



1 **Roles of the Inner Eyewall Structure in the Secondary Eyewall Formation of Simulated**
2 **Tropical Cyclones**

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21 **Abstract.** It has been suggested that the inner eyewall structure may play an important role in the
22 secondary eyewall formation (SEF) of tropical cyclones (TCs). This study is to further examine
23 the role of the inner eyewall structure by comparing two numerical experiments, which were
24 conducted with the same large-scale environment and initial and boundary conditions but different
25 grid sizes. The SEF was simulated in the experiment with the finer grid spacing, but not in the
26 other.

27 Comparing the eyewall structure in the simulated TCs with and without the SEF indicates
28 that the eyewall structure can play an important role in the SEF. For the simulated TC with the
29 SEF, the eyewall is more upright with stronger updrafts, accompanied by a wide eyewall anvil at
30 a higher altitude. Compared to the simulated TC without the SEF, diagnostic analysis reveals that
31 the cooling outside the inner eyewall is induced by the sublimation, melting and evaporation of
32 hydrometeors falling from the eyewall anvil. The cooling also induces upper-level dry, cool inflow
33 below the anvil, prompting the subsidence and moat formation between the inner eyewall and the
34 spiral rainband. In the simulated TC without the SEF, the cooling induced by the falling
35 hydrometeors is significantly reduced and offset by the diabatic warming. There is no upper-level
36 dry inflow below the anvil and no moat formation between the inner eyewall and the spiral
37 rainband. This study suggests that a realistic simulation of the intense eyewall convection is
38 important to the prediction of the SEF in the numerical forecasting model.



39 1 Introduction

40 Many intense tropical cyclones (TCs) usually undergo the secondary eyewall formation (SEF)
41 (Fortner, 1958; Willoughby, 1982). Observational study shows that about 80% of intense TCs
42 (maximum surface wind $> 62 \text{ m s}^{-1}$) in the western North Pacific, 70% in the Atlantic, and 50% in
43 the eastern Pacific possessed concentric eyewalls at least once (Hawkins and Helveston, 2008).
44 The eyewall replacement circle is one of the most important issues remaining in understanding
45 and predicting the change of TC intensity due to the resulting dramatic intensity fluctuations
46 (Samsury and Zipser, 1995; Terwey and Montgomery, 2008; Bell et al., 2012). Although much
47 effort has been made to understand the mechanisms of the SEF, a consensus has not been reached
48 so far.

49 Previous studies have pointed out the dynamic importance of the vortex circulation in the
50 SEF (Montgomery and Kallenbach, 1997; Chen and Yau, 2001; Qiu et al., 2010). Given a negative
51 radial gradient of vorticity outside the primary eyewall, vortex Rossby waves (VRWs) propagate
52 outward and stop at a stagnation radius, where the mean flow strengthens through the interaction
53 of eddies with the azimuthal-mean vortex (Montgomery and Kallenbach, 1997; Qiu et al., 2010;
54 Chen and Yau, 2001; Hogsett and Zhang, 2009; Dai et al., 2021). With the strengthening mean
55 flow, the outer convection occurs and evolves into an outer eyewall through the wind-induced
56 surface heat exchange (Emanuel, 1986). Terwey and Montgomery (2008) proposed that cumulus
57 convection forms and maintains in a far-field region with a weak negative radial gradient of
58 vorticity (the β -skirt) and moderate stretching time. A secondary eyewall forms through the
59 upscale cascade and axisymmetrization of eddy vorticities in the sustained convection. It has been
60 found that the secondary eyewall can be simulated in a barotropic model when the preexisting
61 outer convection is stretched into a closed vorticity band by the rotation of the inner vortex (Kuo



62 et al., 2004, 2008). Based on a nonlinear boundary layer model, Kepert (2013) proposed that the
63 secondary eyewall can form through a positive feedback among the local enhancement of the radial
64 vorticity gradient, the frictional updraft. Those studies highlight the positive feedback of the eddy
65 kinetic energy to the storm-scale flow through the dynamics of the VRW, vorticity interaction, and
66 the Ekman pumping. However, the convective activity related to the generation of the eddy kinetic
67 energy is not fully addressed.

68 Some studies focused on spiral rainbands because the SEF generally starts from convective
69 rainbands (Houze, 2007; Zhao et al., 2008, 2016; Kossin and Sitkowski, 2009). When the rainband
70 outside the eyewall is enhanced by adding a large diabatic heating rate to the rainband in a
71 numerical simulation, the TC can experience the SEF (Wang, 2009). Zhu and Zhu (2014)
72 emphasized that a critical strength of the rainbands is needed for the formation of a secondary wind
73 maximum through diabatic heating. Idealized numerical simulations indicated that the sustained
74 convection in the SEF region was enhanced by the interaction between the unbalanced boundary
75 layer process and the asymmetric inflows induced by the outside rainbands that propagated inward
76 (Qiu and Tan, 2013; Wang and Tan, 2020). Recent studies revealed that, for SEF cases, the
77 descending inflow in the downwind portion of the spiral rainbands transfers high angular
78 momentum inward, leading to the outward expansion of the wind field (Didlake et al., 2018;
79 Wunsch and Didlake, 2018; Wang et al., 2019; Yu et al., 2020). A radial expansion of storm wind
80 precedes the SEF through the boundary layer processes and coupled convective dynamics (Rozoff
81 et al., 2012; Huang et al., 2012; Abarca and Montgomery, 2013; Sun et al., 2013). However, not
82 all the spiral rainbands outside of the TC eyewall can evolve into a closed outer eyewall.

83 Many numerical studies have also shown the importance of various microphysical processes
84 in the SEF since the inner-core structure and intensity of TCs are sensitive to the microphysical



85 processes (Wang, 2002; Zhu and Zhang, 2006). Zhu and Zhang (2006) proposed that varying cloud
86 microphysics processes affect the timing of the spinup of the secondary eyewall since the
87 differences in the inner eyewall convection and the rainband structure of the simulated TCs.
88 Numerical simulations showed that changing the terminal velocity of snow led to changes in the
89 magnitude and distribution of the diabatic heating of inner-core convection at outer radii, which is
90 important for the SEF (Zhu and Zhu, 2015). Influenced by the evaporative cooling from the fallout
91 of hydrometeors, the penetrative downdrafts can promote the local convection outside the primary
92 eyewall, where the SEF occurs (Tyner et al., 2018). Moreover, microphysical processes are also
93 important to the occurrence of the moat, by which the spiral rainband is separated from the inner
94 eyewall with a chance to become a secondary eyewall. Willoughby et al. (1982) considered the
95 moat generated with subsidence as the evaporative cooling of precipitation falling from the
96 cumulus anvil. In our previous study based on a numerical modeling simulation (Qin et al., 2021),
97 we demonstrated that the moat subsidence is mainly caused by the negative buoyancy resulting
98 from the cooling from sublimation, melting and evaporation processes of hydrometeors from the
99 cumulus eyewall and the related well-developed anvil, and the moat subsidence is further enhanced
100 by the compensating upper-level dry-air inflows.

101 The objective of this study is to further examine the roles of the inner eyewall structure and
102 the associated cooling in the formation of the moat between the inner eyewall and the spiral
103 rainband that later becomes the outer eyewall. Our examination was based on two numerical
104 experiments with the same large-scale environment and initial and boundary conditions, but
105 different grid sizes since the strength and distribution of the inner-core convection of TCs are
106 sensitive to the horizontal resolutions (Zhang et al., 2015; Qin and Zhang, 2018; Wu et al., 2018,
107 2019). This paper is organized as follows. Section 2 briefly summarizes the experimental design.



108 Section 3 describes the simulated TCs with different horizontal spacings. In Section 4, different
109 eyewall structures are identified, followed by Section 5, in which how the differences in the
110 eyewall structure affect the SEF is investigated. A summary and concluding remarks are given in
111 the final section.

112 **2 Experimental design**

113 In our previous study, a 72-h simulation (CTL) was conducted using the Weather Research
114 and Forecasting model (WRF, version 3.2.1) with quintuply nested domains (27/9/3/1/0.3 km), in
115 which the simulated TC experienced the SEF (Qin et al., 2021). In order to understand the
116 influence of structural changes of the eyewall on the SEF, a sensitivity experiment (NSEF) was
117 further designed by removing the innermost domain used in CTL. The two experiments were
118 conducted over the open ocean for 72 hours. The sea surface temperature is fixed at 29 °C. The
119 outermost domain is centered at 30 °N, 132.5 °E. The domains with the grid spacing of 3 km and
120 less moved with the TC center. There are 75 vertical levels with the model top at 50 hPa. The
121 National Centers for Environmental Prediction (NCEP) Final Operational Global Analysis data (1°
122 × 1°) is utilized for the initial and lateral boundary conditions. The simulations begin with a TC-
123 like vortex.

124 Model physics options are the same as those used in Chen and Wu (2016) and Qin et al.
125 (2021). The major model physics options include the single-moment 3-class microphysics scheme
126 for the outermost domain, the single-moment 6-class microphysics scheme for the rest of the
127 domains, the Yonsei University planetary boundary layer (PBL) scheme (Noh et al., 2003), the
128 longwave radiation scheme of the Rapid Radiative Transfer Model (RRTM, Mlawer et al., 1997),
129 the shortwave radiation scheme of the Dudhia (Dudhia, 1989). The Kain-Fritsch cumulus
130 parameterization scheme (Kain and Fritsch, 1993) is applied only in the outermost domain.



131 3 Evolution of the simulated TCs

132 There is little difference in the track of the simulated storms largely because the large-scale
133 environmental conditions are the same in the two experiments (figure not shown). Despite the
134 same large-scale environment and initial and boundary conditions, the intensity evolution is
135 different in the two simulations (Fig. 1). In NSEF, after an 18-h spin-up, the near-surface maximum
136 wind speed (V_{MAX}) experiences a persistent increase and reaches its peak intensity of 62.5 m s^{-1} at
137 57 h, then the V_{MAX} decreases. In CTL, the storm experiences a weakening stage from 32 h to 48
138 h and a reintensification from 48 h to 63 h due to the SEF. There are pronounced fluctuations in
139 the V_{MAX} in CTL, suggesting the influence of the small-scale structures simulated with the finer
140 grid size in the innermost domain.

