

Dear Editor, Dear Reviewers,

We would like to thank the Editor and both Reviewers for their effort and their very constructive comments!

Please find enclosed in this response file:

- the point-by-point reply to the Reviewer Comments
- a marked-up manuscript version showing the changes made
- the new supplement that contains a number of single-year plots and parts of one of the former correlation plots

Main changes in the revised manuscript are:

- All figures based on single years have been moved into a supplement
- Sections have been rearranged to first discuss the SAO, and only later its driving by gravity waves
- The different contributions to the total gravity wave drag of the reanalyses are shown and discussed
- We have added more discussion on limitations of absolute momentum fluxes and the proxy for absolute gravity wave drag derived from satellite data

We hope that in the revised manuscript all concerns were adequately addressed.

With best regards,
Manfred Ern

Reply to Reviewer 1

Many thanks to Referee #1 for appreciating our work and the very helpful comments that will significantly help to improve the manuscript!

Please find below our point-by-point reply to the reviewer concerns. Comments by Reviewer #1 are given in red, our reply is given in black, and changes in the manuscript are indicated in blue.

Reply to the Main Concerns by Reviewer # 1:

(Main Concern 1a:) Only the mean annual cycle of the different variables should be shown and should be combined into different figures, according to parameters. The time evolutions could be included as supplemental material.

As recommended, we will move the single-year figures into the supplemental material, and we will merge figures in the main paper.

We will also remove the column showing zonal winds in former Figs. 17 and 18 (the correlation figures) because these figures were quite crowded, too, and the column showing zonal winds is helpful for illustration, but redundant. Further, from former Fig. 17 we will move three of the rows into the Supplement.

(Main Concern 1b) Sections should be rearranged to discuss the SAO first, and the GW driving thereafter.

The sections in the paper will be rearranged, as recommended.

(Main Concern 2) Given the differences between the SAO signal in reanalyses and the SPARC climatology, it seems difficult to believe the "total" GW drag estimations. Therefore, the mean annual cycle of the different terms of the GW drag calculations (i.e. resolved, parameterized and the residual) should be shown to better understand what the different terms are doing in each reanalysis.

Of course, it is not expected that the reanalyses simulate a "perfect" SAO. However, there are features that are common in all datasets: for example, the first SAO period of a year is stronger. Because our knowledge of the SAO and its driving is very poor, estimates of the gravity wave (GW) driving of the SAO from reanalyses will provide important information about the mechanisms that drive the SAO. For this information only relative variations of the GW driving are needed, and not the exact magnitude that might not be very robust.

This will be pointed out more clearly at the beginning of Sect. 5 in the revised manuscript.

Indeed, in the later sections of the paper it turns out that in all reanalyses the GW driving is prevalently eastward in the lower mesosphere, which is in agreement with the satellite observations.

(It should also be kept in mind that, as already mentioned in the paper, the SAO in MERRA-2 is in relatively good agreement with the wind products derived from satellite observations and may therefore be more reliable.)

As explained in the main paper, the total zonal GW drag \overline{X}_{GW} in models consists of three different contributions and can be written as follows:

$$\overline{X}_{GW} = \overline{X}_{res}(k > 20) + \overline{X}_{param} + \overline{X}_{imbalance} \quad (1)$$

with $\overline{X}_{res}(k > 20)$ the GW drag due to model-resolved waves with zonal wavenumbers $k > 20$, \overline{X}_{param} the parameterized zonal GW drag, and $\overline{X}_{imbalance}$ the "residual", or remaining imbalance that is caused, for example, by data assimilation.

As recommended, in a new Sect. 5.2, we will include and discuss in the revised manuscript also the resolved GW drag $\overline{X}_{res}(k > 20)$ for all reanalyses, and the parameterized GW drag \overline{X}_{param} for JRA-55 and MERRA-2. For a further illustration and discussion, the remaining imbalance $\overline{X}_{imbalance}$ can then be calculated for JRA-55 and MERRA-2 as the remaining difference.

For ERA-Interim and ERA-5, parameterized GW drag is not available from the ECMWF MARS archive!

Please note that in the recent paper by Gupta et al. (2021) one of the ERA-5 momentum terms in their paper is named “parameterized drag term (PGWD)”. However, as becomes obvious from their Eq. (1), **their term “PGWD” is not the parameterized GW drag \overline{X}_{param}** , but the sum $\overline{X}_{param} + \overline{X}_{imbalance}$, i.e., the sum of parameterized GW drag and the residual (=remaining imbalance)!

In the following, we will introduce and discuss the different contributions to the “total” GW drag that will be added in the revised paper:

Figure 1 of this reply shows the total gravity wave drag (GWD) \overline{X}_{GW} for the four reanalyses, and Fig. 2 the drag $\overline{X}_{res}(k > 20)$ due to resolved waves of $k > 20$. Figure 3 shows the parameterized GW drag \overline{X}_{param} for JRA-55 and for MERRA-2, and Fig. 4 the remaining imbalance $\overline{X}_{imbalance}$ for JRA-55 and for MERRA-2. For Figs. 1–4 all values are averages over the period 2002–2018 and the latitude band 10S–10N.

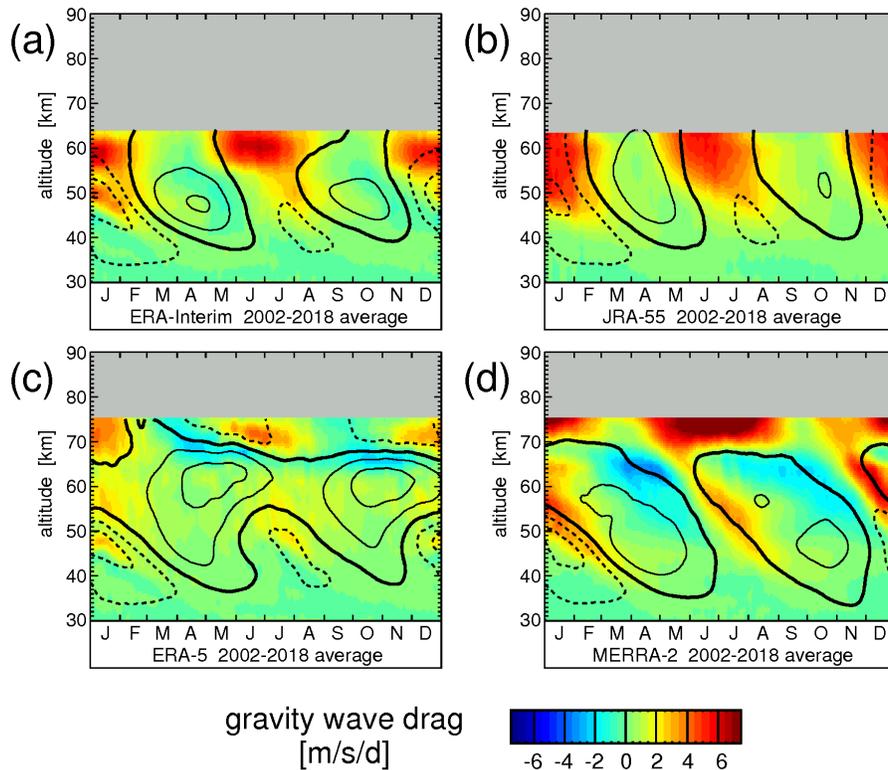


Figure 1: Total zonal GW drag \overline{X}_{GW} for (a) ERA-Interim, (b) JRA-55, (c) ERA-5, and (d) MERRA-2. Overplotted are contour lines of the corresponding zonal average zonal winds for the respective reanalysis dataset. Contour line interval is 20 m/s. The zero wind line is highlighted in bold solid, and westward (eastward) winds are indicated by dashed (solid) contour lines.

As can be seen from Figs. 1 and 2 of this reply, the resolved GW drag is negligible in ERA-Interim, JRA-55, and MERRA-2. (Please note that in Fig. 1 the range of the color scale is

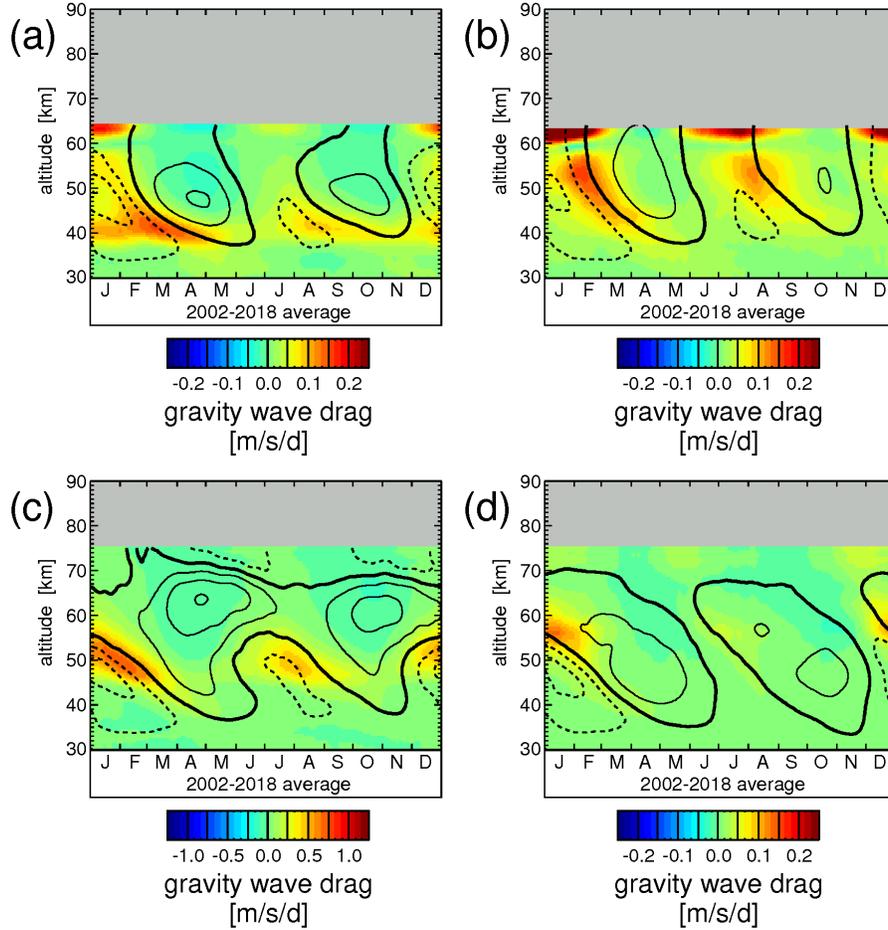


Figure 2: Resolved GW drag $\bar{X}_{res}(k > 20)$ for (a) ERA-Interim, (b) JRA-55, (c) ERA-5, and (d) MERRA-2. Overplotted are contour lines of the corresponding zonal average zonal winds for the respective reanalysis dataset. Contour line interval is 20 m/s. The zero wind line is highlighted in bold solid, and westward (eastward) winds are indicated by dashed (solid) contour lines.

± 7.5 m/s/d, while it is only ± 0.25 m/s/d in Fig. 2a, 2b, and 2d, and only ± 1.25 m/s/d in Fig. 2c.) Only for ERA-5 below 55 km $\bar{X}_{res}(k > 20)$ sometimes contributes as much as about 50% to \bar{X}_{GW} . In both \bar{X}_{GW} and $\bar{X}_{res}(k > 20)$ eastward GW drag is stronger than westward GW drag in the upper stratosphere and lower mesosphere, which is a consequence of the QBO wave filtering in the stratosphere below.

As can be seen from Fig. 3a, the parameterized GW drag \bar{X}_{param} is closely linked with the background wind and opposite to it. This is expected because JRA-55 does not have an explicit nonorographic GW parameterization and uses only Rayleigh friction at upper levels. A similar distribution would be expected for ERA-Interim, because, similar as JRA-55, ERA-Interim uses Rayleigh friction at upper levels and does not have a nonorographic GW parameterization.

Comparing Fig. 1d and Fig. 3b, it is evident that for MERRA-2 in the whole altitude range \bar{X}_{GW} and \bar{X}_{param} are almost the same.

As can be seen from Fig. 4a, for JRA-55, above 40 km the remaining imbalance is strongly positive. This likely indicates that a really large positive assimilation increment is needed to compensate the unrealistic effect of Rayleigh friction, and to keep the model temperature and winds in agreement with assimilated observations. The situation should be similar for ERA-Interim.

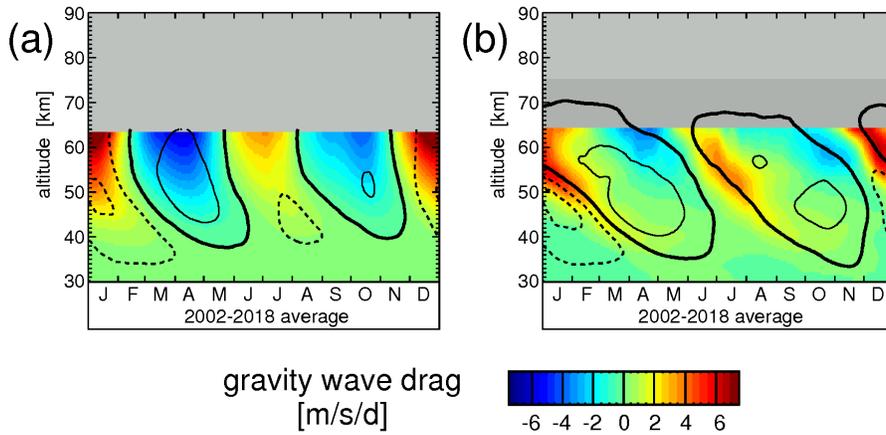


Figure 3: Parameterized GW drag \bar{X}_{param} for (a) JRA-55, and (b) MERRA-2. Please note that from the GES-DISC archive MERRA-2 parameterized GW drag is not available for the whole altitude range. Overplotted are contour lines of the corresponding zonal average zonal winds for the respective reanalysis dataset. Contour line interval is 20 m/s. The zero wind line is highlighted in bold solid, and westward (eastward) winds are indicated by dashed (solid) contour lines.

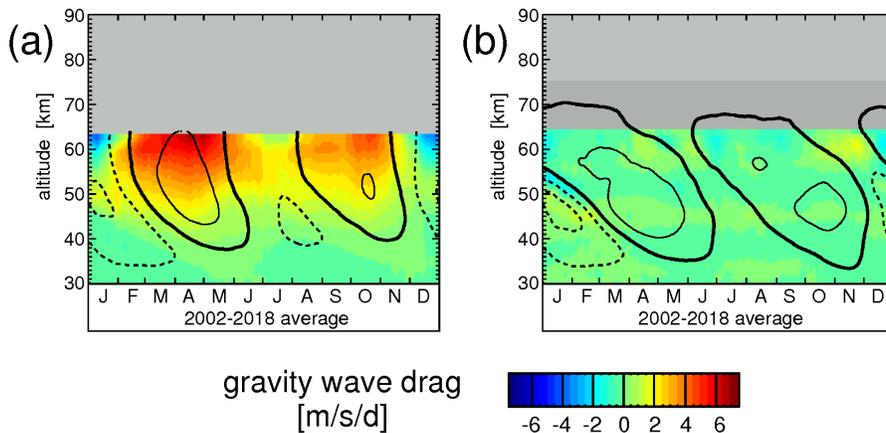


Figure 4: Remaining imbalance $\bar{X}_{imbalance}$ for (a) JRA-55, and (b) MERRA-2. Overplotted are contour lines of the corresponding zonal average zonal winds for the respective reanalysis dataset. Contour line interval is 20 m/s. The zero wind line is highlighted in bold solid, and westward (eastward) winds are indicated by dashed (solid) contour lines.

For MERRA-2, $\bar{X}_{imbalance}$ (Fig. 4b) is close to zero. Apparently, in the tropics, the nonorographic GW drag scheme of MERRA-2 has been tuned in a way to minimize the assimilation increment caused by the assimilation of MLS and other data (see also Molod et al., 2005). This should be the reason why MERRA-2 simulates a reasonable SAO even in the years when MLS data were still not available (in the period prior to August 2004).

Overall, our results show that there are differences between the different reanalyses that reflect the different stages of model development. In particular, our results demonstrate that the use of a nonorographic gravity wave parameterization can be very useful because it can be tuned in a way to produce more realistic results (as was seen for MERRA-2). Even though there are strong differences in the model setups, there are similarities of the total gravity wave drag, particularly in the stratopause region (total GW drag is predominately eastward).

References:

Gupta, A., Birner, T., Dornbrack, A., and Polichtchouk, I.: Importance of gravity wave forcing for springtime southern polar vortex breakdown as revealed by ERA5, *Geophysical Research Letters*, 48, e2021GL092762, <https://doi.org/10.1029/2021GL092762>, 2021.

Molod, A., Takacs, L., Suarez, M., and Bacmeister, J.: Development of the GEOS-5 atmospheric general circulation model: evolution from MERRA to MERRA2, *Geosci. Model Dev.*, 8, 1339-1356, doi:10.5194/gmd-8-1339-2015, 2015.

(Main Concern 3a) Limitations of the momentum flux calculations from SABER should be discussed in more detail, in particular the effect of the trajectory of the satellite being perpendicular to the average GW wavenumber vector.

As recommended, we will add more discussion about the shortcoming of using SABER along-track GW horizontal wavenumbers, instead of “true” GW horizontal wavenumbers.

Generally, the use of along-track GW horizontal wavenumbers as a proxy for the true GW horizontal wavenumbers will lead to a low-bias of SABER momentum fluxes (the momentum flux is proportional to the horizontal wavenumber) because the along-track GW horizontal wavenumber will always underestimate the true horizontal wavenumber.

The AIRS satellite instrument has a similar orbit geometry. Because AIRS provides 3D temperature observations, it is possible to determine from AIRS observations true GW horizontal wavenumbers, as well as along-track GW horizontal wavenumbers. This opportunity has been taken by Ern et al. (2017) to compare true and along-track GW horizontal wavenumbers: AIRS observations indicate an underestimation of the along-track wavenumber (corresponding to an underestimation of momentum fluxes) by a factor between 1.5 and somewhat above 2.

In addition, for SABER there will be aliasing effects (undersampling of observed GWs) and effects of the instrument sensitivity function of limb sounding satellite instruments (cf. Ern et al., 2018), which should both lead to an even stronger underestimation of GW momentum fluxes. Therefore the error of SABER GW momentum fluxes should be at least a factor of two, and momentum fluxes are likely strongly underestimated.

This detailed discussion will be included in the revised manuscript in the newly introduced Sect. 6.1.1.

References:

Ern, M., Hoffmann, L., and Preusse, P.: Directional gravity wave momentum fluxes in the stratosphere derived from high-resolution AIRS temperature data, *Geophys. Res. Lett.*, 44, 475-485, doi:10.1002/2016GL072007, 2017.

Ern, M., Trinh, Q. T., Preusse, P., Gille, J. C., Mlynczak, M. G., Russell III, J. M., and Riese, M.: GRACILE: A comprehensive climatology of atmospheric gravity wave parameters based on satellite limb soundings, *Earth Syst. Sci. Data*, 10, 857-892, doi:10.5194/essd-10-857-2018, 2018.

(Main Concern 3b) The expression SABER “absolute GW drag” should be avoided. For example, the expression “vertical derivative of the absolute momentum flux” could be used, instead.

The reviewer is correct that only under certain conditions the vertical gradient of GW momentum flux can be used to calculate a proxy for absolute net gravity wave drag. However, if these conditions are met, convincing results were obtained in a number of previous studies. This is why, for convenience, we used the expression “absolute gravity wave drag” in the paper.

The problem is that the absolute GW drag proxy is not simply the vertical gradient of absolute GW momentum flux, but it is also normalized by $-1/\varrho$, with ϱ the background density. This makes it difficult to find a short expression for the absolute GW drag proxy.

Therefore, in order to avoid the impression that the vertical gradient of GW momentum flux would always give reliable results, we will introduce an abbreviation which will make the reader check how this proxy is introduced, and what are its limitations:

“SABER MFz-proxy-|GWD|”

To make sure that this introduction is not easily overread, former Sect. 6.1 will be split into two subsections, Sect. 6.1.1 addressing SABER absolute momentum fluxes and its limitations (see **Main Concern 3a**), and Sect. 6.1.2 addressing the SABER GW drag proxy. In Sect. 6.1.2 we will also add more discussion on the limitations of the SABER GW drag proxy. In addition, we will rearrange the final part of the “Summary and Discussion” section to bring out more clearly the implications of a likely low bias in the SABER GW drag proxy.

Reply to the Minor Comments by Reviewer # 1:

(Minor Comment 1) lines 578-585. Could there be an effect of GWs with zonal momentum flux being very few at these high altitudes due to critical level filtering by the QBO and the SSAO?

Thank you very much for this comment!

Of course, GW filtering by the QBO and SSAO will strongly reduce GW momentum fluxes in the tropical mesopause region. This may be one of the reasons why the mesopause SAO (MSAO) occurs only in a narrow layer.

This will be mentioned in the revised paper in Sect. 6.3.3.

(Minor Comment 2) lines 595. Normalized SABER GW drag is the same as GW drag anomalies in Fig. 14?

In order to avoid confusion, the expression “anomaly” will no longer be used in the revised paper.

(Minor Comment 3) Fig. 17, line 598. Why not showing the correlation over the whole period of study, instead of the correlation of the multiyear mean annual cycle? What would be the difference between the two, and its interpretation?

Given the strong interannual variability of the SAO, it is most important that the correlation holds for the majority of single years. This is why the single-year correlations are shown in our paper. The average year is just shown to illustrate that the correlation even holds for the average year — even if the average year might be affected by strong outlier-years, or compensation effects. Correlations over the whole period could also be affected by strong outliers, but in a different way than the average year.

For completeness, we will show the correlation over the whole dataset as an additional column. It turns out that these additional columns give results which are in most cases very similar to those of the average years, or an average-by-eye over the single years.

(Minor Comment 4) Lines 734-743. What is the explanation of a high correlation between the so-called (SABER) absolute GW drag (see main comment #3) and the zonal wind speed, if saturation of GWs due to decrease in density is the proposed mechanism?

There are at least two situations when it makes sense to use SABER MFz-proxy-|GWD| as a proxy for absolute net GW drag:

(1) The GW spectrum is dominated by slow and moderate phase speeds opposite to the background wind:

A layer of (initial) wind shear reducing the wind speed will also reduce the intrinsic phase speed of the GWs dominating the spectrum and bring them closer to saturation. This will lead to a stronger dissipation of those waves and thereby lead to a strengthening and downward propagation of the wind shear layers and wind bands. This effect is seen for the QBO and its wave-driven downward propagation of eastward and westward wind bands. In the middle and lower mesosphere, this effect is also seen for the SAO and its downward propagating eastward wind bands, but only less pronounced for the westward wind bands because GWs of westward phase speeds are weaker due to wind filtering by the asymmetric QBO winds in the stratosphere.

For this mechanism, one would expect correlation between SABER MFz-proxy-|GWD| and zonal wind absolute vertical gradients.

(2) The GW spectrum is dominated by fast phase speed GWs with a directional preference. Minor variations of the background wind will have only little effect on the GW phase speeds

and thus the GW saturation amplitudes. Due to the decrease of atmospheric density with altitude, GW amplitudes will grow exponentially to conserve momentum flux while propagating upward. At some point, however, these GWs will saturate and exert drag on the background flow. As these GWs are not much influenced by the background wind and its variation, the saturation altitude (the altitude where the waves exert their drag) will not be as closely tied to a wind shear zone as for situation (1), but can lead to a reversal and strengthening of the wind by inducing a *temporal wind tendency* (and not to a strengthening of the vertical wind shear and eventually to a downward propagation of the shear zone). The temporal wind tendency will lead to a wind reversal and wind strengthening at the same altitude where the drag is exerted.

Therefore, enhanced GW drag should be observed at the same altitude as the reversed wind jet and lead to a correlation between SABER MFz-proxy-|GWD| and (absolute) wind speed. Situation (2) should match the conditions for the region of the MSAO around 80km altitude and may explain why there is no strong downward propagation of MSAO eastward and westward wind phases.

Case (1) is already discussed in-depth in the paper. However, the reviewer is correct that the discussion of Case (2) was still not very clear. Therefore, we will include the above discussion of Case (2) at the end of Sect. 7.2.2 in the revised manuscript.

(Minor Comment 5) In the same spirit, how can ERA-5 have a realistic GW driving of the SAO if the SAO in ERA-5 is not realistic (section 8.4)?

We do not think that the GW driving of the SAO in ERA-5 is fully realistic:

As already mentioned in Sect. 8.4, in ERA-5 the SAO and its gravity wave driving in the upper stratosphere to middle mesosphere is not considered to be realistic, because there are overly strong eastward wind jets.

At even higher altitudes, the nonorographic GW drag scheme in ERA5 seems to be able to induce a mesopause SAO (MSAO). Even for this altitude range, we find that the characteristics of ERA5 GW drag related to the MSAO show differences to the SABER observations. There are two possible reasons for this: First, the poor representation of the SAO in the lower and middle mesosphere in ERA5 will lead to an incorrect filtering of the GW spectrum, and thus to a not fully realistic forcing of the MSAO. Second, the GW spectrum may be incorrect already at the source level. This means that also the forcing of the MSAO in ERA5 might not be really physically sound.

Obviously, the reviewer comment addresses the question whether the ERA5 gravity wave driving of the MSAO could still be realistic.

This will be addressed at the end of Sect. 8.4 by stating more clearly that differences to SABER observations hint at an underrepresentation of high phase speed GWs in ERA-5, i.e., not all physical mechanisms that lead to the formation of the MSAO are correctly represented in ERA-5. In addition, we mention that the unrealistic SAO at lower altitudes can lead to an unrealistic wind filtering of the gravity wave spectrum, which can also affect the simulation of the MSAO.

(Minor Comment 6) Lines 771-773. I do not understand what the authors mean here. Since MERRA-2 assimilates MLS observations, the driving of the SAO in MERRA-2 at 45-70km is likely the result of this process. But this does not mean that the GW driving of the SAO in MERRA-2 is realistic.

As is indicated in Figs. 1–4 of this reply, the nonorographic GW drag scheme in MERRA-2 was tuned in a way to minimize the assimilation increment due to MLS observations. This means that the SAO in MERRA-2 is mainly a result of the tuned nonorographic GW drag scheme, and might therefore be better also because of more realistic GW drag. Please note

that the SAO in MERRA-2 is generally reasonable — even before 2004 when no MLS data are available and the model is relatively unconstrained in the middle mesosphere. Further, the qualitative agreement between the SABER and MERRA-2 correlations seems to indicate that — at least to some extent — the physical mechanisms of the GW driving of the SAO are realistically simulated by the MERRA-2 nonorographic GW drag scheme.

This additional discussion will be included in the revised paper in Sect. 8.3.

In addition, we will address the four technical comments — thank you very much for finding these inaccuracies!

Reply to Reviewer 2

We would like to thank Referee #2 for appreciating our efforts and for the very helpful comments and suggestions that will definitely improve the manuscript!

Please find below our point-by-point reply to the reviewer concerns. Comments by Reviewer #2 are given in red, our reply is given in black, and changes in the manuscript are indicated in blue.

Reply to the Main Concerns by Reviewer # 2:

(Main Concern 1a:) I.270-272 It is unclear whether a purely zonal approach of assuming $k > 20$ is adequate to extract model-resolved GWs. This would only be the case if zonal propagation of GWs is dominant in the tropics. Otherwise, a more sophisticated approach as proposed by Watanabe et al., 2008, or Becker et al., 2018 would be needed. The contribution of resolved GWs should be shown for more information.

Of course, some care has to be taken whether the major part of the model-inherent gravity wave (GW) drag is from model-resolved GWs, and whether methods as suggested by Reviewer 2 should be applied.

As suggested, we will include the following two references in the revised manuscript as a guidance for readers who want to analyze model-resolved GWs in detail:

Watanabe, S., Kawatani, Y., Tomikawa, Y., Miyazaki, K., Takahashi, M., and Sato, K.: General aspects of a T213L256 middle atmosphere general circulation model, *J. Geophys. Res.*, 113, D12110, doi:10.1029/2008JD010026, 2008.

Becker, E., and Vadas, S. L.: Secondary gravity waves in the winter mesosphere: Results from a high-resolution global circulation model, *J. Geophys. Res.: Atmospheres*, 123, 2605-2627, <https://doi.org/10.1002/2017JD027460>, 2018.

However, there are three reasons why we think that a more sophisticated approach is not required in our paper:

- The GW drag of model-resolved waves with $k > 21$ is only a minor part of the GW drag proxy derived in our paper. This is the case because the spatial resolution of the reanalyses is relatively coarse. As a consequence, they resolve only a limited part of the GW spectrum. This can be seen below from Figs. 5 and 6 which show our estimates of the total and the resolved GW drag. Uncertainties in the resolved GW drag will therefore not much affect our estimates of total GW drag. Introducing a limit of $k > 21$ is somewhat arbitrary, anyhow.
- In the tropics, zonal propagation of GWs should be dominant because zonal winds are usually stronger than meridional winds, and GWs propagating opposite to the background wind can attain larger amplitudes because the intrinsic phase speed of these waves, and thus their saturation amplitudes, are increased. Therefore, the purely zonal analysis should be justified even for the part of the wave spectrum that is resolved in the models (in the tropics, many other studies also use this kind of zonal approach — for example, even the KANTO model group did so in the follow-up paper Kawatani et al., 2010, with S. Watanabe as one of the coauthors).
- The validity of a zonal-only approach is also supported by the fact that at most altitudes all our GW drag proxies (reanalyses and SABER) show strong correlation with either the zonal wind, or its vertical gradient.

These three points will be mentioned in the revised manuscript in the new Sect. 5.2.1, In addition, we will include in the paper — among other new figures — the figure showing the resolved GW drag for the four reanalyses.

A brief discussion of Figs. 5 and 6:

As explained in the main paper, the total zonal GW drag \overline{X}_{GW} in models consists of three different contributions and can be written as follows:

$$\overline{X}_{GW} = \overline{X}_{res}(k > 20) + \overline{X}_{param} + \overline{X}_{imbalance} \quad (2)$$

with $\overline{X}_{res}(k > 20)$ the GW drag due to model-resolved waves with zonal wavenumbers $k > 20$, \overline{X}_{param} the parameterized zonal GW drag, and $\overline{X}_{imbalance}$ the “residual”, or remaining imbalance that is caused, for example, by data assimilation.

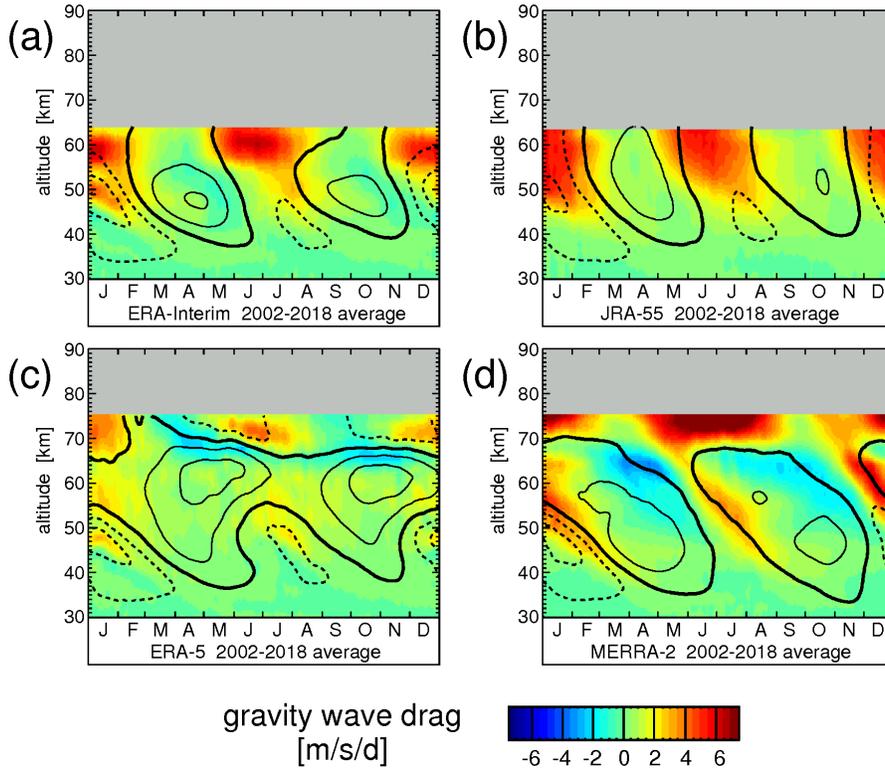


Figure 5: Total zonal GW drag \overline{X}_{GW} for (a) ERA-Interim, (b) JRA-55, (c) ERA-5, and (d) MERRA-2. Overplotted are contour lines of the corresponding zonal average zonal winds for the respective reanalysis dataset. Contour line interval is 20 m/s. The zero wind line is highlighted in bold solid, and westward (eastward) winds are indicated by dashed (solid) contour lines.

As can be seen from Figs. 5 and 6 of this reply, the resolved GW drag is negligible in ERA-Interim, JRA-55, and MERRA-2. (Please note that in Fig. 5 the range of the color scale is ± 7.5 m/s/d, while it is only ± 0.25 m/s/d in Fig. 6a, 6b, and 6d, and only ± 1.25 m/s/d in Fig. 6c.) Only for ERA-5 below 55 km $\overline{X}_{res}(k > 20)$ sometimes contributes as much as about 50% to \overline{X}_{GW} . In both \overline{X}_{GW} and $\overline{X}_{res}(k > 20)$ eastward GW drag is stronger than westward GW drag in the upper stratosphere and lower mesosphere, which is a consequence of the QBO wave filtering in the stratosphere below.

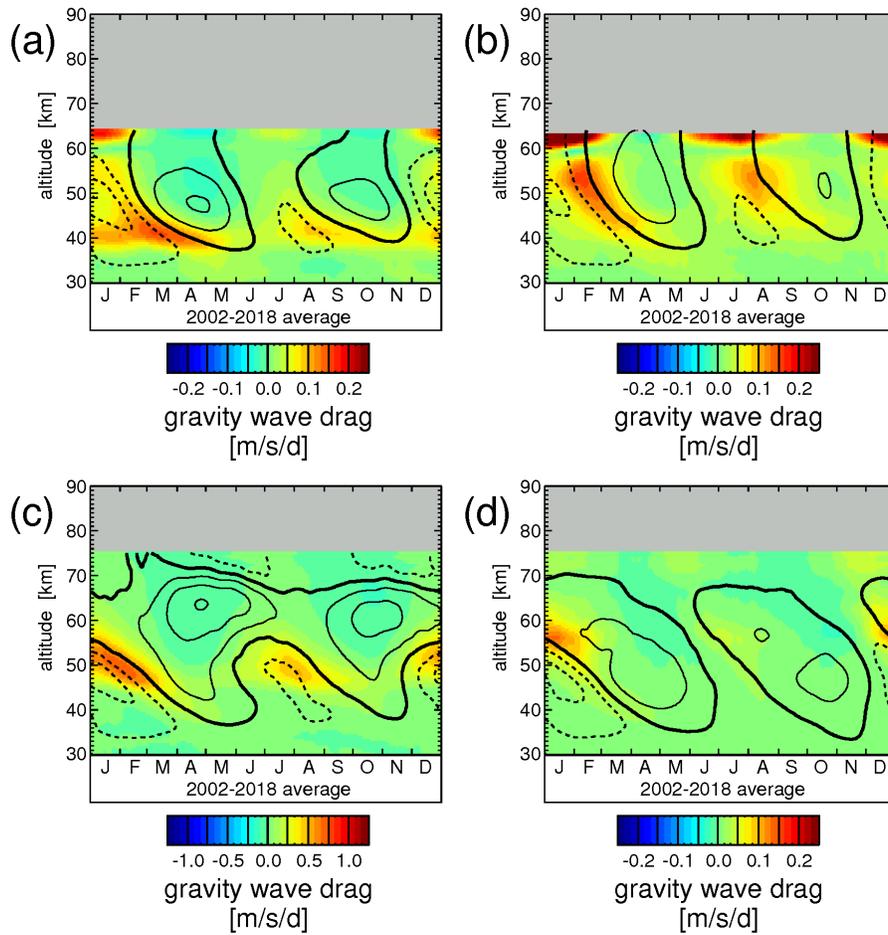


Figure 6: Resolved GW drag $\bar{X}_{res}(k > 20)$ for (a) ERA-Interim, (b) JRA-55, (c) ERA-5, and (d) MERRA-2. Overplotted are contour lines of the corresponding zonal average zonal winds for the respective reanalysis dataset. Contour line interval is 20 m/s. The zero wind line is highlighted in bold solid, and westward (eastward) winds are indicated by dashed (solid) contour lines.

References:

Kawatani, Y., Sato, K., Dunkerton, T. J., Watanabe, S., Miyahara, S., and Takahashi, M.: The roles of equatorial trapped waves and internal inertia gravity waves in driving the quasi-biennial oscillation. Part I: Zonal mean wave forcing, *J. Atmos. Sci.*, 67, 963-980, doi:10.1175/2009JAS3222.1, 2010.

(Main Concern 1b) Assuming zonal propagation of GWs may contradict the flux estimate of SABER, in which the along-track wavelength is regarded as the horizontal wavelength. If zonal propagation of GWs is dominant in the tropics, an error of flux estimate could be large. Please mention the error of flux estimate in more detail.

This concern is the same as **Main Concern 3a** by Reviewer 1. Therefore our corresponding reply is repeated here:

As recommended, We will add more discussion about the shortcoming of using SABER along-track GW horizontal wavenumbers, instead of “true” GW horizontal wavenumbers.

Generally, the use of along-track GW horizontal wavenumbers as a proxy for the true GW horizontal wavenumbers will lead to a low-bias of SABER momentum fluxes (the momentum flux is proportional to the horizontal wavenumber) because the along-track GW horizontal wavenumber will always underestimate the true horizontal wavenumber.

The AIRS satellite instrument has a similar orbit geometry. Because AIRS provides 3D temperature observations, it is possible to determine from AIRS observations true GW horizontal wavenumbers, as well as along-track GW horizontal wavenumbers. This opportunity has been taken by Ern et al. (2017) to compare true and along-track GW horizontal wavenumbers: AIRS observations indicate an underestimation of the along-track wavenumber (corresponding to an underestimation of momentum fluxes) by a factor between 1.5 and somewhat above 2.

