Heavy snowfall event over the Swiss Alps: Did wind shear impact secondary ice production?

Zane Dedekind*1, Jacopo Grazioli*2, Philip H. Austin1, and Ulrike Lohmann3
1Department of Earth, Ocean, and Atmospheric Sciences, University of British Columbia, Earth Sciences Building, 2207 Main Mall, Vancouver, BC, V6T 1Z4, Canada
2Environmental Remote Sensing Laboratory (LTE), École Polytechnique Fédérale de Lausanne (EPFL), Lausanne, Switzerland
3Institute of Atmospheric and Climate Science, ETH Zurich, Switzerland
*Equally contributing authors
Correspondence: Zane Dedekind (zane.dedekind@ubc.ca) and Jacopo Grazioli (jacopo.grazioli@epfl.ch)

Abstract. Intense dual-polarization Doppler signatures in conjunction with strong vertical wind shear were observed by an X-band weather radar during a winter high precipitation event over the Swiss Alps. An enhancement of differential phase shift (Kdp > 1 ° km^-1) around ~15 °C suggested that a large population of oblate ice particles was present in the atmosphere. Here, we will show that ice-graupel collisions are a likely origin of this population. We perform sensitivity simulations that include ice-graupel collisions of a cold frontal passage to investigate whether these simulations can capture the event better and whether the vertical wind shear had an impact on the secondary ice production (SIP) rate. The simulations are conducted with the Consortium for Small scale Modeling (COSMO), at a 1 km horizontal grid spacing in the Davos region in Switzerland. The rime-splintering simulations could not reproduce the high ice number concentrations, produced too large ice particles and therefore overestimated the radar reflectivity. The collisional-breakup simulations reproduced both the measured horizontal reflectivity and the ground-based observations of hydrometeor number concentration more accurately (~20 L^-1). During 14:30-15:45 UTC the vertical wind shear strengthened by 60% within the region favorable for SIP. Calculation of the mutual information between the SIP rate and vertical wind shear and updraft velocity suggested that the SIP rate is best predicted by the vertical wind shear rather than the updraft velocity. The ice-graupel simulations were insensitive to the conversion rate size restriction from ice to graupel and snow to graupel.

1 Introduction

In clouds, ice particles play an important role in the description of Earth’s radiation budget and precipitation formation. Precipitation originates predominantly from mixed-phase clouds (MPCs) and ice clouds in the midlatitudes, especially over continental regions (Mühlmenstädt et al., 2015; Heymsfield et al., 2015, 2020). The formation of ice particles, therefore, needs to be described adequately if any attempt is made to understand the evolution of MPCs and ice clouds.

Ice formation can occur through primary and secondary ice production (SIP) processes. Primary ice production includes homogeneous freezing of supercooled liquid water at temperatures (T) < ~–38°C and heterogeneous ice nucleation of super-
cooled liquid water at warmer subzero \( T > \sim -38^\circ C \). After the first formation of ice particles secondary ice processes may occur. In a narrow temperature range, \(-3 \geq T \geq -8^\circ C\), rime splintering (Hallett and Mossop, 1974) can occur when supercooled liquid water collides with ice particles, freezes from the outside in and shatter as a result of internal pressure buildup.

Rime splintering has been used extensively in models but has been shown to be inadequate, having ice number concentrations orders of magnitude less than observed, in SIP in wintertime orographic MPCs (Henneberg et al., 2017; Dedekind et al., 2021; Georgakaki et al., 2022). Ice-ice collisions have been more widely used in models in the last decade (Yano and Phillips, 2011; Phillips et al., 2017; Sullivan et al., 2018; Hoarau et al., 2018; Sotiropoulou et al., 2020; Zhao et al., 2021) since they were first studied in laboratory conditions about four decades ago (Vardiman, 1978; Takahashi et al., 1995). SIP as a result of ice-ice collisions was shown to contribute significantly to the ice crystal number concentrations and thereby explain the discrepancy between models and observations in the Arctic (Sotiropoulou et al., 2020; Zhao et al., 2021), Antarctic (Sotiropoulou et al., 2021b) and mid-latitudes (Sullivan et al., 2018; Dedekind et al., 2021; Georgakaki et al., 2022). The enhancement of smaller ice particles cause an increase in the combined growth rates (riming and deposition) of up to 33% resulting in larger latent heat release and stronger updraft velocities (Dedekind et al., 2021). When ice-ice collisions occur in wintertime orographic MPCs, the general tendency is for riming to decrease. However, the deposition growth rate, which is the dominant growth mechanism in this case, causes the overall increase in the growth rates of ice particles. Due to the stronger updrafts, ice particles are lofted to higher regions within the cloud reducing the local precipitation rates.

The impact of turbulence associated with baroclinic waves on cloud water and precipitation formation is well known (Baumgartner and Reichel, 1975; Houze and Medina, 2005; Medina and Houze, 2015). Updrafts on the scale of \( \sim 10 \) km from baroclinic waves have properties of shear-induced turbulence and it is these small cells of enhanced updraft and turbulence that drive orographic precipitation (Medina and Houze, 2015). The probability of interactions between cloud hydrometeors, whether through riming and/or aggregation, increases with turbulence and aids in the rapid formation of precipitation regardless of whether the turbulence is associated with orographic flow regimes or in warm conveyor belts (Houze and Medina, 2005; Gehring et al., 2020). These interactions are not limited to the accretion of cloud hydrometeors which causes them to grow but could cause the fracturing of ice particles instead in ice-ice collisions enhancing SIP. Dedekind et al. (2021) hypothesized that ice-graupel collisions could also be sensitive to the rate at which graupel forms, which is a function of the size of ice particle and the riming rate. In the Seifert and Beheng (SB 2006) two-moment cloud microphysics scheme (2M), ice crystals or snow undergoing riming can only be converted to graupel once they reach a size of \( 200 \mu m \). When graupel forms too quickly in the model it could set off SIP earlier and could mask the effects of turbulence on ice-graupel collisions.

Polarimetric radar data has been used extensively to provide information on snowfall microphysics and hydrometeors’ habit (e.g., shape, phase or hydrometeor type). Differential reflectivity \( Z_{DR} \) can be used to distinguish oblate particles (horizontally-aligned where \( Z_{DR} > 0 \)) from prolate ones (vertically aligned where \( Z_{DR} < 0 \)). Therefore, in an environment where preferentially-oriented anisotropic ice particles are dominant, \( Z_{DR} \) signatures are prevalent (Bader et al., 1987; Kumjian et al., 2014). When ice particles form aggregates, larger and less oblate, \( Z_{DR} \) decreases while the horizontal polarization (\( Z_H \)) tends to increase (Schneebeli et al., 2013; Kumjian et al., 2014; Grazioni et al., 2015a). In the instance of ice-ice collisions Grazioni et al. (2015a) suggested that an increase of the specific differential phase shift \( K_{dp} \) can be due to a high number concentrations of anisotropic
ice crystals and that riming also (positively) contributes to this signal. $K_{dp}$ in snow at X-band frequencies can locally exceed $1 \, \text{°km}^{-1}$ (Bechini et al., 2013; Grazioli et al., 2015a) in these cases. A recent study (von Terzi et al., 2022) discussed the $K_{dp}$ enhancement suggesting that a combination of secondary ice production and an appropriate temperature range $T \approx -15^\circ\text{C}$ (where growth of planar crystals by vapor deposition, dendrites in particular, is maximized) can lead to this signature. Dendrites have very low densities, favor aggregation below (hence increase of $Z_H$ below $K_{dp}$ peaks) and can easily fracture on impact with other ice particles.

