

1 Long Range Prediction and the Stratosphere

2

3 Adam A. Scaife^{1,2}, Mark P. Baldwin³, Amy H. Butler⁴, Andrew J. Charlton-Perez⁵, Daniela
4 I.V. Domeisen^{6,7}, Chaim I. Garfinkel⁸, Steven C. Hardiman¹, Peter Haynes⁹, Alexey Yu
5 Karpechko¹⁰, Eun-Pa Lim¹¹, Shunsuke Noguchi^{12,13}, Judith Perlwitz¹⁴, Lorenzo Polvani^{15,16},
6 Jadwiga H. Richter¹⁷, John Scinocca¹⁸, Michael Sigmond¹⁸, Theodore G. Shepherd⁵, Seok-
7 Woo Son¹⁹, and David W.J. Thompson²⁰.

8 ¹ Met Office Hadley Centre for Climate Prediction and Research, Exeter, U.K.

9 ² College of Engineering, Mathematics and Physical Sciences, Exeter University, Exeter, U.K.

10 ³ Department of Mathematics and Global Systems Institute, University of Exeter, Exeter, U.K.

11 ⁴ NOAA Chemical Sciences Laboratory (CSL), Boulder, CO, USA.

12 ⁵ Department of Meteorology, University of Reading, Reading, U.K.

13 ⁶ ETH Zurich, Zurich, Switzerland.

14 ⁷ University of Lausanne, Lausanne, Switzerland

15

16 ⁸ Fredy and Nadine Herrmann Institute of Earth Sciences, Hebrew University of Jerusalem,
17 Jerusalem, Israel

18 ⁹ Department of Applied Mathematics and Theoretical Physics, University of Cambridge, Cambridge,
19 UK

20 ¹⁰ Finnish Meteorological Institute, Helsinki, Finland

21 ¹¹ Bureau of Meteorology, Melbourne, Australia

22 ¹² Research Center for Environmental Modeling and Application, Japan Agency for Marine-Earth
23 Science and Technology (JAMSTEC), Yokohama, Japan

24 ¹³ Meteorological Research Institute, Japan Meteorological Agency, Tsukuba, Japan

25 ¹⁴ NOAA Physical Sciences Laboratory (PSL), Boulder, CO, USA

26 ¹⁵ Columbia University, Department of Applied Physics and Applied Mathematics, U.S.A.

27 ¹⁶ Department of Earth and Environmental Sciences, New York City, NY, U.S.A.

28 ¹⁷ Climate and Global Dynamics Laboratory, National Center for Atmospheric Research, Boulder,
29 Colorado, U.S.A.

30 ¹⁸ Canadian Centre for Climate Modelling and Analysis, Environment and Climate Change Canada,
31 Victoria, BC, Canada

32 ¹⁹ School of Earth and Environmental Sciences, Seoul National University, Seoul, Republic of Korea

33 ²⁰ Department of Atmospheric Science, Colorado State University, Fort Collins, Colorado, U.S.A.

34

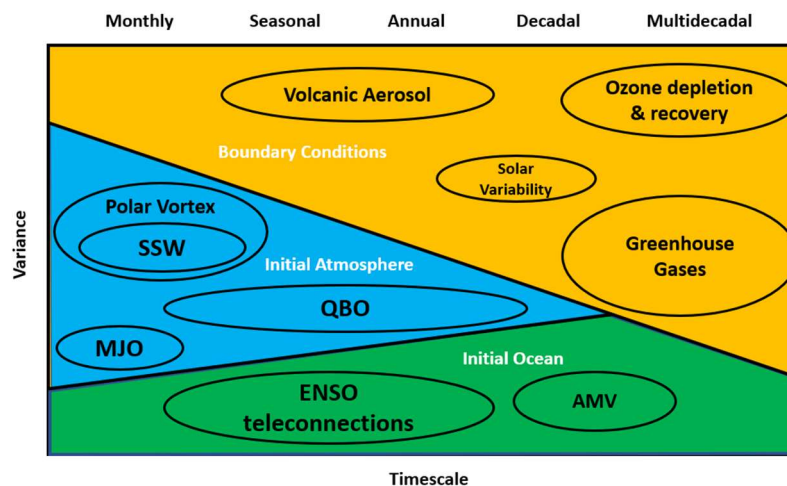
35 *Correspondence to:* Adam A. Scaife (adam.scaife@metoffice.gov.uk)

36 **Abstract.** Over recent years there have been concomitant advances in the development of stratosphere
 37 resolving numerical models, our understanding of stratosphere-troposphere interaction and the
 38 extension of long-range forecasts to explicitly include the stratosphere. These advances are now
 39 allowing new and improved capability in long range prediction. We present an overview of this
 40 development and show how the inclusion of the stratosphere in forecast systems aids monthly, seasonal,
 41 annual to decadal climate predictions and multidecadal projections. We end with an outlook towards
 42 the future and identify areas for improvement that could further benefit these rapidly evolving
 43 predictions.

44

45 **1 Introduction**

46 Daily weather fluctuations are thought to have a deterministic predictability horizon of around two
 47 weeks due to the sensitivity of the evolution of the atmospheric state to small errors in initial conditions
 48 (Lorenz 1969) - the so-called ‘butterfly effect’. Recent estimates (Leung et al., 2020; Domeisen et al.,
 49 2018) as well as tests of the predictability of midlatitude *daily* weather using the latest global prediction
 50 models (Zhang et al., 2019; Son et al., 2020) produce similar estimates for this predictability limit.
 51 However, this does not preclude skilful forecasts of the *statistics* (most notably the average) of
 52 conditions at long range beyond this timescale (e.g. Shukla 1981). This predictability owes its existence
 53 to slowly varying predictable components of the climate system in the ocean, and in some cases the
 54 atmosphere, as well as externally forced changes such as volcanic or solar variability effects (e.g.
 55 Kushnir et al., 2019). Some of the more prominent examples of stratospheric variability such as sudden
 56 stratospheric warmings and their subsequent impact on the stratosphere and the troposphere (Baldwin
 57 et al., 2021), or the quasi-biennial oscillation and its associated teleconnections (Scaife et al., 2014a),
 58 have been shown to be predictable out to timescales well beyond the traditional two-week predictability
 59 horizon from initial tropospheric conditions alone. Other examples involve stratospheric pathways for
 60 teleconnections originating in the troposphere or ocean (e.g., Schwartz and Garfinkel 2017, Byrne et al.
 61 2019) and are shown in Figure 1. On longer timescales, boundary forcing, for example from
 62 composition changes such as ozone depletion and recovery allows the stratosphere to provide relatively
 63 slowly varying conditions to guide the turbulent troposphere and hence provide long range
 64 predictability (e.g., Thompson et al. 2011). The relative importance of stratospheric initial conditions
 65 to boundary conditions decreases with lead time as shown in the schematic in Figure 1.



66 **Figure 1:** Schematic representation of the role of the stratosphere in long range prediction showing the
 67 transition from initial condition predictability in the atmosphere (blue) and the ocean (green), to boundary
 68 condition predictability at longer timescales (orange). Individual mechanisms involving the stratosphere
 69 are labelled in black. The width of the ellipses in the timescale direction shows the approximate range over
 70 which each phenomenon provides predictability. The width of the ellipses in the variance direction
 71 showing their approximate relative contributions to forecast variance at different lead times.

72 The extension of long-range prediction systems to explicitly include representation of the stratosphere
73 follows many years of development of stratosphere resolving general circulation models (GCMs). By
74 the late 20th century many leading centres for climate research had started to include the stratosphere in
75 versions of their GCMs (Pawson et al., 2000; Gerber et al., 2012). Much of the early model development
76 was motivated by the discovery of the ozone hole in the 1980s (Farman et al., 1985) and the need for
77 simulations of ozone depletion and potential recovery of the ozone hole following the 1987 Montreal
78 Protocol, which required atmospheric models that represented both the atmospheric dynamics and
79 chemistry of stratospheric ozone depletion (Molina and Rowland 1974; Crutzen 1974). In most cases
80 this was achieved by adding further quasi-horizontal layers to the domain of existing climate models to
81 extend their representation of the atmosphere to the stratopause or beyond (e.g. Rind et al 1988; Beagley
82 et al., 1997; Swinbank et al., 1998; Sassi et al., 2002), while also incorporating key radiative (e.g. Fels
83 et al., 1985), chemical (e.g. Steil et al., 1998) and dynamical (e.g. Scaife et al., 2000) processes.

84 The early development of so called ‘high top’ climate models, which represent the whole depth of the
85 stratosphere, in general preceded the discovery of the main body of evidence that the variability of the
86 stratosphere is not only affected by, but also interacts with the lower atmosphere and surface climate.
87 Pioneering early studies suggested that the stratosphere might have direct effects on the troposphere
88 and surface climate (e.g. Labitzke 1965; Boville 1984; Koder et al., 1990, 1995; Haynes et al., 1991;
89 Perlwitz and Graf 1995). In subsequent years, as reliable observational records lengthened and large
90 enough samples of stratospheric variability were amassed it was unequivocally demonstrated that
91 stratospheric variability precedes important tropospheric changes in the extratropics (Baldwin and
92 Dunkerton 1999, 2001). There was debate about causality and whether the stratosphere really does
93 affect the atmosphere below (e.g. Plumb and Semeniuk 2003). However, experiments where the
94 stratosphere is perturbed in numerical models show changes in surface climate and reproduce similar
95 patterns of response at the surface to those found in real world observations (e.g. Polvani and Kushner
96 2002; Norton et al., 2003; Scaife et al., 2006; Joshi et al., 2006; Scaife and Knight 2008; Hitchcock and
97 Haynes 2016, White et al., 2020). These involve changes to planetary scale waves and also baroclinic
98 eddies in the troposphere that are consistent with changes in baroclinicity near the tropopause (Kushner
99 and Polvani 2004; Song and Robinson 2004; Wittman et al., 2004, 2007; Scaife et al., 2012; Domeisen
100 et al., 2013; Hitchcock and Simpson 2014; White et al., 2020). Importantly, as we discuss below, the
101 same mechanisms also appear to be at work across a broad range of timescales (Kidston et al., 2015).

102 In recent years, motivated by the evidence of surface effects of stratospheric variability in the mid-
103 latitudes, the high-top model configurations used for stratospheric research were incorporated into
104 leading prediction systems. Improved vertical resolution was already known to improve the atmospheric
105 data assimilation of satellite instrument observations whose sensitivity was often heavily weighted
106 towards stratospheric altitudes. This also provided initial stratospheric conditions for sets of
107 retrospective forecasts, some of which were internationally coordinated (e.g. Butler et al., 2016;
108 Tompkins et al., 2017). A growing number of operational systems are now producing regular ensembles
109 of predictions at lead times of months or years with coupled ocean-atmosphere models that extend to
110 the stratopause or beyond; for example at Environment Canada (Merryfield et al., 2013), the Met Office
111 in the UK (MacLachlan et al., 2014), the German Weather Service DWD (Baehr et al., 2015), the Japan
112 Meteorological Agency (Takaya et al., 2017) and the European Centre for Medium Range Weather
113 Forecasts (Johnson et al., 2019). In the following sections we document the emerging impacts and
114 benefits of this new capability for surface climate predictions at monthly, seasonal, and annual to
115 decadal lead times starting with the shorter-range, initial condition cases and ending with the longer-
116 range boundary-condition cases.

117

118 **2 The stratosphere and monthly prediction**

119 The best-established phenomenon that gives rise to predictability of surface climate from the
120 stratosphere is the tropospheric circulation changes that follow strong and weak conditions in the
121 stratospheric polar vortex (Baldwin and Dunkerton 1999, 2001). For example, weak vortex conditions
122 such as those found in a sudden stratospheric warming (SSW, Baldwin et al., 2021) are typically
123 followed by a weakening and southward shift of the tropospheric mid-latitude jet stream (see e.g.
124 Kidston et al., 2015 and references therein) and thus the negative polarity of the North Atlantic
125 Oscillation (NAO), Arctic Oscillation (AO) and Northern Annular Mode (NAM). These fluctuations
126 also show a tendency to vacillate between strong westerly and weak (SSW) states on subseasonal
127 timescales (Kuroda and Kodera 2001; Hardiman et al., 2020a). The changes in the troposphere persist
128 roughly as long as those in the lower stratosphere, and last for around two months (Baldwin and
129 Dunkerton 2001; Baldwin et al., 2003; Hitchcock et al., 2013; Son et al., 2020; Domeisen 2019). The
130 impacts on surface climate also include changes in the frequency of extremes of temperature and rainfall
131 (Scaife et al., 2008; King et al., 2019; Cai et al., 2016; Domeisen et al., 2020b).

132 Although *major* SSW events, involving a complete reversal of the zonal flow in the mid stratosphere,
133 are rare in the southern hemisphere (Wang et al., 2020; Jucker et al., 2021), variations of the Antarctic
134 polar vortex are likewise followed by similar signatures in the underlying tropospheric flow, in this case
135 via the Southern Annular Mode (SAM). Weakening of the vortex is typically followed by a negative
136 shift in the SAM and associated changes in rainfall and near surface temperature (Thompson et al.,
137 2005; E. Lim et al., 2018, 2019, 2021, Rao et al., 2020e). These changes in Southern Hemisphere
138 circulation typically take longer to reach the surface than their Northern Hemisphere counterparts
139 (Graverson and Christiansen 2003), perhaps due to the stronger stratospheric polar vortex and weaker
140 wave driving in the southern hemisphere, but they are nonetheless better predicted by improving
141 stratospheric resolution of forecast models (Roff et al., 2011). The timescale of weeks for the
142 predictability of sudden warmings is limited by the predictability of weather patterns in the troposphere
143 which might trigger SSW events (e.g. Mukougawa et al., 2005; Taguchi 2016; Garfinkel and Schwarz
144 2017; Jucker and Reichler 2018; Lee et al., 2020a). However, if we add this timescale to the timescale
145 of a month or more for the persistence of lower stratospheric anomalies and their surface effects (e.g.
146 Baldwin et al., 2003; Butler et al., 2019), we arrive at the conclusion that on these occasions at least,
147 initial conditions in the atmosphere can provide predictability well beyond the usual two-week horizon
148 for daily weather in either hemisphere.

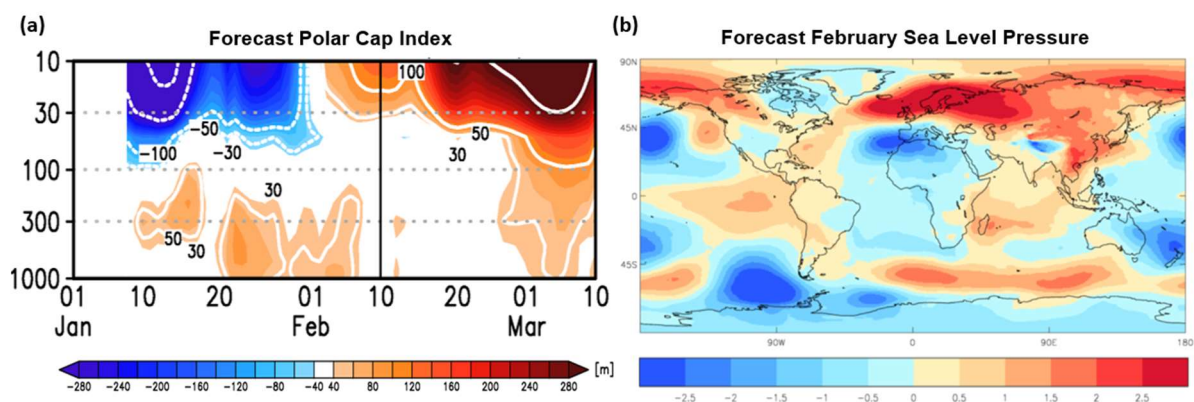
149 Predictability of the atmosphere at monthly lead times is also known to originate in part from the
150 Madden Julian Oscillation (MJO) in the troposphere and its teleconnection to the extratropics (e.g.
151 Vitart 2017). The circulation pattern associated with the MJO resembles a poleward and eastward
152 propagating Rossby wave with centres of action over the Pacific and extending into the Atlantic sector
153 where it also maps strongly onto the North Atlantic Oscillation. The lead time of around 10 days for the
154 impact of a change in the MJO to appear in the extratropical flow (e.g. Cassou 2008; Lin et al., 2009)
155 is also consistent with the timescale for poleward propagation of Rossby waves (e.g. Scaife et al., 2017).
156 It turns out that this tropospheric MJO teleconnection on monthly timescales also interacts with the
157 stratosphere (Garfinkel and Schwartz 2017). The MJO teleconnection to the North Pacific affects the
158 region most strongly associated with tropospheric precursors to SSW events, and consistent with this,
159 SSWs in the observational record have tended to follow certain MJO phases. The subsequent weak
160 vortex anomaly then propagates down to the troposphere (Garfinkel et al 2012), where it may strengthen
161 and prolong any existing negative NAO signal that is directly linked to the MJO via the troposphere
162 (Schwartz and Garfinkel 2017, 2020; Barnes et al., 2019).

