1ComprehensiveQuantificationofHeightDependenceof2Entrainment-MixingbetweenStratiformCloudTopand

3 Environment

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14 Abstract. Different entrainment-mixing processes of turbulence are crucial to processes related to clouds; however, only a few 15 qualitative studies have been concentrated on the vertical distributions of entrainment-mixing mechanisms with low vertical 16 resolutions. To quantitatively study vertical profiles of entrainment-mixing mechanisms with a high resolution, the stratiform 17 clouds observed in the Physics of Stratocumulus Top (POST) project are examined. The unique sawtooth flight pattern allows 18 for an examination of the vertical distributions of entrainment-mixing mechanisms with a 5 m vertical resolution. Relative 19 standard deviation of volume mean radius divided by relative standard deviation of liquid water content is introduced to be a 20 new estimation of microphysical homogeneous mixing degree, to overcome difficulties of determining the adiabatic 21 microphysical properties required in existing measures. The vertical profile of this new measure indicates that entrainment-22 mixing mechanisms become more homogeneous with decreasing altitudes and are consistent with the dynamical measures of 23 Damkohler number and transition scale number. Further analysis shows that the vertical variation of entrainment-mixing 24 mechanisms with decreasing altitudes is due to the increases of turbulent dissipation rate in cloud and relative humidity in 25 droplet-free air, and the decrease of size of droplet-free air. The results offer insights into the theoretical understanding and 26 parameterizations of vertical variation of entrainment-mixing mechanisms.

28 1 Introduction

29 Clouds are identified to be a significant origin of uncertainties in climate research, because of poor simulations of clouds 30 (Bony and Dufresne, 2005; Stephens, 2005; Zheng and Rosenfeld, 2015; Zhao and Garrett, 2015; Wang et al., 2019; Cess et 31 al., 1989; Wang, 2015; Gao et al., 2016; Grabowski, 2006; Morrison, 2015). Entrainment-mixing processes of turbulence have 32 been considered as significant factors for various processes related to clouds (Su et al., 1998; Lasher - trapp et al., 2005; 33 Hoffmann and Feingold, 2019; Xu et al., 2020; Hudson et al., 1997; Liu et al., 2002). Therefore, it is vital to figure out the 34 nature of interaction between clouds and environment and their impacts on cloud droplet properties (Xue and Feingold, 2006). 35 Entrainment-mixing processes are considered to occur primarily near the stratiform cloud top and entrainment-mixing around 36 the stratiform cloud sides is negligible (Wood, 2012; Xu and Xue, 2015).

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38 The question about how entrained air affects cloud microphysics has been debated for a long time. Several conceptual models 39 have been established to study the different entrainment-mixing processes, e.g., entity-type entrainment-mixing (Telford, 1996; 40 Telford and Chai, 1980), vertical circulation entrainment-mixing (Yeom et al., 2017; Yum et al., 2015; Wang et al., 2009) and 41 homogeneous (HM)/inhomogeneous (IM) entrainment-mixing (Baker et al., 1980; Baker et al., 1984). The last one is the most 42 used and studied. During the HM mixing, the time scale for droplets to evaporate completely is larger than the time scale for 43 mixing between entrained air and cloudy air. All droplets are exposed to the same unsaturated state and evaporate concurrently. 44 In this scenario, all droplets' sizes decrease simultaneously, and number concentration also decreases due to the dilution effect 45 of entrained air. While in the IM mixing, mixing time scale is larger than evaporation time scale. Some droplets adjacent to 46 entrained air would evaporate completely to saturate the air, while the other droplets are not affected by the entrainment. In 47 this scenario, number concentration decreases but droplet size remains unchanged. Some observational studies support the 48 extreme IM concept (Burnet and Brenguier, 2007; Lu et al., 2011; Freud et al., 2011; Pawlowska et al., 2000; Haman et al., 49 2007; Freud et al., 2008); while some others indicate that the HM mixing dominates (Gerber et al., 2008; Lu et al., 2013c; 50 Burnet and Brenguier, 2007; Jensen et al., 1985), and still some others find intermediate features fall in between the HM and 51 IM mixing (Lehmann et al., 2009; Lu et al., 2014a; Kumar et al., 2018).

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The vertical variation of entrainment-mixing mechanisms is less studied. For cumulus, Small et al. (2013) and Jarecka et al. (2013) found that a trend existed of entrainment-mixing to be more HM in cloud top, resulted from increasing of cloud droplet radius and turbulence with increasing altitudes. In stratiform clouds, Yum et al. (2015) and Wang et al. (2009) observed positive correlation at middle of cloud and no correlation at cloud top between droplet size and liquid water content. Yum et al. (2015) suggested that entrainment mixing at cloud top region was indeed IM, while during the descent of vertical circulation, the cloud droplets in more diluted parcels would evaporate faster, and observe the generally HM feature at a relatively long depth 59 from cloud top.

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- The above few studies are largely qualitative and based on horizontal flight legs with coarse vertical resolutions. Furthermore, these studies often need to determine adiabatic cloud microphysical properties from observational data, which are full of known and unknown uncertainties (e.g., Jensen et al., 1985; Yum et al., 2015; Lu et al., 2014b; Yeom et al., 2017).
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This study aims to overcome these limitations by examining the data from the field campaign of Physics of Stratocumulus Top (POST) (Hill et al., 2010; Malinowski et al., 2010; Gerber et al., 2010) for the high-resolution vertical variation of entrainmentmixing processes. Four measures of microphysical homogeneous mixing degrees (HMDs) that require the determination of adiabatic cloud properties (Lu et al., 2014b; Lu et al., 2013b; Lu et al., 2014a) are examined and inconsistencies are discussed. A new microphysical measure is proposed to quantify the entrainment-mixing mechanisms to overcome the drawbacks of the existing methods that require cloud adiabatic properties. Physical reasons for the vertical variation of entrainment-mixing mechanisms are analyzed using a comprehensive microphysical-dynamical approach.

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The rest of this study is presented as follows. The POST dataset and the existing methods for calculating microphysical and dynamical measures of HMD are presented in Section 2. Section 3 first shows the analysis of entrainment-mixing mechanisms using the existing microphysical measures and dynamical measures. A new microphysical measure is then introduced to represent entrainment-mixing mechanisms after discussing the potential uncertainties in choosing and determining the adiabatic properties needed for the existing microphysical measures. The key factors affecting vertical variation of entrainment-mixing are examined as well. Section 4 is the concluding remarks.

