

# 1 Less atmospheric radiative heating by dust due to the synergy of 2 coarser size and aspherical shape

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8 **Abstract.** Mineral dust aerosols cool and warm the atmosphere by scattering and absorbing solar (short-wave: SW)  
9 and thermal (long-wave: LW) radiation. However, significant uncertainties remain in dust radiative effects, largely  
10 due to differences in the dust size distribution and spectral optical properties simulated in Earth system models. Dust  
11 models typically underestimate the coarse dust load (more than 2.5  $\mu\text{m}$  in a diameter) and assume a spherical shape,  
12 which leads to an overestimate of the fine dust load (less than 2.5  $\mu\text{m}$ ) after the dust emissions in the models are scaled  
13 to match observed dust aerosol optical depth at 550 nm (DAOD<sub>550</sub>). Here, we improve the simulated dust properties  
14 with datasets that leverage measurements of size-resolved dust concentration, asphericity factor, and refractive index  
15 in a coupled global chemical transport model with a radiative transfer module. After the adjustment of size-resolved  
16 dust concentration and spectral optical properties, the global and annual average of DAOD<sub>550</sub> from the simulation  
17 increases from 0.023 to 0.029, and falls within the range of a semi-observationally-based estimate ( $0.030 \pm 0.005$ ).  
18 The reduction of fine dust load after the adjustment leads to a reduction of the SW cooling at the Top Of the  
19 Atmosphere (TOA). To improve agreement against a semi-observationally-based estimate of the radiative effect  
20 efficiency at TOA, we find that a less absorptive SW dust refractive index is required for coarser aspherical dust. Thus,  
21 only a minor difference is estimated for the net global dust radiative effect at TOA ( $-0.08$  vs.  $-0.00 \text{ W}\cdot\text{m}^{-2}$  on a global  
22 scale). Conversely, our sensitivity simulations reveal that the surface warming is substantially enhanced near the  
23 strong dust source regions (less cooling to  $-0.23$  from  $-0.60 \text{ W}\cdot\text{m}^{-2}$  on a global scale). Thus, less atmospheric radiative  
24 heating is estimated near the major source regions (less heating to 0.15 from  $0.59 \text{ W}\cdot\text{m}^{-2}$  on a global scale), because  
25 of enhanced LW warming at the surface by the synergy of coarser size and aspherical shape.

## 26 1 Introduction

27 Mineral dust aerosols can both cool and warm the climate, but how much dust aerosols net influence global  
28 climate is highly uncertain (Penner, 2019). Global dust modeling studies have suggested that mineral dust exerts  
29 global and annual mean aerosol radiative effect (RE) between  $-0.6$  and  $+0.2 \text{ W m}^{-2}$  at the Top Of the Atmosphere  
30 (TOA) and between  $-0.2$  and  $-2.7 \text{ W m}^{-2}$  at the surface (Miller and Tegen, 1998; Balkanski et al., 2007; Tanaka et  
31 al., 2007; Takemura et al., 2009; Räisänen et al., 2013; Zhao et al., 2013; Albani et al., 2014; Colarco et al., 2014;  
32 Heald et al., 2014; Di Biagio et al., 2020; Tuccella et al., 2020). Whereas a negative RE corresponds to the cooling of  
33 the global system when the sunlight is reflected to space, a positive RE corresponds to an overall warming of the  
34 Earth-atmosphere system by trapping incident short-wave (SW) and outgoing long-wave (LW) radiation. Radiative  
35 effect by dust aerosols perturbs surface temperature, wind speed, rainfall, and vegetation cover, which may induce

36 feedback on dust emissions (Perlwitz et al. 2001; Miller et al., 2004a; Colarco et al., 2014). The climate feedback does  
37 not only depend on RE at TOA or the surface alone but also on the difference to the value at TOA and surface, which  
38 represents radiative heating within the atmosphere (Miller et al., 2004b; Yoshioka et al., 2007; Lau et al., 2009). The  
39 large uncertainties in quantifying the dust RE in the models are mainly propagated from the large spatial heterogeneity  
40 and temporal variability of mineral dust abundance and the physicochemical properties (e.g., size distribution, mineral  
41 composition, and shape), as well as the ground surface characteristics and atmospheric properties (e.g., surface  
42 reflectance, temperature, and atmospheric absorption) (Sicard et al., 2014; Lacagnina et al., 2015; Li and Sokolik,  
43 2018). The model errors in dust size distribution and particle shape can lead to an overestimate of fine dust load after  
44 the dust emissions in the models are scaled to match observed dust aerosol optical depth at 550 nm (DAOD<sub>550</sub>). The  
45 corresponding overestimate of SW cooling might be compensated for in models by using a refractive index that is too  
46 absorbing (Di Biagio et al., 2019, 2020), which depends on the mineral composition of the dust. We regard “fine” and  
47 “coarse” dust as dust particles with a diameter less than 2.5 μm (i.e., PM<sub>2.5</sub>) and between 2.5 and 20 μm, respectively.  
48 Below, we provide a brief discussion of the effects of the dust size distribution, particle shape, and mineral  
49 composition on dust radiative effects.

50         First, there has been increased attention paid to the importance of accurately predicting the abundance of coarse  
51 dust for the global energy balance (Kok et al., 2017; Song et al., 2018; Di Biagio et al., 2020; Adebisi and Kok, 2020).  
52 The coarser particles are expected to be more prevalent closer to the source regions, as they fall much faster than finer  
53 particles (Mahowald et al., 2014). For instance, the lifetime of dust aerosols larger than 30 μm in diameter is less than  
54 12 h in most cases except in large haboobs (Ryder et al., 2013). Current models, however, cannot accurately simulate  
55 observed transport of coarse dust particles across the Atlantic (Weinzierl et al., 2017; Ansmann et al., 2017), although  
56 several hypotheses have been proposed to explain measurements of giant dust particles (larger than 63 μm in diameter)  
57 relatively far from source regions (van der Does et al., 2018). The potential mechanism for long-range transport of  
58 giant dust particles is that the uplift events of coarse dust can be induced by a nocturnal low-level jet or cold pool  
59 outflow from mesoscale convective systems (i.e., haboobs) (Rosenberg et al., 2014; Ryder et al., 2019). At higher  
60 elevation, electrostatic forces might retard the settling of coarse and giant dust particles and thus may facilitate the  
61 transport of these particles over longer distances (Harrison et al., 2018; Toth et al., 2019). Other missing processes  
62 that affect the transport and deposition of giant particles would also need to be incorporated into the models to  
63 reproduce the measurements of the size distribution over the open ocean (van der Does et al., 2018). The coarse dust  
64 particles scatter and absorb both the solar and thermal radiation, causing a net warming effect at TOA. In contrast, the  
65 fine dust particles principally scatter SW radiation, causing a net cooling effect. Since coarse dust tends to warm the

66 climate, the underestimation of the abundance of coarse dust causes Earth system models to underestimate the  
67 warming near the dust source regions.

68 Second, previous studies have shown that the SW radiative effect of dust asphericity on climate simulations is  
69 minor on a global scale, partly because the larger DAOD is compensated for by the larger asymmetry parameter of  
70 aspherical dust, which reduces the amount of radiation scattered backward to space (Räsänen et al., 2013; Colarco et  
71 al., 2014). Moreover, non-spherical calcium-rich dust particles can be converted to spherical particles, due to  
72 heterogeneous reactions with nitrate and sulfate on these particles, especially over polluted regions (Laskin et al.,  
73 2005; Matsuki et al., 2005). As the plumes move downwind to the oceans, the dust aerosols can be aggregated with  
74 sea salt in the marine boundary layer, which leads to more spherical shapes and larger sizes (Zhang and Iwasaka,  
75 2004). However, the assumption of spherical shape in models leads to a substantial underestimation of the extinction  
76 efficiency and thus DAOD near the strong source regions, mainly because the assumption of sphericity causes an  
77 underestimation of the surface-to-volume ratio compared to aspherical dust (Kok et al., 2017, 2021; Hoshyaripour et  
78 al., 2019; Tuccella et al., 2020). Radiative effect efficiency is often used for the evaluation of the models and is defined  
79 as the gradient of a linear least squares fit applied to AOD and dust radiative effect at each two-dimensional (2-D)  
80 grid box ( $W \cdot m^{-2} AOD^{-1}$ ). Thus, the estimates of the dust radiative effect efficiency could be biased, in part, due to  
81 large uncertainties associated with the spherical assumption on AOD retrieval (Zhou et al., 2020).

82 Third, the dust refractive index is often derived from measurements based on dust or individual mineral particles  
83 (Bedidi and Cervelle, 1993; Long et al., 1993; Di Biagio et al., 2017, 2019; Stegmann & Yang, 2017). Indeed, most  
84 dust particles are internal mixtures of various mineral compositions and irregular shapes (Reid, 2003; Wiegner et al.,  
85 2009; Wagner et al., 2012). In desert soils, iron (Fe) oxides are generally hematite ( $\alpha\text{-Fe}_2\text{O}_3$ ) and goethite (FeOOH),  
86 which cause soil-derived dust absorption at ultraviolet (UV) and visible wavelengths (Sokolik and Toon, 1999;  
87 Balkanski et al., 2007). These two minerals have distinct optical properties, which might cause various intensities of  
88 SW absorption and thus RE of dust aerosols (Lafon et al., 2016). The dust complex refractive index in the LW also  
89 depends on the particle mineralogical composition (Sokolik et al., 1998). Di Biagio et al. (2017) found a linear  
90 relationship between the magnitude of the imaginary refractive index at 7.0, 9.2, and 11.4  $\mu\text{m}$  and the mass  
91 concentration of calcite and quartz absorbing at these wavelengths. However, the speciation of dust into its mineral  
92 components inherently comprises uncertainties on soil mineralogy, mineral content in size-segregated dust particles,  
93 and refractive index of mineral, partly due to the differences in prescribed parameters such as the particle size. The  
94 atmospheric aging of Fe-containing aerosols can further modulate the optical properties of Fe oxides (Ito et al., 2018),  
95 while the photochemical transformation of Fe oxides from lithogenic sources due to atmospheric processing is  
96 relatively limited (< 10%), compared to pyrogenic sources (Ito et al., 2019).

97 Here, we focus on the influence of the size-resolved abundance of aspherical dust on the aerosol radiative effects  
98 in a coupled global chemical transport model (IMPACT) (Ito et al., 2020 and references therein) with a radiative  
99 transfer module (RRTMG) (Iacono et al., 2008). We improve the accuracy of these simulations by correcting the bias  
100 in size-resolved dust concentration with the Dust Constraints from joint Observational-Modelling-Experimental  
101 analysis (DustCOMM) data set (Adebiyi et al., 2020), as well as by considering the aspherical shape (Huang et al.,  
102 2020a, 2020b). We then explore the sensitivity to dust refractive index.

## 103 **2 Methods**

104 We examined the dust radiative effects using ten different numerical experiments that varied (1) the simulated  
105 dust concentration and their size distribution, (2) particle shape, and (3) mineralogical composition (Tables 1 and 2).  
106 Two experiments used the dust concentrations calculated from the IMPACT model with the finer dust size (denoted  
107 as “IMPACT”). Subsequently, the simulated dust concentration and the size distribution were adjusted to the semi-  
108 observationally-based concentrations (Adebiyi and Kok, 2020) in the other eight experiments with the coarser dust  
109 size (denoted as “DustCOMM”). The term “semi-observationally-based” is used for DustCOMM, DAOD<sub>550</sub>, and dust  
110 radiative effect efficiency when the estimates are based on the combination of observations and models. Five  
111 sensitivity experiments were handled in the RRTMG calculations performed with different refractive indices and  
112 hourly averaged aerosol concentrations with the two chemical transport model simulations of “IMPACT” and  
113 “DustCOMM”. The other three experiments were calculated from the model output with a post-processor. Two  
114 simulations used the spherical assumption on the particle shape (denoted as “Sphere”), whereas the dust asphericity  
115 was considered in the other eight experiments (denoted as “Asphere”). We then examined different refractive indices  
116 for the dust mineralogy to represent the regional variations in refractive indices (denoted as “Mineral”, “DB17”,  
117 “DB19”, “V83”, “Less SW”, “More LW”, “More SW”, and “Less LW”). These sensitivity simulations and their  
118 radiative effects are summarized in Tables 1 and 2, respectively, with more details below. In section 2.3, we describe  
119 the DustCOMM data set used to adjust (1) size-resolved abundance of dust concentration. In section 2.4, we describe  
120 the adjustment factor of (2) particle shape for spectral optical properties. In section 2.5, we describe differences in  
121 spectral refractive indices due to (3) different mineralogical compositions for the radiative flux calculation.

### 122 **2.1 Aerosol chemistry transport model**

123 This study used the Integrated Massively Parallel Atmospheric Chemical Transport (IMPACT) model (Ito et  
124 al., 2020 and references therein). Simulations were performed for the year 2016, using a horizontal resolution of  
125  $2.0^{\circ} \times 2.5^{\circ}$  for latitude by longitude and 47 vertical layers. The chemical transport model was driven by the Modern

126 Era Retrospective analysis for Research and Applications 2 (MERRA-2) reanalysis meteorological data from the  
127 National Aeronautics and Space Administration (NASA) Global Modeling and Assimilation Office (GMAO) (Gelaro  
128 et al., 2017). The radiative feedback of the dust on the climate model simulation can be predicted by a separate version  
129 of the model (Penner et al., 2018).

130 The model simulated the emissions, chemistry, transport, radiation, and deposition of major aerosol species,  
131 including mineral dust, black carbon (BC), particulate organic matter (POM), sulfate, nitrate, ammonium, and sea  
132 spray aerosols, and their precursor gases. Atmospheric processing of mineral dust aerosols, during transport, were  
133 projected for four distinct aerosol size bins ( $<1.26\ \mu\text{m}$ ,  $1.26\text{--}2.5\ \mu\text{m}$ ,  $2.5\text{--}5\ \mu\text{m}$ , and  $5\text{--}20\ \mu\text{m}$  of diameter). In this  
134 version of the IMPACT model, two modes were used for sulfate aerosol (nuclei and accumulation mode), and two  
135 moments were predicted within each mode (sulfate aerosol number and mass concentration) (Liu et al., 2015). The  
136 surface coating of sulfate on dust aerosols occurred as a result of the condensation of sulfuric acid gas on their surfaces,  
137 coagulation with sulfate aerosol, and formation in aqueous reactions within cloudy regions of the atmosphere (Liu et  
138 al., 2015). The heterogeneous uptake of nitrate, ammonium, and water vapor by each aerosol for each size bin was  
139 interactively simulated in the model following a hybrid dynamical approach (Feng and Penner, 2007). Five types of  
140 aerosols (i.e., dust, nucleated sulfate, carbonaceous aerosols from fossil fuel combustion, carbonaceous aerosols from  
141 biomass burning, and sea salt) were assumed to be externally mixed in each size bin for the computation of spectral  
142 optical properties (Xu and Penner, 2012). Dust emissions were dynamically simulated using a physically-based  
143 emission scheme (Kok et al., 2014; Ito and Kok, 2017) with the soil mineralogical map (Journet et al., 2014; Ito and  
144 Shi, 2016). To derive atmospheric concentration of mineral composition for dust aerosol, “tagged” tracer was used  
145 for each size-resolved mineral source. The direct emissions of dust were evenly distributed in mixing ratio throughout  
146 the planetary boundary layer. The global scaling factor of dust emission was determined from the comparison of the  
147 model results with ground-based AOD measurements near the dust source regions prior to the adjustment to the  
148 DustCOMM (Kok et al., 2014; Ito and Kok, 2017). In recent review papers, multi-model evaluations of aerosol iron  
149 concentrations and their solubilities have been comprehensively summarized on global and regional scales  
150 (Myriokefalitakis et al., 2018; Ito et al., 2021).

151 To improve the accuracy of our simulations of mineral dust, we made several upgrades to the on-line emission  
152 and gravitational settling schemes used in Ito et al. (2020). The dust emissions were extremely sensitive to soil  
153 moisture, and thus the bias was adjusted with satellite observations (Ito and Kok, 2017). However, the satellite  
154 measurements were only available every other day, depending on location. The Soil Moisture Active Passive (SMAP)  
155 Level-4 Soil Moisture data product addressed these limitations by merging the satellite observations into a numerical  
156 model of the land surface water and energy balance while considering the uncertainty of the observations and model

157 estimates (Reichle et al., 2019). In this work, we utilized the 3-hourly data of soil moisture derived from the SMAP  
158 for barren and open shrublands separately (Reichle et al., 2018). To achieve this, we used the MODerate resolution  
159 Imaging Spectroradiometer (MODIS) land cover map at 500 m resolution to calculate the fraction of barren and open  
160 shrublands in each ground surface layer (Friedl et al., 2019)

161 Compared to the assumption on spherical shapes of aerosols, the dust asphericity increased aerodynamic drag  
162 at a given volume and mass, and thus increased gravitational settling lifetime by about 20% (Huang et al., 2020a).  
163 Here, we implemented a globally averaged asphericity factor of 0.87 (Huang et al., 2020a) to the gravitational settling  
164 scheme for mineral dust. Nevertheless, the lifetime of the dust aerosol for the largest-size bin in the IMPACT model,  
165 even after accounting for asphericity (1.4 days for 5–20  $\mu\text{m}$  of diameter), was significantly shorter than an ensemble  
166 of model results ( $2.1 \pm 0.3$  days for the mass mean diameter of 8.3  $\mu\text{m}$ ) (Kok et al., 2017). The impact of this  
167 underestimate of atmospheric lifetime is explored using the DustCOMM data set, as was summarized in Table 2 (E3  
168 – E4).

## 169 **2.2 Integration of IMPACT and RRTMG**

170 To improve the accuracy of our simulations of dust RE, we made upgrades to the radiative transfer calculations  
171 (Ito et al., 2018 and references therein). In this study, we integrated the Rapid Radiative Transfer Model for GCMs  
172 (RRTMG) online within the IMPACT model to calculate the radiative fluxes associated with atmospheric aerosols.  
173 RRTMG is a radiative transfer code that calculates the SW and LW atmospheric fluxes (Iacono et al., 2008). Given  
174 the size range of dust particles, scattering and absorption in the on-line model were described in terms of Mie theory.  
175 Assuming homogeneous spherical particles, the spectral optical properties such as the mass extinction coefficient,  
176 single scattering albedo, and asymmetry parameter were calculated using a look-up table as a function of refractive  
177 index and size parameter (Xu and Penner, 2012). The impact of this spherical assumption is explored using aspherical  
178 factor, as was summarized in Table 2 (E5 – E4).

