

Towards reconstructing the Arctic atmospheric methane history over the 20th century: measurement and modeling results for the NGRIP firn

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Abstract. Systematic measurements of atmospheric methane (CH₄) mole fractions at the northern high latitudes only began in the early 1980s, and whilst CH₄ measurements from Greenland ice cores covered the period before ~1900, no reliable observational record is available for the intermediate period. In this study, we reconstruct the atmospheric CH₄ for that period, when the mole fraction started to increase rapidly. We use a data set of trace gases, measured from the air trapped in firn (an intermediate stage between snow and glacial ice formation) collected at the NGRIP (North Greenland Ice Core Project) site in 2001, in combination with a firn-air transport model whose performance is validated by using a set of published firn-air data at the NEEM (North Greenland Eemian ice Drilling) site. We examine a variety of possible firn diffusivity profiles using a suite of measured trace gases, and reconstruct the CH₄ mole fraction by an iterative dating method, based on the two Arctic firn data sets in the same manner. We find that, given the currently available firn air data sets from Greenland, reconstruction of the Arctic CH₄ mole fraction before the mid 1970s is highly uncertain. Although it is difficult to accurately identify the atmospheric CH₄ history that consistently reproduce the depth profiles of CH₄ in firn at both NGRIP and NEEM sites, both firn data sets are more consistent with the atmospheric CH₄ scenario prepared for the NEEM firn modeling than that for the CMIP6 (Climate Model Intercomparison Project Phase 6) experiments. It is considered that the former is the current best choice for the available synthetic Arctic CH₄ history, but should not be treated as the known history for constraining firn-air transport models until supported by further data from sources such as Arctic ice cores. Given the current difficulty in reconstructing the CH₄ history from the firn-air data sets from Greenland, future sampling and measurements of ice cores at a high-accumulation site may be the only way to accurately reconstruct the atmospheric CH₄ trend over the 20th century.

1 Introduction

Methane (CH₄) is an important atmospheric greenhouse gas emitted from both natural and anthropogenic sources. Despite great efforts for understanding its global budget, emission estimates of individual sources still have large quantitative uncertainties (e.g. Saunois et al., 2020; Chandra et al., 2021). Anthropogenic activities have enhanced CH₄ emissions globally and more than doubled the abundance of atmospheric CH₄ over the industrial era (e.g. Etheridge et al., 1998). The CH₄ emission histories have been estimated based on human activity statistics combined with emission factors (Stern and Kaufmann 1996; van Aardenne et al., 2001). Such historical emission inventories have been examined by atmospheric chemistry transport modeling (Houweling et al., 2000; Monteil et al., 2011; Ghosh et al., 2015), in combination with the records of atmospheric CH₄ mole fraction reconstructed from polar ice cores (Blunier et al., 1993; Nakazawa et al., 1993; Etheridge et al., 1998; MacFarling Meure et al., 2006; Sapart et al., 2012) and air extracted from porous snow layers at the top of ice sheets (firn) (Francey et al., 1999; Buizert et al., 2012; Sapart et al., 2013).

A large fraction of natural and anthropogenic CH₄ sources resides in the northern hemisphere, and thus the atmospheric CH₄ trend of the northern hemisphere can provide important information on the evolution of anthropogenic CH₄ emissions as well as the variations of natural CH₄ emission in response to climatic variability. The interhemispheric gradient of CH₄ mole fraction is also key to the allocation of CH₄ emissions between both hemispheres (e.g. Dlugokencky et al., 2003; Ghosh et al., 2015; Chandra et al., 2021).

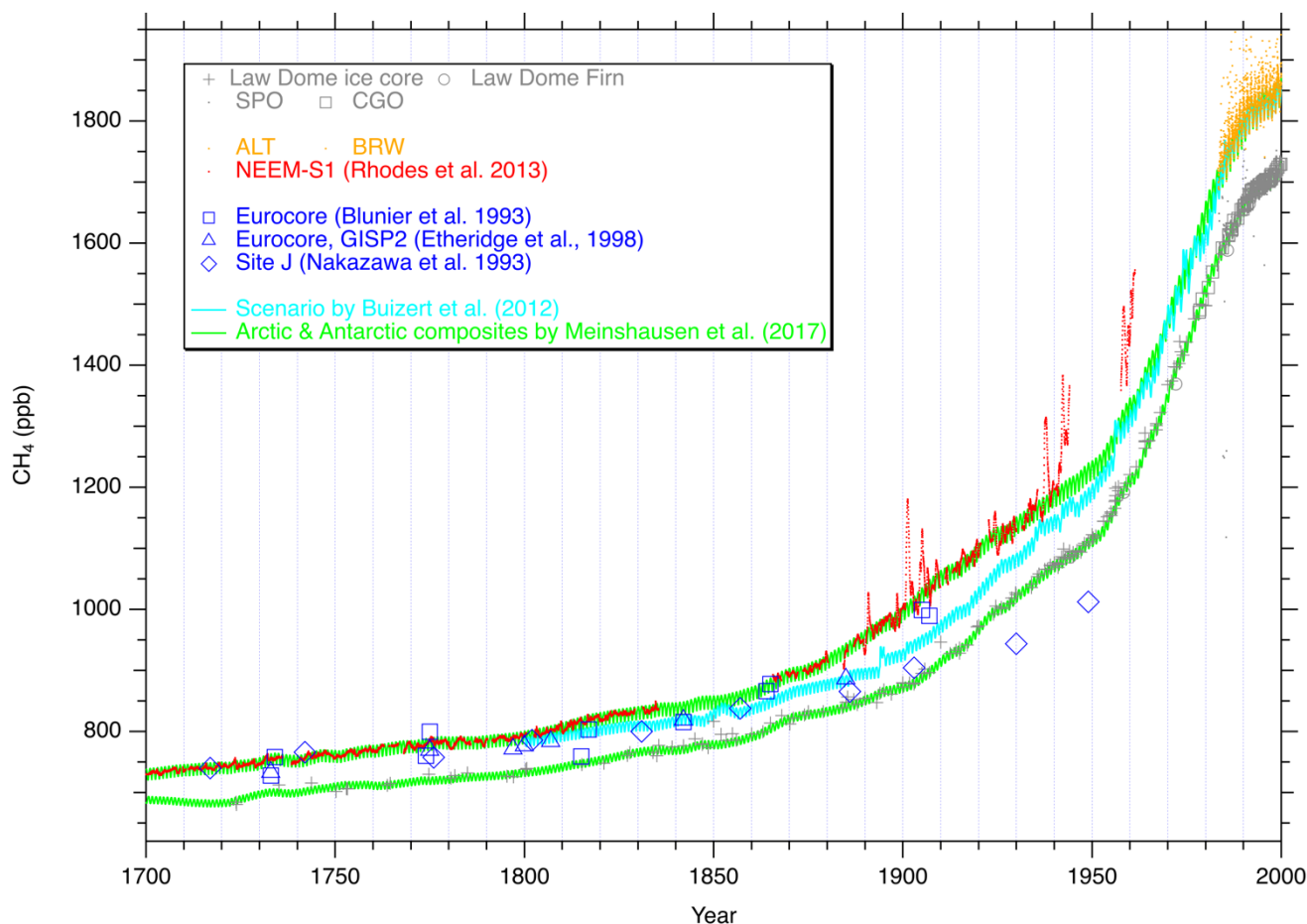


Figure 1: Atmospheric CH₄ mole fraction data covering the last 200 years. Symbols in grey are from the southern hemisphere; crosses and open circles are from the Law Dome ice core and firn, respectively (Etheridge et al., 1998; MacFarling Meure et al., 2006); open squares are from Cape Grim (CGO) (MacFarling Meure et al., 2006); dots are from South Pole (SPO) (<ftp://aftp.cmdl.noaa.gov/>). Colored data (except light green) from the northern hemisphere; open squares, triangles and diamonds are from the Eurocore (Blunier et al., 1993), Eurocore and GISP2 (Etheridge et al., 1998) and Site J (Nakazawa et al., 1993) ice cores; red dots are the NEEM-S1 ice core (Rhodes et al., 2013); orange dots are from Alert, Canada (ALT) and Barrow, Alaska (BRW) (<ftp://aftp.cmdl.noaa.gov/>); light blue and light green lines are the atmospheric scenarios prepared for the NEEM firn modeling (Buizert et al., 2012) and the CMIP6 experiments (Meinshausen et al. 2017), respectively.

Systematic measurements of atmospheric CH₄ mole fraction began in the 1980s. In Figure 1, CH₄ measurements at two Arctic sites: Barrow, Alaska (BRW) and Alert, Canada (ALT) are shown (orange dots), whose records start in 1983 and 1985, respectively (data provided by National Oceanic and Atmospheric Administration/Earth System Research Laboratory/Global Monitoring Laboratory, NOAA/ESRL/GML). Although some sparse data from the 1970s are available (e.g. Rice et al., 2016), such “direct” measurements provide CH₄ data only since around 1980, which means that some reconstruction methodology is required to infer atmospheric CH₄ mole fraction variations before that time. For this purpose, air extracted from ice cores and firn layers have been measured. Figure 1 also presents CH₄ mole fractions analyzed in ice cores from Greenland (open blue

65 symbols), such as Eurocore (Blunier et al., 1993), Eurocore and GISP2 (Greenland Ice Sheet Project 2) (Etheridge et al., 1998) and Site J (Nakazawa et al., 1993). These data show fairly good agreements with each other until ~1900, after which the number of data and the consistency among the records are poor. Continuous measurements from NEEM-S1 ice core (Rhodes et al., 2013) presented CH₄ mole fractions before ~1960 (red in Figure 1), but their data are notably higher than the ice core data after ~1850. Therefore, the inconsistency among the different data sets indicates that the period between ~1900 and ~1980
70 is not covered reliably either by direct observations or ice core reconstructions.

In comparison to these data, higher-resolution CH₄ data are available from Antarctica (grey in Figure 1). The comprehensive Law Dome ice core and firn data set (Etheridge et al., 1998; MacFarling Meure et al., 2006) almost continuously covers the last 200 years and are well connected to the direct measurements at South Pole (SPO, data provided by NOAA/ESRL/GML) and Cape Grim (CGO) (Etheridge et al., 1998; MacFarling Meure et al., 2006). Such consistency and continuity among the
75 datasets suggests that the Antarctic CH₄ data can serve as a good reference to represent the global atmospheric CH₄ trend over the past two centuries.

Currently, two synthetic data sets for the Arctic historical CH₄ mole fractions are available (see section 3.2). Buizert et al., (2012) prepared Arctic historical trends of mole fractions of atmospheric trace gases including CH₄, which in turn was used to constrain the gas diffusivity profile in firn at the NEEM site. As seen in Figure 1 (light blue line), the Arctic CH₄ scenario by
80 Buizert et al. (2012) is consistent with the direct measurements that started in the 1980s, and ice core reconstructions before ~1900. Considered as the most likely synthetic atmospheric CH₄ trend for the northern high latitudes, this scenario was treated as a “known” history, by which the diffusivity profiles in firn were tuned in firn-air transport models (Witrant et al., 2012; Trudinger et al., 2013). The other is the composite data set prepared for use in the CMIP6 experiments (Meinshausen et al. 2017). They provide latitudinal monthly gridded fields of various greenhouse gas mole fractions to be consistent with available
85 measurements. It is seen that their scenario for the northernmost latitude (green in Figure 1) follows the NEEM-S1 ice core data set (red). Figure 1 shows that the two synthetic data sets of the historical CH₄ trend are inconsistent in particular for the early 20th century, and it is highlighted in this study that these scenarios have not been sufficiently validated against independent estimates for the data gap period (from ~1900 to ~1980).