79 2 Dataset and Methods

80 2.1 Dataset

POST was designed to further the understanding of the physical processes around stratiform cloud top zone (Carman et al., 2012; Gerber et al., 2010; Hill et al., 2010; Malinowski et al., 2010; Ma et al., 2017; Jen-La Plante et al., 2016; Ma et al., 2018; Kumala et al., 2013). During POST campaign, thermodynamic, dynamical, and microphysical properties were measured on board in July and August of 2008 with a total of 17 research flights. Flights were implemented in the vicinity of the coast of Santa Cruz/Monterey, California, US, within 36° to 37°N and123° to 124°W (Gerber et al., 2010; Hill et al., 2010; Malinowski et al., 2010).

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88 The Cloud and Aerosol Spectrometer (CAS) probe measured size distributions in the radius range of 0.29 - 25.5 μm at the

89 frequency of 10 Hz. The data in the radius range of 1.0 - 25.5 µm are used to calculate microphysical properties, i.e., number 90 concentration (n_c) , liquid water content (LWC_c) and volume mean radius (r_{vc}) . The Modified Ultrafast Thermometer (UFT-M) 91 was the temperature probe. Only the flights with good quality temperature data (no reports of "noise", "spike" or "holes in the 92 data" in the data description file) are used. Although the time resolution of temperature data was as high as 1000 Hz (Kumala 93 et al., 2013), 10 Hz data are used here. Humidity was measured by the EDGETECH EG&G Chilled Mirror at 10 Hz. For 94 turbulence measurements, the five-hole gust detector provided by University of California, Irvine (UCI) was used to collect 95 high resolution wind velocities at 40 Hz. We use 10 cm⁻³ of n_c and 0.001 g m⁻³ of LWC_c to be the standard of threshold values 96 to select cloudy samples (Lu et al., 2014b; Deng et al., 2009; Zhang et al., 2011). We define the cloud base as the lowest 97 altitudes where the samples satisfy the previously mentioned cloud criteria. We focus only on the non-drizzling clouds, and 98 the threshold value of drizzle water content in cloud using Cloud Imaging Probe (CIP) measurements (radius larger than 25 99 μm) is 0.005 g m⁻³ (Lu et al., 2011). A total of 4 flights in POST (July 16, August 02, 06, 08, 2008) satisfying the above criteria 100 is selected to examine the vertical variation of entrainment-mixing mechanisms.

101 2.2 Sawtooth Pattern Flights

102 Unlike most aircraft campaigns, the POST flights were designed as sawtooth legs to examine detailly the vertical structures of 103 the stratiform cloud top zone (Figure 1 (a)) (Carman et al., 2012; Gerber et al., 2013; Jen-La Plante et al., 2016). About 60 104 sawtooth legs are contained in each flight (Gerber et al., 2013; Carman et al., 2012). In this way, high-resolution vertical 105 profiles near cloud top can be obtained, which are not available from the conventional sampling along horizontal legs. Because 106 the cloud top altitudes vary spatially, we calculate the average cloud top altitude measured by each sawtooth profile and only 107 the sawtooth legs with cloud tops 30 m above/below the average cloud top are selected. The procedure of altitude stratification 108 is illustrated in Figure 1 (b). We take 5 m as the vertical interval of all sawtooth patterns. All the analyses below are based on 109 the cloud properties averaged over the 5 m vertical intervals and each vertical interval consists of thousands of data. Only the 110 height intervals over which the average droplet-free air sizes (i.e., non-cloudy sample sizes between cloudy samples) are larger 111 than zero are analyzed, which is detailed later in Figure 10. The results are similar when the vertical resolution of all sawtooth 112 patterns is set as 3 m and 7 m, respectively (not shown).

113 2.3 Methods

114 2.3.1 Existing Microphysical Measures of Homogeneous Mixing Degree

Based on the diagram of microphysical mixing, four HMDs have been defined to contain all kinds of entrainment mixing mechanisms. The first three measures are based on the diagram of r_{vc}^3/r_{va}^3 versus n_c/n_a (Lu et al., 2014a; Lu et al., 2013b), as

- shown in Figure 2 (a) and (b). Figure 2 (a) declares the various status during a whole process of entrainment-mixing for defining the first measure (ψ_1). The adiabatic cloud is represented by Point A with the number concentration (n_a) and volume
- mean radius (r_{va}) of adiabatic state. After environmental air is entrained into cloud, the state of cloud approaches Point B, which number concentration is n_h and volume mean radius is r_{va} . Then mixing and evaporation processes occur and cloud state approaches Point C, where number concentration after evaporation is n_c and volume mean radius after evaporation is r_{vc} . The included angle between the line connecting Point B to Point E and the extreme IM mixing line is $\pi/2$, and the included angle between the line connecting Point C and the extreme IM mixing line is β . Then ψ_1 is defined as:

124
$$\psi_1 = \frac{\beta}{\pi/2},\tag{1a}$$

125 where β is

126
$$\beta = \arctan(\frac{r_{vc}^3 / r_{va}^3 - 1}{n_c / n_a - n_h / n_a});$$
(1b)

127 $n_{\rm h} = n_{\rm a} \times \chi$ and χ represents the adiabatic cloud fraction after mixing derived from energy conservation and total water 128 conservation in the isobaric mixing (Lehmann et al., 2009; Gerber et al., 2008; Lu et al., 2012). The second HMD (ψ_2) is 129 defined in view of Figure 1 (b):

130
$$\psi_2 = \frac{1}{2} \left(\frac{n_c - n_i}{n_h - n_i} + \frac{r_{vc}^3 - r_{va}^3}{r_{vh}^3 - r_{va}^3} \right),$$
 (2)

131 where
$$n_{\rm i} = \frac{r_{\rm vc}^3}{r_{\rm va}^3} n_{\rm c}$$
 and (3)

132
$$r_{\rm vh}^3 = \frac{n_{\rm c}}{n_{\rm h}} r_{\rm vc}^3$$
. (4)

Here n_i is the number concentration after extreme IM mixing and r_{vh} is the volume mean radius after HM mixing. The third measure of HMD (ψ_3) is given by

135
$$\psi_{3} = \frac{\ln(n_{c}) - \ln(n_{i})}{\ln(n_{h}) - \ln(n_{i})} = \frac{\ln(r_{v_{c}}^{3}) - \ln(r_{v_{a}}^{3})}{\ln(r_{v_{h}}^{3}) - \ln(r_{v_{a}}^{3})}.$$
(5)

The fourth measure (ψ_4) is defined using mixing diagram of r_{vc}^3/r_{va}^3 versus LWC_c/LWC_a (Lu et al., 2014b), as shown in Figure 2 (c),

138
$$\psi_4 = \frac{1 - r_{vc}^3 / r_{va}^3}{1 - LWC_c / (\chi LWC_a)}.$$
 (6)

139 The meanings of the Points A - E are the same as those in Figures 2 (a) and 2 (b). Four kinds of HMDs are expected to range

140 from 0 to 1, the higher probability of HM mixing corresponds to the larger HMD value.

