Interpreting machine learning prediction of fire emissions and comparison with FireMIP process-based models

Sally S.-C. Wang[1], Yun Qian[1], L. Ruby Leung[1], Yang Zhang[2]

[1]Atmospheric Sciences and Global Change Division, Pacific Northwest National Laboratory, Richland, Washington, 99354, USA

[2] Department of Civil and Environmental Engineering, Northeastern University, Boston, Massachusetts, 02115, USA

Correspondence to: Sally S.-C. Wang (sing-chun.wang@pnnl.gov) and L. Ruby Leung (Ruby.Leung@pnnl.gov)

Abstract. Annual burned areas in the United States have increased twofold during the past decades. With more large fires resulting in more emissions of fine particulate matter, an accurate prediction of fire emissions is critical for quantifying the impacts of fires on air quality, human health, and climate. This study aims to construct a machine learning (ML) model with game-theory interpretation to predict monthly fire emissions over the contiguous US (CONUS) and to understand the controlling factors of fire emissions. The optimized ML model is used to diagnose the process-based models in the Fire Modeling Intercomparison Project (FireMIP) to inform future development. Results show promising performance for the ML model, Community Land Model (CLM), and Joint UK Land Environment Simulator-Interactive Fire And Emission Algorithm For Natural Environments (JULES-INFERNO) in reproducing the spatial distributions, seasonality, and interannual variability of fire emissions over CONUS. Regional analysis shows that only the ML model and CLM simulate the realistic interannual variability of fire emissions for most of the subregions (r>0.95 for ML and r=0.14~0.70 for CLM), except for Mediterranean California, where all the models perform poorly (r=0.74 for ML and r<0.30 for the FireMIP models). Regarding seasonality, most models capture the peak emission in July over western US. However, all models except for the ML model fail to reproduce the bimodal peaks in July and October over Mediterranean California, which may be explained by the smaller wind speeds of the atmospheric forcing data during Santa Ana wind events and limitations in model parameterizations for capturing the effects of Santa Ana winds on fire activity. Furthermore, most models struggle to capture the spring peak in emissions in southeastern US, probably due to underrepresentation of human effects and the influences of winter dryness on fires in the models. As for extreme events, both the ML model and CLM successfully reproduce the frequency map of extreme emission occurrence but overestimate the number of months with extremely large fire emissions. Comparing the fire $PM_{2.5}$ emissions from the ML model with process-based fire models highlights their strengths and uncertainties for regional analysis and prediction and provides useful insights on future directions for model improvements.

1. Introduction

Large fires have increased across the United States over the past two decades, especially in the western US. While the total area burned in 2020 increased by 51% compared to the 10-year average for 2010-2019, the total number of fires in 2020 is smaller than the 10-year average. This indicates the contribution of larger and more powerful fires to the growing burned areas (NIFC, 2020). Large fires can directly lead to property damages and pose a threat to human lives (Thomas et al., 2017). Meanwhile, fine particulate matter ($PM_{2.5}$, particles with an aerodynamic diameter smaller than and equal to 2.5 μm) emitted from fires not only have negative impacts on human health but also affect climate and ecosystems (Johnston et al., 2012; Ward et al., 2012; Rap et al., 2013;

Kaulfus et al., 2017; Liu et al., 2018; Wang et al., 2018; Stowell et al., 2019). Driven by stronger fire heating and with higher injection height, aerosols emitted from large fires can be transported to broader area and stay in atmosphere longer. Given the increasing trend of fire emissions, fire smokes may become the predominant source of $PM_{2.5}$ in the US in the future (Yue et al., 2013; Liu et al., 2016; Ford et al., 2018). Thus, an accurate prediction of fire emissions is imperative for investigating the impacts of historical and future fires on air quality, human health, and climate.

One of the widely used methods for predicting fire emission is process-based fire parameterization. These process-based models generally employ universal functions depicting non-linear relationships between fires and the input variables and apply the same functions to all grid cells in a model (Pechony and Shindell, 2009; Thonicke et al., 2010). In addition, the parameters of the process-based model are usually determined by empirical or statistical functions, assuming that the same parameters apply to all the regions or regions with limited fire observations (Crevoisier et al., 2007; Parisien et al., 2016). Recently, Zou et al. (2019) developed the Region-Specific ecosystem feedback Fire (RESFire) model that includes region- and PFT-specific fire parameterizations in subregions over the globe. Their model shows improved spatial distributions and temporal variations of fire activities compared to the CLM fire model. Process-based models are usually included in the dynamic global vegetation models (DGVMs) to simulate fire dynamics, vegetation dynamics, and biogeochemistry driven by atmospheric forcing and socio-economic data (Li et al., 2013; Knorr et al., 2016). Fire emissions, including trace gases and aerosols, are calculated from the simulated fire carbon emissions and the emission factors, with the former computed as the product of the burned area, fuel load, and combustion completeness. The process-based models in DGVM coupled with other components of Earth system models can be used to assess the impacts of environmental factors on fires and the feedback between fire emissions, land processes, and climate (Kloster et al., 2010). In 2014, the Fire Model Intercomparison Project (FireMIP) was initiated to compare nine DGVMs that include fire modules to better understand the performances of the global fire models (Rabin et al., 2017). The FireMIP enables comprehensive evaluation and comparison across various process-based models and provides a dataset of long-term fire simulations for regional and global analysis (Li et al., 2019; Hantson et al., 2020).

Besides process-based fire models, data-driven statistical models are also commonly used to estimate fire activities using relationships between fires and predictor variables. Multiple linear regression (MLR) is a popular simple statistical method used for fire modeling (Spracklen et al., 2009; Morton et al., 2013; Urbieta et al., 2015; Williams et al., 2019). MLR can achieve a good performance, but it fails to capture the non-linear relationships between fires and predictors, and it is sensitive to the collinearity and combinations of predictors (Littell et al., 2009). Unlike MLR, machine learning (ML) is a novel tool for advancing fire modeling, given its strengths in resolving the complex relationships between the target and predictor variables. Different ML approaches have been used to estimate fire occurrence, burned areas, or emissions at various time scales and spatial scales (Cortez and Morais, 2007; Aldersley et al., 2011; Dillon et al., 2011; Birch et al., 2015; Kane et al., 2015; Coffield et al., 2019; Wang and Wang, 2020). Even though ML models generally achieve higher accuracy than simple statistical models, their decision processes are often inscrutable, and hence lack interpretability. The development of explainable ML represents major advances for scientific applications beyond predictions (Gunning, 2017; Arrieta et al., 2020). For example, Wang et al. (2021) used the Extreme Gradient Boosting (XGBoost) algorithm and Shapley Additive explanation (SHAP) to predict wildfire burned area and revealed the relationships between burned areas and predictor variables. As process-based and data-driven models have their own advantages and weaknesses, as listed in Table 1, comparing these models and assessing their uncertainties in historical simulations and future projections are important. Yue et al. (2013) applied an MLR and a parameterization method to estimate burned areas in ecoregions of the western US and found that both models explained ~50% of the variance in the observed burned areas. Although they compared the burned areas estimated by the two methods and quantified their uncertainties in fire projections, both methods are only driven by meteorology while the effects of fuels and human activities are not considered.

84   The FireMIP dataset provides long-term simulations of multiple DGVMs with fire modules, allowing
85 comparisons between process-based and data-driven models, with all models considering all the potential factors
86 influencing fires, including climate, weather, vegetation, and human activities. This study aims to develop an ML
87 model with game theory interpretation for fire emission prediction and to understand controls of fire emissions.
88 The ML model and SHAP are then used to reveal the important factors controlling fire emissions and diagnosis the
89 process-based FireMIP models. The ML model predicts the monthly $PM_{2.5}$ emissions from fires during 2000-2020
90 at a spatial resolution of $0.25° \times 0.25°$ over the contiguous US (CONUS). It uses the XGBoost algorithm and
91 incorporates various predictors, including local and large-scale meteorology, land surface characteristics, and
92 socioeconomic variables, which are common input variables also used by the FireMIP models while some are
93 specifically related to fire activities in CONUS. We acknowledge that different input variables between the ML
94 and FireMIP models might cause additional uncertainty for comparison. This study aims to construct an ML model
95 that predicts fire emissions over CONUS and utilize the ML model and SHAP to reveal the important factors
96 contributing to fire emissions that might not be fully represented in the process-based models. In this context, the
97 ML model and FireMIP models are optimized using different data or predictors at various scales, which enables us
98 to use the ML to diagnose the performance of FireMIP models over CONUS through the comparisons of their
99 performances and variable importance from the ML model. We evaluate and compare the predicted fire emissions
100 from the ML and FireMIP models against the GFED fire emission product, focusing on spatial distributions,
101 seasonality, and interannual variability over selected regions in CONUS. Additionally, the ML model and the
102 SHAP importance are used to identify the important drivers of fire emissions in different regions and compare them
103 with the corresponding parameterizations in the process-based models. Lastly, we compare the process-based and
104 ML model performances in simulating extremely large fire emissions, including the spatial distributions of
105 frequency and two case studies.

106 2. Data

107 2.1 Fire-induced $PM_{2.5}$ emission data

108   Monthly fire $PM_{2.5}$ emission data is obtained from the Global Fire Emissions Database (GFED). GFED
109 version 4 provides monthly burned area at $0.25°$ spatial resolution from 1997 to present, based on a combination of
110 the MODIS burned area product with active fire data from the Tropical Rainfall Measuring Mission (TRMM)
111 Visible and Infrared Scanner (VIRS) and Along-Track Scanning Radiometer (ATSR) family of sensors (Giglio et
112 al., 2013). The GFED fire $PM_{2.5}$ emissions are estimated by combining the burned area boosted by small fire burned
113 area (Randerson et al., 2012) and the emission factors based on Akagi et al. (2011) with a revised version of the
114 Carnegie-Ames-Stanford Approach (CASA) biogeochemical model that estimates fuel loads and combustion
115 completeness for each monthly time step (van der Werf et al., 2017). The emission factors are dependent on the
116 fire types, including savanna, boreal forest, temperate forest, tropical forest, and agriculture (van der Werf et al.,
117 2017). We use the GFED fire $PM_{2.5}$ emission as the target variable in the machine learning model development and
118 for model evaluation.
119   To reduce spatial heterogeneity and help model learning, we apply the inverse distance weighting (IDW)
120 (Bartier and Keller, 1996; Shepard, 1968) to interpolate the monthly gridded fire $PM_{2.5}$ emission at $0.25° \times 0.25°$.
121 The IDW method determines the value at a grid cell as the weighted average of the surrounding values within a
122 search distance, with the weights proportional to the inverse of the distance raised to the power value p. Here we
123 choose a value of 1 for p and a search distance of 35 km for IDW processing. Note that the total fire emitted $PM_{2.5}$
124 within a search distance after IDW processing is constrained to be the same as the original data. In this study, we
125 only include grids with more than eight months of fire emissions larger than zero (in a total of 250 months),

126 encompassing 90% of the total fire emissions and ensuring sufficient data for the XGBoost model training. The
127 interpolated fire emission is normalized based on its 21-year mean and standard deviation for each grid to reduce
128 the skewness and improve data symmetry.

2.2 Predictor variables

130   We develop an empirical model at 0.25° × 0.25° grid resolution driven by various predictor variables at a
131 monthly scale from January 2000 to October 2020. Given the datasets have different spatial resolutions, all the
132 predictor variables are resampled to the spatial resolution of 0.25° × 0.25° by linear interpolation. The predictor
133 variables used in the model along with their original spatial and temporal resolutions are included in Table 2. Most
134 variables were also used in Wang et al. (2021) for developing an ML model of fire burned area over the contiguous
135 U.S.

136 *Local meteorology:* Same as the local meteorological predictors used in Wang et al. (2021), we include monthly
137 data of mean surface temperature, relative humidity (RH) at 2 m, daily precipitation, zonal (U) and meridional (V)
138 components of wind at 10 m from the North American Regional Reanalysis (NARR) (Mesinger et al., 2006) and
139 1000-hour dead fuel moisture (FM1000), Energy Release Component (ERC), and vapor pressure deficit (VPD)
140 from the gridMET dataset (Abatzoglou and Kolden, 2013; Coffield et al., 2019). Drought is a natural phenomenon
141 that influences fires through ignition efficiency, fuel availability, and fuel moisture. Thus, we include the monthly
142 Standardized Precipitation Evapotranspiration Index (SPEI), a multiscalar drought index based on climatic data
143 (Vicente-Serrano et al., 2010). Given that lightning is one of the major ignition sources of fires and makes up
144 approximately 75% of burned areas in western US (Pyne, 1984; Stephens, 2005), in this study, we add the cloud-
145 to-ground (CG) lightning flash density from Severe Weather Data Inventory (SWDI) based on the National
146 Lightning Detection Network (NLDN) (Cummins and Murphy, 2009; NOAA, 2006). The daily number of CG
147 lightning flashes is summarized in 0.1° tiles and we aggregate the daily data to monthly scale.

148 *Large-scale meteorological patterns:* Large-scale meteorological patterns at a synoptic scale have been found to
149 link to large fire events (Crimmins, 2006; Trouet et al., 2009; Zhong et al., 2020; Dong et al., 2021). Furthermore,
150 it has been shown that including predictors of large-scale meteorological patterns conducive to wildfires
151 significantly improves the prediction of burned areas over CONUS (Wang et al., 2021). Thus, we follow the
152 methods developed by Wang et al. (2021) using the singular value decomposition (SVD) method to construct
153 predictors representing the synoptic patterns driving fire emission variability. Note that the only difference between
154 Wang et al. (2021) and this study is that they used wildfire burned area data and we use fire emissions to construct
155 the SVDs. Three regions where large fires periodically occur are selected for constructing SVDs: Northern
156 California, southern Rocky Mountains, and southeastern US, as defined in Wang et al. (2021). For each region, we
157 calculate the daily mean fire $PM_{2.5}$ emissions over the region and compute the day-to-day correlations between the
158 regional mean fire $PM_{2.5}$ emissions and the five gridded daily meteorological variables (surface temperature, 2-
159 meter RH, U-wind and V-wind at 850 hPa, and geopotential height at 500 hPa) for all 1° × 1° grid cells within the
160 large-scale domain, giving a correlation map for each meteorological variable. The correlation maps are then used
161 to derive the SVD modes representing the large-scale meteorological patterns related to fires. Finally, we compute
162 the monthly standard deviation of the daily SVD time series for the first two SVD modes, representing the month-
163 to-month variations of synoptic fluctuations and atmospheric instability. The detailed methods and discussions

164 about the SVDs are provided in Wang et al. (2021). Overall, the identified SVDs for the three regions are similar
165 to the SVDs in Wang et al. (2021) calculated using wildfire burned areas (Figs. S1-3).

166 *Land-surface properties:* We use the same set of variables in the burned area model that represent the effects of
167 fuel and land surface states on fire emissions, including evapotranspiration (ET), surface soil moisture, land types,
168 and topography (Wang et al., 2021). Monthly mean ET, vegetation fraction, and surface soil moisture are obtained
169 from the North American Land Data Assimilation System (NLDAS-2) (Xia et al., 2012). Land cover data of the
170 LAI classification scheme is obtained from the Terra and Aqua combined MODIS Land Cover Climate Modeling
171 Grid (CMG) Version 6 data (Friedl, 2015). Since the land cover data is at yearly intervals from 2001 to 2020, we
172 use the land cover data of 2001 for 2000. Topography data of slope and elevation is obtained from Amatulli et al.
173 (2018).