In this study, we present a set of mole fractions of CH₄ and other trace gases in firn-air samples collected at the NGRIP site.
90 Using the available atmospheric scenarios, we simulate the depth profiles of trace gases in the NGRIP firn with our firn-air transport model as well as those in the NEEM firn reported previously (Buizert et al., 2012). We examine a variety of modeling cases for different diffusivity profiles and reconstruct the Arctic atmospheric CH₄ over the late 20th century using the iterative dating approach (Trudinger et al., 2002). The reconstructed CH₄ trends from both firn are evaluated by comparison to the atmospheric CH₄ scenarios. Uncertainty of the Arctic atmospheric CH₄ history for use in firn-air modeling is discussed.

95 2 Experimental method

Firn air was sampled at the Greenland site NGRIP (75°10'N, 42°32'W, 2959 m AMSL) in May–June 2001. Accumulation, surface density, mean temperature and pressure are 179 kg m⁻² yr⁻¹, 300 kg m⁻³, 241 K and 680 hPa, respectively. Details of the firn and firn-air sampling have been described elsewhere (Kawamura et al., 2006; Ishijima et al., 2007). At the NGRIP site, two shallow holes (EU and Japanese holes) were drilled (Kawamura et al., 2006; Landais et al., 2006), and the present data
100 are from the firn-air samples collected from the Japanese hole. The total number of air-sampling depths is 24.

Since the technical details are reported in Kawamura et al. (2021), only brief descriptions of relevant data presented in this study are given here. CH₄ mole fractions of the firn-air samples were measured using a gas chromatograph (Agilent 6890, Agilent Technologies Inc.) equipped with a flame ionization detector (GC-FID) at Tohoku University (TU), with a reproducibility of 2 ppb (Umezawa et al., 2014). The CH₄ mole fractions were determined against our working standard gases
105 that were calibrated on the TU1987 CH₄ scale (Aoki et al., 1992; Umezawa et al., 2014; Fujita et al., 2018). The difference between the TU1987 CH₄ scale and the WMO CH₄ mole fraction scale (on which the NEEM CH₄ data were measured) is estimated to be ~0.5 ppb at the current atmospheric CH₄ levels (Fujita et al., 2018). Oyabu et al. (2020) reported that ice core data analyzed on the TU1987 and WMO scales showed good agreement within analytical uncertainties, indicating consistency of both scales, including for the lower mole fractions (e.g. ~700 ppb). It is therefore likely that the difference between both
110 scales is well below the variations of interest in this study, and thus no correction is applied for use of the NGRIP and NEEM firn data.

The firn-air samples were measured for CO₂ and SF₆ mole fractions respectively by using a nondispersive infrared gas analyzer (NDIR) and a gas chromatograph equipped with an electron capture detector (GC-ECD) at TU. The measurement reproducibility is estimated to be 0.02 ppm for CO₂ and 0.09 ppt for SF₆ and mole fractions of both gases are reported on the
115 TU2010 CO₂ and TU2002 SF₆ scales, respectively (Sugawara et al., 2018).

The NGRIP firn-air samples were also analyzed for selected halocarbons (CFC-11, CFC-12, CFC-113 and CH₃CCl₃) on the Vacuum Preconcentration and Refocusing-Gas Chromatography-Mass Spectrometry (VPR-GCMS) system, which was developed based on the work by Saito et al. (2006). An aliquot of the sample was transferred into an evacuated canister of ~0.3 L at around ambient pressure (~100 kPa) and the inner pressure of the canister was recorded. The air is extracted by a vacuum
120 pump through a preconcentration trap filled with HayeSep D cooled to -135° C using a Stirling cooler. The preconcentration trap was heated to -70°C to release major atmospheric constituents and then up to 100°C to transfer the trapped compounds to a cryofocusing trap containing Carboxene 1000/Tenax TA at -100°C. The trap was then heated to 180°C to inject the trapped gases onto a PoraBOND Q separation column for subsequent analysis on MS. Mole fractions of individual halocarbons are determined against a working standard gas (compressed dry air) that was calibrated against synthetic standards on the
125 NIES-08 scales.

3 Firn-air transport model

Since the gas diffusivity in firn layers is significantly lower than in the atmosphere, the movements of atmospheric constituents are driven mostly by molecular diffusion according to their vertical mole fraction gradients under the influence of gravity. In general, lighter air components (or isotopologues) diffuse faster under their mole fraction gradients, while heavier components
130 accumulate in the deeper layers due to the gravitational effect. Hence the depth profiles of trace gas mole fractions in firn are determined by the atmospheric histories transferred towards depth in the firn by the molecular diffusion driven by the mole fraction gradient and gravity. At the bottom of firn, the air is trapped as bubbles in the ice sheet, which creates slow downward motion of firn air.

The firn column can be divided into three zones: a convective zone (CZ), a diffusive zone (DZ) and a lock-in zone (LIZ)
135 (Sowers et al., 1992; Kawamura et al., 2006; Buizert et al., 2012). In CZ, primarily driven by surface winds and fluctuations of atmospheric pressure, air is mixed with the overlying atmosphere (Sowers et al., 1992; Kawamura et al., 2006). The CZ thickness at NGRIP is estimated to be below 2 m (Kawamura et al., 2006). In DZ, which is sufficiently isolated from the surface turbulence, movement of air is governed by molecular diffusion. Gravitational enrichment according to the barometric equation (i.e. linear increases of $\delta^{15}\text{N}$ of N_2 and $\delta^{18}\text{O}$ of O_2) occurs with depth, which stops at the top of LIZ (Sowers et al.,
140 1992; Schwander et al., 1993; Kawamura et al., 2006). The top of LIZ (lock-in depth) at NGRIP is at depth 63 m (Kawamura et al., 2006). In LIZ, advection with the enclosing ice matrix dominates the transport of air, and air parcels are gradually isolated as bubbles. Traditionally, it was supposed that high-density impermeable ice layers stop diffusivity in LIZ completely, however, recent studies demonstrated finite diffusivity in LIZ (Severinghaus et al., 2010; Buizert et al., 2012; Trudinger et al., 2013). The deepest air sampling at NGRIP was successfully made at 77.71 m, and total pore closure is considered in the deeper
145 layers in our modeling.

3.1 Modeling firn-air transport

We use a one-dimensional diffusion model that has been used for the reconstruction of isotope ratios of CO_2 and N_2O (Sugawara et al., 2003; Ishijima et al., 2007). The model is conceptually similar to that developed by Trudinger et al. (1997); it is based on a theoretical formation of diffusion (Schwander et al., 1993) and a bubble trapping process (Rommelaere et al.,
150 1997). Air movement in the firn is driven by molecular diffusion and a gravitational effect. Namely, a trace gas flux in firn is expressed by

$$F = -D \left\{ s \frac{\partial}{\partial z} \left(\frac{c}{s} \right) - \frac{mgc}{RT} \right\}, \quad (1)$$

where D is the effective diffusivity of a trace gas molecule, the variables s , c , and T are open porosity, trace gas molar concentration, and firn temperature, respectively, and the constants m , g , and R are the mass number of the trace gas, the
155 acceleration of gravity, and the gas constant, respectively. Vertical advection flux of the trace gas, caused by air trapping at

the close-off zone and downward bulk motion of firm, is expressed by using the equation given by Rommelaere et al. (1997).

Conservation of the trace gas is given by

$$\frac{\partial c}{\partial t} + \frac{\partial(v c)}{\partial z} + \frac{\partial F}{\partial z} + r c = 0, \quad (2)$$

for the open pore space and

$$160 \quad \frac{\partial c_b}{\partial t} + \frac{\partial(v_f c_b)}{\partial z} - r c = 0, \quad (3)$$

for bubbles. Here c and c_b are trace gas molar concentrations in the open pore space and bubbles, respectively. Vertical speed of air in the open pore space v is distinguished from that of firm itself v_f . The vertical speed of firm $v_f(z)$ is simply given by dividing the accumulation rate by the firm density under the assumption of the steady-state densification of firm. At the transition zone where the open pore air is gradually trapped into bubbles, mass conservation is given by using a bubble trapping rate r (s^{-1}), which simply means that a portion of the trace gas molar concentration in the open pore space (rc) is added to bubbles. The bubble trapping rate is given as a function of the open porosity, the total porosity, and the vertical speed of firm itself (Rommelaere et al., 1997). The total porosity was calculated from the firm density data. At the transition zone, the total porosity should be divided into the open and closed porosity. The closed porosity s_c was calculated by the empirical equation given by Schawander (1989).

170 3.2 Atmospheric scenarios

To simulate depth profiles of trace gases in firm, atmospheric histories of the target gases are required. In this study, we used atmospheric histories prepared by the NEEM firm-air modeling (Buizert et al., 2012) and by the CMIP6 experiments (Meinshausen et al., 2017) for all the trace gases presented in this study for the NGRIP and NEEM firm (CH_4 , CO_2 , SF_6 , CFC-11, CFC-12, CFC-113, HFC-134a, CH_3CCl_3 and $^{14}CO_2$). Since Meinshausen et al. (2017) provides latitudinally gridded datasets, their historical data for the northernmost latitude ($82.5^\circ N$) are used. Note that the $^{14}CO_2$ history for CMIP6 is available from another study (Graven et al., 2017), which is also used in this study. The $^{14}CO_2$ data by Graven et al. (2017) are available in $\Delta^{14}CO_2$ for three zonal bands (northern hemisphere, tropics and southern hemisphere), and were converted to $^{14}CO_2$ mole fraction as in Buizert et al. (2012). These atmospheric scenarios (hereafter referred to as the BZ and CMIP6 scenarios) are compared in Figure 2. The BZ (light blue) and CMIP6 (blue) scenarios show compatible historical trends in many trace gases. There are however slight differences in some trace gases between the two scenarios e.g. SF_6 and CFC-12, but we later show that these differences do not cause significant biases in reproducing their depth profiles at the NGRIP and NEEM firm sites. In contrast, the Arctic CH_4 histories by the two studies differ considerably (Figure 2b). The two CH_4 histories show similar trends after 1960, but before this, the data sets diverge the further into the past. This disagreement is also clear in the inter-pole difference (IPD), calculated relative to the CMIP6 histories for Antarctica (right axes). While the BZ scenario shows a gradual increase in IPD, the CMIP6 scenario indicates almost constant values at ~ 130 ppb over the 20th century. This difference stems from the different methodologies that were used to produce the respective scenarios. As described by Buizert et al. (2012), the BZ CH_4 scenario was constructed by adding the presumed IPD to the Antarctic history (the Law Dome data), where the IPD

was assumed to be proportionally correlated with the growth rate of CH₄. This seems a reasonable assumption, given that the IPD and growth rate are both largely subject to changes in emissions from the northern hemisphere (Dlugokencky et al., 2003; Ghosh et al., 2015; Chandra et al., 2021). Meinshausen et al. (2017) compiled historical measurement records from the worldwide networks as well as Antarctic/Greenland ice core and firn samples and constructed latitudinally gridded datasets of various greenhouse gases. For the historical trend of CH₄, they relied on the data set from the NEEM-S1 ice core by Rhodes et al. (2013) to produce the atmospheric histories for the northern hemisphere. They used the 5-yearly averaged values with outliers removed to represent lower bounds of the raw data points as shown in Figure 1. Note that the Rhodes et al. (2013) data set was not available when the BZ scenario was constructed. Therefore, CH₄ is the only compound, with an available atmospheric history, which shows a clear disagreement, thus highlighting the limitation of our current understanding of its atmospheric historical trend for the northern hemisphere. Conversely, this study assumes that the atmospheric scenarios for other trace gases are known with sufficient accuracy. The scenarios of the individual trace gases have inherent uncertainties, but the comparisons of the two scenarios indicate that the other gases are at least better known than CH₄.