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142 A new dimensionless HMD (ψ_5) is introduced to quantify the different entrainment-mixing mechanisms:

143
$$\psi_5 = dis(r_{vc}^3)/dis(LWC_c),$$
 (7)

where *dis* represents the relative standard deviation expressed by the ratio of standard deviation to the average value over each level. During entrainment-mixing and evaporation processes, LWC_c always decreases but r_{vc} decreases in the HM mixing and remains constant in the extreme IM mixing. Therefore, the extreme IM mixing corresponds to $\psi_5 = 0$, and the larger the value of ψ_5 is, the more HM the entrainment mixing is. More discussions on ψ_5 are given in Section 3.2.

148 2.3.2 Dynamical Measures of Homogeneous Mixing Degree

The dynamical aspect, i.e., the mixing process between cloud and environment air *vs*. the evaporation process of cloud droplets, is important to distinguish different entrainment-mixing mechanisms (Baker et al., 1980; Baker and Latham, 1979). The mixing time scale divided by evaporation time scale is defined as Damkohler number (*Da*), which is usually used to quantify mixing process is faster or evaporation process is faster and thus to discern the entrainment-mixing mechanisms (Siebert et al., 2006; Burnet and Brenguier, 2007; Andrejczuk et al., 2009),

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$$Da = \frac{\tau_{\text{mix}}}{\tau_{\text{r}}},$$
 (8)

where τ_{mix} and τ_r are turbulent mixing time and microphysical response time of droplets, respectively (Lehmann et al., 2009). A more IM mixing corresponds to a larger *Da*. Three kinds of microphysical time scales, phase relaxation time (τ_{phase}) (Kumar et al., 2013; Kumar et al., 2012), evaporation time (τ_{evap}) (Andrejczuk et al., 2009; Baker et al., 1980; Burnet and Brenguier, 2007), and reaction time (τ_{react}) (Lehmann et al., 2009; Lu et al., 2011; Lu et al., 2013c; Lu et al., 2014b), have been used to represent τ_r . Lu et al. (2018) found that the most appropriate time scale was τ_{evap} if we focus on the changes of number concentration and radius of droplets. The mixing time scale is defined as follows:

161
$$\tau_{\rm mix} \sim (L^3 / \varepsilon)^{1/3}$$
, (9)

where ε is the turbulent dissipation rate calculated from the three dimensional wind velocities (Meischner et al., 2001) (see Appendix A for details), and *L* is the size of droplet-free air calculated with

$$164 L = F \times TAS/f, (10)$$

where droplet-free sample size divided by the sum of cloud and droplet-free sample size is considered as fraction of dropletfree *F* in each vertical interval (e.g., if there are 90 cloud samples and 10 non-cloudy samples, F = 10/(10+90) = 10%); TAS and *f* are the aircraft true air speed (~ 55 m s⁻¹) and sampling frequency (10 Hz), respectively. The size of droplet-free air is used as a proxy for the entrained air parcels' size. In equation (8), the time scale for a droplet of radius r_{va} to completely evaporate (evaporate time) is given by:

170
$$au_{\text{evap}} = -\frac{r_{\text{va}}^2}{2AS_0},$$
 (11)

where S_0 is the supersaturation of the droplet-free air at the corresponding altitude (Yau and Rogers, 1996); *A* is a affected by air temperature and pressure (see Appendix B for details).

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174 Another dynamical measure given by the ratio of L^* to η is transition scale number (N_L) (Lu et al. (2011)):

175
$$N_{\rm L} = \frac{L^*}{\eta},\tag{12}$$

where transition length (L^*) is considered as the corresponding L value when Da = 1 (Lehmann et al., 2009) and is given as follows:

178
$$L^* = \varepsilon^{1/2} \tau_r^{3/2}$$
. (13)

179 In equation (12), η is the Kolmogorov length scale (Wyngaard, 2010), which is given by:

180
$$\eta = \left(\frac{v^3}{\varepsilon}\right)^{1/4},\tag{14}$$

181 where v is the kinematic viscosity (Wyngaard, 2010). A higher probability of HM mixing corresponds to a larger value of N_L .

182 **3 Results**

183 **3.1 Entrainment-Mixing Mechanisms from the Microphysical and Dynamical Perspectives**

184 It has been known that it can be uncertain and even problematic to determine the representative adiabatic values from the 185 observational data needed in calculation of the above-mentioned microphysical measures (Yeom et al., 2017; Jensen et al., 186 1985; Yum et al., 2015). For example, because vertical velocity and concentration of cloud condensation nuclei can change 187 spatially in clouds, n_a and r_{va} change accordingly. Entrainment-mixing in clouds adds difficulties to determine accurate values 188 of r_{va} , n_a and LWC_a. Improper estimation of adiabatic values may violate the theoretical expectation: $n_a \ge n_b \ge n_c \ge n_i$ and $r_{va} \ge n_b \ge n_c \ge n_i$ 189 $r_{\rm v}$, and then cause unrealistic HMDs. Different adiabatic variables have been used in previous studies. For example, the 190 maximum volume mean radius and number concentration are used as proxy values for r_{va} and n_a for each horizontal penetration, 191 respectively (Yeom et al., 2017; Yum et al., 2015); LWC_a is calculated from the adiabatic growth from cloud base, and the

