| 1 | Influences of an Entrainment-Mixing Parameterization on |
|----|---|
| 2 | Numerical Simulations of Cumulus and Stratocumulus Clouds |
| 3 | Xiaoqi Xu ^{1,2,4} , Chunsong Lu ^{1*} , Yangang Liu ^{3*} , Shi Luo ^{1,5} , Xin Zhou ³ , Satoshi Endo ³ , |
| 4 | Lei Zhu ¹ , Yuan Wang ¹ |
| 5 | 1. Key Laboratory for Aerosol-Cloud-Precipitation of China Meteorological |
| 6 | Administration/Collaborative Innovation Center on Forecast and Evaluation of |
| 7 | Meteorological Disasters (CIC-FEMD), Nanjing University of Information Science & |
| 8 | Technology, Nanjing, China |
| 9 | 2. Nanjing Joint Institute for Atmospheric Sciences, Nanjing, China |
| 10 | 3. Environmental and Climate Sciences Department, Brookhaven National Laboratory, |
| 11 | Upton, US |
| 12 | 4. Key Laboratory of Transportation Meteorology, CMA, Nanjing, China |
| 13 | 5. College of Aviation Meteorology, Civil Aviation Flight University of China, |
| 14 | Guanghan, China |
| 15 | * Correspondence: <u>luchunsong110@gmail.com;</u> <u>lyg@bnl.gov</u> |
| 16 | |

17 Abstract

Different entrainment-mixing processes can occur in clouds; however, a 18 homogeneous mixing mechanism is often implicitly assumed in most commonly used 19 20 microphysics schemes. Here, we first present a new entrainment-mixing 21 parameterization that uses the grid-mean relative humidity without requiring the 22 relative humidity of the entrained air. Then, the parameterization is implemented in a 23 microphysics scheme in a large eddy simulation model, and sensitivity experiments are 24 conducted to compare the new parameterization with the default homogeneous 25 entrainment-mixing parameterization. The results indicate that the new entrainmentmixing parameterization has a larger impact on the number concentration, volume-26 27 mean radius, and cloud optical depth in the stratocumulus case than in the cumulus case. 28 This is because inhomogeneous and homogeneous mixing mechanisms dominate in the 29 stratocumulus and cumulus cases, respectively, which is mainly due to the larger 30 turbulence dissipation rate in the cumulus case. Because stratocumulus clouds break up 31 during the dissipation stage to form cumulus clouds, the effects of this new entrainment-32 mixing parameterization during the stratocumulus dissipation stage are between those during the stratocumulus mature stage and the cumulus case. A large aerosol 33 34 concentration can enhance the effects of this new entrainment-mixing parameterization 35 by decreasing the cloud droplet size and evaporation time scale. The results of this new 36 entrainment-mixing parameterization with grid-mean relative humidity are validated by 37 use of a different entrainment-mixing parameterization that uses parameterized

entrained air properties. This study sheds new light on the improvement of entrainment-mixing parameterizations in models.

40

41 **1. Introduction**

42 The process of entrainment and subsequent mixing between clouds and their 43 environment is one of the most uncertain processes in cloud physics, which is thought 44 to be crucial to many outstanding issues, including warm-rain initiation and subsequent 45 precipitation characteristics, cloud-climate feedback, and evaluating the indirect effects 46 of aerosol (Paluch and Baumgardner, 1989; Yum, 1998; Ackerman et al., 2004; Kim et al., 2008; Huang et al., 2008; Del Genio and Wu, 2010; Lu et al., 2011; Lu et al., 2014; 47 48 Kumar et al., 2013; Zheng and Rosenfeld, 2015; Fan et al., 2016; Gao et al., 2020; Gao 49 et al., 2021; Zhu et al., 2021; Xu et al., 2021; Kumar et al., 2013; Yang et al., 2016; 50 Yang et al., 2021). The most well-studied concepts are homogeneous/inhomogeneous 51 entrainment-mixing mechanisms. During homogeneous mixing, all droplets experience 52 evaporation, and no droplet is evaporated completely. During extremely 53 inhomogeneous mixing, some droplets near the entrained air evaporate completely, 54 while the remaining droplets maintain their original sizes. If the situation is somewhere 55 between these two extreme scenarios, an inhomogeneous mixing process occurs. Some 56 studies suggest that homogeneous mixing is likely to be typical (Jensen et al., 1985; 57 Burnet and Brenguier, 2007; Lehmann et al., 2009), whereas others have claimed that 58 extremely inhomogeneous scenario is dominant (Pawlowska et al., 2000; Burnet and

| 59 | Brenguier, 2007; Haman et al., 2007; Freud et al., 2008; Freud et al., 2011). Different |
|----|---|
| 60 | mechanisms can be undistinguishable when the relative humidity in the entrained air is |
| 61 | high (Gerber et al., 2008). |

62 Some sensitivity studies assuming homogeneous or extremely inhomogeneous 63 mixing have found that different mixing mechanisms can significantly influence the 64 microphysics and radiative properties of clouds (Lasher-Trapp et al., 2005; Grabowski, 65 2006; Chosson et al., 2007; Slawinska et al., 2008). For example, Grabowski (2006) used a cloud-resolving model and found that the amount of solar energy reaching the 66 67 surface in the pristine case, assuming the homogeneous mixing scenario, is the same as in the polluted case with extremely inhomogeneous mixing. This result was verified by 68 69 Slawinska et al. (2008) using a large-eddy simulation (LES) model. Although the 70 influence of different mixing mechanisms in simulations is lower when two-moment 71 microphysics schemes are used (Hill et al., 2009; Grabowski and Morrison, 2011; 72 Slawinska et al., 2012; Xu et al., 2020), Hill et al. (2009) also claimed that there are 73 still many uncertainties in the entrainment-mixing process, and the effect of different 74 mixing mechanisms can be more important over the entire cloud life-cycle.

In recent years, methods have been developed to describe general entrainmentmixing processes, with homogeneous and extremely inhomogeneous scenarios as special cases (Andrejczuk et al., 2006; Andrejczuk et al., 2009; Lehmann et al., 2009; Lu et al., 2011). Hoffmann et al. (2019) and Hoffmann and Feingold (2019) conducted LES at the subgrid-scale with turbulent mixing, using a linear eddy model. Andrejczuk

| 80 | et al. (2009) used the results of direct numerical simulation (DNS) to establish a |
|----|---|
| 81 | relationship between instantaneous microphysical properties and Damköhler number |
| 82 | $(D_a, Burnet and Brenguier, 2007)$, and developed a parameterization of the entrainment- |
| 83 | mixing process. Lu et al. (2013) developed a parameterization of the entrainment- |
| 84 | mixing process based on the relationship between the homogeneous mixing degree (ψ) |
| 85 | and transition scale number (N_L) in the explicit mixing parcel model (EMPM), as well |
| 86 | as aircraft observation data. Gao et al. (2018) investigated how ψ is related to D_a and |
| 87 | $N_{\rm L}$ in a DNS, to improve the parameterization of the entrainment-mixing process. Luo |
| 88 | et al. (2020) simulated more than 12,000 cases with EMPM by changing a variety of |
| 89 | parameters affecting entrainment-mixing processes and developed a parameterization |
| 90 | that improved the one proposed by Lu et al. (2013). |

91 Although several entrainment-mixing parametrizations have been proposed, to the 92 best of our knowledge, only one study (Jarecka et al., 2013) has coupled an entrainment-93 mixing parameterization with cloud microphysics to consider the change in cloud 94 droplet concentration during the entrainment-mixing process. Jarecka et al. (2013) 95 applied an entrainment-mixing parameterization, in terms of the Damköhler number, to 96 a two-moment microphysics scheme and found small impacts of entrainment-mixing 97 parameterization in shallow cumulus clouds. To further explore the influences of entrainment-mixing processes, this study first modifies the entrainment-mixing 98 99 parameterization in terms of the transition scale number proposed by Luo et al. (2020) 100 to couple it more easily with microphysics schemes. The parameterization is then implemented in the two-moment Thompson aerosol-aware scheme (Thompson and
Eidhammer, 2014). Finally, the effects of parameterization on the physical properties
of clouds are examined in both cumulus and stratocumulus clouds.

104 The rest of this paper is organized as follows: Section 2 describes the new 105 entrainment-mixing parameterization, simulated cases, and modelling setup. The major 106 results are presented and discussed in Section 3. The influences of the new entrainment-107 mixing parameterization on cloud physics and the underlying mechanisms are 108 examined, and the effects of turbulence dissipation rate (ε) and aerosol concentration

are also discussed. Some concluding remarks are presented in Section 4.

110

111 **2.** Parameterization, simulated cases, and modeling setup

112 **2.1** The new entrainment-mixing parameterization

113 According to Morrison and Grabowski (2008), the effect of the entrainment-

114 mixing process on cloud microphysical properties can be expressed as follows:

115
$$N_{\rm c} = N_{\rm c0} \left(\frac{q_{\rm c}}{q_{\rm c0}}\right)^{a}$$
, (1)

116 where N_c and N_{c0} are the cloud droplet number concentrations after and before the 117 evaporation process, respectively, and q_c and q_{c0} represent the corresponding cloud 118 water mixing ratios. It is noteworthy that when a new saturation is achieved after 119 evaporation, q_c is determined by q_{c0} , relative humidity (RH), air pressure, and 120 temperature. The parameter α can be pre-set to any value between 0 (homogeneous 121 mixing) and 1 (extremely inhomogeneous mixing) to represent a different degree of 122 subgrid-scale mixing homogeneity. In this study, instead of specifying α as a 123 predetermined constant, here it is determined through expressions (Lu et al., 2013; Luo 124 et al., 2020)

125
$$\alpha = 1 - \psi$$
, (2a)

126
$$\psi = c \exp(aN_{\rm L}^b). \tag{2b}$$

127 where *a*, *b* and *c* are the three fitting parameters (Luo et al., 2020). The dimensionless 128 number $N_{\rm L}$ is a dynamical measure of the degree of subgrid-scale mixing homogeneity 129 (Lu et al., 2011) defined by

$$N_{\rm L} = \frac{L^*}{\eta},\tag{3a}$$

131
$$\eta = \left(\nu^3 / \varepsilon\right)^{1/4}, \tag{3b}$$

132
$$L^* = \varepsilon^{1/2} \tau_{evap}^{3/2},$$
 (3c)

