

SECTION S1: Temperature profiles

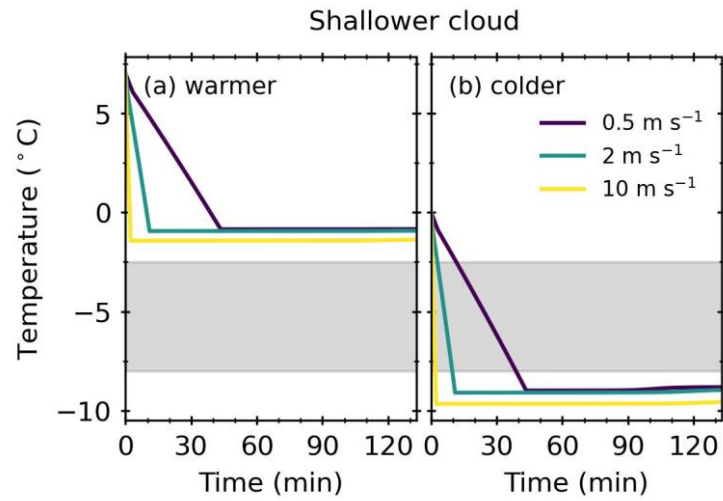


Figure S1 Temperature profiles of a shallower (1.3 km deep) cloud. Warmer refers to cloud base temperatures of 7 °C, and colder refers to cloud base temperatures of 0 °C. The grey shaded regions indicate the temperature region in which rime-splintering could be active.

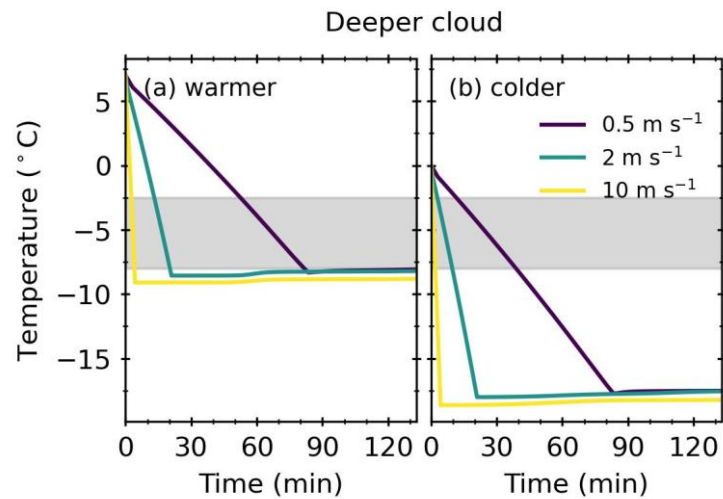


Figure S2 Temperature profiles of a deeper (2.4 km) cloud. Warmer refers to cloud base temperatures of 7 °C, and colder refers to cloud base temperatures of 0 °C. The grey shaded regions indicate the temperature region in which rime-splintering could be active.

SECTION S2: Additional figures for shallower clouds with a natural aerosol size distribution

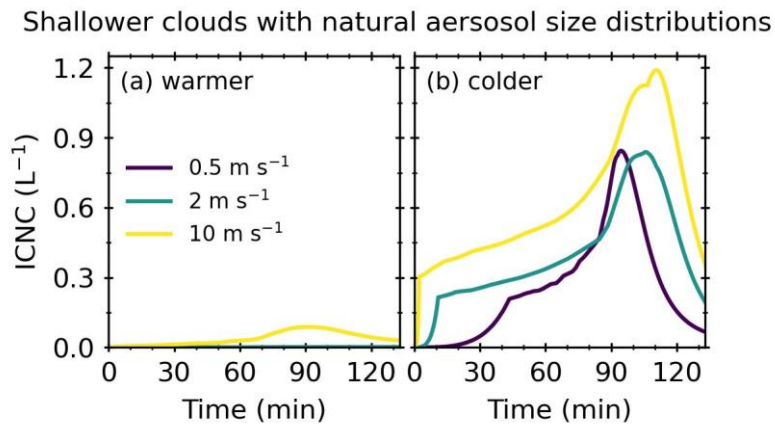


Figure S3 Control simulation ice crystal number concentrations for shallower clouds (1.3 km deep) with a natural aerosol size distribution. Warmer refers to cloud base temperatures of 7 °C, and colder refers to cloud base temperatures of 0 °C.

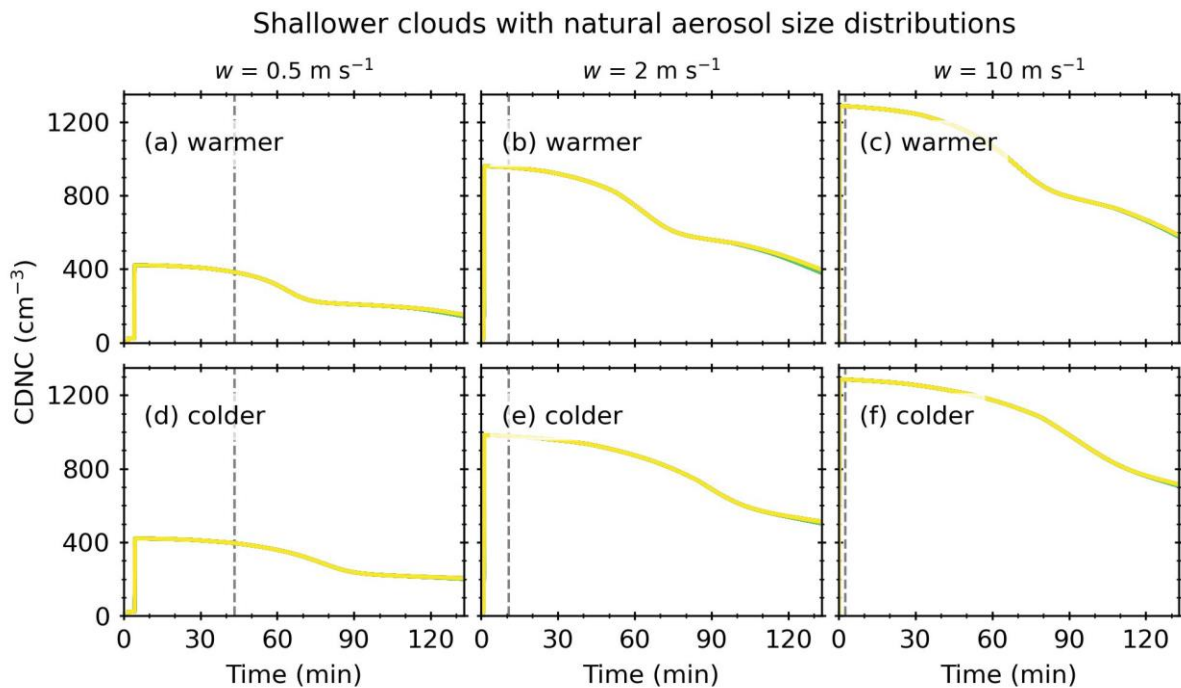


Figure S4 Cloud drop number concentrations for a shallower cloud (1.3-km deep) with a natural aerosol size distribution. Warmer refers to cloud base temperatures of 7 °C, and colder refers to cloud base temperatures of 0 °C.