In this paper, we propose that the vertical wind shear associated with a cold-front passage enhanced the formation of small and numerous oblate ice particles through ice-ice collisions which should be observable with the Doppler dual-polarization radar. We will address the following question:

- Does the radar provide reasonable information showing that high ice number concentrations can be linked to SIP other than rime splintering?
- By including ice-graupel collisions in the model, can we simulate the high ice number concentrations that were observed?
- Was there a correlation between the vertical wind shear and SIP?
- How sensitive are the SIP rates to the conversion rate from ice particles to graupel?

## 2 Methods

### 2.1 The case study

A synoptic system passed over Switzerland on 26 March 2010. The cold front was associated with a south-westerly wind flow at higher altitudes, the development of vertical wind shear closer to the surface, a surface temperature drop of $\sim 7 \, ^\circ\text{C}$ (Fig. S1) and high snowfall during the afternoon. The vertical wind shear, observed by a dual-polarization Doppler weather radar of the École Polytechnique Fédérale de Lausanne Environmental Remote Sensing Laboratory (EPFL-LTE) deployed in the Davos region (see Sec 2.2), was visible between 2 and 5 km amsl. Peculiar polarimetric radar signatures were also observed in this case. In particular $K_{dp}$ reached values around $1.5 \, \text{°km}^{-1}$ at certain height levels and towards the end of the event it was exceeding $2 \, \text{°km}^{-1}$. Because the sub-zero temperature in the region of enhanced radar signatures was warmer than 252 K (e.g. $-21 \, ^\circ\text{C}$), which is in the temperature range favourable for secondary ice production (Hallett and Mossop, 1974), we hypothesize that the in situ cloud conditions coupled with the vertical wind shear could have triggered higher secondary ice production rates that can be reflected in radar measurements, as $K_{dp}$ is an indicator of number high concentrations of oblate hydrometeors in the radar sampling volume (Kennedy and Rutledge, 2011; Bechini et al., 2013; Grazioli et al., 2015a; von Terzi et al., 2022).
2.2 Weather radar and 2 dimensional video disdrometer (2DVD)

An X-band dual-polarization mobile Doppler weather radar (MXPol) well suited for deployment in complex Alpine terrains or remote locations (e.g. Schneebeli et al., 2013; Grazioli et al., 2015a, 2017), was set up at 2133 m a.s.l. on a ski slope overseeing the valley of Davos (Schneebeli et al., 2013) from the southern side as shown in figure 1. MXPol operated from September 2009 to July 2011. Its exact location was 46.79° N and 9.84° E. The radar was routinely scanning over the valley of Davos in a sequence including pseudo-horizontal scans (fixed elevation and variable azimuth) and 2D vertical cross-sections (fixed azimuth scans with elevation ranging from 0° to 90°, better known as Range Height Indicator or RHI scans). One RHI scan in particular, used as a data source of this study, was conducted every 5 minutes towards NE, at an azimuth of 22°. MXPol provides single ($Z_H$) and dual-polarization ($Z_{DR}$, $K_{dp}$, $\rho_{HV}$) measurements as well as Doppler data which have been proven useful in several snowfall microphysics studies (e.g. Schneebeli et al., 2013; Grazioli et al., 2015a; Kumjian and Lombardo, 2017; Oue et al., 2021). Additionally, retrieval algorithms adapted to polarimetric data allow one to estimate properties such as hydrometeor type (Grazioli et al., 2015b, as used in this work) or, under given assumptions, microphysical quantities such as ice number concentration $N_t$, median volume diameter $\bar{D}_m$ or ice water content (IWC). This is done here following the method described in Murphy et al. (2020). The microphysical quantities are estimated from combinations of $Z_H$, $Z_{DR}$, $K_{dp}$ and radar wavelengths in the Rayleigh regime (although at X-band this may not be fulfilled) and assuming that density and size of the hydrometeors are inversely proportional. This retrieval has shown to be most reliable at $T < -10$°C, for low riming degrees and in regions where the $K_{dp}$ and $Z_{DR}$ signals are not close to 0. As recognized by Murphy et al. (2020), the errors may be large and in situ validation efforts are needed to refine these techniques.

A ground-based source of information for this event is provided by a 2 dimensional video disdrometer, 2DVD (For more information about this instrument at this location see Grazioli et al., 2014) which was deployed on the opposite side of the Davos valley with respect to MXPol (46.83° N and 9.81° E, 2543 m. amsl). The 2DVD measures the size and fall velocity of hydrometeors larger than about 0.2 mm in terms of maximum dimension.

2.3 Model setup

2.3.1 Spatial and temporal resolution

The Consortium for Small Scale Modelling (COSMO; Baldauf et al., 2011) non-hydrostatic model, version 5.4.1b, was used for this case study. COSMO has been used to study wintertime (Lohmann et al., 2016; Henneberg et al., 2017; Dedekind et al., 2021) and summertime (Dedekind, 2021; Eirund et al., 2021) orographic MPCs in the Swiss Alps. The model domain roughly covers a region of 500 km x 600 km (44.5 to 49.5° N and 4 to 13° E) at a horizontal grid spacing of 1.1 km x 1.1 km (Fig. 1). A height based hybrid smoothed level vertical coordinate system (Schär et al., 2002) with 80 levels is used and stretched from the surface to 22 km. For this study, we simulate the cold front passage between 11:00 and 18:00 UTC and analyze the results between 13:00 and 18:00 UTC on March 26, 2010. COSMO is forced with hourly initial and boundary conditions re-analysis data at a horizontal resolution of 7 km x 7 km, supplied by MeteoSwiss. The model time step is 4 s with an output frequency every 15 min.
Simulations were conducted including several SIP processes, which consisted of ice-graupel collisions (as thoroughly discussed in section 2.3.2) and a control simulation where only rime splintering (RS) was active. For each of these simulations, 5 ensemble simulations are conducted by perturbing the initial temperature conditions at each grid point through the model domain with unbiased Gaussian noise at a zero mean and a standard deviation of 0.01 K (Selz and Craig, 2015; Keil et al., 2019). The model output was interpolated along the mean of three vertical cross-sectional paths similar to the dual-Doppler radar output (Fig. 1).

2.3.2 Cloud microphysics scheme

We use a detailed two-moment bulk cloud microphysics scheme within COSMO with six hydrometeor categories, including cloud droplets, rain, ice, snow, graupel and hail (Seifert and Beheng, 2006). The 2M scheme has been used extensively to study the evolution, lifetime, persistence and aerosol-cloud interactions of MPCs (Seifert et al., 2006; Baldauf et al., 2011; Lohmann et al., 2016; Possner et al., 2017; Henneberg, 2017; Glassmeier and Lohmann, 2018; Sullivan et al., 2018; Eirund et al., 2019, 2021). We refer to ice particles as any combination of the hail, graupel, snow or ice categories. Cloud droplet activation is based on an empirical activation spectrum which depends on the cloud-base vertical velocity and the prescribed number concentration of cloud condensation nuclei (Seifert and Beheng, 2006). The application is appropriate in atmospheric models with a horizontal grid size and time resolution of \( \Delta x \leq 1 \text{ km} \) and \( \Delta t < 10 \text{ s} \) respectively. The warm-phase autoconversion process from Seifert and Beheng (2001) was updated with the collision efficiencies from Pinsky et al. (2001) and also takes into account the decrease in terminal fall velocity associated with an increase in air density. A better approximation of the collision
rate between hydrometeors was also introduced by Seifert and Beheng (2006), which makes use of the Wisner-approximation (Wisner et al., 1972).