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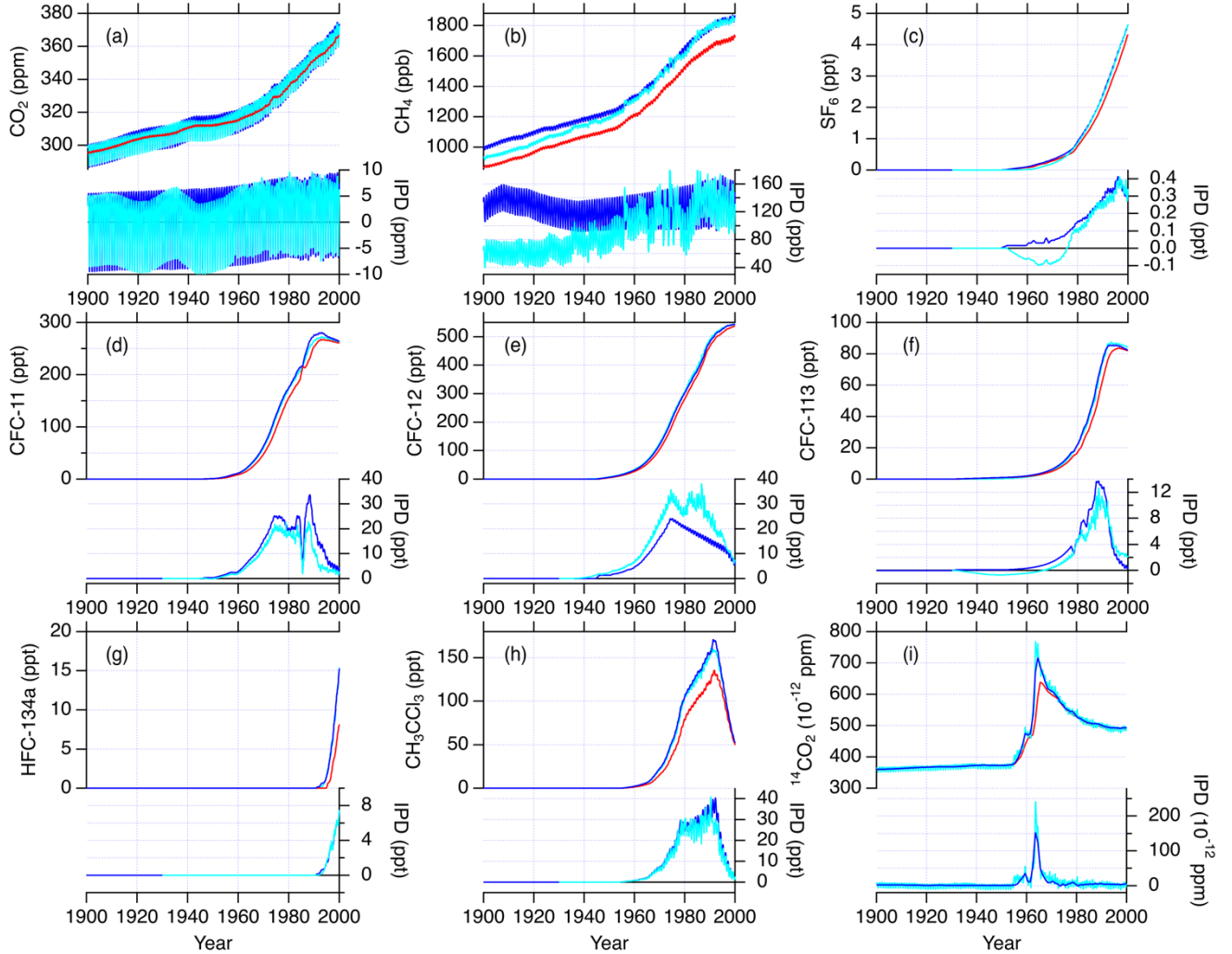


Figure 2: Atmospheric scenarios of various trace gases used in this study. The Arctic histories prepared for the NEEM firn-air modeling (Buizert et al., 2012) are in light blue. The Arctic and Antarctic histories for CMIP6 (Meinshausen et al., 2017) are in blue and red, respectively. For $^{14}\text{CO}_2$, the CMIP6 historical data are from Graven et al. (2017). The inter-polar differences (IPDs) calculated from the Arctic histories with respect to the Antarctic CMIP6 histories are also shown (right axes).

3.3 Effective diffusivity

We follow the previous firn-air studies in which the effective diffusivity in firn is optimized with an iterative method so as to minimize the difference between the simulated and observed depth profiles of CO_2 (Sugawara et al., 2003; Ishijima et al., 2007). In these previous studies, an initial guess of the effective diffusivity for CO_2 , $D_{\text{init}}(z)$, was calculated by:

$$D_{init}(z) = D_0 \left(\frac{T}{253} \right)^{1.85} \left(\frac{1013}{p} \right) \{1.7s(z) - 0.2\}, \quad (4)$$

where $s(z)$ and D_0 represent the open porosity at a depth z and the diffusion coefficient of CO_2 at 253 K and 1013 hPa, respectively. D_0 was set to $1.247 \times 10^{-5} \text{ (m}^2 \text{ s}^{-1}\text{)}$ according to Trudinger et al. (1997). The bulk density was determined by measuring the dimension and weight of cylindrically cut firn core samples (Kawamura et al., 2006). The effective diffusivity of CO_2 thus obtained, was converted to those of other trace gases by multiplying by scaling factors from Buizert et al. (2012). Therefore, the depth profile pattern of the effective diffusivity is identical among all gases, but the magnitude is gas-dependent due to the scaling factors. In this study, the effective diffusivity profile prepared for the NGRIP firn by Ishijima et al. (2007) is referred to as the initial diffusivity and it was modified to improve the reproducibility of our newly measured trace gas profiles. For simulating trace gas profiles for the NEEM firn, we began with the effective diffusivity profiles available from Buizert et al. (2012). Those effective diffusivity profiles, which were originally optimised for individual firn-air transport models that participated in that study, were modified and used for simulating the various trace gas profiles reported for the NEEM firn. The various diffusivity profiles were constructed by modifying the original profiles at a certain range of depths in a stepwise manner. Although this simple method does not guarantee identification of a best-match profile, we are confident that an acceptable range of the diffusivity profile is satisfactorily constrained. We eventually prepared 100 different sets of diffusivity profiles so as to cover a considerable range of diffusivity. Each set of the diffusivity profiles was evaluated based on the root mean square deviation (RMSD) between the model and data according to Buizert et al. (2012). All sets of effective diffusivity profiles for the NGRIP and NEEM firn sites are shown in Figure 3 (top and bottom panels, respectively). The different colors of the diffusivity profiles will be explained later. As shown in the figure, we examined a considerable range of effective diffusivity for different firn layers at both NGRIP and NEEM firn sites. Those diffusivity profiles were evaluated against the observed trace gas profiles, which were regarded as constraints. Note that, in the evaluation, the atmospheric scenarios of the trace gases (except CH_4) are assumed to be known with sufficient accuracy to infer a range of acceptable diffusivity profiles that reproduce the depth profiles of the firn-air composition.

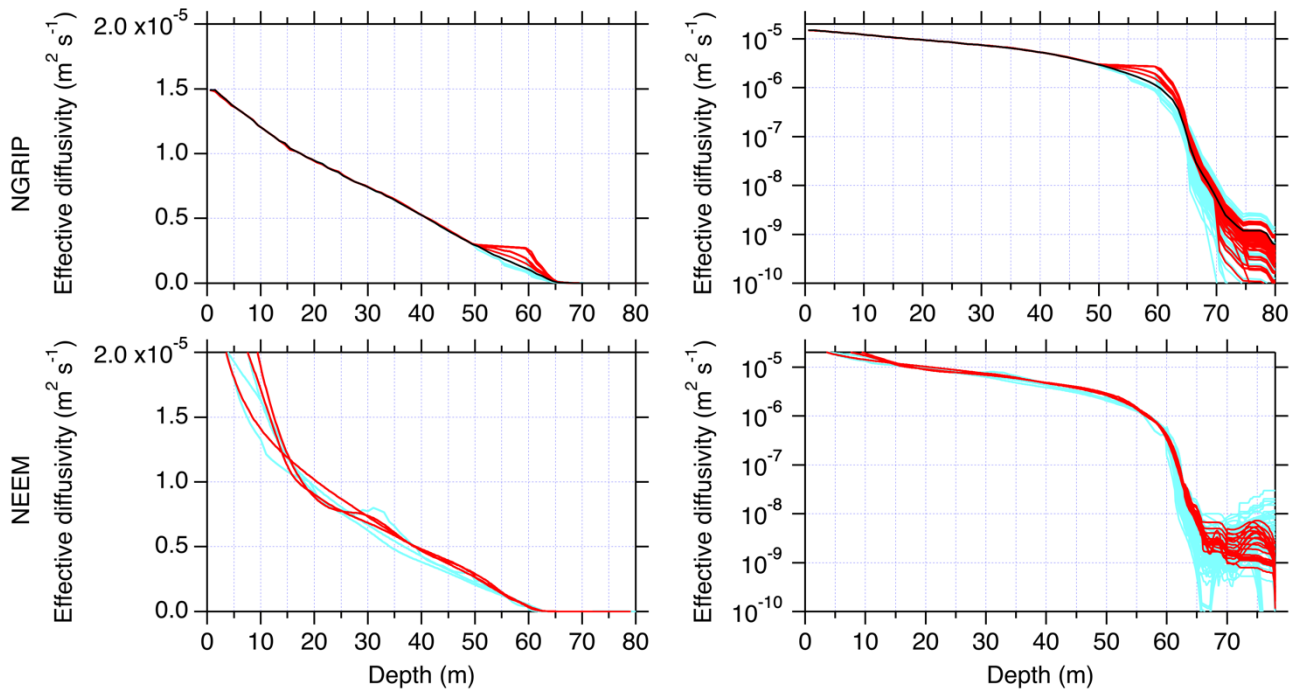


Figure 3: The 100 sets of effective diffusivity profile of CO₂ in the NGRIP (top panels, left panel on a linear scale and right panel on a log scale) and NEEM firn (bottom panels). The initial diffusivity profile (Ishijima et al., 2007) is shown in black (NGRIP only) and modified diffusivity profiles are in colors. The diffusivity profiles whose corresponding mole fraction profiles have RMSD values of <1.0 are colored red and the others light blue.

3.4 Performance of the firn-air transport model

To validate our firn-air transport model, we began by simulating depth profiles of various trace gases in the NEEM firn. Our model did not participate in the model intercomparison study using the NEEM data (Buizert et al., 2012). In this simulation, we employed the BZ scenarios as per their model intercomparison. The simulated depth profiles of the nine trace gases are presented in Figure 4 and compared with those by other models presented in Buizert et al. (2012). The results confirm that the performance of our model is comparable to those by other groups. As a measure of the model performance, Buizert et al. (2012) compared RMSD, which ranged from 0.73 to 0.92 for the six participating models. Following the same approach, our model yields the RMSD value of 0.83 for the NEEM EU borehole. This RMSD value was achieved with an effective diffusivity profile that was prepared by modifying the profile originally optimised for the CIC (Centre for Ice and Climate) model at a certain range of depths. Note that the RMSD value here was calculated including CH₄ as per Buizert et al. (2012), but, as

described in section 3.5, CH₄ is excluded in calculation of RMSD in the following sections.