- 192 maximum number concentration of whole flight penetration is considered as n_a (Burnet and Brenguier, 2007; Lehmann et al.,
- 193 2009); n_a is the mean value of top 2% of n_c for each flight and r_{va} is calculated using adiabatic water vapor mixing ratio, 194 adiabatic total water mixing ratio and n_a for a horizontal penetration (Small et al., 2013).
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196 To examine the influence of using different adiabatic properties, we compare ψ_i (i = 1 - 4) calculated with different adiabatic 197 variables (Table 1) at each level near the stratiform cloud tops for the data collected during the four flights. Only the results 198 for the first microphysical measure are shown in Figure 3; the other results are shown in the Supporting Information. In Figure 199 3, LWC_a is based on the adiabatic growth from cloud base, the maximum number concentration at each level is assumed as n_a , 200 and r_{va} is calculated from LWC_a and n_a . In Figure S1, LWC_a is based on the adiabatic growth from cloud base, the maximum 201 volume mean radius at each level is assumed as r_{va} , and n_a is calculated from LWC_a and r_{va} . In Figure S2, the maximum liquid 202 water content at each level is assumed as LWC_a, the maximum number concentration at each level is assumed as n_{a} , and r_{va} is 203 calculated from LWC_a and n_a . In Figure S3, the maximum liquid water content at each level is assumed as LWC_a, the maximum 204 volume mean radius at each level is assumed as $r_{\rm va}$, and $n_{\rm a}$ is calculated from LWC_a and $r_{\rm va}$. In Figure S4, the maximum number 205 concentration at each level is assumed as n_a , the maximum volume mean radius at each level is assumed as r_{va} , and LWC_a is 206 calculated from n_a and r_{va} . According to the definitions, ψ_i (i = 1 - 4) are expected to range from 0 to 1. However, some values 207 of ψ_i (i = 1 - 4) are larger than 1 or smaller than 0 in Figure 3 and Figures S1 – S4, which could be caused by uncertainties in 208 rva, LWCa, na and cloud base (Lu et al., 2014b; Lu et al., 2014a; Lu et al., 2013b; Gerber et al., 2008). Furthermore, these 209 figures suggest different vertical distributions of HMDs for the same flight, suggesting that high sensitivity of the conventional 210 HMDs to the methods for determining the adiabatic values could pose a serious problem as to which figure represents the 211 reality of entrainment-mixing mechanisms.

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213 Since the above analysis from the microphysical perspective does not tell a consistent story about the vertical variation of 214 HMD, Da and $N_{\rm L}$ are examined from the dynamical perspective. Figures 4 (a), (c), (e) and (g) show the height dependence of 215 Da during each of the four flights. It is obvious that Da decreases with decreasing altitudes. Figures 4 (b), (d), (f) and (h) show 216 a significant increasing trend of $N_{\rm L}$ with decreasing altitudes. The method for setting the adiabatic values in Figure 4 is the 217 same as that in Figure 3, i.e., LWC_a is based on the adiabatic growth from cloud base, the maximum number concentration at 218 each level is assumed as $n_{\rm a}$, and $r_{\rm va}$ is calculated from LWC_a and $n_{\rm a}$. Unlike the microphysical measures, vertical variation of 219 Da or N_L are similar when different methods for determining adiabatic values are used (Figures S5 – S8). It is expected that a 220 smaller Da (larger $N_{\rm L}$) represents a larger HMD. The results of Da and $N_{\rm L}$ both suggest more IM mixing closer to cloud top. 221 It is noteworthy that this result is robust, not affected by the methods for obtaining the adiabatic values, and thus should reflect 222 the real height dependence of entrainment-mixing mechanisms.

224 The different vertical distributions of HMDs and the inconsistency between microphysical HMDs and dynamical measures are 225 mainly due to the improper estimations of adiabatic values. For example, during the flight of 16 July in Figure 3, the HMDs 226 decrease with the decreasing altitudes, and most of the HMDs are negative. The negative values do not meet the theoretical 227 expectations and these trends are completely inconsistent with those of dynamical measures. The vertical variations of some 228 important properties of this case are shown in Figure 5. The negative values of HMDs are due to unexpected result of $r_{va} \le r_{vc}$. 229 Under these circumstances, the difference between r_{vc} and r_{va} becomes larger with the decreasing altitudes, corresponding to 230 the decreasing trends of HMDs with the decreasing altitudes. Besides the first method, the other four methods mentioned above 231 also have their own unreasonable points. For example, $r_{va} \le r_{vc}$ exists under the methods 1, 3 and 4; $n_a \le n_c$ exists under the 232 methods 2 and 4; r_{va} does not always increase with the increasing altitudes under the methods 2, 4 and 5 (See figures S9 to 233 S13 for details). Overall, the inconsistency among the microphysical HMDs estimated with different methods to determine the 234 adiabatic variables calls for a new microphysical measure of entrainment-mixing mechanisms.

235 **3.2 New Microphysical Measure**

As discussed in Section 3.1, the existing microphysical measures of HMDs depend on the different adiabatic values to a great extent. In order to avoid this kind of uncertainty, a new dimensionless HMD (ψ_5) in equation (7) is introduced to quantify the different entrainment-mixing mechanisms. To make sure that ψ_5 is applied properly, the correlation between r_{vc}^3 and LWC_c must be positive. If the correlation is negative, IM mixing with subsequent ascent is likely to occur (Lu et al., 2013a; Lehmann et al., 2009; Wang et al., 2009; Siebert et al., 2006; Lasher - trapp et al., 2005). It is worth mentioning that ψ_5 does not require using adiabatic values, and thus can overcome the deficiencies of ψ_i (i = 1 - 4) associated with choosing different adiabatic cloud properties.

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The vertical variation of ψ_5 for the 4 flights are shown in Figure 6. The small value of ψ_5 near the cloud tops shows that entrainment-mixing approaches extreme IM, consistent with conclusions in several previous studies based on the POST data (Gerber et al., 2013; Gerber et al., 2016; Malinowski et al., 2013). The increase of ψ_5 with decreasing altitudes indicates that the trends towards more HM with the decreasing altitudes, consistent with the results of *Da* and *N*_L (Figure 4 and Figures S5 – S8). We also check the relationship between r_{vc}^3 and LWC_c and the two quantities are positively correlated (not shown).

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The relationships between ψ_5 versus Da and N_L of the 4 flights are shown in Figure 7 and are well fitted by the equations used in Luo et al. (2020)

252
$$\psi_5 = a_1 \exp(b_1 D a^{c_1}),$$
 (15)

253
$$\psi_5 = a_2 \exp(b_2 N_L^{c_2}),$$
 (16)

where the parameters a_1 and a_2 are positive; b_1 and b_2 are negative; c_1 is positive and c_2 is negative. The negative correlation of ψ_5 vs Da and positive correlation of ψ_5 vs N_L are evident and in keeping with theoretical arguments, suggesting that a smaller Da or a larger N_L corresponds to a higher ψ_5 . Such relationships further confirm the utility and applicability of ψ_5 in studying entrainment-mixing mechanisms. The correlation coefficients of the linear regression of for ψ_5 vs Da and ψ_5 vs N_L are about 0.66 and 0.60, respectively, suggesting that Da and N_L are basically equivalent for understanding the entrainment-mixing parameterization.

