^{-0.360}, \quad (6)$$

$$\varepsilon_{all,Y} = \varepsilon_{clr,Y}(1 - 0.201CF^{0.796}) + 0.088CF^{1.038}\phi^{0.221}. \quad (7)$$

where $\varepsilon_{all,B}$, $\varepsilon_{all,W}$, and $\varepsilon_{all,Y}$ represent all-sky emissivity; $\varepsilon_{clr,B}$, $\varepsilon_{clr,W}$, and $\varepsilon_{clr,Y}$ are clear-sky emissivity calculated using Eqs.
190 (2)–(4), respectively; CF is the cloud fraction (0–1); ϕ is relative humidity (%); and the coefficients of determination for Eqs. (5)–(7) are 0.745, 0.748, and 0.750, respectively.

4.3 Emissivity validation

To verify the clear-sky emissivity parameterization models (Eqs. (2)–(4)) defined in section 4.1, this study used an independent clear-sky dataset comprising 1,706 hourly clear-sky measurements of DLR, e , and T_a at four CBSRN stations
195 (YQ, XL, SDZ, and XC) acquired between January 2018 and July 2021. The MBEs (rMBEs) between the measured clear-sky emissivity and that estimated by the Brunt model, the Weng model, and model developed in this study were -0.013 (-1.8%), -0.015 (-2.1%), and 0.007 (1.0%), respectively (Fig. 3a–c). The small positive MBE of the model developed in this study might be attributable to the fact that two parameters (e and T_a) are involved in the equation. Meanwhile, all models yielded analogous RMSEs (~ 0.039) and rRMSEs ($\sim 5.3\%$), which might be a reflection of the dataset and selected
200 independent variables used to establish the formulae. For example, the effects of CO_2 , O_3 , and aerosols on emissivity were not considered in these formulae (Staley and Jurica, 1972; Kjaersgaard et al., 2007; Gubler et al., 2012).

The parameterization models used to estimate all-sky emissivity (Eqs. (5)–(7)) were validated on the basis of an independent dataset comprising 20,970 hourly all-sky measurements (DLR, e , T_a , CF, and ϕ) acquired at three CBSRN
205 stations (XL, SDZ, XC) between January 2021 and April 2022. The MBEs (rMBEs) between the measured all-sky emissivity and that calculated by the Brunt model, the Weng model, and model developed in this study were -0.006 (-0.8%), -0.017 (-2.2%), and -0.004 (-0.5%), respectively (Fig. 3d–f). Note that the MBEs (rMBEs) of the all-sky emissivity were close to or even less than those of the clear-sky emissivity. One possible reason is that more samples (20,970) were adopted in verifying the all-sky emissivity than were adopted in validating the clear-sky emissivity (i.e., 1,706). Another reason is that more input parameters (e.g., CF and RH) other than e and T_a were included in the all-sky emissivity



210 formulae, which alleviated the abrupt variations of e or T_a . However, the RMSE of the all-sky emissivity parameterization model was ~ 0.049 , which is higher than that (~ 0.039) of the clear-sky emissivity model.