163 In addition to the interaction of the MJO with the extratropical stratosphere, a further, completely
164 different link between the stratosphere and the MJO has recently been uncovered which modulates MJO
165 amplitude and persistence in the troposphere via the phase of the Quasi-Biennial Oscillation (QBO) in
166 the tropical lower stratosphere (Liu et al., 2014; Yoo and Son 2016; Martin et al., 2021). In this case,
167 easterly phases of the QBO appear to energise the MJO compared to westerly QBO phases, likely due

168 to changes in temperature and hence static stability close to the tropopause (Hendon and Abhik 2018;
 169 Martin et al., 2019) with a potential contribution of cloud-radiation feedbacks (Son et al., 2017, see
 170 Martin et al., 2021 for a review). This modulation of the MJO is in turn important for predictability as
 171 it gives rise to higher monthly prediction skill of the MJO and its surface teleconnections during the
 172 easterly phase of the QBO (Marshall et al., 2017; Abhik and Hendon 2019; Y. Lim et al., 2019).

173 The traditional view of stratosphere-troposphere interaction involves upward propagation of planetary
 174 scale Rossby waves (Charney and Drazin 1961), but this linear theory applies equally well to downward
 175 propagation. Harnik and Lindzen (2001) and Perlwitz and Harnik (2003) identified a possible source of
 176 downward propagating planetary waves in the form of reflecting surfaces in the winter stratosphere.
 177 Examples of specific reflection events, showing upwards and then downward propagation have since
 178 been observed (e.g. Kodera et al., 2008; Harnik 2009; Kodera and Mukougawa 2017; Mukougawa et
 179 al., 2017; Matthias and Kretschmer 2020). These results suggest that the details of the stratospheric
 180 circulation such as regions of negative vertical wind shear could be important for the formation of
 181 reflecting conditions (Perlwitz and Shaw 2013) and may yet provide a further mechanism by which the
 182 stratosphere can affect the troposphere (Domeisen et al., 2019; Butler et al., 2019).

183 Following studies demonstrating enhanced tropospheric predictability after SSW events in individual
 184 climate models (e.g. Kuroda 2008; Mukougawa et al 2009; Marshall and Scaife 2010; Sigmond et al.
 185 2013), subseasonal forecast systems which explicitly represent the stratosphere in the climate system
 186 were developed and implemented at operational prediction centres worldwide. It is often difficult to
 187 demonstrate significant increases in overall skill (e.g. Richter et al. 2020a) but routinely produced
 188 ensembles of subseasonal predictions show that both stratospheric variability and its subsequent
 189 tropospheric signature are predictable at monthly lead times (Domeisen et al. 2020a, 2020b). The
 190 strongest surface impacts occur if the polar vortex in the lower stratosphere is in a weakened state at
 191 the time of the SSW (Karpechko et al., 2017) and there appears to be a roughly linear relationship
 192 between the strength of these lower stratospheric anomalies and the tropospheric response (e.g. Runde
 193 et al. 2016; White et al. 2020 and see Baldwin et al. 2019 for a review). We should note however that
 194 there is no one-to-one correspondence between stratospheric variability and tropospheric events, and
 195 some prominent examples of sudden stratospheric warmings are followed by differing tropospheric
 196 anomalies (e.g. Charlton-Perez et al., 2018; Knight et al., 2020; Butler et al., 2020; Rao et al., 2020a).
 197 Nevertheless, the canonical response is seen in the majority (~70%) of cases and periods of intense
 198 wintertime stratospheric variability are important windows of opportunity to provide skilful monthly
 199 forecasts (Mariotti et al., 2020; Tripathi et al., 2015a).



200 **Figure 2: Monthly forecasts prior to the 2018 sudden stratospheric warming and severe cold event over**
 201 **northern Europe. Forecast Polar Cap Index (a) and February sea level pressure anomalies (b). Ensemble**
 202 **mean anomalies are shown for the average of forecasts initialised between 8th and 22nd of January 2018**
 203 **relative to hindcasts over the 1993-2016 period using the Met Office Hadley Centre GloSea prediction**
 204 **system (MacLachlan et al., 2015). Sea level pressure is measured in hPa and Polar Cap Index is the**
 205 **geopotential height anomaly (m) averaged over 65N to the North Pole.**

206 These forecast systems are now important tools for national meteorological and hydrological services
207 to monitor impending stratospheric variability and associated surface impacts in real time. Recent
208 extreme examples illustrate the importance of this activity. In February 2018 a major SSW occurred
209 and was followed by a strong negative NAO-like pattern at the surface with easterly wind anomalies
210 over Europe and multiple cold air outbreaks over the following weeks, including extreme snowfall
211 across northern Europe (Figure 2, Karpechko et al., 2018; Knight et al., 2020; Rao et al., 2020a) and an
212 abrupt end to Iberian drought in Southern Europe (Ayarzagueña et al., 2018). Studies of monthly
213 ensemble predictions of this event with operational stratosphere resolving systems showed that the
214 stratospheric event was predictable at least 2 weeks in advance (Figure 2) and that the ensemble
215 forecasts indicated increased likelihood of cold surface conditions for several weeks after the event
216 (Karpechko 2018; Butler et al., 2020; Statnaia et al., 2020; Rao et al., 2020a). Again, as in the analysis
217 of previous events, there was also a strong association with the MJO entering Phase 7 with increased
218 convection in the West Pacific (cf. Garfinkel and Schwartz 2017) in the 2018 event. Finally, we should
219 also note that cases of monthly forecasts where the stratosphere plays an important role are not restricted
220 to winters with sudden stratospheric warmings and periods when the stratospheric polar vortex is above
221 normal strength also provide opportunities for skilful monthly forecasts (Tripathi et al., 2015b; Scaife
222 et al., 2016). In this case an opposite but symmetric surface response results, with strong *positive* NAO.
223 A very recent example occurred in February 2020, when, following an extremely strong polar vortex
224 (Hardiman et al., 2020b; Lee et al., 2020b; Lawrence et al., 2020; Rao et al., 2021a), the tropospheric
225 jet in the Atlantic sector strengthened, and the associated increased storminess and rainfall in this case
226 resulted in UK monthly rainfall reaching a new record high (Davies et al., 2021).

227

228 **3 The stratosphere and seasonal prediction**

229

230 Prior to the advent of dynamical forecast systems which explicitly represent the stratosphere, seasonal
231 forecasts using empirical relationships and statistical methods were proposed. These relied on the prior
232 state of the polar vortex and other predictable factors such as the QBO that are known to have links to
233 surface climate (Thompson et al., 2002; Charlton et al., 2003; Christiansen et al., 2005; Boer and
234 Hamilton 2008). In some cases they indicated additional predictability that was absent in existing
235 operational forecast systems, providing further evidence of predictability involving the stratosphere and
236 further motivating the extension of dynamical forecast systems to properly represent the stratosphere.
237 Similar empirical forecast studies continue, and although they cannot provide evidence of predictability
238 that is as strong as from GCM experiments based on fundamental physical principles, they do continue
239 to be useful to indicate sources of predictability that need to be properly represented in comprehensive
240 forecast systems (e.g. Folland et al., 2012; Wang et al., 2017; Hall et al., 2017; Byrne and Shepherd
241 2018).

242 Following the introduction of dynamical seasonal forecast systems with a good representation of the
243 stratosphere, clear links between successful seasonal prediction of the North Atlantic Oscillation, the
244 closely related Arctic Oscillation and the state of the stratospheric polar vortex have been identified in
245 forecast output (e.g. Scaife et al., 2014b; Stockdale et al., 2015; Jia et al., 2017). Similar signals are also
246 seen in the southern hemisphere in relation to predictability of the Southern Annular Mode (Seviour et
247 al., 2014; Byrne et al., 2019; Lim et al., 2021). Statistically significant increases in overall skill directly
248 attributable to the inclusion of the stratosphere in prediction systems is sometimes difficult to
249 demonstrate (e.g. Butler et al., 2016), especially given that other factors such as horizontal resolution
250 and physical parametrizations are often simultaneously changed. Nevertheless, the body of evidence
251 now weighs heavily in favour of predictability of the NAO and SAM from the stratospheric polar vortex
252 and from analyses showing reduced surface prediction skill in the absence of stratospheric variability
253 (e.g. Hardiman et al 2011; Sigmund et al., 2013; Scaife et al., 2016).

254 A second clear example of seasonal predictability originating in the stratosphere is the Quasi-Biennial
255 Oscillation (QBO). The QBO has such inherently long timescales that it persists for several months in
256 seasonal forecasts from initial atmospheric conditions alone and its regularity means that it can be
257 predicted from simple composites of earlier cycles. Nevertheless, a growing number of numerical
258 models used in seasonal forecast systems can now simulate and predict the oscillation within climate
259 forecasts (Garfinkel et al., 2018; Richter et al., 2020b; Stockdale et al., 2021) with the aid of forcing
260 from parametrized non-orographic gravity waves, and there is skill in predicting QBO phase changes
261 at lead times of a few months (e.g. Pohlman et al., 2013, Scaife et al., 2014a). The surface impact of the
262 QBO is also well established and has stood the test of time since it was first identified in the 1970s
263 (Ebdon 1975; Thompson et al., 2002; Anstey and Shepherd 2014; Gray et al 2018). Yet again this
264 response projects closely onto the North Atlantic Oscillation (and hence the Arctic Oscillation/Northern
265 Annular Mode) and the Southern Annular Mode. The favoured mechanism involves refraction of
266 vertically propagating Rossby waves in the lower stratosphere (Holton and Tan 1980), although other
267 pathways may also be involved (e.g. Inoue et al., 2011; Yamazaki et al., 2020; Rao et al., 2020b, 2021b).
268 The observed magnitude of the QBO teleconnection is also large enough to provide seasonal
269 predictability of surface climate (Boer and Hamilton 2008) but its modelled amplitude at the surface
270 appears to be under-represented in current operational prediction systems and models (Scaife et al.,
271 2014b; Garfinkel et al. 2018; O'Reilly et al. 2019; Rao et al. 2020b; Anstey et al. 2021).

272 In addition to the stratosphere acting as a source of predictability, other mechanisms by which the
273 stratosphere plays a role in seasonal predictions involve a pathway for global scale teleconnections.
274 These often originate in the tropics where the longer timescales of coupled ocean-atmosphere variability
275 such as the El Niño Southern Oscillation (ENSO, L'Heureux et al. 2020) provide a predictable source
276 of low frequency variability. Effects on the extratropics can occur by tropical excitation of anomalous
277 Rossby waves which propagate polewards but also upwards into the stratosphere, as in the case of
278 ENSO (Manzini et al., 2006; Domeisen et al., 2019), giving two pathways for extratropical influence
279 (Butler et al., 2014; Kretschmer et al., 2021). These highly predictable tropical sources of climate
280 variability alter the strength and position of the stratospheric polar vortex in the extratropics as well as
281 the frequency of SSWs (Polvani et al., 2017) and these are followed by changes in the seasonal westerly
282 jets in the troposphere and surface climate via the North Atlantic Oscillation (Ineson and Scaife 2009;
283 Cagnazzo and Manzini 2009) or the Southern Annular Mode (Byrne et al., 2019). As might be expected,
284 both the QBO and ENSO teleconnections are best represented in seasonal forecast systems which
285 contain a well resolved stratosphere (Butler et al., 2016). We note that new examples of the stratosphere
286 acting as a conduit for seasonal teleconnections are still being uncovered (Hurwitz et al., 2012, Woo et
287 al., 2015). For example, the Indian Ocean Dipole (IOD) received little attention in this context until the
288 recent record event of late 2019, when it appears to have driven an extreme winter strengthening of the
289 northern hemisphere stratospheric polar vortex. This strengthening took many weeks to decay, giving
290 rise to extreme yet highly predictable conditions in the stratosphere and around the Atlantic sector in
291 late boreal winter (Hardiman et al., 2020b; Lee et al., 2020b). The same event was also implicated in
292 extreme changes in the polar vortex and the near SSW in the southern hemisphere (Rao et al., 2020e);
293 an event that itself likely helped to drive the extreme summer conditions and wildfires over Australia
294 that year (Lim et al., 2021).

295 Apparent links between Arctic sea ice and seasonal winter climate in the mid latitudes have also been
296 suggested to be mediated by the stratosphere, with increased Rossby wave activity and a weakening of
297 the stratospheric polar vortex in response to reduced sea ice, especially in the Barents-Kara Sea (Jaiser
298 et al., 2013; Kim et al. 2014; King et al., 2016; Kretschmer et al., 2016). Some studies also reproduced
299 surface signals in response to sea ice anomalies in seasonal forecasts of particular years that are in
300 apparent agreement with observational estimates (e.g. Balmaseda et al., 2010; Orsolini et al., 2012).
301 However, recent updates to observational records show a weakening of these apparent effects
302 (Blackport and Screen 2020) and significant non-stationarity (Kolstad and Screen 2019). Subsequent
303 modelling studies with larger samples of simulations have provided mixed results (Zhang et al 2018;

304 Dai and Song 2020; Smith et al 2021), and some have argued that the atmospheric response to sea ice
305 is weak and that while the sensitivity to Barents-Kara sea ice may be stronger, the stratospheric response
306 in particular is highly variable (McKenna et al. 2017). While there may well be a longer-term effect via
307 the stratosphere from sea ice decline (Sun et al., 2015; Screen and Blackport 2019; Kretschmer et al.,
308 2020), sensitivity of the response to the background state complicates the issue (Labe et al., 2019; Smith
309 et al. 2017), as do possible confounding influences from the tropics (Warner et al. 2020) and to date
310 there is no clear consensus for strong enough year-to-year effects to provide significant seasonal
311 predictability.

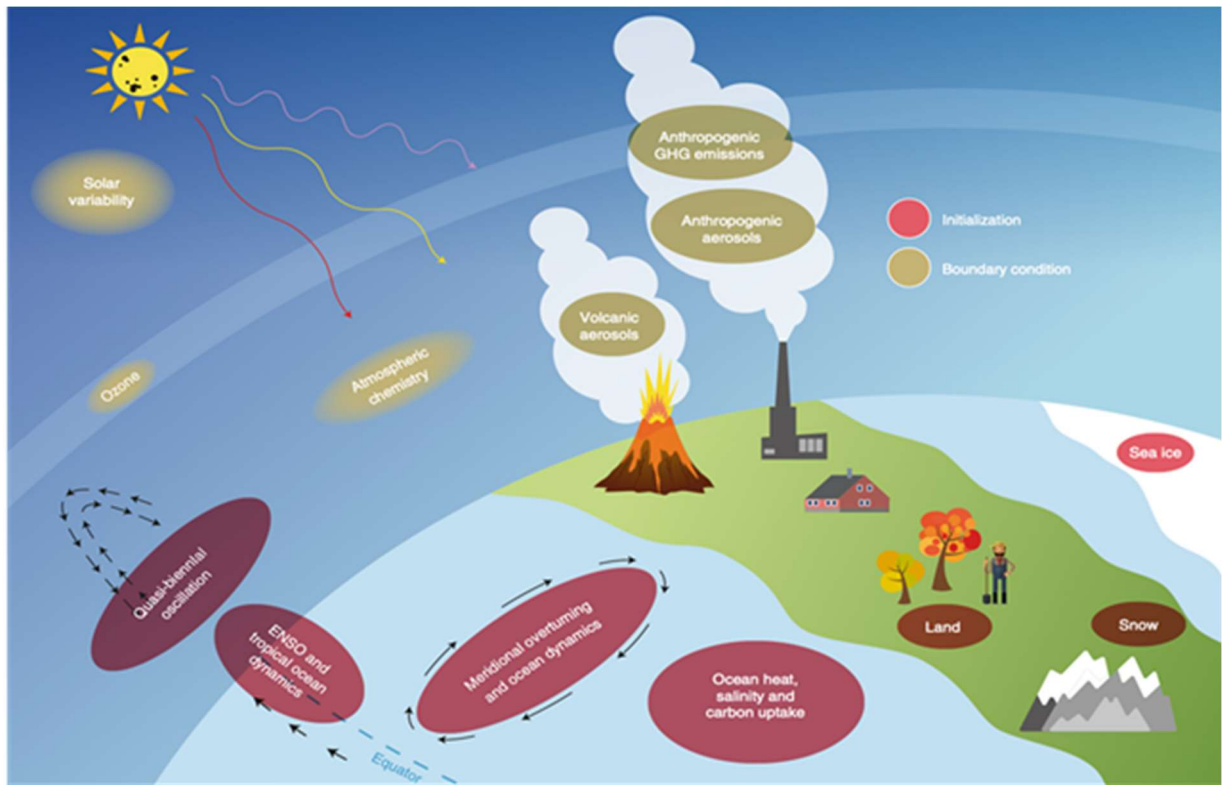
312 Other proposed teleconnections acting via the stratosphere have been found in observations but remain
313 to be confirmed with successful reproduction in physically based climate models. A prominent example
314 involves a proposed link between Eurasian snow amounts and the stratosphere, followed by a return
315 influence on the NAO and surface climate. In this case, enhanced snow cover or depth is associated
316 with high pressure over north Eurasia, an increase in the flux of Rossby wave activity into the
317 stratosphere and a subsequent weakening of the stratospheric polar vortex, followed by the expected
318 negative shift in the NAO and AO (Cohen and Entekhabi 1999, Cohen and Jones 2011; Cohen et al.,
319 2014; Furtado et al., 2015). However, the strength of this link in climate models and seasonal predictions
320 is modest (Fletcher et al., 2009; Riddle et al., 2013; Tyrrell et al., 2018, 2019) and does not agree with
321 apparent links to the AO in observations (Kretschmer et al., 2016; Garfinkel et al., 2020) even when
322 model mean state biases are corrected (Tyrrell et al., 2020). It has also been suggested that
323 teleconnections to snow are non-stationary or non-causal and there is continued debate about its long-
324 term robustness (Peings et al., 2013; Henderson et al., 2018).