133 where L^* is the transition length (Lehmann et al., 2009), η is the Kolmogorov microscale, 134 v is the kinematic viscosity; ε is calculated from the subgrid turbulent kinetic energy 135 (Deardorff, 1980):

136 $\mathcal{E} = C E^{3/2} / L, \tag{4}$

137 where
$$C = 0.70$$
 is an empirical constant, *E* is the subgrid turbulent kinetic energy, and
138 *L* is the model grid size. The evaporation time scale (τ_{evap}) is defined as the time taken
139 for droplets to evaporate completely in an unsaturated environment, and is calculated
140 as

141
$$\tau_{evap} = -\frac{r^2}{2AS_e},$$
 (5a)

142
$$A = \frac{1}{\left[\left(\frac{L_{\rm h}}{R_{\rm v}T} - 1\right)\frac{L_{\rm h}\rho_{\rm L}}{KT} + \frac{\rho_{\rm L}R_{\rm v}T}{De_{\rm s}(T)}\right]},\tag{5b}$$

where *r* is the volume-mean radius of cloud droplets, *A* is a function of pressure and temperature, S_e is the supersaturation (RH-1) of entrained air, L_h is the latent heat, R_v is the specific gas constant for water vapour, *T* is air temperature, ρ_L is the density of liquid water, *K* is the coefficient of thermal conductivity of air, *D* is the diffusion coefficient of water vapour in the air, and $e_s(T)$ is the saturation vapour pressure over a plane water surface at temperature *T*.

149 Unfortunately, S_e in Equation (5a) is generally unavailable in atmospheric models, 150 including LES models. Thus, the entrainment-mixing parameterization developed by 151 Luo et al. (2020) based on the properties of entrained air cannot be used directly. To 152 solve this problem, we modify the entrainment-mixing parameterization of Luo et al. 153 (2020) by replacing S_e with the domain-mean RH in the EMPM, after entrainment but 154 before evaporation, based on 12,218 cases:

155
$$\psi = 107.19 \exp(-1.99 N_{\rm L}^{-0.29}).$$
 (6)

0.00

Figure 1 shows the fitting results of the modified new entrainment-mixing parameterization. Compared to the parametrization proposed by Luo et al. (2020), the modified parameterization has similar ψ - N_L distributions, but with a larger N_L for the same ψ , because the EMPM domain-mean RH is larger than the entrained air RH. With this modification, N_L , ψ , and thus the effect of the entrainment-mixing processes on droplet concentration can be directly calculated using the LES grid-mean RH. It is 162 important to note that the parameterization does not mean that the entrained air RH is 163 equal to that of the LES grid-mean RH. It is also worth noting that a wide range of ε , 164 $S_{\rm e}$, and fraction of entrained air (*f*) are taken into account when establishing the 165 parameterization with the EMPM. The details of the EMPM simulations and related 166 calculations are provided by Luo et al. (2020).

167

168 **2.2 LES model, simulation cases, and modelling setup**

169 The LES model is built by applying the large-scale forcing module presented in 170 Endo et al. (2015) to the Weather Research and Forecasting (WRF) model tailored for 171 solar irradiance forecasting (WRF-Solar, Hacker et al., 2016; Haupt et al., 2016). The large-scale forcing data (VARANAL) used in this process is derived from the 172 173 constrained variational analysis (CVA) approach developed by Zhang et al. (2001) and provided by the U.S. Department of Energy's Atmospheric Radiation Measurement 174 175 Program (www.arm.gov). The modified entrainment-mixing parameterization is 176 implemented in the two-moment Thompson aerosol-aware scheme (Thompson and 177 Eidhammer, 2014).

To investigate the behaviours of the new entrainment-mixing parameterization in different cloud types, cumulus and stratocumulus cases are simulated. For both the cumulus and stratocumulus cases, the horizontal resolution of the model is $100 \text{ m} \times 100$ m with a domain area of 14.4 km × 14.4 km. The vertical direction is divided into 225 layers with a resolution of 30 m. 183 For each cloud case, ψ is first set to 1 for the *default* experiment because most LES models assume a homogeneous entrainment-mixing mechanism. The simulation with 184 185 the new entrainment-mixing parameterization (Equations (1-6)) is hereafter referred to 186 as *new*. First, N_L is diagnosed for each grid, and ψ is then calculated using Equation (6). 187 Finally, the variation in N_c during entrainment-mixing is obtained using Equations (1) 188 and (2a). To examine the influence of the aerosol number concentration on the 189 entrainment-mixing process, we conduct the numerical experiments default 10 and 190 new 10 by multiplying the initial aerosol number concentrations, for the *default* and 191 new models, respectively, by a factor of 10. Thus, four sets of numerical experiments 192 are conducted for both the cumulus and stratocumulus cases; the names of the 193 experiments and corresponding descriptions are summarized in Table 1.

194

195 **3. Results**

196 **3.1 Cumulus case**

For the cumulus case, the simulation starts at 12:00 UTC on 11 June 2016 and ends at 03:00 UTC on 12 June 2016 with an output interval of 10 min and spin-times of 3 h. To demonstrate the utility of the model, Figure 2 compares the temporal evolution of the observed and simulated cloud fraction (a) and solar irradiance (b) from the *default* experiment. Grid points with q_c larger than 0.01 g/kg are defined as "cloudy areas". Also shown for comparison is observational data with a one-hour temporal resolution, which is provided by the LES Atmospheric Radiation Measurement 204 Symbiotic Simulation and Observation (LASSO) campaign (Gustafson et al., 2020). 205 The observations show that the cloud forms at 12:00 UTC on 11 June and dissipates 206 completely by 01:00 UTC on 12 June with a maximum cloud fraction of 0.47 at 16:00 207 UTC on 11 June. Considering the difference between the solar irradiances obtained 208 from point measurements and the value representing the simulation domain, the 209 observed solar irradiance at the Southern Great Plains (SGP) Central Facility are 210 compared with the results of central grid point in simulation (Figure 2(b)). Evidently, 211 although the results of simulation do not fluctuate as much as the observations, the 212 model captures the general behaviours of both cloud fraction and solar irradiance. The 213 general agreement between the simulations and observations lends credence to using 214 the model in further study.

Figure 3 shows the evolution of the microphysical and optical properties of clouds in the cloudy areas of all simulation experiments, including q_c , N_c , droplet volumemean radius (r_v), cloud water path (CWP), and cloud optical depth (τ). To visually and simultaneously compare the change in cloud droplet concentration under different aerosol concentrations, the maximum cloud droplet concentration (N_{cmax}) from *default* is used to normalize N_c in *default* and *new*, while N_{cmax} from *new_10* is used to normalize N_c in *default_10* and *new_10*. The CWP is calculated as:

222
$$CWP = \int_0^H \rho_a q_c(z) dz, \qquad (7)$$

223 where ρ_a is the air density, $q_c(z)$ is the cloud water mixing ratio at each height (z), and 224 *H* is the cloud thickness. The optical depth τ is estimated with

225
$$\tau = \frac{3}{2} \frac{1}{\rho_{\rm w}} \int_0^H \frac{\rho_{\rm a} q_{\rm c}(z)}{r_{\rm e}(z)} dz, \qquad (8)$$

where ρ_w is the water density and $r_e(z)$ is the effective radius of the cloud droplets at each height (z). The time-averaged values of these physical properties of the clouds are listed in Table 2 for convenience.

229 For the low aerosol number concentration, the simulations with the new 230 entrainment-mixing parameterization have smaller N_c (35.53 cm⁻³) and larger r_v (13.29 μ m) than the default homogeneous simulation (35.78 cm⁻³ for N_c and 13.27 μ m for r_v 231 232 in *default*). However, comparing *new* to *default*, the relative changes in N_c , r_v , and τ are 233 very small. When the aerosol concentration increases ten-fold (*default 10* and *new 10*), 234 $q_{\rm c}$, CWP, and τ increase according to the aerosol indirect effect (Peng et al., 2002; Wang et al., 2019; Li et al., 2011; Wang et al., 2011). Meanwhile, r_v decreases significantly 235 236 owing to the larger cloud number concentration. The effects of the new entrainment-237 mixing parameterization also increase, for example, the change in N_c increases from – 238 0.70% (new compared to default) to -2.74% (new 10 compared to default 10), r_v 239 increases from +0.15% to +0.57%, and τ from -0.38% to -0.58%; the reasons for these changes are discussed later. These small changes are similar to those identified in 240 241 previous cumulus studies (Jarecka et al., 2013; Hoffmann et al., 2019).

242

243 **3.2 Stratocumulus case**

The stratocumulus case is simulated from 9:00 UTC on 19 April 2009 to 03:00 UTC on 20 April 2009; the first three hours are set to be spin-up times. We examine the 246 stratocumulus region of the cloud base at ~ 2.1 km and the cloud top at ~ 2.3 km (cloud thickness of ~200 m). Figure 4 shows the time series of the domain-averaged cloud 247 248 fraction and total downward irradiance at the central point in the observation and the 249 default experiment from 12:00 UTC to 24:00 UTC. Similar to the cumulus case, the 250 simulations compare favourably with the observations, which further reinforces the 251 utility of the LES model. The observed data show that the cloud fraction increases with 252 time and peaks at 16:00 UTC. The simulated cloud fraction has a value of 1 before 253 16:00 UTC, fluctuates from 16:00 UTC to 21:00 UTC, and decreases sharply after 254 21:00 UTC. This period can be divided into three stages, namely the mature stage, pre-255 dissipation stage, and dissipation stage.

As with the cumulus case, the temporal evolutions of the physical properties (q_c , N_c, r_v , CWP, and τ) of the clouds are shown in Figure 5. In contrast to the oscillating changes exhibited by the physical quantities in the cumulus case (Figure 3), the physical properties in the stratocumulus case exhibit a mostly smooth temporal evolution. Furthermore, *default* and *new* exhibit clear distinctions during the early periods, but these differences decrease during the dissipation stage. This is also the case with *default 10* and *new 10*.