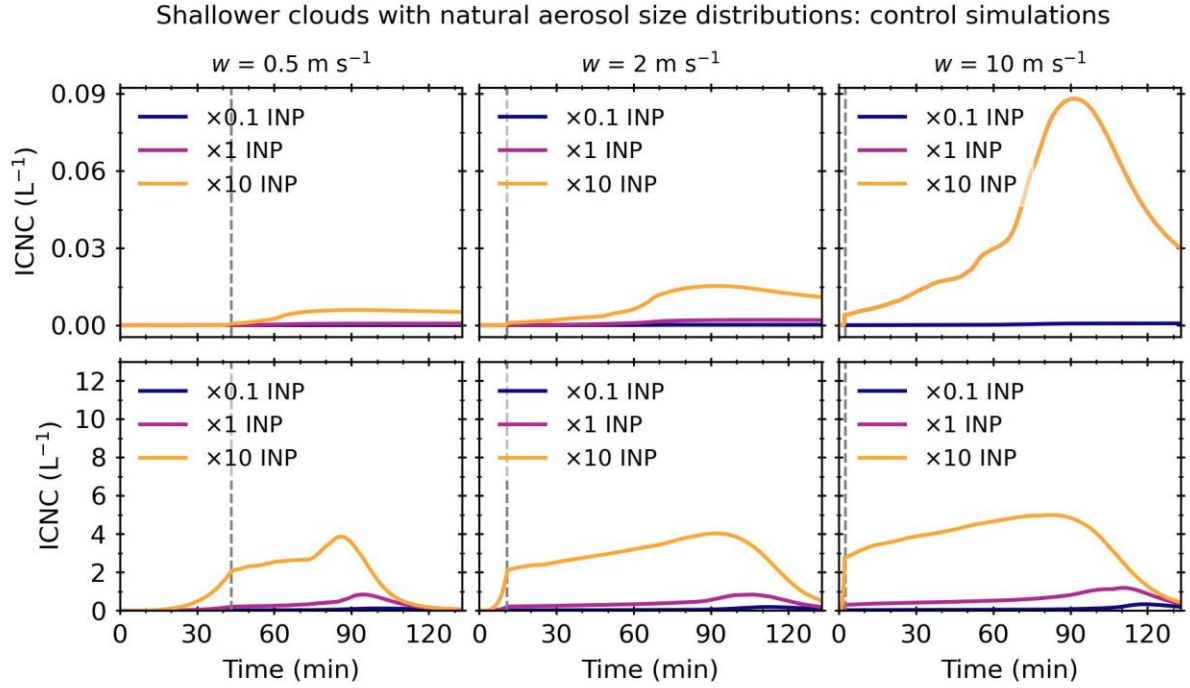


Figure S5 Ice crystal number concentrations for control simulations against simulation time for three initial INP concentrations ($\times 0.1$, $\times 1$ and $\times 10$) for a shallower cloud (1.3 km deep) with a natural aerosol size distribution. Warmer refers to cloud base temperatures of 7 °C, and colder refers to cloud base temperatures of 0 °C.

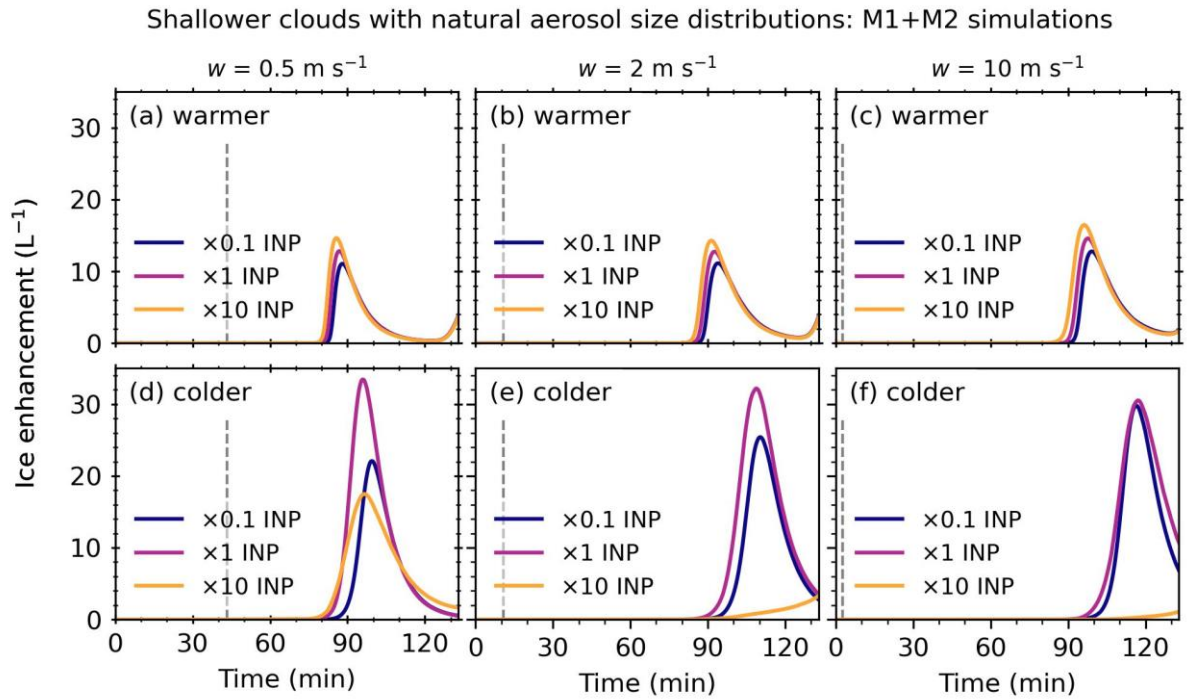


Figure S6 Mode 1 and mode 2 ice enhancement against simulation time for three INP concentrations ($\times 0.1$, $\times 1$ and $\times 10$) for a shallower (1.3 km deep) cloud with a natural aerosol size distribution. Warmer refers to cloud base temperatures of 7 °C, and colder refers to cloud base temperatures of 0 °C.

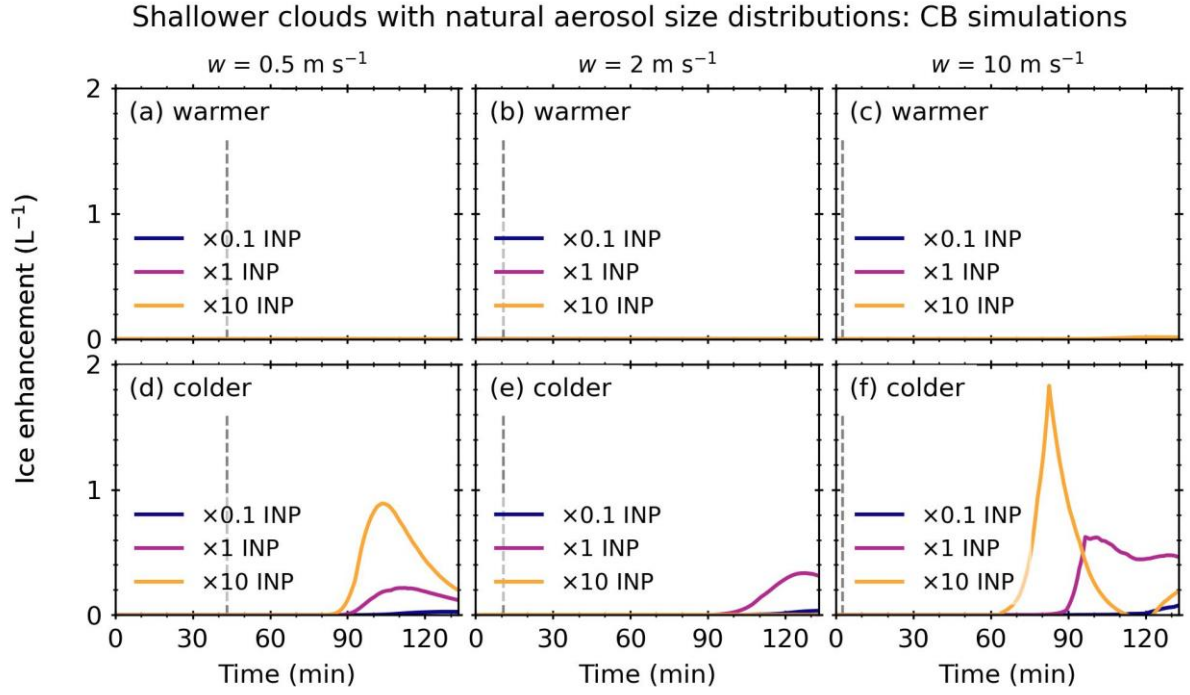


Figure S7 Ice-ice collisional breakup ice enhancement against simulation time for three INP concentrations ($\times 0.1$, $\times 1$ and $\times 10$) for a shallower (1.3 km deep) cloud with a natural aerosol size distribution. Warmer refers to cloud base temperatures of 7°C , and colder refers to cloud base temperatures of 0°C .