The equivalence of Da and N_L is further supported by the tight negative correlation between Da and N_L (Figure 8). Similar results have been reported in Gao et al. (2018) using numerical simulations, and Desai et al. (2021) based on holographic measurements. However, the underlying reasons are different. Figure 9 shows that L and L^* are negatively correlated, opposite to the positive correlation between L^* and the Taylor microscale in Gao et al. (2018); Taylor microscale is used as L in the calculation of τ_{mix} in equation (9) in Gao et al. (2018). It is easy to derive from equations (8), (9), (11) and (12) that $Da : N_L =$ $L : L^*$, others being equal:

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$$\frac{Da}{N_{\rm L}} = \frac{-2AS_0\eta}{\varepsilon^{1/3}r_{\rm va}^2} \cdot \frac{L}{L^*}$$
(17)

Therefore, as long as L and L^* are nearly linearly correlated, Da and N_L are equivalent. When extreme IM mixing dominates near cloud top, ε is small (Figure 10), which mainly determines small L^* ; L is large near cloud top (Figure 10). Therefore, Land L^* are negatively correlated. The vertical distributions of affecting factors on entrainment-mixing are detailed in the next sub-section.

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273 **3.3 Further analysis of Affecting Factors**

According to the analyses in Sections 3.1 and 3.2, the dynamical and microphysical measures both indicate that entrainmentmixing mechanisms change from IM to HM with decreasing altitudes. Here we provide the physical explanation for such behavior under the framework of HM/IM entrainment-mixing mechanisms, by analyzing the vertical variations of all the variables defining Da and N_L , i.e., ε , relative humidity (RH) and L.

- 280 clouds (Small et al. (2013) and Jarecka et al. (2013)). According to definition of Da (equation (8)) and $N_{\rm L}$ (equation (12)), the
- 281 increase of ε leads to the decrease of Da and increase of N_L, others being equal. Therefore, ε is an important factor to cause Da

²⁷⁹ First, Figures 10 (a), (d), (g) and (j) show that ε increases with decreasing altitudes, which is opposite to that for cumulus

282 to decrease and $N_{\rm L}$ to increase with the decreasing altitudes (Figure 4 and Figures S5 – S8). The clouds were sampled in the 283 vicinity of the coast of Santa Cruz/Monterey, California, therefore, these clouds were well-mixed and coupled, which explains 284 the monotonic decrease of ε with the increasing height (Jones et al., 2011; Shupe et al., 2013). Note that the decoupled 285 clouds should be very common in the downstream regions (Bretherton and Wyant, 1997) and midlatitudes (Zheng et al., 2020). 286 The boundary layer decoupling causes a decrease of turbulent kinetic energy near the cloud base, leading to a local minimum 287 near the cloud base and a maximum in the middle of cloud layer which can be used to infer the profile of ε (Stevens, 2000). 288 This is also demonstrated in the observations by Zheng et al. (2016) who found a significant role of decoupling in weakening 289 the cloud-base updrafts. Therefore, in the future studies of decoupled stratocumulus in other regions, the results about 290 entrainment-mixing mechanisms could be different due to the non-monotonic vertical variation of ε .

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Second, the vertical variation of entrainment-mixing can also be attributed to that of entrained air sizes. Figures 10 (b), (e), (h) and (k) show that *L* decreases significantly with decreasing altitudes, which leads to a decrease of *Da* with decreasing altitudes since *Da* is proportional to τ_{mix} , and thus *L*. The importance of *L* has rarely been studied in previous literatures for height dependence of entrainment-mixing. The decrease of *L* with decreasing altitudes agrees generally with the cascade of breakdown of dry air parcels entrained at the cloud top.

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298 Third, vertical variation of entrained air RH plays a significant part in determining the entrainment-mixing mechanisms. In former literatures (Yeom et al., 2017; Lu et al., 2018), RH is commonly assumed to be constant across multiple different 299 300 altitudes when calculating τ_{evap} using $S_0 = RH - 1$. In fact, RH should not be a constant. We determine RH as the mean RH of 301 droplet-free air in each level. Figures 10 (c), (f), (i) and (l) show that RH increases with decreasing altitudes due to droplet evaporation. According to the definition of Da, Da decreases with the increase of τ_{evap} , and thus decreases with the increase of 302 303 RH (equation (7) and (10)). Equations (10), (11) and (12) show that N_L increases with increasing RH. Both Da and N_L indicate 304 more HM mixing at a lower altitude. These results suggest that the increases of ε and RH and the decrease of L with decreasing 305 altitudes are in keeping with the variation of entrainment-mixing processes, together playing the primary role in determining 306 the vertical distribution of HMD observed.

307

It is noted that, r_{va} also affects Da and N_L through its effect on τ_{evap} . However, r_{va} depends on how adiabatic values are estimated in Section 3.1 (Figure S9 – S14 in the Supporting Information). Therefore, the vertical variation of r_{va} is not analyzed here. No matter which method is used to determine the adiabatic values, the trends of vertical variation of Da and N_L do not change (Section 3.1). The vertical variation of Da and N_L indicates the dominance of the combined effects of ε , RH and L in determining the vertical variation of entrainment-mixing processes from IM towards HM with decreasing altitudes.

314 These results are in keeping with the results drawn in Wang et al. (2009) and Yum et al. (2015) in the sense that a trait of IM 315 mixing is prevalent near cloud top but at mid-levels of clouds a trait of HM mixing becomes dominant, according to the 316 analysis of cloud microphysical relationships at different altitudes of marine stratiform clouds. However, there are big 317 differences in the spatial scale of analysis between our and their studies. We focus on near cloud top regions from cloud top to 318 where droplet-free air patches can still be found, mostly less than 100 m from cloud top (Figure 3). On the other hand, Yum et 319 al. (2015) and Wang et al. (2009) examined mid-levels of stratiform clouds where there remained no droplet-free air patches 320 as well as near cloud top regions. They suggested that the vertical variation of cloud microphysical properties relationships 321 could be caused by vertical circulation of diluted parcels affected by entrainment; the actual mixing near cloud top might have 322 been IM as Da and N_{l} at this level suggested; as these parcels moved down, the droplets evaporated fast, resulting in cloud 323 microphysical relationships that would be explained as a trait of HM mixing.

324 4 Concluding Remarks

The observational data of marine stratiform clouds measured from aircraft during the campaign of Physics of Stratocumulus Top (POST) are used to examine the height dependence of entrainment-mixing mechanisms. The sawtooth penetrations are analyzed to acquire fine information on the vertical structure of entrainment-mixing near stratiform cloud tops, from the microphysical and dynamical perspectives. To ensure high vertical resolution, we take 5 m as one altitude distance bin of all sawtooth patterns for the four flights selected in this study.

