



Limitations of the Radon Tracer Method (RTM) to estimate regional Greenhouse Gases (GHG) emissions – a case study for methane in Heidelberg

5 Ingeborg Levin¹, Ute Karstens², Samuel Hammer^{1,3}, Julian DellaColetta^{1,3}, Fabian Maier^{1,3}, Maksym Gachkivskyi¹

¹Institut für Umweltphysik, Heidelberg University, INF 229, 69120 Heidelberg, Germany

²ICOS Carbon Portal, Lund University, Geocentrum II, Sölvegatan 12, 22362 Lund, Sweden

10 ³ICOS Central Radiocarbon Laboratory, Heidelberg University, Berliner Straße 53, 69120 Heidelberg, Germany

Correspondence to: Ingeborg Levin (Ingeborg.Levin@iup.uni-heidelberg.de)



Abstract. Correlations of night-time atmospheric methane (CH_4) and ^{222}Rn observations in Heidelberg, Germany, were evaluated with the Radon Tracer Method (RTM) to estimate the trend of annual CH_4 emissions from 1996 – 2020 in the catchment area of the station. After an initial 30% decrease of emissions from 1996 to 2004, no further systematic trend but small inter-annual variations were observed thereafter. This is in accordance with the trend of emissions until 2010 reported by the EDGARv6.0 inventory for the surroundings of Heidelberg. We show that the reliability of total CH_4 emission estimates with the RTM critically depends on the accuracy and representativeness of the ^{222}Rn exhalation rate from soils in the catchment area of the site. Simply using ^{222}Rn fluxes as estimated by Karstens et al. (2015) could lead to biases in the estimated greenhouse gases (GHG) fluxes as large as a factor of two. RTM-based GHG flux estimates also depend on the parameters chosen for the night-time correlations of CH_4 and ^{222}Rn , such as the night-time period for regressions as well as the R^2 cut-off value for the goodness of the fit. Quantitative comparison of total RTM-based top-down with bottom-up emission inventories requires representative high-resolution footprint modelling, particularly in polluted areas where CH_4 emissions show large heterogeneity. Even then, RTM-based estimates are likely biased low if point sources play a significant role in the station/observation footprint as their emissions are not captured by the RTM method. Long-term representative ^{222}Rn flux observations in the catchment area of a station are indispensable in order to apply the RTM method for reliable quantitative flux estimations of GHG emissions from atmospheric observations.

1 Introduction

Monitoring the global distribution and trends of greenhouse gases (GHG) such as carbon dioxide (CO_2) and methane (CH_4) in marine background air dates back to the 1950s and 1980s, respectively (Brown and Keeling, 1965; Pales and Keeling, 1965; Blake and Rowland, 1988; Dlugokencky et al., 1994). With few exceptions, continuous continental GHG measurements started only in the 1990s, with a denser network established for CH_4 in the first decade of this century. In Europe, CH_4 observations are used in inverse (top-down, TD) modelling studies since 2009 to estimate the EU27&UK emissions of this potent GHG and its changes (Bergamaschi et al., 2009; 2018; Petrescu et al., 2021). Estimated fluxes were regularly compared to bottom-up (BU) emission inventories, based on reported national emissions, e.g. in the framework of the Paris Climate Accord (UNFCCC, 2015). But only the 2019 Refinement to the 2006 Guidelines of the UNFCCC reporting system (Witi and Romano, 2019) acknowledged the complementary capability offered by TD approaches for the reporting of GHG emissions.

40

A possibility to estimate continental GHG emissions on the local scale is the so-called Radon Tracer Method (RTM, Levin et al., 1999). The RTM uses the fact that the activity concentration of the natural short-lived radioactive noble gas ^{222}Rn (^{222}Rn), which is emitted from continental soils but barely from ocean surfaces, is an excellent tracer for boundary layer



45 mixing processes (e.g. Servant et al., 1966; Dörr et al., 1983; Porstendörfer, 1994). ^{222}Rn can be used as a measure of the
“continentality” of an air mass as its radioactive lifetime of about 5.5 days is long enough that ^{222}Rn can accumulate in air
masses residing over the continent. On the other hand, its lifetime is short enough that the ^{222}Rn activity concentration
exhibits a strong vertical decrease from elevated values in the continental boundary layer to small activity concentrations in
the free troposphere (Liu et al., 1984). Similar to other gases, which have net sources close to the ground, ^{222}Rn accumulates
in a shallow (nocturnal) boundary layer when vertical mixing is suppressed. Therefore, if the exhalation rate of ^{222}Rn from
50 the ground is known, the correlated increases of ^{222}Rn and the gas in question (here CH_4) can be used to estimate the flux of
this gas. In the Integrated Carbon Observation System Research Infrastructure (ICOS RI: <https://www.icos-cp.eu/>),
atmospheric ^{222}Rn observations are recommended to use this tracer for transport model validation but also to apply the RTM
at ICOS atmosphere sites.

55 The Radon Tracer Method has been deployed in the past for greenhouse and other gases emission and sink estimates (Levin,
1984; Gaudry et al., 1990; Levin et al., 1999; 2011; Biraud et al., 2000; Schmidt et al., 2001; Hammer and Levin, 2009). In
all these studies, the ^{222}Rn flux from the soil has been assumed as spatially homogeneous and varying only slightly on the
seasonal time scale. Recent research has, however, challenged this perception of a homogeneous and temporally almost
constant flux. Several attempts to model ^{222}Rn exhalation rates from European soils revealed rather large spatial variability
60 (Szegvary et al., 2009; Lopez-Coto et al., 2013; Karstens et al., 2015). The heterogeneity of ^{222}Rn exhalation is caused by
spatial differences in soil texture and soil $^{226}\text{Radium}$ content, the precursor isotope of ^{222}Rn . But even larger variations of soil
 ^{222}Rn exhalation rate are due to temporal changes in soil moisture, which strongly influences diffusive transport of ^{222}Rn
in the soil air (e.g. Nazaroff, 1992). Soil moisture is, thus, the governing parameter for the observed seasonal variations of ^{222}Rn
exhalation (Jutzi, 2001; Schwingshackl, 2013; Karstens et al., 2015). Short-term varying soil moisture has its largest impact
65 on the ^{222}Rn flux during the summer half-year, when missing precipitation over days or weeks can lead to changes in top soil
moisture by more than a factor of two within a few days (e.g. Wollschläger et al., 2009). The basic assumption for estimating
GHG fluxes with the classical RTM, i.e. a well-known and more or less constant ^{222}Rn flux from the soil is, thus, more than
questionable.

70 Based on these findings, the aim of this study is to re-assess the potential, but also the limitations of the RTM for local-to-
regional scale GHG flux estimation, based on 20+ years of continuous atmospheric CH_4 and ^{222}Rn daughter observations at
the Heidelberg measurement site. Along with meteorological information, regional footprint analyses and model-based
sensitivity experiments, we evaluate the influences of ^{222}Rn and CH_4 flux variability in the Heidelberg catchment area on the
observed night-time $\text{CH}_4/^{222}\text{Rn}$ ratios and RTM-based CH_4 emission estimates. This concerns not only short-term day-to-day
75 variations, but also potential long-term changes of the ^{222}Rn flux to be expected in view of an increasing frequency of
summer droughts in Europe. Finally, we compare the RTM-based CH_4 emissions estimates for 1996-2020 and their inherent



uncertainties with bottom-up CH₄ emissions as reported in the EDGARv6.0 inventory (Crippa et al., 2021) for the model-estimated influence area around the Heidelberg measurement site.

2 Methods

80 2.1 Radon Tracer Method (RTM)

The basis of the Radon Tracer Method is the well-known observation that all trace gases with net positive emissions from continental surfaces accumulate in a stable nocturnal boundary layer. In a simple one-dimensional approach, the observed rate of concentration change ($dC_g(t)/dt$) at a fixed height within this layer depends on the mean flux density j_g of the gas and on the actual boundary layer height ($H(t)$)

$$85 \quad \frac{dC_g(t)}{dt} = \frac{j_g}{H(t)} \quad (1).$$

Eq. (1) holds for all stable gases, and can be modified by including a decay term for short-lived (radioactive) gases like ²²²Rn (Schmidt et al., 2001), leading to Eq. (2):

$$\frac{dC_{Rn}(t)}{dt} = \frac{j_{Rn}}{H(t)} - \lambda_{Rn} \cdot C_{Rn}(t) \quad (2).$$

Here λ_{Rn} is the radioactive decay constant of ²²²Rn. The unknown (virtual) mixing layer height $H(t)$, considered to be the same for ²²²Rn and the trace gas g , can be eliminated by combining Eqs. (1) and (2) and solving for the flux density j_g of the trace gas g . In practice, when applying the RTM on a single night, we use measured finite concentration changes ΔC_g and ΔC_{Rn} instead of differentials, leading to the mean trace gas flux density j_g during the observation period:

$$j_g = j_{Rn} \cdot \frac{\Delta C_g(t)}{\Delta C_{Rn}(t)} \left(1 + \frac{\lambda \cdot C_{Rn}(t)}{\Delta C_{Rn}(t) / \Delta t} \right)^{-1} \quad (3).$$

Correction for the radioactive decay of ²²²Rn is taken care of by the term in brackets in Eq. (3). When applying the RTM during a typical night-time inversion situation, lasting from late evening to early morning (i.e. less than 10 hours), the maximum change of ²²²Rn activity concentration due to radioactive decay is less than 10%. Contrary to earlier studies (Schmidt et al., 2001; Hammer and Levin, 2009) we neglect this effect in our evaluations and use instead Eq. (4) without the correction term:

$$j_g = j_{Rn} \cdot \frac{\Delta C_g(t)}{\Delta C_{Rn}(t)} \quad (4).$$

100 The systematic bias towards higher estimated CH₄/²²²Rn slopes, if radioactive decay is not corrected for, is estimated in a dedicated model experiment (Sec. 3.5).



One may argue that the simple one-dimensional model of the RTM is principally only applicable during inversion conditions with a stable or decreasing boundary layer height H ; such situations occur mainly during summer nights. However, in this study we apply the RTM also for other meteorological night-time conditions, when the trace gases – in our case CH_4 and ^{222}Rn - change synchronously. This is justified as we assume that the measured air sample during night consists of two components, emissions from the ground with a certain $\text{CH}_4/^{222}\text{Rn}$ ratio and residual layer air that has a $\text{CH}_4/^{222}\text{Rn}$ ratio similar to that at the start of the night time observation period. While the local nocturnal boundary layer builds up, a residual layer is formed above this surface layer, which has a similar concentration as the well-mixed atmosphere in the late afternoon (Stull, 1998). We also included synoptic changes observed mainly during winter, as we assume that short-term trace gas changes, if large enough, are still mainly governed by recently added emissions from the regional catchment area.

The RTM approach implicitly assumes comparably homogenous spatial source distributions of ^{222}Rn and the trace gas. This means that it is well suited for homogeneous flux distributions, while trace gas plumes from point sources are not captured as they are not correlated with the area source-type fluxes of ^{222}Rn . RTM-based emission estimates will therefore always underestimate real total GHG emissions in the catchment of a station if point source emissions are relevant. Further, as the footprint is not explicitly considered, the RTM (only) provides an (unknown) footprint-weighted average estimate of the trace gas flux. Consequently, without accompanying model simulations, which explicitly link footprints with the underlying emissions in the footprint area, it is not possible to quantitatively compare RTM-based TD fluxes with BU inventories, unless their emissions are very homogeneously distributed.