174 Besides the above-mentioned variables that were also used in Wang et al. (2021), in this study, we consider
175 the effect of fuel load on fire emissions, since fuel load is critical to fire emissions through its controls on fuel
176 consumption and burned areas (Parks et al., 2012; Liu and Wimberly, 2015). As there are limited observations of
177 fuel load, we use LAI to approximate the canopy bulk density, which is important crown characteristics to predict
178 crown fire spread, and vegetation fraction to represent the existing amount of vegetation (Keane et al., 2005). LAI
179 is taken from MODerate resolution Imaging Spectroradiometer (MODIS) instruments (Myneni et al., 2015) and
180 vegetation fraction is obtained from the NLDAS-2. As LAI may not fully represent the available biomass, we also
181 include fuel load simulated by Community Land Model (CLM). Monthly fuel load data from 2000 to 2015 is
182 obtained from a simulation by CLM version 5 with biogeochemistry and prognostic crop, driven by atmospheric
183 forcing from GSWP3v1 (Lawrence et al., 2019). The fuel load after 2015 is taken from a simulation under the SSP3
184 (shared socioeconomic pathways) scenario. CLM fuel load is validated by comparing with the fuel-measured fuel
185 load from the global fuel consumption database (van der Werf et al., 2017; Van Leeuwen et al., 2014), as shown in
186 Fig. S4. The CLM-simulated fuel load is generally consistent with the measured fuel load for different vegetation
187 types across CONUS based on the limited measurements. Additionally, we include normalized fuel load as a
188 predictor to capture the effects of temporal variation of fuel load, as the influence of fuel load on fire emissions is
189 mainly attributed to its spatial variation rather than the temporal variation (Lasslop and Kloster, 2015).
190

191 *Socioeconomic variables:* We use population density and gross domestic product (GDP) per capita to represent
192 human effects on wildfires. The population density data is obtained from the Gridded Population of the World data
193 collection (GPW V4) for the years 2000, 2010, 2015, and 2020, with a spatial resolution of 30 arc-second (CIESIN-
194 Columbia University, 2017). The populations in other years are linearly interpolated between the abovementioned
195 four years. The GDP per capita is taken from a gridded global dataset for 2000-2015 with a spatial resolution of 5
196 arc minutes (Kummu et al., 2018). For the GDP after 2015, we use the data of 2015.

197 **3. Description of fire emission models**

198 **3.1 Process-based fire emission models**

199 The Fire Model Intercomparison Project (FireMIP) includes a set of common fire modeling experiments
200 from nine DGVMs driven by the same forcing data, allowing a better understanding of global fire models (Rabin
201 et al., 2017). The FireMIP dataset provides global gridded burned area fraction and fire emissions, including carbon
202 and 33 species of trace gases and aerosols over 1700-2012. Nine DGVMs with different fire modules are included

203 in FireMIP, including Community Land Model version 4.5 (CLM4.5) with the CLM5 fire module, Canadian
204 Terrestrial Ecosystem Model (CTEM), Jena Scheme for Biosphere-Atmosphere Coupling in Hamburg with Spread
205 and InTensity fire model (JSBACH-SPITFIRE; hereafter referred to as JSBACH), Joint UK Land Environment
206 Simulator with Interactive Fire And Emission Algorithm For Natural Environments (JULES-INFERNO; hereafter
207 referred to as JULES), Lund-Potsdam-Jena General Ecosystem Simulator with Global FIRe Model (LPJ-GUESS-
208 GlobFIRM; hereafter referred to as LPJ-Glob), LPJ-GUESS with SIMple FIRE model and Blaze-Induced Land-
209 Atmosphere Flux Estimator (LPJ-GUESS-SIMFIRE-BLAZE; hereafter referred to as LPJ-SIM), LPJ-GUESS with
210 SPITFIRE model (LPJ-GUESS-SPITFIRE; hereafter referred to as LPJ-SPI), MC2, and Organizing Carbon
211 Hydrology In Dynamic Ecosystems with SPITFIRE model (ORCHIDEE-SPITFIRE; hereafter referred to as
212 ORCHIDEE) (Rabin et al., 2017).
213   The nine DGVMs in FireMIP are driven by the CRU-NCEP v5.3.2 atmospheric forcing data with a spatial
214 resolution of 0.5° and a 6-hourly temporal resolution (Wei et al., 2014; Rabin et al., 2017). Other forcing data,
215 including annual global atmospheric CO_2 concentration, land use and land cover, and population density from 1700
216 to 2012 is taken from various data sources (Klein Goldewijk et al., 2010; Hurtt et al., 2011; Le Quéré et al., 2014).
217 Monthly cloud-to-ground lightning frequency with a resolution of 0.5° × 0.5° over 1901-2012 is calculated based
218 on the observed relationship between present-day lightning and convective available potential energy (CAPE)
219 anomalies (Pfeiffer et al., 2013). Fire emissions in FireMIP are calculated considering the fire carbon emissions
220 and vegetation characteristics based on the plant functional type (PFT) from the FireMIP historical transient control
221 run (SF1). SF1 breaks the simulation period into three phases: the spin-up phase in 1700, the transient phase in
222 1701-1900, and the transient phase in 1901-2012 (see the detailed descriptions and model settings in Rabin et al.,
223 2017, Li et al., 2019, and Hantsan et al., 2020). In the 1901-2012 transient phase, the models are driven by time-
224 varying atmospheric forcing, CO_2 concentration, LULCC, population density, and lightning data. Note that the
225 MC2 and CTEM runs start from 1901 and 1861, while the rest of the models start from 1700. As the spatial
226 resolutions of the FireMIP models are different, the regridded model outputs with 1° × 1° resolution obtained from
227 Li et al. (2019) are used to compare with the GFED data and the ML model.

3.2 ML-based approach: An eXtreme Gradient Boosting (XGBoost) model

229   The eXtreme Gradient Boosting (XGBoost) is a decision-tree-based ensemble machine learning method
230 using the gradient boosting approach (Chen and Guestrin, 2016). The XGBoost model builds multiple decision
231 trees that are added subsequently and learn the errors of the previous tree to reduce the loss and obtain the best
232 prediction. Unlike the gradient boosting machine (GBM) that also uses the gradient boosting approach, XGBoost
233 utilizes a more regularized model formalization to prevent over-fitting and improve the computational efficiency.
234 The formula for the prediction at step t and grid location i can be defined as follows:

$$\hat{y}_i^t = \sum_{k=1}^{t} f_k(x_i) = \hat{y}_i^{(t-1)} + f_t(x_i)$$

236 where $f_t(x_i)$ is the tree model at step t, $\hat{y}_i^t$ and $\hat{y}_i^{(t-1)}$ are the predictions at steps t and t-1, and x_i are the predictor
237 variables. The parameters of the model $f_t(x_i)$ are selected by optimizing the objective function that measures how
238 well the model fit the training data:

$$Obj^t = \sum_{i=1}^{n} L^t + \Omega^t$$

240 which is composed of the loss function L^t and the regularizing term Ω^t in each step. L_t is defined as $l(y_i, \hat{y}_i^{t-1} +$
241 $f_t(x_i))$ and Ω^t is defined as $\gamma T + \frac{1}{2}\lambda\|\omega\|^2$, where γ is the regularization term which penalizes the number of
242 leaves in the tree T and λ is the regularization term which penalizes ω, the weights of different leaves.

243   We use grid search to choose the set of suitable hyperparameters and achieve the best ML model
244 performance. Grid search is a tuning technique for computing the optimal values of hyperparameters considering
245 a range of numbers with a given increment. The parameter set that yields the best 5-fold cross-validation score is
246 selected as the final set of hyper-parameters. The considered hyper-parameters, their search domains, and the final
247 values are denoted in Table S1.

248   The 10-fold cross-validation (CV) technique is applied to evaluate the model and avoid overfitting. First,
249 we randomly divide the fire emission dataset (2000-2020 over CONUS) into ten equal-sized splits. Then, we train
250 the model with nine splits of the data and use the trained model to predict fire emissions for the remaining one split.
251 This process is repeated ten times for each split. Finally, the predictions are evaluated by grids and regions using
252 root mean square error (RMSE), correlation coefficient (R), and the index of agreement (IoA). The IoA represents
253 the ratio of the mean square error and the potential error, and the value closer to 1 indicates better agreement.

254 3.3 Shapley additive explanations (SHAP)

255   We utilize the SHAP to identify the relative importance of the predictor variables. SHAP is a novel
256 approach to resolve and explain variable importance based on game theory (Lundberg and Lee, 2017). Within the
257 scope of game theory, the goal is a prediction for a single observation. Each predictor variable is referred to as a
258 "player" in this game and contributes to the goal ("payout"). For each predictor, the SHAP variable importance
259 measures the marginal contribution considering all possible combinations of the predictor variables. The marginal
260 contribution is calculated by comparing the differences between the model fit $f_x(S \cup \{i\})$ including the predictor i
261 and another model fit $f_x(S)$ without predictor i. When there is more than one predictor i, the marginal contribution
262 also depends on the interactions with other predictors. Thus, the calculation repeats considering the whole set of
263 the predictors. The final contribution ϕ_i of predictor i is the weighted average of all marginal contributions:

$$264 \qquad \phi_i = \sum_{S \subseteq F \setminus \{i\}} \frac{|S|! \, (F - |S| - 1)!}{F!} [f_x(S \cup \{i\}) - f_x(S)]$$

265 where F is the total number of features, S is the subset of predictors from all predictors except for predictor i,
266 $\frac{|S|!(F-|S|-1)!}{F!}$ is the weighting factor counting the number of permutations of the subset S. $f_x(S)$ is the expected
267 output given the predictors subset S. $[f_x(S \cup \{i\}) - f_x(S)]$ is the difference made by predictor i.

268   Compared to the commonly used feature importance, such as gain, or split count, SHAP is more consistent
269 and faithful to the model (Lundberg et al., 2019). More importantly, SHAP provides local importance that measures
270 the variable importance for each sample, while most of the feature importance metrics only have global importance
271 that measures variable contributions limited to the entire dataset. The global importance by SHAP is the average
272 of the absolute SHAP values for each predictor, providing an overall picture of the predominant variables
273 controlling fire emissions in CONUS. The local importance will be used to identify the important predictors for
274 large fire events in the ML model and diagnose the deficiency of the process-based models.

4. Results

4.1 XGBoost model performance and variable importance

277   Table 3 shows the whole CONUS and regional model performance, including RMSE, IoA, and correlation.
278 The model performs well at grid level over CONUS, with an RMSE of 0.16 g/m^2 and an IoA of 0.84. Figure 1a
279 shows the map of correlation between the observed and predicted monthly fire emission time series for each grid
280 over CONUS. Overall, the results indicate the ML model can reproduce the interannual variability of fire emissions
281 at 0.25° resolution over CONUS, with a mean correlation of 0.58 and more than 70% of the grids having
282 correlations larger than 0.4. To better assess model performance in different regions, Table 3 summarizes the model
283 performance for several selected regions: (1) western forest area, (2) Mediterranean California, (3) southwestern
284 US, and (4) southeastern US (color boxes in Fig. 1a). The regions where fires frequently occur are selected by the
285 similarity of ecoregions, vegetation types, and fire regimes. Figs. 1b-e show the time series of observed and
286 predicted fire $PM_{2.5}$ emissions averaged over several regions. Generally, the ML model reproduces the interannual
287 variability of fire emissions for the selected regions (r=0.84-0.98). Among these regions, Mediterranean California
288 has the smallest correlation coefficient and largest RMSE compared to other regions, which can be explained by
289 the fact that fires in this region interact with multiple factors, including human activity, complex terrain, and Santa
290 Ana winds (Syphard et al., 2008; Yue et al., 2014). The interactions between fires and these factors pose
291 uncertainties and challenges in fire prediction over this region. It is also worth noting that the ML model captures
292 the large fire events in September 2020 in Oregon and California but underestimates the peak values by ~30%
293 (Figs. 1b and 1c). In addition, we also test the ML model's ability to provide accurate predictions on unseen data
294 (i.e., generalization) by using data from 2000 to 2019 as a training set and data from 2020 as a testing set. As shown
295 in Fig. S5, the ML model can reproduce the spatial patterns of fire emissions well but underestimates the emissions
296 of the peak in September 2020. The results are within our expectations because the ML model generally fails to
297 make accurate predictions for the data outside of the training domain or has large uncertainties in extrapolation
298 (Tsubaki and Mizoguchi, 2020; Hooker, 2004). Since 2020 features the largest fire emissions in the study period,
299 we conducted another test using 2000-2017 and 2019-2020 to train the ML model and test on the data of 2018. We
300 selected 2018 because 2018 had the largest fires on record before 2020. The ML successfully reproduces the
301 temporal variability of fire emissions (r=0.92) and captures the peak in Aug 2018, as well as the spatial distributions
302 of fire emissions (r=0.52).
303   To improve understanding of the ML prediction, we utilize the SHAP method to quantify the contributions
304 of each predictor variable to the prediction and identify the key contributing factors of fire $PM_{2.5}$ emission. SHAP
305 importance is chosen because it provides not only global importance but also local importance that helps understand
306 which variables have larger contributions to specific events or regions. Here, we first demonstrate the global
307 importance that considers all the samples. Fig. 2 shows the 20 most important variables for the model ranked by
308 the absolute mean SHAP values. The SHAP value for a feature indicates its contribution to the prediction, so larger
309 absolute mean SHAP values indicate larger contributions to the fire emissions. Among the top 10 variables, seven
310 of them are local meteorological variables, indicating local meteorology is the predominant control of fire
311 emissions, as these variables control fire activity directly (Liu and Wimberly, 2015; Abatzoglou et al., 2016; Wang
312 et al., 2021). Besides local meteorology, the predictors of large-scale meteorology (SVD1_SElag2 and
313 SVD2_SElag2) are identified as the eighth and tenth important variables, showing that meteorology is not only
314 important at local scale but also at synoptic scale (Trouet et al., 2009; Pollina et al., 2013; Dong et al., 2021).
315 Finally, in addition to meteorology, fuel load is identified as the fifth important variable in the model, as fuel load
316 affects emission through controlling burned area and fuel consumption (Seiler and Crutzen, 1980). Considering the
317 important variables in different regions, the selected regions in western US (western forest area, Mediterranean
318 California, and southwestern US) generally share the common top 10 variables (Fig. S6). Over western US,

319 predictors controlling fuel dryness and fuel amount, including RH, fuel moisture (FM1000), ERC, vegetation
320 fraction, and fuel load, contribute more to fire emissions. On the other hand, large-scale meteorological patterns
321 (SVDs_SElag2) are more important for fire emissions in southeastern US.
322   As the dominant drivers differ for different temporal scales, we aggregate the monthly SHAP values to
323 obtain annual and seasonal time series of SHAP values for each variable. The annual and seasonal time series are
324 the averaged SHAP values over the study period for each year and month, respectively. Fig. S7 shows the mean
325 |SHAP| values at seasonal and interannual time scale for the whole CONUS. Considering both the mean |SHAP|
326 and larger correlations (r > 0.5) between the annual/seasonal time series of SHAP and mean fire emissions,
327 temperature, VPD, RH, and ERC are the dominant variables controlling the seasonal variation of fire emissions.
328 These factors have relatively stronger seasonality than other variables (e.g., VPD is usually higher in the summer).
329 On the other hand, large-scale circulation patterns, including SVD1_SElag2, SVD2_SElag2, and SVD1_RM, are
330 important variables controlling both the seasonal and interannual variability of fire emissions, while SVD2_RM
331 and SVD2_NCA mainly control interannual variability. Some identified large-scale meteorology has significant
332 seasonality (e.g., SVDs_SElag2 are predominant in spring and SVD1_RM is strongest in summer), and most of
333 them have interannual variability, as shown in Fig. 8. Overall, the SHAP analysis shows different dominant
334 predictors for fire emissions at various time scales.

335 4.2 General comparison between GFED, ML, and FireMIP models

336   This section compares the performance of the ML and FireMIP models benchmarked against observations
337 from GFED, and the evaluations are based on spatial distributions, seasonality, and interannual variability of fire
338 PM$_{2.5}$ emissions. Since the spatial resolutions of the GFED data, ML models, and FireMIP models are different,
339 they are all regridded to 1°× 1° using bilinear interpolation. Note that the simulation period of FireMIP models
340 ends in 2012, so we use the overlapping period of 2000-2012 for comparison and exclude the MC2 model because
341 its simulation ends in 2008.