141 The different eyewall structures between the two experiments can be seen from the evolution
142 of the azimuthal-mean tangential wind. Figure 2 compares the time-radius cross-sections of the
143 azimuthal-mean tangential wind and the vertical motion at 0.5 km between the two simulations. In
144 NSEF, a single maximum wind core maintains and the tangential wind expands radially outward
145 during the intensification. It is indicated that no SEF occurs in this experiment. In CTL, the
146 simulated TC experiences the SEF, as discussed in Qin et al. (2021). The formation of the
147 secondary eyewall begins around 32 h with a secondary maximum tangential wind of over 35 m
148 s^{-1} at the radius of 85 km. After the SEF, the outer eyewall contracts and intensifies with its strength
149 catching up with the primary eyewall at $t = 40 \text{ h}$ (Fig. 2b). A few hours later, the primary eyewall
150 weakens and is replaced by the new eyewall around 46 h.

151 The different inner-core structures can also be seen in the evolution of the azimuthal-mean
152 vertical motion (Figs. 2c and 2d). In NSEF, the strong upward motion in the single eyewall is
153 maintained during the 72-h simulation. The vertical motion in the eyewall with a speed larger than



154 0.2 m s^{-1} extends about 20-30 km at 0.5-km height. In CTL, prior to the SEF, the primary eyewall
155 contracts inward and the width of the eyewall with the upward motion over 0.2 m s^{-1} is reduced.
156 Around 34 h, a secondary maximum upward motion occurs at a radius of around 60 km. After the
157 SEF, the weakening and dissipation of the primary eyewall can also be seen from the upward
158 motion shown in Fig. 2d. It is seen that the double eyewall structure exists for 14 h.

159 Moreover, the simulated inner rainbands evolve differently in the two experiments. Figure 3
160 shows the horizontal distributions of the 5-km radar reflectivity at the selected times. In NSEF, the
161 broad and active rainband is evident in the downshear quadrant of the storm, while the rainband in
162 the upshear quadrant is weak with sporadic convection located around the radii of 100-150 km at
163 28 h. Afterward, the rainbands contract and merge with the inner eyewall, leading to an expansion
164 of the wind field and a broad single eyewall without the formation of a moat. In CTL, the rainbands
165 show a pattern similar to that in NSEF by 28 h (Fig. 3d), but the rainbands are elongated
166 azimuthally and became a closed ring outside the primary eyewall by 32 h. A clear moat region
167 forms at 50-60 km radii between the primary and the outer eyewalls. After a weakening stage, the
168 primary eyewall almost dissipates by 44 h (Fig. 3f), followed by an inward contraction of the outer
169 eyewall.

170 **4 Differences in the vertical structures of the eyewall**

171 One of the major differences in the eyewall between NSEF and CTL is the magnitude and the
172 vertical distribution of the vertical motion, which can be examined with the azimuthally averaged
173 vertical motion within the radius of 100 km (Fig. 4) and the contoured frequency by altitude
174 diagram (CFAD) of the vertical motion (Fig. 5a). The CFAD illustrates the frequency distribution
175 of the vertical motion of the indicated values at each altitude in the region of the 10-km radially
176 inside and outside of the radius of the maximum tangential wind (RMW) for two simulations. The



177 azimuthal-mean upward motion in the eyewall is stronger in CTL than that in NSEF (Fig. 4).
178 Specifically, the upward motion in the eyewall in NSEF is maximized at 10- and 12-km height
179 with peaks of 11 and 13 m s⁻¹ for the 0.1 % and 0.05% percentiles (Fig. 5a), respectively. The weak
180 upward motion between 45- to 75-km radii is associated with the broad rainbands (Figs. 4a and
181 4b). In contrast, the maximum upward motion in CTL is 12 and 14 m s⁻¹ for the 0.1 % and 0.05%
182 percentiles (Fig. 5a). The stronger upward motion in CTL indicates that a higher resolution in the
183 model simulation can resolve more intense eyewall updrafts (Yau et al., 2004). Moreover, the
184 eyewall with strong updrafts in CTL is more upright in the vertical direction.

185 Another important difference in the eyewall between NSEF and CTL is the feature of the
186 upper-level outflow layer. Figure 5b compares the upper-level outflow in the two simulations by
187 showing the 0.1% and 0.05% contoured frequency of the radial wind in the region of a radial
188 distance of 60 km starting from the radius of 10-km outside the eyewall. In NSEF, the upper-level
189 outflow peaks around the 11-km height with maxima of 28 and 26 m s⁻¹ for the 0.05% and 0.1%
190 percentages, respectively. The outflow layer is deep with a magnitude of over 15 m s⁻¹ extending
191 downward to 8 km. In CTL, the maximum outflow with values of over 29 m s⁻¹ is located around
192 the 14-km height. The outflow layer at the higher altitude in CTL is associated with the strong
193 upward motion in the eyewall that can lift the hydrometeors much higher.

194 The different eyewall structures can also be seen in the horizontal distribution of the cloud-
195 top temperature (Fig. 6). In NSEF, the eyewall is wider and possesses relatively weaker convection
196 as indicated by the cloud-top temperature of above -75⁰C (Fig. 6a). In CTL, the cloud associated
197 with the eyewall is deeper since the coldest cloud-top temperature is below -75 ⁰C (Fig. 6b). The
198 coldest cloud-top temperature is located at the downshear- and upshear-right region due to the
199 influence of the southeastward VWS. The strong eyewall convection is accompanied by the strong



200 and high-altitude outflow compared to that in NSEF.

201 **5 Influence of the eyewall structure on the moat formation**

202 **5.1 Buoyancy effects**

203 As discussed above, the rainbands can encircle into a closed outer eyewall instead of merging
204 with the inner eyewall in CTL due to the formation of the moat. First, we investigate the
205 relationship between the distribution of buoyancy and the occurrence of the moat subsidence.
206 Many studies indicated that buoyancy, which is determined by temperature perturbation, affects
207 the vertical motion tendency (e.g., Zhang et al., 2000; Braun, 2002; Miller et al., 2015). It is
208 intended to examine how the buoyancy changes when the SEF fails in NSEF with a different
209 eyewall structure. Following the method used by Braun (2002), the perturbation associated with
210 the buoyancy calculation is defined as $A'(\lambda, r, z) = A(\lambda, r, z) - A_0(z) - A^{0,1}(\lambda, r, z)$, where A
211 represents any variable in a cylindrical coordinate (λ, r, z) , λ , r , z are the azimuthal angle, the
212 radius from the TC center, and the vertical height axis, respectively, A_0 is averaged over the whole
213 area of the 1-km domain, $A^{0,1}$ are the wavenumber-0 and -1 components of the perturbation field
214 from A_0 . $A_0 + A^{0,1}$ denotes the reference state for the buoyancy analysis. Following Houze (1993)
215 and Braun (2002), buoyancy (B) is defined as:

$$216 \quad B = g \left[\frac{\theta'_v}{\theta_{v0} + \theta_v^{0,1}} + (\kappa - 1) \frac{p'}{p_0 + p^{0,1}} - q' \right], \quad (1)$$

217 where g is the gravitational acceleration, θ_v is the virtual potential temperature, $\kappa = 0.286$, p is
218 the pressure, and q is the hydrometeor mixing ratio, including the mixing ratio of the cloud water
219 (q_c), rain water (q_r), graupel (q_g), snow (q_s), and ice (q_i). Terms on the right-hand side of Eq. (1)
220 are the thermal buoyancy, the dynamic buoyancy, and the hydrometeor loading, respectively.
221 Considering that the rainband distributes asymmetrically prior to the SEF, it is appropriate to use
222 quarter-mean variables, i.e. the upshear-right quadrant, to analyze the moat and outer eyewall



223 formation in our following discussions.

224 For the convenience of the following buoyancy analysis, Fig. 7 shows the radius-height cross
225 sections of the perturbation virtual potential temperature (θ'_v). Consistent with the broad eyewall
226 convection in NSEF, positive θ'_v appears under the eyewall anvil, which may force the air parcel
227 upward since the local θ_v exceeds the ambient environmental value. On the contrary, the θ'_v is
228 negative outside and underneath the inner eyewall in CTL (Fig. 7e), which will suppress the
229 upward motion there.

230 Given the different distribution of θ'_v , we next examine the related thermal buoyancy, as well
231 as the dynamic buoyancy and the hydrometeor loading (Fig. 8). In NSEF, we note that the positive
232 buoyancy coinciding with the positive θ'_v appears outside the inner eyewall since the buoyancy is
233 largely determined by the thermal buoyancy and the dynamical buoyancy and the water loading
234 effects are relatively small (Figs. 8a-8d). The positive buoyancy forces upward motion, leading to
235 the widespread upward motion in NSEF (Fig. 8b). There is no moat formation without the
236 considerable subsidence, and the spiral rainband merges with the primary eyewall and no SEF
237 occurs. In CTL, the emergence of the moat subsidence is largely caused by the negative buoyancy,
238 especially the negative thermal buoyancy in response to the negative θ'_v outside the inner eyewall.
239 Moreover, the dynamic buoyancy and the water loading effect both contribute to the enhancement
240 of the moat subsidence. Note that the negative buoyancy also occurs in the inner eyewall below 6-
241 km height (Fig. 8e), which is consistent with the weakening of the primary eyewall when the outer
242 eyewall intensifies. These results indicate that the negative buoyancy beneath the high-altitude
243 eyewall anvil from the inner eyewall is crucial for the subsidence generation and the moat
244 emergence. The moat plays an important role in the SEF by separating the preexisting spiral
245 rainbands from the inner eyewall.



246 To further demonstrate the tendency of the vertical motion, the perturbation vertical pressure
247 gradient force and the net force among the buoyancy and the perturbation vertical pressure gradient
248 force are shown in Fig. 9. Even though the perturbation vertical pressure gradient force exhibits
249 oppositely to the buoyancy in the two simulated TCs, the net force contributes to the upward
250 acceleration of updrafts in NSEF (Fig. 9c) but the downward acceleration of the subsidence outside
251 the primary eyewall in CTL (Fig. 9f). As a result, the subsidence outside the inner eyewall in CTL
252 contributes to the formation of the moat, followed by the SEF, while no SEF occurs in NSEF
253 without the emergence of the moat.

