

# 1 Characterization of Errors in Satellite-based HCHO/NO<sub>2</sub> 2 Tropospheric Column Ratios with Respect to Chemistry, Column to 3 PBL Translation, Spatial Representation, and Retrieval 4 Uncertainties 5 6

7 Amir H. Souri<sup>1\*</sup>, Matthew S. Johnson<sup>2</sup>, Glenn M. Wolfe<sup>3</sup>, James H. Crawford<sup>4</sup>, Alan Fried<sup>5</sup>, Armin  
8 Wisthaler<sup>6,7</sup>, William H. Brune<sup>8</sup>, Donald R. Blake<sup>9</sup>, Andrew J. Weinheimer<sup>10</sup>, Tijnl Verhoelst<sup>11</sup>,  
9 Steven Compornolle<sup>11</sup>, Gaia Pinardi<sup>11</sup>, Corinne Vigouroux<sup>11</sup>, Bavo Langerock<sup>11</sup>, Sungyeon  
10 Choi<sup>3,12</sup>, Lok Lamsal<sup>3,13</sup>, Lei Zhu<sup>14,15</sup>, Shuai Sun<sup>14,15</sup>, Ronald C. Cohen<sup>16,17</sup>, Kyung-Eun Min<sup>18</sup>,  
11 Changmin Cho<sup>18</sup>, Sajeev Philip<sup>19</sup>, Xiong Liu<sup>1</sup>, and Kelly Chance<sup>1</sup>  
12

13 <sup>1</sup>Atomic and Molecular Physics (AMP) Division, Center for Astrophysics | Harvard & Smithsonian,  
14 Cambridge, MA, USA

15 <sup>2</sup>Earth Science Division, NASA Ames Research Center, Moffett Field, CA, USA

16 <sup>3</sup>NASA Goddard Space Flight Center, Greenbelt, MD, USA

17 <sup>4</sup>NASA Langley Research Center, Hampton, VA, USA

18 <sup>5</sup>Institute of Arctic & Alpine Research, University of Colorado, Boulder, CO, USA

19 <sup>6</sup>Institute for Ion Physics and Applied Physics, University of Innsbruck, Technikerstrasse 25, 6020  
20 Innsbruck, Austria

21 <sup>7</sup>Department of Chemistry, University of Oslo, P.O. box 1033, Blindern, 0315 Oslo, Norway

22 <sup>8</sup>Department of Meteorology and Atmospheric Science, Pennsylvania State University, University Park,  
23 PA, USA

24 <sup>9</sup>Department of Chemistry, University of California, Irvine, CA, USA

25 <sup>10</sup>National Center for Atmospheric Research, Boulder, CO, USA

26 <sup>11</sup>Royal Belgian Institute for Space Aeronomy (BIRA-IASB), Ringlaan 3, 1180 Uccle, Belgium

27 <sup>12</sup>Science Systems and Applications, Inc., Lanham, MD 20706, USA

28 <sup>13</sup>Universities Space Research Association, Columbia, MD 21046, USA

29 <sup>14</sup>School of Environmental Science and Engineering, Southern University of Science and Technology,  
30 Shenzhen, Guangdong, China

31 <sup>15</sup>Guangdong Provincial Observation and Research Station for Coastal Atmosphere and Climate of the  
32 Greater Bay Area, Shenzhen, Guangdong, China

33 <sup>16</sup>Department of Earth and Planetary Science, University of California Berkeley, Berkeley, CA 94720, USA

34 <sup>17</sup>Department of Chemistry, University of California Berkeley, Berkeley, CA 94720, USA

35 <sup>18</sup>School of Earth Sciences and Environmental Engineering, Gwangju Institute of Science and Technology,  
36 Gwangju, South Korea

37 <sup>19</sup>Centre for Atmospheric Sciences, Indian Institute of Technology Delhi, New Delhi, India  
38

39 \* Corresponding Author: [ahsouri@cfa.harvard.edu](mailto:ahsouri@cfa.harvard.edu)  
40

## 41 **Abstract.**

42 The availability of formaldehyde (HCHO) (a proxy for volatile organic compound  
43 reactivity) and nitrogen dioxide (NO<sub>2</sub>) (a proxy for nitrogen oxides) tropospheric columns from  
44 Ultraviolet-Visible (UV-Vis) satellites has motivated many to use their ratios to gain some insights  
45 into the near-surface ozone sensitivity. Strong emphasis has been placed on the challenges that  
46 come with transforming what is being observed in the tropospheric column to what is actually in  
47 the planetary boundary layer (PBL) and near to the surface; however, little attention has been paid

48 to other sources of error such as chemistry, spatial representation, and retrieval uncertainties. Here  
49 we leverage a wide spectrum of tools and data to carefully quantify those errors.

50 Concerning the chemistry error, a well-characterized box model constrained by more than  
51 500 hours of aircraft data from NASA's air quality campaigns is used to simulate the ratio of the  
52 chemical loss of HO<sub>2</sub>+RO<sub>2</sub> (LRO<sub>x</sub>) to the chemical loss of NO<sub>x</sub> (LNO<sub>x</sub>). Subsequently, we  
53 challenge the predictive power of HCHO/NO<sub>2</sub> ratios (FNRs), which are commonly applied in  
54 current research, at detecting the underlying ozone regimes by comparing them to LRO<sub>x</sub>/LNO<sub>x</sub>.  
55 FNRs show a strongly linear ( $R^2=0.94$ ) relationship to LRO<sub>x</sub>/LNO<sub>x</sub> in the log-log scale. Following  
56 the baseline (i.e.,  $\ln(\text{LRO}_x/\text{LNO}_x) = -1.0 \pm 0.2$ ) with the model and mechanism (CB06, r2) used for  
57 segregating NO<sub>x</sub>-sensitive from VOC-sensitive regimes, we observe a broad range of FNR  
58 thresholds ranging from 1 to 4. The transitioning ratios strictly follow a Gaussian distribution with  
59 a mean and standard deviation of 1.8 and 0.4, respectively. This implies that FNR has an inherent  
60 20% standard error (1-sigma) resulting from not being able to fully describe the RO<sub>x</sub>-HO<sub>x</sub> cycle.  
61 We calculate high ozone production rates (PO<sub>3</sub>) dominated by large HCHO×NO<sub>2</sub> concentration  
62 levels, a new proxy for the abundance of ozone precursors. The relationship between PO<sub>3</sub> and  
63 HCHO×NO<sub>2</sub> becomes more pronounced when moving towards NO<sub>x</sub>-sensitive regions due to non-  
64 linear chemistry; our results indicate that there is fruitful information in the HCHO×NO<sub>2</sub> metric  
65 that has not been utilized in ozone studies. The vast amount of vertical information on HCHO and  
66 NO<sub>2</sub> concentration from the air quality campaigns enables us to parameterize the vertical shapes  
67 of FNRs using a second-order rational function permitting an analytical solution for an altitude  
68 adjustment factor to partition the tropospheric columns to the PBL region. We propose a  
69 mathematical solution to the spatial representation error based on modeling isotropic  
70 semivariograms. With respect to a high-resolution sensor like Tropospheric Monitoring  
71 Instrument (TROPOMI) (>5.5×3.5 km<sup>2</sup>), Ozone Monitoring Instrument (OMI) loses 12% of  
72 spatial information at its native resolution. A pixel with a grid size of 216 km<sup>2</sup> fails at capturing  
73 ~65% of the spatial information in FNRs at a 50 km length scale comparable to the size of a large  
74 urban center (e.g., Los Angeles). We ultimately leverage a large suite of in-situ and ground-based  
75 remote sensing measurements to draw the error distributions of daily TROPOMI and OMI  
76 tropospheric NO<sub>2</sub> and HCHO columns. At 68% confidence interval (1 sigma) errors pertaining to  
77 daily TROPOMI observations, either HCHO or tropospheric NO<sub>2</sub> columns should be above 1.2-  
78 1.5×10<sup>16</sup> molec.cm<sup>-2</sup> to attain 20-30% standard error in the ratio. This level of error is almost non-  
79 achievable with OMI given its large error in HCHO.

80 The satellite column retrieval error is the largest contributor to the total error (40-90%) in  
81 the FNRs. Due to a stronger signal in cities, the total relative error (<50%) tends to be mild,  
82 whereas areas with low vegetation and anthropogenic sources (e.g., Rocky Mountains) are  
83 markedly uncertain (>100%). Our study suggests that continuing development in the retrieval  
84 algorithm and sensor design and calibration is essential to be able to advance the application of  
85 FNRs beyond a qualitative metric.

## 86 1. Introduction

87 Accurately representing the near-surface ozone (O<sub>3</sub>) sensitivity to its two major precursors,  
88 nitrogen oxides (NO<sub>x</sub>) and volatile organic compounds (VOCs), is an imperative step in  
89 understanding non-linear chemistry associated with ozone production rates in the atmosphere.  
90 While it is often tempting to characterize an airshed as NO<sub>x</sub> or VOC-sensitive, both conditions are  
91 expected as VOC-sensitive (ozone production rates sensitive to VOC) conditions near NO<sub>x</sub>  
92 sources transition to NO<sub>x</sub>-sensitive (ozone production rates sensitive to NO<sub>x</sub>) conditions  
93 downwind as NO<sub>x</sub> dilutes. Thus, reducing the footprint of ozone production can mostly be

94 achieved through NO<sub>x</sub> reductions. VOCs are key to determining both the location and peak in  
95 ozone production which varies nonlinearly to the NO<sub>x</sub> abundance. Thus, knowledge of the relative  
96 levels of NO<sub>x</sub> and VOCs informs the trajectory of ozone production and expectations of where  
97 peak ozone will occur as emissions change. While the near-surface ambient nitrogen dioxide (NO<sub>2</sub>)  
98 concentrations are regularly monitored by a large number of surface stations, the measurements of  
99 several VOCs with different reactivity rates with respect to hydroxyl (OH), are not routinely  
100 available. As such, our knowledge on where and when ozone production rates are elevated, and  
101 their quantitative dependence on a long list of ozone precursors, is fairly limited, except for  
102 observationally-rich air quality campaigns. This limitation has prompted several studies such as  
103 Sillman et al. (1990), Tonnesen and Dennis (2000a,b), and Sillman and He (2002) to investigate if  
104 the ratio of certain measurable compounds can diagnose ozone regimes meaning if the ozone  
105 production rate is sensitive to NO<sub>x</sub> (i.e., NO<sub>x</sub>-sensitive) or VOC (i.e., VOC-sensitive). Sillman  
106 and He (2002) suggested that H<sub>2</sub>O<sub>2</sub>/HNO<sub>3</sub> was a robust measurable ozone indicator as this ratio  
107 could well describe the chemical loss of HO<sub>2</sub>+RO<sub>2</sub> (LRO<sub>x</sub>) to the chemical loss of NO<sub>x</sub> (LNO<sub>x</sub>)  
108 controlling the O<sub>3</sub>-NO<sub>x</sub>-VOC chemistry (Kleinman et al., 2001). Nonetheless, both H<sub>2</sub>O<sub>2</sub> and  
109 HNO<sub>3</sub> measurements are limited to few spatially-sparse air quality campaigns.

110 Formaldehyde (HCHO) is an oxidation product of VOCs and its relatively short lifetime  
111 (~1-9 hr) makes the location of its primary and secondary sources rather identifiable (Seinfeld and  
112 Pandis, 2006; Fried et al., 2020). Fortunately, monitoring HCHO abundance in the atmosphere has  
113 been a key goal of many Ultraviolet-Visible (UV-Vis) viewing satellites for decades (Chance et  
114 al., 1991; Chance et al., 1997; Chance et al., 2000; González Abad et al., 2015; De Smedt et al.,  
115 2008, 2012, 2015, 2018, 2021) with reasonable spatial coverage. Additionally, the strong  
116 absorption of NO<sub>2</sub> in the UV-Vis range has permitted measurements of NO<sub>2</sub> columns from space  
117 (Martin et al., 2002; Boersma et al., 2004, 2007, 2018).

118 Advancements in satellite remote-sensing of these two key compounds have encouraged  
119 many studies to elucidate if the ratio of HCHO/NO<sub>2</sub> (hereafter FNR) could be a robust ozone  
120 indicator (Tonnesen and Dennis, 2000b; Martin et al. 2004, Duncan et al., 2010). Most studies  
121 using the satellite-based FNR columns attempted to provide a qualitative view of the underlying  
122 chemical regimes (e.g., Choi et al., 2012; Choi and Souri, 2015a,b; Jin and Holloway, 2015; Souri  
123 et al., 2017; Jeon et al., 2018; Lee et al., 2021). Relatively few studies (Duncan et al., 2010; Jin et  
124 al., 2017; Schroeder et al., 2017; Souri et al., 2020) have carefully tried to provide a quantitative  
125 view of the usefulness of the ratio. For the most part, the inhomogeneous vertical distribution of  
126 FNR in columns has been emphasized. Jin et al. (2017) and Schroeder et al. (2017) showed that  
127 differing vertical shapes of HCHO and NO<sub>2</sub> can cause the vertical shape of FNR not to be  
128 consistent throughout the troposphere leading to a variable relationship between what is being  
129 observed from the satellite and what is actually occurring in the lower atmosphere. Jin et al. (2017)  
130 calculated an adjustment factor to translate the column to the surface using a relatively coarse  
131 global chemical transport model. The adjustment factor showed a clear seasonal cycle stemming  
132 from spatial and temporal variability associated with the vertical sources and sinks of HCHO and  
133 NO<sub>2</sub>, in addition to the atmospheric dynamics. In a more data driven approach, Schroeder et al.  
134 (2017) found that the detailed differences in the boundary layer vertical distributions of HCHO  
135 and NO<sub>2</sub> lead to a wide range of ambiguous ratios. Additionally, ratios were shown to shift on high  
136 ozone days, raising questions regarding the value of satellite averages over longer timescales. A  
137 goal for our research is to put together an integrated and data-driven mathematical formula to  
138 translate the tropospheric column to the planetary boundary layer (PBL), exploiting the abundant  
139 aircraft measurements available during ozone seasons.

140 Using observationally-constrained box models, Souri et al. (2020) demonstrated that there  
141 was a fundamentally inherent uncertainty related to the ratio originating from the chemical  
142 dependency of HCHO on NO<sub>x</sub> (Wolfe et al., 2016). In VOC-rich (poor) environments, the  
143 transitioning ratios from NO<sub>x</sub>-sensitive to VOC-sensitive occurred in larger (smaller) values than  
144 the conventional thresholds defined in Duncan et al. (2010) due to an increased (dampened) HCHO  
145 production induced by NO<sub>x</sub>. To account for the chemical feedback and to prevent a wide range of  
146 thresholds on segregating NO<sub>x</sub>-sensitive from VOC-sensitive regions, Souri et al. (2020)  
147 suggested using a first-order polynomial matched to the ridgeline in P(O<sub>3</sub>) isopleths. Their study  
148 illuminated the fact that the ratio suffers from an inherent chemical complication. However, Souri  
149 et al. (2020) did not quantify the error and their work was limited to a subset of atmospheric  
150 condition. To challenge the predictive power of FNR from chemistry perspective, we will take  
151 advantage of a large suite of datasets to make maximum use of varying meteorological and  
152 chemical conditions.

153 Not only are satellite-based column measurements unable to resolve the vertical  
154 information of chemical species in the tropospheric column, but they are also unable to resolve the  
155 horizontal spatial variability due to their spatial footprint. The larger the footprint is, the more  
156 horizontal information is blurred out. For instance, Souri et al. (2020) observed a substantial spatial  
157 variance (information) in FNR columns at the spatial resolution of 250×250 m<sup>2</sup> observed by an  
158 airborne sensor over Seoul, South Korea. It is intuitively clear that a coarse resolution sensor would  
159 lose a large degree of spatial variance (information). This error, known as the spatial representation  
160 error, has not been studied with respect to FNR. We will leverage what we have learned from Souri  
161 et al. (2022), which modeled the spatial heterogeneity in discrete data using geostatistics, to  
162 quantify the spatial representation error in the ratio over an urban environment.

163 A longstanding challenge is to have a reliable estimate on the satellite retrieval errors of  
164 tropospheric column NO<sub>2</sub> and HCHO. Significant efforts have been made recently to assemble,  
165 analyze, and estimate the retrieval errors for two key satellite sensors, TROPOspheric Monitoring  
166 Instrument (TROPOMI) and Ozone Monitoring Instrument (OMI), using various in-situ  
167 measurements (Verhoelst et al., 2021; Vigouroux et al., 2020, Choi et al., 2020; Laughner et al.,  
168 2019; Zhu et al., 2020). In this study, we will exploit paired comparisons from some of these new  
169 studies to propagate individual uncertainties in HCHO and NO<sub>2</sub> to the FNR errors.

170 The overarching science goal of this study is to address the fact that the accurate diagnosis  
171 of surface O<sub>3</sub> photochemical regimes is impeded by numerous uncertainty components, which will  
172 be addressed in the current paper, and can be classified into four major categories: i) inherent  
173 uncertainties associated with the approach of FNRs to diagnose local O<sub>3</sub> production and sensitivity  
174 regimes, ii) translation of tropospheric column satellite retrievals to represent PBL- or surface-  
175 level chemistry, iii) spatial representativity of ground pixels of satellite sensors, and iv)  
176 uncertainties associated with satellite-retrieved column-integrated concentrations of HCHO and  
177 NO<sub>2</sub>. We will address all of these sources of uncertainty using a broad spectrum of data and tools.

178 Our paper is organized with the following sections. Section 2 describes the chemical box  
179 model setup and data applied. Sections 3.1 to 3.4 deal with chemistry aspects of FNRs and show  
180 the results from a box model. Section 3.5 introduces a data-driven framework to transform the  
181 FNR tropospheric columns to the PBL region. Section 3.6 offers a new way to quantify the spatial  
182 representation error in satellites. Section 3.7 deals with the satellite error characterization and their  
183 impacts on the ratio. Section 3.8 summarizes the fractional contribution of each error to the  
184 combined error. Finally, Sect. 4 provides a summary and conclusions of the study.

## 185 2. Photochemical Box Modeling and Aircraft Data Used

186 To quantify the uncertainty of FNR from a chemistry perspective, and to obtain several  
187 imperative parameters including the calculated ozone production rates, and the loss of NO<sub>x</sub> (LNO<sub>x</sub>)  
188 and RO<sub>x</sub> (LRO<sub>x</sub>), we utilize the Framework for 0-D Atmospheric Modeling (F0AM) v4 (Wolfe et  
189 al., 2016). We adopt the Carbon Bond 6 (CB06, r2) chemical mechanism and heterogenous  
190 chemistry is not considered in our simulations. The model is initialized with the measurements of  
191 several compounds, many of which constrain the model by being held constant for each timestep  
192 (see Table 1).

193 Figure 1 shows the map of data points from Deriving Information on Surface Conditions  
194 from Column and Vertically Resolved Observations Relevant to Air Quality (DISCOVER-AQ)  
195 Baltimore-Washington (2011), DISCOVER-AQ Houston-Texas (2013), DISCOVER-AQ  
196 Colorado (2014), and Korea United States Air Quality Study (KORUS-AQ) (2016).  
197 Meteorological inputs come from the observed pressure, temperature, and relative humidity. The  
198 measurements of photolysis rates are not available for all photolysis reactions; therefore, our initial  
199 guess of those rates comes from a look-up-table populated by the National Center for Atmospheric  
200 Research (NCAR) Tropospheric Ultraviolet And Visible (TUV) model calculations. These values  
201 are a function of solar zenith angle, total ozone column density, surface albedo, and altitude. We  
202 set the total ozone column and the surface albedo to fixed numbers of 325 (Dobson) DU and 0.15,  
203 respectively. The initial guess is then corrected by applying the ratio of observed photolysis rates  
204 of NO<sub>2</sub>+hv (jNO<sub>2</sub>) and/or O<sub>3</sub>+hv (jO<sup>1</sup>D) to the calculated ones to all j-values (i.e., wavelength  
205 independent). If both observations of jNO<sub>2</sub> and jO<sup>1</sup>D are available, the correction factor is  
206 averaged. The KORUS-AQ campaign is the only one that provides jO<sup>1</sup>D measurements; therefore  
207 the use of the wavelength-independent correction factor based on the observed to calculated jNO<sub>2</sub>  
208 values for all j-values including jO<sup>1</sup>D is a potential source of error in the model especially when  
209 aerosols are present. The model calculations are based on the observations merged to a temporal  
210 resolution varying from 10 to 15 seconds. Each calculation was run for five consecutive days with  
211 an integration time of 1 hour to approach diel steady state. We test the number of solar cycle  
212 against ten days on the KORUS-AQ setup, and observe no noticeable difference in simulated OH  
213 and HCHO (Figure S1) indicating that five solar cycles suffice. Some secondarily-formed species  
214 must be unconstrained for the purpose of model validation. Therefore, the concentrations of several  
215 secondarily-formed compounds such as HCHO and PAN are unconstrained. Nitric oxide (NO) and  
216 NO<sub>2</sub> are also allowed to cycle, while their sum (i.e., NO<sub>x</sub>) is constrained. Because the model does  
217 not consider various physical loss pathways including deposition and transport, which vary by  
218 time and space, we oversimplify their physical loss through a first-order dilution rate set to  
219 1/86400-1/43200 s<sup>-1</sup> (i.e., 24- or 12-hr lifetime), which in turn prevents relatively long-lived  
220 species from accumulating over time. Our decision on unconstraining HCHO, a pivotal compound  
221 impacting the simulation of HO<sub>x</sub>, may introduce some systematic biases in the simulation of  
222 radicals determining ozone chemistry (Schroeder et al., 2020). Therefore, to mitigate the potential  
223 bias in HCHO, we set the dilution factor to maintain the campaign-averaged bias in the simulated  
224 HCHO with respect to observations of less than 5%. However, it is essential to recognize that  
225 HCHO can fluctuate freely for each point measurement because the dilution constraint is set to a  
226 fixed value for an individual campaign. Each time tag is independently simulated meaning we do  
227 not initialize the next run using the simulated values from the previous one; this in turn permits  
228 parallel computation. Regarding the KORUS-AQ campaign where HO<sub>x</sub> observations were  
229 available, we only ran the model for data points with HO<sub>x</sub> measurements. Similar to Souri et al.  
230 (2020), we filled gaps in VOC observations with a bilinear interpolation method with no

231 extrapolation allowed. In complex polluted atmospheric conditions such as that over Seoul, South  
 232 Korea, Souri et al. (2020) observed that this simplistic treatment yielded comparable results with  
 233 respect to the NASA LaRC model (Schroeder et al. 2020) which incorporated a more  
 234 comprehensive data harmonization. to Table 1 lists the major configuration along with the  
 235 observations used for the box model.