330

331 From the microphysical perspective, the traditional homogeneous mixing degrees vary distinctly with the decreasing altitudes 332 due to different methods for obtaining adiabatic values. In order to overcome this difficulty, a new homogeneous mixing degree 333 describing the distributions of scatters in the mixing diagram is introduced to quantify different entrainment-mixing 334 mechanisms. The new homogeneous mixing degree is introduced by relative standard deviation of cubic volume mean radius 335 divided by relative standard deviation of liquid water content. If the new homogeneous mixing degree is larger, the mixing is 336 more likely to be homogeneous. The new measure increases with the decreasing altitudes, i.e., more homogeneous with 337 decreasing altitudes. This new measure is not affected by the methods for obtaining adiabatic values and shed new light on the 338 study of entrainment-mixing mechanisms.

339

From the dynamical perspective, Damkohler number decreases and transition scale number increases with decreasing altitudes. The relationships between the new homogeneous mixing degree *vs*. Damkohler number and transition scale number are negative and positive, respectively, consistent with theoretical expectation. Therefore, both microphysical and dynamical analyses indicate the trends from inhomogeneous mixing to homogeneous mixing when altitude decreases.

The factors underlying the vertical variation of entrainment-mixing mechanisms are examined, including vertical distributions of dissipation rate, size of droplet-free air and relative humidity in droplet-free air. Dissipation rate increases and droplet-free air size decreases with the decreasing altitudes. Therefore, mixing is faster at the lower altitude and homogeneous mixing is more likely to occur. Relative humidity increases with decreasing altitudes, which indicates that droplets are less likely to be completely evaporated at the lower altitude. The combined effects of the three factors determine the entrainment-mixing vertical evolution.

351

352 It is noteworthy that the traditional homogeneous mixing degrees are still useful properties to quantify entrainment-mixing 353 mechanisms, if adiabatic values of microphysical properties are properly determined. The new homogeneous mixing degree 354 defined here is a relative measure of homogeneous mixing degree as deviation from the extremely inhomogeneous mixing line, 355 but does not quantify the amount of homogeneous mixing precisely. The relative dispersion of volume-mean radius and liquid 356 water content increases due to differences in mixing states (Khain et al., 2018) and in-cloud activation of cloud condensation 357 nuclei (Derksen et al., 2009; Khain et al., 2018), which affects the calculation of the new homogeneous mixing degree. As 358 pointed out by Khain et al. (2018), the mixing diagram has limitations to analyze entrainment-mixing mechanisms using in 359 situ observations, due to transient mixing states. However, this new measure still provides an alternative method to quantify 360 entrainment-mixing mechanisms, supported by the independent Damkohler and transition scale numbers. This new method 361 can be applied to other datasets with different cloud droplet size probes (e.g., the Forward Scattering Spectrometer Probe, 362 FSSP), since the new definition is based on theoretical understanding of entrainment-mixing mechanisms, which is not limited 363 to the dataset used here. It would be interesting to apply this method to other stratocumulus and cumulus observations in 364 different climate zones.

365

366 Code and Data Availability

367 The codes can be accessed by contacting Chunsong Lu via <u>luchunsong110@gmail.com.</u> The POST data is available on
 368 <u>https://archive.eol.ucar.edu/projects/post/</u>.

369

370 Author Contributions

371 SG performed the data analysis and manuscript writing. CL proposed the idea, guided this work and modified the 372 manuscript. YL and SSY supervised this work and helped revise the manuscript. JZ and LZ offered helps to the data analysis. ND, YM and SW also contributed to the modification of manuscript.

Competing Interests

376 The authors declare that they have no conflict of interest.

378 Appendix A

379 Turbulent dissipation rate (ε) is calculated by three dimensional wind velocities (Meischner et al., 2001)

380
$$\varepsilon \approx \frac{D_{\rm NN}^{3/2}}{(4.01m)^{3/2}d},$$

382 with $m \approx 0.2(2\pi)^{2/3}$ (Panofsky, 1984). $D_{\rm NN}$ is the local spatial structure function using three wind components and is defined as:

383
$$D_{\rm NN}(t,d) = \frac{1}{3} \{ \frac{8}{7} [u(t) - u(t - \frac{d}{TAS})]^2 + \frac{8}{7} [v(t) - v(t - \frac{d}{TAS})]^2 + [w(t) - w(t - \frac{d}{TAS})]^2 \},$$
(A2)

where three wind components, east, north and vertical, are represented by u, v and w, respectively; TAS is the aircraft true air speed (~55m s⁻¹); t is the time; d is the scale parameter:

$$386 \qquad d = \text{TAS}\Delta t \,. \tag{A3}$$

387 where Δt is the time interval, which is set to 0.1 s.

389 Appendix B

390 The parameter A in equation (10) is

$$A = \frac{1}{\left[\left(\frac{L_{h}}{R_{v}T} - 1\right)\frac{L_{h}\rho_{L}}{KT} + \frac{\rho_{L}R_{v}T}{De_{s}(T)}\right]},$$
(B1)

392 where R_v , L_h , T, K, ρ_L , D, and $e_s(T)$ are water vapor specific gas constant, latent heat, temperature, coefficient of air thermal 393 conductivity coefficient, liquid water density, water vapor diffusion coefficient in air and vapor pressure of saturation, 394 respectively.

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404 **References**

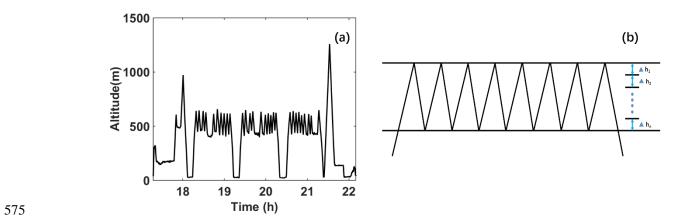
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- 572

Number	Methods
1	LWC _a : calculated from the adiabatic growth from cloud base; n_a : maximum number concentration in each level;
	$r_{\rm va}$: calculated by $r_{\rm va} = \sqrt[3]{\frac{\rm LWC_a}{\frac{4}{3}\pi\rho_{\rm L}n_{\rm a}}}$.
	LWC _a : calculated from the adiabatic growth from cloud base;
2	$r_{\rm va}$: maximum volume mean radius in each level;
	$n_{\rm a}$: calculated by $n_{\rm a} = \frac{\rm LWC_{\rm a}}{\frac{4}{3}\pi\rho r_{\rm va}^3}$.
	LWC _a : maximum liquid water content in each level
3	$n_{\rm a}$: maximum number concentration in each level;
	$r_{\rm va}$: calculated by $r_{\rm va} = \sqrt[3]{\frac{\rm LWC_a}{\frac{4}{3}\pi\rho n_a}}$.
	LWC _a : maximum liquid water content in each level;
	$r_{\rm va}$: maximum volume mean radius in each level;
4	$n_{\rm a}$: calculated by $n_{\rm a} = \frac{\rm LWC_{\rm a}}{\frac{4}{3}\pi\rho r_{\rm va}^3}$.
5	$n_{\rm a}$: maximum number concentration in the interval;
	$r_{\rm va}$: maximum volume mean radius in the interval;
5	LWC _a : calculated by LWC _a = $\frac{4}{3} \pi \rho r_{va}^3 n_a$.



