

1 Long Range Prediction and the Stratosphere

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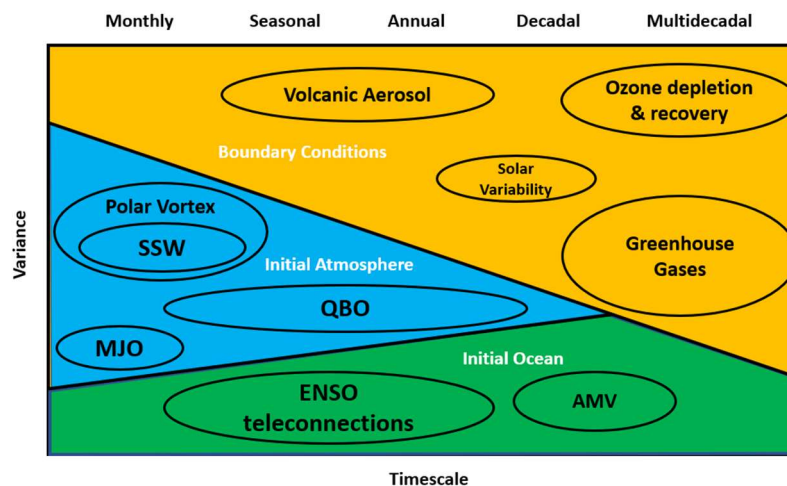
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36 **Abstract.** Over recent years there have been concomitant advances in the development of stratosphere
 37 resolving numerical models, our understanding of stratosphere-troposphere interaction and the
 38 extension of long-range forecasts to explicitly include the stratosphere. These advances are now
 39 allowing new and improved capability in long range prediction. We present an overview of this
 40 development and show how the inclusion of the stratosphere in forecast systems aids monthly, seasonal,
 41 annual to decadal climate predictions and multidecadal projections. We end with an outlook towards
 42 the future and identify areas for improvement that could further benefit these rapidly evolving
 43 predictions.

44

45 **1 Introduction**

46 Daily weather fluctuations are thought to have a deterministic predictability horizon of around two
 47 weeks due to the sensitivity of the evolution of the atmospheric state to small errors in initial conditions
 48 (Lorenz 1969) - the so-called ‘butterfly effect’. Recent estimates (Leung et al., 2020; Domeisen et al.,
 49 2018) as well as tests of the predictability of midlatitude *daily* weather using the latest global prediction
 50 models (Zhang et al., 2019; Son et al., 2020) produce similar estimates for this predictability limit.
 51 However, this does not preclude skilful forecasts of the *statistics* (most notably the average) of
 52 conditions at long range beyond this timescale (e.g. Shukla 1981). This predictability owes its existence
 53 to slowly varying predictable components of the climate system in the ocean, and in some cases the
 54 atmosphere, as well as externally forced changes such as volcanic or solar variability effects (e.g.
 55 Kushnir et al., 2019). Some of the more prominent examples of stratospheric variability such as sudden
 56 stratospheric warmings and their subsequent impact on the stratosphere and the troposphere (Baldwin
 57 et al., 2021), or the quasi-biennial oscillation and its associated teleconnections (Scaife et al., 2014a),
 58 have been shown to be predictable out to timescales well beyond the traditional two-week predictability
 59 horizon from initial tropospheric conditions alone. Other examples involve stratospheric pathways for
 60 teleconnections originating in the troposphere or ocean (e.g., Schwartz and Garfinkel 2017, Byrne et al.
 61 2019) and are shown in Figure 1. On longer timescales, boundary forcing, for example from
 62 composition changes such as ozone depletion and recovery allows the stratosphere to provide relatively
 63 slowly varying conditions to guide the turbulent troposphere and hence provide long range
 64 predictability (e.g., Thompson et al. 2011). The relative importance of stratospheric initial conditions
 65 to boundary conditions decreases with lead time as shown in the schematic in Figure 1.



66 **Figure 1: Schematic representation of the role of the stratosphere in long range prediction showing the**
 67 **transition from initial condition predictability in the atmosphere (blue) and the ocean (green), to boundary**
 68 **condition predictability at longer timescales (orange). Individual mechanisms involving the stratosphere**
 69 **are labelled in black. The width of the ellipses in the timescale direction shows the approximate range over**
 70 **which each phenomenon provides predictability. The width of the ellipses in the variance direction shows**
 71 **their relative contributions to forecast variance.**

72 The extension of long-range prediction systems to explicitly include representation of the stratosphere
73 follows many years of development of stratosphere resolving general circulation models (GCMs). By
74 the late 20th century many leading centres for climate research had started to include the stratosphere in
75 versions of their GCMs (Pawson et al., 2000; Gerber et al., 2012). Much of the early model development
76 was motivated by the discovery of the ozone hole in the 1980s (Farman et al., 1985) and the need for
77 simulations of ozone depletion and potential recovery of the ozone hole following the 1987 Montreal
78 Protocol, which required atmospheric models that represented both the atmospheric dynamics and
79 chemistry of stratospheric ozone depletion (Molina and Rowland 1974; Crutzen 1974). In most cases
80 this was achieved by adding further quasi-horizontal layers to the domain of existing climate models to
81 extend their representation of the atmosphere to the stratopause or beyond (e.g. Rind et al 1988; Beagley
82 et al., 1997; Swinbank et al., 1998; Sassi et al., 2002), while also incorporating key radiative (e.g. Fels
83 et al., 1985), chemical (e.g. Steil et al., 1998) and dynamical (e.g. Scaife et al., 2000) processes.

84 The early development of so called ‘high top’ climate models, which represent the whole depth of the
85 stratosphere, in general preceded the discovery of the main body of evidence that the variability of the
86 stratosphere is not only affected by, but also interacts with the lower atmosphere and surface climate.
87 Pioneering early studies suggested that the stratosphere might have direct effects on the troposphere
88 and surface climate (e.g. Labitzke 1965; Boville 1984; Koder et al., 1990, 1995; Haynes et al., 1991;
89 Perlwitz and Graf 1995). In subsequent years, as reliable observational records lengthened and large
90 enough samples of stratospheric variability were amassed it was unequivocally demonstrated that
91 stratospheric variability precedes important tropospheric changes in the extratropics (Baldwin and
92 Dunkerton 1999, 2001). There was debate about causality and whether the stratosphere really does
93 affect the atmosphere below (e.g. Plumb and Semeniuk 2003). However, experiments where the
94 stratosphere is perturbed in numerical models show changes in surface climate and reproduce similar
95 patterns of response at the surface to those found in real world observations (e.g. Polvani and Kushner
96 2002; Norton et al., 2003; Scaife et al., 2006; Joshi et al., 2006; Scaife and Knight 2008; Hitchcock and
97 Haynes 2016, White et al., 2020). These involve changes to planetary scale waves and also baroclinic
98 eddies in the troposphere that are consistent with changes in baroclinicity near the tropopause (Kushner
99 and Polvani 2004; Song and Robinson 2004; Wittman et al., 2004, 2007; Scaife et al., 2012; Domeisen
100 et al., 2013; Hitchcock and Simpson 2014; White et al., 2020). Importantly, as we discuss below, the
101 same mechanisms also appear to be at work across a broad range of timescales (Kidston et al., 2015).