325 In summary, a number of mechanisms by which the stratosphere acts to provide seasonal predictability
326 either by acting directly as a source of predictable variability (e.g. the QBO, SSWs), or as a conduit for
327 teleconnections (e.g. ENSO, MJO, IOD) have now been established in observations and have been
328 confirmed using climate model simulations based on first principles. These operate in seasonal forecast
329 systems, albeit with remaining errors such as the weakness of the QBO connection to surface climate.
330 Meanwhile, other mechanisms involving the stratosphere (for example the response to snow cover
331 variations) have been proposed based on apparent observed relationships, but until we have agreement
332 between these observations and theory (model simulations), scientists remain sceptical of whether they
333 represent actual sources of seasonal predictability and these remain topics of current research.

334

335 **4 The stratosphere and annual to decadal prediction**

336 In recent years, initialised predictions on longer timescales were developed on the premise of multiyear
337 memory in the ocean (e.g. Smith et al 2007), and following the development pathway mapped out by
338 seasonal forecasts in the past, these are now being run operationally to produce real time multi-model
339 forecasts (Smith et al., 2013). Kushnir et al. (2019) mapped out this operational development of annual
340 to decadal predictions and highlighted a number of sources of predictability, some of which involve the
341 stratosphere (Figure 3), but not all of which are fully represented in climate prediction systems.



342

343 **Figure 3. Sources of annual to decadal predictability, some of which involve the stratosphere through the**
 344 **response to external forcing, internal atmospheric dynamics, or ozone chemistry changes. After Kushnir et**
 345 **al., 2019.**

346 Despite common misconceptions, not all annual to decadal predictability stems from the ocean. Indeed,
 347 it has been clearly demonstrated that multiyear predictability of the QBO exists in current decadal
 348 predictions systems out to lead times of several years (Pohlman et al., 2013; Scaife et al., 2014a). This
 349 offers the prospect of a stratospheric contribution to multiyear predictability of the extratropics through
 350 the teleconnection with the Arctic Oscillation (Anstey and Shepherd 2014, Gray et al., 2018) and to
 351 tropical predictability through links to the MJO (e.g. Martin et al., 2021) and wider tropical climate
 352 variability (Haynes et al., 2021).

353 Although it is more important on multidecadal timescales (see below), external forcing of the
 354 stratosphere can also act as a source of decadal predictability. Forced climate signals from changes in
 355 greenhouse gases or stratospheric effects such as ozone depletion occur on a much longer timescale
 356 than the lead time of decadal forecasts but their contribution to the skill of predictions is not trivial. For
 357 example, it is not immediately obvious whether the slow changes from multidecadal forced signals
 358 would simply be swamped by unpredictable internal variability on decadal timescales, rendering long
 359 term external forcing changes useless for decadal predictions. However, this is not the case and long-
 360 term forcing is now known to be an important source of decadal prediction skill (Smith et al., 2019,
 361 2020).

362 External forcing involving the stratosphere on shorter timescales is also important for annual to decadal
 363 predictions. The stratosphere has long been known to be influenced by volcanic eruptions, particularly
 364 in the case of tropical volcanic eruptions which are powerful enough to inject significant quantities of
 365 sulphur dioxide into the atmosphere. Here it reacts with water to form sulphuric acid and persists in
 366 aerosol form, leading to predictable multiyear global surface cooling, tropical stratospheric warming
 367 and an intensification of the westerly stratospheric polar vortex in the extratropics (Robock and Mao
 368 1992). Although the sample of observed events is limited, modelling studies have reproduced an
 369 observed post-eruption intensification of the westerly winds in the stratosphere and some impacts on

370 the surface Arctic Oscillation. However, generations of models have struggled to reproduce the two-
371 year persistence of volcanic effects seen in observations and the observed magnitude of the effect on
372 the winter AO (e.g. Stenchikov et al., 2006; Marshall et al., 2009; Charlton-Perez et al., 2013, Bittner
373 et al., 2016). In addition to these changes in the atmosphere, the intensification of stratospheric
374 westerlies and hence Arctic Oscillation also combines with surface cooling of the ocean to generate
375 predictable changes in the Atlantic meridional overturning circulation (Reichler et al., 2012) which can
376 extend the volcanic influence to decadal timescales (Swingedouw et al., 2015). Finally, although the
377 mechanism is debated, there is also evidence of a multiyear effect of tropical volcanic eruptions on
378 ENSO, presumably requiring the persistent radiative forcing that arises through the long residence time
379 of volcanic products, particularly sulphate aerosols, in the stratosphere. This reportedly increases the
380 frequency of El Nino events by a factor of two in the years following volcanic eruptions (Adams et al.,
381 2003), again suggesting an important source of multiannual predictability via the stratosphere.

382 A second source of multiannual predictability from external forcing originates from solar variability
383 and in particular the 11-year solar activity cycle. Although a number of alternative mechanisms have
384 been proposed (see Gray et al., 2010 for a review), the established mechanism for surface effects via
385 the stratosphere is the change in the polar vortex that results from changes in upper stratospheric heating
386 over the course of each cycle between solar minimum and solar maximum. Atmospheric wave-mean
387 flow interactions amplify the initial radiatively driven change and drive its descent to the troposphere
388 (Kodera and Kuroda 2002; Marsh et al 2007; Ineson et al., 2011; Givon et al., 2021), where changes in
389 the extratropical jets result in a negative (positive) Arctic Oscillation pattern following solar minimum
390 (maximum). There is also evidence that it contributes to interannual prediction skill (Dunstone et al.,
391 2016) and an interesting aspect that has emerged in recent years is the integrating effect of the ocean on
392 solar induced changes in the NAO via interannual persistence of ocean heat content anomalies which
393 leads to a lag of around 3 years ($\pi/2$ cycles) in the peak response, as would be expected if the ocean is
394 integrating the effects of a periodic solar forcing (Scaife et al., 2013; Gray et al., 2013; Andrews et al.,
395 2015; Thiéblemont et al., 2015). However, debate continues as to whether the solar signal is indeed
396 large enough to be detectable in observations in the presence of large internal tropospheric variability
397 (Chiodo et al., 2019).

398 Perhaps the longest known timescale for predictability from initial conditions, which also involves the
399 stratosphere, is the interaction of Atlantic Multidecadal Variability (AMV) with the stratospheric
400 circulation. The Atlantic has followed pronounced multidecadal variations over the last century (Mann
401 et al., 1995) and these variations are predictable out to years ahead (Hermanson et al., 2014). Some
402 studies link these variations to the stratosphere and the NAO/AO (Reichler et al., 2012; Omrani et al.,
403 2014). Indeed, the pronounced multidecadal increase in the surface NAO between the 1960s and 1990s
404 is strongly coupled to changes in the strength of the stratospheric polar night jet (Scaife et al., 2005).
405 Although current models simulate weak coupling between the AMV and the free atmosphere, this
406 coupling appears to increase with model resolution (Lai et al., 2021) suggesting that the links between
407 AMV, the stratosphere and the NAO offer potential for improved decadal scale prediction involving
408 the stratosphere.

409 The currently recognised role of the stratosphere in decadal forecasts of surface climate again appears
410 mainly via the impact on annular modes and, in the northern hemisphere, the North Atlantic Oscillation.
411 Indeed, while current decadal prediction systems are now able to produce skilful predictions of
412 variations in the NAO on multiyear lead times (Smith et al., 2019, 2020; Athanassiadis et al., 2020),
413 much work is still needed to attribute these variations to external forcing or internal variability and to
414 understand the interaction between boundary and initial conditions which blurs the simple distinction
415 between the two. These new results are important because they indicate new-found decadal
416 predictability of events like the high NAO of the 1990s which yielded a run of mild but wet and stormy
417 winters in northern Europe and the eastern USA. These winters are well known to have caused
418 significant impact for example on the insurance sector (Leckebusch et al., 2007) and coincided with the

419 longest observed absence of SSW events (Pawson and Naujokat 1999; Domeisen 2019). Given the
420 indications of coupled stratosphere-troposphere variations on decadal timescales (Scaife et al., 2005;
421 Omrani et al., 2014; Garfinkel et al., 2017; Woo et al., 2015), understanding the role of the stratosphere
422 in extratropical decadal predictions needs further investigation.

423

424 **5 The stratosphere and multidecadal projection**

425 The importance of the stratosphere for climate projections on multidecadal timescales was generally
426 recognised before its role in predictions on shorter timescales. This is in part a legacy of the early
427 development of stratosphere-troposphere models for ozone depletion studies described in the
428 introduction. On these longer timescales, coupling between stratospheric composition, thermal structure
429 and atmospheric circulation gives rise to [surface-climate-predictability-improved climate projections](#).

430 Perhaps the best-known case for the stratosphere affecting multidecadal projections of surface climate
431 is the influence of ozone depletion on the southern annular mode (SAM; Thompson and Solomon 2002,
432 2005; McLandress et al., 2011; Polvani et al., 2011; Son et al., 2018) where decreasing ozone in the late
433 20th century led to a strengthened pole-to-equator temperature gradient, a stronger stratospheric polar
434 vortex and a shift to strong positive SAM phases at the surface. In this case, studies again show the
435 importance of stratospheric resolution to generate the full response, consistent with a genuine downward
436 influence (Karpechko et al., 2008). The associated poleward shift in the tropospheric jet is connected to
437 a delay in the spring breakdown of the stratospheric polar vortex (Byrne et al., 2017) and delivered
438 significant and prolonged changes in rainfall across many regions of the southern hemisphere (Kang et
439 al., 2011; Purich and Son 2012). Implementation of the Montreal Protocol in 1987 and subsequent
440 reductions in the rate of ozone depletion mean that recovery of the ozone layer is now expected over
441 the coming decades and the reversible effects of this on the surface climate form an important element
442 of current multidecadal projections (Thompson et al., 2011; Previdi and Polvani 2014; Solomon et al.,
443 2016; Banarjee et al., 2020, Zambri et al., 2021) where they are expected to play an important role
444 alongside other changes in the southern stratosphere due to continuing increases in greenhouse gases
445 (Son et al., 2009; Barnes et al., 2012), some of which occur via the stratospheric polar vortex in a similar
446 way to those from ozone depletion and recovery (Ceppi and Shepherd, 2019).

447 The more limited effects of ozone depletion in the northern hemisphere meant that the role of the
448 stratosphere in multidecadal projections took longer to become established. Some early studies found
449 potential amplification of positive Arctic Oscillation trends under climate change when the stratosphere
450 was included (Shindell et al., 2001). However, this was not borne out in later studies as simulations
451 with other fully coupled ocean-troposphere-stratosphere models suggested weakening of the
452 stratospheric polar vortex (e.g. Huebener et al., 2007). Subsequent studies with multiple models also
453 indicated a southward shift in the polar night jet with weakening high latitude winds and strengthening
454 subtropical winds (Scaife et al., 2012; Manzini et al., 2014). These changes result from increased
455 atmospheric wave driving of the winds which can overwhelm the cooling effect of greenhouse gases
456 (Karpechko and Manzini 2012) and can lead to important differences in future surface climate, for
457 example in regional rainfall in areas typically affected by the stratosphere via the Arctic Oscillation and
458 NAO (Scaife et al., 2012). There is still significant uncertainty due to the diversity of modelled
459 stratospheric responses to greenhouse gas increases (Manzini et al., 2014, Simpson et al., 2018, Zappa
460 and Shepherd 2017), and it has proved difficult to identify any clear change in the frequency of sudden
461 stratospheric warmings (Ayarzagüena et al., 2018, 2020; Rao et al., 2020c). This is perhaps due to the
462 competition between strengthening latitudinal temperature gradients near the tropopause and enhanced
463 meridional overturning in the mid stratosphere. There is also strong inherent unpredictable variability
464 from decade to decade in the frequency of SSW occurrence (Butchart et al., 2000; McLandress and
465 Shepherd 2009).

466 Other aspects of future climate change where the stratosphere plays a role have also been identified, for
467 example, in the debate over the response to future levels of Arctic sea ice. In this case it seems that the
468 response of the mid-latitude circulation involves a negative shift in the Arctic Oscillation (Screen et al.,
469 2018; Zappa et al., 2018; McKenna et al., 2018). This could again be amplified by interaction with the
470 stratosphere as some studies suggest that the stratospheric response is necessary for a large surface
471 response (Kim et al., 2014), while others highlight that the stratospheric interaction is sensitive to the
472 regional pattern of sea ice decline (McKenna et al., 2018), and still others show evidence of non-linear
473 stratospheric, and stratosphere-mediated surface response (Manzini et al., 2018), coincident with the
474 time when the Barents and Kara seas become ice-free (Kretschmer et al., 2020). Furthermore, studies
475 also indicate that the surface climate response to sea ice decline depends systematically on the phase of
476 the stratospheric QBO (Labe et al., 2019).

477 Although it is much less certain than anthropogenic climate change, there have also been suggestions
478 of a multidecadal decline of external solar irradiance which can impact multidecadal climate projections
479 via the stratosphere. Previous multidecadal solar minima, so called ‘grand minima’, have occurred in
480 sunspot records and have been connected to the Little Ice Age period around the end of the 17th century
481 using proxy and other data (Owens et al., 2017). Given recent weak amplitude 11 year solar cycles,
482 there are now suggestions of a future solar ‘grand minimum’ where the 11 year cycle described above
483 could become muted or even absent for a prolonged period (Lockwood et al., 2010). In this case, the
484 upper stratospheric cooling in the tropics and summer hemisphere can change the meridional
485 temperature gradient in a similar fashion to the 11 year cycle (Maycock et al., 2015) and leads to a
486 negative shift in the AO and the NAO, and hence affects regional climate (Ineson et al., 2015). However,
487 in this case it appears that while regional changes could be significant, they are generally much smaller
488 than the surface warming due to anticipated levels of anthropogenic greenhouse gases (Anet et al., 2013;
489 Ineson et al., 2015; Maycock et al., 2015).

490 Finally, we note that although low frequency variability in teleconnections is observed (e.g. Garfinkel
491 et al., 2019), it is often unclear whether this is a systematic variation or simply due to sampling
492 variability of an underlying stationary process (Jain et al., 2018). Nevertheless, there is growing
493 evidence for systematic climate change in some of the teleconnections by which the stratosphere enables
494 surface predictability. Under future climate change it appears that some of the teleconnections discussed
495 above may *strengthen* in amplitude. For example, the strength of ENSO induced anomalies in the
496 extratropical Atlantic/European sector increases in future climate projections (Müller and Roeckner
497 2006; Fereday et al., 2020). Similarly, recent analyses suggest that the MJO teleconnection to the
498 extratropics increases in amplitude under climate change (Samarasinghe et al., 2020). The same is also
499 true of the extratropical effects of the stratospheric QBO, where in this case, the amplitude of the
500 teleconnection in composite anomalies doubles under future climate change (Rao et al., 2020d) despite
501 the QBO itself becoming weaker (Richter et al., 2020c).