The primary production of ice formation is described by the homogeneous and heterogeneous nucleation pathways. Homogeneous nucleation of cloud droplets is calculated for $0 > T \geq -50 \, ^\circ\text{C}$ (Cotton and Field, 2002), otherwise the homogeneous freezing of all cloud droplets occurs when $T < -50 \, ^\circ\text{C}$. The homogeneous nucleation of solution droplets, typically associated with cirrus cloud formation follows Kärcher et al. (2006). Here, the number density and size of nucleated ice crystals is determined by the vertical wind speed, temperature and pre-existing cloud ice. Heterogeneous nucleation is empirically derived which depends on the chemical composition and surface area of multiple species of aerosols, namely organics, soot and dust (Phillips et al., 2008).

Secondary ice production through rime splintering is the only process that is included in the standard version of COSMO which has been used extensively in other numerical weather models (Blyth and Latham, 1997; Ovtchinnikov and Kogan, 2000; Phillips et al., 2006; Milbrandt and Morrison, 2016; Phillips et al., 2017). In COSMO, rime splintering occurs at $-3 \geq T \geq -8 \, ^\circ\text{C}$ (Hallett and Mossop, 1974) when supercooled droplets and rain drops ($D_{c,r} \geq 25 \, \mu\text{m}$) collide with ice hydrometeors ($D_{i,s,g} \geq 100 \, \mu\text{m}$) (e.g Seifert and Beheng, 2006). Another SIP process, collisional breakup, was added to COSMO and tested in several studies (Sullivan et al., 2018; Dedekind et al., 2021). During collisional breakup graupel collides with either ice and/or snow particles and fractures. This can increase the ice particles at temperatures warmer than 252 K. Several studies (e.g Sotiropoulou et al., 2021b; Dedekind et al., 2021) have considered reducing the effectiveness of the collisional breakup parameterization due to the discrepancies in the large hail particles and their corresponding fall velocities used in the laboratory study conducted by Takahashi et al. (1995). In this study of the heavy snowfall event during which high $K_{dp}$ values were recorded, we use the parameterizations for ice-graupel collisional breakup from Dedekind et al. (2021) and Sotiropoulou et al. (2021b) in COSMO in different forms:

\[
\mathcal{N}_{BR} = \frac{F_{BR}}{\alpha} (T - 252)^{1.2} \exp \left[ -\frac{(T - 252)}{\gamma_{BR}} \right], \quad \text{for BR28} \quad (F_{BR, \alpha, \gamma_{BR}}) = (280, 10, 2.5) \tag{1}
\]

\[
\mathcal{N}_{BR} = \frac{F_{BR}}{\alpha} (T - 252)^{1.2} \exp \left[ -\frac{(T - 252)}{\gamma_{BR}} \right], \quad \text{for BR2.8T} \quad (F_{BR, \alpha, \gamma_{BR}}) = (280, 100, 5) \tag{2}
\]

\[
\mathcal{N}_{BR} = F_{BR} (T - 252)^{1.2} \exp \left[ -\frac{(T - 252)}{\gamma_{BR}} \right] \frac{\bar{D}}{\bar{D}_0}, \quad \text{for BR-Sot} \quad (F_{BR, \bar{D}_0, \gamma_{BR}}) = (280, 0.02, 5) \tag{3}
\]

where $\alpha$ is the scale factor, $F_{BR}$ is the leading coefficient, $T$ is the temperature in Kelvin, $\gamma_{BR}$ is the decay rate of the fragment number at warmer temperatures, $\bar{D}$ is the diameter of particle undergoing fracturing and $\bar{D}_0$ is the diameter of the hail particles used in Takahashi et al. (1995). Only using ice-graupel collisions would limit the full description of SIP as a result of wind shear when graupel formation becomes restricted. Equations 1 and 2 were applied in Dedekind et al. (2021) where BR28 is scaled by 10 and has a slower decay rate of fragment number at warmer temperatures and BR2.8T is only scaled by 100.
Equation 3 was applied in Sotiropoulou et al. (2021b) which was scaled by $D_0 = 0.02 \text{ mm}$. Similar to Dedekind (2021), the ICNC in COSMO is limited to $2,000 \text{ L}^{-1}$. Furthermore, Dedekind (2021) concluded that the conversion rate from ice crystals or snow to graupel, which is a function of the riming rate of ice crystals or snow with raindrops, may contribute to enhanced collisional breakup (Seifert et al., 2006). In the current version of the 2M scheme, early graupel formation is promoted when ice crystals or snow with $D_{i,s} \geq 200 \mu \text{m}$ are converted to graupel (eq. (70): $D_{i,s} \geq 500 \mu \text{m}$ used in Seifert and Beheng, 2006). In this study, we will set-up sensitivity studies promoting slower graupel formation to understand how the conversion rate impacts SIP processes. To accomplish this we change the ice category conversion size requirement, $D_{i,s}$, during riming from $200 \mu \text{m}$ (BR2.8T), to $300 \mu \text{m}$ (BR2.8T_300), to $400 \mu \text{m}$ (BR2.8T_400) and lastly to $500 \mu \text{m}$ (BR2.8T_500).

To investigate the impact of vertical wind shear and updraft on SIP the probability density functions (PDFs) for the variables from the collisional breakup simulations are analyzed. Furthermore, the joint PDFs are calculated along with the mutual information (MI, Shannon and Weaver, 1949) score which quantifies the strengths of dependencies between the SIP rate and cloud properties (e.g., Dawe and Austin, 2013). For this purpose a $10\text{ km} \times 10\text{ km}$ region was selected and masked by the levels in which SIP occurred ($T > -21^\circ \text{C}$) from 15:15 to 16:30 UTC. This resulted in the 16,121 data points for which an expression from Hacine-Gharbi et al. (2013) was used for finding the optimal number of bins (17 bins in our case) to estimate the MI for continuous random variables.

3 Results

3.1 Simulated vs observed radar reflectivity

3.1.1 Model and Doppler radar comparison

Horizontal reflectivity $Z_H$ is used to compare the model to the observations throughout the cloud and to analyze the impact of secondary ice production on the simulated radar reflectivity. During the early afternoon, the median of $Z_H$ remained mostly below 20 dBz. At around 15:15 UTC larger ice hydrometeors were present (either as a result of enhanced aggregation or depositional growth) between 4 and 6 km amsl which then started to sediment (Fig. 2a and b). A peak in $Z_H$ at 3 km amsl was observed in the fall streaks when the cloud droplets rimed onto the sedimenting ice hydrometeors. The radar-derived hydrometeor classification showed that much of the ice hydrometeor growth occurred through aggregation and riming. At 15:30 UTC, a very high median $K_{dp} > 1 \text{ km}^{-1}$ and $Z_{DR} > 1 \text{ dB}$ were observed. The vertical evolution of $K_{dp}$ and $Z_{DR}$ is similar, with a peak observed about 4 km amsl, which is 1 km above the peak in $Z_H$. The large and colocated values of $Z_{DR}$ and $K_{dp}$ suggest that a large population of oblate particles were present at these heights. The increase in $Z_H$ and colocated decrease of $K_{dp}$ and $Z_{DR}$ below suggest that larger (and/or denser) and more isotropic particles were forming. Aggregation and riming, not mutually exclusive, both explain this behavior. The occurrence of peaks in polarimetric variables at certain heights above ground ($K_{dp}$ in particular) has been observed during intense snowfall events (e.g. Kennedy and Rutledge, 2011; Schneebeli et al., 2013; Grazioli et al., 2015a). The $K_{dp}$ enhancement in particular has often been observed near the $-15^\circ \text{C}$ isotherm and has been interpreted as the signature of enhanced dendritic growth (Kennedy and Rutledge, 2011; Bechini et al.,
Figure 2. Hofmoller diagrams of radar reflectively for panels a) Doppler radar, c) RS , d) BR28, e) BR2.8T and f) BR-Sot between 13:00 and 17:30 UTC. Panel b) shows the hydrometeor class categories derived from the doppler radar. The hatched area is defined as the MPC where the cloud droplet mass concentration and ice mass concentration is greater than 10 and 0.1 mg m\(^{-3}\) respectively. The pink line is the homogeneous freezing line at 235 K, and the shaded gray area is the cloud area fraction.

