



Towards monitoring CO₂ source-sink distribution over India via inverse modelling: Quantifying the fine-scale spatiotemporal variability of atmospheric CO₂ mole fraction

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Abstract

The prospect of improving the estimates of CO₂ sources and sinks over India through inverse methods calls for a
15 comprehensive atmospheric monitoring system involving atmospheric transport models that make a realistic
accounting of atmospheric CO₂ variability. In the context of expanding atmospheric CO₂ measurement networks
over India, this study aims to investigate the importance of a high-resolution modelling framework to utilize
these observations and to quantify the uncertainty due to the misrepresentation of fine-scale variability of CO₂ in
the employed model. The spatial variability of atmospheric CO₂ is represented by implementing WRF-Chem at
20 a spatial resolution of 10 km × 10 km. We utilize these high-resolution simulations for sub-grid variability
calculation within the coarse model grid at a horizontal resolution of one degree (about 100 km). We show that
the unresolved variability in the coarse model reaches up to a value of 10 ppm at the surface, which is
considerably larger than the sampling errors, even comparable to the magnitude of mixing ratio enhancements in
source regions. We find a significant impact of monsoon circulation in sub-grid variability, causing ~3 ppm
25 average representation error between 12 – 14 km altitude ranges in response to the tropical easterly jet. The
cyclonic storm Ockhi during November 2017 generates completely different characteristics in sub-grid
variability than the rest of the period, whose influence increases the average representation error by ~1 ppm at
the surface. By employing a first-order inverse modelling scheme using pseudo observations from nine tall
tower sites over India and a constellation of satellite instruments, we show that the Net Ecosystem Exchange
30 (NEE) flux uncertainty solely due to unresolved variability is in the range of 6.3 to 16.2 % of the total NEE. We
illustrate an example to test the efficiency of a simple parameterization scheme during non-monsoon periods to
capture the unresolved variability in the coarse models, which reduces the bias in flux estimates from 9.4% to
2.2 %. By estimating the fine-scale variability and its impact during different seasons, we emphasise the need
for implementing a high-resolution modelling framework over the Indian subcontinent to better understand
35 processes regulating CO₂ sources and sinks.



1 Introduction

Accurate assessment of sources and sinks of CO₂ is essential in planning and implementing the mitigation strategies for greenhouse gas emission and associated climate change. However, estimations of CO₂ fluxes contain significant uncertainties which increase even more with finer spatial scales such as those required for the climate change mitigation policies at regional and national levels (e.g., Ciais et al., 2014; Li et al., 2016; Cervarich et al., 2016). By using atmospheric CO₂ concentration measurements, the CO₂ fluxes can be estimated by a multi-constrained observation-modelling approach, often referred to as top-down approach or inverse modelling (Enting, 2002). For about two decades, these top-down approaches are being widely used to understand the modifications in the carbon cycle through natural and anthropogenic induced environmental changes (Bousquet, 2000; Schimel et al., 2001; Rödenbeck et al., 2003; Patra et al., 2005). In addition to the observations, the inverse modelling system makes use of an atmospheric transport model (forward model), which determines the distribution of CO₂ concentration. Thereby, the inverse optimization approach derives the surface fluxes that are consistent with measured concentration. The UNFCCC (United Nations Framework Convention on Climate Change) has acknowledged the increasing capability of inverse modelling to systematically monitor GHG concentrations (Bergamaschi et al., 2018).

Most of the inverse modelling systems relies on global atmospheric transport models with coarse horizontal resolution (often greater than one degree) (Rödenbeck et al., 2003; Peters et al., 2007; Rödenbeck et al., 2018a, b; Inness et al., 2019). However, regional estimation of fluxes using global models is hindered by the inability of transport models to represent observed CO₂ variability. The observed variability, as seen from the spatial and temporal distribution of atmospheric CO₂, is highly correlated with the space and time scales of weather systems (Parazoo et al., 2011). This explains the presence of large model-data mismatches in regions where mesoscale circulation is predominant (Ahmadov et al., 2007). Wind speed, wind direction, and height of the planetary boundary layer (PBL) are the critical variables that determine the atmospheric CO₂ variability. Strong wind normalizes other small-scale variations in observed concentration due to mixing, and the predictability can be higher during these conditions (Sarrat et al., 2007). The height of PBL is an essential variable in modelling CO₂ concentration since the atmospheric CO₂ is subjected to rapid mixing up to this altitude. Hence, for a given location with a negative gradient in CO₂ vertical distribution, the overestimation of PBL height leads to underestimation of CO₂ concentration and vice-versa (Gerbig et al., 2008).

Another important variable that impacts the CO₂ variability is the heterogeneous topography. When the small-scale orographic details are not adequately represented in the models, they can lead to representation errors in CO₂ simulations as large as 3 ppm at scales of 100 km (Tolk et al., 2008; Pillai et al., 2010). The horizontal gradients in CO₂ concentrations can go up to values of 30 ppm within a spatial scale of 200 km, depending on the land surface heterogeneity (van der Molen and Dolman, 2007). Previous studies based on airborne measurements reported that transport models need a spatial resolution which is smaller than 30 km to be able to represent CO₂ spatial variability in the continental boundary layer (Gerbig et al., 2003). Significant efforts have been invested to derive fluxes by taking to account these fine-scale variations (e.g., Gerbig et al., 2003; Lauvaux et al., 2009; Carouge et al., 2010; Pillai et al., 2011, 2012; Broquet et al., 2013) over North American and Eurasian domains in the past decade. However, there still exists lower confidence in estimates over the region,



where there is a lack of both advanced modelling systems at relevant spatio-temporal resolutions and good coverage of ground-based monitoring stations.

In the context of the Indian sub-continent, the inverse-based estimation of fluxes at fine scales is essentially new; hence many questions remain. A number of monitoring sites measuring atmospheric greenhouse gases have become available in India from the last decade (Tiwari et al., 2011; Lin et al., 2015). Aside from the ongoing progress in augmenting observational data streams, it remains challenging to assimilate these data for deducing process-specific information effectively (e.g., McKain et al., 2012; Bréon et al., 2015; Pillai et al., 2016). The limitation of these coarse models on representing observations over the Indian subcontinent is reflected in the analysis made by Patra et al. (2011).

The seasonally reversing South Asian monsoon system is a prominent meteorological phenomenon affecting the Indian subcontinent, which is also expected to influence the terrestrial-atmosphere flux exchanges. Various studies have demonstrated the role of Indian monsoon circulations on regional atmospheric transport by strong south westerlies during the summer monsoon (June to September) and by north easterlies during the winter monsoon (October to November) (e.g., Goswami and Xavier, 2005; Krishnamurthy and Shukla, 2007). The monsoon convection that transports the boundary layer air into the free atmosphere (mainly to the upper troposphere and to the lower stratosphere with the help of diabatic heating (Vogel et al., 2019)) complicates atmospheric transport simulations (Willettts et al., 2016). Moreover, a significant component of flux variations can arise from biospheric fluxes (Schimel et al., 2014), which is influenced by variables such as rainfall, availability of radiation, and temperature (Chen et al., 2019). Several studies showed that the monsoon system substantially impacts vegetation growth, generating distinct spatio-temporal patterns of the biogenic fluxes (e.g., Gadgil, 2003; Valsala and Maksyutov, 2013). It is noteworthy that the cropping patterns over India have a strong dependence on seasons and are mainly determined by dry and wet seasons for nearly 65 to 70 % of the country's area except over north-eastern and south-western (Western Ghats) regions of India. Therefore, employing a higher resolution modelling over Indian subcontinent is desirable, which can take into account the fine-scale variations generated by both mesoscale transport processes and surface flux patterns.

The study focuses on accounting the unresolved sub-grid scale variability when employing current generation global models. Assimilation of observations in an inverse framework requires the characterization of these error structures at relevant scales that can be utilized to retrieve source-sink distribution over India. The main objectives of this paper are to describe and quantify the expected spatiotemporal variability of atmospheric CO₂ that is not resolved by the current generation global models, quantify to what extent these variations cause uncertainty in flux estimations, and assess how these uncertainties can be minimized by modelling the sub-grid variations in the global models. Specifically, we address the following questions: 1) how good is the level of agreement among global transport models that are used in the current generation inversion systems for predicting atmospheric CO₂ concentrations over Indian subcontinent? 2) how large are the variations of atmospheric CO₂ that are unresolved by global and regional models which operate at a spatial scale of 1°× 1° and 0.5°× 0.5° respectively? 3) what is the role of seasonal changes and synoptic events on generating different patterns in these sub-grid variations of CO₂? 4) how much is the uncertainty in the inverse-based flux estimation, caused by these unresolved variations in the coarse models when utilizing a given network of surface observations and satellite measurements over the domain? 5) how effectively can we capture the key aspects of



115 the variability and take into account for it in flux estimations? We present an analysis based on our high-
resolution simulations at a spatial resolution of $10\text{ km} \times 10\text{ km}$, and the sub-grid variability derived using these
high-resolution simulations. By designing a pseudo surface observation network and hypothetical satellite
measurements over the domain, we investigate the impact of these unresolved variations on the regional flux
estimations and assess how a simple parameterization scheme can help in reducing these errors in the global
120 model.

In this article, we present results based on the analyses of the high-resolution simulations for the months of July
and November 2017. The year 2017 is characterized by neutral Indian Ocean Dipole conditions over the Indian
Ocean and with the beginning of a mild La Nina over the Pacific by the end of the year. The month of July
represents a monsoon period when the biospheric activity is significant together with atmospheric convection
125 activities. On the other hand, the month of November is more representative of post-monsoon wintertime in
Indian subcontinent. At the same time, the period from 23 to 30 November 2017 provides us with
the opportunity to study the impact of a synoptic event on contributing to CO_2 variability. To our knowledge,
there is no comprehensive published study of this kind over the Indian subcontinent until now assessing the
magnitude and impact of temporal and spatial variability exhibited by atmospheric CO_2 .

130 The outline of the paper is as follows. Section 2 describes our modelling system, data and approaches including
the methods used for estimating the sub-grid scale variability of CO_2 . Inter-model comparisons using global
models and our investigations on spatial variability are discussed in section 3. Through the global model
comparisons and spatial variability analysis, we highlight potential difficulties for estimating current
 CO_2 budget assessments over India and provide the quantification of expected spatiotemporal variability as well
135 as its impacts. Finally, we provide the implications of our findings in section 4, suggesting the ways forward to
yielding an improved estimation of CO_2 budgets over India.