502

503 **6 Outlook**

504 Long range prediction has evolved quickly in recent years (Merryfield et al., 2017; 2020, Butler et al.,
505 2019; Meehl et al., 2021) and this rapid development is due in part to the improved representation of
506 stratospheric processes and stratospheric initial conditions in ensemble prediction systems. The long-
507 range forecast community originally focused on predictability from initial ocean conditions and this
508 remains the primary source of long-range predictability, for example from ENSO, but some of these
509 long-range prediction systems contained poor representations of the stratosphere. In the meantime,
510 those working in parallel on climate modelling of the stratosphere were rarely involved in initialised
511 long-range prediction, instead being driven primarily by the ozone depletion problem. Knowledge
512 exchange across fields is important in science and precursors to a new paradigm often occur when a
513 topic is investigated by researchers from outside the field (Kuhn 1970). The crossover and collaboration

514 between long range prediction and stratospheric research communities is no exception and the
515 interaction between these communities has yielded rapid progress and new insights. Examples where
516 initial atmospheric conditions can provide predictability beyond the usually assumed limit have been
517 demonstrated, particularly for the extratropics but also for the tropics, and we now know that in some
518 situations, for example when sudden stratospheric warmings occur, the initial conditions in the
519 stratosphere can have more impact than initial conditions in the ocean (Thompson et al 2002; Scaife
520 and Knight 2008; Polvani et al 2017). This suggests that initial atmospheric conditions in the
521 stratosphere are likely to be more important for long range forecasts than previously assumed
522 (Mukougawa et al., 2005, 2009; Stockdale et al., 2015; Noguchi et al., 2016, 2020a; Choi and Son 2019;
523 O'Reilly et al., 2019; Nie et al., 2019), not least because the overturning and breaking of Rossby waves
524 in the stratosphere is followed by long lived atmospheric anomalies due to synoptic scale eddy
525 feedbacks that prolong the effects in the troposphere (Kunz and Greatbatch 2013 Kang et al., 2011;
526 White et al., 2020). More research on the initial conditions in the stratosphere might therefore help to
527 reveal potential for further improvements in prediction skill.

528 A notable simplification to understanding the role of the stratosphere, at least in extratropical long-
529 range predictions, is its apparently seamless mechanism across different timescales and different
530 phenomena. Following the early ground-breaking studies showing surface impacts of stratospheric
531 variability (e.g. Labitzke 1965, Boville 1984) and a multitude of studies on individual teleconnections
532 between the stratosphere and surface climate, the projection of stratospheric variability onto the Arctic
533 Oscillation/North Atlantic Oscillation/Annular Mode circulation patterns across timescales and
534 hemispheres is now well established (see the review by Kidston et al., 2015). This suggests that similar
535 coupling processes occur between the stratosphere and troposphere from months to decades and these
536 processes lead to some of the most intense extratropical climate extremes, in winter in the northern
537 hemisphere and in late spring/early summer in the southern hemisphere (Karpechko et al., 2018;
538 Fereday et al., 2012, Kautz et al., 2019; Domeisen and Butler 2020). While studies point to changes in
539 upper tropospheric baroclinicity and tropospheric eddy feedbacks as crucial in these teleconnections, a
540 full mechanistic understanding of how this occurs is still lacking.

541 Some, but not all, leading forecast systems now include a well resolved stratosphere with reasonable
542 representation of relevant processes such as the body force from sub-grid orographic and non-
543 orographic gravity waves. However, many outstanding problems remain. Although their number is
544 increasing, only a subset of current GCMs have the ability to simulate a realistic QBO beyond its decay
545 from initial conditions and it seems that all GCMs have problems with the fidelity of modelled QBO
546 teleconnections, which are either too weak or absent altogether (Scaife et al., 2014a; Kim et al., 2020;
547 Anstey et al., 2021). Even the relatively well studied ENSO teleconnection via the stratosphere to the
548 extratropics still has outstanding questions, such as whether the northern hemisphere stratosphere
549 exhibits more SSW events during the La Niña phase (Butler and Polvani 2011; Song and Son 2012).
550 This is not generally reproduced in modelling systems (Garfinkel et al., 2012) but occurred in the recent
551 La Niña winter of 2020/2021. Similarly, while the increased monthly predictability from the MJO
552 during the easterly phase of the QBO has been detected in monthly forecast experiments, the QBO-
553 MJO connection does not persist in longer predictions and simulations with current models (Kim et al.,
554 2020). Research and model development on stratosphere-troposphere interaction, including tropical
555 effects (Noguchi et al., 2020b), will no doubt lead to further progress in resolving this issue (Haynes et
556 al., 2021).

557 Errors in the modelled climatological mean climate are inevitably present to varying degrees in even
558 the latest climate models. The common protocol of running a set of retrospective predictions to allow
559 these mean biases to be estimated and hence subtracted from real time predictions may well correct for
560 much of this error. However, the degree to which biases have a nonlinear, state dependent impact on
561 the predictions is not fully understood. In some contexts, the nonlinear impacts of biases may be
562 minimal (Karpechko et al., 2021) while others show sensitivity (Sigmond et al., 2008, 2010) and

563 increases of prediction skill occur under certain background conditions, for example during Easterly
564 QBO phases (Taguchi 2018). Other processes generally omitted from long range predictions include
565 interactive variations of ozone and other trace gases. Although reports of impacts and benefits have
566 varied, it is thought that surface signals on interannual timescales come mainly from dynamical rather
567 than chemical changes (Seviour et al., 2014; Harari et al., 2019). Nevertheless, some studies suggest
568 detectable effects from interannual variability of ozone and it may be that ozone fluctuations could help
569 to amplify surface signals (Karpechko et al., 2014; Son et al., 2013; Smith and Polvani 2014; Oehrlein
570 et al., 2020; Hendon et al., 2020), providing a further area for future development. Given that the cost
571 of full atmospheric chemistry schemes remains computationally expensive, it seems likely that simple
572 parametrizations of ozone chemistry (e.g. Monge-Sanz et al., 2021) would be valuable in this context.

573 We end with a pointer to an issue that has now been found to affect long-range predictions from monthly
574 to seasonal to decadal and multidecadal timescales, particularly in the extratropics. So called ‘perfect
575 model studies’, which test the ability of models to predict their own ensemble members, are now known
576 to *underestimate* the true predictability of climate in some regions, particularly around the Atlantic
577 basin, and so models are better at predicting real world variations than they are at predicting themselves.
578 This so-called ‘Signal to Noise Paradox’ (Scaife and Smith 2018) is at first surprising, because perfect
579 model prediction scores are often assumed to represent an upper (rather than lower) limit for prediction
580 skill of the real world. The problem can be understood in terms of unrealistically weak ensemble mean
581 predictions (e.g. Eade et al., 2014) but whether the stratosphere is involved directly in the cause of this
582 problem remains to be seen (Saito et al., 2017; Stockdale et al., 2015), as it initially appears in the
583 troposphere rather than the stratosphere in long range forecasts (Domeisen et al., 2020a). Nevertheless,
584 the unrealistically weak amplitude of ensemble mean predictions may well have the same root cause as
585 the weaker than observed amplitude of modelled teleconnections to the stratosphere discussed in this
586 review, including, for example, the under-representation of the surface impact of the QBO. Resolving
587 this problem will therefore likely amplify these signals, provide greater levels of prediction skill, and
588 further strengthen the role of the stratosphere in long range predictions of surface climate.

589 **Author Contributions**

590 AAS wrote the draft manuscript. All other co-authors contributed relevant references and input to
591 revisions and editing of the manuscript. SWS helped produce Figure 1.

592 **Acknowledgements**

593 AAS and SCH were supported by the Met Office Hadley Centre Climate Programme funded by BEIS
594 and Defra. MPB was supported by the Natural Environment Research Council (grant number
595 NE/M006123/1). JHR was supported by the Regional and Global Model Analysis (RGMA) component
596 of the Earth and Environmental System Modeling Program of the U.S. Department of Energy’s Office
597 of Biological & Environmental Research (BER) via NSF Interagency Agreement 1844590. SN was
598 supported by the Japan Society for the Promotion of Science (KAKENHI, Grant Number: 19K14798).
599 EPL was supported by the Australian government’s National Environmental Science Program Phase 2
600 and the Victorian Water and Climate Initiative Phase 2. SWS was supported by the National Research
601 Foundation of Korea (NRF) grant funded by the South Korean government (Ministry of Science and
602 ICT) (2017R1E1A1A01074889). DWJT is supported by the US National Science Foundation Climate
603 and Large-Scale Dynamics program. Support from the Swiss National Science Foundation through
604 projects PP00P2_170523 and PP00P2_198896 to D.D. is gratefully acknowledged. CIG was supported
605 by a European Research Council starting Grant under the European Union Horizon 2020 research and
606 innovation program (Grant agreement 677756).

607

608 **References**

609 Abhik, S. and Hendon, H.H.: Influence of the QBO on the MJO during coupled model multiweek
610 forecasts. *Geophysical Research Letters*, 46(15), 9213-9221, 2019.

611 Adams, B. J., Mann, M. and Ammann, C. Proxy evidence for an El Niño-like response to volcanic
612 forcing. *Nature*, 426, 274–278, 2003.

613 Andrews, M., Knight, J. & Gray, L. A simulated lagged response of the North Atlantic Oscillation to
614 the solar cycle over the period 1960–2009. *Env. Res. Lett.* 10, L054022, 2015.

615 Anet, J. G., et al.: Impact of a potential 21st century “grand solar minimum” on surface temperatures
616 and stratospheric ozone, *Geophys. Res. Lett.*, 40, 4420– 4425, doi:10.1002/grl.50806, 2003.

617 Anstey, J.A. and Shepherd, T.G.: High-latitude influence of the Quasi-Biennial Oscillation. *Quart. J.*
618 *Roy. Meteor. Soc.*, 140, 1–21, 2014.

619 Anstey, J.A., Simpson, I.R., Richter, J.H., Naoe, H., Taguchi, M., Serva, F., et al.: Teleconnections of
620 the Quasi-Biennial Oscillation in a multi-model ensemble of QBO-resolving models. *Q J R Meteorol*
621 *Soc*, 1– 26, 2021.

622 Ayarzagüena, B., L.M. Polvani, U. Langematz, and CCMI co-authors: No robust evidence of future
623 changes in major stratospheric sudden warmings: A multi-model assessment from CCMI, *Atmos.*
624 *Chem. Phys.*, 18, 11277-11287, 2018.

625 Ayarzagüena, B., Barriopedro, D., Garrido-Perez, J. M., Abalos, M., de la Cámara, A., García-
626 Herrera, R., et al.: Stratospheric connection to the abrupt end of the 2016/2017 Iberian drought.
627 *Geophysical Research Letters*, 45, 12, 639– 12, 646, 2018.

628 Ayarzagüena et al.: Uncertainty in the response of stratospheric sudden warmings and stratosphere-
629 troposphere coupling to quadrupled CO2 concentrations in CMIP6 models, *J. Geophys. Res.*, 126, 6,
630 e2019JD032345, 2020.

631 Baehr, J., Fröhlich, K., Botzet, M., Domeisen, D. I. V., Kornblueh, L., Notz, D., et al.: The prediction
632 of surface temperature in the new seasonal prediction system based on the MPI-ESM coupled climate
633 model. *Climate Dynamics*, 44(9-10), 2723–2735, 2015.

634 Baldwin, M. P., and Dunkerton, T. J.: Propagation of the Arctic Oscillation from the stratosphere to
635 the troposphere, *J. Geophys. Res.*, 104 (D24), 30937– 30946, 1999.

636 Baldwin, M.P. and T.J. Dunkerton: Stratospheric Harbingers of Anomalous Weather Regimes.
637 *Science*, 294, 5542, 581-584, 2001.

638 Baldwin M.P., David B. Stephenson, David W. J. Thompson, Timothy J. Dunkerton, Andrew
639 J. Charlton, Alan O’Neill. Stratospheric Memory and Skill of Extended-Range Weather Forecasts.
640 *Science*, 301, 636-640, 2003.

641 Baldwin M.P., et al.: 100 Years of Progress in Understanding the Stratosphere and Mesosphere. *Met.*
642 *Monographs*, 59, 27.1-27.62, 2019.

643 Baldwin, M. P., Ayarzagüena, B., Birner, T., Butchart, N., Butler, A. H., Charlton-Perez, A. J., et al.:
644 Sudden stratospheric warmings. *Reviews of Geophysics*, 59, e2020RG000708, 2021.

645 Balmaseda, M.A., Ferranti, L., Molteni, F. and Palmer, T.N.: Impact of 2007 and 2008 Arctic ice
646 anomalies on the atmospheric circulation: Implications for long-range predictions. *Q.J.R. Meteorol.*
647 *Soc.*, 136: 1655-1664, 2010.

648 Barnes, E.A, N.W. Barnes and L.M. Polvani: Delayed Southern Hemisphere climate change induced
649 by stratospheric ozone recovery, as projected by the CMIP5 models, *J. Climate*, 27, 852-867, 2014.

650 Barnes, E. A., Samarasinghe, S. M., Ebert-Uphoff, I., & Furtado, J. C.: Tropospheric and stratospheric
651 causal pathways between the MJO and NAO. *Journal of Geophysical Research: Atmospheres*, 124,
652 9356– 9371, 2019.

653 Beagley, S. R., J. de Grandpre', J. N. Koshyk, N. A. McFarlane, and T. G. Shepherd. Radiative-
654 dynamical climatology of the first-generation Canadian middle atmosphere model. *Atmosphere-*
655 *Ocean* 35, 293-331, 1997.

656 Bittner, M., Timmreck, C., Schmidt, H., Toohey, M., and Krüger, K.: The impact of wave-mean flow
657 interaction on the Northern Hemisphere polar vortex after tropical volcanic eruptions, *J. Geophys.*
658 *Res. Atmos.*, 121, 5281– 5297, 2016.

659 Blackport, R. and J.A. Screen. Weakened evidence for mid-latitude impacts of Arctic warming.
660 *Nature. Clim. Change*, 10, 1065-1666, 2020.

661 Boer, G.J., Hamilton, K. QBO influence on extratropical predictive skill. *Clim Dyn* 31, 987–1000,
662 2008.

663 Boville, B. A.: The Influence of the Polar Night Jet on the Tropospheric Circulation in a GCM, *J.*
664 *Atm. Sci.*, 41(7), 1132-1142, 1984.

665 Butchart, N., Austin, J., Knight, J. R., Scaife, A. A., & Gallani, M. L.: The Response of the
666 Stratospheric Climate to Projected Changes in the Concentrations of Well-Mixed Greenhouse Gases
667 from 1992 to 2051, *Journal of Climate*, 13(13), 2142-2159, 2000.

668 Butler, A.H., A. Charlton-Perez, D.I.V. Domeisen, I.R. Simpson, and J. Sjoberg, The predictability of
669 Northern Hemisphere final stratospheric warmings and their surface impacts, *Geophys. Res. Lett.*, 46,
670 10578-10588, 2019.

671 Butler A.H., Arribas A., Athanassiadou M., Baehr J., Calvo N., Charlton-Perez A., Deque M.,
672 Domeisen D.I.V., Fröhlich K., Hendon H., Imada Y., Ishii M., Iza M., Karpechko A.Y., Kumar A.,
673 Maclachlan C., Merryfield W.J., Muller W.A., O'Neill A., Scaife A.A., Scinocca, J., Sigmond M.,
674 Stockdale T.N., Yasuda T.: The Climate-system Historical Forecast Project: Do stratosphere-
675 resolving models make better seasonal climate predictions in boreal winter? *Quart. J. Roy. Met. Soc.*,
676 142, 1413-1427, doi:10.1002/qj.2743, 2016.

677 Butler, A.H., Z.D. Lawrence, S.H. Lee, S.P. Lillo, and C.S. Long: Differences between the 2018 and
678 2019 stratospheric polar vortex split events, *Quar. Jour. Roy. Met. Soc.*, 1-19, 2020.

679 Butler, A.H., A. Charlton-Perez, D.I.V. Domeisen, C. Garfinkel, E.P. Gerber, P. Hitchcock, A.-Yu
680 Karpechko, A.C. Maycock, M. Sigmond, I. Simpson, S.-W. Son. Sub-seasonal Predictability and the
681 Stratosphere- Chapter 11, *The Gap Between Weather and Climate Forecasting*, p. 223-241, 2019.

682 Butler, A.H., L.M. Polvani and C. Deser: Separating the stratospheric and tropospheric pathways of El
683 Niño-Southern Oscillation teleconnections, *Environ. Res. Lett.*, 9, 024014, 2014.

684 Butler A.H. and L.M. Polvani: El Niño, La Niña, and stratospheric sudden warmings: A re-evaluation
685 in light of the observational record, *Geophys. Res. Lett.*, 38, L13807, 2011.

686 Byrne, N.J., Shepherd, T.G., Woollings, T. and Plumb, R.A.: Non-stationarity in Southern
687 Hemisphere climate variability associated with the seasonal breakdown of the stratospheric polar
688 vortex. *J. Clim.*, 30, 7125–7139, 2017.

689 Byrne, N. J., and T. G. Shepherd: Seasonal persistence of circulation anomalies in the Southern
690 Hemisphere stratosphere and its implications for the troposphere. *J. Clim.*, 31, 3467–3483,
691 doi:10.1175/JCLI-D-17-0557.1, 2018.