2013) in combination with secondary ice production (von Terzi et al., 2022). Dendrites are prone to aggregation and therefore the \(K_{dp}\) peak disappears (and \(Z_H\) increases) as particles approach the ground level.

\(Z_H\) was significantly overestimated by the RS simulation between 13:00 and 17:30 UTC. Typically in 2M schemes (also seen here), excessive size sorting occurs within the sedimentation parameterizations in regions of vertical wind shear or updraft cores (Milbrandt and McTaggart-Cowan, 2010; Kumjian and Ryzhkov, 2012). Overestimations of \(Z_H\) may occur because rime splintering is not very active, if at all, in wintertime MPCs (e.g., Dedekind et al., 2021) and ice particles can grow to larger sizes which widens their size distributions (Figs. 4a, b and S2a, b). The ice crystal and snow categories both had number concentrations less than 100 L\(^{-1}\) with particle sizes of up to 0.8 and 2 mm respectively which may have allowed for enhanced size sorting at 15:30 UTC (Fig. 4a and b). The size sorting, most likely in combination with larger ice particles enhancing \(Z_H\), contributed to the large overestimations in \(Z_H\) of at least 8 dBz throughout the vertical profile compared to the observations. In contrast to this overestimation, the IWC and ice number concentration (NICE) in the RS simulation, however, did fall within the 10 and 90\(^{th}\) percentiles range of the observations below 5 km. Inferring the diameters of the ice particles using the IWC, NICE and the diameter-mass relations from Seifert and Beheng (2006), showed that the RS simulation was in agreement with the fewer, but larger ice particles. The disagreement in \(Z_H\) and contradicting agreement in the IWC and NICE between the RS
Figure 3. Hofmoller diagrams of graupel and rain mixing ratio for panels a) RS, c) BR28, c) BR2.8T and d) BR-Sot between 13:00 and 17:30 UTC. The hatched area is defined as the MPC where the cloud droplet mass concentration and ice mass concentration is greater than 10 and 0.1 mg m$^{-3}$ respectively. The pink line is the homogeneous freezing line at 235 K, and the shaded gray area is the cloud area fraction.

When collisional breakup was allowed to occur in the BR28, BR2.8T and BR-Sot simulations, the ice particles from the ice crystal and snow categories did not get time to grow as large. Throughout the vertical profile below 6 km at 15:30 UTC, the ice number concentration was at least an order of magnitude larger than expected from the RS simulation with a SIP rate in excess of 20 L$^{-1}$s$^{-1}$ (Fig. 5c, f). In both figures 5 and S3 the observed ice crystal number concentration recorded by the disdrometer were remarkably well represented at the surface by the BR2.8T and BR-Sot simulations (similar results are shown in Dedekind et al., 2021). The ice crystal and snow number concentrations were orders of magnitudes larger for $\bar{D}_i < 0.4$ mm and $\bar{D}_s < 0.8$ mm respectively compared to the RS simulation (Fig. 4a and b). The smaller ice particles caused a reduction in $Z_H$ which compared better to the observations than for the RS simulations. It is also likely that the narrower ice crystal and snow size distributions meant that the excessive size sorting in 2M schemes may have not been as pronounced, which contributed to the lowering of $Z_H$. At 17:00 UTC, the replenishment of graupel diminished rapidly (Figs. 3 and S2c) causing a substantial reduction in the SIP rate (Fig. S3). Less collisional breakup gave time for the ice crystals and snow to grow to larger sizes, $\bar{D}_i \sim 1.2$ mm and $\bar{D}_s \sim 3.3$ mm respectively, primarily through deposition and/or aggregation (Fig. S2a, b). A lower...
Figure 4. Particle size distribution over the number concentrations for panels a) ice, b) snow, c) graupel, d) cloud droplets and e) raindrops for all the simulations at 15:30 UTC.

\(Z_{\text{DR}}\) is consistent with highly reflective and less anisotropic particles produced by aggregation and/or riming. However, the enhanced concentration of oblate particles (increase in \(K_{\text{dp}}\)) was in contrast to the simulations showing a reduction in cloud content as the cloud began to dissipate earlier than in the observations. None of the simulations were able to describe the high ice particle formation event that was most likely triggered through ice-ice collisions of dendrites. In the event that snow (e.g., ice-snow collisions) would have also been considered as a collider species in the simulations (e.g., Sotiropoulou et al., 2021a), they might have been able to simulate higher ice particle formation rates as suggested in the high \(K_{\text{dp}}\) radar observations. The breakup simulations, in general, did simulate \(Z_{\text{H}}\) more accurately than the conventionally used rime-splintering scheme and did show to improve the ice crystal number concentration at the surface and in the vertical column.
Figure 5. a) Ice water content (IWC), b) liquid water content (LWC), c) ice number concentration (NICE), d) model and radar reflectivity, e) Specific differential phase ($K_{dp}$), differential reflectivity ($Z_{DR}$), and f) secondary ice production (SIP). The solid lines are the mean with shaded areas and errorbars showing the 10th and 90th percentiles for the model simulations and doppler radar respectively at 15:30 UTC. The green triangle is the 2DVD surface observations for hydrometeors $D>0.2$ mm.

### 3.1.2 Differences in collisional breakup simulations

Similar to Dedekind et al. (2021) collisional breakup had a drastic impact on the MPC (Fig. 3). The cloud liquid water that aids in the formation of graupel when cloud droplets larger than 15 µm rime onto ice crystals or snow was less than the in RS simulation (e.g., at 15:30 UTC in Figs. 3 and 5b and S3b). The parameterization for BR28 (Eq. 1) was set up such that...
more (less) ice fractures are generated at colder (warmer) temperatures than $-10^\circ C$ compared to the BR2.8T simulation (Eq. 2). Although the graupel number concentration, which is responsible for generating ice fractures upon colliding with other ice particles decreased with altitude, the BR28 simulation still generated factor of 8 times more ice particles than the BR2.8T and BR-Sot simulations at 4 km amsl at $T \sim -15^\circ C$ (Figs. 3b, c and 5f). At temperatures of $-10^\circ C$ (3 km amsl), the SIP rate decreased rapidly from 100 to almost $0 \text{L}^{-1}\text{s}^{-1}$ at the surface. As a result of the lower SIP rates (less ice-graupel collisions) compared to the BR2.8T and BR-Sot simulations, there were several implications: 1) ice crystals and snow particles had more time to grow to larger sizes as seen in the wider particle size distributions (Fig. 4); 2) the number of ice hydrometeors was an order of magnitude below (worst of the collisional-breakup simulations) the observed ground-based video disdrometer observations of $\sim 20 \text{L}^{-1}$ at 15:30 and 17:00 UTC (Figs. 5c and S3c) and; 3) interestingly, the simulated $Z_H$ compared better with the radar observations although the ice hydrometeors were underestimated (Figs. 5d and S3d). It is not clear which one of the collisional-breakup simulations performed better in general because one would perform better against one set of observations and then worse against another set of observations. However, ice-graupel collisions are important for representing the observed $Z_H$ better. For instance, the breakup of fast-growing, low density, dendrites at $T \sim -15^\circ C$ reduces the ice particle size and therefore reduces the simulated $Z_H$. Figure S3(d and f) showed a spike in the SIP rate at these temperatures resulting in a better agreement with the observed $Z_H$.