179 The mineral dust particles were assumed to follow prescribed size distributions within each size bin (Liu et al.,  
180 2015). In applying the look-up table, the size spectrum for mineral dust was divided into 30 sub bins (Wang and  
181 Penner, 2009). As for the SW, the particle size increased with the uptake of sulfate, nitrate, ammonium, and water by  
182 the aerosols (Xu and Penner, 2012). These coating materials were treated as internally mixed with dust aerosol in each  
183 size bin and thus can reduce solar absorption of mineral dust. Subsequently, these optical properties were used by the  
184 RRTMG to calculate RE based on dust mixing ratio distributions in the IMPACT model. The dust RE was estimated  
185 as the difference in the calculated radiative fluxes with all aerosols and with all aerosols except the dust aerosols for  
186 each bin. As the LW scattering was not accounted for in the RRTMG, we multiplied the LW radiative fluxes by the

187 adjustment factors of  $1.18 \pm 0.01$  and  $2.04 \pm 0.18$  for the dry particles at the surface and TOA (Dufresne et al., 2002),  
188 following Di Biagio et al. (2020). The larger adjustment factor at TOA reflects the fact that the upward LW radiation  
189 emitted from the ground surface can be trapped through scattering and absorption compared to the surface.

190 The broadband direct and diffuse albedos for both the UV visible and visible IR were specified from the hourly  
191 MERRA-2. The surface emissivity was based on the hourly MERRA-2. Long-lived greenhouse gas concentrations  
192 were obtained from historical greenhouse gas concentrations for climate models (Meinshausen et al., 2017). Water  
193 vapor concentrations were specified according to the MERRA-2. Cloud optical properties were calculated based on  
194 the liquid and ice visible optical depths from the MERRA-2, prescribing effective radii of  $10 \mu\text{m}$  for water droplets  
195 and  $25 \mu\text{m}$  for ice particles, respectively (Gettelman et al., 2010; Heald et al., 2014).

### 196 **2.3 DustCOMM dataset and sensitivity experiments to size-resolved dust concentration**

197 Dust Constraints from joint Observational-Modelling-experiMental analysis (DustCOMM) is a dataset of  
198 three-dimensional (3-D) dust properties obtained by combining observational, experimental, and modeling constraints  
199 on dust properties. While details can be found in Adebisi et al. (2020) and Adebisi and Kok (2020), we provide a  
200 brief overview here. First, DustCOMM's constraint on the 3-D dust size distribution combines dozens of previously  
201 published in-situ measurements of dust size distributions taken during several field campaigns, with an ensemble of  
202 climate model simulations. The framework used those in-situ measurements first to constrain the globally averaged  
203 size distribution (Adebisi and Kok, 2020), which is used subsequently to adjust the bias in an ensemble of six global  
204 model simulations (Adebisi et al., 2020). The constraints on dust size distribution range from  $0.2 \mu\text{m}$  to  $20 \mu\text{m}$  in  
205 diameter, where a generalized analytical function describes the sub-bin distribution based on brittle fragmentation  
206 theory (Kok, 2011). The second DustCOMM product – atmospheric dust mass loading – combines the constraints on  
207 dust size distribution with constraints on dust extinction efficiency and dust aerosol optical depth (Adebisi et al., 2020).  
208 The constraints on dust extinction efficiency used the single-scattering database of Meng et al. (2010) and leveraged  
209 measurements of the dust index of refraction as well as accounts for the non-spherical shape of dust particles (Kok et  
210 al., 2017). For this, we approximate dust as tri-axial ellipsoidal particles described by the globally representative  
211 values of measured dust aspect ratio (the length-to-width ratio), and the height-to-width ratio (HWR) obtained from  
212 Huang et al. (2020a). Furthermore, the dust aerosol optical depth used to obtain the dust mass loading combines the  
213 semi-observationally-based dataset from Ridley et al. (2016) with information from four reanalysis products. This  
214 includes the MERRA-2, Navy Aerosol Analysis and Prediction System (NAAPS), Japanese Reanalysis for Aerosol  
215 (JRAero), and Copernicus Atmosphere Monitoring Service interim ReAnalysis (CAMSiRA) (Adebisi et al., 2020).

216 The aerosol RE of mineral dust strongly depends on both the magnitude of dust load and the dust size  
217 distribution (Tegen and Lacis, 1996; Liao and Seinfeld, 1998). The DustCOMM data set contains total column loading  
218 and concentration of mineral dust resolved by season and particle size (Adebisi et al., 2020). To correct the bias in  
219 the seasonally averaged size-resolved dust emission in the IMPACT model, the sum of bin 1, bin 2, and bin 3 dust  
220 emission flux was scaled by the seasonal mean of the ratio of the sum of bin 1, bin 2, and bin 3 dust column loading  
221 between the model and DustCOMM at each 2-D grid box. When the source function was used for high-latitude dust  
222 in the Northern Hemisphere, this led to substantially high emissions and thus RE over there, likely due to the influences  
223 from long-range transported dust. Therefore, the direct emissions of dust from the nine major source regions only  
224 (Kok et al., 2021) were adjusted using the DustCOMM data (Fig. 1). To adjust the size bias in dust emissions, the  
225 mass fraction of emitted dust for each bin was prescribed according to the size-resolved total column loading of  
226 DustCOMM at each 2-D grid box. Overall, the IMPACT-simulated lifetime of the dust aerosol for the second-size bin  
227 (7.8 days 1.26–2.5  $\mu\text{m}$  of diameter) was in good agreement with the ensemble of model results ( $8.5 \pm 1.1$  days for the  
228 mass mean diameter of 1.8  $\mu\text{m}$ ) (Kok et al., 2017). To correct the bias in the seasonally averaged 3-D dust size  
229 distribution after the transport, the mass fraction of dust concentration for each bin between 0.2 and 20.0  $\mu\text{m}$  of  
230 diameter was scaled at each 3-D grid box prior to calculating the radiative fluxes using the RRTMG by the ratio of  
231 mass concentration of  $\text{PM}_{2.5}$  (i.e., the sum of bin 1 and bin 2) to each bin (Table 3).

#### 232 **2.4 Asphericity factor for optical properties and sensitivity experiments to particle shape**

233 To account for the dust asphericity, an adjustment factor was applied to the spherical optical properties at each  
234 dust size parameter and refractive index. The adjustment factors for the spectral optical properties of non-spherical  
235 particles were calculated after Huang et al. (2020b). The atmospheric aging of mineral dust can form a uniform coating  
236 around the mineral core and therefore decrease particle asphericity during transport. This is implicitly considered in  
237 the globally averaged shape distribution of dust (Huang et al., 2019). Specifically, Huang et al. (2020b) combined  
238 globally representative dust shape distributions (Huang et al., 2020a) with a shape-resolved single-scattering database  
239 (Meng et al., 2010). This database combines four computational methods (Mie theory, T-matrix method, discrete  
240 dipole approximation, and an improved geometric optics method) to compute the single-scattering properties of non-  
241 spherical dust for a wide range of shape descriptors. Huang et al. (2020b) provided the look-up table containing optical  
242 properties of non-spherical dust as functions of size parameter and refractive index.

243 The approximation of particles to spheres is evaluated by applying aspherical factors to the optical properties  
244 of the mass extinction coefficient, single scattering albedo, and asymmetry parameter for SW, as well as absorption  
245 fraction of extinction for the LW. At the same time, we maintained the consideration of asphericity on the gravitational



246 velocity and kept the dust concentrations unaltered between the spherical (denoted as “Sphere”) and aspherical  
247 (denoted as “Asphere”) cases.

## 248 **2.5 Spectral refractive index and sensitivity experiments to mineralogical compositions**

249 The aerosol RE of mineral dust depends on mineralogical composition. For the sensitivity simulation to the  
250 SW and LW refractive indices, we used the global mean of laboratory measurements of the refractive index from 19  
251 natural soils from various source regions around the world in Di Biagio et al. (2019) (denoted as “DB19”) and in Di  
252 Biagio et al. (2017) (denoted as “DB17”), respectively. To illustrate the regional heterogeneity of refractive index, the  
253 refractive index obtained from 19 samples was aggregated into 9 main source regions, and the arithmetic mean was  
254 calculated for each source region (Di Biagio et al., 2017, 2019). The regionally averaged imaginary parts of the  
255 refractive indices at the wavelength of 0.52  $\mu\text{m}$  and 9.7  $\mu\text{m}$  showed large differences in SW and LW absorptivity,  
256 respectively, between different samples collected at various geographical locations (Fig. 1).

257 The optical properties from the measurements for dust samples generated from 19 natural soils suggested a  
258 considerable role of Fe oxides in determining the SW absorption (Di Biagio et al., 2019). The refractive indices for  
259 mineral components were used for hematite, goethite (Bedidi and Cervelle, 1993), silicate particle group, quartz,  
260 gypsum ( $\text{CaSO}_4$ ) (Stegmann & Yang, 2017), and calcite ( $\text{CaCO}_3$ ) (Long et al., 1993) in the simulations denoted as  
261 “Mineral”. The hematite and goethite were treated separately according to the mineralogical map (Journet et al., 2014).  
262 Consequently, hematite mass content averaged in the dust at emission (0.79% for fine and 0.50% for coarse from the  
263 IMPACT simulation) was lower than goethite content (1.8% and 1.3%, respectively) on a global scale. In addition to  
264 the primary emission of gypsum,  $\text{CaSO}_4$  is secondarily formed due to the dissolution/precipitation of  $\text{CaCO}_3$  in  
265 thermodynamic equilibrium condition (Ito and Feng, 2010). To illustrate the difference in refractive index, the global  
266 mean of the mineral composition was used for the comparison with DB19 (Fig. 1). The imaginary parts of the  
267 refractive indices from mineralogical map were higher than DB17, resulting in a stronger absorption over the SW  
268 spectrum.

269 The mineral dust LW refractive index also depends on its mineralogical composition (Sokolik et al., 1998; Di  
270 Biagio et al., 2017). The LW refractive index of Volz (1983) has been widely used in climate models and satellite  
271 remote sensing algorithms and thus was examined here (denoted as “V83”) (Song et al., 2018). The imaginary parts  
272 of the refractive indices from V83 were higher than DB19, resulting in a stronger absorption over most of the LW  
273 spectrum. To analyze the dependence of the results on less (more) absorptive SW and less (more) absorptive LW  
274 refractive indices, we made further sensitivity simulations by varying the values of imaginary parts of the refractive  
275 index within the range of values from Di Biagio et al. (2017, 2019) (10% or 90% percentiles for SW or LW,

276 respectively) (denoted as “Less” or “More”). The associated real parts with 10% or 90% percentile imaginary parts  
277 for LW were calculated to account for the Kramers-Kronig relation (Lucarini et al., 2005).

## 278 **2.6 Semi-observationally-based dust SW and LW radiative effect efficiency**

279 To estimate dust radiative effect efficiency, aerosol and radiation remote sensing products have been used with  
280 various methods (Table 4) (Zhang and Christopher 2003; Li et al. 2004; Christopher and Jones 2007; Brindley and  
281 Russell 2009; Yang et al. 2009; Di Biagio et al. 2010; Hansell et al. 2010; Hansell et al. 2012; Song et al. 2018).

282 The instantaneous SW radiative effect efficiency at TOA is obtained from the linear regression of TOA  
283 radiation flux versus AOD observations, although the values in low-dust periods can be substantially influenced by  
284 other types of aerosols such as biomass burning (Li et al. 2004). This radiative effect efficiency corresponds to the  
285 instantaneous value derived under the limited condition at the measurements (e.g., solar position, atmospheric  
286 condition). From the extrapolation of the instantaneous value, the diurnal mean dust SW radiative effect efficiency at  
287 the surface and TOA can be derived based on model calculations.

288 The LW radiative effect efficiency at TOA can be obtained from the linear regression of TOA radiation flux  
289 versus AOD observations over the source regions (Brindley and Russell 2009). However, the observed outgoing LW  
290 radiation is not only dependent on DAOD but also on other factors such as dust layer height, water vapor content, and  
291 other types of aerosols. Thus, the LW radiative effect efficiency is estimated from the difference between observed  
292 outgoing LW radiation and the dust-free outgoing LW radiation, which can be estimated using radiative transfer model  
293 (Song et al., 2018).

294 Consequently, the semi-observationally-based estimates of the dust radiative effect efficiency could be biased,  
295 in part, due to large uncertainties associated with the estimation method, the selection of cloud-free and dust-dominant  
296 data, and dust physicochemical properties. To understand the sensitivity of the dust radiative effect efficiency to the  
297 particle size distribution, asphericity, and refractive index of dust, radiative transfer computations have been carried  
298 out in previous studies (Li et al., 2004; Song et al., 2018). Song et al. (2018) found that the combination of the coarser  
299 dust particle size distribution and the more absorptive LW refractive index (V83) yielded the best simulation of the  
300 dust LW radiative effect in comparison with the satellite flux observations (i.e., CERES), compared to the less  
301 absorptive LW refractive index (DB17).

## 302 **3. Results and Discussions**

303 We evaluate our results from the sensitivity simulations against semi-observationally-based estimates of  
304 DAOD<sub>550</sub> in section 3.1 and radiative effect efficiency for SW and LW in section 3.2 and section 3.3, respectively.  
305 We focus this evaluation on the North Africa and the North Atlantic in boreal summer (June, July, and August) partly

306 because that is the region and season for which most observational constraints on dust radiative effects are available.  
307 The better agreement is obtained for the less absorptive SW (Di Biagio et al., 2019) and the more absorptive LW  
308 (Volz, 1983) dust refractive indices with adjustments of size-resolved dust concentration and particle shape. Our  
309 improved simulation from IMPACT-Sphere-Mineral-V83 (E1) to DustCOMM-Asphere-DB19-V83 (E2)  
310 substantially reduces the model estimates of atmospheric radiative heating by mineral dust near the major source  
311 regions even though it induces only a minor difference in RE at TOA on a global scale (section 3.4). To elucidate the  
312 differences in dust radiative effects between different simulations, the results from the sensitivity simulations in  
313 conjunction with previous modeling studies are analyzed in section 3.5.

### 314 **3.1 Dust load and aerosol optical depth**

315 We compared our model estimates of DAOD<sub>550</sub> against semi-observationally-based data in box plots and  
316 Taylor diagrams (Taylor, 2001) for the evaluation of the various model experiments against semi-observationally-  
317 based estimates (Ridley et al., 2016; Adebisi et al., 2020) to provide a concise statistical summary of the bias,  
318 correlation coefficient, root mean square errors, and the ratio of standard deviation (Fig. 2, Tables S1 and S2).  
319 IMPACT-Sphere-Mineral-V83 (E1) simulations resulted in a significant underestimation of the global and annual  
320 mean of DAOD<sub>550</sub> (0.023) (Fig. 2 and Table 3). The lower DAOD<sub>550</sub> from E2 than E1 was mostly found over East  
321 Asia and Bodele/Sudan in winter (Fig. 2, Table S2). After considering the dust asphericity for spectral optical  
322 properties, we adjusted IMPACT-simulated dust loads against the constraints on dust load from the DustCOMM data  
323 set. This adjustment led the simulated total dust load to increase from 25 Tg (E1) to 32 Tg (E2), which addressed the  
324 issue of coarse dust underestimation and fine dust overestimation by the model (Fig. 3, Table 3). Consequently, the  
325 global and annual mean of DAOD<sub>550</sub> from DustCOMM-Asphere-DB19-V83 (E2) simulation (0.029) fell within the  
326 range in the semi-observationally-based estimate ( $0.030 \pm 0.005$ ) (Ridley et al., 2016) (Table 3). We found that the  
327 agreement in the median with the semi-observationally-based estimate (0.127) was improved from IMPACT-Sphere-  
328 Mineral-DB17 (0.049) to DustCOMM-Asphere-DB19-V83 (0.117) (solid line within the box mark in Fig. 2d). We  
329 also found improvements over East Asia and Bodele/Sudan in winter (Table S2). The better agreement suggested that  
330 DustCOMM-Asphere-DB19-V83 (E2) simulation was reasonably constrained by the DAOD<sub>550</sub> (Ridley et al., 2016;  
331 Adebisi et al., 2020).

### 332 **3.2 Dust SW radiative effect efficiency**

333 Modeled estimates of clear-sky dust SW radiative effect efficiencies ( $W \cdot m^{-2} DAOD_{550}^{-1}$ ) at the surface (Table  
334 S3) and TOA (Table S4) were compared with estimates reported by regional studies based on satellite observations

335 over the North Africa and the North Atlantic (Fig. 4). Comparisons for other regions and seasons were also included  
336 for SW in Figs. 4(g), 4(h), 4(i), and 4(j). Sensitivity simulations demonstrated that the radiative effect efficiency  
337 strongly depended on the particle size, refractive index, and particle shape (Fig. 4). The adjustment of size-resolved  
338 dust concentration and shape with the same refractive index led to overestimates of the SW radiative effect efficiencies  
339 against semi-observationally-based data at TOA (from E1 to E6 in Fig. 4h). Subsequently, the use of less absorptive  
340 SW refractive index with DustCOMM-Asphere-DB19-V83 (E2) simulations led to a better agreement (from E6 to E2  
341 in Fig. 4). On the other hand, the use of much less (10% percentile) absorptive SW refractive index from DustCOMM-  
342 Asphere-Less-More (E7) simulation deteriorated the agreement due to the underestimate of cooling at the surface (Fig.  
343 4g). In contrast, the use of a more absorptive SW refractive index from DustCOMM-Asphere-Mineral-V83 (E6)  
344 improved the agreement at the surface. However, the semi-observationally-based estimates of diurnally averaged  
345 radiative effect efficiency at the surface were derived from extrapolation of the instantaneous values, which would  
346 affect the comparison due to differences in the methodologies between dust models (section 2.6). The differences in  
347 the model-based estimates of radiative effect efficiency might arise from different data sets of the refractive index,  
348 size distribution, and particle shape (Song et al., 2018).

### 349 **3.3 Dust LW radiative effect efficiency**

350 Modeled estimates of clear-sky dust LW (Fig. 5) radiative effect efficiencies ( $\text{W} \cdot \text{m}^{-2} \text{DAOD}_{550}^{-1}$ ) at the surface  
351 (Table S5) and TOA (Table S6) were compared with estimates reported by regional studies based on satellite  
352 observations over North Africa and the North Atlantic. Comparisons for other regions and seasons were also included  
353 for LW Figs. 5(g), 5(h), 5(i), and 5(j). Sensitivity simulations demonstrated that the radiative effect efficiency strongly  
354 depended on the particle size, refractive index, and particle shape (Fig. 5). Both the IMPACT-Sphere-Mineral-V83  
355 (E1) and DustCOMM-Asphere-DB19-V83 (E2) simulations yielded better agreement with semi-observationally-  
356 based data at the surface and TOA, compared to the less absorptive LW dust refractive indices (E3, E4, E5, and E7)  
357 (Fig. 5). The relatively high LW radiative effect efficiencies over western Africa were also consistent with the semi-  
358 observationally-based data. On the other hand, the relatively low LW radiative effect efficiencies were found over  
359 eastern Africa. Moving toward the northeastern side of the region, however, the associated uncertainties in the semi-  
360 observationally-based values increased (Brindley and Russell 2009). The dust LW radiative effect efficiency depends  
361 strongly on the vertical profile of dust concentration, temperature, and water vapor, which would affect the comparison  
362 due to a high variability in these factors (section 2.6).