To compare the different behaviours of the simulation experiments at different stages, the results at the mature and dissipation stages are analysed in detail. The mean values of the main microphysical and optical properties of the clouds are summarised in Table 3. As expected, the cloud microphysical and optical properties at the mature

| 267 | stage are all larger than those at the dissipation stage. The effects of the new |
|-----|--|
| 268 | entrainment-mixing parametrization are also more significant at the mature stage. |
| 269 | Compared to <i>default</i> , the <i>new</i> model results in a 7.36% smaller N_c , 3.20% larger r_v , and |
| 270 | 5.98% smaller τ during the mature stage. During the dissipation stage, the changes in |
| 271 | $N_{\rm c}$, $r_{\rm v}$, and τ are -4.76%, +2.12 %, and -2.56%, respectively. The largest influence of |
| 272 | the new entrainment-mixing parametrization occurs during the mature stage when the |
| 273 | aerosol concentration is ten times greater. The differences in $N_{\rm c}$, $r_{\rm v}$, and τ between |
| 274 | new_10 and default_10 are -9.69%, +3.88%, and -5.85%, respectively, averaged over |
| 275 | the mature stage. These differences are much larger than those reported by Hill et al. |
| 276 | (2009) who found that assuming extremely inhomogeneous mixing has a negligible |
| 277 | effect on stratocumulus simulations. Our results also prove the speculation of Hill et al. |
| 278 | (2009) that the mixing process might play an important role when the stratocumulus is |
| 279 | thin (~200 m in this study). Furthermore, implementing the new entrainment-mixing |
| 280 | parameterization has similar effects on cloud properties to those described by Hoffmann |
| 281 | and Feingold (2019) who used the linear eddy model to represent subgrid-scale |
| 282 | turbulent mixing. Note that stratocumulus clouds occur in most regions around the |
| 283 | world and are important contributors to the surface radiation budget (Wood, 2012; |
| 284 | Zheng et al., 2016; Wang et al., 2021; Wang and Feingold, 2009). Stratocumulus clouds |
| 285 | dominate in some regions and occur over 60% of the time as vast long-lived sheets, |
| 286 | such as the semi-permanent subtropical marine stratocumulus sheets (Wood, 2012). In |
| 287 | these regions, a nearly 6% decrease in τ , caused by the new entrainment-mixing |

parameterization is expected to have significant effects on the simulation of regionalradiative properties and climate change.

290 The averaged influences of the new entrainment-mixing parametrization over all 291 the simulation periods are also examined (Table 4). Quantitatively, the effect of the new 292 entrainment-mixing parameterization is much greater on stratocumulus clouds than on 293 cumulus clouds. Compared to *default*, *new* has an average change of -6.20% in N_c, +2.01% in r_v , and -3.23% in τ . When the aerosol concentration increases ten-fold, the 294 differences in N_c , r_v , and τ between *default 10* and *new 10* are -9.00%, +3.16%, and 295 296 -4.14%, respectively. These differences are larger than the largest changes in the 297 cumulus case.

298

299 **3.3** Mechanisms of the effects of the new entrainment-mixing parameterization

The different effects of the new entrainment-mixing parameterization on different types of clouds and even on different stages of stratocumulus clouds are likely be related to variations in the dominant mixing mechanism. To confirm this, we calculate the average ψ at all grid points experiencing evaporation, the proportion of inhomogeneous mixing grid points to all grid points experiencing evaporation, and the average ψ at the inhomogeneous mixing grid points in *new* and *new_10* (Table 5) for the cumulus case, and mature and dissipation stages in the stratocumulus case.

307 For the cumulus case, simulations exhibit large ψ and a small proportion of 308 inhomogeneous mixing, indicating that homogeneous mixing is the dominant

309 entrainment-mixing mechanism (Luo et al., 2020; Lu et al., 2013). Correspondingly, 310 the influences of the new entrainment-mixing parameterization on the cloud physical 311 properties are not significant, as shown in Figure 3 and Table 2. The *new_10* model 312 exhibit a smaller average ψ and a larger proportion of inhomogeneous mixing than *new*, 313 which results in larger changes in cloud physics, as mentioned in Section 3.1.

314 For the stratocumulus case, Table 5 shows the average ψ at all grid points experiencing evaporation, the proportion of inhomogeneous mixing grid points to all 315 316 grid points experiencing evaporation, and the average ψ at the inhomogeneous mixing 317 grid points during the two stages. The mature stage always has a smaller ψ but a larger 318 proportion of inhomogeneous mixing than the dissipation stage. The inhomogeneous 319 mixing process dominates the mature stage in *new*, because more than 60% of the grid 320 points experience inhomogeneous mixing. The inhomogeneous mixing process is more dominant in new 10, because less than 3% of the cloudy grid points experience a 321 322 homogeneous mixing process during the mature stage, which explains why new 10 has 323 the largest influence when implementing the new entrainment-mixing parametrization. 324 Meanwhile, the average ψ in both stages is smaller than that in the cumulus case for the 325 same simulation configuration. Thus, the effects of the new entrainment-mixing 326 parameterization are more significant for stratocumulus than for cumulus clouds, 327 especially at the mature stage. It is noted that the average ψ and the proportion of 328 inhomogeneous mixing at the dissipation stage of *new* in the stratocumulus case are 329 very close to the results of new 10 in the cumulus case. This is because the cloud

fraction decreases sharply during the dissipation stage; the stratocumulus clouds breakup and produces cumulus clouds with small cloud droplet radius.

332

333 3.4 The effects of dissipation rate and aerosol concentration on the entrainment-

334 mixing process

335 Previous studies have shown the notable effects of the dissipation rate and aerosol 336 concentration on the entrainment-mixing process. For example, Luo et al. (2020) changed ε from 10⁻⁵ m² s⁻³ to 10⁻² m² s⁻³ and noted huge differences in the corresponding 337 338 ψ . Small et al. (2013) compared aircraft observations with different background 339 concentrations and found that higher pollution flights tended to slightly more 340 inhomogeneous mixing; Jarecka et al. (2013) also showed various homogeneities of 341 subgrid mixing when aerosol concentration increases ten-fold. To explain the different 342 behaviours of different simulations with the new entrainment-mixing parameterization, 343 the influences of ε and aerosol concentration are examined. Figure 6 shows the probability distribution functions (PDFs) of ε , r_v , τ_{evap} , and N_L for cloud grids 344 345 experiencing entrainment-mixing processes in new and new 10 for the cumulus and 346 stratocumulus cases, respectively. The PDFs from the mature and dissipation stages of 347 the stratocumulus case are shown in Figure 7.

348

349 **3.4.1 Dissipation rate**

350 According to Equation (3), $N_{\rm L}$ is a function of $\varepsilon^{3/4}$; hence, the PDF of ε directly

| 351 | affects $N_{\rm L}$ and further results in different ψ . For the cumulus case, the mean ε of 0.0043 |
|-----|--|
| 352 | $m^2 s^{-3}$ in <i>new</i> is similar to those obtained for cumulus clouds in previous studies (e.g. |
| 353 | Lu et al., 2016; Hoffmann et al., 2019). As shown in Figure 1, cloud grids experience a |
| 354 | homogeneous mixing process if N_L is larger than ~10 ⁵ , the limited distribution of N_L |
| 355 | values less than 10^5 in <i>new</i> results in a very small number of cloud grid points |
| 356 | undergoing inhomogeneous mixing process. Even at the cloud grid points that undergo |
| 357 | inhomogeneous mixing, the average ψ is large (98.62%), because most of the N _L values |
| 358 | are larger than 10^3 . Therefore, the cloud properties in <i>new</i> are close to those in <i>default</i> . |
| 359 | For the stratocumulus case, the mean value of ε (2.9×10 ⁻⁴ m ² s ⁻³ in <i>new</i>) is an order |
| 360 | of magnitude less than those in the cumulus case. Therefore, compared with the |
| 361 | cumulus case, $N_{\rm L}$ is reduced in the stratocumulus case, while the peak value of <i>new</i> |
| 362 | almost reaches the criterion of inhomogeneous mixing ($\sim 10^5$). For the two stages of |
| 363 | stratocumulus clouds, ε is an order of magnitude smaller, but r_v was larger (Figure 7) |
| 364 | during the mature stage than during the dissipation stage. According to Equation (5a), |
| 365 | droplets with smaller r_v are more prone to complete evaporation and have a smaller τ_{evap} . |
| 366 | The combination of smaller ε and larger r_v results in a smaller N_L (Equation (3)). This |
| 367 | is the reason for the new entrainment-mixing parametrization having more significant |
| 368 | effects during the mature stage than during the dissipation stage. In addition, the |
| 369 | similarity of the ε and r_v values during the dissipation stage of the stratocumulus case |
| 370 | in new, compared to the cumulus case in new_10 (Figures 6a and 6b), explains the |
| 371 | similar average ψ values of these scenarios and the proportion of inhomogeneous |

372 mixing (Table 5).

Therefore, the distribution of ε has a vital impact on the influence of the new 373 entrainment-mixing parameterization. Smaller values of ε result in the new 374 375 entrainment-mixing parameterization having a more significant influence. Moreover, 376 the r_v in the stratocumulus case is smaller than that in the cumulus case, which is also 377 conducive to a more inhomogeneous mixing process. These are the reasons why the 378 implementation of the new entrainment-mixing parameterization has a larger influence 379 in the stratocumulus case than in the cumulus case, when compared to a homogeneous 380 mixing mechanism.

381

382 3.4.2 Aerosol concentration

383 The aerosol concentration affects the entrainment-mixing process by decreasing 384 the cloud droplet radius. As r_v decreases, the distributions of τ_{evap} in new 10 moves to 385 a smaller overall value, while the mean value is an order of magnitude smaller than that in *new*, which causes a much smaller $N_{\rm L}$ because $N_{\rm L}$ is proportional to $\tau_{\rm evap}^{3/2}$ (Equations 386 387 (3a) and (3b)). The larger percentage of smaller $N_{\rm L}$ values indicates that in *new 10*, more grid points undergo an inhomogeneous mixing process, and the proportion of such 388 389 grid points is much larger than in the new model (Table 5). Therefore, compared to new, 390 *new 10* exhibit a smaller ψ and the effects of the new entrainment-mixing 391 parameterization on cloud properties are more obvious, for both the cumulus and 392 stratocumulus cases.