2 Data & Methodology

A major part of this study is performed using the simulations generated by our high-resolution modelling system
(see Sect. 2.1). For providing a more comprehensive overview of the inter-model agreements among the existing
140 model simulations over Indian subcontinent, we use a variety of global model simulations as explained in Sect.
2.2. These global model outputs are derived from the inverse model simulations, which estimates the source-
sink distributions of CO_2 and then three-dimensional CO_2 concentration fields are generated consistent with the
optimized posterior fluxes. These models differ in terms of the model configuration, observational datasets that
were assimilated (e.g., data from surface monitoring stations, aircraft missions, ship cruises, AirCore balloon
145 soundings, and satellite's total column retrievals), prior datasets, and spatiotemporal resolutions. For quantifying
the spatial variability of CO_2 over India, we use our high-resolution simulations, focusing on the representation
error approach as explained in Sect. 2.3. Following a first-order assumption, a simple method is used to estimate
the impact of the derived sub-grid scale variations on flux estimations over India (see Sect. 2.4).

2.1 WRF-Chem GHG Modelling System

150 For this study, we use the modelling system WRF-Chem GHG in which the Weather Research and Forecasting
model (WRF) version 3.9.1.1 (Skamarock et al., 2008) is coupled with the greenhouse gas module (WRF-



Chem-GHG, Beck et al., 2011), implemented as part of the WRF-Chem distribution (WRF-Chem, Grell et al., 2005). For simulating the atmospheric transport, the model uses fully compressible Eulerian non-hydrostatic equations on Arakawa C- staggered grid, conserving mass, momentum, entropy and scalars (Skamarock et al., 2008). In the WRF-Chem GHG (hereafter referred simply as WRF-GHG), we use the passive tracer chemistry option to simulate changes in CO₂ mixing ratios associated with surface fluxes and atmospheric transport. We utilize a biospheric model and emission inventory data to simulate atmospheric CO₂ enhancements associated with biogenic and emission fluxes as described in Sect. 2.1.1 and 2.1.2. Table. 1 summarizes the model configuration, including physics parameterizations and input data used in this study.

The model domain covers a region spanning from 65°E to 100°E and 5°N to 40°N, configured in a Lambert conformal conic (LCC) projection with 307 × 407 grid points. The spatial resolution of the grid is 10 km × 10 km and model time-step of 60 s. We have used model output with a temporal resolution of 1 hour for this study. The simulations are performed using 39 vertical levels with the model top at 50 hPa and 10 levels within the lowest 2 km. WRF-GHG simulations are performed for the entire July and November 2017 for this study. Implementation of the WRF-GHG system over Indian subcontinent enables us to customize it according to the domain features and build a state-of-the-art modelling system, which eventually estimates CO₂ fluxes through regional inverse systems. The potential of the WRF-GHG model in simulating fine-scale spatial variability is also established in previous studies (Ahmadov et al., 2009; Pillai et al., 2011; Park et al., 2018).

2.1.1 Representation of biospheric fluxes

We use the Vegetation Photosynthesis and Respiration Model (VPRM) in the modelling system to calculate Net Ecosystem Exchange (NEE) representing the biospheric fluxes (Mahadevan et al., 2008). VPRM is a diagnostic biosphere model, which utilizes remote sensing products: Enhanced Vegetation Index (EVI) and Land Surface Water Index (LSWI) derived from reflectance data of the Moderate resolution Imaging Spectroradiometer (MODIS) as well as meteorological data: solar radiation and air temperature. In this study, these hourly NEE calculations are performed within WRF-GHG, simultaneously with the meteorology simulations in which NEE is calculated as a sum of gross ecosystem exchange (GEE) and ecosystem respiration (R_{eco}). VPRM, in this case, uses the meteorological data provided by WRF-GHG. VPRM uses the SYNMAP vegetation classification (Jung et al., 2006) as well as EVI and LSWI from MODIS surface reflectance data at a resolution of 1 km and 8 days. We aggregate these indices specific for different vegetation types onto the LCC projection for the entire domain at the model's spatial resolution. A number of studies have used VPRM for other regions around the world in which derived NEE shows good prediction skills for hourly to monthly timescales (Ahmadov et al., 2009; Pillai et al., 2011; Liu et al., 2018; Park et al., 2018).

2.1.2 Representation of emission fluxes

Anthropogenic CO₂ emission fluxes are prescribed from the Emission Database for Global Atmospheric Research (EDGAR) dataset, version 4.3.2, provided at a horizontal resolution of 0.1° × 0.1°. We disaggregate the available annual emission data into hourly emissions, using the country and sector-specific temporal profiles of CO₂ emissions available at the product website (<https://edgar.jrc.ec.europa.eu>) (Steinbach et al., 2011; Kretschmer et al., 2014). To represent biomass burning emission, we have used data from the Global Fire Assimilation System (GFAS) with a spatial resolution of 0.1° × 0.1° and a temporal resolution of one day.



190 GFAS is based on satellite data, which calculate the fire emission by assimilating fire radiative power (FRP) observations from MODIS instruments (Kaiser et al., 2012). All these flux data are gridded and projected to WRF-GHG's model domain.

2.1.3 Initial and boundary conditions

195 Meteorological and chemical initial and boundary conditions are required in WRF-GHG to account for initial state and inflow or background flow. The initial and lateral boundary conditions for the meteorological variables, including horizontal wind components, pressure, specific humidity, sea surface temperature (SST), and the necessary surface initialization fields are obtained from the ERA5 dataset, the European Centre for Medium-Range Weather Forecasts (ECMWF), extracted at a horizontal resolution of 25 km and a temporal resolution of 1 hour (Hersbach et al., 2020). In the case of CO₂ tracers, the initial and lateral boundary
 200 conditions are obtained from the Copernicus Atmosphere Monitoring Service (CAMS, 2.2.4). (Massart et al., 2016; Agusti-Panareda et al., 2019). We have used the dry air mole fractions of CO₂ from the CAMS-GHG, which has a temporal resolution of 6 hour and horizontal resolution of 0.5° × 0.5° with 137 vertical levels. The data is taken from the greenhouse gas analysis experiment, which is conducted with the objective of providing realistic 3D fields of atmospheric GHG concentrations in dry air mole fractions. Note that there exists a CAMS
 205 product at 9 km × 9 km resolution, which is in the developmental phase and not yet available to the general public (personal contact: Anna.Agusti-Panareda@ecmwf.int).

We have utilized a different simulation strategy to take advantage of assimilated meteorological fields from ECMWF. The model is reinitialized each day with ECMWF assimilated data at 00.00 UTC after a spin-up period of 6 hours started from 18.00 UTC of the previous day. In the case of CO₂, the initial values at the
 210 beginning of the restart hour are taken from the last hour (Ahmadov et al., 2012).

2.2 Global atmospheric transport models

In addition to our high-resolution simulations, we have used other optimized products at global scales and examined the representation of CO₂ variability over the Indian subcontinent. Four global inverse modelling products - CarbonTracker, CarboScope, LSCE v18r3 and LSCE FT18r1- available during the year 2017 are
 215 used for our analysis. These global models depend on different formulations (e.g., transport and the employed inversion methodology) and associated data (e.g., the choice of measured atmospheric mixing-ratio observations and emission fluxes) in simulating the underlying processes. We have used the daytime (11:30 to 16:30 local time) concentration values from all these models for the analysis. A brief description of each model is followed (see Table. 2 for more details).

220 2.2.1 CarbonTracker (CT-2019B)

CarbonTracker is a global reanalysis system for CO₂ fluxes developed by the Earth System Research Laboratory (ESRL) at the National Oceanographic and Atmospheric Administration (NOAA) (Peters et al., 2007; Jacobson et al., 2020). We have used CO₂ mole fractions from the CarbonTracker (CT2019B version), having a horizontal resolution of 3° × 2° with 25 vertical levels and a temporal resolution of 3 hours.

225 2.2.2 CarboScope



In this study, we have used the atmospheric CO₂ concentration from the CarboScope Inversion v2020 with a horizontal resolution of 5° × 3.8° with 19 vertical levels and a temporal resolution of 6 hours (Rödenbeck et al., 2003; Rödenbeck et al., 2018a, b). The major focus of this inversion system is the inter-annual variability of the CO₂ fluxes, homogeneously covering time periods containing all data records to avoid spurious jumps.

230 2.2.3 LSCE

This atmospheric inversion system (Chevallier et al., 2005; Chevallier et al., 2010; Chevallier, 2013) provides atmospheric CO₂ concentration with horizontal resolution 3.7° × 1.8° and 39 vertical levels and temporal resolution of 3 hours. Version FT18r1 (hereafter LSCE FT in this manuscript), which we utilized for the current study uses satellite retrievals from the Orbiting Carbon Observatory (OCO-2) for optimization of CO₂ fluxes.

235 We also used version v18r3 (hereafter LSCE in this manuscript), which utilizes surface observations for the optimization.

2.3 Quantification of spatial variability

For quantifying the spatial variability due to sub-grid scale processes which cannot be resolved by the coarse resolution models, we follow the approach as described in Pillai et al. (2010). The term ‘representation error’ indicates the mismatch between the scales of model simulations and observations collected (Pillai et al., 2010; Janjić et al., 2017). In other words, the representation errors arise due to unresolved scales, which could not be captured by the model. Here we calculate the representation errors in the coarse resolution models, which can be fully resolved by implementing the high-resolution model. For estimating the representation error in a coarse model with a typical spatial resolution of 1° × 1°, we have calculated the standard deviation of CO₂ dry air mole fraction simulated by the WRF-GHG model within the coarse grid boxes of 1° × 1° as follows:

$$245 \quad \sigma_{CO_2} = \sqrt{\frac{1}{n-1} \sum_{j=1}^n (m_j - \bar{m})^2} \quad (1)$$

where $\bar{m} = \frac{1}{n} \sum_{j=1}^n m_j$

n is the number of 0.1° boxes inside the coarser grid cell of 1° × 1°; m is the CO₂ dry air mole fraction corresponding to 0.1° boxes; and \bar{m} is the average within the coarser grid cell. So, the estimated values represent the sub-grid scale variability within the coarse model grid cell which is having a horizontal resolution of 1° × 1°. As the observations can also be made by the space-borne instruments, we extend the analysis to column-averaged dry air mole fraction (XCO₂) as measured by the satellite instrument. i.e., m represents either CO₂ at the second model level or XCO₂.

255 The surface representation errors are calculated using the model simulations from the second model level (~200m) to avoid the inconsistency that can be generated from inputting emission fluxes at the first model level. Representation errors are calculated separately for daytime (11:30 to 16:30 local time) and nighttime (23:30 to 4:30 local time) to account for the difference in the sub-grid scale process during these times. To disentangle the correlated term from the total representation error, the monthly averages of representation errors are taken. The effect of random errors can be minimized when averaging over long time periods. However, we have also analysed the sub-monthly temporal variations in the representation errors by using representation errors



calculated at an hourly time scale (Sect. 3.2.2). Note that all discussions presented in this study except for Sect. 3.2.2 are based on monthly averaged values of representation errors. Both July and November are used to understand the differences in the variability during summer and winter.