576 Figure 1. (a) Flight track on 16 July 2008. (b) Altitude stratification procedure of the sawtooth patterns, with the mean vertical resolution of

577 5 m such that $\Delta h_1 = \Delta h_2 = \cdots = \Delta h_n = 5$ m.

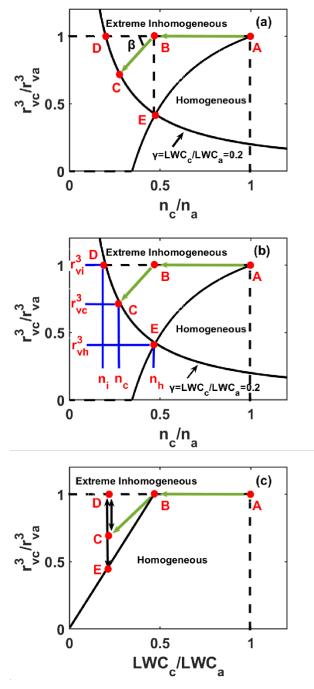
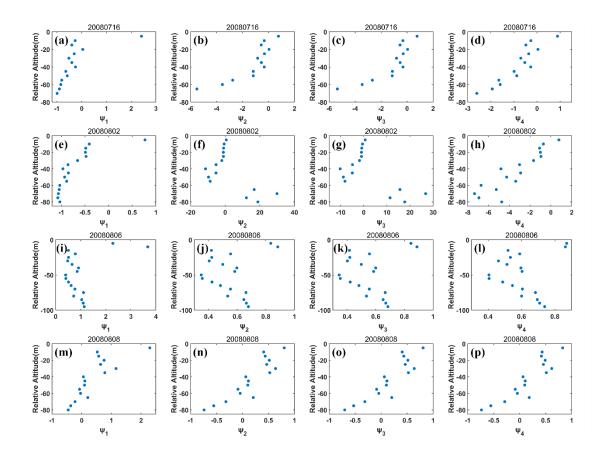


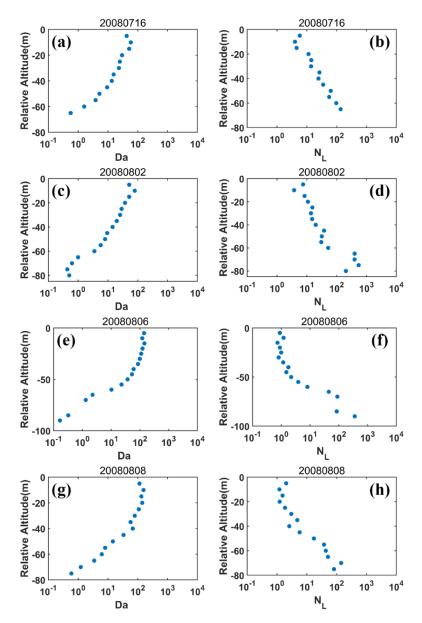


Figure 2. Microphysical diagram interpretating the definition for different homogeneous mixing degrees ((a) ψ_1 ; (b) ψ_2 , ψ_3 ; (c) ψ_4). The Points A and B represent the adiabatic state and the state after entrainment, respectively. If the extreme inhomogeneous mixing process occurs, the cloud state approaches Point D; if the homogeneous mixing process occurs, the cloud state approaches Point E. The actual mixing and evaporation processes are between the two extremes and cloud state approaches Point C. Extreme inhomogeneous mixing process is represented by the horizontal dashed line; homogeneous mixing process is represented by the solid line starting from Point A in (a) and (b), and the solid line starting from Point B in (c). Another black line in (a) and (b) corresponds to contour of $\gamma = 0.2$ defined as the ratio of liquid water content (LWC_c) to its adiabatic value (LWC_a). See text for the meanings of other symbols.



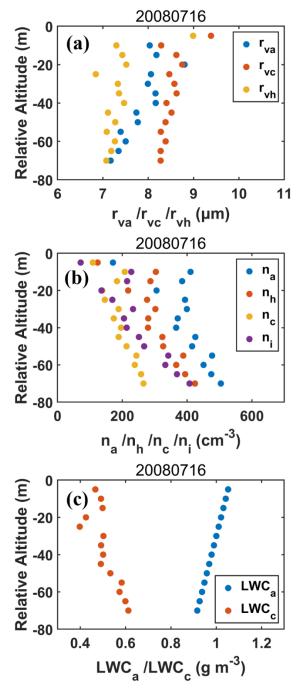
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Figure 3. Height dependence of the first homogeneous mixing degree (ψ_1) on (a) 16 July 2008, (e) 02 August 2008, (i) 06 August 2008 and (m) 08 August 2008; height dependence of the second homogeneous mixing degree (ψ_2) on (b) 16 July 2008, (f) 02 August 2008, (j) 06 August 2008 and (n) 08 August 2008; height dependence of the third homogeneous mixing degree (ψ_3) on (c) 16 July 2008, (g) 02 August 2008, (k) 06 August 2008 and (o) 08 August 2008; and the fourth homogeneous mixing degree (ψ_4) on (d) 16 July 2008, (h) 02 August 2008, (l) 06 August 2008 and (p) 08 August 2008. The relative altitude on the y-axis equal to 0 represents the cloud tops. Adiabatic liquid water content (LWC_a) is obtained by the adiabatic growth from cloud base, adiabatic number concentration (n_a) is assumed to be the maximum volume mean radius at each level, and adiabatic volume mean radius (r_{va}) is calculated with LWC_a and r_{va} .