### 3.2 Process understanding

In this section, the dependence of the SIP rate on wind patterns is examined over the region (blue box) depicted in figure 1 during three time periods; 13:00-14:15 UTC (early: Fig. S4), 14:30-15:45 UTC (middle: Fig. 6) and 16:00-17:15 UTC (late: Fig. S5), of which 14:30-15:45 UTC was the most important in terms of SIP and is therefore shown here. Regions, in which SIP did not occur (e.g. $T < -21^\circ C$), were masked out for this analysis. Because the BR2.8T and BR-Sot simulations showed similar results, only the probability density functions (PDFs) for the wind variables from the BR2.8T simulation were analyzed. The Doppler wind at lower altitudes shifted from having a southerly to a northerly component which was captured in all simulations, albeit not as prominent as the observations (Figs. 7b to d and S6g). Table 1 shows a strong shift in the V-wind median and interquartile range from 20.53 to $-0.72 \text{m s}^{-1}$ and 6.63 to 21.26 $\text{m s}^{-1}$ respectively compared to the U-wind which had a small variability between the early and middle period. The wind shear, especially for the V-wind component, and the associated updrafts (fig 7) may have contributed to an enhanced SIP rate between 3 and 5 km in the collisional breakup simulations. Strong shear layers at low-levels approaching a barrier was emphasized by Houze and Medina (2005) to set up turbulence which in turn aids in precipitation growth (by accretion) on the windward side of a mountain. Medina et al. (2005) showed in idealized simulations that a shear layer can develop as a response of flow to the terrain, by which they concluded that this mechanism, in actual topography, caused turbulent overturning which enhanced precipitation formation. In their simulation, the precipitation formation was linked to enhanced accretion (see also Medina and Houze, 2015). In our study, the enhanced interaction between ice particles can cause enhanced ice-graupel collisions. Figure 6 (e to h) show the vertical profiles as a PDF for each model level for the temperatures during the middle period, which are synthesized for the entire layer in figure 6 (a to d), the PDF of the entire layer. As the afternoon progressed the median of the strongest V-wind shear
ascended from near the surface at 14:30 to 5 km amsl at 16:30 (Figs. 6 and 7). Above this level of strong vertical wind shear between 10 and 20 m s\(^{-1}\) km\(^{-1}\) updraft cells appeared. Houze and Medina (2005) and Medina and Houze (2015) illustrated that updraft cells occurred at times and locations where the shear was strongest (>\(\sim\) 10 m s\(^{-1}\) km\(^{-1}\)). During the middle time period, the variability in the V-wind shear was the largest with an interquartile range of 16.29 m s\(^{-1}\) km\(^{-1}\) which coincided with the highest SIP rate (Fig. 6d and Table 1). The vertical V-wind shear increased from 10 to 16 m s\(^{-1}\) km\(^{-1}\) (60% increase) and remained above 10 m s\(^{-1}\) km\(^{-1}\) below 4.4 km amsl (Fig. 6e and h). The joint PDF (\(P(SIP \text{ rate, V-wind shear})\)) illustrates that the median of correlation between the V-wind shear and SIP rate peaked at 9 m s\(^{-1}\) km\(^{-1}\) and 80 L\(^{-1}\) s\(^{-1}\) (Fig. 9e). This peak coincided with the region where the wind shifted from south-westerly to northerly (along the valley), predominantly as a result of the change in the V-wind speed from negative to positive at 2.9 km amsl. The joint probability between the V-wind and SIP (Fig. 9 b) was the highest at these altitudes. Here, the strong and variable V-wind shear was mostly responsible for the strong overall wind shear, which, not surprisingly, was the most important determinant of SIP of all the variables (Fig. 9f and Table 1). The contribution of the updraft velocity was not as clear. To understand the correlation of the wind variables to SIP rates, the mutual information and significance is discussed in the next paragraph. Figure 8 shows the normalized median of different variables in Table 1 during the three time periods. The increase (early to middle period) and decrease (middle to late period) of the median of the SIP rate were not as related with the U-wind shear or updraft as it was with the V-wind shear. It
Figure 7. Hofmoller diagrams of wind speed and vertical velocity for panels a) Doppler radar, b) RS, c) BR28, d) BR2.8T and e) BR-Sot between 13:00 and 17:30 UTC. The blue and red colors denote wind blowing towards and away from the radar respectively. The pink line is the homogeneous freezing line at 252 K, and the shaded gray area is the cloud area fraction.

Figure 8. Normalized median values of the PDFs of the variables in Table 1 for the three different time periods.

appeared that the V-wind shear played the major role in the SIP and to further show the significance we calculated the mutual information shared between different sets of variables.
Figure 9. Joint probability density function multiplied by bin area \((P(x, y)\Delta x\Delta y)\) for the model output of SIP versus (a) U-wind, (b) V-wind, (c) Updraft, (d) U-wind shear, (e) V-wind shear and (f) Wind shear. White lines are the 50\(^{th}\) percentile as a function of the \(x\)-axis variable.

The mutual information (MI: \(I(X; Y)\)) between variables \(X\) and \(Y\) was further analyzed for non-linear relationships (Shannon and Weaver, 1949) where \(X \in [\text{SIP rate}]\) and \(Y \in [\text{U-wind, V-wind, Updraft, U-wind shear, V-wind shear, Wind Shear}]\). \(I(X; Y)\) of 0 bits means no information is shared between \(X\) and \(Y\) and therefore \(Y\) cannot be inferred from \(X\). Further information about MI can be found in Appendix A and also in Dawe and Austin (2013). From the wind components, U-, V-wind and Updraft, \(I(\text{SIP rate}; \text{V-Wind})\) was the most informative, especially during the middle and last periods (Table 2). Consistent with this was that \(I(\text{SIP rate}; \text{V-Wind shear})\) was more than \(I(\text{SIP rate}; \text{U-Wind shear})\), but it was only significant during the early and middle periods. The higher MI values for V-wind shear with SIP is most likely why the wind shear had larger and significant MI values with SIP. During the last period the mean wind shear decreased slightly by 2.2 m s\(^{-1}\) km\(^{-1}\) while the variability decreased substantially by 7.3 m s\(^{-1}\) km\(^{-1}\) as a result in the weakening of the V-wind shear (Fig. 7 and Table 1). The relationship of \(I(\text{SIP rate}; \text{Wind shear})\) weakened drastically to 0.021 bits and was not significant any longer. This was expected because the diminishing cloud liquid water caused a reduction in the riming rates and therefore graupel formation which in turn reduced ice-graupel collisions. Because the mean wind shear was still strong it would be expected that the aggregation rates would persist between ice and snow crystals. Interestingly, \(I(\text{SIP rate}; \text{Updraft})\) was significant, but most likely for the previously discussed relationship that exists between the wind shear and updraft cell development.