102 In recent years, motivated by the evidence of surface effects of stratospheric variability in the mid-
103 latitudes, the high-top model configurations used for stratospheric research were incorporated into
104 leading prediction systems. Improved vertical resolution was already known to improve the atmospheric
105 data assimilation of satellite instrument observations whose sensitivity was often heavily weighted
106 towards stratospheric altitudes. This also provided initial stratospheric conditions for sets of
107 retrospective forecasts, some of which were internationally coordinated (e.g. Butler et al., 2016;
108 Tompkins et al., 2017). A growing number of operational systems are now producing regular ensembles
109 of predictions at lead times of months or years with coupled ocean-atmosphere models that extend to
110 the stratopause or beyond; for example at Environment Canada (Merryfield et al., 2013), the Met Office
111 in the UK (MacLachlan et al., 2014), the German Weather Service DWD (Baehr et al., 2015), the Japan
112 Meteorological Agency (Takaya et al., 2017) and the European Centre for Medium Range Weather
113 Forecasts (Johnson et al., 2019). In the following sections we document the emerging impacts and
114 benefits of this new capability for surface climate predictions at monthly, seasonal, and annual to
115 decadal lead times starting with the shorter-range, initial condition cases and ending with the longer-
116 range boundary-condition cases.

117

118 **2 The stratosphere and monthly prediction**

119 The best-established phenomenon that gives rise to predictability of surface climate from the
120 stratosphere is the tropospheric circulation changes that follow strong and weak conditions in the
121 stratospheric polar vortex (Baldwin and Dunkerton 1999, 2001). For example, weak vortex conditions
122 such as those found in a sudden stratospheric warming (SSW, Baldwin et al., 2021) are typically
123 followed by a weakening and southward shift of the tropospheric mid-latitude jet stream (see e.g.
124 Kidston et al., 2015 and references therein) and thus the negative polarity of the North Atlantic
125 Oscillation (NAO), Arctic Oscillation (AO) and Northern Annular Mode (NAM). These fluctuations
126 also show a tendency to vacillate between strong westerly and weak (SSW) states on subseasonal
127 timescales (Kuroda and Kodera 2001; Hardiman et al., 2020a). The changes in the troposphere persist
128 roughly as long as those in the lower stratosphere, and last for around two months (Baldwin and
129 Dunkerton 2001; Baldwin et al., 2003; Hitchcock et al., 2013; Son et al., 2020; Domeisen 2019). The
130 impacts on surface climate also include changes in the frequency of extremes of temperature and rainfall
131 (Scaife et al., 2008; King et al., 2019; Cai et al., 2016; Domeisen et al., 2020b).

132 Although *major* SSW events, involving a complete reversal of the zonal flow in the mid stratosphere,
133 are rare in the southern hemisphere (Wang et al., 2020; Jucker et al., 2021), variations of the Antarctic
134 polar vortex are likewise followed by similar signatures in the underlying tropospheric flow, in this case
135 via the Southern Annular Mode (SAM). Weakening of the vortex is typically followed by a negative
136 shift in the SAM and associated changes in rainfall and near surface temperature (Thompson et al.,
137 2005; E. Lim et al., 2018, 2019, 2021, Rao et al., 2020e). These changes in Southern Hemisphere
138 circulation typically take longer to reach the surface than their Northern Hemisphere counterparts
139 (Graverson and Christiansen 2003), perhaps due to the stronger stratospheric polar vortex and weaker
140 wave driving in the southern hemisphere, but they are nonetheless better predicted by improving
141 stratospheric resolution of forecast models (Roff et al., 2011). The timescale of weeks for the
142 predictability of sudden warmings is limited by the predictability of weather patterns in the troposphere
143 which might trigger SSW events (e.g. Mukougawa et al., 2005; Taguchi 2016; Garfinkel and Schwarz
144 2017; Jucker and Reichler 2018; Lee et al., 2020a). However, if we add this timescale to the timescale
145 of a month or more for the persistence of lower stratospheric anomalies and their surface effects (e.g.
146 Baldwin et al., 2003; Butler et al., 2019), we arrive at the conclusion that on these occasions at least,
147 initial conditions in the atmosphere can provide predictability well beyond the usual two-week horizon
148 for daily weather in either hemisphere.

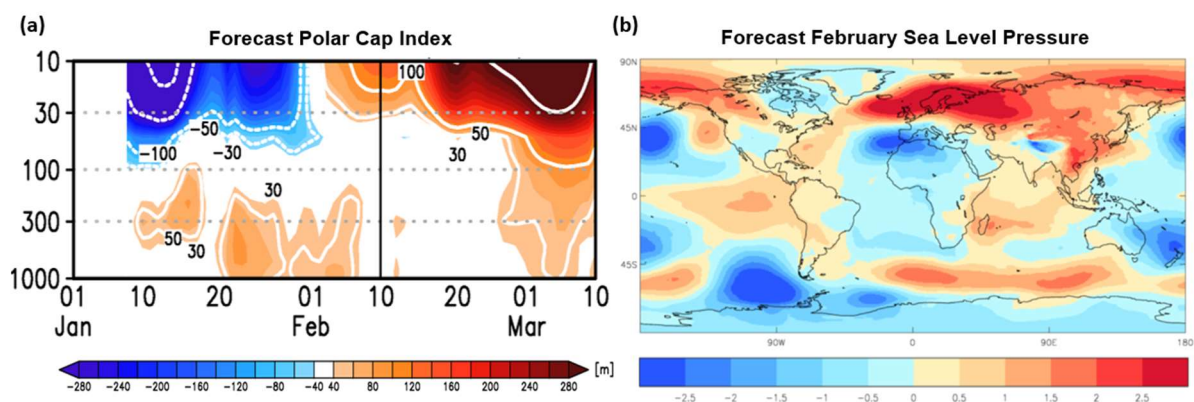
149 Predictability of the atmosphere at monthly lead times is also known to originate in part from the
150 Madden Julian Oscillation (MJO) in the troposphere and its teleconnection to the extratropics (e.g.
151 Vitart 2017). The circulation pattern associated with the MJO resembles a poleward and eastward
152 propagating Rossby wave with centres of action over the Pacific and extending into the Atlantic sector
153 where it also maps strongly onto the North Atlantic Oscillation. The lead time of around 10 days for the
154 impact of a change in the MJO to appear in the extratropical flow (e.g. Cassou 2008; Lin et al., 2009)
155 is also consistent with the timescale for poleward propagation of Rossby waves (e.g. Scaife et al., 2017).
156 It turns out that this tropospheric MJO teleconnection on monthly timescales also interacts with the
157 stratosphere (Garfinkel and Schwartz 2017). The MJO teleconnection to the North Pacific affects the
158 region most strongly associated with tropospheric precursors to SSW events, and consistent with this,
159 SSWs in the observational record have tended to follow certain MJO phases. The subsequent weak
160 vortex anomaly then propagates down to the troposphere (Garfinkel et al 2012), where it may strengthen
161 and prolong any existing negative NAO signal that is directly linked to the MJO via the troposphere
162 (Schwartz and Garfinkel 2017, 2020; Barnes et al., 2019).