236 Several parameters are calculated based on the box model outputs.  $LRO_x$  is defined through  
 237 the sum of primarily radical-radical reactions:

$$LRO_x = k_{HO_2+HO_2}[HO_2]^2 + \sum k_{RO_{2i}+HO_2}[RO_{2i}][HO_2] + \sum k_{RO_{2i}+RO_{2i}}[RO_{2i}]^2 \quad (1)$$

238 where  $k$  is the reaction rate constant.  $LNO_x$  mainly occurs via the  $NO_2+OH$  reaction:

$$LNO_x = k_{OH+NO_2+M}[OH][NO_2][M] \quad (2)$$

239 where M is a third body. We calculate  $P(O_3)$  by subtracting the ozone loss pathways dictated by  
 240  $HO_x$  ( $HO+HO_2$ ),  $NO_2+OH$ ,  $O_3$  photolysis, ozonolysis, and the reaction of  $O(^1D)$  with water vapor  
 241 from the formation pathways through the removal of NO via  $HO_2$  and  $RO_2$ :

$$P(O_3) = k_{HO_2+NO}[HO_2][NO] + \sum k_{RO_{2i}+NO}[RO_{2i}][NO] - k_{OH+NO_2+M}[OH][NO_2][M] - P(RONO_2) - k_{HO_2+O_3}[HO_2][O_3] - k_{OH+O_3}[OH][O_3] - k_{O(^1D)+H_2O}[O(^1D)][H_2O] - L(O_3) + alkenes \quad (3)$$

## 242 3. Results and Discussion

### 243 3.1. Box Model Validation

244 There are uncertainties associated with the box model (e.g., Brune et al., 2022; Zhang et  
 245 al., 2021; Lee et al., 2021) which can be attributed to: i) the lack of inclusion of physical processes  
 246 such as entrainment/detrainment and diffusion, ii) discounting the heterogenous chemistry, iii)  
 247 invalid assumption of the diel steady state in areas close to large emission sources or in  
 248 photochemically less active environments (Thornton et al., 2002; Souri et al., 2021), iv) errors in  
 249 the chemical mechanism, and v) errors in the measurements. These limitations necessitate a  
 250 thorough validation of the model using unconstrained observations. While models have been  
 251 known for a long time to not be 100% accurate (Box, 1976), it is important to characterize whether  
 252 the model can effectively represent reality. For instance, if the simulated HCHO is poorly  
 253 correlated with observations and/or displayed large magnitude biases, it will be erroneous to  
 254 assume that the sources of HCHO along with relevant chemical pathways are appropriate. It is  
 255 important to acknowledge that the VOC constraints for these model calculations are incomplete,  
 256 especially for the DISCOVER-AQ campaigns which lacked comprehensive VOC observations.  
 257 Nevertheless, we will show that the selected VOCs are sufficient to reproduce a large variance  
 258 (>70%) in observed HCHO.

259 We diagnose the performance of the box model by comparing the simulated values of five  
 260 compounds to observations: HCHO, NO,  $NO_2$ , PAN, hydroperoxyl radical ( $HO_2$ ), and OH. Figure  
 261 2 depicts the scatterplot of the comparisons along with several statistics. HCHO observations are  
 262 usually constrained in box models to improve the representation of  $HO_2$  (Schroeder et al., 2017;  
 263 Souri et al., 2020; Brune et al., 2022); however, this constraint may mask the realistic  
 264 characterization of the chemical mechanism with respect to the treatment of VOCs. Additionally,

265 it is important to know if the sources of HCHO are adequate. Therefore, we detach the model from  
266 this constraint to carry out a more fair and stringent validation.

267 Concerning HCHO, our model does have considerable skill at reproducing the variability  
268 of observed HCHO ( $R^2=0.73$ ). To evaluate if this agreement is accidentally caused by the choice  
269 of the dilution factor and to identify if our VOC treatment is inferior compared to the one adopted  
270 in the NASA LaRC (Schroeder et al., 2021), we conducted three sets of sensitivity tests for the  
271 KORUS-AQ campaign, including ones with and without considering a dilution factor and another  
272 one without HNO<sub>3</sub> and H<sub>2</sub>O<sub>2</sub> constraints (Figure S2). When not considering a dilution factor results  
273 in no difference in the variance in HCHO captured by our model ( $R^2=0.81$ ). Our model without  
274 the dilution factor is still skillful at replicating the magnitude of HCHO with less than 12% bias.  
275 It is because of this reason that the optimal dilution factor for each camping is within 12 hr to 24  
276 hr which is not different than other box modeling studies (e.g., Brune et al., 2022; Miller and  
277 Brune, 2022). We observed no difference in the simulated HCHO when HNO<sub>3</sub> and H<sub>2</sub>O<sub>2</sub> values  
278 were not constrained. The unconstrained NASA LaRC setup oversampled at 10-sec frequency  
279 captures 86% variance in the measurements, only slightly (6%) outperforming our result.  
280 However, the unconstrained NASA LaRC setup greatly underestimates the magnitude of HCHO  
281 compared to our model results.

282 The model performs well with regards to the simulation of NO ( $R^2=0.89$ ) and NO<sub>2</sub>  
283 ( $R^2=0.99$ ) in the log scale. Immediately evident is the underestimation of NO in highly polluted  
284 regions contrary to an overestimation in clean ones. This discrepancy leads to an underestimation  
285 (overestimation) of NO/NO<sub>2</sub> in polluted (clean) regions. The primary drivers of NO/NO<sub>2</sub> are jNO<sub>2</sub>  
286 and O<sub>3</sub> both of which are constrained in the model. What can essentially deviate the partitioning  
287 between NO and NO<sub>2</sub> from that of observations in polluted areas is the assumption of the diel  
288 steady state which is rarely strictly valid where measurements are close to large emitters. The  
289 overestimation of NO in low NO<sub>x</sub> areas is often blamed on the lack of chemical sink pathways of  
290 NO in chemical mechanisms (e.g., Newland et al., 2021). A relatively reasonable performance of  
291 PAN ( $R^2=0.63$ ) is possibly due to constraining some of the oxygenated VOCs such as  
292 acetaldehyde. Xu et al. (2021) observed a strong dependency of PAN concentrations on NO/NO<sub>2</sub>  
293 ratios. Smaller NO/NO<sub>2</sub> ratios are usually associated with larger PAN mixing ratios because NO  
294 can effectively remove peroxyacetyl radicals. We observe an overestimation of PAN (0.27 ppbv)  
295 possibly due to an underestimation of NO/NO<sub>2</sub>. Moreover, we should not rule out the impact of  
296 the first-order dilution factor which was only empirically set in this study. For instance, if we  
297 ignore the dilution process for the KORUS-AQ campaign, the bias of the model in terms of PAN  
298 will increase by 33% resulting in a poor performance ( $R^2=0.40$ ) (Figure S3). We notice that this  
299 poor performance primarily occurs for high altitude measurements where PAN is thermally stable  
300 (Figure S4); therefore, this does not impact the majority of rapid atmospheric chemistry occurring  
301 in the lower troposphere such the formation of HCHO. Schroeder et al. (2020) found that proper  
302 simulation of PAN in the polluted PBL during KORUS-AQ required a first-order loss rate based  
303 on thermal decomposition at the average PBL temperature, which was more realistic than the  
304 widely varying local PAN lifetimes associated with temperature gradients between the surface and  
305 the top of the PBL. This solution is computationally equivalent to the dilution rate used in this  
306 study.

307 KORUS-AQ was the only field campaign providing OH and HO<sub>2</sub> measurements.  
308 Concerning HO<sub>2</sub>, former studies such as Schroeder et al. (2017), Souri et al. (2020), and Brune et  
309 al. (2022) managed to reproduce HO<sub>2</sub> mixing ratios with  $R^2$  ranging from 0.6 to 0.7. The  
310 performance of our model ( $R^2=0.66$ ) is similar to these past studies with near negligible biases

311 (<1%). One may argue that the absence of the HO<sub>2</sub> uptake by aerosols is contributing to some of  
312 the discrepancies we observe in the HO<sub>2</sub> comparison. Brune et al. (2022) provided compelling  
313 evidence showing that the consideration of the HO<sub>2</sub> uptake made their results significantly  
314 inconsistent with the observations suggesting that the HO<sub>2</sub> uptake might have been inconsequential  
315 during the campaign. Our model manages to reproduce 64% of the variance of observed OH  
316 outperforming the simulations presented in Souri et al. (2020) and Brune et al. (2022) by >10%.  
317 The slope (= 1.03) is not too far from the identity line indicating that our box model systematically  
318 overestimates OH by 0.62 10<sup>6</sup> cm<sup>-3</sup>. This may be attributed to a missing OH sink in the mechanism  
319 or the lack of inclusion of some VOCs. A sensitivity test involving removing the first-order  
320 dilution process demonstrates that the simulation of HO<sub>x</sub> is rather insensitive to this parameter  
321 (Figure S5). This might be caused by the fact that the simulated HCHO already agrees relatively  
322 well with the observations without the dilution factor. In general, the model performance is  
323 consistent, or outperforms, results from recent box modelling studies which is an indication of it  
324 being at least roughly representative of the real-world ozone chemistry and sensitivity regimes.

### 325 3.2. *Can HCHO/NO<sub>2</sub> ratios fully describe the HO<sub>x</sub>-RO<sub>x</sub> cycle?*

326 Kleinman et al. (2001) demonstrated that LRO<sub>x</sub>/LNO<sub>x</sub> is the most robust ozone regime  
327 indicator. Thus, the predictive power of FNR at detecting the underlying chemical conditions can  
328 be challenged by comparing FNR to LRO<sub>x</sub>/LNO<sub>x</sub>. Ideally, if they show a strong degree of  
329 correspondence (i.e., R<sup>2</sup>=1.0), we can confidently say that FNR can realistically portray the  
330 chemical regimes. Any divergence of these two quantities is indicative of inadequacy of the FNR  
331 indicator. Souri et al. (2020) observed a strong linear relationship between the logarithmic  
332 transformed FNR and those of LRO<sub>x</sub>/LNO<sub>x</sub>. Our analysis in this study will be based upon the  
333 simulated values to ensure that the relationship is coherent based on a realization from the well-  
334 characterized box model. As pointed out by Schroeder et al. (2017) and Souri et al. (2020), a  
335 natural logarithm of LRO<sub>x</sub>/LNO<sub>x</sub> roughly equal to -1.0 (i.e., LRO<sub>x</sub>/LNO<sub>x</sub> = 0.35-0.37)  
336 perceptibly separates VOC-sensitive from NO<sub>x</sub>-sensitive regimes, which would make this  
337 threshold the baseline of our analysis.

338 Figure 3 demonstrates the log-log relationship of LRO<sub>x</sub>/LNO<sub>x</sub> and FNR, and P(O<sub>3</sub>), from  
339 all four air quality campaigns. The log-log relationships from each individual campaign are shown  
340 in Figure S6-S9. We overlay the LRO<sub>x</sub>/LNO<sub>x</sub> baseline threshold along with two commonly used  
341 thresholds for FNR suggested by Duncan et al. (2010); they defined the VOC-sensitive regimes if  
342 FNR<1 and the NO<sub>x</sub>-sensitive ones if FNR>2. Any region undergoing a value between these  
343 thresholds is unlabeled and considered to be in a transitional regime. The size of each data point  
344 is proportional to the HCHO×NO<sub>2</sub> concentration magnitude. One striking finding from this plot is  
345 that there is indeed a strong linear relationship between the logarithmic-transformed LRO<sub>x</sub>/LNO<sub>x</sub>  
346 and FNR (R<sup>2</sup>=0.91). A strong linear relationship between the two quantities in the log-log scale is  
347 indicative of a power law dependence (i.e., y=ax<sup>b</sup>). A strong power law dependency means that  
348 these two quantities have a poor correlation at their low and high values. This is mainly caused by  
349 the fact that HCHO does not fully describe VOC reactivity rates in rich and poor VOC  
350 environments (Souri et al., 2020). A question is what range of FNR will fall in ln(LRO<sub>x</sub>/LNO<sub>x</sub>) =  
351 -1.0±0.2? Following the baseline, the transitioning ratios follow a normal distribution with a mean  
352 of 1.8, a standard deviation of 0.4, and a range from 1 to 4 (Figure S10). We define the chemical  
353 error in the application of FNR to separate the chemical regimes as the relative error standard  
354 deviation (i.e., σ/μ) of the transitioning ratios leading to ~ 20%. These numbers are based on a  
355 single model realization and can change if a different mechanism is used; nonetheless, the model  
has considerable skill at reproducing many different unconstrained compounds, especially OH,



357 suggesting that it is a rather reliable realization. The comparison of the transitioning FNRs to the  
358  $\text{NO}_2$  concentrations suggests no correlation ( $r=0.02$ ) whereas there is a linear correlation between  
359 the transitioning ratios and the HCHO concentrations ( $r=0.56$ ). This tendency reinforces the study  
360 of Souri et al. (2020) who, primarily due to the HCHO- $\text{NO}_2$  feedback, observed a larger FNR  
361 threshold in VOC-rich environments to be able to detect the chemical regimes.

### 362 **3.3. Large $\text{PO}_3$ rates occur in regions with large HCHO $\times$ $\text{NO}_2$ concentrations when** 363 **moving towards $\text{NO}_x$ -sensitive regions**

364 A striking and perhaps intuitive tendency observed from Figure 3 is that large  $\text{PO}_3$  rates  
365 are mostly tied to higher HCHO $\times$  $\text{NO}_2$ . But this relationship gradually weakens as we move  
366 towards VOC-sensitive regions (smaller LRO $_x$ /LNO $_x$  ratios). This is a textbook example of non-  
367 linear ozone chemistry. In VOC-sensitive areas,  $\text{PO}_3$  can be strongly inhibited by  $\text{NO}_2$ +OH and  
368 the formation of organic nitrates despite the abundance of the precursors. In application of remote-  
369 sensing of ozone precursors, the greatest unused metric describing the mass of the ozone precursors  
370 is HCHO $\times$  $\text{NO}_2$ . However, this metric should only be used in conjunction with FNR. To  
371 demonstrate this, based on what the baseline (LRO $_x$ /LNO $_x$ ) suggests against thresholds on FNRs  
372 defined by Duncan et. al. (2010), we group the data into four regions namely as  $\text{NO}_x$ -sensitive –  
373  $\text{NO}_x$ -sensitive,  $\text{NO}_x$ -sensitive–transitional, VOC-sensitive–transitional, and VOC-sensitive–  
374 VOC-sensitive. A different perspective into this categorization is that the transitional regimes are  
375 a weaker characterization of the main regime; for instance,  $\text{NO}_x$ -sensitive–transitional regions are  
376 less  $\text{NO}_x$ -sensitive than  $\text{NO}_x$ -sensitive –  $\text{NO}_x$ -sensitive. Subsequently, the cumulative distribution  
377 functions (CDFs) of  $\text{PO}_3$  and HCHO $\times$  $\text{NO}_2$  with respect to the aforementioned groups are  
378 calculated, which is shown in Figure 4. Regarding  $\text{NO}_x$ -sensitive— $\text{NO}_x$ -sensitive regions, we see  
379 the  $\text{PO}_3$  CDF very quickly converging to the probability of 100% indicating that the distribution  
380 of  $\text{PO}_3$  is skewed towards very low values. The median of  $\text{PO}_3$  for this particular regime (where  
381 CDF = 50%) is only 0.25 ppbv/hr. This agrees with previous studies such as Martin et al. (2002),  
382 Choi et al. (2012), Jin et al. (2017), and Souri et al. (2017) reporting that  $\text{NO}_x$ -sensitive regimes  
383 dominate in pristine areas. The  $\text{PO}_3$  CDFs between  $\text{NO}_x$ -sensitive—transitional and VOC-  
384 sensitive—VOC-sensitive are not too distinct, whereas their HCHO $\times$  $\text{NO}_2$  CDFs are substantially  
385 different. The non-linear ozone chemistry suppresses  $\text{PO}_3$  in highly VOC-sensitive areas such that  
386 those values are not too different than those in mildly polluted areas ( $\text{NO}_x$ -sensitive—transitional).  
387 Perhaps the most interesting conclusion from this figure is that elevated  $\text{PO}_3$  values (median = 4.6  
388 ppbv/hr), a factor of two larger than two previous regimes, are mostly found in VOC-sensitive—  
389 transitional. This is primary due to two causes: i) this particular regime is not strongly inhibited by  
390 the nonlinear chemistry, particularly  $\text{NO}_2$ +OH, and ii) it is associated with abundant precursors  
391 evident in the median of HCHO $\times$  $\text{NO}_2$  being as three times as large of those in  $\text{NO}_x$ -sensitive—  
392 transitional. This tendency illustrates the notion of the non-linear chemistry and how this may  
393 affect regulations. Simply knowing where the regimes are might not suffice to pinpoint the peak  
394 of  $\text{PO}_3$ , as this analysis suggests that we need to take both FNR and HCHO $\times$  $\text{NO}_2$  into  
395 consideration; both metrics are readily accessible from satellite remote-sensing sensors.

### 396 **3.4. Can we estimate $\text{PO}_3$ using the information from HCHO/ $\text{NO}_2$ and HCHO $\times$ $\text{NO}_2$ ?**

397 It may be advantageous to construct an empirical function fitted to these two quantities and  
398 elucidate the maximum variance (information) we can potentially gain to recreate  $\text{PO}_3$ . After  
399 several attempts, we found a bilinear function ( $z=a_0+a_1x+a_2y+a_3xy$ ) to be a good fit without  
400 overparameterization. Due to presence of extreme values in both FNR and HCHO $\times$  $\text{NO}_2$ , we use a  
401 weighted least squares method for the curve fitting based on the distance of the fitted curve to the

402 data points (known as bi-squares weighting). The best fit with  $R^2$  equals to 0.94 and an RMSE of  
403 0.60 ppbv/hr is:

$$PO_3 = 0.74 - 0.09x - 0.02y + 0.25xy \quad (4)$$

404 where  $x$  and  $y$  are FNR (unitless) and  $HCHO \times NO_2$  (ppbv<sup>2</sup>), respectively. The residual of the fit is  
405 shown in Figure S11. The gradients of  $PO_3$  with respect to  $x$  and  $y$  are:

$$\frac{dPO_3}{dx} = 0.25y - 0.09 \quad (5)$$

$$\frac{dPO_3}{dy} = 0.25x - 0.02 \quad (6)$$

406 An apparent observation arises from these equations that is the derivatives of  $PO_3$  to each  
407 metric depends on the other one underscoring their interconnectedness. For instance, Eq. (6)  
408 suggests that larger FNRs ( $x$ ) result in a larger gradient of  $PO_3$  to the abundance of  $HCHO \times NO_2$   
409 ( $y$ ). In very low FNRs, this gradient can become very small rendering  $PO_3$  insensitive (or in  
410 extreme cases, negatively correlated) to  $HCHO \times NO_2$ . This analysis provides encouraging results  
411 about the future application of the satellite-derived  $HCHO \times NO_2$ ; however, the wide class of  
412 problems relating to the application of satellite-derived FNR columns such as satellite errors in  
413 columns or the translation between columns to PBL are also present in Eq. (4), even in a more  
414 pronounced way due to  $HCHO \times NO_2$  and  $HCHO^2 (=xy)$ . This new perspective into  $PO_3$  estimation  
415 deserves a separate study.

### 416 3.5. Altitude dependency and its parametrization

417 A lingering concern over the application of satellite-based FNR tropospheric columns is  
418 that the vertical distribution of HCHO and  $NO_2$  are integrated in columns thus this vertical  
419 information is permanently lost. As such, here we provide insights on the vertical distribution of  
420 FNR within the tropospheric column. This task requires information about the differences between  
421 i) the vertical shape of HCHO and that of  $NO_2$  and ii) the vertical shape in the sensitivity of the  
422 retrievals to the different altitude layers (described as scattering weights). Ideally, if both  
423 compounds show an identically relative shape, the FNR columns will be valid for every air parcel  
424 along the vertical path (i.e., a straight line). Previous studies such as Jin et al. (2017) and Schroeder  
425 et al. (2017) observed a large degree of vertical inhomogeneity in both HCHO and  $NO_2$   
426 concentrations suggesting that this ideal condition cannot be met. We do not always know the  
427 precise knowledge of HCHO and  $NO_2$  vertical distributions, but we can constitute some degree of  
428 generalizations by leveraging the measurements made during the aircraft campaigns. As for the  
429 differences in the vertical shapes (i.e., the curvature) of the sensitivity of the retrievals between  
430 HCHO and  $NO_2$  channels (i.e., ~340 nm and ~440 nm), under normal atmospheric and viewing  
431 geometry conditions, several studies such as Nowlan et al. 2018 and Lorente et al. 2017 showed  
432 small differences in the vertical shapes of the scattering weights within first few kilometers altitude  
433 above the surface where the significant fluctuations in FNRs usually take place. Therefore, we do  
434 not consider the varying vertical shapes in the scattering weights in our analysis. This assumption  
435 might not hold for excessive aerosol loading with variable extinction efficiency between ~340 nm  
436 and ~440 nm wavelengths or extreme solar zenith angles.

437 Figure 5 demonstrates the violin plot of the afternoon (> 12:00 LST) vertical distribution  
438 of HCHO,  $NO_2$ , and FNR observed by NASA's aircrafts during the four field campaigns analyzed  
439 in this study superimposed by the simulated  $PO_3$  rates. The vertical layers are grouped into sixteen  
440 altitudes ranging from 0.25 km to 7.75 km. Each vertical layer incorporates measurements  $\pm 0.25$   
441 km of the altitude mid-layer height. The observations do not follow a normal distribution,

442 particularly in the lower parts of the atmosphere; thus medians are preferred to represent the central  
 443 tendency. While the largest PO<sub>3</sub> rates tend to occur in areas close to the surface (< 2 km agl), a  
 444 nonnegligible fraction of the elevated PO<sub>3</sub> rates are also observed in other parts of the atmosphere  
 445 such as ~~those in~~ the free troposphere.