### 363 **3.4 Atmospheric radiative heating by dust due to coarser size and aspherical shape**

364 The Saharan dust cools the ground surface by reducing the solar radiation reaching the surface and warms the  
365 atmosphere by absorbing solar radiation (Fig. 6). On the other hand, thermal emission by dust warms the surface and  
366 cools the atmosphere (Fig. 7). Our sensitivity simulations showed that the annually averaged net instantaneous  
367 radiative effect due to mineral aerosol (NET) ranged from  $-0.48$  (DustCOMM-Asphere-Less-Less) to  $+0.25$   
368 (DustCOMM-Asphere-Mineral-V83)  $\text{W}\cdot\text{m}^{-2}$  at TOA (Table 5). The net RE from both the IMPACT-Sphere-Mineral-  
369 V83 ( $-0.00 \text{ W}\cdot\text{m}^{-2}$ ) and DustCOMM-Asphere-DB19-V83 ( $-0.08 \text{ W}\cdot\text{m}^{-2}$ ) simulations resulted within 98%  
370 confidential interval of DustCOMM data set ( $-0.27$  to  $0.14 \text{ W}\cdot\text{m}^{-2}$ ).

371 The SW RE by dust outweighs the LW warming effect at the surface in the IMPACT-Sphere-Mineral-V83  
372 (E1) simulation (Fig. 8). Consequently, the highly absorbing dust could play an important role in the aerosol radiative  
373 forcing for the climate models to alter the West African monsoon, with the radiative heating concentrated in the dust  
374 layer (Miller et al., 2004b; Lau et al., 2009). Our model results of dust RE from DustCOMM-Asphere-DB19-V83  
375 (E2) simulation, however, suggested that the surface warming was substantially enhanced near the strong dust source  
376 regions ( $-0.23 \text{ W}\cdot\text{m}^{-2}$  on a global scale) (Fig. 8), compared to the V83 simulation ( $-0.60 \text{ W}\cdot\text{m}^{-2}$  on a global scale).  
377 Thus, our results demonstrated that the atmospheric radiative heating by mineral dust was substantially reduced for  
378 DustCOMM-Asphere-DB19-V83 (E2) simulation ( $0.15 \text{ W}\cdot\text{m}^{-2}$ ), compared to the IMPACT-Sphere-Mineral-V83 (E1)  
379 simulation ( $0.59 \text{ W}\cdot\text{m}^{-2}$ ).

### 380 **3.5 Synergy of coarser size and aspherical shape**

381 To elucidate the differences in dust radiative effects between the IMPACT-Sphere-Mineral-V83 (E1) and  
382 DustCOMM-Asphere-DB19-V83 (E2) simulations (Fig. 9), the differences in annually averaged radiative effects of  
383 mineral dust from DustCOMM-Asphere-DB19-DB17 (E4) simulation were shown in Fig. 10. A slope of one in Fig.  
384 10 represented an identical change in both the surface and TOA and thus corresponded to no change in radiative  
385 heating within the atmosphere. The distances from the DustCOMM-Asphere-DB19-DB17 (E4) simulation  
386 demonstrated that large uncertainties existed for the size distribution and spectral optical properties. Our sensitivity  
387 simulations revealed that the DustCOMM-Asphere-DB19-V83 (E2) simulation led to a similar net RE at TOA to the  
388 IMPACT-Sphere-Mineral-V83 (E1) simulation but resulted in less cooling at the surface (Fig. 9). This revision can  
389 be divided into (1) the size-resolved abundance (black hexagons in Fig. 10), (2) refractive index (red diamonds and  
390 triangles), and (3) particle shape (red circles).

391 First, at TOA, the SW RE was more sensitive to the size-resolved abundance ( $-0.17 \text{ W}\cdot\text{m}^{-2}$  at the vertical axis  
392 of black hexagon in Fig. 10a), compared to LW ( $0.00 \text{ W}\cdot\text{m}^{-2}$  at the vertical axis of black hexagon in Fig. 10b). Second,

393 this less SW cooling effect with coarser dust was partially compensated for by more SW cooling by the less absorptive  
394 SW refractive index ( $0.34 \text{ W}\cdot\text{m}^{-2}$  at the vertical axis of red diamond in Fig. 10a). Thirdly, the sensitivity of SW RE  
395 to dust asphericity was rather minor ( $0.04 \text{ W}\cdot\text{m}^{-2}$  at the vertical axis of red circle in Fig. 10a), partly because the lower  
396 DAOD was compensated for by the lower asymmetry parameter of spherical dust, which enhanced the amount of  
397 radiation scattered backward to space (Räisänen et al., 2013; Colarco et al., 2014). The partial compensation led to a  
398 small enhancement of SW RE for the IMPACT-Sphere-Mineral-V83 (E1) simulation and thus the resulting similar  
399 net RE to DustCOMM-Asphere-DB19-V83 (E2) at TOA (Fig. 9).

400 In contrast, at the surface, our sensitivity simulations demonstrated substantially different responses in the RE,  
401 mostly because of LW warming effects (Fig. 9). The enhanced LW warming by coarser dust ( $-0.08 \text{ W}\cdot\text{m}^{-2}$  at the  
402 horizontal axis of black hexagon in Fig. 10b) was accompanied by the asphericity ( $-0.15 \text{ W}\cdot\text{m}^{-2}$  at the horizontal axis  
403 of red circle in Fig. 10b), because the enhancement of the absorption fraction of extinction due to asphericity was  
404 larger at coarser size. The enhanced LW warming effects of each as well as the synergy was further amplified using  
405 the more absorptive LW dust refractive index (Volz, 1983) (at the horizontal axis of red diamond in Fig. 10b). As a  
406 result, our sensitivity simulations revealed that substantially less dust absorption at LW due to the underestimation of  
407 the coarse dust load and the assumption of the spherical shape (IMPACT-Sphere-Mineral-V83) contributed to the less  
408 surface warming, compared to DustCOMM-Asphere-DB19-V83 (Fig. 9).

409 A relatively good agreement of net RE by dust at TOA with Di Biagio et al. (2020) ( $-0.06 \text{ W}\cdot\text{m}^{-2}$ ) could be  
410 obtained from both the IMPACT-Sphere-Mineral-V83 (E1) and DustCOMM-Asphere-DB19-V83 (E2) simulations  
411 (Fig. 9 and Table 5). On the other hand, our modeled dust net RE at the surface from DustCOMM-Asphere-DB19-  
412 V83 (E2) was much larger than Di Biagio et al. (2020) ( $-0.63 \text{ W}\cdot\text{m}^{-2}$ ) and IMPACT-Sphere-Mineral-V83 (E1). The  
413 synergy of coarser size and aspherical dust could contribute to the less surface warming of the DustCOMM-Asphere-  
414 DB19-V83 (E2). At the same time, the more absorptive LW dust refractive index (V83) than DB17 (red diamond in  
415 Fig. 10b) could also contribute to the less surface warming, which might be partially compensated for in our model  
416 by the omission of dust with diameters in excess of  $20 \mu\text{m}$ . Consequently, our estimate of atmospheric radiative heating  
417 by dust from DustCOMM-Asphere-DB19-V83 (E2) was lower than Di Biagio et al. (2020) ( $0.63 \text{ W}\cdot\text{m}^{-2}$ ) and  
418 IMPACT-Sphere-Mineral-V83 (E1). Additionally, the hot and dry climate over brighter desert surface exaggerates  
419 differences in RE at the surface between the models (Miller et al., 2014). The low humidity allows dust particles to  
420 absorb LW radiation with reduced competition from water vapor, while high temperatures within the boundary layer  
421 increase downward thermal emission by dust (Liao and Seinfeld, 1998). The reduction of fine dust load after the  
422 adjustment leads to underestimates of the SW cooling at TOA. To improve agreement against semi-observationally-  
423 based estimate of the radiative effect efficiency at TOA, the less absorptive SW dust refractive index is required for

424 coarser aspherical dust. Thus, uncertainties in the size-resolved dust concentration, particle shape, and refractive index  
425 contribute to the diversity in the simulated dust RE at the surface.

#### 426 **4. Conclusions**

427 Accurate estimates of the size-resolved dust abundance, their spectral optical properties, and their seasonality  
428 in regional and vertical scales provide a step towards a more reliable projection of the climatic feedback of mineral  
429 aerosols. The radiative effect efficiency depends on numerous variables in model simulations, including the spatial  
430 distribution and temporal variation of size-resolved dust concentrations, the mass extinction coefficient, single  
431 scattering albedo, and asymmetry parameter of dust. Since the models typically underestimate the coarse dust load  
432 and overestimate the fine dust load, the sensitivity to the aerosol absorptivity might be considerably different from  
433 previous studies. Thus, the model results should be re-evaluated against semi-observationally-based estimate of the  
434 DAOD<sub>550</sub> and dust radiative effect efficiency.

435 We improved the accuracy of the simulations by adjusting the bias in size-resolved aspherical dust  
436 concentration with the DustCOMM data set. Alternatively, dust mineralogy might contribute to the underestimation  
437 of modeled aerosol absorption compared to satellite observations (Lacagnina et al., 2015). This enhanced aerosol  
438 absorption was examined by specifying the mineralogy with varying amounts of light-absorbing Fe oxides for SW.  
439 The better agreement with the semi-observationally-based data of dust radiative effect efficiency was obtained using  
440 the less absorptive SW and the more absorptive LW dust refractive indices after the adjustments of dust sizes and  
441 shapes.

442 The diversity of modeled dust net RE at the surface ( $-1.74 \text{ W}\cdot\text{m}^{-2}$  to  $-0.20 \text{ W}\cdot\text{m}^{-2}$ ) is much larger than at TOA  
443 ( $-0.01 \text{ W}\cdot\text{m}^{-2}$  to  $-0.61 \text{ W}\cdot\text{m}^{-2}$ ), partly because the refractive index is optimized to obtain reasonable agreement against  
444 satellite observations of TOA radiation flux (e.g., CERES). The uncertainties in the size-resolved dust concentration,  
445 particle shape, and refractive index contribute to the model diversity at the surface. DustCOMM-Asphere-DB19-V83  
446 (E2) simulation resulted in less cooling at the surface by the synergy of coarser size and aspherical shape, compared  
447 to IMPACT-Sphere-Mineral-V83 (E1) simulation ( $-0.23$  vs.  $-0.88 \text{ W}\cdot\text{m}^{-2}$  on a global scale). Consequently, the  
448 atmospheric heating due to mineral dust was substantially reduced for the DustCOMM-Asphere-DB19-V83 (E2)  
449 simulation ( $0.15 \text{ W}\cdot\text{m}^{-2}$ ), compared to the intensified atmospheric heating from the IMPACT-Sphere-Mineral-V83  
450 (E1) simulation ( $0.59 \text{ W}\cdot\text{m}^{-2}$ ). The less intensified atmospheric heating due to mineral dust could substantially modify  
451 the vertical temperature profile in Earth system models and thus has important implications for the projection of dust  
452 feedback near the major source regions in the past and future climate changes (Kok et al., 2018). More accurate  
453 estimates of semi-observationally-based dust SW and LW radiative effect efficiencies over strong dust source regions  
454 are needed to narrow the uncertainty in the RE.

455 Currently, the model did not include dust particles above 20  $\mu\text{m}$ , but a substantial fraction of airborne dust near  
456 source regions may be above this threshold (Ryder et al., 2019). Moreover, such large particles can be transported to  
457 higher altitudes and longer distances than the model prediction. The higher the dust layer resides, the larger the dust  
458 LW RE at TOA is estimated under the clear-sky conditions (Liao and Seinfeld, 1998). Marine sediment traps, which  
459 are located underneath the main Saharan dust plume in the Atlantic Ocean, suggest that giant particles are dominated  
460 by platy mica and rounded quartz particles (van der Does et al., 2016). Thus, mineral composition of the giant particles  
461 could be different from the aerosol samples generated from soils in the laboratory by Di Biagio et al. (2017), which  
462 may reflect less absorbing LW refractive index of DB17 than V83. Indeed, the dust sample was collected for V83  
463 from rainwater after strong wind. On the other hand, the contribution of the LW scattering might be underestimated  
464 in the models, as Di Biagio et al. (2020) noted that the adjustment factor was estimated for dust of diameter less than  
465 10  $\mu\text{m}$  and thus might be a lower approximation of the LW scattering by coarse dust. Therefore, a better understanding  
466 of the effect of such large particles beyond 20  $\mu\text{m}$  and mineralogical composition on radiation balance remains a topic  
467 of active research, given their potential to amplify the warming of the climate system. In such an extreme case as the  
468 “Godzilla” dust storm over the North Africa and the tropical Atlantic in June 2020 (Francis et al., 2020), the dust  
469 loading could be larger than that examined for this study, and our estimates of the warming effects might be  
470 conservative during such events. However, to keep the giant particles in the atmosphere, the modeled deposition fluxes  
471 should be reduced from the current model. Therefore, models should improve their ability to capture the evolution of  
472 the dust size distribution as the plumes move downwind of the source regions.

#### 473 **Code availability.**

474 The source code of the RRTMG has been obtained from the website at [https://github.com/AER-RC/RRTMG\\_LW](https://github.com/AER-RC/RRTMG_LW) and  
475 [https://github.com/AER-RC/RRTMG\\_SW](https://github.com/AER-RC/RRTMG_SW). The source code of the Kramers-Kronig relations has been obtained from  
476 the website at [https://www.mathworks.com/matlabcentral/fileexchange/8135-tools-for-data-analysis-in-optics-  
477 acoustics-signal-processing](https://www.mathworks.com/matlabcentral/fileexchange/8135-tools-for-data-analysis-in-optics-acoustics-signal-processing). The source code of the Taylor diagram has been obtained from the web site at  
478 <https://www.mathworks.com/matlabcentral/fileexchange/20559-taylor-diagram>.

#### 479 **Data availability.**

480 SMAP data have been obtained from the website at <https://nsidc.org/data/smap/smap-data.html>. MODIS land data  
481 have been retrieved from the website at <https://ladsweb.modaps.eosdis.nasa.gov/>. MERRA-2 data have been provided  
482 by the Global Modeling and Assimilation Office (GMAO) at NASA Goddard Space Flight Center



483 (<https://disc.gsfc.nasa.gov/datasets/>). The DustCOMM data are available at <https://dustcomm.atmos.ucla.edu/>. The  
484 datasets supporting the conclusions of this article are included within the article and its supplement file.

485 **Supplement.**

486 The supplement related to this article is available online at:

487 **Author contributions.**

488 AI and JFK initiated the modeling collaboration with semi-observationally-based data sets. AI carried out the  
489 modeling study. AAA, YH, JFK contributed semi-observationally-based data sets of DustCOMM and asphericity  
490 factor. All authors read and approved the final manuscript.

491 **Competing interests.**

492 The authors declare that they have no competing interests.

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506 **References**

- 507 Adebisi, A. A., Kok, J. F., Wang, Y., Ito, A., Ridley, D. A., Nabat, P., and Zhao, C.: Dust Constraints from joint  
508 Observational-Modelling-experiMental analysis (DustCOMM): comparison with measurements and model  
509 simulations, *Atmos. Chem. Phys.*, 20, 829–863, <https://doi.org/10.5194/acp-20-829-2020>, 2020.
- 510 Adebisi, A. A. and Kok, J. F.: Climate models miss most of the coarse dust in the atmosphere, *Sci. Adv.*, 6, eaaz9507,  
511 <https://doi.org/10.1126/sciadv.aaz9507>, 2020.
- 512 Albani, S., Mahowald, N. M., Perry, A. T., Scanza, R. A., Heavens, N. G., Zender, C. S., Maggi, V., Kok, J. F., and  
513 Otto-Bliesner, B. L.: Improved dust representation in the Community Atmosphere Model. *J. Adv. Model.*  
514 *Earth Syst.*, 6, 541–570, <https://doi.org/10.1002/2013MS000279>, 2014.
- 515 Ansmann, A., Rittmeister, F., Engelmann, R., Basart, S., Jorba, O., Spyrou, C., Remy, S., Skupin, A., Baars, H., Seifert,  
516 P., Senf, F., and Kanitz, T.: Profiling of Saharan dust from the Caribbean to western Africa – Part 2:  
517 Shipborne lidar measurements versus forecasts, *Atmos. Chem. Phys.*, 17, 14987–15006,  
518 <https://doi.org/10.5194/acp-17-14987-2017>, 2017.
- 519 Balkanski, Y., Schulz, M., Claquin, T., and Guibert, S.: Reevaluation of Mineral aerosol radiative forcings suggests a  
520 better agreement with satellite and AERONET data, *Atmos. Chem. Phys.*, 7, 81–95,  
521 <https://doi.org/10.5194/acp-7-81-2007>, 2007.
- 522 Bedidi, A. and Cervelle, B.: Light scattering by spherical particles with hematite and goethitelike optical properties:  
523 effect of water impregnation, *J. Geophys. Res.*, 98, 11941–11952, 1993, <https://doi.org/10.1029/93JB00188>.
- 524 Brindley, H. E. and Russell, J. E.: An assessment of Saharan dust loading and the corresponding cloud-free longwave  
525 direct radiative effect from geostationary satellite observations, *J. Geophys. Res.-Atmos.*, 114, D23201,  
526 <https://doi.org/10.1029/2008jd011635>, 2009.
- 527 Colarco, P. R., Nowotnick, E. P., Randles, C. A., Yi, B. Q., Yang, P., Kim, K. M., Smith, J. A., and Bardeen, C. G.:  
528 Impact of radiatively interactive dust aerosols in the NASA GEOS-5 climate model: Sensitivity to dust  
529 particle shape and refractive index, *J. Geophys. Res.-Atmos.*, 119, 753–786,  
530 <https://doi.org/10.1002/2013JD020046>, 2014.
- 531 Christopher, S. A. and Jones, T.: Satellite-based assessment of cloud-free net radiative effect of dust aerosols over the  
532 Atlantic Ocean, *Geophys. Res. Lett.*, 34, L02810, doi:10.1029/2006GL027783, 2007.
- 533 Di Biagio, C., di Sarra, A., and Meloni, D.: Large atmospheric shortwave radiative forcing by Mediterranean aerosol  
534 derived from simultaneous ground-based and spaceborne observations, and dependence on the aerosol type  
535 and single scattering albedo, *J. Geophys. Res.*, 115, D10209, <https://doi.org/10.1029/2009JD012697>, 2010.

536 Di Biagio, C., Formenti, P., Balkanski, Y., Caponi, L., Cazaunau, M., Pangui, E., Journet, E., Nowak, S., Caquineau,  
537 S., Andreae, M. O., Kandler, K., Saeed, T., Piketh, S., Seibert, D., Williams, E., and Doussin, J.-F.: Global  
538 scale variability of the mineral dust long-wave refractive index: a new dataset of in situ measurements for  
539 climate modeling and remote sensing, *Atmos. Chem. Phys.*, 17, 1901–1929, [https://doi.org/10.5194/acp-17-](https://doi.org/10.5194/acp-17-1901-2017)  
540 1901-2017, 2017.