163 In addition to the interaction of the MJO with the extratropical stratosphere, a further, completely
164 different link between the stratosphere and the MJO has recently been uncovered which modulates MJO
165 amplitude and persistence in the troposphere via the phase of the Quasi-Biennial Oscillation (QBO) in
166 the tropical lower stratosphere (Liu et al., 2014; Yoo and Son 2016; Martin et al., 2021). In this case,
167 easterly phases of the QBO appear to energise the MJO compared to westerly QBO phases, likely due

168 to changes in temperature and hence static stability close to the tropopause (Hendon and Abhik 2018;
 169 Martin et al., 2019) with a potential contribution of cloud-radiation feedbacks (Son et al., 2017, see
 170 Martin et al., 2021 for a review). This modulation of the MJO is in turn important for predictability as
 171 it gives rise to higher monthly prediction skill of the MJO and its surface teleconnections during the
 172 easterly phase of the QBO (Marshall et al., 2017; Abhik and Hendon 2019; Y. Lim et al., 2019).

173 The traditional view of stratosphere-troposphere interaction involves upward propagation of planetary
 174 scale Rossby waves (Charney and Drazin 1961), but this linear theory applies equally well to downward
 175 propagation. Harnik and Lindzen (2001) and Perlwitz and Harnik (2003) identified a possible source of
 176 downward propagating planetary waves in the form of reflecting surfaces in the winter stratosphere.
 177 Examples of specific reflection events, showing upwards and then downward propagation have since
 178 been observed (e.g. Kodera et al., 2008; Harnik 2009; Kodera and Mukougawa 2017; Mukougawa et
 179 al., 2017; Matthias and Kretschmer 2020). These results suggest that the details of the stratospheric
 180 circulation such as regions of negative vertical wind shear could be important for the formation of
 181 reflecting conditions (Perlwitz and Shaw 2013) and may yet provide a further mechanism by which the
 182 stratosphere can affect the troposphere (Domeisen et al., 2019; Butler et al., 2019).

183 Following studies demonstrating enhanced tropospheric predictability after SSW events in individual
 184 climate models (e.g. Kuroda 2008; Mukougawa et al 2009; Marshall and Scaife 2010; Sigmond et al.
 185 2013), subseasonal forecast systems which explicitly represent the stratosphere in the climate system
 186 were developed and implemented at operational prediction centres worldwide. It is often difficult to
 187 demonstrate significant increases in overall skill (e.g. Richter et al. 2020a) but routinely produced
 188 ensembles of subseasonal predictions show that both stratospheric variability and its subsequent
 189 tropospheric signature are predictable at monthly lead times (Domeisen et al. 2020a, 2020b). The
 190 strongest surface impacts occur if the polar vortex in the lower stratosphere is in a weakened state at
 191 the time of the SSW (Karpechko et al., 2017) and there appears to be a roughly linear relationship
 192 between the strength of these lower stratospheric anomalies and the tropospheric response (e.g. Runde
 193 et al. 2016; White et al. 2020 and see Baldwin et al. 2019 for a review). We should note however that
 194 there is no one-to-one correspondence between stratospheric variability and tropospheric events, and
 195 some prominent examples of sudden stratospheric warmings are followed by differing tropospheric
 196 anomalies (e.g. Charlton-Perez et al., 2018; Knight et al., 2020; Butler et al., 2020; Rao et al., 2020a).
 197 Nevertheless, the canonical response is seen in the majority (~70%) of cases and periods of intense
 198 wintertime stratospheric variability are important windows of opportunity to provide skilful monthly
 199 forecasts (Mariotti et al., 2020; Tripathi et al., 2015a).



200 **Figure 2: Monthly forecasts prior to the 2018 sudden stratospheric warming and severe cold event over**
 201 **northern Europe. Forecast Polar Cap Index (a) and February sea level pressure anomalies (b). Ensemble**
 202 **mean anomalies are shown for the average of forecasts initialised between 8th and 22nd of January 2018**
 203 **relative to hindcasts over the 1993-2016 period using the Met Office Hadley Centre GloSea prediction**
 204 **system (MacLachlan et al., 2015). Sea level pressure is measured in hPa and Polar Cap Index is the**
 205 **geopotential height anomaly (m) averaged over 65N to the North Pole.**

206 These forecast systems are now important tools for national meteorological and hydrological services
207 to monitor impending stratospheric variability and associated surface impacts in real time. Recent
208 extreme examples illustrate the importance of this activity. In February 2018 a major SSW occurred
209 and was followed by a strong negative NAO-like pattern at the surface with easterly wind anomalies
210 over Europe and multiple cold air outbreaks over the following weeks, including extreme snowfall
211 across northern Europe (Figure 2, Karpechko et al., 2018; Knight et al., 2020; Rao et al., 2020a) and an
212 abrupt end to Iberian drought in Southern Europe (Ayarzagueña et al., 2018). Studies of monthly
213 ensemble predictions of this event with operational stratosphere resolving systems showed that the
214 stratospheric event was predictable at least 2 weeks in advance (Figure 2) and that the ensemble
215 forecasts indicated increased likelihood of cold surface conditions for several weeks after the event
216 (Karpechko 2018; Butler et al., 2020; Statnaia et al., 2020; Rao et al., 2020a). Again, as in the analysis
217 of previous events, there was also a strong association with the MJO entering Phase 7 with increased
218 convection in the West Pacific (cf. Garfinkel and Schwartz 2017) in the 2018 event. Finally, we should
219 also note that cases of monthly forecasts where the stratosphere plays an important role are not restricted
220 to winters with sudden stratospheric warmings and periods when the stratospheric polar vortex is above
221 normal strength also provide opportunities for skilful monthly forecasts (Tripathi et al., 2015b; Scaife
222 et al., 2016). In this case an opposite but symmetric surface response results, with strong *positive* NAO.
223 A very recent example occurred in February 2020, when, following an extremely strong polar vortex
224 (Hardiman et al., 2020b; Lee et al., 2020b; Lawrence et al., 2020; Rao et al., 2021a), the tropospheric
225 jet in the Atlantic sector strengthened, and the associated increased storminess and rainfall in this case
226 resulted in UK monthly rainfall reaching a new record high (Davies et al., 2021).