Due to the paucity of adequate ground-level observations over India, satellite observations play an essential role in the estimation of CO₂ fluxes. Satellite observations can provide column average CO₂ (XCO₂) concentration with a precision of 1 to 1.5 ppm (O'Dell et al., 2012; Wunch et al., 2017). In order to utilize these satellite observations, the transport models being used in the inverse estimation must be highly accurate as small errors in atmospheric transport simulations (a few tenths of ppm) can cause significant biases (a few hundreds of MtC/year) in the inferred surface carbon budget at the scale of subcontinents (Chevallier et al., 2010). To assess the ability of current-generation models in utilizing the XCO₂ over India, we have also performed a similar representation error analysis for XCO₂.

2.4 Estimation of representation error induced flux uncertainty using pseudo measurements

2.4.1 Using surface measurements

In order to quantify the impact of representation errors on flux estimations when utilizing surface measurements, we have devised the following strategy. For this, we use nine CO₂ surface monitoring sites representing various geographical regions over India (Fig. 1). Not all these observation stations are currently fully operational or having continuous measurements. We have performed an observation system simulation experiment (OSSE) using high-resolution CO₂ simulations generated by the WRF-GHG model for each of these stations. We focus on the biospheric flux component, NEE. For deducing the contribution of the representation error to the biospheric flux uncertainty, we have taken the following assumptions: 1) there are no model/observation errors other than representation error, and 2) the model captures the spatial and temporal patterns of flux correctly. This means that the difference between observations (OSSE) and simulations of atmospheric CO₂ is the representation error in ppm. Additionally, as a first-order simplification for the inversion, we assume that the footprints of each observation site span for a radius of 200 km based on our analysis using the Stochastic Time-Inverted Lagrangian Model (STILT, Lin et al., 2003) and approximation of area covering of 50-90 percentile of contributions from STILT-derived footprints of each station. The STILT is driven with ECMWF IFS (Integrated Forecasting System) meteorological fields and the trajectories are calculated based on 100 virtual particles that are released for each time interval and location. The residence time of particles in the surface layer is weighted by the atmospheric density to derive the footprints of each location.

Through our simple least-square inversion approach, we retrieve monthly NEE by utilizing hourly CO₂ observations (from OSSE) and simulations over a month. Both the observation and simulation vector have 6480 (=1×9×30×24) elements for a month having 30 days, and the state vector has 9 (=1×9) elements corresponding to scaling factors of monthly fluxes over regions around 9 sites. In other words, each site has been assigned with one scaling factor for NEE, and there is a total of 9 scaling factors for a given month. As it is the case for OSSE, we know the flux Φ_{true} ("true" flux) and can be utilized for calculating the deviation of posterior fluxes from the true fluxes. Here we use the VPRM NEE fluxes as the "true" fluxes in OSSE (see Sect. 2.1.2). We use the unit vector λ as initial scaling factors. The linear inversion provides the optimized scaling factors λ_{retr} , and these scaling factors are applied to Φ_{true} within the area covering of 50-90 percentile of the footprints in order to



300 derive the posterior fluxes Φ_{retr} . For the rest of the region outside the footprint area of each site, the Φ_{retr} remains the same as Φ_{true} .

The optimized monthly scaling factors (λ_{retr}) of fluxes can be obtained by minimizing the following cost function $J(\lambda)$:

$$J(\lambda) = \frac{1}{N} \sum_{n=1}^N (\mathbf{y}_{OSSE} - \mathbf{y}_{sim})^2 \quad (2)$$

where N is the size of observation and simulation vectors, \mathbf{y}_{OSSE} is given by:

$$305 \quad \mathbf{y}_{OSSE} = \mathbf{H} \cdot \mathbf{f}_m(\lambda) \quad (3)$$

where \mathbf{H} is the transport operator and $\mathbf{f}_m(\lambda)$ is the flux model in which a subset of parameters λ out of total model parameters \mathbf{p} will be optimized. Here $\mathbf{f}_m(\lambda)$ is taken as linearly dependent on λ ; hence can be expressed as

$$\mathbf{f}_m(\lambda) = \Phi_{true} \cdot \lambda \quad (4)$$

310 Note that \mathbf{y} represents the biospheric contribution (in ppm) of the atmospheric CO_2 mixing ratio. By minimizing the cost function as given in Eq. (2), we get the optimized estimate of scaling factors λ_{retr} . By this inverse design, the deviation of posterior fluxes from the true fluxes is thus the uncertainty in retrieved fluxes, \mathbf{S}_{rep} , that arises solely due to the contribution from the representation error and is calculated as:

$$\mathbf{S}_{rep} = |\Phi_{true} - \Phi_{retr}| = |\Phi_{true} - \Phi_{true} \cdot \lambda_{retr}| = |(1 - \lambda_{retr}) \Phi_{true}| \quad (5)$$

315 Note that by following the above inversion design and assumptions, there is a high likelihood of underestimating the impact of the modelling error on flux estimations since we have not considered other sources of uncertainties such as model transport uncertainty and inappropriate prior assumptions. Thus, the quantification of flux uncertainty using this approach can be inferred as the lower bound of the uncertainty (i.e., the minimum flux uncertainty one may expect while estimating fluxes using a model with a grid cell of $1^\circ \times 1^\circ$ and 9 stations with representativeness of 200 km).

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2.4.2 Using satellite measurements

Following the approach as given in Sect. 2.4.1, we have estimated the NEE flux uncertainty when using satellite observations over the model domain. For this, we have assumed an idealized dense spatial sampling of a constellation of satellites which sample as frequently as possible over each location with a wide swath enabling to cover a large geographical area, typically a few hundred kilometres. As our focus is to deduce the flux uncertainty solely due to the representation error, we assumed no measurement errors. In practice, the satellite spectra are altered by atmospheric scattering by air molecules and the presence of aerosols and clouds, which contribute to the measurement error. The presence of clouds significantly influences the number of available (quality-filtered) observations over a region. To take this into account, only cloud-free observations are considered. For this, we use cloud fraction derived from the radiance and reflectance measurements by MODIS aboard NASA's Terra satellite product (MOD35).

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Based on WRF-GHG simulations, we perform the analysis for November at 10.30 AM each day and sample the data after considering the cloud cover. We have used a cloud fraction threshold of 20%, and data from the region below this threshold are only used. We have only used 15 random days from November for the estimation. Because of this criterion, there is a reduction of 90.4% observations over the domain. Due to the monsoon overcast, the month of July is excluded since the number of cloud-free data is significantly low to deduce any meaningful results. As explained in Sect. 2.4.1, the modelled simulations are obtained by adding the corresponding representation error to the pseudo observations. Both the observation and simulation vector have 181320 ($=1 \times 12088 \times 15$) elements, and the state vector has only one element, which represents the scaling factor of NEE fluxes over the entire domain. Posterior fluxes are calculated using the scaling factor, derived from minimizing the cost function (Eq. (2)).

3 Results and Discussions

3.1 Agreement among global models

We first analyse the performance of current-generation global transport models in simulating CO_2 concentration over Indian subcontinent. Note that a mere agreement among the coarse models is not sufficient to justify the models' performance over the region due to their large model errors in common and interdependency in terms of data sources. As mentioned in Sect. 2.2, we restrict this analysis to daytime-only values since different processes control the variability of CO_2 concentration at daytime and nighttime, and simulating nighttime variability is more complicated than the daytime (Lauvaux et al., 2009). For a consistent comparison among global models, all the products are sampled at the same time for the region spanning from 67°E to 98°E and 7°N to 38°N . Figure 2a depicts the annual vertical profiles of CO_2 concentration, showing models' discrepancy in simulating the vertical gradients in concentration values including the boundary layer and the free troposphere. A notable difference is observed in the simulation of the gradient within the boundary layer by different models. The magnitude and the height up to which this positive gradient is observed is different for these models. LSCE (both versions) has the largest positive gradient among these models ($\sim 1 \text{ ppm}$). It shows the maximum concentration at around 700 m height and then a decrease in concentration. CarbonTracker also shows this positive gradient in the surface layers up to a height of 900 m. But the gradient is much smaller compared to the other two models. Among these four models, CarboScope does not exhibit this tendency in the lower atmosphere. Its concentration decreases linearly from the surface as the height increases.

The seasonal variability of CO_2 uptake through photosynthesis, release through ecosystem respiration, and the vertical transport is seen while analysing the monthly averaged CO_2 concentration profiles over Indian subcontinent (Figs. 2b and 3). Comparatively lower surface CO_2 concentrations are found during months with an active biosphere (June to October) than the rest of the period, owing to the more ecosystem productivity over Indian subcontinent in response to the availability of monsoon rainfall. Also, the presence of strong southwest monsoon winds during June to September may result in bringing CO_2 depleted air from the southern hemisphere and thereby lowering the CO_2 concentration over the domain. Further, we see a CO_2 vertical profile with very small vertical gradient ($\sim 0.5 \text{ ppm}$ within an altitude range of $\sim 500 \text{ m}$ to 4000 m) from June to October (Fig. 3). This is likely linked to the increased convective activities associated with the monsoon. The considerable inter-model variation in monthly averaged CO_2 concentration profiles as predicted by different global models is



problematic as it indicates the significant uncertainties in flux estimations over India. A part of this discrepancy can come from the coarse resolution global model's inability to represent transport processes like convection and vertical mixing, strength and distribution of anthropogenic sources and ecosystem activities that operate at fine scales. The spatial distribution of CO₂ concentration shows structural differences among these models (see Supplementary Fig. S1), indicating a substantial knowledge gap on accounting atmospheric CO₂ variability over Indian subcontinent, which will have severe implications for the country's carbon budget estimations.

3.2 Representation errors in global transport models

As described in Sect. 2.3, we have calculated the representation error in the current generation global models with a spatial resolution of 1° × 1°, which allows us to identify the regions and processes with high variability in CO₂ concentration. The larger the representation error, the larger are the variations that are caused due to sub-grid processes within the grid box of 1° × 1°. The spatio-temporal variability of representation error and the influence of various factors in creating this variability are examined here.