541 Di Biagio, C., Formenti, P., Balkanski, Y., Caponi, L., Cazaunau, M., Pangui, E., Journet, E., Nowak, S., Andreae, M.  
542 O., Kandler, K., Saeed, T., Piketh, S., Seibert, D., Williams, E., and Doussin, J.-F.: Complex refractive  
543 indices and single-scattering albedo of global dust aerosols in the shortwave spectrum and relationship to  
544 size and iron content, *Atmos. Chem. Phys.*, 19, 15503–15531, <https://doi.org/10.5194/acp-19-15503-2019>,  
545 2019.

546 Di Biagio, C., Balkanski, Y., Albani, S., Boucher, O., and Formenti, P.: Direct radiative effect by mineral dust aerosols  
547 constrained by new microphysical and spectral optical data. *Geophys. Res. Lett.*, 47, e2019GL086186,  
548 <https://doi.org/10.1029/2019GL086186>, 2020.

549 Dufresne, J., Gautier, C., Ricchizzi, P., and Fouquart, Y.: Longwave scattering effects of mineral aerosols, *J. Atmos.*  
550 *Sci.*, 59(12), 1959–1966, 2002, [https://doi.org/10.1175/1520-0469\(2002\)059<1959:LSEOMA>2.0.CO;2](https://doi.org/10.1175/1520-0469(2002)059<1959:LSEOMA>2.0.CO;2).

551 Feng, Y. and Penner, J. E.: Global modeling of nitrate and ammonium: Interaction of aerosols and tropospheric  
552 chemistry, *J. Geophys. Res.*, 112, D01304, doi:10.1029/2005JD006404, 2007.

553 Francis, D., Fonseca, R., Nelli, N., Cuesta, J., Weston, M., Evan, A., and Temimi, M.: The atmospheric drivers of the  
554 major Saharan dust storm in June 2020. *Geophys. Res. Lett.*, 47, e2020GL090102,  
555 <https://doi.org/10.1029/2020GL090102>, 2020.

556 Friedl, M. and Sulla-Menashe, D.: MCD12Q1 MODIS/Terra+Aqua Land Cover Type Yearly L3 Global 500m SIN  
557 Grid V006 [Data set]. NASA EOSDIS Land Processes DAAC,  
558 <https://doi.org/10.5067/MODIS/MCD12Q1.006>, 2019.

559 Gelaro, R., McCarty, W., Suárez, M. J., Todling, R., Molod, A., Takacs, L., Randles, C. A., Darmenov, A., Bosilovich,  
560 M. G., Reichle, R., Wargan, K., Coy, L., Cullather, R., Draper, C., Akella, S., Buchard, V., Conaty, A., da  
561 Silva, A. M., Gu, W., Kim, G.-K., Koster, R., Lucchesi, R., Merkova, D., Nielsen, J. E., Partyka, G., Pawson,  
562 S., Putman, W., Rienecker, M., Schubert, S. D., Sienkiewicz, M., and Zhao, B.: The Modern-Era  
563 Retrospective Analysis for Research and Applications, Version 2 (MERRA-2), *J. Climate*, 30, 5419–5454  
564 <https://doi.org/10.1175/JCLI-D-16-0758.1>, 2017,.

565 Gettelman, A., Liu, X., Ghan, S. J., Morrison, H., Park, S., Conley, A. J., Klein, S. A., Boyle, J., Mitchell, D. L., and  
566 Li, J. L. F.: Global simulations of ice nucleation and ice supersaturation with an improved cloud scheme in

567 the Community Atmosphere Model, *J. Geophys. Res.*, 115, D18216, <https://doi.org/10.1029/2009jd013797>,  
568 2010.

569 Harrison, R. G., Nicoll, K. A., Marlton, G. J., Ryder, C. L., and Bennett, A. J.: Saharan dust plume charging observed  
570 over the UK, *Environ. Res. Lett.*, 13, 054018, <https://doi.org/10.1088/1748-9326/aabcd9>, 2018.

571 Hansell, R. A., Tsay, S., Hsu, N. C., Ji, Q., Bell, S.W., Brent, N. H., Welton, E. J., Roush, T. L., Zhang, W., Huang,  
572 J., Li Z. Q., and Chen, H.: An assessment of the surface longwave direct radiative effect of airborne dust in  
573 Zhangye, China, during the Asian Monsoon Years field experiment (2008), *J. Geophys. Res.*, 117, D00K39,  
574 <https://doi.org/10.1029/2011JD017370>, 2012.

575 Hansell, R. A., Tsay, S. C., Ji, Q., Hsu, N. C., Jeong, M. J., Wang, S. H., Reid, J. S., Liou, K. N., and Ou, S. C.: An  
576 assessment of the surface longwave direct radiative effect of airborne saharan dust during the NAMMA field  
577 campaign, *J. Atmos. Sci.* 67, 1048–1065, doi:10.1175/2009JAS3257.1, 2010.

578 Heald, C. L., Ridley, D. A., Kroll, J. H., Barrett, S. R. H., Cady-Pereira, K. E., Alvarado, M. J., and Holmes, C. D.:  
579 Contrasting the direct radiative effect and direct radiative forcing of aerosols, *Atmos. Chem. Phys.*, 14, 5513–  
580 5527, <https://doi.org/10.5194/acp-14-5513-2014>, 2014.

581 Huang, Y., Kok, J. F., Kandler, K., Lindqvist, H., Nousiainen, T., Sakai, T., Adebisi, A., and Jokinen, O.: Climate  
582 Models and Remote Sensing Retrievals Neglect Substantial Desert Dust Asphericity, *Geophys. Res. Lett.*,  
583 47, e2019GL086592, <https://doi.org/10.1029/2019GL086592>, 2020a.

584 Huang, Y., Adebisi, A., and Kok, J. 2020b, Linking the different diameter types of aspherical desert dust indicates  
585 that models underestimate coarse dust emission, American Geophysical Union, Fall Meeting 2020, abstract  
586 A007-0016, doi: 10.1002/essoar.10504925.1.

587 Hoshyaripour, G. A., Bachmann, V., Förstner, J., Steiner, A., Vogel, H., Wagner, F., Walter, C., and Vogel, B.: Effects  
588 of Particle Nonsphericity on Dust Optical Properties in a Forecast System: Implications for Model-  
589 Observation Comparison, *J. Geophys. Res.-Atmos.*, 124, 2018JD030228,  
590 <https://doi.org/10.1029/2018JD030228>, 2019.

591 Iacono, M. J., Delamere, J. S., Mlawer, E. J., Shephard, M. W., Clough, S. A., and Collins, W. D.: Radiative forcing  
592 by long-lived greenhouse gases: Calculations with the AER radiative transfer models, *J. Geophys. Res.*, 113,  
593 D13103, <https://doi.org/10.1029/2008JD009944>, 2008.

594 Ito, A. and Feng, Y.: Role of dust alkalinity in acid mobilization of iron, *Atmos. Chem. Phys.*, 10, 9237–9250,  
595 <https://doi.org/10.5194/acp-10-9237-2010>, 2010.

596 Ito, A. and Shi, Z.: Delivery of anthropogenic bioavailable iron from mineral dust and combustion aerosols to the  
597 ocean, *Atmos. Chem. Phys.*, 16, 85–99, <https://doi.org/10.5194/acp-16-85-2016>, 2016.

598 Ito, A. and Kok, J. F.: Do dust emissions from sparsely vegetated regions dominate atmospheric iron supply to the  
599 Southern Ocean?, *J. Geophys. Res.-Atmos.*, 122, 3987–4002, <https://doi.org/10.1002/2016JD025939>, 2017.

600 Ito, A., Lin, G., and Penner, J. E.: Radiative forcing by lightabsorbing aerosols of pyrogenetic iron oxides, *Sci. Rep.-*  
601 *UK*, 8, 7347, <https://doi.org/10.1038/s41598-018-25756-3>, 2018.

602 Ito, A., Myriokefalitakis, S., Kanakidou, M., Mahowald, N. M., Scanza, R. A., Hamilton, D. S., Baker, A. R., Jickells,  
603 T., Sarin, M., Bikkina, S., Gao, Y., Shelley, R. U., Buck, C. S., Landing, W. M., Bowie, A. R., Perron, M.  
604 M. G., Guieu, C., Meskhidze, N., Johnson, M. S., Feng, Y., Kok, J. F., Nenes, A., and Duce, R. A.: Pyrogenic  
605 iron: The missing link to high iron solubility in aerosols, *Sci. Adv.*, 5, eaau7671,  
606 <https://doi.org/10.1126/sciadv.aau7671>, 2019.

607 Ito, A., Perron, M. M. G., Proemse, B. C., Strzelec, M., Gault-Ringold, M., Boyd, P. W., and Bowie, A. R.: Evaluation  
608 of aerosol iron solubility over Australian coastal regions based on inverse modeling: implications of bushfires  
609 on bioaccessible iron concentrations in the Southern Hemisphere, *Prog. Earth Planet. Sci.*, 7, 42,  
610 <https://doi.org/10.1186/s40645-020-00357-9>, 2020.

611 Ito, A., Ye, Y., Baldo, C., and Shi, Z.: Ocean fertilization by pyrogenic aerosol iron, *npj Clim. Atmos. Sci.*, 4, 30,  
612 <https://doi.org/10.1038/s41612-021-00185-8>, 2021.

613 Journet, E., Balkanski, Y., and Harrison, S. P.: A new data set of soil mineralogy for dust-cycle modeling, *Atmos.*  
614 *Chem. Phys.*, 14, 3801–3816, <https://doi.org/10.5194/acp-14-3801-2014>, 2014.

615 Kok, J. F.: A scaling theory for the size distribution of emitted dust aerosols suggests climate models underestimate  
616 the size of the global dust cycle, *P. Natl. Acad. Sci. USA*, 108, 1016–1021,  
617 <https://doi.org/10.1073/pnas.1014798108>, 2011.

618 Kok, J. F., Parteli, E. J. R., Michaels, T. I., and Karam, D. B.: The physics of wind-blown sand and dust, *Rep. Prog.*  
619 *Phys.*, 75, 106901, doi:10.1088/0034-4885/75/10/106901, 2012.

620 Kok, J. F., Mahowald, N. M., Fratini, G., Gillies, J. A., Ishizuka, M., Leys, J. F., Mikami, M., Park, M.-S., Park, S.-  
621 U., Van Pelt, R. S., and Zobeck, T. M.: An improved dust emission model – Part 1: Model description and  
622 comparison against measurements, *Atmos. Chem. Phys.*, 14, 13023–13041, [https://doi.org/10.5194/acp-14-](https://doi.org/10.5194/acp-14-13023-2014)  
623 [13023-2014](https://doi.org/10.5194/acp-14-13023-2014), 2014.

624 Kok, J. F., Ridley, D. A., Zhou, Q., Miller, R. L., Zhao, C., Heald, C. L., Ward, D. S., Albani, S., and Haustein, K.:  
625 Smaller desert dust cooling effect estimated from analysis of dust size and abundance, *Nat. Geosci.*, 10, 274–  
626 278, <https://doi.org/10.1038/ngeo2912>, 2017.

627 Kok, J. F., Ward, D. S., Mahowald, N. M., and Evan, A. T.: Global and regional importance of the direct dust-climate  
628 feedback, *Nat. Commun.*, 9, 241, <https://doi.org/10.1038/s41467-017-02620-y>, 2018.

629 Kok, J. F., Adebisi, A. A., Albani, S., Balkanski, Y., Checa-Garcia, R., Chin, M., Colarco, P. R., Hamilton, D. S.,  
630 Huang, Y., Ito, A., Klose, M., Leung, D. M., Li, L., Mahowald, N. M., Miller, R. L., Obiso, V., Pérez García-  
631 Pando, C., Rocha-Lima, A., Wan, J. S., and Whicker, C. A.: Improved representation of the global dust cycle  
632 using observational constraints on dust properties and abundance, *Atmos. Chem. Phys.*, 21, 8127–8167,  
633 <https://doi.org/10.5194/acp-21-8127-2021>, 2021.

634 Lacagnina, C., Hasekamp, O. P., Bian, H., Curci, G., Myhre, G., van Noije, T., Schulz, M., Skeie, R. B., Takemura,  
635 T., and Zhang, K.: Aerosol single-scattering albedo over the global oceans: Comparing PARASOL retrievals  
636 with AERONET, OMI, and AeroCom models estimates, *J. Geophys. Res.*, 120, 9814–9836,  
637 <https://doi.org/10.1002/2015JD023501>, 2015.

638 Laskin, A., Iedema, M. J., Ichkovich, A., Graber, E. R., Taraniukb, I., and Yinon, R.: Direct observation of completely  
639 processed calcium carbonate dust particles, *Faraday Discuss.*, 130, 453–468,  
640 <https://doi.org/10.1039/B417366J>, 2005.

641 Lau, K. M., Kim, K. M., Sud, Y. C., and Walker, G. K.: A GCM study of the response of the atmospheric water cycle  
642 of West Africa and the Atlantic to Saharan dust radiative forcing, *Ann. Geophys.*, 27, 4023–4037,  
643 <https://doi.org/10.5194/angeo-27-4023-2009>, 2009.

644 Li, F., Vogelmann, A. M., and Ramanathan, V.: Dust aerosol radiative forcing measured from space over the Western  
645 Africa, *J. Climate*, 17(13), 2558–2571, [https://doi.org/10.1175/1520-0442\(2004\)017<2558:SDARFM>2.0.CO;2](https://doi.org/10.1175/1520-0442(2004)017<2558:SDARFM>2.0.CO;2), 2004.

647 Li, L., and Sokolik, I. N.: The dust direct radiative impact and its sensitivity to the land surface state and key minerals  
648 in the WRF-Chem-DuMo model: A case study of dust storms in Central Asia, *J. Geophys. Res.-Atmos.*, 123,  
649 4564–4582, <https://doi.org/10.1029/2017JD027667>, 2018.

650 Liao, H. and Seinfeld, J.: Radiative forcing by mineral dust aerosols: sensitivity to key variables, *J. Geophys. Res.*,  
651 103, 31637–31645, <https://doi.org/10.1029/1998JD200036>, 1998.

652 Liu, X. H., Penner, J. E. and Herzog, M.: Global modeling of aerosol dynamics: Model description, evaluation, and  
653 interactions between sulfate and nonsulfate aerosols, *J. Geophys. Res.*, 110, D18206,  
654 [doi:10.1029/2004jd005674](https://doi.org/10.1029/2004jd005674), 2005.

655 Long, L. L., Querry, M. R., Bell, R. J., and Alexander, R. W.: Optical properties of calcite and gypsum in crystalline  
656 and powdered form in the infrared and far-infrared, *Infrared Phys.*, 34, 191–201,  
657 [https://doi.org/10.1016/0020-0891\(93\)90008-U](https://doi.org/10.1016/0020-0891(93)90008-U), 1993.

658 Lucarini, V., Saarinen, J. J., Peiponen, K.-E., and Vartiainen, E. M.: *Kramers-Kronig relations in optical materials*  
659 research, vol. 110, Switzerland: Springer Science & Business Media, 2005.

660 Mahowald, N., Albani, S., Kok, J. F., Engelstaeder, S., Scanza, R., Ward, D. S., and Flanner, M. G.: The size  
661 distribution of desert dust aerosols and its impact on the Earth system, *Aeolian Res.*, 15, 53–71, 2014,  
662 <https://doi.org/10.1016/j.aeolia.2013.09.002>, 2014.

663 Matsuki, A., Iwasaka, Y., Shi, G., Zhang, D., Trochkin, D., Yamada, M., Kim, Y.-S., Chen, B., Nagatani, T.,  
664 Miyazawa, T., Nagatani, M., and Nakata, H.: Morphological and chemical modification of mineral dust:  
665 Observational insight into the heterogeneous uptake of acidic gases, *Geophys. Res. Lett.*, 32, L22806,  
666 <https://doi.org/10.1029/2005gl024176>, 2005.

667 Meinshausen, M., Vogel, E., Nauels, A., Lorbacher, K., Meinshausen, N., Etheridge, D. M., Fraser, P. J., Montzka, S.  
668 A., Rayner, P. J., Trudinger, C. M., Krummel, P. B., Beyerle, U., Canadell, J. G., Daniel, J. S., Enting, I. G.,  
669 Law, R. M., Lunder, C. R., O'Doherty, S., Prinn, R. G., Reimann, S., Rubino, M., Velders, G. J. M., Vollmer,  
670 M. K., Wang, R. H. J., and Weiss, R.: Historical greenhouse gas concentrations for climate modelling  
671 (CMIP6), *Geosci. Model Dev.*, 10, 2057–2116, <https://doi.org/10.5194/gmd-10-2057-2017>, 2017.

672 Meng, Z., Yang, P., Kattawar, G. W., Bi, L., Liou, K. N., and Laszlo, I.: Single-scattering properties of tri-axial  
673 ellipsoidal mineral dust aerosols: a database for application to radiative transfer calculations, *J. Aerosol Sci.*,  
674 41, 501–512, <https://doi.org/10.1016/j.jaerosci.2010.02.008>, 2010.

675 Miller, R. L. and Tegen, I.: Climate response to soil dust aerosols, *J. Climate*, 11, 3247–3267,  
676 [https://doi.org/10.1175/1520-0442\(1998\)011<3247:CRTSDA>2.0.CO;2](https://doi.org/10.1175/1520-0442(1998)011<3247:CRTSDA>2.0.CO;2), 1998.

677 Miller, R. L., Perlwitz, J., and Tegen, I.: Feedback upon dust emission by dust radiative forcing through the planetary  
678 boundary layer, *J. Geophys. Res.*, 109, D24209, doi:10.1029/2004JD004912, 2004a.

679 Miller, R. L., Tegen, I., and Perlwitz, J.: Surface radiative forcing by soil dust aerosols and the hydrologic cycle, *J.*  
680 *Geophys. Res.*, 109, D04203, <https://doi.org/10.1029/2003JD004085>, 2004b.

681 Miller, R. L., Knippertz, P., Pérez García-Pando, C., Perlwitz, J. P., and Tegen, I.: Impact of dust radiative forcing  
682 upon climate, in: *Mineral Dust: A Key Player in the Earth System*, edited by: Knippertz, P. and Stuut, J.-B.  
683 W., Springer, 327–357, doi:10.1007/978-94-017-8978-3\_13, 2014.

684 Myriokefalitakis, S., Ito, A., Kanakidou, M., Nenes, A., Krol, M. C., Mahowald, N. M., Scanza, R. A., Hamilton, D.  
685 S., Johnson, M. S., Meskhidze, N., Kok, J. F., Guieu, C., Baker, A. R., Jickells, T. D., Sarin, M. M., Bikkina,  
686 S., Shelley, R., Bowie, A., Perron, M. M. G., and Duce, R. A.: Reviews and syntheses: the GESAMP  
687 atmospheric iron deposition model intercomparison study, *Biogeosciences*, 15, 6659–6684,  
688 <https://doi.org/10.5194/bg-15-6659-2018>, 2018.