227

228 **3 The stratosphere and seasonal prediction**

229

230 Prior to the advent of dynamical forecast systems which explicitly represent the stratosphere, seasonal
231 forecasts using empirical relationships and statistical methods were proposed. These relied on the prior
232 state of the polar vortex and other predictable factors such as the QBO that are known to have links to
233 surface climate (Thompson et al., 2002; Charlton et al., 2003; Christiansen et al., 2005; Boer and
234 Hamilton 2008). In some cases they indicated additional predictability that was absent in existing
235 operational forecast systems, providing further evidence of predictability involving the stratosphere and
236 further motivating the extension of dynamical forecast systems to properly represent the stratosphere.
237 Similar empirical forecast studies continue, and although they cannot provide evidence of predictability
238 that is as strong as from GCM experiments based on fundamental physical principles, they do continue
239 to be useful to indicate sources of predictability that need to be properly represented in comprehensive
240 forecast systems (e.g. Folland et al., 2012; Wang et al., 2017; Hall et al., 2017; Byrne and Shepherd
241 2018).

242 Following the introduction of dynamical seasonal forecast systems with a good representation of the
243 stratosphere, clear links between successful seasonal prediction of the North Atlantic Oscillation, the
244 closely related Arctic Oscillation and the state of the stratospheric polar vortex have been identified in
245 forecast output (e.g. Scaife et al., 2014b; Stockdale et al., 2015; Jia et al., 2017). Similar signals are also
246 seen in the southern hemisphere in relation to predictability of the Southern Annular Mode (Seviour et
247 al., 2014; Byrne et al., 2019; Lim et al., 2021). Statistically significant increases in overall skill directly
248 attributable to the inclusion of the stratosphere in prediction systems is sometimes difficult to
249 demonstrate (e.g. Butler et al., 2016), especially given that other factors such as horizontal resolution
250 and physical parametrizations are often simultaneously changed. Nevertheless, the body of evidence
251 now weighs heavily in favour of predictability of the NAO and SAM from the stratospheric polar vortex
252 and from analyses showing reduced surface prediction skill in the absence of stratospheric variability
253 (e.g. Hardiman et al 2011; Sigmund et al., 2013; Scaife et al., 2016).

254 A second clear example of seasonal predictability originating in the stratosphere is the Quasi-Biennial
255 Oscillation (QBO). The QBO has such inherently long timescales that it persists for several months in
256 seasonal forecasts from initial atmospheric conditions alone and its regularity means that it can be
257 predicted from simple composites of earlier cycles. Nevertheless, a growing number of numerical
258 models used in seasonal forecast systems can now simulate and predict the oscillation within climate
259 forecasts (Garfinkel et al., 2018; Richter et al., 2020b; Stockdale et al., 2021) with the aid of forcing
260 from parametrized non-orographic gravity waves, and there is skill in predicting QBO phase changes
261 at lead times of a few months (e.g. Pohlman et al., 2013, Scaife et al., 2014a). The surface impact of the
262 QBO is also well established and has stood the test of time since it was first identified in the 1970s
263 (Ebdon 1975; Thompson et al., 2002; Anstey and Shepherd 2014; Gray et al 2018). Yet again this
264 response projects closely onto the North Atlantic Oscillation (and hence the Arctic Oscillation/Northern
265 Annular Mode) and the Southern Annular Mode. The favoured mechanism involves refraction of
266 vertically propagating Rossby waves in the lower stratosphere (Holton and Tan 1980), although other
267 pathways may also be involved (e.g. Inoue et al., 2011; Yamazaki et al., 2020; Rao et al., 2020b, 2021b).
268 The observed magnitude of the QBO teleconnection is also large enough to provide seasonal
269 predictability of surface climate (Boer and Hamilton 2008) but its modelled amplitude at the surface
270 appears to be under-represented in current operational prediction systems and models (Scaife et al.,
271 2014b; Garfinkel et al. 2018; O'Reilly et al. 2019; Rao et al. 2020b; Anstey et al. 2021).

272 In addition to the stratosphere acting as a source of predictability, other mechanisms by which the
273 stratosphere plays a role in seasonal predictions involve a pathway for global scale teleconnections.
274 These often originate in the tropics where the longer timescales of coupled ocean-atmosphere variability
275 such as the El Niño Southern Oscillation (ENSO, L'Heureux et al. 2020) provide a predictable source
276 of low frequency variability. Effects on the extratropics can occur by tropical excitation of anomalous
277 Rossby waves which propagate polewards but also upwards into the stratosphere, as in the case of
278 ENSO (Manzini et al., 2006; Domeisen et al., 2019), giving two pathways for extratropical influence
279 (Butler et al., 2014; Kretschmer et al., 2021). These highly predictable tropical sources of climate
280 variability alter the strength and position of the stratospheric polar vortex in the extratropics as well as
281 the frequency of SSWs (Polvani et al., 2017) and these are followed by changes in the seasonal westerly
282 jets in the troposphere and surface climate via the North Atlantic Oscillation (Ineson and Scaife 2009;
283 Cagnazzo and Manzini 2009) or the Southern Annular Mode (Byrne et al., 2019). As might be expected,
284 both the QBO and ENSO teleconnections are best represented in seasonal forecast systems which
285 contain a well resolved stratosphere (Butler et al., 2016). We note that new examples of the stratosphere
286 acting as a conduit for seasonal teleconnections are still being uncovered (Hurwitz et al., 2012, Woo et
287 al., 2015). For example, the Indian Ocean Dipole (IOD) received little attention in this context until the
288 recent record event of late 2019, when it appears to have driven an extreme winter strengthening of the
289 northern hemisphere stratospheric polar vortex. This strengthening took many weeks to decay, giving
290 rise to extreme yet highly predictable conditions in the stratosphere and around the Atlantic sector in
291 late boreal winter (Hardiman et al., 2020b; Lee et al., 2020b). The same event was also implicated in
292 extreme changes in the polar vortex and the near SSW in the southern hemisphere (Rao et al., 2020e);
293 an event that itself likely helped to drive the extreme summer conditions and wildfires over Australia
294 that year (Lim et al., 2021).

295 Apparent links between Arctic sea ice and seasonal winter climate in the mid latitudes have also been
296 suggested to be mediated by the stratosphere, with increased Rossby wave activity and a weakening of
297 the stratospheric polar vortex in response to reduced sea ice, especially in the Barents-Kara Sea (Jaiser
298 et al., 2013; Kim et al. 2014; King et al., 2016; Kretschmer et al., 2016). Some studies also reproduced
299 surface signals in response to sea ice anomalies in seasonal forecasts of particular years that are in
300 apparent agreement with observational estimates (e.g. Balmaseda et al., 2010; Orsolini et al., 2012).
301 However, recent updates to observational records show a weakening of these apparent effects
302 (Blackport and Screen 2020) and significant non-stationarity (Kolstad and Screen 2019). Subsequent
303 modelling studies with larger samples of simulations have provided mixed results (Zhang et al 2018;

304 Dai and Song 2020; Smith et al 2021), and some have argued that the atmospheric response to sea ice
305 is weak and that while the sensitivity to Barents-Kara sea ice may be stronger, the stratospheric response
306 in particular is highly variable (McKenna et al. 2017). While there may well be a longer-term effect via
307 the stratosphere from sea ice decline (Sun et al., 2015; Screen and Blackport 2019; Kretschmer et al.,
308 2020), sensitivity of the response to the background state complicates the issue (Labe et al., 2019; Smith
309 et al. 2017), as do possible confounding influences from the tropics (Warner et al. 2020) and to date
310 there is no clear consensus for strong enough year-to-year effects to provide significant seasonal
311 predictability.