446 Several intriguing features are observed from Figure 5: First, up to the 5.75 km range,  
 447 which encompasses the PBL area and a large portion of the free-troposphere, NO<sub>2</sub> concentrations  
 448 tend to decrease quicker than those of HCHO in line with previous studies such as Schroeder et al.  
 449 (2017), Jin et al. (2017), Chan et al. (2019), and Ren et al. (2022). Second, above 5.75 km, HCHO  
 450 levels off whereas NO<sub>2</sub> shows an increasing trend. As a result of their different vertical trends, we  
 451 observe nonuniformities in the vertical distribution of FNR: they become more NO<sub>x</sub>-sensitive with  
 452 altitude up to a turning point at 5.75 km and then shift backwards to VOC-sensitive.

453 It is attractive to model these shapes and apply parameterizations to understand how their  
 454 shapes will complicate the use of tropospheric column retrieval from satellites. First order rational  
 455 functions are a good candidate to use. Concerning the vertical dependency of HCHO and NO<sub>2</sub>, we  
 456 find reasonable fit ( $R^2=0.73$ ) as:

$$HCHO, NO_2 = \frac{a_0 z + a_1}{z + a_2} \quad (7)$$

457 where  $z$  is altitude in km.  $a_i$  ( $i=0,1,2$ ) are fitting parameters. From this equation it is determined  
 458 that FNRs follow a second order rational function:

$$f(z) = \frac{HCHO}{NO_2} = \frac{b_0 z^2 + b_1 z + b_2}{b_3 z^2 + b_4 z + b_5} \quad (8)$$

459 where  $b_i$  ( $i=0, \dots, 5$ ) are fitting parameters. One can effortlessly fit this function to different bounds  
 460 of the vertical distribution of FNR such as the 25<sup>th</sup> and 75<sup>th</sup> percentiles, and subsequently estimate  
 461 the first moment of the resultant polygon along  $z$  divided by the total area bounded to the polygon  
 462 (the centroid,  $G$ ) via:

$$G(z_1, z_2) = \frac{1}{2A} \int_{z_1}^{z_2} f^2(z)_{75th} - f^2(z)_{25th} dz \quad (9)$$

463 where  $A$  is the area of the polygon bounded by the 75<sup>th</sup> percentiles,  $f(z)_{75th}$ , and the 25<sup>th</sup>  
 464 percentiles ( $f(z)_{25th}$ ) of FNR (shown in Figure 5 as solid black lines). We define an altitude  
 465 adjustment factor ( $f_{adj}$ ) such that one can translate an observed FNR tropospheric column ratios,  
 466 such as those retrieved from satellites, to a defined altitude and below that point ( $z_t$ ) through:

$$f_{adj} = \frac{G(0, z_t)}{G(0, 8 \text{ km})} \quad (10)$$

467 where  $z_t$  can be interchanged to match the PBLH. This definition is more beneficial than using the  
 468 entire tropospheric column to the surface conversion (e.g., Jin et al., 2017) because ozone can be  
 469 formed in various vertical layers. Using the observations collected during the campaign, we  
 470 estimate Eq. (10) along with  $\pm 1\sigma$  boundaries shown in Figure 6. To determine the adjustment factor  
 471 error, we reestimate Eq.9 with  $\pm 1\sigma$  level in the coefficients obtained from Eq.8. The resultant error  
 472 is shown in the dashed red line in Figure 6. This error results from uncertainties associated with  
 473 assuming that the second-order rational function can explain the vertical distribution of FNRs. The  
 474 shape of the resulting adjustment factor is **in line with of** the vertical distribution of FNR (see  
 475 Figure 5): the adjustment factor curve closer to the surface has values smaller than one, increases  
 476 to values larger than one in the mid-troposphere, and finally converges to one near the top of the  
 477 tropospheric column. If one picks out an altitude pertaining to a PBLH, they can easily apply  $f_{adj}$   
 478 to the observed FNR columns to estimate the corresponding ratio for that specific PBLH. A more

479 evolved PBLH (i.e., a large  $z_t$ ) results in stronger vertical mixing rendering  $f_{adj}$  closer to one. The  
480 standard error deviation of this conversion is around 26%.

481 It is beneficial to model this curve to make this data-driven conversion easier for future  
482 applications. A second-order polynomial can well describe ( $R^2=0.99$ ) this curve:

$$f_{adj} = az_t^2 + bz_t + c \quad a = -0.02, b = 0.25, c = 0.41 \quad (11)$$

483 Although Eq. (11) does not include observations above 8 km, the area bounded between  $f(z)_{75th}$   
484 and  $f(z)_{25th}$  in higher altitudes is too small to make a noticeable impact on this adjustment factor.

485 One may object that since we estimated the adjustment factor based on two boundaries  
486 (25<sup>th</sup> and 75<sup>th</sup> percentiles) of the data we are no longer really dealing with 50% of features observed  
487 in the vertical shapes of FNR. This valid critique can be overcome by gradually relaxing the lower  
488 and upper limits and examine the resulting change in  $f_{adj}$ . When we reduce the lower limit in Eq.  
489 (9) from the 25<sup>th</sup> to 1<sup>st</sup> percentiles the optimal curve is similar to the one shown in Figure 6 (Figure  
490 S12). However, when we extend the upper limit from 75<sup>th</sup> percentiles to greater values, we see the  
491 fit becoming less robust above the 80<sup>th</sup> percentiles indicating that the formulation is applicable for  
492 ~80% of the data. The reason behind the poor representation of the adjustment factor for the upper  
493 tail of the population is the extremely steep turning point between 5.5 and 6.0 km necessitating a  
494 higher order rational function to be used for Eq. (7) and Eq. (8). We prefer to limit this analysis to  
495 both boundaries and the order defined in Eq. (8) and Eq. (9) because extreme value predictions  
496 usually lack robustness.

497 **A caution with these results** is that our analysis is limited to afternoon observations because  
498 our focus is on afternoon low orbiting sensors such as OMI and TROPOMI. Nonetheless,  
499 Schroeder et al. (2017) and Crawford et al. (2021) observed a large diurnal variability in these  
500 profiles due to diurnal variability in sinks and sources of  $\text{NO}_2$  and  $\text{HCHO}$ , and atmospheric  
501 dynamics. The diurnal cycle has indeed an important implication for geostationary satellites such  
502 as Tropospheric Emissions: Monitoring of Pollution (TEMPO) (Chance et al., 2019).

503 Another important caveat with our analysis is that it is based upon four air quality  
504 campaigns taking place in warm seasons avoiding times/areas with convective transport; as such  
505 our analysis is ignorant about the vertical shapes of FNR during convective activities and cold  
506 seasons. These oversights can be **downplayed** by a few compelling assumptions: first, it is very  
507 atypical to encounter elevated ozone production rates during cold seasons with few exceptions  
508 (Ahmadov et al., 2015; Rappenglück et al., 2014); second, the notion of ozone regimes is only  
509 appropriate in photochemically active environments where the ROx-HOx cycle is active; an  
510 example of this can be found in Souri et al. (2021) who observed an enhancement of surface ozone  
511 in central Europe during a lockdown in April 2020 (up to 5 ppbv) compared to a baseline which  
512 was explainable by the reduced  $\text{O}_3$  titration through  $\text{NO}$  in place of the photochemically induced  
513 production. An exaggerated extension to this example is the nighttime chemistry where  $\text{NO}-\text{O}_3-$   
514  $\text{NO}_2$  partitioning is the major driver of negative ozone production rates; at night, the definition of  
515  $\text{NO}_x$ -sensitive or  $\text{VOC}$ -sensitive is meaningless, **so is in** photochemically less active  
516 environments; third, it is rarely advisable to use cloudy scenes in satellite UV-Vis gas retrievals  
517 due to the arguable assumption on Lambertian clouds and highly uncertain cloud optical centroid  
518 and albedo; accordingly, convection occurring during storms or fires are commonly masked in  
519 satellite-based studies. Therefore, the limitations associated with the adjustment factor are mild  
520 compared to the advantages.

### 521 3.6. Spatial Heterogeneity

522 The spatial representation error resulting from both unresolved processes and scales (Janić  
 523 et al., 2016; Valin et al., 2011; Souri et al., 2022) refers to the amount of information lost due to  
 524 satellite footprint or unresolved inputs used in satellite retrieval algorithms. This source of error  
 525 cannot be determined when we do not know the true state of the spatial variability. There is,  
 526 however, a practical way to determine this by conducting multi-scale intercomparisons of a coarse  
 527 spatial resolution output against a finer one. Yet, despite the absence of the truth in this approach,  
 528 we tend to find their comparisons useful in giving us an appreciation of the error.

529 We build the reference data on qualified pixels ( $qa\_value > 0.75$ ) of offline TROPOMI  
 530 tropospheric  $NO_2$  version 2.2.0 (van Geffen et al., 2021; Boersma et al., 2018) and total HCHO  
 531 columns version 2.02.01 (De Smedt et al., 2018) oversampled at  $3 \times 3 \text{ km}^2$  in summer 2021 over  
 532 the US. Figure 7 shows the map of those tropospheric columns as well as FNR. Encouragingly,  
 533 the small footprint and relatively low detection limit of TROPOMI compared to its predecessor  
 534 satellite sensors (e.g., OMI) enables us to have possibly one of the finest maps of HCHO over the  
 535 US to date. Large values of HCHO columns are found in the southeast due to strong isoprene  
 536 emissions (e.g., Zhu et al., 2016; Wells et al., 2020). Cities like Houston (Boeke et al., 2011; Zhu  
 537 et al., 2014; Pan et al., 2015; Diao et al., 2016), Kansas City, Phoenix (Nunnermacker et al., 2004),  
 538 and Los Angeles (de Gouw et al., 2018) also show pronounced enhancements of HCHO possibly  
 539 due to anthropogenic sources. Expectedly, large tropospheric  $NO_2$  columns are often confined to  
 540 cities and some coal-fired power plants along Ohio river basin. Concerning FNR, low values  
 541 dominate cities whereas high values are found in remote regions. An immediate tendency observed  
 542 from these maps is that the length scale of HCHO columns is longer than that of  $NO_2$ . This  
 543 indicates that  $NO_2$  columns are more heterogenous. It is because of this reason that we observe a  
 544 large degree of the spatial heterogeneity with respect to FNRs.

545 Here we limit our analysis to Los Angeles due to computational costs imposed by the  
 546 subsequent experiment. To quantify the spatial representation errors caused by satellite footprint  
 547 size, we upscale the FNRs by convolving the values with four low pass box filters with the size of  
 548  $13 \times 24$ ,  $36 \times 36$ ,  $108 \times 108$ , and  $216 \times 216 \text{ km}^2$ , shown in the first column of Figure 8. Subsequently,  
 549 to extract the spatial variance (information), we follow the definition of the experimental  
 550 semivariogram (Matheron, 1963):

$$551 \quad \gamma(\mathbf{h}) = \frac{1}{2N(\mathbf{h})} \sum_{|x_i - x_j| - |\mathbf{h}| \leq \varepsilon} [Z(x_i) - Z(x_j)]^2 \quad (12)$$

552 where  $Z(x_i)$  (and  $Z(x_j)$ ) is discrete pixels of FNRs,  $N(\mathbf{h})$  is the number of paired pixels separated  
 553 by the vector of  $\mathbf{h}$ . The  $|\cdot|$  operator indicates the length of a vector. The condition of  $|x_i - x_j| -$   
 554  $|\mathbf{h}| \leq \varepsilon$  is to permit certain tolerance for differences in the length of the vector. Here, we rule out  
 555 the directional dependency in  $\gamma(\mathbf{h})$ , which in turn, makes the vector of  $\mathbf{h}$  scalar ( $h = |\mathbf{h}|$ ). Moreover,  
 556 we bin  $\gamma$  values in 100 evenly-spaced intervals ranging from 0 to 5 degree. To remove potential  
 557 outliers (such as noise), it is wise to model the semivariogram using an empirical regression model.  
 To model the semivariogram, we follow the stable Gaussian function used in Souri et al. (2022):

$$558 \quad \gamma(h) = s(1 - e^{-\frac{h}{r}c_0}): c_0=1.5 \quad (13)$$

559 where  $r$  and  $s$  are fitting parameters. For the most part, geophysical quantities become spatially  
 560 uncorrelated at a certain distance called the range and the variance associated with that distance is  
 called the sill. The fitting parameters,  $r$  and  $s$ , describe these two quantities as long as the stable

561 Gaussian function can well fit to the shape of semivariogram. The semivariograms, and the fits,  
562 associated with each map is depicted in the second column of Figure 8.

563 The modeled semivariograms suggest that a coarser field comes with a smaller sill,  
564 implying a loss in the spatial information (variance). The length scale (i.e., the range) only sharply  
565 increases at coarser footprints ( $>36\times36$  km<sup>2</sup>). This indicates that several coarse resolution satellite  
566 sensors such as OMI ( $13\times24$  km<sup>2</sup>) are rather able to determine the length scales of FNR over a  
567 major city such as Los Angeles. By leveraging the modeled semivariograms, we can effortlessly  
568 determine the spatial representation error for specific scale (e.g.,  $h=10$  km) through

$$e^2(h) = 1 - \frac{\gamma(h)}{\gamma_{ref}(h)} \quad (14)$$

569 where  $\gamma(h)$  and  $\gamma_{ref}(h)$  is the modeled semivariogram of the target and the reference fields ( $3\times3$   
570 km<sup>2</sup>). This equation articulates the amount of information lost in the target field for the reference.  
571 Accordingly, the proposed formulation of the spatial representation error is relative. For the most  
572 part, the OMI nadir pixel ( $13\times24$  km<sup>2</sup>) only have a  $\sim 12\%$  loss of the spatial variance. On the  
573 contrary, a grid box with a size of  $216\times216$  km<sup>2</sup> fails at capturing  $\sim 65\%$  of the spatial information  
574 in FNR with a 50 km length scale comparable to the extent of Los Angeles. The advantage of our  
575 method is that we can mathematically describe the spatial representation error as function of the  
576 length of our target. The present method can be easily applied to other atmospheric compounds  
577 and locations. We have named this method SpaTial Representation Error EstimaTor (STREET)  
578 which is publicly available as an open-source package (Souri, 2022).

579 An oversight in the above experiment lies in its lack of appreciation of unresolved physical  
580 processes in the satellite measurements: weaker sensitivity of some spectra windows to the near-  
581 surface pollution (Yang et al., 2014), using 1-D air mass factor calculation instead of 3-D  
582 (Schwaerzel et al., 2020), and discounting aerosol effect on the light path are just few  
583 examples to point out. To account for the unresolved processes, one can recalculate Eqs. (12)-(14) using outputs  
584 coming from different retrieval frameworks, which is beyond the scope of this study.

### 585 3.7. Satellite errors

#### 586 3.7.1. Concept

587 Two types of retrieval errors can affect our analysis: systematic errors (bias) and  
588 unsystematic ones (random errors). In theory, it is very compelling to understand their differences.  
589 In reality, the distinction between random and systematic errors is not as clear-cut as it seems. One  
590 may wish to establish the credibility of a satellite retrieval by comparing it to a sky-radiance  
591 measurement over time. Because each measurement is made at a different time, their comparison  
592 is not a repetition of the same experiment; each time, the atmosphere differs in some aspects so  
593 each comparison is unique. Adding more sky-radiance measurements will simply add new  
594 experiments. For each paired data points, there are many unique issues contributing differently to  
595 errors; as such our problem is grossly under-determined (i.e., more unknowns for a given  
596 observation). Here, we do not attempt to separate those types of errors in the subsequent analysis,  
597 thereby limiting the analysis to the total uncertainty.

598 We focus on analyzing the statistical errors drawn from the differences between benchmark  
599 and the retrievals on daily basis. Two sensors are used for this analysis: TROPOMI and OMI. To  
600 propagate individual uncertainties in HCHO and NO<sub>2</sub> to FNRs, we follow an analytical approach  
601 involving Jacobians of the ratio to HCHO and NO<sub>2</sub>. Assuming that errors in HCHO and NO<sub>2</sub> are  
602 uncorrelated, the relative error of the ratio can be estimated by:

$$\frac{\sigma}{ratio} = \sqrt{\left(\frac{\sigma_{HCHO}}{HCHO}\right)^2 + \left(\frac{\sigma_{NO_2}}{NO_2}\right)^2} \quad (15)$$

603 where  $\sigma_{HCHO}$  and  $\sigma_{NO_2}$  are total uncertainties of HCHO and  $NO_2$  observations. It is important to  
 604 recognize that the errors in HCHO and  $NO_2$  are not strictly uncorrelated due to assumptions made  
 605 in their air mass factor calculations. The consequence of disregarding the correlated errors is an  
 606 underestimation in the final error.

### 607 3.7.2. Error Distributions in TROPOMI and OMI

608 We begin our analysis with the error distribution of daily TROPOMI tropospheric  $NO_2$   
 609 columns (v1.02.02) against 22 MAX-DOAS instruments from May to Sep in 2018-2021. The data  
 610 are paired based on the criteria defined in Verhoelst et al. (2021). The spatial locations of the  
 611 stations are mapped in Figure S13. Figure 10a shows the histogram of the TROPOMI minus the  
 612 MAX-DOAS instruments. The first observation from this distribution is that it is skewed towards  
 613 lower differences evident in the skewness parameter around -4.6. As a result of the skewness, the  
 614 median should be a better representative of the central tendency which is around  $-1 \times 10^{15}$   
 615 molec./cm<sup>2</sup>. In general, TROPOMI tropospheric  $NO_2$  columns show a low bias. We fit a normal  
 616 distribution to the data using non-linear Levenberg-Marquardt method. This fitted normal  
 617 distribution ( $R^2=0.94$ ) is used to approximate  $\sigma_{NO_2}$  for different confidence intervals and **to play**  
 618 **down blunders**. To understand how much of these disagreements are caused by systematic errors  
 619 as opposed to random errors, we redo the histogram using monthly-based observations (Figure  
 620 S14). A slight change in the dispersions between the daily and the monthly-basis analysis indicates  
 621 the significance of unresolved systematic (or relative) biases. This tendency suggests, when  
 622 conducting the analysis on a monthly basis, the relative bias cannot be mitigated by averaging.  
 623 Verhoelst et al. (2021) rigorously studied the potential root cause of some discrepancies between  
 624 MAX-DOAS and TROPOMI. An important source of error stems from the fundamental  
 625 differences in the vertical sensitivities of MAX-DOAS (more sensitive to the lower tropospheric  
 626 region) and TROPOMI (more sensitive to the upper tropospheric area). This systematic error can  
 627 only be mitigated using reliably high-resolution vertical shape factors instead of spatiotemporal  
 628 averaging of the satellite data.

629 The error analysis for OMI follows the same methods applied for TROPOMI; however,  
 630 with different benchmarks. We follow the comparisons made between the operational product  
 631 version 3.1 and measured columns derived from NCAR's  $NO_2$  measurements integrated along  
 632 aircraft spirals during four NASA's air quality campaigns. More information regarding this data  
 633 comparison can be found in Choi et al. (2020). Figure 10b shows the histogram of OMI minus the  
 634 integrated spirals. Compared to TROPOMI, the OMI bias is worse by a factor of two. The standard  
 635 deviation calculated from a Gaussian fit ( $2.31 \times 10^{15}$  molec./cm<sup>2</sup>) is not substantially different than  
 636 that of TROPOMI ( $2.11 \times 10^{15}$  molec./cm<sup>2</sup>).

637 As for the error distribution of TROPOMI HCHO columns (version 1.1.(5-7)), we use 24  
 638 FTIR measurements during the same time period based on the criteria specified in Vigouroux et  
 639 al. (2020). The stations are mapped in Figure S13. The frequency of the paired data is daily. Figure  
 640 11a depicts the error distribution. The distribution is slightly broader compared to that of  $NO_2$ ,  
 641 manifested in a larger standard deviation  $4.32 \times 10^{15}$  molec./cm<sup>2</sup>. This is primarily due to the fact  
 642 that the molecular absorption of HCHO is much smaller/narrower than that of  $NO_2$  in the UV-Vis  
 643 range (Gonzalez Abad et al., 2019); consequently, HCHO observations are more contaminated by

644 noise. Similar to the  $\text{NO}_2$ , we fit a normal distribution ( $R^2=0.90$ ) to specify  $\sigma_{\text{HCHO}}$  for different  
645 confidence intervals.

646 Concerning OMI HCHO columns from SAO version 3 (Gonzalez Abad et al., 2015), we  
647 follow the intercomparison approach proposed in Zhu et al. (2020). Based on this approach, the  
648 benchmarks come from GEOS-Chem simulated HCHO columns corrected by in-situ aircraft  
649 measurements. The measurements were made during ozone seasons from KORUS-AQ,  
650 DISCOVERs, FRAPPE, NOMADSS, and SENEX campaigns (see Table 1 in Zhu et al. 2020).  
651 OMI values ranging from  $-0.5 \times 10^{15}$  molec./ $\text{cm}^2$  and  $1.0 \times 10^{17}$  molec./ $\text{cm}^2$  with effective cloud  
652 fraction between 0.0 and 0.3, and SZA between 0 and 60 degrees are only considered in the  
653 comparison. Any pixels from OMI and grid boxes from the corrected GEOS-Chem simulation that  
654 fall into a polygon enclosing the campaign domain are used to create the error distribution shown  
655 in Figure 11b. The distribution has much denser data because the model output covers a large  
656 portion of the satellite swath. The error distribution suggests that OMI HCHO is inferior to  
657 TROPOMI evident in larger bias and standard deviation. The OMI bias is twice as large as that of  
658 TROPOMI. De Smedt et al. (2021) observed the same level of bias from their comparisons of  
659 OMI/TROPOMI with MAX-DOAS instruments (see Table 3 in their paper). Moreover, their OMI  
660 vs MAX-DOAS comparisons were severely scattered. Likewise, we observe the standard deviation  
661 of OMI from the fitted Gaussian function to be roughly five times as large of that TROPOMI. This  
662 can primarily due to a weaker signal-to-noise (and sensor degradation) in OMI. It is because of  
663 this reason that OMI HCHO should be oversampled for few months. Another possible reason for  
664 the large standard deviation is the fact that the benchmark arises from a modeling experiment  
665 whose ability at resolving spatiotemporal variations in HCHO may be uncertain. This partly leads  
666 to the performance of OMI to look poor.