689 Penner, J. E., Zhou, C., Garnier, A., and Mitchell, D. L.: Anthropogenic aerosol indirect effects in cirrus clouds. *J.*  
690 *Geophys. Res.*, 123, 11,652–11,677. <https://doi.org/10.1029/2018JD029204>, 2018.

691 Penner, J.: Soot, sulfate, dust and the climate—Three ways through the fog. *Nature*, 570, 158–159,  
692 <https://doi.org/10.1038/d41586-019-01791-6>, 2019.

693 Perlwitz, J., Tegen, I., and Miller, R.: Interactive soil dust aerosol model in the GISS GCM 1. Sensitivity of the soil  
694 dust cycle to radiative properties of soil dust aerosols, *J. Geophys. Res.*, 106(D16), 18,167–18,192,  
695 <https://doi.org/10.1029/2000JD900668>, 2001

696 Räisänen, P., Haapanala, P., Chung, C. E., Kahnert, M., Makkonen, R., Tonttila, J., and Nousiainen, T.: Impact of  
697 dust particle nonsphericity on climate simulations, *Q. J. Roy. Meteor. Soc.*, 139, 2222–2232,  
698 <https://doi.org/10.1002/qj.2084>, 2013.

699 Reichle, R. H., de Lannoy, G., Koster, R. D., Crow, W. T., Kimball, J. S., and Liu, Q.: SMAP L4 global 3-hourly 9  
700 km EASE-grid surface and root zone soil moisture geophysical data, version 4. NASA National Snow and  
701 Ice Data Center Distributed Active Archive Center, <https://doi.org/10.5067/kpjnn2gi1dqr>, 2018.

702 Reichle, R. H., Liu, Q., Koster, R. D., Crow, W. T., De Lannoy, G. J. M., Kimball, J. S., Ardizzone, J. V., Bosch, D.,  
703 Colliander, A., Cosh, M., Kolassa, J., Mahanama, S. P., Prueger, J., Starks, P., and Walker, J. P.: Version 4  
704 of the SMAP Level-4 Soil Moisture algorithm and data product. *J. Adv. Model Earth Syst.*, 11, 3106–3130,  
705 <https://doi.org/10.1029/2019MS001729>, 2019.

706 Reid, E. A., Reid, J. S., Meier, M. M., Dunlap, M. R., Cliff, S. S., Broumas, A., Perry, K., and Maring, H.:  
707 Characterization of African dust transported to Puerto Rico by individual particle and size segregated bulk  
708 analysis, *J. Geophys. Res.*, 108, 8591, <https://doi.org/10.1029/2002JD002935>, D19, 2003.

709 Ridley, D. A., Heald, C. L., Kok, J. F., and Zhao, C.: An observationally constrained estimate of global dust aerosol  
710 optical depth, *Atmos. Chem. Phys.*, 16, 15097–15117, <https://doi.org/10.5194/acp-16-15097-2016>, 2016.

711 Rosenberg, P. D., Parker, D. J., Ryder, C. L., Marsham, J. H., Garcia-Carreras, L., Dorsey, J. R., Brooks, I. M., Dean,  
712 A. R., Crosier, J., McQuaid, J. B., and Washington, R.: Quantifying particle size and turbulent scale  
713 dependence of dust flux in the Sahara using aircraft measurements, *J. Geophys. Res.-Atmos.*, 119, 7577–  
714 7598, <https://doi.org/10.1002/2013JD021255>, 2014.

715 Ryder, C. L., Highwood, E. J., Lai, T. M., Sodemann, H., and Marsham, J. H.: Impact of atmospheric transport on the  
716 evolution of microphysical and optical properties of Saharan dust, *Geophys. Res. Lett.*, 40, 2433–2438,  
717 <https://doi.org/10.1002/grl.50482>, 2013.

718 Ryder, C. L., Highwood, E. J., Walser, A., Seibert, P., Philipp, A., and Weinzierl, B.: Coarse and giant particles are  
719 ubiquitous in Saharan dust export regions and are radiatively significant over the Sahara, *Atmos. Chem.*  
720 *Phys.*, 19, 15353–15376, <https://doi.org/10.5194/acp-19-15353-2019>, 2019.



721 Sicard, M., Bertolín, S., Mallet, M., Dubuisson, P., and Comerón, A.: Estimation of mineral dust long-wave radiative  
722 forcing: sensitivity study to particle properties and application to real cases in the region of Barcelona, *Atmos.*  
723 *Chem. Phys.*, 14, 9213–9231, <https://doi.org/10.5194/acp-14-9213-2014>, 2014.

724 Sokolik, I. N., Toon, O. B., and Bergstrom, R. W.: Modeling the radiative characteristics of airborne mineral aerosols  
725 at infrared wavelengths, *J. Geophys. Res.*, 103, 8813–8826, <https://doi.org/10.1029/98JD00049>, 1998.

726 Sokolik, I. N. and Toon, O. B.: Incorporation of mineralogical composition into models of the radiative properties of  
727 mineral aerosol from UV to IR wavelengths, *J. Geophys. Res.*, 104(D8), 9423–9444,  
728 <https://doi.org/10.1029/1998JD200048>, 1999.

729 Song, Q., Zhang, Z., Yu, H., Kato, S., Yang, P., Colarco, P., Remer, L. A., and Ryder, C. L.: Net radiative effects of  
730 dust in the tropical North Atlantic based on integrated satellite observations and in situ measurements, *Atmos.*  
731 *Chem. Phys.*, 18, 11303–11322, <https://doi.org/10.5194/acp-18-11303-2018>, 2018.

732 Stegmann, P. G. and Yang, P.: A regional, size-dependent, and causal effective medium model for Asian and Saharan  
733 mineral dust refractive index spectra, *J. Aerosol Sci.*, 114, 327–341,  
734 <https://doi.org/10.1016/j.jaerosci.2017.10.003>, 2017.

735 Takemura, T., Egashira, M., Matsuzawa, K., Ichijo, H., O'ishi, R., and Abe-Ouchi, A.: A simulation of the global  
736 distribution and radiative forcing of soil dust aerosols at the Last Glacial Maximum, *Atmos. Chem. Phys.*, 9,  
737 3061–3073, <https://doi.org/10.5194/acp-9-3061-2009>, 2009.

738 Tanaka, T. Y., Aoki, T., Takahashi, H., Shibata, K., Uchiyama, A., and Mikami, M.: Study of the sensitivity of optical  
739 properties of mineral dust to the direct aerosol radiative perturbation using a global aerosol transport model,  
740 *SOLA*, 3, 33–36, <https://doi.org/10.2151/sola.2007-009>, 2007.

741 Tegen, I. and Lacis, A.: Modeling of particle size distribution and its influence on the radiative properties of mineral  
742 dust aerosol, *J. Geophys. Res.*, 101, 19237–19244, <https://doi.org/10.1029/95JD03610>, 1996.

743 Toth III, J. R., Rajupet, S., Squire, H., Volbers, B., Zhou, J., Xie, L., Sankaran, R. M., and Lacks, D. J.: Electrostatic  
744 forces alter particle size distributions in atmospheric dust, *Atmos. Chem. Phys.*, 20, 3181–3190,  
745 <https://doi.org/10.5194/acp-20-3181-2020>, 2020.

746 Tuccella, P., Curci, G., Pitari, G., Lee, S., and Jo, D. S.: Direct radiative effect of absorbing aerosols: sensitivity to  
747 mixing state, brown carbon and soil dust refractive index and shape, *J. Geophys. Res.-Atmos.*, 125,  
748 e2019JD030967, <https://doi.org/10.1029/2019JD030967>, 2020.

749 van der Does, M., Korte, L. F., Munday, C. I., Brummer, G.-J. A., and Stuut, J.-B. W.: Particle size traces modern  
750 Saharan dust transport and deposition across the equatorial North Atlantic, *Atmos. Chem. Phys.*, 16, 13697–  
751 13710, <https://doi.org/10.5194/acp-16-13697-2016>, 2016.

752 van der Does, M., Knippertz, P., Zschenderlein, P., Giles Harrison, R., and Stuut, J.-B. W.: The mysterious long-range  
753 transport of giant mineral dust particles, *Sci. Adv.*, 4, eaau2768, <https://doi.org/10.1126/sciadv.aau2768>,  
754 2018.

755 Volz, F.: Infrared optical constants of aerosols at some locations, *Appl. Optics*, 22, 23, 3690–3700,  
756 <https://doi.org/10.1364/AO.11.000755>, 1983.

757 Wagner, R., Ajtai, T., Kandler, K., Lieke, K., Linke, C., Müller, T., Schnaiter, M., and Vragel, M.: Complex refractive  
758 indices of Saharan dust samples at visible and near UV wavelengths: a laboratory study, *Atmos. Chem. Phys.*,  
759 12, 2491–2512, <https://doi.org/10.5194/acp-12-2491-2012>, 2012.

760 Wan, Z., Hook, S., and Hulley, G.: MOD11C2 MODIS/Terra Land Surface Temperature/Emissivity 8-Day L3 Global  
761 0.05Deg CMG V006 [Data set]. NASA EOSDIS Land Processes DAAC,  
762 <https://doi.org/10.5067/MODIS/MOD11C2.006>, 2015.

763 Wang, M. and Penner, J. E.: Aerosol indirect forcing in a global model with particle nucleation, *Atmos. Chem. Phys.*,  
764 9, 239–260, <https://doi.org/10.5194/acp-9-239-2009>, 2009.

765 Wiegner, M., Gasteiger, J., Kandler, K., Weinzierl, B., Rasp, K., Esselborn, M., Freudenthaler, V., Heese, B.,  
766 Toledano, C., Tesche, M., and Althausen, D.: Numerical simulations of optical properties of Saharan dust  
767 aerosols with emphasis on lidar applications, *Tellus B*, 61, 180–194, <https://doi.org/10.1111/j.1600->  
768 0889.2008.00381.x, 2009.

769 Xu, L. and Penner, J. E.: Global simulations of nitrate and ammonium aerosols and their radiative effects, *Atmos.*  
770 *Chem. Phys.*, 12, 9479–9504, <https://doi.org/10.5194/acp-12-9479-2012>, 2012.

771 Yang, E.-S., Gupta, P., and Christopher, S. A.: Net radiative effect of dust aerosols from satellite measurements over  
772 Sahara, *Geophys. Res. Lett.*, 36, L18812, <https://doi.org/10.1029/2009GL039801>, 2009.

773 Yoshioka, M., Mahowald, N., Conley, A. J., Collins, W. D., Fillmore, D.W., Zender, C. S., and Coleman, D. B.:  
774 Impact of desert dust radiative forcing on Sahel precipitation: relative importance of dust compared to sea  
775 surface temperature variations, vegetation changes and greenhouse gas warming, *J. Climate*, 16, 1445–1467,  
776 <https://doi.org/10.1175/JCLI4056.1>, 2007.

777 Zhang, D., and Iwasaka, Y.: Size change of Asian dust particles caused by sea salt interaction: Measurements in  
778 southwestern Japan, *Geophys. Res. Lett.*, 31, L15102, <https://doi.org/10.1029/2004GL020087>, 2004.

779 Zhang, J. and Christopher, S. A.: Longwave radiative forcing of Saharan dust aerosols estimated from MODIS, MISR,  
780 and CERES observations on Terra, *Geophys. Res., Lett.*, 30(23), 2188,  
781 <https://doi.org/10.1029/2003GL018479>, 2003.

782 Zhao, C., Chen, S., Leung, L. R., Qian, Y., Kok, J. F., Zaveri, R. A., and Huang, J.: Uncertainty in modeling dust mass  
783 balance and radiative forcing from size parameterization, *Atmos. Chem. Phys.*, 13, 10733–10753,  
784 <https://doi.org/10.5194/acp-13-10733-2013>, 2013.

785 Zhou, Y., Levy, R. C., Remer, L. A., Mattoo, S., and Espinosa, W. R.: Dust aerosol retrieval over the oceans with the  
786 MODIS/VIIRS dark target algorithm: 2. Nonspherical dust model, *Earth Space Sci.*, 7, e2020EA001222,  
787 <https://doi.org/10.1029/2020EA001222>, 2020.

788 **Figure captions**

789 Figure 1. Imaginary part of the refractive index at SW and LW for the nine main source regions and the global  
790 mean for others. The refractive index obtained from 19 samples was aggregated into 9 main source regions  
791 and the arithmetic mean was calculated for each source region (Di Biagio et al., 2017, 2019). The coordinates  
792 of the nine source regions were: (S1) western North Africa (20°W – 7.5°E; 18°N – 37.5°N), (S2) eastern  
793 North Africa (7.5°E – 35°E; 18°N – 37.5°N), (S3) the Sahel (20°W – 35°E; 0°N – 18°N), (S4) Middle East  
794 / Central Asia (30°E – 70°E for 0°N – 35°N, and 30°E – 75°E for 35°N – 50°N), (S5) East Asia (70°E –  
795 120°E; 35°N – 50°N), (S6) North America (130°W – 80°W; 20°N – 45°N), (S7) Australia (110°E – 160°E;  
796 10°S – 40°S), (S8) South America (80°W – 20°W; 0°S – 60°S), and (S9) Southern Africa (0°E – 40°E; 0°S  
797 – 40°S).

798 Figure 2. The model better reproduced semi-observationally-based data of DAOD<sub>550</sub> after adjusting the size-  
799 resolved dust load with DustCOMM and considering the dust asphericity. (a) semi-observationally-based  
800 estimates of the DAOD<sub>550</sub> were averaged over 2004–2008 (Ridley et al., 2016; Adebisi et al., 2020). The  
801 annually averaged model results were shown for (b) DustCOMM-Asphere-DB19-V83 (E2) and (c) the  
802 differences between IMPACT-Sphere-Mineral-V83 (E1) and E2 simulations. (d) Comparison of seasonally  
803 averaged DAOD<sub>550</sub> for semi-observationally-based (SOB) data, E1, E2, IMPACT-Asphere-DB19-DB17  
804 (E3), and DustCOMM-Sphere-DB19-DB17 (E5). The square symbol represents the mean. The solid line  
805 within the box mark shows the median. The boundaries of the box mark the 25th and 75th percentiles. The  
806 whiskers above and below the box indicate the 1.5 × interquartile range, and the points indicate the outside  
807 of the range. (e) Taylor diagram summarizing the statistics of the comparison against the seasonally averaged  
808 regional DAOD<sub>550</sub> for the different experiments. The horizontal axis shows the standard deviation of the data  
809 set or model prediction, the curved axis shows the correlation, and the green dashed lines denote the root-  
810 mean-squared errors between the semi-observationally-based data and the model predictions. As such, the  
811 distance between the semi-observationally-based data and the model predictions is a measure of the model's  
812 ability to reproduce the spatiotemporal variability in the semi-observationally-based data. The coordinates of  
813 the fifteen regions were: (A1) Mid-Atlantic (4°–40°N, 50°–20°W), (A2) African West Coast (10°–34°N,  
814 20°–5°W), (A3) Northern Africa (26°–40°N, 5°W–30°E), (A4) Mali/Niger (10°–26°N, 5°W–10°E), (A5)  
815 Bodele/Sudan (10°–26°N, 10°–40°E), (A6) Northern Middle East (26°–40°N, 30°–50°E), (A7) Southern  
816 Middle East (0°–26°N, 40°–67.5°E), (A8) Kyzyl Kum (26°–50°N, 50°–67.5°E), (A9) Thar (20°–50°N,  
817 67.5°–75°E), (A10) Taklamakan (30°–50°N, 75°–92.5°E), (A11) Gobi (36°–50°N, 92.5°–115°E), (A12)  
818 North America (20°–45°N, 80°–130°W), (A13) South America (0°–55°S, 80°–55°W), (A14) Southern

819 Africa ( $10^{\circ}$ – $35^{\circ}$ S,  $10^{\circ}$ – $40^{\circ}$ E), and (A15) Australia ( $10^{\circ}$ – $40^{\circ}$ S,  $110^{\circ}$ – $160^{\circ}$ E). The values of  $DAOD_{550}$  at the  
820 15 regions (marked in Fig. 3a) in summer were listed in Table S1. The comparison for other seasons was  
821 presented in Table S2.

822 Figure 3. Model-simulated dust loads at fine (smaller than  $2.5\ \mu\text{m}$  of diameter) and coarse size ranges (larger  
823 than  $2.5\ \mu\text{m}$  of diameter) before and after adjusting the size-resolved dust load with DustCOMM. Results  
824 were shown for (a) fine dust from DustCOMM, (b) fine dust from IMPACT-Sphere-Mineral-V83 (E1), (c)  
825 fine dust from DustCOMM-Asphere-DB19-V83 (E2), (d) coarse dust from DustCOMM, (e) coarse dust from  
826 E1, and (f) coarse dust from E2 simulations. The parentheses represented the global dust burden (Tg). The  
827 values of dust load at each bin were listed in Table 3.

828 Figure 4. Dust clear-sky SW radiative effect efficiency ( $\text{W}\cdot\text{m}^{-2}\ \text{DAOD}^{-1}$ ). Semi-observationally-based data  
829 at (a) the surface and (b) TOA were based on satellite observations (Yang et al. 2009; Li et al., 2004; Song  
830 et al., 2018; Christopher and Jones, 2007). The model results were shown for (c) and (d) IMPACT-Sphere-  
831 Mineral-V83 (E1), and (e) and (f) DustCOMM-Asphere-DB19-V83 (E2) simulations at the surface and TOA,  
832 respectively. (g) Comparison of seasonally averaged SW radiative effect efficiency for semi-observationally-  
833 based (SOB) data and the different experiments. The square symbol represents the mean. The solid line  
834 within the box mark shows the median. The boundaries of the box mark the 25th and 75th percentiles. The  
835 whiskers above and below the box indicate the  $1.5 \times$  interquartile range, and the points indicate the outside  
836 of the range. (h) Taylor diagram summarizing the statistics of the comparison against the seasonally averaged  
837 regional SW radiative effect efficiency for the different experiments. The horizontal axis shows the standard  
838 deviation of the data set or model prediction, the curved axis shows the correlation, and the green dashed  
839 lines denote the root-mean-squared errors between the semi-observationally-based data and the model  
840 predictions. As such, the distance between the semi-observationally-based data and the model predictions is  
841 a measure of the model's ability to reproduce the spatiotemporal variability in the semi-observationally-based  
842 data. The regionally averaged values were listed in Tables S3 and S4 at the surface and TOA, respectively.