2.2 Heidelberg measurement site and methane sources in its catchment area

Heidelberg is a medium size city (ca. 160'000 inhabitants, 49.42°N, 8.67°E, 116 m a.s.l.) in south-west Germany, located at the outlet of the Neckar valley and extending into the densely populated upper Rhine valley (see map in Fig. 1). Continuous GHG and ^{222}Rn measurements are conducted on the University campus, with air sampling from the roof of the Institute of Environmental Physics building from about 30 m above ground level (a.g.l.). Depending on local wind direction, CH_4 concentrations are potentially influenced by local emissions from a close-by residential area and the Heidelberg city centre to the east. To the north of the University campus we find intensively managed agricultural land with some cattle breeding further away in the north-east. A large industrial area, Mannheim/Ludwigshafen (MA/LU) with chemical industry (BASF), solid waste landfills and waste water treatment facilities is located about 20 km to the north-west of Heidelberg. Further CH_4 hot spot emission areas, although much further away are larger cities like Karlsruhe, Heilbronn and the highly populated Rhein/Main area. The 2010 CH_4 emissions distribution from EDGARv6.0 (Crippa et al., 2021) in an area of about 150 km x 150 km with Heidelberg located in the centre, is displayed as gridded map in the left panel of Fig. 1. Here the MA/LU area sticks out as a hot spot with annual emissions of more than 0.05 kg CH_4 m^{-2} , i.e. more than a factor of 3-5 larger than mean emissions from any of the $0.1^\circ \times 0.1^\circ$ pixels in the closer surroundings of Heidelberg.



135

The topography of the Rhine valley (\approx north - south) and the Neckar valley (east - west) influences the regional air flow, being dominated by southerly winds (Fig. 2); north-westerly winds from the MA/LU area are less frequent. Typical wind roses for the year 2015 (separated into daytime and nighttime hours) are displayed in the upper panels of Fig. 2. From these distributions we also see that the wind velocity (radius of the distributions) measured at 37 m a.g.l. on the roof of the Institute's building lies most frequently between 2 and 4 m s⁻¹. We calculated nighttime and daytime only footprints and simulated preliminary CH₄ and ²²²Rn concentrations for Heidelberg for selected years to determine the main influence area of our measurements. These footprint and concentration simulations are based on hourly runs with the Stochastic Time-Inverted Lagrangian Transport model STILT (Lin et al., 2003), that was implemented at the ICOS Carbon Portal (<https://www.icos-cp.eu/about-stilt>). Footprints estimate the main influence area for ground level emissions on the concentrations measured in Heidelberg at 30 m a.g.l., which is approximately located in its centre. With a mean observed wind velocity of 3 m s⁻¹ (about 11 km per hour, Fig. 2), the approximate distance an air mass travels within the seven hours we use for the correlation of CH₄ and ²²²Rn changes in the RTM, would then be ca. 75 km. This is why we chose to display in Fig. 1 the distribution of CH₄ emissions for a total area of 150 km x 150 km ("large" catchment area), being aware that strongest influences come from sources closer to the station (see aggregated footprints in Fig. 2). We thus also mark, by black rectangle, a so-called "small" catchment area in the EDGARv6.0 CH₄ emissions map and also in the map of aggregated footprints in Fig. 2.

Long-term trends of total annual mean EDGARv6.0 emissions from 1995 to 2018 for the large 150 km x 150 km, the small (ca. 70 km x 70 km) and a third "intermediate" (110 km x 110 km) catchment area are displayed in Fig. 3. The 2010 mean seasonal cycle of the large catchment area is shown on the right of the figure. For all three catchment areas, a significant decrease of about 30% is reported from 1995 to 2010. In the small catchment area this trend is interrupted in 2011 by an abrupt increase, which is associated to an increase in the "gas flaring and venting sector" (EDGAR sector: PRO, Janssens-Meanhout et al., 2019) in the pixel where BASF is located. The average fluxes in the larger catchment areas show similar abrupt increases in 2011, but smaller in size. After consulting the EDGAR team, it turned out that this abrupt increase is an artefact caused by the introduction of a new proxy for the gas flaring and venting sector in 2011 (D. Guizzardi, pers. communication). Before 2011 mean CH₄ fluxes from the large catchment area are similar to those of the small catchment, while the intermediate catchment area generally shows only 80 – 85% of that mean flux. As expected for a highly populated and industrialised region, we see only a small seasonality in anthropogenic CH₄ emissions, originating from the seasonality in the sector "energy for buildings" (EDGAR sector: RCO).

165

As already mentioned in Sec. 2.1, given their predominant point source nature, it will not be possible to provide reliable information on the total CH₄ source strengths e.g. from MA/LU with the RTM, as this method is only applicable for area sources that are similarly homogeneously distributed as those of ²²²Rn (Eq. 4). Potentially large contributions from industrial



point sources to the total flux will thus be missing in the RTM-based TD flux estimate so that results are likely biased low.

170 As large point source emissions have to be reported directly to the European pollutant release and transfer (E-RPRT) register data base (<https://prtr.eea.europa.eu/>) by the facility, these bottom-up data are, however, likely much more accurate than any top-down estimate, as they are often based on direct measurements. But the more homogeneously distributed area sources dominating in the immediate neighbourhood of Heidelberg, such as energy for buildings, road transport, enteric fermentation and de-centralised waste management will probably be well represented in the RTM-based flux estimates. In the inventories

175 these fluxes are associated with much larger uncertainties than those from point sources, and are thus a rewarding target for the RTM.

2.3 Radon exhalation rates in the Heidelberg catchment area

The most important pre-requisite to apply the Radon Tracer Method for quantitative GHGs flux estimates are representative ^{222}Rn soil exhalation rates in the catchment area. The four panels on the left of Fig. 4 show the spatial distributions of ^{222}Rn fluxes in the large ca. 150 km x 150 km catchment area of Heidelberg as estimated by Karstens et al. (2015) from bottom-up

180 soil parameters and modelled soil moisture. The upper left panels show the estimated ^{222}Rn fluxes for January and July based on the 2006-2010 soil moisture climatology from the ERA-Interim/Land model, while the lower left panels show the flux distributions using the GLDAS Noah soil moisture (averaged over 2006-2012) (<https://doi.pangaea.de/10.1594/PANGAEA.854715>). Large differences are seen between the models. Along the Rhine river

185 in the north-west of Heidelberg (black dot in the centre of each map) where also a few excavated lakes are located, we find reduced ^{222}Rn fluxes compared to the areas in the immediate surroundings of Heidelberg. This flux reduction is caused by the assumption of Karstens et al. (2015) that the low water table depth close to the rivers reduces mean ^{222}Rn exhalation rates. As was shown and discussed by Karstens et al. (2015), the flux estimates based on the two soil moisture models show huge differences in their absolute values all over Europe. In the surroundings of Heidelberg these differences are larger than

190 a factor of two throughout the year. But in both maps we see similar seasonal variations of the ^{222}Rn flux, which are due to the seasonality of soil moisture with highest values in winter and dryer soils in summer and autumn. Note that in the STILT model runs discussed in Sec. 3.5 we use the average of both ^{222}Rn flux maps, which we call “climatology”.

In Heidelberg we are in the favourable situation that long-term observations of the ^{222}Rn flux from soils have been conducted

195 since the late 1980s (Dörr and Münnich, 1990; Schübler, 1996). Jutzi (2001) has gathered these early data from five long-term measurement sites south of Heidelberg with different soil types to estimate mean seasonal cycles of the ^{222}Rn flux. The data from three of these sites, i.e. those which have soil properties closest to the soil textures underlying the map of Karstens et al. (2015), are displayed in Fig. 4 (upper right panel). Measurements from the sandy soils of M1 and M3 have not been included as they are less representative for our catchment and showed annual mean ^{222}Rn fluxes a factor of two smaller than

200 at all other sites, which have been sampled in the last ten years in the surroundings of Heidelberg (Schwingshackl, 2013). The ^{222}Rn flux measurements south of Heidelberg had also been used by Karstens et al. (2015), together with more recent



measurements from Schmithüsen (2012) and Schwingshackl (2013), conducted north of Heidelberg to evaluate their bottom-up process-based calculations of the ^{222}Rn flux for the respective pixels. They reported significant differences in ^{222}Rn flux when based on the different soil moisture models, ERA-Interim/Land or GLDAS-Noah LSM, but also between models and observations (cf. their Figs. 6 and 7). Here we compare in Fig. 4 (upper right panel) both model estimates for the two pixels where the measurement sites south of Heidelberg are located with the observations from M2, M4 and M5. These measured ^{222}Rn fluxes for sandy loam (M2) and loam (M4 and M5) lie in between the two model estimates, with the latter covering a range of (annual) mean ^{222}Rn fluxes of more than a factor of two. Therefore, if no representative ^{222}Rn flux observations are available at a monitoring site where the RTM shall be applied, depending on the soil moisture model we chose for the ^{222}Rn flux estimate, GHG emissions will differ by a factor of two or more. In addition, if the distribution of soil types is very heterogeneous, this will cause further uncertainty in individual RTM-based flux estimation. Based on the maps shown in Fig. 4 for the Heidelberg catchment areas (large or small), this heterogeneity of soil textures together with water table depth flux adjustment would contribute about 15-30% to the spatial variability of estimated night time $\text{CH}_4/^{222}\text{Rn}$ ratios.

On the other hand, the upper right panel of Fig. 4 indicates, that the relative seasonality is similar in the two modelled as well as in the observed fluxes. This seasonality of \pm (25-30) % will introduce a seasonality in RTM-based GHG fluxes and needs to be corrected in the final results. Normalised, to the respective annual means, measured and modelled seasonality of ^{222}Rn fluxes in the two pixels south of Heidelberg were, thus, calculated and are shown in the lower right panel of Fig. 4. Here we also plotted the normalised average seasonality of monthly mean observed ^{222}Rn fluxes at M2, M4 and M5. The seasonality of this mean observed flux (dashed line in Fig. 4, lower right panel) is used to normalise the $\text{CH}_4/^{222}\text{Rn}$ slopes of the individual night time correlations (Sec. 3.1). To finally estimate annual mean CH_4 fluxes with the Radon Tracer Method (Sec. 3.4) we will use the mean observed total flux at M2, M4 and M5 of $18.3 \pm 4.7 \text{ mBq m}^{-2} \text{ s}^{-1}$. The uncertainty of this observation-based mean flux represents the 1σ standard error of the mean at all three sites.

In Fig. 4 we present only monthly mean ^{222}Rn fluxes and their spatial and temporal variability. However, we also expect variability of the ^{222}Rn flux from day to day due to short-term soil moisture variations (Lehmann et al., 2000). In order to estimate this variability, we would need ^{222}Rn flux data at higher temporal resolution. Such high-frequency data are, however, not available for the Heidelberg catchment area. We therefore estimated hypothetical daily mean ^{222}Rn fluxes from soil moisture data at the long-term measurement site Grenzhof, which is located about 6 km to the west of the Heidelberg monitoring station. Monthly mean soil moisture measurements from Grenzhof 2007 – 2008 had already been shown in Karstens et al. (2015) in their comparison with *monthly* mean modelled soil moisture data (see their Fig. 7d). Here we use the *daily* mean measurements of soil moisture and temperature in the upper 30 cm of the soil from Grenzhof (Wollschläger et al., 2009) and estimate daily mean hypothetical ^{222}Rn fluxes for this site with the same methodology as used by Karstens et al. (2015). We assume a ^{222}Rn source strength of the soil material of $Q = 40 \text{ mBq m}^{-3} \text{ s}^{-1}$, chosen such that the annual mean



235 ^{222}Rn flux for 2007 and 2008 fits the annual average observation-based flux value for the Heidelberg catchment area
($18.3 \pm 4.7 \text{ mBq m}^{-2} \text{ s}^{-1}$). Details of the calculations are given in Appendix A; the results are displayed in Fig. A1.