692 Byrne, N.J., Shepherd, T.G. and Polichtchouk, I.: Subseasonal-to-seasonal predictability of the
693 Southern Hemisphere eddy-driven jet during austral spring and early summer. *J. Geophys. Res.*, 124,
694 6841–6855, 2019.

695 Cai, M., Yu, Y. Deng, H.M. van den Dool, R. Ren, S. Saha, X. Wu, J. Huang: Feeling the pulse of
696 the stratosphere: an emerging opportunity for predicting continental-scale cold-air outbreaks 1 month
697 in advance. *Bull. Am. Meteorol. Soc.*, 97, pp. 1475-1489, 2016.

698 Cassou, C.: Intraseasonal interaction between the Madden–Julian Oscillation and the North Atlantic
699 Oscillation. *Nature* 455, 523–527, 2008.

700 Christiansen B.: Downward propagation and statistical forecast of the near-surface weather. *J.*
701 *Geophys. Res. Atmos.*, 110, 2005.

702 Ceppi, P. and Shepherd, T.G.: The role of the stratospheric polar vortex for the austral jet response to
703 greenhouse gas forcing. *Geophys. Res. Lett.*, 46, 6972–6979, 2019.

704 Charlton, A.J., O'Neill, A., Stephenson, D.B., Lahoz, W.A. and Baldwin, M.P.: Can knowledge of the
705 state of the stratosphere be used to improve statistical forecasts of the troposphere?. *Q.J.R. Meteorol.*
706 *Soc.*, 129: 3205-3224, 2003.

707 Charlton-Perez AJ, et al.: On the lack of stratospheric dynamical variability in low-top versions of the
708 CMIP5 models, *J. Geophys. Res. Atmos.*, 118, 2494–2505, 2013.

709 Charlton-Perez, A. J., Ferranti, L. and Lee, R. W.: The influence of the stratospheric state on North
710 Atlantic weather regimes. *Quarterly Journal of the Royal Meteorological Society*, 144 (713). pp.
711 1140-1151. ISSN 1477-870X, 2018.

712 Chiodo, G., Oehrlein, J., Polvani, L.M. et al.: Insignificant influence of the 11-year solar cycle on the
713 North Atlantic Oscillation. *Nat. Geosci.* 12, 94–99, 2019.

714 Choi, J., and S.-W. Son: Stratospheric initial condition for skillful surface prediction in the ECMWF
715 model, *Geophysical Research Letters*, 21, 12556-12564, 2019.

716 Cohen J. and D. Entekhabi: Eurasian snow cover variability and northern hemisphere climate
717 variability. *Geophys. Res. Lett.*, 26, 345-348, 1999.

718 Cohen, J., and Jones, J.: A new index for more accurate winter predictions. *Geophysical Research*
719 *Letters*, 38, L21701, 2011.

720 Cohen J., Furtado JC, Jones J, Barlow M, Whittleston D, Entekhabi D.: Linking Siberian snow cover
721 to precursors of stratospheric variability. *J Clim.*, 27(14), 5422–5432, 2014.

722 Crutzen P.J.: Estimates of Possible Variations in Total Ozone Due to Natural Causes and Human
723 Activities. *Ambio*, 3, No. 6, 201-210, 1974.

724 Dai, A., Song, M.: Little influence of Arctic amplification on mid-latitude climate. *Nat. Clim. Chang.*
725 10, 231–237, 2020.

726 Davies, P.A., McCarthy, M., Christidis, N., Dunstone, N., Fereday, D., Kendon, M., Knight, J.R.,
727 Scaife, A.A. and Sexton, D.: The wet and stormy UK winter of 2019/2020. *Weather*,
728 <https://doi.org/10.1002/wea.3955>, 2021.

729 Domeisen, D. I. V., Sun, L., & Chen, G.: The role of synoptic eddies in the tropospheric response to
730 stratospheric variability. *Geophysical Research Letters*, 40, 1–5, 2013.

731 Domeisen, D. I. V., Badin, G., & Koszalka, I. M.: How Predictable Are the Arctic and North Atlantic
732 Oscillations? Exploring the Variability and Predictability of the Northern Hemisphere. *Journal of*
733 *Climate*, 31(3), 997–1014, 2018.

734 Domeisen, D. I. V.: Estimating the Frequency of Sudden Stratospheric Warming Events From Surface
735 Observations of the North Atlantic Oscillation. *Journal of Geophysical Research-Atmospheres*,
736 124(6), 3180–3194, 2019.

737 Domeisen, D. I. V., Garfinkel, C. I., & Butler, A. H.: The Teleconnection of El Niño Southern
738 Oscillation to the Stratosphere. *Reviews of Geophysics*, 57(1), 5–47, 2019.

739 Domeisen, D. I. V., & Butler, A. H.: Stratospheric drivers of extreme events at the Earth's surface.
740 *Communications Earth & Environment*, 1–8, 2020.

741 Domeisen, D.I.V., A.H. Butler, A.J. Charlton-Perez, B. Ayarzagüena, M.P. Baldwin, E. Dunn-
742 Sigouin, J.C. Furtado, C.I. Garfinkel, P. Hitchcock, A. Yu. Karpechko, H. Kim, J. Knight, A.L. Lang,
743 E.-P. Lim, A. Marshall, G. Roff, C. Schwartz, I.R. Simpson, S.-W. Son, M. Taguchi: The role of
744 stratosphere-troposphere coupling in sub-seasonal to seasonal prediction. 1. Predictability in the
745 Stratosphere, *J. Geophys. Res.*, 125, e2019JD030920, 2020a.

746 Domeisen, D.I.V., A.H. Butler, A.J. Charlton-Perez, B. Ayarzagüena, M.P. Baldwin, E. Dunn-
747 Sigouin, J.C. Furtado, C.I. Garfinkel, P. Hitchcock, A. Yu. Karpechko, H. Kim, J. Knight, A.L. Lang,
748 E.-P. Lim, A. Marshall, G. Roff, C. Schwartz, I.R. Simpson, S.-W. Son, M. Taguchi: The role of
749 stratosphere-troposphere coupling in sub-seasonal to seasonal prediction. 2. Predictability arising
750 from stratosphere-troposphere coupling, *J. Geophys. Res.*, 125, e2019JD030923, 2020b.

751 Douville H.: Stratospheric polar vortex influence on Northern Hemisphere winter climate variability.
752 *Geophys. Res. Lett.*, 36, L18703, 2009.

753 Eade R., D. Smith, A.A. Scaife and E. Wallace. Do seasonal to decadal climate predictions
754 underestimate the predictability of the real world? *Geophys. Res. Lett.*, 5620– 5628, 2014.

755 Farman, J., Gardiner, B. & Shanklin, J.: Large losses of total ozone in Antarctica reveal seasonal
756 ClO_x/NO_x interaction. *Nature* 315, 207–210, 1985.

757 Fels S.B.: Radiative–Dynamical Interactions in the Middle Atmosphere. *Advances in Geophysics*, 28,
758 Part A, 277-300, 1985.

759 Fereday D. R. et al.: Seasonal forecasts of northern hemisphere winter 2009/10. *Environ. Res. Lett.* 7,
760 034031, 2012.

761 Fereday D. et al.: Tropical rainfall drives stronger future ENSO-NAO teleconnection in CMIP5
762 models. *Geophys. Res. Lett.*, 47, e2020GL088664, 2020.

763 Fletcher, C. G., S. C. Hardiman, P. J. Kushner, and J. Cohen: The dynamical response to snow cover
764 perturbations in a large ensemble of atmospheric GCM integrations, *J. Climate*, 22(5), 1208-1222,
765 doi:10.1175/2008JCLI2505.1, 2009.

766 Furtado, J.C., Cohen, J.L., Butler, A.H. et al.: Eurasian snow cover variability and links to winter
767 climate in the CMIP5 models. *Clim Dyn* 45, 2591–2605, 2015.

768 Garfinkel, C.I., C. Schwartz, D.I.V. Domeisen, S.-W. Son, A.H. Butler, and I.P. White, Extratropical
769 atmospheric predictability from the Quasi-Biennial Oscillation in subseasonal forecast models, *Jour.*
770 *Geophys. Res.*, 123 (15), 7855-7866, 2018.

771 Garfinkel, C. I., Schwartz, C., Butler, A. H., Domeisen, D. I. V., Son, S.-W., & White, I. P.:
772 Weakening of the Teleconnection From El Niño–Southern Oscillation to the Arctic Stratosphere Over
773 the Past Few Decades: What Can Be Learned From Subseasonal Forecast Models? *Journal of*
774 *Geophysical Research-Atmospheres*, 124(14), 7683–7696, 2019.

775 Garfinkel, C.I. and C. Schwartz: MJO-related tropical convection anomalies lead to more accurate
776 stratospheric vortex variability in subseasonal forecast models, *GRL*, doi:10.1002/2017GL074470,
777 2017.

778 Garfinkel, C. I., Son, S.-W., Song, K., Aquila, V., and Oman, L. D.: Stratospheric variability
779 contributed to and sustained the recent hiatus in Eurasian winter warming, *Geophys. Res. Lett.*, 44,
780 374– 382, 2017.

781 Garfinkel C.I., C. Schwartz, D. I. P. Domeisen, S-W Son, A. H. Butler, I. P. White: Extratropical
782 atmospheric predictability from the Quasi-Biennial Oscillation in subseasonal forecast models , *JGR*,
783 doi: 10.1029/2018JD028724., 123 (15), 7855-7866, 2018.

784 Garfinkel, C. I., A.H. Butler, D. W. Waugh, M. M. Hurwitz, L. M. Polvani: Why might stratospheric
785 sudden warmings occur with similar frequency in El Nino and La Nina winters?, *J. Geophys. Res.*
786 *Atmos.*, 117, D19106, doi:10.1029/2012JD017777, 2012.

787 Garfinkel, C. I., Feldstein, S. B., Waugh, D. W., Yoo, C., and Lee, S.: Observed connection between
788 stratospheric sudden warmings and the Madden-Julian Oscillation, *Geophys. Res. Lett.*, 39, L18807,
789 2012.

790 Gerber, E. P., A. Butler, N. Calvo, A. Charlton-Perez, M. Giorgetta, E. Manzini, J. Perlwitz, L. M.
791 Polvani, F. Sassi, A. A. Scaife, T. A. Shaw, S.-W. Son and S. Watanabe: Assessing and
792 Understanding the Impact of Stratospheric Dynamics and Variability on the Earth System. *Bull.*
793 *Amer. Met. Soc.*, 93, 845-859, 2012.

794 Givon, Y., Garfinkel, C.I. and White, I.: Transient extratropical response to solar ultraviolet radiation
795 in the Northern Hemisphere winter. *Journal of Climate*, 34(9), pp.3367-3383, 2021.

796 Graversen, R. G., and B. Christiansen: Downward propagation from the stratosphere to the
797 troposphere: A comparison of the two hemispheres. *J. Geophys. Res. Atmos.*, 108, 4780, 2003.

798 Gray, L. J., et al.: Solar influences on climate, *Rev. Geophys.*, 48, RG4001, 2010.

799 Gray, L. J., Scaife, A. A., Mitchell, D. M., Osprey, S., Ineson, S., Hardiman, S., Butchart, N., Knight,
800 J., Sutton, R., and Kodera, K.: A lagged response to the 11 year solar cycle in observed winter
801 Atlantic/European weather patterns, *J. Geophys. Res. Atmos.*, 118, 13,405– 13, 420, 2013.

802 Gray, L. J., Anstey, J. A., Kawatani, Y., Lu, H., Osprey, S., and Schenzinger, V.: Surface impacts of
803 the Quasi-Biennial Oscillation, *Atmos. Chem. Phys.*, 18, 8227–8247, 2018.

804 Hall, R. J., Scaife, A. A., Hanna, E., Jones, J. M., & Erdélyi, R.: Simple statistical probabilistic
805 forecasts of the winter NAO. *Weather and Forecasting*, 32(4), 1585–1601, 2017.

806 Harari, O., C.I. Garfinkel, O. Morgenstern, G. Zeng, S. Tilmes, D. Kinnison, M. Deushi, P. Jockel, A.
807 Pozzer, and F. M. O'Connor, Influence of Arctic Stratospheric Ozone on Surface Climate in CCMI
808 models, *ACP*, doi: 10.5194/acp-2018-1031, 2019.

809 Hardiman, Steven C., Adam A. Scaife, Nick. J. Dunstone, and Lin Wang: Subseasonal vacillations in
810 the winter stratosphere, *Geophys. Res. Lett.*, 47, e2020GL087766, 2020a.

811 Hardiman, Steven C., Nick J. Dunstone, Adam A. Scaife, Doug M. Smith, Jeff R. Knight, Paul
812 Davies, Martin Claus, and Richard J. Greatbatch (2020b), Predictability of European winter 2019/20:
813 Indian Ocean dipole impacts on the NAO, *Atmos. Sci. Lett.* 2020, e1005, 2020b.

814 Hardiman, Steven C., Neal Butchart, Andrew J. Charlton-Perez, Tiffany A. Shaw, Hideharu Akiyoshi,
815 Andreas Baumgaertner, Slimane Bekki, Peter Braesicke, Martyn Chipperfield, Martin Dameris,
816 Rolando R. Garcia, Martine Michou, Steven Pawson, Eugene Rozanov, and Kiyotaka Shibata:

817 Improved predictability of the troposphere using stratospheric final warmings, *J. Geophys. Res.*, 116,
818 D18113, 11 PP., 2011.

819 Harnik N.. Observed stratospheric downward reflection and its relation to upward pulses of wave
820 activity. *J. Geophys. Res.*, 114, Article D08120, 2009.

821 Harnik, N. and R.S. Lindzen. The effect of reflecting surfaces on the vertical structure and variability
822 of stratospheric planetary waves. *J. Atmos. Sci.*, 58, 2872-2894, 2001.

823 Haynes, P. H., McIntyre, M. E., Shepherd, T. G., Marks, C. J., & Shine, K. P.: On the “Downward
824 Control” of Extratropical Diabatic Circulations by Eddy-Induced Mean Zonal Forces, *Journal of*
825 *Atmospheric Sciences*, 48(4), 651-678, 1991.

826 Haynes, P., Hitchcock, P., Hitchman, M., Yoden, S., Hendon, H., Kiladis, G., Kodera, K., Simpson,
827 I.: The influence of the stratosphere on the tropical troposphere. *J. Meteor. Soc. Japan*, 2021.

828 Haynes, P., Hitchcock, P., Hitchman, M., Yoden, S., Hendon, H., Kiladis, G., Kodera, K., Simpson,
829 I.: The influence of the stratosphere on the tropical troposphere. *J. Meteor. Soc. Japan*, (accepted
830 subject to final small changes), 2021.

831 Henderson GR, Peings Y, Furtado JC, Kushner PJ: Snow-atmosphere coupling in the northern
832 hemisphere. *Nat Clim Change* 8(11), 954–963, 2018

833 Hendon, H. H., and S. Abhik: Differences in vertical structure of the Madden-Julian oscillation
834 associated with the quasi-biennial oscillation. *Geophys. Res. Lett.*, 45, 4419–4428, 2018.

835 Hendon, H. H., E. -P. Lim, and S. Abhik: Impact of Interannual Ozone Variations on the Downward
836 Coupling of the 2002 Southern Hemisphere Stratospheric Warming. *J. Geophys. Res. Atmos.*, 1–16,
837 doi:10.1029/2020JD032952, 2020.

838 Hermanson L., R. Eade, N.H. Robinson , M.B. Andrews , J.R. Knight, A.A. Scaife and D.M. Smith,
839 Forecast cooling of the Atlantic subpolar gyre and associated impacts. *Geophys. Res. Lett.*, 41, 5167-
840 5174, 2014.

841 Hitchcock, P., Shepherd, T.G., Taguchi, M., Yoden, S. and Noguchi, S.: Lower-stratospheric radiative
842 damping and Polar-night Jet Oscillation events. *J. Atmos. Sci.*, 70, 1391–1408, 2013.

843 Hitchcock, P., & Simpson, I. R.: The Downward Influence of Stratospheric Sudden Warmings,
844 *Journal of the Atmospheric Sciences*, 71(10), 3856-3876, 2014.

845 Hitchcock, P., Haynes, P.H.: Stratospheric control of planetary waves. *Geophys. Res. Lett.*, 43,
846 11,884–11,892, doi:10.1002/2016GL071372, 2016.

847 Holton, J.R., H.-C. Tan. The influence of the equatorial quasi-biennial oscillation on the global
848 circulation at 50 mb. *J. Atmos. Sci.*, 37, 2200-2208, 1980.

849 Honda, M., Inoue, J., and Yamane, S.: Influence of low Arctic sea-ice minima on anomalously cold
850 Eurasian winters, *Geophys. Res. Lett.*, 36, L08707, doi:10.1029/2008GL037079, 2009.