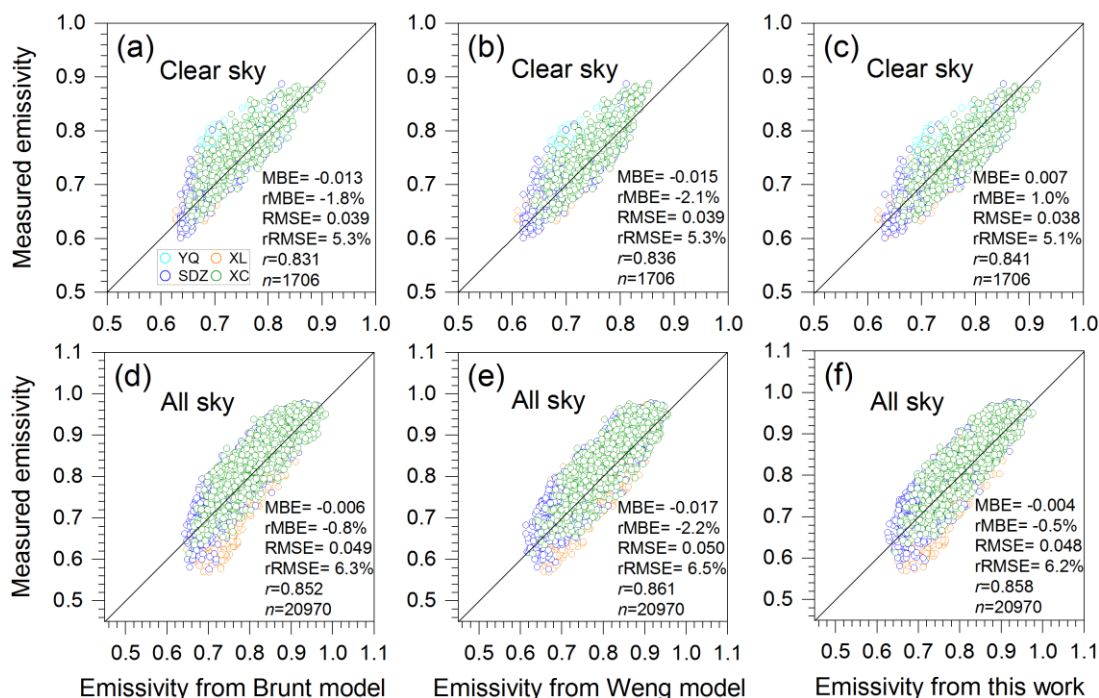


Figure 3. Measurements versus calculations of effective atmospheric emissivity by the Brunt model, the Weng model, and the model developed in this study for (a)–(c) clear-sky and (d)–(f) all-sky conditions. Black lines denote the 1:1 line.

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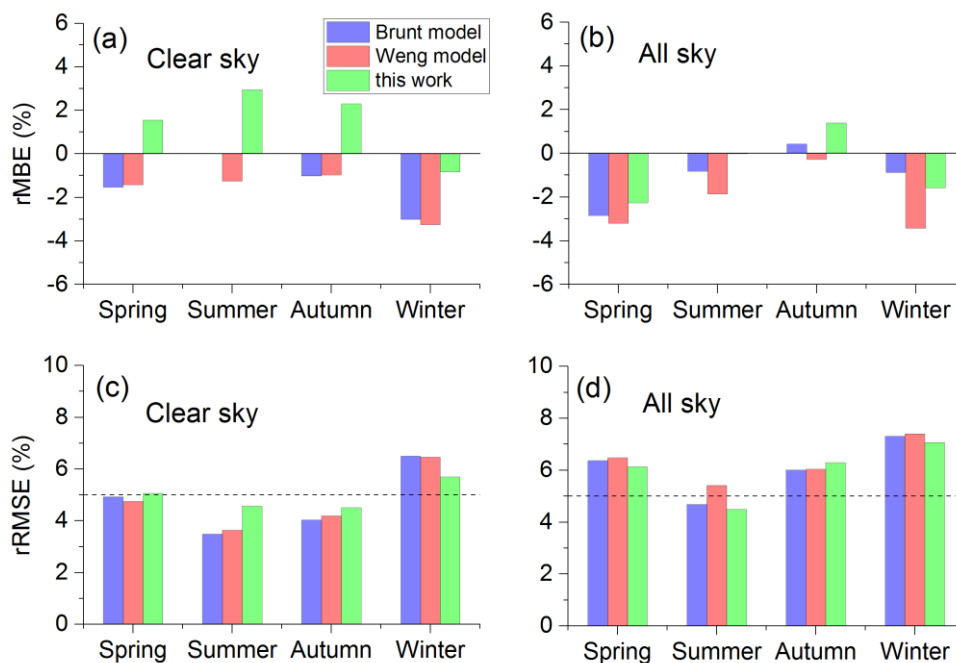
To illustrate the performance of each of the parameterization models in estimating both clear- and all-sky emissivity in different seasons, several statistics are summarized in Table 3 and plotted in Fig. 4. The model developed in this study can overestimate clear-sky emissivity in all seasons except winter (with rRMBE of -1.1%), whereas, both the Brunt model and the Weng model can underestimate clear-sky emissivity in all seasons (Fig. 4a). The influence of involving T_a in the model would be more noteworthy during summer and winter because T_a reaches its maximum and minimum value in these seasons, respectively. Furthermore, all parametrization models exhibited apparent negative rMBEs in winter, unlike in other seasons. In winter, the CO_2 content over China usually reaches its annual maximum (Fang et al., 2014). Therefore, underestimation of clear-sky emissivity using parameterization models would be greater in winter owing to the effect of neglecting CO_2 in the models. Under all-sky conditions, the rMBEs of the parameterization models were negative in all seasons, except for the Brunt model (rMBE of 0.6%) and the model developed in this study (rMBE of 1.5%) in autumn (Figure 4b).