In addition, for SABER there will be aliasing effects (undersampling of observed GWs) and effects of the instrument sensitivity function of limb sounding satellite instruments (cf. Ern et al., 2018), which should both lead to an even stronger underestimation of GW momentum fluxes. Therefore the error of SABER GW momentum fluxes should be at least a factor of two, and momentum fluxes are likely strongly underestimated.

This detailed discussion will be included in the revised manuscript in the newly introduced Sect. 6.1.1.

References:

Ern, M., Hoffmann, L., and Preusse, P.: Directional gravity wave momentum fluxes in the stratosphere derived from high-resolution AIRS temperature data, *Geophys. Res. Lett.*, 44, 475-485, doi:10.1002/2016GL072007, 2017.

Ern, M., Trinh, Q. T., Preusse, P., Gille, J. C., Mlynczak, M. G., Russell III, J. M., and Riese, M.: GRACILE: A comprehensive climatology of atmospheric gravity wave parameters based on satellite limb soundings, *Earth Syst. Sci. Data*, 10, 857-892, doi:10.5194/essd-10-857-2018, 2018.

(Main Concern 2) Figures for respective years are shown throughout this paper. However, there is little discussion of interannual variation. It is better to reduce unnecessary figures and make them larger and easier to see.

This comment is similar to **Main Concern 1a** by Reviewer 1.

We will move the single-year figures into the supplemental material and only keep the multi-year averages in the main paper. Further, we will merge figures in the main paper. In addition, in former Figs. 17 and 18 we will omit the column showing the zonal wind, because it is redundant. Further, we will move three rows of former Fig. 17 into the Supplement.

(Main Concern 3) It is mentioned that the effect of tide is large for satellite data above 80 km and contaminate the GW contribution to the SAO driving throughout this paper. Although I understand that it is the signature of the interaction between the tide and GWs and important, it looks far from the primary purpose of this paper. I recommend moving it to another paper.

Because the local time of SABER observations is continuously changing, a brief discussion of local-time effects, including tides, cannot be avoided. Further, the correlation between SABER vertical gradients of absolute momentum flux and the background winds has very different characteristics in different altitude ranges.

For a full understanding, these differences need to be explained, even if these differences are caused by the QBO or tides, and not directly by the SAO. Otherwise, readers will start to question our methods.

Therefore we still mention the effect of tides, but significantly shorten the discussion — particularly in Sects. 7.1.3 and 7.2.2.

Reply to the Minor Comments by Reviewer # 2:

(Minor Comment 1) **The SPARC climatology is regarded “true” and the difference from it is expressed as “bias” throughout this paper. However, it may be better to change the expression because it could be caused by the difference in time resolution and interannual variation as shown in L. 225-228. At least, it is better to compare monthly averages between SPARC climatology and reanalysis/satellite data, which clarify the effect of time resolution.**

As recommended, the word “bias” has been removed in connection with the SPARC climatology.

Just to clarify: we do not regard the SPARC climatology as “true”!

We show the SPARC climatology just for comparison because our general knowledge of the SAO is very poor. In spite of its shortcomings, this climatology gives some information on the basic structure of the SAO, which is helpful to guide the discussion throughout the paper. This might have caused the impression we would consider the SPARC climatology to be the “truth”.

In order to clearly emphasize that the SPARC climatology is not the “truth”, we feel that more discussion on the weaknesses of this climatology is needed. A number of weaknesses of the URAP/SPARC climatology is listed below, and a brief version of this listing will be included as additional discussion in the revised paper in Sect. 4.1.

Some potential limitations of the URAP/SPARC climatology:

- The SPARC climatology is based on the URAP zonal wind climatology, which uses direct wind observations by the HRDI instrument. HRDI observes the Doppler shift of spectral lines from satellite. An inherent problem of this method is that the zero-wind is not clearly defined (e.g., Hays et al., 1993; Baron et al., ACP, 2013), which involves assumptions and may introduce biases.
- HRDI uses only daytime data and covers only 50 to 75% of local times in the mesosphere (cf. Fig. 2 in Swinbank et al. 2003) which can introduce biases, although a correction of tidal effects was attempted.
- URAP uses HRDI observations from the 7 years 1992-1998, but HRDI temporal coverage is reduced to much less than ~50% after mid 1996. Strictly speaking, this means that the SPARC climatology contains only a short period of 4.5 years of quasi-continuous HRDI observations. Only this period should be more reliable because directly guided by HRDI observations. Consequently, interannual variability will still have strong effect on the monthly averages of the SPARC climatology.
- Spatial and temporal gaps in the HRDI wind observations are filled by a climatology, or by interpolation based on model data (UKMO analyses) and balanced winds (cf. Randel et al., 2002). This combination of different data sets, as well as the data processing, may introduce certain biases. Multi-year averaging over a longer dataset with good temporal resolution (like in our paper) was not possible for the SPARC climatology due to the shortness and further shortcomings of the datasets.
- There is a HRDI data gap (no observations) centered around 0.3 hPa (55km, cf. Swinbank 2003, their p.2, and their Figs. 3a and 6) that needs to be filled by climatology, model data, or interpolation, and could introduce biases. This makes the continuously eastward directed winds at 60km in SPARC questionable. Particularly, because there is strong interannual variability, including also periods of **westward** directed winds, at that

altitude in all our datasets. Therefore, already in the ACPD paper version we dedicated some discussion to the question whether this feature in the URAP/SPARC climatology could be reliable.

Given these facts, it should be clear that the SPARC climatology can contain biases and should not be considered to be the “truth”.

Since the SPARC climatology is not considered to be a reference, or the “truth”, it does not make much sense to, for example, reduce the time resolution of our better resolved datasets to that of the SPARC climatology. Further, we hope that the better time resolution of our dataset may be considered helpful by others.

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(Minor Comment 2) It seems unnecessary to discuss the correlation in QBO and sponge layers in this paper.

The Rayleigh drag exerted in the sponge layers is one of the contributions of the GW drag proxy. For JRA-55 and ERA-Interim, this is even one of the main contributions. In the discussion in Sect. 8 we point out that this contribution is not considered to be very realistic. We feel that this discussion is needed because Reviewer 1 in his **Major Concern 2** was worried that the residual drag from reanalyses would not always be representative of GW drag. For this reason, we keep this discussion in order not to appear to be too uncritical about our results. In addition, the altitude where the negative correlation between the residual drag and the zonal wind strengthens gives valuable information above which altitude the residual drag becomes increasingly unrealistic.

Therefore we decided to keep the discussion about Rayleigh drag in the sponge layers.

The biennial variations seen in our correlation analysis are a striking feature that needs to be explained. Without an explanation, readers would think this correlation would be an artifact, and doubt our methods. Overall, the discussion of the QBO-correlations does not take much space, anyhow.

Therefore, for completeness, we decided to keep the discussion related to the QBO.

The semiannual oscillation (SAO) in the tropical middle atmosphere and its gravity wave driving in reanalyses and satellite observations

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Abstract. Gravity waves play a significant role in driving the semiannual oscillation (SAO) of the zonal wind in the tropics. However, detailed knowledge of this forcing is missing, and direct estimates from global observations of gravity waves are sparse. For the period 2002–2018, we investigate the SAO in four different reanalyses: ERA-Interim, JRA-55, ERA-5, and MERRA-2. Comparison with the SPARC zonal wind climatology and quasi-geostrophic winds derived from Microwave Limb
5 Sounder (MLS) and Sounding of the Atmosphere using Broadband Emission Radiometry (SABER) satellite observations show that the reanalyses reproduce some basic features of the SAO. However, there are also large differences, depending on the model setup. Particularly, MERRA-2 seems to benefit from dedicated tuning of the gravity wave drag parameterization and assimilation of MLS observations. To study the interaction of gravity waves with the background wind, absolute values of gravity wave momentum fluxes ~~and~~, [and a proxy for absolute gravity wave](#) drag derived from SABER satellite observations are compared
10 with different wind data sets: the SPARC wind climatology, data sets combining ERA-Interim at low altitudes and MLS or SABER quasi-geostrophic winds at high altitudes, as well as data sets that combine ERA-Interim, SABER quasi-geostrophic winds, and direct wind observations by the TIMED Doppler Interferometer (TIDI). In the lower and middle mesosphere [the](#) SABER absolute gravity wave drag [proxy](#) correlates well with positive vertical gradients of the background wind, indicating that gravity waves contribute mainly to the driving of the SAO eastward wind phases and their downward propagation with
15 time. At altitudes 75–85 km, [the](#) SABER absolute gravity wave drag [proxy](#) correlates better with absolute values of the background wind, suggesting a more direct forcing of the SAO winds by gravity wave amplitude saturation. Above about 80 km SABER gravity wave drag is mainly governed by tides rather than by the SAO. The reanalyses reproduce some basic features of the SAO gravity wave driving: All reanalyses show stronger gravity wave driving of the SAO eastward phase in the stratopause region. For the higher-top models ERA-5 and MERRA-2 this is also the case in the lower mesosphere. However,
20 all reanalyses are limited by model-inherent damping in the upper model levels, leading to unrealistic features near the model top. Our analysis of the SABER and reanalysis gravity wave drag suggests that the magnitude of SAO gravity wave forcing is often too weak in the free-running general circulation models, therefore, a more realistic representation is needed.

1 Introduction

In the tropics, the zonal wind in the middle atmosphere exhibits characteristic oscillations of semiannual and quasi-biennial periods. The quasi-biennial oscillation (QBO) has an approximate average period of 28 months and is the dominant mode in the stratosphere. The semiannual oscillation (SAO) dominates in the upper stratosphere and in the mesosphere with one amplitude peak in the stratopause region, the stratopause semiannual oscillation (SSAO), and another amplitude peak somewhat below the mesopause, the mesopause semiannual oscillation (MSAO). For further details regarding the QBO and the SAO please see Baldwin et al. (2001).

First observations of the SAO winds were made by rocketsondes and radars at single stations in the tropics (e.g., Reed, 1966; Groves, 1972; Hirota, 1978; Dunkerton, 1982; Hamilton, 1982; Palo and Avery, 1993), and observations at tropical stations are still continued (e.g., Gurubaran and Rajaram, 2001; Venkateswara Rao et al., 2012; Day and Mitchell, 2013; Kishore Kumar et al., 2014). Direct observations of the SAO winds from satellite were made, for example, by the High Resolution Doppler Imager (HRDI) onboard the Upper Atmosphere Research Satellite (UARS) (e.g., Lieberman et al., 1993; Burrage et al., 1996), or by the Superconducting Submillimeter-Wave Limb-Emission Sounder (SMILES) instrument onboard the International Space Station (e.g., Baron et al., 2013).

Based on multiple observations including HRDI zonal winds, a first comprehensive climatology of the SAO in the tropical middle atmosphere was introduced by Garcia et al. (1997). A later assessment led to the Stratospheric-Stratosphere-troposphere Processes And their Role in Climate (SPARC) global monthly climatology of zonal mean winds (Swinbank and Ortland, 2003; Randel et al., 2002, 2004). Unfortunately, direct global wind observations from satellite in the stratosphere and mesosphere are sparse. Therefore, Smith et al. (2017) recently investigated whether it is possible to interpolate quasi-geostrophic winds derived from Sounding of the Atmosphere using Broadband Emission Radiometry (SABER) and Microwave Limb Sounder (MLS) satellite observations into the tropics. Useful results were obtained for altitudes below about 80 km.

The SAO plays an important role in the whole atmosphere system. Effects of the SAO are also observed in temperatures (e.g., Reed, 1962; Delisi and Dunkerton, 1988a; Garcia and Clancy, 1990; Huang et al., 2008), and the SAO modulates the distribution of trace species in the stratosphere (e.g., Shu et al., 2013), as well as in the mesosphere and lower thermosphere (MLT) (e.g., Huang et al., 2008; Kumar et al., 2011; Zhu et al., 2015). It was found that the QBO and the SAO interact with each other. For example, the phases of the QBO and SAO can synchronize (e.g., Dunkerton and Delisi, 1997; Krismer et al., 2013), and eastward phases of the SAO can initiate QBO eastward phases (e.g., Kuai et al., 2009). This effect of the SAO is of relevance because the QBO couples to the extratropics (e.g., Holton and Tan, 1980; Anstey and Shepherd, 2014), and has effects on surface weather and climate (e.g., Ebdon, 1975; Marshall and Scaife, 2009; Kidston et al., 2015). Climate and weather models have difficulties to simulate this influence of the QBO (e.g., Scaife et al., 2014). Further, there is evidence that both the QBO and the SAO influence the timing of sudden stratospheric warmings (e.g., Pascoe et al., 2006), and a correct representation of the SAO is needed to explain and better predict such extreme polar vortex events and their influence on surface weather conditions (Gray et al., 2020). For these reasons it is very important to learn more about the mechanisms that drive the SAO.

It is known that atmospheric gravity waves contribute to the driving of both the QBO and the SAO. As was shown by several model studies, particularly gravity waves generated by deep convection in the tropics should contribute significantly to the driving of the QBO and the stratopause SAO (e.g., Beres et al., 2005; Kim et al., 2013; Kang et al., 2018), as well as
60 to the mesopause SAO (e.g., Beres et al., 2005). While critical level filtering of gravity waves of either eastward or westward directed phase speed plays a major role for the driving of the QBO (e.g., Lindzen and Holton, 1968; Lindzen, 1987; Dunkerton, 1997; Baldwin et al., 2001; Ern et al., 2014), the situation is more complicated for the SAO. It was suggested that the forcing of the stratopause SAO should be asymmetric because gravity waves are selectively filtered by the QBO in the stratosphere before entering the altitude range dominated by the SAO (e.g., Hamilton and Mahlmann, 1988; Dunkerton and Delisi, 1997).
65 The QBO westward phase has a stronger magnitude, and therefore a larger part of the gravity wave spectrum at westward directed phase speeds is filtered out by encountering critical levels. For the stratopause region, this means that the gravity wave spectrum is dominated by eastward propagating waves. Due to this excess of eastward momentum, gravity waves should mainly contribute to the driving of the SAO eastward phase, and only to a lesser extent to the driving of the SAO westward phase. Instead, the driving of the SAO westward phase should be dominated by horizontal advection and the influence of planetary
70 waves from the extratropics (e.g., Delisi and Dunkerton, 1988b; Hamilton and Mahlmann, 1988).

For the stratopause SAO, this asymmetry was confirmed by High Resolution Dynamics Limb Sounder (HIRDLS) satellite observations of gravity waves (Ern et al., 2015). Semiannual modulations of the global distribution of gravity waves are indeed observed over a large altitude range in the tropical mesosphere (e.g., Kovalam et al., 2006; Krebsbach and Preusse, 2007; Sridharan and Sathishkumar, 2008; Venkateswara Rao et al., 2012; Matsumoto et al., 2016; Chen et al., 2019). However, there
75 is large uncertainty in which way those gravity waves contribute to the driving of the SAO, and how far the aforementioned asymmetry of gravity wave driving extends upward into the mesosphere. Recent work by Smith et al. (2020) revealed that current global climate models have difficulties in simulating a realistic SSAO. One of the main ~~reasons~~ reasons that was identified is a general lack of eastward forcing by waves in the model — either by large-scale waves, or by gravity waves. Therefore validation of the SAO wave forcing would be required. Another recent study shows that also in current meteorological reanalyses
80 the SSAO differs strongly between the different reanalyses (Kawatani et al., 2020).

The mesopause SAO is out-of-phase, or even in anti-phase, with the SAO at lower altitudes (e.g., Hirota, 1980; Dunkerton, 1982; Hamilton, 1982). Of course, not only gravity waves, but also advection and medium-scale and global-scale waves (including tides) contribute to the driving of the SAO in the MLT region (e.g., Sassi and Garcia, 1997; Richter and Garcia, 2006). However, likely reason for this out-of-phase relationship is the selective wave filtering of gravity waves by the SSAO and the
85 SAO in the middle mesosphere. After the selective filtering of the gravity wave spectrum by the background winds, the spectrum is dominated by gravity waves propagating opposite to the wind direction, either eastward or westward, in the middle and lower mesosphere. This is confirmed, for example, by radar observations of gravity wave momentum fluxes (e.g., Matsumoto et al., 2016). If these remaining waves saturate and break in the upper mesosphere and the mesopause region, this results in driving of either the eastward or westward SAO phase, opposite to the wind in the middle mesosphere (e.g., Dunkerton, 1982;
90 Mengel et al., 1995). This mechanism is also supported by HRDI wind observations (Burrage et al., 1996), as well as by model simulations (see, for example, Richter and Garcia, 2006; Peña-Ortiz et al., 2010). To some extent, even selective wave filter-

ing by the QBO in the stratosphere has effects on the mesopause SAO (e.g., Garcia and Sassi, 1999; Peña-Ortiz et al., 2010) (e.g., Garcia and Sassi, 1999; Lieberman et al., 2006; Peña-Ortiz et al., 2010). Overall, the driving of the MSAO is not fully understood, and observations of gravity wave momentum flux at the equator are needed to resolve this issue, as stated in a recent review by Vincent (2015).

Our study investigates the SAO and its gravity wave driving in the whole middle atmosphere in the altitude range 30–90 km. We focus on the latitude range 10°S–10°N, and the years 2002–2018 for which satellite data are available. For four reanalyses, the ERA-Interim and ERA-5 reanalyses of the European Centre for Medium-Range Weather Forecasts (ECMWF), the Japanese 55-year Reanalysis (JRA-55) of the Japanese Meteorological Agency (JMA), and the Modern-Era Retrospective Analysis for Research and Applications, Version 2 (MERRA-2) reanalysis of the National Aeronautics and Space Agency Administration (NASA), we determine the zonal winds averaged over 10°S–10°N, and we estimate the driving of the SAO by gravity waves from the residual term (“missing drag”) in the transformed Eulerian mean (TEM) zonal-average momentum budget (e.g., Andrews et al., 1987; Alexander and Rosenlof, 1996). We also investigate the SAO in quasi-geostrophic zonal winds derived from satellite observations of the MLS and the SABER satellite instruments, and in the winds directly observed by the TIMED Doppler Interferometer (TIDI) satellite instrument. Both SABER and TIDI are on the Thermosphere-Ionosphere-Mesosphere Energetics and Dynamics (TIMED) satellite. Further, we investigate the gravity wave driving of the SAO based on absolute gravity wave momentum fluxes and a proxy for absolute values of gravity wave drag derived from SABER satellite observations, and a correlation analysis between zonal winds and absolute gravity wave drag is carried out to reveal details of the SAO gravity wave driving.

The manuscript is organized as follows: Section 2 gives a description of the four reanalyses used in our study, and Sect. 3 gives a description of the instruments that provided the satellite data used in our study. In Sect. 4.1–4 we discuss the reanalysis SAO zonal winds and the SAO gravity wave driving expected from the reanalysis zonal momentum budget. Section 4.2 shows how the SAO is seen in the zonal winds determined in the reanalyses (Sect. 4.1) and the SAO zonal winds derived from satellite data (Sect. 4.2). The winds derived from satellite data are quasi-geostrophic winds determined from SABER and MLS observations, as well as direct wind observations by TIDI, and. The SAO gravity wave driving expected from the reanalysis zonal momentum budget is discussed in Sect. 5, and in Sect. 6 discusses we discuss the driving of the SAO based on SABER observations of absolute gravity wave momentum fluxes and the SABER absolute gravity wave drag proxy. A correlation analysis is carried out in Sect. 7 to investigate the relation between the SABER absolute gravity wave drag proxy and the SAO in more detail, and in Sect. 8 a similar correlation analysis is carried out for the reanalyses. Finally, Sect. 9 gives a summary of the paper.

2 Reanalysis data

In this paper four different meteorological reanalyses are used, interpolated to a longitude/latitude resolution of $1^\circ \times 1^\circ$. For a summary of different reanalyses see also, for example, Fujiwara et al. (2017) and Martineau et al. (2018). The reanalysis ERA-Interim (see also Dee et al., 2011) of the European Centre for Medium-Range Weather Forecasts (ECMWF) has a horizontal

125 model resolution of T255, corresponding to a longitudinal grid spacing of ~ 79 km at the equator. It uses 60 levels in the vertical with a model top level at 0.1 hPa, i.e. somewhat above the stratopause (see also Fig. ??1). A parameterization of orographic gravity waves after Lott and Miller (1997) is included. A parameterization for nonorographic gravity waves, however, is missing and only included in later ECMWF model versions (see also Orr et al., 2010). To avoid reflection of model-resolved waves at the model top artificial damping (Rayleigh friction) is used at pressures lower than 10 hPa (altitudes above ~ 32 km). For a
130 ~~summary of different reanalyses see also, for example, Fujiwara et al. (2017) and Martineau et al. (2018).~~

The Japanese 55-year Reanalysis (JRA-55) (see also Kobayashi et al., 2015) of the Japanese Meteorological Agency (JMA) has a finer grid spacing with a horizontal resolution of T319 (~ 55 km at the equator). Like ERA-Interim, JRA-55 uses 60 model levels with the model top level at 0.1 hPa (cf. Fig. ??1), a parameterization of orographic gravity waves is included (Iwasaki et al., 1989a,b), but no parameterization for nonorographic gravity waves. Rayleigh damping is applied at pressures
135 below 50 hPa (altitudes above ~ 21 km). In addition, the horizontal diffusion coefficient is gradually increased with altitude at pressures lower than 100 hPa.

Unlike ERA-Interim and JRA-55, the Modern-Era Retrospective Analysis for Research and Applications, Version 2 (MERRA-2) reanalysis (see also Gelaro et al., 2017) uses 72 layers in the vertical with a model top at 0.01 hPa, and a top layer mid level at 0.015 hPa (~ 78 km) in the upper mesosphere. The horizontal resolution is 0.5° latitude \times 0.625° longitude. Parameteriza-
140 tions for both orographic (McFarlane, 1987) and nonorographic gravity waves (Garcia and Boville, 1994; Molod et al., 2015) are included. Additional damping is applied at pressures less than 0.24 hPa (altitudes above ~ 58 km), i.e. at altitudes much higher than in ERA-Interim and JRA-55. One peculiarity of MERRA-2 is that, starting in August 2004, MLS temperature data are assimilated. This means that MERRA-2 is constrained by observations even in the mesosphere, while other reanalyses usually do not include observations above the stratopause. Further, the MERRA-2 nonorographic gravity wave drag scheme
145 was optimized for a better representation of the QBO and the SAO in the tropics (Molod et al., 2015).

Similar to MERRA-2, the ECMWF reanalysis ERA-5 (see also Hersbach and Dee, 2016; Hersbach et al., 2018, 2019, 2020) has a high model top with the top level at 0.01 hPa (~ 80 km). The number of model levels is 137, resulting in a better vertical resolution than for all reanalyses previously described, including MERRA-2 (Fig. ??1). The horizontal resolution is T639, according to a longitudinal grid spacing of ~ 31 km at the equator. In our work we use the updated version ERA5.1 that uses an
150 improved assimilation scheme for the period 2000–2006 (Simmons et al., 2020). ERA-5 uses parameterizations for orographic (Lott and Miller, 1997; Sandu et al., 2013) and nonorographic (Orr et al., 2010) gravity waves, but does not assimilate MLS data. The sponge layer starts at pressures lower than 10 hPa (altitudes above ~ 32 km) and depends on model level and zonal wavenumber in order to damp vertically propagating waves (e.g., Polichtchouk et al., 2017). An additional sponge layer starts at pressures lower than 1 hPa (altitudes above ~ 48 km). Unlike ERA-Interim, no Rayleigh friction is applied at pressures
155 lower than 10 hPa. For comparison, Fig. ??1 illustrates the model levels used in the different reanalyses for the altitude range of 30 to 90 km covered in this study.

3 The satellite instruments MLS, SABER, and TIDI

The Microwave Limb Sounder (MLS) is one of the instruments onboard the NASA satellite Aura. MLS is a limb sounding radiometer that observes atmospheric microwave emissions (e.g., Waters et al., 2006; Livesey et al., 2017). From these limb observations, atmospheric temperature and a number of trace species are derived. In our study we use MLS version 4.2 atmospheric temperatures and geopotential height, which are available from the middle troposphere to the mesopause region (pressures from 316 to 0.001 hPa). The vertical resolution is between ~ 4 km in the stratosphere and ~ 14 km around the mesopause. A detailed description of the temperature/pressure retrieval is given, for example, in Schwartz et al. (2008). The Aura satellite is in a sun-synchronous orbit. Therefore, MLS observations are always at two fixed local solar times. In the tropics, these local times are about 13:45 local solar time (LST) for the ascending orbit parts (i.e., when the satellite is flying northward) and 01:45 LST for the descending orbit parts (i.e., when the satellite is flying southward), according to the satellite equator crossing times. Measurements of MLS started on 8 August 2004 and are still ongoing at the time of writing.

The Sounding of the Atmosphere using Broadband Emission Radiometry (SABER) instrument was launched onboard the Thermosphere-Ionosphere-Mesosphere Energetics and Dynamics (TIMED) satellite in December 2001. SABER measurements started on 25 January 2002 and are still ongoing at the time of writing. TIMED has been approved to operate for three more years, until September 2023. Another three more years of operations will be proposed in near future. SABER is a broadband radiometer that observes atmospheric infrared emissions in limb-viewing geometry with an altitude resolution of about 2 km. Atmospheric temperatures are derived from infrared emissions of carbon dioxide (CO_2) at around $15 \mu\text{m}$. The SABER temperature-pressure retrieval is described in detail by Remsberg et al. (2004) and Remsberg et al. (2008). More details on the SABER instrument are given, for example, in Mlynczak (1997) and Russell et al. (1999). In our study we use SABER version 2 temperatures, and in Sect. 6.1 we briefly introduce the method how absolute gravity wave momentum fluxes and a proxy for absolute gravity wave drag can be derived from these temperature observations.

The TIMED satellite orbit is slowly precessing with a period of about 120 days. ~~To make sure~~ To ensure that always the same side of the satellite stays in the dark, TIMED performs yaw maneuvers approximately every 60 days. Accordingly, the local solar time of the satellite observations slowly drifts over one of the ~ 60 -day periods, and then jumps when a satellite yaw is performed. ~~In Fig. ?? this~~ This is illustrated for the equatorial local solar times of SABER observations ~~during ascending (black diamonds) and descending (black crosses) orbit parts, respectively,~~ for the time period 2002 until ~~2018.~~ 2018 in Fig. S1 in the Supplement of this paper.

Since launch, the TIMED spacecraft has been decreasing in altitude by about 1 km per year. The inclination of the spacecraft has remained stable at 74° . However, the change in altitude has resulted in a drift of local time sampling, and hence, of the yaw date. The first TIMED yaw was in January 2002. At the time of writing, that yaw is now occurring in late December. As a consequence, the local time sampled in a given day or month changes every year. This effect could affect trend studies, but should not impact our work.

Another instrument onboard the TIMED satellite is the TIMED Doppler Interferometer (TIDI). Detailed information about TIDI can be found, for example, in Killeen et al. (2006) or Niciejewski et al. (2006). The TIDI instrument is a Fabry-Perot

interferometer that was designed to observe atmospheric winds in the altitude range 70–120 km with an altitude resolution of about 2 km. This is achieved by using four ~~individual separate~~ telescopes to observe atmospheric emissions of rotational lines in the molecular oxygen (O_2) (0-0) band around 762 nm in limb-viewing geometry. One pair of telescopes is located on the sunlit side of the TIMED satellite (warm side), the other pair is located on the dark side (cold side). In each pair, one telescope views forward at an angle of 45° with respect to the satellite velocity vector, the other telescope views 45° rearward. In this way, the same air volume is observed by the two telescopes of a pair with a time difference of only 9 minutes. Based on these orthogonal measurements, wind vectors can be derived from the Doppler-shift of the atmospheric emissions. The wind vector observations form two tracks on either side of the spacecraft, i.e. the warm side and the cold side, respectively. ~~Figure ?? shows that these~~ These two tracks are at different local solar times with the local solar time of the cold side track differing from the local solar time of the corresponding SABER observations by only about half an hour. ~~This is visible in~~ (See also Fig. ?? where local solar times of TIDI equatorial observations are indicated by red diamonds (warm, ascending), red crosses (warm, descending), blue diamonds (cold, ascending), and blue crosses (cold, descending), respectively. S1 in the Supplement.) Like for SABER, also TIDI observations are still ongoing at the time of writing.

4 The SAO zonal wind in the ERA-Interim, JRA-55, ERA-5, and MERRA-2 reanalyses and satellite data

205 4.1 The SAO in the reanalyses ERA-Interim, JRA-55, ERA-5, and MERRA-2

4.2 Zonal wind

In our study, we focus on the 2002–2018 period ~~during which because~~ gravity wave observations by the SABER instrument are available ~~only starting from 2002~~. From the reanalyses, we use global distributions of meteorological fields at 00:00, 06:00, 12:00, and 18:00 UT. For comparison with SABER data, we calculate values of the zonal wind averaged over 7 days and over the latitude band $10^\circ S$ – $10^\circ N$. Values are calculated in steps of 3 days, i.e. the time periods used for averaging are overlapping.

215 ~~Figure ?? shows zonal winds averaged over~~ For the four reanalyses considered, Figs. 2a–2d show the variations of the zonal wind in the tropics for the “typical year”. This “typical year” is obtained by averaging the zonal wind over the latitude band $10^\circ S$ – $10^\circ N$ for the 2002–2018 time period for ERA-Interim, as well as the multi-year average for the time period 2002–2018. For comparison and the years from 2002 until 2018. Distributions for the single years are shown in the Supplement of this paper.

For guiding the discussion, Fig. ?? shows in the lower right panel 2e shows also the zonal wind of the SPARC zonal wind climatology, averaged over the latitude band $10^\circ S$ – $10^\circ N$. The same comparison is repeated in Figs. ??–?? for the JRA-55, ERA-5, and MERRA-2 reanalyses, respectively. SPARC wind climatology is a monthly climatology that is based on the UARS (Upper Atmosphere Research Satellite) Reference Atmosphere Project (URAP) wind climatology (Swinbank and Orland, 2003; Randel et al. 2001). For the time period 1992–1998, it combines wind observations by the High Resolution Doppler Imager (HRDI) instrument on UARS (cf. Hays et al., 1993) and model data to interpolate gaps. There are several uncertainties that potentially affect this climatology:

- There may be wind biases due to uncertainties of the zero-wind — an inherent problem of wind observations based on the Doppler shift method applied from a satellite (e.g., Hays et al., 1993; Baron et al., 2013).
- 225 - HRDI observations are during daytime only. Although a correction of tidal effects was applied, there could be remaining biases.
- In the period 1992–1998 there are only about 4.5 years of quasi-continuous HRDI observations. Therefore, interannual variability will still have strong effect on the monthly averages of the SPARC climatology.
- 230 - HRDI data gaps had to be interpolated for the climatology. This could introduce biases and interpolation artifacts. In particular, there is a HRDI data gap centered around 0.3 hPa (~55 km altitude). In Sect. 4.1.2 we will discuss whether the continuously eastward directed winds at this altitude could be a reliable feature.

In spite of these shortcomings, at SAO altitudes the SPARC climatology is still the only global climatology based on direct wind observations, and it summarizes our poor knowledge of the SAO. Therefore this climatology is very useful for guiding the discussion throughout the paper. However, given the above uncertainties, the SPARC climatology should not be considered a reference, or the “truth”.

235

4.1.1 The stratopause SAO

All reanalyses capture some basic features of the SAO in the stratopause region and in the lower mesosphere. In all reanalyses, the first SAO period of a given year has the larger amplitude, as expected from observations (e.g., Garcia et al., 1997; Swinbank and Ortland, 2003). It is noteworthy that, while there is strong interannual variability in all reanalyses, this variability differs strongly among the different reanalyses, See Figs. S2–S5 in the Supplement. There are also other significant differences. For example, in ERA-Interim, the eastward winds of the first SAO period of a given year are somewhat stronger than in JRA-55, or in MERRA-2. Further, ERA-5 eastward jets are generally too strong at altitudes above ~45 km, consistent with previous studies (Hersbach et al., 2018; Shepherd et al., 2018). These overly strong eastward winds are caused by severe tapering of vorticity errors in the mesosphere, and this issue has been resolved from the introduction of IFS cycle 43r3 (11 July 2017) (Hersbach et al., 2018).

240

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Generally, large differences at high altitudes result because ERA-Interim and JRA-55 have lower model tops and introduce stronger artificial damping at lower altitudes than in MERRA-2 and ERA-5. Therefore, ERA-Interim winds strongly weaken at altitudes above 50 km, which, however, is less the case for JRA-55.

~~Next, we compare the four reanalyses with the SPARC zonal wind climatology (lower right panel in Figs. ?? to ??, respectively). The SPARC wind is a monthly climatology (Swinbank and Ortland, 2003; Randel et al., 2002, 2004) that combines wind observations by the Upper Atmosphere Research Satellite (UARS) instrument High Resolution Doppler Imager (HRDI) (cf. Hays et al., 1993) and model data to interpolate gaps. Effects of the QBO and of tides have been widely removed (Randel et al., 2002).~~

250

~~Compared to the SPARC climatology, the SAO in all four reanalyses has a larger amplitude in the upper stratosphere. Partly, this is caused by the fact that the SPARC climatology has only a monthly temporal resolution and will therefore smear out~~

255 rapid temporal changes like the SAO. In addition, ~~the SPARC climatology is based on an average of the years 1992–1998 (with reduced coverage after mid-1996), and the SAO in the upper stratosphere might have changed on average~~some of the above mentioned error sources could affect the SPARC climatology.

4.1.2 The SAO in the mesosphere, and the MSAO

At altitudes above ~ 60 km, deviations between the SPARC climatology and the reanalyses become large. In the SPARC
260 climatology at altitudes between 60 and 70 km, the zonal wind is continuously eastward, which, on average, is only the case in ERA-5. In ERA-5, however, eastward directed winds in this altitude range are often too strong.

~~Those~~These eastward directed winds around 60 and 70 km altitude seem to be a real feature in climatological averages. For example, continuously eastward winds at the equator have been observed around 0.1 hPa (~ 65 km) from October 2009 until April 2010 by the Superconducting Submillimeter-Wave Limb-Emission Sounder (SMILES) instrument (Baron et al., 2013).
265 During this period also in MERRA-2 eastward winds are seen around ~ 65 km, but not in a multi-year average. Also multi-year averages of quasi-geostrophic winds that are derived from satellite observations and interpolated to the tropics show persistent eastward winds around ~ 65 km. There is, however, strong interannual variability, and in several years it is observed that the zonal winds at altitudes around ~ 65 km alternate between eastward and westward due to the SAO (see Smith et al. (2017) and Sects. 4.2.2 and 4.2.3).

270 Another important feature in the SPARC climatology is a mesopause SAO that is in an anti-phase relation with the SAO at lower altitudes (see also, for example, Burrage et al., 1996) and has its peak amplitude around ~ 80 km. Of course, the MSAO is not captured by ERA-Interim and JRA-55 because of their low model tops. Also MERRA-2 does not capture the MSAO; Due to a strong sponge layer the zonal wind in MERRA-2 is gradually damped to near zero close to the model top. Only ERA-5 partly captures the MSAO, and the wind reverses to westward at altitudes around 70 km, i.e. near the model top.

275 4.2 The SAO as seen in satellite data

4.2.1 Interpolated quasi-geostrophic winds in the tropics

Following the approach used in previous studies (e.g., Oberheide et al., 2002; Ern et al., 2013; Smith et al., 2017; Sato et al., 2018), quasi-geostrophic winds can be calculated from the geopotential fields derived from satellite soundings. For stationary conditions, and neglecting the drag exerted by atmospheric waves, the zonal and meridional momentum equations can be
280 written as follows

$$\underbrace{-\left(f + \frac{u \tan \phi}{a}\right)v + \frac{1}{a \cos \phi} \frac{\partial \Phi}{\partial \lambda}}_{=} = 0 \quad (1)$$

$$\underbrace{\left(f + \frac{u \tan \phi}{a}\right)u + \frac{1}{a} \frac{\partial \Phi}{\partial \phi}}_{=} = 0 \quad (2)$$

285 Here, u and v are the zonal and the meridional wind, respectively, a the Earth radius, ϕ the geographic latitude, and Φ the
geopotential. For further details see Andrews et al. (1987), Oberheide et al. (2002), or Ern et al. (2013). These equations can
be easily solved for u and v .

The quasi-geostrophic approach gives good results in the extratropics, but is not reliable in the tropics because the Coriolis
parameter is close to zero. Recently, it has been shown by Smith et al. (2017) that an interpolation of the quasi-geostrophic
zonal wind starting from 10°S and 10°N can be used as a proxy for the zonal wind at the equator, and is in good agreement
290 with wind observations by lidar below about 80 km.

As direct wind observations in the tropical mesosphere are sparse, we will also make use of this approach, even though
interpolated quasi-geostrophic winds will still be affected by biases. In order to make sure that our findings are robust, we will
use a number of different zonal wind data sets in Sects. 6 and 7 to check whether our findings of the SAO gravity wave driving
hold for different choices of background winds.

295 For our study, we utilize zonal-average quasi-geostrophic zonal winds calculated for time intervals of three days with a
time step of three days, i.e. the time windows used for calculating the winds are non-overlapping. This data set has been
previously used for studies in the extratropics (Ern et al., 2013, 2016; Matthias and Ern, 2018). For studying the interaction of
gravity waves with the SAO zonal wind in the latitude band 10°S – 10°N , we use the average of the quasi-geostrophic wind at
 12°S and 12°N as a proxy for the zonal wind in this latitude band at altitudes above 45 km, similar as in Smith et al. (2017)
300 . At lower altitudes, reanalysis winds should be more reliable, so we do not use quasi-geostrophic winds at altitudes below
35 km. Instead, we use the ERA-Interim winds presented in Fig. 2a (and in Fig. S2 in the Supplement), and a smooth transition
between ERA-Interim and quasi-geostrophic winds derived from SABER or MLS satellite observations in the altitude range
35–45 km.

4.2.2 MLS quasi-geostrophic winds

305 For comparison with the MERRA-2 reanalysis that assimilates MLS data, Fig. 3a shows the average year of the merged data
set of ERA-Interim and interpolated MLS quasi-geostrophic winds. As MLS observations started in mid-2004, averaging was
performed only over the years 2004 until 2018. To reduce the effect of tides, MLS winds are calculated from an average over
ascending and descending orbit branches, i.e. data from the two MLS equator crossing times are averaged.