851 Huebener H, Cubasch U, Langematz U, Spanghel T, Niehörster F, Fast I and Kunze M.: Ensemble
852 climate simulations using a fully coupled ocean–troposphere–stratosphere general circulation
853 model. *Phil. Trans. R. Soc. A*.3652089–2101, 2007.

854 Hurwitz, M. M., Newman, P. A., and Garfinkel, C. I.: On the influence of North Pacific sea surface
855 temperature on the Arctic winter climate, *J. Geophys. Res.*, 117, D19110, 2012.

856 Ineson S. and Scaife A.A.: The role of the stratosphere in the European climate response to El Nino.
857 *Nature Geoscience*, 2, 32-36, 2009.

858 Ineson S., A. A. Scaife, J.R. Knight, J.C. Manners, N.J. Dunstone, L.J. Gray and J.D. Haigh: Solar
859 Forcing of Winter Climate Variability in the Northern Hemisphere. *Nat. Geosci.*, 4, 753-757, 2011.

860 Ineson, S., Maycock, A., Gray, L. *et al.*: Regional climate impacts of a possible future grand solar
861 minimum. *Nat Commun* 6, 7535, 2015.

862 Inoue, M., M. Takahashi, H. Naoe: Relationship between the stratospheric quasi-biennial oscillation
863 and tropospheric circulation in northern autumn. *J. Geophys. Res. Atmos.*, 116, 2011.

864 Jain, S., Scaife, A.A. & Mitra, A.K.: Skill of Indian summer monsoon rainfall prediction in multiple
865 seasonal prediction systems. *Clim Dyn* 52, 5291–5301, 2019.

866 Jaiser R, Dethloff K, Handorf D. Stratospheric response to arctic sea ice retreat and associated
867 planetary wave propagation changes. *Tellus A Dyn Meteorol Oceanogr* 65(1):19375, 2013.

868 Jia, L., Yang, X., Vecchi, G., Gudgel, R., Delworth, T., Fueglistaler, S., Lin, P., Scaife, A. A.,
869 Underwood, S., and Lin, S.: Seasonal Prediction Skill of Northern Extratropical Surface Temperature
870 Driven by the Stratosphere, *Journal of Climate*, 30(12), 4463-4475, 2017.

871 Johnson, S. J., Stockdale, T. N., Ferranti, L., Balmaseda, M. A., Molteni, F., Magnusson, L., Tietsche,
872 S., Decremet, D., Weisheimer, A., Balsamo, G., Keeley, S. P. E., Mogensen, K., Zuo, H., and Monge-
873 Sanz, B. M.: SEAS5: the new ECMWF seasonal forecast system, *Geosci. Model Dev.*, 12, 1087–
874 1117, 2019.

875 Joshi, M. M., A. J. Charlton, and A. A. Scaife: On the influence of stratospheric water vapor changes
876 on the tropospheric circulation. *Geophys. Res. Lett.*, 33, L09806, 2006.

877 Jucker, M., & Reichler, T.: Dynamical precursors for statistical prediction of stratospheric sudden
878 warming events. *Geophysical Research Letters*, 45, 13,124– 13,132, 2018.

879 Jucker, M., Reichler, T., & Waugh, D. W.: How frequent are Antarctic sudden stratospheric warmings
880 in present and future climate? *Geophysical Research Letters*, 48, e2021GL093215, 2021.

881 Kang, I.S., Kug, JS., Lim, MJ. et al: Impact of transient eddies on extratropical seasonal-mean
882 predictability in DEMETER models. *Clim Dyn* 37, 509–519, 2011.

883 Kang, S.M., L.M. Polvani, J.C. Fyfe and M. Sigmond: Impact of Polar Ozone Depletion on
884 Subtropical Precipitation, *Science*, 332, 951-954, 2011.

885 Karpechko A., N.P. Gillett, G.J. Marshall and A.A. Scaife: Stratospheric influence on circulation
886 changes in the Southern Hemisphere troposphere in coupled climate models. *Geophys. Res. Lett.*,
887 L20806, 2008.

888 Karpechko, A. Y., and Manzini, E.: Stratospheric influence on tropospheric climate change in the
889 Northern Hemisphere, *J. Geophys. Res.*, 117, D05133, doi:10.1029/2011JD017036, 2012.

890 Karpechko, A. Yu., J. Perlwitz, and E. Manzini: A model study of tropospheric impacts of the Arctic
891 ozone depletion 2011, *J. Geophys. Res. Atmos.*, 119, 7999–8014, 2014

892 Karpechko A. Yu., P. Hitchcock, D. H.W. Peters, A. Schneidereit: Predictability of downward
893 propagation of sudden stratospheric warmings, *Quart. J. Roy. Meteor. Soc.*, v. 143, 704, 1459-1470,
894 2017.

895 Karpechko A. Y., A. Charlton-Perez, M. Balmaseda, N. Tyrrell, and F. Vitart: Predicting sudden
896 stratospheric warming 2018 and its climate impacts with a multimodel ensemble, *Geophys. Res. Lett.*,
897 45, 13538–13546, 2018.

- 898 Karpechko A. Yu.: Predictability of Sudden Stratospheric Warmings in the ECMWF Extended-Range
899 Forecast System, *Mon. Wea. Rev.*, 146(4), 1063–1075, doi: 10.1175/MWR-D-17-0317.1, 2018.
- 900 Karpechko, AY, Tyrrell, NL, Rast, S.: Sensitivity of QBO teleconnection to model circulation biases.
901 *Q J R Meteorol Soc.* 147, 2147– 2159, 2021.
- 902 Kautz, L. A., Polichtchouk, I., Birner, T., Garny, H., and Pinto, J. G.: Enhanced extended-range
903 predictability of the 2018 late-winter Eurasian cold spell due to the stratosphere, *Q. J. Roy.*
904 *Meteorol.Soc.*, 146, 1040–1055, 2019.
- 905 Kidston, J., A. A. Scaife, S. C. Hardiman, D. M. Mitchell, N. Butchart, M. P. Baldwin and L. J. Gray.
906 Stratospheric influence on tropospheric jet streams, storm tracks and surface weather, *Nature*
907 *Geoscience*, 8, 433–440, 2015.
- 908 Kim, BM., Son, SW., Min, SK. et al.: Weakening of the stratospheric polar vortex by Arctic sea-ice
909 loss. *Nat Comm.*, 5, 4646, 2014.
- 910 Kim, H., Caron, J. M., Richter, J. H., & Simpson, I. R.: The lack of QBO-MJO connection in CMIP6
911 models. *Geophysical Research Letters*, 47, e2020GL087295, 2020.
- 912 King, M.P., Hell, M. & Keenlyside, N. Investigation of the atmospheric mechanisms related to the
913 autumn sea ice and winter circulation link in the Northern Hemisphere. *Clim. Dyn.*, 46, 1185–1195,
914 2016.
- 915 King, A. D., A.H. Butler, M. Jucker, N.O. Earl, and I. Rudeva, Observed relationships between
916 sudden stratospheric warmings and European climate extremes, *J. Geophys. Res.*, 124, 13943-13961,
917 2019.
- 918 Kodera, K. and Kuroda, Y. Dynamical response to the solar cycle. *J. Geophys. Res.* 107, 4749, 2002.
- 919 Kolstad, E. W., & Screen, J. A.. Non-stationary relationship between autumn Arctic sea ice and the
920 winter North Atlantic Oscillation. *Geophysical Research Letters*, 46, 7583– 7591, 2019.
- 921 Knight J. et al.: Predictability of European winters 2017/2018 and 2018/2019: Contrasting Influences
922 from the Tropics and Stratosphere. *Atm. Sci. Lett.*, e1009, doi.org/10.1002/asl.1009, 2020.
- 923 Kodera, K., Yamazaki, K., Chiba, M., Shibata, K.: Downward propagation of upper stratospheric
924 mean zonal wind perturbation to the troposphere. *Geophys. Res. Lett.*, 17, 9, 0094-8276, 1990.
- 925 Kodera, K.: On the origin and nature of the interannual variability of the winter stratospheric
926 circulation in the northern hemisphere, *J. Geophys. Res.*, 100 (D7), 14077– 14087, 1995.
- 927 Kodera, K., Mukougawa, H., and Itoh, S.: Tropospheric impact of reflected planetary waves from the
928 stratosphere, *Geophys. Res. Lett.*, 35, L16806, doi:10.1029/2008GL034575, 2008.
- 929 Kretschmer, M., Coumou, D., Donges, J.F., and Runge, J.: Using causal effect networks to analyze
930 different Arctic drivers of midlatitude winter circulation. *J. Clim.*, 29, 4069–4081, 2016.
- 931 Kretschmer, M., Zappa, G. and Shepherd, T.G.: The role of Barents-Kara sea ice loss in projected
932 polar vortex changes. *Wea. Clim. Dyn.*, 1, 715–730, 2020.
- 933 Kretschmer, M., Adams, S.V., Arribas, A., Prudden, R., Robinson, N., Saggioro, E. and Shepherd,
934 T.G.: Quantifying causal pathways of teleconnections. *Bull. Amer. Meteor. Soc.*, in press, doi:
935 10.1175/BAMS-D-20-0117.1, 2021.
- 936 Kuhn, T. S.: *The Structure of Scientific Revolutions*. University of Chicago Press, 1970.
- 937 Kunz, T., & Greatbatch, R. J.: On the Northern Annular Mode Surface Signal Associated with
938 Stratospheric Variability, *Journal of the Atmospheric Sciences*, 70(7), 2103-2118, 2013.

939 Kuroda, Y.: Role of the stratosphere on the predictability of medium-range weather forecast: A case
940 study of winter 2003–2004. *Geophysical Research Letters*, 35, L19701, 2008.

941 Kushnir, Y., Scaife, A.A., Arritt, R. et al.: Towards operational predictions of the near-term climate.
942 *Nature Clim. Change* 9, 94–101, 2019.

943 Kushner P.J. and L.M. Polvani: Stratosphere-troposphere coupling in a relatively simple AGCM: The
944 role of eddies, *J. Climate*, 17, 629-639, 2004.

945 Labe, Z., Peings, Y., & Magnusdottir, G.: The effect of QBO phase on the atmospheric response to
946 projected Arctic sea ice loss in early winter. *Geophysical Research Letters*, 46, 7663– 7671, 2019.

947 Labitzke, K.: On the Mutual Relation between Stratosphere and Troposphere during Periods of
948 Stratospheric Warmings in Winter, *J. Appl. Met. Climatol.*, 4(1), 91-99, 1965.

949 Lai, W. K. M., Robson, J. I., Wilcox, L. J., & Dunstone, N. Mechanisms of Internal Atlantic
950 Multidecadal Variability in HadGEM3-GC3.1 at Two Different Resolutions, *Journal of Climate*,
951 2021.

952 Lawrence, Z. D., Perlwitz, J., Butler, A. H., Manney, G. L., Newman, P. A., Lee, S. H., & Nash, E.
953 R.: The remarkably strong Arctic stratospheric polar vortex of winter 2020: Links to record-breaking
954 Arctic Oscillation and ozone loss. *Journal of Geophysical Research: Atmospheres*, 125,
955 e2020JD033271, 2020.

956 Leckebusch, G. C., Ulbrich, U., Fröhlich, L., and Pinto, J. G.: Property loss potentials for European
957 midlatitude storms in a changing climate, *Geophys. Res. Lett.*, 34, L05703, 2007.

958 Lee, SH, Charlton-Perez, AJ, Furtado, JC, Woolnough, SJ. Representation of the Scandinavia–
959 Greenland pattern and its relationship with the polar vortex in S2S forecast models. *Q J R Meteorol*
960 *Soc.* 146: 4083– 4098, 2020a.

961 Lee, S.H., Z.D. Lawrence, A.H. Butler, and A. Karpechko. Seasonal forecasts of the exceptional
962 Northern Hemisphere winter of 2020, *Geophys. Res. Lett.*, 47, e2020GL090328, 2020b.

963 Leung, T.Y., Leutbecher, M., Reich, and Shepherd, T.G.. Impact of the mesoscale range on error
964 growth and the limits to atmospheric predictability. *J. Atmos. Sci.*, 77, 3769–3779, 2020.

965 L'Heureux, M.L., Levine, A.F.Z., Newman, M., Ganter, C., Luo, J.-J., Tippett, M.K. and Stockdale,
966 T.N.: ENSO Prediction. In *El Niño Southern Oscillation in a Changing Climate* (eds M.J. McPhaden,
967 A. Santoso and W. Cai), 2020.

968 Lim, E.-P., H. H. Hendon, and D. W. J. Thompson: Seasonal evolution of stratosphere-troposphere
969 coupling in the Southern Hemisphere and implications for the predictability of surface climate. *J.*
970 *Geophys. Res. Atmos.*, 123, 12,002–12,016, 2018.

971 Lim, E.-P., H. H. Hendon, G. Boschat, D. Hudson, D. W. J. Thompson, A. J. Dowdy, and J. Arblaster:
972 Australian hot and dry extremes induced by weakening of the stratospheric polar vortex. *Nature*
973 *Geoscience*, 12 (11), 896-901, 2019.

974 Lim, E.-P., and Coauthors: The 2019 Southern Hemisphere polar stratospheric warming and its
975 impacts. *BAMS*. 102 (6), E1150-E1171, 2021.

976 Lim, Y., S.-W. Son, A. G. Marshall, H. H. Hendon, and K.-H. Seo: Influence of the QBO on MJO
977 prediction skill in the subseasonal-to-seasonal prediction models, *Climate Dynamics*, 53, 1681-1695,
978 2019.

979 Lin, H., Brunet, G., & Derome, J.: An Observed Connection between the North Atlantic Oscillation
980 and the Madden–Julian Oscillation, *Journal of Climate*, 22(2), 364-380, 2009.

981 Lockwood, M.: Solar change and climate: An update in the light of the current exceptional solar
982 minimum, *Proc. R. Soc. A*, 466, 303–329, 2010.

983 Lorenz, E.N.: The predictability of a flow which possesses many scales of motion. *Tellus*, 21: 289-
984 307, 1969.

985 Manzini, E., Giorgetta, M. A., Esch, M., Kornblueh, L., & Roeckner, E.: The Influence of Sea Surface
986 Temperatures on the Northern Winter Stratosphere: Ensemble Simulations with the MAECHAM5
987 Model, *Journal of Climate*, 19(16), 3863-3881, 2006.

988 Manzini, E., Karpechko, A. Y., and Kornblueh, L.: Nonlinear Response of the Stratosphere and the
989 North Atlantic-European Climate to Global Warming, *Geophys. Res. Lett.*, 45, 4255–4263, 2018.

990 Mariotti, A., C. Baggett, E. A. Barnes, E. Becker, A.H. Butler, D.C. Collins, P.A. Dirmeyer, L.
991 Ferranti, N.C. Johnson, J. Jones, B. P. Kirtman, A.L. Lang, A. Molod, M. Newman, A.W. Robertson,
992 S. Schubert, Waliser, D.E. and J. Albers, Windows of opportunity for skillful forecasts subseasonal to
993 seasonal and beyond, *BAMS*, 101, E608-E625, 2020.

994 Marsh, D. R., Garcia, R. R., Kinnison, D. E., Boville, B. A., Sassi, F., Solomon, S. C., and Matthes,
995 K.: Modeling the whole atmosphere response to solar cycle changes in radiative and geomagnetic
996 forcing, *J. Geophys. Res.*, 112, D23306, 2007.

997 Marshall A. and A.A. Scaife: Improved predictability of stratospheric sudden warming events in an
998 AGCM with enhanced stratospheric resolution. *J. Geophys. Res.*, 115, D16114, 2010.

999 Marshall, A.G., Hendon, H.H., Son, S.W. and Lim, Y.: Impact of the quasi-biennial oscillation on
1000 predictability of the Madden–Julian oscillation. *Climate Dynamics*, 49(4), pp.1365-1377, 2017.

1001 Martin, Z., Wang, S., Nie, J., & Sobel, A.: The Impact of the QBO on MJO Convection in Cloud-
1002 Resolving Simulations, *Journal of the Atmospheric Sciences*, 76(3), 669-688, 2019.

1003 Martin, Z., Son, SW., Butler, A. et al.: The influence of the quasi-biennial oscillation on the Madden–
1004 Julian oscillation. *Nat Rev Earth Environ* 2, 477–489, 2021.

1005 Matthias, V., & Kretschmer, M.: The Influence of Stratospheric Wave Reflection on North American
1006 Cold Spells, *Monthly Weather Review*, 148(4), 1675-1690, 2020.

1007 Maycock, A. C., Ineson, S., Gray, L. J., Scaife, A. A., Anstey, J. A., Lockwood, M., Butchart, N.,
1008 Hardiman, S. C., Mitchell, D. M., and Osprey, S. M.: Possible impacts of a future grand solar
1009 minimum on climate: Stratospheric and global circulation changes, *J. Geophys. Res. Atmos.*, 120,
1010 9043– 9058, 2015.