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For clear-sky emissivity (Fig. 4c), the rRMSEs between the measurements and the estimations of three models were $\sim 5\%$ in spring (March–May), summer (June–August), and autumn (September–November), but $>5.7\%$ in winter (December–



February). For all-sky emissivity, the rRMSEs between the measurements and the estimations of three models were closer with values of ~6.5 %, ~5.0 %, ~6.3 %, and ~7.4 % in spring, summer, autumn, and winter, respectively (Fig. 4d, Table 3).



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Figure 4. Seasonal statistics of rMBEs for three parameterization models (a) under clear-sky conditions and (b) under all-sky conditions; the corresponding rRMSEs for three models (c) under clear-sky conditions and (d) under all-sky conditions. Dashed line denotes the rRMSE value of 5 %.

Table 3. Comparison between the measured emissivity and those estimated using three models in four seasons under clear- and all-sky conditions.

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Season	Sky condition	Model	MBE	rMBE (%)	RMSE	rRMSE (%)	<i>r</i>	Sample number
Spring	Clear sky	Brunt	-0.012	-1.7	0.038	5.1	0.762	445
		Weng	-0.012	-1.5	0.037	4.9	0.772	
		This work	0.011	1.4	0.038	5.0	0.772	
	All sky	Brunt	-0.022	-2.8	0.051	6.5	0.815	4389
		Weng	-0.025	-3.2	0.052	6.6	0.819	
		This work	-0.018	-2.3	0.049	6.3	0.816	
Summer	Clear sky	Brunt	-0.001	-0.1	0.029	3.6	0.769	254
		Weng	-0.011	-1.3	0.030	3.7	0.750	
		This work	0.023	2.9	0.037	4.6	0.769	
	All sky	Brunt	-0.007	-0.9	0.041	4.8	0.810	5036
		Weng	-0.016	-1.9	0.047	5.5	0.763	
		This work	0.000	-0.1	0.040	4.6	0.822	
Autumn	Clear sky	Brunt	-0.008	-1.1	0.032	4.2	0.841	369
		Weng	-0.008	-1.0	0.033	4.3	0.841	
		This work	0.017	2.2	0.035	4.5	0.848	



	All sky	Brunt	0.005	0.6	0.049	6.3	0.873	5106
		Weng	-0.001	-0.2	0.048	6.1	0.886	
		This work	0.012	1.5	0.050	6.5	0.878	
Winter	Clear sky	Brunt	-0.022	-3.1	0.047	6.6	0.670	638
		Weng	-0.024	-3.5	0.047	6.6	0.688	
		This work	-0.007	-1.1	0.040	5.7	0.695	
	All sky	Brunt	-0.003	-0.5	0.054	7.6	0.592	6439
		Weng	-0.024	-3.4	0.054	7.5	0.709	
		This work	-0.010	-1.4	0.052	7.2	0.657	

4.4 DLR validation

Based on the Eq. (1), DLR can be calculated in terms of the measurements of screen-level temperature and the corresponding emissivity estimated using the parameterization models. Statistical results (Table 3) indicated that the MBEs (rMBEs) between the measured clear-sky DLR and that estimated using the Brunt model, the Weng model, and model developed in this study were -4.3 W m^{-2} (-1.5%), -5.1 W m^{-2} (-1.8%), and 3.7 W m^{-2} (1.3%), respectively (Fig. 5a–c). The RMSE (rRMSE) of both the Brunt model and the Weng model was 13.8 W m^{-2} (4.9%), i.e., slightly lower than that of the model developed in this study (RMSE: 14.3 W m^{-2} , rRMSE: 5.1%).