As expected from the soil moisture variability (Fig. A1 upper panel) the short-term changes of the hypothetical ^{222}Rn flux
(Fig. A1 middle panel) are smallest during December to March, when soil moisture is at its maximum and much less variable
240 than during spring, early summer and autumn. In these latter seasons, the day-to-day variability can reach up to $\pm 30\%$. On
average the day-to-day variability of the virtual ^{222}Rn flux at Grenzhof was estimated to $\pm 10\%$ (Fig. A1, lowest panel).
Besides this short-term variability, we also observe a large difference of soil moisture in early summer between the two
years: The rather wet June and July 2007 yield more than 30% lower ^{222}Rn fluxes than estimated for June and July 2008.
Early summer and autumn months' precipitation and thus soil moisture can vary strongly, causing potentially huge
245 differences in the ^{222}Rn flux from year to year. These short-term and inter-annual variations of the ^{222}Rn exhalation rate will
contribute to the day-to-day and inter-annual variability of night-time $\text{CH}_4/^{222}\text{Rn}$ ratios. They increase the uncertainty of
individual (e.g. monthly) RTM flux estimates and potentially their long-term trends. Note that the dry summers of the last
decade in Europe (e.g. Hanel et al., 2018) are likely associated with higher ^{222}Rn fluxes, at least in summer and autumn. If
not accounted for, these ^{222}Rn flux variations may lead to systematic biases in RTM-based emission estimates and their long-
250 term trends.

2.4 CH_4 measurements

Air sampling from the roof of the Institute of Environmental Physics building (INF 229) for gas chromatographic (GC)
analysis was performed via two separate intake lines, one in the south-eastern and one in the south-western corner of the
roof. These two intake lines were installed to detect potential very local contamination by GHGs emissions from the air
255 exhaust of the building or from other very close-by sources. Only during very few occasions data were manually rejected, if
concentrations from the two intake lines showed a major deviation. In all such cases this deviation could be attributed to a
problem with the intake system. Half hourly mean values of both intake lines were then calculated and used for further
evaluation. Data from the years 1996-1998 stem from sampling at the old IUP building (INF 366), about 500 m to the west
of the new building (INF 229). Also in these early years, air was collected from the roof of the building from approximately
260 25 m a.g.l.. The GC instrumentation was the same as in INF 229.

The combined Heidelberg gas chromatographic system (Combi-GC) was designed to simultaneously measure CO_2 , CH_4 ,
 N_2O , SF_6 , CO and H_2 . It was optimised to measure ambient concentration levels for each trace gas with a temporal resolution
of 5 min (Hammer et al., 2008). For CH_4 analysis, a HP5890II (Hewlett-Packard) GC equipped with a Flame Ionisation
265 Detector (FID) was used. Ambient air was dried to a dew point of ca. -35°C before analysis. Methane mole fraction is
referenced to the WMO X2004A mole fraction scale (Dlugokencky et al., 2005) with a precision of about ± 3 ppb for
individual measurements. A linear response of the FID was assumed over the whole range of ambient CH_4 mole fractions.



For details of the measurement technique, see Hammer et al. (2008). Since January 2018, a Picarro G2401 Cavity Ring-Down Spectroscopy (CRDS) gas analyser was used for CH₄ analysis. Air for this analyser is collected from the south-eastern intake line with one-minute mean values stored and averaged to half-hourly values, following the procedures of the European ICOS atmosphere network (ICOS RI, 2020). The typical standard deviation of these half-hourly data as calculated from the 1-minute data is about ±2-10 ppb, depending on ambient air variability. As for the GC, CRDS measurements are reported on the WMO X2004A mole fraction scale.

2.5 Atmospheric ²²²Rn and meteorological measurements

Atmospheric ²²²Rn activity concentration is determined via its measured ²¹⁴Polonium daughter activity using the static filter method as described by Levin et al. (2002). Based on the results from a European-wide radon comparison study, which included parallel measurements of the Heidelberg monitor with a calibrated radon detector from ANSTO (Williams and Chambers, 2016; Griffiths et al., 2016), we applied a constant ²²²Rn/²¹⁴Po disequilibrium correction factor to the data of 1.11, and report all data on the ANSTO scale, which turned out to be another factor of 1.11 higher than the original IUP Heidelberg calibration (Schmithüsen et al., 2017). Depending on the activity concentration level, half-hourly ²²²Rn activity concentration measurements in Heidelberg have a typical uncertainty of ±15%, including the uncertainty of all correction factors. The wind sensors are mounted on a mast on the southern side of the Institute's roof, at a height of 37 m a.g.l. Until 2011, wind speed was measured using a spherical cup anemometer and wind direction by a weather vane. From spring 2011 onwards, wind speed and wind direction is measured using a 2D sonic anemometer (Thiess, Germany). For both instrument generations data was averaged to 5 min means.

3 Results

3.1 Estimating mean night-time CH₄/²²²Rn ratios from half hourly observations

For the period of 1996 to 2020 (except for 1999, when the Institute moved from INF 366 to INF 229 and no CH₄ observations are available), we calculated least squares fits of the half-hourly atmospheric CH₄ and ²²²Rn observations from 21:00 h to 4:00 h CET in the next morning. To ensure that meaningful signals are evaluated, we set a lower limit of 1.5 Bq m⁻³ for the ²²²Rn range during the correlation period, which is about half of a typical mean range during all nights. In most years more than 45 nights were left, in which the correlation coefficient (R²) of the night time CH₄/²²²Rn regressions was better or equal to 0.7. Anthropogenic CH₄ emissions in the Heidelberg catchment area have only a small seasonal variation of less than ±15 % (Crippa et al., 2021, and Fig. 3 right panel), and there are no wetlands with temperature-dependent anaerobic CH₄ production in our region. However, the ²²²Rn exhalation rate from soils has a pronounced seasonality. In our observations and also in both model estimates the ²²²Rn flux during winter is up to 30 % lower than the annual average and it is up to 26% higher during late summer months (Fig. 4, lower right panel). This seasonality of the ²²²Rn flux imposes a seasonality on the CH₄/²²²Rn ratios. We therefore normalised (de-seasonalised) all ratios on a monthly basis by



300 multiplication with a corresponding factor to the annual mean ^{222}Rn flux. In the following we will first discuss these normalised $\text{CH}_4/^{222}\text{Rn}$ ratios and only in Sec. 3.5 RTM-based CH_4 fluxes are estimated. This intermediate step was taken because of the large uncertainty of the *absolute* ^{222}Rn flux in contrast to its much better defined seasonality (cf. Sec. 2.3 and Fig. 4).

305 All selected normalised $\text{CH}_4/^{222}\text{Rn}$ regression slopes with an $R^2 \geq 0.7$ are displayed in Fig. 5 upper panel. On average, more than 80% of $\text{CH}_4/^{222}\text{Rn}$ slopes vary between about 7 and 30 ppb (Bq m^{-3}) $^{-1}$. However, we also occasionally find slopes, which are much larger than 40 ppb (Bq m^{-3}) $^{-1}$. In order to evaluate how sensitive $\text{CH}_4/^{222}\text{Rn}$ slopes are on the selected night-time interval chosen for the regressions, we also calculated slopes for an increased and a reduced time span, i.e. from 20:00 h to 5:00 h and from 22:00 h to 3:00 h CET. The general shape of the distributions (frequency of positive outliers) is very similar and also the overall means differ by only $\pm 3\%$. However, differences can be more than 15% in individual years. We also evaluated how sensitive the annual mean slopes are to the threshold of correlation coefficient R^2 . When selecting only the nights where R^2 is equal or larger than 0.8, mean slopes are about 3% higher than when including all slopes with an $R^2 \geq 0.7$. Thus, a small bias may be introduced, depending on the choice of the night-time regression interval and also depending on the requested goodness of correlation between CH_4 and ^{222}Rn . It is also important to note that the number of nights with $R^2 \geq 0.7$ increases systematically with the length of the tested regression time periods. The RTM is based on the co-variation of trace gases and ^{222}Rn through changing atmospheric mixing. Since there is no causal correlation between the emission processes of the two gases, their different spatial source heterogeneity in combination with changing footprints leads to a reduced number of valid correlations with a shorter observation period. In contrast, more extended regression periods with variable footprints increase the probability of averaging across spatial heterogeneity of emissions.

320 Interestingly, mean slopes are only about 3% different (larger) if only values obtained for situations when both concentrations increase are included, compared to when we also include the about 20% situations when both gases show a decrease between the start and the end of the regression interval. This finding may be a special characteristic of our sampling site, where the air intake is only at 30 m a.g.l. During very stable situations and calm winds the air intake can obviously be either below or above the local surface inversion (if this is around 30 m), which results in very abrupt but synchronous changes of both gases in some nights. As mentioned in Sec. 2.1 we can describe this as a case where two air mass components, i.e. one enriched by emissions from ground level sources with a well-defined $\text{CH}_4/^{222}\text{Rn}$ ratio and another, cleaner, component from the residual layer that has a $\text{CH}_4/^{222}\text{Rn}$ ratio similar to that during well-mixed situations in the afternoon before. These two components are mixed at various ratios. In such a situation all measured $\text{CH}_4/^{222}\text{Rn}$ ratios lie on one mixing line, which corresponds to the regression line in our approach. With this picture in mind, it becomes immediately clear that in Eqs. (1) and (2) (Sec. 2.1), besides the concentrations of CH_4 and ^{222}Rn , also the mixing height $H(t)$ may vary temporally and does not need to be constant during a single night to apply the RTM. We, thus, kept all nights when CH_4 and ^{222}Rn are well correlated for calculating annual means and further evaluating the slopes.



3.2 Relating CH₄/²²²Rn slopes to influence areas

The CH₄/²²²Rn slopes displayed in Fig. 5 show large variability, and we wondered, if this variability can be explained by
335 spatial variations in the CH₄ emissions, and if yes, if we can associate e.g. the high slopes to one of the hot spot emission
areas in the footprint of Heidelberg. We, therefore, evaluated the air mass influence based on local wind data for all nights
when we obtained good ($R^2 \geq 0.7$) correlation between CH₄ and ²²²Rn. Let us assume that the ²²²Rn flux is spatially
homogeneous; then we would expect higher slopes if the air mass origin is from the north-westerly or westerly sectors where
the large CH₄ emitters from MA/LU are located (Fig. 1). Figure 6 shows in the first column polar plots of wind direction
340 (angle) and speed (radius axis) with the value of the corresponding slopes color-coded (i.e. larger slopes plotted in darker red
colours). Note that we use here the original 5-minute mean values of wind speed and direction, together with the mean slope
during the entire night (7 hours). Each polar plot shows the distribution for all selected nights of the entire year (2016, 2017
and 2018 as typical examples from the later years of our record); the colour-coded segments represent annual mean values of
all slopes where a five-minute value fell into the respective wind rose segment. The second column of Fig. 6 shows the
345 frequency distribution of the wind during all selected nights, while the third column shows the distribution during all nights
in the respective year (21:00 h – 04:00 h).

The frequency distributions of 2016 and 2017 indeed show higher average slopes when the wind comes from north-westerly
directions, but in 2018 high slopes are also associated to the northern or north-eastern wind direction. Interestingly, the
350 easterly and south-easterly sectors show average slopes that are often smaller than about 20 ppb (Bq m⁻³)⁻¹. This is a wind
sector where also EDGARv6.0 generally reports lower than average emissions (Fig. 1). A problem with this analysis is that
during low wind speed, the wind direction is not well defined and may change by (more than) 180° within a single night. The
measured air would then be influenced by emissions from various sectors with different CH₄ emissions. This could smooth
out an otherwise clear association of slopes to certain wind sectors. Also, low wind speed situations are more frequent during
355 stable nights (as indicated for the selected nights in Fig. 6 middle panel) with a shallow boundary layer and large nocturnal
increases of CH₄ and ²²²Rn, i.e. nights with good correlation between the two gases and where the RTM can be principally
applied. We should also keep in mind that part of the high emissions in the MA/LU hotspot area are probably from point
sources that will not be captured by the RTM. Also the frequency distribution of wind directions generally (for all nights)
favours more southerly and south-easterly winds, which reduces the likelihood to monitor the high CH₄ emissions from the
360 MA/LU area. Nevertheless, can we roughly separate influence areas, which, on an annual mean basis, differ in their mean
slopes by more than a factor of two. This indicates that a large share of the variability of slopes (Fig. 5) is caused by the
heterogeneity of CH₄ emissions around Heidelberg.