Figures 2d and 3a show that at altitudes below ~ 60 km MLS and MERRA-2 winds are very similar. For the single years,
310 this is also seen in the Supplement from Figs. S5 and S6. On the one hand, this is expected because MLS data are assimilated
in MERRA-2. On the other hand, this shows that our interpolated quasi-geostrophic winds are useful in the tropics. Still, these
interpolated winds are not considered to be reliable at altitudes above ~ 75 km. For example, above ~ 75 km eastward winds
are relatively strong, and the duration of the SAO westward wind phases at altitudes above ~ 70 km is relatively short when
compared with the other datasets. Both these effects could be an effect of tides. Although both ascending and descending nodes
315 enter the estimation of MLS quasi-geostrophic winds, it is not expected that tidal effects will completely cancel out.

4.2.3 Merged SABER quasi-geostrophic and TIDI wind observations

So far we have discussed wind data sets of four reanalyses, as well as interpolated quasi-geostrophic winds based on MLS observations. Another main purpose of our work is to study the interaction of SABER gravity wave observations with the background wind. Of course, both the SAO and tides contribute to the variations of the winds in the tropics. As shown in Fig. S1 in the Supplement, the local solar times of SABER equator crossings slowly change over time. Therefore, it is important to compare gravity wave observations and winds observed at the same local solar times.

For this purpose, we have composed a combined data set of SABER quasi-geostrophic winds in the altitude range 45–75 km, ERA-Interim winds below 35 km, and a smooth transition between ERA-Interim and SABER winds in the altitude range 35–45 km. At altitudes above ~ 80 km we use directly observed TIDI “cold side” winds. As shown in Fig. S1, the local solar time of TIDI cold side winds matches the local solar times of SABER observations better than about half an hour. Winds in the gap between 75 and 80 km are interpolated. Similar as in the study of Dhadly et al. (2018), we omit less reliable TIDI data from periods when the angle β between orbital plane and the Earth-Sun vector exceeds 55° , i.e. when the TIMED orbital plane is near the terminator. Data gaps that are caused by omitting these data, as well as other data gaps that are shorter than 40 days are closed by linear interpolation in time. A larger data gap from November 2016 until March 2017 is closed by using interpolated SABER quasi-geostrophic winds also at altitudes above 75 km. Interpolated SABER quasi-geostrophic winds are used above 75 km also before April 2002, because TIDI cold side winds are available only after that date.

Figure 3b shows the 2002–2018 average year of this combined wind dataset. Single years are shown in Fig. S7 in the Supplement. In the following, this combined wind dataset will be termed for convenience “E/S/T-winds”. SABER and TIDI winds were averaged over ascending and descending TIMED satellite equator passages, i.e., they represent an average over different local solar times. At altitudes below ~ 70 km these winds are very similar to those derived from MLS (see Fig. 3a). Although ascending and descending orbit data are combined, there are notable variations that are related to the 60-day yaw cycle of the TIMED satellite and the corresponding changes in the local solar time of SABER and TIDI observations. This shows the importance of selecting wind data at the correct local solar time, particularly at higher altitudes.

The main difference between Fig. 3a and Fig. 3b, however, are the winds at altitudes above 80 km where TIDI wind observations are used. On average, the TIDI winds are more westward than the quasi-geostrophic winds derived from MLS, and even somewhat more westward than the SPARC climatology (Fig. 3c). Particularly the maxima of both SAO eastward phases at altitudes above around 85 km are less pronounced. Because at altitudes above 80 km variations that are linked to the TIMED yaw cycles and the corresponding changes in local solar time are quite strong, this could be an effect of tides. The TIDI instrument samples atmospheric tides at the same phase as SABER. Since wind variations due to tides can be of the same magnitude as variations due to the SAO, the combined data set of SABER and TIDI winds should therefore be the best choice for representing the atmospheric background conditions relevant for SABER gravity wave observations.

A more comprehensive analysis of tides based on TIDI winds has been carried out in previous studies (e.g., Oberheide et al., 2006; Wu et al., 2018). An in-depth investigation of the effect of tides on the distribution of gravity waves, however, is beyond the scope of our study. Overall, the differences between the different wind data sets show the importance of further global wind observations in the

350 upper mesosphere and lower thermosphere, and particularly in the tropics. As there are notable differences between different
wind data sets, in Sect. 7 we will compare SABER gravity wave observations to several different wind data sets in order to find
out which findings are robust and widely independent of the wind data used.

5 Gravity wave driving of the SAO in reanalyses

355 Given the limitations of the different reanalyses, and the differences in the representation of the SAO, it is not expected that
estimates of the SAO gravity wave driving from the reanalyses will be fully realistic. In particular the magnitude of the gravity
wave driving might not be very robust. However, our knowledge of the driving of the SAO is relatively poor, and in Sect. 4.1
we have seen that all reanalyses are capable of reproducing some features of the SAO. Therefore, it is expected that estimates
of the SAO gravity wave driving in reanalyses will provide important information about the mechanisms that drive the SAO.
360 This information can already be obtained from relative variations of the gravity wave driving, and the exact magnitude is not
needed.

5.1 Estimates of gravity wave drag from reanalyses

Based on the transformed Eulerian mean (TEM) zonal mean momentum budget an expected value of the zonal-mean zonal gravity wave drag can be estimated from reanalyses. The zonal mean momentum equation is given by

$$\frac{\partial \bar{u}}{\partial t} + \bar{v}^* \left(\frac{(\bar{u} \cos \phi)_\phi}{a \cos \phi} - f \right) + \bar{w}^* \bar{u}_z = \bar{X}_{PW} + \bar{X}_{GW} \quad (3)$$

365 Here, \bar{u} is the zonal-mean zonal wind, $\partial \bar{u} / \partial t$ the zonal wind tendency, \bar{v}^* and \bar{w}^* are the TEM meridional and vertical wind, respectively, f is the Coriolis frequency, a the Earth's radius, and ϕ the geographic latitude. \bar{X}_{PW} and \bar{X}_{GW} are the zonal-mean zonal wave drag due to global-scale waves and gravity waves, respectively. Subscripts ϕ and z stand for differentiation in meridional and vertical direction, respectively. Overbars indicate zonal averages.

All terms in Eq. (3) except for \bar{X}_{GW} can be calculated from the resolved meteorological fields of the reanalysis. The resolu-
370 tion (both horizontally and vertically) of the general circulation models used in the reanalyses, however, is too coarse to properly resolve all scales of gravity waves. This means that part of the gravity wave spectrum is not resolved by the models, and amplitudes of resolved gravity waves are usually underestimated (e.g., Schroeder et al., 2009; Preusse et al., 2014; Jewtoukoff et al., 2015). Therefore, free-running general circulation models and reanalyses utilize parameterizations to simulate the contribution of gravity waves to the momentum budget (e.g., Fritts and Alexander, 2003; Kim et al., 2003; Alexander et al., 2010;
375 Geller et al., 2013).

Unlike those of free-running models, the meteorological fields of reanalyses are constrained by assimilation of numerous observations. Where constrained by observations, the meteorological fields of reanalyses can be assumed to be quite realistic. Under this assumption, the contribution \bar{X}_{GW} in Eq. (3) can be calculated from the residual term (“missing drag”) remaining after quantifying all other contributions from the model-resolved fields (e.g., Alexander and Rosenlof, 1996; Ern et al., 2014,
380 2015).

Like in Ern et al. (2015), we calculate the zonal-mean zonal wave drag \overline{X}_{res} due to waves that are resolved by the model from the divergence of the Eliassen-Palm flux (EP-flux). Further, we assume that the zonal drag due to global-scale waves can be approximated based on the resolved flux at zonal wavenumbers k lower than 21:

$$\overline{X}_{PW} = \overline{X}_{res}(k < 21) \quad (4)$$

385 Under this assumption, our estimate of the “total” zonal mean gravity wave drag \overline{X}_{GW} comprises the drag of model-resolved waves at zonal wavenumbers higher than 20 ($\overline{X}_{res}(k > 20)$), gravity wave drag that is parameterized in the model (\overline{X}_{param}), and the remaining imbalance ($\overline{X}_{imbalance}$) in the momentum budget that is caused by, for example, data assimilation:

$$\overline{X}_{GW} = \overline{X}_{res}(k > 20) + \overline{X}_{param} + \overline{X}_{imbalance} \quad (5)$$

with the “missing drag” consisting of the sum of \overline{X}_{param} and $\overline{X}_{imbalance}$.

390 5.1.1 ERA-Interim and JRA-55

~~Figures ?? and ?? show the estimated~~

5.2 Discussion of the different contributions to \overline{X}_{GW}

Figure 4 shows the “typical year” of the estimated “total” gravity wave drag ~~for ERA-Interim and JRA-55, respectively,~~ averaged \overline{X}_{GW} for the four reanalyses considered. Again, the “typical year” was obtained by averaging over the latitude band
395 10°S–10°N and the years 2002 until 2018. Distributions for the single years are shown in Figs. S8–S11 in the Supplement.

5.2.1 Model-resolved gravity wave drag $\overline{X}_{res}(k > 20)$

Similar as Fig. 4, Fig. 5 shows the contribution $\overline{X}_{res}(k > 20)$ of model-resolved gravity waves at zonal wavenumbers $k > 20$. The corresponding distributions for the single years are shown in the Supplement in Figs. S12–S15. ~~Similar as~~

As can be seen from Figs. 4 and 5, the resolved gravity wave drag is negligible in ERA-Interim, JRA-55, and MERRA-2.
400 (Please note that in Fig. ??, the 4 the range of the color scale is $\pm 7.5 \text{ m s}^{-1} \text{ day}^{-1}$, while it is only $\pm 0.25 \text{ m s}^{-1} \text{ day}^{-1}$ in Fig. 5a, 5b, and 5d, and $\pm 1.25 \text{ m s}^{-1} \text{ day}^{-1}$ in Fig. 5c.) Only for ERA-5 below 55 km $\overline{X}_{res}(k > 20)$ sometimes contributes as much as about 50% to \overline{X}_{GW} . In the upper stratosphere and lower mesosphere, for both \overline{X}_{GW} and $\overline{X}_{res}(k > 20)$ eastward gravity wave drag is ~~given~~ stronger than westward gravity wave drag, which is likely a consequence of the QBO wave filtering in the stratosphere below.

405 Strictly speaking, introducing a zonal wavenumber limit of $k = 20$ in order to separate gravity waves from larger-scale atmospheric variations is somewhat arbitrary. In particular, it is assumed that gravity waves propagate mainly zonally. In the tropics, this assumption should be fulfilled because the gravity wave distribution is modulated by the background wind, and in the tropics zonal winds are usually much stronger than meridional winds. Further, the fact that for the reanalyses the resolved gravity wave drag $\overline{X}_{res}(k > 20)$ contributes only to a minor extent to the total gravity wave drag \overline{X}_{GW} shows
410 that the exact choice of a wavenumber threshold will not affect \overline{X}_{GW} by much. Therefore, it is not expected that different

methods to extract gravity waves from the model fields — for example, by introducing thresholds using spherical coordinates (e.g., Watanabe et al., 2008; Becker and Vadas, 2018) — would lead to different conclusions.

5.2.2 Parameterized gravity wave drag \overline{X}_{param}

415 For JRA-55 and MERRA-2 also the parameterized gravity wave drag is provided in the data repositories. Fig. 6a shows the “typical year” of parameterized gravity wave drag \overline{X}_{param} for JRA-55, and Fig. 6b shows the same, but for MERRA-2 (please note that for MERRA-2 \overline{X}_{param} is not available for the whole altitude range). Distributions for the single years 2002–until 2018, as well as averaged over these years (lower right panel 2002–2018 are shown in the Supplement in Figs. S16 and S17.

420 As can be seen from Fig. 6a, for JRA-55 the parameterized gravity wave drag \overline{X}_{param} is closely linked with and opposite to the background wind. This is expected because JRA-55 does not have an explicit nonorographic gravity wave parameterization and uses only Rayleigh friction at upper levels. A similar distribution would be expected for ERA-Interim, because ERA-Interim also uses Rayleigh friction at upper levels and does not have a nonorographic gravity wave parameterization.

425 For MERRA-2 (Fig. 6b), the situation is completely different. Comparing Fig. 4d and Fig. 6b, it is evident that for MERRA-2 in the whole altitude range \overline{X}_{GW} and \overline{X}_{param} are almost the same, and both are linked more closely to the vertical gradient of the zonal wind, and not to the zonal wind speed itself. Obviously, this is an effect of the MERRA-2 nonorographic gravity wave drag scheme (Garcia and Boville, 1994; Molod et al., 2015) which includes some realistic gravity wave physics instead of just using Rayleigh friction.

5.2.3 The imbalance gravity wave drag term $\overline{X}_{imbalance}$

430 For JRA-55 and MERRA-2 also the imbalance term $\overline{X}_{imbalance}$ can be calculated. For JRA-55 the “typical year” is given in Fig 6c, and for MERRA-2 in Fig 6d. The distribution for single years is given in Figs. ?? and ??, respectively). Figures ?? and ?? show that S18 and S19 in the Supplement.

As can be seen from Fig. 6c, for JRA-55, above 40 km the remaining imbalance is strongly positive. This likely indicates that a really large positive assimilation increment is needed to compensate the unrealistic effect of Rayleigh friction, and to keep the model temperature and winds in agreement with assimilated observations. The situation should be similar for ERA-Interim.

435 For MERRA-2 $\overline{X}_{imbalance}$ (Fig. 6d) is close to zero. Apparently, in the tropics the nonorographic gravity wave drag scheme of MERRA-2 has been tuned in a way to minimize the assimilation increment caused by the assimilation of MLS and other data (see also Molod et al., 2015). This should be the reason why MERRA-2 simulates a reasonable SAO even in the years when MLS data were not yet available (i.e., in the period prior to August 2004).

5.3 Gravity wave driving of the SAO in ERA-Interim and JRA-55

440 Figures 4a and 4b show the “typical year” of the estimated “total” gravity wave drag in \overline{X}_{GW} for ERA-Interim and JRA-55, respectively. In the altitude range 45–55 km total gravity wave drag \overline{X}_{GW} is usually directed eastward, contributing to the driving of the eastward phase of the stratopause SAO with a maximum value of about $5 \text{ m s}^{-1} \text{ day}^{-1}$. Westward gravity wave

driving in the stratopause region is much weaker and, on average, does not contribute much to the driving of the stratopause SAO. This asymmetry has been pointed out before for ERA-Interim by Ern et al. (2015). At high altitudes eastward gravity wave drag strongly increases, which is likely not realistic and an effect of the sponge layer close to the model tops. This increase is most obvious above ~ 55 km for ERA-Interim, and above ~ 45 km for JRA-55. Still, even though not very physical, the sponge layer effect seems to help simulate a more realistic SAO (Polichtchouk et al., 2017). Switching off the sponge leads to stronger mesospheric eastward winds at the equator.

5.3.1 MERRA-2

5.4 Gravity wave driving of the SAO in MERRA-2

Analogously to ERA-Interim and JRA-55, Fig. ??-4d shows that the MERRA-2 gravity wave driving \overline{X}_{GW} in the altitude region 45–55 km (around the stratopause) is prevalently directed eastward with peak values of. Peak values of eastward gravity wave drag in the single years are about $7 \text{ m s}^{-1} \text{ day}^{-1}$ (see Fig. S11 in the Supplement), i.e. stronger than in ERA-Interim and JRA-55 (see Figs. S8 and S9 in the Supplement). Westward directed gravity wave drag in the stratopause region is generally weaker with peak values of usually $\sim 2 \text{ m s}^{-1} \text{ day}^{-1}$.

In the stratosphere, the QBO westward and eastward phases are usually stacked, and, since the zonal wind is usually stronger during QBO westward phases than during QBO eastward phases, the range of westward gravity wave phase speeds encountering critical level filtering is usually larger than the range of eastward phase speeds. This will lead to an asymmetry of the gravity wave spectrum with a larger amount of eastward momentum flux entering the stratopause region and the mesosphere, and, consequently, to the prevalently eastward driving of the stratopause SAO by gravity waves.

At times, the QBO eastward and westward phases are not perfectly stacked, resulting in less pronounced asymmetric wave filtering by the QBO. This is the case, for example, during April to June 2006 and April to June 2013. During these periods we find also relatively strong westward directed gravity wave drag in the stratopause region (around 50 km altitude), and these enhancements seem to contribute to the formation of stronger downward propagating SAO westward phases (see Fig. S11 in the Supplement). Indications for the less asymmetric filtering of the gravity wave spectrum during 2006 were also found before from satellite observations (Ern et al., 2015).

Different from ERA-Interim and JRA-55, MERRA-2 assimilates MLS observations in the mesosphere. Further, the MERRA-2 model top is at higher altitudes, and increased damping is used only above ~ 58 km. Therefore, reasonable estimates of gravity wave drag should also be possible in the middle mesosphere. It is striking that in the altitude range 55 km to somewhat above 65 km westward gravity wave drag is increased compared to the stratopause region, and sometimes is as strong as eastward gravity wave drag. In this altitude range, the westward gravity wave drag often contributes to the closure of the mesospheric SAO eastward wind jet at its top. Nevertheless, in this altitude range, the westward gravity wave drag is still, on average, only about half as strong as eastward gravity wave drag as shown from the multi-year average (Fig. ??, lower-right panel 4d). At altitudes above ~ 65 km there is a sudden increase of eastward gravity wave drag in MERRA-2, which is likely unrealistic and related to damping in the sponge layer close to the model top, similar as in ERA-Interim and JRA-55.

475 Note that MERRA-2 gravity wave drag is more strongly linked to vertical gradients of the background wind than is the case
 for ERA-Interim and JRA-55. Different from ERA-Interim and JRA-55, MERRA-2 uses a nonorographic gravity wave drag
 scheme. This scheme was additionally tuned to improve the QBO and the SAO in the tropics (Molod et al., 2015). Therefore,
 the strong link between gravity wave drag and vertical gradients of the background wind could be an effect of the dedicated
 tuning of this gravity wave drag parameterization. This effect will be investigated in more detail in Sect. 7 based on satellite
 480 data, and in Sect. 8 for the reanalyses.

5.4.1 ERA-5

5.5 Gravity wave driving of the SAO in ERA-5

Like ERA-Interim, JRA-55, and MERRA-2, the ERA-5 reanalysis shows an asymmetry between eastward and westward
 gravity wave drag in the stratopause region (Fig. ??4c). However, peak values of eastward gravity wave drag are somewhat
 485 lower than those of MERRA-2. Furthermore, in the stratopause region, enhanced values of gravity wave drag are not as closely
 linked to zonal wind vertical gradients as it is the case for MERRA-2. This finding is surprising because, like MERRA-2,
 ERA-5 contains a nonorographic gravity wave drag scheme. Possibly, this difference is caused by different settings of the
 gravity wave drag schemes. For instance, enhanced gravity wave momentum fluxes were introduced in the tropics to improve
 the representation of the QBO and the SAO in MERRA-2 (Molod et al., 2015), which is different in ERA-5.

490 The ERA-5 characteristics change at altitudes above about 65 km. At these altitudes also in ERA-5 enhanced gravity wave
 drag is closely linked to zonal wind vertical gradients, and strong westward directed gravity wave drag contributes to the
 reversal of the mesospheric eastward directed winds and the formation of the mesopause SAO, qualitatively consistent with
 MERRA-2. In MERRA-2, however, there is no clear wind reversal. Possibly, the sponge layer in MERRA-2 is stronger than
 that in ERA-5, preventing the formation of a clear MSAO. Still, there is some eastward directed gravity wave drag near the
 495 model top in ERA-5 that seems to be related to the model sponge layer, but that is much weaker than in MERRA-2.

6 The SAO as seen in satellite data

5.1 Interpolated quasi-geostrophic winds in the tropics

Following the approach used in previous studies (e.g., Oberheide et al., 2002; Ern et al., 2013; Smith et al., 2017; Sato et al., 2018)
 , quasi-geostrophic winds can be calculated from the geopotential fields derived from satellite soundings. For stationary
 500 conditions, and neglecting the drag exerted by atmospheric waves, the zonal and meridional momentum equations can be
 written as follows-

$$\underline{- \left(f + \frac{u \tan \phi}{a} \right) v + \frac{1}{a \cos \phi} \frac{\partial \Phi}{\partial \lambda} = 0}$$

$$\underline{\left(f + \frac{u \tan \phi}{a} \right) u + \frac{1}{a} \frac{\partial \Phi}{\partial \phi} = 0}$$

505 Here, u and v are the zonal and the meridional wind, respectively, a the Earth radius, ϕ the geographic latitude, and Φ the geopotential. For further details see Andrews et al. (1987), Oberheide et al. (2002), or Ern et al. (2013). These equations can be easily solved for u and v .

The quasi-geostrophic approach gives good results in the extratropics, but is not reliable in the tropics because the Coriolis parameter is close to zero. Recently, it has been shown by Smith et al. (2017) that an interpolation of the quasi-geostrophic zonal wind starting from 10°S and 10°N can be used as a proxy for the zonal wind at the equator and is in good agreement with wind observations by lidar below about 80 .

As direct wind observations in the tropical mesosphere are sparse, we will also make use of this approach, even though interpolated quasi-geostrophic winds will still be affected by biases. In order to make sure that our findings are robust, we will use a number of different zonal wind data sets in Sects. 6 and 7 to check whether our findings of the SAO gravity wave driving hold for different choices of background winds.

For our study, we utilize zonal-average quasi-geostrophic zonal winds calculated for time intervals of three days with a time step of three days, i.e. the time windows used for calculating the winds are non-overlapping. This data set has been previously used for studies in the extratropics (Ern et al., 2013, 2016; Matthias and Ern, 2018). For studying the interaction of gravity waves with the SAO zonal wind in the latitude band 10°S – 10°N , we use the average of the quasi-geostrophic wind at 12°S and 12°N as a proxy for the zonal wind in this latitude band at altitudes above 45 , similar as in Smith et al. (2017). At lower altitudes, reanalysis winds should be more reliable, so we do not use quasi-geostrophic winds at altitudes below 35 . Instead, we use the ERA-Interim winds already presented in Fig. ??, and a smooth transition between ERA-Interim and quasi-geostrophic winds derived from SABER or MLS satellite observations in the altitude range 35 – 45 .

5.1 MLS quasi-geostrophic winds

525 For particular comparison with the MERRA-2 reanalysis that assimilates MLS data, Fig. ?? shows zonal winds for the merged data set of ERA-Interim and interpolated MLS quasi-geostrophic winds. To reduce the effect of tides, MLS winds are calculated from an average over ascending and descending orbit branches, i.e. data from the two MLS equator crossing times are averaged. As MLS observations started in mid-2004, the panels for the years 2002 and 2003 are left blank.

Figures ?? and ?? show that at altitudes below ~ 60 MLS and MERRA-2 winds are very similar. On the one hand, this is expected because MLS data are assimilated in MERRA-2. On the other hand, this shows that our interpolated quasi-geostrophic winds are useful in the tropics. Still, these interpolated winds are not considered to be reliable at altitudes above ~ 75 . This is indicated, for example, by the more eastward winds and the overly short duration of the SAO westward wind phases at altitudes above ~ 70 when compared with the SPARC climatology. This bias is possibly an effect of tides. Although both ascending and descending nodes enter the estimation of MLS quasi-geostrophic winds, it is not expected that tidal effects will completely cancel out.

5.1 Merged SABER quasi-geostrophic and TIDI wind observations

So far we have discussed wind data sets of four reanalyses, as well as interpolated quasi-geostrophic winds based on MLS observations. Another main purpose of our work is to study the interaction of SABER gravity wave observations with the background wind. Of course, both the SAO and tides contribute to the variations of the winds in the tropics. As shown in Fig. ??, the local solar times of SABER equator crossings slowly change over time. Therefore, it is important to compare gravity wave observations and winds observed at the same local solar times.

For this purpose, we have composed a combined data set of SABER quasi-geostrophic winds in the altitude range 45–75, ERA-Interim winds below 35, and a smooth transition between ERA-Interim and SABER winds in the altitude range 35–45. At altitudes above ~ 80 we use directly observed TIDI “cold side” winds. As shown in Fig. ??, the local solar time of TIDI cold side winds matches the local solar times of SABER observations better than about half an hour. Winds in the gap between 75 and 80 are interpolated. Similar as in the study of Dhadly et al. (2018), we omit less reliable TIDI data from periods when the angle β between orbital plane and the Earth-Sun vector exceeds 55° , i.e. when the TIMED orbital plane is near the terminator. Data gaps that are caused by omitting these data, as well as other data gaps that are shorter than 40 are closed by linear interpolation in time. A larger data gap from November 2016 until March 2017 is closed by using interpolated SABER quasi-geostrophic winds also at altitudes above 75. Interpolated SABER quasi-geostrophic winds are used above 75 also before April 2002, because TIDI cold side winds are available only after that date.

Figure ?? shows these combined winds. SABER and TIDI winds were averaged over ascending and descending TIMED satellite equator passings, i.e., they represent an average over different local solar times. At altitudes below ~ 70 these winds are very similar to those derived from MLS (see Fig. ??). Although ascending and descending orbit data are combined, there are notable variations that are related to the 60-day yaw cycle of the TIMED satellite and the corresponding changes in the local solar time of SABER and TIDI observations. This shows the importance of selecting wind data at the correct local solar time, particularly at higher altitudes.

The main difference between Fig. ?? and Fig. ??, however, are the winds at altitudes above 80 where TIDI wind observations are used. On average, the TIDI winds are more westward than the quasi-geostrophic winds derived from MLS, and even somewhat more westward than the SPARC climatology (Fig. ??, lower right). Particularly the maxima of both SAO eastward phases at altitudes above around 85 are less pronounced. Because at altitudes above 80 variations that are linked to the TIMED yaw cycles and the corresponding changes in local solar time are quite strong, this could be an effect of tides. The TIDI instrument samples atmospheric tides at the same phase as SABER. Since wind variations due to tides can be of the same magnitude as variations due to the SAO, the combined data set of SABER and TIDI winds should therefore be the best choice for representing the atmospheric background conditions relevant for SABER gravity wave observations.

A more comprehensive analysis of tides based on TIDI winds has been carried out in previous studies (e.g., Oberheide et al., 2006; Wu et al., 2017). An in-depth investigation of the effect of tides on the distribution of gravity waves, however, is beyond the scope of our study. Overall, the differences between the different wind data sets show the importance of further global wind observations in the upper mesosphere and lower thermosphere, and particularly in the tropics. As there are notable differences between different wind data sets, in Sect. 7 we will compare SABER gravity wave observations to several different wind data sets in order to find out which findings are robust and widely independent of the wind data used.

6 Satellite observations of the SAO driving by gravity waves

One of the key parameters that is relevant for the interaction of gravity waves with the background flow is the vertical flux of gravity wave pseudomomentum (\mathbf{F}_{ph}), denoted in the following as “gravity wave momentum flux”. The momentum flux of a gravity wave is given as:

$$\mathbf{F}_{ph} = (F_{px}, F_{py}) = \rho \left(1 - \frac{f^2}{\hat{\omega}^2} \right) (\overline{u'w'}, \overline{v'w'}) \quad (6)$$

with F_{px} and F_{py} the gravity wave momentum flux in zonal and meridional direction, respectively, ρ the atmospheric density, f the Coriolis frequency, $\hat{\omega}$ the intrinsic frequency of the gravity wave, and (u', v', w') the vector of zonal, meridional and vertical wind perturbations due to the gravity wave (e.g., Fritts and Alexander, 2003). If a gravity wave propagates conservatively, the momentum flux of a gravity wave stays constant. However, if a gravity wave dissipates while propagating upward, momentum flux is no longer conserved, and the gravity wave exerts drag on the background flow. This drag (X, Y) is related to the vertical gradient of momentum flux:

$$(X, Y) = -\frac{1}{\rho} \frac{\partial \mathbf{F}_{ph}}{\partial z} \quad (7)$$

with X and Y the gravity wave force in zonal and meridional direction, respectively, and z the vertical direction. As will be explained in the next subsection, gravity wave momentum flux can also be derived from temperature observations of satellite instruments.

6.1 Estimates of absolute gravity wave momentum fluxes and drag from SABER observations

6.1.1 Absolute momentum fluxes

For deriving gravity wave momentum fluxes from temperature altitude profiles observed by SABER, we make use of the method described in our previous studies (Ern et al., 2004, 2011; Ern et al., 2018). First, the atmospheric background temperature is estimated, separately for each altitude profile. This estimate consists of the zonal average temperature profile. Further, 2D zonal-wavenumber / wave-frequency spectra are determined from SABER temperatures for a set of latitudes and altitudes. Based on these spectra, the contribution of global-scale waves is calculated at the location and time of each SABER observation. Both zonal average profile and global scale waves are removed from each altitude profile.

For our study, it is important that this 2D spectral approach is capable of ~~effectively~~ effectively removing all global-scale waves that are important in the tropics, such as inertial instabilities in the tropical stratosphere and stratopause region (e.g., Rapp et al., 2018; Strube et al., 2020), and different equatorial wave modes in the stratosphere (e.g., Ern et al., 2008) and in the mesosphere and mesopause region (e.g., Garcia et al., 2005; Ern et al., 2009). In particular, Kelvin waves contribute significantly to the temperature variances in the tropics and are difficult to remove by other techniques because they can have very short wave periods, and their vertical wavelengths are in the same range as that of small scale gravity waves. Each altitude profile is additionally high-pass filtered to remove fluctuations of vertical wavelengths longer than about 25 km to focus on those gravity waves that are covered by our momentum flux analysis, and to remove remnants of global-scale waves. Further,

we explicitly remove tides by removing offsets and quasi-stationary zonal wavenumbers of up to 4, separately for ascending and descending orbit parts of SABER. In this way, we cover major tidal modes, such as the diurnal westward zonal wavenumber 1 (DW1), the semidiurnal westward zonal wavenumber 2 (SW2), and the diurnal eastward zonal wavenumber 3 (DE3). The final result of this procedure are altitude profiles of temperature fluctuations that can be attributed to small scale gravity waves.

As introduced by Preusse et al. (2002), for each altitude profile the amplitude, vertical wavelength λ_z , and the phase of the strongest wave component are determined in sliding 10–km vertical windows. Provided a close enough spacing in space and time, the gravity wave horizontal wavelength parallel to the satellite measurement track ($\lambda_{h,AT}$) can be estimated from pairs of consecutive altitude profiles if the same wave is observed with both profiles of a pair. To make sure that the same wave is observed in both profiles of a pair, a vertical wavelength threshold is introduced and we assume that the same wave is observed if λ_z differs between the two profiles by not more than 40%. Pairs with non-matching vertical wavelengths are discarded. This omission of pairs does not introduce significant biases in distributions of gravity wave squared amplitudes (e.g., Ern et al., 2018). Therefore the selected pairs should be representative of the whole distribution of gravity waves.

Taking $\lambda_{h,AT}$ as a proxy for the true horizontal wavelength λ_h of a gravity wave, absolute values of gravity wave momentum flux F_{ph} can be estimated:

$$F_{ph} = \frac{1}{2} \rho \left(\frac{g}{N} \right)^2 \frac{\lambda_z}{\lambda_h} \left(\frac{\hat{T}}{\bar{T}} \right)^2 \quad (8)$$

with g the gravity acceleration, N the buoyancy frequency, \bar{T} the background temperature, and \hat{T} the gravity wave temperature amplitude (see also Ern et al., 2004).

~~Main error sources of F_{ph} are the undersampling of short horizontal wavelength waves (aliasing), the overestimation of λ_h by $\lambda_{h,AT}$. Generally, the use of along-track gravity wave horizontal wavenumbers $k_{h,AT} = 2\pi/\lambda_{h,AT}$ as a proxy for the true gravity wave horizontal wavenumbers $k_h = 2\pi/\lambda_h$ will lead to a low-bias of SABER momentum fluxes (the momentum flux is proportional to the horizontal wavenumber). This is the case because $k_{h,AT}$ will always underestimate k_h (see also, for example Preusse et al. (2009), Alexander (2015), Ern et al. (2017, 2018), or Song et al. (2018)), and the attenuation of gravity wave amplitudes by.~~ In the tropics, the measurement tracks of satellites in low Earth orbit are usually oriented close to north-south, while the wave vectors of gravity waves should be oriented close to east-west, which will lead to even increased errors and stronger low-biases of momentum fluxes in the tropics.

This effect has roughly been estimated by Ern et al. (2017) using observations of the Atmospheric Infrared Sounder (AIRS) satellite instrument. Because AIRS provides 3D temperature observations, it is possible to determine from AIRS observations true gravity wave horizontal wavenumbers, as well as along-track gravity wave horizontal wavenumbers. This opportunity has been taken by Ern et al. (2017) to compare true and along-track gravity wave horizontal wavenumbers: AIRS observations indicate an underestimation of the along-track wavenumber (corresponding to an underestimation of momentum fluxes) by a factor between 1.5 and somewhat above 2.

In addition, for SABER there will be aliasing effects (undersampling of observed gravity waves) and effects of the instrument sensitivity function of limb sounding satellite instruments (see also, for example Preusse et al., 2002), which should both lead

to an even stronger underestimation of gravity wave momentum fluxes. The approximate SABER sensitivity function is given in Ern et al. (2018), and a comprehensive discussion of the observational filter of infrared limb sounders is given in Trinh et al. (2015). As was estimated by Ern et al. (2004) overall errors of F_{ph} are large, at least a factor of two, and F_{ph} is likely strongly low-biased.

640 ~~In situations of strong vertical shear of the background winds~~

6.1.2 A proxy for absolute gravity wave drag (SABER MFz-proxy-|GWD|)

Using the vertical gradient of absolute gravity wave momentum flux, a proxy of the absolute gravity wave forcing XY on the background flow can be estimated ~~from the vertical gradient of absolute gravity wave momentum flux:~~

$$XY = -\frac{1}{\rho} \frac{\partial F_{ph}}{\partial z}. \quad (9)$$

645 ~~For additional details please see Warner et al. (2005) and Ern et al. (2011). Similar to~~ In the following, this proxy will be called “SABER MFz-proxy-|GWD|”.

~~A strong limitation is that, like for absolute gravity wave momentum fluxes, no directional information is available for XY , but it can often be assumed that the SABER MFz-proxy-|GWD|. Without further criteria being met, net gravity wave drag and the could be even zero due to cancellation effects, while SABER MFz-proxy-|GWD| may result in substantial drag.~~

650 However, if predominately gravity waves of one preference propagation direction dissipate, the vertical gradient of absolute gravity wave momentum flux is dominated by momentum loss in that direction and the results are meaningful. This will be the case in two scenarios: first, in a strong vertical gradient of the background wind ~~have the same direction. Based on this assumption, meaningful results were obtained already in several studies in the extratropics (Ern et al., 2013, 2016) and, particularly, in the tropics for the QBO in the stratosphere (Ern et al., 2014) and the stratopause SAO (Ern et al., 2015). close to~~
655 a wind reversal, gravity waves intrinsically propagating opposite to the wind are refracted to shorter vertical wavelengths and dissipate. The corresponding momentum transfer will mainly act to further decelerate the jet and facilitate the wind reversal. Second, if gravity waves dissipate that have already a strong preference direction, e.g., by filtering at altitudes below, the resulting drag will act in this preference direction. In these two cases cancellation effects due to dissipation of gravity waves of different propagation direction are relatively low, and SABER MFz-proxy-|GWD| can give information about the relative
660 variations of absolute net gravity wave drag. For a further discussion please see Warner et al. (2005) and Ern et al. (2011). And for previous applications of SABER MFz-proxy-|GWD|, please see, for example, Ern et al. (2013, 2014, 2015), and Ern et al. (2016).

~~Of course, the same low biases and observational limitations as mentioned in Sect 6.1.1 for absolute gravity wave momentum fluxes apply, which means that the magnitude of the SABER MFz-proxy-|GWD| is highly uncertain, and is likely underestimated in the cases when the SABER MFz-proxy-|GWD| provides meaningful information.~~

Similarly to Ern et al. (2015), our data sets of SABER absolute gravity wave momentum fluxes and ~~gravity wave drag of SABER MFz-proxy-|GWD|~~ are averages over 7 days with a step of 3 days, i.e., the time windows used for averaging are

overlapping. In the following, we will discuss the interaction of the observed gravity waves with the background winds in the tropics.

670 6.2 Effect of the background winds on SABER gravity wave momentum fluxes

First, we investigate how SABER absolute gravity wave momentum fluxes are modulated by the background winds. ~~Figure ?? shows absolute gravity wave momentum fluxes observed by SABER, averaged~~ Figure 7a shows the “typical year” of SABER absolute momentum fluxes. Values were obtained by averaging over the years 2002 until 2018, and over the latitude band 10°S – 10°N . We also average over data from ascending and descending parts of the satellite orbit to reduce the effect of tides. ~~Shown are distributions for the~~ Distributions for the single years 2002–2018 ~~, as well as an average over the whole 2002–2018 period (lower right are shown~~ in Fig. ??). ~~S20 in the Supplement.~~ Contour lines represent the combined data set of zonal winds from ERA-Interim, SABER quasi-geostrophic winds, and TIDI direct wind observations (E/S/T-winds), as presented in Fig. ??3b.

~~Figure ??~~ Figure 7a shows that absolute gravity wave momentum flux in the stratopause region and in the middle mesosphere ~~is usually strongest during periods of westward winds. This finding is consistent with the results obtained for the SSAO by Ern et al. (2015) and indicates that, due to the selective filtering of the gravity wave spectrum by the QBO in the stratosphere, the gravity wave spectrum in the stratopause region and in the middle mesosphere is dominated by gravity waves of eastward directed phase speeds. An overall decrease of momentum fluxes with altitude shows that gravity waves dissipate gradually with increasing altitude. In addition to this overall decrease, momentum fluxes decrease more strongly in zones of eastward~~ ~~(positive) wind shear, which indicates that gravity waves interact with the SAO winds in the stratopause region and middle mesosphere and contribute to the driving of the SAO. This effect will be investigated in more detail in Sect. 6.3 based on~~ vertical gradients of absolute gravity wave momentum fluxes, the SABER MFz-proxy-|GWD|. In the upper mesosphere and in the mesopause region, there is no such clear relationship between momentum fluxes and positive wind shear. This effect will also be discussed later in Sect. 6.3.