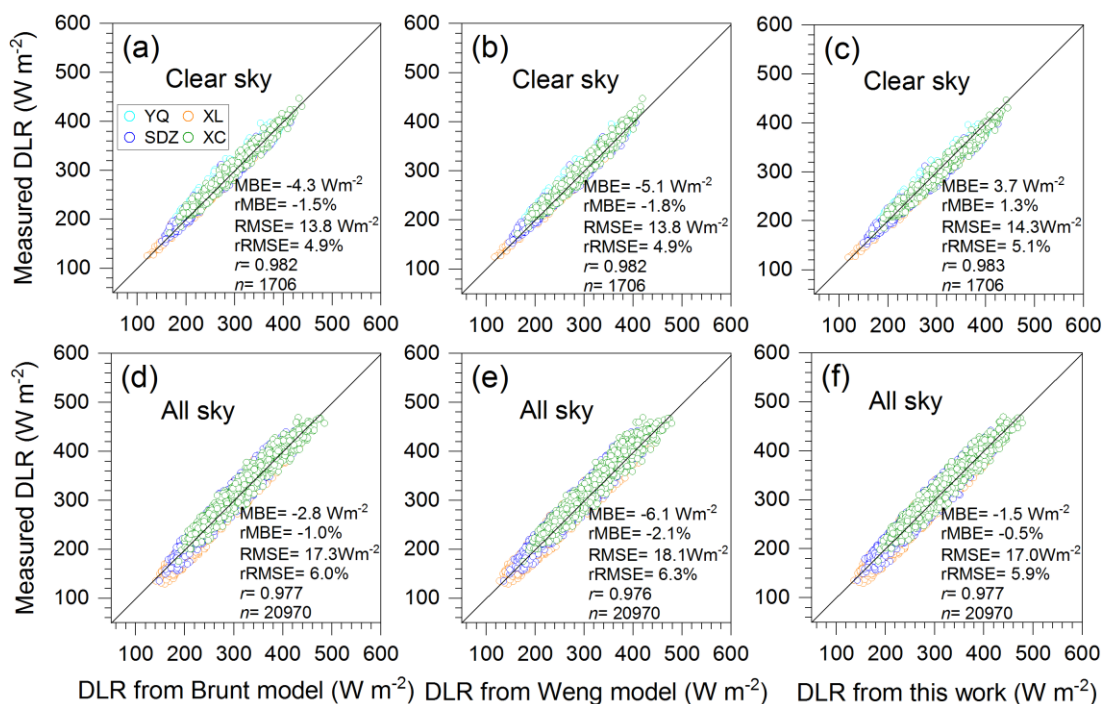


Figure 5. Same as Fig. 3 except for the DLR.

Under all-sky conditions, the MBEs (rMBEs) of the Brunt model, the Weng model, and parametric formula developed in this study were -2.8 W m^{-2} (-1.0%), -6.1 W m^{-2} (-2.1%), and -1.5 W m^{-2} (-0.5%), respectively (Fig. 5d–f). The



RMSEs (rRMSEs) between the measured all-sky DLR and that retrieved using the Brunt model, the Weng model, and model developed in this study were 17.3 W m^{-2} (6.0 %), 18.1 W m^{-2} (6.3 %), and 17.0 W m^{-2} (5.9 %), respectively. It can be seen that the RMSE (rRMSE) of the all-sky DLR retrieved from the parameterization models was $\sim 3.5 \text{ W m}^{-2}$ (1.0 %) greater than that of the clear-sky DLR retrieval. Occurrence of clouds and wider ranges of temperature and humidity under all-sky conditions would disperse the relationship between the observations and the predictions of DLR.

It can be seen from Table 4 that both the Brunt model and the Weng model could underestimate clear-sky DLR in all seasons (MBEs in the range of -7.1 to 0.0 W m^{-2}), while the model developed in this study could overestimate clear-sky DLR in all seasons except winter (MBE of -1.8 W m^{-2}). Additionally, all models could underestimate all-sky DLR (MBEs in the range of -9.4 to -0.1 W m^{-2}) in all cases, except the Brunt model and the model developed in this study could overestimate all-sky DLR in autumn (MBE of 1.2 and 4.0 W m^{-2} , respectively). The RMSEs (rRMSEs) of clear-sky DLR estimated by the parameterization models were approximately 14.8 W m^{-2} (5.0 %), 14.4 W m^{-2} (4.0 %), 13.0 W m^{-2} (4.2 %), and 13.6 W m^{-2} (6.2 %) in spring, summer, autumn, and winter, respectively; the counterparts of all-sky DLR were approximately 18.6 W m^{-2} (6.3 %), 18.4 W m^{-2} (4.9 %), 17.7 W m^{-2} (6.1 %), and 15.6 W m^{-2} (7.3 %) in spring, summer, and winter, respectively.

Table 4. Comparison between the measured DLR and those estimated using three models in four seasons under clear- and all-sky conditions.