### 667 3.7.3. *The impact of retrieval error on the ratio*

668 Following Eq. (15), we calculate the standard error for a wide range of  $\text{NO}_2$  and HCHO  
669 columns at 68% confidence interval (1 sigma) for both TROPOMI and OMI derived from the fitted  
670 Gaussian function to the histograms; the standard errors are shown in Figure 12. We observe  
671 smaller errors to be associated with larger tropospheric column concentrations. As for TROPOMI,  
672 either daily HCHO or tropospheric  $\text{NO}_2$  columns should be above  $1.2\text{-}1.5 \times 10^{16}$  molec./ $\text{cm}^2$  to  
673 achieve 20-30% standard error. The TROPOMI errors start diminishing the application of FNR  
674 when both measurements are below this threshold. Regarding OMI, it is nearly impossible to get  
675 the standard error below of 20-30% given its problematically large HCHO standard deviation. For  
676 50% error, the daily HCHO columns should be above  $3.2 \times 10^{16}$  molec./ $\text{cm}^2$ . This range of error  
677 can also be achieved if OMI tropospheric  $\text{NO}_2$  columns are above  $8 \times 10^{15}$  molec./ $\text{cm}^2$ .

### 678 3.8. *The fractional errors to the combined error*

679 The ultimate task is to compile the aforementioned errors to gauge how each individual  
680 source of error contributes to the overall error. Although each error is different in nature, combined  
681 they explain the uncertainties of one quantity (FNR) and can be roughly considered independent;  
682 therefore, the combined error is given by:

$$\sigma_{total} = \sqrt{\sigma_{\text{Col2PBL}}^2 + \sigma_{\text{SpatialRep}}^2 + \sigma_{\text{Retrieval}}^2} \quad (16)$$

683  $\sigma_{\text{Col2PBL}}$  is the error in the adjustment-factor defined in this study. We calculated a 26% standard  
684 error for a wide range of PBLHs. Therefore,  $\sigma_{\text{Col2PBL}}$  equals to 26% of the observed ratio (i.e.,  
685 magnitude dependent).  $\sigma_{\text{SpatialRep}}$  is more complex. It is a function of the footprint of the satellite



686 (or a model), the spatial variability of the reference field which varies from environment to  
687 environment, and the length scale of our target (e.g., a district, a city, or a state). Eq. (14) explicitly  
688 quantifies this error. The product of the square root of that value and the observed ratio defines  
689  $\sigma_{SpatialRep}$ . The last error depends on the magnitude of HCHO and NO<sub>2</sub> tropospheric columns. It  
690 can be estimated from Eq. (15) times the observed ratio. We did not include the chemistry error in  
691 Eq. (16) because it was suited only for segregating the chemical conditions; it does not describe  
692 the level of uncertainties that comes with the observed columnar ratio. Figure 13 shows the total  
693 relative error given the observed TROPOMI ratio seen in Figure 7. We consider the OMI spatial  
694 representation error (13% variance loss) for this case that was computed in a city environment.  
695 The retrieval errors are based on TROPOMI sigma values. Areas associated with relatively small  
696 errors (<50%) are mostly seen in cities due to a stronger signal (smaller  $\sigma_{Retrieval}$ ). Places with  
697 low vegetation and anthropogenic sources (i.e., Rocky Mountains) possess the largest errors  
698 (>100%).

699 To produce some examples of the fractional errors to the combined error, we focus on two  
700 different environments with two different sets of HCHO and NO<sub>2</sub> columns. One represents a  
701 heavily polluted area, and the other one a moderately polluted region. We also include two  
702 footprints: OMI (13×24 km<sup>2</sup>) and a 108×108 km<sup>2</sup> pixel. Finally, we calculate the percentage of  
703 each error component for both OMI and TROPOMI sensors. Figure 14 shows the pie charts  
704 describing the percentage of each individual error to the total error for TROPOMI. Unless the  
705 footprint of the sensor is coarse enough (e.g., 108 km<sup>2</sup>) to give rise to the spatial representation  
706 error dominance, the retrieval error stands out. It is not expected for new satellites to have very  
707 large footprints; as such, the retrieval errors appear to be the major obstacle for using FNR in a  
708 robust manner. Figure 15 shows the same calculation but using OMI errors; the retrieval errors  
709 massively surpass other errors. This motivates us to do one more experiment; we recalculate the  
710 HCHO error distribution in OMI using monthly-averaged data instead of daily (Figure S15). This  
711 experiment suggests a standard deviation of  $9.4 \times 10^{15}$  molec./cm<sup>2</sup> with which we again observe  
712 the retrieval error to be the largest contributor (>80%) of the combined error (Figure S16). A recent  
713 study (Johnson et al., 2022) also suggests that retrieval errors can result in considerable  
714 disagreement between FNRs from various sensors and retrieval frameworks.

#### 715 4. Summary

716 The main goal of this study was to characterize the errors associated with the ratio of  
717 satellite-based HCHO to NO<sub>2</sub> columns which has been widely used for ozone sensitivity studies.  
718 From the realization of the complexity of the problem we now know that four major errors should  
719 be carefully quantified so that we can reliably represent the underlying ozone regimes. The errors  
720 are broken down into i) the chemistry error, ii) the column to the PBL translation, iii) the spatial  
721 representation error, and iv) the retrieval error. Each error has its own dynamics and has been  
722 tackled differently by leveraging a broad spectrum of tools and data.

723 The chemistry error refers to the predictive power of HCHO/NO<sub>2</sub> ratio (hereafter FNR) at  
724 describing the HO<sub>x</sub>-RO<sub>x</sub> cycle which can be well explained by the ratio of the chemical loss of  
725 HO<sub>2</sub>+RO<sub>2</sub> (LRO<sub>x</sub>) to the chemical loss of NO<sub>x</sub> (LNO<sub>x</sub>). Because those chemical reactions are not  
726 directly observable, we set up a chemical box model constrained with a large suite of in-situ aircraft  
727 measurements collected during DISCOVER-AQs and KORUS-AQ campaigns (~ 500 hr of flight).  
728 Our box model showed a reasonable performance at recreating some of unconstrained key  
729 compounds such as OH (R<sup>2</sup>=0.64, bias=17%), HO<sub>2</sub> (R<sup>2</sup>=0.66, bias<1%), and HCHO (R<sup>2</sup>=0.73).  
730 Subsequently we compared the simulated FNRs to LRO<sub>x</sub>/LNO<sub>x</sub>. They showed a high degree of

731 correspondence ( $R^2=0.93$ ) but only in the log-log scale; this indicated that FNRs poorly described  
732 the HO<sub>x</sub>-RO<sub>x</sub> cycle for heavily polluted environments as well as pristine ones. Following a robust  
733 baseline indicator ( $\ln(\text{LRO}_x/\text{LNO}_x) = -1.0 \pm 0.2$ ) segregating NO<sub>x</sub>-sensitive from VOC-sensitive  
734 regimes, we observed a diverse range of FNR ranging from 1 to 4. These transitioning ratios had  
735 a Gaussian distribution with a mean of 1.8 and standard deviation of 0.4. This implied that the  
736 relative standard error associated with the ratio from the chemistry perspective at 68% confidence  
737 interval was 20%. Although this threshold with its error was based on a single model realization  
738 and can be different for a different chemical mechanism, it provided a useful universal baseline  
739 derived from various chemical and meteorological conditions. At 68% confidence level, any  
740 uncertainty beyond 20% in the ozone regime identification from FNRs likely originates from other  
741 sources of error such as the retrieval error.

742 Results from the box model showed that ozone production rates in extremely polluted  
743 regions (VOC-sensitive) were not significantly different than those in pristine ones (NO<sub>x</sub>-  
744 sensitive) due to non-linear chemical feedback mostly imposed by NO<sub>2</sub>+OH. Indeed, the largest  
745 PO<sub>3</sub> rates (median = 4.6 ppbv/hr) were predominantly seen in VOC-sensitive regimes tending  
746 towards the transitional regime. This was **primary** caused by the abundance of ozone precursors  
747 (i.e., HCHO×NO<sub>2</sub>) in addition to the diminished negative chemical feedback. We also revealed  
748 that HCHO×NO<sub>2</sub> can be used as a sensible proxy for the ozone precursors abundance. In theory,  
749 this metric in conjunction with the ratio provided reasonable estimates on PO<sub>3</sub> rates (RMSE =  
750  $\pm 0.60$  ppbv/hr).

751 We then analyzed the afternoon vertical distribution of HCHO, NO<sub>2</sub>, and their ratio  
752 observed from aircrafts during the air quality campaigns binned to the near surface to 8 km. For  
753 altitudes below 5.75 km, HCHO concentration steadily decreased with altitude but at a smaller rate  
754 compared to NO<sub>2</sub>. Above that altitude, NO<sub>2</sub> concentrations stabilized and slightly increased due to  
755 lightning and stratospheric sources. The dissimilarity between the vertical shape of NO<sub>2</sub> versus  
756 HCHO resulted in a non-linear shape of FNR. This non-linear shape necessitated a mathematical  
757 formulation to transform an observed columnar ratio to a ratio at a desired vertical height  
758 expanding from the surface. We fit a second-order rational function to the profile and formulated  
759 the altitude adjustment factor which clearly followed a second-order polynomial function starting  
760 from values below 1 for lower altitudes, following values above 1 for some high altitudes, and  
761 finally converging to 1 at 8 km. This behavior means that for a given tropospheric columnar ratio,  
762 the ozone regime tends to get pushed towards the VOC-sensitive regime near the surface. This  
763 data-driven adjustment factor exclusively derived from afternoon aircraft profiles during warm  
764 seasons in non-convective conditions had a standard error of 26%.

765 An important error in the satellite-based observations stemmed from unresolved spatial  
766 variability in trace gas concentrations within a satellite pixel (Souri et al., 2022; Tang et al., 2021).  
767 The amount of unresolved spatial variability (the spatial representation error) can in principle be  
768 modeled if we base our reference on a distribution map made from a high spatial resolution dataset.  
769 We modeled semivariograms (or spatial auto-correlation) computed for a reference map of FNR  
770 observed by TROPOMI at 3×3 km<sup>2</sup> over Los Angeles. Subsequently, we coarsened the map to  
771 13×24, 36×36, 108×108, and 216×216 km<sup>2</sup> and modeled their semivariograms. As for 13×24 km<sup>2</sup>,  
772 which is equivalent of the OMI nadir spatial resolution, around 12% of spatial information  
773 (variance) was lost due to its footprint. The larger the footprint, the bigger spatial representation  
774 error. For instance, a grid box with the size of 216×216 km<sup>2</sup> lost 65% of the spatial information in  
775 the ratio at 50 km length scale. Our method is compelling to understand and easy to apply for other

776 products and different atmospheric environments. We developed an open-source package called  
777 SpaTial Representation Error EstimaTor (STREET) (Souri, 2022) based on this approach.

778 We presented estimates of retrieval errors associated with daily TROPOMI and OMI  
779 tropospheric NO<sub>2</sub> columns by comparing them against a large suite of MAX-DOAS (Verhoelst et  
780 al. 2021) and vertically-integrated measurements from aircraft spirals (Choi et al., 2020). Both  
781 products were smaller than the benchmark. Furthermore, they show a relatively consistent  
782 dispersion at 68% confidence level ( $\sim 2 \times 10^{15}$  molec./cm<sup>2</sup>) suggested by fitting a normal function  
783 ( $R^2 > 0.9$ ) to their error distributions. As for daily TROPOMI and OMI HCHO products, we used  
784 global FTIR observations (Vigouroux et al., 2020) and data-constrained GEOS-Chem outputs from  
785 multiple campaigns (Zhu et al., 2020), respectively. TROPOMI HCHO indeed outperforms OMI  
786 HCHO with respect to bias and dispersion on a daily basis. The standard deviation of OMI HCHO  
787 was found to be roughly five times as large compared to TROPOMI. While this error can be partly  
788 reduced by oversampling over a span of a month or a season, it is critical to recognize that ozone  
789 events are episodic, thus daily observations should be the standard mean for understanding the  
790 chemical pathways for the formation of tropospheric ozone. After combining the daily biases from  
791 both HCHO and NO<sub>2</sub> TROPOMI comparisons, we came to the conclusion that either daily HCHO  
792 or tropospheric NO<sub>2</sub> columns should be above  $1.2\text{-}1.5 \times 10^{16}$  molec./cm<sup>2</sup> to achieve 20-30%  
793 standard error in the ratio. Due to the large error in daily OMI HCHO, it was nearly impossible to  
794 achieve 20-30% standard error given the observable range of HCHO and NO<sub>2</sub> columns over our  
795 planet. To reach to 50% error using daily OMI data, either HCHO columns should be above  
796  $3.2 \times 10^{16}$  molec./cm<sup>2</sup> or tropospheric NO<sub>2</sub> columns should be above  $8 \times 10^{15}$  molec./cm<sup>2</sup>.

797 To build intuition in the significance of the errors above, we finally calculated the  
798 combined error in the ratio by linearly combining the root sum of the squares of the TROPOMI  
799 retrieval errors, the spatial representation error pertaining to OMI nadir footprint over a city-like  
800 environment, and the altitude adjustment error for a wide range of observed HCHO and NO<sub>2</sub>  
801 columns over the US. These observations were based on the TROPOMI in summertime 2021. The  
802 total errors were relatively mild (<50%) in cities due to a stronger signal, whereas they easily  
803 exceeded 100% in regions with low vegetation and anthropogenic sources (i.e., Rocky Mountains).  
804 The dominant source of the combined error (40-90%) was the retrieval error.

805 All of these aspects highlight the necessity of improving the trace gas satellite retrieval  
806 algorithms in conjunction with sensor calibration, although with the realization that a better  
807 retrieval is somewhat limited by the advancements made in other disciplines such as atmospheric  
808 modeling and molecular spectroscopy.

## 809 **Acknowledgment**

810 This study was funded by NASA's Aura Science Team (grant number: 80NSSC21K1333). PTR-  
811 MS measurements were supported by the Austrian Federal Ministry for Transport, Innovation and  
812 Technology (bmvit, FFG-ALR-ASAP). The PTR-MS instrument team (P. Eichler, L. Kaser, T.  
813 Mikoviny, M. Müller) is acknowledged for their support with field work and data processing. We  
814 acknowledge FTIR HCHO measurements team including T. Blumenstock, M. De Mazière, M.  
815 Grutter, J. W. Hannigan, N. Jones, R. Kivi, E. Lutsch, E. Mahieu, M. Makarova, I. Morino, I.  
816 Murata, T. Nagahama, J. Notholt, I. Ortega, M. Palm, A. Röhlting, M. Schneider, D. Smale, W.  
817 Stremme, K. Strong, Y. Sun, R. Sussmann, Y. Té, and P. Wang. The measurements at Paramaribo  
818 have been supported by the BMBF (German Ministry of Education and Research) in the project  
819 ROMIC-II subproject TroStra (01LG1904A). The NDACC FTIR stations Bremen, Garmisch,  
820 Izaña, Ny-Ålesund, Paramaribo and Karlsruhe have been supported by the German  
821 Bundesministerium für Wirtschaft und Energie (BMWi) via DLR under grants 50EE1711A, B and

822 D. We thank the Meteorological Service Suriname and Cornelis Becker for support. The  
823 measurements and data analysis at Bremen are supported by the Senate of Bremen. The NCAR  
824 FTS observation programs at Thule, GR, Boulder, CO and Mauna Loa, HI are supported under  
825 contract by the National Aeronautics and Space Administration (NASA). The National Center for  
826 Atmospheric Research is sponsored by the National Science Foundation. The Thule effort is also  
827 supported by the NSF Office of Polar Programs (OPP). Operations at the Rikubetsu and Tsukuba  
828 FTIR sites are supported in part by the GOSAT series project. The Paris TCCON site has received  
829 funding from Sorbonne Université, the French research center CNRS and the French space agency  
830 CNES. The Jungfraujoch FTIR data are primarily available thanks to the support provided by the  
831 F.R.S. - FNRS (Brussels), the GAW-CH program of MeteoSwiss (Zürich) and the HFSJG.ch  
832 Foundation (Bern). The MAX-DOAS data used in this publication were obtained from A. Bais, J.  
833 Burrows, K. Chan, M. Grutter, C. Liu, H. Irie, V. Kumar, Y. Kanaya, A. Piters, C. Rivera-  
834 Cárdenas, M. Van Roozendaal, R. Ryan, V. Sinha, and T. Wagner. Fast delivery of MAX-DOAS  
835 data tailored to the S5P validation was organized through the S5PVT AO project NIDFORVAL.  
836 IUP-Bremen ground-based measurements are funded by DLR-Bonn received through project  
837 50EE1709A. We thank the IISER Mohali atmospheric chemistry facility for supporting the MAX-  
838 DOAS measurements at Mohali, India. KNMI ground-based measurements in De Bilt and Cabauw  
839 are partly supported by the Ruisdael Observatory project, Dutch Research Council (NWO) contract  
840 184.034.015, by the Netherlands Space Office (NSO) for Sentinel-5p/TROPOMI validation, and  
841 by ESA via the EU CAMS-27 project. LZ and SS acknowledge grants from Guangdong Basic and  
842 Applied Basic Research Foundation (2021A1515110713) and Shenzhen Science and Technology  
843 Program (JCYJ20210324104604012). The TROPOMI validation work was supported by  
844 BELSPO/ESA through the ProDEx project TROVA-E2 (grant no. PEA 4000116692). TV  
845 acknowledges support from BELSPO through BRAIN-BE 2.0 project LEGO-BEL-AQ (contract  
846 B2/191/P1/LEGO-BEL-AQ). We thank Glenn Diskin for providing CO, CO<sub>2</sub>, and CH<sub>4</sub>  
847 measurements. We thank Paul Wennberg for H<sub>2</sub>O<sub>2</sub> and HNO<sub>3</sub> measurements.  
848

#### 849 **Data Access**

850 The FTIR and MAXDOAS data used in this publication were partly obtained from the Network  
851 for the Detection of Atmospheric Composition Change (NDACC) and are available through the  
852 NDACC website [www.ndacc.org](http://www.ndacc.org). The spatial representation error is estimated based on publicly  
853 available package, SpaTial Representation Error EstimaTor (STREET)  
854 (<https://github.com/ahsouri/STREET>). DISCOVER-AQ and KORUS-AQ aircraft data can be  
855 downloaded from <https://www-air.larc.nasa.gov/missions/discover-aq/discover-aq.html> and  
856 <https://www-air.larc.nasa.gov/missions/korus-aq/>. TROPOMI NO<sub>2</sub> and HCHO data can be  
857 downloaded from [https://disc.gsfc.nasa.gov/datasets/S5P\\_L2\\_NO2\\_1/summary](https://disc.gsfc.nasa.gov/datasets/S5P_L2_NO2_1/summary) and  
858 [https://disc.gsfc.nasa.gov/datasets/S5P\\_L2\\_HCHO\\_1/summary](https://disc.gsfc.nasa.gov/datasets/S5P_L2_HCHO_1/summary). The box model results can be  
859 obtained by contacting the corresponding author through [ahsouri@cfa.harvard.edu](mailto:ahsouri@cfa.harvard.edu).  
860

#### 861 **Author contributions**

862 AHS designed the research, analyzed the data, conducted the simulations, made all figures, and  
863 wrote the paper. MSJ, SP, XL, and KC helped with conceptualization, fundraising, and analysis.  
864 GMW helped with configuring the box model. AF, AW, WB, DRB, AJW, RCC, KM, and CC  
865 measured various compounds during the air quality campaigns. JHC orchestrated all these  
866 campaigns and contributed to the model interpretation. TV, SC, and GP provided paired MAX-  
867 DOAS and TROPOMI tropospheric NO<sub>2</sub> observations. CV and BL provided paired FTIR and

868 TROPOMI HCHO observations. SC and LL provided paired integrated aircraft spirals and OMI  
869 tropospheric NO<sub>2</sub> observations. LZ and SS provided the paired observations between the corrected  
870 GEOS-Chem HCHO and OMI HCHO columns. All authors contributed to the discussion and  
871 edited the paper.