342 4.2.1 Spatial distributions of fire PM$_{2.5}$ emissions and sensitivities to RH and temperature

343   Fig. 3 compares the observed and simulated spatial distributions of long-term mean monthly fire PM$_{2.5}$
344 emissions averaged over 2000-2012. Among the models, the ML model, CLM, and JULES have better performance
345 in reproducing the spatial distributions of fire emissions over CONUS, with a correlation coefficient of 0.83, 0.52,
346 0.40, respectively. The ML model shows the best agreement with GFED, though it overestimates fire emissions
347 over Northern California. Both CLM and JULES simulate more PM$_{2.5}$ emissions over southeastern US, and JULES
348 overestimates fire emissions in Northern California. Some other models, such as CTEM, JSBACH, and LPJ-SIP,
349 tend to overestimate fire emissions over central US (e.g., Great Plains and Texas). LPJ-SIM captures the hotspots
350 of fire emissions over western US and southeastern US, but it simulates much more PM$_{2.5}$ emissions over the Rocky
351 Mountain and northeastern US. In terms of the total amount of PM$_{2.5}$ emissions, all models except ORCHIDEE-
352 SPITFIRE overestimate PM$_{2.5}$ emissions (8.33-79.49 Tg), compared to the GFED estimate of 4.98 Tg during 2000-
353 2012 over CONUS (Table 4).
354   The overestimations in some models may be explained by the sensitivities of fire emissions to individual
355 meteorological variables. Fig. 4 shows the slopes for the dependence of annual mean fire PM$_{2.5}$ emissions on annual
356 mean RH from the CRUNCEP atmospheric forcing data for GFED and the ten models based on linear regression.
357 Since the ML model uses NARR meteorology as predictors, we also include sensitivities of the fire emissions
358 predicted by the ML model to the NARR meteorology (Fig. 4b). Almost all models capture the negative dependence
359 of PM$_{2.5}$ emissions on RH over western US (r=-0.06~0.84), but the sensitivities in the models are much stronger
360 (steeper negative slope) than in GFED. For temperature, positive sensitivity is shown over western US in GFED

(Fig. 5), with the largest slope in northern California. The sensitivities to temperature in models agree with the observed sensitivities (r=-0.06~0.64), but some models show much stronger sensitivities over western, central, and southeastern US. Generally, the spatial distributions of the long-term mean fire emissions shown in Fig. 3 match well with the spatial distributions of sensitivities to RH or temperature, suggesting an important role of the sensitivities in the model biases of predicting fire emissions. However, the correspondence of large fire emissions to the sensitivities to RH or temperature shows regional differences. For instance, in western US, the stronger sensitivities to both RH and temperature correspond to the overestimations in this region for most models, including the ML model, CLM, CTEM, JSBACH, JULES, LPJ-SIM, and LPJ-SPI (Figs. 4 and 5). On the other hand, over central US, larger $PM_{2.5}$ emissions simulated by CTEM and JSBACH only correspond to stronger sensitivity to temperature (Fig. 5). Similar to central US, in southeastern US, the overestimations in CLM and JULES only correlate with stronger sensitivity to temperature (Fig. 5). Regional differences in the correspondences between the predicted fire emissions and their sensitivity to meteorology can be explained by several factors. For western US, the overestimations of fire emissions correspond to both stronger sensitivities to RH and temperature, given that fire activities are sensitive to fuel aridity that is controlled by temperature and fuel moisture (Abatzoglou and Williams, 2016; Holden et al., 2018). As for southeastern US, fuels in this region typically burn at higher RH and the interannual RH variation (standard deviation) is smaller (Balch et al., 2017; Brey et al., 2018). With higher RH values and less variation in RH, the fire emissions in southeastern US show weaker sensitivity to RH than to temperature in observation (Table S2). The above analysis shows that the overestimation of fire emissions in the models may be attributed to the stronger sensitivities to meteorology. However, fire activities are controlled by meteorology and other factors such as vegetation and human, so the analysis of fire emission sensitivity to meteorology only provides a potential explanation to the overestimation of fire emissions in the models (Forkel et al., 2019).

4.2.2 Seasonality and interannual variability over CONUS

In addition to evaluating spatial distributions, it is also important to compare the models' ability to reproduce the temporal variability of fire emissions. As the models may systematically over-or underestimate fire emissions, we normalize the emissions by the mean and standard deviation and focus only on its temporal variability. Fig. 6a shows the seasonality of normalized fire $PM_{2.5}$ emission over CONUS. Most models capture the seasonality of fire emission successfully (r>0.85), except LPJ-SIM which simulates peak emission in August-October (r=0.65). Among the models, the ML model has the highest correlation coefficient between prediction and observation from GFED (r=0.98) and successfully reproduces the peak in August. The seasonal peaks simulated by the FireMIP models are broader and flatter than the peak in GFED, with an early peak in June-July continuing to September (Fig. 6a).

In terms of interannual variability (Fig. 6b), the ML model, CLM, and JULES perform better than other models, with larger correlation coefficient between simulated and observed fire $PM_{2.5}$ emissions (r=0.87, 0.71, and 0.55 for ML, CLM, and JULES, respectively; Table 4). Other models have relatively poor performance in capturing the interannual variability. The interannual variability of fire emissions shows several peaks in 2002, 2007, and 2012 (black line in Fig. 6b), when western US contributes 76% of the total emissions to the peaks in these years. Almost all models except ORCHIDEE capture the peak in 2012. However, most models miss the peaks in 2002 and 2007. Among all models, LPJ-Glob model simulates the peaks in the two years, while ML, JULES, and CLM only capture the largest emission in 2007 (Fig. 6b).

4.2.3 Seasonality and interannual variability by regions

As the temporal variability of fire activities varies by region, we compare the performance between GFED and the ML and FireMIP models by the regions defined in Sec. 4.1. Fig. 7 shows the seasonality and interannual variability of normalized fire $PM_{2.5}$ emission over western forest area, Mediterranean California, southwestern US, and the southeastern US. All models generally capture the seasonality of the western forest area peaking in summer, with correlation coefficients larger than 0.8 (Table 4). Even though the FireMIP models generally reproduce the peaks in summer, the predicted peaks are broad and flat, indicating a relatively longer fire season starting in June and ending in September (Fig. 7a). When looking at the interannual variability, we find that the ML model has the best performance with a correlation coefficient of 0.93, and it successfully captures the largest fire emission in 2007. CLM, JULES, and LGJ-Glob perform better than the rest of the models (r=0.70, 0.60, and 0.51 for CLM, JULES, and LPJ-Glob, respectively; Table 4), but all of them still miss the peaks in 2007 and overestimate fire emissions in 2001 and 2003 (Fig. 7b). The emission peak in 2007 is mainly attributed to the large fires in Idaho, which were associated with synoptic weather patterns characterized by positive geopotential height and temperature anomalies over the Pacific Coast and western US (Zhong et al., 2020). Consistent with prior findings, SHAP importance shows that in the ML model SVD predictors (SVD_NCA and SVD_RM in July and August 2007 Fig. 8a) are the dominant factors of fire emissions in 2007 (contribute 27% and 28% for July and August 2007, respectively), which are characterized by high pressure, low RH, and northeasterly winds over western US (Figs. S1 and S2). Thus, the underestimation of peak emission in 2007 may be explained by the fact that the influences of large-scale meteorology on fire activity are not fully considered in the FireMIP models, which are point models driven only by local atmospheric forcing.

In Mediterranean California, the seasonality of fire emissions shows a bimodal pattern, peaking in August and October. The peak in October is mainly due to the extremely large fires associated with Santa Ana winds in 2003 and 2007 (Keeley et al., 2009; Yue et al., 2014). The ML model simulates a flatter peak from July to October, while all the FireMIP models except ORCHIDEE capture the first emission peak in summer but fail to simulate the large fire emission in October (Fig. 7c). The underestimation associated with the Santa Ana winds is also shown in the interannual time series in Fig. 7d. Several models, including LPJ-Glob, CTEM, LPJ-SPI, and JULES, capture the peak in 2007 but only the ML model predicts both peaks in 2003 and 2007 even though the peak in 2003 is underestimated. According to the SHAP importance from the ML model, the peak emissions in October 2003 and October 2007 are mainly contributed by the SVD predictors and ERC (SVD2_NCA and SVD1_RM together contribute 20% to the fire emissions for October 2003 and SVDs_SElag2 and SVD2_RM together contribute 31% to the fire emissions for October 2007) and ERC (15% and 18% for October 2003 and 2007, respectively) (Fig. 8b). The results indicate that the ML model captures the effect of synoptic weather patterns on fire activity by including the SVD predictors. Even though the wind speed is included in simulating fire spread in the FireMIP models, the spatial resolutions of the models and/or the atmospheric forcing data may not be fine enough to resolve the strengthened offshore winds through the complex terrain, and subsequently, they may not well capture the effects of Santa Ana winds on fires. As shown in Fig. S8, the wind speeds from NARR are significantly larger than from CRUNCEP for the strong wind days (daily wind speed > 4.5 m/s) over southwestern California (116-119 ºW, 32.6-34.8 ºN) during 2000-2012 October as well as the during Oct 2003 and 2007 (Table S3). The results indicate the lower wind speeds in the CRUNCEP atmospheric forcing used in FireMIP may partially explain the model biases for the events associated with Santa Ana winds. Besides the above-mentioned shortfall, all the models have problems reproducing the interannual variability of the fire emissions over Mediterranean California, with very low correlations (r<0.25) for the FireMIP models and a relatively low correlation (r=0.72) for the ML model (Table 4; Fig. 7d). The poor performance for this region may be due to the complex relations between fires and multiple factors, including meteorology, complex terrain, fuel, and human, which may not be fully represented in the models (Mann et al., 2016; Radeloff et al., 2018).

446   Both the ML model and LPJ-SIM successfully reproduce the seasonality of fire emission in southwestern
447 US peaking in June (r=0.99 and 0.94 for ML and LPJ-SIM, respectively), while other models simulate relatively
448 smooth seasonality (Fig. 7e and Table 4). The ML model, LPJ-SIM, and ORCHIDEE have better performance for
449 the interannual variability, with correlation coefficients of 0.95, 0.40, and 0.45, respectively (Table 4). However,
450 most FireMIP models show larger variability in fire emissions than the GFED, and they all fail to capture the
451 extremely large fire emission in 2011 (Fig. 7f). The peak fire emission in 2011 over southwestern US was caused
452 by extremely low atmospheric moisture along with moderately high temperature, leading to record-breaking VPD
453 and wildfire activities (Williams et al., 2015). To explain why the FireMIP models fail to capture the peak of 2011,
454 we compare the VPD calculated from CRUNCEP data and the VPD data from gridMET used in the ML model. As
455 Fig. S9 shows, CRUNCEP shows smaller positive anomalies of VPD over southwestern US in 2011 summer, while
456 gridMET data demonstrates a significantly larger VPD anomaly. The biases in CRUNCEP data may partially
457 explain the underestimations in all FireMIP models.

458   For southeastern US, the seasonal cycle of fire $PM_{2.5}$ emissions displays a bimodal pattern, peaking in
459 spring (March-April) and fall (September and October) (Fig. 7g). Most models fail to reproduce the bimodal fire
460 emissions, but the ML model, LPJ-SIM, and LPJ-SPI can capture the bimodal pattern. Although LPJ-SIM and LPJ-
461 SPI predict the bimodal peaks, the first peak simulated by LPJ-SIM shows a one-month delay, and the second peak
462 simulated by LPJ-SIM and LPJ-SPI is one month early and one month late, respectively (Fig. 7g). In addition, the
463 ML model, CLM, and JSBACH reproduce the interannual variability of fire $PM_{2.5}$ emissions relatively well (r=0.96,
464 0.57, and 0.72 for the ML model, CLM, and JSBACH, respectively) (Table 4 and Fig. 7h). Interestingly, CLM and
465 JSBACH can capture several peaks in 2007, 2010, and 2011 but they do not simulate seasonality correctly, which
466 may be explained by the underestimation in spring compensated by the overestimations in summer related to
467 abnormal dryness or drought.

4.3 Performance in modeling extreme events

469   Fire activity in the US is becoming more hazardous, particularly over western US, due to more frequent
470 hotter and drier conditions as climate continues to warm (Williams et al., 2019). Thus, it is necessary to assess
471 whether the ML model and process-based models can capture the extreme events in terms of their magnitude,
472 frequency, timing, and location, which is essential to future projection and adaptation. As CLM performs relatively
473 well among the FireMIP models, we select CLM for comparison with the ML model at 1º × 1º resolution, focusing
474 on the spatial patterns of extreme event frequency and two case studies with extremely large fire emissions.

4.3.1 Frequency of extreme event occurrence

476   Fig. 9 shows the frequency maps of months with large fire emissions during 2000-2012 for GFED, the ML
477 model, and CLM. Large fire emission is defined as monthly fire $PM_{2.5}$ emissions greater than the 95th percentile of
478 fire $PM_{2.5}$ emission considering all the grids over CONUS in 2000-2012. GFED shows hot spots with a higher
479 frequency over northern California, the Pacific Northwest, and southeastern US, with total counts ranging from 15
480 to 105 (Fig. 9a). The ML model captures the spatial patterns (r=0.74), but it overestimates the number of months
481 by a factor of two to three compared to GFED, especially over western US (Fig. 9b). The spatial patterns of large
482 fire emission occurrence simulated by CLM are generally consistent with the observed distribution by GFED
483 (r=0.35). However, it overestimates the frequency, particularly over Idaho and northeastern US, and simulates more
484 significant numbers of months with extreme events over large spatial extents, may be due to its coarse spatial
485 resolution (Fig. 9c).

4.3.2 Case studies

To evaluate how well the models simulate the large fire emissions, we compare model performance for the two recent cases reported to be the largest fire events during 2000-2012, including the fires in southern US in 2011 and western US in 2012. During 2011, a severe drought leading to large wildfires was observed over southern US, including Arizona, New Mexico, and Texas (NOAA, 2012; Wang et al., 2015). Fig. 10 shows the maps of annual mean fire $PM_{2.5}$ emissions over southern US from GFED, the ML model, and CLM. GFED shows the largest fire emissions close to the border of Arizona and New Mexico in conjunction with other small hotspots over New Mexico, Texas, and Louisiana (Fig. 10a). The ML model overall reproduces the spatial distributions of the fire emissions (r=0.97) and captures the largest fire emission in Arizona and New Mexico in 2011 (Fig. 10b). However, CLM does not capture the hotspots observed in GFED over Arizona and New Mexico but simulates larger fire emissions in Louisiana instead (Fig. 10c). In terms of the time series, the ML model reproduces the temporal variability of fire emissions and successfully captures the peak of total fire $PM_{2.5}$ emissions in June 2011 (r=0.98; Figs. 10d and 10e). Although CLM simulates the peak in June, it overestimates fire emissions in the following months by a factor of 4 (r=0.52; Figs. 10d and 10e).

In 2012, western US experienced several major wildfires (NOAA, 2013). The warm and dry conditions led to large wildfires in California, Oregon, New Mexico, and Colorado (Fig. 11). Both the ML model and CLM capture the hotspots with large fire emissions (Fig. 11b and 11c) and have correlation coefficients of 0.90 and 0.37, respectively. However, the ML model tends to overestimate fire emissions, especially in areas surrounding the grids with extremely large fire emissions (Fig. 11b). CLM misses some large fire emissions in Colorado and New Mexico and underestimates the larger fire emissions in several hotspots (Fig. 11a), which may be explained by its coarse resolution. The time series of normalized fire $PM_{2.5}$ emissions in 2012 show one peak in August. The ML model captures the peak and presents a high correlation between the simulated and observed normalized and total fire $PM_{2.5}$ emissions (r=0.98). CLM captures the peak in August but overestimates emissions in September and October (r=0.84; Figs. 11d and 11e). To test model generalization, we train the model using data of 2000-2009 and 2013-2020 and test on 2010-2012 and compare the ML performance with CLM (Figs. S10-11). The ML model performance is as good as the 10-fold cross-validation, demonstrating that the ML model performs well on predicting unseen data.