254 **5.2 Diabatic heating**

255 Since the negative buoyancy is associated with the negative temperature disturbance, the
256 diabatic heating is examined. Figure 10 shows the radius-height distributions of the diabatic
257 heating and diabatic cooling induced by the sublimation, melting, and evaporation of hydrometeors.
258 In NSEF, the diabatic warming dominates the region within the radius of 100 km, except for the
259 eye and a local area around 40-km radius from 1- to 6-km heights (Fig. 10a). This broad warming
260 is caused by the wider eyewall convection as shown in Fig. 3 and Fig 4a. Although the diabatic
261 cooling related to the sublimation, melting and evaporation processes always exist in the storm
262 (Figs. 10b-10d), the low- to middle-level convection outside the inner eyewall produces much
263 diabatic warming than cooling, leading to net diabatic warming appearing outside the primary
264 eyewall in NSEF. In contrast, instead of diabatic warming, the net diabatic cooling appears with
265 the absence of convection outside of the inner eyewall in CTL (Fig. 10e). This cooling is
266 maximized at 6- to 10-km height, which is largely induced by the sublimation of hydrometeors
267 beneath the eyewall anvil (Figs. 10f-10h), while the cooling located below 6-km height is caused
268 by the melting and evaporative processes.



269 The evolution of subsidence in the moat area is largely controlled by the distribution of the
270 diabatic cooling. The azimuthal extension of the diabatic cooling and the related moat subsidence
271 and their differences in CTL and NSEF at upper levels are further examined in Fig. 11. Before 24
272 h, both the diabatic cooling and the related subsidence in NSEF and CTL are characterized by a
273 highly asymmetric structure with intense subsidence/cooling located in the upshear-left quadrant
274 (see Figs. 11a, 11b, and Fig. 3). After 24 h, the evolution of the diabatic cooling and subsidence
275 differs in the two simulations. The asymmetric structure of the intense diabatic cooling and
276 subsidence maintains in NSEF, while the diabatic cooling and subsidence extend cyclonically from
277 the upshear-left quadrant to the downshear-right quadrant, ending with a quasi-symmetric structure
278 from 24 h to 32 h (Fig. 11b), which is also confirmed by showing the differences in the diabatic
279 cooling and moat subsidence between NSEF and CTL in Fig. 11c.

280 5.3 Subsidence in response to the diabatic cooling

281 The Sawyer-Eliassen equation (SEE) is used to better understand how the diabatic heating
282 with the different eyewall structures affects the evolution of the moat and outer eyewall without
283 considering the momentum forcing. The SEE is a useful analytical tool for diagnosing the response
284 of the transverse circulation to diabatic heating (Smith et al., 2005; Bui et al., 2009; Zhu and Zhu,
285 2014; Qin et al., 2021). According to Qin et al. (2021), the SEE used in this study is

$$286 \frac{\partial}{\partial r} \left[\frac{\chi}{\rho r} \frac{\partial b}{\partial z} \frac{\partial \psi}{\partial r} - \frac{\chi}{\rho r} \frac{\partial b}{\partial r} \frac{\partial \psi}{\partial z} \right] + \frac{\partial}{\partial z} \left[\left(\chi \xi \zeta_a - \frac{C \chi}{g} \frac{\partial b}{\partial r} \right) \frac{1}{\rho r} \frac{\partial \psi}{\partial z} - \frac{\chi}{\rho r} \frac{\partial b}{\partial r} \frac{\partial \psi}{\partial r} \right] = g \frac{\partial \chi^2 Q}{\partial r} + \frac{\partial C \chi^2 Q}{\partial z}, \quad (2)$$

287 where $\chi = 1/\theta$ and θ is the potential temperature, ρ is the density, b is the buoyancy term, ψ is a
288 stream function, $\xi = 2v/r + f$ is the local Coriolis parameter and f is the Coriolis parameter, ζ_a
289 is the vertical component of the absolute vorticity, $C = v^2/r + fv$ is the sum of the centrifugal
290 force and Coriolis force where v is the tangential wind, g is the gravitational acceleration, r and z
291 are the radial and vertical coordinate, and Q is the diabatic heating rate (heating forcing). Note that,



292 in the absence of the momentum forcing, the diagnosed radial inflow within the boundary layer is
293 largely underestimated, while the diagnosed secondary circulation above the boundary is
294 comparable to the simulated results, which is also found in other studies (Bui et al., 2009; Zhu and
295 Zhu, 2014; Qin et al., 2021).

296 Figure 12 shows the radius-height cross sections of the SEE-diagnosed vertical and radial
297 wind forced by the diabatic heating, diabatic cooling, and cooling induced by the sublimation,
298 melting and evaporation of hydrometeors, respectively. Significantly, in NSEF, the diabatic heating
299 released by the wider eyewall convection induces the upward motion and deep-layer outflows
300 outside the inner eyewall, and a compensated downdraft in the eye (Fig. 12a). In CTL, intense
301 diabatic cooling forces subsidence of over -0.3 m s^{-1} outside the inner eyewall, which contributes
302 to the formation of the moat. Meanwhile, the diabatic cooling also induces the upper-level inflow
303 below the strong outflow layer (Fig. 12e). These results suggest that the formation of the moat is
304 sensitive to the diabatic heating, especially the diabatic cooling beneath the eyewall anvil.

305 Although the diabatic cooling caused by phase changes usually occurs in TCs, the magnitude
306 of the diabatic cooling, especially the cooling due to the sublimation of ice particles, matters much
307 in the formation of the moat (Figs. 12c and 12g). The cooling due to the sublimation process is
308 much less outside the primary eyewall in NSEF compared to that in CTL (cf. Figs. 12c and 12g).
309 In NSEF, the diabatic warming released by the low- to middle-level convection outside the primary
310 eyewall exceeds the cooling, resulting in net diabatic warming (Fig. 12a). Thus, a wider eyewall
311 with warming-forced upward motion prevails due to the positive feedback among the diabatic
312 heating and the convection (Fig. 12a). In addition, the warming-forced upward motion is
313 accompanied by the deep-layer outflow (Fig. 13a), under which the low-level inflow appears
314 below the 8-km height (Fig. 13a), which brings moist air enhancing the convection in NSEF. In



315 CTL, with the considerable cooling forced by the sublimation outside of the inner eyewall (Fig.
316 12g), the subsidence is induced outside the primary eyewall. Of importance is that the cooling-
317 forced inflow is located at a higher level, which send dry air inward (Fig. 13b). The penetration of
318 dry air through the upper-level inflow plays an important role in increasing the diabatic cooling
319 that promotes the subsidence. The cooling-induced subsidence contributes significantly to the
320 formation of the moat. Subsequently, the spiral rainband evolves into the separated outer eyewall
321 in CTL with the formation of the moat.

322 The differences in the azimuthal distributions of the subsidence and the related upper-level
323 radial inflow between NSEF and CTL are shown in Fig. 14. In NSEF, a highly asymmetric
324 structure with strong subsidence located in the upshear-left quadrant persists during 18-32 hours
325 (Fig. 14a). Although there is upper-level inflow appearing in the upshear-right region (Fig. 14a),
326 it is largely offset by the strong upper-level outflow, leading to net outflow at upper levels as seen
327 in Fig. 13a. In contrast, the subsidence in CTL extends azimuthally, ending with a quasi-symmetric
328 structure from 18 h to 32 h (Fig. 14b). The azimuthal extension of the subsidence follows the
329 appearance of the upper-level inflow, which advects dry air inward to enhance the cooling
330 processes. Therefore, without the penetration of dry air by the upper-level descending inflow, the
331 diabatic cooling and the cooling-forced subsidence beneath the eyewall anvil are limited, which
332 are unfavorable for the moat formation outside the inner eyewall.

333 **6 Summary**

334 In this study, two numerical experiments are conducted with the same large-scale
335 environment and initial and boundary conditions. The simulated inner eyewall structures are
336 different due to different grid spacings used in the two experiments. The SEF occurs in CTL with
337 a fine resolution of 333 m, while no SEF occurs in the other with a coarse resolution of 1 km.



338 There are two major differences in the eyewall structure by comparing the simulated TCs
339 with and without the SEF. For the simulated TC with the SEF, the eyewall updrafts are stronger
340 and the eyewall is more upright. The eyewall anvil is located at a higher altitude together with the
341 deep eyewall convection. As illustrated in Fig. 15, the upper-level dry-air inflow beneath the high-
342 altitude anvil from the inner eyewall is important to the formation of the moat. Diagnostic analysis
343 indicates that the dry inflow below the eyewall anvil is induced by the diabatic cooling released
344 by the sublimation, melting and evaporation of hydrometeors falling from the eyewall anvil. With
345 the penetration of dry air by the upper-level inflow, subsidence occurs, promoting the formation
346 of the moat between the inner eyewall and the spiral rainband. Afterward, the SEF occurs by
347 showing the double eyewall structure and the moat with subsidence. In the TC without the SEF,
348 the eyewall updrafts are weak and tilt much outward, showing an eyewall anvil at the lower altitude.
349 The cooling induced by the falling hydrometeors beneath the low-altitude eyewall anvil is
350 significantly reduced and offset by the diabatic warming. As a result, no upper-level dry-air inflow
351 occurs below the eyewall anvil, and no moat forms between the inner eyewall and the spiral
352 rainband.

353 Our study highlights the importance of the inner eyewall structure in the moat formation
354 through the cooling-induced upper-level inflow and subsidence beneath the eyewall anvil. While
355 the subsidence induced by the evaporative cooling from the precipitation at the outer radii from
356 the anvil is revealed by Tyner et al. (2018), who emphasized the role of the penetrative downdraft
357 in promoting the local rainband convection and the subsequent outer eyewall formation, the
358 cooling-induced upper-level dry-air inflow and its important role in the moat formation are not
359 mentioned in their study. Recent studies indicated that a mesoscale descending inflow driven by
360 the middle-level melting and evaporative cooling in the downwind portion of the rainband can



361 trigger new convective updrafts that are important to the subsequent SEF (Didlake et al., 2018;
362 Wunsch and Didlake, 2018; Yu et al., 2020). In addition to the mesoscale descending inflow at
363 middle levels, the upper-level dry inflow also contributes to the SEF by forcing the moat formation.
364 In this sense, both the inner-eyewall and the rainband structures are important to the SEF. In
365 addition, our study suggests that a realistic simulation of the eyewall convection is important to
366 the prediction of the SEF in the numerical forecasting model.