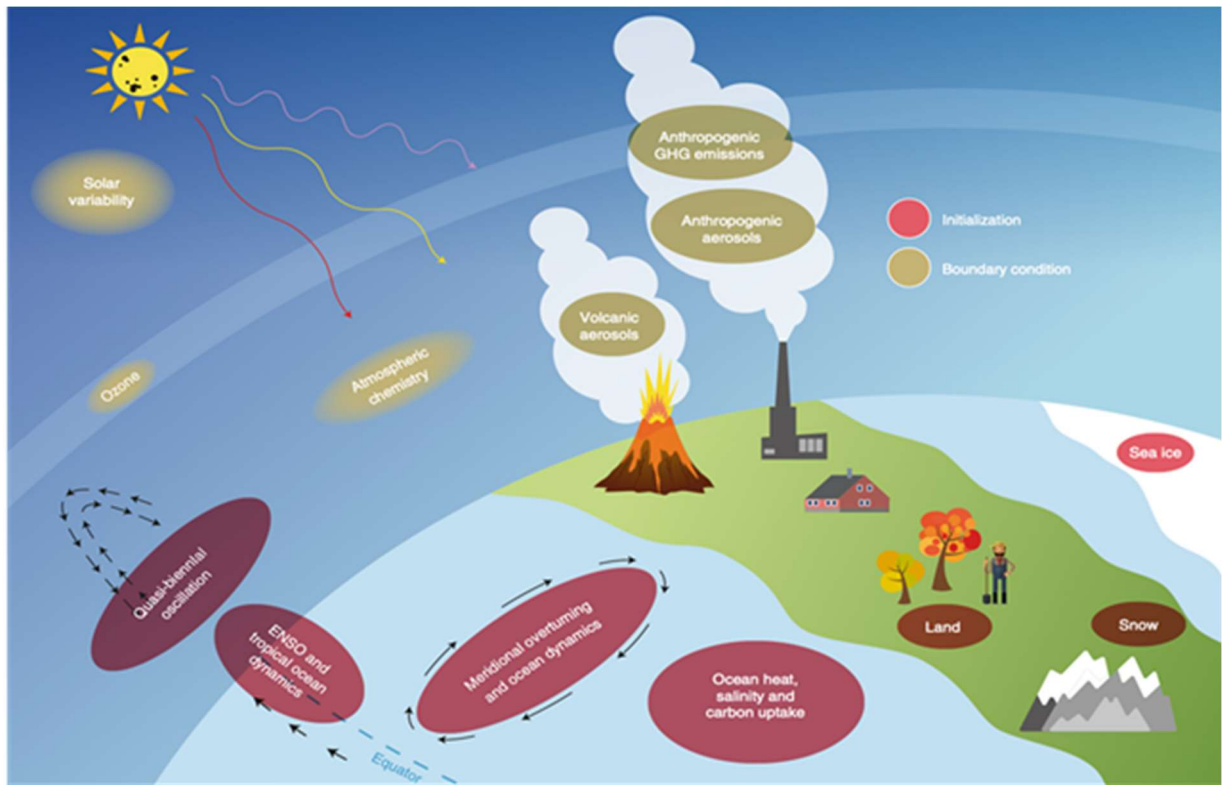
312 Other proposed teleconnections acting via the stratosphere have been found in observations but remain
313 to be confirmed with successful reproduction in physically based climate models. A prominent example
314 involves a proposed link between Eurasian snow amounts and the stratosphere, followed by a return
315 influence on the NAO and surface climate. In this case, enhanced snow cover or depth is associated
316 with high pressure over north Eurasia, an increase in the flux of Rossby wave activity into the
317 stratosphere and a subsequent weakening of the stratospheric polar vortex, followed by the expected
318 negative shift in the NAO and AO (Cohen and Entekhabi 1999, Cohen and Jones 2011; Cohen et al.,
319 2014; Furtado et al., 2015). However, the strength of this link in climate models and seasonal predictions
320 is modest (Fletcher et al., 2009; Riddle et al., 2013; Tyrrell et al., 2018, 2019) and does not agree with
321 apparent links to the AO in observations (Kretschmer et al., 2016; Garfinkel et al., 2020) even when
322 model mean state biases are corrected (Tyrrell et al., 2020). It has also been suggested that
323 teleconnections to snow are non-stationary or non-causal and there is continued debate about its long-
324 term robustness (Peings et al., 2013; Henderson et al., 2018).

325 In summary, a number of mechanisms by which the stratosphere acts to provide seasonal predictability
326 either by acting directly as a source of predictable variability (e.g. the QBO, SSWs), or as a conduit for
327 teleconnections (e.g. ENSO, MJO, IOD) have now been established in observations and have been
328 confirmed using climate model simulations based on first principles. These operate in seasonal forecast
329 systems, albeit with remaining errors such as the weakness of the QBO connection to surface climate.
330 Meanwhile, other mechanisms involving the stratosphere (for example the response to snow cover
331 variations) have been proposed based on apparent observed relationships, but until we have agreement
332 between these observations and theory (model simulations), scientists remain sceptical of whether they
333 represent actual sources of seasonal predictability and these remain topics of current research.

334

335 **4 The stratosphere and annual to decadal prediction**

336 In recent years, initialised predictions on longer timescales were developed on the premise of multiyear
337 memory in the ocean (e.g. Smith et al 2007), and following the development pathway mapped out by
338 seasonal forecasts in the past, these are now being run operationally to produce real time multi-model
339 forecasts (Smith et al., 2013). Kushnir et al. (2019) mapped out this operational development of annual
340 to decadal predictions and highlighted a number of sources of predictability, some of which involve the
341 stratosphere (Figure 3), but not all of which are fully represented in climate prediction systems.



342

343 **Figure 3. Sources of annual to decadal predictability, some of which involve the stratosphere through the**
 344 **response to external forcing, internal atmospheric dynamics, or ozone chemistry changes. After Kushnir et**
 345 **al., 2019.**

346 Despite common misconceptions, not all annual to decadal predictability stems from the ocean. Indeed,
 347 it has been clearly demonstrated that multiyear predictability of the QBO exists in current decadal
 348 predictions systems out to lead times of several years (Pohlman et al., 2013; Scaife et al., 2014a). This
 349 offers the prospect of a stratospheric contribution to multiyear predictability of the extratropics through
 350 the teleconnection with the Arctic Oscillation (Anstey and Shepherd 2014, Gray et al., 2018) and to
 351 tropical predictability through links to the MJO (e.g. Martin et al., 2021) and wider tropical climate
 352 variability (Haynes et al., 2021).