843 Figure 5. Dust clear-sky LW radiative effect efficiency ( $\text{W}\cdot\text{m}^{-2}\ \text{DAOD}^{-1}$ ). Semi-observationally-based  
844 estimates at (a) surface and (b) TOA were based on satellite observations (Song et al., 2018; Christopher and  
845 Jones, 2007; Zhang and Christopher, 2003; Brindley and Russell, 2009; Yang et al., 2009). The model results  
846 were shown for (c) and (d) IMPACT-Sphere-Mineral-V83 (E1), and (e) and (f) DustCOMM-Asphere-DB19-  
847 V83 (E2) simulations at the surface and TOA, respectively. (g) Comparison of seasonally averaged LW  
848 radiative effect efficiency for semi-observationally-based (SOB) data and the different experiments. The  
849 square symbol represents the mean. The solid line within the box mark shows the median. The boundaries of

850 the box mark the 25th and 75th percentiles. The whiskers above and below the box indicate the  $1.5 \times$   
851 interquartile range, and the points indicate the outside of the range. (h) Taylor diagram summarizing the  
852 statistics of the comparison against the seasonally averaged regional SW radiative effect efficiency for the  
853 different experiments. The horizontal axis shows the standard deviation of the data set or model prediction,  
854 the curved axis shows the correlation, and the green dashed lines denote the root-mean-squared errors  
855 between the semi-observationally-based data and the model predictions. As such, the distance between the  
856 semi-observationally-based data and the model predictions is a measure of the model's ability to reproduce  
857 the spatiotemporal variability in the semi-observationally-based data. The regionally averaged values were  
858 listed in Tables S5 and S6 at the surface and TOA, respectively.

859 Figure 6. Dust SW radiative effect ( $\text{W}\cdot\text{m}^{-2}$ ) and radiative heating of the atmosphere (i.e., the subtraction of  
860 radiative effects from TOA to the surface in unit of  $\text{W}\cdot\text{m}^{-2}$ ). The model results were shown for the simulations  
861 for (a) IMPACT-Sphere-Mineral-V83 (E1) at the surface, (b) DustCOMM-Asphere-DB19-V83 (E2) at the  
862 surface, (c) E1 in atmospheric column, (d) E2 in atmospheric column, (e) E1 at TOA, and (f) E2 simulations  
863 at TOA. The numbers in parentheses represented the global mean.

864 Figure 7. Dust LW radiative effect ( $\text{W}\cdot\text{m}^{-2}$ ) and radiative heating of the atmosphere (i.e., the subtraction of  
865 radiative effects from TOA to the surface in unit of  $\text{W}\cdot\text{m}^{-2}$ ). The model results were shown for the simulations  
866 for (a) IMPACT-Sphere-Mineral-V83 (E1) at the surface, (b) DustCOMM-Asphere-DB19-V83 (E2) at the  
867 surface, (c) E1 in atmospheric column, (d) E2 in atmospheric column, (e) E1 at TOA, and (f) E2 simulations  
868 at TOA. The numbers in parentheses represented the global mean.

869 Figure 8. Dust radiative effect ( $\text{W}\cdot\text{m}^{-2}$ ) and radiative heating of the atmosphere (i.e., the subtraction of  
870 radiative effects from TOA to the surface in unit of  $\text{W}\cdot\text{m}^{-2}$ ). The model results were shown for the simulations  
871 for (a) IMPACT-Sphere-Mineral-V83 (E1) at the surface, (b) DustCOMM-Asphere-DB19-V83 (E2) at the  
872 surface, (c) E1 in atmospheric column, (d) E2 in atmospheric column, (e) E1 at TOA, and (f) E2 simulations  
873 at TOA. The numbers in parentheses represented the global mean.

874 Figure 9. Radiative effect ( $\text{W}\cdot\text{m}^{-2}$ ) of mineral dust due to different studies at the surface and TOA for (a) total  
875 dust SW, (b) total dust LW, and (c) total dust NET. The annually averaged values were listed in Table 5.

876 Figure 10. Radiative effect ( $\text{W}\cdot\text{m}^{-2}$ ) of mineral dust due to various aerosol absorptivity at the surface and TOA  
877 for (a) total dust SW, (b) total dust LW, and (c) total dust NET. The annually averaged values were listed in  
878 Table 5. The dashed line represented a 1 : 1 correspondence and corresponded to no change in radiative  
879 heating within the atmosphere.

**Table 1.** Summary of ten experiments compared in this study.

Number	Experiment	Size-resolved dust	Sphericity	SW refractive index	LW refractive index
E1	IMPACT-Sphere-Mineral-V83	IMPACT	Spherical	Mineralogical map <sup>d</sup>	Volz (1983)
E2 <sup>a</sup>	DustCOMM-Asphere-DB19-V83	DustCOMM <sup>b</sup>	Aspherical <sup>c</sup>	Di Biagio et al. (2019)	Volz (1983)
E3	IMPACT-Asphere-DB19-DB17	IMPACT	Aspherical <sup>c</sup>	Di Biagio et al. (2019)	Di Biagio et al. (2017)
E4	DustCOMM-Asphere-DB19-DB17	DustCOMM <sup>b</sup>	Aspherical <sup>c</sup>	Di Biagio et al. (2019)	Di Biagio et al. (2017)
E5	DustCOMM-Sphere-DB19-DB17	DustCOMM <sup>b</sup>	Spherical	Di Biagio et al. (2019)	Di Biagio et al. (2017)
E6	DustCOMM-Asphere-Mineral-V83	DustCOMM <sup>b</sup>	Aspherical <sup>c</sup>	Mineralogical map <sup>d</sup>	Volz (1983)
E7	DustCOMM-Asphere-Less-More	DustCOMM <sup>b</sup>	Aspherical <sup>c</sup>	Less SW <sup>e</sup>	More LW <sup>g</sup>
E8	DustCOMM-Asphere-Less-Less	DustCOMM <sup>b</sup>	Aspherical <sup>c</sup>	Less SW <sup>e</sup>	Less LW <sup>h</sup>
E9	DustCOMM-Asphere-More-More	DustCOMM <sup>b</sup>	Aspherical <sup>c</sup>	More SW <sup>f</sup>	More LW <sup>g</sup>
E10	DustCOMM-Asphere-More-Less	DustCOMM <sup>b</sup>	Aspherical <sup>c</sup>	More SW <sup>f</sup>	Less LW <sup>h</sup>

<sup>a</sup>Combination of DustCOMM-Asphere-DB19-DB17 (E4) for SW and DustCOMM-Asphere-Mineral-V83 (E6) for LW.

<sup>b</sup>Size-resolved dust concentration was adjusted with semi-observationally-based estimate (Adebiyi & Kok, 2020).

<sup>c</sup>Dust asphericity was considered in calculating the optical properties, which further assumed internal mixing of minerals (Huang et al., 2020b) using a volume-weighted mixture for each size bin.

<sup>d</sup>Mineralogical composition of dust aerosol for each size was prescribed at emission by mineralogical map (Journet et al., 2014; Ito and Shi 2016). The more absorptive SW refractive indices (Bedidi and Cervelle, 1993; Stegmann & Yang, 2017; Long et al., 1993) were used for mineral dust, compared to the less absorptive global mean data set (Di Biagio et al., 2019).

<sup>e</sup>Less absorptive SW refractive indices were calculated by varying the values of the imaginary parts of the refractive index within the range of values from Di Biagio et al. (2019) (10% percentile).

<sup>f</sup>More absorptive SW refractive indices were calculated by varying the values of the imaginary parts of the refractive index within the range of values from Di Biagio et al. (2019) (90% percentile).

<sup>g</sup>More absorptive LW refractive indices were calculated by varying the values of the imaginary parts of the refractive index within the range of values from Di Biagio et al. (2017) (90% percentile).

<sup>h</sup>Less absorptive LW refractive indices were calculated by varying the values of the imaginary parts of the refractive index within the range of values from Di Biagio et al. (2017) (10% percentile).

**Table 2.** Summary of radiative effects estimated in this study.

SW radiative effect	LW radiative effect	Difference
Less absorptive SW, coarser particle size, & aspherical shape	Coarser particle size & aspherical shape	E2 – E1
Less absorptive SW & aspherical shape	Less absorptive LW & aspherical shape	E3 – E1
Size-resolved dust abundance	Size-resolved dust abundance	E3 – E4
Aspherical shape	Aspherical shape	E5 – E4
Mineralogical variability in refractive index (more absorptive SW)	Mineralogical variability in refractive index (more absorptive LW)	E6 – E4
Less absorptive SW (10% percentile)	More absorptive LW (90% percentile)	E7 – E4
Less absorptive SW (10% percentile)	Less absorptive LW (10% percentile)	E8 – E4
More absorptive SW (90% percentile)	More absorptive LW (90% percentile)	E9 – E4
More absorptive SW (90% percentile)	Less absorptive LW (10% percentile)	E10 – E4



**Table 3.** Annually averages of dust load (Tg), mass extinction efficiency ( $\text{m}^2\cdot\text{g}^{-1}$ ), and  $\text{DAOD}_{550}$  at each bin on a global scale. The size-resolved dust concentration and shape in IMPACT-Sphere-Mineral-V83 (E1) simulation was adjusted to DustCOMM in DustCOMM-Asphere-DB19-V83 (E2) simulation. At the same time, we maintained the consideration of asphericity on the gravitational velocity and kept the dust concentrations unaltered between IMPACT-Sphere-Mineral-V83 (E1) and IMPACT-Asphere-DB19-DB17 simulations (E3).

Dust size bin	Dust load			Mass extinction efficiency				$\text{DAOD}_{550}$			
	E1	E2	DustCOMM	E1	E2	E3	DustCOMM	E1	E2	E3	DustCOMM
Bin 1 <sup>a</sup>	1.2	0.8	$1.2 \pm 0.7$	2.11	3.41	3.33	3.06	0.0050	0.0055	0.0078	0.0070
Bin 2 (1.26–2.5 $\mu\text{m}$ )	4.7	2.6	$3.5 \pm 2.1$	0.73	1.25	1.21	1.22	0.0067	0.0064	0.0111	0.0084
Bin 3 (2.5–5 $\mu\text{m}$ )	8.2	6.2	$6.8 \pm 3.8$	0.37	0.59	0.57	0.57	0.0060	0.0071	0.0092	0.0077
Bin 4 (5–20 $\mu\text{m}$ )	10.9	22.2	$16.8 \pm 9.0$	0.23	0.24	0.29	0.19	0.0050	0.0104	0.0063	0.0063
Sum of 4 bins	25.0	31.8	$28.4 \pm 15.5$	0.46	0.47	0.70	0.53	0.0227	0.0295	0.0345	0.0294

<sup>a</sup>Bin 1 in IMPACT-Sphere-Mineral-V83 (E1) is 0.1–1.26  $\mu\text{m}$ , whereas bin1 in DustCOMM-Asphere-DB19-V83 (E2) and DustCOMM is 0.2–1.26  $\mu\text{m}$ .

**Table 4.** Semi-observationally-based data set of clear-sky dust radiative effect efficiency at the surface and TOA.

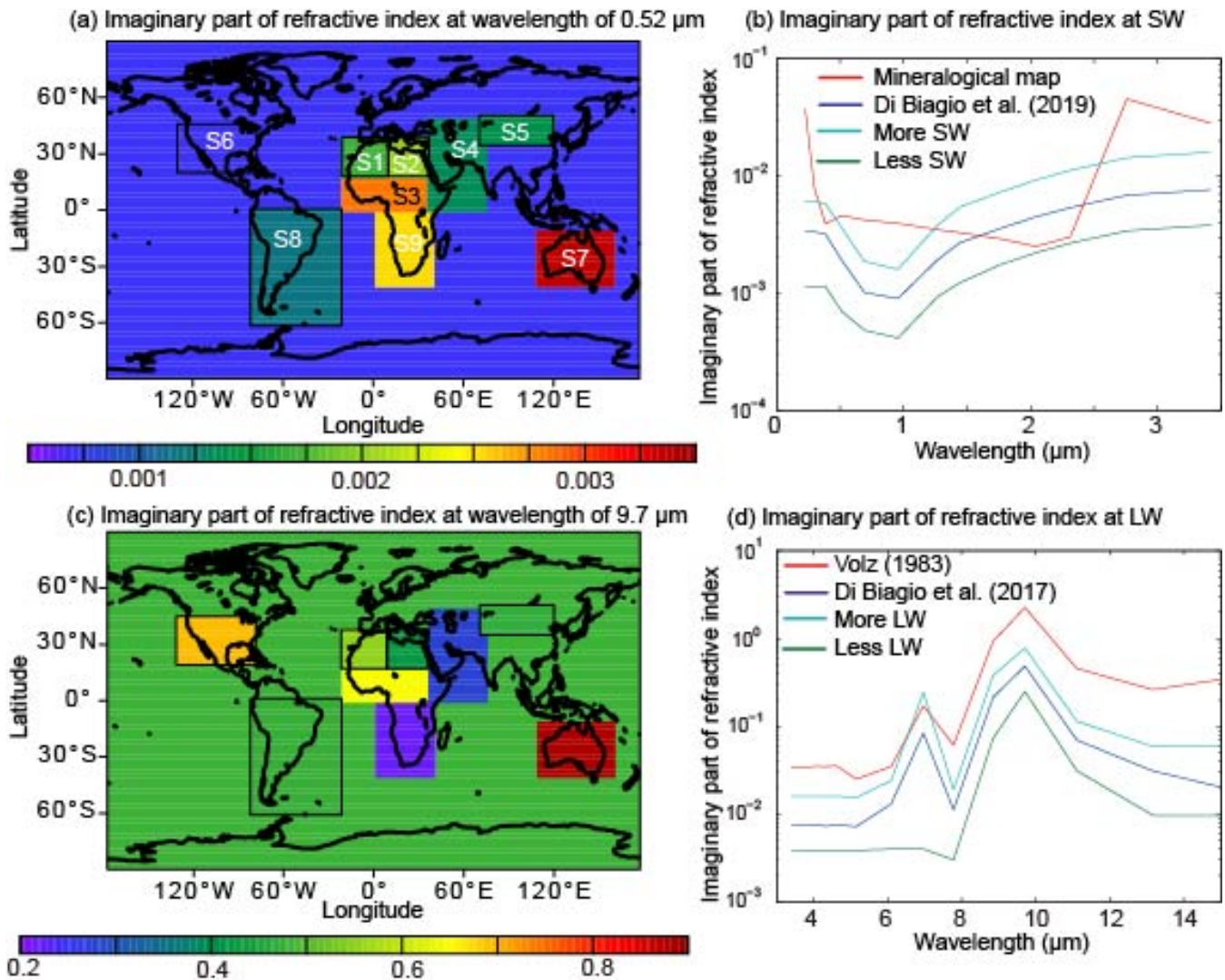
Number	Region name	Season	Region coordinates	Aerosol type selection	AOD data
R1 <sup>a</sup>	Sahara Desert	Summer	15°–30°N, 10°W–30°E	No selection	OMI-MISR
R2 <sup>b</sup>	Tropical Atlantic	Summer	15°–25°N, 45°–15°W	MODIS effective radius peaks 0.8–0.9 $\mu\text{m}$	MODIS
R3 <sup>c</sup>	Tropical Atlantic	Summer	10°–30°N, 45°–20°W	CALIOP dust and polluted dust	CERES-CALIPSO-CloudSat-MODIS
R4 <sup>d</sup>	Atlantic Ocean	Summer	0°–30°N, 60°–10°W	Dust detection based on DAOD <sub>550</sub> and fraction	MODIS
R5 <sup>e,f</sup>	North Africa	Summer	15°–35°N, 18°W–40°E	No selection	MISR <sup>e</sup> or SEVIRI <sup>f</sup>
R6 <sup>e,f</sup>	West Africa	Summer	16°–28°N, 16°–4°W	No selection	MISR <sup>e</sup> or SEVIRI <sup>f</sup>
R7 <sup>e,f</sup>	Niger-Chad	Summer	15°–20°N, 15°–22°E	No selection	MISR <sup>e</sup> or SEVIRI <sup>f</sup>
R8 <sup>e,f</sup>	Sudan	Summer	15°–22°N, 22°–36°E	No selection	MISR <sup>e</sup> or SEVIRI <sup>f</sup>
R9 <sup>e,f</sup>	Egypt-Israel	Summer	23°–32°N, 23°–35°E	No selection	MISR <sup>e</sup> or SEVIRI <sup>f</sup>
R10 <sup>e,f</sup>	North Libya	Summer	27°–33°N, 15°–25°E	No selection	MISR <sup>e</sup> or SEVIRI <sup>f</sup>
R11 <sup>e,f</sup>	South Libya	Summer	23°–27°N, 15°–25°E	No selection	MISR <sup>e</sup> or SEVIRI <sup>f</sup>
R12 <sup>g</sup>	Mediterranean	Summer	35.5°N, 12.6°E	Dust detection based on optical property	Ground-based measurements
R13 <sup>h</sup>	Cape Verde	Summer	16.7°N, 22.9°E	Dust detection based on brightness temperature	Ground-based measurements
R14 <sup>i</sup>	China	Spring	39°N, 101°E	Dust detection based on brightness temperature	Ground-based measurements

<sup>a</sup>Yang et al. (2009). <sup>b</sup>Li et al. (2004). <sup>c</sup>Song et al. (2018). <sup>d</sup>Christopher and Jones (2007). <sup>e</sup>Zhang and Christopher (2003). <sup>f</sup>Brindley and Russell (2009). <sup>g</sup>Di Biagio et al. (2010). <sup>h</sup>Hansell et al. (2010). <sup>i</sup>Hansell et al. (2012).

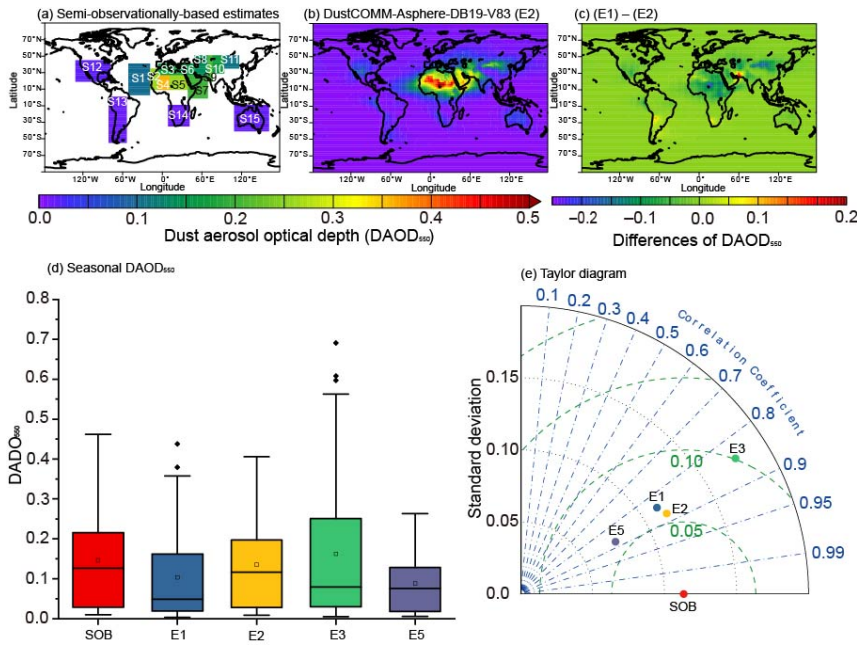
**Table 5.** Annually averages of short-wave (SW) ( $W \cdot m^{-2}$ ), long-wave (LW) ( $W \cdot m^{-2}$ ), and net radiative effect (NET) ( $W \cdot m^{-2}$ ) at the surface, TOA, and atmospheric radiative heating on a global scale.