872

873

874

875

876

877

878 **References**

- 879 Ahmadov, R., McKeen, S., Trainer, M., Banta, R., Brewer, A., Brown, S., Edwards, P.M., de  
880 Gouw, J.A., Frost, G.J., Gilman, J., Helmig, D., Johnson, B., Karion, A., Koss, A.,  
881 Langford, A., Lerner, B., Olson, J., Oltmans, S., Peischl, J., Pétron, G., Pichugina, Y.,  
882 Roberts, J.M., Ryerson, T., Schnell, R., Senff, C., Sweeney, C., Thompson, C., Veres, P.R.,  
883 Warneke, C., Wild, R., Williams, E.J., Yuan, B., Zamora, R., 2015. Understanding high  
884 wintertime ozone pollution events in an oil- and natural gas-producing region of the western  
885 US. *Atmospheric Chemistry and Physics* 15, 411–429. [https://doi.org/10.5194/acp-15-411-](https://doi.org/10.5194/acp-15-411-2015)  
886 [2015](https://doi.org/10.5194/acp-15-411-2015)
- 887 Bela, M.M., Barth, M.C., Toon, O.B., Fried, A., Ziegler, C., Cummings, K.A., Li, Y., Pickering,  
888 K.E., Homeyer, C.R., Morrison, H., Yang, Q., Mecikalski, R.M., Carey, L., Biggerstaff,  
889 M.I., Betten, D.P., Alford, A.A., 2018. Effects of Scavenging, Entrainment, and Aqueous  
890 Chemistry on Peroxides and Formaldehyde in Deep Convective Outflow Over the Central  
891 and Southeast United States. *Journal of Geophysical Research: Atmospheres* 123, 7594–  
892 7614. <https://doi.org/10.1029/2018JD028271>
- 893 Boeke, N.L., Marshall, J.D., Alvarez, S., Chance, K.V., Fried, A., Kurosu, T.P., Rappenglück, B.,  
894 Richter, D., Walega, J., Weibring, P., Millet, D.B., 2011. Formaldehyde columns from the  
895 Ozone Monitoring Instrument: Urban versus background levels and evaluation using aircraft  
896 data and a global model. *Journal of Geophysical Research: Atmospheres* 116.  
897 <https://doi.org/10.1029/2010JD014870>
- 898 Boersma, K.F., Eskes, H.J., Brinksma, E.J., 2004. Error analysis for tropospheric NO<sub>2</sub> retrieval  
899 from space. *Journal of Geophysical Research: Atmospheres* 109.  
900 <https://doi.org/10.1029/2003JD003962>
- 901 Boersma, K.F., Eskes, H.J., Richter, A., De Smedt, I., Lorente, A., Beirle, S., van Geffen,  
902 J.H.G.M., Zara, M., Peters, E., Van Roozendaal, M., Wagner, T., Maasackers, J.D., van der  
903 A, R.J., Nightingale, J., De Rudder, A., Irie, H., Pinardi, G., Lambert, J.-C., Compernelle,  
904 S.C., 2018. Improving algorithms and uncertainty estimates for satellite NO<sub>2</sub> retrievals:  
905 results from the quality assurance for the essential climate variables (QA4ECV) project.  
906 *Atmospheric Measurement Techniques* 11, 6651–6678. [https://doi.org/10.5194/amt-11-](https://doi.org/10.5194/amt-11-6651-2018)  
907 [6651-2018](https://doi.org/10.5194/amt-11-6651-2018)
- 908 Boersma, K.F., Eskes, H.J., Veefkind, J.P., Brinksma, E.J., van der A, R.J., Sneep, M., van den  
909 Oord, G.H.J., Levelt, P.F., Stammes, P., Gleason, J.F., Bucsela, E.J., 2007. Near-real time  
910 retrieval of tropospheric NO<sub>2</sub> from OMI. *Atmospheric Chemistry and Physics* 7, 2103–  
911 2118. <https://doi.org/10.5194/acp-7-2103-2007>
- 912 Box, G.E.P., 1976. Science and Statistics. *Journal of the American Statistical Association* 71,  
913 791–799. <https://doi.org/10.1080/01621459.1976.10480949>
- 914 Brune, W.H., Miller, D.O., Thames, A.B., Brosius, A.L., Barletta, B., Blake, D.R., Blake, N.J.,  
915 Chen, G., Choi, Y., Crawford, J.H., Digangi, J.P., Diskin, G., Fried, A., Hall, S.R., Hanisco,  
916 T.F., Huey, G.L., Hughes, S.C., Kim, M., Meinardi, S., Montzka, D.D., Pusede, S.E.,  
917 Schroeder, J.R., Teng, A., Tanner, D.J., Ullmann, K., Walega, J., Weinheimer, A.,  
918 Wisthaler, A., Wennberg, P.O., 2022. Observations of atmospheric oxidation and ozone  
919 production in South Korea. *Atmospheric Environment* 269, 118854.  
920 <https://doi.org/10.1016/j.atmosenv.2021.118854>
- 921 Chan, K.L., Wang, Z., Ding, A., Heue, K.-P., Shen, Y., Wang, J., Zhang, F., Shi, Y., Hao, N.,  
922 Wenig, M., 2019. MAX-DOAS measurements of tropospheric NO<sub>2</sub> and HCHO in Nanjing

923 and a comparison to ozone monitoring instrument observations. *Atmospheric Chemistry and*  
924 *Physics* 19, 10051–10071. <https://doi.org/10.5194/acp-19-10051-2019>

925 Chance, K., Palmer, P.I., Spurr, R.J.D., Martin, R.V., Kurosu, T.P., Jacob, D.J., 2000. Satellite  
926 observations of formaldehyde over North America from GOME. *Geophysical Research*  
927 *Letters* 27, 3461–3464. <https://doi.org/10.1029/2000GL011857>

928 Chance, K., Liu, X., Miller, C.C., Abad, G.G., Huang, G., Nowlan, C., Souri, A., Suleiman, R.,  
929 Sun, K., Wang, H., Zhu, L., Zoogman, P., Al-Saadi, J., Antuña-Marrero, J.-C., Carr, J.,  
930 Chatfield, R., Chin, M., Cohen, R., Edwards, D., Fishman, J., Flittner, D., Geddes, J.,  
931 Grutter, M., Herman, J.R., Jacob, D.J., Janz, S., Joiner, J., Kim, J., Krotkov, N.A., Lefer, B.,  
932 Martin, R.V., Mayol-Bracero, O.L., Naeger, A., Newchurch, M., Pfister, G.G., Pickering,  
933 K., Pierce, R.B., Cárdenas, C.R., Saiz-Lopez, A., Simpson, W., Spinei, E., Spurr, R.J.D.,  
934 Szykman, J.J., Torres, O., Wang, J., 2019. TEMPO Green Paper: Chemistry, physics, and  
935 meteorology experiments with the Tropospheric Emissions: monitoring of pollution  
936 instrument, in: *Sensors, Systems, and Next-Generation Satellites XXIII*. Presented at the  
937 *Sensors, Systems, and Next-Generation Satellites XXIII*, SPIE, pp. 56–67.  
938 <https://doi.org/10.1117/12.2534883>

939 Chance, K.V., Burrows, J.P., Perner, D., Schneider, W., 1997. Satellite measurements of  
940 atmospheric ozone profiles, including tropospheric ozone, from ultraviolet/visible  
941 measurements in the nadir geometry: a potential method to retrieve tropospheric ozone.  
942 *Journal of Quantitative Spectroscopy and Radiative Transfer* 57, 467–476.  
943 [https://doi.org/10.1016/S0022-4073\(96\)00157-4](https://doi.org/10.1016/S0022-4073(96)00157-4)

944 Chance, K.V., Burrows, J.P., Schneider, W., 1991. Retrieval and molecule sensitivity studies for  
945 the global ozone monitoring experiment and the scanning imaging absorption spectrometer  
946 for atmospheric cartography, in: *Remote Sensing of Atmospheric Chemistry*. Presented at  
947 the *Remote Sensing of Atmospheric Chemistry*, SPIE, pp. 151–165.  
948 <https://doi.org/10.1117/12.46657>

949 Choi, S., Lamsal, L.N., Follette-Cook, M., Joiner, J., Krotkov, N.A., Swartz, W.H., Pickering,  
950 K.E., Loughner, C.P., Appel, W., Pfister, G., Saide, P.E., Cohen, R.C., Weinheimer, A.J.,  
951 Herman, J.R., 2020. Assessment of NO<sub>2</sub> observations during DISCOVER-AQ and KORUS-  
952 AQ field campaigns. *Atmospheric Measurement Techniques* 13, 2523–2546.  
953 <https://doi.org/10.5194/amt-13-2523-2020>

954 Choi, Y., Kim, H., Tong, D., Lee, P., 2012b. Summertime weekly cycles of observed and  
955 modeled NO<sub>x</sub> and O<sub>3</sub> concentrations as a function of satellite-derived ozone production  
956 sensitivity and land use types over the Continental United States. *Atmospheric Chemistry*  
957 *and Physics* 12, 6291–6307. <https://doi.org/10.5194/acp-12-6291-2012>

958 Choi, Y., Souri, A.H., 2015a. Seasonal behavior and long-term trends of tropospheric ozone, its  
959 precursors and chemical conditions over Iran: A view from space. *Atmospheric*  
960 *Environment* 106, 232–240. <https://doi.org/10.1016/j.atmosenv.2015.02.012>

961 Choi, Y., Souri, A.H., 2015b. Chemical condition and surface ozone in large cities of Texas  
962 during the last decade: Observational evidence from OMI, CAMS, and model analysis.  
963 *Remote Sensing of Environment* 168, 90–101. <https://doi.org/10.1016/j.rse.2015.06.026>

964 Crawford, J.H., Ahn, J.-Y., Al-Saadi, J., Chang, L., Emmons, L.K., Kim, J., Lee, G., Park, J.-H.,  
965 Park, R.J., Woo, J.H., Song, C.-K., Hong, J.-H., Hong, Y.-D., Lefer, B.L., Lee, M., Lee, T.,  
966 Kim, S., Min, K.-E., Yum, S.S., Shin, H.J., Kim, Y.-W., Choi, J.-S., Park, J.-S., Szykman,  
967 J.J., Long, R.W., Jordan, C.E., Simpson, I.J., Fried, A., Dibb, J.E., Cho, S., Kim, Y.P., 2021.

968 The Korea–United States Air Quality (KORUS-AQ) field study. *Elementa: Science of the*  
969 *Anthropocene* 9, 00163. <https://doi.org/10.1525/elementa.2020.00163>

970 de Gouw, J.A., Gilman, J.B., Kim, S.-W., Alvarez, S.L., Dusanter, S., Graus, M., Griffith, S.M.,  
971 Isaacman-VanWertz, G., Kuster, W.C., Lefer, B.L., Lerner, B.M., McDonald, B.C.,  
972 Rappenglück, B., Roberts, J.M., Stevens, P.S., Stutz, J., Thalman, R., Veres, P.R.,  
973 Volkamer, R., Warneke, C., Washenfelder, R.A., Young, C.J., 2018. Chemistry of Volatile  
974 Organic Compounds in the Los Angeles Basin: Formation of Oxygenated Compounds and  
975 Determination of Emission Ratios. *Journal of Geophysical Research: Atmospheres* 123,  
976 2298–2319. <https://doi.org/10.1002/2017JD027976>

977 De Smedt, I., Müller, J.-F., Stavrou, T., van der A, R., Eskes, H., Van Roozendaal, M., 2008.  
978 Twelve years of global observations of formaldehyde in the troposphere using GOME and  
979 SCIAMACHY sensors. *Atmospheric Chemistry and Physics* 8, 4947–4963.  
980 <https://doi.org/10.5194/acp-8-4947-2008>

981 De Smedt, I., Pinardi, G., Vigouroux, C., Compernelle, S., Bais, A., Benavent, N., Boersma, F.,  
982 Chan, K.-L., Donner, S., Eichmann, K.-U., Hedelt, P., Hendrick, F., Irie, H., Kumar, V.,  
983 Lambert, J.-C., Langerock, B., Lerot, C., Liu, C., Loyola, D., PETERS, A., Richter, A., Rivera  
984 Cárdenas, C., Romahn, F., Ryan, R.G., Sinha, V., Theys, N., Vlietinck, J., Wagner, T.,  
985 Wang, T., Yu, H., Van Roozendaal, M., 2021. Comparative assessment of TROPOMI and  
986 OMI formaldehyde observations and validation against MAX-DOAS network column  
987 measurements. *Atmospheric Chemistry and Physics* 21, 12561–12593.  
988 <https://doi.org/10.5194/acp-21-12561-2021>

989 De Smedt, I., Stavrou, T., Hendrick, F., Danckaert, T., Vlemmix, T., Pinardi, G., Theys, N.,  
990 Lerot, C., Gielen, C., Vigouroux, C., Hermans, C., Fayt, C., Veeffkind, P., Müller, J.-F., Van  
991 Roozendaal, M., 2015. Diurnal, seasonal and long-term variations of global formaldehyde  
992 columns inferred from combined OMI and GOME-2 observations. *Atmospheric Chemistry*  
993 *and Physics* 15, 12519–12545. <https://doi.org/10.5194/acp-15-12519-2015>

994 De Smedt, I., Stavrou, T., Müller, J.-F., van der A, R.J., Van Roozendaal, M., 2010. Trend  
995 detection in satellite observations of formaldehyde tropospheric columns. *Geophysical*  
996 *Research Letters* 37. <https://doi.org/10.1029/2010GL044245>

997 De Smedt, I., Theys, N., Yu, H., Danckaert, T., Lerot, C., Compernelle, S., Van Roozendaal, M.,  
998 Richter, A., Hilboll, A., Peters, E., Pedernana, M., Loyola, D., Beirle, S., Wagner, T.,  
999 Eskes, H., van Geffen, J., Boersma, K.F., Veeffkind, P., 2018. Algorithm theoretical baseline  
1000 for formaldehyde retrievals from S5P TROPOMI and from the QA4ECV project.  
1001 *Atmospheric Measurement Techniques* 11, 2395–2426. [https://doi.org/10.5194/amt-11-](https://doi.org/10.5194/amt-11-2395-2018)  
1002 [2395-2018](https://doi.org/10.5194/amt-11-2395-2018)

1003 Diao, L., Choi, Y., Czader, B., Li, X., Pan, S., Roy, A., Souri, A.H., Estes, M., Jeon, W., 2016.  
1004 Discrepancies between modeled and observed nocturnal isoprene in an urban environment  
1005 and the possible causes: A case study in Houston. *Atmospheric Research* 181, 257–264.  
1006 <https://doi.org/10.1016/j.atmosres.2016.07.009>

1007 Duncan, B.N., Yoshida, Y., Olson, J.R., Sillman, S., Martin, R.V., Lamsal, L., Hu, Y., Pickering,  
1008 K.E., Retscher, C., Allen, D.J., Crawford, J.H., 2010. Application of OMI observations to a  
1009 space-based indicator of NO<sub>x</sub> and VOC controls on surface ozone formation. *Atmospheric*  
1010 *Environment* 44, 2213–2223. <https://doi.org/10.1016/j.atmosenv.2010.03.010>

1011 Fried, A., Walega, J., Weibring, P., Richter, D., Simpson, I.J., Blake, D.R., Blake, N.J., Meinardi,  
1012 S., Barletta, B., Hughes, S.C., Crawford, J.H., Diskin, G., Barrick, J., Hair, J., Fenn, M.,  
1013 Wisthaler, A., Mikoviny, T., Woo, J.-H., Park, M., Kim, Jinseok, Min, K.-E., Jeong, S.,



1014 Wennberg, P.O., Kim, M.J., Crounse, J.D., Teng, A.P., Bennett, R., Yang-Martin, M.,  
1015 Shook, M.A., Huey, G., Tanner, D., Knote, C., Kim, JongHo, Park, R., Brune, W., 2020.  
1016 Airborne formaldehyde and volatile organic compound measurements over the Daesan  
1017 petrochemical complex on Korea's northwest coast during the Korea-United States Air  
1018 Quality study: Estimation of emission fluxes and effects on air quality. *Elementa: Science of*  
1019 *the Anthropocene* 8, 121. <https://doi.org/10.1525/elementa.2020.121>

1020 González Abad, G., Liu, X., Chance, K., Wang, H., Kurosu, T.P., Suleiman, R., 2015. Updated  
1021 Smithsonian Astrophysical Observatory Ozone Monitoring Instrument (SAO OMI)  
1022 formaldehyde retrieval. *Atmospheric Measurement Techniques* 8, 19–32.  
1023 <https://doi.org/10.5194/amt-8-19-2015>

1024 Gonzalez Abad, G., Souri, A.H., Bak, J., Chance, K., Flynn, L.E., Krotkov, N.A., Lamsal, L., Li,  
1025 C., Liu, X., Miller, C.C., Nowlan, C.R., Suleiman, R., Wang, H., 2019. Five decades  
1026 observing Earth's atmospheric trace gases using ultraviolet and visible backscatter solar  
1027 radiation from space. *Journal of Quantitative Spectroscopy and Radiative Transfer* 238,  
1028 106478. <https://doi.org/10.1016/j.jqsrt.2019.04.030>

1029 Janjić, T., Bormann, N., Bocquet, M., Carton, J.A., Cohn, S.E., Dance, S.L., Losa, S.N., Nichols,  
1030 N.K., Potthast, R., Waller, J.A., Weston, P., 2018. On the representation error in data  
1031 assimilation. *Quarterly Journal of the Royal Meteorological Society* 144, 1257–1278.  
1032 <https://doi.org/10.1002/qj.3130>

1033 Jeon, W., Choi, Y., Souri, A.H., Roy, A., Diao, L., Pan, S., Lee, H.W., Lee, S.-H., 2018.  
1034 Identification of chemical fingerprints in long-range transport of burning induced upper  
1035 tropospheric ozone from Colorado to the North Atlantic Ocean. *Science of The Total*  
1036 *Environment* 613–614, 820–828. <https://doi.org/10.1016/j.scitotenv.2017.09.177>

1037 Jin, X., Fiore, A.M., Murray, L.T., Valin, L.C., Lamsal, L.N., Duncan, B., Folkert Boersma, K.,  
1038 De Smedt, I., Abad, G.G., Chance, K., Tonnesen, G.S., 2017. Evaluating a Space-Based  
1039 Indicator of Surface Ozone-NO<sub>x</sub>-VOC Sensitivity Over Midlatitude Source Regions and  
1040 Application to Decadal Trends. *Journal of Geophysical Research: Atmospheres* 122,  
1041 10,439-10,461. <https://doi.org/10.1002/2017JD026720>

1042 Jin, X., Holloway, T., 2015. Spatial and temporal variability of ozone sensitivity over China  
1043 observed from the Ozone Monitoring Instrument. *Journal of Geophysical Research:*  
1044 *Atmospheres* 120, 7229–7246. <https://doi.org/10.1002/2015JD023250>

1045 Kleinman, L.I., Daum, P.H., Lee, Y.-N., Nunnermacker, L.J., Springston, S.R., Weinstein-Lloyd,  
1046 J., Rudolph, J., 2001. Sensitivity of ozone production rate to ozone precursors. *Geophysical*  
1047 *Research Letters* 28, 2903–2906. <https://doi.org/10.1029/2000GL012597>

1048 Laughner, J.L., Zhu, Q., Cohen, R.C., 2019. Evaluation of version 3.0B of the BEHR OMI NO<sub>2</sub>  
1049 product. *Atmospheric Measurement Techniques* 12, 129–146. [https://doi.org/10.5194/amt-](https://doi.org/10.5194/amt-12-129-2019)  
1050 [12-129-2019](https://doi.org/10.5194/amt-12-129-2019)

1051 Lee, H.-J., Chang, L.-S., Jaffe, D.A., Bak, J., Liu, X., Abad, G.G., Jo, H.-Y., Jo, Y.-J., Lee, J.-B.,  
1052 Yang, G.-H., Kim, J.-M., Kim, C.-H., 2022. Satellite-Based Diagnosis and Numerical  
1053 Verification of Ozone Formation Regimes over Nine Megacities in East Asia. *Remote*  
1054 *Sensing* 14, 1285. <https://doi.org/10.3390/rs14051285>

1055 Lee, Y., Huey, L.G., Wang, Y., Qu, H., Zhang, R., Ji, Y., Tanner, D.J., Wang, X., Tang, J., Song,  
1056 W., Hu, W., Zhang, Y., 2021. Photochemistry of Volatile Organic Compounds in the  
1057 Yellow River Delta, China: Formation of O<sub>3</sub> and Peroxyacyl Nitrates. *Journal of*  
1058 *Geophysical Research: Atmospheres* 126, e2021JD035296.  
1059 <https://doi.org/10.1029/2021JD035296>

1060 Lorente, A., Folkert Boersma, K., Yu, H., Dörner, S., Hilboll, A., Richter, A., Liu, M., Lamsal,  
1061 L.N., Barkley, M., De Smedt, I., Van Roozendael, M., Wang, Y., Wagner, T., Beirle, S.,  
1062 Lin, J.-T., Krotkov, N., Stammes, P., Wang, P., Eskes, H.J., Krol, M., 2017. Structural  
1063 uncertainty in air mass factor calculation for NO<sub>2</sub> and HCHO satellite retrievals.  
1064 Atmospheric Measurement Techniques 10, 759–782. [https://doi.org/10.5194/amt-10-759-](https://doi.org/10.5194/amt-10-759-2017)  
1065 [2017](https://doi.org/10.5194/amt-10-759-2017)

1066 Martin, R.V., Chance, K., Jacob, D.J., Kurosu, T.P., Spurr, R.J.D., Bucsela, E., Gleason, J.F.,  
1067 Palmer, P.I., Bey, I., Fiore, A.M., Li, Q., Yantosca, R.M., Koelemeijer, R.B.A., 2002. An  
1068 improved retrieval of tropospheric nitrogen dioxide from GOME. Journal of Geophysical  
1069 Research: Atmospheres 107, ACH 9-1-ACH 9-21. <https://doi.org/10.1029/2001JD001027>

1070 Martin, R.V., Fiore, A.M., Van Donkelaar, A., 2004. Space-based diagnosis of surface ozone  
1071 sensitivity to anthropogenic emissions. Geophysical Research Letters 31.  
1072 <https://doi.org/10.1029/2004GL019416>

1073 Matheron, G., 1963. Principles of geostatistics. Economic Geology 58, 1246–1266.  
1074 <https://doi.org/10.2113/gsecongeo.58.8.1246>

1075 Miller, D.O., Brune, W.H., 2022. Investigating the Understanding of Oxidation Chemistry Using  
1076 20 Years of Airborne OH and HO<sub>2</sub> Observations. Journal of Geophysical Research:  
1077 Atmospheres 127, e2021JD035368. <https://doi.org/10.1029/2021JD035368>

1078 Newland, M.J., Bryant, D.J., Dunmore, R.E., Bannan, T.J., Acton, W.J.F., Langford, B.,  
1079 Hopkins, J.R., Squires, F.A., Dixon, W., Drysdale, W.S., Ivatt, P.D., Evans, M.J., Edwards,  
1080 P.M., Whalley, L.K., Heard, D.E., Slater, E.J., Woodward-Massey, R., Ye, C., Mehra, A.,  
1081 Worrall, S.D., Bacak, A., Coe, H., Percival, C.J., Hewitt, C.N., Lee, J.D., Cui, T., Surratt,  
1082 J.D., Wang, X., Lewis, A.C., Rickard, A.R., Hamilton, J.F., 2021. Low-NO atmospheric  
1083 oxidation pathways in a polluted megacity. Atmospheric Chemistry and Physics 21, 1613–  
1084 1625. <https://doi.org/10.5194/acp-21-1613-2021>

1085 Nowlan, C.R., Liu, X., Janz, S.J., Kowalewski, M.G., Chance, K., Follette-Cook, M.B., Fried, A.,  
1086 González Abad, G., Herman, J.R., Judd, L.M., Kwon, H.-A., Loughner, C.P., Pickering,  
1087 K.E., Richter, D., Spinei, E., Walega, J., Weibring, P., Weinheimer, A.J., 2018. Nitrogen  
1088 dioxide and formaldehyde measurements from the GEOstationary Coastal and Air Pollution  
1089 Events (GEO-CAPE) Airborne Simulator over Houston, Texas. Atmospheric Measurement  
1090 Techniques 11, 5941–5964. <https://doi.org/10.5194/amt-11-5941-2018>