3.3 The influence of ^{222}Rn flux variability on the variability of $\text{CH}_4/^{222}\text{Rn}$ slopes

365 Besides the heterogeneous distribution of CH_4 emissions in the Heidelberg catchment, we expect part of the variability in the
 $\text{CH}_4/^{222}\text{Rn}$ slopes to be also due to variations of the spatial distribution of the ^{222}Rn exhalation rate. Figure 4 shows the
spatial ^{222}Rn flux distribution for the large Heidelberg influence area in January and July for both soil moisture models.
Although mean fluxes from the two different soil moisture models differ by more than a factor of two, the spatial variability
within one map varies by only $\pm(15\text{-}25)\%$ within the large catchment and slightly more in the small $70\text{ km} \times 70\text{ km}$
370 catchment area. Therefore, the spatial variability of the ^{222}Rn flux probably contributes much less to the variability of slopes
than that of the CH_4 flux (see also Sec. 3.5 where we investigate the contributions of CH_4 versus ^{222}Rn flux heterogeneity on
modelled $\text{CH}_4/^{222}\text{Rn}$ slopes). Also the short-term day-to-day variability of the estimated “hypothetical” ^{222}Rn flux, as
elaborated in Appendix A and displayed in Fig. A1 for the years 2007 and 2008, may contribute to the variability of slopes.
The hypothetical daily flux estimates, which are based on the measured daily mean soil moistures, show a mean day-to-day
375 variability of $\pm 10\%$, but during early summer 2007, and likely also in other years, particularly during spring and autumn,
short-term deviations from monthly mean fluxes can be as large as 30%. However, these deviations are still too small to
explain a major share of the observed slope variability displayed in Fig. 5.

3.4 Estimating CH_4 fluxes with the RTM and comparison with EDGARv6.0 emission trends

380 As shown in the previous section, the spatial variability of CH_4 emissions and, to some extent, also the spatial and temporal
variations of the ^{222}Rn flux in the catchment area of Heidelberg are large and make reliable estimates of RTM-based CH_4
emissions from selected sectors (e.g. of industrial processes in MA/LU) or for individual short periods highly uncertain. But
we can estimate average CH_4 emissions from the footprint of the station. As a first attempt to apply the RTM we use the
observation-based ^{222}Rn flux, which was estimated as the mean of our measurements at M2, M4 and M5 to $18.3 \pm 4.7\text{ Bq m}^{-2}$
385 s^{-1} (Sec. 2.3). The corresponding CH_4 flux it is plotted as black histogram in Fig. 7. The uncertainty of the absolute RTM-
based CH_4 fluxes is dominated by the uncertainty of the mean ^{222}Rn flux and is exemplarily plotted as black error bars for the
first and last year of observations. A significant decrease of emissions by about 30% is observed from 1995 until about 2004.
This decrease is in agreement with the trend of bottom-up EDGARv6.0 emissions from 1995 – 2010 calculated for all three
catchment areas in Fig. 3. However, while EDGARv6.0 emissions show a further decrease after 2004, our RTM-based
390 estimates are more or less constant after 2004, showing an inter-annual variability of less than $\pm 10\%$.

In Fig. 7 we also included the range of CH_4 emissions we would estimate when using the mean ^{222}Rn flux from the maps by
Karstens et al. (2015). For this estimate we used the mean ^{222}Rn fluxes from the small catchment area. As expected from the
huge difference in ^{222}Rn fluxes between the two soil moisture models (Fig. 4), possible RTM-based CH_4 emission estimates
395 would cover a range of more than a factor of two (indicated in Fig. 7 by the coloured area). Using the *mean* ^{222}Rn flux from



both model estimates, i.e. the climatology, would – accidentally - yield a similar (ca. 10% lower) RTM-based CH₄ flux as when using the observation-based ²²²Rn flux for the Heidelberg catchment.

3.5 Comparing the observation-based RTM results with the RTM application on preliminary STILT CH₄ and ²²²Rn simulations

400 One important shortcoming of RTM-based GHG flux estimates is the lack of information on the actual influence area for which the estimated flux is representative. In Sec. 2.2 and Fig. 2 we could only roughly localise the large ca. 150 km x 150 km catchment area for Heidelberg, contributing most of the source influence on the nighttime concentration changes within the 7 hours used for the RTM-based flux estimates. Quantitative comparison with bottom-up emission inventories, however, requires actual weighting of the influence area, in particular if the distribution of the GHG emissions is as heterogeneous as

405 in the Heidelberg surroundings. This weighting can be achieved with regional transport model simulations. For the following STILT model estimates the footprints were mapped on a 1/12° latitude x 1/8° longitude grid and were coupled (offline) to the EDGARv6.0 emission inventory (Crippa et al., 2021) for CH₄ concentration estimation, neglecting seasonality of emissions. We also simulated atmospheric ²²²Rn activity concentrations based on the two ²²²Rn flux maps of Karstens et al. (2015) (the average climatology of ERA/Interim-Land and Noah GLDAS was used for the simulations). The modelled

410 regional concentration components represent only the influence from surface fluxes inside the model domain (covering the greater part of Europe, i.e. an area much larger than the large catchment area defined in Sec. 2.2). The background concentrations for CH₄ and ²²²Rn outside our modelling domain have been neglected as we are here only interested in nighttime changes of both trace gases. We then applied the RTM also on these preliminary model results and compared the slopes and their typical distribution to those from the observations. Comparing modelled with observed slopes rather than absolute

415 concentrations has the advantage that incorrect parameterisation of the nighttime boundary layer height by the model partly cancels, while the relative footprint area weighting may still be reliable, even for nighttime simulations.

Figure 8 shows the normalised observed and modelled CH₄/²²²Rn slopes in Heidelberg for the years 2007 – 2010 and their distributions. We did run the STILT model also for 2011, but due to the error in the EDGARv6.0 emissions from 2011

420 onwards, we used the results only as a sensitivity test (see below). Although we use the same selection criteria for the modelled concentration regressions as for the observations, the number of nights with good correlations of CH₄ and ²²²Rn is about five times higher than for the observations. Note that we do not want to compare here modelled with observed slopes of individual nights, e.g. in a scatter plot, because we are mainly interested to compare mean values (to further translate them into mean emission rates as displayed in Fig. 7) and their distributions. In the model-based slopes we find a number of very

425 high values, which we do not see in 2007 – 2010 in the observed slopes. We can clearly identify these high modelled slopes as being associated with north-westerly winds and thus as strong influence from hot-spot CH₄ emissions in these situations. Although the hot-spots in reality have most probably very localised emissions and are not captured by the RTM in the real world, in the model these emissions are distributed over the area of the entire about 10 km x 10 km wide pixel, so that during



430 stable winds good correlations between ^{222}Rn and CH_4 may occur over an entire night, and very high $\text{CH}_4/^{222}\text{Rn}$ ratios can be obtained. This finding is confirmed by STILT model results for the year 2011, where CH_4 emissions in EDGARv6.0 are more than doubled in the MA/LU pixel. In this year we find a larger number of high slopes than in the years 2007 – 2010, some of them exceeding $100 \text{ ppb} (\text{Bq m}^{-3})^{-1}$.

435 If we exclude the three outliers above $70 \text{ ppb} (\text{Bq m}^{-3})^{-1}$ in 2008 and 2009 in the averaging of the modelled slopes, we obtain rather good agreement with the mean observed slopes (i.e. observations = $(15.6 \pm 7.9) \text{ ppb} (\text{Bq m}^{-3})^{-1}$; model = $(16.7 \pm 8.5) \text{ ppb} (\text{Bq m}^{-3})^{-1}$). Also the relative variability is then very similar in the modelled compared to the observed slopes, i.e. 50% vs. 52%. This justifies quantitative comparison between model results and observations. However, even under the assumption that the modelled footprint area is correct, we are still not able to quantitatively validate EDGARv6.0 emission estimates through comparison between model and observations as long as we do not know the true ^{222}Rn flux in this footprint area. But
440 we can go one step further and normalise the model results to the same ^{222}Rn flux as we believe is the best estimate for the Heidelberg catchment area based on observations. The model simulations were based on the ^{222}Rn flux climatology of Karstens et al. (2015), which give an annual mean flux averaged over the small footprint area of $16.7 \text{ mBq m}^{-2} \text{ s}^{-1}$ (the mean flux in the large catchment would be 2.5% lower). Normalisation then increases the mean modelled slopes by a factor of $18.3/16.7$, leading to an over-estimation of the modelled slopes compared to the observations by a factor of
445 model/observation = $16.7 * 18.3 / 16.7 / 15.6 = 1.17$. The uncertainty of this result would be about 25%, i.e. the estimated uncertainty of the mean observation-based ^{222}Rn flux. Within this uncertainty we could come to the conclusion that EDGARv6.0 emissions in the Heidelberg footprint area would be slightly over-estimated by $(17 \pm 25) \%$. However, we must not forget that the observation-based RTM results (and, to some extent, also the STILT-based results) are biased low because we do not (or only partly) catch emissions from very localised CH_4 sources. How big the respective biases are, is hard to
450 quantify; it would require a dedicated sensitivity study with a realistic very high-resolution transport model and an emission inventory that separates area and point source emissions.

We further used STILT model simulation experiments to investigate the sole influence of (1) CH_4 flux heterogeneity, (2) ^{222}Rn flux heterogeneity and (3) neglecting radioactive decay of ^{222}Rn in the calculation of $\text{CH}_4/^{222}\text{Rn}$ slopes in Heidelberg.
455 For these experiments we compared the standard model results with those where we used (1) a constant CH_4 source distribution, (2) a constant ^{222}Rn flux and (3) treated ^{222}Rn as a stable tracer. Experiments (1) and (2) confirmed that most of the variability of $\text{CH}_4/^{222}\text{Rn}$ slopes in Heidelberg is due to the heterogeneity of the CH_4 source distribution. Keeping ^{222}Rn fluxes constant had no significant influence on the standard deviation of the $\text{CH}_4/^{222}\text{Rn}$ slopes, however, spatially homogeneous CH_4 emissions reduced the variability of the slopes from about 50% to less than 20%. When treating ^{222}Rn as
460 a stable tracer in the model, mean slopes were 7% lower than in the run, which included radioactive decay in the modelled ^{222}Rn activity concentration. This means that both, modelled and observed slopes need to be corrected downwards by 7%.



This has, however, no influence on our finding that EDGARv6.0 emissions in the Heidelberg catchment may be (17±25) % too high.

4 Discussion

465 4.1 How reliable can RTM-based GHGs flux estimates be?

The Radon Tracer Method is a purely observation-based method to estimate nighttime fluxes from homogeneously distributed ground level sources of trace gases. Its application is simple; in principle, it does not require sophisticated atmospheric transport modelling. Depending on the height above ground level of co-located ²²²Rn and trace gas observations, RTM-estimated fluxes can be representative for an area of several hundred square-kilometres. However, the exact area for which the estimated mean nighttime flux is representative must be estimated separately, e.g. by footprint modelling. The accuracy of the RTM-based trace gas flux estimates is almost solely determined by the exact knowledge of the ²²²Rn exhalation rate from the soils in the catchment area of the atmospheric station. Still, even if the absolute ²²²Rn exhalation rate is not well known, and with that the absolute trace gas flux, the RTM can provide validation of long-term trace gas emission trends, for example of GHG emission reductions. This, however, requires that the ²²²Rn flux does not show a systematic long-term trend, which, for example, may be caused by long-term changes of soil moisture in the catchment area of the measurement site. Also the mean footprint should not show a systematic trend, e.g. due to climate-driven changes of local transport patterns. This is particularly important if ²²²Rn and/or trace gas emissions show large spatial heterogeneity in the footprint.

480 The RTM-based CH₄ emission *trend* calculated from Heidelberg observations is in good agreement with the *trend* of the EDGARv6.0 bottom-up inventory data. However, after 2004 our observations do not show a further decrease, contrary to the values reported by EDGARv6.0. Comparison of *absolute* emissions is, however, difficult as point source emissions are not captured by the RTM; therefore, our RTM-based fluxes are biased low. As we rely on modelled footprints for a quantitative comparison of RTM-based top-down fluxes with inventory-based bottom-up emission estimates, it will depend on the share of point source emissions how reliably we can compare observed with modelled slopes. Due to the coarse grid of the STILT model we used in this study and the coarse resolution of the inventory, point source emissions were distributed over 10 km x 10 km grid areas. This resulted in a larger number of high slopes in the model results compared to observations if the air mass came from the MA/LU hot spot emissions area. Modelling CH₄ and ²²²Rn with a higher resolution model and emission inventory could improve comparability of model results and observations, and therewith help quantifying the bias in observation-based RTM results caused by point source emissions in a particular setting.