367

368 *Data availability.* The simulation data is archived at the High-Performance Computing Center of
369 Nanjing University of Information Science and Technology and is available upon request.

370

371 *Author contributions.* LW designed research; NQ conceptualized the analysis and wrote the
372 manuscript; LW provided scientific suggestions for the manuscript. QL carried out the simulations
373 and modified the model code. All authors were involved in helpful discussions and contributions
374 to the manuscript.

375 *Competing interests.* The authors declare that they have no conflict of interest.

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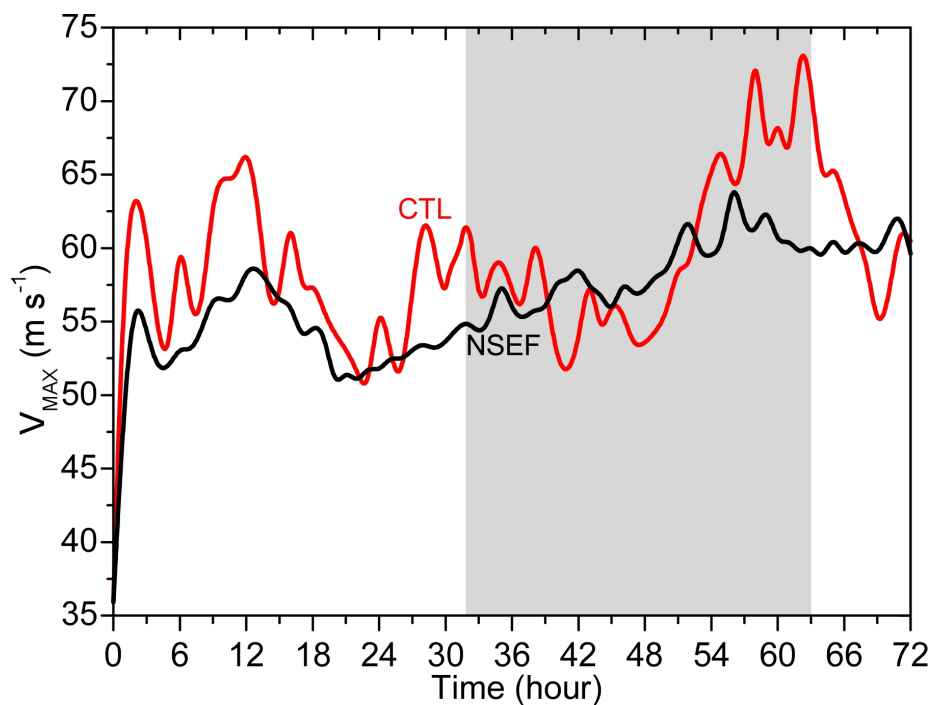
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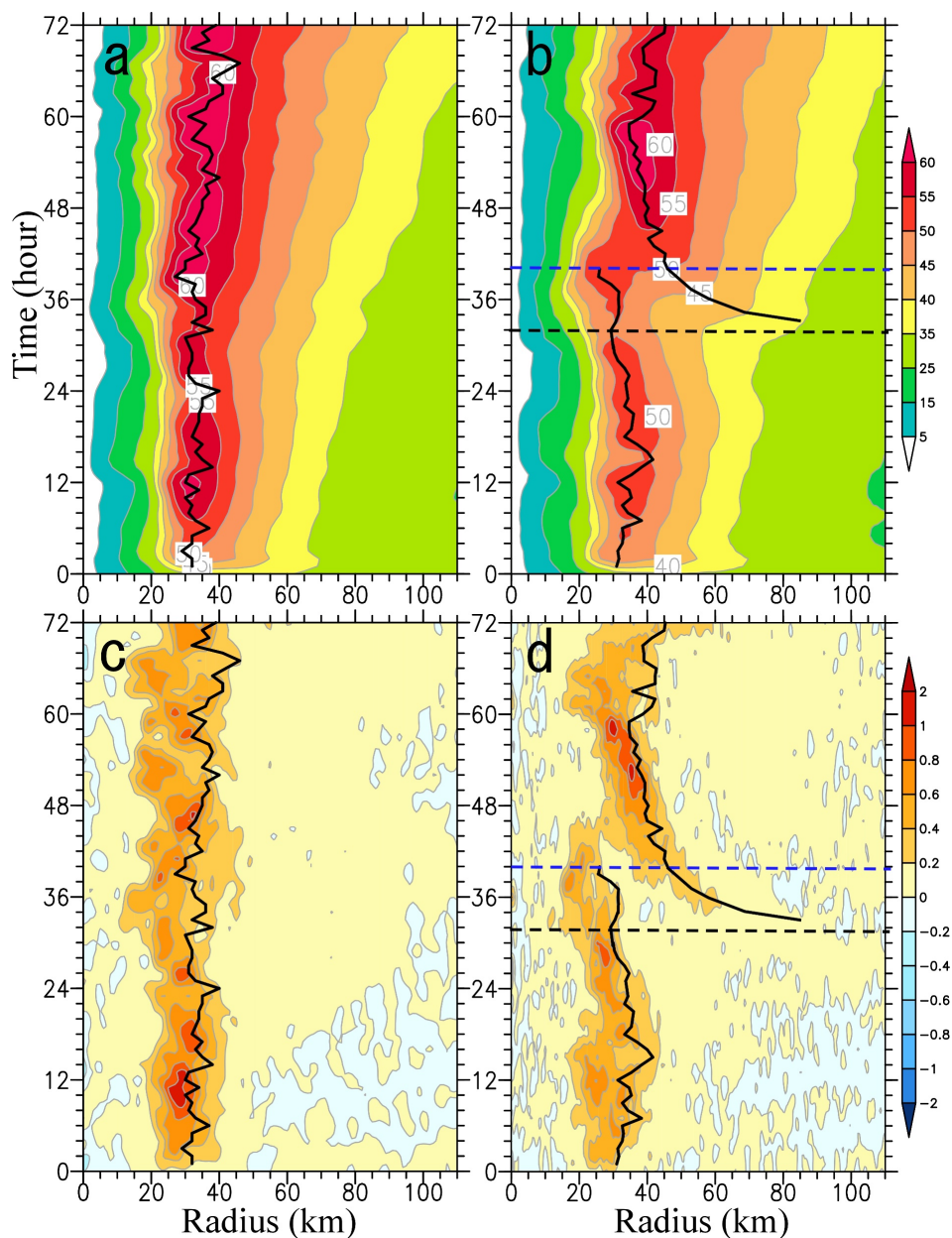
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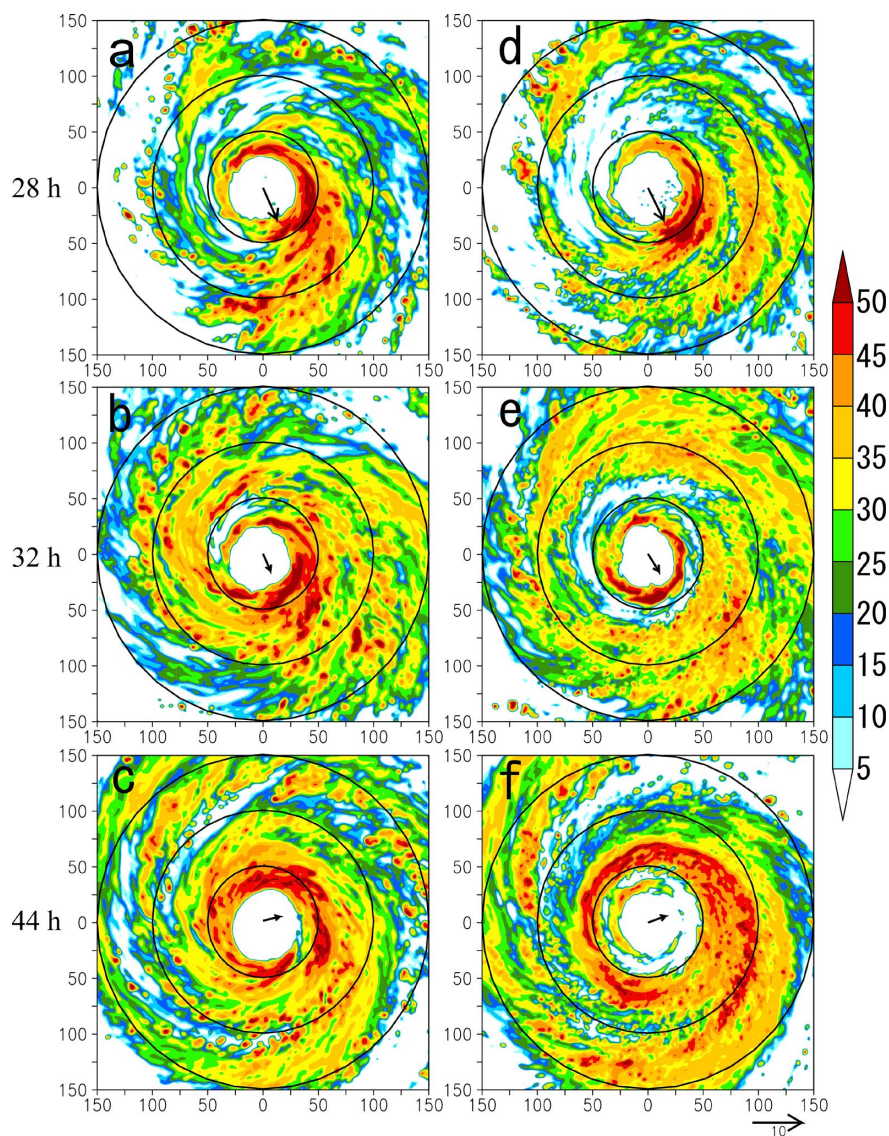
534

535 Figure 1. Time series of intensity changes for the maximum azimuthal-mean near-surface wind
536 (V_{MAX} , $m s^{-1}$) during the 72-h sensitivity (NSEF, black) and control run (CTL, red). The gray
537 shading denotes the period of the eyewall replacement circle.