SECTION S3: Additional figures for shallower clouds with a near-city size distribution

Shallow cloud with a near-city aerosol size distributions

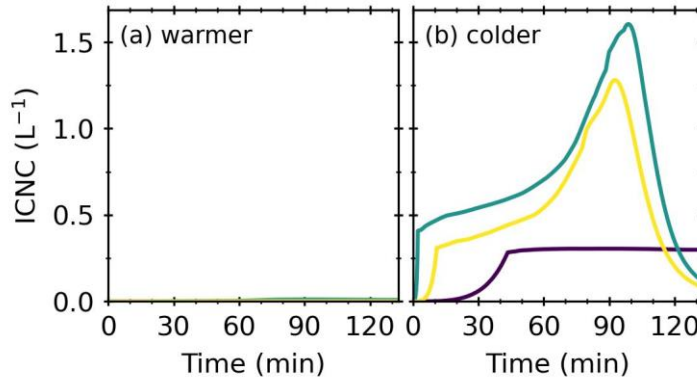


Figure S8 Control simulation ice crystal number concentrations for shallower clouds (1.3 km deep) with a natural aerosol size distribution. Warmer refers to cloud base temperatures of 7 °C, and colder refers to cloud base temperatures of 0 °C.

Shallower clouds with near-city aerosol size distributions

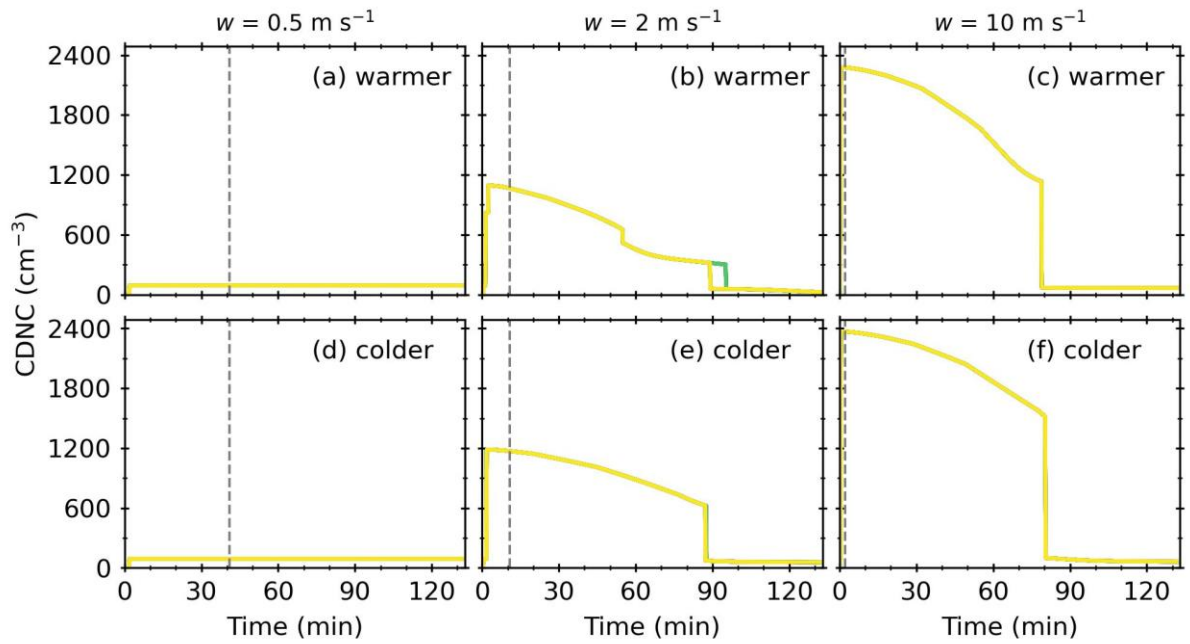


Figure S9 Cloud drop number concentrations for a shallower cloud (1.3~km deep) with a near-city aerosol size distribution. Warmer refers to cloud base temperatures of 7 °C, and colder refers to cloud base temperatures of 0 °C.

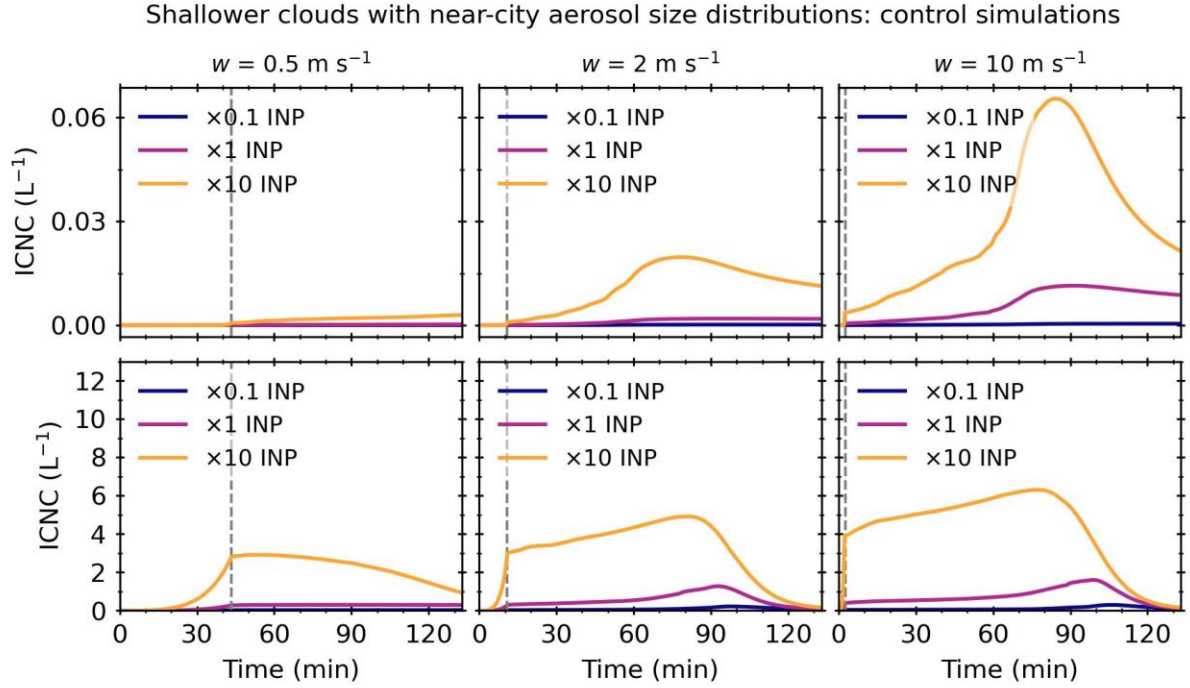


Figure S10 Ice crystal number concentrations for control simulations against simulation time for three initial INP concentrations ($\times 0.1$, $\times 1$ and $\times 10$) for a shallower cloud (1.3 km deep) with a near-city aerosol. Warmer refers to cloud base temperatures of 7 °C, and colder refers to cloud base temperatures of 0 °C.