Large potential biases in observation- and model-based RTM flux estimates are introduced by the uncertainty of the ²²²Rn flux in the catchment area. For the Heidelberg catchment, the uncertainty of 25% for the mean ²²²Rn flux is probably an



495 upper limit, because soil texture and $^{226}\text{Radium}$ content of the soils in the catchment of our station show only small
variability (<10%) (Schwingshackl, 2013; Karstens et al., 2015). But we would need more systematic and representative
 ^{222}Rn flux observations, also at larger distances from Heidelberg, to estimate a more accurate mean observation-based flux
with smaller uncertainty range.

500 On the other hand, we want to emphasise that comparing simulated mean nighttime $\text{CH}_4/^{222}\text{Rn}$ slopes with observed slopes
could be a more accurate method to evaluate bottom-up emissions than directly comparing simulated and observed nighttime
 CH_4 concentrations or using model inversions of nighttime data to optimise CH_4 fluxes. This problem is certainly less
serious if only daytime observations are used in the inversions. However, the about five-fold larger surface influences
(sensitivity) during night than during day (Fig. 2) may help improving top-down results. The normalisation of modelled
505 nighttime CH_4 with modelled ^{222}Rn largely eliminates errors in model transport, such as e.g. deficiencies in the
parameterisation of the nocturnal boundary layer height, but also in this approach the final outcome and its significance
depend on the correctness of the underlying ^{222}Rn exhalation rate. This exhalation rate can easily have larger uncertainties
than the GHG emission inventory we target to evaluate. For example, for Europe, different bottom-up CH_4 emission
inventories agree to within 10% or better (e.g. Petrescu et al., 2021). It is still likely that the uncertainty of BU GHG fluxes
510 in a smaller area, that have been disaggregated from national totals, and thus depend on generalised assumptions about
emission factors and proxies for the different sectors, are much larger than these 10%, or may even have flaws (see Sec. 2.2
and Fig. 3).

It should, perhaps, also be noted that our Heidelberg site may be a special case with advantages and disadvantages to apply
the RTM. First, we have conducted the long-term observations with the same instrumentation, except for CH_4 in the last
515 three years. More importantly, the air intake at about 30 m a.g.l. may be favourable for RTM applications, as it frequently
lies in the nocturnal surface layer, which implies that we observe sufficiently large nighttime increases of both gases to
obtain good correlations. Nevertheless, at this height above ground we monitor a footprint that is large enough to not only
being influenced by very local emissions. A major advantage for estimating potentially accurate CH_4 fluxes were long-term
observations of the ^{222}Rn exhalation rate and its seasonality from typical soil types around the station. This made the results
520 presented here fully independent from modelled soil moisture-based ^{222}Rn flux estimation. If we had to solely rely on
modelled ^{222}Rn fluxes, e.g. from Karstens et al. (2015) the uncertainty range of RTM-based estimates would have been as
large as a factor of two (Fig. 7, coloured area). The largest disadvantage of our setting is, however, that CH_4 emissions in our
catchment area are very heterogeneous and contain point sources, which cannot be evaluated with the RTM. Therefore,
observation-based but also STILT-based CH_4 flux estimates are biased low to a currently unquantifiable extent.

525

There are a number of other issues that need to be kept in mind when applying the RTM: It is important to carefully evaluate
what the most appropriate night time period is to calculate representative trace gas fluxes. We investigated this parameter for



Heidelberg and found on average about 3% smaller CH₄ fluxes when extending the regression period from 7 to 9 hours and 3% higher fluxes when reducing it to 5 hours. But for individual years mean slopes showed differences larger than 10%
530 when changing the length of the regression period. Also, in these scenarios the number of nights with good correlation (i.e. $R^2 \geq 0.7$) decreased significantly when the correlation period was shortened to 5 hours or even less. The heterogeneity of CH₄ emissions in the Heidelberg catchment area may have contributed to this effect, as we often have very variable wind directions during stable nights, and changes in the CH₄/²²²Rn slopes may lead to bad correlations if only a smaller number of data points are correlated. Also increasing the quality of the regression from $R^2 \geq 0.7$ to $R^2 \geq 0.8$ led to an increase of the
535 mean slope (here by 3% on average). As the average correlation coefficient did not change when changing the regression period and selecting only nights with $R^2 \geq 0.7$, we finally decided to fix this period to those 7 hours, which always, during winter and summer fall into dark night time (i.e. 21:00 h – 4:00 h CET). However, we have to admit that this decision was made in a rather subjective way.

4.2 Would reliable RTM-based GHG flux estimates be possible at ICOS stations?

540 At many stations in the ICOS atmosphere network continuous ²²²Rn observations are conducted, however, almost no systematic ²²²Rn flux observations exist close to these stations. This is a serious deficiency if the RTM shall be routinely applied in this network for top-down GHGs flux estimation. Even if these measurements may be introduced in the future, they need to be conducted at a number of representative soils in the catchment area and over a longer time period. We could show that the day-to-day variability of the ²²²Rn exhalation rate can be large (Fig. A1). Also inter-annual variations of soil
545 moisture due to variations in seasonal precipitation ask for systematic long-term ²²²Rn flux measurements to allow for representative estimates of the mean flux and its typical seasonality. A second problem to reliably apply the RTM at ICOS stations may be the relatively high air intake for ²²²Rn (generally > 100m a.g.l.). Nighttime increases of soil-borne trace gases are much smaller at these heights than at 30 m, and the layer with the air intake may be decoupled from ground level emissions. This increases the catchment area of the station with potentially more heterogeneous and possibly less well-
550 defined ²²²Rn fluxes.

However, we could show in our study that the long-term trends of RTM- and inventory-based emission estimates did not significantly deviate from each other. Monitoring potential trends of GHG fluxes is an important task of ICOS and could very well contribute to the regular stocktakes under the UNFCCC accord (UNFCCC, 2015), providing independent
555 validation of reported trends. Still, this would require confidence that ²²²Rn fluxes have not changed over the monitoring period.

4.3 Could a better ²²²Rn flux map help to improve RTM-based GHG flux estimates?

As was shown in Fig. 4, the current ²²²Rn flux maps from Karstens et al. (2015) show huge differences depending on the soil moisture model that was used. In the case of Heidelberg, a simple averaging of these two model estimates (what we called



560 climatology) would have fit rather well to the observations (the average ^{222}Rn flux for the Heidelberg catchment area would then be between $16.3 \text{ mBq m}^{-2} \text{ s}^{-1}$ and $16.7 \text{ mBq m}^{-2} \text{ s}^{-1}$, compared to the observation-based flux of $18.3 \pm 4.7 \text{ mBq m}^{-2} \text{ s}^{-1}$). Averaging both estimates would thus have been a tempting solution for the Heidelberg catchment if no observations had been available. But would averaging both maps yield reliable estimates of the ^{222}Rn flux also at other sites in Europe? As was shown by Karstens et al. (2015), it is not obvious that one or the other soil moisture model or the average of both models

565 would fit observed ^{222}Rn fluxes best. There is some indication that the ERA/Interim-Land-based fluxes are generally underestimating observations (Karstens et al., 2015, Fig. 8). Today, improved so-called third generation land reanalysis models are available (see Li et al., 2020, for an overview). Soil moisture estimates from these third generation models have been compared to observations and it turned out that “the European Centre for Medium-Range Weather Forecasts ERA5 model (Hersbach et al., 2018) shows higher skills than the other four products and a significant improvement over its

570 predecessor” (Li et al., 2020). However, although the ERA5 results give realistic variability, they often show systematically higher soil moisture than the observations. In order to use these new reanalysis data, which have the advantage that they are available now at much higher temporal and spatial resolution, a method needs to be developed to scale them to observations. Only then will we be able to apply them in a process-based approach to calculate realistic high-resolution ^{222}Rn fluxes for Europe that compare well with observations, also in their absolute values. This task is part of the European EMPIR project

575 traceRadon (<https://www.euramet.org/research-innovation/search-research-projects/details/project/radon-metrology-for-use-in-climate-change-observation-and-radiation-protection-at-the-environmental/>), which will also conduct dedicated campaigns of quasi-continuous ^{222}Rn flux and soil moisture measurements. With this objective, it has the potential to deliver a much more detailed data set to validate the new map and increase the observational basis also at ICOS stations to apply the Radon Tracer Method in the future.

580 5 Conclusions

The Radon Tracer Method provides a useful observation-based top-down tool to evaluate bottom-up inventories of greenhouse and other trace gas fluxes with a homogeneous source distribution similar to that of ^{222}Rn . Applying the RTM for quantitative flux estimation relies on the accuracy of the ^{222}Rn flux in the catchment area of the station. Its application for CH_4 at the Heidelberg measurement station had serious limitations due to the large heterogeneity of emissions in the

585 catchment area, which caused a huge variability of $\text{CH}_4/^{222}\text{Rn}$ ratios. Large point source emissions were not captured by the RTM, thus under-estimating the total flux. Results of GHG flux estimates further depend on the parameters used to apply the RTM, such as the night-time period chosen as well as the requested quality of the regression (R^2). Only slightly changing these parameters, e.g. extending or reducing the night-time regression period by 2 hours or choosing an R^2 cut-off value of 0.8 rather than 0.7 introduces systematic differences of several percent each. Quantitative comparison of RTM-based with

590 bottom-up emission data is not directly possible without reliable footprint modelling of the nighttime observations. This may be hampered by the reliability of nighttime model transport; but applying the RTM also on model results may be an



appropriate way to circumvent this deficit. The model resolution should, however, be good enough to realistically represent the real source heterogeneity in the footprint of the station, in particular concerning point source emissions, so that model results are comparable with the observations. The caveat will then be that also the model-based RTM estimates will be biased low. Therefore, in order to make reliable quantitative trace gas flux estimates with the RTM the unknown trace gas emissions should be distributed as homogeneously as possible. In Heidelberg, the top-down estimated CH₄ trend showing a 30% reduction of emissions from the mid-1990s to the mid-2000s compared well with the bottom-up EDGARv6.0 emission trend. But we could not observe a significant decrease of emissions thereafter, a sign that further efforts to reduce CH₄ emissions have not yet been successful in our Heidelberg catchment area.

600 Appendix A

In order to estimate the potential day-to-day variability of the ²²²Rn flux from a typical soil in the Heidelberg catchment, we use the daily mean measurements of soil moisture (Fig. A1 upper panel) and temperature in the upper 30 cm of the Grenzhof soil (Wollschläger et al., 2009). We estimate the ²²²Rn flux j for this site close to Heidelberg according to Karstens et al. (2015, their Eq. 8):

$$j(z=0) = -Q \sqrt{\frac{D_e}{\lambda}} \quad (\text{A1}).$$

We use a ²²²Rn source strength of the soil material of $Q = 40 \text{ mBq m}^{-3} \text{ s}^{-1}$, chosen such that the mean ²²²Rn flux for 2007 and 2008 fits the average extrapolated flux for our small catchment area of $18.3 \text{ mBq m}^{-2} \text{ s}^{-1}$. λ is the decay constant of ²²²Rn ($2.0974 \cdot 10^{-6} \text{ s}^{-1}$). The effective diffusivity D_e is calculated according to Millington and Quirk (1960) from the molecular diffusivity of ²²²Rn in air ($D_{a0} = 1.1 \cdot 10^{-5} \text{ m}^2 \text{ s}^{-1}$), the measured total porosity of the Grenzhof soil ($\theta_p = 0.395$, Schmitt et al., 2009) and the measured water-filled porosity θ_w (with $\theta_a = \theta_p - \theta_w$)

$$D_{e0} = D_{a0} \frac{\theta_a^2}{\theta_p^3} = D_{a0} \frac{(\theta_p - \theta_w)^2}{\theta_p^3} \quad (\text{A2}).$$

The dependency of the effective diffusivity on temperature was calculated according to Schery and Wasiolek (1998)

$$D_e(T) = D_{e0} \left(\frac{T}{273 \text{ K}} \right)^{\frac{3}{2}} \quad (\text{A3})$$

615 The day-to-day ²²²Rn flux variability for 2007-2008 is displayed in the lower panel of Fig. A1.



Code and data availability

CH₄ and ²²²Rn data as well as computational codes will be made available at the ICOS carbon Portal (<https://www.icos-cp.eu/>).