3.2.1 Spatio-temporal patterns

Representation errors in the surface CO₂ concentrations for July and November are shown in Fig. 4. There is a relatively high representation error in the coastal regions due to the temporal covariance between the coastal meteorology and exchange fluxes. The CO₂ fluxes from coastal regions can be transported over the ocean and accumulated in the shallow boundary layer over the ocean. The shallow boundary layer is a characteristic of the marine atmosphere due to the less vertical mixing compared to land regions. Horizontal CO₂ gradients can also be generated by the influence of highly varying biospheric fluxes under different advection patterns over the land and ocean boundary. A similar mechanism is applicable to mountain regions where temporal covariance of mountain-valley circulation and respired CO₂ fluxes are regulated by atmospheric radiation. We find that the representation error for nighttime is characterized by high values compared to the daytime throughout the analysed domain. This is expected due to the coupling between nocturnal shallow transport and different flux processes, causing more local effects. During the nighttime, photosynthesis is absent, and respiration is the major biospheric activity, leading to an increase in CO₂ concentration in the atmosphere. Together with the large heterogeneity in flux distribution, mostly from respired CO₂ flux, the shallow boundary layer processes and weak turbulence during nighttime cause CO₂ to be accumulated locally near the surface, showing large variations.

In July, many low-pressure systems were active in the monsoon trough region (IMD weather reports, <https://mausam.imd.gov.in>) whose presence influence the atmospheric transport (Li et al., 2021) and creates representation error due to the associated mesoscale activity. The influence of the synoptic systems on CO₂ concentration can be observed during July (Fig. 5a) and November (Fig. 6b) with regions exhibiting well mixed vertical gradients. Strong mixing and vertical transport associated with the low-pressure systems are visible from these CO₂ concentration figures. Compared to July, we find higher representation error in November owing to the wintertime transport with decreased vertical mixing and less biospheric uptake. A significant part of this variation in November comes from the formation of low-pressure systems over the Bay of Bengal and over the Lakshadweep area (≈ 8° N, 74° E) from 22 November onwards. One of these low-pressure systems in the Bay of Bengal further developed and intensified as deep depression and moved to the southeast Arabian Sea



and evolved into a severe cyclonic storm (Ockhi) by 30 November. In addition to this, there persisted a western disturbance as an upper air cyclonic circulation over northern parts of Jammu and Kashmir during the period of November 23-30. Figure 6 shows the latitudinal averaged vertical cross-section atmospheric CO₂ concentration from the WRF-GHG simulation during two separate periods (period during days 11-20 and 21-30) in November. By comparing these two periods in November, we can see the influence of low-pressure systems on the CO₂ concentrations. Due to the impact of large horizontal and vertical flows associated with these synoptic systems, we have observed low CO₂ concentration values and high spatial variability in the eastern part of the domain. These variations create significantly large representation errors compared to other periods during November, as will be discussed in more detail in section 3.2.2.

In the case of XCO₂, the magnitude of sub-grid scale variability is much smaller than that of surface CO₂ (Fig.7), but it follows a similar spatial pattern of surface sub-grid variations. This confirms the dominance of surface-level processes in causing sub-grid variability of column averages. The sub-grid scale variability in XCO₂ reaches up to 3 ppm in some parts of the region especially where there are high variations in topographic features. For a large part of the domain, the representation error is found to be above 1 ppm, which is very close to or even larger than the typical precision of current satellite measurements ($\approx 1 - 1.5$ ppm) and it is capable of causing significant biases in the satellite inferred CO₂ fluxes over India. This result also reasserts the need for high resolution modelling over India when utilizing satellite observations.

Figure 8 shows the statistical distribution of the representation error during July and November, separated by daytime and nighttime. July shows a median representation error of 1 ppm and 1.5 ppm during daytime and nighttime respectively, while November shows a median value of 3 ppm and 3.5 ppm for daytime and nighttime respectively. During July, 95 % of the representation error is less than 3.2 ppm for daytime (6 ppm for nighttime) while it is 6 ppm for daytime (8 ppm for nighttime) in the case of November. For column average, median values for representation error are 0.7 ppm and 1.3 ppm for July and November respectively. To further reduce the effect of random error that might be introduced by short-term weather phenomena, the correlated representation errors are calculated from the monthly averaged CO₂ field and is denoted as a systematic error ("Sys" in Fig. 8). Note that uncorrelated errors are expected to decrease when averaging over a sufficiently long period. As expected, the median representation errors for systematic representation errors are reduced for all cases, showing the effect of random errors. Especially for November when the cyclonic event was present, the values for systematic errors (in the 95% percentile) for the surface CO₂ is considerably lower than total errors, reducing from 6ppm (daytime) and 8 ppm (nighttime) to 3 ppm (daytime) and 4 ppm (nighttime). In the case of column CO₂, this reduction is from 3.5 ppm (daytime) and 3.6 ppm (nighttime) to 1.5 ppm (daytime) and 1.6 ppm (nighttime) in the 95% percentile. Consistent with Fig. 8a both median and 95% percentile of the nighttime representation errors are found to be higher than daytime except for November night.

We further carried out the estimation of representation errors for a spatial resolution of $0.5^\circ \times 0.5^\circ$ (Supplementary Figs. S2 and S3) to explore how much these variations can be resolved by a typical model operating at this spatial scale (e.g., regional models). On average, we find a decrease in representation errors to 0.78 ppm (~22 % reduction), and 1.6 ppm (~47% reduction) in the month of July (daytime) and November (daytime) respectively. Exhibiting a similar spatial pattern of error for both resolutions of 0.5° and 1° indicates the need for a much finer modelling system than that of regional models with a typical resolution of 0.5° for



adequately representing the CO₂ dynamics. Though a reduction of representation error is observed for 0.5° compared to 1°, the emission hotspots and point sources are still pronounced, with high sub-grid scale variability, especially during nighttime. The above analyses indicate that the representation error alone can have significantly high values compared to the sampling errors (e.g., 0.1 ppm as per WMO standards for surface measurements), which demands higher resolution inversion systems for the optimal estimation of CO₂ fluxes.

3.2.2 Intra-month variability

Here we have used hourly representation errors to see its sub-monthly variations in July and November. Results show that daily variations in surface representation errors are minimal (± 0.14 ppm) within a month for July, although there exists a clear distinction between daytime and nighttime values (existence of diurnal variability, see Fig. 9). Compared to other days in November, higher surface representation errors (~5 ppm) are found from 23 to 30 November in response to the synoptic systems prevailed. These results indicate that small variations in daily representation errors can be expected within a month. But noticeable variations with higher representation errors do happen in the occurrence of synoptic events like a cyclone. Such events need to be adequately represented in the model to capture the temporal changes in the regional spatial variability, which is difficult to be handled by global models because of the spatial-scale mismatches between model and synoptic events.

Interestingly, column representation error in July shows different behaviour compared to surface concentrations. We find comparatively higher (factor of more than two) representation error during 10 to 18 July than the rest of the period. This is due to the upper-troposphere dynamics associated with the development of low-level jet (LLJ) in the lower troposphere and the Tropical Easterly Jet (TEJ) in the upper troposphere during the monsoon season, as seen in Kottayil et al., (2019). Though the effect of LLJ and TEJ is visible throughout July (Fig. 5b), strong convective activity associated with the low-pressure systems is visible during July 10-18 (Fig. 5a). The combined effect of LLJ and TEJ can also be seen in the vertical distribution of the representation error (next section).

3.2.3 Vertical distribution

Figure 10 shows the vertical profile of representation error distribution within different bins of altitude. In addition to using 24 hours (denoted as “full-day”), we have also separated daytime and nighttime for the profile distribution. For November, we find the maximum representation error in the surface layer and most of the higher values are found to be within the lowest 4-6 km bins. Also, sub-grid scale variability decreases sharply with increasing altitude for November. This dominance of variability in surface concentration for November can be explained by surface flux heterogeneity influencing mole fractions in lower atmospheric layers (PBL) as described in van der Molen and Dolman, (2007) and Pillai et al., (2010). These dominances are found to be even more significant during the synoptic-scale event when the associated variations were mostly confined within the lower atmospheric levels (Supplementary Fig. S4). On the other hand, the representation error for July increases with altitude up to 12 to 14 km, showing the significant impact of meteorology above the boundary layer owing to the combined effect of LLJ and TEJ. Local convection can also produce variations in the upper level, but its scale of variations is expected to be less compared to the monsoon circulation systems during July. This implies that the monsoon circulations, along with extensive convective activities, can dominate the surface flux



heterogeneity in producing sub-grid variability, thereby causing significant biases in the flux estimations when transport is not adequately accounted.

3.3. Influence of terrain heterogeneity on representation errors

The influence of terrain heterogeneity on representation error can be seen from the spatial figures in Figs. 4 and 7, where the large sub-grid scale variations are found in the Himalayan regions. Spatial variations in topography produce mesoscale circulation patterns and hence the variations in atmospheric CO₂ at fine scales. To further explore the importance of using the high-resolution topography data on representing the CO₂ variability, we analyse the dependence of terrain variations (as derived from the standard deviation of terrain height) on representation error distribution. We have calculated the linear fit between topographic variability within the global climate models' grids and corresponding representation error to estimate the relation between them. Topographic variability within 1° × 1° box is estimated as the standard deviation of topography (m) for all 0.1° × 0.1° boxes within the larger grid. Bins are created based on the values of this topographic variability, in which different points from different parts of the domain are binned together on the basis of their standard deviation of topography. Each bin is created with a size of 50 m variation in terrain height. The linear fit is estimated between the average value of topographic variability within a bin and the average value of representation error of the corresponding points in the bin. Our results show that the terrain heterogeneity alone can explain about 53-62% of the surface representation errors over the domain (see Supplementary Fig. S5). In a similar way, we have estimated the influence of topographic variability in the formation of representation error in the column averaged model simulations. It is found that both surface and column representation errors show a very high correlation with the topographic variations in which topography alone can explain 81-89 % of representation errors in the column-averaged simulations. Though there exists a slight correlation between surface flux heterogeneity (as derived from the standard deviation of VPRM-derived fluxes) and surface representation errors during daytime (11-35%), we find that this relationship is absent during nighttime, which is consistent with the findings from Pillai et al., (2010). This result underlines the need for using accurate Digital Elevation Models (DEMs) in the atmospheric transport models as one of the most critical datasets for determining the mesoscale atmospheric flows adequately.

3.4 Estimation of NEE flux uncertainty due to representation error

By following the assumptions and approach as given in Sect. 2.4, we have estimated the NEE flux uncertainty resulting from the representation errors. The results based on the OSSEs for nine observation sites are given in Table. 3. The scaling factors, which are calculated separately for each site by adjusting the prior fluxes using pseudo-observations, are applied to the VPRM fluxes. The total NEE flux for India estimated by VPRM for July and November are -373.3 MtCO₂ per month and -417.1 MtCO₂ per month respectively. The flux uncertainties over India that arise solely due to the contribution from the representation error are estimated to be 54.4 to 60.8 MtCO₂ per month (14.5% to 16.2%) for July and 26.2 to 31.4 MtCO₂ per month (6.3% to 7.5%) for November while utilizing data from nine observation stations. July showed the maximum flux uncertainty due to the enhanced biosphere activity and unresolved convection activities. As expected, the flux uncertainty is higher when using nighttime values for both months. In the same manner, as explained in Sect. 2.4.2, we have estimated the flux uncertainty while using satellite observations. We have only estimated the NEE flux



uncertainty during daytime in November in accordance with the availability of satellite observations over the domain. The scaling factor is calculated for the entire domain where the cloud fraction is less than 20%. The total flux uncertainty, while using satellite observations for November over India, is 39.2 MtCO₂ per month (9.4%). The estimated uncertainties are considerable for the carbon budget assessment especially given that these errors are arising solely from the global models' representation error. Note that calculated representation error does not include other transport error sources such as advection, convection or vertical mixing.