Number	Data	Total dust SW		Total dust LW		Total dust NET	
		TOA (surface) <sup>a</sup>	Atmosphere	TOA (surface) <sup>a</sup>	Atmosphere	TOA (surface) <sup>a</sup>	Atmosphere
E1	IMPACT-Sphere-Mineral-V83	-0.18 (-1.26)	1.07	+0.18 (0.66)	-0.48	-0.00 (-0.60)	0.59
E2	DustCOMM-Asphere-DB19-V83	<b>-0.32 (-1.23)<sup>b</sup></b>	<b>0.91<sup>b</sup></b>	<b>+0.23 (1.00)<sup>b</sup></b>	<b>-0.77<sup>b</sup></b>	<b>-0.08 (-0.23)<sup>b</sup></b>	<b>0.15<sup>b</sup></b>
E3	IMPACT-Asphere-DB19-DB17	-0.49 (-1.35)	0.86	+0.12 (0.50)	-0.38	-0.37 (-0.84)	0.48
E4	DustCOMM-Asphere-DB19-DB17	<b>-0.32 (-1.23)<sup>b</sup></b>	<b>0.91<sup>b</sup></b>	+0.12 (0.58)	-0.46	-0.20 (-0.65)	0.45
E5	DustCOMM-Sphere-DB19-DV17	-0.28 (-0.90)	0.62	+0.08 (0.43)	-0.34	-0.20 (-0.47)	0.28
E6	DustCOMM-Asphere-Mineral-V83	+0.02 (-1.61)	1.63	<b>+0.23 (1.00)<sup>b</sup></b>	<b>-0.77<sup>b</sup></b>	+0.25 (-0.62)	0.87
E7	DustCOMM-Asphere-Less-More	-0.54 (-0.98)	0.43	+0.16 (0.76)	-0.60	-0.38 (-0.22)	-0.16
E8	DustCOMM-Asphere-Less-Less	-0.54 (-0.98)	0.43	+0.06 (0.35)	-0.29	-0.48 (-0.36)	0.15
E9	DustCOMM-Asphere-More-More	-0.08 (-1.51)	1.43	+0.16 (0.76)	-0.60	+0.09 (-0.75)	0.84
E10	DustCOMM-Asphere-More-Less	-0.08 (-1.51)	1.43	+0.06 (0.35)	-0.29	-0.01 (-1.16)	1.15
	DustCOMM (Adebisi & Kok, 2020)	-0.59 to 0.17 <sup>c</sup>		+0.25 to 0.41 <sup>c</sup>		-0.27 to 0.14 <sup>c</sup>	
M1	Miller et al. (2004b)	-0.33 (-1.82)	1.49	+0.15 (0.18)	-0.03	-0.18 (-1.64)	1.46
M2	Tanaka et al. (2007)	-0.38 (-1.22)	0.84	+0.16 (0.57)	-0.41	-0.22 (-0.65)	0.43
M3	Yoshioka et al. (2007)	-0.92 (-1.59)	0.67	+0.31 (1.13)	-0.81	-0.60 (-0.46)	-0.14
M4	Takemura et al. (2009)	-0.10 (-0.38)	0.28	+0.09 (0.18)	-0.09	-0.01 (-0.20)	0.19
M5	Albani et al. (2014)	-0.38 (-1.20)	0.81	+0.15 (0.64)	-0.49	-0.23 (-0.56)	0.33
M6	Colarco et al. (2014)	-0.32 (-1.25)	0.93	+0.05 (0.30)	-0.25	-0.27 (-0.95)	0.68
M7	Di Biagio et al. (2020)	-0.29 (-1.17) <sup>d</sup>	0.88 <sup>d</sup>	+0.23 (0.48) <sup>d</sup>	-0.26 <sup>d</sup>	-0.06 (-0.69) <sup>d</sup>	0.63 <sup>d</sup>

<sup>a</sup>The parentheses represent the RE at the surface. <sup>b</sup>The bold represents the combination of DB19 for SW and V83 for LW (i.e., DustCOMM-Asphere-DB19-V83). <sup>c</sup>98% confidential interval of DustCOMM data set is listed. <sup>d</sup>For a comparison with our estimates, sum of single mode simulations from Di Biagio et al. (2019) is listed.



**Figure 1.** Imaginary part of the refractive index at SW and LW for the nine main source regions and the global mean for others. The refractive index obtained from 19 samples was aggregated into 9 main source regions and the arithmetic mean was calculated for each source region (Di Biagio et al., 2017, 2019). The coordinates of the nine source regions were: (S1) western North Africa (20°W – 7.5°E; 18°N – 37.5°N), (S2) eastern North Africa (7.5°E – 35°E; 18°N – 37.5°N), (S3) the Sahel (20°W – 35°E; 0°N – 18°N), (S4) Middle East / Central Asia (30°E – 70°E for 0°N – 35°N, and 30°E – 75°E for 35°N – 50°N), (S5) East Asia (70°E – 120°E; 35°N – 50°N), (S6) North America (130°W – 80°W; 20°N – 45°N), (S7) Australia (110°E – 160°E; 10°S – 40°S), (S8) South America (80°W – 20°W; 0°S – 60°S), and (S9) Southern Africa (0°E – 40°E; 0°S – 40°S).



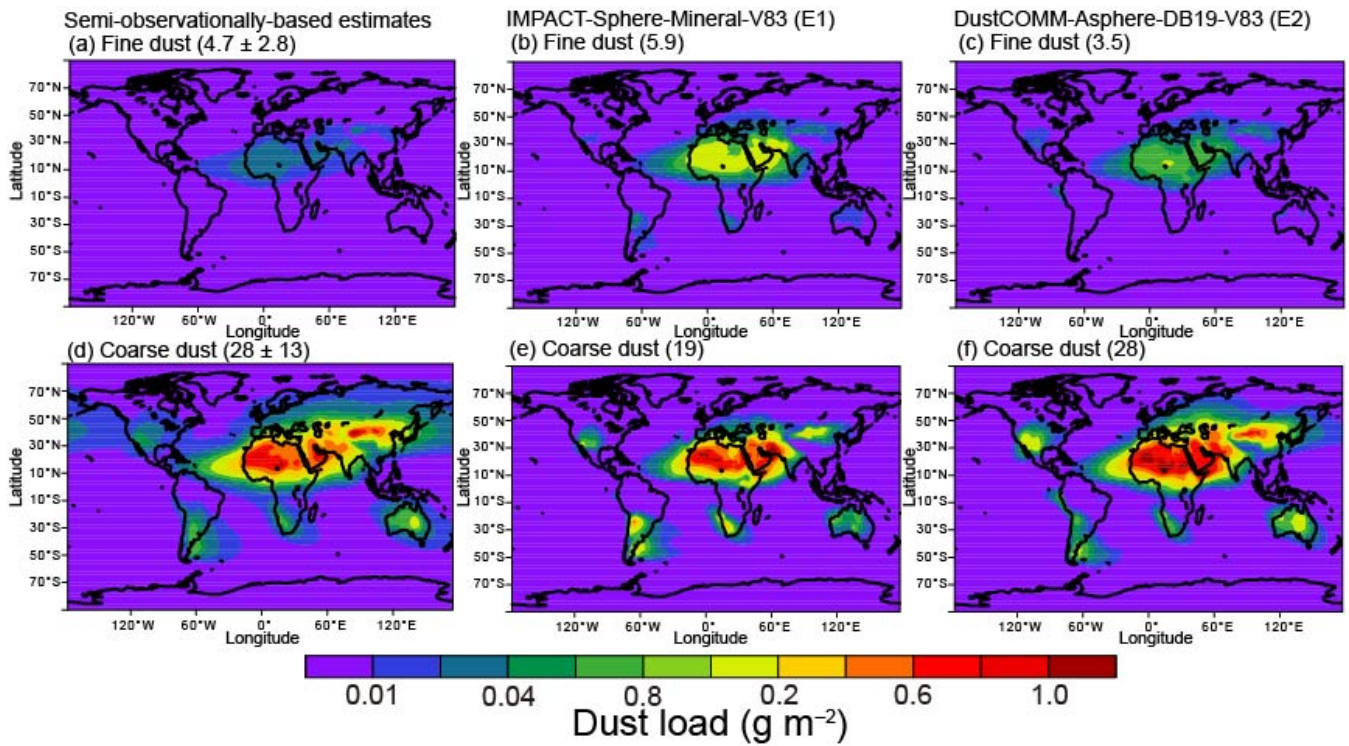
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**Figure 2.** The model better reproduced semi-observationally-based data of  $DAOD_{550}$  after adjusting the size-resolved dust load with DustCOMM and considering the dust asphericity. (a) semi-observationally-based estimates of the  $DAOD_{550}$  were averaged over 2004–2008 (Ridley et al., 2016; Adebisi et al., 2020). The annually averaged model results were shown for (b) DustCOMM-Asphere-DB19-V83 (E2) and (c) the differences between IMPACT-Sphere-Mineral-V83 (E1) and E2 simulations. (d) Comparison of seasonally averaged  $DAOD_{550}$  for semi-observationally-based (SOB) data, E1, E2, IMPACT-Asphere-DB19-DB17 (E3), and DustCOMM-Sphere-DB19-DB17 (E5). The square symbol represents the mean. The solid line within the box mark shows the median. The boundaries of the box mark the 25th and 75th percentiles. The whiskers above and below the box indicate the  $1.5 \times$  interquartile range, and the points indicate the outside of the range. (e) Taylor diagram summarizing the statistics of the comparison against the seasonally averaged regional  $DAOD_{550}$  for the different experiments.

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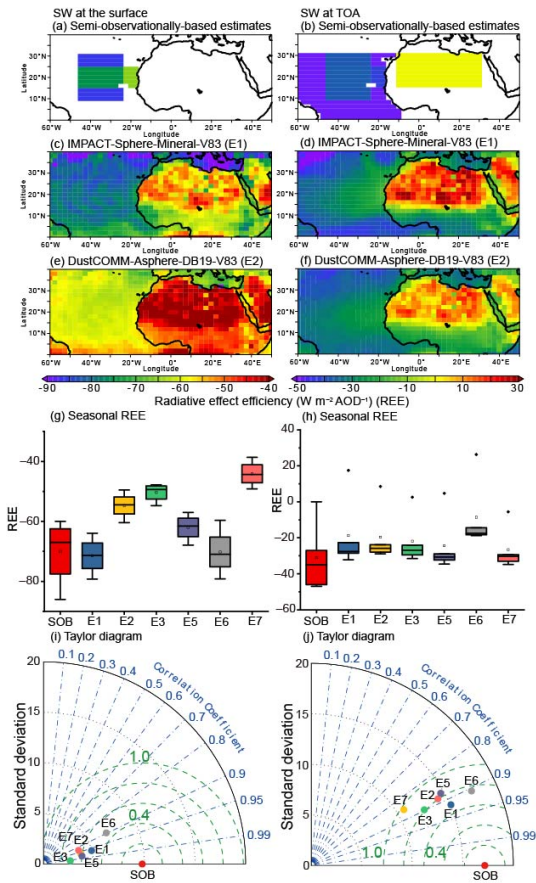
The horizontal axis shows the standard deviation of the data set or model prediction, the curved axis shows the correlation, and the green dashed lines denote the root-mean-squared errors between the semi-observationally-based data and the model predictions. As such, the distance between the semi-observationally-based data and the model predictions is a measure of the model's ability to reproduce the spatiotemporal variability in the semi-observationally-based data. The coordinates of the fifteen regions were: (A1) Mid-Atlantic ( $4^{\circ}$ – $40^{\circ}$ N,  $50^{\circ}$ – $20^{\circ}$ W), (A2) African West Coast ( $10^{\circ}$ – $34^{\circ}$ N,  $20^{\circ}$ – $5^{\circ}$ W), (A3) Northern Africa ( $26^{\circ}$ – $40^{\circ}$ N,  $5^{\circ}$ W– $30^{\circ}$ E), (A4) Mali/Niger ( $10^{\circ}$ – $26^{\circ}$ N,  $5^{\circ}$ W– $10^{\circ}$ E), (A5) Bodele/Sudan ( $10^{\circ}$ – $26^{\circ}$ N,  $10^{\circ}$ – $40^{\circ}$ E), (A6) Northern Middle East ( $26^{\circ}$ – $40^{\circ}$ N,  $30^{\circ}$ – $50^{\circ}$ E), (A7) Southern Middle East ( $0^{\circ}$ – $26^{\circ}$ N,  $40^{\circ}$ – $67.5^{\circ}$ E), (A8) Kyzyl Kum ( $26^{\circ}$ – $50^{\circ}$ N,  $50^{\circ}$ – $67.5^{\circ}$ E), (A9) Thar ( $20^{\circ}$ – $50^{\circ}$ N,  $67.5^{\circ}$ – $75^{\circ}$ E), (A10) Taklamakan ( $30^{\circ}$ – $50^{\circ}$ N,  $75^{\circ}$ – $92.5^{\circ}$ E), (A11) Gobi ( $36^{\circ}$ – $50^{\circ}$ N,  $92.5^{\circ}$ – $115^{\circ}$ E), (A12) North America ( $20^{\circ}$ – $45^{\circ}$ N,  $80^{\circ}$ – $130^{\circ}$ W), (A13) South America ( $0^{\circ}$ – $55^{\circ}$ S,  $80^{\circ}$ – $55^{\circ}$ W), (A14) Southern Africa ( $10^{\circ}$ – $35^{\circ}$ S,  $10^{\circ}$ – $40^{\circ}$ E), and (A15) Australia ( $10^{\circ}$ – $40^{\circ}$ S,  $110^{\circ}$ – $160^{\circ}$ E). The values of  $DAOD_{550}$  at the 15 regions (marked in Fig. 2a) in summer were listed in Table S1. The comparison for other seasons was presented in Table S2.

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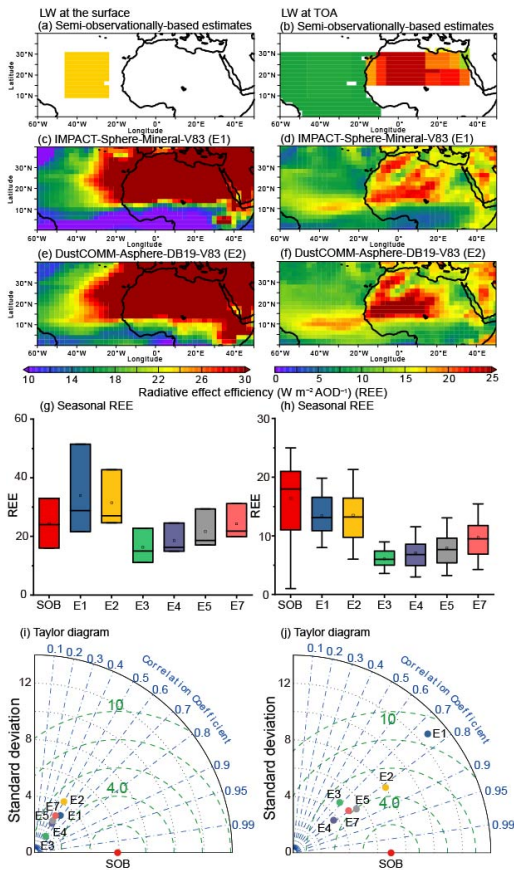


**Figure 3.** Model-simulated dust loads at fine (smaller than 2.5  $\mu\text{m}$  of diameter) and coarse size ranges (larger than 2.5  $\mu\text{m}$  of diameter) before and after adjusting the size-resolved dust load with DustCOMM. Results were shown for (a) fine dust from DustCOMM, (b) fine dust from IMPACT-Sphere-Mineral-V83 (E1), (c) fine dust from DustCOMM-Asphere-DB19-V83 (E2),  
 35 (d) coarse dust from DustCOMM, (e) coarse dust from E1, and (f) coarse dust from E2 simulations. The parentheses represented the global dust burden ( $T_g$ ). The values of dust load at each bin were listed in Table 3.



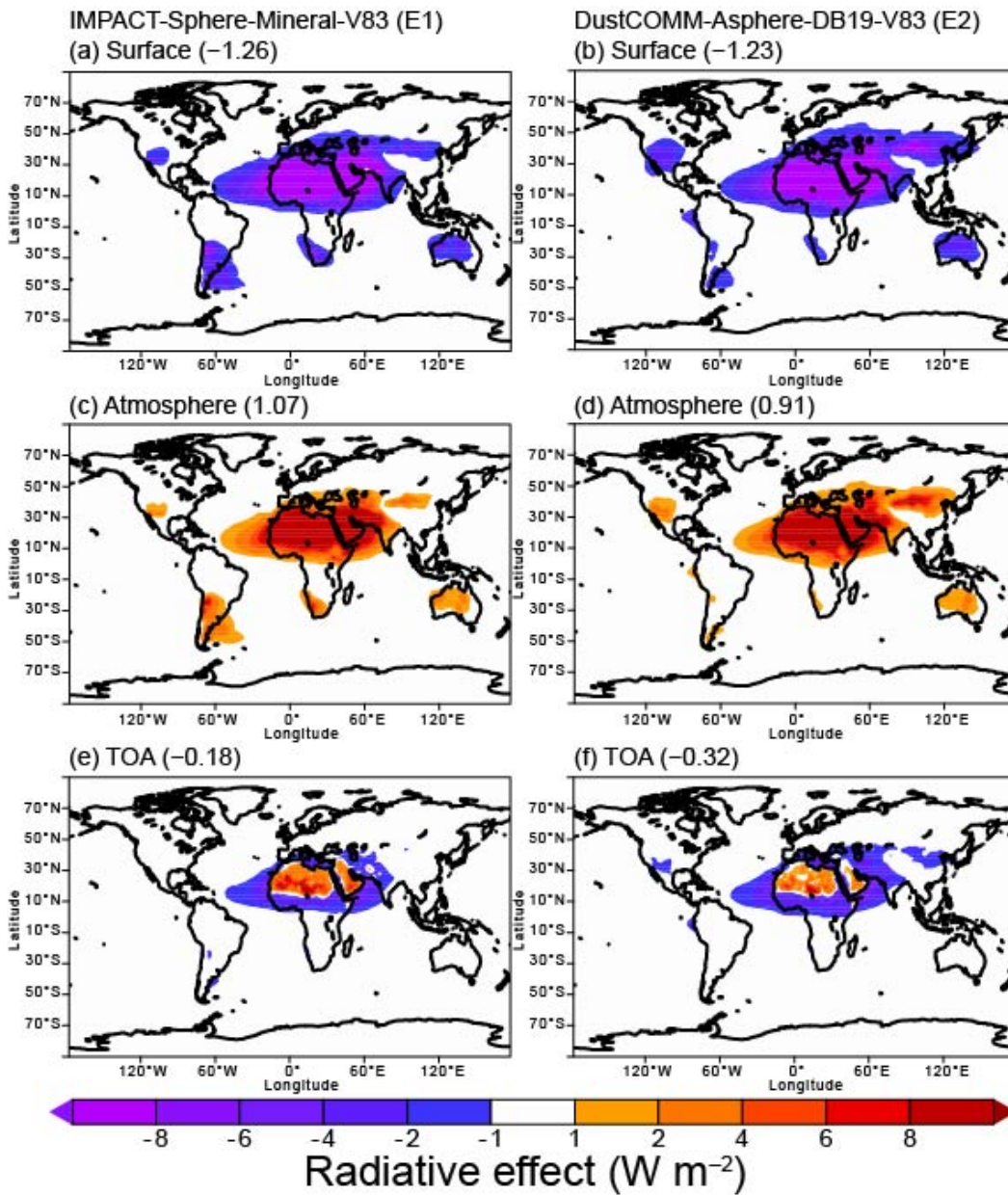


**Figure 4.** Dust clear-sky SW radiative effect efficiency ( $\text{W}\cdot\text{m}^{-2}\text{ DAOD}^{-1}$ ). Semi-observationally-based data at (a) the surface and (b) TOA were based on satellite observations (Yang et al. 2009; Li et al., 2004; Song et al., 2018; Christopher and Jones, 2007). The model results were shown for (c) and (d) IMPACT-Sphere-Mineral-V83 (E1), and (e) and (f) DustCOMM-Asphere-DB19-V83 (E2) simulations at the surface and TOA, respectively. (g) Comparison of seasonally averaged SW radiative effect efficiency for semi-observationally-based (SOB) data and the different experiments. The square symbol represents the mean. The solid line within the box mark shows the median. The boundaries of the box mark the 25th and 75th percentiles. The whiskers above and below the box indicate the  $1.5 \times$  interquartile range, and the points indicate the outside of the range. (h) Taylor diagram summarizing the statistics of the comparison against the seasonally averaged regional SW radiative effect efficiency for the different experiments. The horizontal axis shows the standard deviation of the data set or model prediction, the curved axis shows the correlation, and the green dashed lines denote the root-mean-squared errors between the semi-observationally-based data and the model predictions. As such, the distance between the semi-observationally-based data and the model predictions is a measure of the model's ability to reproduce the spatiotemporal variability in the semi-observationally-based data. The regionally averaged values were listed in Tables S3 and S4 at the surface and TOA, respectively.