353 Although it is more important on multidecadal timescales (see below), external forcing of the
 354 stratosphere can also act as a source of decadal predictability. Forced climate signals from changes in
 355 greenhouse gases or stratospheric effects such as ozone depletion occur on a much longer timescale
 356 than the lead time of decadal forecasts but their contribution to the skill of predictions is not trivial. For
 357 example, it is not immediately obvious whether the slow changes from multidecadal forced signals
 358 would simply be swamped by unpredictable internal variability on decadal timescales, rendering long
 359 term external forcing changes useless for decadal predictions. However, this is not the case and long-
 360 term forcing is now known to be an important source of decadal prediction skill (Smith et al., 2019,
 361 2020).

362 External forcing involving the stratosphere on shorter timescales is also important for annual to decadal
 363 predictions. The stratosphere has long been known to be influenced by volcanic eruptions, particularly
 364 in the case of tropical volcanic eruptions which are powerful enough to inject significant quantities of
 365 sulphur dioxide into the atmosphere. Here it reacts with water to form sulphuric acid and persists in
 366 aerosol form, leading to predictable multiyear global surface cooling, tropical stratospheric warming
 367 and an intensification of the westerly stratospheric polar vortex in the extratropics (Robock and Mao
 368 1992). Although the sample of observed events is limited, modelling studies have reproduced an
 369 observed post-eruption intensification of the westerly winds in the stratosphere and some impacts on

370 the surface Arctic Oscillation. However, generations of models have struggled to reproduce the two-
371 year persistence of volcanic effects seen in observations and the observed magnitude of the effect on
372 the winter AO (e.g. Stenchikov et al., 2006; Marshall et al., 2009; Charlton-Perez et al., 2013, Bittner
373 et al., 2016). In addition to these changes in the atmosphere, the intensification of stratospheric
374 westerlies and hence Arctic Oscillation also combines with surface cooling of the ocean to generate
375 predictable changes in the Atlantic meridional overturning circulation (Reichler et al., 2012) which can
376 extend the volcanic influence to decadal timescales (Swingedouw et al., 2015). Finally, although the
377 mechanism is debated, there is also evidence of a multiyear effect of tropical volcanic eruptions on
378 ENSO, presumably requiring the persistent radiative forcing that arises through the long residence time
379 of volcanic products, particularly sulphate aerosols, in the stratosphere. This reportedly increases the
380 frequency of El Nino events by a factor of two in the years following volcanic eruptions (Adams et al.,
381 2003), again suggesting an important source of multiannual predictability via the stratosphere.

382 A second source of multiannual predictability from external forcing originates from solar variability
383 and in particular the 11-year solar activity cycle. Although a number of alternative mechanisms have
384 been proposed (see Gray et al., 2010 for a review), the established mechanism for surface effects via
385 the stratosphere is the change in the polar vortex that results from changes in upper stratospheric heating
386 over the course of each cycle between solar minimum and solar maximum. Atmospheric wave-mean
387 flow interactions amplify the initial radiatively driven change and drive its descent to the troposphere
388 (Kodera and Kuroda 2002; Marsh et al 2007; Ineson et al., 2011; Givon et al., 2021), where changes in
389 the extratropical jets result in a negative (positive) Arctic Oscillation pattern following solar minimum
390 (maximum). There is also evidence that it contributes to interannual prediction skill (Dunstone et al.,
391 2016) and an interesting aspect that has emerged in recent years is the integrating effect of the ocean on
392 solar induced changes in the NAO via interannual persistence of ocean heat content anomalies which
393 leads to a lag of around 3 years ($\pi/2$ cycles) in the peak response, as would be expected if the ocean is
394 integrating the effects of a periodic solar forcing (Scaife et al., 2013; Gray et al., 2013; Andrews et al.,
395 2015; Thiéblemont et al., 2015). However, debate continues as to whether the solar signal is indeed
396 large enough to be detectable in observations in the presence of large internal tropospheric variability
397 (Chiodo et al., 2019).

398 Perhaps the longest known timescale for predictability from initial conditions, which also involves the
399 stratosphere, is the interaction of Atlantic Multidecadal Variability (AMV) with the stratospheric
400 circulation. The Atlantic has followed pronounced multidecadal variations over the last century (Mann
401 et al., 1995) and these variations are predictable out to years ahead (Hermanson et al., 2014). Some
402 studies link these variations to the stratosphere and the NAO/AO (Reichler et al., 2012; Omrani et al.,
403 2014). Indeed, the pronounced multidecadal increase in the surface NAO between the 1960s and 1990s
404 is strongly coupled to changes in the strength of the stratospheric polar night jet (Scaife et al., 2005).
405 Although current models simulate weak coupling between the AMV and the free atmosphere, this
406 coupling appears to increase with model resolution (Lai et al., 2021) suggesting that the links between
407 AMV, the stratosphere and the NAO offer potential for improved decadal scale prediction involving
408 the stratosphere.

409 The currently recognised role of the stratosphere in decadal forecasts of surface climate again appears
410 mainly via the impact on annular modes and, in the northern hemisphere, the North Atlantic Oscillation.
411 Indeed, while current decadal prediction systems are now able to produce skilful predictions of
412 variations in the NAO on multiyear lead times (Smith et al., 2019, 2020; Athanassiadis et al., 2020),
413 much work is still needed to attribute these variations to external forcing or internal variability and to
414 understand the interaction between boundary and initial conditions which blurs the simple distinction
415 between the two. These new results are important because they indicate new-found decadal
416 predictability of events like the high NAO of the 1990s which yielded a run of mild but wet and stormy
417 winters in northern Europe and the eastern USA. These winters are well known to have caused
418 significant impact for example on the insurance sector (Leckebusch et al., 2007) and coincided with the

419 longest observed absence of SSW events (Pawson and Naujokat 1999; Domeisen 2019). Given the
420 indications of coupled stratosphere-troposphere variations on decadal timescales (Scaife et al., 2005;
421 Omrani et al., 2014; Garfinkel et al., 2017; Woo et al., 2015), understanding the role of the stratosphere
422 in extratropical decadal predictions needs further investigation.

423

424 **5 The stratosphere and multidecadal projection**

425 The importance of the stratosphere for climate projections on multidecadal timescales was generally
426 recognised before its role in predictions on shorter timescales. This is in part a legacy of the early
427 development of stratosphere-troposphere models for ozone depletion studies described in the
428 introduction. On these longer timescales, coupling between stratospheric composition, thermal structure
429 and atmospheric circulation gives rise to improved climate projections.