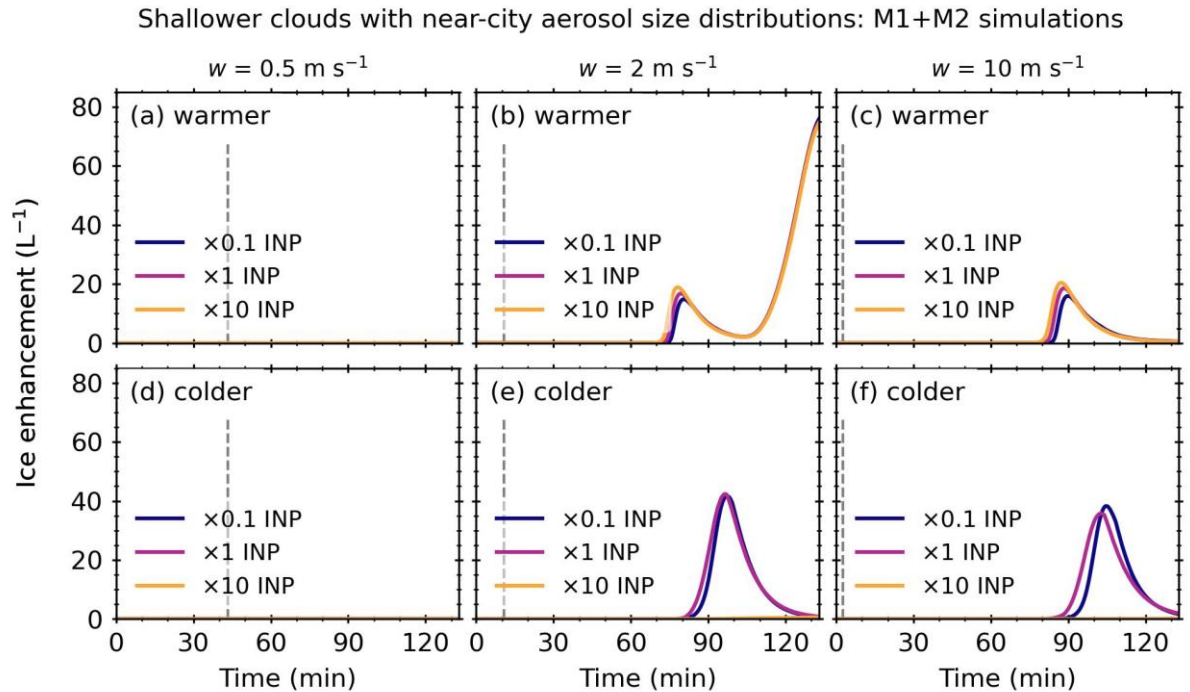


Figure S11 Mode 1 and mode 2 ice enhancement against simulation time for three INP concentrations ($\times 0.1$, $\times 1$ and $\times 10$) for a shallower (1.3 km deep) cloud with a near-city aerosol size distribution. Warmer refers to cloud base temperatures of 7 °C, and colder refers to cloud base temperatures of 0 °C.

Shallower clouds with near-city aerosol size distributions: CB simulations

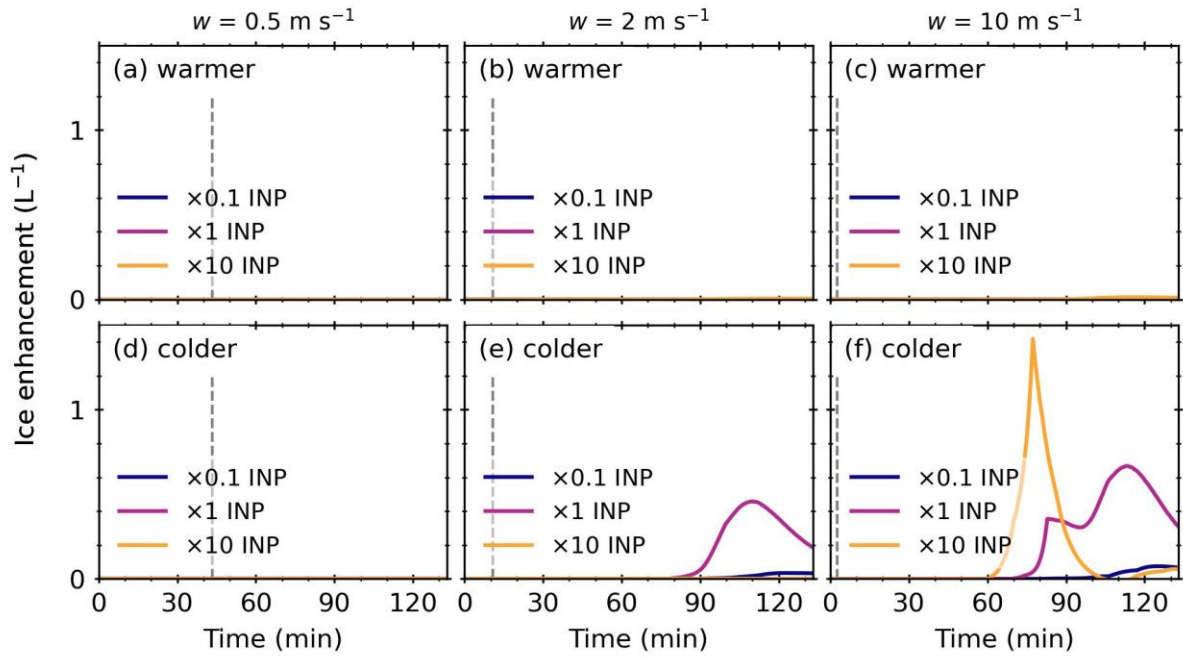


Figure S12 Ice-ice collisional breakup ice enhancement against simulation time for three INP concentrations ($\times 0.1$, $\times 1$ and $\times 10$) for a shallower (1.3 km deep) cloud with a natural aerosol size distribution. Warmer refers to cloud base temperatures of 7 °C, and colder refers to cloud base temperatures of 0 °C.

SECTION S4: Additional figures for deeper clouds with a natural aerosol size distribution

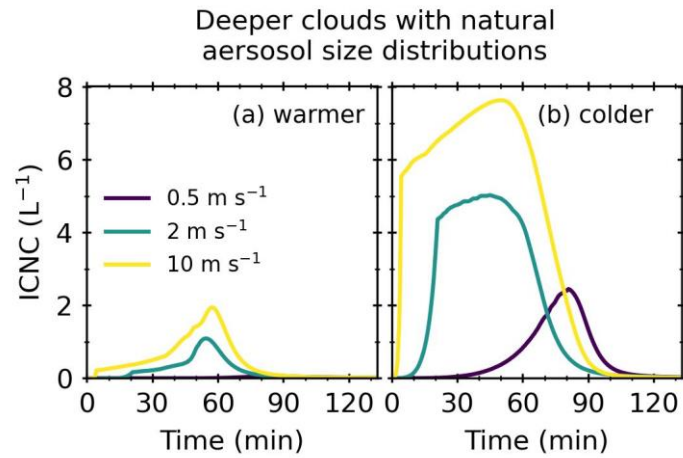


Figure S13 Control simulation ice crystal number concentrations for deeper clouds (1.3 km deep) with a natural aerosol size distribution. Warmer refers to cloud base temperatures of 7°C , and colder refers to cloud base temperatures of 0°C .