690 6.3 Interaction of the SABER ~~absolute gravity wave drag~~ MFz-proxy-|GWD| and the tropical zonal wind

~~Figure ?? shows SABER absolute gravity wave drag that is calculated from vertical gradients of SABER absolute gravity wave momentum fluxes.~~ Figure 7b shows the “typical year” of the SABER MFz-proxy-|GWD| obtained by averaging over the years 2002 until 2018. Again, values are averaged over the latitude band 10°S – 10°N and over ascending and descending orbit data. ~~Similarly to Fig. ??, distributions of absolute gravity wave drag are shown for each given year of the~~ Distributions for the single years 2002–2018 ~~period. The lower right panel are shown~~ in Fig. ?? ~~is an average over the whole 2002–2018 period.~~ S21 in the Supplement. Contour lines represent the zonal winds shown in Fig. ??-3b. From Fig. ??-7b we can see that ~~SABER absolute gravity wave drag~~ the SABER MFz-proxy-|GWD| generally increases with height from close to zero at 30 km to around $20 \text{ m s}^{-1} \text{ day}^{-1}$ between 80 and 90 km. It has a local maximum around 50 km with peak values of about $1\text{--}2 \text{ m s}^{-1} \text{ day}^{-1}$, and another local maximum between around 80 and 85 km with peak values of about $30 \text{ m s}^{-1} \text{ day}^{-1}$ during

700 single years. Peak values are somewhat reduced for the “typical year”. The first maximum is likely related to the SSAO, while the second maximum is likely related to the MSAO.

6.3.1 The SSAO and the SAO in the middle mesosphere

In the stratopause region, peak values of ~~SABER absolute gravity wave drag~~ SABER MFz-proxy-|GWD| are seen mainly during eastward wind shear, while values are much reduced during westward wind shear, indicating that gravity wave drag is mainly directed eastward and contributes to the driving of the SAO eastward wind phases. This finding is consistent with the HIRDLS observations discussed by Ern et al. (2015) and becomes even clearer when looking at Figs. ~~?? and ??~~ 7c and 7d.

705 Figures ~~?? and ?? show for each year, as well as for the 2002–2018 average year, the SABER absolute gravity wave drag anomaly, i.e. for each year~~ 7c and 7d show the absolute gravity wave drag is divided by the “typical year” of SABER MFz-proxy-|GWD| normalized by the altitude-dependent annual mean. These normalized distributions are calculated for each year 2002 until 2018 (see Figs. S22 and S23 in the Supplement), and then averaged to obtain the “typical year”. Overplotted contour lines in Fig. ~~??~~ 7c represent the zonal winds shown in Fig. ~~??~~ 3b, while the contour lines in Fig. ~~??~~ 7d represent the vertical gradient of this zonal wind. ~~Figures ?? and ?? reveal that SABER absolute gravity wave drag~~ Figures 7c and 7d reveal that SABER MFz-proxy-|GWD| is enhanced mainly during eastward wind shear, not only in the stratopause region, but in the whole altitude range of about 40–70 km.

715 Parts of the gravity wave spectrum, particularly those of slow ground based phase speeds, have encountered critical levels already at lower altitudes by the QBO (cf. Ern et al., 2014, 2015) and cannot contribute to the SAO driving. Therefore, an enhancement of gravity wave drag mainly during eastward zonal wind shear does not necessarily mean that critical level filtering of gravity waves is the only dominant process. Another effect of vertical wind shear, in addition to the formation of critical levels, is a reduction of intrinsic phase speeds for parts of the gravity wave spectrum and, thus, a reduction of gravity wave saturation amplitudes for this part of the spectrum. This means that wave saturation apart from critical levels, i.e. saturation of high ground based phase speed gravity waves, can also play an important role in the stratopause region, and even more at higher altitudes. Indications for the importance of saturation of high phase speed gravity waves for the SSAO were indeed found by Ern et al. (2015) by investigating gravity wave momentum flux spectra observed from satellite.

725 In the stratopause region the magnitudes of ~~SABER gravity wave drag~~ SABER MFz-proxy-|GWD| (peak values of around $1\text{--}2\text{ m s}^{-1}\text{day}^{-1}$) are similar or even stronger than those obtained by model simulations of the SSAO (e.g., Richter and Garcia, 2006; Osprey et al., 2010; Peña–Ortiz et al., 2010; Smith et al., 2020) and similar to values derived from Rayleigh lidar observations (Deepa et al., 2006; Antonita et al., 2007). Comparison with the reanalyses gives a somewhat different picture: SABER gravity wave drag is usually weaker than peak values of eastward gravity wave drag of the four reanalyses considered in our study. For example, at around 50 km altitude peak values of eastward gravity wave drag in the multi-year averages are around $3\text{ to }4\text{ m s}^{-1}\text{day}^{-1}$ for ERA-Interim (cf. Fig. ~~??~~ 4a), $3\text{ to }6\text{ m s}^{-1}\text{day}^{-1}$ for JRA-55 (cf. Fig. ~~??~~ 4b), but values could be already affected by the model sponge layer), $\sim 3\text{ m s}^{-1}\text{day}^{-1}$ for ~~MERRA-2~~ ERA-5 (cf. Fig. ~~??~~ 4c), and $\sim 2\text{ m s}^{-1}\text{day}^{-1}$ for ~~ERA-5~~ MERRA-2 (cf. Fig. ~~??~~ 4d).

Generally, observations cover only parts of the whole spectrum of gravity waves and should therefore underestimate gravity wave drag. An underestimation of the gravity wave drag derived from SABER observations would be expected for two reasons. First, SABER momentum fluxes are likely underestimated due to overestimation of derived horizontal wavelengths by undersampling of observed gravity waves (aliasing) and by adopting along-track wavelengths instead of the true horizontal wavelengths (cf. Ern et al., 2018, and references therein). Second, the SABER instrument is sensitive only to gravity waves of horizontal wavelengths longer than 100–200 km and does therefore not cover the whole spectrum of gravity waves. In particular, it is indicated that short horizontal wavelength convectively generated gravity waves that cannot be seen by SABER contribute significantly to the driving of the SSAO (e.g., Beres et al., 2005; Kang et al., 2018). For further discussion regarding the observational filter of the instrument please see Trinh et al. (2015).

In their study, Smith et al. (2020) conclude that free-running models would have difficulties to simulate a realistic SSAO because of insufficient gravity wave forcing. ~~Taking into account the observational filter effect, this~~ This conclusion is supported by the fact that ~~SABER absolute gravity wave drag is similar to the~~ the magnitude of gravity wave drag of free-running global models ~~, but lower than that of the~~ is similar to the magnitude of SABER MFz-proxy-|GWD| (that should be low-biased by observational filter effects), and lower than the magnitude of total gravity wave drag in reanalyses.

6.3.2 Upper mesosphere: the MSAO

In the upper mesosphere, at altitudes between about ~ 75 km and 80 km, the clear relationship between eastward wind shear and ~~absolute gravity wave drag~~ SABER MFz-proxy-|GWD| apparently does not hold any longer (see Figs. ~~?? and ??~~ 7c and 7d). This is expected because the asymmetric wind filtering effect of the gravity wave spectrum induced by the QBO in the stratosphere should gradually fade out. Instead, the wind filtering in the stratopause region and the middle mesosphere should become more relevant.

This is supported by the fact that the MSAO is approximately in anti-phase with the SAO at the stratopause and in the middle mesosphere. It is believed that this is anti-phase relationship is caused by the dissipation of gravity waves that are selectively filtered by the winds in the middle mesosphere. Gravity waves that have phase speeds opposite to the prevailing wind direction in the stratopause region and the middle mesosphere, consequently, have high intrinsic phase speeds and, thus, high saturation amplitudes (see also Fritts, 1984; Ern et al., 2015, and references therein). When reaching the upper mesosphere, these waves saturate and contribute to the wind reversal, resulting in the observed anti-correlation of SAO winds in the middle and the upper mesosphere. This means that winds in the upper mesosphere are westward when they are eastward in the middle mesosphere, and vice versa. Accordingly, in the upper mesosphere gravity waves are expected to contribute both to the MSAO eastward and the MSAO westward winds.

Interestingly, as shown by the SPARC zonal wind climatology, the downward propagation with time of the MSAO eastward and westward wind phases is much slower than the downward propagation of the eastward wind phase of the SSAO and the SAO in the middle mesosphere. Therefore, the characteristics of the gravity wave forcing should also be different in these two altitude ranges. This will be investigated in more detail in Sect. 7.

Peak values of ~~SABER absolute gravity wave drag~~ SABER MFz-proxy-|GWD| in the altitude range of 75–80 km are about $20\text{--}30\text{ m s}^{-1}\text{ day}^{-1}$ (see Fig. ?? (see Figs. 7b and S21)). As stated before, due to the SABER observational filter, these values are expected to be likely a lower estimate of the total gravity wave drag. Indeed, in the mesopause region, Lieberman et al. (2010) obtained gravity wave peak values of typically around $100\text{ m s}^{-1}\text{ day}^{-1}$, estimated as residual drag from the momentum budget using TIMED observations of SABER and TIDI. However, similar as for the simulation of the stratopause SAO, gravity wave drag peak values of model simulations are much weaker. For example, Richter and Garcia (2006) or Peña–Ortiz et al. (2010) obtained peak values of gravity wave drag of only around $10\text{--}20\text{ m s}^{-1}\text{ day}^{-1}$ in their simulations of the SAO in the altitude range 75–85 km.

6.3.3 The region above the MSAO

Also at altitudes above 80 km, there is no clear relationship between eastward wind shear and ~~absolute gravity wave drag~~ SABER MFz-proxy-|GWD|. Moreover, compared to the altitude range 30–80 km, there is a structural change in the distribution of ~~absolute gravity wave drag~~ SABER MFz-proxy-|GWD| (see Figs. ?? and ??7c and 7d).

In the whole lower altitude regime 30–80 km we find downward propagation of ~~absolute gravity wave drag~~ SABER MFz-proxy-|GWD| enhancements with time. At altitudes $\sim 30\text{--}75$ km this downward propagation is relatively steep and related to the zones of eastward directed SAO wind shear. At altitudes 75–80 km we still find downward propagation, although much slower, and seemingly related to the downward propagation rate of the SAO wind phases (cf. Fig. ??3b).

Conversely, in the upper altitude regime above 80 km, enhancements of ~~absolute gravity wave drag~~ SABER MFz-proxy-|GWD| propagate *upward* with time. These variations are obviously not directly related to the SAO winds, but to the variations that are caused by the varying local solar time of SABER observations. The variations of ~~absolute gravity wave drag~~ SABER MFz-proxy-|GWD| at altitudes above ~ 80 km are caused by tides that are sampled at different local solar times while the TIMED satellite orbit precesses. For upward propagating tides the phase propagation is downward with time (e.g., Smith, 2012; Sridharan, 2019). However, due to orbit precession of the TIMED satellite, the SABER sampling gradually shifts to earlier local solar times, as shown in Fig. ??S1 in the Supplement. This leads to an apparent upward phase propagation with time of observed tides and, accordingly, to the observed apparent upward propagation of gravity wave drag maxima because gravity wave drag should be directly linked with the wind shear induced by the tides.

At high altitudes, an increasing influence of tides on the distribution of gravity waves would also be expected ~~from previous findings. At some point~~ the gravity wave momentum flux spectrum is strongly filtered by the QBO, the SSAO, and the SAO in the middle mesosphere. Consequently, not much momentum flux is still available for driving the MSAO in more than a narrow altitude layer. Also previous findings show that the MSAO occurs only in a narrow layer, and at some point the effect of tides should dominate starts to dominate over the effect of the SAO. ~~Figure~~ For instance, Fig. 30 in Baldwin et al. (2001) shows that the MSAO in the upper mesosphere has a sharp amplitude peak of 30 m s^{-1} at 80 km altitude. The MSAO amplitude drops below $\sim 10\text{ m s}^{-1}$ already below 90 km. Simultaneously, the amplitude of tides increases with altitude. For example, Fritts et al. (1997) found amplitudes of $5\text{--}10\text{ m s}^{-1}$ below 75 km, increasing to about 20 m s^{-1} at 90 km for diurnal tides observed by radar near the equator during August 1994. These values are roughly in agreement with simulations of the

800 Canadian Middle Atmosphere Model (CMAM) (McLandress et al., 2002). Based on these findings, it would be expected that in the altitude range 80–90 km there should be a transition between a regime that is mainly dominated by the MSAO around 80 km, and another regime that is increasingly dominated by tides at higher altitudes. Worthy of remark, this is also reflected in the observed ~~SABER absolute gravity wave drag distribution~~ distribution of SABER MFz-proxy-|GWD|.

7 Correlation between ~~the observed absolute gravity wave drag~~ SABER MFz-proxy-|GWD| and tropical zonal wind

805 Next, we carry out a correlation analysis in order to quantify the robustness of the interaction between ~~SABER absolute gravity drag~~ SABER MFz-proxy-|GWD| and tropical zonal background wind. To do so, we calculate the temporal correlation between ~~absolute gravity wave drag~~ SABER MFz-proxy-|GWD| and the vertical gradient of the background zonal wind as well as the temporal correlation between ~~absolute gravity wave drag~~ SABER MFz-proxy-|GWD| and absolute values of the zonal background wind. These correlations are calculated for fixed altitudes, separately for each given year of the 2002–2018 period, 810 ~~and~~ and for the complete time series as a whole.

Figure 8 shows 2002–2018 averages of ~~zonal winds (first column)~~, ~~SABER absolute gravity wave drag~~ SABER MFz-proxy-|GWD| with zonal wind contour lines (~~second~~ first column), normalized ~~SABER gravity wave drag~~ SABER MFz-proxy-|GWD| with contour lines of zonal wind vertical gradients (~~third~~ second column), correlation coefficients between ~~SABER gravity wave drag~~ SABER MFz-proxy-|GWD| and du/dz ~~for each year, as well as for the 2002–2018 average distribution (fourth~~, (third 815 column), and correlation coefficients between ~~SABER gravity wave drag~~ SABER MFz-proxy-|GWD| and $|u|$ ~~for each year, as well as for the 2002–2018 average distribution (fifth~~ (fourth column). In order to find out whether the results are robust and insensitive to details of a wind data set considered, the correlation analysis is carried out for different wind data sets.

Given the strong interannual variability of the SAO, it is most important that existing correlations hold for the majority of single years, and this is why in Figs. 8 and 9 we show the correlations for each year of the 2002–2018 period. For completeness, 820 also the correlations are shown for the 2002–2018 average distribution, as well as for the complete 2002–2018 time series as a whole. These correlations might, however, differ somewhat from the correlations of the single years. For example, the correlations for the average might be affected by strong outlier-years, or compensation effects, and also the correlation over the whole dataset might be affected by strong outlier-years (even though in a different way).

7.1 Correlation between SABER ~~absolute gravity wave drag~~ MFz-proxy-|GWD| and du/dz

825 From theoretical considerations (e.g., Hamilton and Mahlmann, 1988; Dunkerton and Delisi, 1997), from first satellite observations of the gravity wave driving of the SAO in the stratopause region (Ern et al., 2015), and from the findings in Sect. 6.3, we expect that in a certain altitude range gravity waves mainly contribute to the driving of the SAO eastward phases and their downward propagation with time. For this altitude range, it is expected that gravity wave drag should mainly act during eastward wind shear.

830 To find out in which altitude range this is the case, we calculated for each year separately the temporal correlation between ~~SABER absolute gravity wave drag~~ SABER MFz-proxy-|GWD| and du/dz . ~~Since only absolute values of gravity wave drag~~

~~are available~~Since ~~SABER MFz-proxy-[GWD]~~ can attain only positive values, some care has to be taken when interpreting these results. If a correlation coefficient is positive, this means that in a given year, at the altitude considered, the gravity wave forcing takes mainly place during eastward wind shear, and the forcing is very likely eastward. Similarly, if the correlation coefficient is negative, the gravity wave forcing takes mainly place during westward wind shear, and the forcing is very likely westward. If the correlation is close to zero, this means that either the relationship between gravity wave drag and du/dz is random, or eastward and westward forcing could be similarly strong.

7.1.1 Stratosphere (QBO)

Figure. 8, first row, shows the results for the combined data set of ERA-Interim, SABER, and TIDI winds, averaged over ascending and descending orbit data. In the stratosphere between about 30 and 40 km, there is an alternating pattern of strong positive and weak correlations, which is likely not an effect of the SAO. In this altitude range the QBO is the dominant mode of tropical wind variability. It has been shown by Ern et al. (2014) that ~~absolute~~-HIRDLS and SABER ~~absolute~~ gravity wave drag ~~is-proxies are~~ stronger during eastward directed QBO wind shear. Although the 10 km vertical window used in our study is relatively coarse and will often average over the stacked zones of eastward and westward directed QBO wind shear, this asymmetry can lead to the observed alternating pattern of correlations. Since the QBO averages out in the 2002–2018 multi-year average, correlations for the average distributions are generally weak at altitudes below about 45 km; ~~the same holds for the correlations over the complete 2002–2018 time series as a whole~~. Similar alternating patterns are also found for all other wind data sets presented in Fig. 8 (~~and in Fig. S24 in the Supplement~~) that contain the QBO. Even for the correlation between the SPARC zonal wind climatology and ~~absolute-gravity-wave-drag-SABER MFz-proxy-[GWD]~~ an alternating pattern can be found in the stratosphere. However, this pattern is different because the QBO signal is only contained in the ~~SABER-absolute-gravity-wave-drag-SABER MFz-proxy-[GWD]~~, but not in the winds, as the same wind climatology is assumed for all years.

7.1.2 Stratopause region (SSAO) and middle mesosphere

In all panels of the ~~fourth-third~~ column in Fig. 8, starting from about 45 km upward, correlation coefficients are mostly strongly positive for the quasi-geostrophic data sets based on the SABER observations (Fig. 8, first to ~~sixth-row~~~~fourth row,~~ ~~and Fig. S24, first two rows~~), independently of the treatment of ascending and descending orbit data. This is also the case if MLS quasi-geostrophic winds (Fig. 8, ~~seventh-S24, bottom~~ row), or the SPARC wind climatology (Fig. 8, bottom row) are used as background winds.

For the SABER ~~and-MLS~~-quasi-geostrophic wind data sets (Fig. 8, rows ~~1-7~~~~1-4~~) the altitude range of positive correlations is from about 45 km to 75–80 km, indicating that in this altitude range gravity waves mainly contribute to the driving of the eastward SAO phase. Interestingly, for the SPARC wind climatology (Fig. 8, bottom row) the altitude range of positive correlations starts only at ~ 50 km, which is somewhat higher than for all other data sets. Possible reason could be that for the SPARC climatology the SAO in the stratopause is less pronounced than for the other data sets, and is somewhat shifted in its phase. However, as in the other data sets, the upper edge of the positive correlations with du/dz is at about 75 km. At around 60 km altitude the correlation between SPARC zonal wind vertical gradients and SABER gravity wave drag is

865 somewhat weaker, possibly because this altitude range is interpolated in the SPARC climatology and might be less reliable (cf. Swinbank and Ortland, 2003).

7.1.3 Upper mesosphere: MSAO and effect of tides

At altitudes above about 75–80 km the positive correlation between ~~absolute gravity wave drag~~ the SABER MFz-proxy-|GWD| and du/dz does no longer hold. For the MSAO this means that the mechanisms of the gravity wave driving are somewhat
870 different than at lower altitudes. This will be discussed in Sect. 7.2.

Above 80 km there is even an anti-correlation between ~~absolute gravity wave drag~~ SABER MFz-proxy-|GWD| and du/dz when the SABER quasi-geostrophic winds are used also in the whole altitude range above 75 km and separated into data from ascending and descending orbit legs (Fig. 8, ~~fifth and sixth~~ third and fourth row). The fact that this effect occurs when ascending and descending data, i.e., different local solar times, are treated separately hints at an effect of tides.

875 ~~Figure 8 fifth and sixth rows, center panels, show that for ascending-only and descending-only data at altitudes above 75–80 km enhancements of absolute gravity wave drag are shifted in phase~~

~~There is even a phase shift~~ by about 180° , ~~i.e. maxima of absolute gravity wave drag~~; maxima of SABER MFz-proxy-|GWD| from ascending-only data fall onto minima of ~~absolute gravity wave drag~~ SABER MFz-proxy-|GWD| from descending-only data, and vice versa. ~~This phase shift between the different local solar times indicates that (Fig. 8, third and fourth rows, second column). A similar phase shift is seen in the ascending-only and descending-only quasi-geostrophic winds at altitudes above about 75–80 km tides have a stronger influence on the gravity wave drag distribution than the SAO. As can be seen from Figs (Fig. 8, fifth third row, left, and sixth fourth row, left, also the ascending-only and descending-only quasi-geostrophic winds are approximately in anti-phase at altitudes above about 75–80, which is further evidence for tidal influences.)~~

~~Of course, interpolated quasi-geostrophic winds at these altitudes are affected by large biases and are not very realistic. Still, these findings show that obviously~~ Obviously, enhancements of absolute gravity wave drag are phase-locked with tidal winds and their vertical shear. This is not surprising ~~, because it is known that~~ because gravity waves can interact with ~~global-scale waves and can even contribute to their forcing (e.g., Holton, 1984; Smith, 2003; Matthias and Ern, 2018). Similarly, it is known~~ global scale waves (e.g., Holton, 1984; Smith, 2003; Matthias and Ern, 2018), and, in particular, tides as seen from model simulations ~~that momentum deposition of gravity waves can affect the amplitude and phase of tides (e.g., Mayr et al., 2001; England et al., 2006; Ortland and Alexander, 2006; Liu et al., 2014), and the global distribution of tides cannot be understood without gravity wave tidal interactions (e.g., Ribstein and Achatz, 2016). Also previous observations show that the distribution of gravity waves in the mesopause region is modulated by tides (e.g., Mayr et al., 2001; England et al., 2006; Ortland and observations~~ (e.g., Fritts and Vincent, 1987; Preusse et al., 2001; Tang et al., 2014).

895 However, an in-depth investigation of the impact of tides on the gravity wave distribution is beyond the scope of this paper, and for an in-depth study direction-resolved observations of momentum fluxes would be very helpful. Still, because of the anti-phase relationship between ascending and descending data, we can assume that cancellation effects will take effect if ascending and descending data are averaged, and the contribution of the SAO should become more clearly visible. This cancellation should hold for both the zonal wind and ~~absolute gravity wave drag~~ the SABER MFz-proxy-|GWD|.

7.2 Correlation between SABER ~~absolute gravity wave drag~~ MFz-proxy-|GWD| and absolute zonal wind

900 So far we have mainly discussed the case of gravity wave forcings when a strong vertical wind shear coincides with enhance-
ments of ~~absolute gravity wave drag~~ the SABER MFz-proxy-|GWD|. Under these conditions, it is likely that either critical level
filtering of gravity waves takes place (background winds and ground-based phase speeds become equal for parts of the gravity
wave spectrum), or the vertical gradient of the background wind leads to a reduction of intrinsic phase speeds for parts of the
gravity wave spectrum such that those waves saturate and dissipate.

905 Of course, wave saturation can also occur independent of gradients of the background wind. If a gravity wave propagates
upward conservatively in a background of constant wind and temperature, its amplitude will grow exponentially due to the
decrease of atmospheric density with altitude. Upon reaching the saturation amplitude, the gravity wave will break and dissipate
(e.g., Fritts, 1984). This mechanism is assumed to cause the wind reversals of the midlatitude mesospheric wind jets in the
mesopause region (e.g., Lindzen, 1981). It is expected that this mechanism should also be relevant for the driving of the
910 MSAO, and it would explain the out-of-phase or anti-phase relationship with the SAO at lower altitudes (e.g., Dunkerton,
1982; Mengel et al., 1995), as well as the relatively slow downward propagation of the MSAO phases. While correlations
between du/dz and absolute gravity wave drag can be explained by critical level filtering or by gravity wave saturation, it is
difficult to explain correlations between the strength of the zonal wind and absolute gravity wave drag by processes other than
a general saturation mechanism of gravity waves.

915 First indications for a relationship between the strength of the zonal wind and absolute gravity wave drag were found in
Sect. 6.3.2 for certain altitude ranges. This will now be investigated in more detail. ~~Because~~ Because SABER MFz-proxy-|GWD|
provides only absolute values of ~~SABER gravity wave drag are available~~, we will investigate in the following the correlation
between *absolute values* of the zonal wind ($|u|$) and ~~absolute gravity wave drag~~ SABER MFz-proxy-|GWD|. A correlation
analysis between ~~absolute gravity wave drag~~ SABER MFz-proxy-|GWD| and zonal wind, including its sign, would not make
920 sense because correlations for situations where both positive and negative wind phases are driven by gravity wave dissipation
(as would be expected for the MSAO) would be near-zero due to cancellation effects. Correlation coefficients for the relation
between $|u|$ and ~~SABER absolute gravity wave drag~~ SABER MFz-proxy-|GWD| are shown in the rightmost column of Fig. 8
in the same manner as before, i.e. for the different wind data sets, separately for each year, as well as for the multi-year average,
and the time series as a whole.

925 7.2.1 Altitudes below about 75 km

At altitudes below about 40 km the dominant mode of stratospheric variability in the tropics is the QBO. Indeed, there is some
interannual variability due to the QBO in all panels of the rightmost column of Fig. 8. However, as mentioned before, this QBO
signal should be only spurious because the 10 km vertical window of our SABER momentum flux analysis will average out
much of the QBO signal.

930 In the altitude range from about 40 to 50 km we find a positive correlation between ~~SABER absolute gravity wave drag~~
SABER MFz-proxy-|GWD| and $|u|$ for all wind data sets. One reason is the asymmetry of the SAO in this altitude region so

that most of the positive wind gradient falls into the negative (=westward) phase of the SAO, which is stronger than the eastward phase. Another reason is that part of the gravity wave driving, particularly during the first SAO westward phase of the year, takes place not only during eastward wind shear, but also around the line of zero wind shear, i.e. around maximum westward winds (see Fig. 8, ~~third-second~~ column). As was argued by Ern et al. (2015), this effect could be caused by gravity waves of eastward directed phase speeds that saturate before the vertical gradient du/dz of the background wind becomes positive. This is supported by the fact that for this case most of the momentum flux reduction happens at high gravity wave intrinsic phase speeds (Ern et al., 2015). Further, during the first stratopause SAO westward phase for a given year, the gravity wave drag estimated from the reanalyses is mostly eastward (cf. Figs. ~~??-??4a-4d~~). Still, as can be seen from Figs. ~~??-??4a-4d~~, sometimes the net forcing can also be westward.

In the altitude range from about 50 to 75 km correlations are usually weak (floating around zero), or even negative. Strongest negative correlations are found for the SPARC zonal wind climatology (Fig. 8, lower right panel) at altitudes between 50 and 60 km, indicating that for the SPARC climatology the timing of the SAO in the lower mesosphere is somewhat different from the other data sets. Overall, the weak or negative correlations confirm that in the altitude range 50 to 75 km the SAO gravity wave driving indeed mainly happens during eastward wind shear.

7.2.2 Upper mesosphere and mesopause region

In the upper mesosphere, at altitudes above 75 km, the correlation between ~~SABER absolute gravity wave drag~~ ~~SABER MFz-proxy-|GWD|~~ and du/dz is usually weak, consistent with our findings in Sect. 7.1.3. Remarkably, there is a strong positive correlation between ~~absolute gravity wave drag~~ ~~SABER MFz-proxy-|GWD|~~ and $|u|$ in the altitude region of about 75 to 85 km for most of the wind data sets presented in Fig. 8 ~~and Fig. S24~~. This correlation holds for each given year ~~and also~~, for the average year of the 2002–2018 period.

~~, as well as for the 2002–2018 time series as a whole.~~ The only exception is the data set of MLS winds (see Fig. 8, ~~seventh S24, third~~ row, rightmost column). ~~As MLS observations are always at two fixed local solar times, about 13:45 and 01:45 LST, tides are usually sampled at the same phase, which could introduce altitude-dependent wind biases. Such biases could be the reason why the phases of MSAO westward winds in the altitude range 75–85 are comparably weak, and even weaker than MSAO eastward winds. Since the strongest maxima of SABER absolute gravity wave drag are usually located in the MSAO westward phases, this potential bias will result in a weakening of correlations between SABER absolute gravity wave drag and $|u|$ be an altitude dependent bias caused by sampling tides always at the same phases.~~

Apart from this exception, good correspondence between ~~absolute gravity wave drag~~ ~~SABER MFz-proxy-|GWD|~~ and absolute zonal wind is found for the data sets that are based on SABER quasi-geostrophic winds merged with TIDI direct wind observations (Fig. 8, first ~~three-row, rightmost column; Fig. S24, first two~~ rows, rightmost column) and for the data sets that (in this altitude region) are based solely on SABER quasi-geostrophic winds (Fig. 8, rows ~~four to six~~ ~~two to four~~, rightmost column). Note that this correlation holds for ascending-only data, for descending-only data, as well as for the averages of ascending and descending data. Further, it is remarkable that the same altitude range of positive correlations is also found for the SPARC climatology (Fig. 8, bottom row, rightmost column).

At altitudes above 85 km, in the mesopause region, correlations fluctuate around zero, or are negative again. As stated in Sect. 7.1.3, this altitude region is dominated by tides, and ~~absolute gravity wave drag-SABER MFz-proxy-|GWD|~~ seems to be phase-locked with the tidal component of the SABER quasi-geostrophic winds. An interpretation of these results, however, is difficult and beyond the scope of this study.

970 Overall, the positive correlations between ~~SABER absolute gravity wave drag-SABER MFz-proxy-|GWD|~~ and absolute zonal wind speed at altitudes 75–85 km support the mechanism proposed by previous studies (e.g., Dunkerton, 1982; Mengel et al., 1995; Burrage et al., 1996) that in this altitude range selectively filtered gravity waves saturate and directly contribute to the formation of the MSAO westward and eastward phases. The direction of the wave forcing is given by the selective filtering of gravity waves at altitudes below, leading to the observed anti-correlation of the MSAO (i.e., the SAO in the upper mesosphere) and the SAO in the middle mesosphere. The wave saturation seems to take place independent of zonal wind vertical gradients, 975 which means that gravity waves of phase speeds much higher than the background wind are involved.

The saturation amplitudes of ~~those waves are relatively insensitive to changes in high phase speed gravity waves are not much influenced by~~ the background wind ~~. Possibly, this explains and its variation. Consequently, the saturation altitude (the altitude where the waves exert their drag) will not be as closely tied to a wind shear zone as is the case for the QBO and the SAO at lower altitudes. Still, the dissipation of high phase speed gravity waves with a directional preference can lead to a reversal and strengthening of the wind by inducing a temporal wind tendency, which is different from the dissipation mechanism that leads to a strengthening of vertical wind shear and eventually to a downward propagation of the shear zone. The temporal wind tendency will lead to a wind reversal and wind strengthening at the same altitude where the drag is exerted. Therefore, enhanced gravity wave drag should be observed at the same altitude as the reversed wind jet, and lead to a correlation between~~ 980 ~~SABER MFz-proxy-|GWD| and (absolute) wind speed. This mechanism seems to be relevant for the driving of the MSAO, and it would explain~~ why there is no strong downward propagation of the MSAO ~~eastward and westward wind~~ phases with time. For an in-depth understanding of this mechanism, however, more detailed model studies would be needed. 985

8 Correlation between reanalysis gravity wave drag and zonal wind

Next, we will investigate whether the gravity wave drag expected from the reanalyses exhibits similar characteristic patterns 990 that are consistent with the SABER observations. Similar as in Fig. 8, Fig. 9 shows for the four reanalyses, averaged over the period 2002–2018 and latitudes 10°S–10°N: ~~zonal wind (Fig. 9, left column),~~ gravity wave drag overplotted with zonal wind contour lines (Fig. 9, ~~second-left~~ column), and gravity wave drag overplotted with contour lines of the zonal wind vertical gradient du/dz (Fig. 9, ~~third-second~~ column). Further shown are for each altitude temporal correlations ~~for each year, as well as for the 2002–2018 average distributions~~ between gravity wave drag and the zonal wind vertical gradient (Fig. 9, ~~fourth-third~~ 995 column), and gravity wave drag and zonal wind including direction (Fig. 9, right column). Unlike ~~for SABER gravity wave drag for SABER MFz-proxy-|GWD|~~, the latter makes sense for the reanalyses because the gravity wave drag derived from the reanalyses has directionality. ~~Again, correlations are shown for each year, for the 2002–2018 average distributions, and for the complete 2002–2018 time series as a whole.~~

8.1 ERA-Interim

1000 As can be seen from Fig. 9, first row, ~~fourth~~third column, ERA-Interim gravity wave drag is generally positively correlated with du/dz with some interannual variation at altitudes below about 45 km that may be related to the QBO. This is consistent with our findings for SABER gravity wave drag (cf. Fig. 8). However, for ERA-Interim there is a strong anti-correlation between zonal wind and gravity wave drag at altitudes above ~ 45 km (Fig. 9, first row, right column). This correlation is not observed for ~~SABER gravity wave drag~~ ~~SABER MFz-proxy-|GWD|~~ and should be an effect of the model sponge layer near the model
1005 top. Therefore, patterns of ERA-Interim gravity wave drag are likely not very realistic at altitudes above 45 km.

8.2 JRA-55

For JRA-55, at altitudes below ~ 45 km the correlation between gravity wave drag and du/dz is much stronger than for ERA-Interim, or for SABER. This indicates that details in the gravity wave driving of the QBO are different in JRA-55 (cf. Fig. 9, second row, ~~fourth~~third column). At altitudes above ~ 40 km, i.e., at altitudes even somewhat lower than for ERA-Interim,
1010 there is a strong anti-correlation between zonal wind and gravity wave drag, likely related to the model sponge layer (see Fig. 9, second row, right column). Therefore, similar as for ERA-Interim, patterns of gravity wave drag are probably not very realistic at altitudes above ~ 40 km.

8.3 MERRA-2

For MERRA-2, in the whole altitude range 30–70 km we find generally very strong positive correlation between gravity wave
1015 drag and du/dz (cf. Fig. 9, third row, ~~fourth~~third column). Similarly to JRA-55, for altitudes below ~ 45 km the MERRA-2 correlations do not show much interannual variation, which is different for ERA-Interim and SABER gravity wave drag, and may indicate differences in details of the driving of the QBO.

For the altitude range 45–70 km, the positive correlations are qualitatively in agreement with the SABER correlations;
~~suggesting that in this altitude range the~~. As was shown in Sects. 5.2.2 and 5.2.3, the nonorographic gravity wave drag scheme
1020 in MERRA-2 was tuned in a way to minimize the assimilation increment due to MLS observations. Therefore, MERRA-2 even simulates a reasonable SAO in the years before 2004 when no MLS data are available and the model is relatively unconstrained in the middle mesosphere. The qualitative agreement with the SABER correlations seems to indicate that the physical mechanisms of the SAO ~~gravity wave driving may driving by gravity waves are — at least to some extent be realistic.~~ — realistically simulated by the MERRA-2 nonorographic gravity wave drag scheme.

1025 Note that above ~ 65 km the correlation between gravity wave drag and du/dz is even more positive for the years after 2004 that are fully covered by MLS observations, likely reflecting the positive influence of assimilating MLS data in MERRA-2. At altitudes above ~ 65 km, there is a strong anti-correlation between gravity wave drag and zonal wind, which is likely caused by the sponge layer near the model top (cf. Fig. 9, third row, right column).

8.4 ERA-5

1030 In the altitude range below ~ 45 km ERA-5 shows interannual variability of the positive correlation between gravity wave drag and du/dz that is similar to the ERA-Interim and SABER correlations. However, in the altitude range 45–65 km there is no clear positive correlation between gravity wave drag and du/dz as would be expected from SABER observations. This indicates that the gravity wave driving of the SSAO and the SAO in the middle mesosphere is not realistic, and might be linked to the model imbalances that lead to the unrealistically strong eastward jets around 60 km altitude (cf. Fig. 9, fourth row, ~~fourth~~
1035 ~~third~~ column).

The strong positive correlation in the altitude range 65–70 km seems to be related to the gravity wave drag at the top of the eastward jets that leads to the wind reversals toward westward winds and the formation of the MSAO in ERA-5. In this altitude range positive correlations are also found for SABER (cf. Fig. 8). However, strongest values of ~~SABER gravity wave drag~~ ~~SABER MFz-proxy-|GWD|~~ are found at somewhat higher altitudes and are correlated with absolute wind speed rather than
1040 with du/dz . This correlation is not found in ERA-5 (cf. Fig. 9, fourth row, right column). On the one hand, this means that the model sponge in ERA-5 is not as pronounced as in the other reanalyses. On the other hand, however, ~~it looks like the different characteristics of ERA-5 gravity wave drag and SABER observations might indicate that in ERA-5 high gravity wave phase speeds are underrepresented in the MSAO region, i.e.,~~ not all physical mechanisms that lead to the formation of the MSAO are correctly represented in ERA-5. ~~In addition, the unrealistic SAO at lower altitudes can lead to an unrealistic wind filtering of~~
1045 ~~the gravity wave spectrum, which can also affect the simulation of the MSAO.~~

9 Summary and discussion

In this study, we have investigated the driving of the semiannual oscillation (SAO) of the zonal wind in the tropics by gravity waves. The study covers the whole middle atmosphere from 30–90 km altitude and focuses on the latitude band 10°S – 10°N and the 2002–2018 time period of available satellite data.

1050 First, the SAO was investigated in four different reanalyses, the ERA-Interim and ERA-5 reanalyses of the European Centre for Medium-range Weather Forecasts (ECMWF), the JRA-55 reanalysis of the Japanese Meteorological Agency (JMA), and the MERRA-2 reanalysis of the National Aeronautics and Space ~~Agency-Administration~~ (NASA). The expected drag due to small-scale gravity waves was estimated as sum of the residual (“missing drag”) in the transformed Eulerian mean (TEM) zonal momentum budget and of the drag due to resolved waves of zonal wavenumbers larger than 20. All reanalyses are
1055 capable to simulate a SAO in the stratopause region (SSAO) and show the expected asymmetry of gravity wave drag with enhanced eastward gravity wave drag during eastward wind shear. Westward directed gravity wave drag is usually much weaker. This asymmetry is expected because the zonal wind of the quasi-biennial oscillation (QBO) in the stratosphere has a stronger westward phase such that a larger part of the gravity wave spectrum at westward directed phase speeds encounters critical levels in the stratosphere and cannot propagate into the stratopause region and the mesosphere (cf. Dunkerton, 1982;
1060 Hamilton and Mahlmann, 1988; Ern et al., 2015).