394 3.5 Verification by the simulations with a different parameterization using 395 entrained air relative humidity

396 In the above simulations, the new entrainment-mixing parameterization is based 397 on the grid-mean RH. This section serves to verify these simulations using the the 398 entrainment-mixing parameterization proposed by Luo et al. (2020)

399
$$\psi = 107.96 \exp(-0.95 N_{\rm L}^{-0.35}),$$
 (9)

which was developed using the entrained air RH in the EMPM. This parameterization
needs the entrained air RH within each grid in WRF, which is estimated following
Grabowski (2007) and Jarecka et al. (2009). Briefly, assuming that RH mixes linearly
when the dry air entrains into the cloud, then entrained air RH can be simply calculated
by

405
$$RH_{\text{entrained}} = \frac{RH_{\text{grid}} - (1 - f)RH_{\text{cloud}}}{f},$$
 (10)

406 where the subscripts entrained, cloud, and grid indicate the RH of the entrained, cloudy, 407 and grid point air, respectively. In Equation (10), although the cloudy air RH is 408 approximately 100% and grid-mean RH is predicted in the model, the entrained air 409 fraction f needs to be further parameterized. To obtain f at 100 m, a parameterization of 410 f is developed based on the simulations for both the cumulus and stratocumulus cases with a higher resolution of 10 m; the other configurations are the same as those in the 411 412 experiment default. The 10 m-resolution simulation results are then averaged to the resolution of 100 m. Following Xu and Randall (1996), "1 - f" can be fitted by the 413

414 function

417

418

415
$$1 - f = RH_{\text{grid}}^{\gamma} \left[1 - \exp(-\beta q_{\text{c}}) \right], \qquad (11)$$

416 where γ and β are empirical parameters. Figure 8 shows that the parameterization with $\gamma = 8.72$ and $\beta = 1.47 \times 10^4$ can well reproduce the simulated values of "1 - f", with the

correlation coefficient (R) of 0.89 and significant level p value < 0.01. Considering

that local shear (dw/dz) and buoyancy (B) may drive turbulence generation and 419

entrainment for a microscale process, the two quantities are also used to fit "1 - f" 420

except for RH_{grid} and q_c . However, the addition of dw/dz and B to Equation (11) does 421

422 not increase R. Therefore, using RH_{grid} and q_c to parametrize "1 – f" is good and

423 reasonable for a microscale process.

424 Equations (9-11) are applied in the simulations for both the cumulus and 425 stratocumulus cases with different aerosol background (hereafter new f and new f 10). Same as Figures 3 and 5, the temporal evolutions of the cloud physical 426 properties (q_c , N_c , r_v , CWP, and τ) in default, default 10, new f, and new f 10 are 427 428 shown in Figures 9 and 10. The results are similar to Figures 3 and 5. The mean values 429 of these properties of new f and new f 10 for the cumulus and stratocumulus cases 430 are also shown in Table 6, the results of new and new 10 are also shown in the 431 parentheses for the convenience of comparison. The results of *new f* and *new* are very 432 similar, with the maximum difference being no more than 1%, so are the results of 433 tenfold aerosol background. Such a close agreement suggests that the results of the 434 new entrainment-mixing parametrization with grid-mean RH are reliable.

456 number concentration. The results of implementing the new entrainment-mixing457 parameterization are finally verified by the results using entrained air properties.

458 Unlike the commonly assumed homogeneous mixing scenario, the new 459 entrainment-mixing parameterization produces a smaller cloud droplet number 460 concentration and larger cloud droplet radius, with the degree of difference depending 461 on cloud types and stages. Sensitivity tests show that in the cumulus case, the largest 462 average influence of the new entrainment-mixing parameterization occurs under a high aerosol background, but results in only a 2.74% decrease in cloud droplet number 463 464 concentration and a 0.57% increase in cloud droplet volume-mean radius. The changes 465 become even smaller with a low aerosol background because of the larger cloud droplet 466 radius. In contrast, the new entrainment-mixing parameterization has a larger influence 467 on the microphysical and optical properties of stratocumulus clouds, especially under a 468 high aerosol background and during the mature stage, with a cloud fraction equal to 1. 469 The largest changes resulting from the new entrainment-mixing parameterization are -9.69%, +3.88%, and -5.85%, for cloud number concentration, cloud droplet volume-470 471 mean radius, and cloud optical depth, respectively. The new entrainment-mixing parameterization has less of an influence on the dissipation stage than on the mature 472 473 stage of the stratocumulus case, but affects this case more than the cumulus case.

The varying effects of the new entrainment-mixing parameterization are caused by variations in the dominant entrainment-mixing mechanism between different cloud types and stages. Compared to the cumulus case, the stratocumulus case has a much 477 smaller homogeneous mixing degree and a larger proportion of inhomogeneous mixing grid points, especially during the mature stage, which indicates that the inhomogeneous 478 479 mixing mechanism dominates in the stratocumulus case, while the homogeneous 480 mixing mechanism dominates in the cumulus case. As mentioned above, the changes 481 in physical properties of stratocumulus clouds in the dissipation stage are between those 482 in the mature stage and those of the cumulus case; this is because stratocumulus clouds 483 dissipate sharply to form small cumulus clouds, and the degree of homogeneous mixing during the dissipation stage is therefore between that which occurs during the mature 484 485 stage and the cumulus case.

Sensitivity studies show that turbulence dissipation rate and aerosol concentration 486 487 can have notable effects on the subgrid homogeneity of the mixing process. A larger 488 dissipation rate can accelerate the mixing process, which results in a larger transition 489 scale number and homogeneous mixing degree; and therefore, a mostly homogenous 490 mixing mechanism. This is why the cumulus case exhibit smaller changes than the 491 stratocumulus case after the new entrainment-mixing parameterization is implemented. 492 Larger aerosol number concentrations cause a smaller cloud droplet radius. Smaller 493 droplets evaporate more easily, which leads to a smaller transition scale number and a 494 smaller homogeneous mixing degree. Thus, the entrainment-mixing mechanism tends 495 to be inhomogeneous. Therefore, a larger aerosol number concentration increases the 496 influence of the new entrainment-mixing parameterization in both the cumulus and 497 stratocumulus cases.

| 498 | The influences of implementing the new entrainment-mixing parameterization |
|-----|--|
| 499 | with grid-mean relative humidity have been verified by simulations with entrained air |
| 500 | properties. The entrained air properties are obtained and calculated from simulations |
| 501 | with a finer resolution (10 m). Sensitivity tests show similar cloud microphysical and |
| 502 | optical properties in the two different methods, which suggests that the new |
| 503 | entrainment-mixing parameterization with grid-mean relative humidity is convincing. |
| 504 | Note that the new entrainment-mixing parameterization could be more important |
| 505 | in the models if the relative humidity near the cloud is more accurately simulated, |
| 506 | because numerical diffusion may spuriously humidify the entrained air (Hoffmann and |
| 507 | Feingold, 2019). The artificially increased relative humidity limits the influences of the |
| 508 | new entrainment-mixing parameterization, because homogeneous and inhomogeneous |
| 509 | entrainment-mixing processes are close to each other under conditions of high relative |
| 510 | humidity. |
| 511 | |

Author contributions. XX, CL and YL designed the experiments. XX carried out the
experiments and conducted the data analysis with contributions from all coauthors. XX,
CL, XZ, and SE developed the model code. XX prepared the paper with help from CL,
YL, YW, SL, and LZ.

Competing interests. The authors declare that they have no conflict of interest.

| 519 | Acknowledgements. This research is supported by the National Key Research and |
|-----|---|
| 520 | Development Program of China (2017YFA0604001), the National Natural Science |
| 521 | Foundation of China (41822504, 42175099, 42027804, 41975181, 42075073). Liu, |
| 522 | Zhou, and Endo are supported by the U.S. Department of Energy's Office of Energy |
| 523 | Efficiency and Renewable Energy (EERE) under Solar Energy Technologies Office |
| 524 | (SETO) Award Number 33504, and Office of Science Biological and Environmental |
| 525 | Research as part of the Atmospheric Systems Research (ASR) Program. Brookhaven |
| 526 | National Laboratory is operated by Battelle for the U.S. Department of Energy under |
| 527 | Contract DE-SC00112704. The large-scale forcing data used in this paper can be |
| 528 | downloaded from the U.S. Department of Energy's Atmospheric Radiation |
| 529 | Measurement Program with https://adc.arm.gov/discovery/#/results. The LASSO data |
| 530 | can be downloaded from https://archive.arm.gov/lassobrowser. The views expressed |
| 531 | herein do not necessarily represent the views of the U.S. Department of Energy or the |
| 532 | United States Government. |

534 **Reference**

Ackerman, A. S., Kirkpatrick, M. P., Stevens, D. E., and Toon, O. B.: The impact of
humidity above stratiform clouds on indirect aerosol climate forcing, Nature, 432,
1014-1017, 2004.

Andrejczuk, M., Grabowski, W. W., Malinowski, S. P., and Smolarkiewicz, P. K.:
Numerical simulation of cloud-clear air interfacial mixing: Effects on cloud
microphysics, J. Atmos. Sci., 63, 3204-3225, doi:10.1175/JAS3813.1, 2006.

541 Andrejczuk, M., Grabowski, W. W., Malinowski, S. P., and Smolarkiewicz, P. K.:

542 Numerical simulation of cloud-clear air interfacial mixing: Homogeneous versus

543 inhomogeneous mixing, J. Atmos. Sci., 66, 2493-2500, doi:10.1175/2009JAS2956.1,
544 2009.