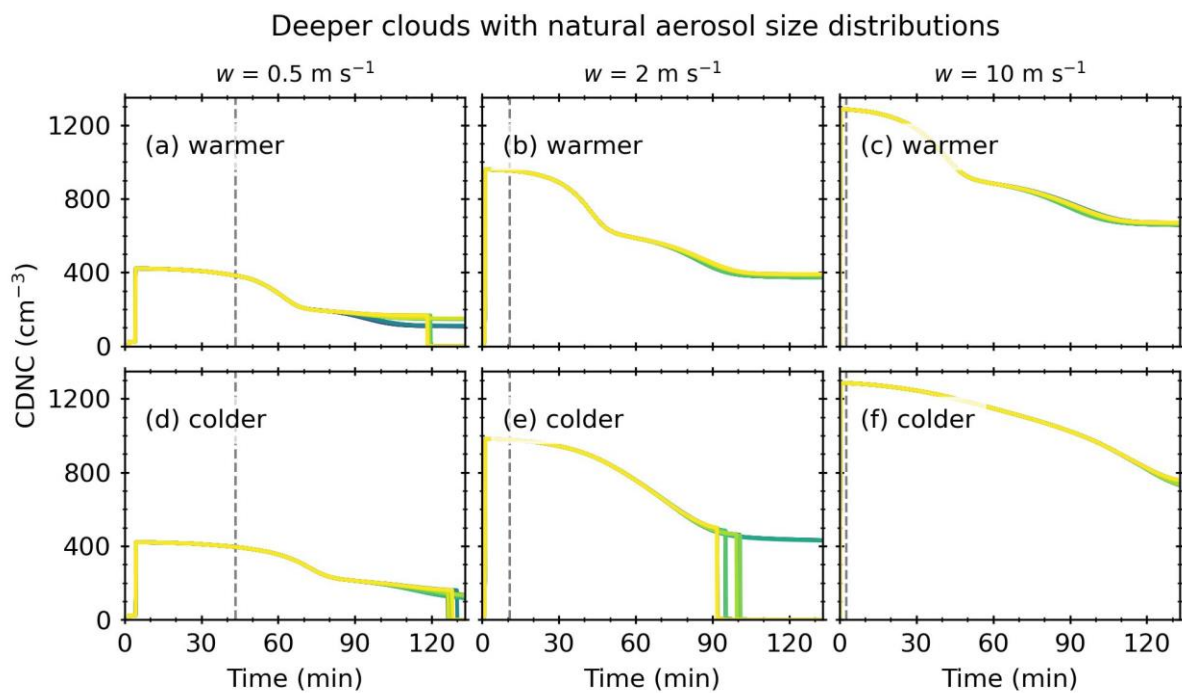


Figure S14 Cloud drop number concentrations for a deeper cloud (1.3 km deep) with a natural aerosol size distribution. Warmer refers to cloud base temperatures of 7°C , and colder refers to cloud base temperatures of 0°C .

SECTION S5: Additional figures for deeper clouds with a near-city size distribution

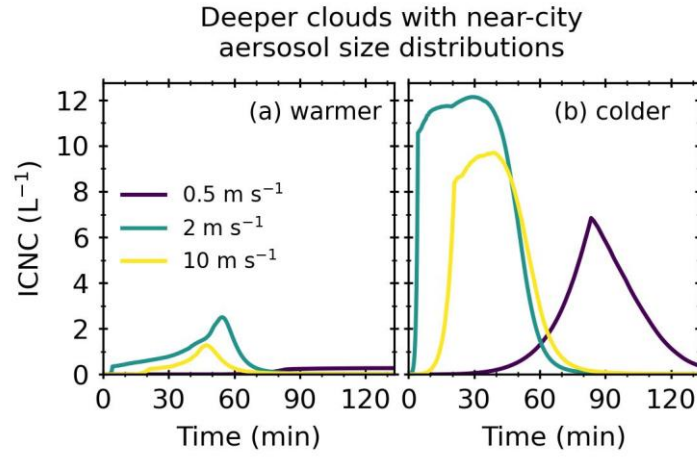


Figure S15 Control simulation ice crystal number concentrations for deeper clouds (2.4 km deep) with a near-city aerosol size distribution. Warmer refers to cloud base temperatures of $7\text{ }^{\circ}\text{C}$, and colder refers to cloud base temperatures of $0\text{ }^{\circ}\text{C}$.

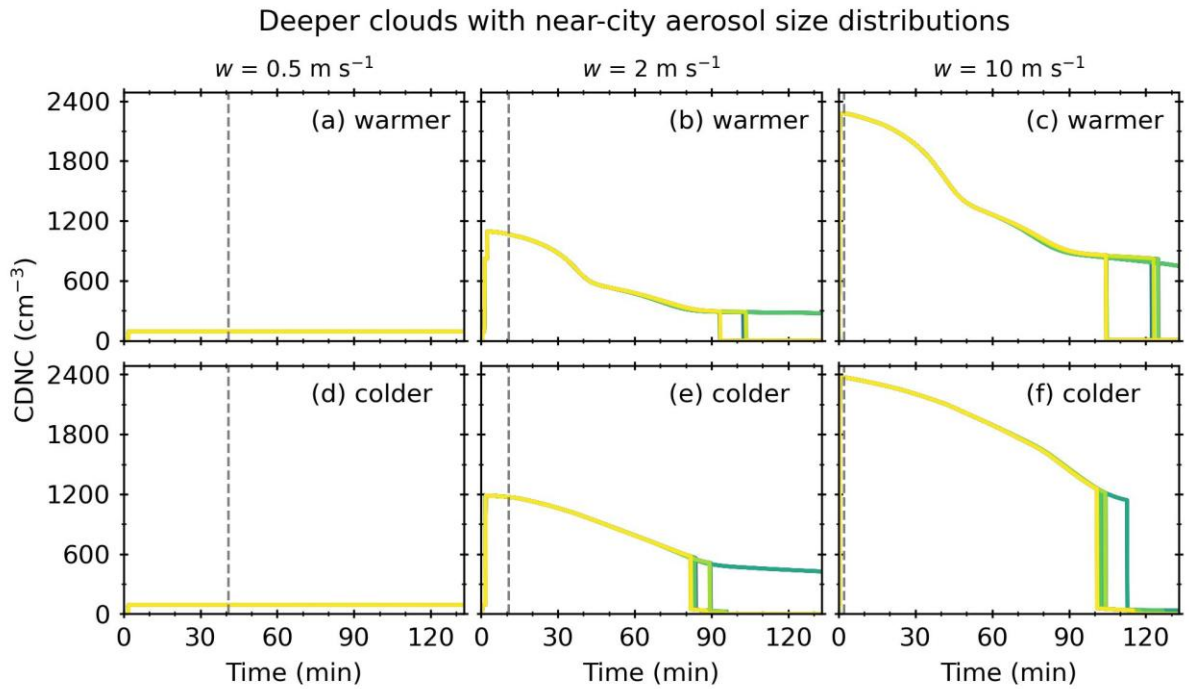


Figure S16 Cloud drop number concentrations for a deeper cloud (2.4 km deep) with a near-city aerosol size distribution. Warmer refers to cloud base temperatures of $7\text{ }^{\circ}\text{C}$, and colder refers to cloud base temperatures of $0\text{ }^{\circ}\text{C}$.