1091 Nunnermacker, L.J., Weinstein-Lloyd, J., Kleinman, L., Daum, P.H., Lee, Y.N., Springston,  
1092 S.R., Klotz, P., Newman, L., Neuroth, G., Hyde, P., 2004. Ground-based and aircraft  
1093 measurements of trace gases in Phoenix, Arizona (1998). Atmospheric Environment 38,  
1094 4941–4956. <https://doi.org/10.1016/j.atmosenv.2004.04.033>

1095 Pan, S., Choi, Y., Roy, A., Li, X., Jeon, W., Souri, A.H., 2015. Modeling the uncertainty of  
1096 several VOC and its impact on simulated VOC and ozone in Houston, Texas. Atmospheric  
1097 Environment 120, 404–416. <https://doi.org/10.1016/j.atmosenv.2015.09.029>

1098 Rappenglück, B., Ackermann, L., Alvarez, S., Golovko, J., Buhr, M., Field, R.A., Soltis, J.,  
1099 Montague, D.C., Hauze, B., Adamson, S., Risch, D., Wilkerson, G., Bush, D., Stoeckenius,  
1100 T., Keslar, C., 2014. Strong wintertime ozone events in the Upper Green River basin,  
1101 Wyoming. Atmospheric Chemistry and Physics 14, 4909–4934. [https://doi.org/10.5194/acp-](https://doi.org/10.5194/acp-14-4909-2014)  
1102 [14-4909-2014](https://doi.org/10.5194/acp-14-4909-2014)

1103 Ren, B., Xie, P., Xu, J., Li, A., Qin, M., Hu, R., Zhang, T., Fan, G., Tian, X., Zhu, W., Hu, Z.,  
1104 Huang, Y., Li, X., Meng, F., Zhang, G., Tong, J., Ren, H., Zheng, J., Zhang, Z., Lv, Y.,  
1105 2022. Vertical characteristics of NO<sub>2</sub> and HCHO, and the ozone formation regimes in

1106 Hefei, China. *Science of The Total Environment* 823, 153425.  
1107 <https://doi.org/10.1016/j.scitotenv.2022.153425>

1108 Schroeder, J.R., Crawford, J.H., Fried, A., Walega, J., Weinheimer, A., Wisthaler, A., Müller,  
1109 M., Mikoviny, T., Chen, G., Shook, M., Blake, D.R., Tonnesen, G.S., 2017. New insights  
1110 into the column CH<sub>2</sub>O/NO<sub>2</sub> ratio as an indicator of near-surface ozone sensitivity. *Journal*  
1111 *of Geophysical Research: Atmospheres* 122, 8885–8907.  
1112 <https://doi.org/10.1002/2017JD026781>

1113 Schroeder, J.R., Crawford, J.H., Ahn, J.-Y., Chang, L., Fried, A., Walega, J., Weinheimer, A.,  
1114 Montzka, D.D., Hall, S.R., Ullmann, K., Wisthaler, A., Mikoviny, T., Chen, G., Blake,  
1115 D.R., Blake, N.J., Hughes, S.C., Meinardi, S., Diskin, G., Digangi, J.P., Choi, Y., Pusede,  
1116 S.E., Huey, G.L., Tanner, D.J., Kim, M., Wennberg, P., 2020. Observation-based modeling  
1117 of ozone chemistry in the Seoul metropolitan area during the Korea-United States Air  
1118 Quality Study (KORUS-AQ). *Elementa: Science of the Anthropocene* 8, 3.  
1119 <https://doi.org/10.1525/elementa.400>

1120

1121 Schwaerzel, M., Emde, C., Brunner, D., Morales, R., Wagner, T., Berne, A., Buchmann, B.,  
1122 Kuhlmann, G., 2020. Three-dimensional radiative transfer effects on airborne and ground-  
1123 based trace gas remote sensing. *Atmospheric Measurement Techniques* 13, 4277–4293.  
1124 <https://doi.org/10.5194/amt-13-4277-2020>

1125 Seinfeld, J. H. and Pandis, S. N., 2006: *Atmospheric Chemistry and Physics: From Air Pollution*  
1126 *to Climate Change*, 2nd Edn., Wiley-Interscience, Hoboken, N.J., ISBN: 978-1-118-94740-  
1127 1.

1128 Sillman, S., He, D., 2002. Some theoretical results concerning O<sub>3</sub>-NO<sub>x</sub>-VOC chemistry and  
1129 NO<sub>x</sub>-VOC indicators. *Journal of Geophysical Research: Atmospheres* 107, ACH 26-1-ACH  
1130 26-15. <https://doi.org/10.1029/2001JD001123>

1131 Sillman, S., Logan, J.A., Wofsy, S.C., 1990. The sensitivity of ozone to nitrogen oxides and  
1132 hydrocarbons in regional ozone episodes. *Journal of Geophysical Research: Atmospheres*  
1133 95, 1837–1851. <https://doi.org/10.1029/JD095iD02p01837>

1134 Souri, A.H., Chance, K., Bak, J., Nowlan, C.R., González Abad, G., Jung, Y., Wong, D.C., Mao,  
1135 J., Liu, X., 2021. Unraveling pathways of elevated ozone induced by the 2020 lockdown in  
1136 Europe by an observationally constrained regional model using TROPOMI. *Atmospheric*  
1137 *Chemistry and Physics* 21, 18227–18245. <https://doi.org/10.5194/acp-21-18227-2021>

1138 Souri, A.H., Chance, K., Sun, K., Liu, X., Johnson, M.S., 2022. Dealing with spatial  
1139 heterogeneity in pointwise-to-gridded- data comparisons. *Atmospheric Measurement*  
1140 *Techniques* 15, 41–59. <https://doi.org/10.5194/amt-15-41-2022>

1141 Souri, A.H., Nowlan, C.R., Wolfe, G.M., Lamsal, L.N., Chan Miller, C.E., Abad, G.G., Janz,  
1142 S.J., Fried, A., Blake, D.R., Weinheimer, A.J., Diskin, G.S., Liu, X., Chance, K., 2020.  
1143 Revisiting the effectiveness of HCHO/NO<sub>2</sub> ratios for inferring ozone sensitivity to its  
1144 precursors using high resolution airborne remote sensing observations in a high ozone  
1145 episode during the KORUS-AQ campaign. *Atmospheric Environment* 224, 117341.  
1146 <https://doi.org/10.1016/j.atmosenv.2020.117341>

1147 Souri. (2022). ahsouri/STREET: STREET 0.0.2 (0.0.2). Zenodo.  
1148 <https://doi.org/10.5281/zenodo.6993116>

1149 Tang, W., Edwards, D.P., Emmons, L.K., Worden, H.M., Judd, L.M., Lamsal, L.N., Al-Saadi,  
1150 J.A., Janz, S.J., Crawford, J.H., Deeter, M.N., Pfister, G., Buchholz, R.R., Gaubert, B.,  
1151 Nowlan, C.R., 2021. Assessing sub-grid variability within satellite pixels over urban regions

1152 using airborne mapping spectrometer measurements. *Atmospheric Measurement Techniques*  
1153 14, 4639–4655. <https://doi.org/10.5194/amt-14-4639-2021>

1154 Thornton, J.A., Wooldridge, P.J., Cohen, R.C., Martinez, M., Harder, H., Brune, W.H., Williams,  
1155 E.J., Roberts, J.M., Fehsenfeld, F.C., Hall, S.R., Shetter, R.E., Wert, B.P., Fried, A., 2002.  
1156 Ozone production rates as a function of NO<sub>x</sub> abundances and HO<sub>x</sub> production rates in the  
1157 Nashville urban plume. *Journal of Geophysical Research: Atmospheres* 107, ACH 7-1-ACH  
1158 7-17. <https://doi.org/10.1029/2001JD000932>

1159 Tonnesen, G.S., Dennis, R.L., 2000a. Analysis of radical propagation efficiency to assess ozone  
1160 sensitivity to hydrocarbons and NO<sub>x</sub> : 1. Local indicators of instantaneous odd oxygen  
1161 production sensitivity. *Journal of Geophysical Research: Atmospheres* 105, 9213–9225.  
1162 <https://doi.org/10.1029/1999JD900371>

1163 Tonnesen, G.S., Dennis, R.L., 2000b. Analysis of radical propagation efficiency to assess ozone  
1164 sensitivity to hydrocarbons and NO<sub>x</sub> : 2. Long-lived species as indicators of ozone  
1165 concentration sensitivity. *Journal of Geophysical Research: Atmospheres* 105, 9227–9241.  
1166 <https://doi.org/10.1029/1999JD900372>

1167 Valin, L.C., Russell, A.R., Hudman, R.C., Cohen, R.C., 2011. Effects of model resolution on the  
1168 interpretation of satellite NO<sub>2</sub> observations. *Atmospheric Chemistry and Physics* 11,  
1169 11647–11655. <https://doi.org/10.5194/acp-11-11647-2011>

1170 van Geffen, J., Eskes, H., Compornolle, S., Pinardi, G., Verhoelst, T., Lambert, J.-C., Sneep, M.,  
1171 ter Linden, M., Ludewig, A., Boersma, K.F., Veeffkind, J.P., 2022. Sentinel-5P TROPOMI  
1172 NO<sub>2</sub> retrieval: impact of version v2.2 improvements and comparisons with OMI and  
1173 ground-based data. *Atmospheric Measurement Techniques* 15, 2037–2060.  
1174 <https://doi.org/10.5194/amt-15-2037-2022>

1175 Verhoelst, T., Compornolle, S., Pinardi, G., Lambert, J.-C., Eskes, H.J., Eichmann, K.-U.,  
1176 Fjæraa, A.M., Granville, J., Niemeijer, S., Cede, A., Tiefengraber, M., Hendrick, F.,  
1177 Pazmiño, A., Bais, A., Bazureau, A., Boersma, K.F., Bogner, K., Dehn, A., Donner, S.,  
1178 Elokhov, A., Gebetsberger, M., Goutail, F., Grutter de la Mora, M., Gruzdev, A., Gratsea,  
1179 M., Hansen, G.H., Irie, H., Jepsen, N., Kanaya, Y., Karagkiozidis, D., Kivi, R., Kreher, K.,  
1180 Levelt, P.F., Liu, C., Müller, M., Navarro Comas, M., Piders, A.J.M., Pommereau, J.-P.,  
1181 Portafaix, T., Prados-Roman, C., Puentedura, O., Querel, R., Remmers, J., Richter, A.,  
1182 Rimmer, J., Rivera Cárdenas, C., Saavedra de Miguel, L., Sinyakov, V.P., Stremme, W.,  
1183 Strong, K., Van Roozendaal, M., Veeffkind, J.P., Wagner, T., Wittrock, F., Yela González,  
1184 M., Zehner, C., 2021. Ground-based validation of the Copernicus Sentinel-5P TROPOMI  
1185 NO<sub>2</sub> measurements with the NDACC ZSL-DOAS, MAX-DOAS and Pandonia global  
1186 networks. *Atmospheric Measurement Techniques* 14, 481–510. [https://doi.org/10.5194/amt-](https://doi.org/10.5194/amt-14-481-2021)  
1187 [14-481-2021](https://doi.org/10.5194/amt-14-481-2021)

1188 Vigouroux, C., Langerock, B., Bauer Aquino, C. A., Blumenstock, T., Cheng, Z., De Mazière,  
1189 M., De Smedt, I., Grutter, M., Hannigan, J. W., Jones, N., Kivi, R., Loyola, D., Lutsch, E.,  
1190 Mahieu, E., Makarova, M., Metzger, J.-M., Morino, I., Murata, I., Nagahama, T., Notholt,  
1191 J., Ortega, I., Palm, M., Pinardi, G., Röhling, A., Smale, D., Stremme, W., Strong, K.,  
1192 Sussmann, R., Té, Y., van Roozendaal, M., Wang, P., and Winkler, H.: TROPOMI–  
1193 Sentinel-5 Precursor formaldehyde validation using an extensive network of ground-based  
1194 Fourier-transform infrared stations, *Atmos. Meas. Tech.*, 13, 3751–3767,  
1195 <https://doi.org/10.5194/amt-13-3751-2020>, 2020.

1196 Wells, K.C., Millet, D.B., Payne, V.H., Deventer, M.J., Bates, K.H., de Gouw, J.A., Graus, M.,  
1197 Warneke, C., Wisthaler, A., Fuentes, J.D., 2020. Satellite isoprene retrievals constrain

1198 emissions and atmospheric oxidation. *Nature* 585, 225–233. <https://doi.org/10.1038/s41586->  
1199 [020-2664-3](https://doi.org/10.1038/s41586-020-2664-3)

1200 Wolfe, G. M., Kaiser, J., Hanisco, T.F., Keutsch, F.N., de Gouw, J.A., Gilman, J.B., Graus, M.,  
1201 Hatch, C.D., Holloway, J., Horowitz, L.W., Lee, B.H., Lerner, B.M., Lopez-Hilifiker, F.,  
1202 Mao, J., Marvin, M.R., Peischl, J., Pollack, I.B., Roberts, J.M., Ryerson, T.B., Thornton,  
1203 J.A., Veres, P.R., Warneke, C., 2016. Formaldehyde production from isoprene oxidation  
1204 across NO<sub>x</sub> regimes. *Atmospheric Chemistry and Physics* 16, 2597–2610.  
1205 <https://doi.org/10.5194/acp-16-2597-2016>

1206 Wolfe, Glenn M., Marvin, M.R., Roberts, S.J., Travis, K.R., Liao, J., 2016. The Framework for  
1207 0-D Atmospheric Modeling (F0AM) v3.1. *Geoscientific Model Development* 9, 3309–3319.  
1208 <https://doi.org/10.5194/gmd-9-3309-2016>

1209 Xu, W., Zhang, G., Wang, Y., Tong, S., Zhang, W., Ma, Z., Lin, W., Kuang, Y., Yin, L., Xu, X.,  
1210 2021. Aerosol Promotes Peroxyacetyl Nitrate Formation During Winter in the North China  
1211 Plain. *Environ. Sci. Technol.* 55, 3568–3581. <https://doi.org/10.1021/acs.est.0c08157>

1212 Yang, K., Carn, S.A., Ge, C., Wang, J., Dickerson, R.R., 2014. Advancing measurements of  
1213 tropospheric NO<sub>2</sub> from space: New algorithm and first global results from OMPS.  
1214 *Geophysical Research Letters* 41, 4777–4786. <https://doi.org/10.1002/2014GL060136>

1215 Zhang, K., Duan, Y., Huo, J., Huang, L., Wang, Yangjun, Fu, Q., Wang, Yuhang, Li, L., 2021.  
1216 Formation mechanism of HCHO pollution in the suburban Yangtze River Delta region,  
1217 China: A box model study and policy implementations. *Atmospheric Environment* 267,  
1218 118755. <https://doi.org/10.1016/j.atmosenv.2021.118755>

1219 Zhu, L., González Abad, G., Nowlan, C.R., Chan Miller, C., Chance, K., Apel, E.C., DiGangi,  
1220 J.P., Fried, A., Hanisco, T.F., Hornbrook, R.S., Hu, L., Kaiser, J., Keutsch, F.N., Permar,  
1221 W., St. Clair, J.M., Wolfe, G.M., 2020. Validation of satellite formaldehyde (HCHO)  
1222 retrievals using observations from 12 aircraft campaigns. *Atmospheric Chemistry and*  
1223 *Physics* 20, 12329–12345. <https://doi.org/10.5194/acp-20-12329-2020>

1224 Zhu, L., Jacob, D.J., Kim, P.S., Fisher, J.A., Yu, K., Travis, K.R., Mickley, L.J., Yantosca, R.M.,  
1225 Sulprizio, M.P., De Smedt, I., González Abad, G., Chance, K., Li, C., Ferrare, R., Fried, A.,  
1226 Hair, J.W., Hanisco, T.F., Richter, D., Jo Scarino, A., Walega, J., Weibring, P., Wolfe,  
1227 G.M., 2016. Observing atmospheric formaldehyde (HCHO) from space: validation and  
1228 intercomparison of six retrievals from four satellites (OMI, GOME2A, GOME2B, OMPS)  
1229 with SEAC<sup>4</sup>RS aircraft observations over the southeast US. *Atmospheric Chemistry and*  
1230 *Physics* 16, 13477–13490. <https://doi.org/10.5194/acp-16-13477-2016>

1231 Zhu, L., Jacob, D.J., Mickley, L.J., Marais, E.A., Cohan, D.S., Yoshida, Y., Duncan, B.N., Abad,  
1232 G.G., Chance, K.V., 2014. Anthropogenic emissions of highly reactive volatile organic  
1233 compounds in eastern Texas inferred from oversampling of satellite (OMI) measurements of  
1234 HCHO columns. *Environ. Res. Lett.* 9, 114004. <https://doi.org/10.1088/1748->  
1235 [9326/9/11/114004](https://doi.org/10.1088/1748-9326/9/11/114004)

1236

1237  
1238  
1239

**Table1.** The box model configurations and inputs.

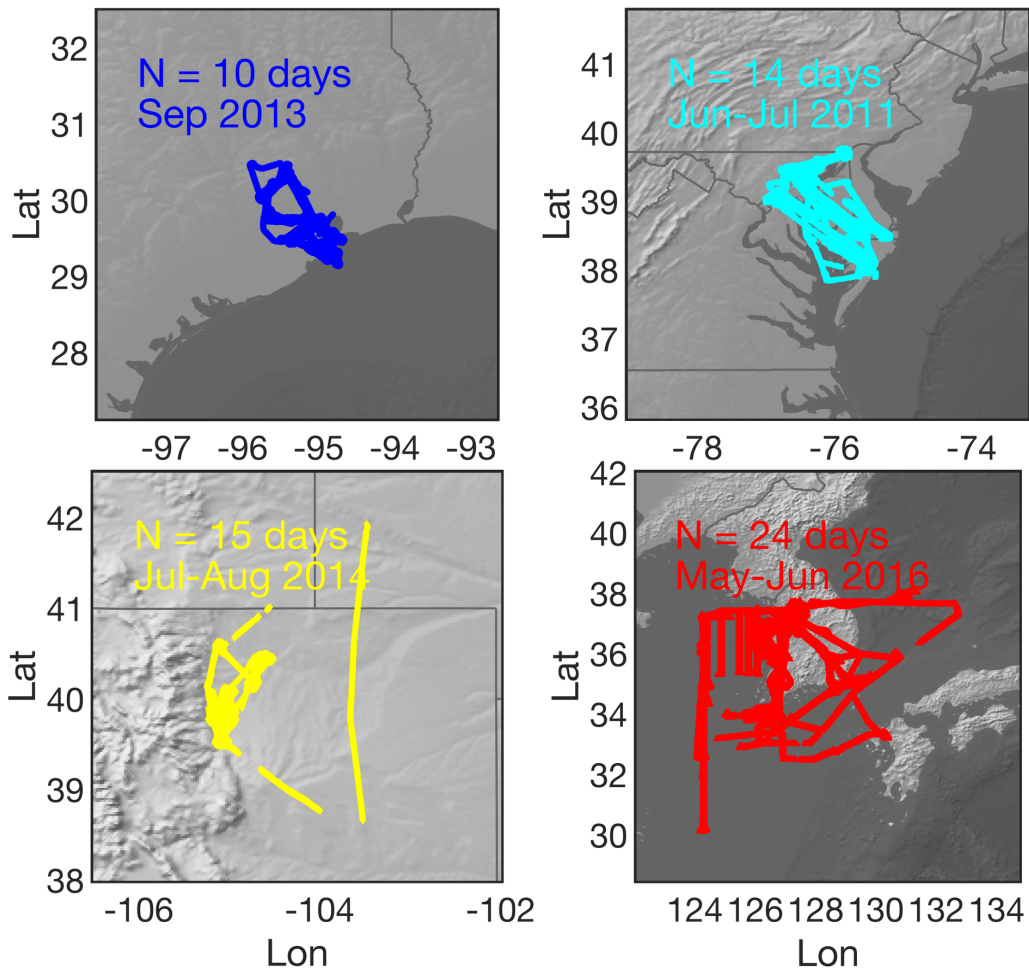
Temporal resolution of samples	10-15 sec
Time steps	1 hour
Number of solar cycles	5
Dilution constant	1/86400 -1/43200 (s <sup>-1</sup> )
Meteorological Inputs	Pressure, Temperature, and Relative Humidity
Photolysis frequencies estimates	LUT based on the NCAR TUV model calculations
Photolysis frequencies constraints (campaign#‡)	Measured jNO <sub>2</sub> (1-4) and jO <sup>1</sup> D (4)
Compounds (Instrument#†, campaign#‡) used for constraining the box model	H <sub>2</sub> (1, 4)§, CO (4, 1-4), NO <sub>x</sub> (2, 1-4), O <sub>3</sub> (2, 1-4), SO <sub>2</sub> (6, 4) , CH <sub>4</sub> (4, 1-4), HNO <sub>3</sub> (10, 1-4), Isoprene (9, 1-4), Monoterpenes (9, 1-4), Acetone (9, 1-4), Ethylene (1, 4), Ethane (1, 4), Methanol (9, 1-4), Propane (1, 4), Benzene (1 or 9, 2-4), Xylene (1 or 9, 1 and 4), Toluene (1 or 9, 1-4), Glyoxal (8, 4), Acetaldehyde (9, 1-4), Methyl vinyl ketone (9, 1-4), Methyl Ethyl Ketone (9, 2-4), Propene (1 or 9, 2 and 4), Acetic acid (9, 2-4), Glycolaldehyde (5, 4), H <sub>2</sub> O <sub>2</sub> (5, 4)
Unconstrained compounds (Instrument#†, campaign#‡) used for validation	HO <sub>2</sub> (3, 4), OH (3, 4), NO (2, 1-4), NO <sub>2</sub> (2, 1-4), PAN (10, 1-4), HCHO (7, 1-4)
Chemical Mechanism	CB06

1240  
1241  
1242  
1243  
1244  
1245  
1246  
1247  
1248  
1249  
1250  
1251  
1252  
1253

† (1) UC Irvine's Whole Air Sampler (WAS), (2) NCAR 4-Channel Chemiluminescence, (3) Penn State's Airborne Tropospheric Hydrogen Oxides Sensor (ATHOS), (4) NASA Langley's DACOM tunable diode laser spectrometer, (5) Caltech's single mass analyzer, (6) Georgia Tech's ionization mass spectrometer, (7) The University of Colorado at Boulder's the Compact Atmospheric Multi-species Spectrometer (CAMS), (8) Korean Airborne Cavity Enhances Spectrometer, (9) University of Innsbruck's PTR-TOF-MS instrument, and (10) University of California, Berkeley's TD-LIF.