5. Discussion and conclusions

This study provides the first assessment to evaluate the performance of data-driven and process-based models in predicting fire $PM_{2.5}$ emissions over CONUS. We first demonstrate that the developed ML model performs well in predicting monthly fire $PM_{2.5}$ emissions nationwide at grid cells of 0.25º × 0.25 º resolution from 2000 to 2020, with an RMSE of 0.16 g/m^2 and IoA of 0.84. The ML model outperforms prior statistical models predicting fire activities at similar spatial and temporal scales (Carvalho et al., 2008; Bedia et al., 2014). Considering the performance at a regional scale, the ML model reproduces the interannual variability of fire emissions for the selected regions, with correlation coefficients ranging from 0.84 to 0.98. Therefore, the ML model has a promising performance in predicting fire emission over CONUS at a relatively fine spatial resolution. Compared to the wildfire burned area model in Wang et al. (2021), the fire emission model in this study shows slight degradations in capturing the interannual variability of fire emission at grid level (e.g., percentage of grids with correlations larger than 0.4). This may be explained by the fact that the fire emission model may not effectively resolve the relationships between fires and predictors when more grids with less fire occurrence are included (i.e., more zeros or unburned grids) without reliable information about ignition. As a side note, both burned area and emission ML models have relatively poor performance over Mediterranean California, indicating the challenges in

528 modeling fire activities in this region where the terrain and land use are complex. The SHAP variable importance
529 shows that meteorology at both local and synoptic scale as well as fuel loads are important variables controlling
530 fire emissions over CONUS. Regional analysis of predictors indicates that fuel dryness such as fuel moisture and
531 energy release component (ERC) and fuel load are important for predicting fire emissions in western US, while
532 large-scale meteorological patterns (SVDs_SElag2) contribute more to fire emissions in southeastern US.
533   We then compare the simulated fire $PM_{2.5}$ emissions from the ML model and FireMIP models against
534 GFED from 2000 to 2012 at the spatial resolution of $1^\circ \times 1^\circ$. The ML model, CLM, and JULES reproduce the
535 spatial distribution more reasonably than the rest of the FireMIP models (r=0.83, 0.52, and 0.40 for the ML, CLM,
536 and JULES, respectively). Both CLM and JULES simulate more fire $PM_{2.5}$ emissions over southeastern US, which
537 can be explained by several reasons. First, it has been shown that the satellite-observed burned areas in southeastern
538 US are much smaller than the burned areas estimated from the ground-based fire records, which might have resulted
539 from the small prescribed and agricultural fires (Hu et al., 2016; Nowell et al., 2018). In addition, large differences
540 exist among different satellite estimated fire $PM_{2.5}$ emissions in southeastern US (Li et al., 2019). As a consequence,
541 these studies highlighted uncertainties about the GFED estimated burned area and emission over southeastern US.
542 Second, cropland fires are one of the predominant fire types in this region. Among the FireMIP models, CLM is
543 the only model that simulates cropland fires (Li et al., 2013). For JULES, even though it does not simulate cropland
544 fires, it treats croplands as natural grasslands. The emission factors of grasslands and croplands used in the FireMIP
545 models are larger than in GFED4s, thereby causing larger fire $PM_{2.5}$ emissions in southeastern US in CLM and
546 JULES (van der Werf et al., 2017; Li et al., 2019). Furthermore, Li et al. (2019) noted that CLM4.5 simulates
547 higher fuel loads in croplands than the CASA model used by GFED4s, leading to higher fire carbon emissions
548 estimated by CLM than by GFED. It is worth noting that the ML model incorporates fuel load simulated by CLM4.5
549 but it predicts fire emissions closer to GFED4s, indicating a smaller sensitivity of fire emission to fuel load in the
550 ML model. Lastly, the overestimation of fire $PM_{2.5}$ emissions can also be explained by the sensitivity to
551 meteorology. The spatial distributions of the long-term mean fire emissions shown in Fig. 3 correlate with the
552 spatial distributions of sensitivities to RH and/or temperature, with regional differences. For western US, large fire
553 emissions are associated with stronger sensitivities to both RH and temperature in the ML and most FireMIP
554 models. For central and southeastern US, overestimation of fire $PM_{2.5}$ emissions only corresponds to stronger
555 sensitivity to temperature in some FireMIP models.
556   Besides comparing model performance aggregated over CONUS, we analyze the model performance for
557 several regions, including the western forest area, Mediterranean California, southwestern US, and southeastern
558 US. For the western forest area, the ML model performs well in capturing both seasonality and interannual
559 variability of fire $PM_{2.5}$ emissions, with correlation coefficients of 0.98 and 0.96, respectively. In contrast, the
560 FireMIP models generally reproduce the seasonality well but do not simulate the interannual variability well,
561 especially underestimating the peak in 2007, which related to large-scale meteorological patterns favorable for fires
562 in Pacific Northwest (Zhong et al., 2020). For Mediterranean California, all FireMIP models only capture the first
563 peak in August but fail to simulate the second peak in October, which is caused by large fires related to Santa Ana
564 winds in 2003 and 2007. Such lack of peak emission is also shown in the interannual variability, as all FireMIP
565 models show limited ability to simulate the peaks in these two years. By contrast, the ML model successfully
566 predicts the bimodal seasonality and the large fire emissions related to the Santa Ana winds in 2003 and 2007. The
567 underestimation of the peak in the FireMIP models may be attributed to the underrepresentation of the effects of
568 large-scale meteorology in the two regions, as the ML model and SHAP importance show that SVD predictors
569 have larger contributions to the fire emissions in both events. The results of the two regions in the western US
570 suggest that fire parameterization in the FireMIP models could be improved by including the effects of regional
571 and large-scale meteorology (e.g., Santa Ana winds) on fire activity (Yue et al., 2014). Modeling the effect of Santa
572 Ana winds on wildfires may be particularly challenging as the offshore Santa Ana winds exhibit variability related

573 to both synoptic scale pressure anomaly over the Great Basin and local thermodynamic forcing associated with
574 strong desert-ocean temperature gradient (Hughes and Hall, 2010).
575   As for southwestern US, the ML model and LPJ-SIM estimate the peak in June (r=0.99 and 0.94 for ML
576 and LPJ-SIM, respectively), which highly agrees with the GFED observation. Interestingly, most FireMIP models
577 fail to capture the extremely large fire emission in the 2011 summer mainly due to the low biases of VPD anomalies
578 in CRUNCEP (Tang et a., 2017). Unlike southwestern US, the seasonality of southeastern US has peaks in March-
579 April and September-October. The two peaks of fire emissions correspond to wildfires (Mar-Apr and Sep),
580 cropland fires (Feb-Mar and Aug-Oct), and prescribed fires (Feb-Apr and Oct) that include burnings for pest
581 controls and land cleaning (Knapp et al., 2009; Lin et al., 2014). Most models fail to reproduce the bimodal fire
582 emissions, but the ML model, LPJ-SIM, and LPJ-SPI can capture the bimodal pattern. Even though the seasonality
583 of fires over this region is not simulated accurately, the CLM and JSBACH well reproduce the interannual
584 variability of fire $PM_{2.5}$ emissions and predict the peaks. The FireMIP models' shortfall in reproducing the bimodal
585 seasonality can be explained by two reasons. First, the relationships between human and fire spread implemented
586 in the process-based models may not be realistic compared to the observed relationships. Parisien et al. (2016)
587 demonstrated the large spatial variability of human impacts on burned areas in North America, which is not well
588 represented in the FireMIP models (Li et al., 2019). Second, drier conditions in winter would promote fires in
589 springtime (Wear and Greis, 2013; Wang et al., 2021), which may not be directly considered in the FireMIP models
590 but are incorporated as SVD predictors in the ML model. Overall, the representations of the effects of human and
591 large-scale meteorology on fires may explain why the models simulate the seasonality incorrectly in southeastern
592 US. In addition to the comparison of general model performance, we also compare the ability of the data-driven
593 and processed-based models in predicting extremely large fire emissions. Both ML and CLM models reproduce
594 the spatial pattern of extreme fire events and reasonably simulate the historical events of large fires in southwestern
595 and western US.
596   It is known that different fire emission inventories have their uncertainties and prior studies have compared
597 fire emission inventories over the globe or CONUS (Urbanski et al., 2018; Liu et al., 2020). The GFED fire
598 emissions used in this study are known to underestimate the fire emission peak in springtime over the southeastern
599 US, which may be explained by the fact that other products such as FINN or QFED capture more small fire activity
600 compared to the GFED approach (Koplitz et al., 2018; Carter et al., 2020). Although FINN can capture more small
601 fires, it underestimates the intensity of large fires for some cases, which has been attributed to the cloud coverage
602 on daily scale detection (Paton-Walsh et al., 2012). QFED and GFAS, which estimate emissions using fire radiative
603 power (FRP) from satellites, are also more sensitive to small fires than GFED. However, QFED tends to estimate
604 much larger emissions than other products, which can be explained by the fact that the emission coefficients used
605 to obtain emissions are constrained by MODIS AOD and the uncertainties within FRP (Pan et al., 2020). Despite
606 the known discrepancy between GFED and other data products, the GFED data still shows bimodal peaks in spring
607 and fall over the southeastern US, while most FireMIP models fail to reproduce the first peak (Fig. 7g in the
608 manuscript). For the western US, GFED and FINN are generally consistent regarding the magnitude and variability
609 of fire emissions (Urbanski et al., 2018). As stated above, different fire emission inventories have uncertainties.
610 Future works are required to include other fire emission datasets for model evaluation.
611   To summarize, we utilize the ML model with SHAP importance to diagnose the fire emissions simulated
612 by process-based models and attributed model biases to several factors. First, the sensitivies of fire emissions to
613 meteorology in the models are stronger than the observed, leading to overestimations. Second, the large-scale
614 meteorological patterns conducive to fires are not fully considered in the process-based models, which are
615 important contributors of large fire emissions in western US and southeastern US. Third, the spatial resolutions of
616 models and/or the atmospheric forcing they used may be too coarse to resolve the effects of regional weather
617 phenomenon such as Santa Ana winds. Fourth, biases in the atmospheric forcing data may result in biases of fire
618 emission predictions. Last but not least, human activities are a critical component shaping fire regimes but the

human effects on fire activities in the FireMIP models may not reflect the human-fire relationships in the real-world. This is also an issue in the ML model as the human-related predictors in the ML model may be too simple to represent the human influences. The underrepresentation of human effects in both types of models may cause additional uncertainties in projecting future fire activities and their impacts on climate. By training the ML model using the GFED emissions, the ML model is able to better explain fire emissions in the US, which makes it a useful tool for diagnosing processes or relationships that may be missing or not well represented in the process-based models to guide future development for improving their performance. Besides its use in diagnosing process-based models, the ML model with SHAP provides a different and novel approach to simulate fire emissions more accurately and identify the important predictor variables. While the ML model generally has higher accuracy than the FireMIP models, the feedbacks between fire emissions and climate are not included, which could potentially affect the reliability of ML-based models in fire emission prediction under future climate change scenario (Zou et al., 2020). Lastly, due to limited training data, the ML model cannot predict fires in regions with longer fire return intervals, posing additional uncertainties in their use for making future projections.

Code availability. Model code is available upon request to the first author.

Data availability. The ML prediction and predictor dataset used in this study are publicly accessible online at https://zenodo.org/record/5076646#.YOZI4zZKjOQ.

Author contributions. SW, YQ, RL conceived the research ideas. SW wrote the initial draft of the paper, performed analyses, and model development. All authors contributed to the interpretation of the results and the preparation of the manuscript.

Acknowledgements.
This research was performed at PNNL and funded under Assistance Agreement No. RD835871 by the U.S. Environmental Protection Agency to Yale University through the SEARCH (Solutions for Energy, AiR, Climate, and Health) Center. It has not been formally reviewed by EPA. The views expressed in this document are solely those of the SEARCH Center and do not necessarily reflect those of the Agency. EPA does not endorse any products or commercial services mentioned in this publication.

References

Akagi, S. K., Yokelson, R. J., Wiedinmyer, C., Alvarado, M. J., Reid, J. S., Karl, T., Crounse, J. D., and Wennberg, P. O.: Emission factors for open and domestic biomass burning for use in atmospheric models, 11, 4039–4072, https://doi.org/10.5194/acp-11-4039-2011, 2011.

Abatzoglou, J. T. and Kolden, C. A.: Relationships between climate and macroscale area burned in the western United States, Int. J. Wildland Fire, 22, 1003–1020, https://doi.org/10.1071/WF13019, 2013.

Abatzoglou, J. T. and Williams, A. P.: Impact of anthropogenic climate change on wildfire across western US forests, PNAS, 113, 11770–11775, https://doi.org/10.1073/pnas.1607171113, 2016.

Abatzoglou, J. T., Kolden, C. A., Balch, J. K., and Bradley, B. A.: Controls on interannual variability in lightning-caused fire activity in the western US, Environ. Res. Lett., 11, 045005, https://doi.org/10.1088/1748-9326/11/4/045005, 2016.

Aldersley, A., Murray, S. J., and Cornell, S. E.: Global and regional analysis of climate and human drivers of wildfire, Science of The Total Environment, 409, 3472–3481, https://doi.org/10.1016/j.scitotenv.2011.05.032, 2011.

Arrieta, A. B., Díaz-Rodríguez, N., Del Ser, J., Bennetot, A., Tabik, S., Barbado, A., Garcia, S., Gil-Lopez, S., Molina, D., Benjamins, R., Chatila, R., and Herrera, F.: Explainable Artificial Intelligence (XAI): Concepts, taxonomies, opportunities and challenges toward responsible AI, Information Fusion, 58, 82–115, https://doi.org/10.1016/j.inffus.2019.12.012, 2020.

Balch, J. K., Bradley, B. A., Abatzoglou, J. T., Nagy, R. C., Fusco, E. J., and Mahood, A. L.: Human-started wildfires expand the fire niche across the United States, PNAS, 114, 2946–2951, https://doi.org/10.1073/pnas.1617394114, 2017.

Bartier, P. M. and Keller, C. P.: Multivariate interpolation to incorporate thematic surface data using inverse distance weighting (IDW), Computers & Geosciences, 22, 795–799, https://doi.org/10.1016/0098-3004(96)00021-0, 1996.

Bedia, J., Herrera, S., and Gutiérrez, J. M.: Assessing the predictability of fire occurrence and area burned across phytoclimatic regions in Spain, 14, 53–66, https://doi.org/10.5194/nhess-14-53-2014, 2014.

Birch, D. S., Morgan, P., Kolden, C. A., Abatzoglou, J. T., Dillon, G. K., Hudak, A. T., and Smith, A. M. S.: Vegetation, topography and daily weather influenced burn severity in central Idaho and western Montana forests, 6, art17, https://doi.org/10.1890/ES14-00213.1, 2015.

Brey, S. J., Barnes, E. A., Pierce, J. R., Wiedinmyer, C., and Fischer, E. V.: Environmental Conditions, Ignition Type, and Air Quality Impacts of Wildfires in the Southeastern and Western United States, 6, 1442–1456, https://doi.org/10.1029/2018EF000972, 2018.

Carter, T. S., Heald, C. L., Jimenez, J. L., Campuzano-Jost, P., Kondo, Y., Moteki, N., Schwarz, J. P., Wiedinmyer, C., Darmenov, A. S., da Silva, A. M., and Kaiser, J. W.: How emissions uncertainty influences the distribution and radiative impacts of smoke from fires in North America, 20, 2073–2097, https://doi.org/10.5194/acp-20-2073-2020, 2020.

Carvalho, A., Flannigan, M. D., Logan, K., Miranda, A. I., and Borrego, C.: Fire activity in Portugal and its relationship to weather and the Canadian Fire Weather Index System, 17, 328–338, https://doi.org/10.1071/WF07014, 2008.

Center For International Earth Science Information Network-CIESIN-Columbia University: Gridded Population of the World, Version 4 (GPWv4): Population Density, Revision 11, https://doi.org/10.7927/H49C6VHW, 2017.

Chen, T. and Guestrin, C.: XGBoost: A Scalable Tree Boosting System, in: Proceedings of the 22nd ACM SIGKDD International Conference on Knowledge Discovery and Data Mining, New York, NY, USA, 785–794, https://doi.org/10.1145/2939672.2939785, 2016.

Coffield, S. R., Graff, C. A., Chen, Y., Smyth, P., Foufoula-Georgiou, E., and Randerson, J. T.: Machine learning to predict final fire size at the time of ignition, 28, 861–873, 2019.

Cortez, P. and Morais, A.: A Data Mining Approach to Predict Forest Fires using Meteorological Data, Proceedings of the 13th Portuguese Conference on Artificial Intelligence, Portugal, 512–523, 2007.

Crevoisier, C., Shevliakova, E., Gloor, M., Wirth, C., and Pacala, S.: Drivers of fire in the boreal forests: Data constrained design of a prognostic model of burned area for use in dynamic global vegetation models, 112, https://doi.org/10.1029/2006JD008372, 2007.