SECTION S6: Particle and ice size distribution contour plots

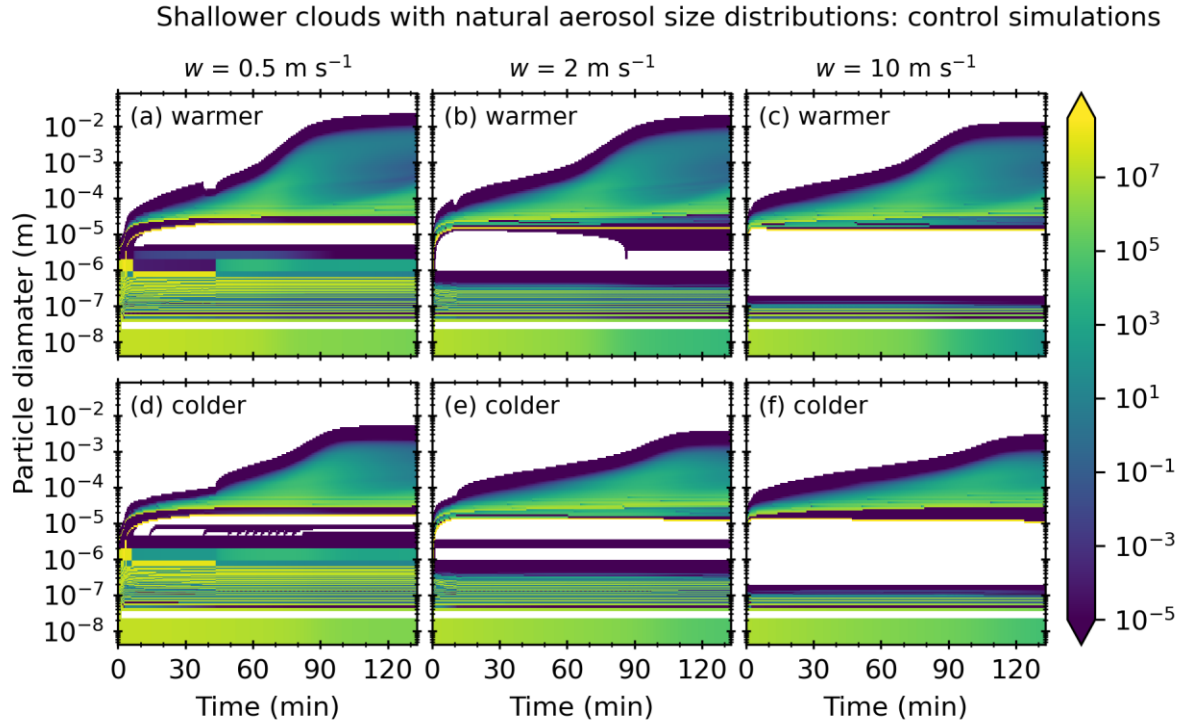


Figure S17 Contour plot showing the particle size distribution as a function of simulation time for shallower clouds (1.3 km deep) with natural aerosol size distributions. Warmer refers to cloud base temperatures of 7 °C, and colder refers to cloud base temperatures of 0 °C.

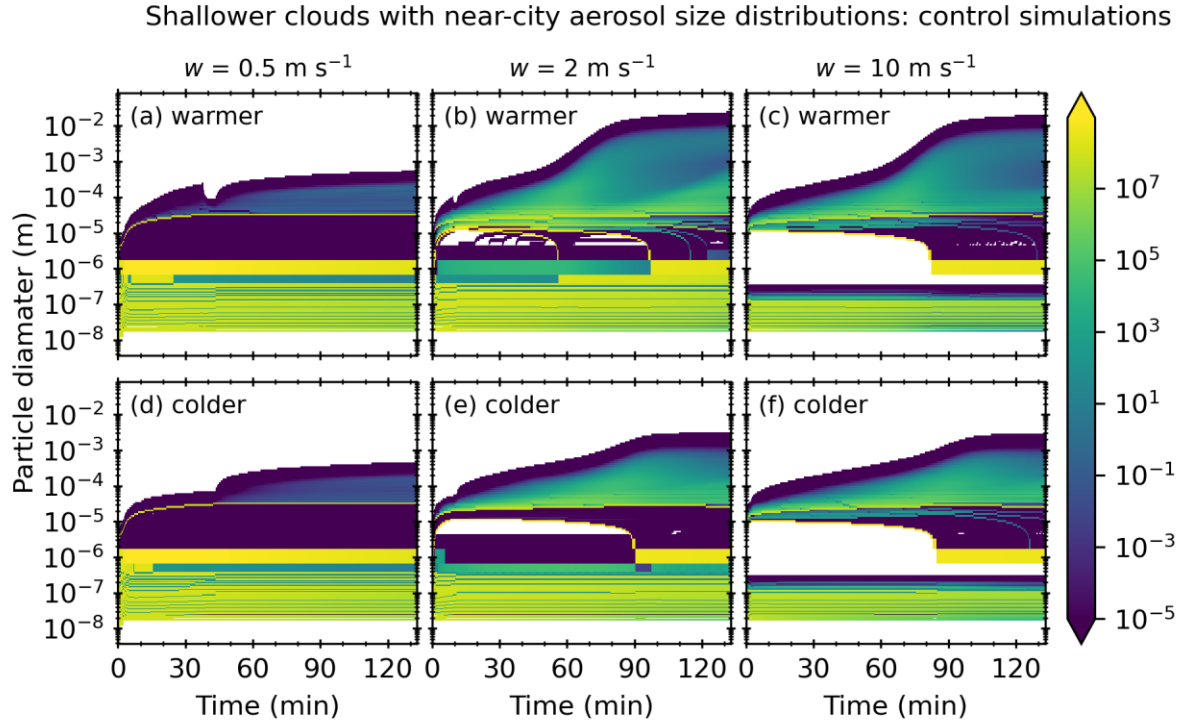


Figure S18 Contour plot showing the particle size distribution as a function of simulation time for shallower clouds (1.3 km deep) with near-city aerosol size distributions. Warmer refers to cloud base temperatures of 7 °C, and colder refers to cloud base temperatures of 0 °C.

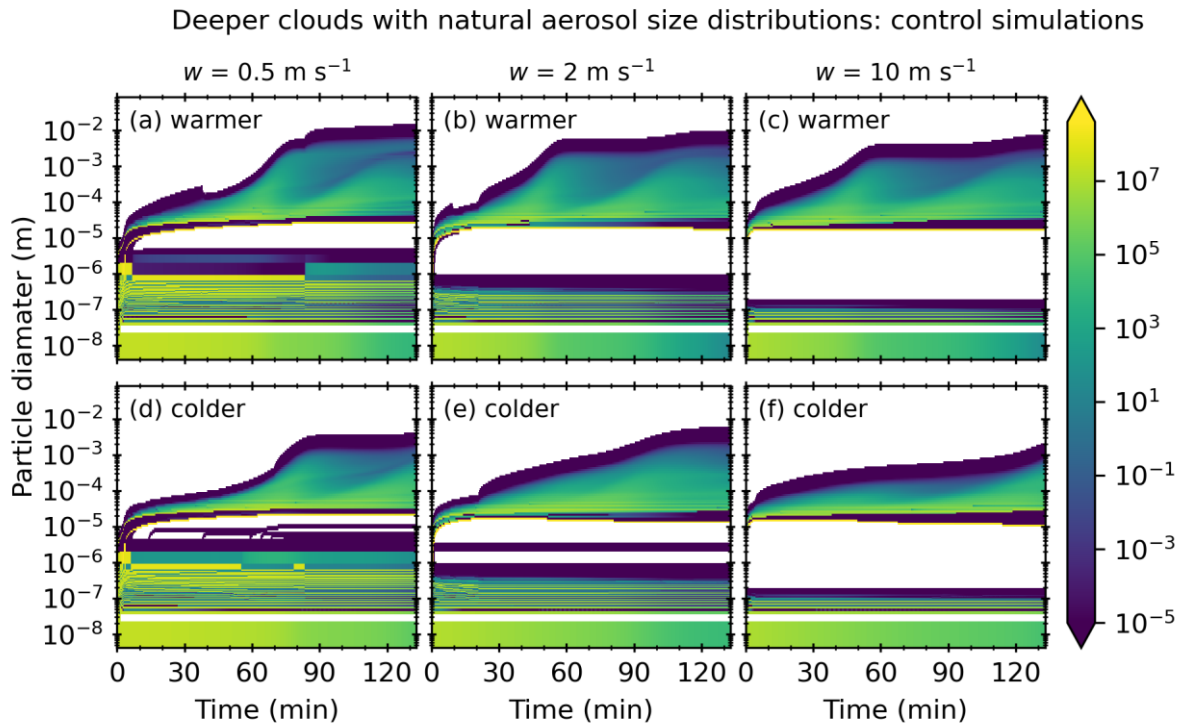


Figure S19 Contour plot showing the particle size distribution as a function of simulation time for deeper clouds (2.4 km deep) with natural aerosol size distributions. Warmer refers to cloud base temperatures of 7 °C, and colder refers to cloud base temperatures of 0 °C.