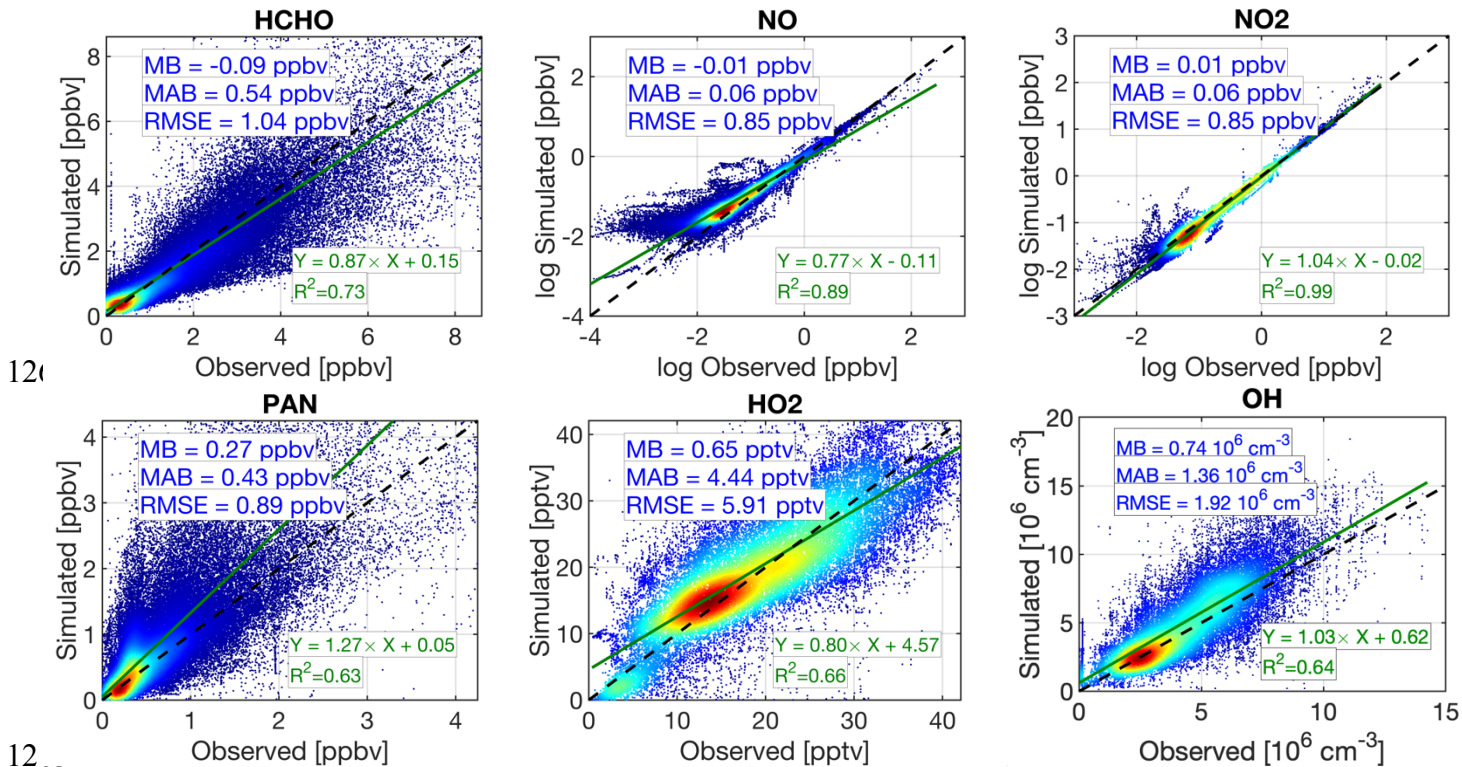
‡ (1) DISCOVER-Baltimore-Washington, (2) DISCOVER-Texas-Houston, (3) DISCOVER-Colorado, and (4) KORUS-AQ

§ In the absence of measurements, a default value of 550 ppbv is specified.



1255  
 1256  
 1257  
 1258  
 1259  
 1260  
 1261

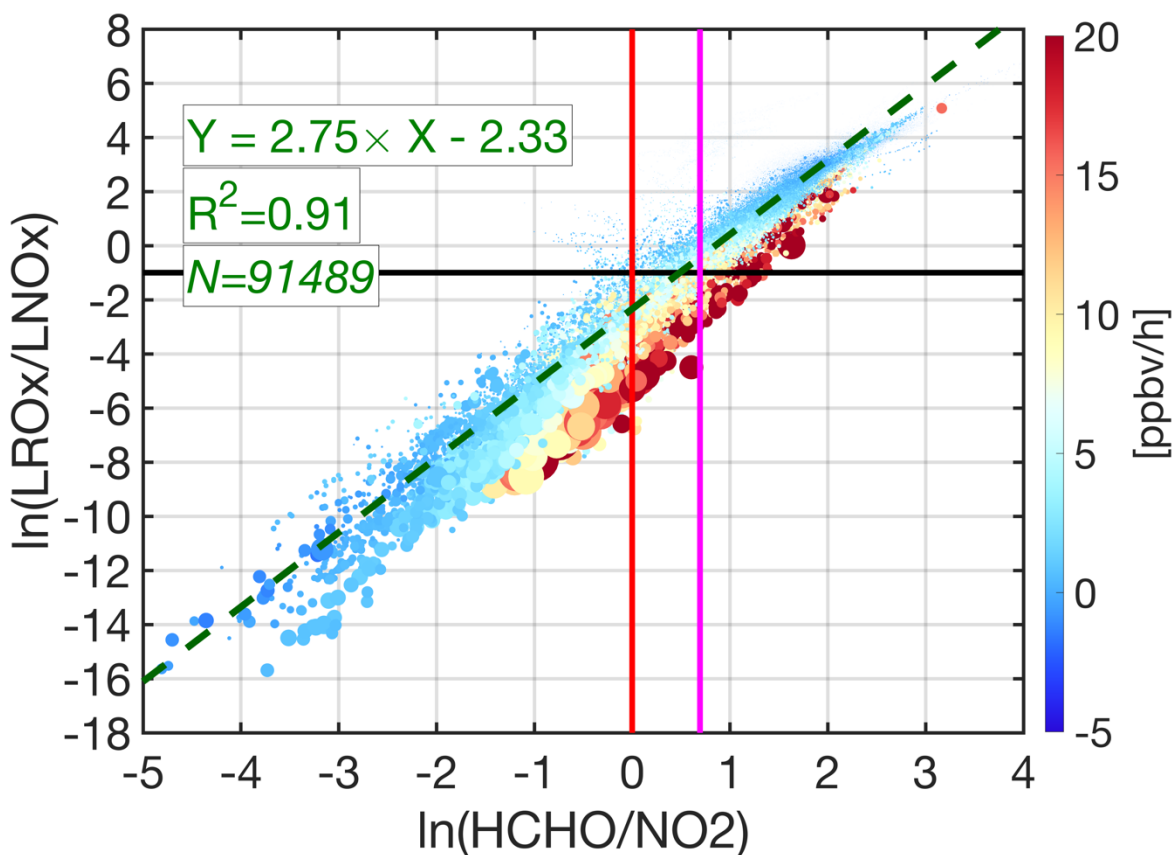
**Figure 1.** The spatial distributions of aircraft measurements collected during NASA's a) DISCOVER-AQ Houston-Texas, b) DISCOVER-AQ Baltimore-Washington, c) DISCOVER-AQ Colorado, and d) KORUS-AQ. The duration of each campaign is based on how long the aircraft was in the air.



12  
1264  
1265  
1266  
1267  
1268  
1269  
1270

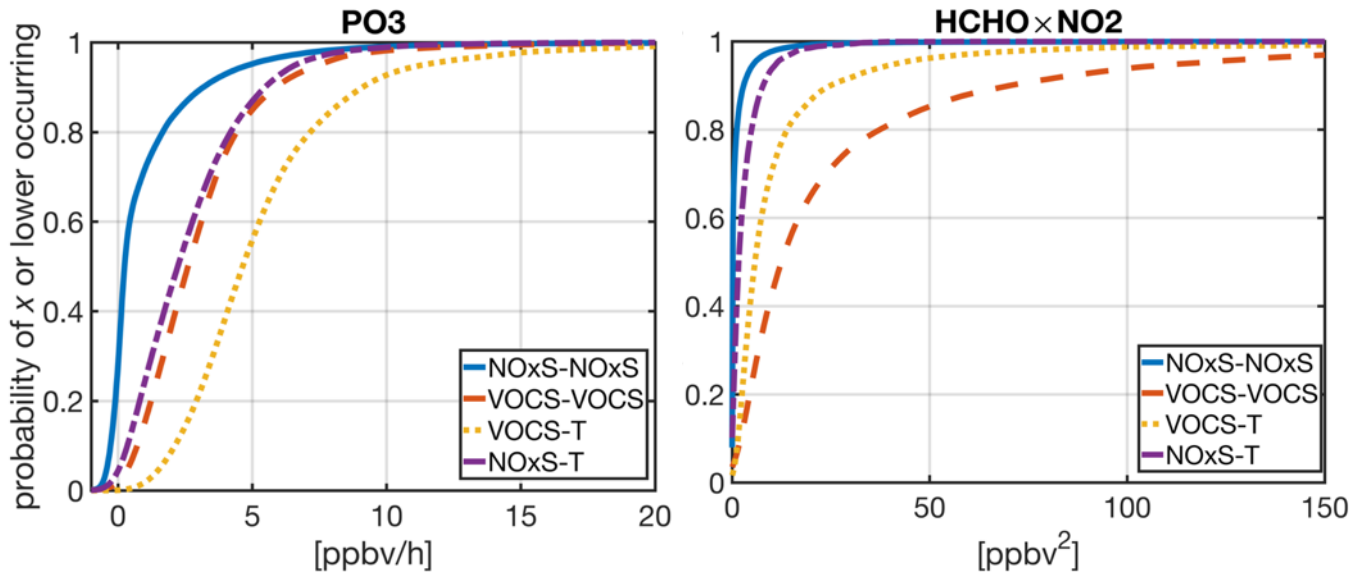
**Figure 2.** The comparisons of the observed concentrations of several critical compounds to those simulated by our FOAM box model. Each subplot contains mean bias (MB), mean absolute bias (MAB), and root mean square error (RMSE). The least-squares fit to the paired data along with the coefficient of determination ( $R^2$ ) is also individually shown for each compound. Note that we do not account for the observations errors in the x-axis. The concentrations of NO and NO<sub>2</sub> are log-transformed.



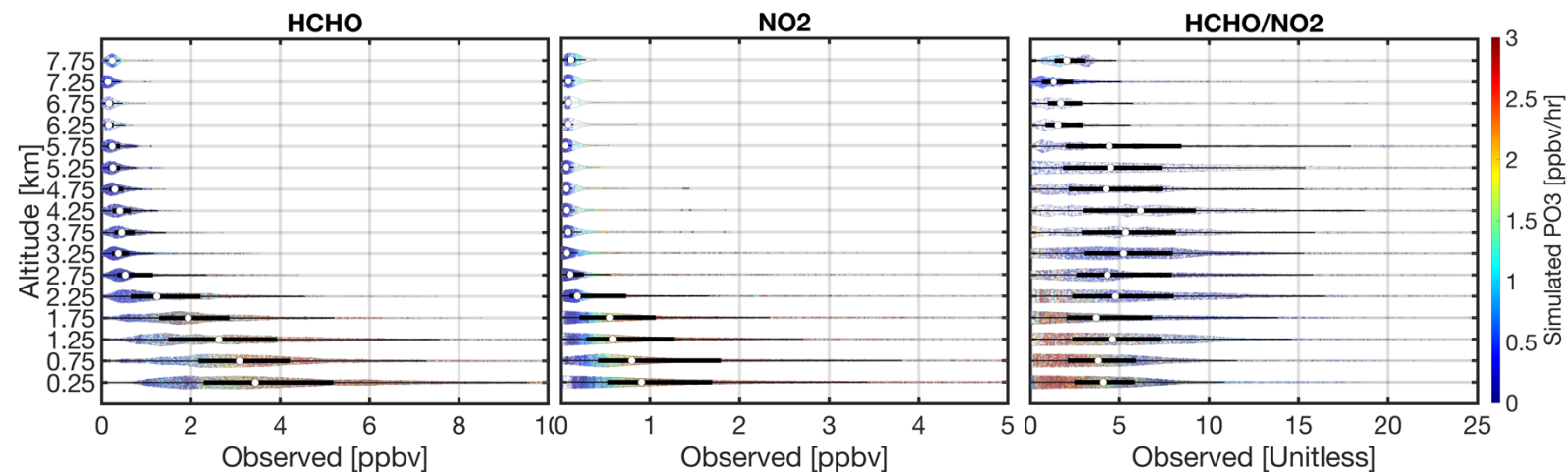


1271  
 1272  
 1273  
 1274  
 1275  
 1276  
 1277  
 1278  
 1279  
 1280

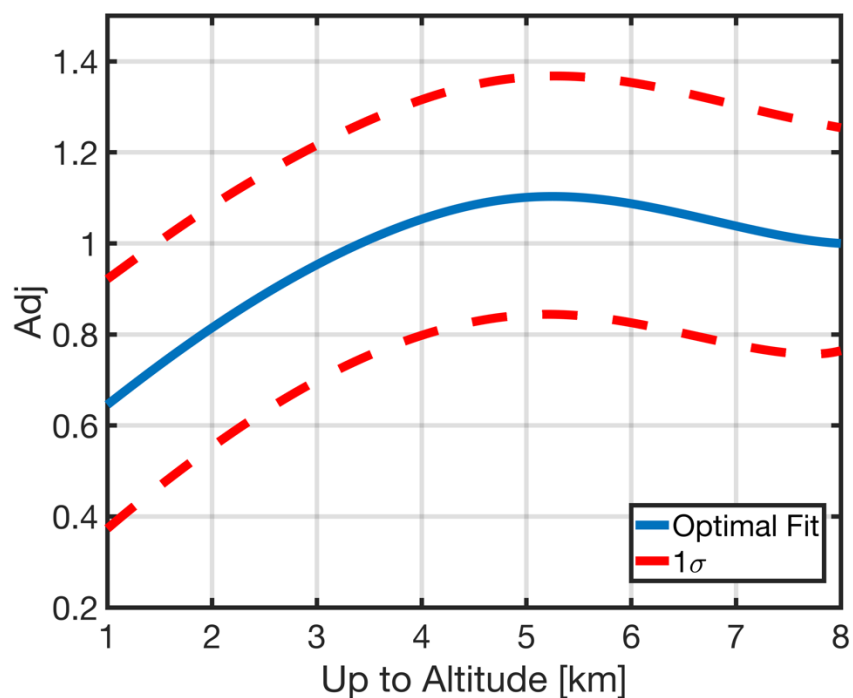
**Figure 3.** The scatterplot of natural logarithm-transformed of HCHO/NO<sub>2</sub> versus LROx/LNOx based on the simulated values performed by the F0AM box model. The heat color indicates the calculated ozone production rates (PO<sub>3</sub>). The size of each data point is proportional to HCHO×NO<sub>2</sub>. The black line is the baseline separator of NOx-sensitive (above the line) and VOC-sensitive (below the line) regimes. We overlay HCHO/NO<sub>2</sub>=1 and HCHO/NO<sub>2</sub>=2 as red and purple lines, respectively. The dashed dark green line indicates the least-squares fit to the paired data. The HCHO/NO<sub>2</sub> = 1.8 with 20% error is the optimal transitioning point based on this result.



128  
 1282 **Figure 4.** Cumulative distribution functions of  $\text{PO}_3$  and  $\text{HCHO} \times \text{NO}_2$  simulated by the box model  
 1283 constrained by NASA's aircraft observations. Four regions namely as  $\text{NO}_x$ -sensitive —  $\text{NO}_x$ -sensitive,  
 1284  $\text{NO}_x$ -sensitive—transitional, VOC-sensitive—transitional, and VOC-sensitive—VOC-sensitive are shown.  
 1285 The first name of the regime is based on the baseline ( $\ln(\text{LRO}_x/\text{LNO}_x)=-1.0$ ), whereas the second one  
 1286 follows those defined in Duncan et al. (2010): VOC-sensitive if  $\text{HCHO}/\text{NO}_2 < 1$ , transitional if  
 1287  $1 < \text{HCHO}/\text{NO}_2 < 2$ , and  $\text{NO}_x$ -sensitive if  $\text{HCHO}/\text{NO}_2 > 2$ .  
 1288

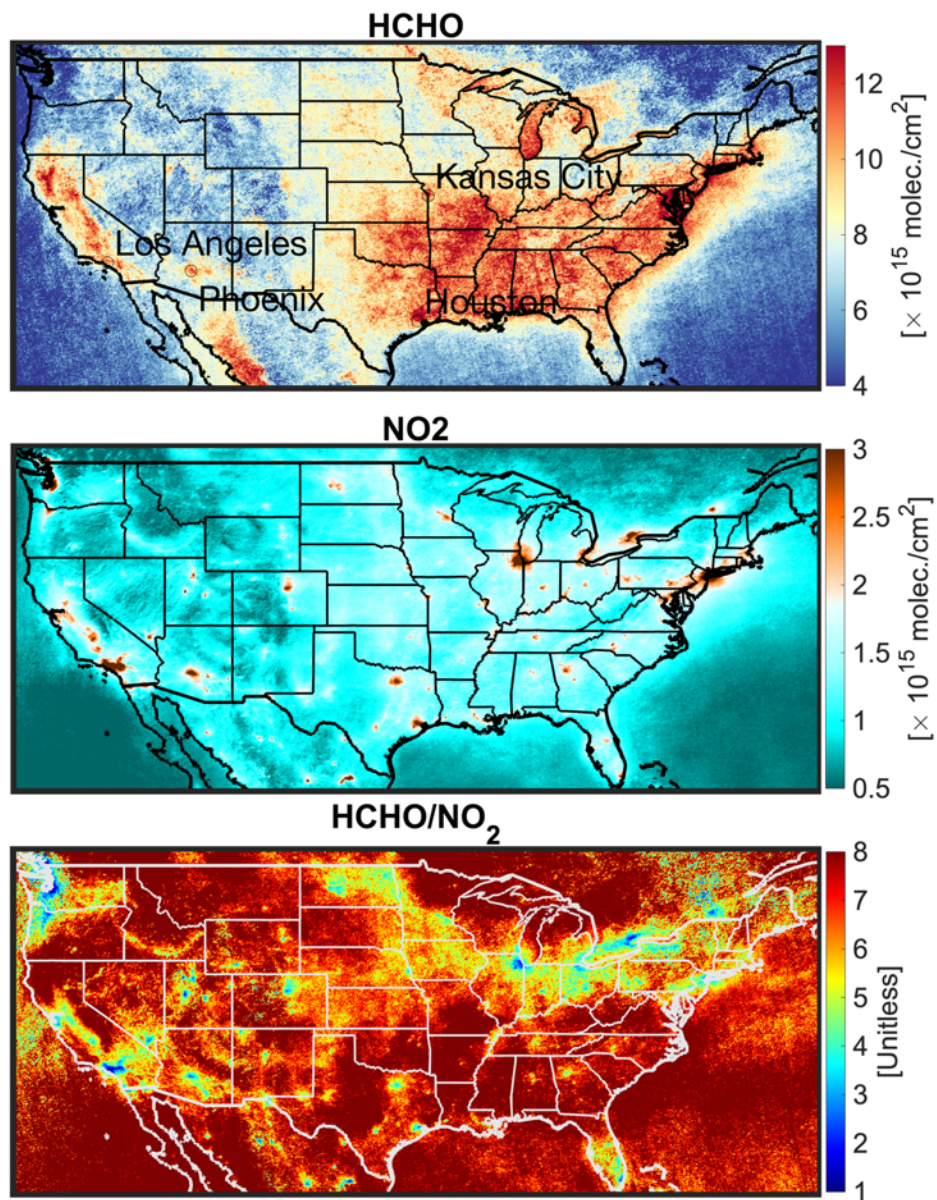


1290 **Figure 5.** The violin plots of the afternoon vertical distribution of HCHO, NO<sub>2</sub>, and HCHO/NO<sub>2</sub>  
 1291 observations collected during DISCOVER-AQ Texas, Colorado, Maryland, and KORUS-AQ campaigns.  
 1292 The violin plots demonstrate the distribution of data (i.e., a wider width means a higher frequency). The  
 1293 median is shown by white dots. Both 25<sup>th</sup> and 75<sup>th</sup> percentiles are shown by a solid black line. The  
 1294 heatmap denotes the simulated ozone production rates.  
 1295