The reason for the impact of the wind shear on the SIP rate was a result of the strengthening of the northerly valley winds during the early afternoon hours when the predominant wind aloft was south-westerly (generating the dominant V-wind shear).
Table 1. The 25th, 50th and 75th percentiles and the interquartile range (IQR) between the 10th and 90th percentiles of the vertical profiles for the BR2.8T simulations.

<table>
<thead>
<tr>
<th>Time (UTC)</th>
<th>Variable</th>
<th>25th perc.</th>
<th>50th perc.</th>
<th>75th perc.</th>
<th>IQR.</th>
</tr>
</thead>
<tbody>
<tr>
<td>13:00-14:15</td>
<td>SIP rate (L^{-1}s^{-1})</td>
<td>0.04</td>
<td>0.44</td>
<td>3.45</td>
<td>3.41</td>
</tr>
<tr>
<td></td>
<td>U-Wind (m s^{-1})</td>
<td>3.85</td>
<td>7.88</td>
<td>11.28</td>
<td>7.43</td>
</tr>
<tr>
<td></td>
<td>V-Wind (m s^{-1})</td>
<td>15.89</td>
<td>20.53</td>
<td>22.52</td>
<td>6.63</td>
</tr>
<tr>
<td></td>
<td>Wind Speed (m s^{-1})</td>
<td>16.28</td>
<td>22.92</td>
<td>24.82</td>
<td>8.54</td>
</tr>
<tr>
<td></td>
<td>Updraft (m s^{-1})</td>
<td>0.17</td>
<td>0.57</td>
<td>0.95</td>
<td>0.79</td>
</tr>
<tr>
<td></td>
<td>U-Wind Shear (m s^{-1} km^{-1})</td>
<td>1.99</td>
<td>4.26</td>
<td>7.44</td>
<td>5.45</td>
</tr>
<tr>
<td></td>
<td>V-Wind Shear (m s^{-1} km^{-1})</td>
<td>1.64</td>
<td>3.93</td>
<td>10.67</td>
<td>9.02</td>
</tr>
<tr>
<td></td>
<td>Wind Shear (m s^{-1} km^{-1})</td>
<td>4.05</td>
<td>7.10</td>
<td>14.75</td>
<td>10.70</td>
</tr>
<tr>
<td>14:30-15:45</td>
<td>SIP rate (L^{-1}s^{-1})</td>
<td>4.73</td>
<td>28.52</td>
<td>78.65</td>
<td>73.92</td>
</tr>
<tr>
<td></td>
<td>U-Wind (m s^{-1})</td>
<td>0.82</td>
<td>4.22</td>
<td>8.64</td>
<td>7.81</td>
</tr>
<tr>
<td></td>
<td>V-Wind (m s^{-1})</td>
<td>-5.51</td>
<td>-0.72</td>
<td>15.76</td>
<td>21.27</td>
</tr>
<tr>
<td></td>
<td>Wind Speed (m s^{-1})</td>
<td>6.53</td>
<td>10.25</td>
<td>17.34</td>
<td>10.80</td>
</tr>
<tr>
<td></td>
<td>Updraft (m s^{-1})</td>
<td>0.05</td>
<td>0.45</td>
<td>0.87</td>
<td>0.83</td>
</tr>
<tr>
<td></td>
<td>U-Wind Shear (m s^{-1} km^{-1})</td>
<td>4.14</td>
<td>8.43</td>
<td>13.94</td>
<td>9.80</td>
</tr>
<tr>
<td></td>
<td>V-Wind Shear (m s^{-1} km^{-1})</td>
<td>3.43</td>
<td>9.39</td>
<td>19.72</td>
<td>16.29</td>
</tr>
<tr>
<td></td>
<td>Wind Shear (m s^{-1} km^{-1})</td>
<td>8.59</td>
<td>16.78</td>
<td>25.16</td>
<td>16.57</td>
</tr>
<tr>
<td>16:00-17:15</td>
<td>SIP rate (L^{-1}s^{-1})</td>
<td>0.76</td>
<td>17.15</td>
<td>53.24</td>
<td>52.48</td>
</tr>
<tr>
<td></td>
<td>U-Wind (m s^{-1})</td>
<td>5.25</td>
<td>10.41</td>
<td>15.41</td>
<td>10.15</td>
</tr>
<tr>
<td></td>
<td>V-Wind (m s^{-1})</td>
<td>-2.24</td>
<td>-0.22</td>
<td>3.73</td>
<td>5.97</td>
</tr>
<tr>
<td></td>
<td>Wind Speed (m s^{-1})</td>
<td>7.43</td>
<td>12.37</td>
<td>16.58</td>
<td>9.15</td>
</tr>
<tr>
<td></td>
<td>Updraft (m s^{-1})</td>
<td>-0.04</td>
<td>0.18</td>
<td>0.45</td>
<td>0.49</td>
</tr>
<tr>
<td></td>
<td>U-Wind Shear (m s^{-1} km^{-1})</td>
<td>5.92</td>
<td>11.33</td>
<td>16.48</td>
<td>10.56</td>
</tr>
<tr>
<td></td>
<td>V-Wind Shear (m s^{-1} km^{-1})</td>
<td>3.07</td>
<td>6.05</td>
<td>9.84</td>
<td>6.77</td>
</tr>
<tr>
<td></td>
<td>Wind Shear (m s^{-1} km^{-1})</td>
<td>10.30</td>
<td>14.52</td>
<td>19.55</td>
<td>9.25</td>
</tr>
</tbody>
</table>

The development of the northerly winds could have been a result low-level blocking that occurred generating the shear layer (Medina et al., 2005). The sharp change in the wind speed and direction enhanced the turbulent overturning and therefore promoting the riming of ice crystals and snow leading to the formation of graupel which in turn enhanced the SIP rates. During the late period the overall wind shear only weakened slightly, but was not significant to the SIP because of the reduced graupel formation which is essential for ice-graupel collisions. We hypothesise that if ice-ice collisions were included in the model configuration, the simulations could well have captured the intense $K_d$ values in excess of 1.4 ° km^{-1} seen in Doppler observations after 16:40 UTC (Figs. S3e and S7). Such a configuration may have even shown a better correlation between the vertical wind shear and ice-ice collisions from 17:00 UTC on-wards. The diminishing graupel number concentration limited
Table 2. Mutual information between SIP rate and wind properties of the vertical profiles for the BR2.8T simulations. The significance level is calculated by taking the maximum of 1000 Monte Carlo simulations of mutual information between a random permutation of SIP rates and each variable.