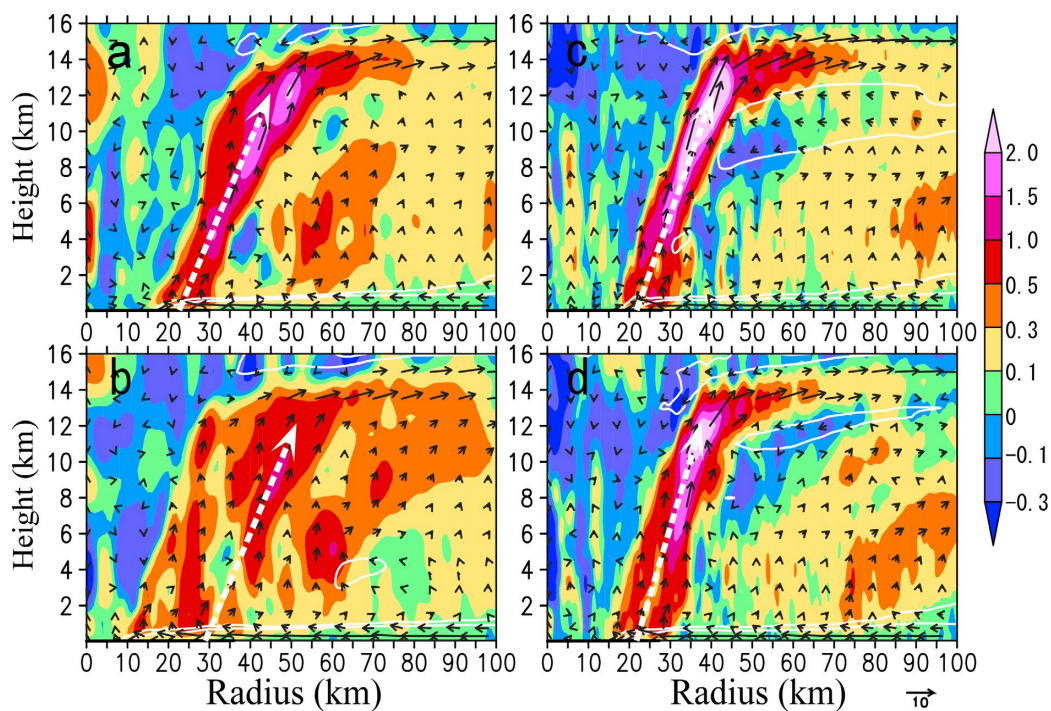
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Figure 2. Time-radius cross-sections of the azimuthal-mean (a, b) tangential wind ($m s^{-1}$) and (c, d) vertical motion ($m s^{-1}$) at 0.5-km height for (a, c) NSEF and (b, d) CTL. The solid lines indicate the radius of the maximum tangential wind (RMW). The black dashed lines indicate the SEF, while the blue dashed lines denote the time when the secondary maximum wind is equal to the primary maximum wind.



544

545 Figure 3. Horizontal distributions of the radar reflectivity at 5-km height at (a, d) 28, (b, e) 32, and
546 (c, f) 44 h for (a-c) NSEF and (d-f) CTL. Vectors are the large-scale vertical wind shear (VWS,
547 Vspeed (200 hPa) - Vspeed (850 hPa)).

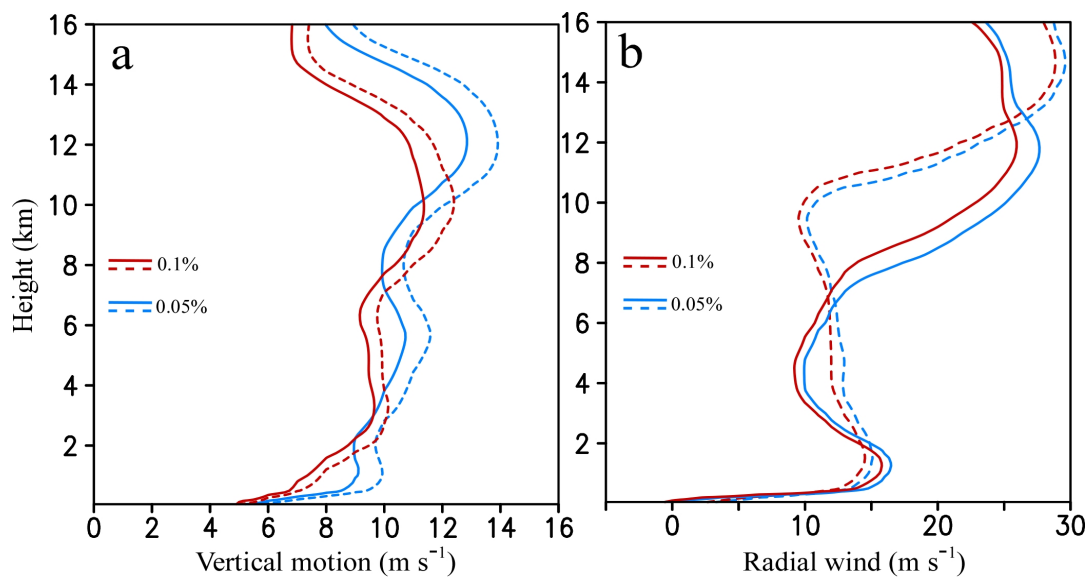


548

549 Figure 4. Radius-height cross-sections of the azimuthal-mean vertical motion (shaded, m s^{-1}), in-
550 plain flow (vector, m s^{-1}) and radial inflows of -1 and -3 m s^{-1} (white contours) at (a, c) 30 h
551 and (b, d) 32 h for (a, b) NSEF and (c, d) CTL. The white dashed arrows denote the eyewall.
552

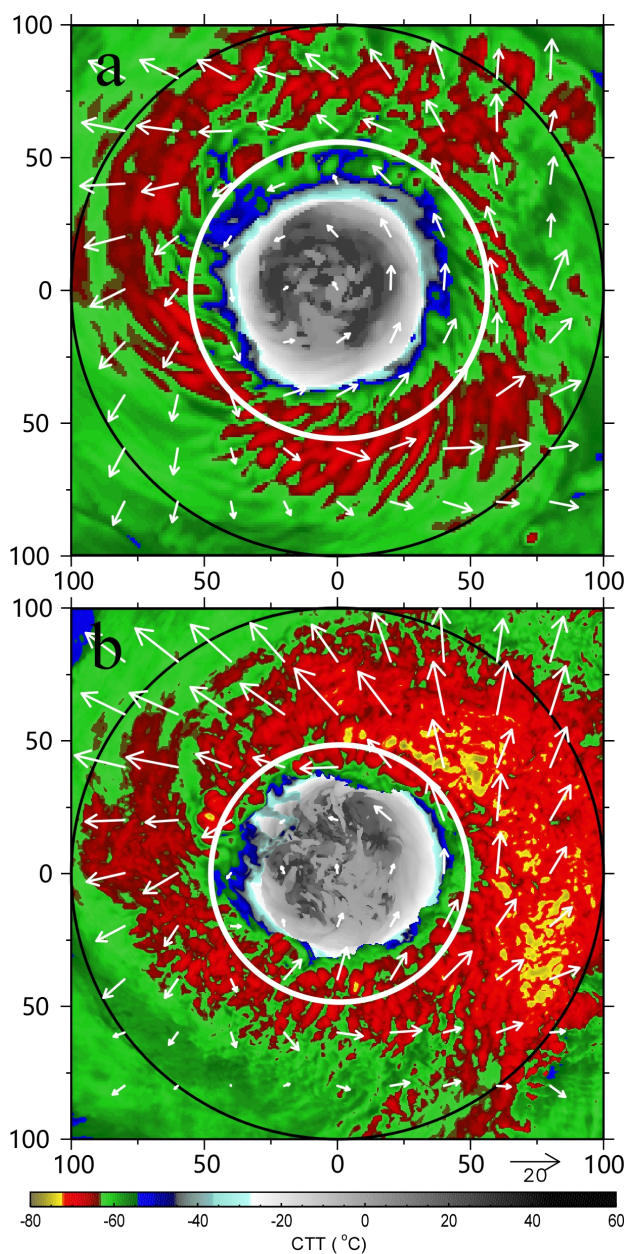


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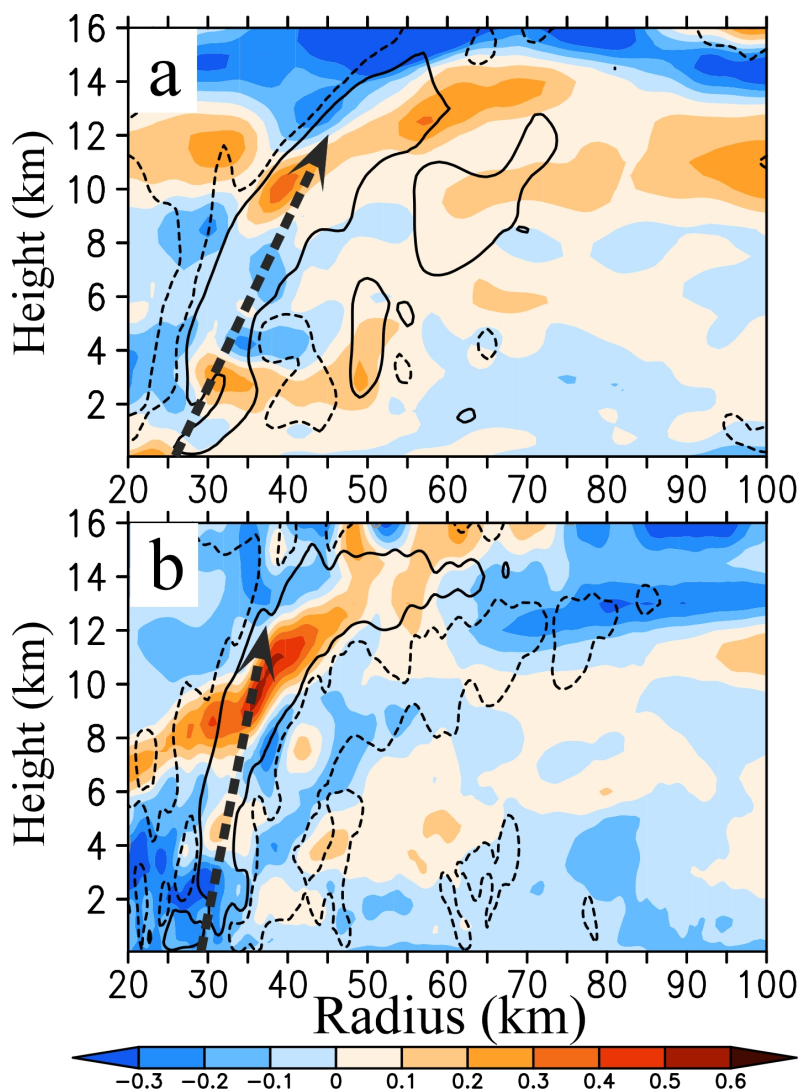
554

555 Figure 5. The contoured frequency by altitude diagram (CFAD, %) of (a) the vertical motion for
556 the 10-km radially inside and outside of the RMW and (b) the radial wind within a radial
557 distance of 60 km starting from the radius of 10-km outside the eyewall (RMW+10 km to
558 RMW+70 km) for CTL (dashed lines) and NSEF (solid lines) at 30 h. The red and blue lines
559 are the 0.1, and 0.05 percentile.