1011 McKenna, C.M., Bracegirdle, T.J., Shuckburgh, E.F., Haynes, P.H., Joshi, M.M.: Arctic sea-ice loss
1012 in different regions leads to contrasting Northern Hemisphere impacts. *Geophys. Res. Lett.*, 45, 945–
1013 954, 2018.

1014 MacLachlan, C., Arribas, A., Peterson, K.A., Maidens, A., Fereday, D., Scaife, A.A., Gordon, M.,
1015 Vellinga, M., Williams, A., Comer, R.E., Camp, J., Xavier, P. and Madec, G.: Global Seasonal
1016 forecast system version 5 (GloSea5): a high-resolution seasonal forecast system. *Q.J.R. Meteorol.*
1017 *Soc.*, 141: 1072-1084, 2015.

1018 Mann, M. E., J. Park, and R. S. Bradley. Global interdecadal and century-scale climate oscillations
1019 during the past 5 centuries, *Nature*, 378, 266 – 270, 1995.

1020 McLandress, C. and Shepherd, T.G.: Impact of climate change on stratospheric sudden warmings as
1021 simulated by the Canadian Middle Atmosphere Model. *J. Clim.*, 22, 5449–5463, 2009.

- 1022 McLandress, C., Shepherd, T.G., Scinocca, J.F., Plummer, D.A., Sigmond, M., Jonsson, A.I. and
 1023 Reader, M.C.: Separating the dynamical effects of climate change and ozone depletion: Part 2.
 1024 Southern Hemisphere Troposphere. *J. Clim.*, 24, 1850–1868, 2011.
- 1025 Meehl G. et al.: Initialised Earth System Prediction from Subseasonal to Decadal Timescales. *Nat.*
 1026 *Rev. Earth. Environ.* 2, 340–357, 2021.
- 1027 Merryfield, W.J., J. Baehr, L. Batté, E.J. Becker, A.H. Butler, et al., Current and emerging
 1028 developments in subseasonal to decadal prediction, *BAMS*, 101, E869–E896, 2020.
- 1029 Merryfield, W. J., F. J. Doblas-Reyes, L. Ferranti, J.-H. Jeong, Y. J. Orsolini, R. I. Saurral, A. A.
 1030 Scaife, M. A. Tolstykh, and M. Rixen. Advancing climate forecasting. *EOS*, 98, 17-21, 2017.
- 1031 Merryfield, W. J., Lee, W., Boer, G. J., Kharin, V. V., Scinocca, J. F., Flato, G. M., Ajayamohan, R.
 1032 S., Fyfe, J. C., Tang, Y., & Polavarapu, S.: The Canadian Seasonal to Interannual Prediction System.
 1033 Part I: Models and Initialization, *Monthly Weather Review*, 141(8), 2910-2945, 2013.
- 1034 Mechoso, C.R., A. Molod, A. O'Neill, R.B. Pierce, W.J. Randel, R.B. Rood, F. Wu: The GCM-
 1035 Reality Intercomparison Project for SPARC (GRIPS): Scientific Issues and Initial Results. *Bull.*
 1036 *Amer. Met. Soc.*, 81, 781-796, 2000.
- 1037 Molina, M., Rowland, F.: Stratospheric sink for chlorofluoromethanes: chlorine atom-catalysed
 1038 destruction of ozone. *Nature* 249, 810–812, 1974.
- 1039 Monge-Sanz, B., et al.: A stratospheric prognostic ozone for seamless Earth System Models:
 1040 performance, impacts and future. *Atmos. Chem. Phys. Disc.*, doi: 10.5194/acp-2020-1261, 2021.
- 1041 Müller, W. A., and Roeckner, E.: ENSO impact on midlatitude circulation patterns in future climate
 1042 change projections, *Geophys. Res. Lett.*, 33, L05711, 2006.
- 1043 Mukougawa, H., Sakai, H., & Hirooka, T.: High sensitivity to the initial condition for the prediction
 1044 of stratospheric sudden warming. *Geophysical Research Letters*, 32, L17806, 2005.
- 1045 Mukougawa, H., Hirooka, T., and Kuroda, Y.: Influence of stratospheric circulation on the
 1046 predictability of the tropospheric Northern Annular Mode, *Geophys. Res. Lett.*, 36, L08814,
 1047 doi:10.1029/2008GL037127, 2009.
- 1048 Mukougawa, H., Noguchi, S., Kuroda, Y., Mizuta, R., & Kodera, K.: Dynamics and predictability of
 1049 downward-propagating stratospheric planetary waves observed in March 2007. *Journal of the*
 1050 *Atmospheric Sciences*, 74(11), 3533–3550, 2017.
- 1051 Nie Y. et al.: Stratospheric initial conditions provide seasonal predictability of the North Atlantic and
 1052 Arctic Oscillations. *Env. Res. Lett.*, 14, 3, 2019.
- 1053 Noguchi, S., Mukougawa, H., Kuroda, Y., Mizuta, R., Yabu, S., & Yoshimura, H.: Predictability of
 1054 the stratospheric polar vortex breakdown: An ensemble reforecast experiment for the splitting event in
 1055 January 2009. *Journal of Geophysical Research: Atmospheres*, 121, 3388–3404, 2016.
- 1056 Noguchi, S., Kuroda, Y., Mukougawa, H., Mizuta, R., & Kobayashi, C.: Impact of satellite
 1057 observations on forecasting sudden stratospheric warmings. *Geophysical Research Letters*, 47,
 1058 e2019GL086233, 2020a.
- 1059 Noguchi, S., Kuroda, Y., Kodera, K., & Watanabe, S.: Robust enhancement of tropical convective
 1060 activity by the 2019 Antarctic sudden stratospheric warming. *Geophysical Research Letters*, 47,
 1061 e2020GL088743, 2020b.

- 1062 Oehrlein J., G. Chiodo and L.M. Polvani: The effect of interactive ozone chemistry on weak and
1063 strong stratospheric polar vortex events, *Atmos. Chem. Phys.*, 20, 10531-10544, 2020.
- 1064 Omrani, NE., Keenlyside, N.S., Bader, J. et al.: Stratosphere key for wintertime atmospheric response
1065 to warm Atlantic decadal conditions. *Clim Dyn* 42, 649–663, 2014.
- 1066 O'Reilly CH, Weisheimer A, Woollings T, Gray LJ, MacLeod D: The importance of stratospheric
1067 initial conditions for winter North Atlantic Oscillation predictability and implications for the signal-
1068 to-noise paradox. *Q J R Meteorol Soc* 145(718):131–146, 2019.
- 1069 Orsolini YJ, Senan R, Benestad RE, Melsom A. Autumn atmospheric response to the 2007 low Arctic
1070 sea ice extent in coupled ocean–atmosphere hindcasts. *Clim Dyn* 38:2437–2448, 2012.
- 1071 Owens, M.J., Mike Lockwood, Ed Hawkins, Ilya Usoskin, Gareth S. Jones, Luke Barnard, Andrew
1072 Schurer and John Fasullo: The Maunder minimum and the Little Ice Age: an update from recent
1073 reconstructions and climate simulations. *J. Space Weather Space Clim.*, 7 (2017) A33, 2017.
- 1074 Pawson, S. and B. Naujokat: The cold winters of the middle 1990s in the northern lower stratosphere.
1075 *J. Geophys. Res.*, 104, 14 209–14 222, 1999.
- 1076 Pawson, S., Kodera, K., Hamilton, K., Shepherd, T. G., Beagley, S. R., Boville, B. A., Farrara, J. D.,
1077 Fairlie, T. D. A., Kitoh, A., Lahoz, W. A., Langematz, U., Manzini, E., Rind, D. H., Scaife, A. A.,
1078 Shibata, K., Simon, P., Swinbank, R., Takacs, L., Wilson, R. J., Al-Saadi, J. A., Amodei, M., Chiba,
1079 M., Coy, L., de Grandpré, J., Eckman, R. S., Fiorino, M., Grose, W. L., Koide, H., Koshyk, J. N., Li,
1080 D., Lerner, J., Mahlman, J. D., McFarlane, N. A., Mechoso, C. R., Molod, A., O'Neill, A., Pierce, R.
1081 B., Randel, W. J., Rood, R. B., & Wu, F.: The GCM-Reality Intercomparison Project for SPARC
1082 (GRIPS): Scientific Issues and Initial Results, *Bulletin of the American Meteorological Society*, 81(4),
1083 781-796, 2000.
- 1084 Peings, Y. E. Brun, V. Mauvais, H. Douville: How stationary is the relationship between Siberian
1085 snow and Arctic Oscillation over the 20th century? *Geophys. Res. Lett.*, 40, 183-188, 2013.
- 1086 Perlwitz, J., and N. Harnik: Observational evidence of a stratospheric influence on the troposphere by
1087 planetary wave reflection, *J. Clim.*, 16, 3011–3026, 2003.
- 1088 Perlwitz, J., & Graf, H.: The Statistical Connection between Tropospheric and Stratospheric
1089 Circulation of the Northern Hemisphere in Winter, *Journal of Climate*, 8(10), 2281-2295, 1995.
- 1090 Plumb, R. A., and Semeniuk, K.: Downward migration of extratropical zonal wind anomalies, *J.*
1091 *Geophys. Res.*, 108, 4223, doi:10.1029/2002JD002773, D7, 2003.
- 1092 Polvani L.M. and P.J. Kushner: Tropospheric response to stratospheric perturbations in a relatively
1093 simple general circulation model, *Geophys. Res. Lett.*, 29, no. 7 (2002) Liu C., B. Tian, K.-F. Li, G.L.
1094 Manney, N.J. Livesey, Y.L. Yung, D.E. Waliser. Northern Hemisphere mid-winter vortex-
1095 displacement and vortex-split stratospheric sudden warmings: influence of the Madden-Julian
1096 Oscillation and Quasi-Biennial Oscillation. *J. Geophys. Res. Atmos.*, 119, 12,599-12,620, 2014.
- 1097 Polvani, L.M., D.W. Waugh, G.J.P. Correa and S.-W. Son: Stratospheric ozone depletion: the main
1098 driver of 20th Century atmospheric circulation changes in the Southern Hemisphere, *J. Climate*, 24,
1099 795-812, 2011.
- 1100 Polvani L.M., L. Sun, A.H. Butler, J.H. Richter and C. Deser: Distinguishing stratospheric sudden
1101 warmings from ENSO as key drivers of wintertime climate variability over the North Atlantic and
1102 Eurasia, *J. Clim.*, 30, 1959-1969, 2017.
- 1103 Polvani, L. M., and Kushner, P. J., Tropospheric response to stratospheric perturbations in a relatively
1104 simple general circulation model, *Geophys. Res. Lett.*, 29(7), doi:10.1029/2001GL014284, 2002.

- 1105 Polvani, L.M., L. Sun, A.H. Butler, J.H. Richter and C. Deser: Distinguishing stratospheric sudden
 1106 warmings from ENSO as key drivers of wintertime climate variability over the North Atlantic and
 1107 Eurasia, *J. Climate*, 30, 1959-1969, 2017.
- 1108 Previdi, M. and L.M. Polvani: Climate System Response to Stratospheric Ozone Depletion and
 1109 Recovery, *Quart. J. Roy. Meteor. Soc.*, 140, 2401-2419, 2014.
- 1110 Purich, A., and S.-W. Son: Impact of Antarctic ozone depletion and recovery on Southern Hemisphere
 1111 precipitation, evaporation and extreme changes, *Journal of Climate*, 25, 3145-3154, 2012.
- 1112 Rao, J., C. I. Garfinkel, and I. P. White: Predicting the downward and surface influence of the
 1113 February 2018 and January 2019 sudden stratospheric warming events in subseasonal to seasonal
 1114 (S2S) models, *Journal of Geophysical Research: Atmospheres*, 125, 2020a
- 1115 Rao, J., C. I. Garfinkel, I. P. White, C. Schwartz: How does the Quasi-Biennial Oscillation affect the
 1116 boreal winter tropospheric circulation in CMIP5/6 models?, *Journal of Climate*, 33, 8975-8996,
 1117 2020b.
- 1118 Rao, J. and C. I. Garfinkel: CMIP5/6 Models Project Little Change in the Statistical Characteristics of
 1119 Sudden Stratospheric Warmings in the 21st Century, *Environmental Research Letters*, 2020c.
- 1120 Rao, J., C. I. Garfinkel, and I. P. White: Projected strengthening of the extratropical surface impacts
 1121 of the stratospheric Quasi Biennial Oscillation, *Geophysical Research Letters*, 47, e2020GL089149,
 1122 2020d.
- 1123 Rao, J., C. I. Garfinkel, I. P. White, C. Schwartz: The Southern Hemisphere Minor Sudden
 1124 Stratospheric Warming in September 2019 and its predictions in S2S Models , *Journal of Geophysical
 1125 Research: Atmospheres*, 125, e2020JD032723, doi:10.1029/2020JD032723, 2020e.
- 1126 Rao, J. and Garfinkel, C.I.: The Strong Stratospheric Polar Vortex in March 2020 in Sub-Seasonal to
 1127 Seasonal Models: Implications for Empirical Prediction of the Low Arctic Total Ozone Extreme.
 1128 *Journal of Geophysical Research: Atmospheres*, 126(9), p.e2020JD034190., 2021a.
- 1129 Rao, J., Garfinkel, C. I., & White, I. P. Development of the Extratropical Response to the Stratospheric
 1130 Quasi-Biennial Oscillation. *Journal of Climate*, 34(17), 7239-7255, 2021. Reichler, T., Kim, J.,
 1131 Manzini, E., & Kröger, J. A stratospheric connection to Atlantic climate variability. *Nature
 1132 Geoscience*, 5(11), 783–787, 2012.
- 1133 Richter, J. H., Pegion, K., Sun, L., Kim, H., Caron, J. M., Glanville, A., LaJoie, E., Yeager, S., Kim,
 1134 W. M., Tawfik, A., & Collins, D.: Subseasonal Prediction with and without a Well-Represented
 1135 Stratosphere in CESM1, *Weather and Forecasting*, 35(6), 2589-2602, 2020a.
- 1136 Richter, J. H., Anstey, J. A., Butchart, N., Kawatani, Y., Meehl, G. A., Osprey, S., & Simpson, I.
 1137 R.: Progress in simulating the quasi-biennial oscillation in CMIP models. *Journal Geophysical
 1138 Research: Atmospheres*, 125, e2019JD032362, 2020b.
- 1139 Richter, JH, Butchart, N, Kawatani, Y, et al.: Response of the Quasi-Biennial Oscillation to a
 1140 warming climate in global climate models. *Q J R Meteorol Soc.*; 1– 29, 2020c.
- 1141 Riddle, E.E., A.H. Butler, J.C. Furtado, J.L. Cohen, and A. Kumar, CFSv2 ensemble prediction of the
 1142 wintertime Arctic Oscillation, *Climate Dynamics*, 41, 1099-1116, 2013.
- 1143 Rind, D., Suozzo, R., Balachandran, N. K., Lacis, A., & Russell, G.. The GISS global climate-middle
 1144 atmosphere model. Part I: Model structure and climatology. *Journal of the Atmospheric Sciences*, 45,
 1145 329– 370, 1988.
- 1146 Roff, G., D. W. J. Thompson, and H. Hendon: Does increasing model stratospheric resolution
 1147 improve extended-range forecast skill? *Geophys. Res. Lett.*, 38, L05809, 2011.