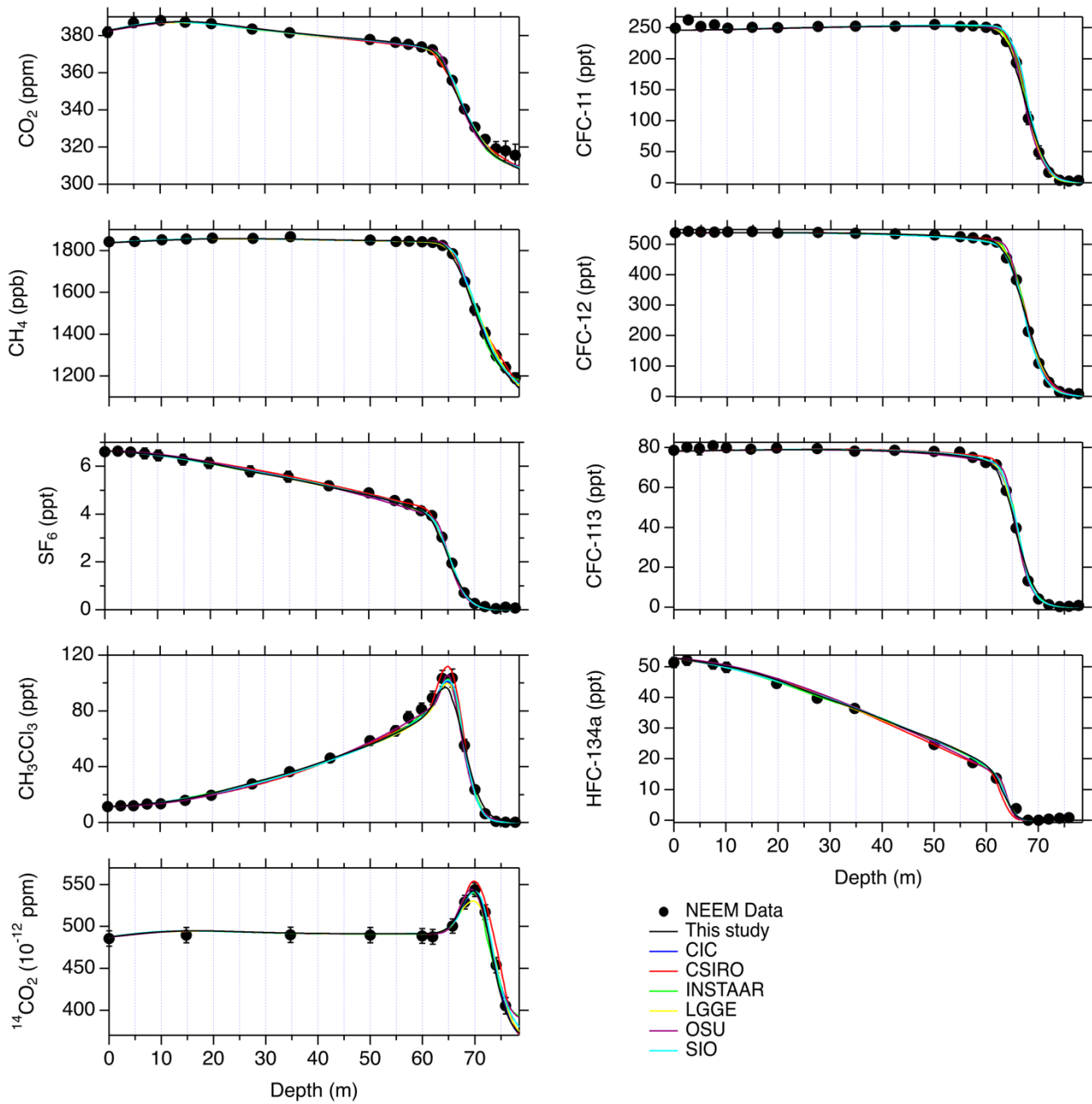


Figure 4: Modeled depth profiles of various compounds in the NEEM firn. Closed circles in black are the observed data with uncertainty estimated by Buizert et al. (2012). Our model results are shown in black solid lines and results from other models are in colors. Different models are labeled by institutions according to Buizert et al. (2012): CIC (Centre for Ice and Climate), CSIRO (Commonwealth Scientific and Industrial Research Organization), INSTAAR (Institute of Arctic and Alpine Research), LGGE (Laboratoire de Glaciologie et Géophysique de l'Environnement), OSU (Oregon State University) and SIO (Scripps Institution of Oceanography).

3.5 Modeling procedure

Our modeling procedure for reconstructing the atmospheric histories of CH₄ was as follows:

260 (1) To represent atmospheric trace gas trends in the Arctic region, we began by employing the two sets of atmospheric scenarios (section 3.2). The firm transport model calculates depth profiles of the various trace gases at the NGRIP and NEEM firn sites using the large set of modified ($N=100$) effective diffusivities described in section 3.3. The simulation case with each diffusivity profile was evaluated based on RMSD. As we aim to estimate the historical atmospheric trend of CH₄, the RMSD-based evaluations were made using all of the available trace gas data, excluding CH₄. In the RMSD calculation, we used the
265 measurement uncertainties of 0.2 ppm for CO₂, 0.2 ppt for SF₆, 1.1 ppt for CFC-11, 3.3 ppt for CFC-12, 0.6 ppt for CFC-113 and 3.2 ppt for CH₃CCl₃ for the NGRIP firn. For the NEEM firn, we employed the uncertainties provided by Buizert et al. (2012). It should be noted that the present study does not follow the uncertainty estimation as done by Buizert et al. (2012). They indicated that uncertainties in the atmospheric scenarios as well as measurement uncertainties are the two largest contributors to the total uncertainties for individual data points for the NEEM firn. We consider that the uncertainties in the
270 atmospheric scenarios are appreciably examined through comparisons of series of simulations using the two independent scenarios.

(2) We ran the model with 100 different sets of diffusivity profiles to calculate the depth profile of CH₄. Note that, based on the earlier step, we know the diffusivity profiles that generate reasonable firn-air profiles for the trace gases other than CH₄. Every diffusivity profile was used in combination with the firn-air CH₄ data for reconstructing an atmospheric CH₄ history.
275 We employed an iterative dating approach (Trudinger et al., 2002) where the initial atmospheric scenario (the BZ scenario) was modified to improve model reproducibility of the CH₄ depth profile (see below). The corrected atmospheric CH₄ scenarios were then compared to the original scenarios (BZ and CMIP6) for further discussion.

The iterative dating for CH₄ was performed as follows:

- (I) Depth profile of CH₄ was calculated with the initial atmospheric CH₄ scenario.
- 280 (II) The modeled CH₄ mole fraction, calculated in step I, was compared to the input atmospheric CH₄ scenario, and effective age at each sampling depth was determined as the time when the modeled CH₄ agreed with a value in the atmospheric CH₄ scenario. It is noted that the smoothing spline curve applied to the BZ CH₄ scenario was used for calculation of the effective age, as the input scenario with seasonal variation (Figure 2) would not allow the effective age to be uniquely determined.
- (III) A new atmospheric CH₄ scenario was constructed by assigning the observed CH₄ mole fraction, at each depth, to the
285 effective age determined in step II. The observed CH₄ versus the effective age data set was interpolated by a smoothing spline function and it is considered as a revised atmospheric CH₄ scenario.
- (IX) Depth profile of CH₄ was again calculated with the revised atmospheric CH₄ scenario constructed in step III.

(X) The above steps II–IX were repeated until the model-data difference converged within an acceptable range (typically after a few iterations) (Trudinger et al., 2002; Ishijima et al., 2007). In this study, we made five iterations for each modified diffusivity case as we confirmed sufficient convergence of the result.

4 Result

4.1 Initial and modified diffusivity simulations

Figure 5 presents the simulation results with the initial diffusivity in comparison to the observed profiles for the six trace gases excluding CH₄ (CO₂, SF₆, CFC-11, CFC-12, CFC-113 and CH₃CCl₃) for the NGRIP firn. As seen in this figure, measured profiles of these trace gases (except CH₃CCl₃) show gradual decreases with depth in the DZ and sharp decreases in the LIZ. In contrast, CH₃CCl₃ increases with depth in the DZ and sharply decreases in the LIZ. The difference of the depth profile pattern among species is due to their different historical atmospheric trends. It is known that the atmospheric mole fractions of the five trace gases (CO₂, SF₆, CFC-11, CFC-12 and CFC-113) have increased monotonically since the mid 20th century (Sturrock et al., 2002; Martinerie et al., 2009). In contrast, CH₃CCl₃ has increased until the early 1990s and has decreased since then (Sturrock et al., 2002; Rigby et al., 2017), which is also observed in Figure 2. Our simulation reproduces the observed depth profiles of these six trace gases in the NGRIP firn fairly accurately using the BZ scenarios.