430 Perhaps the best-known case for the stratosphere affecting multidecadal projections of surface climate
431 is the influence of ozone depletion on the southern annular mode (SAM; Thompson and Solomon 2002,
432 2005; McLandress et al., 2011; Polvani et al., 2011; Son et al., 2018) where decreasing ozone in the late
433 20th century led to a strengthened pole-to-equator temperature gradient, a stronger stratospheric polar
434 vortex and a shift to strong positive SAM phases at the surface. In this case, studies again show the
435 importance of stratospheric resolution to generate the full response, consistent with a genuine downward
436 influence (Karpechko et al., 2008). The associated poleward shift in the tropospheric jet is connected to
437 a delay in the spring breakdown of the stratospheric polar vortex (Byrne et al., 2017) and delivered
438 significant and prolonged changes in rainfall across many regions of the southern hemisphere (Kang et
439 al., 2011; Purich and Son 2012). Implementation of the Montreal Protocol in 1987 and subsequent
440 reductions in the rate of ozone depletion mean that recovery of the ozone layer is now expected over
441 the coming decades and the reversible effects of this on the surface climate form an important element
442 of current multidecadal projections (Thompson et al., 2011; Previdi and Polvani 2014; Solomon et al.,
443 2016; Banarjee et al., 2020, Zambri et al., 2021) where they are expected to play an important role
444 alongside other changes in the southern stratosphere due to continuing increases in greenhouse gases
445 (Son et al., 2009; Barnes et al., 2012), some of which occur via the stratospheric polar vortex in a similar
446 way to those from ozone depletion and recovery (Ceppi and Shepherd, 2019).

447 The more limited effects of ozone depletion in the northern hemisphere meant that the role of the
448 stratosphere in multidecadal projections took longer to become established. Some early studies found
449 potential amplification of positive Arctic Oscillation trends under climate change when the stratosphere
450 was included (Shindell et al., 2001). However, this was not borne out in later studies as simulations
451 with other fully coupled ocean-troposphere-stratosphere models suggested weakening of the
452 stratospheric polar vortex (e.g. Huebener et al., 2007). Subsequent studies with multiple models also
453 indicated a southward shift in the polar night jet with weakening high latitude winds and strengthening
454 subtropical winds (Scaife et al., 2012; Manzini et al., 2014). These changes result from increased
455 atmospheric wave driving of the winds which can overwhelm the cooling effect of greenhouse gases
456 (Karpechko and Manzini 2012) and can lead to important differences in future surface climate, for
457 example in regional rainfall in areas typically affected by the stratosphere via the Arctic Oscillation and
458 NAO (Scaife et al., 2012). There is still significant uncertainty due to the diversity of modelled
459 stratospheric responses to greenhouse gas increases (Manzini et al., 2014, Simpson et al., 2018, Zappa
460 and Shepherd 2017), and it has proved difficult to identify any clear change in the frequency of sudden
461 stratospheric warmings (Ayarzagüena et al., 2018, 2020; Rao et al., 2020c). This is perhaps due to the
462 competition between strengthening latitudinal temperature gradients near the tropopause and enhanced
463 meridional overturning in the mid stratosphere. There is also strong inherent unpredictable variability
464 from decade to decade in the frequency of SSW occurrence (Butchart et al., 2000; McLandress and
465 Shepherd 2009).

466 Other aspects of future climate change where the stratosphere plays a role have also been identified, for
467 example, in the debate over the response to future levels of Arctic sea ice. In this case it seems that the
468 response of the mid-latitude circulation involves a negative shift in the Arctic Oscillation (Screen et al.,
469 2018; Zappa et al., 2018; McKenna et al., 2018). This could again be amplified by interaction with the
470 stratosphere as some studies suggest that the stratospheric response is necessary for a large surface
471 response (Kim et al., 2014), while others highlight that the stratospheric interaction is sensitive to the
472 regional pattern of sea ice decline (McKenna et al., 2018), and still others show evidence of non-linear
473 stratospheric, and stratosphere-mediated surface response (Manzini et al., 2018), coincident with the
474 time when the Barents and Kara seas become ice-free (Kretschmer et al., 2020). Furthermore, studies
475 also indicate that the surface climate response to sea ice decline depends systematically on the phase of
476 the stratospheric QBO (Labe et al., 2019).

477 Although it is much less certain than anthropogenic climate change, there have also been suggestions
478 of a multidecadal decline of external solar irradiance which can impact multidecadal climate projections
479 via the stratosphere. Previous multidecadal solar minima, so called ‘grand minima’, have occurred in
480 sunspot records and have been connected to the Little Ice Age period around the end of the 17th century
481 using proxy and other data (Owens et al., 2017). Given recent weak amplitude 11 year solar cycles,
482 there are now suggestions of a future solar ‘grand minimum’ where the 11 year cycle described above
483 could become muted or even absent for a prolonged period (Lockwood et al., 2010). In this case, the
484 upper stratospheric cooling in the tropics and summer hemisphere can change the meridional
485 temperature gradient in a similar fashion to the 11 year cycle (Maycock et al., 2015) and leads to a
486 negative shift in the AO and the NAO, and hence affects regional climate (Ineson et al., 2015). However,
487 in this case it appears that while regional changes could be significant, they are generally much smaller
488 than the surface warming due to anticipated levels of anthropogenic greenhouse gases (Anet et al., 2013;
489 Ineson et al., 2015; Maycock et al., 2015).

490 Finally, we note that although low frequency variability in teleconnections is observed (e.g. Garfinkel
491 et al., 2019), it is often unclear whether this is a systematic variation or simply due to sampling
492 variability of an underlying stationary process (Jain et al., 2018). Nevertheless, there is growing
493 evidence for systematic climate change in some of the teleconnections by which the stratosphere enables
494 surface predictability. Under future climate change it appears that some of the teleconnections discussed
495 above may *strengthen* in amplitude. For example, the strength of ENSO induced anomalies in the
496 extratropical Atlantic/European sector increases in future climate projections (Müller and Roeckner
497 2006; Fereday et al., 2020). Similarly, recent analyses suggest that the MJO teleconnection to the
498 extratropics increases in amplitude under climate change (Samarasinghe et al., 2020). The same is also
499 true of the extratropical effects of the stratospheric QBO, where in this case, the amplitude of the
500 teleconnection in composite anomalies doubles under future climate change (Rao et al., 2020d) despite
501 the QBO itself becoming weaker (Richter et al., 2020c).