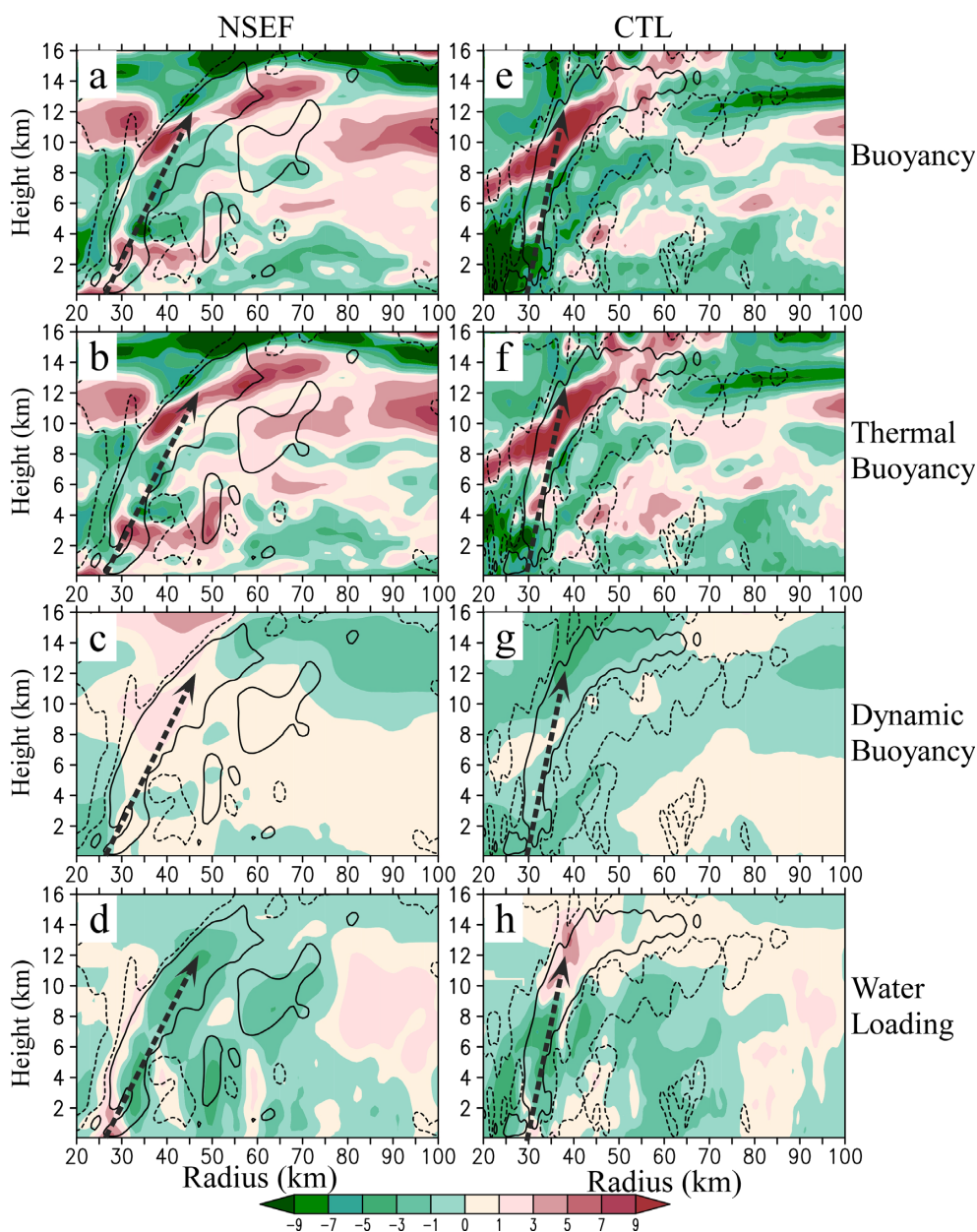
560

561 Figure 6. Horizontal distribution of the cloud-top temperature (CTT, shaded, C°) superimposed
562 with the 15-km horizontal wind field (vector, $m\ s^{-1}$) and RMW (white circle) at 30 h for (a)
563 NSEF and (b) CTL. The black circle indicates the radius of 100 km relative to the TC center.



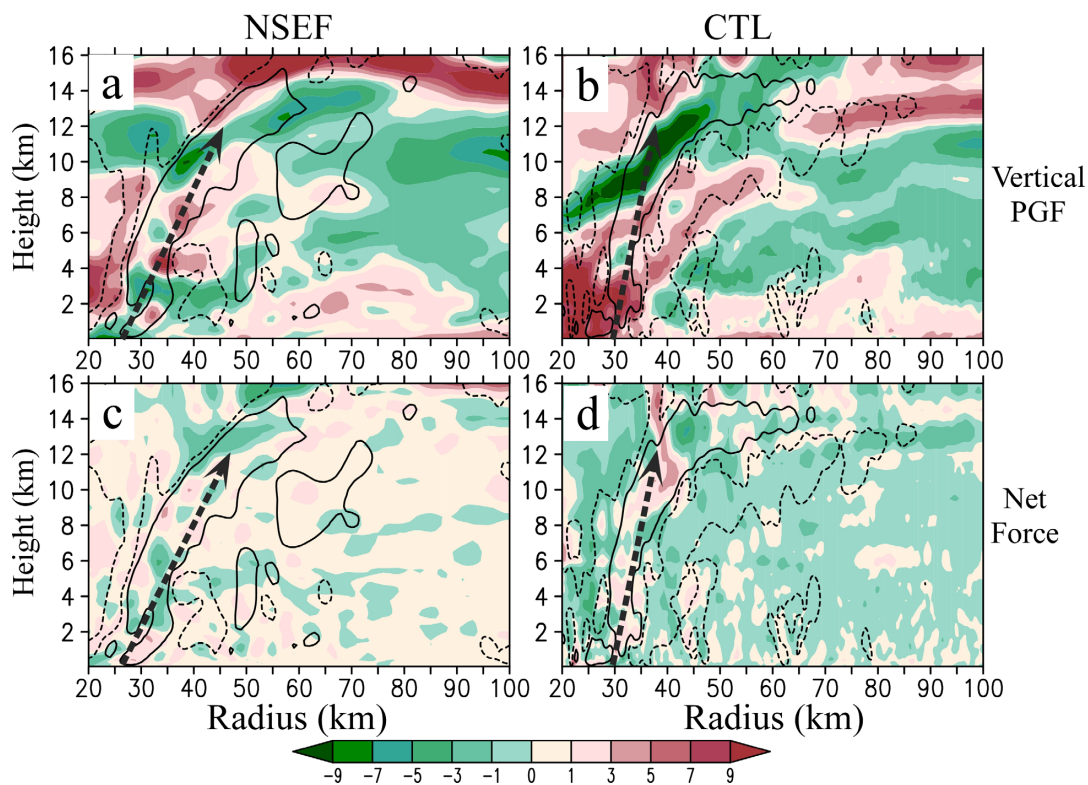
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565 Figure 7. Radius-height cross-sections of the upshear-right quadrant-mean perturbation virtual
566 potential temperature (shaded, K) at 30 h for (a) NSEF and (b) CTL. Contours are the vertical
567 motion (updraft, black solid contours: 0.5 m s^{-1} ; downdrafts, black dashed contours: 0.05 m
568 s^{-1}). The black dashed arrows denote the eyewall.