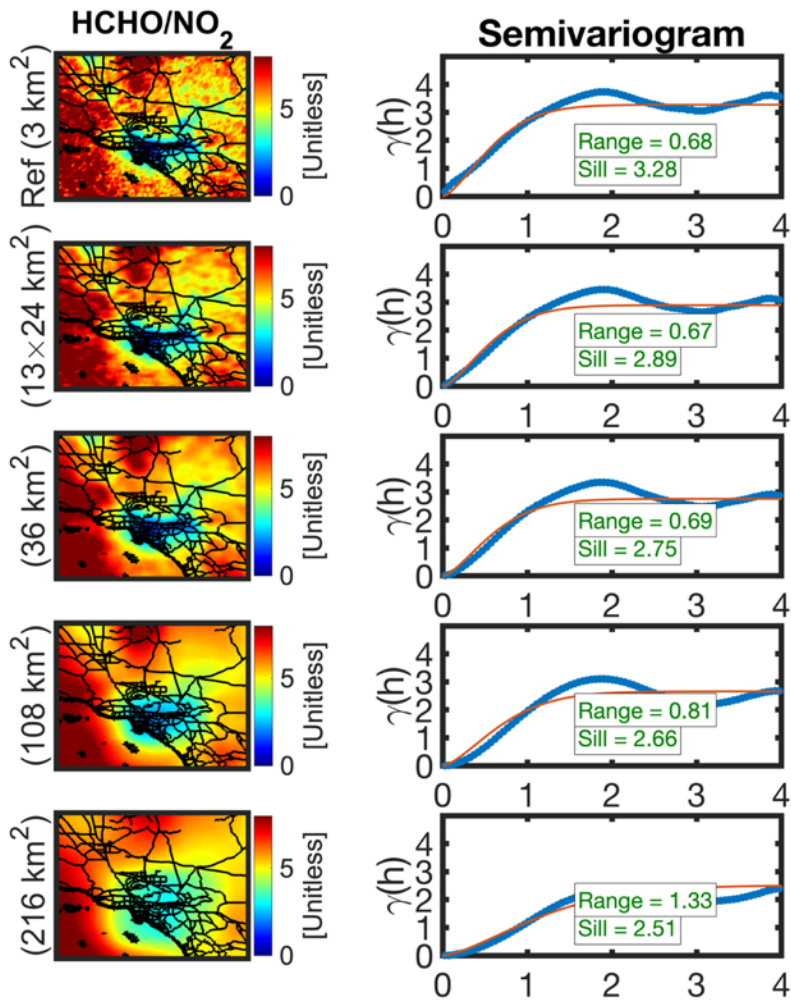


1296  
 1297  
 1298  
 1299  
 1300  
 1301  
 1302  
 1303  
 1304

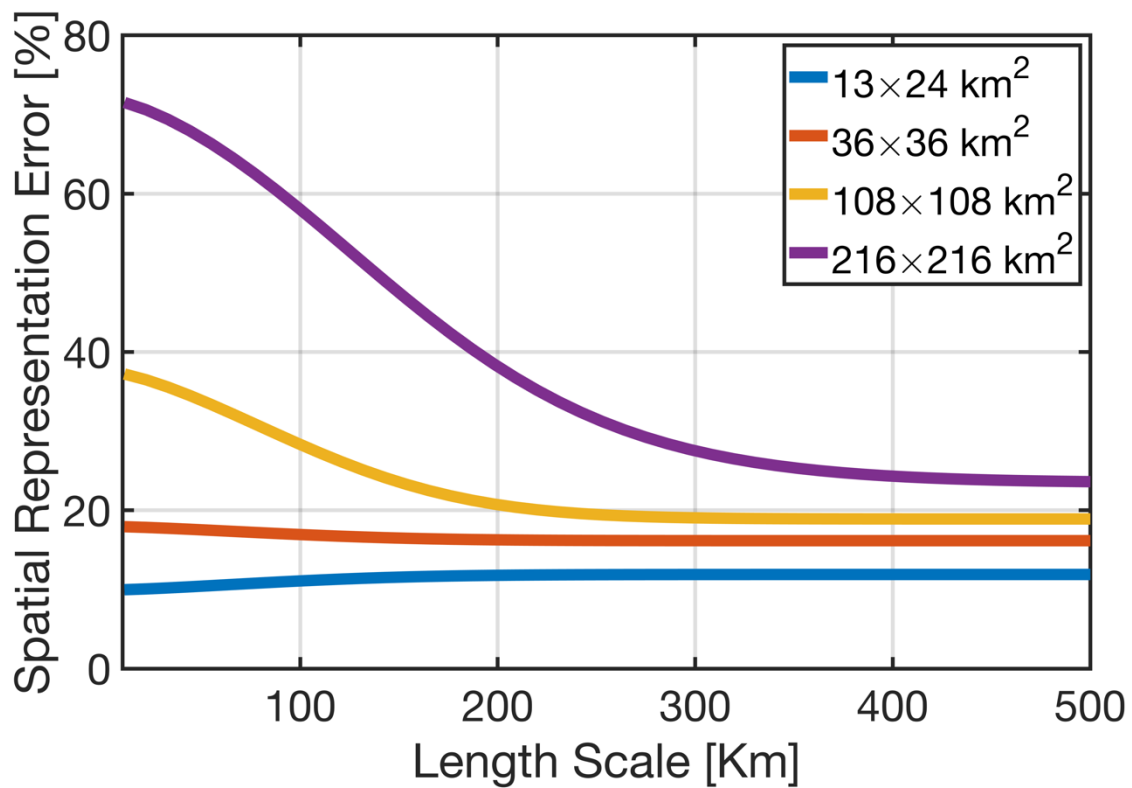
**Figure 6.** The adjustment factor defined as the ratio of the **centroid** (first moment) of the polygon bounding 25<sup>th</sup> and 75<sup>th</sup> percentiles of the observed HCHO/NO<sub>2</sub> columns by the NASA’s aircraft between the surface to 8 km to the ones between the surface and a desired altitude. This factor can be easily applied to the observed HCHO/NO<sub>2</sub> columns to translate the value to a desired altitude stretching down to the surface (i.e., PBLH). The optimal curve follows a quadratic function formulated in Eq11.



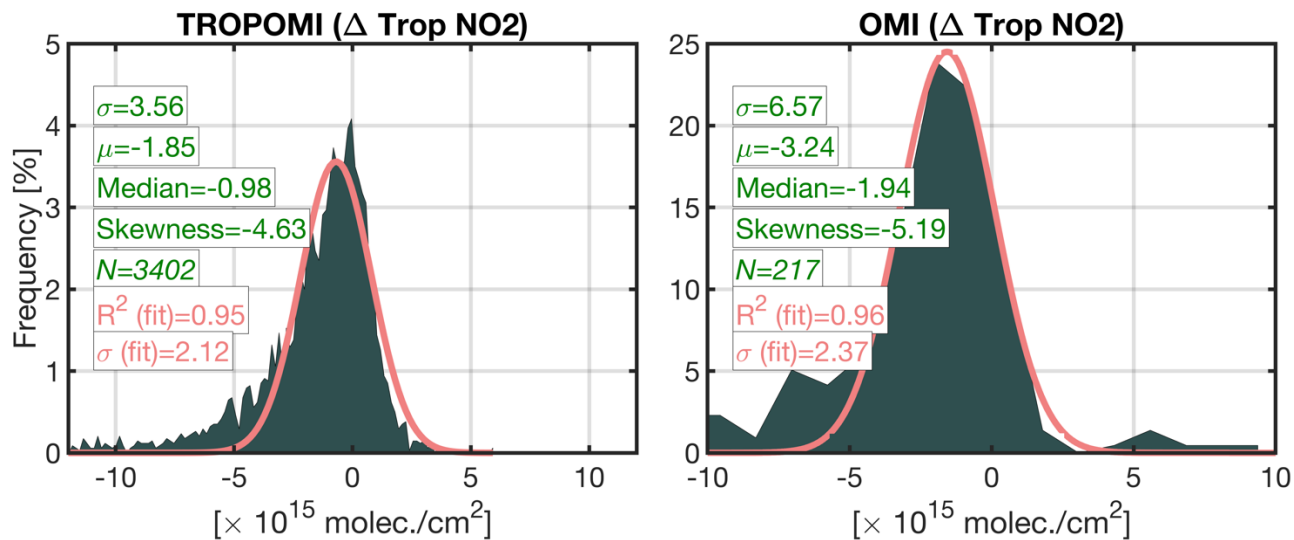
1305  
 1306 **Figure 7.** Oversampled TROPOMI total HCHO columns (top), tropospheric NO<sub>2</sub> columns  
 1307 (middle), and the ratio (bottom) at  $3 \times 3 \text{ km}^2$  from June till August 2021 over the US.  
 1308



1309  
 1310 **Figure 8.** The first column represents the spatial map of HCHO/NO<sub>2</sub> ratios over Los Angeles in  
 1311 June till August 2021 at different spatial resolutions. To upscale each map to a coarser footprint,  
 1312 we use an ideal box filter tailored to the target resolution. The second column shows the  
 1313 semivariograms corresponding to the left map along with the fitted curve (red line). The sill and the  
 1314 range are computed based on the fitted curve. The x-axis in the semivariogram is in degree (1 degree  
 1315 ~ 110 km).  
 1316

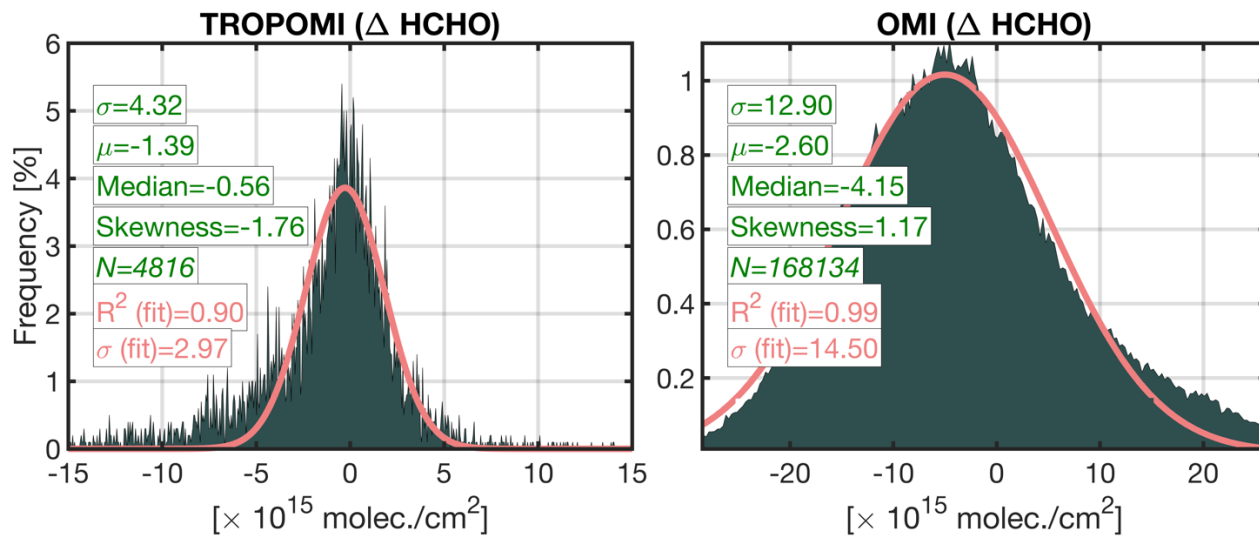


1317  
 1318 **Figure 9.** The spatial representation errors quantified based on the proposed method in this study.  
 1319 The error explains the spatial loss (or variance) due to the footprint of a hypothetical sensor at  
 1320 different length scales. To put this error in perspective, a grid box with 216x216 km<sup>2</sup> will naturally  
 1321 lose 65% of the spatial variance existing in the ratio at the scale of Los Angeles which roughly is  
 1322 50 km wide. All of these numbers are in reference to the TROPOMI 3x3 km<sup>2</sup>.  
 1323

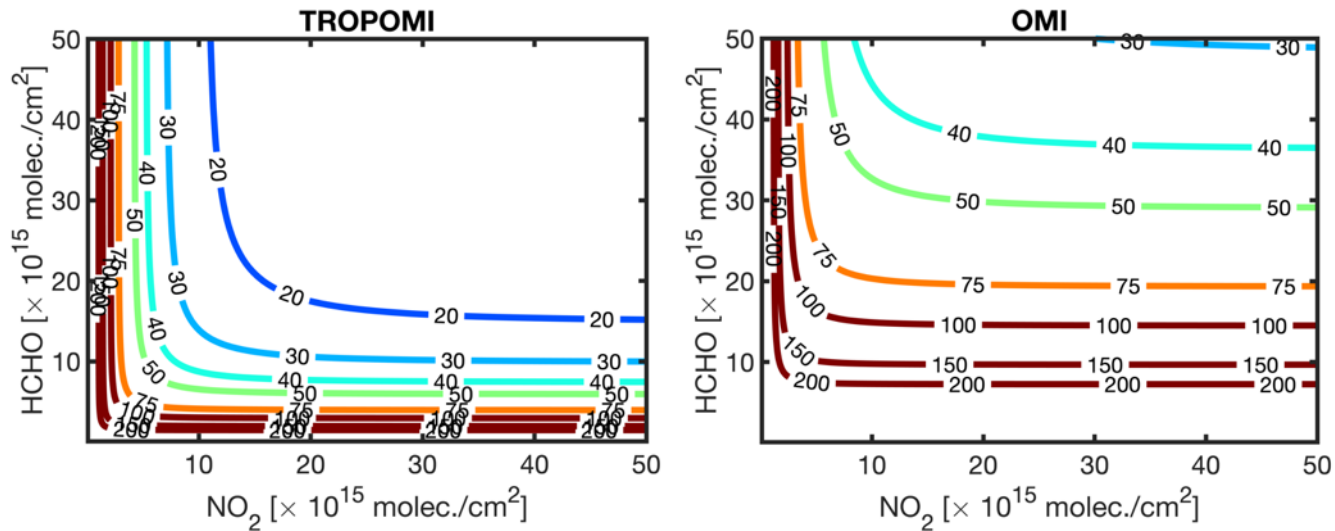


1.  
 1325 **Figure 10.** The histogram of the differences between TROPOMI and OMI and benchmarks. MAX-  
 1326 DOAS and integrated aircraft spirals are the TROPOMI and the OMI benchmarks, respectively.  
 1327 The data curation and relevant criteria on how they have been paired can be found in Verhoest et  
 1328 al. (2021) and Choi et al. (2020). The statistics in green color are based on all data, whereas those  
 1329 in pink are based on the fitted Gaussian function.  
 1330

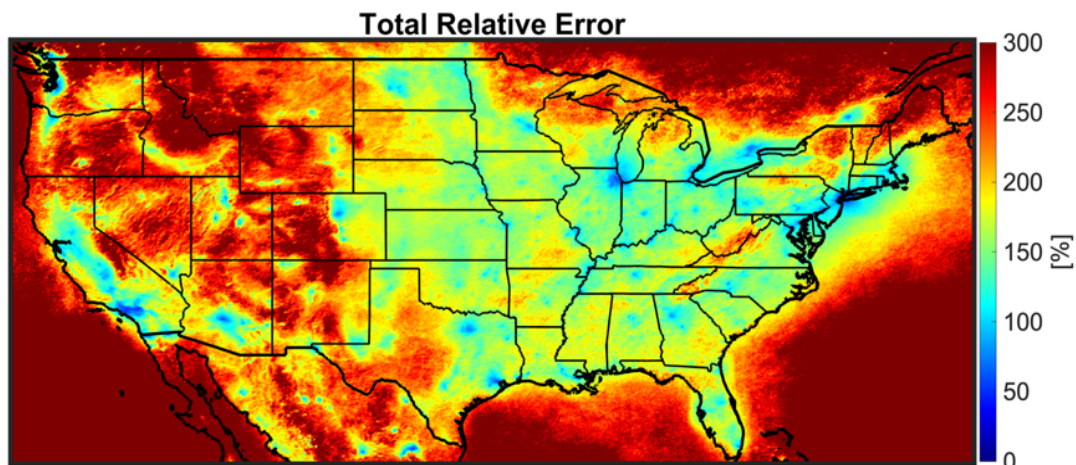




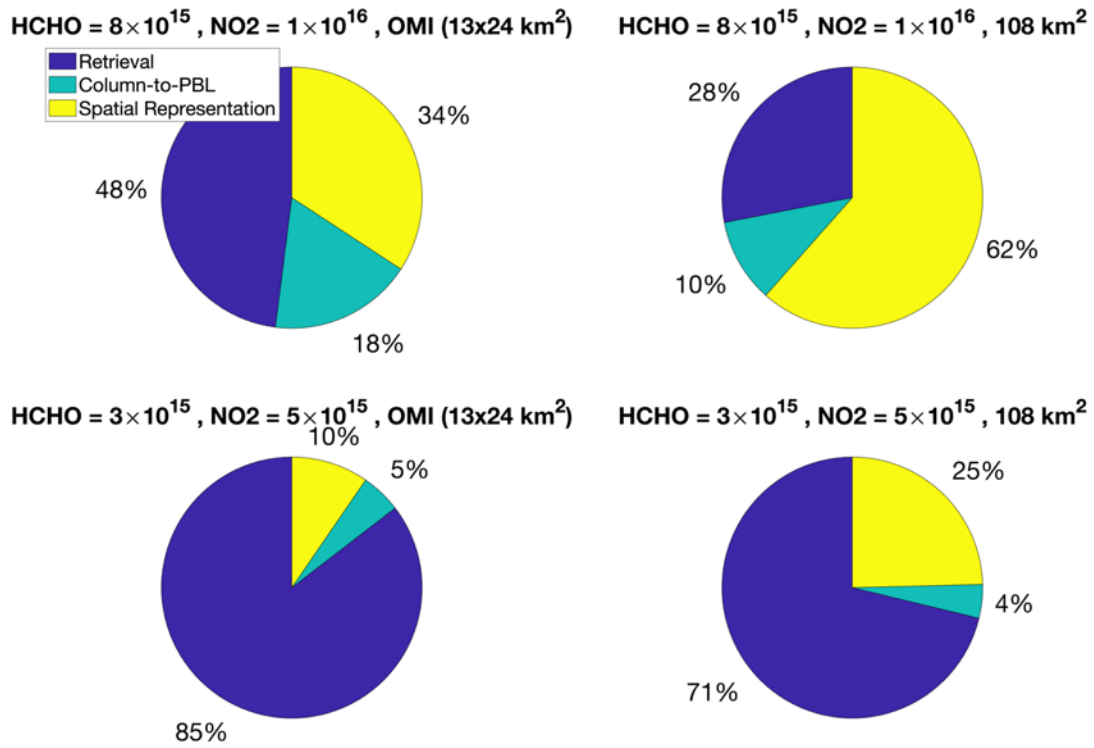
13  
 1332 **Figure 11.** The histogram of the differences between TROPOMI and OMI and benchmarks. FTIR  
 1333 and corrected GEOS-Chem simulations are respectively the TROPOMI and the OMI benchmarks.  
 1334 The data curation and relevant criteria on how they have been paired can be found in Vigouroux  
 1335 et al. (2021) and Zhu et al. (2020). The statistics in green color are based on all data, whereas those  
 1336 in pink are based on the fitted Gaussian function.  
 1337  
 1338



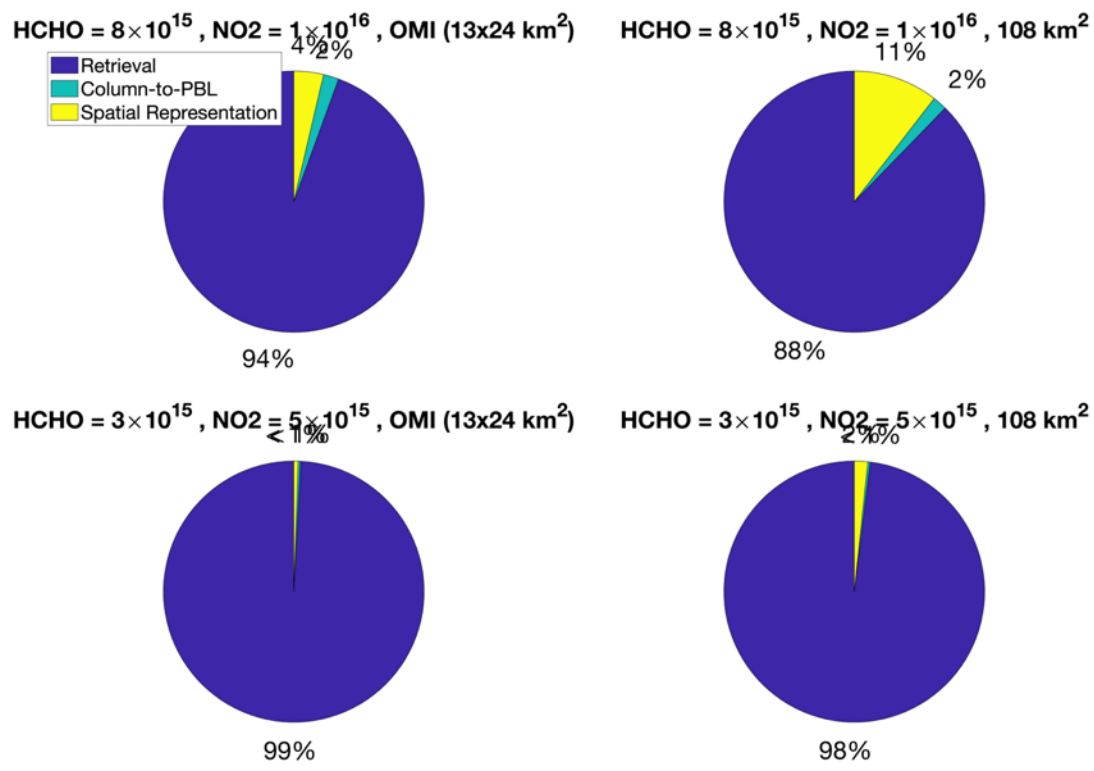
133  
 1340 **Figure 12.** The contour plots of the relative errors in TROPOMI (left) and OMI (right) based on  
 1341 dispersions derived from Figure 10 and 11. The errors used for these estimates are based on daily  
 1342 observations.  
 1343



1344  
 1345 **Figure 13.** The total relative error for observed TROPOMI HCHO/NO<sub>2</sub> ratios considering the  
 1346 daily TROPOMI retrieval errors ( $\sigma_{NO_2} = 2.11 \times 10^{15}$  molec./cm<sup>2</sup> and  $\sigma_{HCHO} = 2.97 \times 10^{15}$   
 1347 molec./cm<sup>2</sup>), the spatial representation pertaining to OMI footprint over a city environment (13%  
 1348 loss in the spatial variance), and the column to the PBL translation parameterization (26%)  
 1349 proposed in this study. Please note that the observed FNR is based on mean values from June till  
 1350 August 2021, while the uncertainties used for error calculation are on daily-basis.  
 1351  
 1352



1353  
 1354 **Figure 14.** The fractional errors of retrieval (blue), column to PBL translation (green), and spatial  
 1355 representation (yellow) of the total error budget for different concentrations and footprints based  
 1356 on TROPOMI sigma values. The retrieval error used for the error budget is on daily basis.



1357  
1358  
1359

**Figure 15.** Same as Figure 14 but based on OMI sigma values.