- 545 Burnet, F. and Brenguier, J. L.: Observational study of the entrainment-mixing process
- in warm convective clouds, J. Atmos. Sci., 64, 1995-2011, doi:10.1175/JAS3928.1,
 2007.
- 548 Chosson, F., Brenguier, J.-L., and Schüller, L.: Entrainment-mixing and radiative
- transfer simulation in boundary layer clouds, J. Atmos. Sci., 64, 2670-2682,
 doi:10.1175/JAS3975.1, 2007.
- 551 Deardorff, J.: Stratocumulus-capped mixed layers derived from a three-dimensional 552 model, Boundary-Layer Meteorol, 18, 495-527, 10.1007/BF00119502, 1980.
- 553 Del Genio, A. D. and Wu, J.: The role of entrainment in the diurnal cycle of continental 554 convection, J. Climate, 23, 2722-2738, doi: 10.1175/2009JCLI3340.1, 2010.
- 555 Endo, S., Fridlind, A. M., Lin, W., Vogelmann, A. M., Toto, T., Ackerman, A. S.,
- 556 McFarquhar, G. M., Jackson, R. C., Jonsson, H. H., and Liu, Y.: RACORO continental
- boundary layer cloud investigations: 2. Large eddy simulations of cumulus clouds
 and evaluation with in situ and ground based observations, Journal of Geophysical
- 559 Research: Atmospheres, 120, 5993-6014, 2015.
- 560 Fan, J., Wang, Y., Rosenfeld, D., and Liu, X.: Review of Aerosol–Cloud Interactions:
- Mechanisms, Significance, and Challenges, Journal of the Atmospheric Sciences, 73,
 4221-4252, 10.1175/jas-d-16-0037.1, 2016.
- 502 4221-4252, 10.1175/jas-d-10-0057.1, 2010.
- Freud, E., Rosenfeld, D., and Kulkarni, J. R.: Resolving both entrainment-mixing and
 number of activated CCN in deep convective clouds, Atmos. Chem. Phys., 11, 1288712900, 2011.
- Freud, E., Rosenfeld, D., Andreae, M. O., Costa, A. A., and Artaxo, P.: Robust relations
 between CCN and the vertical evolution of cloud drop size distribution in deep
 convective clouds, Atmos. Chem. Phys., 8, 1661-1675, 2008.
- 569 Gao, S., Lu, C., Liu, Y., Mei, F., Wang, J., Zhu, L., and Yan, S.: Contrasting Scale
- 570 Dependence of Entrainment Mixing Mechanisms in Stratocumulus Clouds, 571 Geophysical Research Letters, 47, 10.1029/2020gl086970, 2020.
- 572 Gao, S., Lu, C., Liu, Y., Yum, S. S., Zhu, J., Zhu, L., Desai, N., Ma, Y., and Wu, S.:
- 573 Comprehensive quantification of height dependence of entrainment mixing between
- stratiform cloud top and environment, Atmospheric Chemistry and Physics, 21, 11225-11241, 2021.
- 576 Gao, Z., Liu, Y., Li, X., and Lu, C.: Investigation of Turbulent Entrainment-Mixing
- 577 Processes with a New Particle-Resolved Direct Numerical Simulation Model, J.
- 578 Geophys. Res., 123, 2194-2214, 2018.
- 579 Gerber, H. E., Frick, G. M., Jensen, J. B., and Hudson, J. G.: Entrainment, mixing, and 580 microphysics in trade-wind cumulus, J. Meteorol. Soc. Japan, 86A, 87-106, 2008.
- 581 Grabowski, W. W.: Indirect impact of atmospheric aerosols in idealized simulations of
- 582 convective-radiative quasi equilibrium, J. Climate, 19, 4664-4682,
- 583 doi:10.1175/JCLI3857.1, 2006.
- 584 Grabowski, W. W.: Representation of turbulent mixing and buoyancy reversal in bulk
- cloud models, Journal of the atmospheric sciences, 64, 3666-3680, 2007.
- 586 Grabowski, W. W. and Morrison, H.: Indirect Impact of Atmospheric Aerosols in

- 587 Idealized Simulations of Convective-Radiative Quasi Equilibrium. Part II: Double-
- 588 Moment Microphysics, Journal of Climate, 24, 1897-1912, 10.1175/2010jcli3647.1, 589 2011.
- 590 Gustafson, W. I., Vogelmann, A. M., Li, Z., Cheng, X., Dumas, K. K., Endo, S., Johnson,
- 591 K. L., Krishna, B., Fairless, T., and Xiao, H.: The Large-Eddy Simulation (LES)
- 592 Atmospheric Radiation Measurement (ARM) Symbiotic Simulation and Observation
- 593 (LASSO) Activity for Continental Shallow Convection, Bulletin of the American
- 594 Meteorological Society, 101, E462-E479, 10.1175/bams-d-19-0065.1, 2020.
- 595 Hacker, J. P., Jimenez, P. A., Dudhia, J., Haupt, S. E., Ruiz-Arias, J. A., Gueymard, C.
- 596 A., Thompson, G., Eidhammer, T., and Deng, A.: WRF-Solar: Description and Clear-
- 597 Sky Assessment of an Augmented NWP Model for Solar Power Prediction, Bulletin of
- 598 the American Meteorological Society, 97, 1249-1264, 10.1175/bams-d-14-00279.1,
- 599 2016.
- 600 Haman, K. E., Malinowski, S. P., Kurowski, M. J., Gerber, H., and Brenguier, J.-L.:
- Small scale mixing processes at the top of a marine stratocumulus a case study, Q. J.
 Roy. Meteor. Soc., 133, 213-226, doi:10.1002/qj.5, 2007.
- $(02 \quad \text{Holy, Metcol, 500, 155, 215, 220, doi:10.1002/<math>(1.5, 200)$
- Haupt, S. E., Kosovic, B., Jensen, T., Lee, J., Jimenez, P., Lazo, J., Cowie, J.,
- 604 McCandless, T., Pearson, J., and Weiner, G.: The SunCast solar-power forecasting
- system: the results of the public-private-academic partnership to advance solar powerforecasting, National Center for Atmospheric Research (NCAR), Boulder (CO):
- Research Applications Laboratory, Weather Systems and Assessment Program (US),2016.
- Hill, A. A., Feingold, G., and Jiang, H.: The influence of entrainment and mixing
 assumption on aerosol-cloud interactions in marine stratocumulus, J. Atmos. Sci., 66,
 1450-1464, 2009.
- 612 Hoffmann, F. and Feingold, G.: Entrainment and mixing in stratocumulus: Effects of a
- 613 new explicit subgrid-scale scheme for large-eddy simulations with particle-based 614 microphysics, J. Atmos. SCi., 76, 1955-1973, 10.1175/jas-d-18-0318.1, 2019.
- 615 Hoffmann, F., Yamaguchi, T., and Feingold, G.: Inhomogeneous mixing in Lagrangian
- 616 cloud models: Effects on the production of precipitation embryos, Journal of the617 Atmospheric Sciences, 76, 113-133, 2019.
- Huang, J., Lee, X., and Patton, E. G.: A modelling study of flux imbalance and the
- 619 influence of entrainment in the convective boundary layer, Boundary-layer meteorology,
- 620 127, 273**-**292, 2008.
- 621 Jarecka, D., Grabowski, W. W., and Pawlowska, H.: Modeling of Subgrid-Scale Mixing
- 622 in Large-Eddy Simulation of Shallow Convection, Journal of the Atmospheric Sciences,
- 623 66, 2125-2133, 10.1175/2009jas2929.1, 2009.
- 624 Jarecka, D., Grabowski, W. W., Morrison, H., and Pawlowska, H.: Homogeneity of the
- 625 subgrid-scale turbulent mixing in large-eddy simulation of shallow convection, J.
- 626 Atmos. Sci., 70, 2751-2767, 2013.
- 627 Jensen, J. B., Austin, P. H., Baker, M. B., and Blyth, A. M.: Turbulent mixing, spectral
- evolution and dynamics in a warm cumulus cloud, J. Atmos. Sci., 42, 173-192,

- 629 doi:10.1175/1520-0469(1985)042<0173:TMSEAD>2.0.CO;2, 1985.
- 630 Kim, B.-G., Miller, M. A., Schwartz, S. E., Liu, Y., and Min, Q.: The role of adiabaticity
- 631 in the aerosol first indirect effect, J. Geophys. Res., 113, D05210, doi:
 632 10.1029/2007jd008961, 2008.
- Kumar, B., Schumacher, J., and Shaw, R.: Cloud microphysical effects of turbulent
 mixing and entrainment, Theor. Comp. Fluid Dyn., 27, 361-376, 2013.
- 635 Lasher-Trapp, S. G., Cooper, W. A., and Blyth, A. M.: Broadening of droplet size
- distributions from entrainment and mixing in a cumulus cloud, Q. J. Roy. Meteor. Soc.,
- 637 131, 195-220, doi:10.1256/qj.03.199, 2005.
- 638 Lehmann, K., Siebert, H., and Shaw, R. A.: Homogeneous and inhomogeneous mixing
- 639 in cumulus clouds: dependence on local turbulence structure, J. Atmos. Sci., 66, 3641640 3659, doi:10.1175/2009JAS3012.1, 2009.
- 641 Li, Z., Li, C., Chen, H., Tsay, S. C., Holben, B., Huang, J., Li, B., Maring, H., Qian, Y.,
- 642 and Shi, G.: East Asian studies of tropospheric aerosols and their impact on regional
- 643 climate (EAST AIRC): An overview, Journal of Geophysical Research: Atmospheres,644 116, 2011.
- Lu, C., Liu, Y., and Niu, S.: Examination of turbulent entrainment-mixing mechanisms
 using a combined approach, J. Geophys. Res., 116, D20207,
 doi:10.1029/2011JD015944, 2011.
- Lu, C., Liu, Y., Niu, S., and Endo, S.: Scale dependence of entrainment mixing
 mechanisms in cumulus clouds, Journal of Geophysical Research: Atmospheres, 119,
 13,877-813,890, 2014.
- Lu, C., Liu, Y., Niu, S., Krueger, S., and Wagner, T.: Exploring parameterization for
 turbulent entrainment-mixing processes in clouds, Journal of Geophysical Research:
 Atmospheres, 118, 185-194, 10.1029/2012jd018464, 2013.
- Lu, C., Liu, Y., Zhang, G. J., Wu, X., Endo, S., Cao, L., Li, Y., and Guo, X.: Improving
- parameterization of entrainment rate for shallow convection with aircraft measurements
 and large eddy simulation, J. Atmos. Sci., 73, 761-773, 10.1175/JAS-D-15-0050.1,
 2016.
- 658 Luo, S., Lu, C., Liu, Y., Bian, J., Gao, W., Li, J., Xu, X., Gao, S., Yang, S., and Guo, X.:
- 659 Parameterizations of Entrainment Mixing Mechanisms and Their Effects on Cloud
- 660 Droplet Spectral Width Based on Numerical Simulations, Journal of Geophysical
- 661 Research: Atmospheres, 125, e2020JD032972, 2020.
- Morrison, H. and Grabowski, W. W.: Modeling supersaturation and subgrid-scale
 mixing with two-moment bulk warm microphysics, J. Atmos. Sci., 65, 792-812,
 doi:10.1175/2007JAS2374.1, 2008.
- 665 Paluch, I. R. and Baumgardner, D. G.: Entrainment and fine-scale mixing in a
- 666 continental convective cloud, J. Atmos. Sci., 46, 261-278, doi:10.1175/1520-667 0469(1989)046<0261:EAFSMI>2.0.CO;2, 1989.
- 668 Pawlowska, H., Brenguier, J. L., and Burnet, F.: Microphysical properties of
- 669 stratocumulus clouds, Atmos. Res., 55, 15-33, 2000.
- 670 Peng, Y., Lohmann, U., Leaitch, R., Banic, C., and Couture, M.: The cloud albedo-cloud