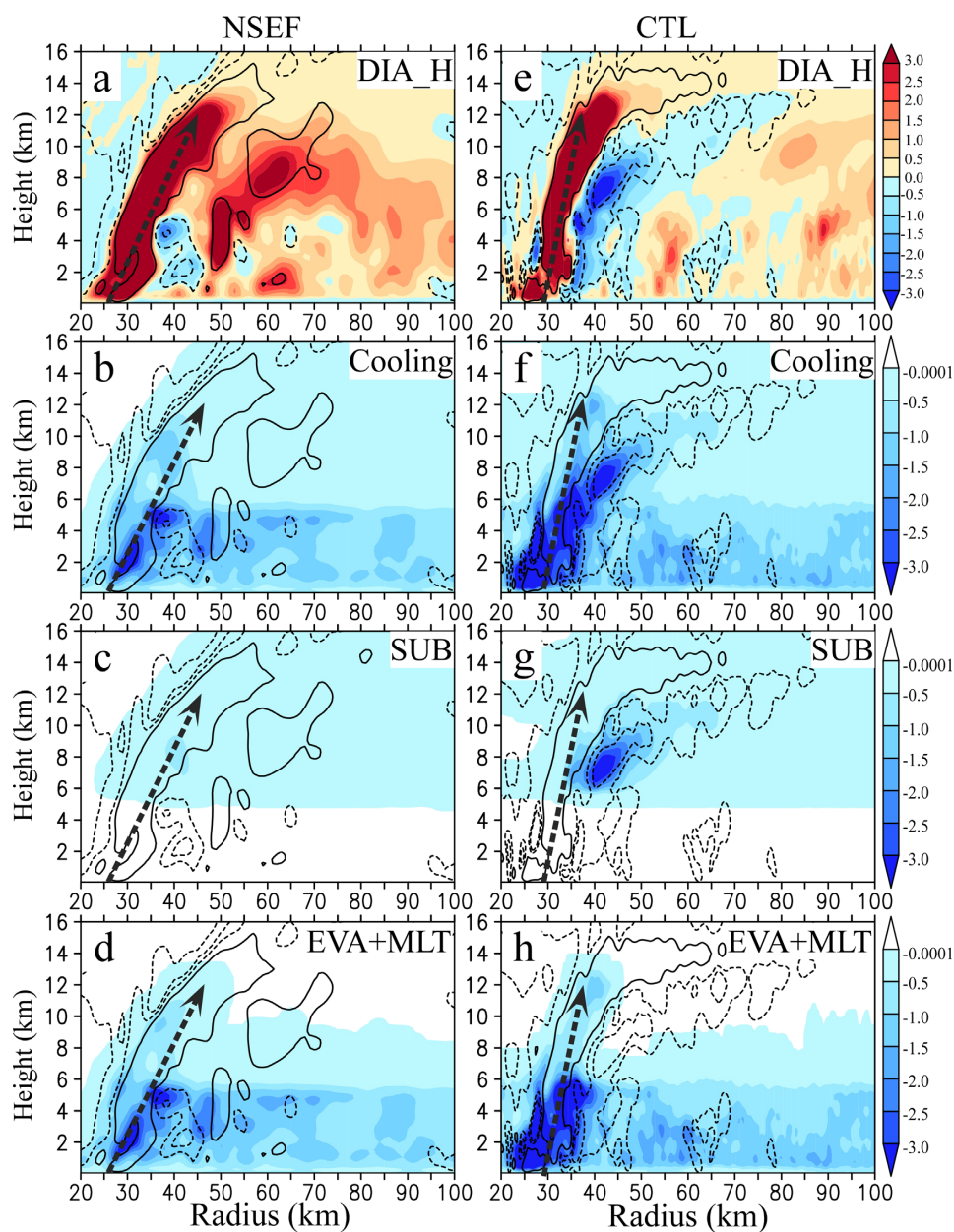
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570 Figure 8. Radius-height cross-sections of the upshear-right quadrant-mean (a, e) buoyancy force
 571 (shaded, 10^{-3} m s^{-2}), (b, f) the thermal buoyancy (shaded, 10^{-3} m s^{-2}), (c, g) the dynamic
 572 buoyancy (shaded, 10^{-3} m s^{-2}), and (d, h) the hydrometeor loading (shaded, 10^{-3} m s^{-2})
 573 superimposed with the vertical motion (updraft, black solid contours: 0.5 m s^{-1} ; downdrafts,
 574 black dashed contours: 0.05 m s^{-1}) at 30 h for (a-d) NSEF and (e-h) CTL. The black dashed
 575 arrows denote the eyewall.

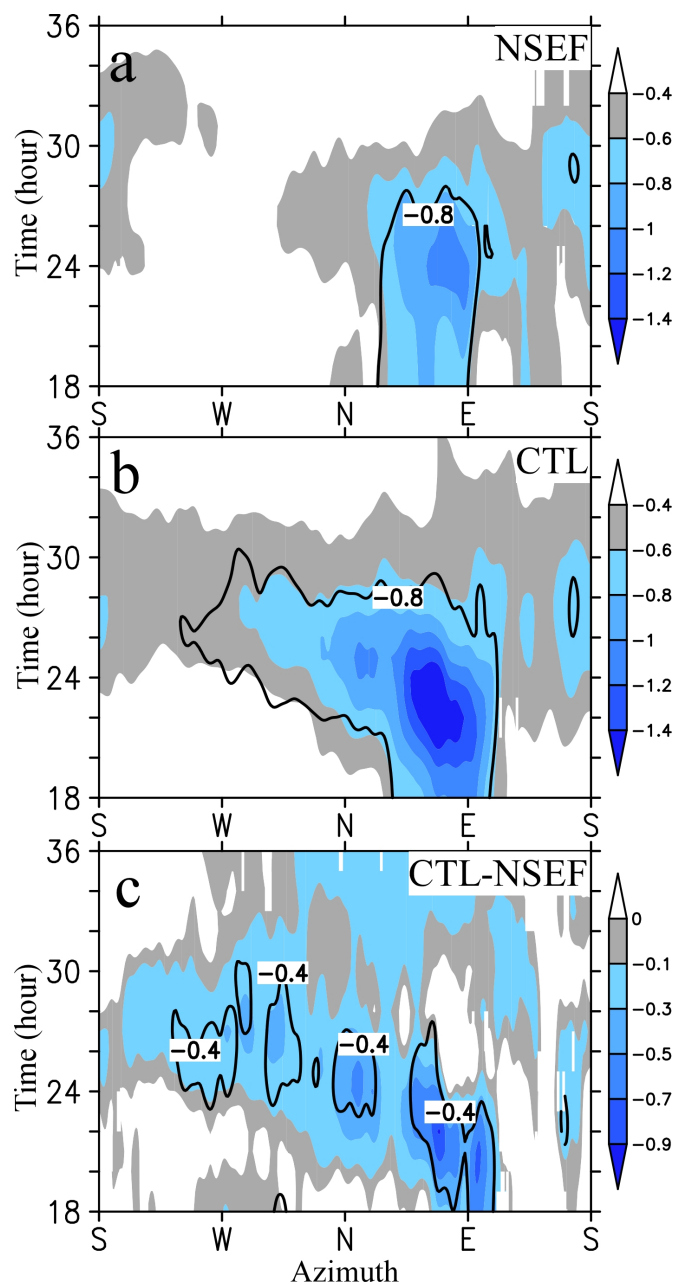


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577 Figure 9. Radius-height cross-sections of the upshear-right quadrant-mean (a, b) vertical pressure
578 gradient force (shaded, 10^{-3} m s^{-2}) and (c, d) the sum of buoyancy and vertical pressure
579 gradient force (shaded, 10^{-3} m s^{-2}), superimposed with the vertical motion (updraft, black solid
580 contours: 0.5 m s^{-1} ; downdrafts, black dashed contours: 0.05 m s^{-1}) at 30 h for (a, c) NSEF
581 and (b, d) CTL. The black dashed arrows denote the eyewall.

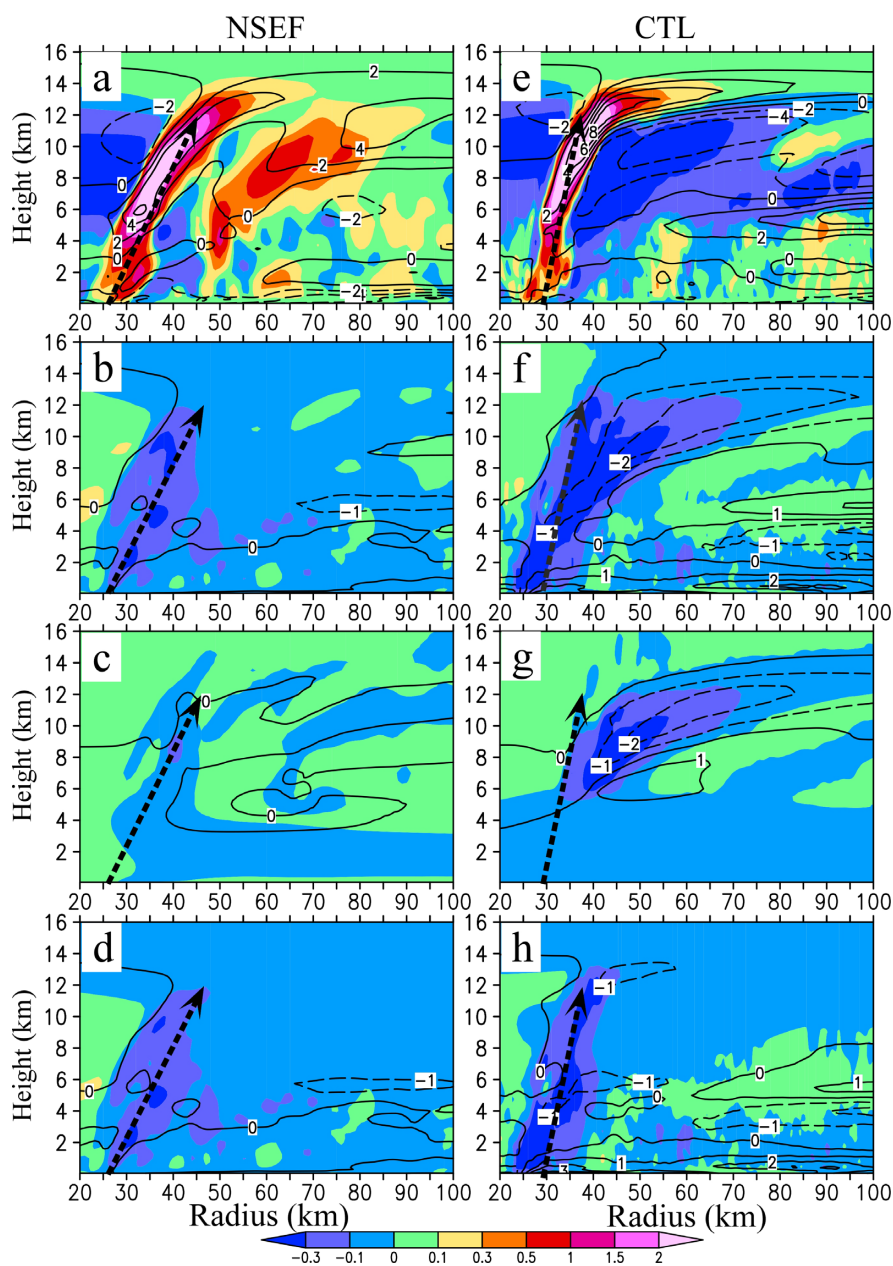


582
583 Figure 10. Radius-height cross-sections of the upshear-right quadrant-mean (a, e) diabatic heating
584 rate (shaded, 10^{-3} K s^{-1}), (b, f) cooling rate including evaporation, melting and sublimation
585 processes (shaded, 10^{-3} K s^{-1}), (c, g) sublimation cooling rate, and (d, h) melting and
586 evaporation cooling rates superimposed with the vertical motion (updraft, solid lines of 0.5
587 m s⁻¹; downdrafts, dashed lines of -0.05 and -0.3 m s⁻¹) at 30 h for (a-d) NSEF and (e-h) CTL.
588 The black dashed arrows denote the eyewall.