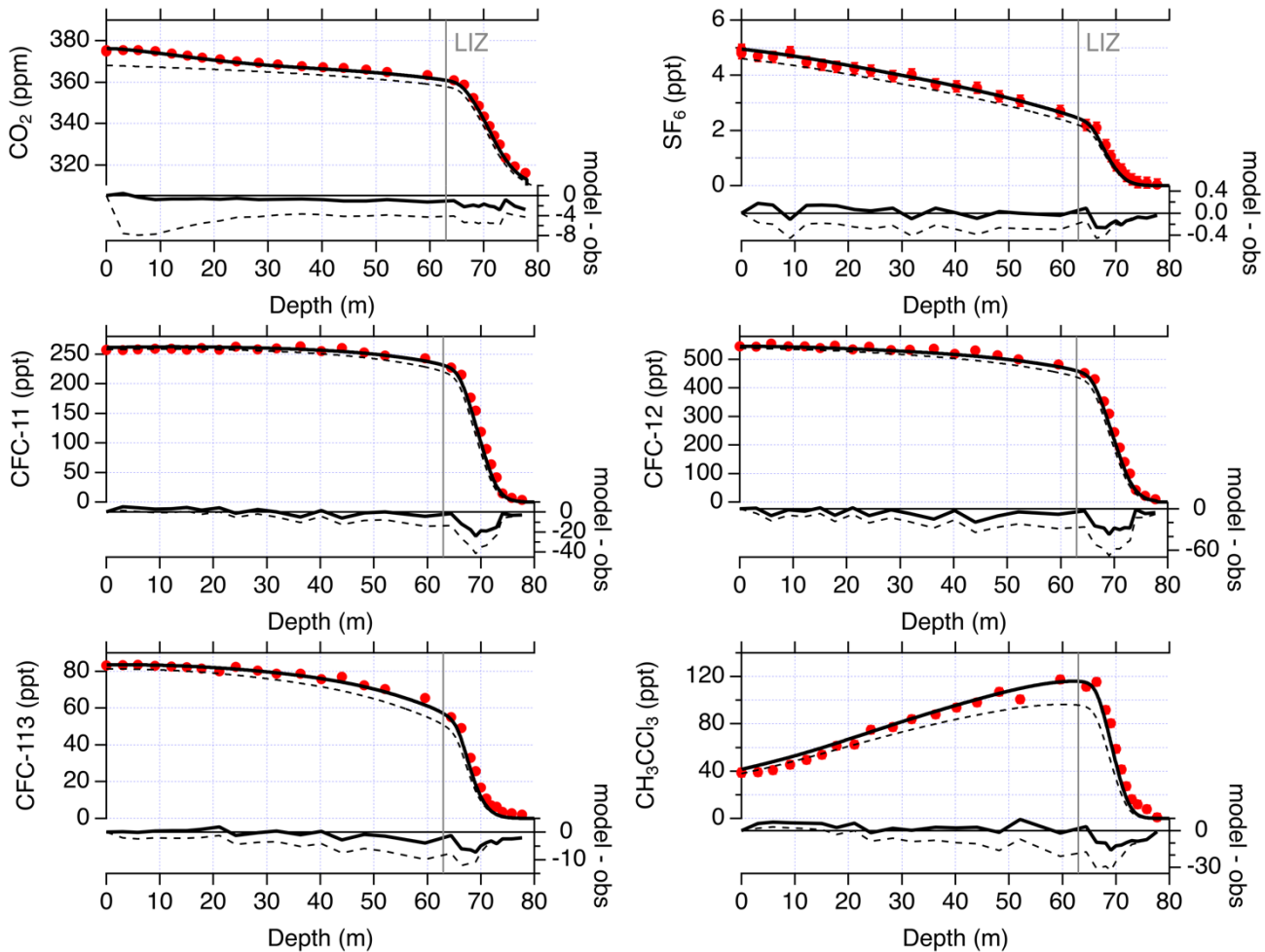


Figure 5: Depth profiles of CO₂, SF₆, CFC-11, CFC-12, CFC-113 and CH₃CCl₃ in the NGRIP firn. The measurement and model results are shown by red circles and black solid lines, respectively (left axis). The measurement uncertainties are shown as vertical error bars though in many cases they are smaller than the circle sizes. Black solid lines show the modeled profiles with the initial diffusivity and the BZ scenarios. The black dashed lines indicate the profiles calculated with the atmospheric scenarios for Antarctica (red lines in Figure 2). The model-data differences are also shown (right axis). The vertical solid line in each panel indicates the upper depth of LIZ.

It is interesting to note that the depth profiles of CH₃CCl₃ at NGRIP and NEEM are remarkably different. Whereas the NEEM data show a relatively sharp CH₃CCl₃ peak in the LIZ (~65 m, Figure 4), NGRIP does not show such a narrow peak. This is due to the timing of firn-air sampling i.e. 2001 for NGRIP and 2008 for NEEM. When the NGRIP firn air was sampled, the signal of the maximum atmospheric CH₃CCl₃ in the early 1990s had only reached near the top of the LIZ at the site, thereby formulating the relatively gentle changes at the shallower depths. On the other hand, seven years later at the NEEM site, such a signal was found deeper in the LIZ where the age of air changes rapidly with depth in both deeper and shallower sides. We

emphasize that, despite the differences in the depth profiles of CH_3CCl_3 at the two sites, our simulations reproduce both profiles measured at both sites well, using the same atmospheric CH_3CCl_3 scenario.

320 Figure 5 shows that the model-data difference increases in the LIZ for all the trace gases. In particular, the model-data difference is pronounced as a dip around 70 m for all trace gases, implying that the mismatches may originate in a common factor in the modeling e.g. depth profile of diffusivity. To examine the impact of diffusivity modification on the simulated depth profiles and their agreements with the data, we examined the 100 sets of modified diffusivity profiles (Figure 3). It was found that, to reduce the model-data difference in the LIZ (Figure 5), the diffusivity needs to be increased in the shallower layers compared with the top LIZ i.e. 50–65 m. The diffusivity was also modified in the deeper layers (>65 m) and simulations
325 were made accordingly.

To examine the sensitivity of the trace gas depth profiles to the IPD, we calculated depth profiles that would be expected if the Antarctic atmospheric scenarios (red lines in Figure 2) are given for the NGRIP firn. This sensitivity experiment shows that IPD causes significant biases larger than the measurement precisions of the respective trace gases. We calculated the difference between the simulations for the BZ scenario (solid line) and the Antarctic scenario (dashed line) and found that sensitivities to
330 the IPD for these six trace gases are no more than 20 times the respective measurement uncertainties. Such relative sensitivities of these suite of gases to the IPDs are much smaller than that of CH_4 , which reaches 40 times the measurement uncertainty. The CH_4 simulation with the Antarctic scenario for the NGRIP firn resulted in the depth profile >100 ppb less than the original simulation (dotted lines in Figure 8), showing the pronounced impact on CH_4 .

The simulated profiles for depths deeper than 50 m using the 100 diffusivity profiles are presented for the six trace gases
335 (Figure 6). In this figure, the modeling results with the modified diffusivity profiles are shown in colors on the left axis, and the model-data differences of the respective cases are plotted on the right axis. It is clear that the model-data differences could be significantly reduced with some diffusivity cases. The RMSD values are as little as 0.51 for a particular case. In Figure 6 and associated figures, the model results with a RMSD of <1.0 are colored red and other cases are colored light blue.

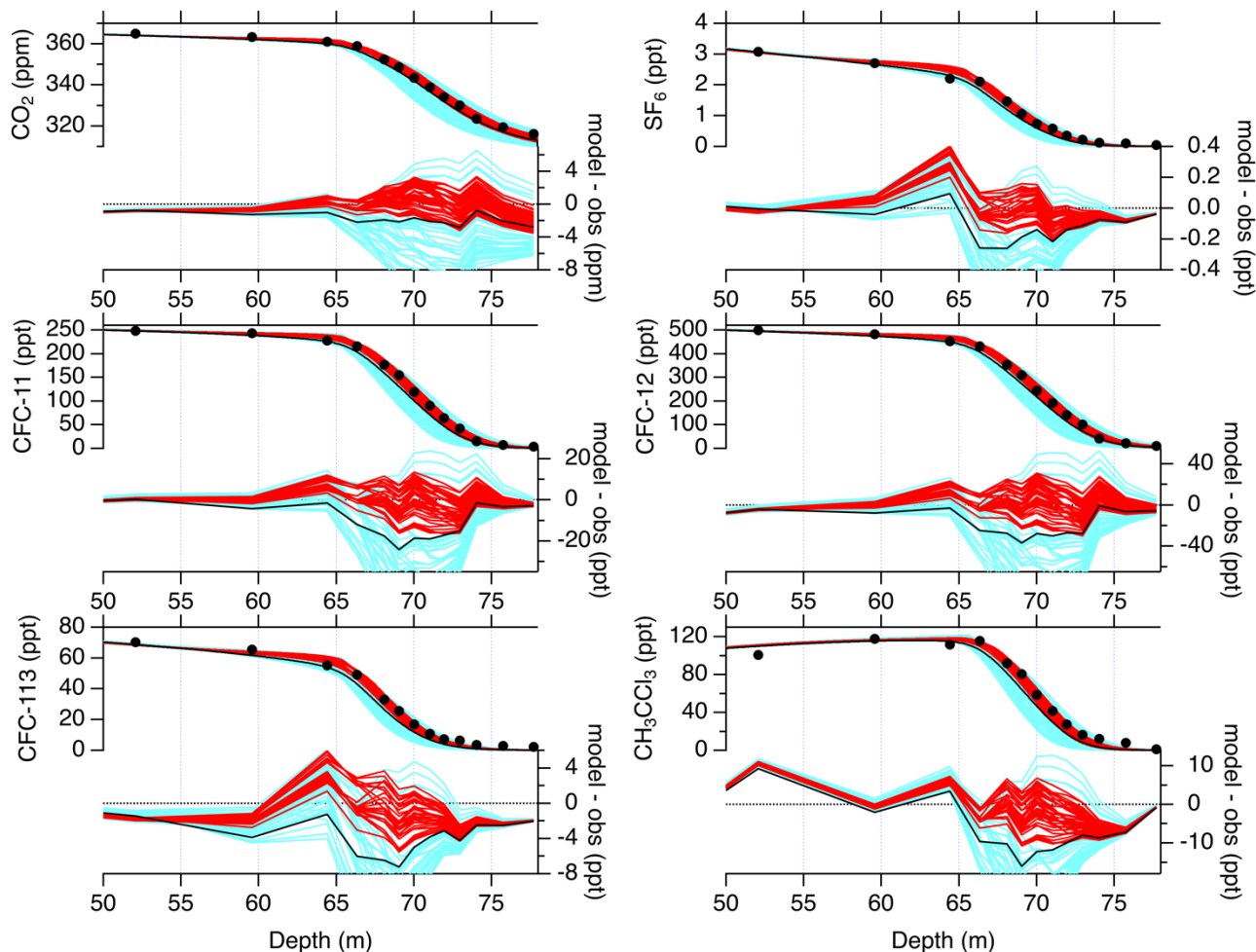


Figure 6: Depth profiles of the six trace gases below 50 m depth in the NGRIP firn. Black circles indicate the measurements and solid lines in colors are the model results with different diffusivity profiles and the BZ scenarios (left axis). Black lines are modeled results with the initial diffusivity. Also shown are the model-data differences (right axis). See text for difference in line colors.

In Figure 7, modeled depth profiles with different sets of the atmospheric scenarios (BZ and CMIP6) are compared. For simplicity, only the results with RMSD of <1.0 are presented. This figure shows that the differences in the atmospheric histories (Figure 2) produces relatively small differences in the depth profiles in the firn. There are small offsets due to the differences of the histories in some gases; difference in the SF_6 history before 1980 (<0.2 ppt) corresponds to the small (<0.1 ppt) offsets below 65 m; significant differences in the histories of CFC-11 (<10 ppt) and CFC-12 (<20 ppt) for 1960–1990 resulted in the overall offsets (roughly <5 and <10 ppt, respectively) below 50 m; difference in the CH_3CCl_3 history (<10 ppt) in the early 1990s produced the offsets (~ 3 ppt) above 66 m. The smaller offsets in the calculated depth profiles than in the input atmospheric scenarios are due to the smoothing effect of diffusion in the firn layers. We calculated the difference

between the modeled profiles with the two scenarios for individual diffusivity cases and found that those differences in the LIZ are within the measurement precisions for SF₆, CFC-113 and CH₃CCl₃. They are a bit larger for CO₂, CFC-11 and CFC-12, which are up to five times the respective measurement precisions. The largest impact of the scenario difference occurs in CH₄. In the LIZ, the difference between depth profiles with the two scenarios reaches to 5–10 times the measurement precision (see Figure 8).