Crimmins, M. A.: Synoptic climatology of extreme fire-weather conditions across the southwest United States, 26, 1001–1016, https://doi.org/10.1002/joc.1300, 2006.

Cummins, K. L. and Murphy, M. J.: An Overview of Lightning Locating Systems: History, Techniques, and Data Uses, With an In-Depth Look at the U.S. NLDN, 51, 499–518, https://doi.org/10.1109/TEMC.2009.2023450, 2009.

Dillon, G. K., Holden, Z. A., Morgan, P., Crimmins, M. A., Heyerdahl, E. K., and Luce, C. H.: Both topography and climate affected forest and woodland burn severity in two regions of the western US, 1984 to 2006, 2, art130, https://doi.org/10.1890/ES11-00271.1, 2011.

Dong, L., Leung, L. R., Qian, Y., Zou, Y., Song, F., and Chen, X.: Meteorological Environments Associated With California Wildfires and Their Potential Roles in Wildfire Changes During 1984–2017, 126, e2020JD033180, https://doi.org/10.1029/2020JD033180, 2021.

Ford, B., Martin, M. V., Zelasky, S. E., Fischer, E. V., Anenberg, S. C., Heald, C. L., and Pierce, J. R.: Future Fire Impacts on Smoke Concentrations, Visibility, and Health in the Contiguous United States, 2, 229–247, https://doi.org/10.1029/2018GH000144, 2018.

Forkel, M., Andela, N., Harrison, S. P., Lasslop, G., van Marle, M., Chuvieco, E., Dorigo, W., Forrest, M., Hantson, S., Heil, A., Li, F., Melton, J., Sitch, S., Yue, C., and Arneth, A.: Emergent relationships with respect to burned area in global satellite observations and fire-enabled vegetation models, 16, 57–76, https://doi.org/10.5194/bg-16-57-2019, 2019.

Friedl, M. and Sulla-Menashe, D.: MCD12C1 MODIS/Terra+Aqua Land Cover Type Yearly L3 Global 0.05Deg CMG V006, https://doi.org/10.5067/MODIS/MCD12C1.006, 2015.

Giglio, L., Randerson, J. T., and Werf, G. R. van der: Analysis of daily, monthly, and annual burned area using the fourth-generation global fire emissions database (GFED4), 118, 317–328, https://doi.org/10.1002/jgrg.20042, 2013.

Gunning, D.: Explainable artificial intelligence (xAI), Defense Advanced Research Projects Agency (DARPA), 2017.

Hantson, S., Kelley, D. I., Arneth, A., Harrison, S. P., Archibald, S., Bachelet, D., Forrest, M., Hickler, T., Lasslop, G., Li, F., Mangeon, S., Melton, J. R., Nieradzik, L., Rabin, S. S., Prentice, I. C., Sheehan, T., Sitch, S., Teckentrup, L., Voulgarakis, A., and Yue, C.: Quantitative assessment of fire and vegetation properties in simulations with fire-enabled vegetation models from the Fire Model Intercomparison Project, 13, 3299–3318, https://doi.org/10.5194/gmd-13-3299-2020, 2020.

Holden, Z. A., Swanson, A., Luce, C. H., Jolly, W. M., Maneta, M., Oyler, J. W., Warren, D. A., Parsons, R., and Affleck, D.: Decreasing fire season precipitation increased recent western US forest wildfire activity, PNAS, 115, E8349–E8357, https://doi.org/10.1073/pnas.1802316115, 2018.

Hooker, G.: Diagnostics and Extrapolation in Machine Learning, Stanford University, 2004.

Hu, X., Yu, C., Tian, D., Ruminski, M., Robertson, K., Waller, L. A., and Liu, Y.: Comparison of the Hazard Mapping System (HMS) fire product to ground-based fire records in Georgia, USA, 121, 2901–2910, https://doi.org/10.1002/2015JD024448, 2016.

Hughes, M. and Hall, A.: Local and synoptic mechanisms causing Southern California's Santa Ana winds, Clim Dyn, 34, 847–857, https://doi.org/10.1007/s00382-009-0650-4, 2010.

Hurtt, G. C., Chini, L. P., Frolking, S., Betts, R. A., Feddema, J., Fischer, G., Fisk, J. P., Hibbard, K., Houghton, R. A., Janetos, A., Jones, C. D., Kindermann, G., Kinoshita, T., Klein Goldewijk, K., Riahi, K., Shevliakova, E., Smith, S., Stehfest, E., Thomson, A., Thornton, P., van Vuuren, D. P., and Wang, Y. P.: Harmonization of land-use scenarios for the period 1500–2100: 600 years of global gridded annual land-use transitions, wood harvest, and resulting secondary lands, Climatic Change, 109, 117, https://doi.org/10.1007/s10584-011-0153-2, 2011.

Johnston, F. H., Henderson, S. B., Chen, Y., Randerson, J. T., Marlier, M., Defries, R. S., Kinney, P., Bowman, D. M. J. S., and Brauer, M.: Estimated global mortality attributable to smoke from landscape fires, Environ Health Perspect, 120, 695–701, https://doi.org/10.1289/ehp.1104422, 2012.

Kane, V. R., Cansler, C. A., Povak, N. A., Kane, J. T., McGaughey, R. J., Lutz, J. A., Churchill, D. J., and North, M. P.: Mixed severity fire effects within the Rim fire: Relative importance of local climate, fire weather, topography, and forest structure, Forest Ecology and Management, 358, 62–79, https://doi.org/10.1016/j.foreco.2015.09.001, 2015.

Kaulfus, A. S., Nair, U., Jaffe, D., Christopher, S. A., and Goodrick, S.: Biomass Burning Smoke Climatology of the United States: Implications for Particulate Matter Air Quality, Environ. Sci. Technol., 51, 11731–11741, https://doi.org/10.1021/acs.est.7b03292, 2017.

Keane, R. E., Reinhardt, E. D., Scott, J., Gray, K., and Reardon, J.: Estimating forest canopy bulk density using six indirect methods, 724–739, 2005.

Keeley, J. E., Safford, H., Fotheringham, C. J., Franklin, J., and Moritz, M.: The 2007 Southern California Wildfires: Lessons in Complexity, Journal of Forestry, 107, 287–296, https://doi.org/10.1093/jof/107.6.287, 2009.

Klein Goldewijk, K., Beusen, A., and Janssen, P.: Long-term dynamic modeling of global population and built-up area in a spatially explicit way: HYDE 3.1, The Holocene, 20, 565–573, https://doi.org/10.1177/0959683609356587, 2010.

Kloster, S., Mahowald, N. M., Randerson, J. T., Thornton, P. E., Hoffman, F. M., Levis, S., Lawrence, P. J., Feddema, J. J., Oleson, K. W., and Lawrence, D. M.: Fire dynamics during the 20th century simulated by the Community Land Model, 7, 1877–1902, https://doi.org/10.5194/bg-7-1877-2010, 2010.

Knorr, W., Jiang, L., and Arneth, A.: Climate, CO_2 and human population impacts on global wildfire emissions, 13, 267–282, https://doi.org/10.5194/bg-13-267-2016, 2016.

Koplitz, S. N., Nolte, C. G., Pouliot, G. A., Vukovich, J. M., and Beidler, J.: Influence of uncertainties in burned area estimates on modeled wildland fire PM2.5 and ozone pollution in the contiguous U.S., Atmos Environ (1994), 191, 328–339, https://doi.org/10.1016/j.atmosenv.2018.08.020, 2018.

Kummu, M., Taka, M., and Guillaume, J. H. A.: Gridded global datasets for Gross Domestic Product and Human Development Index over 1990–2015, Sci Data, 5, 180004, https://doi.org/10.1038/sdata.2018.4, 2018.

Lasslop, G. and Kloster, S.: Impact of fuel variability on wildfire emission estimates, Atmospheric Environment, 121, 93–102, https://doi.org/10.1016/j.atmosenv.2015.05.040, 2015.

Lawrence, D. M., Fisher, R. A., Koven, C. D., Oleson, K. W., Swenson, S. C., Bonan, G., Collier, N., Ghimire, B., Kampenhout, L. van, Kennedy, D., Kluzek, E., Lawrence, P. J., Li, F., Li, H., Lombardozzi, D., Riley, W. J., Sacks, W. J., Shi, M., Vertenstein, M., Wieder, W. R., Xu, C., Ali, A. A., Badger, A. M., Bisht, G., Broeke, M. van den, Brunke, M. A., Burns, S. P., Buzan, J., Clark, M., Craig, A., Dahlin, K., Drewniak, B., Fisher, J. B., Flanner, M., Fox, A. M., Gentine, P., Hoffman, F., Keppel-Aleks, G., Knox, R., Kumar, S., Lenaerts, J., Leung, L. R., Lipscomb, W. H., Lu, Y., Pandey, A., Pelletier, J. D., Perket, J., Randerson, J. T., Ricciuto, D. M., Sanderson, B. M., Slater, A., Subin, Z. M., Tang, J., Thomas, R. Q., Martin, M. V., and Zeng, X.: The Community Land Model Version 5: Description of New Features, Benchmarking, and Impact of Forcing Uncertainty, 11, 4245–4287, https://doi.org/10.1029/2018MS001583, 2019.

Le Quéré, C., Peters, G. P., Andres, R. J., Andrew, R. M., Boden, T. A., Ciais, P., Friedlingstein, P., Houghton, R. A., Marland, G., Moriarty, R., Sitch, S., Tans, P., Arneth, A., Arvanitis, A., Bakker, D. C. E., Bopp, L., Canadell, J. G., Chini, L. P., Doney, S. C., Harper, A., Harris, I., House, J. I., Jain, A. K., Jones, S. D., Kato, E., Keeling, R. F., Klein Goldewijk, K., Körtzinger,

770   A., Koven, C., Lefèvre, N., Maignan, F., Omar, A., Ono, T., Park, G.-H., Pfeil, B., Poulter, B., Raupach, M. R., Regnier, P.,
771   Rödenbeck, C., Saito, S., Schwinger, J., Segschneider, J., Stocker, B. D., Takahashi, T., Tilbrook, B., van Heuven, S., Viovy,
772   N., Wanninkhof, R., Wiltshire, A., and Zaehle, S.: Global carbon budget 2013, 6, 235–263, https://doi.org/10.5194/essd-6-
773   235-2014, 2014.

774   Li, F., Levis, S., and Ward, D. S.: Quantifying the role of fire in the Earth system – Part 1: Improved global fire modeling
775   in the Community Earth System Model (CESM1), 10, 2293–2314, https://doi.org/10.5194/bg-10-2293-2013, 2013.

776   Li, F., Val Martin, M., Andreae, M. O., Arneth, A., Hantson, S., Kaiser, J. W., Lasslop, G., Yue, C., Bachelet, D., Forrest, M.,
777   Kluzek, E., Liu, X., Mangeon, S., Melton, J. R., Ward, D. S., Darmenov, A., Hickler, T., Ichoku, C., Magi, B. I., Sitch, S., van
778   der Werf, G. R., Wiedinmyer, C., and Rabin, S. S.: Historical (1700–2012) global multi-model estimates of the fire emissions
779   from the Fire Modeling Intercomparison Project (FireMIP), 19, 12545–12567, https://doi.org/10.5194/acp-19-12545-2019,
780   2019.

781   Littell, J. S., McKenzie, D., Peterson, D. L., and Westerling, A. L.: Climate and wildfire area burned in western U.S.
782   ecoprovinces, 1916-2003, 19, 1003–1021, 2009.

783   Liu, J. C., Mickley, L. J., Sulprizio, M. P., Dominici, F., Yue, X., Ebisu, K., Anderson, G. B., Khan, R. F. A., Bravo, M. A.,
784   and Bell, M. L.: Particulate Air Pollution from Wildfires in the Western US under Climate Change, Clim Change, 138, 655–
785   666, https://doi.org/10.1007/s10584-016-1762-6, 2016.

786   Liu, T., Mickley, L. J., Marlier, M. E., DeFries, R. S., Khan, M. F., Latif, M. T., and Karambelas, A.: Diagnosing spatial biases
787   and uncertainties in global fire emissions inventories: Indonesia as regional case study, Remote Sensing of Environment, 237,
788   111557, https://doi.org/10.1016/j.rse.2019.111557, 2020.

789   Liu, Y., Zhang, K., Qian, Y., Wang, Y., Zou, Y., Song, Y., Wan, H., Liu, X., and Yang, X.-Q.: Investigation of short-term
790   effective radiative forcing of fire aerosols over North America using nudged hindcast ensembles, 18, 31–47,
791   https://doi.org/10.5194/acp-18-31-2018, 2018.

792   Liu, Z. and Wimberly, M. C.: Climatic and Landscape Influences on Fire Regimes from 1984 to 2010 in the Western United
793   States, PLOS ONE, 10, e0140839, https://doi.org/10.1371/journal.pone.0140839, 2015.

794   Lundberg, S. and Lee, S.: A Unified Approach to Interpreting Model Predictions, Neural Information Processing Systems
795   (NIPS 2017), Long Beach, CA, USA, 2017.

796   Lundberg, S. M., Erion, G. G., and Lee, S.-I.: Consistent Individualized Feature Attribution for Tree Ensembles, 2019.

797   Mann, M. L., Batllori, E., Moritz, M. A., Waller, E. K., Berck, P., Flint, A. L., Flint, L. E., and Dolfi, E.: Incorporating
798   Anthropogenic Influences into Fire Probability Models: Effects of Human Activity and Climate Change on Fire Activity in
799   California, PLOS ONE, 11, e0153589, https://doi.org/10.1371/journal.pone.0153589, 2016.

800   Mesinger, F., DiMego, G., Kalnay, E., Mitchell, K., Shafran, P. C., Ebisuzaki, W., Jović, D., Woollen, J., Rogers, E., Berbery,
801   E. H., Ek, M. B., Fan, Y., Grumbine, R., Higgins, W., Li, H., Lin, Y., Manikin, G., Parrish, D., and Shi, W.: North American
802   Regional Reanalysis, Bull. Amer. Meteor. Soc., 87, 343–360, https://doi.org/10.1175/BAMS-87-3-343, 2006.

803   Morton, D. C., Collatz, G. J., Wang, D., Randerson, J. T., Giglio, L., and Chen, Y.: Satellite-based assessment of climate
804   controls on US burned area, 10, 247–260, https://doi.org/10.5194/bg-10-247-2013, 2013.

805   Myneni, R., Knyazikhin, Y., and Park, T.: MCD15A2H MODIS/Terra+Aqua Leaf Area Index/FPAR 8-day L4 Global 500m
806   SIN Grid V0006, https://doi.org/10.5067/MODIS/MCD15A2H.006, 2015.

807 NIFC: Total Wildland Fires and Acres (1983-2020), National Interagency Fire Center, 2020.

808 NOAA: Severe Weather Data Inventory (SWDI), https://www1.ncdc.noaa.gov/pub/data/swdi, 2006.

809 NOAA: State of the Climate: Wildfires for Annual 2011, National Centers for Environmental Information, 2012.

810 NOAA: State of the Climate: Wildfires for Annual 2012, National Centers for Environmental Information, 2013.

811 Nowell, H. K., Holmes, C. D., Robertson, K., Teske, C., and Hiers, J. K.: A New Picture of Fire Extent, Variability, and
812 Drought Interaction in Prescribed Fire Landscapes: Insights From Florida Government Records, 45, 7874–7884,
813 https://doi.org/10.1029/2018GL078679, 2018.

814 Pan, X., Ichoku, C., Chin, M., Bian, H., Darmenov, A., Colarco, P., Ellison, L., Kucsera, T., da Silva, A., Wang, J., Oda, T.,
815 and Cui, G.: Six global biomass burning emission datasets: intercomparison and application in one global aerosol model, 20,
816 969–994, https://doi.org/10.5194/acp-20-969-2020, 2020.

817 Parisien, M.-A., Miller, C., Parks, S. A., DeLancey, E. R., Robinne, F.-N., and Flannigan, M. D.: The spatially varying
818 influence of humans on fire probability in North America, Environ. Res. Lett., 11, 075005, https://doi.org/10.1088/1748-
819 9326/11/7/075005, 2016.

820 Parks, S. A., Parisien, M.-A., and Miller, C.: Spatial bottom-up controls on fire likelihood vary across western North America,
821 3, art12, https://doi.org/10.1890/ES11-00298.1, 2012.