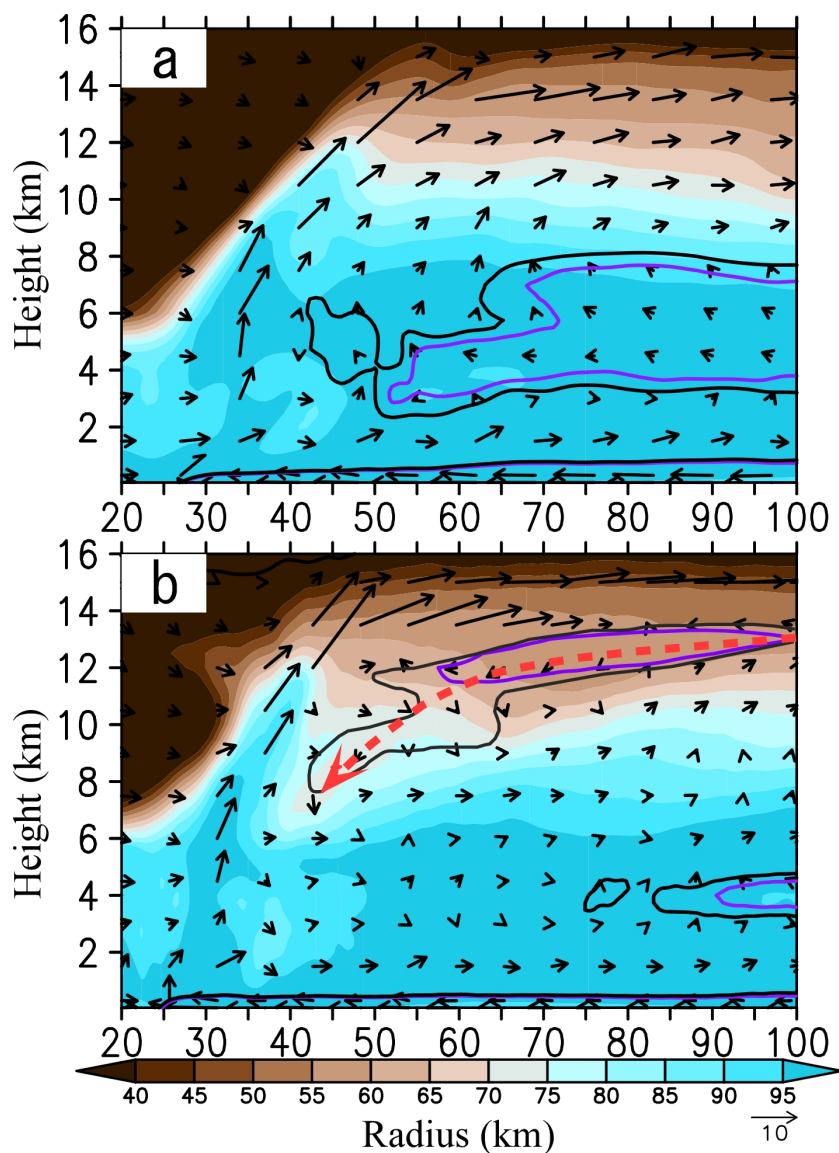
589

590 Figure 11. Azimuthal-time cross-sections of the layer-mean (11.5-12.5 km) diabatic cooling
591 (shaded, 10^{-3} K s^{-1}) and subsidence (contour, m s^{-1}) averaged within a radial distance of 25
592 km starting from the radius of 5-km outside the eyewall (RMW+5 km to RMW+30 km) of
593 (a) NSEF, (b) CTL, and (c) differences between CTL and NSEF. The black contours are -0.8
594 m s^{-1} in (a, b) and -0.4 m s^{-1} in (c).



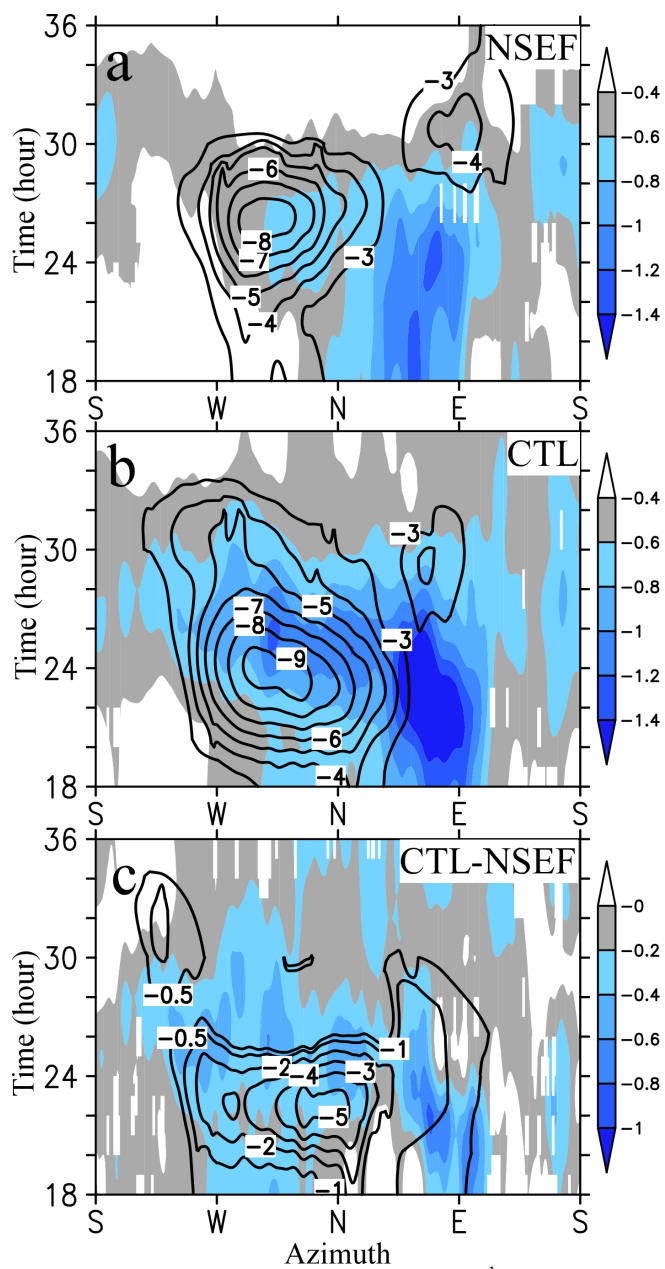
595

596 Figure 12. Radius-height cross-sections of the upshear-right quadrant-mean vertical (shaded, m s^{-1})
 597 and radial motion (contours, m s^{-1}) forced by the (a, e) diabatic heating, (b, f) hydrometeors
 598 cooling, (c, g) sublimation cooling, (d, h) melting and evaporation cooling at 30 h for (a-d)
 599 NSEF and (c-h) CTL. Note that the radial wind is at 2 m s^{-1} intervals in (a) and (e), and 1 m s^{-1}
 600 intervals in others. The white dashed lines with 0.5 m s^{-1} vertical motion indicate the
 601 eyewall convection region. The black dashed arrows denote the eyewall.



602

603 Figure 13. Radius-height cross-sections of the the upshear-right quadrant-mean relative humidity
604 (shaded, %) and in-plane flows (vector, m s^{-1}) at $t = 30$ h for (a) NSEF and (b) CTL. The black
605 and purple lines are radial inflows of -0.01 and -1 m s^{-1} , respectively. The red dashed arrow
606 indicates the upper-level dry inflows.

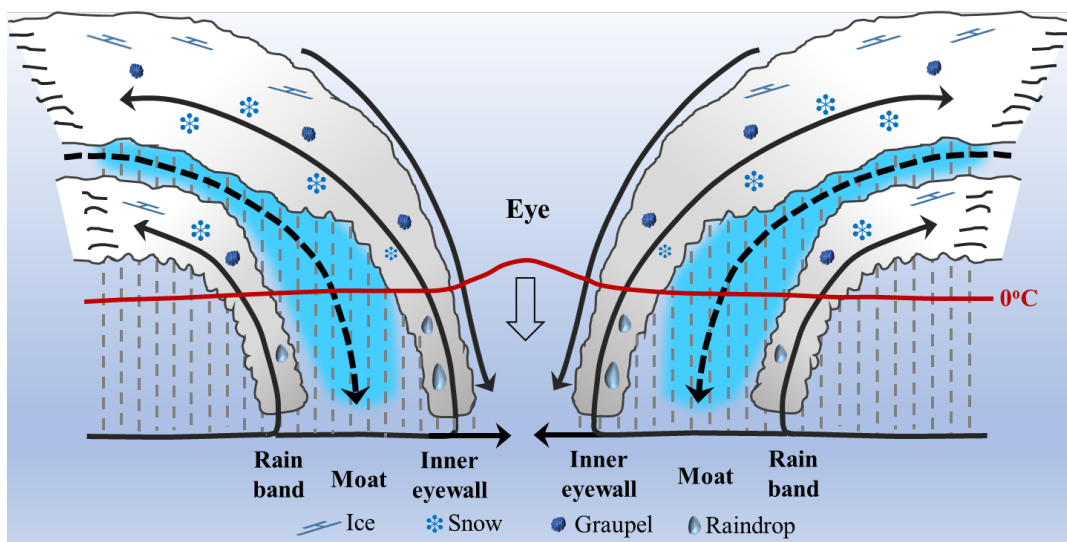


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Figure 14. Same as in Fig. 11 but for subsidence (shaded, m s^{-1}) and radial inflows (contour, m s^{-1}) of (a) NSEF, (b) CTL, and (c) differences between CTL and NSEF.



611



612

613 Figure 15. The inner-core structures of a hurricane undergoing the eyewall replacement circle,
614 including the eye, the primary eyewall, the moat, and the rainband of evolving into the
615 secondary eyewall. The black solid arrows denote the air motion relative to the TC. The black
616 dashed arrows show the upper-level descending inflows beneath the cumulus anvil from the
617 inner eyewall. The light blue shading indicates the cooling induced by the sublimation,
618 melting, and evaporation of hydrometeors (ice, snow, graupel, and raindrops) associated with
619 the moat subsidence. The gray dashed lines indicate the precipitation below the clouds. The
620 red solid line denotes the 0 °C temperature of the melting level.