3.5 Possible treatment of representation error in the global model.

The simplest possible way to minimize the uncertainty in flux estimation using a coarse model is to construct a parameterization model that can take to the account of representation error using explanatory variables. For this, we assert a multivariable model to capture spatial patterns in the representation error. The hypothetical satellite observations are used for this analysis. The linear model using only one explanatory variable, terrain heterogeneity, as derived from the previous analysis in Sect. 3.3, captures the derived representation error in the southern part of India with less than 1 ppm bias (see Supplementary Fig. S6). However, in the northern part of the region, especially in the Indo Gangetic Plain (IGP) and Rajasthan, we find that the terrain heterogeneity alone cannot explain the spatial patterns of the representation error, and the bias is larger than 1 ppm. Our further analysis using a multivariable linear model with explanatory variables that include sub-grid variations of terrain, biospheric and anthropogenic fluxes shows a remarkable improvement in representing the derived representation error all over the domain with a R² value of 0.68 (Fig. 11). The bias between the modelled and derived representation error is found to be well below 1 ppm in most parts of the domain. By employing this model, we see that the total inferred flux uncertainty, while using satellite observations for November over the entire domain, is reduced from 9.4% (39.2 MtCO₂ per month) to 2.2% (9.1 MtCO₂ per month). This finding provides a possibility for a parameterization that can be further developed in inverse models or data assimilation systems, which defines the degrees of freedom for describing the posterior states. However, note that this simple parameterization may not be useful when there exists large influence from monsoon circulations as seen for July (see Sects. 3.2.1 and 3.2.3). Applying this parameterization scheme to the specific problem requires a high-resolution map of the terrain and prior information on anthropogenic and biogenic fluxes. The uncertainties in the topography can significantly impact flux estimation, and the likely reduction of flux uncertainty depends on the accuracy of the DEM employed. The caveat of this linear model is that the uncorrelated spatial variability in the prior and true states of the fluxes is ignored in the present form, which cannot be the case for the real inverse problems. This assumption obviously hampers the system in achieving the maximum reduction in uncertainty, and further study is needed to refine this model from a practical perspective. We emphasise, however, that the above parameterization does not require high-resolution simulation of transport, which has high computational costs.

4. Conclusion

Given the upcoming availability of atmospheric observations over India, significant effort is required to critically enhance the modelling capabilities to derive carbon budgets over India within the definite confidence intervals and at scales relevant to ecosystem and countrywide policy-making. The misrepresentation of transport phenomena and unresolved flux variations in the modelling system operating at coarse grids hinders the



560 effective utilization of observations. In this context, quantification of the spatial variability of atmospheric
 CO₂ mixing ratio and assessment of its seasonal dependence are necessary to make optimal use of observations
 in the inverse framework. In this study, the atmospheric CO₂ spatial variability is represented using the WRF-
 GHG model at 10 km spatial resolution. While investigating the shortcomings of the current-generation model
 on quantifying regional sources and sinks of CO₂, the present study demonstrates the potential of implementing
 565 a high-resolution atmospheric CO₂ transport modelling framework over India. The importance of horizontal
 resolution in the models and the adequate representation of topography and flux variations in capturing CO₂
 variability is given a focus here, by quantifying the representation error resulting from the coarse model's
 inability to resolve the fine-scale variations accurately.

Through our inter-model comparisons, we quantify the variability in the CO₂ mole fractions predicted by the
 570 state-of-the-art global models (CarboScope, LSCE and CarbonTracker) in terms of their spatial and vertical
 variations even at a monthly scale. The large model spread among the vertical profiles (~1 ppm) and differences
 in vertical gradient indicate a severe knowledge gap in the estimations of fluxes even at the global scale. It can
 be argued that a significant part of these differences arises due to the lack of observational constraints over
 India, which leads to a possible compensatory model artefact over this region in order to match the global mass
 575 constraint. Noteworthy is that none of these models includes ground-based data from the Indian subcontinent. At
 the same time, it is also expected that the spatial variability of the observed atmospheric CO₂ mole fractions can
 be large so that these coarse models fail to represent them adequately, thereby leading the inverse optimization
 to infer the state which is not close to the truth as is required in regional CO₂ budget for various applications.

By quantifying the unresolved variation of the global models with a spatial resolution of $1^\circ \times 1^\circ$, overall, we
 580 find that the representation error can be up to ~10 ppm for the surface CO₂ and about 3 ppm for column-
 averaged values, which are markedly larger than the sampling errors. For example, the achievable precision of
 satellite-based XCO₂ is around 1 ppm for current satellites: OCO2 and GOSAT (Liang et al., 2017; O'Dell et
 al., 2012; Wunch et al., 2017). In the case of high accuracy in situ measurements, the typical uncertainty for
 CO₂ measurements is less than 0.1 ppm (Andrews et al., 2014). These sampling errors are significantly smaller
 585 than the size of the corresponding model's representation error. This indicates that the employed models need to
 be critically improved in terms of capturing mesoscale phenomena and fine-scale flux variability in order to
 maximize the potential of deducing the information obtained from these high precision measurements, thereby
 improving the estimation of surface fluxes. The mesoscale features and associated CO₂ gradients can be
 generally captured by increasing the spatial and temporal resolution of the transport models. However, by
 590 merely increasing the resolution without having a realistic representation of terrain heterogeneity and flux (both
 natural and anthropogenic) variability would not be beneficial. Note that the uncertainties in the high-resolution
 fluxes can worsen the model's skills, whose effect would not be more pronounced at coarser resolutions due to
 the diffusive nature of fluxes, as seen in Agustí-Panareda et al. (2019).

Although the magnitude of the sub-grid variability of the total column is an order smaller than the variability at
 595 the surface, the spatial pattern remains similar for both, owing to the dominance of surface heterogeneity in
 topography and fluxes. Our results are consistent with Pillai et al. (2010), who show that there exist regional
 differences in the sub-grid variability for both surface and column CO₂. Coastal sites and mountain are
 pronounced with high representation error (~6 ppm), while emission hotspots are distinguishable with



variability as large as ≈ 8 ppm. Larger values are typically associated with the nocturnal shallow boundary layer
600 dynamics and the stronger respiration signal with considerable flux variability.

We identify the seasonal changes in the sub-grid variability over India through our analysis during monsoon and
post-monsoon periods. November shows a median representation error of 3 ppm during daytime which is three
times more than the median representation error for July. The derived seasonal differences in structural patterns
of the sub-grid variability facilitate to (1) quantify what would be transport errors associated with incorporating
605 seasonally varying observations (both surface and column observations) into atmospheric transport models
when the model resolution differs from the spatial scales of observations (which reflects in the confidence
intervals of the inferred CO_2 fluxes via inverse modelling) (2) determine what drives the seasonality in sub-grid
variability and ultimately (3) design the possible parameterization of representation error with a seasonal
component in the inverse modelling framework as well as identify periods (or seasons) where the use of this
610 parameterization would be valid to improve our estimations of CO_2 fluxes. Further, the seasonal spatial
variability analysis of column averages can provide useful information for the satellite community to gap-fill the
satellite soundings over India when large data gaps and low sounding precision on daily or monthly time scales
are present, which is especially the case for monsoon periods in India. For example, the impact of the combined
effect of LLJ and TEJ associated with monsoon can be seen in the vertical distribution of sub-grid variability for
615 July. During this period, the average representation error increases to ~ 3 ppm with altitude up to 12 to 14 km, in
contrast to the post-monsoon period in which representation error decreases sharply with increasing altitude.
This sharp decrease of sub-grid variability with altitude is expected and is consistent with (Pillai et al., 2010;
van der Molen and Dolman, 2007). The results for the monsoon period assert the need for high resolution
modelling over India incorporating both upper and lower troposphere. The cyclonic storm (Ockhi) in November
620 generates considerably more CO_2 spatial gradients than the rest of the period, which increases the sub-grid
variability of CO_2 by ~ 1 ppm on average. The impact of cyclonic activities on CO_2 distribution and their
frequent occurrence over the Indian subcontinent reassert the need to employ the models at high resolution for
capturing the fine-scale CO_2 variability that coarser-resolution models cannot resolve. Increasing the model's
resolution to $0.5^\circ \times 0.5^\circ$ has shown an improvement in capturing variability with representation error reduction
625 of 22% and 47% for summer time and winter time respectively. By showing the existence of considerable
magnitude of unresolved variability in 0.5° sub-grid scale with a similar spatial pattern of error as of 1° spatial
resolution, we demonstrate the need for a much finer resolution than 0.5° for representing the atmospheric CO_2
over India.

The inaccuracies, as mentioned above, are large enough to manifest themselves in transport model biases. We
630 construct a simple inversion example to illustrate the impact of derived representation error on estimating the
fluxes. In the light of the upcoming network of observations, we use pseudo-observations from nine
observatories over India and hypothetical satellite observations. With the underlying assumptions, the total flux
uncertainty solely due to the unresolved sub-grid variations is estimated to be 6.3 to 16.2% of the total NEE
while utilizing data from nine observation stations over India. Similarly, the total expected flux uncertainty,
635 while using satellite observations for November over the entire domain is estimated to be 9.4%.

Further, the potential of a simple parameterization scheme has been presented to understand the origin of the
representation error and take into account its effects in a global model. For this case, we have shown that a



640 multivariable linear model with explanatory variables of sub-grid variations of terrain, biospheric and anthropogenic fluxes can help to simulate the expected representation error in the global model. Employing this linear model in a global model would thus redefine the likelihood of better estimates (improving the state of knowledge) with variance greater than that of the measurement error in the inverse framework by minimizing the modelling error. In our specific example, on utilizing satellite observations for November, we see a significant reduction in the total flux uncertainty from 9.4% to 2.2% after applying the linear model. The proposed method is easy to implement in the coarse models as it does not require computationally expensive transport simulations at high-resolution. However, more work is needed to demonstrate the extent of applicability of this method to minimize the flux uncertainties while utilizing actual observations. As we see a significant dependence of the distribution of sub-grid variability on terrain variations, our results reinforce the requirement for using accurate DEMs in the atmospheric transport models to accurately determine the mesoscale atmospheric flows. The terrain heterogeneity alone can explain about 53 to 62% of the surface representation errors over the domain. At the same time, we also note that such a simple parameterization as proposed here might not be adequate to capture the key aspects of the sub-variability when there exists large influence from monsoon circulations.