822 Paton-Walsh, C., Emmons, L. K., and Wiedinmyer, C.: Australia's Black Saturday fires – Comparison of techniques for
823 estimating emissions from vegetation fires, Atmospheric Environment, 60, 262–270,
824 https://doi.org/10.1016/j.atmosenv.2012.06.066, 2012.

825 Pechony, O. and Shindell, D. T.: Fire parameterization on a global scale, 114, https://doi.org/10.1029/2009JD011927, 2009.

826 Pfeiffer, M., Spessa, A., and Kaplan, J. O.: A model for global biomass burning in preindustrial time: LPJ-LMfire (v1.0), 6,
827 643–685, https://doi.org/10.5194/gmd-6-643-2013, 2013.

828 Pollina, J. B., Colle, B. A., and Charney, J. J.: Climatology and Meteorological Evolution of Major Wildfire Events over the
829 Northeast United States, Wea. Forecasting, 28, 175–193, https://doi.org/10.1175/WAF-D-12-00009.1, 2013.

830 Pyne, S. J.: Introduction to wildland fire. Fire management in the United States., John Wiley & Sons, New York, NY, USA,
831 1984.

832 Rabin, S. S., Melton, J. R., Lasslop, G., Bachelet, D., Forrest, M., Hantson, S., Kaplan, J. O., Li, F., Mangeon, S., Ward, D.
833 S., Yue, C., Arora, V. K., Hickler, T., Kloster, S., Knorr, W., Nieradzik, L., Spessa, A., Folberth, G. A., Sheehan, T.,
834 Voulgarakis, A., Kelley, D. I., Prentice, I. C., Sitch, S., Harrison, S., and Arneth, A.: The Fire Modeling Intercomparison
835 Project (FireMIP), phase 1: experimental and analytical protocols with detailed model descriptions, 10, 1175–1197,
836 https://doi.org/10.5194/gmd-10-1175-2017, 2017.

837 Radeloff, V. C., Helmers, D. P., Kramer, H. A., Mockrin, M. H., Alexandre, P. M., Bar-Massada, A., Butsic, V., Hawbaker,
838 T. J., Martinuzzi, S., Syphard, A. D., and Stewart, S. I.: Rapid growth of the US wildland-urban interface raises wildfire risk,
839 PNAS, 115, 3314–3319, https://doi.org/10.1073/pnas.1718850115, 2018.

840 Randerson, J. T., Chen, Y., Werf, G. R. van der, Rogers, B. M., and Morton, D. C.: Global burned area and biomass burning
841 emissions from small fires, 117, https://doi.org/10.1029/2012JG002128, 2012.

Rap, A., Scott, C. E., Spracklen, D. V., Bellouin, N., Forster, P. M., Carslaw, K. S., Schmidt, A., and Mann, G.: Natural aerosol direct and indirect radiative effects, 40, 3297–3301, https://doi.org/10.1002/grl.50441, 2013.

Seiler, W. and Crutzen, P. J.: Estimates of gross and net fluxes of carbon between the biosphere and the atmosphere from biomass burning, Climatic Change, 2, 207–247, https://doi.org/10.1007/BF00137988, 1980.

Shepard, D.: A two-dimensional interpolation function for irregularly-spaced data, in: Proceedings of the 1968 23rd ACM national conference, New York, NY, USA, 517–524, https://doi.org/10.1145/800186.810616, 1968.

Spracklen, D. V., Mickley, L. J., Logan, J. A., Hudman, R. C., Yevich, R., Flannigan, M. D., and Westerling, A. L.: Impacts of climate change from 2000 to 2050 on wildfire activity and carbonaceous aerosol concentrations in the western United States, 114, https://doi.org/10.1029/2008JD010966, 2009.

Stephens, S. L.: Forest fire causes and extent on United States Forest Service lands, Int. J. Wildland Fire, 14, 213, https://doi.org/10.1071/WF04006, 2005.

Stowell, J. D., Geng, G., Saikawa, E., Chang, H. H., Fu, J., Yang, C.-E., Zhu, Q., Liu, Y., and Strickland, M. J.: Associations of wildfire smoke PM2.5 exposure with cardiorespiratory events in Colorado 2011–2014, Environment International, 133, 105151, https://doi.org/10.1016/j.envint.2019.105151, 2019.

Syphard, A. D., Radeloff, V. C., Keuler, N. S., Taylor, R. S., Hawbaker, T. J., Stewart, S. I., Clayton, M. K., Syphard, A. D., Radeloff, V. C., Keuler, N. S., Taylor, R. S., Hawbaker, T. J., Stewart, S. I., and Clayton, M. K.: Predicting spatial patterns of fire on a southern California landscape, Int. J. Wildland Fire, 17, 602–613, https://doi.org/10.1071/WF07087, 2008.

Thomas, D. S., Butry, D. T., Gilbert, S. W., Webb, D. H., and Fung, J. F.: The Costs and Losses of Wildfires, 2017.

Thonicke, K., Spessa, A., Prentice, I. C., Harrison, S. P., Dong, L., and Carmona-Moreno, C.: The influence of vegetation, fire spread and fire behaviour on biomass burning and trace gas emissions: results from a process-based model, 7, 1991–2011, https://doi.org/10.5194/bg-7-1991-2010, 2010.

Trouet, V., Taylor, A. H., Carleton, A. M., and Skinner, C. N.: Interannual variations in fire weather, fire extent, and synoptic-scale circulation patterns in northern California and Oregon, 95, 349–360, https://doi.org/10.1007/s00704-008-0012-x, 2009.

Tsubaki, M. and Mizoguchi, T.: Quantum Deep Field: Data-Driven Wave Function, Electron Density Generation, and Atomization Energy Prediction and Extrapolation with Machine Learning, Phys. Rev. Lett., 125, 206401, https://doi.org/10.1103/PhysRevLett.125.206401, 2020.

Urbanski, S. P., Reeves, M. C., Corley, R. E., Silverstein, R. P., and Hao, W. M.: Contiguous United States wildland fire emission estimates during 2003–2015, 10, 2241–2274, https://doi.org/10.5194/essd-10-2241-2018, 2018.

Urbieta, I. R., Zavala, G., Bedia, J., Gutiérrez, J. M., Miguel-Ayanz, J. S., Camia, A., Keeley, J. E., and Moreno, J. M.: Fire activity as a function of fire–weather seasonal severity and antecedent climate across spatial scales in southern Europe and Pacific western USA, Environ. Res. Lett., 10, 114013, https://doi.org/10.1088/1748-9326/10/11/114013, 2015.

Vicente-Serrano, S. M., Beguería, S., and López-Moreno, J. I.: A Multiscalar Drought Index Sensitive to Global Warming: The Standardized Precipitation Evapotranspiration Index, 23, 1696–1718, https://doi.org/10.1175/2009JCLI2909.1, 2010.

Wang, S. S.-C. and Wang, Y.: Quantifying the effects of environmental factors on wildfire burned area in the south central US using integrated machine learning techniques, 20, 11065–11087, https://doi.org/10.5194/acp-20-11065-2020, 2020.

877 Wang, S. S.-C., Qian, Y., Leung, L. R., and Zhang, Y.: Identifying Key Drivers of Wildfires in the Contiguous US Using
878 Machine Learning and Game Theory Interpretation, 9, e2020EF001910, https://doi.org/10.1029/2020EF001910, 2021.

879 Wang, S.-C., Wang, Y., Estes, M., Lei, R., Talbot, R., Zhu, L., and Hou, P.: Transport of Central American Fire Emissions to
880 the U.S. Gulf Coast: Climatological Pathways and Impacts on Ozone and PM2.5, 123, 8344–8361,
881 https://doi.org/10.1029/2018JD028684, 2018.

882 Wang, Y., Xie, Y., Cai, L., Dong, W., Zhang, Q., and Zhang, L.: Impact of the 2011 Southern U.S. Drought on Ground-Level
883 Fine Aerosol Concentration in Summertime, 72, 1075–1093, https://doi.org/10.1175/JAS-D-14-0197.1, 2015.

884 Ward, D. S., Kloster, S., Mahowald, N. M., Rogers, B. M., Randerson, J. T., and Hess, P. G.: The changing radiative forcing
885 of fires: global model estimates for past, present and future, 12, 10857–10886, https://doi.org/10.5194/acp-12-10857-2012,
886 2012.

887 Wear, D. N. and Greis, J. G.: The Southern Forest Futures Project: technical report, 178, 1–542, 2013.

888 Wei, Y., Liu, S., Huntzinger, D. N., Michalak, A. M., Viovy, N., Post, W. M., Schwalm, C. R., Schaefer, K., Jacobson, A. R.,
889 Lu, C., Tian, H., Ricciuto, D. M., Cook, R. B., Mao, J., and Shi, X.: The North American Carbon Program Multi-scale Synthesis
890 and Terrestrial Model Intercomparison Project – Part 2: Environmental driver data, 7, 2875–2893,
891 https://doi.org/10.5194/gmd-7-2875-2014, 2014.

892 van der Werf, G. R., Randerson, J. T., Giglio, L., van Leeuwen, T. T., Chen, Y., Rogers, B. M., Mu, M., van Marle, M. J. E.,
893 Morton, D. C., Collatz, G. J., Yokelson, R. J., and Kasibhatla, P. S.: Global fire emissions estimates during 1997–2016, 9,
894 697–720, https://doi.org/10.5194/essd-9-697-2017, 2017.

895 Williams, A. P., Seager, R., Macalady, A. K., Berkelhammer, M., Crimmins, M. A., Swetnam, T. W., Trugman, A. T.,
896 Buenning, N., Noone, D., McDowell, N. G., Hryniw, N., Mora, C. I., and Rahn, T.: Correlations between components of the
897 water balance and burned area reveal new insights for predicting forest fire area in the southwest United States, Int. J. Wildland
898 Fire, 24, 14–26, https://doi.org/10.1071/WF14023, 2015.

899 Williams, A. P., Abatzoglou, J. T., Gershunov, A., Guzman-Morales, J., Bishop, D. A., Balch, J. K., and Lettenmaier, D. P.:
900 Observed Impacts of Anthropogenic Climate Change on Wildfire in California, 7, 892–910,
901 https://doi.org/10.1029/2019EF001210, 2019.

902 Xia, Y., Mitchell, K., Ek, M., Sheffield, J., Cosgrove, B., Wood, E., Luo, L., Alonge, C., Wei, H., Meng, J., Livneh, B.,
903 Lettenmaier, D., Koren, V., Duan, Q., Mo, K., Fan, Y., and Mocko, D.: Continental-scale water and energy flux analysis and
904 validation for the North American Land Data Assimilation System project phase 2 (NLDAS-2): 1. Intercomparison and
905 application of model products, 117, https://doi.org/10.1029/2011JD016048, 2012.

906 Yue, X., Mickley, L. J., Logan, J. A., and Kaplan, J. O.: Ensemble projections of wildfire activity and carbonaceous aerosol
907 concentrations over the western United States in the mid-21st century, Atmospheric Environment, 77, 767–780,
908 https://doi.org/10.1016/j.atmosenv.2013.06.003, 2013.

909 Yue, X., Mickley, L. J., and Logan, J. A.: Projection of wildfire activity in southern California in the mid-twenty-first century,
910 Clim Dyn, 43, 1973–1991, https://doi.org/10.1007/s00382-013-2022-3, 2014.

911 Zhong, S., Yu, L., Heilman, W. E., Bian, X., and Fromm, H.: Synoptic weather patterns for large wildfires in the northwestern
912 United States—a climatological analysis using three classification methods, 76, https://doi.org/10.1007/s00704-020-03235-y,
913 2020.

914 Zou, Y., Wang, Y., Ke, Z., Tian, H., Yang, J., and Liu, Y.: Development of a REgion-Specific Ecosystem Feedback Fire
915 (RESFire) Model in the Community Earth System Model, 11, 417–445, https://doi.org/10.1029/2018MS001368, 2019.

916 Zou, Y., Wang, Y., Qian, Y., Tian, H., Yang, J., and Alvarado, E.: Using CESM-RESFire to understand climate–fire–
917 ecosystem interactions and the implications for decadal climate variability, 20, 995–1020, https://doi.org/10.5194/acp-20-995-
918 2020, 2020.

919

920

921

922

923 **Table 1.** Advantages and limitations of different types of fire models

	Representative method	Advantages	Limitations
Data-driven model	Multiple Linear regression (MLR)	1. Computationally efficient 2. Simple model 3. It is easy to interpret	1. It cannot capture the non-linear relationships between fires and predictors 2. It assumes that the predictor variables are independent 3. It is sensitive to outliers
	Machine learning method (e.g., neural network, decision tree etc.)	1. Computationally cheap compared to process-based models 2. The performance improves when more training data are included 3. It can easily handle multi-dimensional data	1. It requires a lot of training data 2. It is relatively hard to interpret 3. The interactions between fires and vegetation/atmosphere cannot be updated to the model
Process-based model	Dynamic global vegetation model (DGVM)	1. Physics-driven 2. The simulations can include feedbacks between fires and climate or vegetation	1. Computationally expensive 2. The same parameterization may not be applied to all regions 3. It only parameterizes the known processes or phenomena

924

925

926

927 **Table 2.** Predictor variables used in the ML model

Variables	Abbreviation	Categories	Temporal resolution	Spatial resolution	Data Source	References
Monthly mean surface temperature	temp	Local meteorology	monthly	32 km	North American Reanalysis (NARR)	Mesinger et al. (2006)
Monthly mean relative humidity	RH	Local meteorology	monthly	32 km	North American Reanalysis (NARR)	Mesinger et al. (2006)
Monthly mean of daily precipitation	precip	Local meteorology	monthly	32 km	North American Reanalysis (NARR)	Mesinger et al. (2006)
Monthly mean zonal component of wind speed	U	Local meteorology	monthly	32 km	North American Reanalysis (NARR)	Mesinger et al. (2006)
Monthly mean meridional component of wind speed	V	Local meteorology	monthly	32 km	North American Reanalysis (NARR)	Mesinger et al. (2006)
Monthly Standardized Precipitation Evapotranspiration Index	SPEI	Local meteorology	monthly	$0.5°×0.5°$	SPEI	Vicente-Serrano et al. (2010)
Monthly mean 1000-hour dead fuel moisture	FM1000	Local meteorology	daily	4 km	gridMET	Abatzoglou (2013)
Monthly mean energy release component	ERC	Local meteorology	daily	4 km	gridMET	Abatzoglou (2013)
Monthly mean vapor pressure deficit	VPD	Local meteorology	daily	4 km	gridMET	Abatzoglou (2013)
Monthly lightning flashes density	lightning	Local meteorology	daily	$0.1°×0.1°$	SWDI/NLDN	NOAA (2006); Cummins and Murphy (2009)
Monthly standard deviation of daily SVDs for northern California	SVD1_NCA and SVD2_NCA	Large-scale meteorological patterns	monthly	Regional	North American Reanalysis (NARR)	Wang et al. (2021)
Monthly standard deviation of daily SVDs for southern Rocky Mountain	SVD1_SRM and SVD2_SRM	Large-scale meteorological patterns	monthly	Regional	North American Reanalysis (NARR)	Wang et al. (2021)

Monthly standard deviation of daily SVDs for southeastern US (with 2-month lag)	SVD1_SElag2 and SVD2_SElag2	Large-scale meteorological patterns	monthly	Regional	North American Reanalysis (NARR)	Wang et al. (2021)
Monthly mean evapotranspiration	ET	Land-surface properties	monthly	0.25º×0.25º	North American Land Data Assimilation System (NLDAS-2)	Xia et al. (2012)
Monthly mean surface soil moisture	soilm	Land-surface properties	monthly	0.25º×0.25º	Global Land Data Assimilation System (GLDAS-2)	Xia et al. (2012)
Monthly mean vegetation fraction	Veg_frac	Land-surface properties	monthly	0.25º×0.25º	Global Land Data Assimilation System (GLDAS-2)	Xia et al. (2012)
Monthly mean Leaf Area Index	LAI	Land-surface properties	8 days	500 m	MODerate resolution Imaging Spectroradiometer (MODIS); LAI classification scheme	Myneni et al. (2015)
Monthly fuel load/normalized fuel load	fuel_load/fuel_load_nor	Land-surface properties	monthly	0.9º×1.25º	Community Land Model (CLM)	Lawrence et al. (2019)
Land cover percentage	p_	Land-surface properties	Yearly	0.05º×0.05º	MODerate resolution Imaging Spectroradiometer (MODIS); LAI classification scheme	Friedl (2015)
Median Topography (slope and elevation)	Slope and elevation	Land-surface properties	Not change by time	100 km		Amatulli et al. (2018)
Gross domestic product	GDP	Socioeconomic and coordinate variables	Yearly	5 arc		Kummu et al. (2018)
Population density	Pop	Socioeconomic and coordinate variables	Yearly	30 arc	Gridded Population of the World data collection (GPW v4)	CIESIN-Columbia University (2017)