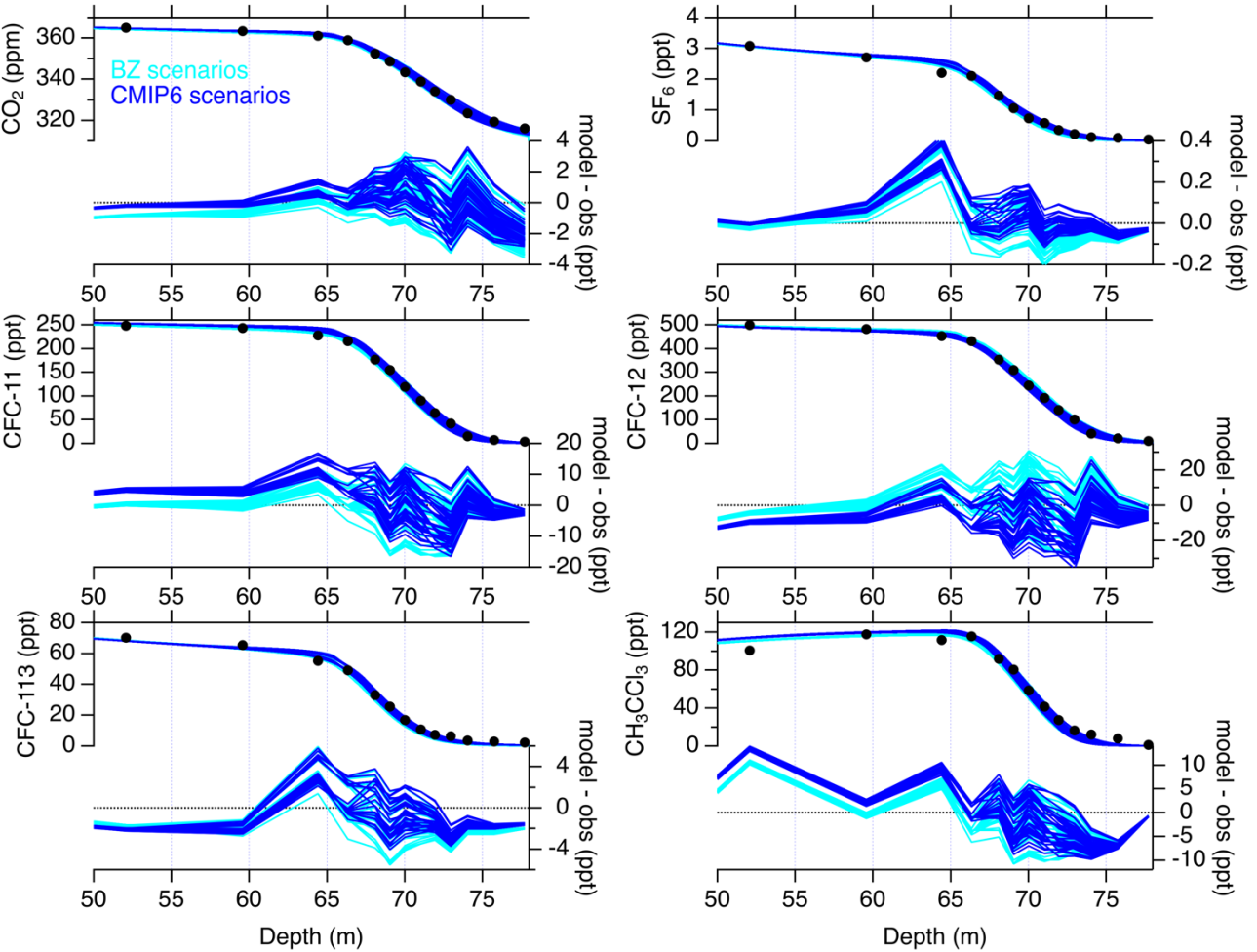


Figure 7: Same as Figure 6, but for comparison of the modeled profiles with different atmospheric scenarios of BZ and CMIP6 in light blue and blue, respectively. Only the simulation results with RMSD values of <1.0 are shown.

Modeled depth profiles of CH₄ are shown in Figure 8. These calculations were made with the 100 diffusivity profiles and the atmospheric CH₄ scenarios of BZ (left) and CMIP6 (right). It is interesting to note that the characteristics of the model-data difference for CH₄ are different from those for the other six trace gases (Figure 6). For the other trace gases, the initial simulation showed increased model-data differences around 70 m, and they were reduced with some modified diffusivity

365 profiles. For CH₄, the model run with the initial diffusivity profile of the BZ scenario reproduces the observed CH₄ profile quite well down to ~73 m, but significantly overestimates by >20 ppb for the lowest three depths (the black solid line in the left panel). Using the modified diffusivity profiles that allowed better agreements for the other six trace gases (red lines), we find larger model-data CH₄ differences than in the initial simulation. These features are commonly seen for the simulation results with the CMIP6 scenario (right panel), but the overestimate in the LIZ is more pronounced, because the CH₄ mole fractions for the early to mid 20th century are higher in the CMIP6 than in the BZ scenario. As described earlier, the difference of depth profiles with the two scenarios exceeds 30 ppb in some diffusivity cases, ten times the measurement precision. Figure 8 also shows the depth profiles which would be expected when the Antarctic CH₄ scenario is used to the firm model (dashed line). The calculated profiles are aligned ~120 ppb below the simulations with the Arctic scenarios, illustrating the large impact of IPD on the CH₄ profile in the Arctic firm.

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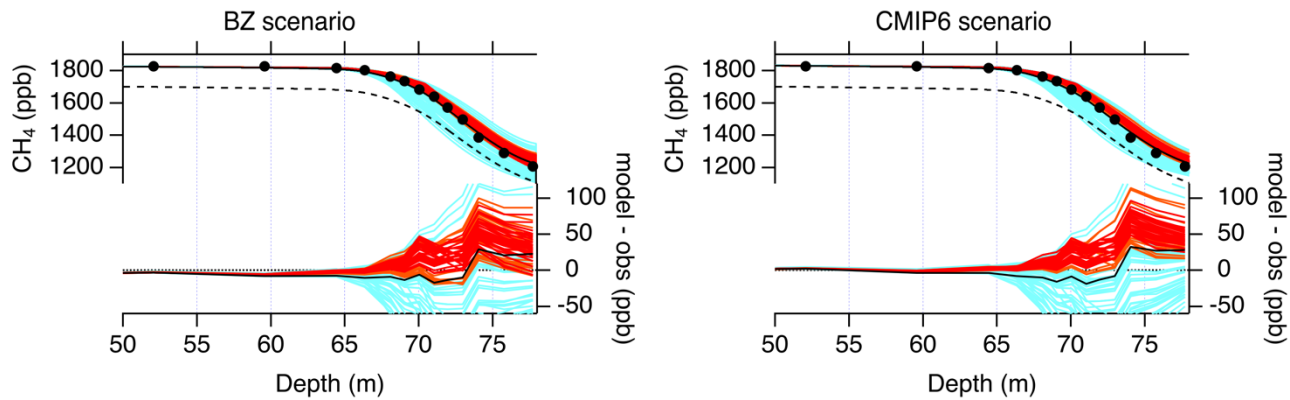


Figure 8: Same as Figure 6, but for CH₄. Simulation results with the atmospheric scenarios of BZ and CMIP6 are shown in left and right panels, respectively. The black dashed lines indicate the profiles calculated with the atmospheric scenarios for Antarctica (red line in Figure 2).

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In addition to the above simulations for the NGRIP firm, we examined the impact of the difference of the atmospheric scenarios on the depth profiles for the NEEM firm. In Figure 9, comparisons between simulations with the different scenarios for the nine trace gases including CH₄ are presented. We found some common characteristics at the NGRIP and NEEM firm sites. While the difference between the simulations with the two scenarios are relatively small for most trace gases, the large difference between the CH₄ scenarios (i.e. higher CH₄ mole fraction in the CMIP6 scenario, see Figure 2) produces enlarged overestimate in the LIZ (> 63 m) in the modeled profiles with the CMIP6 scenario. In the LIZ, the difference of the depth profiles with the two scenario exceeds 30 ppb, being comparable to the magnitude observed in the NGRIP firm (Figure 8).

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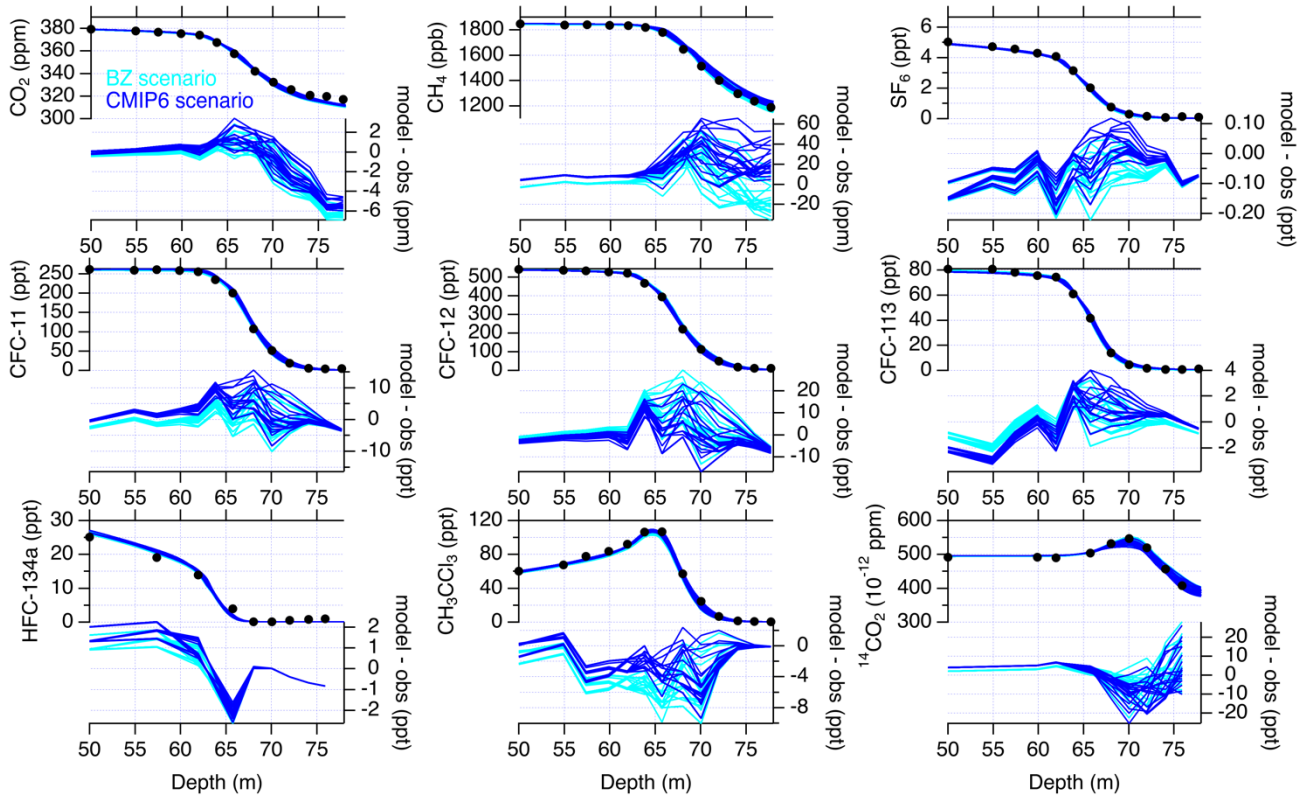


Figure 9. Same as Figure 7, but for the NEEM firn. Only the simulation results with RMSD values of <1.0 are shown.