620 Author contributions

IL designed the study together with UK and SH. IL evaluated the data and wrote the manuscript with help of all co-authors. SH was responsible for the CH₄ measurements. JD and MG conducted ²²²Rn observations and evaluated the data. UK contributed STILT footprint and concentration modelling and, together with FM programmed the evaluation codes.

Acknowledgements

625 The long-term atmospheric observations of CH₄ and ²²²Radon in Heidelberg have been conducted in the framework of numerous research projects funded by German Ministries and by the European Commission. These measurements are now part of the observational program at the ICOS pilot station of the Central Radiocarbon Laboratory of ICOS RI. Ute Karstens is partly funded by the metrology project EMPIR 19ENV01 “traceRadon”.

References

- 630 Bergamaschi, P., Frankenberg, C., Meirink, J.F., Krol, M., Villani, M.G., Houweling, S., Dentener, F., Dlugokencky, E.J., Miller, J.B., Gatti, L.V., Engel, A., and Levin, I.: Inverse modeling of global and regional CH₄ emissions using SCIAMACHY satellite retrievals, *J. Geophys. Res.*, 114, D22301, 28 PP, doi:10.1029/2009JD012287, 2009.
- Bergamaschi, P., Karstens, U., Manning, A., Saunois, M., Tsuruta, A., Berchet, A., Vermeulen, A., Arnold, T., Janssens-Maenhout, G., Hammer, S., Levin, I., Schmidt, M., Ramonet, M., Lopez, M., Lavric, J., Aalto, T., Chen, H., Feist, D.G.,
- 635 Gerbig, C., Haszpra, L., Hermansen, O., Manca, G., Moncrieff, J., Meinhardt, F., Necki, J., Galkowski, M., O'Doherty, S., Paramonova, N., Scheeren, H., Steinbacher, M., and Dlugokencky, E.: Inverse modelling of European CH₄ emissions during 2006–2012 using different inverse models and reassessed atmospheric observations, *Atmos. Chem. Phys.*, 18, 901–920, doi.org:10.5194/acp-18-901-2018, 2018.
- Biraud, S., Ciais, P., Ramonet, M., Simmonds, P., Kazan, V., Monfray, P., O'Doherty, S., Spain, T.G., and Jennings, S.G.:
- 640 European greenhouse gas emissions estimated from continuous atmospheric measurements and radon ²²² at Mace Head, Ireland, *J. Geophys. Res.* 105(D1), 1351–1366, 2000.
- Blake, D., and F. Rowland: Continuing worldwide increase in tropospheric methane, *Science*, 239, 1129–1131, 1988.
- Brown, C. W., and C. D. Keeling: The concentration of atmospheric carbon dioxide in Antarctica, *J. Geophys. Res.*, 70(24), 6077–6085, doi:10.1029/JZ070i024p06077, 1965.



- 645 Crippa, M., Guizzardi, D., Schaaf, E., Solazzo, E., Muntean, M., Monforti-Ferrario, F., Olivier, J.G.J., Vignati, E.: Fossil CO₂ and GHG emissions of all world countries - 2021 Report, in prep. (https://edgar.jrc.ec.europa.eu/dataset_ghg60#p2)
Dlugokencky, E. J., Steele, L. P., Lang, P. M., and Masarie, K. A.: The growth rate and distribution of atmospheric methane, *J. Geophys. Res.-Atmos.*, 99 (D8), 17021-17043, doi:10.1029/94jd01245, 1994.
Dlugokencky, E. J., Myers, R. C., Lang, P. M., Masarie, K. A., Crotwell, A. M., Thoning, K. W., Hall, B. D., Elkins, J. W.,
650 and Steele, L. P.: Conversion of NOAA atmospheric dry air CH₄ mole fractions to a gravimetrically prepared standard scale, *J. Geophys. Res.*, 110, D18306, doi:10.1029/2005JD006035, 2005.
Dörr, H., Kromer, B., Levin, I., Münnich, K. O., and Volpp H. J.: CO₂ and Radon-222 as tracers for atmospheric transport, *J. Geophys. Res.* 88, C2, 1309-1313, 1983.
Dörr, H., and K.O. Münnich: ²²²Rn flux and soil air concentration profiles in West-Germany; soil ²²²Rn as tracer for gas
655 transport in the unsaturated soil zone, *Tellus*, 42B, 20-28, 1990.
Gaudry, A., Polian, G., Ardouin, B., and Lambert, G.: Radon-calibrated emissions of CO₂ from South Africa, *Tellus* 42B, 9-19, 1990.
Griffiths, A. D., Chambers, S. D., Williams, A. G., and Werczynski, S.: Increasing the accuracy and temporal resolution of two-filter radon-222 measurements by correcting for the instrument response, *Atmos. Meas. Tech.*, 9, 2689–2707,
660 <https://doi.org/10.5194/amt-9-2689-2016>, 2016.
Hammer, S., Glatzel-Mattheier, H., Müller, L., Sabasch, M., Schmidt, M., Schmitt, S., Schönherr, C., Vogel, F., Worthy, D.E., and Levin, I.: A gas chromatographic system for high-precision quasi-continuous atmospheric measurements of CO₂, CH₄, N₂O, SF₆, CO and H₂, available from <https://www.researchgate.net/publication/255704060>, 2008.
Hammer, S., and Levin, I.: Seasonal variation of molecular hydrogen uptake by soils inferred from atmospheric observations
665 in Heidelberg, south-west Germany, *Tellus*, 61B, 556-565, DOI: 10.1111/j.1600-0889.2009.00417.x, 2009.
Hanel, M., Rakovec, O., Markonis, Y., Máca, P., Samaniego, L., Kyselý, J., and Kumar, R.: Revisiting the recent European droughts from a long-term perspective. *Sci Rep* 8, 9499, <https://doi.org/10.1038/s41598-018-27464-4>, 2018.
Hersbach, H., Rosnay, P. d., Bell, B., Schepers, D., Simmons, A., Soci, C., Abdalla, S., Alonso-Balmaseda, M., Balsamo, G., Bechtold, P., Berrisford, P., Bidlot, J.-R., de Boissésón, E., Bonavita, M., Browne, P., Buizza, R., Dahlgren, P., Dee, D.,
670 Dragani, R., Diamantakis, M., Flemming, J., Forbes, R., Geer, A. J., Haiden, T., Hólm, E., Haimberger, L., Hogan, R., Horányi, A., Janiskova, M., Laloyaux, P., Lopez, P., Munoz-Sabater, J., Peubey, C., Radu, R., Richardson, D., Thépaut, J.-N., Vitart, F., Yang, X., Zsótér, E., and Zuo, H. (2018). Operational global reanalysis: progress, future directions and synergies with NWP. Available at: <https://www.ecmwf.int/node/18765>
ICOS RI: ICOS Atmosphere Station Specification V2.0, edited by: Laurent, O., ICOS ERIC, <https://doi.org/10.18160/GK28-2188>, 2020.
675 Janssens-Maenhout, G., Crippa, M., Guizzardi, D., Muntean, M., Schaaf, E., Dentener, F., Bergamaschi, P., Pagliari, V., Olivier, J. G. J., Peters, J. A. H. W., van Aardenne, J. A., Monni, S., Doering, U., Petrescu, A. M. R., Solazzo, E., and



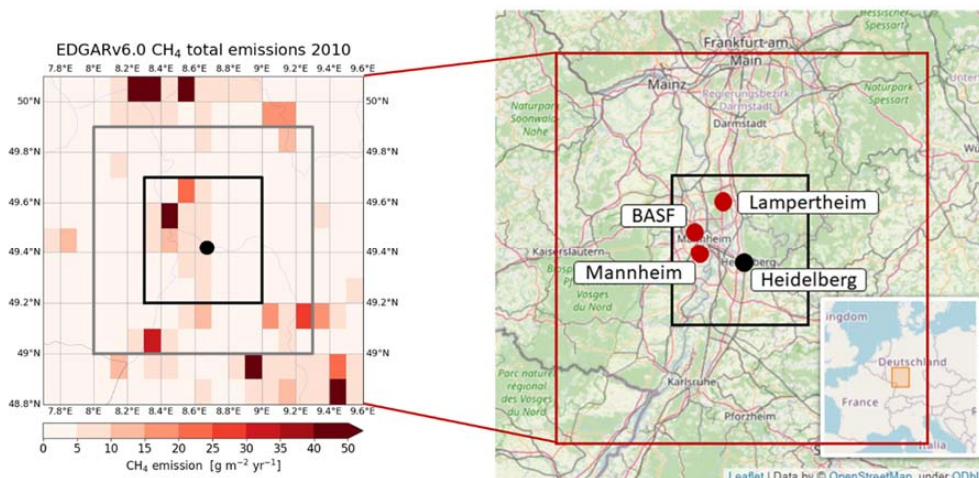
- Oreggioni, G. D.: EDGAR v4.3.2 Global Atlas of the three major greenhouse gas emissions for the period 1970–2012, *Earth Syst. Sci. Data*, 11, 959–1002, <https://doi.org/10.5194/essd-11-959-2019>, 2019.
- 680 Jutzi, S.: Verteilung der Boden-Radon Exhalation in Europa, Staatsexamensarbeit, Institut für Umwelphysik, Heidelberg University, Germany, 57 pp., 2001.
- Karstens, U., Schwingshackl, C., Schmithüsen, D., and Levin, I.: A process-based ²²²Radon flux map for Europe and its comparison to long-term observations, *Atmos. Chem. Phys.*, 15, 12845–12865, <https://doi.org/10.5194/acp-15-12845-2015>, 2015.
- 685 Lehmann, B. E., Lehmann, M., Neftel, A., and Tarakanov, S. V.: Radon-222 Monitoring of Soil Diffusivity, *Geophys. Res. Lett.*, 27, 23, 3917–3920, 2000.
- Levin, I.: Atmosphärisches CO₂, Quellen und Senken auf dem Europäischen Kontinent. *PhD thesis*, University of Heidelberg, 1984.
- Levin, I., Glatzel-Mattheier, H., Marik, T., Cuntz, M., Schmidt, M., and Worthy, D. E.: Verification of German methane
690 emission inventories and their recent changes based on atmospheric observations, *J. Geophys. Res.*, 104, D3, 3447 – 3456, 1999.
- Levin, I., Born, M., Cuntz, M., Langendörfer, U., Mantsch, S., Naegler, T., Schmidt, M., Varlagin, A., Verclas, S., and Wagenbach, D: Observations of atmospheric variability and soil exhalation rate of Radon-222 at a Russian forest site: Technical approach and deployment for boundary layer studies, *Tellus*, 54B, 462–475, 2002.
- 695 Levin, I., Hammer, S., Eichelmann, E., and Vogel, F.: Verification of greenhouse gas emission reductions: The prospect of atmospheric monitoring in polluted areas, *Philosophical Transactions A*, 369, 1906–1924, doi:10.1098/rsta.2010.0249, 2011.
- Li, M., Wu, P. and Ma, Z.: A comprehensive evaluation of soil moisture and soil temperature from third-generation atmospheric and land reanalysis data sets, *Int. J. Climatol.*, 40, 5744–5766, <https://doi.org/10.1002/joc.6549>, 2020.
- Lin, J. C., Gerbig, C., Wofsy, S. C., Andrews, A. E., Daube, B. C., Davis, K. J., and Grainger, C. A.: A near-field tool for
700 simulating the upstream influence of atmospheric observations: The Stochastic Time-Inverted Lagrangian Transport (STILT) model, *J. Geophys. Res.*, 108, 4493, doi:10.1029/2002JD003161, 2003.
- Liu, S. C., McAfee, J. R., and Cicerone, R. J.: Radon-222 and tropospheric vertical transport. *J. Geophys. Res.*, 89, 7291–7297, 1984.
- López-Coto, J., Mas, J. L., and Bolivar, J. P.: A 40-year retrospective European radon flux inventory including
705 climatological variability, *Atmos. Environ.*, 73, 22–33, doi:10.1016/j.atmosenv.2013.02.043, 2013.
- Miguez-Macho, G., Li, H., and Fan, Y.: Simulated Water Table and Soil Moisture Climatology Over North America, *B. Am. Meteorol. Soc.*, 89, 663–672, doi:10.1175/BAMS-89-5-663, 2008.
- Millington, R. J. and Quirk, J. P.: Transport in Porous media, *Proceedings of the 7th International Congress of soil Science*, Madison, Wisconsin, USA, 97–106, 1960.
- 710 Nazaroff, W.: Radon transport from soil to air, *Rev. Geophys.*, 30, 137–160, 1992.