MERRA-2 and ERA-5 cover a larger altitude range than ERA-Interim and JRA-55. MERRA-2 applies stronger damping only above ~ 58 km, uses a nonorographic gravity wave parameterization, and assimilates Microwave Limb Sounder (MLS) data in the stratosphere and mesosphere. Therefore MERRA-2 produces a reasonable SAO also in the middle mesosphere, and the SAO in the stratopause region is likely more realistic than in ERA-Interim and JRA-55. On average, also in the middle mesosphere the eastward gravity wave driving of the SAO in MERRA-2 is stronger than the westward driving. However, there is strong interannual variability, and there are several episodes of strong westward directed gravity wave driving, for example in the year 2006. This strong inter-annual variability is also supported by satellite observations of the SAO gravity wave driving (Ern et al., 2015).

Similarly to MERRA-2, ERA-5 also uses a nonorographic gravity wave parameterization, but ERA-5 does not assimilate MLS data. While the SSAO still looks realistic, the SAO eastward jets at altitudes around 60 km are overly strong, a fact that has already been reported in previous studies (Hersbach et al., 2018; Shepherd et al., 2018), and which was improved in the operational ECMWF model after 11 July 2017 (Hersbach et al., 2018). Among the four reanalyses investigated here, ERA-5 is the only reanalysis that simulates the mesopause SAO (MSAO) above 70 km with a strong wind reversal above the middle mesosphere SAO eastward jets.

We have also investigated the SAO based on satellite observations. According to the findings of Smith et al. (2017), quasi-geostrophic winds derived from satellite observations and interpolated into the tropics give reasonable results at altitudes below about 75–80 km. Based on quasi-geostrophic zonal winds derived from MLS observations, averaged over ascending and descending parts of the satellite orbit, we found that the SAO in the lower and middle mesosphere agrees remarkably well with the SAO in MERRA-2. Only in the upper mesosphere and in the mesopause region MLS zonal winds seem to have an eastward bias compared to the ~~Stratospheric Processes And their Role in Climate (SPARC) climatology of zonal winds (Swinbank and Ortland, 2003; Randel et al., 2002, 2004)~~-other datasets. Possibly, this bias is caused by tidal effects that do not completely cancel out by averaging over ascending and descending orbit data. (Data of ascending and descending MLS orbit parts are observed at different local solar time (LST), about 13:45 LST for ascending, and 01:45 LST for descending data.)

To investigate the gravity wave driving of the SAO based on satellite data, we have derived absolute gravity wave momentum fluxes and a proxy for absolute gravity wave drag (~~SABER MFz-proxy-|GWD|~~) from SABER temperature observations. SABER observations are not at fixed local solar times because the TIMED satellite is in a slowly precessing orbit. To capture the local solar time dependent effect of tides, as well as to account for the reduced reliability of interpolated quasi-geostrophic winds at altitudes above ~ 75 km, a combined data set of ERA-Interim, interpolated SABER quasi-geostrophic winds, and winds directly observed by TIDI has been composed that should represent realistic background conditions for those gravity waves that are observed by the SABER instrument.

We found that ~~SABER absolute gravity wave drag~~ the ~~SABER MFz-proxy-|GWD|~~ has two maxima: One maximum in the stratopause region seems to be related to the SSAO, and the other maximum in the upper mesosphere to the MSAO. Further, in a large altitude range from the stratopause region, where the SSAO has its amplitude maximum, to about 75 km, ~~SABER absolute gravity wave drag~~-~~SABER MFz-proxy-|GWD|~~ is mainly enhanced during eastward vertical wind shear du/dz . This

modulation confirms that in the stratopause region and in the middle mesosphere gravity waves mainly contribute to the driving of the eastward phase of the SAO and its downward propagation with time. This asymmetry is caused by the asymmetric wave filtering by the QBO in the stratosphere. Further, because slow phase speed gravity waves encounter critical levels already due to the QBO in the stratosphere, it is expected that in addition to critical level filtering also saturation of gravity waves apart from critical levels will play an important role in the stratopause region and the middle mesosphere.

In the altitude [range](#) 75–80 km where the MSAO has its amplitude maximum, there is a structural change in the gravity wave interaction with the background wind. Maxima of ~~absolute gravity wave drag~~ [SABER MFz-proxy-|GWD|](#) are no longer observed in regions of strong du/dz , but in regions where the absolute zonal wind maximizes. Simultaneously, the downward propagation rate of the SAO eastward and westward wind phases is much reduced. This finding supports the theoretical expectation that gravity waves of high phase speed, that are relatively insensitive to changes in the background wind, generally saturate. Since the spectrum is dominated by gravity waves that propagate opposite to the zonal wind in the stratopause region and middle mesosphere, this results in wave drag that is opposite to the wind direction at lower altitudes and leads to the well-known out-of-phase relationship, or even anti-correlation of the MSAO zonal wind and the SAO zonal wind at lower altitudes.

These findings were confirmed by a correlation analysis investigating the temporal correlation between ~~SABER absolute gravity wave drag~~ [SABER MFz-proxy-|GWD|](#) and different zonal wind data sets, separately for each year, ~~as well as~~ for an average over the whole period 2002–2018, [as well as for the complete 2002–2018 time series as a whole](#). It is found that the results are robust for the combined data set of SABER and TIDI winds, regardless whether ascending and descending orbit data are averaged, or whether ascending-only, or descending-only data are considered. The same is true if just SABER interpolated quasi-geostrophic winds are used, or whether winds of the SPARC climatology are used as atmospheric background. Only for the case of MLS interpolated quasi-geostrophic winds is the correlation between ~~SABER absolute gravity wave drag~~ [SABER MFz-proxy-|GWD|](#) and MLS absolute zonal winds in the altitude range 75–80 km widely absent, attributable to an eastward bias of MLS winds in the upper MLT.

At altitudes above about 85 km we do not find strong correlations between ~~SABER absolute gravity wave drag~~ [SABER MFz-proxy-|GWD|](#) and the SAO zonal winds. Instead, ~~absolute gravity wave drag~~ [SABER MFz-proxy-|GWD|](#) seems to be phase-locked with the tidal wind component of the SABER interpolated quasi-geostrophic winds, which becomes most obvious if ascending and descending data are treated separately. This clearly indicates that gravity waves interact with the tides. However, an in-depth investigation of this effect is difficult and beyond the scope of our study.

Analysis of the correlation between background wind and gravity wave drag derived from the reanalyses reveals that positive correlation between gravity wave drag and du/dz is indeed found for ERA-Interim, JRA-55, and MERRA-2. ERA-Interim and JRA-55, however, are strongly limited by the sponge layers close to their model tops. Particularly, MERRA-2 seems to benefit from the assimilation of MLS data and from tuning of the gravity wave drag parameterization, such that positive correlations between gravity wave drag and du/dz are seen in a large altitude range in the mesosphere, in agreement with SABER observations. However, MERRA-2 does not simulate a proper MSAO because it is limited by the model sponge layer above 70 km. ERA-5 does not seem to have such a strong model sponge and simulates the MSAO. However, enhanced gravity

wave drag is not correlated with the magnitude of MSAO winds, which might indicate that not all parts of the gravity wave spectrum are realistically simulated by the nonorographic gravity wave parameterization.

1135 Magnitudes of ~~SABER absolute gravity wave drag~~ SABER MFz-proxy-|GWD| peak values are about $1\text{--}2\text{ m s}^{-1}\text{day}^{-1}$ in the stratopause region, and about $20\text{--}30\text{ m s}^{-1}\text{day}^{-1}$ in the altitude range around 80 km. ~~These values are roughly in agreement with simulations of the SAO by free-running general circulation models (e.g., Richter and Garcia, 2006; Osprey et al., 2010; Peña-Ortiz et al., 2010), but lower than our estimates from the four reanalyses considered here, and also lower than estimates by Lieberman et al. (2010) based on TIMED observations in the mesopause region.~~

1140 ~~In a recent study, Smith et al. (2020) concluded that in free-running general circulation models, too weak gravity wave forcing would be one of the main reasons for misrepresentations of the SSAO. Indeed, we would expect~~ It is expected that the total gravity wave driving should be stronger than indicated by the SABER ~~absolute gravity wave drag~~ MFz-proxy-|GWD| because SABER observes only a certain part of the gravity wave spectrum (in particular, only horizontal wavelengths longer than about 100-200 km). Further, the SABER observations are affected by observational filter effects that should result in a low bias of ~~gravity wave drag~~ SABER MFz-proxy-|GWD| (see, for example Trinh et al., 2015; Ern et al., 2018). Still, it might be possible that ~~SABER absolute gravity wave drag~~ SABER MFz-proxy-|GWD| could be an overestimation, because
1145 no directional information is available, and there could be contributions of eastward and westward drag that do not cancel. However, such effects would make it difficult to explain the close relationship between positive du/dz and ~~absolute gravity wave drag~~ the SABER MFz-proxy-|GWD| in the stratopause region and middle mesosphere. Further, the SABER observations in the stratopause region are roughly in agreement with lidar observations (e.g., Deepa et al., 2006; Antonita et al., 2007) that also cover only a certain part of the whole spectrum of gravity waves.

1150 Although values of SABER MFz-proxy-|GWD| are likely strongly low biased, they are roughly in agreement with simulations of the SAO by free-running general circulation models (e.g., Richter and Garcia, 2006; Osprey et al., 2010; Peña-Ortiz et al., 2010). This indicates that gravity wave drag in free-running models is likely too weak. This is further supported by the fact that the gravity wave drag in free-running models is much lower than our estimates from the four reanalyses considered here, and also lower than estimates by Lieberman et al. (2010) based on TIMED observations in the mesopause region. Indeed, in a recent model intercomparison Smith et al. (2020) concluded that in free-running general circulation models too weak gravity wave forcing would be one of the main reasons for misrepresentations of the SSAO. Still, because our gravity wave observations do not provide any directional information, the magnitudes of net gravity wave momentum flux and of net gravity wave drag remain an open issue that needs to be addressed by better global observations providing information about the full 3D structure of gravity waves (see also, for example Preusse et al., 2014; Ern et al., 2017; Gumbel et al., 2020).

1160 *Data availability.* The satellite data used in our study are open access: SABER data are available from GATS Inc. at <http://saber.gats-inc.com>. Aura-MLS version 4.2 level 2 data are freely available via the NASA Goddard Earth Sciences Data and Information Services Center (GES DISC) at <http://disc.sci.gsfc.nasa.gov/Aura>. TIDI level 3 vector winds can be obtained from the National Center for Atmospheric Research (NCAR) High Altitude Observatory (HAO) website at <http://timed.hao.ucar.edu/tidi/data.html>.

1165 The ERA-5 (<https://apps.ecmwf.int/data-catalogues/era5/?class=ea>, last access: 1 March 2021) and ERA-Interim data (<https://apps.ecmwf.int/archive-catalogue/?class=ei>, last access: 1 March 2021) are available from the European Centre for Medium-Range Weather Forecasts (ECMWF).

1170 MERRA-2 data used in this work are available at: Global Modeling and Assimilation Office (GMAO) (2015), MERRA-2 inst3_3d_asm_Nv: 3d, 3-Hourly, Instantaneous, Model-Level, Assimilation, Assimilated Meteorological Fields V5.12.4, Greenbelt, MD, USA, Goddard Earth Sciences Data and Information Services Center (GES DISC), Accessed: 1 July 2021, 10.5067/WWQSXQ8IVFW8, as well as Global Modeling and Assimilation Office (GMAO) (2015), MERRA-2 tavg3_3d_udt_Np: 3d, 3-Hourly, Time-Averaged, Pressure-Level, Assimilation, Wind Tendencies V5.12.4, Greenbelt, MD, USA, Goddard Earth Sciences Data and Information Services Center (GES DISC), Accessed: 1 July 2021, 10.5067/CWV0G3PPPFWF. The MERRA-2 model level data used in this study can be accessed under <https://doi.org/10.5067/WWQSXQ8IVFW8> and the pressure level wind tendencies under <https://doi.org/10.5067/CWV0G3PPPFWF> (last access 1 July 2021).

1175 JRA-55 data used in this work are available at: Japan Meteorological Agency/Japan. 2013, updated monthly. JRA-55: Japanese 55-year Reanalysis, Daily 3-Hourly and 6-Hourly Data. Research Data Archive at the National Center for Atmospheric Research, Computational and Information Systems Laboratory. <https://doi.org/10.5065/D6HH6H41>. Accessed 1 July 2021.

1180 The SPARC temperature and zonal wind climatology is available at: <http://www.sparc-climate.org/data-center/data-access/reference-climatologies/randels-climatologies/temperature-wind-climatology/>. Accessed 1 July 2021.

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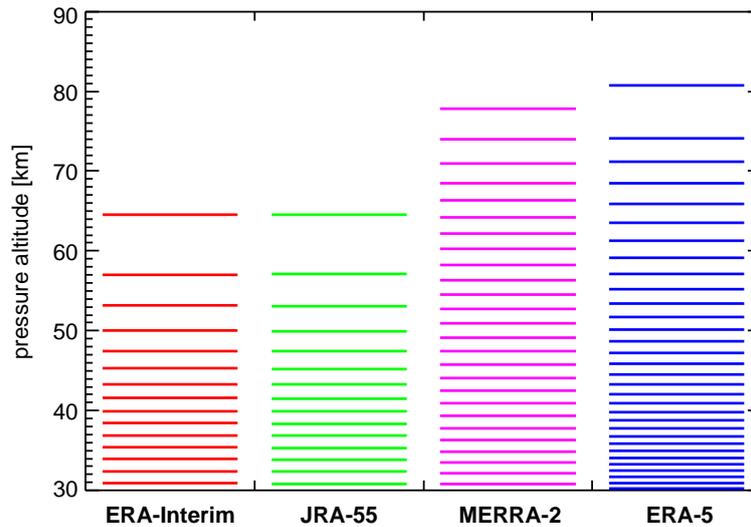


Figure 1. Altitude levels of the four reanalyses in the approximate altitude range 30 to 90 km used in this study. Altitudes given in this figure are pressure altitudes using a fixed pressure scale height of 7 km.

1540 ~~Local solar times of SABER and TIDI observations at the equator for the 2002–2018 time period. Local solar times are given for the following: SABER ascending (black diamonds), SABER descending (black crosses) TIDI warm side ascending (red diamonds), TIDI warm side descending (red crosses), TIDI cold side ascending (blue diamonds), and TIDI cold side descending (blue crosses).~~

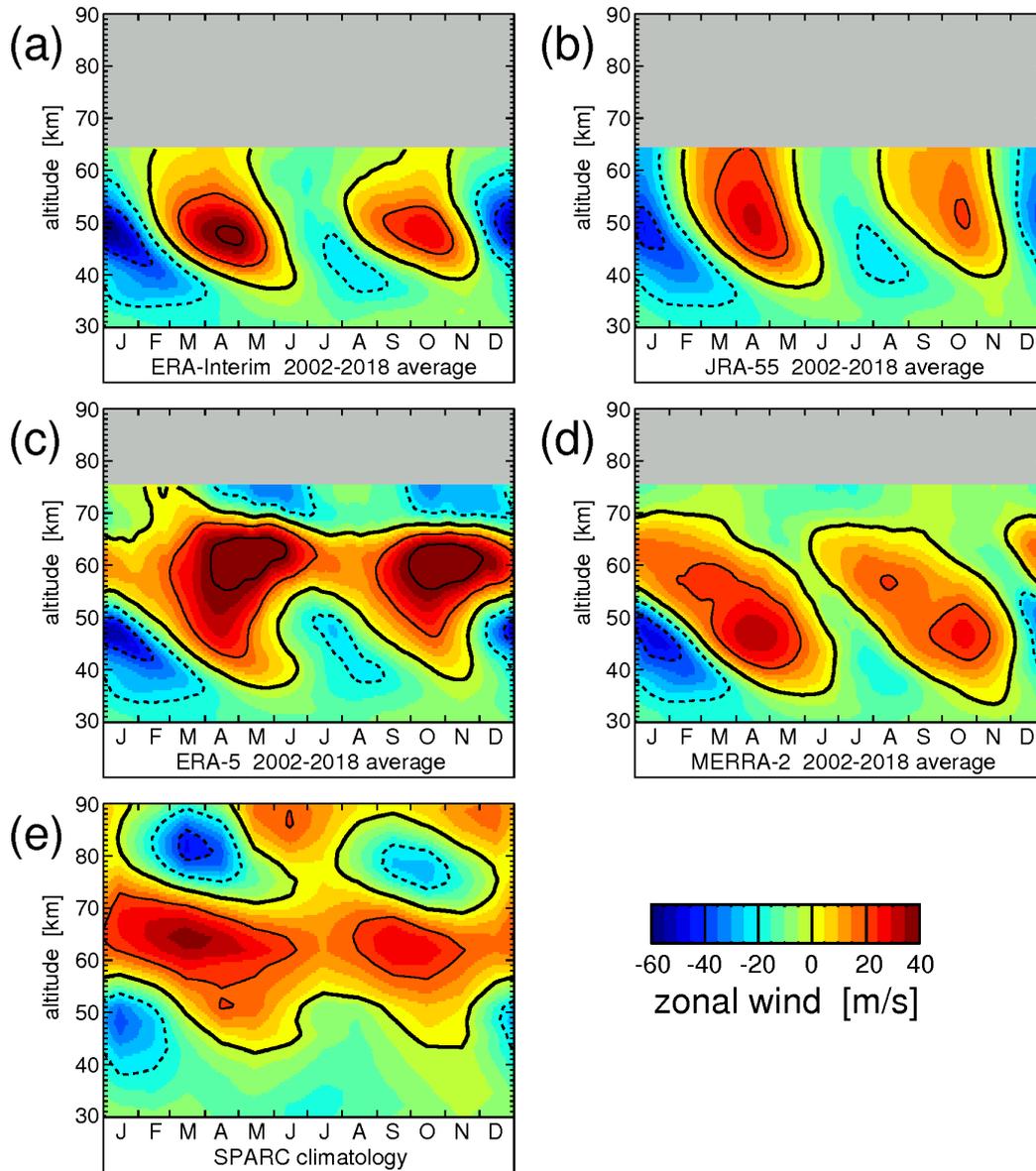


Figure 2. ERA-Interim Typical seasonal variation of the zonal-average zonal wind averaged over 10°S – 10°N for and the 2002–2018-time period together with the multi-year mean seasonal cycle over 2002–2018 for the same period (lower row four reanalyses (a) ERA-Interim, middle panel) (b) JRA-55, (c) ERA-5, and (d) MERRA-2. For comparison the lower right panel, (e) shows the corresponding zonal winds of the SPARC climatology (cf. Swinbank and Ortland, 2003; Randel et al., 2002, 2004). Overplotted are contour lines of the respective wind data set. Contour line increment is 20 m s^{-1} . The zero wind line is highlighted in bold solid, and westward (eastward) winds are indicated by dashed (solid) contour lines.

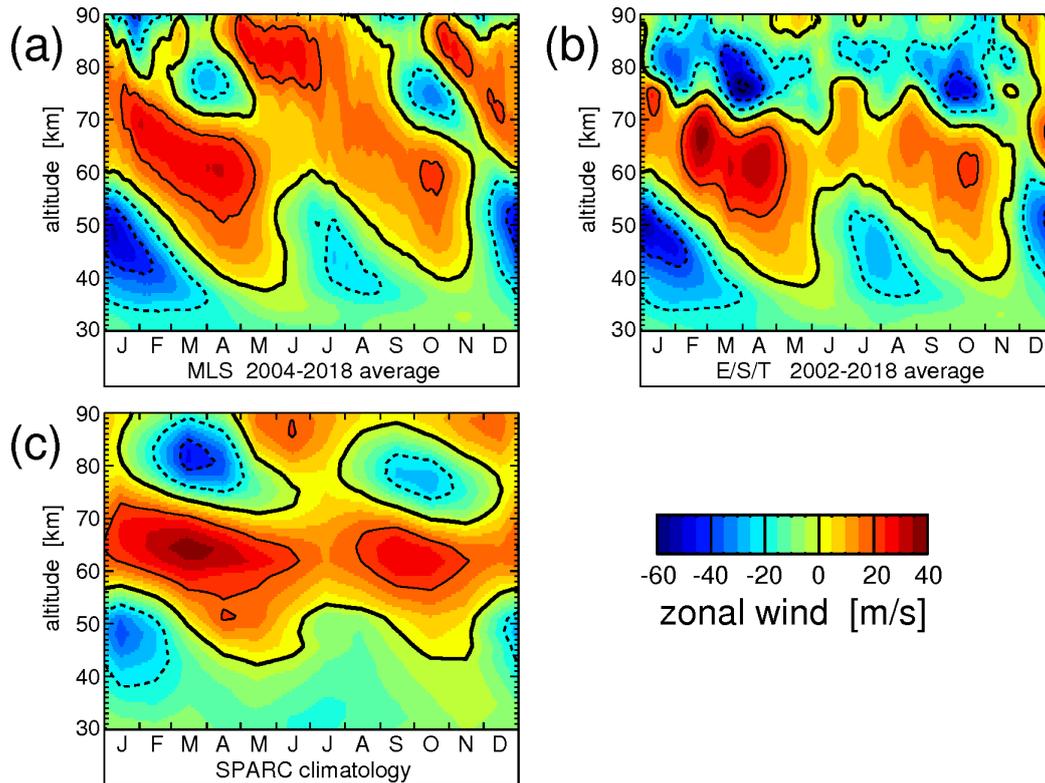


Figure 3. Same as Fig. ?? Typical seasonal variation of the zonal-average zonal wind averaged over 10°S – 10°N and the time period 2002–2018 for two datasets that use satellite data. ?? (a) is a dataset that uses ERA-Interim winds at altitudes <35 km, but for MLS quasi-geostrophic winds at altitudes >45 km, and a smooth transition between ERA-Interim and MLS winds between 35 and 45 km. (b) is a dataset called “E/S/T-winds” that uses ERA-Interim winds at altitudes <35 km, SABER quasi-geostrophic winds at altitudes 45–75 km, and TIDI cold side winds, i.e. direct wind observations, at altitudes above 80 km. Between 35 and 45 km, there is a smooth transition between ERA-Interim and SABER winds. The gap between 75 and 80 km is interpolated. In (a) and (b), MLS, SABER and TIDI winds are an average over ascending and descending orbit branches. For comparison, (c) shows the JRA-55 reanalysis corresponding zonal winds of the SPARC climatology (cf. Swinbank and Orland, 2003; Randel et al., 2002, 2004). Overplotted are contour lines of the respective wind data set. Contour line increment is 20 m s^{-1} . The zero wind line is highlighted in bold solid, and westward (eastward) winds are indicated by dashed (solid) contour lines.

Same as Fig. ??, but for the ERA-5 reanalysis.

Same as Fig. ??, but for MERRA-2.

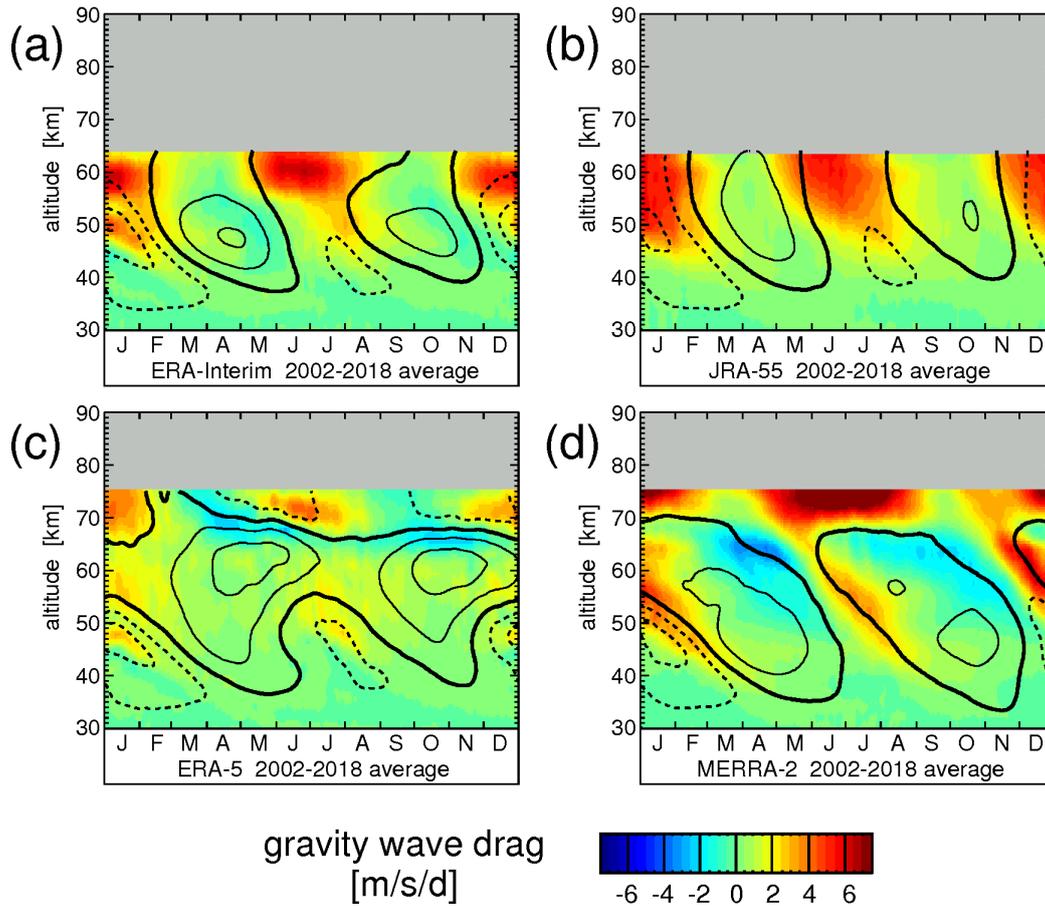


Figure 4. ERA-Interim estimates Typical seasonal variation of the “total” gravity wave drag averaged \bar{X}_{GW} estimated from the TEM momentum budget. The values are averages over 10°S – 10°N for and the 2002–2018 time period, as well as 2002–2018 for the multi-year average over these years four reanalyses (a) ERA-Interim, (b) JRA-55, (c) ERA-5, and (d) MERRA-2. Overplotted are contour lines are ERA-Interim zonal winds averaged over 10°S – 10°N (cf. Fig ?? of the respective wind data set). Contour line increment is 20 m s^{-1} . The zero wind line is highlighted in bold solid, and westward (eastward) zonal wind is winds are indicated by dashed (solid) contour lines.

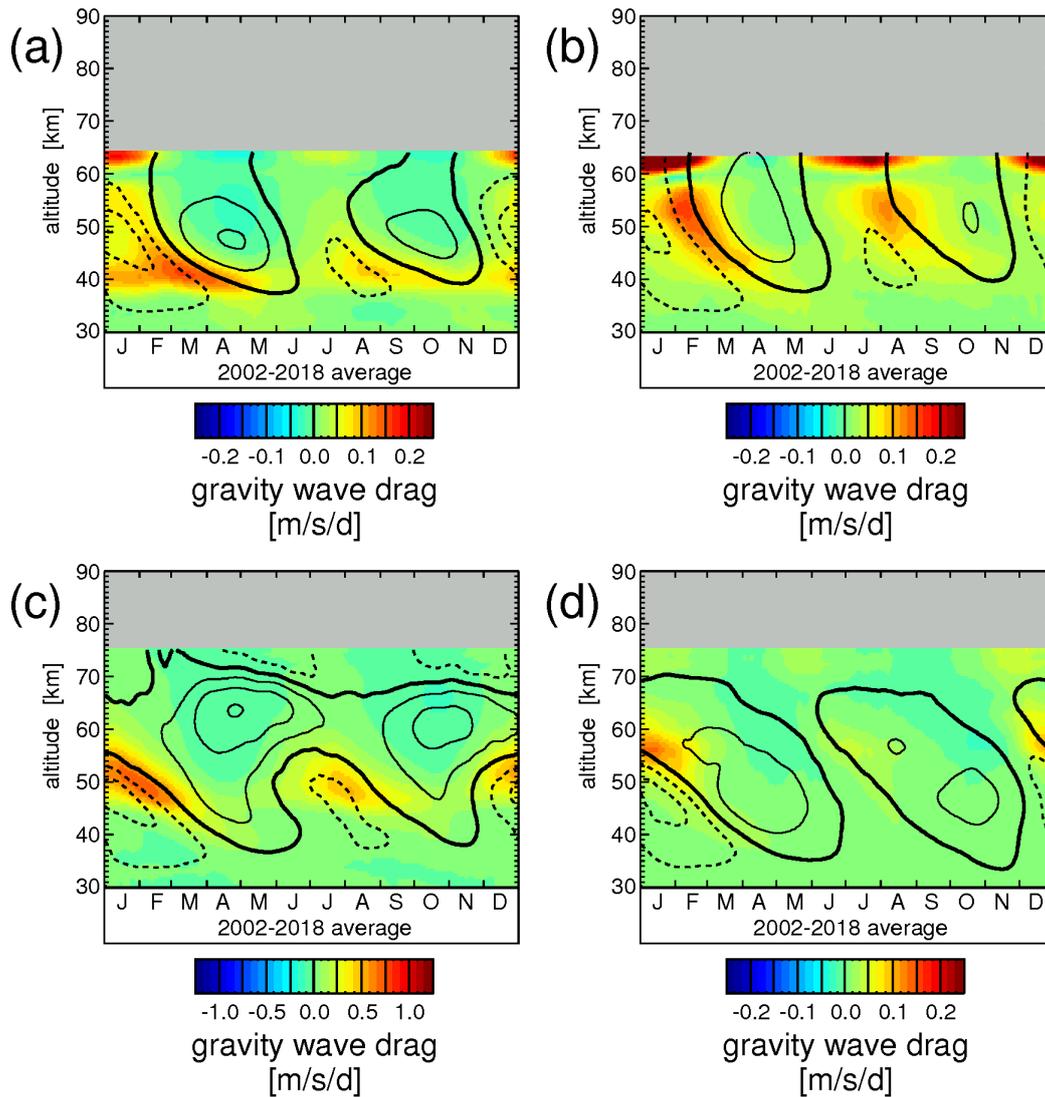


Figure 5. Same as Fig. ??4, but for JRA-55 the zonal gravity wave drag $\bar{X}_{res}(k > 20)$ of model-resolved gravity waves at zonal wavenumbers exceeding $k = 20$.

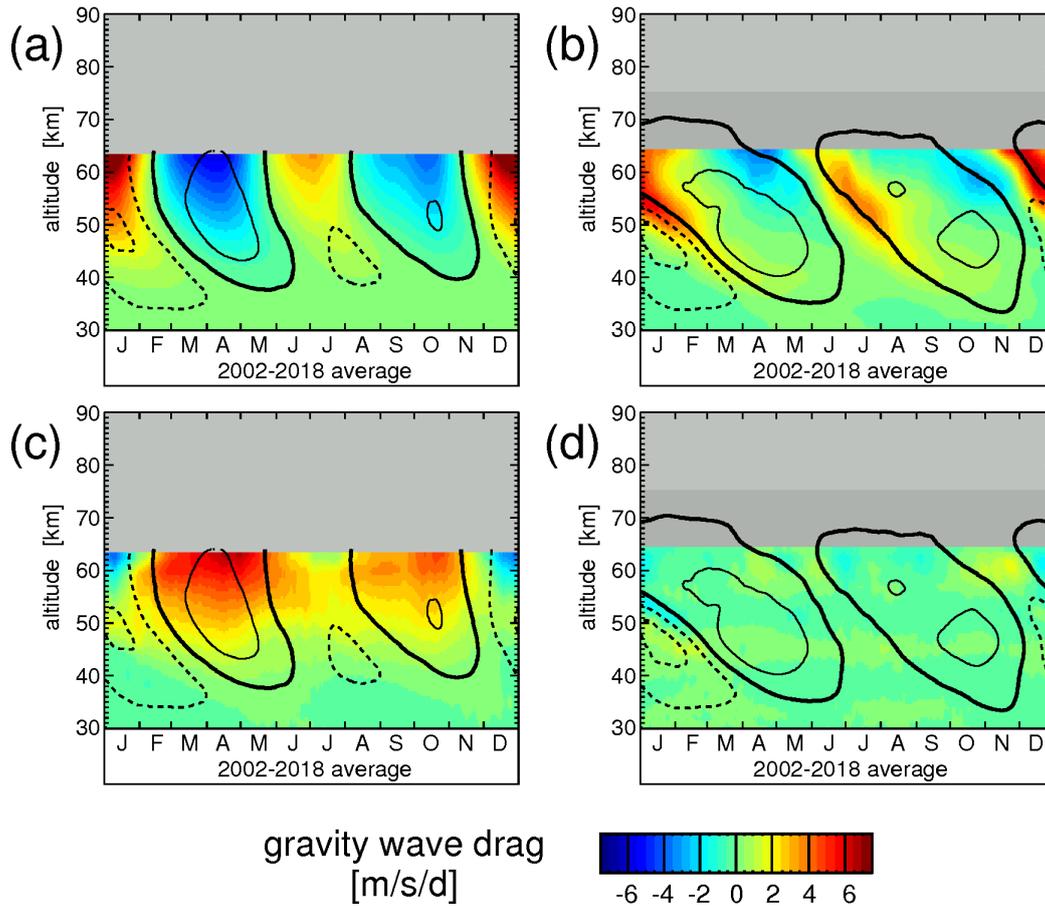


Figure 6. Typical seasonal variation of parameterized gravity wave drag \bar{X}_{drag} for the reanalyses (a) JRA-55 and (b) MERRA-2, as well as the gravity wave drag term $\bar{X}_{imbalance}$ for (c) JRA-55 and (d) MERRA-2. The term $\bar{X}_{imbalance}$ includes, but for MERRA-2 example, the model imbalance that is caused by data assimilation. Again, values are averages over 10°S – 10°N and the time period 2002–2018, and contour lines of the respective wind data set are overplotted. Contour line increment is 20 m s^{-1} . The zero wind line is highlighted in bold solid, and westward (eastward) winds are indicated by dashed (solid) contour lines.

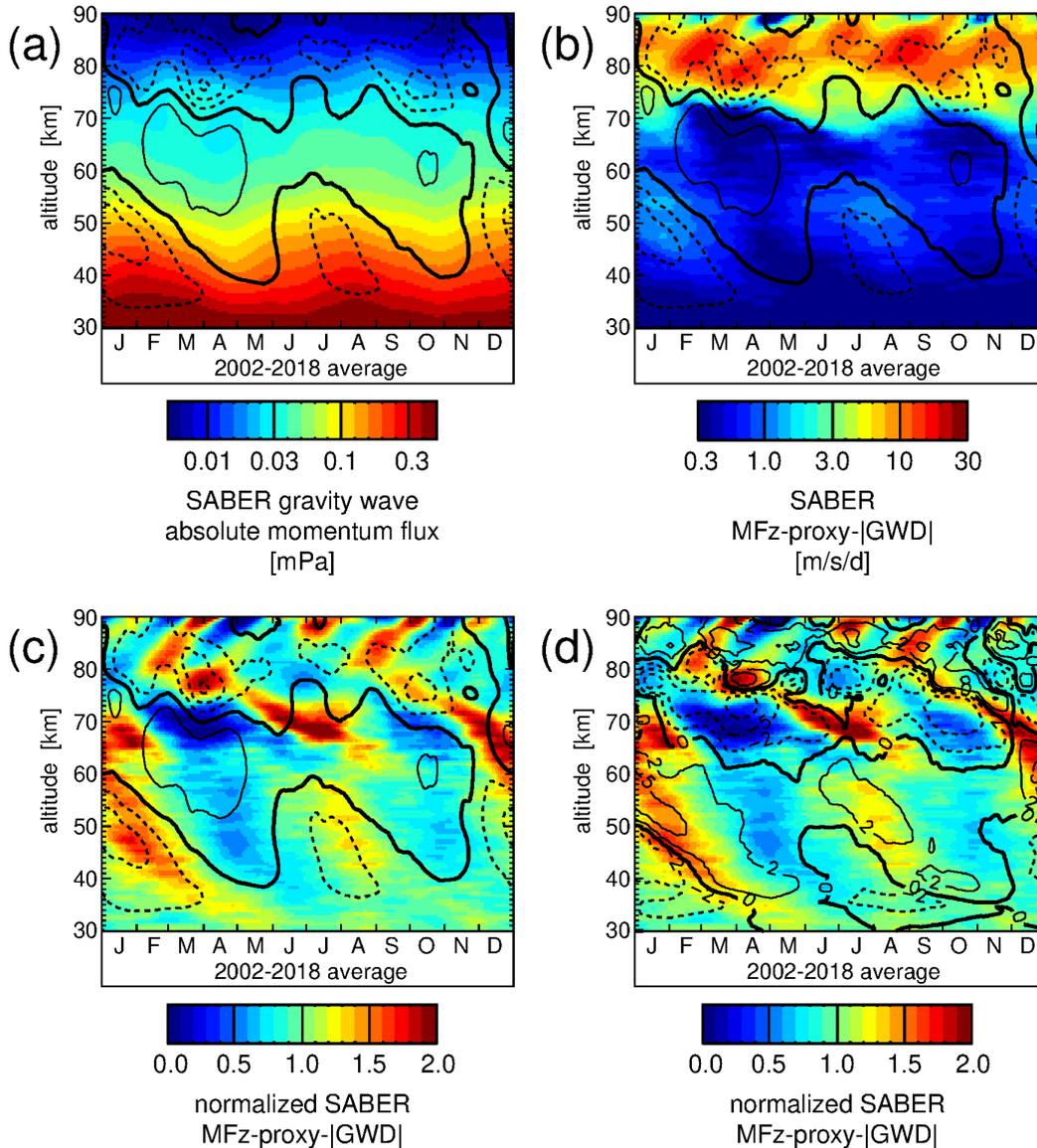


Figure 7. Same as Fig. Typical seasonal variation of (a) SABER absolute gravity wave momentum fluxes, (b) SABER MFz-proxy-|GWD|, and (c) SABER MFz-proxy-|GWD| normalized by the altitude-dependent annual means. Overplotted in (a)–(c) are contour lines of the E/S/T-wind dataset. Contour line increment is 20 m s^{-1} . The zero wind line is highlighted in bold solid, and westward (eastward) winds are indicated by dashed (solid) contour lines. In addition, (d) shows the same as (c), but for ERA-5 overplotted contour lines are the vertical gradient du/dz of the E/S/T-winds. Contour lines are at $0, \pm 2, \pm 5, \text{ and } \pm 10 \text{ m s}^{-1} \text{ km}^{-1}$. Westward (=negative) gradients are indicated by dashed contour lines.