928

929

930

931 **Table 3.** The ML model performance for different regions: western forest area, Mediterranean California, southwestern US,
932 and southeastern US

	Western forest area	Mediterranean California	Southwestern US	Southeastern US	Whole US
Grid scale (individual grid)					
RMSE (km^2)	0.29	0.32	0.10	0.02	0.16
Correlation (r)	0.79	0.51	0.76	0.84	0.76
IoA	0.86	0.60	0.85	0.90	0.84
Percentage of grids with correlation > 0.4 (%)	68	47	52	80	74
Regional scale (summation over the region)					
RMSE (km^2)	37.80	13.94	2.76	3.37	49.98
Correlation (r)	0.98	0.81	0.94	0.97	0.97
IoA	0.98	0.81	0.95	0.98	0.97

933

934

935 **Table 4.** The model performance for the ML model and FireMIP models

	ML model	CLM	CTEM	JSBACH	LPJ-SPI	LPJ-Glob	LPJ-SIM	ORCHIDEE	JULES
Total amounts of fire PM$_{2.5}$ emissions (Tg=10^{12} g) (GFED: 4.89 Tg)									
Total fire PM$_{2.5}$ emissions over 2000-2012 (Tg)	8.33	16.54	41.50	19.92	16.23	79.49	35.38	2.43	33.43
Correlation of interannual/seasonal variability for the CONUS									
Correlation (interannual/seasonal)	0.87/0.98	0.71/0.92	0.28/0.87	0.15/0.89	0.15/0.92	0.02/-	0.23/0.65	0.03/0.91	0.55/0.93
Correlation of interannual/seasonal variability for the selected regions									
Western forest area	0.93/0.98	0.70/0.93	0.33/0.88	0.21/0.88	0.38/0.79	0.51/-	0.46/0.98	0.05/0.94	0.60/0.92
Mediterranean California	0.72/0.97	-0.01/0.87	0.05/0.94	-0.30/0.89	-0.07/0.90	-0.14/-	-0.19/0.83	0.25/0.13	-0.21/0.87
Southwestern US	0.95/0.99	0.14/0.85	-0.26/0.62	-0.28/0.45	0.34/0.42	0.30/-	0.40/0.94	0.45/0.72	-0.07/0.69
Southeastern US	0.96/0.99	0.57/-0.27	-0.16/0.09	0.72/-0.14	0.08/0.35	0.39/-	0.18/0.68	0.16/0.13	0.36/0.01

936

937

938

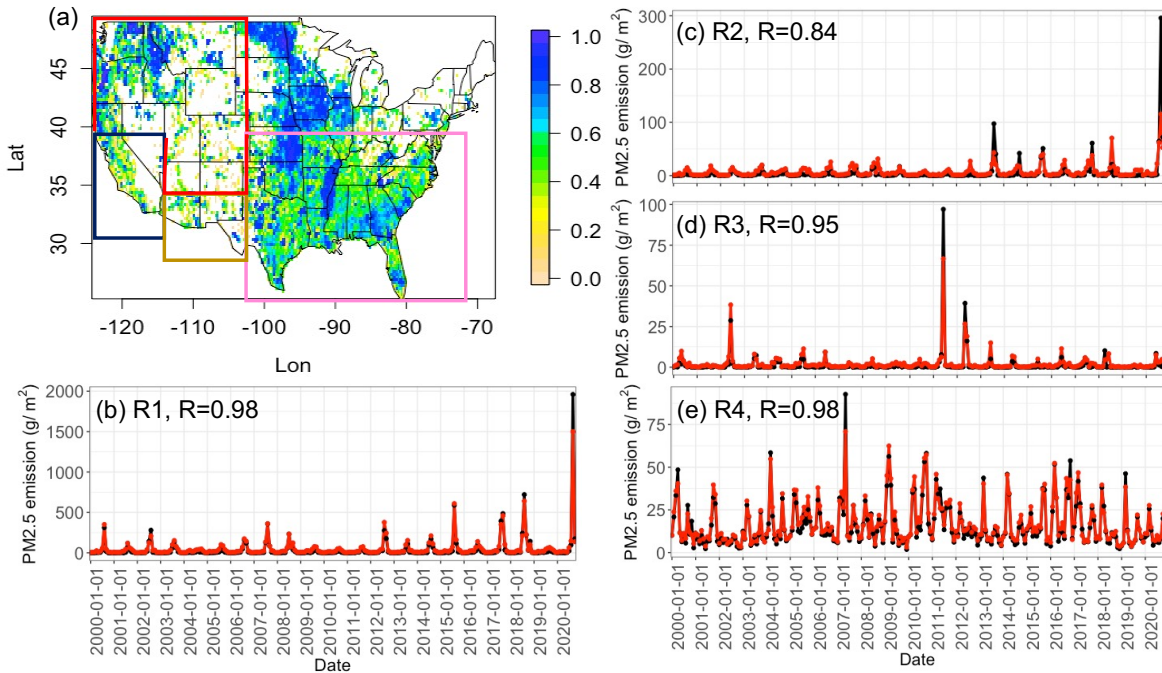



Fig. 1. (a) The map of temporal correlation between observed and predicted fire PM$_{2.5}$ emission for each grid. Time series of observed (black) and predicted (red) fire PM$_{2.5}$ emission average across (b) western forest area (red box in 1a), (c) Mediterranean California (blue box), (d) southwestern US (dusty box), (e) southeastern US (pink box).

942

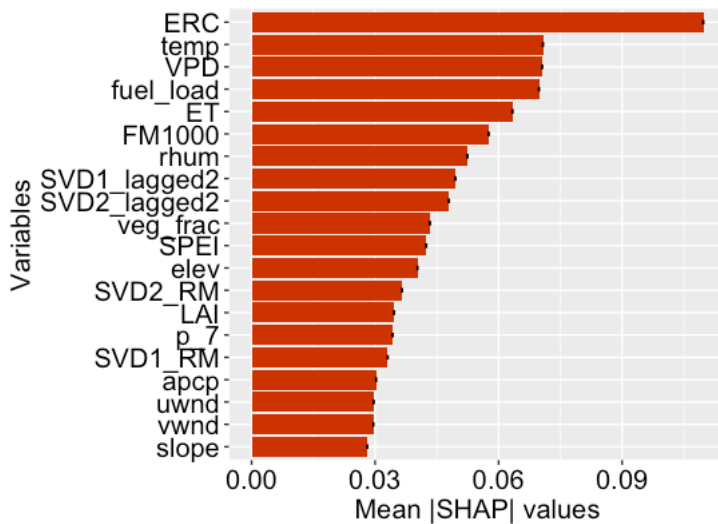
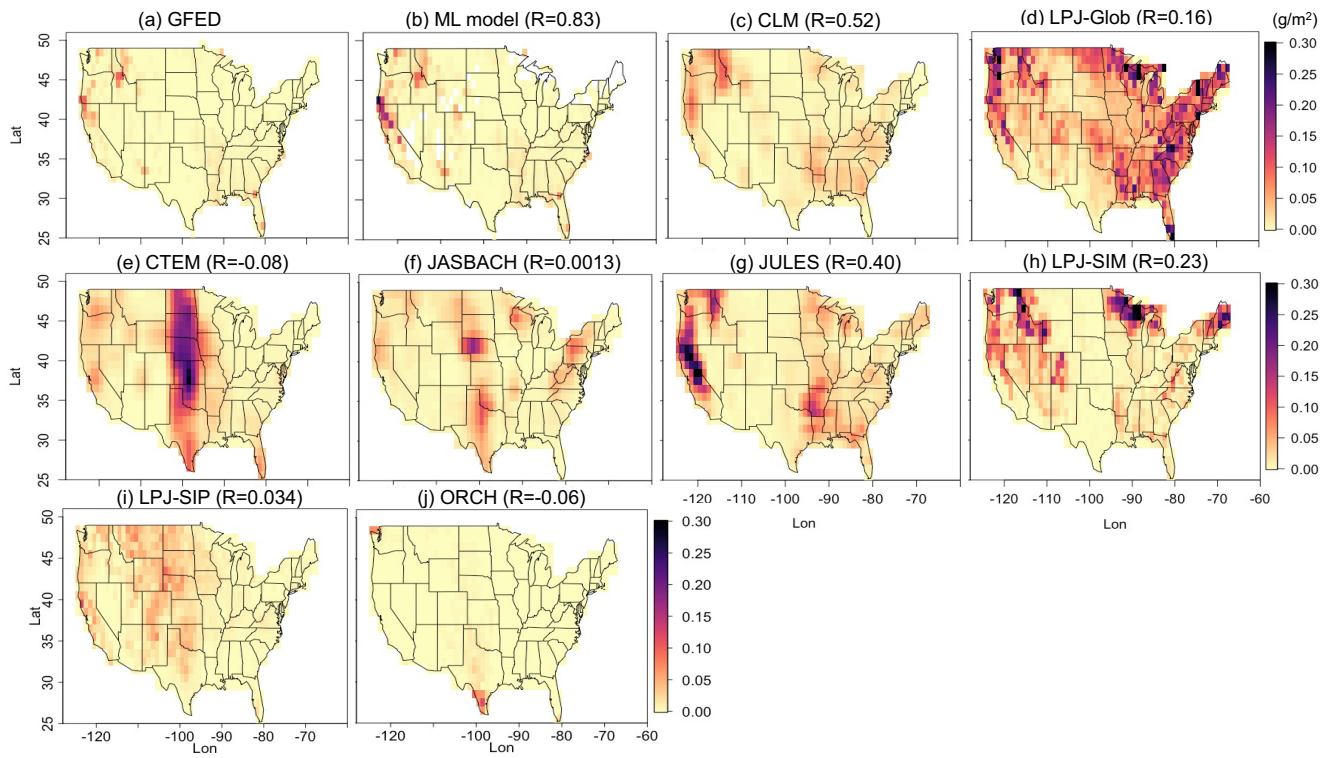
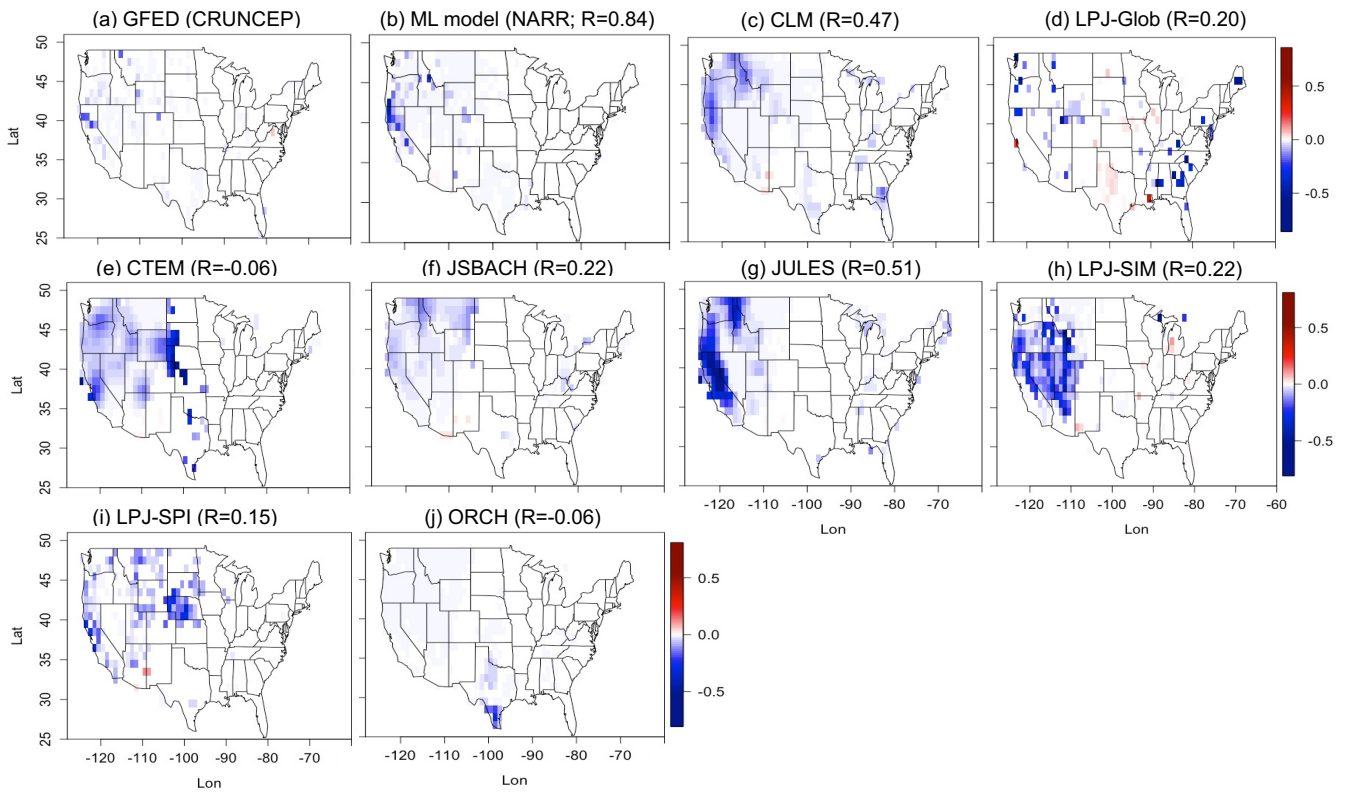



Fig. 2. Top 20 variables for the model based on the mean absolute SHAP value with the 95% confidence intervals.

944

945

946   **Fig. 3.** Spatial distributions of the monthly mean fire PM$_{2.5}$ emission (g/m^2/month) over 2000-2012.

947

948

949 **Fig. 4.** Spatial distributions of the linear regression slope for the dependence of annual mean fire PM$_{2.5}$ emissions on annual

950 mean RH. Only the grids with slopes that are statistically significant (p<0.05) are shown.