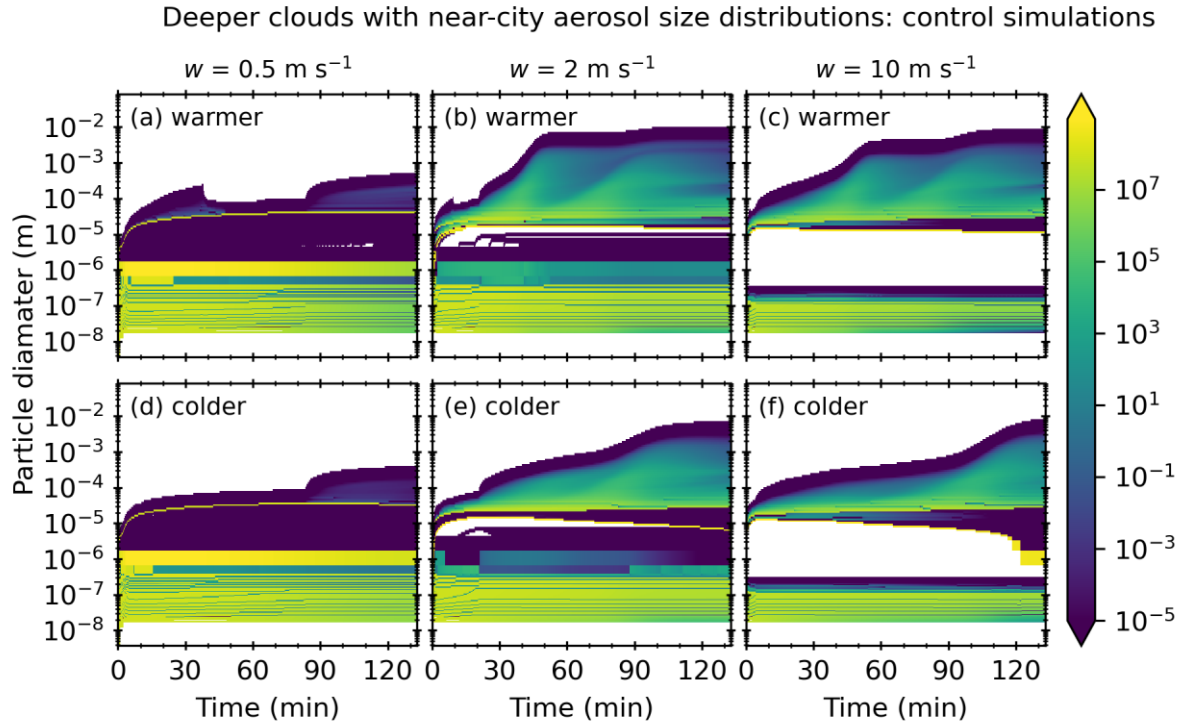


Figure S20 Contour plot showing the particle size distribution as a function of simulation time for deeper clouds (2.4 km deep) with natural aerosol size distributions. Warmer refers to cloud base temperatures of 7 °C, and colder refers to cloud base temperatures of 0 °C.

SECTION S7: Ice particle aspect ratio figures

Shallower clouds with natural aerosol size distributions

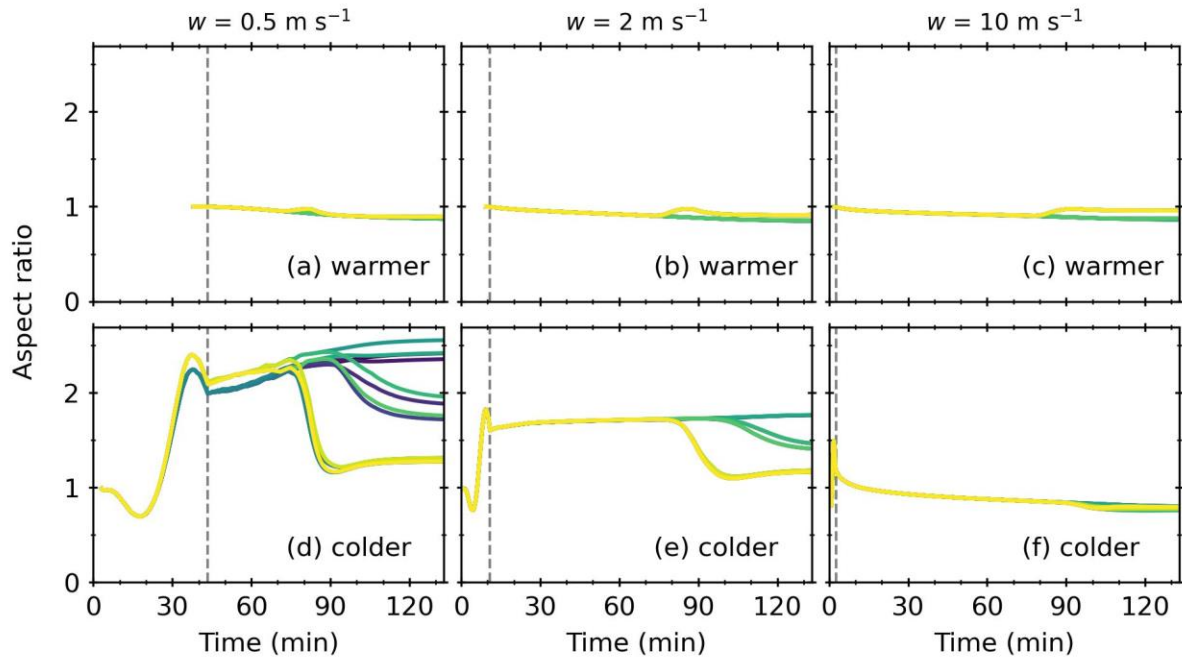


Figure S21 Ice particle aspect ratio for a shallower cloud (1.3 km deep) with a natural aerosol size distribution. Warmer refers to cloud base temperatures of 7 °C, and colder refers to cloud base temperatures of 0 °C.