1545 Same as Fig. ??, but for interpolated MLS quasi-geostrophic zonal winds averaged over the latitude band 10°S – 10°N . These winds represent an average over both local solar times (ascending and descending orbit nodes are combined). MLS observations started in 2004. Therefore the panels for 2002 and 2003 are left blank.

1550 Same as Fig. ??, but for the combined data set of ERA-Interim zonal winds below 35, interpolated SABER quasi-geostrophic zonal winds at altitudes 45–75, and a smooth transition between ERA-Interim and SABER winds at altitudes 35–45. Winds above ~ 80 are TIDI cold-side zonal winds. Several smaller TIDI data gaps are closed by linear interpolation in time. For one larger data gap and in the beginning of 2002 SABER quasi-geostrophic winds are used also above 75. Otherwise the data gap between SABER winds at 75 and TIDI winds at 80 is interpolated. Winds are an average over 10°S – 10°N , and SABER and TIDI winds are an average over ascending and descending orbit branches.

1555 SABER absolute gravity wave momentum flux in on a logarithmic scale for the 2002–2018 time period averaged over the latitude band 10°S – 10°N , and the average over these years (lower right panel). Contour lines are zonal-average zonal winds of the merged data set based on ERA-Interim, SABER, and TIDI, as described in Sect. 4.2.3.

SABER absolute gravity wave drag in $^{-1-1}$ on a logarithmic scale for the 2002–2018 time period averaged over the latitude band 10°S – 10°N , and the average over these years (lower right panel). Contour lines are zonal-average zonal winds of the merged data set based on ERA-Interim, SABER, and TIDI, as described in Sect. 4.2.3.

1560 Same as Fig. ??, but for the gravity wave drag anomaly, i.e., the absolute gravity wave drag shown in Fig. ?? normalized by the average gravity wave drag, separately for each year and altitude.

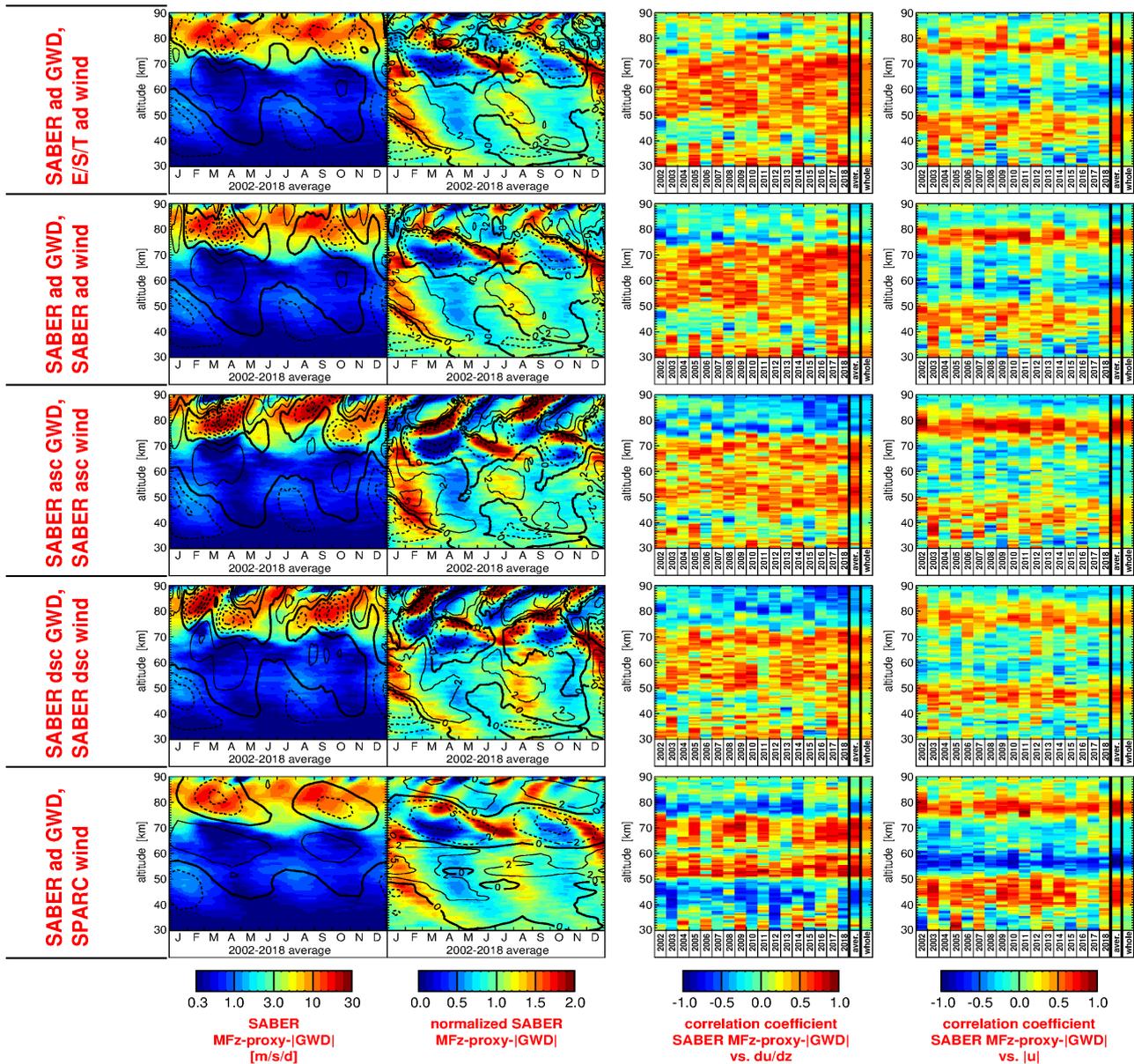


Figure 8. Left column: the SABER MFz-proxy-|GWD| (a proxy for absolute gravity wave drag) averaged over 10°S – 10°N and the years 2002–2018, overplotted with zonal wind contour lines of different zonal wind data sets averaged over the same latitudes and period. Second column: Same as Fig. ?? left column, but for normalized SABER MFz-proxy-|GWD| overplotted with contour lines are the vertical gradient of zonal-average zonal winds of wind vertical gradients. Third column: Temporal correlations between SABER MFz-proxy-|GWD| and zonal wind vertical gradients, separately for each year, for the multi-year averages, and for the whole time series. Right column: Same as third column, but for the correlation between SABER MFz-proxy-|GWD| and zonal wind absolute values. The different rows are (from top to bottom) for (1) the merged data set based on ERA-Interim, SABER \bar{u} , and TIDI \bar{u} data set as described in Sect. 4.2.3 averaged over ascending and descending orbit legs, (2) ERA-Interim and SABER winds merged, similar as for MLS in Sect. Contour lines 4.2.2, averaged over ascending and descending orbit legs (i.e. SABER geostrophic winds are at 0 used also above 75 km), \pm (3) same as (2), \pm 5 but only for ascending orbit legs, (4) same as (2), but only for descending orbit legs, and \pm 10 (5) SPARC climatology winds (same wind used for each year). For zonal winds, contour line increment is 20 m s^{-1} . Westward (eastward) winds are indicated by dashed (solid) contour lines.

Left column: Different zonal wind data sets averaged over 10°S – 10°N and the years 2002–2018 (2004–2018 for MLS).
Second column: SABER absolute gravity wave drag averaged over the same latitudes and corresponding periods, overplotted
with zonal wind contour lines. Third column: Same as second column, but for normalized SABER absolute gravity wave drag
overplotted with contour lines of zonal wind vertical gradients. Fourth column: Temporal correlations between SABER gravity
1565 wave drag and zonal wind vertical gradients, separately for each year, and for the multi-year averages. Right column: Same
as fourth column, but for the correlation between SABER gravity wave drag and zonal wind absolute values. The different
rows are (from top to bottom) for (1) the merged ERA-Interim, SABER and TIDI data set as described in Sect. 4.2.3 averaged
over ascending and descending orbit legs, (2) same as (1), but only for ascending orbit legs, (3) same as (1), but only for
1570 descending orbit legs, (4) ERA-Interim and SABER winds merged, similar as for MLS in Sect. 4.2.2, averaged over ascending
and descending orbit legs (i.e. SABER geostrophic winds are used also above 75), (5) same as (4), but only for ascending orbit
legs, (6) same as (4), but only for descending orbit legs, (7) ERA-Interim and MLS winds merged as described in Sect. 4.2.2,
averaged over both orbit legs, and (8) SPARC climatology winds (same wind used for each year).

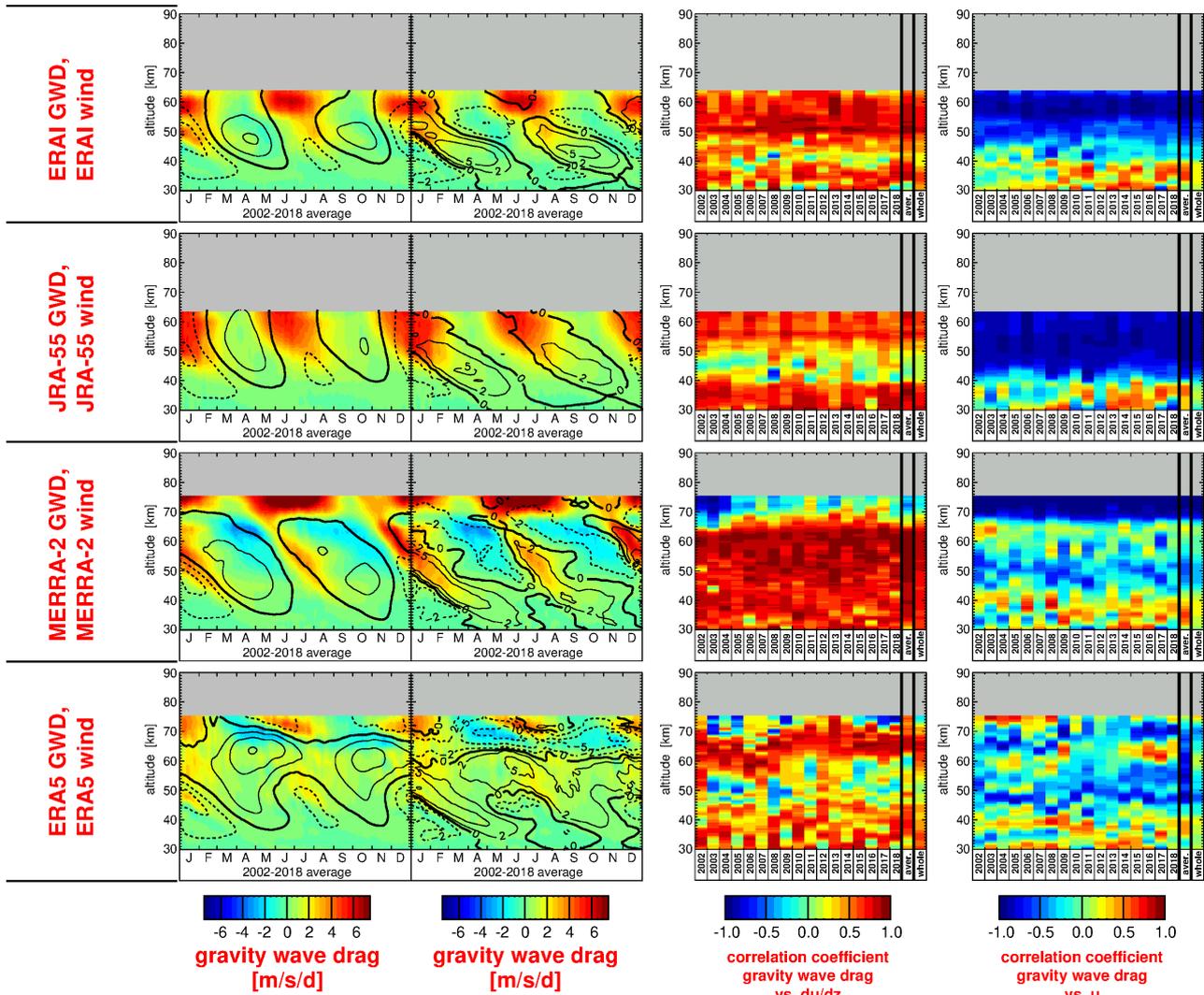


Figure 9. Left column: zonal winds of Gravity wave drag in $\text{m s}^{-1}\text{day}^{-1}$ derived from the four reanalyses considered in this study, averaged over the latitude band 10°S – 10°N and the years 2002–2018. Second column: Gravity wave drag in $^{-1-1}$ derived from the different reanalyses and averaged over the years 2002 until 2018, overplotted with zonal wind contour lines of the corresponding zonal winds averaged over the same latitudes and time period. Third-Second column: Same as second-left column, but contour lines are the vertical gradient of the zonal wind. Fourth-Third column: Temporal correlations between reanalysis gravity wave drag and zonal wind vertical gradients, separately for each year, and for the averages over the different years, and for the time series as a whole. Right column: Temporal correlations between reanalysis gravity wave drag and zonal wind, separately for each year, and for the averages over the different years, and for the time series as a whole. The different rows are (from top to bottom) for (1) ERA-Interim, (2) JRA-55, (3) MERRA-2, and (4) ERA-5. For zonal winds, contour line increment is 20 m s^{-1} . The zero wind line is highlighted in bold solid, and westward (eastward) winds are indicated by dashed (solid) contour lines.

Supplement to:

“The semiannual oscillation (SAO) in the tropical middle atmosphere and its gravity wave driving in reanalyses and satellite observations”

published in *Atmos. Chem. Phys.*, 2021.

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In the main paper only distributions of the different parameters averaged over multiple years are shown. However, also the distributions for single years contain important information. This is the case because the semiannual oscillation (SAO) undergoes strong interannual variability, and there are peculiarities of the gravity wave driving in certain years. Further, before the year 2004 no MLS data are assimilated in the MERRA-2 reanalysis. Therefore, the distributions for the single years are important to show that MERRA-2 simulates a reasonable SAO also in the years before 2004. The reasonable SAO in the early MERRA-2 years is likely an effect of the parameterized gravity wave drag in MERRA-2 that was tuned in a way to simulate a reasonable SAO in all years. This is indicated by the rather low imbalance term shown in Fig. S19. For these reasons, we provide the distributions for the single years 2002 until 2018, as well as the average distributions in this supplement.

The following figures are shown in the supplement:

Figure S1 shows the local solar times of SABER and TIDI observations at the equator.

Figures S2–S5 show zonal-average zonal wind averaged over 10°S–10°N for the four reanalyses ERA-Interim, JRA-55, ERA-5, and MERRA-2.

Figure S6 shows a merged zonal wind product that uses ERA-Interim at low altitudes, and, at higher altitudes, zonal wind estimated from MLS observations using the quasi-geostrophic assumption.

Figure S7 shows a merged zonal wind product that uses ERA-Interim at low altitudes, SABER quasi-geostrophic winds at mid altitudes, and TIDI wind observations at high altitudes (“E/S/T-winds”). For details see the main paper.

Further, zonal total gravity wave drag \overline{X}_{GW} was estimated for the four reanalyses. \overline{X}_{GW} comprises the drag of model-resolved waves at zonal wavenumbers k higher than 20 ($\overline{X}_{res}(k > 20)$), gravity wave drag that is parameterized in the model (\overline{X}_{param}), and the remaining imbalance ($\overline{X}_{imbalance}$) in the momentum budget that is caused by, for example, data assimilation:

$$\overline{X}_{GW} = \overline{X}_{res}(k > 20) + \overline{X}_{param} + \overline{X}_{imbalance} \quad (1)$$

Figures S8–S10 show the zonal total gravity wave drag \overline{X}_{GW} for the four reanalyses, and Figs. S12–S14 the model-resolved gravity wave drag $\overline{X}_{res}(k > 20)$. Figures S16–S17 show the parameterized gravity wave drag \overline{X}_{param} for JRA-55 and MERRA-2, and Figs. S18–S19 the imbalance term $\overline{X}_{imbalance}$ for JRA-55 and MERRA-2 that contributes to the estimate \overline{X}_{GW} of the total gravity wave drag. For ERA-Interim and ERA-5 \overline{X}_{param} and $\overline{X}_{imbalance}$ are not available.

Figure S20 shows SABER absolute gravity wave momentum flux.

Figure S21 shows the SABER proxy “MFz-proxy-|GWD|” which is obtained from vertical gradients of SABER absolute gravity wave momentum flux normalized by the negative background density. Under certain assumptions, MFz-proxy-|GWD| can be used as a proxy for absolute net gravity wave drag.

Figures S22 and S23 show the same as Fig. S21, but values are normalized by the altitude-dependent annual averages.

Similar as Fig. 8 in the main paper, Fig. S24 shows correlations between SABER MFz-proxy-|GWD| and the vertical gradient of the zonal wind, as well as correlations between SABER MFz-proxy-|GWD| and absolute zonal wind speed, but for three additional combinations of MFz-proxy-|GWD| and wind data set.

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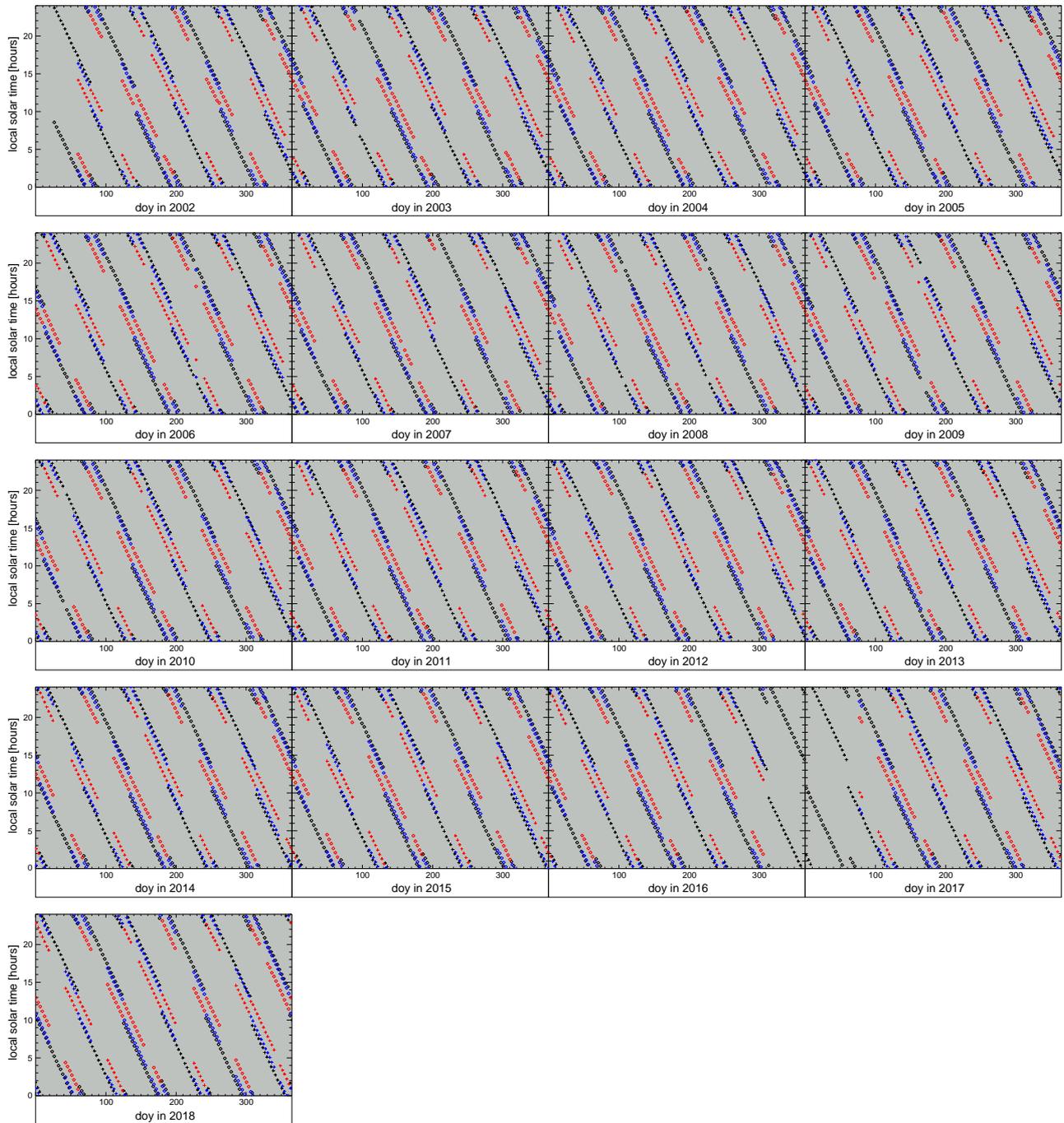


Figure S1. Local solar times of SABER and TIDI observations at the equator for the 2002–2018 time period. Local solar times are given for the following: SABER ascending (black diamonds), SABER descending (black crosses) TIDI warm side ascending (red diamonds), TIDI warm side descending (red crosses), TIDI cold side ascending (blue diamonds), and TIDI cold side descending (blue crosses).

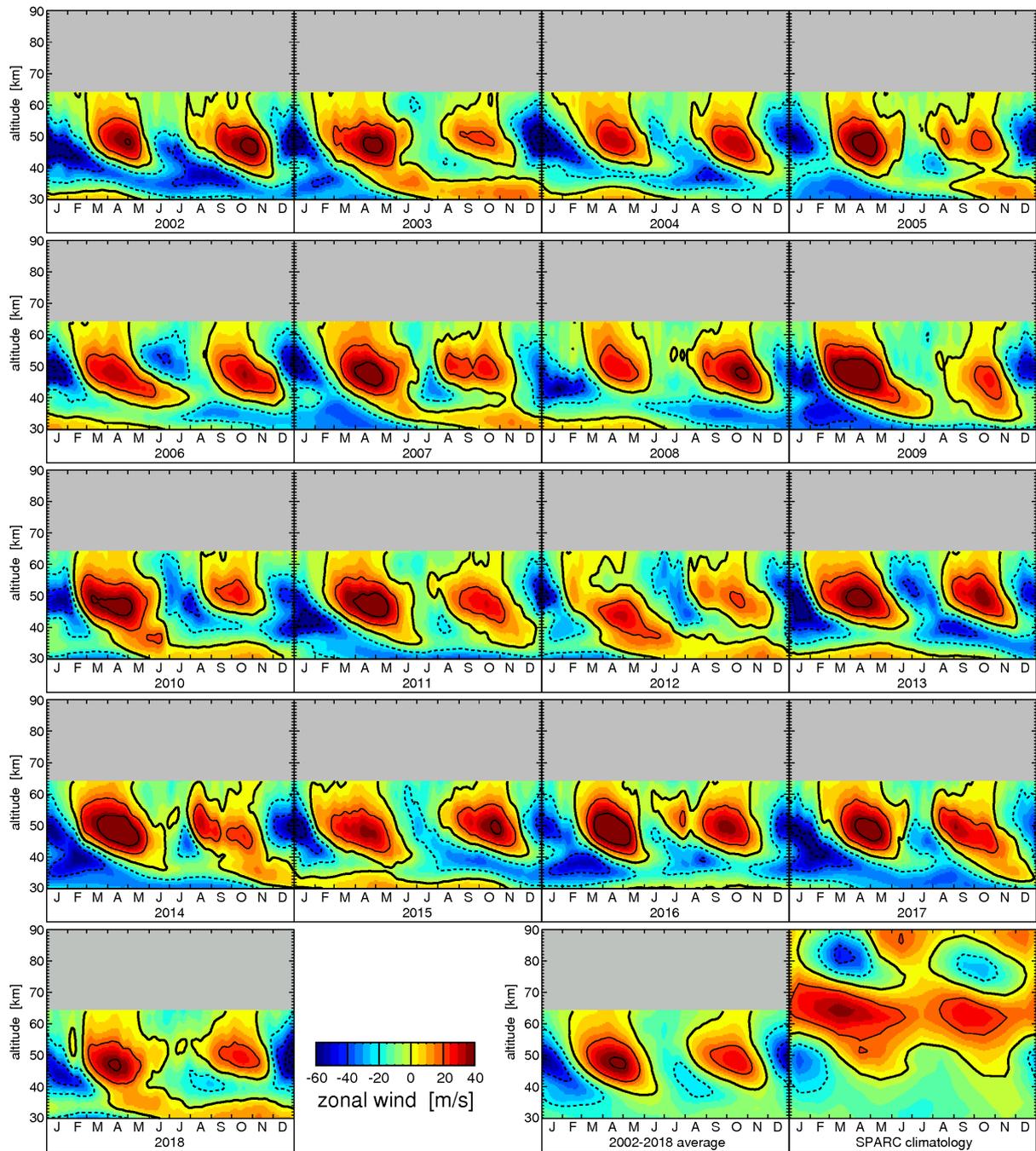


Figure S2. ERA-Interim zonal-average zonal wind averaged over 10°S – 10°N for the 2002–2018 time period together with the multi-year mean seasonal cycle over the same period (lower row, middle panel). For comparison the lower right panel shows the corresponding zonal winds of the SPARC climatology (cf. Swinbank and Orland, 2003; Randel et al., 2002, 2004). Contour line increment is 20 m s^{-1} . The zero wind line is highlighted in bold solid, and westward (eastward) winds are indicated by dashed (solid) contour lines.

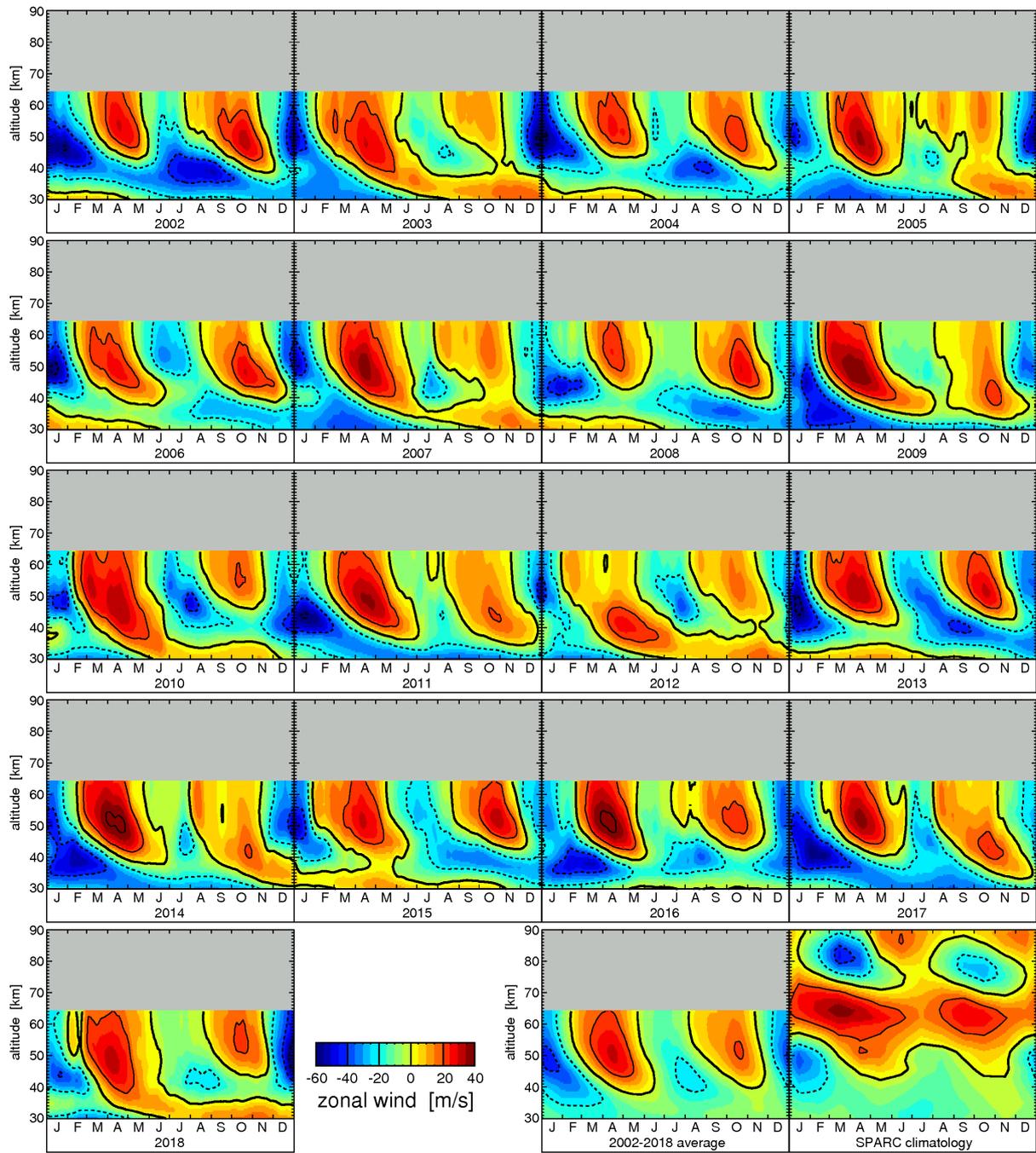


Figure S3. Same as Fig. S2, but zonal-average zonal wind for the JRA-55 reanalysis.

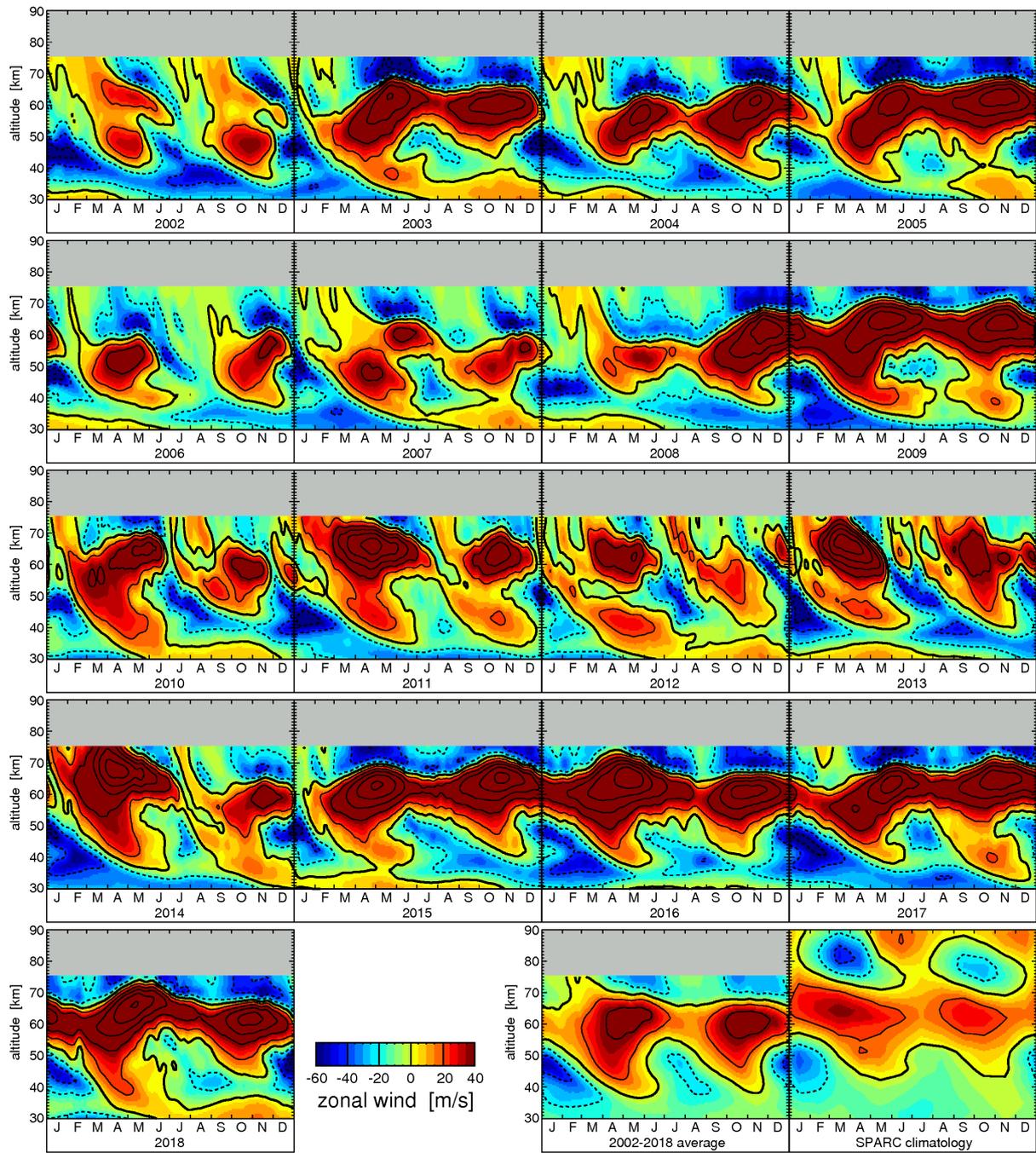


Figure S4. Same as Fig. S2, but zonal-average zonal wind for the ERA-5 reanalysis.

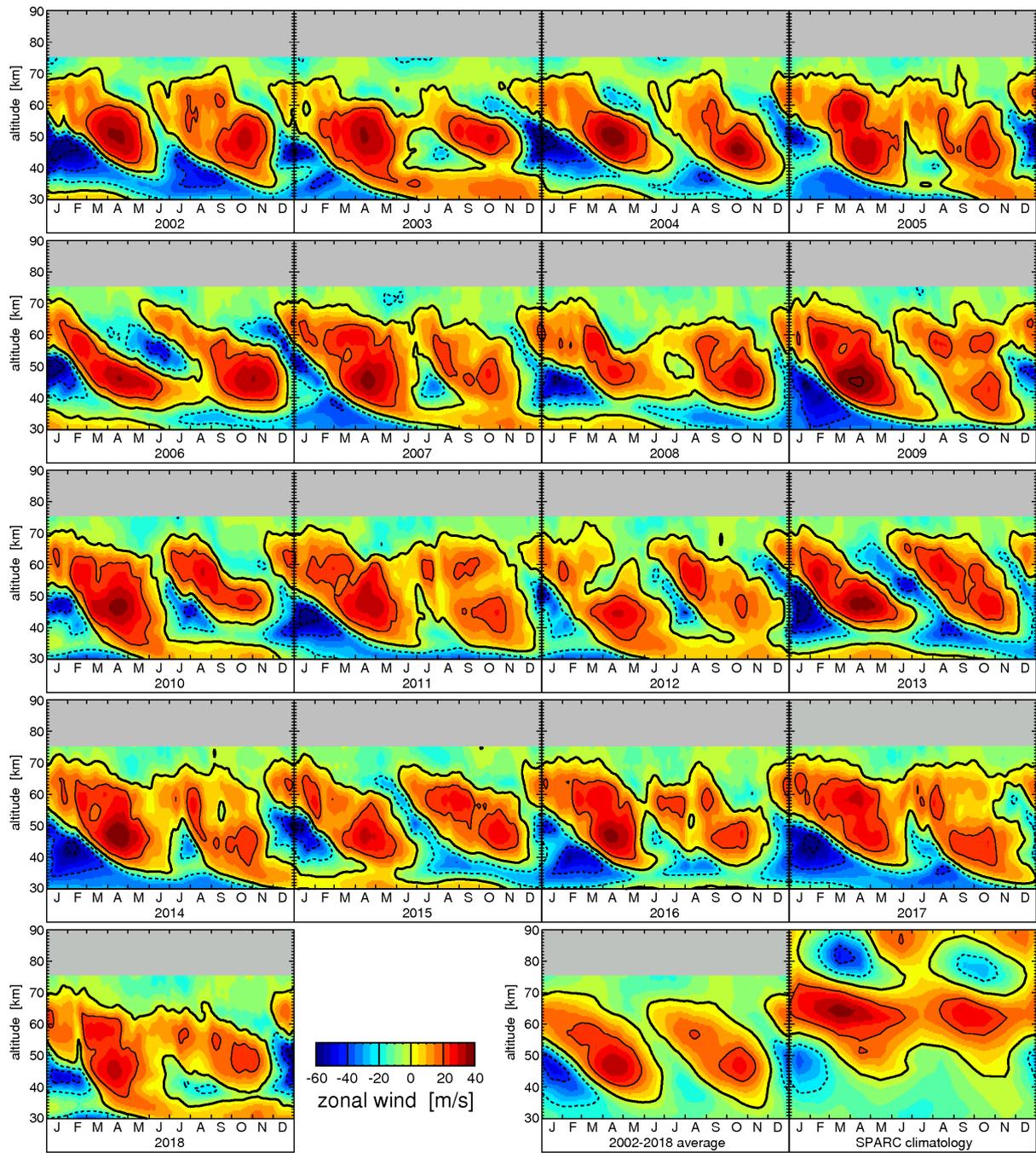


Figure S5. Same as Fig. S2, but zonal-average zonal wind for MERRA-2.