4.2 Reconstruction by iterative dating

We explore the possibility of reconstructing the Arctic CH_4 mole fractions by the iterative dating method. This approach has a fixed diffusivity profile (assumed to be correct) and aims to find an acceptable atmospheric history to reproduce the firn-air depth profile. It is considered that the modified diffusivity profiles with the low RMSD values are adequately evaluated by the trace gases except CH_4 and that the model-data mismatch in the CH_4 modeling is therefore attributable to uncertainty in the atmospheric CH_4 scenario. The historical atmospheric CH_4 variations obtained by the iterative dating method are presented in Figure 10 for the 100 modeling cases of the modified diffusivity. The different simulation cases are colored in the same manner as in the earlier figures according to the RMSD (Figures 3, 6 and 8). Note that the reconstruction cases colored in light blue are considered to be less likely, due to poorer reproduction of the depth profiles (Figures 6 and 8). The NGRIP reconstruction results (red, Figure 10a) are in good agreement with the BZ scenario after around 1980. For the earlier period, however, the upper bounds of the reconstructions match with the BZ scenario, and the overall range of acceptable histories is below the BZ scenario (circles and shades in red). On the other hand, the NEEM reconstruction results show that the range of acceptable

histories are distributed closely around the original BZ scenario or below it after around 1960, whereas the lower bound of the reconstruction aligns with the BZ scenario before that (Figure 10b).

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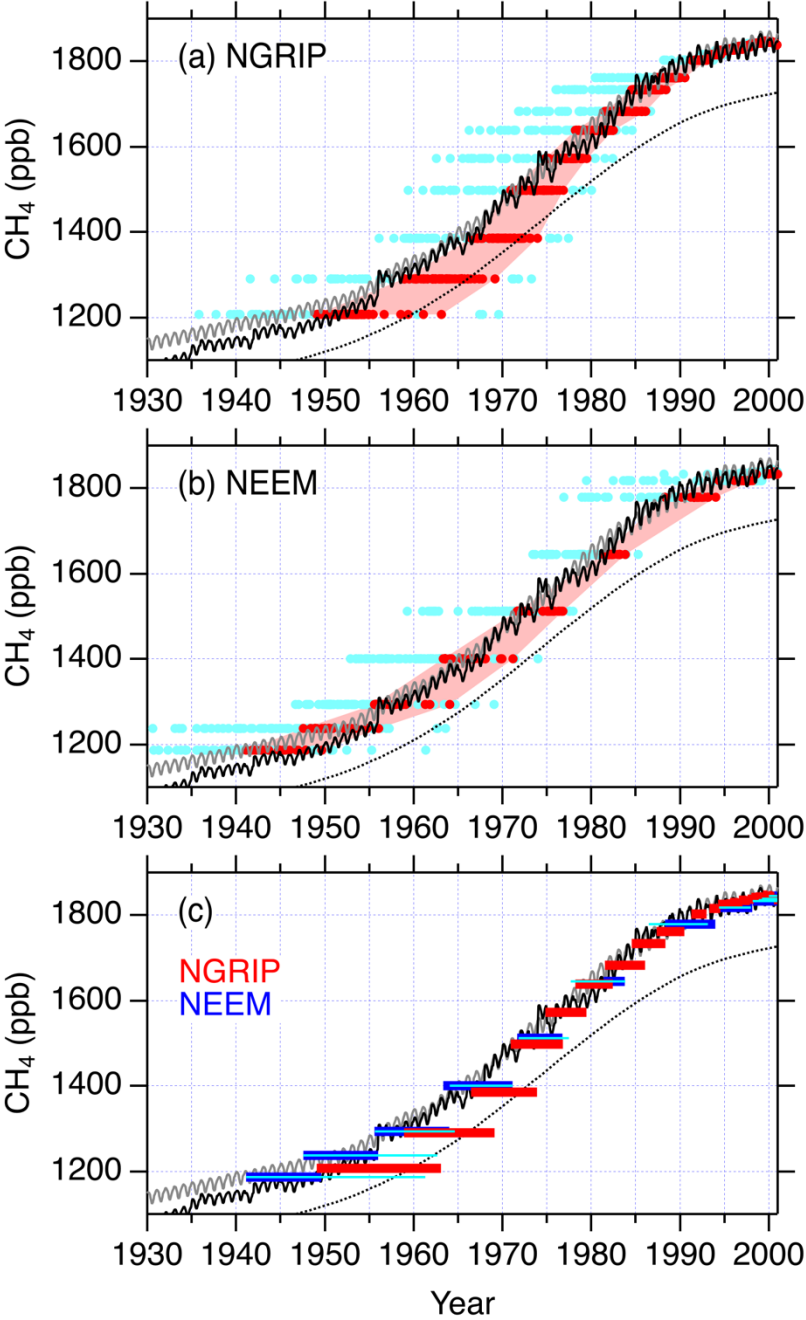


Figure 10: Results of reconstructions by the iterative dating method for the model cases with the 100 different diffusivity profiles (circles colored in the same manner as in Figures 3, 6 and 8) from the (a) NGRIP and (b) NEEM firn air, and (c) the ranges of reconstructions from both firn. The red shades indicate the range of CH₄ mole fraction trends reconstructed using the diffusivity profiles that better reproduce the trace gases except CH₄. Black and grey solid lines are the atmospheric CH₄ scenarios of BZ and CMIP6, respectively, and black dotted line is the smoothed Antarctic CH₄ mole fraction (spline curve) from the Antarctic data shown in Figure 1. The thick horizontal bars in red and blue in panel c correspond to red shades in panels a and b. The light blue thin bars in panel c indicate the range of the reconstructions for cases in which ¹⁴CO₂ data are excluded for evaluations of the diffusivity profiles.

It should be stressed that the reconstructions for the time period before 1980 rely on CH₄ data from the lowest four or five depths of the NGRIP and NEEM firn air. The differences between the initial and corrected atmospheric CH₄ scenario from the three deepest data for the NGRIP firn are up to ~100 ppb. As seen in Figure 10, such reduction in the Arctic atmospheric CH₄ scenario over the period would result in alignment with the atmospheric CH₄ trend in Antarctica inferred from the Law Dome and other datasets (black dotted line). It is again noted that all the reconstruction cases colored in red used diffusivity profiles that yield relatively good model reproducibility with RMSD values of <1.0. It is therefore seen that iterative dating-based reconstruction from the NGRIP firn data suggests decreased CH₄ mole fraction from the 1950s to 1970s in any case, albeit with large uncertainty. It is however noted that, as shown in Figure 10c, this result is not fully compatible with that from the NEEM firn. In particular, the discrepancies between the reconstructions from both firn data diverge with time before 1970. When compared to these reconstructions, the BZ scenario (black line) tracks the overlapping ranges of both reconstructions, while the CMIP6 scenario passes above them before around 1955.

5 Discussion and conclusion

In section 4, we have shown that, with the two atmospheric scenarios (BZ and CMIP6), depth profiles of CO₂, SF₆, CFC-11, CFC-12, CFC-113 and CH₃CCl₃ in the NGRIP and NEEM firn are reproduced with sufficient accuracy by using range of modified diffusivity profiles (Figures 6, 7 and 9). This suggests that the atmospheric scenarios of these trace gases used in the modeling are consistent with the depth profiles observed at both firn sites in Greenland (NEEM and NGRIP). In contrast, the observed CH₄ profile in the NGRIP firn was not accurately reconciled using the two atmospheric scenarios and the diffusivity profiles that allow adequate reproducibility for the trace gases (except CH₄). This suggests either that the Arctic atmospheric scenarios of CH₄ are uncertain or that the diffusivity profile of the NGRIP firn is underconstrained.

We explored the correction of the atmospheric scenario of CH₄ by the iterative dating approach. This method improves agreement to the observed CH₄ depth profile, with an implicit assumption that the diffusivity profile in each case is correct. Although uncertainty due to the under-constrained diffusivity profile in the LIZ is large, this attempt for the NGRIP firn suggested that the CH₄ mole fractions over the period 1950–1980 could be decreased in comparison to the original BZ scenario (Figure 10). The decrease of up to 100 ppb from the BZ scenario over the period 1950–1980, as suggested by the iterative

dating for the NGRIP firm, would make the CH₄ mole fraction as low as that in Antarctica (Figure 10). We point out that such a nearly-zero IPD of the CH₄ mole fraction is highly unlikely, given that a major fraction of both natural and anthropogenic CH₄ sources resides in the northern hemisphere in both preindustrial and industrial periods (Houweling et al., 2000; Ghosh et al., 2015; Saunio et al., 2020; Chandra et al., 2021). In contrast, the iterative dating reconstruction for the NEEM firm agrees with the BZ scenario. Although the spread of the reconstructions is large, particularly for the NGRIP firm, it was found that the BZ scenario passes within the ranges of the reconstructions from both firm data, but that the CMIP6 scenario is notably higher than the reconstructions for the period before 1960. This suggests that the BZ scenario is more consistent with the two sets of the Greenland firm data sets (NGRIP and NEEM) than the CMIP6 scenario for the mid 20th century when the two scenarios begin to diverge as time goes back.

It is important to note that the reconstructions for the period before 1980 from the NGRIP firm were heavily influenced by the five deepest data in the LIZ (> 72 m). Figure 11a shows distributions of the effective age of CH₄ at depths below 55 m in the NGRIP firm, colored the same as in the earlier figures. In addition, the spread of the effective age (σ_{age}) at each sampling depth is shown on the right axis. This figure shows that firm-air samples collected at the five lowest sampling depths at NGRIP have effective ages corresponding to the period from ~1950 to the late 1970s. At those depths, even the acceptable diffusivities yield the spread of the effective age of >5 years (black vertical bars). This shows that the reconstruction of the CH₄ mole fraction for the period is subject to much uncertainty in effective age. For the NEEM firm, the reconstructions before 1980 also rely on the five deepest data in the LIZ (Figure 11b). The σ_{age} values at those depths in the NEEM firm ranges from 5 to 8 years (thick vertical bars), comparable to those in the NGRIP firm. The Antarctic atmospheric CH₄ record (see Figures 1 and 10) indicates that the atmospheric increase rate of CH₄ was 10–15 ppb yr⁻¹ over the period. The 5-year uncertainty in the age estimate for the NGRIP firm-air samples could therefore be translated to an uncertainty of >50 ppb in the Arctic atmospheric CH₄ level. This is comparable to the IPD of CH₄ mole fraction during the 1950s to 1970s, which was assumed when Buizert et al. (2012) prepared the BZ CH₄ scenario. It is also interesting to note that σ_{age} at the four deepest depths in the NEEM firm is almost constant, whereas it increases with depth in the NGRIP firm and exceeds 10 years at the two deepest depths. This indicates that effective age in the oldest firm-air layers can be estimated with better accuracy in the NEEM firm than in the NGRIP firm, thereby providing the reconstructions with smaller uncertainties. As σ_{age} was calculated from the simulation cases with acceptable ranges of diffusivity, its magnitude reflects how tightly the diffusivity profile is constrained at each firm site. In other words, our simulations infer that the diffusivity profile in the NEEM firm can be better constrained than the NGRIP firm. In order to see the degree of constraint to the effective diffusivity from different trace gases, we calculated RMSD values for different combinations of the trace gases for the NEEM firm. The choice of the NEEM firm is due to the availability of a larger number of gas species. It was found that the ¹⁴CO₂ data provide strong constraints for narrowing the acceptable range of diffusivity profiles in the LIZ. The evaluated RMSD with the ¹⁴CO₂ data excluded and the historical CH₄ reconstruction from the simulation cases with RMSD < 1.0 is presented in Figure 10c (thin horizontal bars in light blue). The corresponding spread of the effective age is also shown in Figure 11b (thin vertical bars in black). These results show that, for the NEEM reconstruction, uncertainty of the effective age would be doubled at the two deepest depths if it were not for the ¹⁴CO₂ data. It

is also interesting that the range of the CH₄ reconstruction without ¹⁴CO₂ would deviate to the younger ages and would suggest a historical trend lower than the BZ scenario (Figure 10c). In turn, the CH₄ trend reconstructed from the NGRIP firm might be different if ¹⁴CO₂ measurement was available. The above contribution of the ¹⁴CO₂ data for the NEEM firn implies that the NGRIP reconstruction could have been closer to the NEEM reconstruction. It is also noted that constraints from halocarbon species to the diffusivity profile are relatively weak as their mole fractions in the LIZ are decreased to close to zero.