655 Overall, our results show that the mesoscale transports associated with seasonally reversing monsoon systems and flux variability contribute to fine-scale variations that the current-generation models cannot resolve. By employing a high-resolution model that relies on the resolution of transport and surface fluxes as well as the resolution of the topography, our results provide a baseline for overcoming the shortcomings as mentioned above and accounting for the realistic distribution of atmospheric CO₂.



Code/Data availability

660 The WRF-Chem source code is publicly available at <https://ruc.noaa.gov/wrf/wrf-chem/> (last access: 10 August 2019). The CarbonTracker (CT-2019B) products are available online at <http://carbontracker.noaa.gov> (last access: 21 July 2020, Jacobson et al., 2020). The data from the CarboScope inversion system are available online at <http://www.bgc-jena.mpg.de/CarboScope/> (last access: 20 July 2020, Rödenbeck et al., 2003). The data from the LSCE modelling system used in this study are available at <http://atmosphere.copernicus.eu> (last access: 22 July 2020, Chevallier et al., 2019). The sub-grid variability products based on the WRF-GHG model simulations can be accessed from <https://zenodo.org/record/4781938> (last access: 23 May 2021, Thilakan and Pillai, 2021). The WRF-GHG model CO₂ simulations used for this study are available upon request to the corresponding author, Dhanyalekshmi Pillai (dhanya@iiserb.ac.in, kdhanya@bgc-jena.mpg.de). The EDGAR data used in this study are publicly available at <https://edgar.jrc.ec.europa.eu/> (last access: 15 March 2020, Crippa et al., 2018). The GFAS data are publicly available at <http://apps.ecmwf.int/datasets/data/cams-gfas/> (last access: 15 March 2020, Kaiser et al., 2012). The ERA5 data are available at <https://cds.climate.copernicus.eu/cdsapp#!/home> (last access: 18 March 2020, Hersbach et al., (2020)).

Author Contribution

675 DP designed the study and performed the model simulations. VT performed the analysis and wrote the paper. VT and DP interpreted the results. CG, MG, AR and TAM provided significant input to the interpretation, and the improvement of the paper. All authors discussed the results and commented on the paper.

Competing interests

The authors declare they have no conflict of interest.

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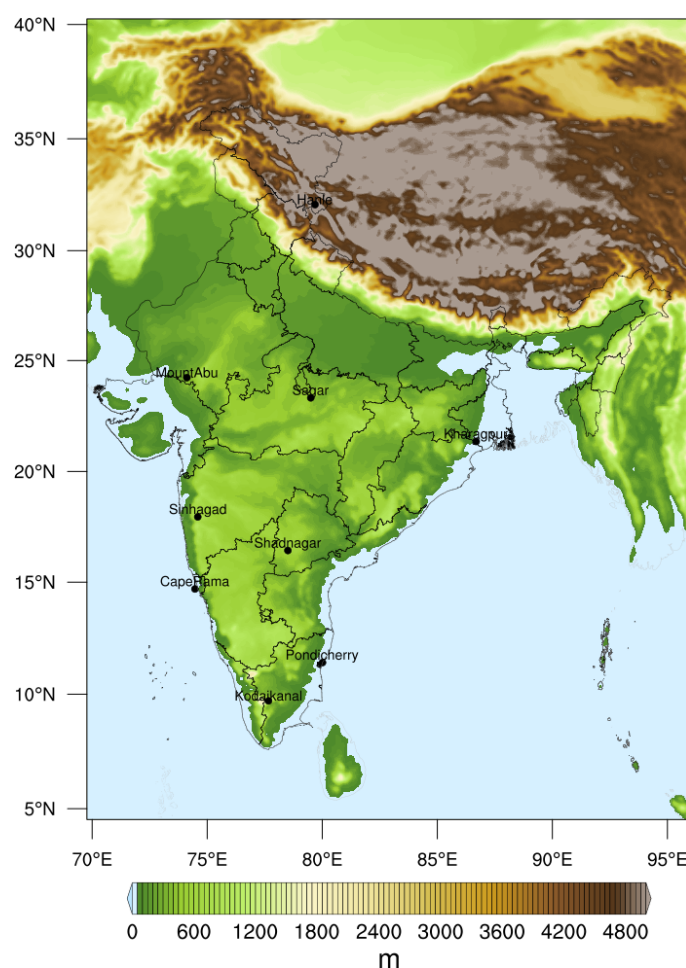


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Figure 1: The WRF-GHG model domain used in this study, showing topography. The CO₂ monitoring sites over India used for the OSSE experiments are marked. Not all these observation stations are currently fully operational. The colour scale is restricted to 5000 m for the better visualization of terrain details over the Indian subcontinent.

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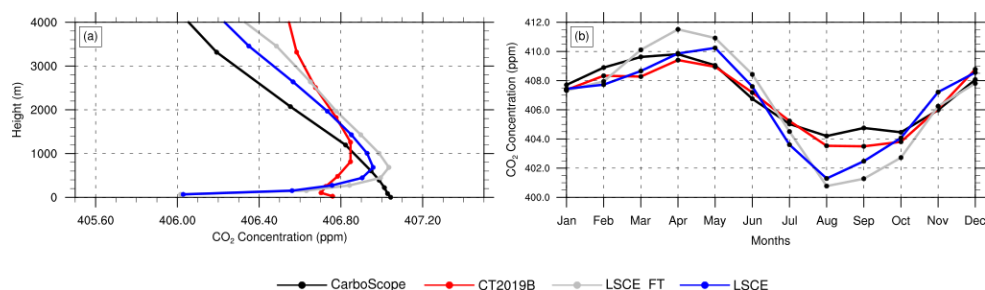


Figure 2: Comparison of global models over the model domain during daytime (11:30 to 16:30 local time) in 2017. a) Annually averaged vertical profiles of CO₂ concentration in the lower troposphere b) Time series of monthly averaged CO₂ concentration at surface (~100 m above surface).

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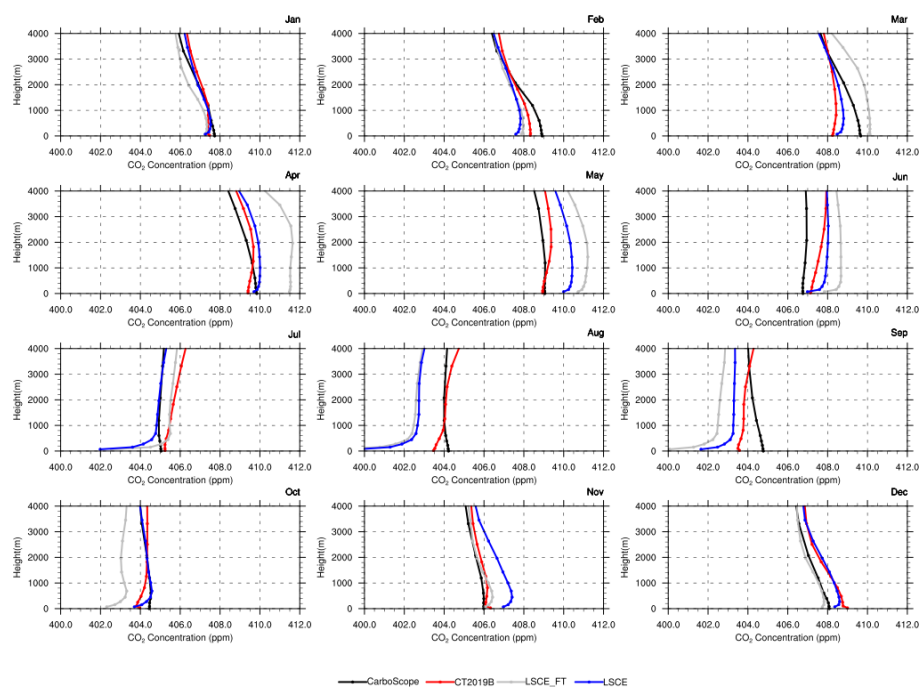


Figure 3: Comparison of average monthly vertical profiles of CO₂ concentration from global atmospheric transport models over the model domain during daytime (11:30 to 16:30 local time) in 2017. Panels show data for respective months as indicated on the top of each panel.