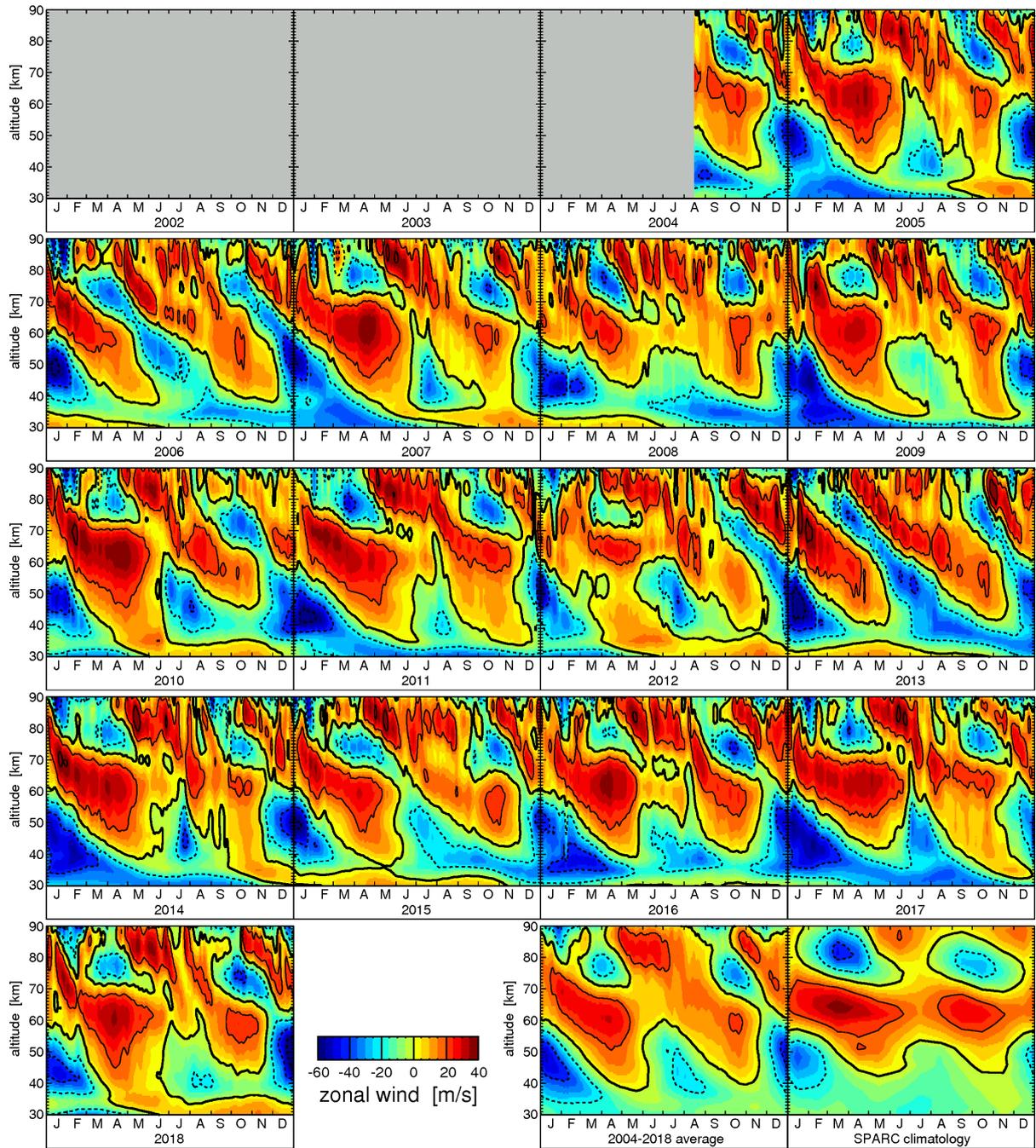


Figure S6. Same as Fig. S2, but for the combined data set of ERA-Interim zonal winds below 35 km and, at higher altitudes, interpolated MLS quasi-geostrophic zonal winds averaged over the latitude band 10°S – 10°N . At altitudes 35–45 km a smooth transition between ERA-Interim and MLS winds is made. The MLS winds represent an average over both local solar times (ascending and descending orbit nodes are combined). MLS observations started in 2004. Therefore, the panels for 2002 and 2003 are left blank.

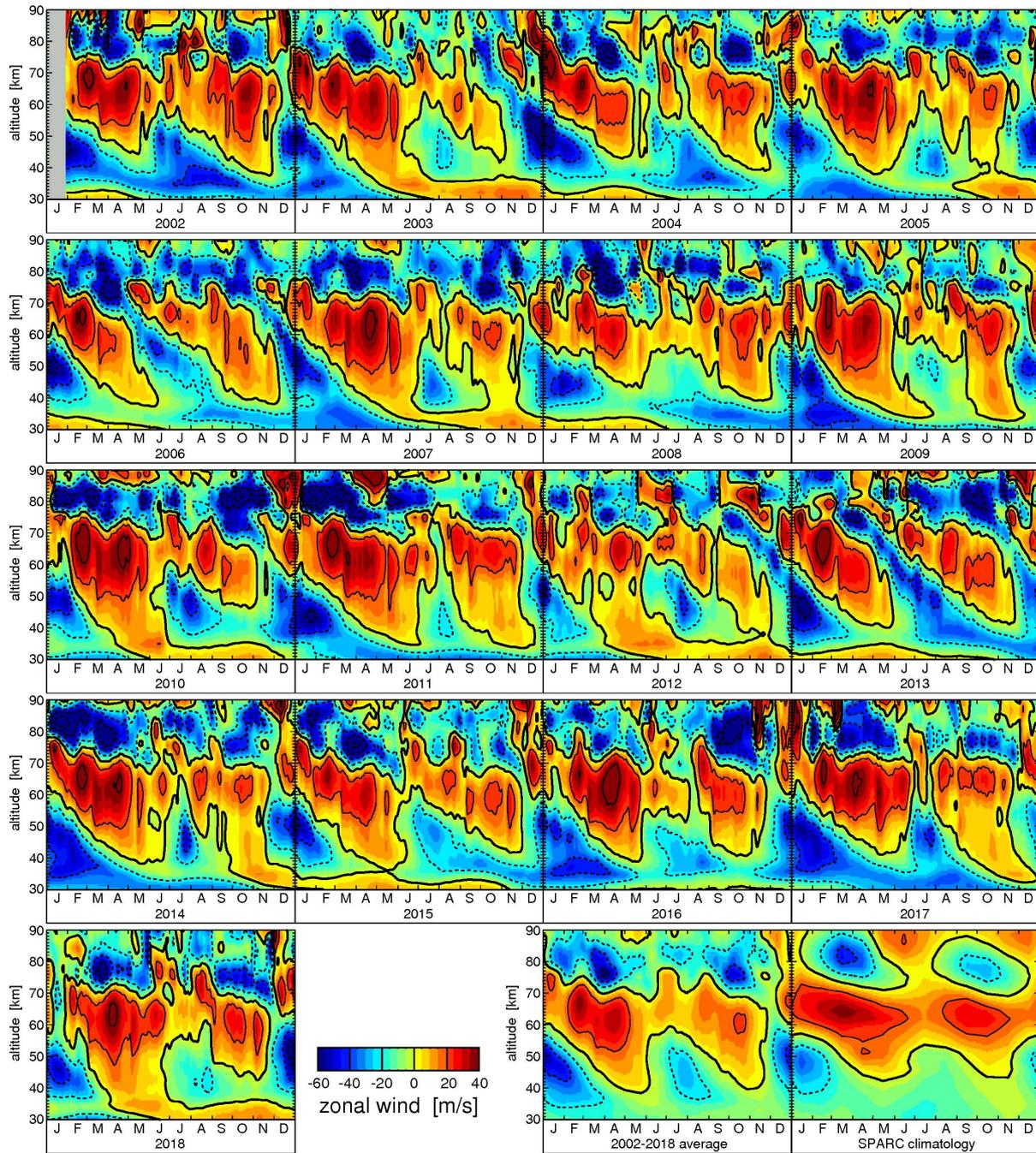


Figure S7. Same as Fig. S2, but for the combined data set (E/S/T-winds) of ERA-Interim zonal winds below 35 km, interpolated SABER quasi-geostrophic zonal winds at altitudes 45–75 km, and a smooth transition between ERA-Interim and SABER winds at altitudes 35–45 km. Winds above ~ 80 km are TIDI cold side zonal winds. Several smaller TIDI data gaps are closed by linear interpolation in time. For one larger data gap and in the beginning of 2002 SABER quasi-geostrophic winds are used also above 75 km. Otherwise the data gap between SABER winds at 75 km and TIDI winds at 80 km is interpolated. Winds are an average over 10°S – 10°N , and SABER and TIDI winds are an average over ascending and descending orbit branches.

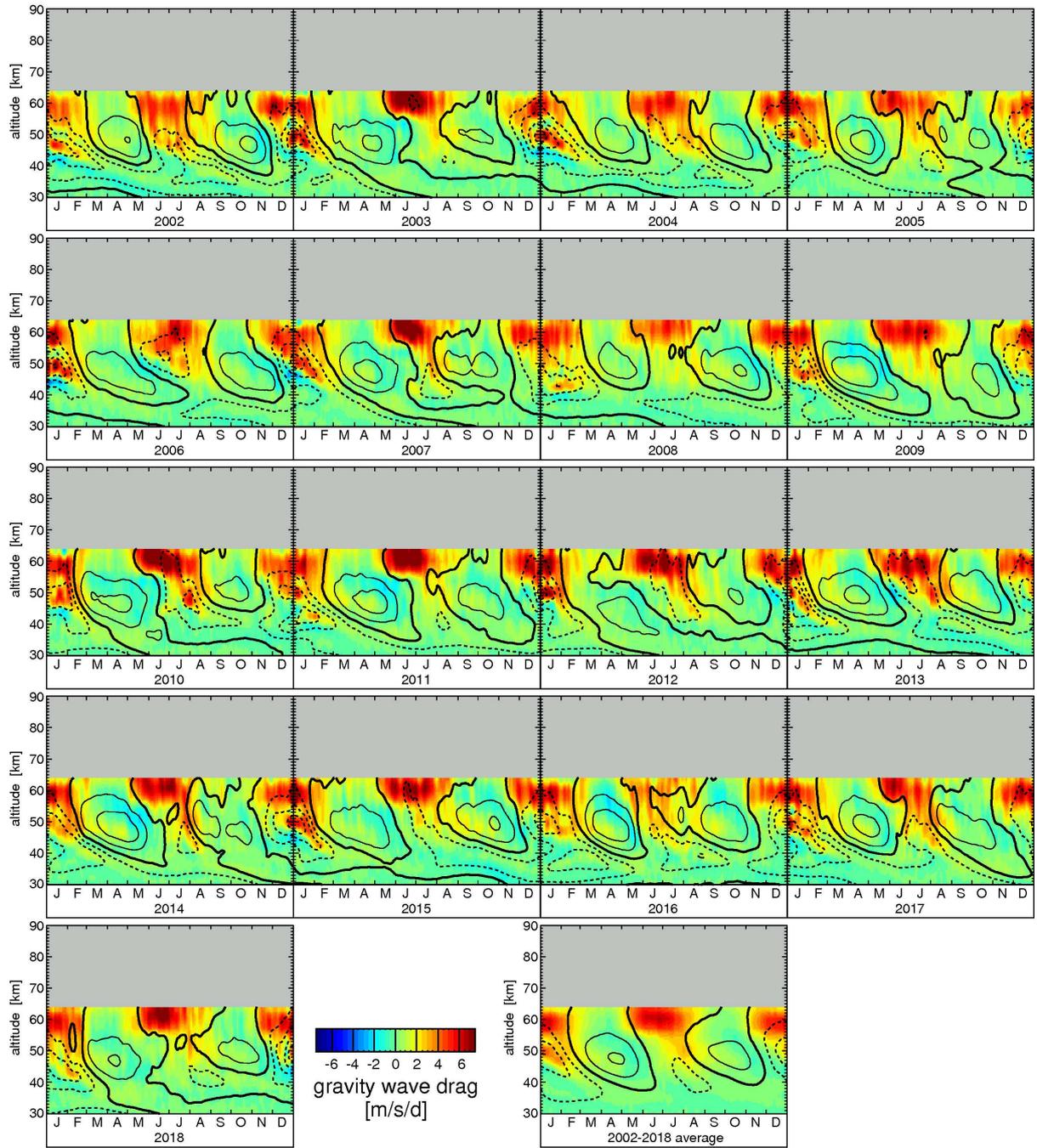


Figure S8. ERA-Interim estimates of zonal total gravity wave drag \overline{X}_{GW} averaged over 10°S – 10°N for the 2002–2018 time period, as well as the multi-year average over these years. Overplotted contour lines are ERA-Interim zonal winds averaged over 10°S – 10°N (cf. Fig S2). Contour line increment is 20 m s^{-1} . The zero line is highlighted in bold solid, and westward (eastward) zonal wind is indicated by dashed (solid) contour lines.

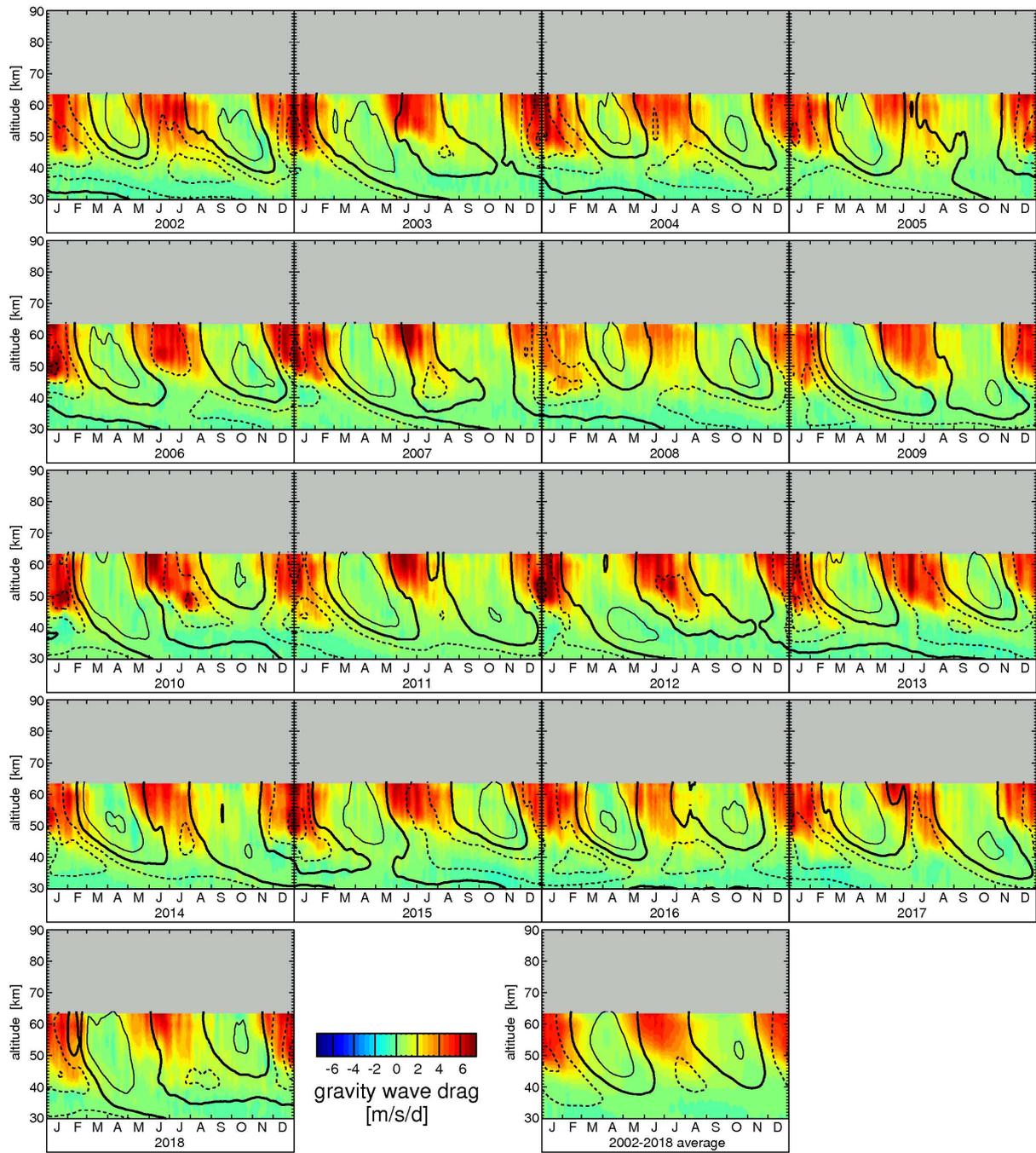


Figure S9. Same as Fig. S8, but zonal total gravity wave drag for JRA-55, overlotted with contour lines of JRA-55 winds (cf. Fig S3).

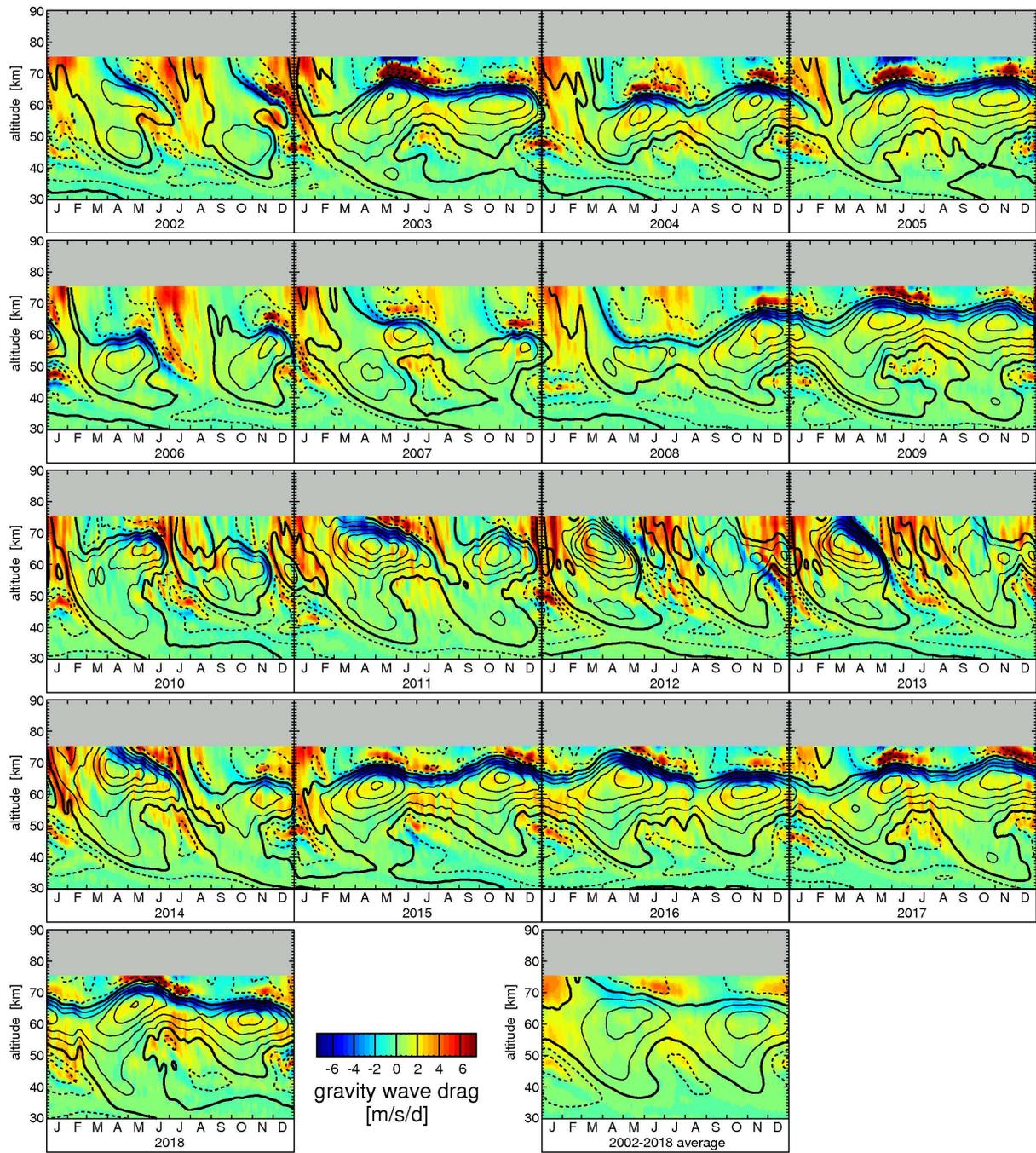


Figure S10. Same as Fig. S8, but zonal total gravity wave drag for ERA-5, overplotted with contour lines of ERA-5 winds (cf. Fig S4).

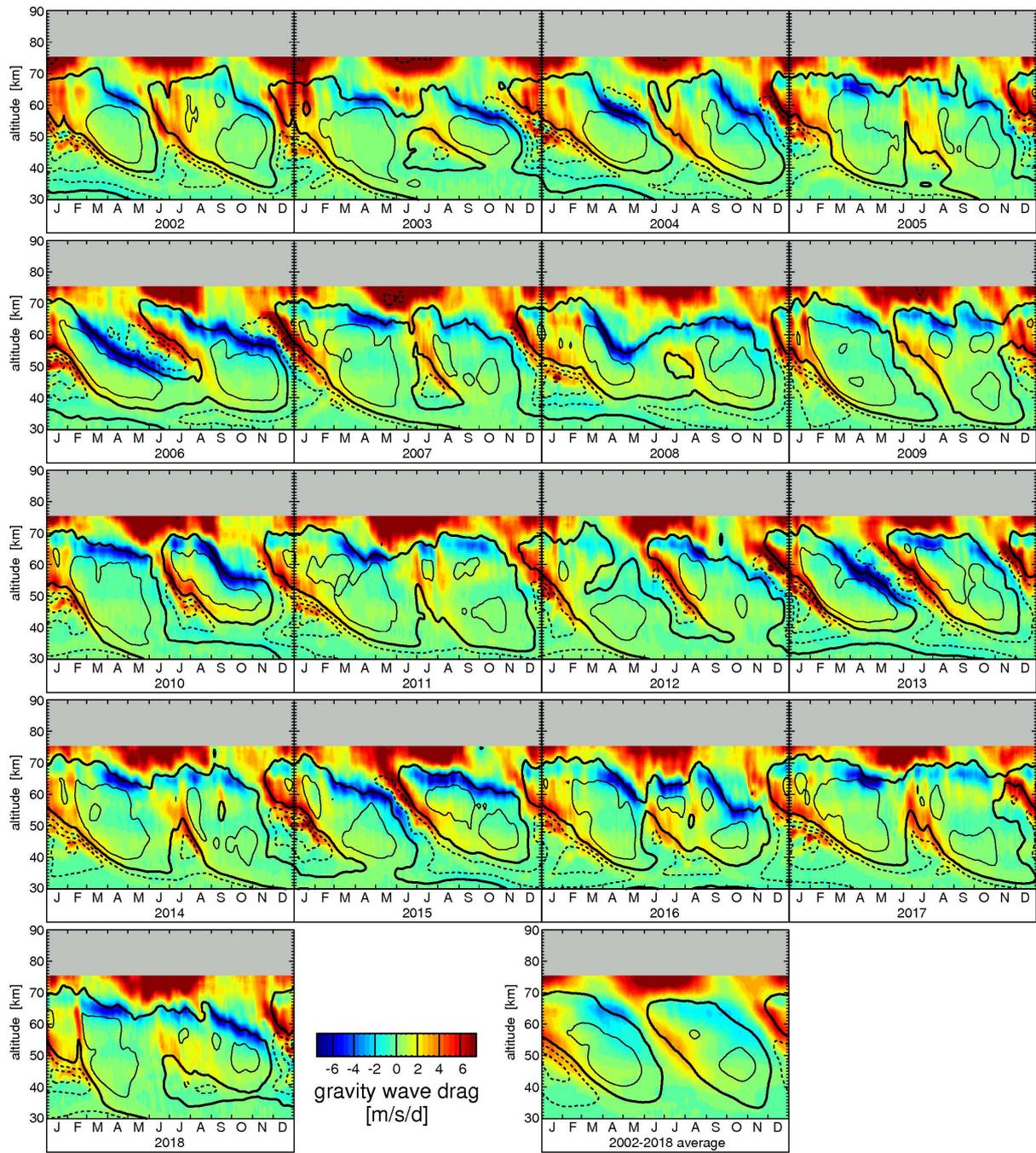


Figure S11. Same as Fig. S8, but zonal total gravity wave drag for MERRA-2, overplotted with contour lines of MERRA-2 winds (cf. Fig S5).

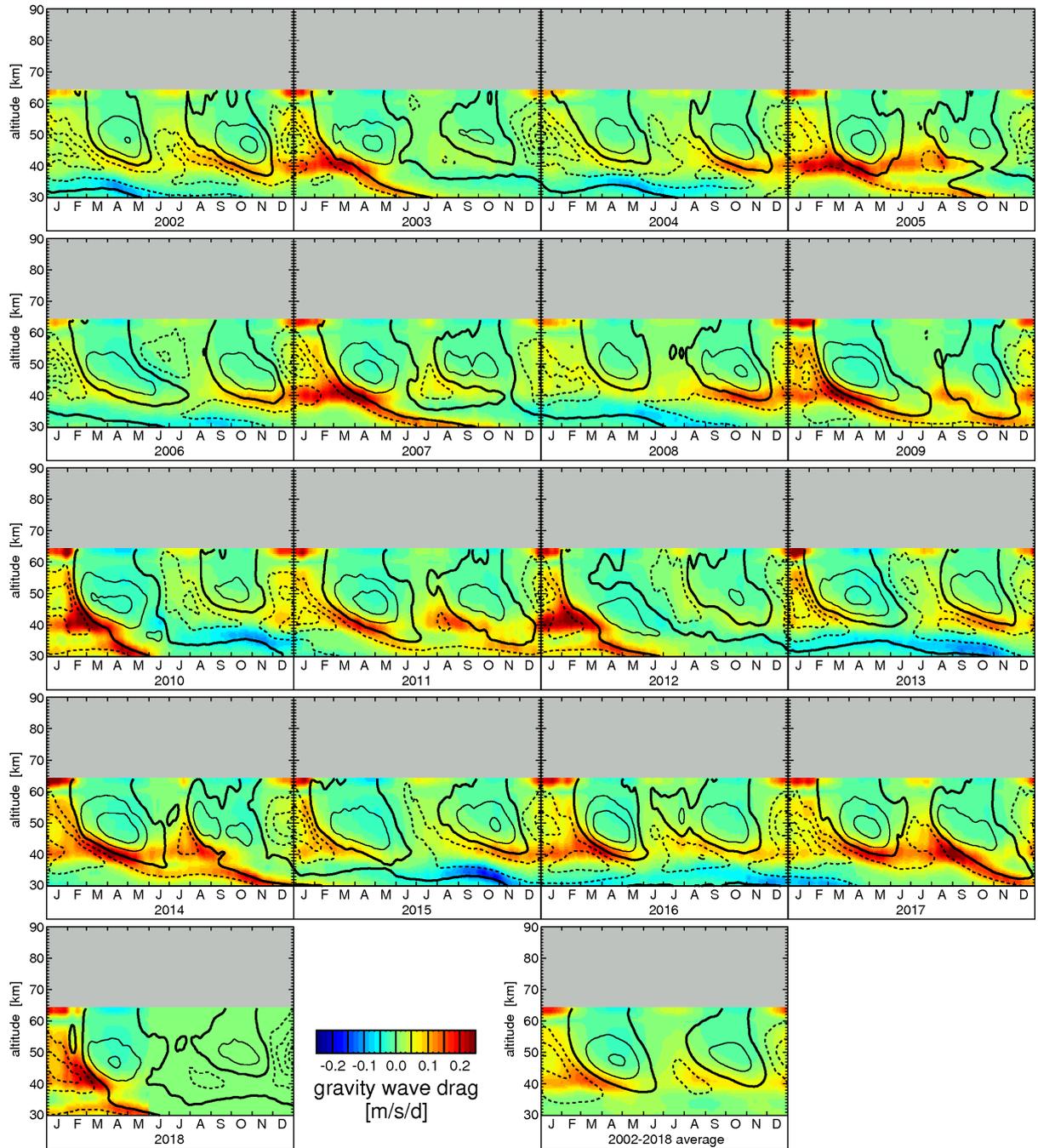


Figure S12. ERA-Interim estimates of model-resolved zonal gravity wave drag $\overline{X}_{res}(k > 20)$ averaged over 10°S – 10°N for the 2002–2018 time period, as well as the multi-year average over these years. Overplotted contour lines are ERA-Interim zonal winds averaged over 10°S – 10°N (cf. Fig S2). Contour line increment is 20 m s^{-1} . The zero line is highlighted in bold solid, and westward (eastward) zonal wind is indicated by dashed (solid) contour lines.

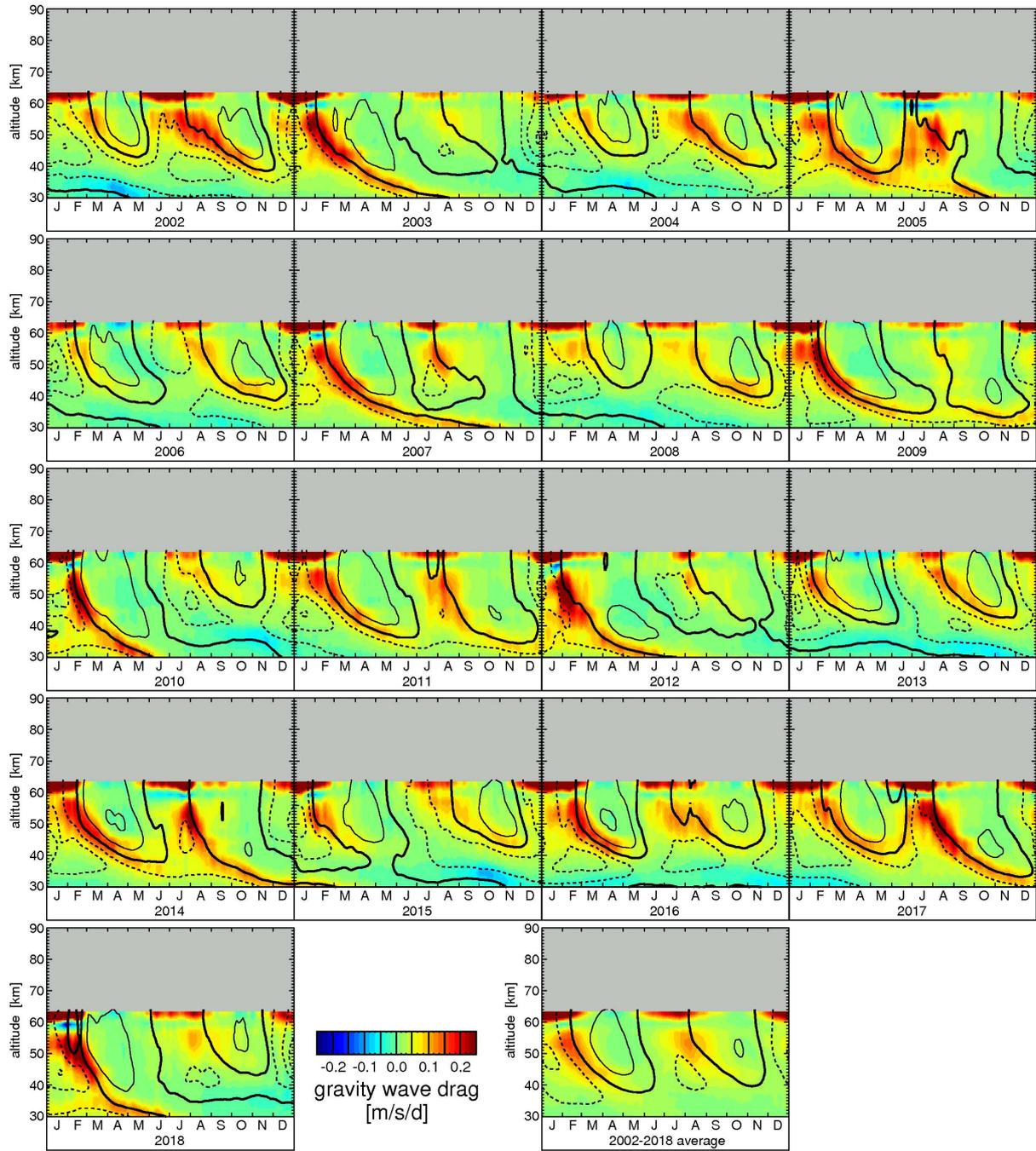


Figure S13. Same as Fig. S12, but model-resolved zonal gravity wave drag $\overline{X}_{res}(k > 20)$ for JRA-55, overlotted with contour lines of JRA-55 winds (cf. Fig S3).

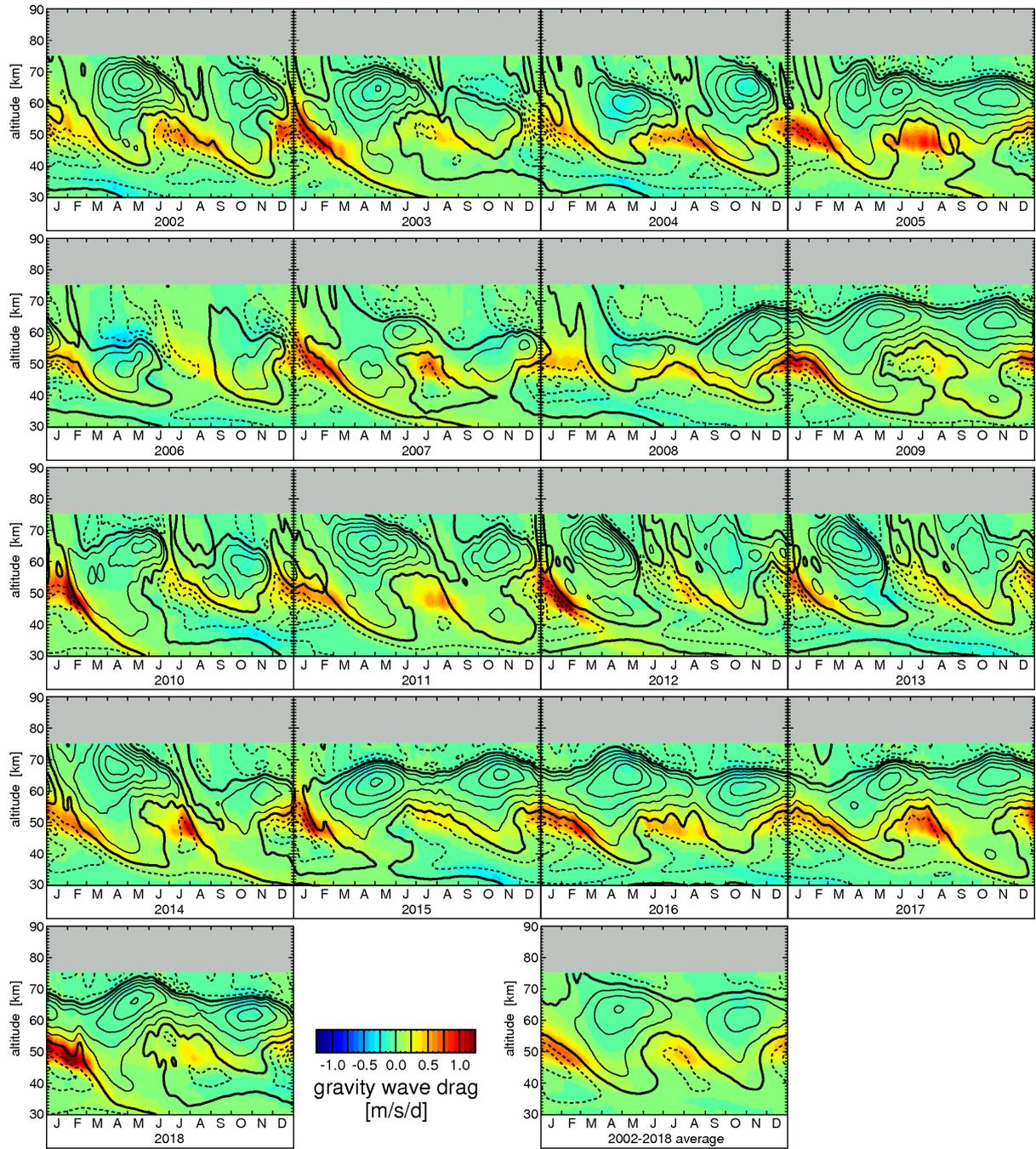


Figure S14. Same as Fig. S12, but model-resolved zonal gravity wave drag $\overline{X}_{res}(k > 20)$ for ERA-5, overplotted with contour lines of ERA-5 winds (cf. Fig S4).

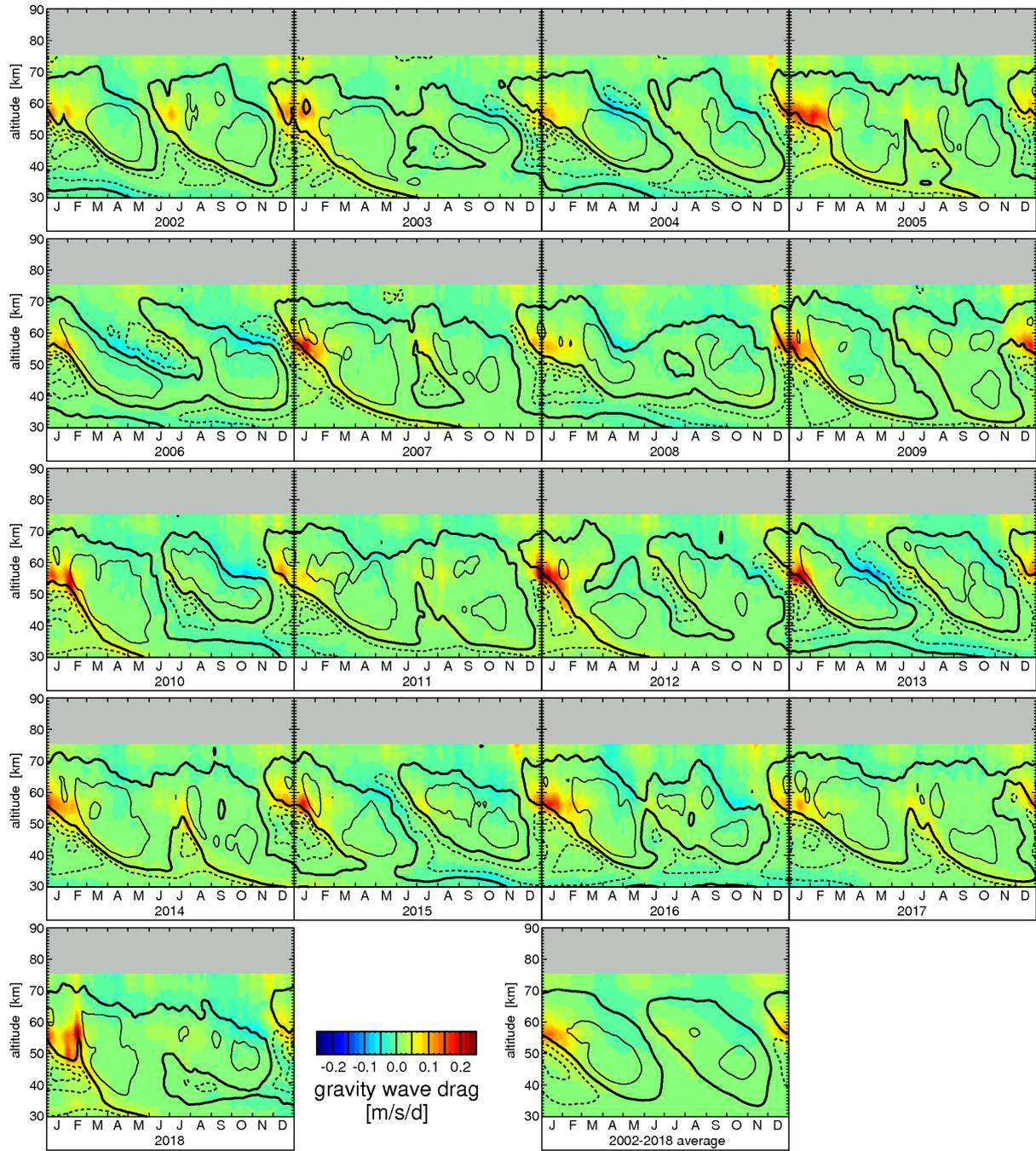


Figure S15. Same as Fig. S12, but model-resolved zonal gravity wave drag $\overline{X_{res}(k > 20)}$ for MERRA-2, overplotted with contour lines of MERRA-2 winds (cf. Fig S5).