- 1148 Runde, T., Dameris, M., Garny, H., & Kinnison, D. E.: Classification of stratospheric extreme events
1149 according to their downward propagation to the troposphere. *Geophysical Research Letters*, 43(12),
1150 6665–6672, 2016.
- 1151 Saito, N., Maeda, S., Nakaegawa, T., Takaya, Y., Imada, Y., & Matsukawa C.: Seasonal predictability
1152 of the North Atlantic Oscillation and zonal mean fields associated with stratospheric influence in
1153 JMA/MRI-CPS2. *Scientific Online Letters on the Atmosphere*, 13, 209–213, 2017.
- 1154 Samarasinghe, S. M., Connolly, C., Barnes, E. A., Ebert-Uphoff, I., & Sun, L.: Strengthened causal
1155 connections between the MJO and the North Atlantic with climate warming. *Geophysical Research*
1156 *Letters*, 48, e2020GL091168, 2021.
- 1157 Sassi, F., Garcia, R. R., Boville, B. A., and Liu, H.: On temperature inversions and the mesospheric
1158 surf zone, *J. Geophys. Res.*, 107(D19), 4380, 2002.
- 1159 Scaife A.A., T. Spanghel, D. Fereday, U. Cubasch, U. Langematz, H. Akiyoshi, S. Bekki, P.
1160 Braesicke, N. Butchart, M. Chipperfield, A. Gettelman, S. Hardiman, M. Michou, E. Rozanov and
1161 T.G. Shepherd. *Climate Change and Stratosphere-Troposphere Interaction*. *Clim. Dyn.*, 38, Page
1162 2089-2097, 2012.
- 1163 Scaife A.A., N. Butchart, C.D. Warner, D. Stainforth, W.A. Norton and J. Austin. Realistic Quasi-
1164 Biennial Oscillations in a simulation of the global climate. *Geophys. Res. Let.* 27, 3481-3484, 2000.
- 1165 Scaife A.A., J.R. Knight, G.K. Vallis, C.K. Folland. A stratospheric influence on the winter NAO and
1166 North Atlantic surface climate. *Geophys. Res. Let.*, 32, L18715, 2005.
- 1167 Scaife A.A. and J.R. Knight. Ensemble simulations of the cold European winter of 2005/6. *Q. J. R.*
1168 *Meteorol. Soc.*, 134, 1647-1659, 2008.
- 1169 Scaife A.A., C.K. Folland, L. Alexander, A. Moberg and J.R. Knight: European climate extremes and
1170 the North Atlantic Oscillation. *J. Clim.*, 21, 72-83, 2008.
- 1171 Scaife, A. A., et al.: Predictability of the quasi-biennial oscillation and its northern winter
1172 teleconnection on seasonal to decadal timescales, *Geophys. Res. Lett.*, 41, 1752– 1758, 2014a.
- 1173 Scaife, A. A., et al.: Skillful long-range prediction of European and North American winters,
1174 *Geophys. Res. Lett.*, 41, 2514– 2519, 2014b.
- 1175 Scaife A.A., A.-Yu. Karpechko, M.P. Baldwin, A. Brookshaw, A.H. Butler, R. Eade, M. Gordon, C.
1176 MacLachlan, N. Martin, N. Dunstone and D. Smith: Seasonal winter forecasts and the stratosphere.
1177 *Atm. Sci. Lett.*, 2016.
- 1178 Schwartz, C. and C.I. Garfinkel: Relative Roles of the MJO and Stratospheric Variability in North
1179 Atlantic and European Winter Climate . *J. Geoph. Res.*, doi: 10.1002/2016JD025829, 2017.
- 1180 Schwartz, C. and C.I. Garfinkel: Troposphere-stratosphere coupling in subseasonal-to-seasonal
1181 models and its importance for a realistic extratropical response to the Madden-Julian Oscillation.
1182 *Journal of Geophysical Research: Atmospheres*, 125(10), p.e2019JD032043, 2020.
- 1183 Screen, J.A., Deser, C., Smith, D.M. et al.: Consistency and discrepancy in the atmospheric response
1184 to Arctic sea-ice loss across climate models. *Nature Geosci* 11, 155–163, 2018.
- 1185 Screen, J. A. and Blackport, R.: How robust is the atmospheric response to projected Arctic sea ice
1186 loss across climate models?. *Geophysical Research Letters*, 46, 11406– 11415, 2019.
- 1187 Seviour, W. J. M., S. C. Hardiman, L. J. Gray, N. Butchart, C. MacLachlan, and A. A. Scaife: Skillful
1188 seasonal prediction of the Southern Annular Mode and Antarctic ozone. *J. Clim.*, 27, 7462–7474,
1189 doi:10.1175/JCLI-D-14-00264.1, 2014.
- 1190 Shukla, J.: Dynamical Predictability of Monthly Means. *J. Atmos. Sci.*, 38(12), 2547-2572, 1981.

- 1191 Shindell, D. T., Schmidt, G. A., Miller, R. L., and Rind, D.: Northern hemisphere winter climate
1192 response to greenhouse gas, ozone, solar, and volcanic forcing, *J. Geophys. Res.*, 106(D7), 7193–
1193 7210, 2001.
- 1194 Sigmond, M., Scinocca, J.F., Kharin, V.V. and Shepherd, T.G.. Enhanced seasonal forecast skill
1195 following stratospheric sudden warmings. *Nature Geosci.*, 6, 98–102, 2013.
- 1196 Simpson, I. R., Hitchcock, P., Seager, R., Wu, Y., & Callaghan, P.: The Downward Influence of
1197 Uncertainty in the Northern Hemisphere Stratospheric Polar Vortex Response to Climate Change.
1198 *Journal of Climate*, 31(16), 6371–6391., 2018.
- 1199 Sigmond, M., J. F. Scinocca and P. J. Kushner: The impact of the stratosphere on tropospheric climate
1200 change. *Geophys. Res. Lett.*, 35, L12706, 2008.
- 1201 Sigmond, M. and J.F. Scinocca: The influence of basic state on the Northern Hemisphere circulation
1202 response to climate change. *J. Clim.*, 23, 1434-1446, , 2010.
- 1203 Sigmond M., Scinocca J.F., Kharin V.V., Shephard T.G.. Enhanced seasonal forecast skill following
1204 stratospheric sudden warmings. *Nature Geoscience*, 6, 98-102, 2013.
- 1205 Shaw T.A. and J. Perlwitz. The life cycle of Northern Hemisphere downward wave coupling between
1206 the stratosphere and troposphere. *J. Clim.*, 26, 1745-1763, 2013
- 1207 Smith K.L. and L M Polvani. The surface impacts of Arctic stratospheric ozone anomalies. *Environ.*
1208 *Res. Lett.* 9 074015, 2014.
- 1209 Solomon, S., Ivy, D. J., Kinnison, D., Mills, M. J., Neely, R. R., & Schmidt, A.: Emergence of healing
1210 in the Antarctic ozone layer. *Science*, 353(6296), 269–274, 2016.
- 1211 Son, S.W. , L.M. Polvani, D.W. Waugh and CCMVal co-authors: The impact of stratospheric ozone
1212 recovery on the Southern Hemisphere westerly jet, *Science*, 320, 1486-1489, 2008.
- 1213 Son, S.-W., Purich, A., Hendon, H. H., Kim, B.-M., and Polvani, L. M.: Improved seasonal forecast
1214 using ozone hole variability?, *Geophys. Res. Lett.*, 40, 6231– 6235, 2013.
- 1215 Son, S-W., Y. Lim, C. Yoo, H. H. Hendon, and J. Kim: Stratospheric control of Madden-Julian
1216 Oscillation, *Journal of Climate*, 30, 1909-1922, 2017.
- 1217 Son. S-W, B-R. Han, C.I. Garfinkel, and 26 others: Tropospheric jet response to Antarctic ozone
1218 depletion: An update with Chemistry-Climate Model Initiative (CCMI) models, *Environmental*
1219 *Research Letters*, 13, 054024, 2018.
- 1220 Son, S.-W., H. Kim, K. Song, S.-W. Kim, P. Martineau, Y.-K. Hyun, and Y. Kim: Extratropical
1221 prediction skill of the subseasonal-to-seasonal (S2S) prediction models, *Journal of Geophysical*
1222 *Research - Atmosphere*, 125, e2019JD031273, 2020.
- 1223 Song, K. and Son, S.: Revisiting the ENSO–SSW Relationship, *Journal of Climate*, 31(6), 2133-2143,
1224 2018.
- 1225 Statnaia, I., A. Yu. Karpechko, H. Järvinen: Mechanisms and predictability of Sudden Stratospheric
1226 Warming in winter 2018, *Weather and Climate Dynamics*, 2020.
- 1227 Steil, B., Dameris, M., Brühl, C. et al.: Development of a chemistry module for GCMs: first results of
1228 a multiannual integration. *Annales Geophysicae* 16, 205–228, 1998.
- 1229 Stenchikov, G., Hamilton, K., Stouffer, R. J., Robock, A., Ramaswamy, V., Santer, B., and Graf, H.-
1230 F.: Arctic Oscillation response to volcanic eruptions in the IPCC AR4 climate models, *J. Geophys.*
1231 *Res.*, 111, D07107, 2006.

- 1232 Stockdale, T. N., Molteni, F. and Ferranti, L. (2015), Atmospheric initial conditions and the
 1233 predictability of the Arctic Oscillation. *Geophys. Res. Lett.*, 42: 1173– 1179. doi:
 1234 10.1002/2014GL062681.
- 1235 Stockdale et al.: Multi-Model Predictions of the Quasi-Biennial Oscillation. *Quart. J. Roy. Met. Soc.*,
 1236 in press, 2021.
- 1237 Sun, L., Deser, C., & Tomas, R. A.: Mechanisms of Stratospheric and Tropospheric Circulation
 1238 Response to Projected Arctic Sea Ice Loss, *Journal of Climate*, 28(19), 7824-7845, 2015.
- 1239 Swinbank, R., Douglas, C.S., Lahoz, W.A., O'Neill, A. and Heaps, A.: Middle atmosphere variability
 1240 in the UK Meteorological Office Unified Model. *Q.J.R. Meteorol. Soc.*, 124: 1485-1525, 1998.
- 1241 Swingedouw, D., Pablo Ortega, Juliette Mignot, Eric Guilyardi, Valérie Masson-Delmotte, Paul G.
 1242 Butler, Myriam Khodri, Roland Séférian: Bidecadal North Atlantic ocean circulation variability
 1243 controlled by timing of volcanic eruptions. *Nature Communications*, 2015; 6: 6545, 2015.
- 1244 Taguchi, M.: Seasonal Winter forecasts of the northern stratosphere and troposphere: Results from
 1245 JMA seasonal hindcast experiments. *Journal of the Atmospheric Sciences*, 75 (3), 827-840, 2018.
-
- 1246 Taguchi, M.: Predictability of Major Stratospheric Sudden Warmings: Analysis Results from JMA
 1247 Operational 1-Month Ensemble Predictions from 2001/02 to 2012/13, *Journal of the Atmospheric
 1248 Sciences*, 73(2), 789-806, 2016.
- 1249 Takaya, Y., T. Yasuda, Y. Fujii, S. Matsumoto, T. Soga, H. Mori, M. Hirai, I. Ishikawa, H. Sato, A.
 1250 Shimpo, M. Kamachi, T. Ose: Japan Meteorological Agency/Meteorological Research Institute-
 1251 Coupled Prediction System version 1 (JMA/MRI-CPS1) for operational seasonal forecasting, *Clim.
 1252 Dyn.*,1–2, 313–333, 2017.
- 1253 Thiéblemont, R., Matthes, K., Omrani, NE. et al.: Solar forcing synchronizes decadal North Atlantic
 1254 climate variability. *Nat. Comm.* 6, 8268, 2015.
- 1255 Thompson, D.W.J., Susan Solomon: Interpretation of Recent Southern Hemisphere Climate Change.
 1256 *Science*, 296, Issue 5569, pp. 895-899, 2002.
- 1257 Thompson, D.W.J., M.P. Baldwin, and J. M. Wallace: Stratospheric connection to Northern
 1258 Hemisphere wintertime weather: Implications for prediction. *J. Climate*, 15, 1421-1428, 2002.
- 1259 Thompson, D. W. J., M. P. Baldwin, and S. Solomon: Stratosphere–troposphere coupling in the
 1260 Southern Hemisphere. *J. Atmos. Sci.*, 62, 708–715, 2005.
- 1261 Thompson, D., Solomon, S., Kushner, P. et al.: Signatures of the Antarctic ozone hole in Southern
 1262 Hemisphere surface climate change. *Nature Geosci* 4, 741–749 (2011).
- 1263 Tompkins, A. M., Ortiz De Zárate, M. I., Saurral, R. I., Vera, C., Saulo, C., Merryfield, W. J.,
 1264 Sigmond, M., Lee, W., Baehr, J., Braun, A., Butler, A., Déqué, M., Doblas-Reyes, F. J., Gordon, M.,
 1265 Scaife, A. A., Imada, Y., Ishii, M., Ose, T., Kirtman, B., Kumar, A., Müller, W. A., Pirani, A.,
 1266 Stockdale, T., Rixen, M., & Yasuda, T.: The Climate-System Historical Forecast Project: Providing
 1267 Open Access to Seasonal Forecast Ensembles from Centers around the Globe, *Bulletin of the
 1268 American Meteorological Society*, 98(11), 2293-2301, 2017.
- 1269 Tripathi, O.P., M. Baldwin, A. Charlton-Perez, M. Charron, S. Eckermann, E. Gerber, G. Harrison, D.
 1270 Jackson, B. Kim, Y. Kuroda, A. Lang, C. Lee, S. Mahmood, R. Mizuta, G. Roff, M. Sigmond, S-W.
 1271 Son: The predictability of the extra-tropical stratosphere on monthly timescales and its impact on the
 1272 skill of tropospheric forecasts, *Q. J. R. Meteorol. Soc.*, 141, 987-1003, 2015a.
- 1273 Tripathi, O., Charlton-Perez, A., Sigmond, M., and Vitart, F: Enhanced long-range forecast skill in
 1274 boreal winter following stratospheric strong vortex conditions. *Environ. Res. Lett.* 10, 104007, 2015b

- 1275 Tyrrell, N. L., A. Yu. Karpechko and P. Raisanen: The Influence of Eurasian Snow Extent on the
1276 Northern Extratropical Stratosphere in a QBO Resolving Model, *J. Geophys. Res.*, 123, 1, 315-328,
1277 2018.
- 1278 Tyrrell N. L., Karpechko A. Y., Uotila P., Vihma T.: Atmospheric circulation response to anomalous
1279 Siberian forcing in October 2016 and its long-range predictability. *Geophys. Res. Lett.*, 46, 2800–
1280 2810, 2019.
- 1281 Tyrrell, N., A. Yu. Karpechko and S. Rast: Siberian snow forcing in a dynamically bias-corrected
1282 model, *J. Climate*, v. 33, 10455–10467, 2020.
- 1283 Vitart, F.: Madden—Julian Oscillation prediction and teleconnections in the S2S database. *Q.J.R.*
1284 *Meteorol. Soc.*, 143: 2210-2220, 2017.
- 1285 Wang, L., Ting, M. & Kushner, P.J.: A robust empirical seasonal prediction of winter NAO and
1286 surface climate. *Sci Rep* 7, 279, 2017.
- 1287 Wang L. et al.: What chance of a sudden stratospheric warming in the southern hemisphere? *Environ.*
1288 *Res. Lett.*, 15, 104038, 2020.
- 1289 Warner, J. L., Screen, J. A., & Scaife, A. A.: Links between Barents-Kara sea ice and the extratropical
1290 atmospheric circulation explained by internal variability and tropical forcing. *Geophysical Research*
1291 *Letters*, 47, e2019GL085679, 2020.
- 1292 White, I., C. I. Garfinkel, E. P. Gerber, M. Jucker, P. Hitchcock, and J. Rao: The generic nature of the
1293 tropospheric response to sudden stratospheric warmings, *Journal of Climate*, 33, 5589-5610, 2020.
- 1294 Wittman, L.M. Polvani, R.K. Scott and A.J. Charlton: Stratospheric influence on baroclinic lifecycles
1295 and its connection to the Arctic Oscillation, *Geophys. Res. Lett.*, 31, L16113, 2004.
- 1296 Wittman, A.J. Charlton and L.M. Polvani: The effect of lower stratospheric shear on baroclinic
1297 instability, *J. Atmos. Sci.*, 64, 479-496, 2007.
- 1298 Woo, SH., Sung, MK., Son, SW. et al.: Connection between weak stratospheric vortex events and the
1299 Pacific Decadal Oscillation. *Clim Dyn* 45, 3481–3492 (2015).
- 1300 Yamazaki, K., Nakamura, T., Ukita, J., and Hoshi, K.: A tropospheric pathway of the stratospheric
1301 quasi-biennial oscillation (QBO) impact on the boreal winter polar vortex, *Atmos. Chem. Phys.*, 20,
1302 5111–5127, 2020.
- 1303 Yoo, C., and Son, S.-W.: Modulation of the boreal wintertime Madden-Julian oscillation by the
1304 stratospheric quasi-biennial oscillation, *Geophys. Res. Lett.*, 43, 1392– 1398, 2016.
- 1305 Zappa, G. and Shepherd, T.G.: Storylines of atmospheric circulation change for European regional
1306 climate impact assessment. *J. Clim.*, 30, 6561–6577, 2017.
- 1307 Zappa, G., Pithan, F. and Shepherd, T.G.: Multimodel evidence for an atmospheric circulation
1308 response to Arctic sea ice loss in the CMIP5 future projections. *Geophys. Res. Lett.*, 45, 1011–1019,
1309 2018.
- 1310 Zhang, F., Sun, Y. Q., Magnusson, L., Buizza, R., Lin, S., Chen, J., & Emanuel, K.: What Is the
1311 Predictability Limit of Midlatitude Weather?, *J. Atm. Sci.*, 76(4), 1077-1091, 2019.
- 1312 Zhang, P., Wu, Y., Simpson, I. R., Smith, K. L., Zhang, X., De, B., & Callaghan, P.: A stratospheric
1313 pathway linking a colder Siberia to Barents-Kara Sea sea ice loss. *Science Advances*, 4(7), eaat6025,
1314 2018.
-