<table>
<thead>
<tr>
<th>Time (UTC)</th>
<th>Variable</th>
<th>MI</th>
<th>Sig. level</th>
</tr>
</thead>
<tbody>
<tr>
<td>13:00-14:15</td>
<td>$I(SIP \text{ rate}; U-Wind)$</td>
<td>0.025</td>
<td>0.009</td>
</tr>
<tr>
<td></td>
<td>$I(SIP \text{ rate}; V-Wind)$</td>
<td>0.037</td>
<td>0.009</td>
</tr>
<tr>
<td></td>
<td>$I(SIP \text{ rate}; \text{Wind speed})$</td>
<td>0.029</td>
<td>0.009</td>
</tr>
<tr>
<td></td>
<td>$I(SIP \text{ rate}; \text{Updraft})$</td>
<td>0.027</td>
<td>0.009</td>
</tr>
<tr>
<td></td>
<td>$I(SIP \text{ rate}; U-Wind Shear)$</td>
<td>0.008</td>
<td>0.011</td>
</tr>
<tr>
<td></td>
<td>$I(SIP \text{ rate}; V-Wind Shear)$</td>
<td>0.015</td>
<td>0.011</td>
</tr>
<tr>
<td></td>
<td>$I(SIP \text{ rate}; \text{Wind Shear})$</td>
<td>0.011</td>
<td>0.009</td>
</tr>
<tr>
<td>14:30-15:45</td>
<td>$I(SIP \text{ rate}; U-Wind)$</td>
<td>0.091</td>
<td>0.018</td>
</tr>
<tr>
<td></td>
<td>$I(SIP \text{ rate}; V-Wind)$</td>
<td>0.116</td>
<td>0.018</td>
</tr>
<tr>
<td></td>
<td>$I(SIP \text{ rate}; \text{Wind speed})$</td>
<td>0.112</td>
<td>0.018</td>
</tr>
<tr>
<td></td>
<td>$I(SIP \text{ rate}; \text{Updraft})$</td>
<td>0.035</td>
<td>0.018</td>
</tr>
<tr>
<td></td>
<td>$I(SIP \text{ rate}; U-Wind Shear)$</td>
<td>0.039</td>
<td>0.022</td>
</tr>
<tr>
<td></td>
<td>$I(SIP \text{ rate}; V-Wind Shear)$</td>
<td>0.043</td>
<td>0.021</td>
</tr>
<tr>
<td></td>
<td>$I(SIP \text{ rate}; \text{Wind Shear})$</td>
<td>0.048</td>
<td>0.015</td>
</tr>
<tr>
<td>16:00-17:15</td>
<td>$I(SIP \text{ rate}; U-Wind)$</td>
<td>0.105</td>
<td>0.054</td>
</tr>
<tr>
<td></td>
<td>$I(SIP \text{ rate}; V-Wind)$</td>
<td>0.117</td>
<td>0.054</td>
</tr>
<tr>
<td></td>
<td>$I(SIP \text{ rate}; \text{Wind speed})$</td>
<td>0.103</td>
<td>0.054</td>
</tr>
<tr>
<td></td>
<td>$I(SIP \text{ rate}; \text{Updraft})$</td>
<td>0.095</td>
<td>0.054</td>
</tr>
<tr>
<td></td>
<td>$I(SIP \text{ rate}; U-Wind Shear)$</td>
<td>0.014</td>
<td>0.067</td>
</tr>
<tr>
<td></td>
<td>$I(SIP \text{ rate}; V-Wind Shear)$</td>
<td>0.029</td>
<td>0.067</td>
</tr>
<tr>
<td></td>
<td>$I(SIP \text{ rate}; \text{Wind Shear})$</td>
<td>0.021</td>
<td>0.055</td>
</tr>
</tbody>
</table>

the duration of SIP in our results and revealed a shortcoming in describing ice number concentrations through ice-graupel collisions when clouds enter a glaciated state.

3.3 SIP sensitivity to conversion rates

In this section the sensitivity of SIP to the rate of graupel formation, which is dependent on ice or snow crystals being larger than a given size when riming occurs, is analyzed. Fig. 10 shows the PSD for the sensitivity studies during which the size restrictions are modified which could slow the conversion process of the ice crystals and snow particles to graupel. The PSD over the cross-section at 15:30 UTC showed little difference in the ice crystal number concentrations where we expected higher ice crystal number concentration for BR2.8T and consequently higher snow number concentrations due to enhanced aggregation (Fig. 10a and b). The largest differences from the BR2.8T_300 simulation were in the form of enhanced
Table 3. The Kullback-Leibler divergence, $D_{KL}(P \parallel Q)$, between two probability distributions $P$ and $Q$ from 14:14 to 15:45 UTC. $P$ (BR2.8T_300, BR2.8T_400 and BR2.8T_500) is the measured probability distribution against the reference probability distribution $Q$ (BR2.8T). Each distribution consist of $\sim$10800 grid points separated into 24 bins over the cross-section in Fig. 1.

<table>
<thead>
<tr>
<th>Variable</th>
<th>$P$</th>
<th>$Q$</th>
<th>$D_{KL}(P \parallel Q)$ (bits)</th>
</tr>
</thead>
<tbody>
<tr>
<td>NISG</td>
<td>BR2.8T_300</td>
<td>BR2.8T</td>
<td>0.064</td>
</tr>
<tr>
<td></td>
<td>BR2.8T_400</td>
<td></td>
<td>0.026</td>
</tr>
<tr>
<td></td>
<td>BR2.8T_500</td>
<td></td>
<td>0.032</td>
</tr>
<tr>
<td>SIP</td>
<td>BR2.8T_300</td>
<td>BR2.8T</td>
<td>1.067</td>
</tr>
<tr>
<td></td>
<td>BR2.8T_400</td>
<td></td>
<td>0.055</td>
</tr>
<tr>
<td></td>
<td>BR2.8T_500</td>
<td></td>
<td>0.063</td>
</tr>
<tr>
<td>Ice</td>
<td>BR2.8T_300</td>
<td>BR2.8T</td>
<td>0.054</td>
</tr>
<tr>
<td></td>
<td>BR2.8T_400</td>
<td></td>
<td>0.019</td>
</tr>
<tr>
<td></td>
<td>BR2.8T_500</td>
<td></td>
<td>0.029</td>
</tr>
<tr>
<td>Graupel</td>
<td>BR2.8T_300</td>
<td>BR2.8T</td>
<td>3.327</td>
</tr>
<tr>
<td></td>
<td>BR2.8T_400</td>
<td></td>
<td>0.842</td>
</tr>
<tr>
<td></td>
<td>BR2.8T_500</td>
<td></td>
<td>0.608</td>
</tr>
</tbody>
</table>

Snow (for diameters: $0.14 < D_s < 0.42$ mm) and graupel number concentrations (for diameters: $1.2 < D_g < 2.2$ mm). However, at 15:30 UTC there is no clear signal beyond model variability, showing that the slower conversion rates to graupel affect the simulations (Fig. 10b and c). To further illustrate this point, we compared the probability distributions of the total number of ice hydrometeors (NISG), SIP rate, ice crystal and graupel number concentrations of the simulations over the vertical cross-sections when the largest graupel concentrations were observed between 14:15 to 15:45 UTC (Fig. 3b). The Kullback-Leibler divergence ($D_{KL}(P \parallel Q)$), which measures how one probability distribution $P$ is different from a second probability distribution, $Q$, shows little information loss between variables in Table 3, except for graupel. A value of 0 bits means that the probability distributions are the same (e.g., no information loss). The largest $D_{KL}(\text{BR2.8T}_300 \parallel \text{BR2.8T})$ was 3.327 bits for the graupel distribution and was reflected in larger differences in the SIP rate of of 1.067 bits and ice number concentration of 0.054 bits (Table 3 and Fig. 10c). If the SIP rate was sensitive to the conversion rate it is expected that the information loss would be the greatest between BR2.8T_500 and BR2.8T and not between BR2.8T_300 and BR2.8T (e.g., $D_{KL}(\text{BR2.8T}_500 \parallel \text{BR2.8T}) > D_{KL}(\text{BR2.8T}_400 \parallel \text{BR2.8T}) > D_{KL}(\text{BR2.8T}_300 \parallel \text{BR2.8T})$). This result leads us to conclude that the different conversion rates from ice crystals and snow to graupel, used in the paper in conjunction with the collisional breakup parameterization, were not significant for SIP.
Figure 10. Particle size distribution over the number concentrations for panels a) ice, b) snow, c) graupel, d) cloud droplets and e) raindrops for all the sensitivity simulations at 15:30 UTC. BR2.8T, BR2.8T_300, BR2.8T_400 and BR2.8T_500 represent the size restriction of 200, 300, 400 and 500 µm respectively before ice crystals and snow can be converted to graupel.