951

952

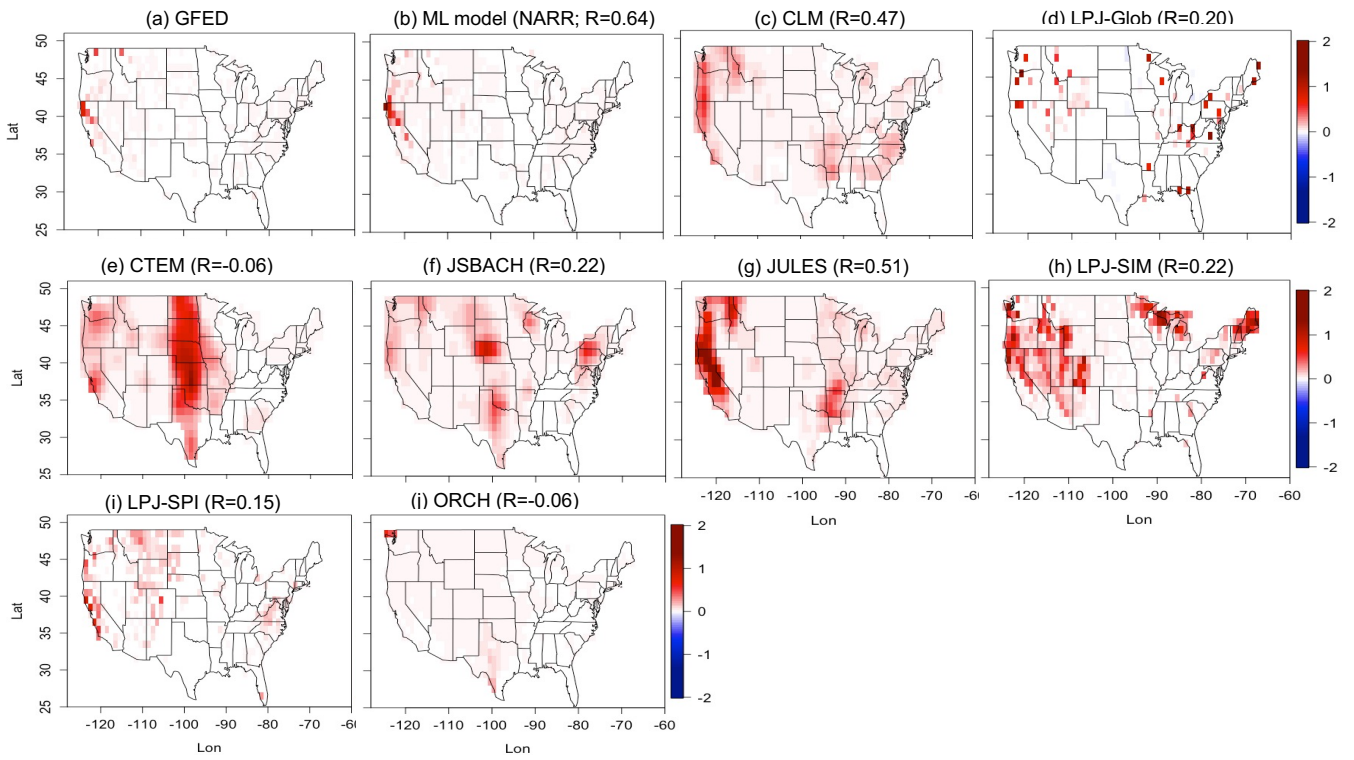



Fig. 5. Spatial distributions of the linear regression slope for the dependence of annual mean fire $PM_{2.5}$ emissions on annual

mean temperature. Only the grids with slopes that are statistically significant ($p<0.05$) are shown.

955

956

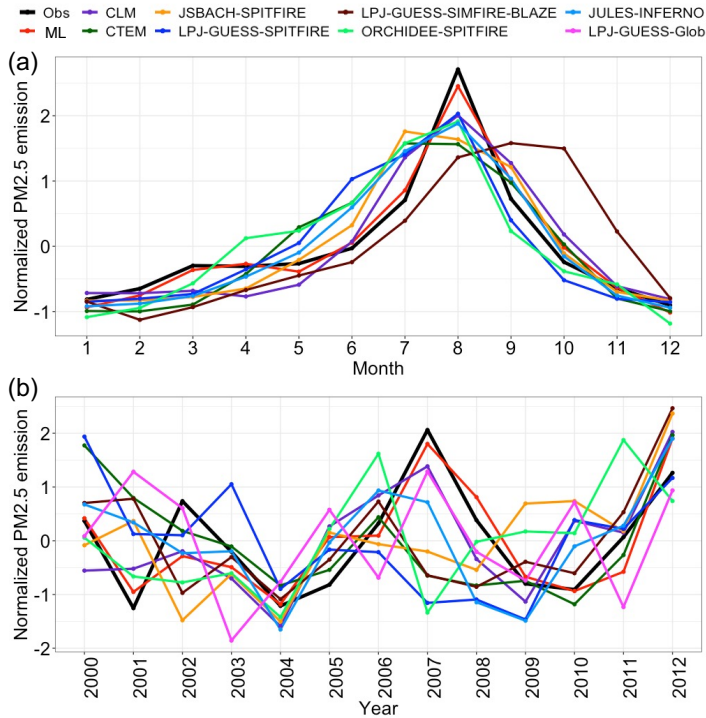



Fig. 6. (a) Seasonality and (b) interannual variability of the normalized averaged fire PM$_{2.5}$ emission from the GFED (black line), ML model (red line), and the FireMIP models (color lines). The fire PM$_{2.5}$ emissions are first averaged over CONUS and normalized by the monthly (annual) mean and standard deviation for seasonality (interannual variability) plots.

960

961

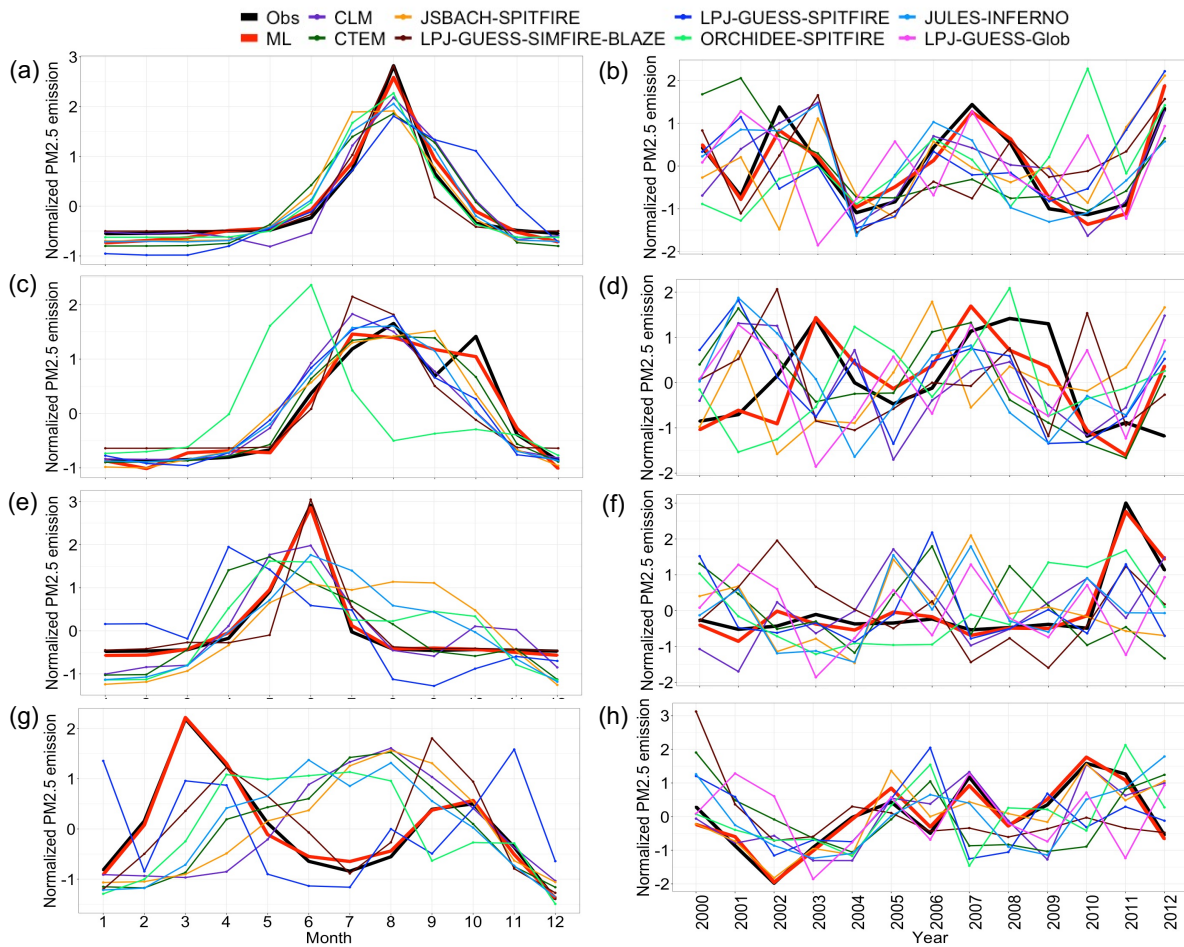
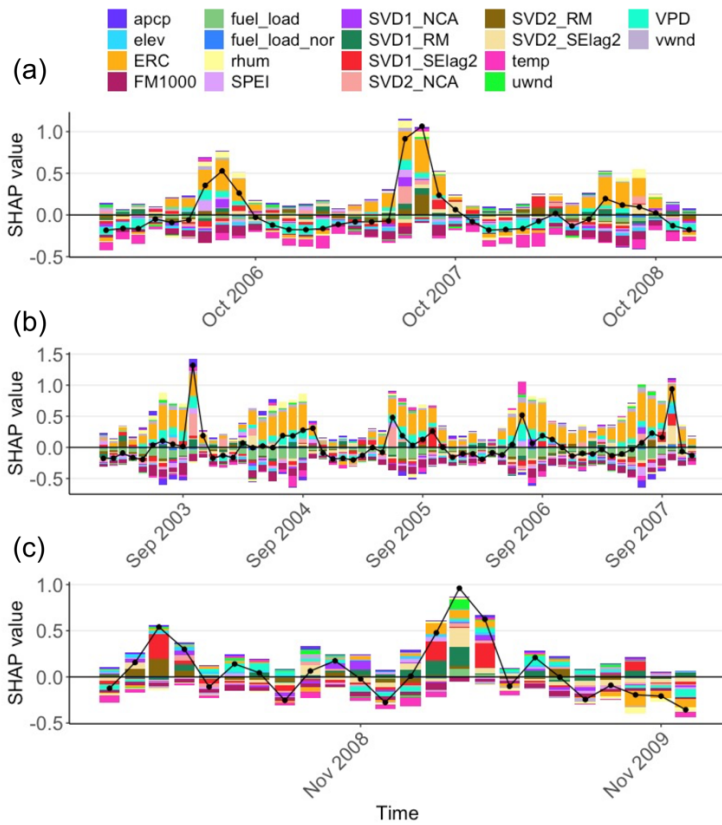



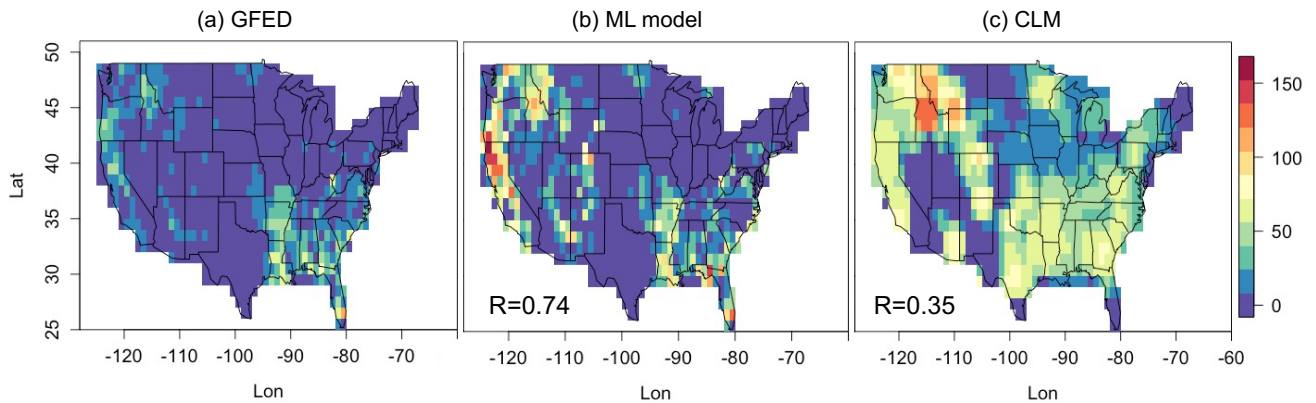
Fig. 7. Seasonality and interannual variability of the fire PM$_{2.5}$ emission from the GFED (black line), ML model (red line), and the FireMIP models (color lines) for (a, b) western forest area, (c, d) Mediterranean California, (e, f) southwestern US, and (g, h) southeastern US.

962
963
964

965

966

967 **Fig. 8.** Time series of the average SHAP values (bar) and predicted normalized fire PM2.5 emission (line) for (a) western forest
968 area from 2006 to 2008, (b) Mediterranean California from 2003 to 2007, and (c) southeastern US from 2008 to 2009. The
969 SHAP values indicate the contribution of the predictors to the prediction of normalized fire emission.

970

971

972

973 **Fig. 9.** Spatial distributions of number of months with large fire emissions (> 95th percentiles of fire PM2.5 emission over all
974 the grids in 2000-2012) for (a) GFED, (b) ML model, and (c) CLM.

976

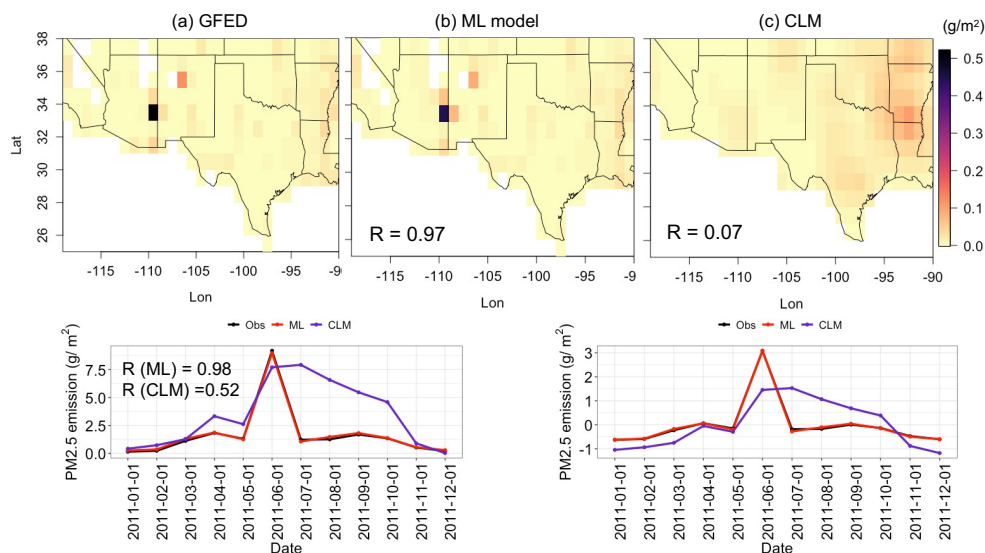



Fig. 10. Top panel: Spatial distributions of the annual mean fire PM$_{2.5}$ emission in 2011 for (a) GFED, (b) ML model, and (c) CLM. Bottom panel: Time series of the (d) total fire PM$_{2.5}$ emissions and (e) normalized fire PM$_{2.5}$ emission over southern US domain during 2011.

980

981

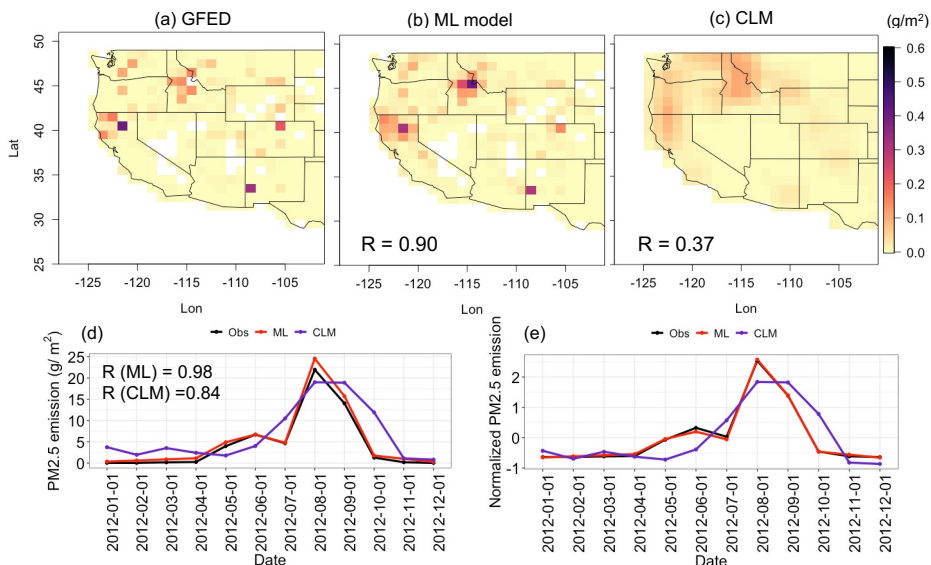



Fig. 11. Top panel: Spatial distributions of the annual mean fire PM$_{2.5}$ emission in 2012 for (a) GFED, (b) ML model, and (c) CLM. Bottom panel: Time series of the (d) total fire PM$_{2.5}$ emissions and (e) normalized fire PM$_{2.5}$ emission over western US domain during 2012.