- Pales, J. C., and C. D. Keeling: The concentration of atmospheric carbon dioxide in Hawaii, *J. Geophys. Res.*, 70(24), 6053–6076, 1965.
- Petrescu, A. M. R., Qiu, C., Ciais, P., Thompson, R. L., Peylin, P., McGrath, M. J., Solazzo, E., Janssens-Maenhout, G., Tubiello, F. N., Bergamaschi, P., Brunner, D., Peters, G. P., Höglund-Isaksson, L., Regnier, P., Lauerwald, R., Bastviken, D., Tsuruta, A., Winiwarter, W., Patra, P. K., Kuhnert, M., Oreggioni, G. D., Crippa, M., Saunio, M., Perugini, L., Markkanen, T., Aalto, T., Groot Zwaaftink, C. D., Yao, Y., Wilson, C., Conchedda, G., Günther, D., Leip, A., Smith, P., Haussaire, J.-M., Leppänen, A., Manning, A. J., McNorton, J., Brockmann, P., and Dolman, H.: The consolidated European synthesis of CH₄ and N₂O emissions for EU27 and UK: 1990–2018, *Earth Syst. Sci. Data Discuss.* [preprint], <https://doi.org/10.5194/essd-2020-367>, accepted, 2021.
- Porstendörfer, J.: Tutorial/Review: Properties and behaviour of Radon and Thoron and their decay products in the air, *Journal of Aerosol Sciences* 25(2), 219–263, 1994.
- Schery, S. D. and Wasiolek, M. A.: Radon and Thoron in the Human Environment, chap. Modeling Radon Flux from the Earth's Surface, World Scientific Publishing, Singapore, 207–217, 1998.
- Schmidt, M., Glatzel-Mattheier, H., Sartorius, H., Worthy, D. E., and Levin, I.: Western European N₂O emissions – a top down approach based on atmospheric observations, *J. Geophys. Res.* 106, D6, 5507-5516, 2001.
- Schmithüsen, D.: Atmospheric and soil flux radon measurements in Heidelberg, Diplomarbeit, Institut für Umweltp Physik, Heidelberg University, Germany, 66 pp., 2012.
- Schmithüsen, D., Chambers, S., Fischer, B., Gilge, S., Hatakka, J., Kazan, V., Neubert, R., Paatero, J., Ramonet, M., Schlosser, C., Schmid, S., Vermeulen, A., and Levin, I.: A European-wide ²²²Radon and ²²²Radon progeny comparison study, *Atm. Meas. Tech.*, 10, 1299–1312, 2017, doi:10.5194/amt-10-1299-2017, 2017.
- Schmitt, S., Hanselmann, A., Wollschläger, U., Hammer, S., and Levin, I.: Investigation of parameters controlling the soil sink of atmospheric molecular hydrogen, *Tellus*, 61B, 416-423, 2009.
- Schüßler, W.: Effektive Parameter zur Bestimmung des Gasaustauschs zwischen Boden und Atmosphäre, PhD thesis, Heidelberg University, Germany, 1996.
- Schwingshackl, C.: Experimental Validation of a Radon-222 Flux Map, Master Thesis, Institut für Umweltp Physik, Heidelberg University, Germany, 100 pp., 2013.
- Servant, J.: Temporal and spatial variations of the concentration of the short-lived decay products of radon in the lower atmosphere, *Tellus* 18, 663-671, <https://doi.org/10.1111/j.2153-3490.1966.tb00283.x>, 1966.
- Stull, R.: An Introduction to Boundary Layer Meteorology. Kluwer Academic Publishers, pp, 1998.
- Szegvary, T., Conen, F., and Ciais, P.: European ²²²Rn inventory for applied atmospheric studies. *Atmos. Environ.*, doi 10.1016/j.atmosenv.2008.11.025, 2009.
- UNFCCC: The Paris Agreement. http://unfccc.int/files/essential_background/convention/application/pdf/english_paris_agreement.pdf, 2015.



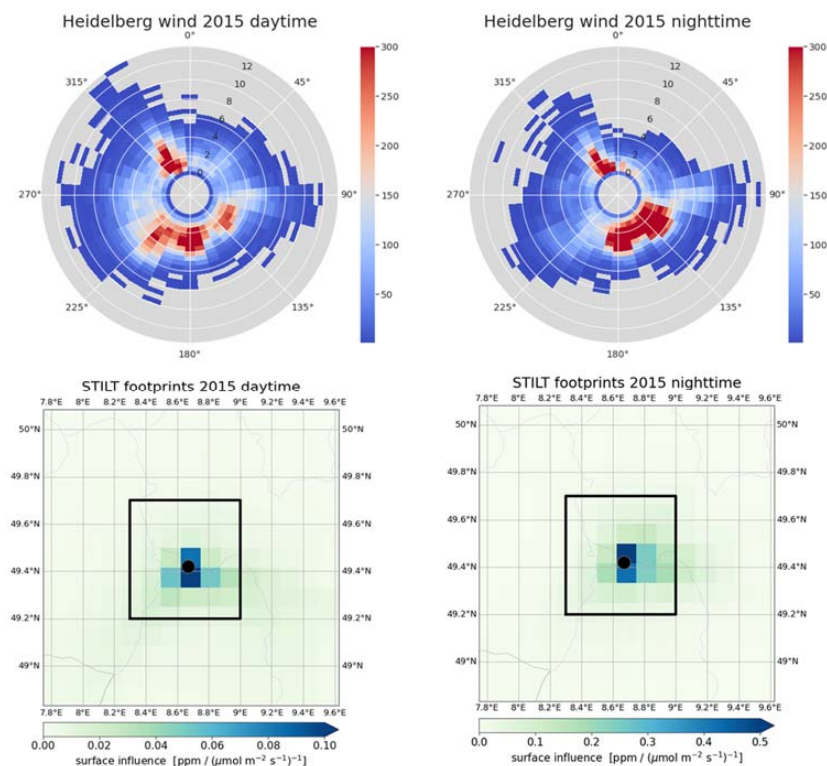
- Williams, A. G., and Chambers, S. D.: A history of radon measurements at Cape Grim, Baseline Atmospheric Program
745 (Australia) History and Recollections, 40th Anniversary Special edn., 131–146, 2016.
- Witi, J., and Romano, D.: Reporting guidance and tables. 2019 Refinement to the 2006 IPCC Guidelines for National
Greenhouse Gas Inventories, Vol. 1, D. Gomez and W. Irving, Eds., IPCC, 8.1–8.36, [www.ipcc-nggip.iges.or.jp/
public/2019rf/pdf/1_Volume1/19R_V1_Ch08_Reporting_Guidance.pdf](http://www.ipcc-nggip.iges.or.jp/public/2019rf/pdf/1_Volume1/19R_V1_Ch08_Reporting_Guidance.pdf), 2019.
- Wollschläger, U., Pfaff, T., and Roth, K.: Field-scale apparent hydraulic parameterisation obtained from TDR time series
750 and inverse modelling, *Hydrology and Earth System Sciences*, 13 (10), 1953–1966, doi: 10.5194/hess-13-1953-2009, 2009.



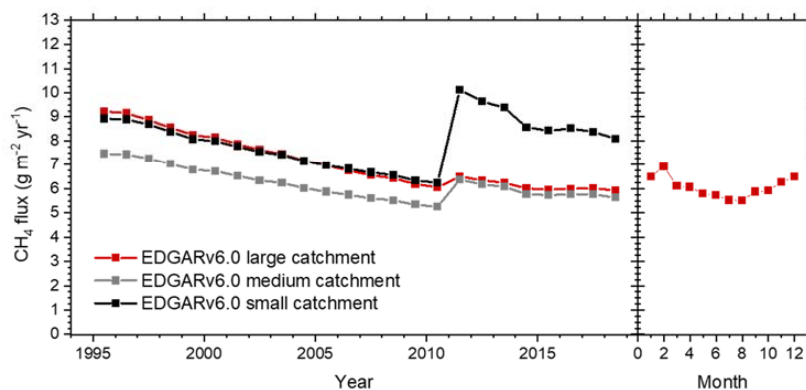
755

Figure 1, right panel: Map of the upper Rhine valley south of Frankfurt/Main with the location of Heidelberg (black dot). The red dots indicate industrial areas (Mannheim/Ludwigshafen with the BASF chemical factory) as well as locations of large solid waste deposits (Lampertheim, Mannheim) in the small catchment of the station (© OpenStreetMap contributors 2021). Distributed under the Open Data Commons Open Database License (ODbL) v1.0, 2021). Left panel. Gridded CH₄ emissions as reported by the EDGARv6.0 inventory for 2010 (Crippa et al., 2021) covering a ca. 150 km x 150 km (“large”) area surrounding Heidelberg. Two smaller areas, the so-called “small” (ca. 70 km x 70 km) and “intermediate” (ca. 110 km x 110 km) catchment areas of Heidelberg are marked as black and grey rectangle, respectively. Long-term trends of average CH₄ emissions from the three catchment areas are displayed in Fig. 3.

765



770 **Figure 2:** The upper two panels show the wind distributions (5-minute mean values, wind velocity in m s^{-1} displayed on the radius) in 2015 measured on the roof of the Institute for Environmental Physics building at a height of 37 m a.g.l. Daytime (left panel) and nighttime (right panel) wind distributions are similar. The lower two panels show the annually aggregated surface influences of potential emissions for 2015 (left: daytime and right: nighttime). Note the different scales for day and night, indicating an appr. 5-fold sensitivity of emissions on concentrations observed at 30 m a.g.l. during nighttime compared to daytime. The black rectangle marks the “small” catchment area with Heidelberg in the approximate centre (black dot).



775

Figure 3: Long-term trends of CH₄ fluxes as reported by the EDGARv6.0 emission inventory (Crippa et al., 2021). Trends for all three catchment areas show a significant decrease from 1995 to 2010 of about 30%. In 2011 an abrupt increase is observed, which is largest for the small catchment and due to an artefact of reported emissions in the MA/LU pixel (see text). The seasonal cycle of 2010 emissions in the large catchment is displayed on the right hand side of the diagram.