- 671 droplet effective radius relationship for clean and polluted clouds from RACE and
- 672 FIRE.ACE, J. Geophys. Res., 107, AAC 1-1-AAC 1-6, 10.1029/2000JD000281, 2002.
- 673 Slawinska, J., Grabowski, W. W., Pawlowska, H., and Morrison, H.: Droplet activation
- and mixing in large-eddy simulation of a shallow cumulus field, J. Atmos. Sci., 69, 444-462, 2012.
- 402, 2012.
- 676 Slawinska, J., Grabowski, W. W., Pawlowska, H., and Wyszogrodzki, A. A.: Optical
- 677 properties of shallow convective clouds diagnosed from a bulk-microphysics large-
- 678 eddy simulation, J. Climate, 21, 1639-1647, 2008.
- Small, J. D., Chuang, P., and Jonsson, H.: Microphysical imprint of entrainment inwarm cumulus, Tellus B, 65, 6647-6662, 2013.
- Thompson, G. and Eidhammer, T.: A study of aerosol impacts on clouds and
 precipitation development in a large winter cyclone, Journal of the atmospheric
 sciences, 71, 3636-3658, 2014.
- Wang, H. and Feingold, G.: Modeling mesoscale cellular structures and drizzle in
 marine stratocumulus. Part I: Impact of drizzle on the formation and evolution of open
 cells, Journal of the Atmospheric Sciences, 66, 3237-3256, 2009.
- 687 Wang, M., Ghan, S., Ovchinnikov, M., Liu, X., Easter, R., Kassianov, E., Qian, Y., and
- 688 Morrison, H.: Aerosol indirect effects in a multi-scale aerosol-climate model PNNL-
- 689 MMF, Atmospheric Chemistry and Physics, 11, 5431-5455, 2011.
- 690 Wang, Y., Zhao, C., McFarquhar, G. M., Wu, W., Reeves, M., and Li, J.: Dispersion of
- 691 Droplet Size Distributions in Supercooled Non precipitating Stratocumulus from
- 692 Aircraft Observations Obtained during the Southern Ocean Cloud Radiation Aerosol
- Transport Experimental Study, Journal of Geophysical Research: Atmospheres, 126,
 e2020JD033720, 2021.
- 695 Wang, Y., Niu, S., Lv, J., Lu, C., Xu, X., Wang, Y., Ding, J., Zhang, H., Wang, T., and
- Kang, B.: A new method for distinguishing unactivated particles in cloud condensationnuclei measurements: Implications for aerosol indirect effect evaluation, Geophysical
- 698 Research Letters, 46, 14185-14194, 2019.
- Wood, R.: Review: Stratocumulus Clouds, Monthly Weather Review, 140, 2373-2423,2012.
- Xu, K.-M. and Randall, D. A.: A semiempirical cloudiness parameterization for use in
 climate models, Journal of the atmospheric sciences, 53, 3084-3102, 1996.
- Xu, X., Sun, C., Lu, C., Liu, Y., Zhang, G. J., and Chen, Q.: Factors affecting
 entrainment rate in deep convective clouds and parameterizations, Journal of
 Geophysical Research: Atmospheres, 126, e2021JD034881, 2021.
- 706 Xu, X., Lu, C., Liu, Y., Gao, W., Wang, Y., Cheng, Y., Luo, S., and Van Weverberg, K.:
- 707 Effects of cloud liquid phase microphysical processes in mixed phase cumuli over
- the Tibetan Plateau, Journal of Geophysical Research: Atmospheres, 125,e2020JD033371, 2020.
- 710 Yang, B., Wang, M., Zhang, G. J., Guo, Z., Huang, A., Zhang, Y., and Qian, Y.: Linking
- 711 Deep and Shallow Convective Mass Fluxes via an Assumed Entrainment Distribution
- 712 in CAM5 CLUBB: Parameterization and Simulated Precipitation Variability, Journal

- of Advances in Modeling Earth Systems, 13, e2020MS002357, 2021.
- 714 Yang, F., Shaw, R., and Xue, H.: Conditions for super-adiabatic droplet growth after
- 715 entrainment mixing, Atmos. Chem. Phys., 16, 9421-9433, 10.5194/acp-2016-94, 2016.
- 716 Yum, S.: Cloud droplet spectral broadening in warm clouds: An observational and
- 717 model study, Dissertation for the Doctoral Degree, University of Nevada, Reno, Nevada,
- 718 USA, 191 pp., 1998.
- 719 Zhang, M. H., Lin, J. L., Cederwall, R. T., Yio, J. J., and Xie, S. C.: Objective analysis
- of ARM IOP data: Method and sensitivity, Mon. Weather Rev., 129, 295-311,
 10.1175/1520-0493(2001)129<0295:OAOAID>2.0.CO;2, 2001.
- 722 Zheng, Y. and Rosenfeld, D.: Linear relation between convective cloud base height and
- updrafts and application to satellite retrievals, Geophysical Research Letters, 42, 64856491, 10.1002/2015gl064809, 2015.
- 725 Zheng, Y., Rosenfeld, D., and Li, Z.: Quantifying cloud base updraft speeds of marine
- stratocumulus from cloud top radiative cooling, Geophysical Research Letters, 43,
 11,407-411,413, 2016.
- 728 Zhu, L., Lu, C., Yan, S., Liu, Y., Zhang, G. J., Mei, F., Zhu, B., Fast, J. D., Matthews,
- A., and Pekour, M. S.: A New Approach for Simultaneous Estimation of Entrainment
- and Detrainment Rates in Non Precipitating Shallow Cumulus, Geophysical Research
- 731 Letters, 48, 10.1029/2021gl093817, 2021.
- 732

Table 1. Summary of names and corresponding descriptions of the four experiments for

735 each case of cumulus and stratocumulus. The meaning of each symbol for each

| 700 | • | 1 | C 1 | • | .1 | |
|-----|---------------|--------|-------|-----|-----|-------|
| 736 | evneriment (| can he | tound | 1m | the | tovt |
| 150 | experiment of | | Iounu | 111 | unc | IUAL. |
| | 1 | | | | | |

| | Entrainment-mixing | Dissinction rate | Aerosol number |
|------------|--|-------------------------------|----------------|
| | parameterization | Dissipation rate | concentration |
| default | $\alpha = 0$ | - | default |
| new | $\alpha = 1 - \psi,$ $\psi = 107.19 \exp(-1.99 N_{\rm L}^{-0.29}).$ | $\varepsilon = CE^{3/2} / L.$ | default |
| default_10 | $\alpha = 0$ | - | default×10 |
| new_10 | $\alpha = 1 - \psi,$ $\psi = 107.19 \exp(-1.99 N_{\rm L}^{-0.29}).$ | $\varepsilon = CE^{3/2} / L.$ | default×10 |

| he case mean values of the key quantities in all the simulations |
|---|
| ontaining cloud water mixing ratio (q_c) , cloud droplet number |
| ud droplet volume-mean radius (r_v), cloud water path (CWP), |
| |

and cloud optical depth (τ). The experiments are detailed in Table 1.

| | default | new | default_10 | new_10 |
|----------------------------|---------|--------|------------|--------|
| $q_{\rm c}({ m g/kg})$ | 0.44 | 0.44 | 0.56 | 0.57 |
| $N_{\rm c}({\rm cm}^{-3})$ | 35.78 | 35.53 | 278.80 | 271.16 |
| $r_{\rm v}(\mu{ m m})$ | 13.27 | 13.29 | 7.05 | 7.09 |
| CWP(g/m ²) | 142.30 | 144.25 | 186.52 | 187.13 |
| τ | 13.07 | 13.02 | 31.29 | 31.11 |
| | | | | |

| 744 | Table 3. Summary of the case mean values of the key quantities in all the simulations |
|-----|--|
| 745 | of the stratocumulus case, including cloud water mixing ratio (q_c) , cloud droplet number |
| 746 | concentration (N_c), cloud droplet volume-mean radius (r_v), cloud water path (CWP), |
| 747 | and cloud optical depth (τ). The numbers in and out of the parentheses are the results at |
| 748 | the mature and dissipation stages, respectively. The experiments are detailed in Table 1. |

| default | new | default_10 | new_10 |
|---------|---|---|---|
| 0.13 | 0.13 | 0.16 | 0.16 |
| (0.039) | (0.039) | (0.041) | (0.041) |
| 35.74 | 33.11 | 256.82 | 231.93 |
| (19.76) | (18.82) | (138.74) | (126.90) |
| 10.32 | 10.65 | 5.15 | 5.35 |
| (7.53) | (7.69) | (4.02) | (4.14) |
| 41.39 | 41.78 | 56.21 | 57.03 |
| (2.57) | (2.43) | (2.71) | (2.77) |
| 4.68 | 4.40 | 13.17 | 12.40 |
| (0.39) | (0.38) | (0.78) | (0.78) |
| | 0.13 (0.039) 35.74 (19.76) 10.32 (7.53) 41.39 (2.57) 4.68 | $\begin{array}{c cccc} 0.13 & 0.13 \\ \hline 0.039 & (0.039) \\ \hline 35.74 & 33.11 \\ \hline (19.76) & (18.82) \\ \hline 10.32 & 10.65 \\ \hline (7.53) & (7.69) \\ \hline 41.39 & 41.78 \\ \hline (2.57) & (2.43) \\ \hline 4.68 & 4.40 \\ \hline \end{array}$ | 0.13 0.13 0.16 (0.039) (0.039) (0.041) 35.74 33.11 256.82 (19.76) (18.82) (138.74) 10.32 10.65 5.15 (7.53) (7.69) (4.02) 41.39 41.78 56.21 (2.57) (2.43) (2.71) 4.68 4.40 13.17 |

| 750 | Table 4. Cloud water mixing ratio (q_c) , cloud droplet number concentration (N_c) , cloud |
|-----|---|
| 751 | droplet volume-mean radius (r_v), cloud water path (CWP), cloud optical depth (τ) in all |
| 752 | simulations for the entire lifetime of the stratocumulus case. The experiments are |
| 753 | detailed in Table 1. |