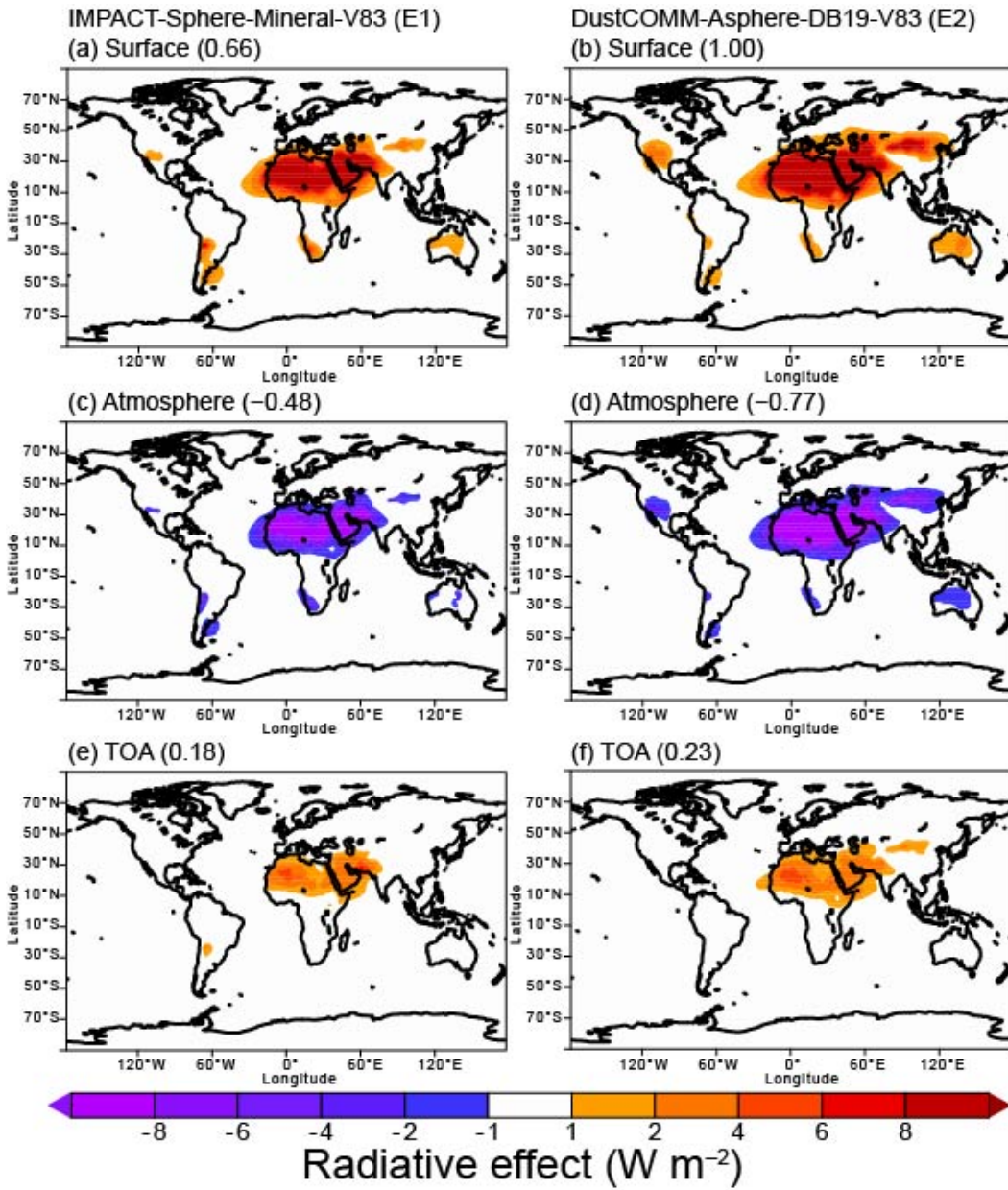


**Figure 5.** Dust clear-sky LW radiative effect efficiency ( $\text{W} \cdot \text{m}^{-2} \text{ DAOD}^{-1}$ ). Semi-observationally-based estimates at (a) surface and (b) TOA were based on satellite observations (Song et al., 2018; Christopher and Jones, 2007; Zhang and Christopher, 2003; Brindley and Russell, 2009; Yang et al., 2009). The model results were shown for (c) and (d) IMPACT-Sphere-Mineral-V83 (E1), and (e) and (f) DustCOMM-Asphere-DB19-V83 (E2) simulations at the surface and TOA, respectively. (g) Comparison of seasonally averaged LW radiative effect efficiency for semi-observationally-based (SOB) data and the different experiments. The square symbol represents the mean. The solid line within the box mark shows the median. The boundaries of the box mark the 25th and 75th percentiles. The whiskers above and below the box indicate the  $1.5 \times$  interquartile range, and the points indicate the outside of the range. (h) Taylor diagram summarizing the statistics of the comparison against the seasonally averaged regional SW radiative effect efficiency for the different experiments. The horizontal axis shows the standard deviation of the data set or model prediction, the curved axis shows the correlation, and the green dashed lines denote the root-mean-squared errors between the semi-observationally-based data and the model predictions. As such, the distance between the semi-observationally-based data and the model predictions is a measure of the model's ability to reproduce the spatiotemporal variability in the semi-observationally-based data. The regionally averaged values were listed in Tables S5 and S6 at the surface and TOA, respectively.





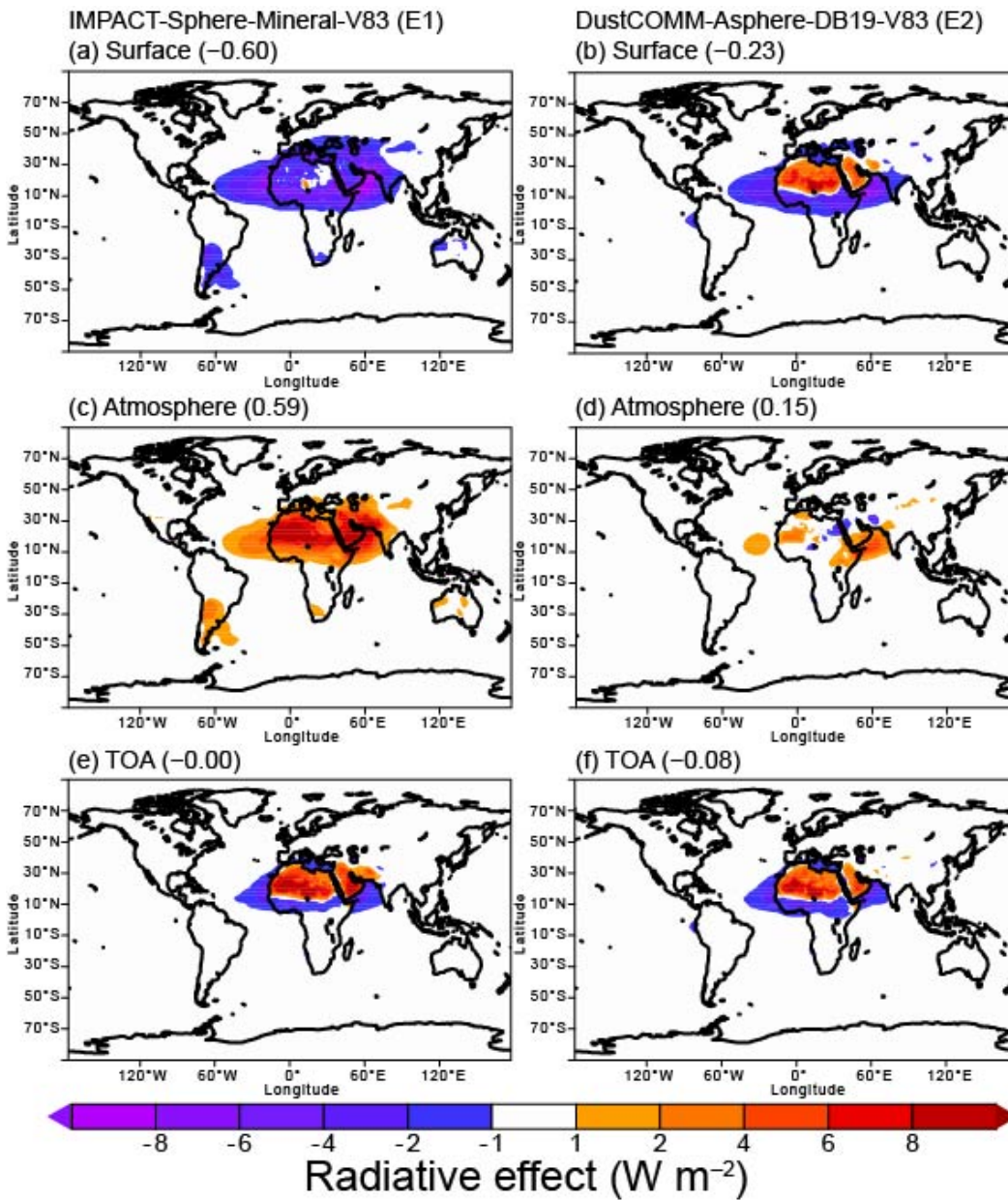
**Figure 6.** Dust SW radiative effect ( $\text{W}\cdot\text{m}^{-2}$ ) and radiative heating of the atmosphere (i.e., the subtraction of radiative effects from TOA to the surface in unit of  $\text{W}\cdot\text{m}^{-2}$ ). The model results were shown for the simulations for (a) IMPACT-Sphere-Mineral-V83 (E1) at the surface, (b) DustCOMM-Asphere-DB19-V83 (E2) at the surface, (c) E1 in atmospheric column, (d) E2 in atmospheric column, (e) E1 at TOA, and (f) E2 simulations at TOA. The numbers in parentheses represented the global mean.



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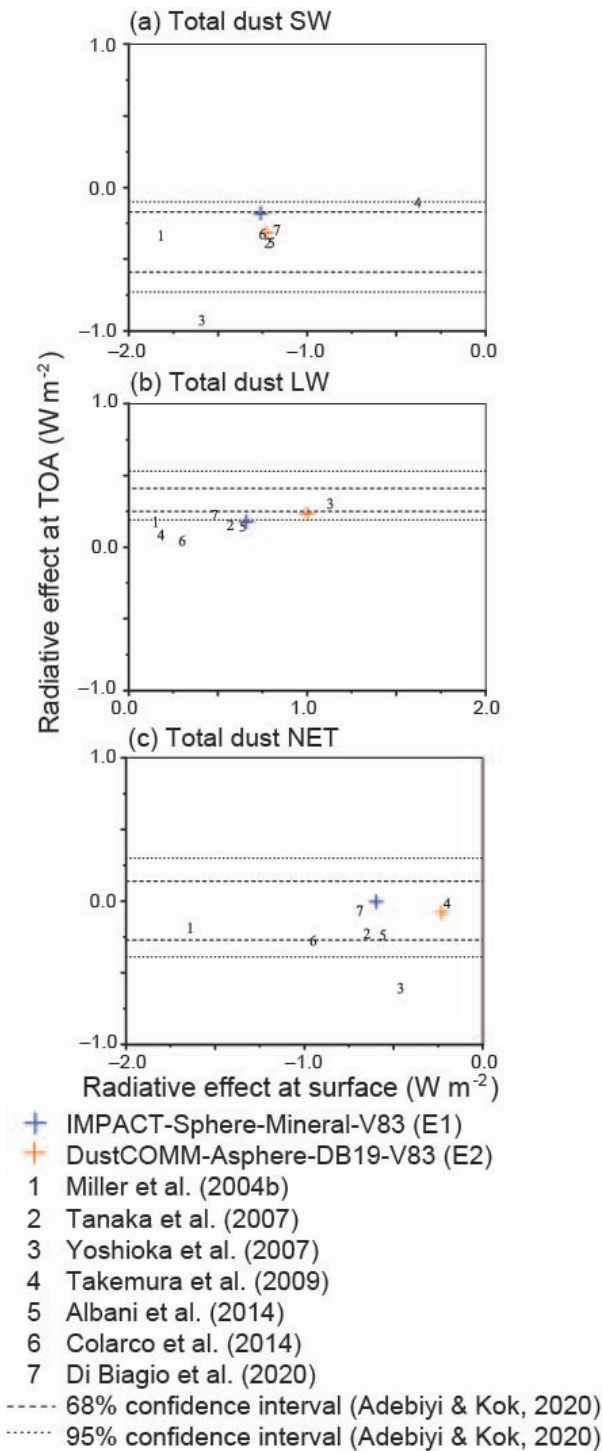
**Figure 7.** Dust LW radiative effect ( $\text{W}\cdot\text{m}^{-2}$ ) and radiative heating of the atmosphere (i.e., the subtraction of radiative effects from TOA to the surface in unit of  $\text{W}\cdot\text{m}^{-2}$ ). The model results were shown for the simulations for (a) IMPACT-Sphere-Mineral-V83 (E1) at the surface, (b) DustCOMM-Asphere-DB19-V83 (E2) at the surface, (c) E1 in atmospheric column, (d) E2 in atmospheric column, (e) E1 at TOA, and (f) E2 simulations at TOA. The numbers in parentheses represented the global

80 mean.

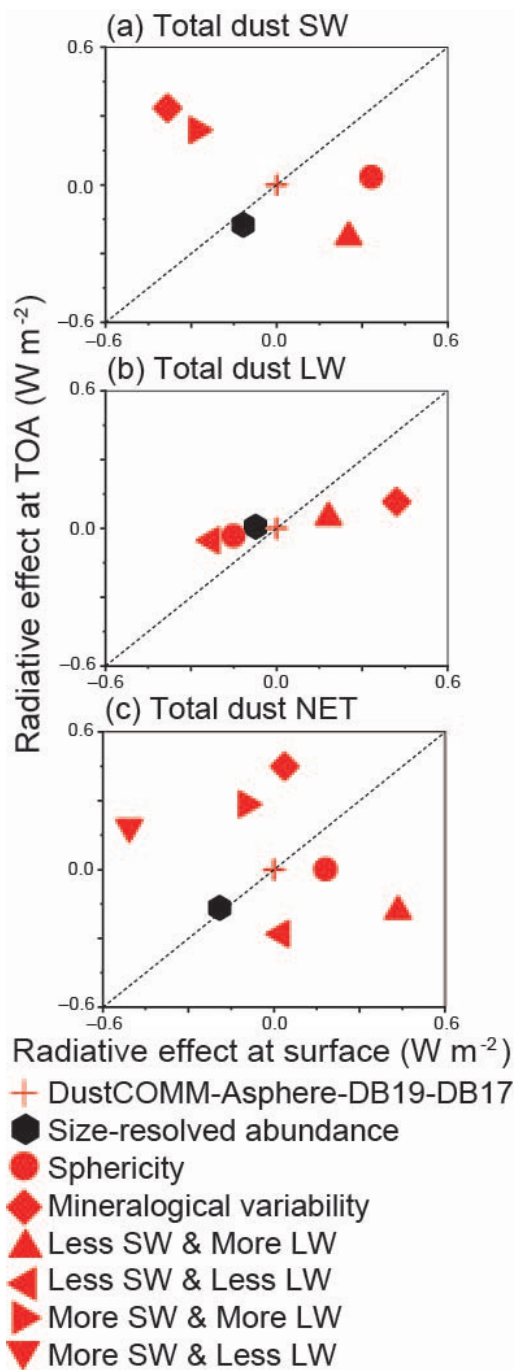


**Figure 8.** Dust radiative effect ( $\text{W} \cdot \text{m}^{-2}$ ) and radiative heating of the atmosphere (i.e., the subtraction of radiative effects from TOA to the surface in unit of  $\text{W} \cdot \text{m}^{-2}$ ). The model results were shown for the simulations for (a) IMPACT-Sphere-Mineral-V83 (E1) at the surface, (b) DustCOMM-Asphere-DB19-V83 (E2) at the surface, (c) E1 in atmospheric column, (d) E2 in atmospheric column, (e) E1 at TOA, and (f) E2 simulations at TOA. The numbers in parentheses represented the global mean.





**Figure 9.** Radiative effect ( $W \cdot m^{-2}$ ) of mineral dust due to different studies at the surface and TOA for (a) total dust SW, (b) total dust LW, and (c) total dust NET. The annually averaged values were listed in Table 5.



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**Figure 10.** Radiative effect ( $W \cdot m^{-2}$ ) of mineral dust due to various aerosol absorptivity at the surface and TOA for (a) total dust SW, (b) total dust LW, and (c) total dust NET. The annually averaged values were listed in Table 5. The dashed line represented a 1 : 1 correspondence and corresponded to no change in radiative heating within the atmosphere.