4 Conclusions

A cold front passage on 26 March 2010, over the Swiss Alps, associated with strong vertical wind shear and high polarimetric signatures was observed with a dual-polarization Doppler weather radar deployed at Davos. This study investigates the role of vertical wind shear on the rate of SIP by making simulations of wintertime orographic MPCs with a non-hydrostatic, limited area model, COSMO, which has a two-moment bulk microphysics scheme with six hydrometeor categories, and two additional parameterizations for ice-graupel collisions (e.g., Sotiropoulou et al., 2020; Dedekind, 2021) based on Takahashi et al. (1995). To conclude, our main finding can be summarized as follows:

– Large and colocated values of $Z_{DR} > 1$ dB and $K_{dp} > 1^\circ$ km$^{-1}$ suggest that a large population of oblate particles was present, most likely originated by ice-ice collisions, at 4 km amsl. This level coincided with the $-15^\circ$C isotherm which
supports evidence of fast, low-density dendrite growth which is prone to fracturing and aggregating. At lower altitudes $Z_H$ increased while $K_{dp}$ and $Z_{DR}$ decreased suggesting aggregation and/or riming were occurring.

– The rime splintering simulations overestimated the $Z_H$ through out the vertical profile and underestimated the disdrometers’ number concentration of hydrometeors at the surface. Both shortcomings can be explained by the omission of ice-graupel collisions.

– The breakup simulations (BR28, BR2.8T and BR-Sot) caused narrower ice crystal and snow distributions (enhanced number concentrations of smaller ice particles) resulting in a better representation of $Z_H$. The enhanced number concentrations of ice particles meant that these simulations, in particular BR2.8T and BR-Sot, captured the disdrometer observations of $\sim 20 \text{ L}^{-1}$ at 15:30 and 17:00 UTC.

– During the middle period, 14:30-15:45 UTC, the V-wind shear increased by 60% causing conditions favorable for accretion causing enhanced graupel formation and SIP in the region favorable for SIP.

– Another time period with high $K_{dp}$, but low $Z_{DR}$ was observed at 17:00 which was not captured by the breakup simulations because the graupel mixing ratio was depleted. The breakup parameterization does not include ice-ice collisions and relies only on graupel as the collider specie. At this time the radar signatures suggested that dendrite collisions caused the formation of small oblate particles (increasing $K_{dp}$) but also the formation of a few, larger, isotropic aggregates (decreasing $Z_{DR}$).

– The mutual information between the SIP rate and other variables like vertical wind shear and updraft velocity suggested that the SIP rate is best predicted by the overall wind shear.

– The sensitivity of the ice-graupel simulations to the conversion rate size restriction was measured using the Kullback-Leibler divergence. Ice and snow (with diameters of 300 µm) that were converted to graupel showed the biggest deviation from the reference size of 200 µm. However, the sensitivity simulations were not sensitive to the conversion rate size restriction.

Turbulent overturning, whether it is associated with and not exclusive to i.e., baroclinic waves (Gehring et al., 2020) or low-level blocking (Medina et al., 2005; Houze and Medina, 2005; Medina and Houze, 2015), has been shown to play an important role in accreting hydrometeors to form precipitation. Here, we considered that the interactions of ice hydrometeors can lead to ice-graupel collisions, causing enhanced small ice fragments, as opposed to only growing larger through aggregation. These smaller fragments fall slower against updraft and may decrease local precipitation rates enhancing precipitation downstream of the flow (Dedekind et al., 2021). Wind shear plays a significant role in ice-graupel collisions and may even be more important when all ice-ice collisions are considered in more physically robust collisional breakup parameterizations (Yano and Phillips, 2011; Phillips et al., 2017). By only considering ice-graupel collisions we are limited to mainly investigating collisional breakup in MPCs where riming can occur to form graupel. In the case where a cloud becomes glaciated and graupel cannot form through riming, our parameterization will not be able to simulate SIP, which may still prove to be very important. In the case of using
more advanced collisional breakup parameterizations, the burst of \( K_{dp} \) (small oblate particles) observed at 17:00 in our case study can most likely be explained by models. It may even highlight a stronger correlation between the wind shear and ice-ice collisions than shown here which ultimately would impact the location and timing of precipitation.

5 Data availability

The COSMO model output, radar and 2DVD datasets used for our analysis are available at https://doi.org/10.5281/zenodo.6609251 and the software to analyze the data can be found at https://doi.org/10.5281/zenodo.6612296

Appendix A: Mutual Information

The entropy \( H \) of the variable \( x \)’s probability density function \( P(x) \) is defined by Shannon and Weaver (1949) to be:

\[
H = - \int P(x) \ln(P(x)) \, dx
\]  

(A1)

where \( x \) is the information content of a single measurement of \( P(x) = -\ln P(x) \). The entropy is a measure of the amount of information that is required to represent the PDF. From here both the Kullback-Leibler divergence and the mutual information can be calculated.

The Kullback-Leibler divergence, also known as the relative entropy, measures the distance between two probability distributions, \( P(x) \) and \( Q(x) \) over a discrete random variable \( X \). The Kullback-Leibler divergence is defined as follows:

\[
D_{KL}(P \parallel Q) = \int P(x) \ln \left( \frac{P(x)}{Q(x)} \right) \, dx.
\]  

(A2)

The mutual information (MI) is a measure of the mutual dependence between two random variable \( X \) and \( Y \) (e.g., the entropy of \( X \) subtracted from the entropy of \( X \) conditioned on \( Y \)):

\[
I(X;Y) = H(X) - H(X|Y).
\]  

(A3)

MI describes therefore how different the joint distribution of the pair \( (X,Y) \) is from the distribution of \( X \) and \( Y \). Combining equations (A1) and (A3) yield:

\[
I(X;Y) = \int [P(x) \ln(P(x)) - P(x,y) \ln(P(x|y))] \, dx \, dy
\]  

(A4)
and because $P(x|y) = P(x,y)/P(y)$, equation (A5) can be reduced to:

$$I(X;Y) = -\int P(x,y) \ln \left( \frac{P(x,y)}{P(x)P(y)} \right) \, dx \, dy.$$  

(A5)

The range of the MI is described as follows:

$$\text{MI} = \begin{cases} 
0, & \text{if } P(x,y) = P(x)P(y), \quad (X \text{ and } Y \text{ are completely independent}) \\
H(X), & \text{if } P(x,y) = P(x) = P(y), \quad (X \text{ and } Y \text{ are perfectly correlated})
\end{cases}$$  

(A6)

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