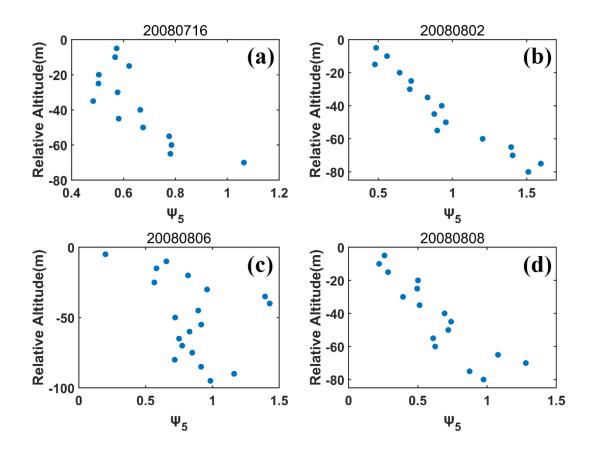
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Figure 4. Height dependence of Damkohler number (Da) on (a) 16 July 2008, (c) 02 August 2008, (e) 06 August 2008 and (g) 08 August 2008; height dependence of transition scale number (N_L) on (b) 16 July 2008, (d) 02 August 2008, (f) 06 August 2008 and (h) 08 August 2008. The relative altitude on the y-axis equal to 0 represents the cloud tops. Adiabatic liquid water content (LWC_a) is obtained by the adiabatic growth from cloud base, adiabatic number concentration (n_a) is assumed to be the maximum volume mean radius at each level, and adiabatic volume mean radius (r_{va}) is calculated with LWC_a and r_{va} .

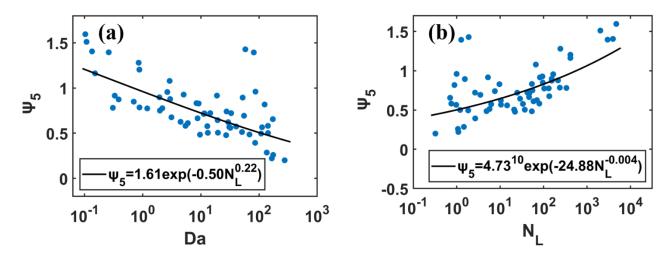


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Figure 5. Height dependence of (a) r_{va} , r_{vc} , r_{vh} , (b) n_a , n_h , n_c , n_i and (c) LWC_a, LWC_c on 16 July 2008. The relative altitude on the y-axis equal to 0 represents the cloud tops. Adiabatic liquid water content (LWC_a) is obtained by the adiabatic growth from cloud base, the maximum number concentration at each level is assumed to be adiabatic number concentration (n_a), and adiabatic volume radius (r_{va}) is calculated with LWC_a and n_a .

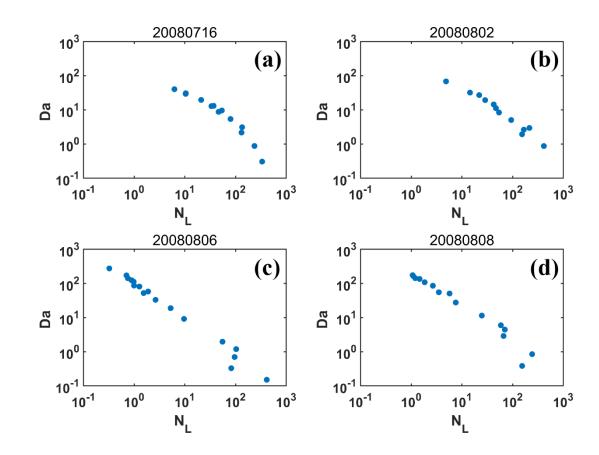


606Figure 6. Height dependence of the newly defined homogeneous mixing degree (ψ_5) on (a) 16 July 2008, (b) 02 August 2008, (c) 06 August6072008 and (d) 08 August 2008. The relative altitude on the y-axis equal to 0 represents the cloud tops.



610 Figure 7. Relationships of the newly defined homogeneous mixing degree (ψ_5) versus (a) Damkohler number (*Da*) and (b) transition scale





612

613 Figure 8. Relationships of Damkohler number (*Da*) versus transition scale number (*N*_L) on (a) 16 July 2008, (b) 02 August 2008, (c) 06

614 August 2008 and (d) 08 August 2008.

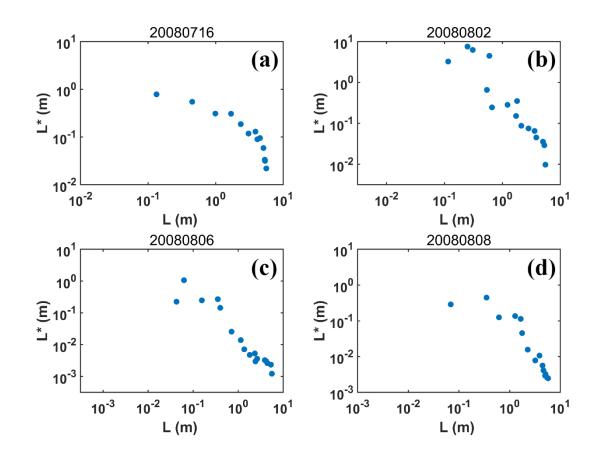


Figure 9. Relationships of transitional scale (L*) versus droplet-free air length (L) on (a) 16 July 2008, (b) 02 August 2008, (c) 06 August
2008 and (d) 08 August 2008.

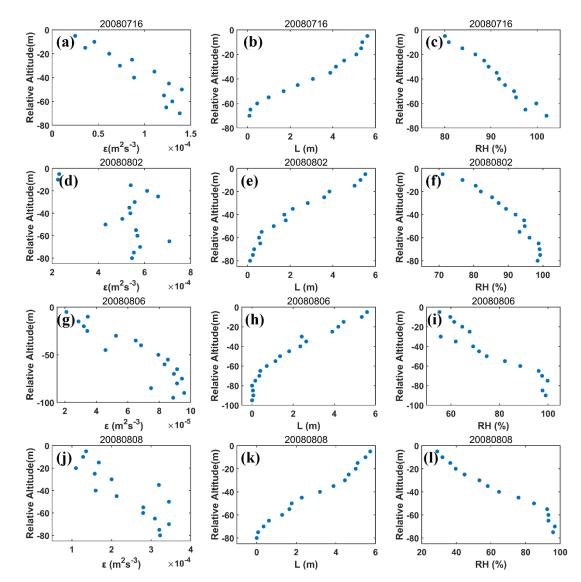


Figure 10. Height dependence of dissipation rate (ɛ) on (a) 16 July 2008, (d) 02 August 2008, (g) 06 August 2008 and (j) 08 August 2008;
height dependence of relative humidity (RH) of droplet-free air on (b) 16 July 2008, (e) 02 August 2008, (h) 06 August 2008 and (k) 08
August 2008; and height dependence of length of droplet-free air (L) on (c) 16 July 2008, (f) 02 August 2008, (i) 06 August 2008 and (l) 08
August 2008. The relative altitude on the y-axis equal to 0 represents the cloud tops.