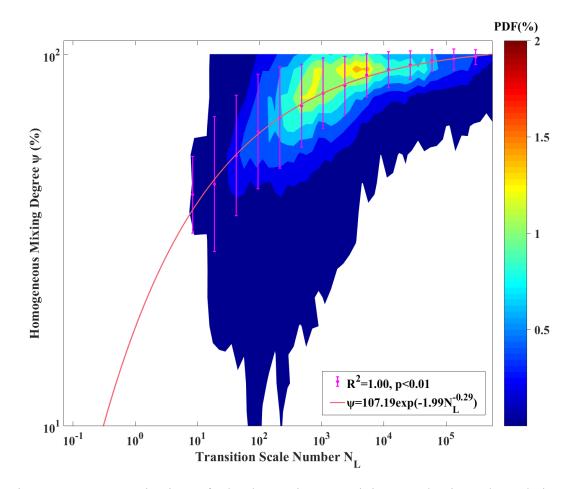
| default | new | default_10 | new_10 |
|---------|--------------------------------|---|--|
| 0.11 | 0.11 | 0.13 | 0.13 |
| 29.98 | 28.12 | 223.65 | 203.50 |
| 9.38 | 9.57 | 5.06 | 5.22 |
| 30.78 | 29.92 | 42.22 | 43.13 |
| 4.02 | 3.89 | 10.39 | 9.96 |
| | 0.11 29.98 9.38 30.78 | 0.11 0.11 29.98 28.12 9.38 9.57 30.78 29.92 | 0.11 0.11 0.13 29.98 28.12 223.65 9.38 9.57 5.06 30.78 29.92 42.22 |

| 756 | Table 5. Homogeneous mixing degree (ψ) at all grid points experiencing evaporation, |
|-----|---|
| 757 | the proportion of inhomogeneous mixing grid points to all grid points experiencing |
| 758 | evaporation, and ψ at the inhomogeneous mixing grid points in the experiments <i>new</i> |
| 759 | and new_10 (Table 1) for the cumulus (Cu) and stratocumulus (St) cases. The numbers |
| 760 | in and out of the parentheses are the results at the mature and dissipation stages in the |
| 761 | stratocumulus (St) case, respectively. The experiments are detailed in Table 1. |

| | | Proportion of | ψ at the |
|--------------------|-------------------------|------------------|------------------|
| | ψ at all grids (%) | inhomogeneous | inhomogeneous |
| | | mixing grids (%) | mixing grids (%) |
| new (Cu) | 99.93 | 4.52 | 98.62 |
| <i>new_10</i> (Cu) | 95.33 | 25.10 | 92.96 |
| new (St) | 78.56 | 63.07 | 71.56 |
| | (94.68) | (40.61) | (89.33) |
| <i>new_10</i> (St) | 68.20 | 97.31 | 65.01 |
| | (88.11) | (73.54) | (84.99) |

| 764 | Table 6. Cloud water mixing ratio (q_c), cloud droplet number concentration (N_c), cloud |
|-----|--|
| 765 | droplet volume-mean radius (r_v), cloud water path (CWP), cloud optical depth (τ) in |
| 766 | <i>new_f</i> and <i>new_f_10</i> for the cumulus (Cu) and stratocumulus (Sc) cases. The results of |
| 767 | new and new_10 in Tables 2 and 4 are shown in the parentheses. |

| | Cu | | Sc | |
|----------------------------|----------|----------|---------|----------|
| | new_f | new_f_10 | new_f | new_f_10 |
| | (new) | (new_10) | (new) | (new_10) |
| q _c (g/kg) | 0.44 | 0.57 | 0.11 | 0.13 |
| | (0.44) | (0.57) | (0.11) | (0.13) |
| $N_{\rm c}({\rm cm}^{-3})$ | 35.52 | 270.56 | 28.08 | 202.99 |
| | (35.53) | (271.16) | (28.12) | (203.50) |
| r _v (μm) | 13.30 | 7.10 | 9.60 | 5.21 |
| | (13.29) | (7.09) | (9.57) | (5.22) |
| CWP(g/m ²) | 143.15 | 185.95 | 30.16 | 43.32 |
| | (144.25) | (187.13) | (29.92) | (43.13) |
| | 13.00 | 31.08 | 3.89 | 9.93 |
| τ | (13.02) | (31.11) | (3.89) | (9.96) |



771 Figure 1. Parameterization of cloud entrainment-mixing mechanisms by relating homogeneous mixing degree (ψ) to transition scale number (N_L) from EMPM. The 772 773 contours represent the joint probability distribution function (PDF) of ψ vs N_L. The magenta dots and error bars are mean values and standard deviations of ψ in each N_L 774 775 bin, respectively. The mean values are fitted using a weighted least squares method with 776 the number of data points in each $N_{\rm L}$ bin as the weight. The fitting equation, coefficient of determination (R^2) , and p-value are also given. N_L is calculated by with the domain-777 778 averaged relative humidity after entrainment but before evaporation in the EMPM.

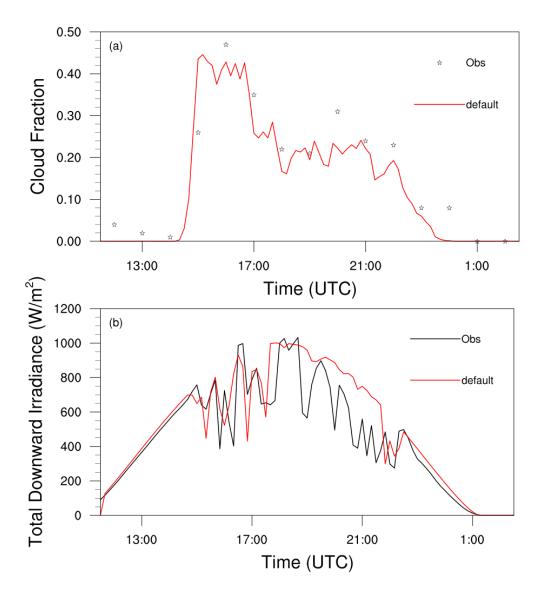
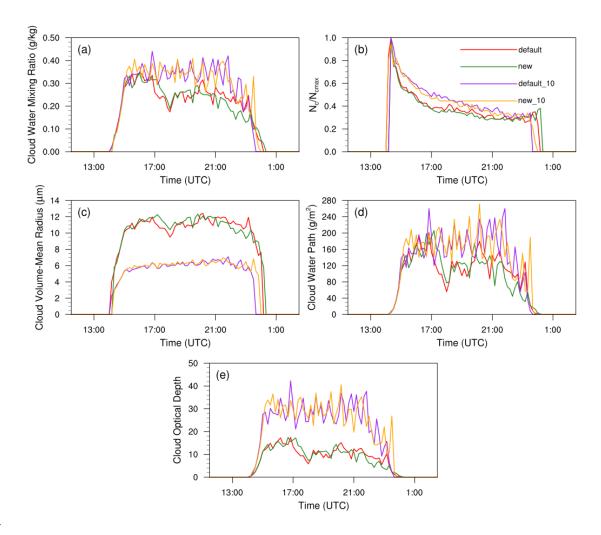


Figure 2. Time series of (a) domain-averaged cloud fraction and (b) total downward
irradiance at the central point from the observation and the *default* experiment in the
cumulus case.



784

785 Figure 3. The temporal evolutions of main cloud microphysical and optical properties in all simulation experiments for the cumulus case, including (a) cloud water mixing 786 ratio (q_c) (g/kg), (b) cloud droplet number concentration (N_c) (/cm³), (c) cloud droplet 787 volume-mean radius (r_v) (µm), (d) cloud water path (CWP) (g/m²), and (e) cloud optical 788 789 depth (τ). In (b), N_c in the experiments *default* and *new* are normalized by the maximum 790 cloud droplet concentration (N_{cmax}) from *default*, respectively; N_c in the experiments 791 default 10 and new 10 are normalized by N_{cmax} from default 10, respectively. The four 792 experiments are detailed in Table 1.

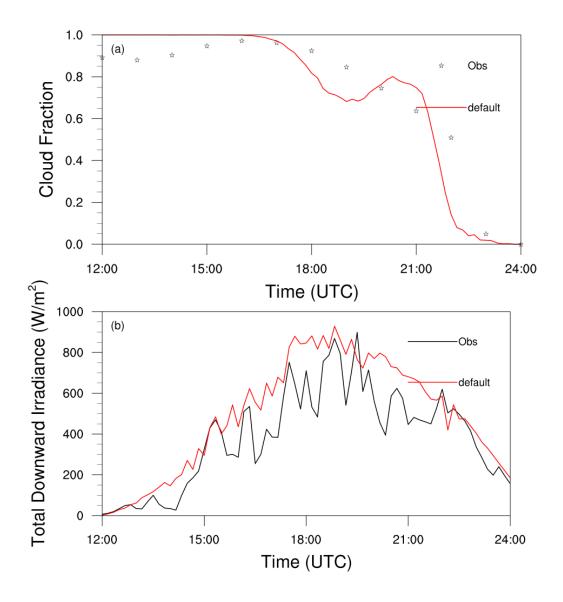


Figure 4. Time series of (a) domain-averaged cloud fraction and (b) total downward
irradiance at the central point from the observation and the *default* experiment in the
stratocumulus case.