502

503 **6 Outlook**

504 Long range prediction has evolved quickly in recent years (Merryfield et al., 2017; 2020, Butler et al.,
505 2019; Meehl et al., 2021) and this rapid development is due in part to the improved representation of
506 stratospheric processes and stratospheric initial conditions in ensemble prediction systems. The long-
507 range forecast community originally focused on predictability from initial ocean conditions and this
508 remains the primary source of long-range predictability, for example from ENSO, but some of these
509 long-range prediction systems contained poor representations of the stratosphere. In the meantime,
510 those working in parallel on climate modelling of the stratosphere were rarely involved in initialised
511 long-range prediction, instead being driven primarily by the ozone depletion problem. Knowledge
512 exchange across fields is important in science and precursors to a new paradigm often occur when a
513 topic is investigated by researchers from outside the field (Kuhn 1970). The crossover and collaboration

514 between long range prediction and stratospheric research communities is no exception and the
515 interaction between these communities has yielded rapid progress and new insights. Examples where
516 initial atmospheric conditions can provide predictability beyond the usually assumed limit have been
517 demonstrated, particularly for the extratropics but also for the tropics, and we now know that in some
518 situations, for example when sudden stratospheric warmings occur, the initial conditions in the
519 stratosphere can have more impact than initial conditions in the ocean (Thompson et al 2002; Scaife
520 and Knight 2008; Polvani et al 2017). This suggests that initial atmospheric conditions in the
521 stratosphere are likely to be more important for long range forecasts than previously assumed
522 (Mukougawa et al., 2005, 2009; Stockdale et al., 2015; Noguchi et al., 2016, 2020a; Choi and Son 2019;
523 O'Reilly et al., 2019; Nie et al., 2019), not least because the overturning and breaking of Rossby waves
524 in the stratosphere is followed by long lived atmospheric anomalies due to synoptic scale eddy
525 feedbacks that prolong the effects in the troposphere (Kunz and Greatbatch 2013 Kang et al., 2011;
526 White et al., 2020). More research on the initial conditions in the stratosphere might therefore help to
527 reveal potential for further improvements in prediction skill.

528 A notable simplification to understanding the role of the stratosphere, at least in extratropical long-
529 range predictions, is its apparently seamless mechanism across different timescales and different
530 phenomena. Following the early ground-breaking studies showing surface impacts of stratospheric
531 variability (e.g. Labitzke 1965, Boville 1984) and a multitude of studies on individual teleconnections
532 between the stratosphere and surface climate, the projection of stratospheric variability onto the Arctic
533 Oscillation/North Atlantic Oscillation/Annular Mode circulation patterns across timescales and
534 hemispheres is now well established (see the review by Kidston et al., 2015). This suggests that similar
535 coupling processes occur between the stratosphere and troposphere from months to decades and these
536 processes lead to some of the most intense extratropical climate extremes, in winter in the northern
537 hemisphere and in late spring/early summer in the southern hemisphere (Karpechko et al., 2018;
538 Fereday et al., 2012, Kautz et al., 2019; Domeisen and Butler 2020). While studies point to changes in
539 upper tropospheric baroclinicity and tropospheric eddy feedbacks as crucial in these teleconnections, a
540 full mechanistic understanding of how this occurs is still lacking.

541 Some, but not all, leading forecast systems now include a well resolved stratosphere with reasonable
542 representation of relevant processes such as the body force from sub-grid orographic and non-
543 orographic gravity waves. However, many outstanding problems remain. Although their number is
544 increasing, only a subset of current GCMs have the ability to simulate a realistic QBO beyond its decay
545 from initial conditions and it seems that all GCMs have problems with the fidelity of modelled QBO
546 teleconnections, which are either too weak or absent altogether (Scaife et al., 2014a; Kim et al., 2020;
547 Anstey et al., 2021). Even the relatively well studied ENSO teleconnection via the stratosphere to the
548 extratropics still has outstanding questions, such as whether the northern hemisphere stratosphere
549 exhibits more SSW events during the La Niña phase (Butler and Polvani 2011; Song and Son 2012).
550 This is not generally reproduced in modelling systems (Garfinkel et al., 2012) but occurred in the recent
551 La Niña winter of 2020/2021. Similarly, while the increased monthly predictability from the MJO
552 during the easterly phase of the QBO has been detected in monthly forecast experiments, the QBO-
553 MJO connection does not persist in longer predictions and simulations with current models (Kim et al.,
554 2020). Research and model development on stratosphere-troposphere interaction, including tropical
555 effects (Noguchi et al., 2020b), will no doubt lead to further progress in resolving this issue (Haynes et
556 al., 2021).

557 Errors in the modelled climatological mean climate are inevitably present to varying degrees in even
558 the latest climate models. The common protocol of running a set of retrospective predictions to allow
559 these mean biases to be estimated and hence subtracted from real time predictions may well correct for
560 much of this error. However, the degree to which biases have a nonlinear, state dependent impact on
561 the predictions is not fully understood. In some contexts, the nonlinear impacts of biases may be
562 minimal (Karpechko et al., 2021) while others show sensitivity (Sigmond et al., 2008, 2010) and

563 increases of prediction skill occur under certain background conditions, for example during Easterly
564 QBO phases (Taguchi 2018). Other processes generally omitted from long range predictions include
565 interactive variations of ozone and other trace gases. Although reports of impacts and benefits have
566 varied, it is thought that surface signals on interannual timescales come mainly from dynamical rather
567 than chemical changes (Seviour et al., 2014; Harari et al., 2019). Nevertheless, some studies suggest
568 detectable effects from interannual variability of ozone and it may be that ozone fluctuations could help
569 to amplify surface signals (Karpechko et al., 2014; Son et al., 2013; Smith and Polvani 2014; Oehrlein
570 et al., 2020; Hendon et al., 2020), providing a further area for future development. Given that the cost
571 of full atmospheric chemistry schemes remains computationally expensive, it seems likely that simple
572 parametrizations of ozone chemistry (e.g. Monge-Sanz et al., 2021) would be valuable in this context.

573 We end with a pointer to an issue that has now been found to affect long-range predictions from monthly
574 to seasonal to decadal and multidecadal timescales, particularly in the extratropics. So called ‘perfect
575 model studies’, which test the ability of models to predict their own ensemble members, are now known
576 to *underestimate* the true predictability of climate in some regions, particularly around the Atlantic
577 basin, and so models are better at predicting real world variations than they are at predicting themselves.
578 This so-called ‘Signal to Noise Paradox’ (Scaife and Smith 2018) is at first surprising, because perfect
579 model prediction scores are often assumed to represent an upper (rather than lower) limit for prediction
580 skill of the real world. The problem can be understood in terms of unrealistically weak ensemble mean
581 predictions (e.g. Eade et al., 2014) but whether the stratosphere is involved directly in the cause of this
582 problem remains to be seen (Saito et al., 2017; Stockdale et al., 2015), as it initially appears in the
583 troposphere rather than the stratosphere in long range forecasts (Domeisen et al., 2020a). Nevertheless,
584 the unrealistically weak amplitude of ensemble mean predictions may well have the same root cause as
585 the weaker than observed amplitude of modelled teleconnections to the stratosphere discussed in this
586 review, including, for example, the under-representation of the surface impact of the QBO. Resolving
587 this problem will therefore likely amplify these signals, provide greater levels of prediction skill, and
588 further strengthen the role of the stratosphere in long range predictions of surface climate.

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590 AAS wrote the draft manuscript. All other co-authors contributed relevant references and input to
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607

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