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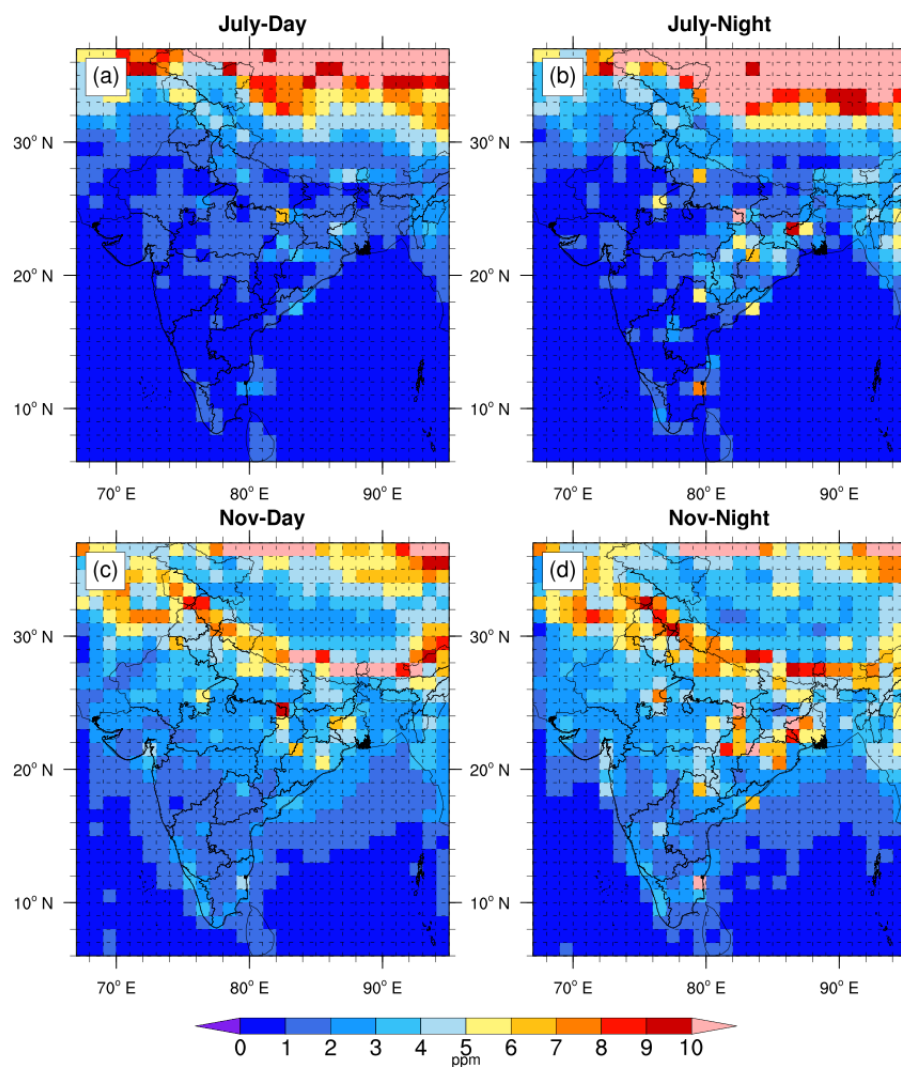
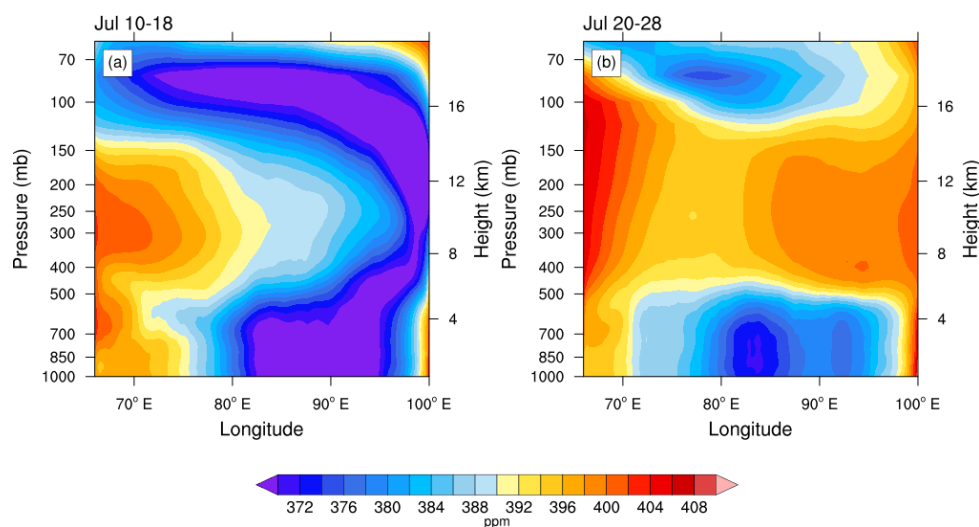


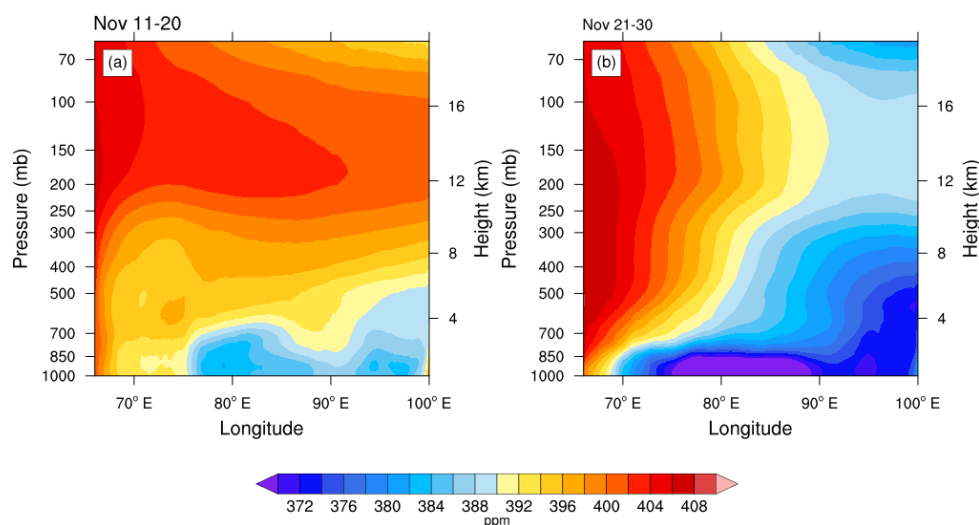
Figure 4: Monthly averaged values of representation error estimated for surface CO_2 concentration (second model level ~ 200 m) during 2017. a) July daytime (11:30 to 16:30 local time) b) July nighttime (23:30 to 4:30 local time). c) November daytime. d) November nighttime.



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Figure 5: Latitudinal averaged vertical cross-section of CO₂ concentration from WRF-GHG simulations during July 2017. a) Vertical cross-section of CO₂ concentration during July 10-18. There are a number of low-pressure systems present over the monsoon-trough region during this period b) Vertical cross-section of CO₂ concentration during July 20-28. Low-pressure systems are not so pronounced during this time. The effect of LLJ and TEJ is visible throughout the whole month.

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Figure 6: Latitudinal averaged vertical cross-section of CO₂ concentration from WRF-GHG simulations during November 2017. a) Vertical cross-section of CO₂ concentration during November 11-20. There are no low-pressure systems present during this period. b) Vertical cross-section of CO₂ concentration during November 21-30. This period is characterized with low-pressure systems in Bay of Bengal and Arabian sea, one of which intensified further and formed into the severe cyclone Ockhi.



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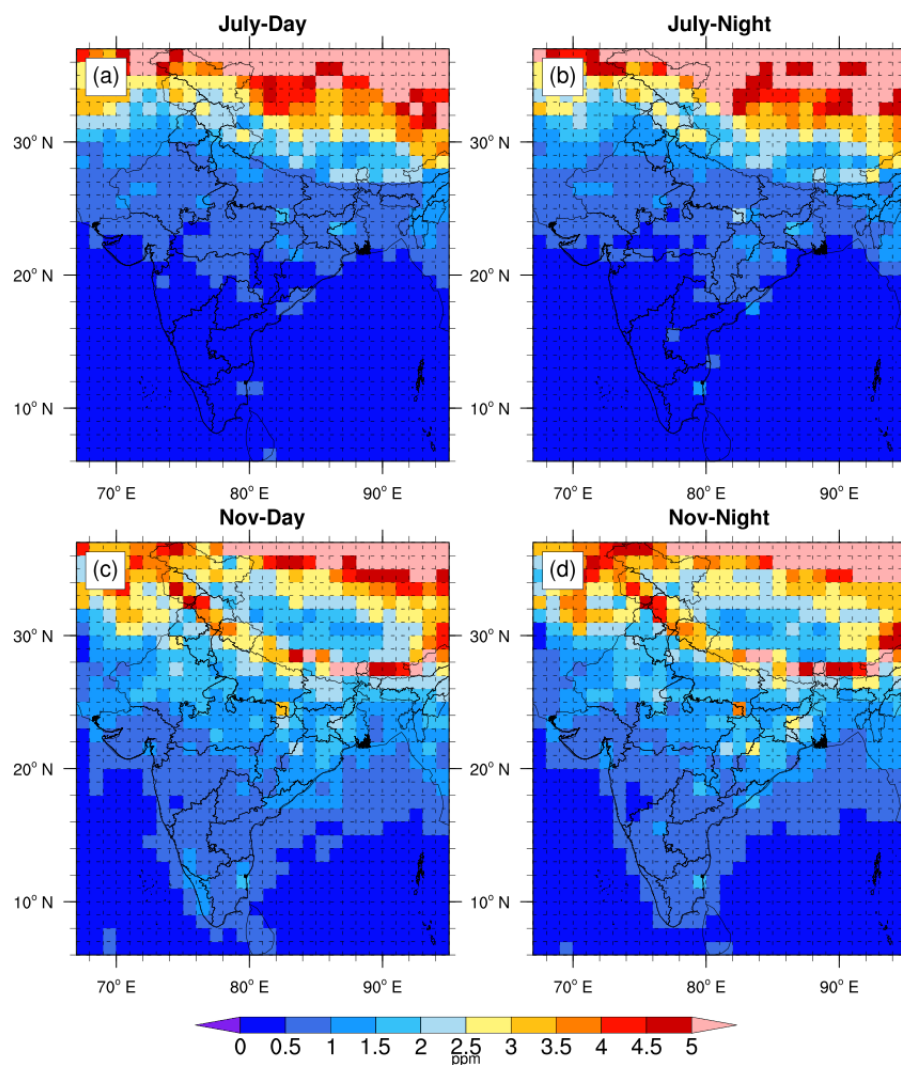


Figure 7: Monthly averaged values of representation error estimated for column averaged CO₂ concentration during 2017. a) July daytime (11:30 to 16:30 local time) b) July nighttime (23:30 to 4:30 local time). c) November daytime. d) November nighttime.

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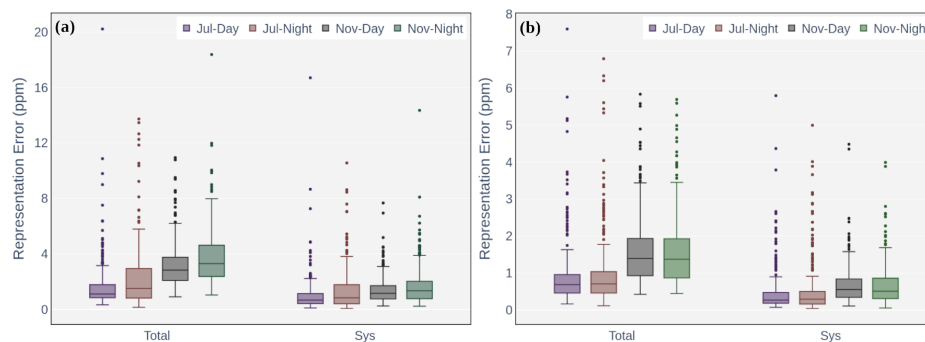
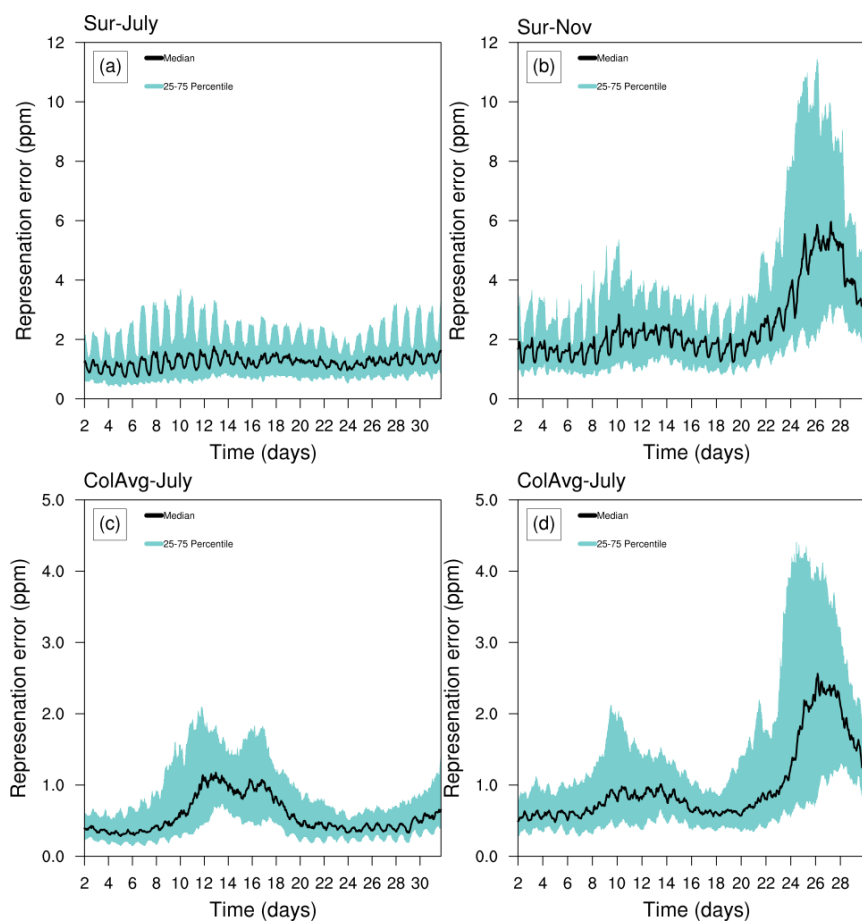