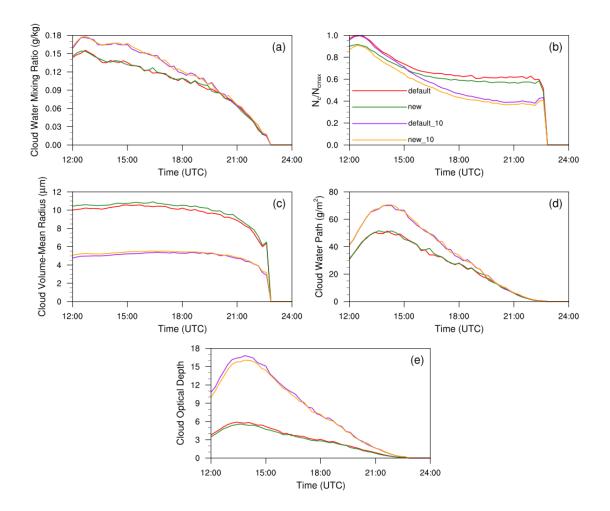


Figure 5. The temporal evolutions of main cloud microphysical and optical properties 798 799 in all simulation experiments for the stratocumulus case, including (a) cloud water 800 mixing ratio (q_c) (g/kg), (b) cloud droplet number concentration (N_c) (/cm³), (c) cloud droplet volume-mean radius (r_v) (µm), (d) cloud water path (CWP) (g/m²), and (e) cloud 801 802 optical depth (τ). In (b), N_c in the experiments *default* and *new* are normalized by the 803 maximum cloud droplet number concentration (N_{cmax}) from *default*, respectively; N_c in the experiments default 10 and new 10 are normalized by N_{cmax} from default 10, 804 respectively. The four experiments are detailed in Table 1. 805

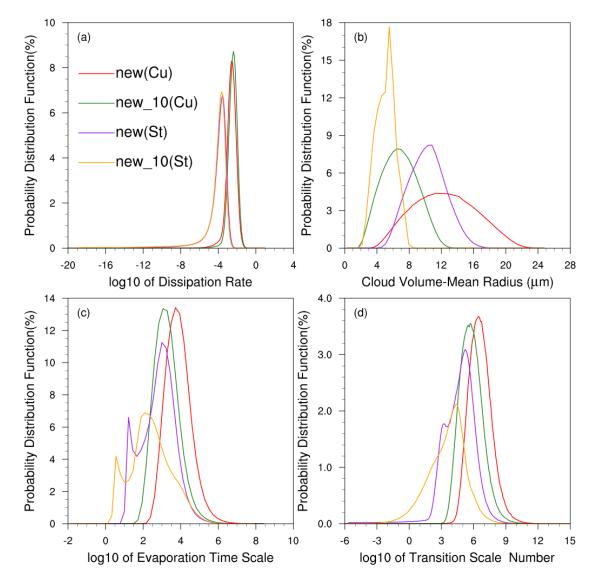


Figure 6. Probability distribution functions (PDFs) of (a) turbulence dissipation rate (ε), (b) cloud droplet volume-mean radius (r_v), (c) evaporation time scale (τ_{evap}), and (d) transition scale number (N_L) of cloud grids experiencing the entrainment-mixing process in the simulations with the new entrainment-mixing parameterization for the cumulus case (Cu, the solid lines) and the stratocumulus case (St, the dash lines), respectively. The experiments are detailed in Table 1.

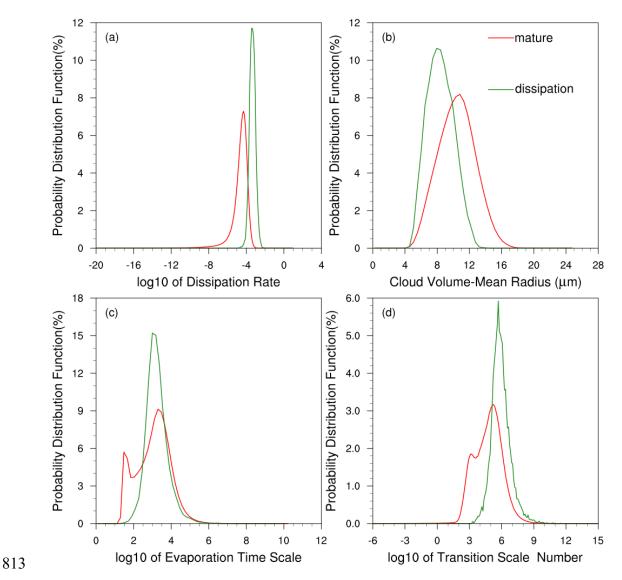
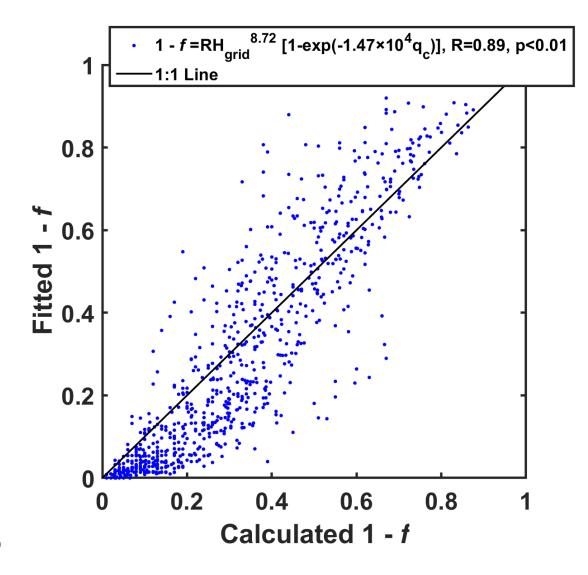


Figure 7. Probability distribution functions (PDFs) of (a) turbulence dissipation rate (ε), (b) cloud droplet volume-mean radius (r_v), (c) evaporation time scale (τ_{evap}), and (d) transition scale number (N_L) of cloud grids experiencing the entrainment-mixing process at the mature stage from 12:00 UTC to 16:00 UTC (the red lines) and the dissipation stage from 21:00 UTC to 24:00 UTC (the green lines) in *new* for the stratocumulus case. The experiment is detailed in Table 1.



820

Figure 8. The fitted 1 - f as a function of the calculated 1 - f. The fitted 1 - f is obtained by the fitting functions with grid-mean relative humidity (RH_{grid}) and cloud water mixing ratio (q_c). The black line denotes the 1:1 line.

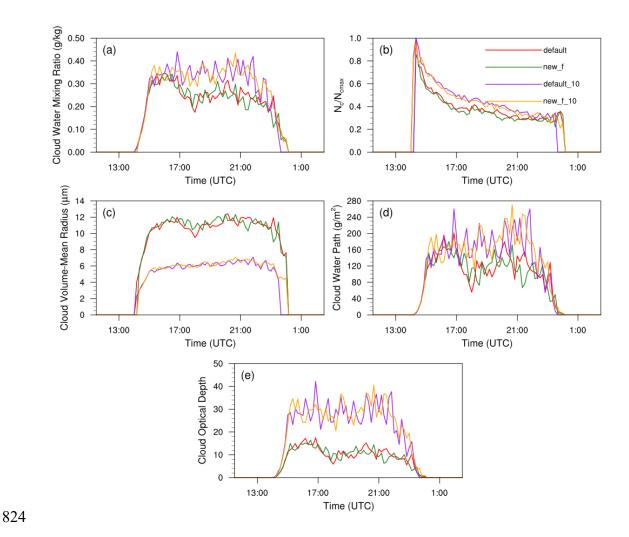


Figure 9. The temporal evolutions of main cloud microphysical and optical properties 825 826 in all simulation experiments for the cumulus case, including (a) cloud water mixing 827 ratio (q_c) (g/kg), (b) cloud droplet number concentration (N_c) (/cm³), (c) cloud droplet volume-mean radius (r_v) (µm), (d) cloud water path (CWP) (g/m²), and (e) cloud optical 828 829 depth (τ). In (b), N_c in the experiments *default* and *new f* are normalized by the 830 maximum cloud droplet concentration (N_{cmax}) from *default*, respectively; N_c in the experiments default 10 and new f 10 are normalized by N_{cmax} from default 10, 831 respectively. *new* f and *new* f 10 are the experiments using entrained air relative 832 833 humidity.

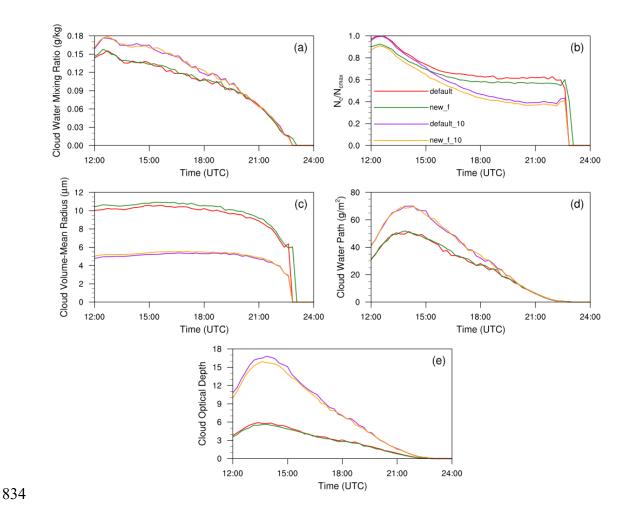


Figure 10. The temporal evolutions of main cloud microphysical and optical properties 835 in all simulation experiments for the stratocumulus case, including (a) cloud water 836 mixing ratio (q_c) (g/kg), (b) cloud droplet number concentration (N_c) (/cm³), (c) cloud 837 droplet volume-mean radius (r_v) (µm), (d) cloud water path (CWP) (g/m²), and (e) cloud 838 839 optical depth (τ). In (b), N_c in the experiments *default* and *new* are normalized by the 840 maximum cloud droplet number concentration (N_{cmax}) from *default*, respectively; N_c in the experiments default 10 and new 10 are normalized by N_{cmax} from default 10, 841 842 respectively. new f and new f 10 are the experiments using entrained air relative 843 humidity.