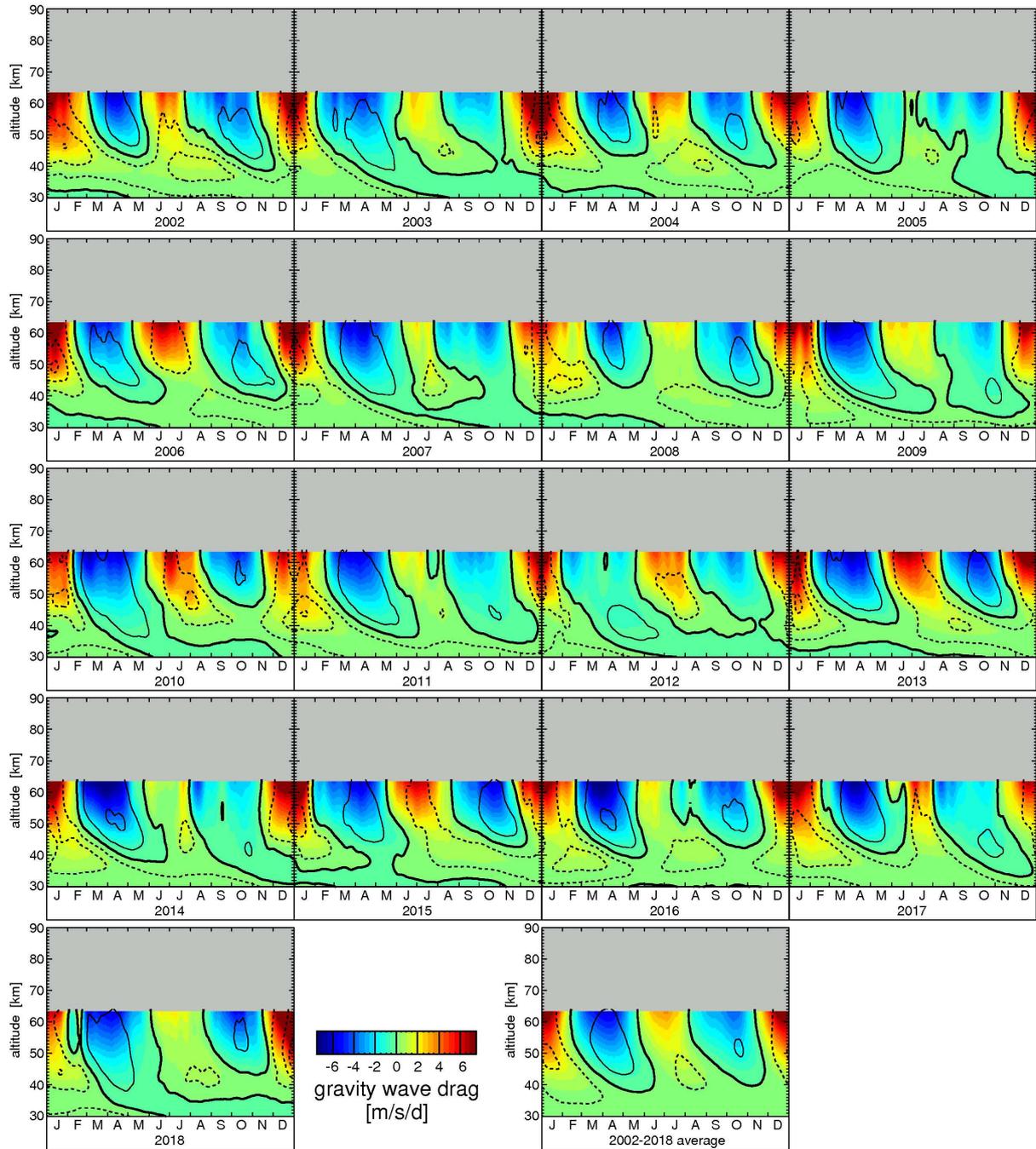


Figure S16. JRA-55 estimates of parameterized zonal gravity wave drag $\overline{X_{param}}$ averaged over 10°S – 10°N for the 2002–2018 time period, as well as the multi-year average over these years. Overplotted contour lines are JRA-55 zonal winds averaged over 10°S – 10°N (cf. Fig S3). Contour line increment is 20 m s^{-1} . The zero line is highlighted in bold solid, and westward (eastward) zonal wind is indicated by dashed (solid) contour lines.

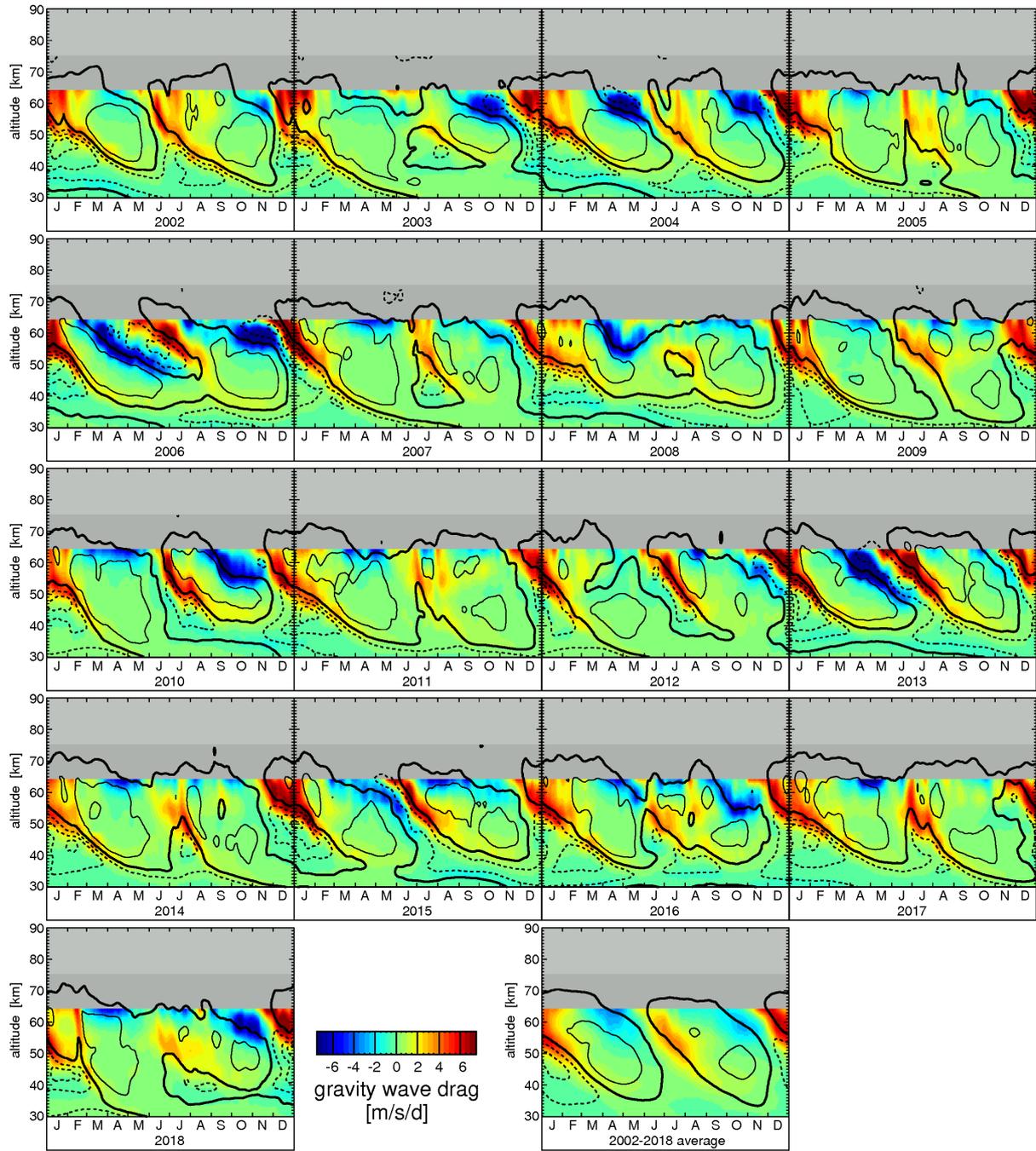


Figure S17. Same as Fig. S16, but parameterized zonal gravity wave drag \overline{X}_{param} for MERRA-2, overplotted with contour lines of MERRA-2 winds (cf. Fig S5).

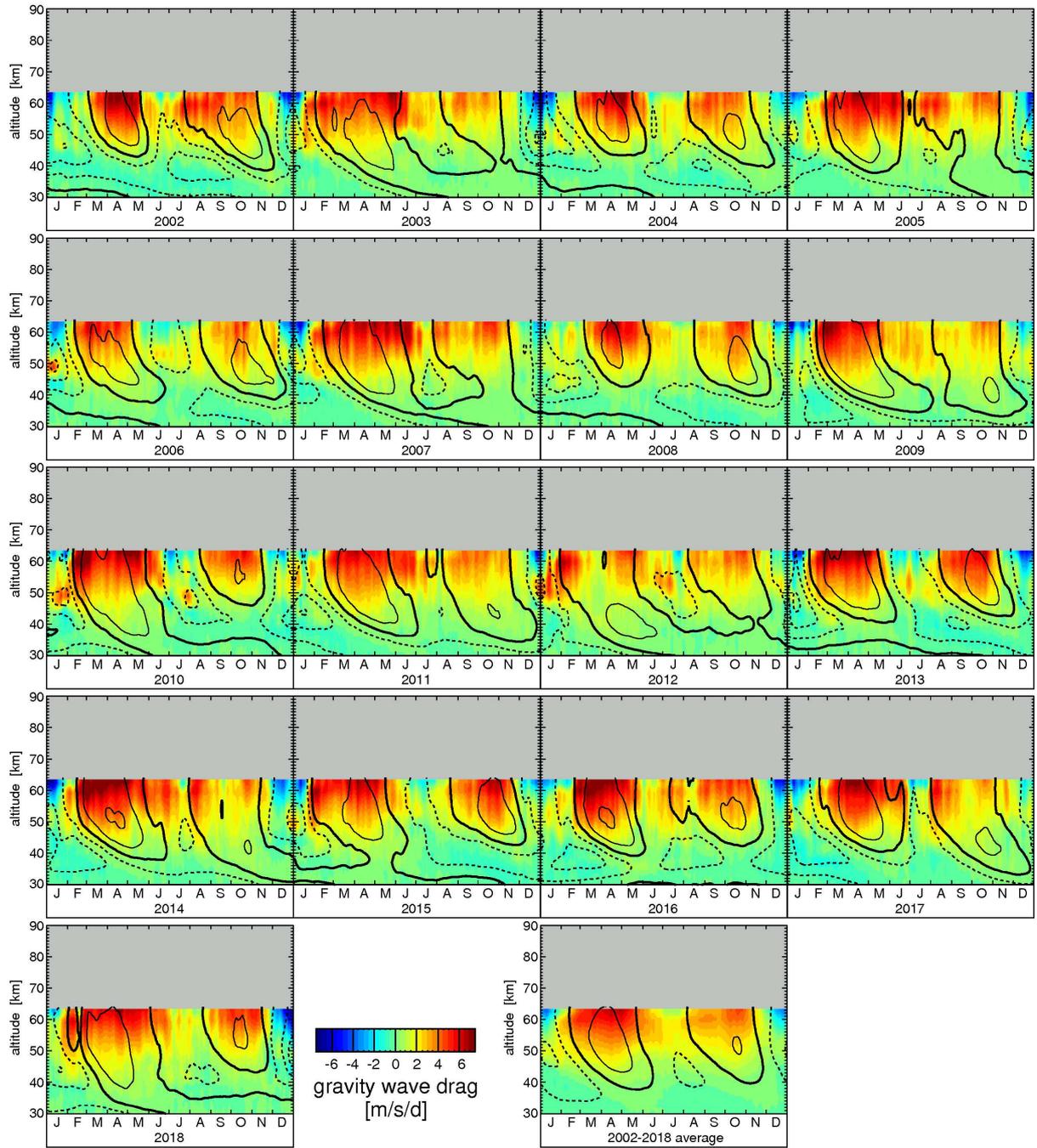


Figure S18. JRA-55 estimates of the imbalance contribution $\overline{X}_{imbalance}$ to the total gravity wave drag averaged over 10°S – 10°N for the 2002–2018 time period, as well as the multi-year average over these years. Overplotted contour lines are JRA-55 zonal winds averaged over 10°S – 10°N (cf. Fig S3). Contour line increment is 20 m s^{-1} . The zero line is highlighted in bold solid, and westward (eastward) zonal wind is indicated by dashed (solid) contour lines.

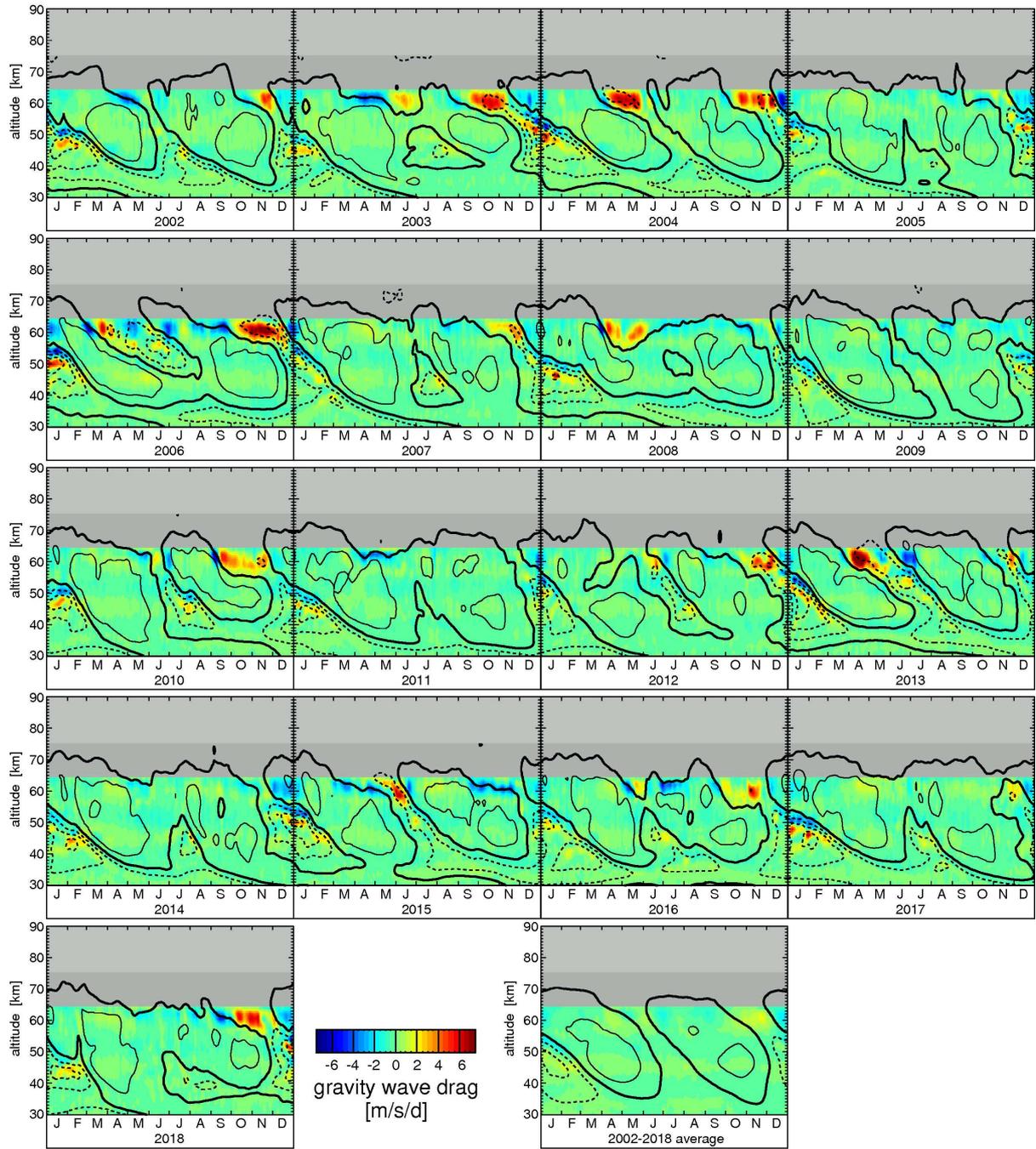


Figure S19. Same as Fig. S18, but the imbalance contribution $\overline{X}_{imbalance}$ for MERRA-2, overplotted with contour lines of MERRA-2 winds (cf. Fig S5).

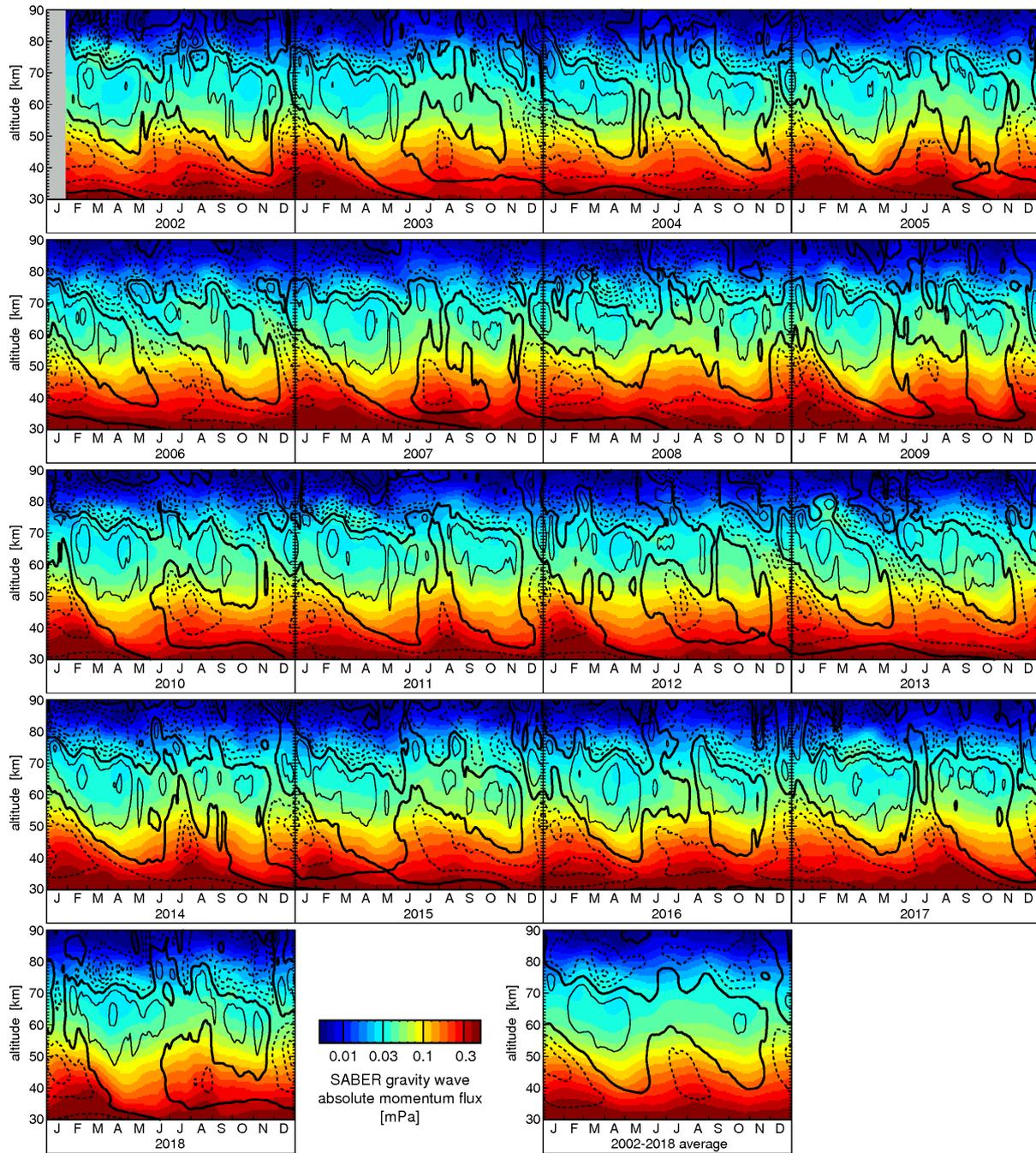


Figure S20. SABER absolute gravity wave momentum flux in mPa on a logarithmic scale for the 2002–2018 time period averaged over the latitude band 10°S–10°N, and the average over these years (lower right panel). Contour lines are zonal-average zonal winds of the merged data set based on ERA-Interim, SABER, and TIDI (E/S/T-winds), as described in the main paper.

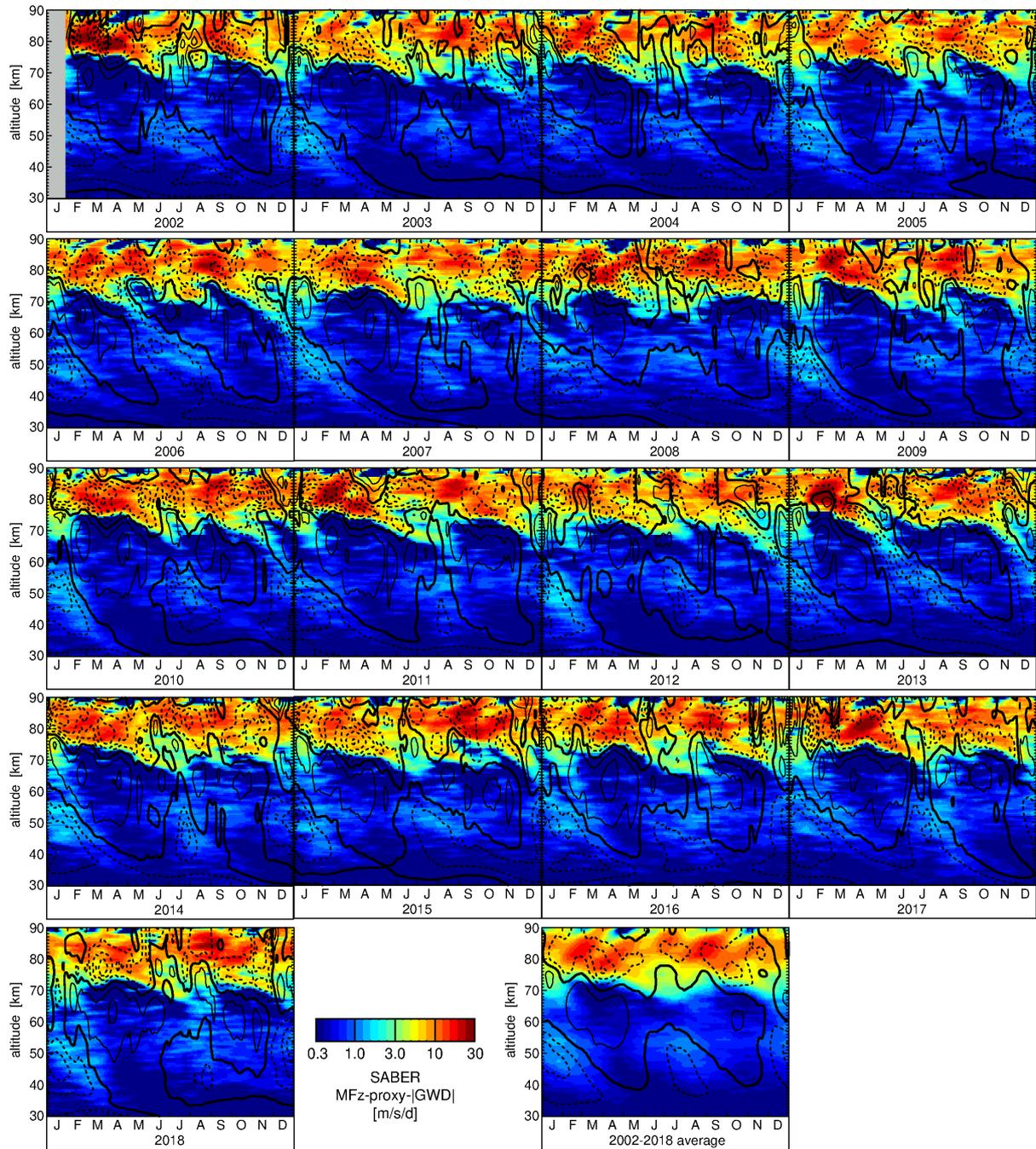


Figure S21. SABER proxy for absolute gravity wave drag (MFz-proxy-|GWD|) obtained from vertical gradients of absolute momentum flux normalized by the negative background density. Values are in $\text{m s}^{-1}\text{day}^{-1}$ on a logarithmic scale. Values are shown for the 2002–2018 time period averaged over the latitude band 10°S – 10°N , as well as the average over these years (lower right panel). Contour lines are zonal-average zonal winds of the merged data set based on ERA-Interim, SABER, and TIDI (E/S/T-winds), as described in the main paper.

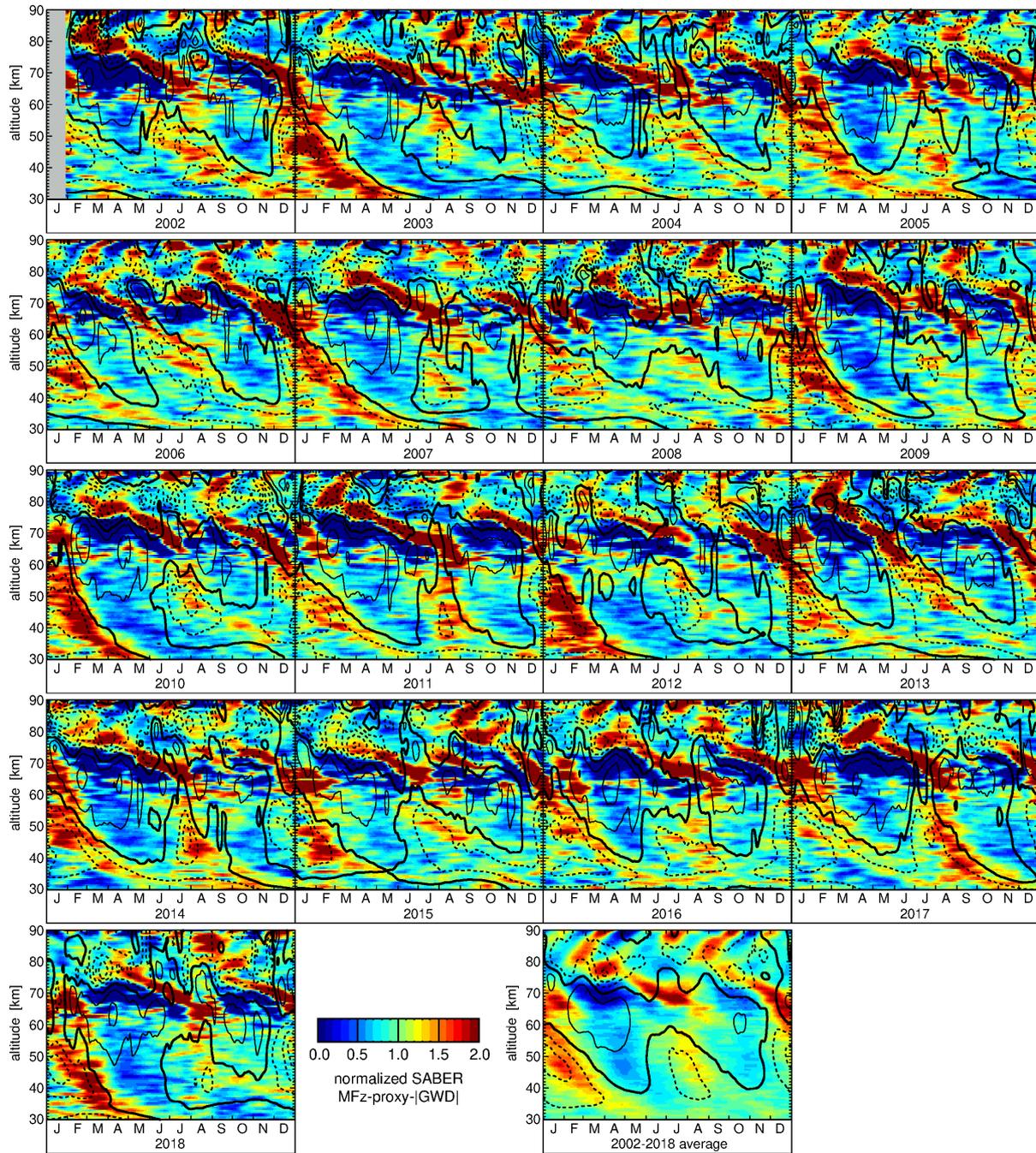


Figure S22. Same as Fig. S21, but values are normalized by the annual average, separately for each year and altitude.

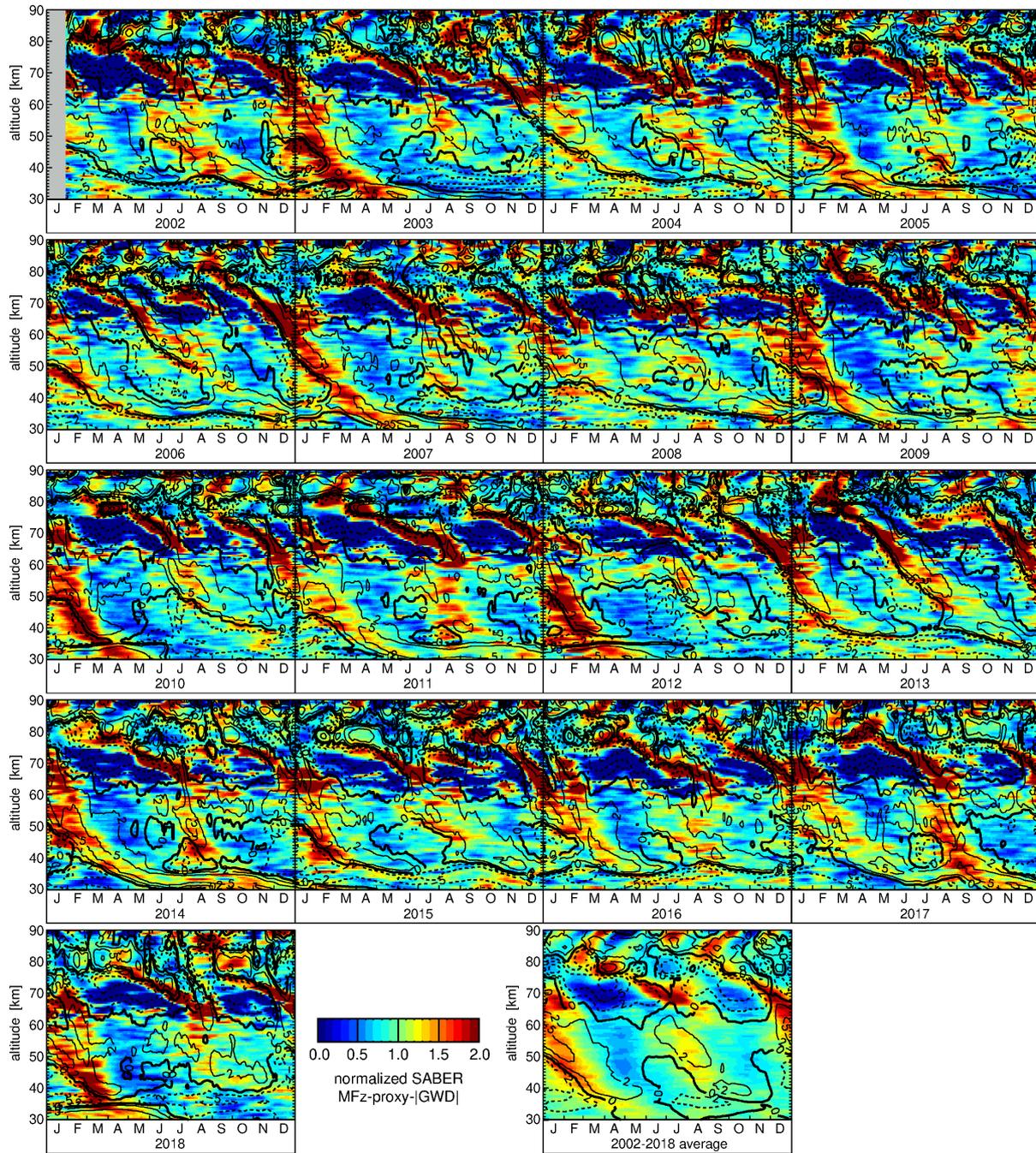


Figure S23. Same as Fig. S22, but contour lines are the vertical gradient of zonal-average zonal winds of the merged data set based on ERA-Interim, SABER, and TIDI (“E/S/T-winds”), as described in the main paper. Contour lines are at 0, ± 2 , ± 5 , and $\pm 10 \text{ m s}^{-1} \text{ km}^{-1}$. Westward (=negative) gradients are indicated by dashed contour lines.

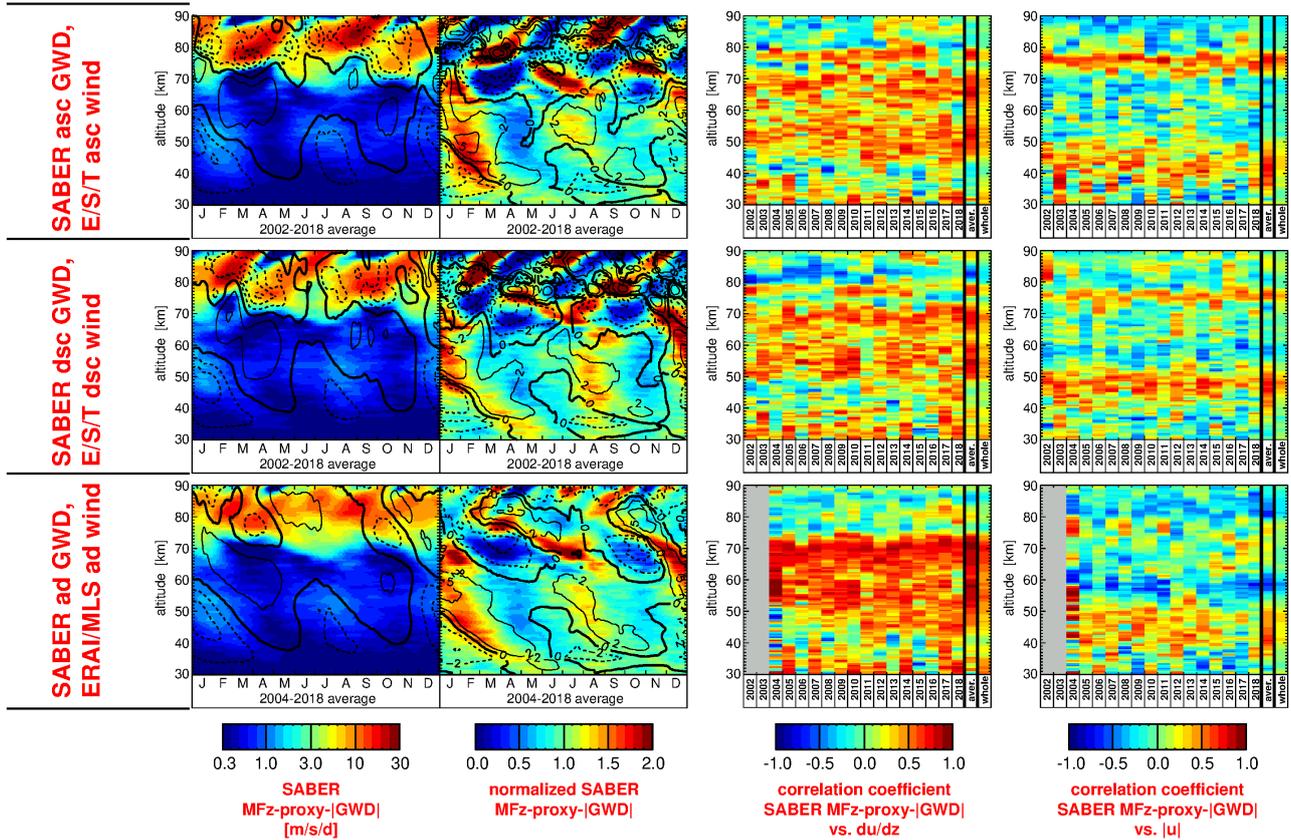


Figure S24. Left column: the SABER MFz-proxy-|GWD| (a proxy for absolute gravity wave drag) averaged over 10°S – 10°N and the years 2002–2018 (2004–2018 for MLS), overplotted with zonal wind contour lines of different zonal wind data sets averaged over the same latitudes and period. Second column: Same as left column, but for normalized SABER MFz-proxy-|GWD| overplotted with contour lines of zonal wind vertical gradients. Third column: Temporal correlations between SABER MFz-proxy-|GWD| and zonal wind vertical gradients, separately for each year, for the multi-year averages, and for the whole time series. Right column: Same as third column, but for the correlation between SABER MFz-proxy-|GWD| and zonal wind absolute values. The different rows are (from top to bottom) for (1) the merged ERA-Interim, SABER and TIDI data set as described in Sect. 4.2.3 of the main paper, but here only for ascending orbit legs, (2) same as (1), but only for descending orbit legs, and (3) the merged dataset of ERA-Interim and MLS quasi-geostrophic winds as described in Sect. 4.2.2 of the main paper (i.e., averaged over ascending and descending orbit legs). For zonal winds, contour line increment is 20 m s^{-1} . The zero wind line is highlighted in bold solid, and westward (eastward) winds are indicated by dashed (solid) contour lines.