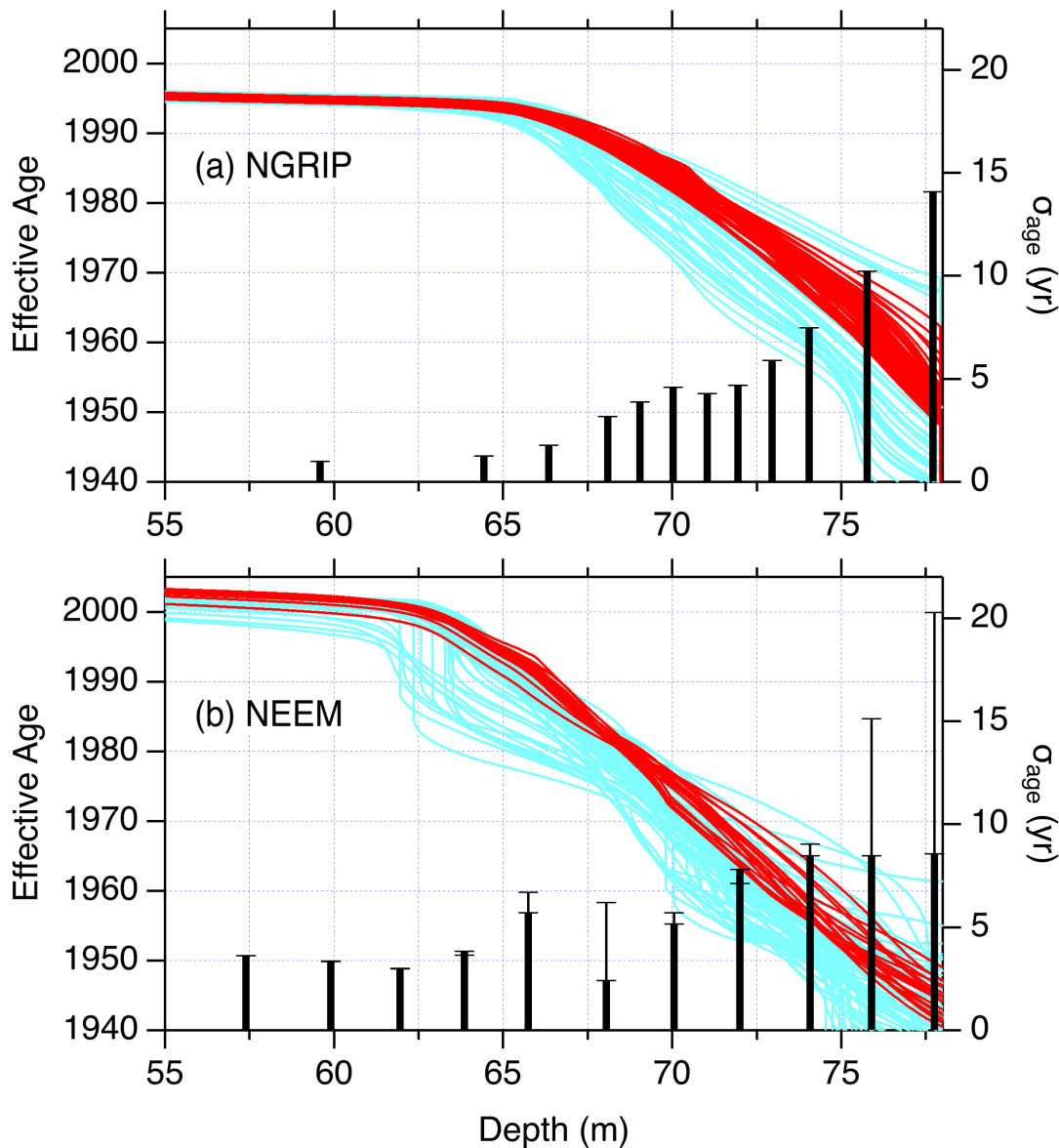


Figure 11: Depth profiles of effective age of CH₄ calculated after the iterative dating calculations for depths below 55 m at the (a) NGRIP and (b) NEEM firn sites (left axis). The solid lines represent cases for different diffusivity profiles and are colored in the same manner as in the earlier figures. Vertical bars in black indicate spread of the effective age (maximum minus minimum) at the

485 individual sampling depths among the modeling cases in red. For the NEEM firn, the thin vertical bars correspond to the spread for
simulation cases in which $^{14}\text{CO}_2$ data are excluded for evaluations of the diffusivity profiles.

The IPD of the atmospheric CH_4 mole fraction is important for better understanding the evolution of the global CH_4 budget.
Given that the Antarctic ice core and firn measurements have provided relatively reliable CH_4 records over the 20th century,
490 improved reconstructions from Greenland ice cores and firn air should better constrain the changes in the IPD. To sufficiently
constrain the historical global CH_4 budget, the reconstruction for Greenland needs to be accurate within ~ 10 ppb, corresponding
to $\sim 30 \text{ Tg CH}_4 \text{ yr}^{-1}$ global emission. Unfortunately, based on the firn CH_4 data from NGRIP and NEEM, this study
demonstrated that consistent and accurate reconstruction of the Arctic CH_4 mole fraction is achievable only back to the mid
1970s, and that the uncertainty of reconstruction is still very large (around 50 ppb) for the 1950s to 1970s.

495 Previous studies have used CH_4 as one of tracers that constrain diffusivity profiles in firn (Witrant et al., 2012; Trudinger et
al., 2013). These studies have shown that CH_4 effectively contributed to constraining diffusivity for deep layers i.e. LIZ in the
NEEM firn. However, the use of CH_4 as an effective constraint is valid only when its atmospheric scenario given as input to
the models was assumed to be correct. Figures 6 and 8 show a larger spread in the model-data differences of CH_4 among the
different diffusivity cases spread widely in the deepest layers of the LIZ of the NGRIP firn, in comparison to the other six
500 gases. This fact highlights that subtle changes of the diffusivity profile in the LIZ have a large impact on simulating CH_4 , and
it indeed indicates that the species could serve as an effective diffusivity constraint, if its atmospheric scenario was correctly
given with low uncertainty. This study indicated that the two currently available Greenland firn data sets (NGRIP and NEEM)
prefer the BZ CH_4 scenario (Buizert et al., 2012) over the CMIP6 scenario (Meinshausen et al., 2017). Furthermore, it should
be again pointed out that the CMIP6 scenario suggests an almost constant IPD of ~ 130 ppb over the 20th century (Figure 2).
505 Such constant IPD is unlikely, because CH_4 emissions are considered to have increased in the northern hemisphere for that
period, which requires IPD to increase with time as discussed in the previous studies (Dlugokencky et al. 2003; Ghosh et al.,
2015; Chandra et al., 2021). Accordingly, the BZ scenario appears a useful choice in firn modeling at Greenland sites, but it
should be kept in mind that the use of CH_4 as a tuning tracer could lead to overfitting of the diffusivity profile.

Sapart et al. (2013) examined the reconstruction of stable carbon isotope ratio ($\delta^{13}\text{C}$) of atmospheric CH_4 using firn-air
510 measurements from both northern and southern hemispheres. They concluded that, with the available firn measurements and
understanding of firn-air transport, it is difficult to reliably reconstruct the past trend of $\delta^{13}\text{C}$ of CH_4 because of multiple reasons
including uncertainty in the atmospheric CH_4 mole fraction scenario. Although there are many important and uncertain factors,
the accurate reconstruction of the atmospheric CH_4 mole fraction is particularly important, because the trend in the mole
fraction can lead to significant signal in the modeled $\delta^{13}\text{C}$ profile in firn due to the difference in the molecular diffusion
515 coefficient, even in the absence of a temporal trend in atmospheric $\delta^{13}\text{C}$. This study revealed a large uncertainty in the Arctic
 CH_4 mole fraction trend over the 20th century, which supports the conclusion of Sapart et al. (2013) on the difficulty of
reconstruction of the $\delta^{13}\text{C}$ of atmospheric CH_4 in the northern hemisphere. The NGRIP firn-air samples were also analyzed for

$\delta^{13}\text{C}$ and stable hydrogen isotope ratio (δD) of CH_4 (Kawamura et al., 2021), but we regrettably report that reconstruction of $\delta^{13}\text{C}$ of CH_4 has not been possible despite our best modeling efforts (not shown).

520 A possibility to improve the reproducibility of the depth profile of CH_4 in the NGRIP firn could come from additional constraint to the diffusivity profile along with those currently made by the six trace gases (CO_2 , SF_6 , CFC-11, CFC-12, CFC-113 and CH_3CCl_3). In particular, it was indicated that $^{14}\text{CO}_2$, if available, would have strongly constrained the diffusivity profile and reduced uncertainty of the historical CH_4 trend reconstructed from the NGRIP firn. This study showed that the currently available firn data from Greenland (NGRIP and NEEM) are in better agreement with the historical CH_4 scenario prepared for
525 the NEEM firn modelling (Buizert et al., 2012), then that for the CMIP6 experiments (Meinshausen et al., 2017). Since the latter scenario relies on the NEEM-S1 ice core data (Rhodes et al., 2013), this study highlighted inconsistency between the ice core and two sets of firn data in Greenland. Given that reconstruction of the CH_4 history from the deepest firn layers is challenging (in terms of the diffusivity versus history problem as shown in this study), future sampling and measurements of ice cores at a high-accumulation site in Greenland (where age of air occluded can be determined accurately) may be the only
530 way to reconstruct the atmospheric CH_4 trend over the 20th century.

Data Availability

The composition data of the NGRIP firn-air samples are available on the Arctic Data archive System (ADS) of National Institute of Polar Research (<https://ads.nipr.ac.jp/dataset/A20210609-001>). The NEEM firn-air data are available in the supplementary file of Buizert et al. (2012). The CMIP6 historical scenarios of the various trace gases used in this study are
535 available via <https://esgf-node.llnl.gov/search/input4mips/> as described in Meinshausen et al. (2017). Those of $^{14}\text{CO}_2$ are available in the supplementary file of Graven et al. (2017). Our modeling data are available upon request (umezawa.taku@nies.go.jp).

Author Contribution

TU, SS, KK and IO discussed on design of the study. KK, SA and TN conducted firn-air sampling at the NGRIP site. SS, KK,
540 TU and TS analyzed the firn-air samples for trace gases. SJA set up the measurement system for the halocarbons. TU and SS made firn-air model simulations. TU analyzed the measurement/modeling data and prepared the manuscript with contributions from all co-authors.

Completing interests

The authors declare that they have no conflict of interest.

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550 (RannIs), Japan (MEXT), Sweden (SPRS), Switzerland (SNF) and the USA (NSF, Office of Polar Programs). We are grateful to the efforts for the measurement and modeling data from NOAA/ESRL/GML and the NEEM firn campaign, both of which are made freely available. This work was supported by JSPS/MEXT (Japan) KAKENHI Grants-in-Aid for Young Scientists B (17K18342 for TU), Grants-in-Aid for Scientific Research on Innovative Areas (17H06320 for KK) and the GRENE Arctic Climate Change Research Project (for SA). We thank the two anonymous referees for helpful comments to improve the
555 manuscript.

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