Figure 8: Variability of derived representation error over India. Boxes indicate the central 50%, the bar across the box is the median value, and the whiskers indicate the values between 5 and 95 percentiles. Individual data points shown are the outliers. a) Representation error estimated for the surface CO_2 . b) Representation error estimated for the column averaged CO_2 . The notations, “Total” indicates the total error containing systematic and random errors and “Sys” represents systematic errors only.

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1070 **Figure 9: Intra month variability of representation error over India. a) Variability of surface representation error**
 1075 **during July 2017 b) Variability of surface representation error during November 2017 c) Variability of column**
 1080 **averaged representation error during July 2017 d) Variability of column averaged representation error during**
November 2017. Median values are plotted with black curves and a shaded region indicates 25 to 75 percentiles of
data.



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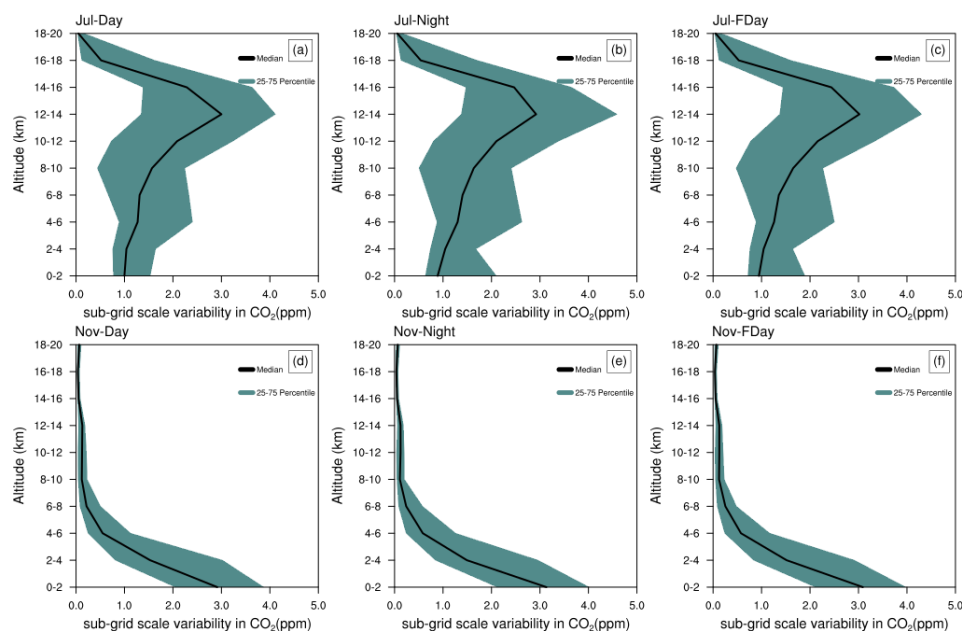


Figure 10: Variability of representation error over India with altitude for July and November 2017. a) July daytime, b) July nighttime, c) July full time, d) November daytime, e) November nighttime, and f) November full time. Median values are plotted with black curves and the shaded region indicates 25 to 75 percentiles of data.

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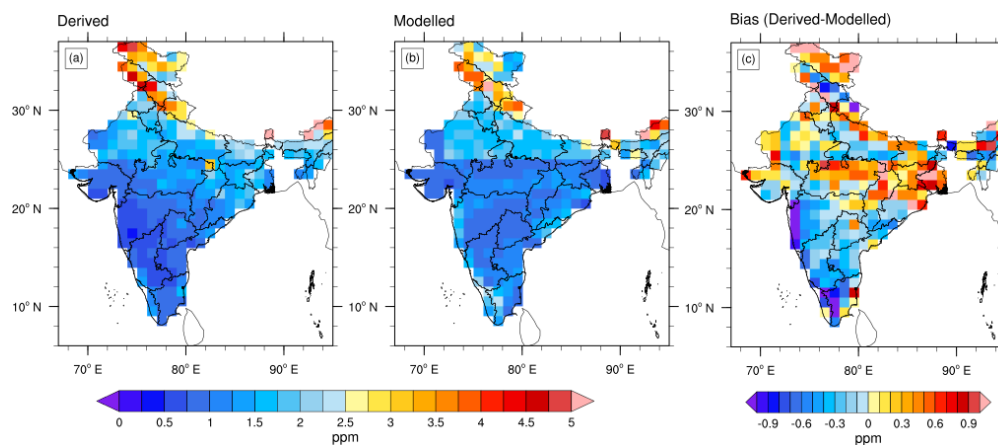


Figure 11: Monthly averaged values of representation error estimated for column averaged CO_2 concentration during daytime (11:30 to 16:30 local time) in 2017. a) Representation error derived from WRF-GHG simulations as explained in Sect. 2.3. b) Representation error calculated from the multivariable linear model as described in Sect. 3.5. c) Bias of multivariable linear model (difference between (a) and (b)).



Table 1: WRF-GHG Model setup

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Domain						
Configuration	Single domain with horizontal resolution of 10 km; 39 vertical levels; 307 × 407 grid points					
Vertical coordinates	Terrain-following hydrostatic pressure vertical coordinates					
Basic equations	non-hydrostatic; compressible					
Grid type	Arakawa-C grid					
Time integration	3rd order Runge-Kutta split-explicit					
Spatial integration	3rd and 5th order differencing for vertical and horizontal advection respectively; both for momentum and scalars					
Timestep	60 s					
Physics schemes						
Radiation	Rapid Radiative Transfer Model (RRTM) for Longwave & Dudhia for shortwave					
Microphysics	WSM 3-classic simple ice scheme					
PBL	YSU					
Surface layer	Monin-Obukhov					
Land-surface	NOAH LSM					
Cumulus	Grell-Devenyi ensemble scheme					
Emission fields						
Flux type	Product	Version	Spatial resolution	Temporal resolution	Source/website	Reference
Anthropogenic	EDGAR	v4.3	10km	Annual	https://edgar.jrc.ec.europa.eu/ http://apps.ecmwf.int/datasets/data/cams-gfas/	Crippa et al., (2018)
Biomass burning	GFAS	v1.2	10km	Daily		Kaiser et al., (2012)
Biospheric	VPRM		Adapted to model	Adapted to model		Mahadevan et al., (2008)
Initial and Lateral Boundary conditions						
Field	Product	Version	Spatial resolution	Temporal resolution	Source/website	Reference
Meteorology	ERA5	n/a	25km	1hour	https://cds.climate.copernicus.eu/cdsapp#!/home	Hersbach et al., (2020)
Tracer	ECMWF /CAMS	gqi	50km	6hour	http://atmosphere.copernicus.eu	Agusti-Panareda et al., (2019)



1130 **Table 2: Specifications of the different global model products used in this study**

Data availability							
Product	Version	Spatial resolution	Vertical levels	Temporal resolution	Source/website		Reference
Cabron Tracker	CT2019 B	3 x 2	25	3 hours	http://carbontracker.noaa.gov		Jacobson et al., (2020)
CarboScope	v2020	5x3.8	19	6hours	http://www.bgc-jena.mpg.de/CarboScope/		Rödenbeck et al., (2003)
LSCE	v18r3	3.7x1.8	39	3hours	http://atmosphere.copernicus.eu		Chevallier et al., (2019)
LSCE	FT18r1	3.7x1.8	39	3hours	http://atmosphere.copernicus.eu		Chevallier et al., (2019)
Data used in the inverse model simulations							
Product	Version	Forward Model	Observation data	Anthropogenic emission fields	Biospheric emission	Fire emission	Oceanic emission
Cabron Tracker	CT2019 B	TM5	Ground based	Miller and ODIAC	CASA	GFED and GFED CMS	OIF and Takahashi et al., (2009)
CarboScope	v2020	TM3	Ground based	EDGAR	LPJ Biosphere Model	CDIAC	SOCAT
LSCE/PyVar	v18r3	LMDz 6A	Ground based	CDIAC and GCP	ORCHIDE E 4.6.9.5	FED and GFAS	Denvil-Sommer et al., (2019) with updates described in Friedlingstein et al., (2019)
LSCE/PyVar	FT18r1	LMDz 6A	Satellite (OCO-2 NASA)	EDGAR, CDIAC and GCP	ORCHIDE E 1.9.5.2	GFED and GFAS	Landschutzer et al., (2018)



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Table 3: Flux uncertainty over India calculated from the OSSE experiments using pseudo-observation network of surface observations. The time Filter indicates the time of the data sampled for estimation of the scaling factors. Full day – 24 hours in each day; Day – 11:30 to 16:30 local time; Night – 23:30 to 4:30 local time. * The fraction of uncertainty to the total NEE.

Month	Time Filter	True flux, Φ_{true} (MtCO ₂ per month)	Flux uncertainty, \bar{S}_{rep} (MtCO ₂ per month) In brackets: fraction of uncertainty* (%)
July	Full Day	-373.31	46.35 (12.4)
July	Day	-373.31	54.40 (14.5)
July	Night	-373.31	60.84 (16.2)
November	Full day	-417.12	28.62 (6.8)
November	Day	-417.12	26.28 (6.3)
November	Night	-417.12	31.41 (7.5)

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