780

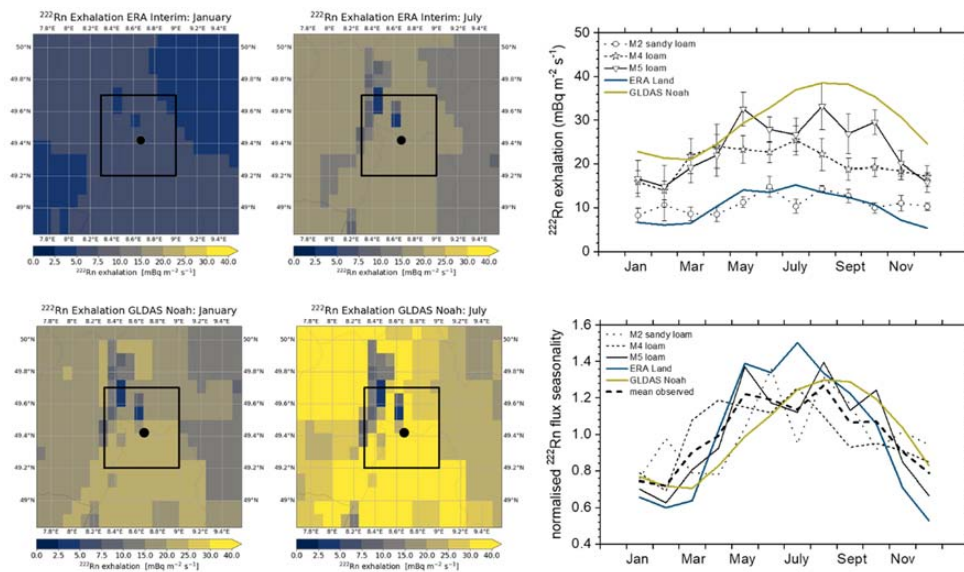
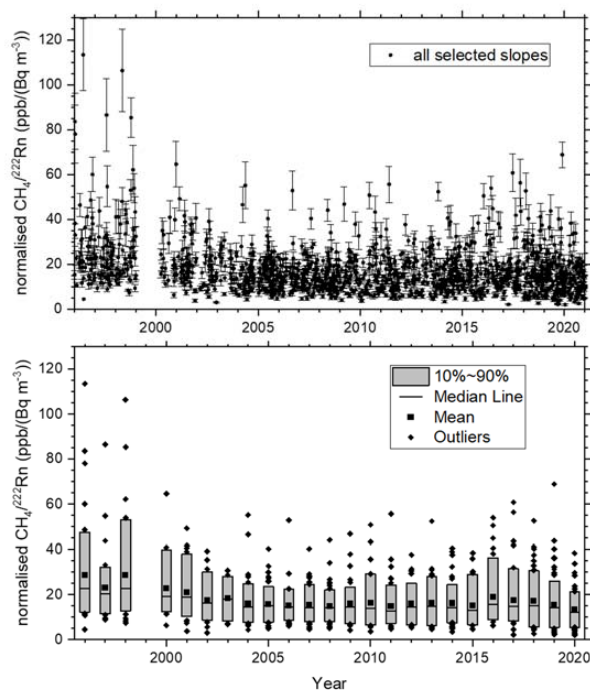
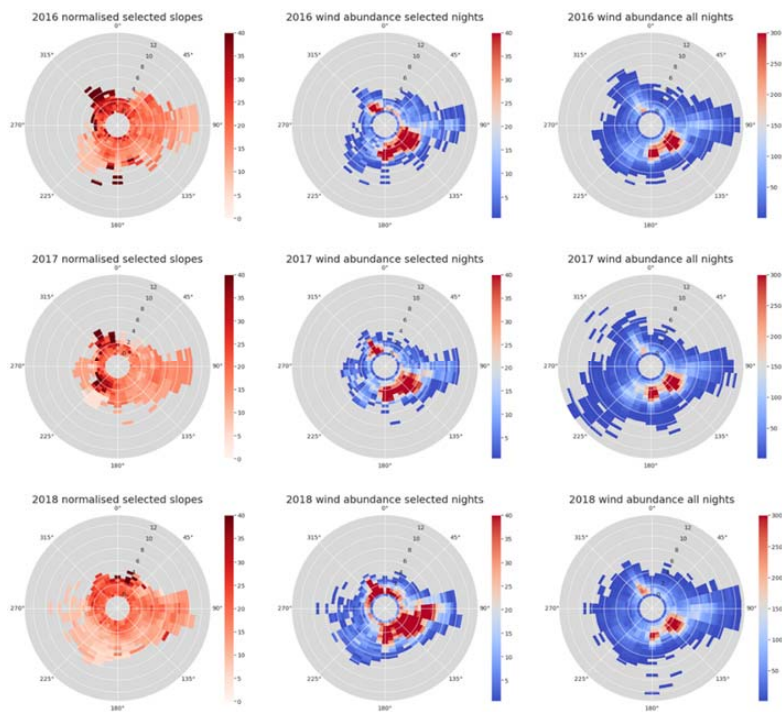


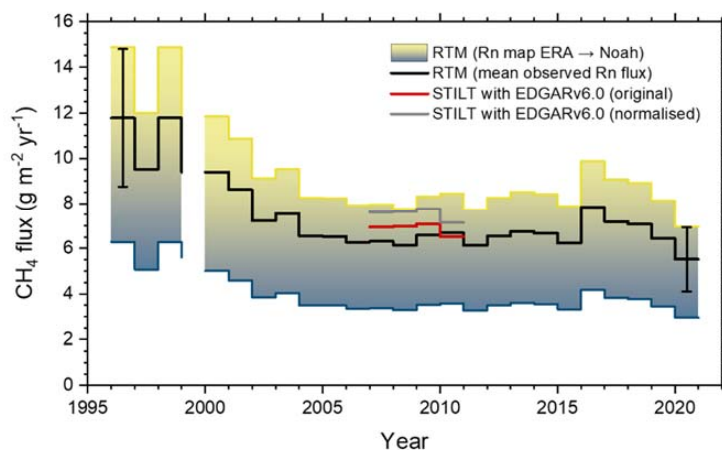
Figure 4, left panels: ^{222}Rn exhalation rates as estimated by Karstens et al. (2015) for the large Heidelberg catchment area based on the ERA Interim Land (upper panels) and GLDAS Noah (lower panels) soil moisture models for January (left) and July (middle). The small catchment area is marked by the black rectangle with Heidelberg in its appr. centre (black dot). The very low ^{222}Rn fluxes north-west of Heidelberg stem from the ^{222}Rn flux limitation assumed in Karstens et al. (2015) based on the water table depth map by Miguez-Macho et al. (2008). The upper right panel shows the mean seasonal cycle of the modelled fluxes in comparison to measurements conducted south of Heidelberg on sandy loam (M2) and loamy soils (M4, M5). Normalised (to their annual means) seasonal cycles of the fluxes shown in the upper right panel are displayed in the lower right panel. The mean observed ^{222}Rn flux seasonality is also shown as thick dashed line.



795 **Figure 5, upper panel: Individual normalised $\text{CH}_4/^{222}\text{Rn}$ slopes and their 1σ uncertainties of linear regressions with $R^2 \geq 0.7$, calculated from half-hourly night time (21:00 h to 04:00 h CET) data. Lower panel: annually aggregated $\text{CH}_4/^{222}\text{Rn}$ slopes presented as box-plots with the boxes including 80% of the data.**



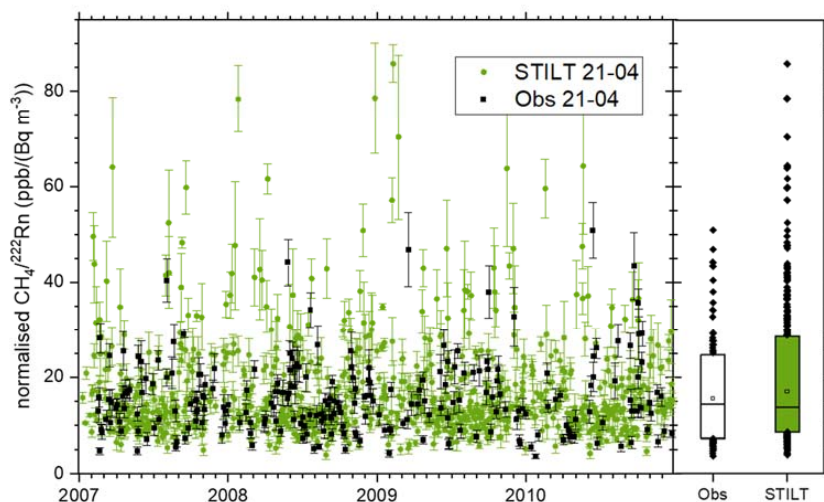
800 **Figure 6 left column: Distribution of night time slopes (in ppb (Bq m⁻³)⁻¹) by local wind direction (°) and velocity (m s⁻¹) for the years 2016, 2017 and 2019. The corresponding frequency distributions of wind direction and velocity for the selected nights are displayed in the second column while the distribution for all nights of the respective year (from 21:00 h – 04:00 h CET) are shown in the third column. It is clearly visible that wind velocities are generally lower during the selected nights than during all nights.**



805

Figure 7: Long-term trend of the RTM-based CH_4 flux in the Heidelberg catchment area. The black histogram (with typical RTM-based uncertainties shown for the first and the last year of observations) was calculated based on the observation-based ^{222}Rn flux of $18.3 \pm 4.7 \text{ Bq m}^{-2} \text{ s}^{-1}$. The coloured area shows the range of RTM-based CH_4 flux estimates if either the GLDAS Noah soil moisture (yellow) or the ERA Interim Land soil moisture (blue) based ^{222}Rn flux average of the small catchment area would have been used to calculate RTM-based CH_4 fluxes. Also included in the diagram are RTM-based results from STILT-modelled CH_4 and ^{222}Rn data for 2007 – 2010 (based on the slopes in Fig. 8). The red line shows the original results using the EDGARv6.0 emission inventory and the ^{222}Rn flux climatology while the grey line shows the STILT results normalised to the observation-based ^{222}Rn flux (see text).

810



815

Figure 8: Variability of observed (Obs, black squares) and simulated (STILT, green dots) night-time $\text{CH}_4/^{222}\text{Rn}$ slopes from 2007 to 2010 (left panel). The right panel shows the distributions of all slopes with the boxes including 80% of the data, the open squares representing the mean and the horizontal lines the median values. Note that for the further discussion we excluded the three modelled values >70 ppb (Bq m⁻³)⁻¹.

820

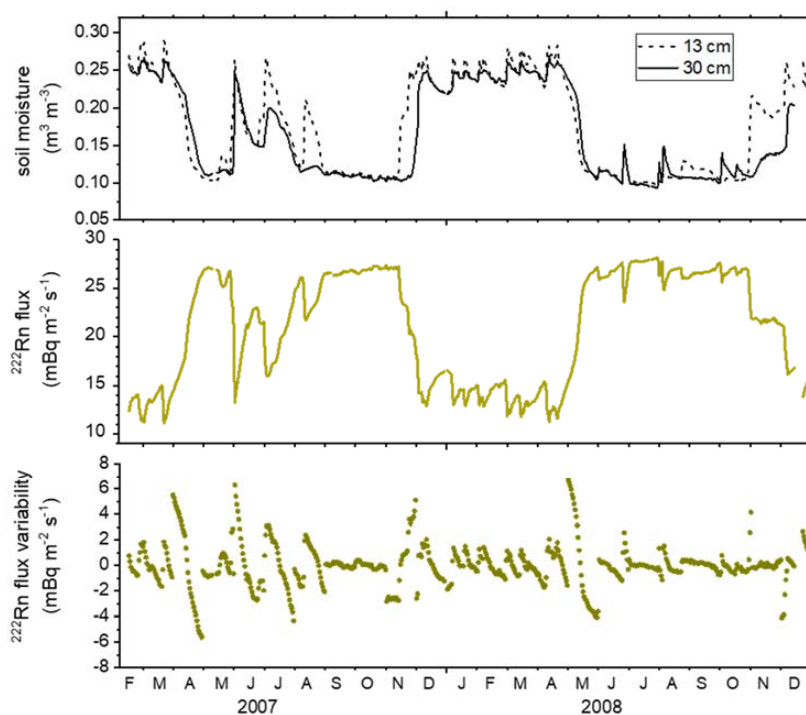


Figure A1, upper panel: Daily variations of measured soil moisture at the Grenzhof site near Heidelberg at 13 cm and 30 cm depth. The hypothetical ^{222}Rn flux estimated from the soil moisture (and temperature) variability is shown in the middle panel, while the day-to-day variability around the corresponding monthly means of the ^{222}Rn flux is shown in the lowest panel. The average variability corresponds to 10% around the monthly mean flux.