Season	Sky condition	Model	MBE (Wm^{-2})	rMBE (%)	RMSE (Wm^{-2})	rRMSE (%)	<i>r</i>	Sample number
Spring	Clear sky	Brunt	-4.6	-1.5	14.8	4.9	0.954	445
		Weng	-4.3	-1.4	14.3	4.8	0.956	
		This work	4.7	1.6	15.2	5.1	0.955	
	All sky	Brunt	-8.3	-2.8	18.7	6.4	0.948	4389
		Weng	-9.4	-3.2	19.1	6.5	0.948	
		This work	-6.6	-2.3	18.0	6.1	0.947	
Summer	Clear sky	Brunt	-0.0	-0.0	12.9	3.5	0.921	254
		Weng	-4.6	-1.3	13.5	3.6	0.913	
		This work	10.9	2.9	16.9	4.6	0.919	
	All sky	Brunt	-3.1	-0.8	17.8	4.7	0.922	5036
		Weng	-7.0	-1.9	20.5	5.4	0.902	
		This work	-0.1	-0.0	17.0	4.5	0.924	
Autumn	Clear sky	Brunt	-3.1	-1.0	12.4	4.0	0.966	369
		Weng	-3.0	-1.0	12.9	4.2	0.963	
		This work	7.1	2.3	13.9	4.5	0.967	
	All sky	Brunt	1.2	0.4	17.4	6.0	0.965	5106
		Weng	-0.8	-0.3	17.5	6.0	0.965	
		This work	4.0	1.4	18.2	6.3	0.963	
Winter	Clear sky	Brunt	-6.6	-3.0	14.2	6.5	0.940	638
		Weng	-7.1	-3.3	14.2	6.5	0.946	
		This work	-1.8	-0.8	12.5	5.7	0.947	
	All sky	Brunt	-1.9	-0.9	15.7	7.3	0.941	6439



Weng	-7.4	-3.4	15.9	7.4	0.947
This work	-3.4	-1.6	15.2	7.1	0.942

5 Discussion and conclusions

To date, several empirical parameterization models to derive DLR from near-surface meteorological elements have been developed on the basis of field observations obtained at a few sites in China. In this study, we utilized a long-term dataset of hourly observations from seven CBSRN stations to recalculate the coefficients of the Brunt model, the Weng model, and a new parameterization model to estimate atmospheric effective emissivity and DLR under clear-sky and all-sky conditions. The main conclusions of this study are as follows.

Generally, three parameterization models can reliably estimate emissivity and DLR under clear- and all-sky conditions, i.e., the MBEs between the measured clear-sky DLR and that estimated using the Brunt model, the Weng model, and new model developed in this study were -4.3 , -5.1 , and 3.7 W m^{-2} , respectively; for all-sky DLR, the corresponding MBEs were -2.8 , -6.1 , and -1.5 W m^{-2} , respectively.

On the basis of the long-term (2011–2022) hourly data measured at the seven CBSRN stations adopted in this study, it is reasonable to suggest that the parameterization models considered in this study have reasonable spatial representation and robustness.

This study used continuous hourly CF observations from the HY-WP1A, which remarkably improved the consideration of cloud effects on estimations of emissivity and DLR. For example, CF data with high temporal resolution can improve accuracy in estimating emissivity and DLR, and provide the opportunity to study diurnal variations in DLR.

In spite of seven CBSRN stations located in various representative regions in China were adopted in this study, however, more CBSRN stations in China are still expected to establish to improve the spatial homogeneity of the parameterization models. On the other hand, the IR02 pyrgeometers currently used at the CBSRN stations should be replaced with more precise instruments such as the CGR4 pyrgeometer. The IR02 was found usually to produce irrational positive records of DLR under extreme cold and dry synoptic conditions, which might be caused by its large temperature dependency (within $\pm 3\%$ under -10 to $40 \text{ }^\circ\text{C}$).

Though the dominant emitter of longwave radiation in the atmosphere is water vapor, other gases (e.g., CO_2 and O_3) and aerosols also emit longwave radiation. The effects of gases and aerosols on DLR, whereas, are not considered sufficiently in the parameterization models. It is expected that the influences of atmospheric components on the relationships between clear-sky emissivity and screen-level meteorological variables will be further explored by means of the comprehensive observations at Global Atmosphere Watch station such as SDZ.

Data availability. The data used in this study can be provided by the corresponding author upon reasonable request.



Author contributions. JH and QC contributed to shaping the ideas and presenting research goal and constructive comments on the research. JY and WQ presented the construction of the paper. JY contributed to processing and analysis of the data as well as preparing the manuscript. WQ contributed the ideas, organized the research, performed the review, edited the manuscript, and provided the funding acquisitions.

Competing interests. The authors declare that they have no conflict of interest.

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