Shallower clouds with near-city aerosol size distributions

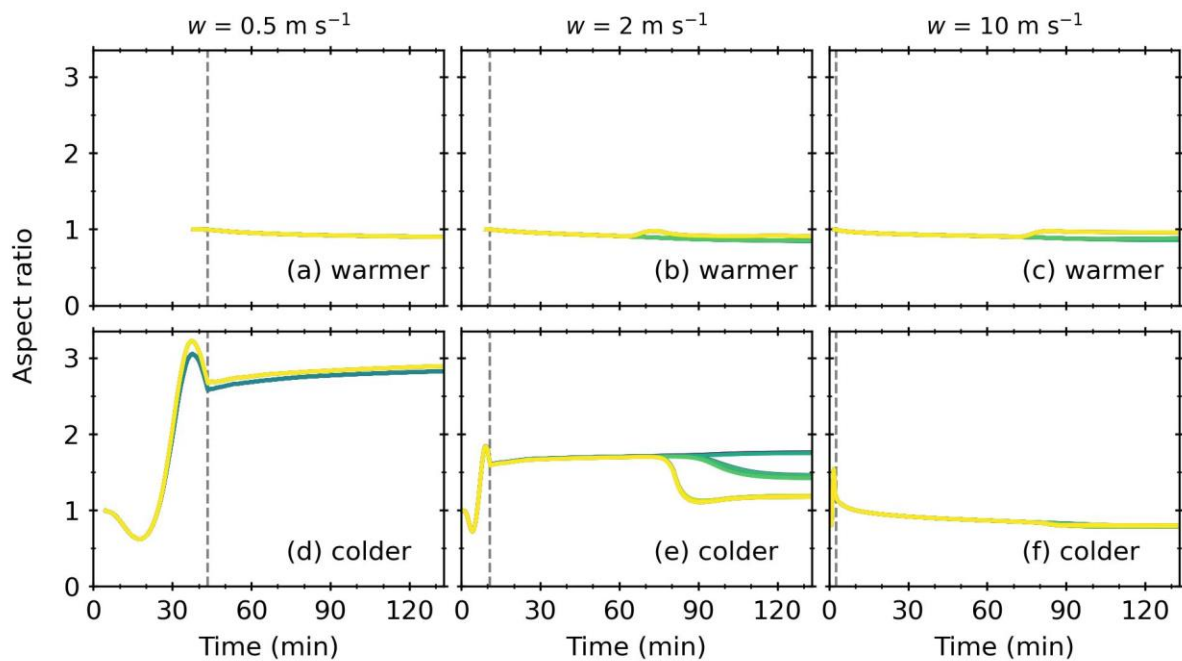


Figure S22 Ice particle aspect ratio for a shallower cloud (1.3 km deep) with a near-city aerosol size distribution. Warmer refers to cloud base temperatures of 7 °C, and colder refers to cloud base temperatures of 0 °C.

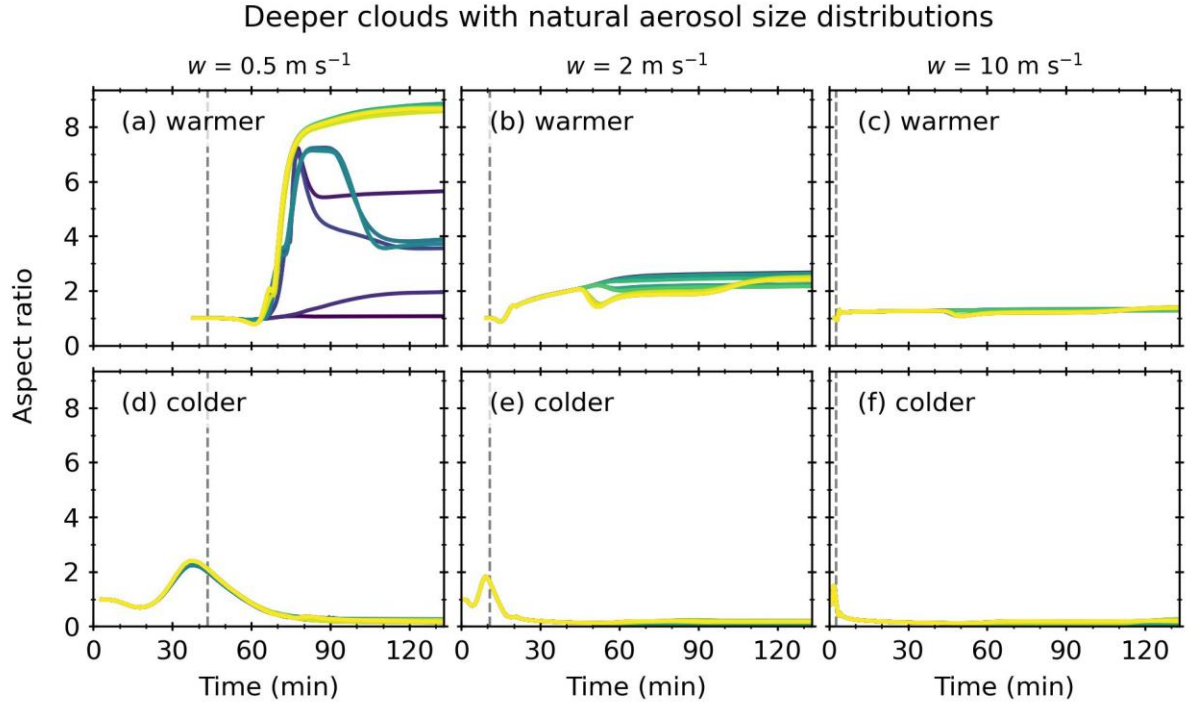


Figure S23 Ice particle aspect ratio for a deeper cloud (2.4 km deep) with a natural aerosol size distribution. Warmer refers to cloud base temperatures of 7 °C, and colder refers to cloud base temperatures of 0 °C.

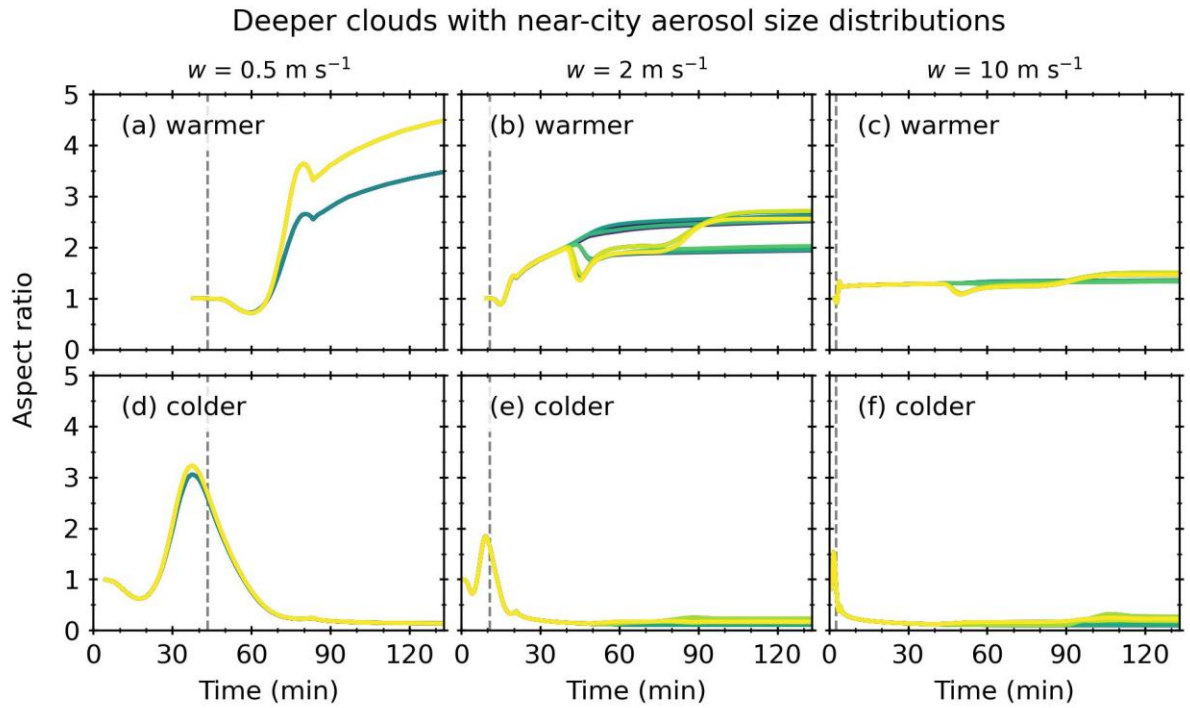


Figure S24 Ice particle aspect ratio for a deeper cloud (2.4 km deep) with a near-city aerosol size distribution. Warmer refers to cloud base temperatures of 7 °C, and colder refers to cloud base temperatures of 0 °C.