Less atmospheric radiative heating by dust due to the synergy of coarser size and aspherical shape

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Abstract. Mineral dust aerosols cool and warm the atmosphere by scattering and absorbing solar (short-wave: SW) and thermal (long-wave: LW) radiation. However, significant uncertainties remain in dust radiative effects, largely due to differences in the dust size distribution and spectral optical properties simulated in Earth system models. Dust models typically underestimate the coarse dust load (more than 2.5 µm in a diameter) and assume a spherical shape, which leads to an overestimate of the fine dust load (less than 2.5 µm) after the dust emissions in the models are scaled to match observed dust aerosol optical depth at 550 nm ($DAOD_{550}$). Here, we improve the simulated dust properties with datasets that leverage measurements of size-resolved dust concentration, asphericity factor, and refractive index in a coupled global chemical transport model with a radiative transfer module. After the adjustment of size-resolved dust concentration and spectral optical properties, the global and annual average of $DAOD_{550}$ from the simulation increases from 0.023 to 0.029 and falls within the range of a semi-observationally-based estimate (0.030 ± 0.005). The reduction of fine dust load after the adjustment leads to a reduction of the SW cooling at the Top Of the Atmosphere (TOA). To improve agreement against a semi-observationally-based estimate of the radiative effect efficiency at TOA, we find that a less absorptive SW dust refractive index is required for coarser aspherical dust. Thus, only a minor difference is estimated for the net global dust radiative effect at TOA (-0.08 vs. -0.00 W·m^{-2} on a global scale). Conversely, our sensitivity simulations reveal that the surface warming is substantially enhanced near the strong dust source regions (less cooling to -0.23 from -0.60 W·m^{-2} on a global scale). Thus, less atmospheric radiative heating is estimated near the major source regions (less heating to 0.15 from 0.59 W·m^{-2} on a global scale), because of enhanced LW warming at the surface by the synergy of coarser size and aspherical shape.

1 Introduction

Mineral dust aerosols can both cool and warm the climate, but how much dust aerosols net influence global climate is highly uncertain (Penner, 2019). Global dust modeling studies have suggested that mineral dust exerts global and annual mean aerosol radiative effect (RE) between -0.6 and $+0.2$ W m^{-2} at the Top Of the Atmosphere (TOA) and between -0.2 and -2.7 W m^{-2} at the surface (Miller and Tegen, 1998; Balkanski et al., 2007; Tanaka et al., 2007; Takemura et al., 2009; Räisänen et al., 2013; Zhao et al., 2013; Albani et al., 2014; Colarco et al., 2014; Heald et al., 2014; Di Biagio et al., 2020; Tuccella et al., 2020). Whereas a negative RE corresponds to the cooling of the global system when the sunlight is reflected to space, a positive RE corresponds to an overall warming of the Earth-atmosphere system by trapping incident short-wave (SW) and outgoing long-wave (LW) radiation. Radiative effect by dust aerosols perturbs surface temperature, wind speed, rainfall, and vegetation cover, which may induce

36 feedback on dust emissions (Perlwitz et al. 2001; Miller et al., 2004a; Colarco et al., 2014). The climate feedback does

37 not only depend on RE at TOA or the surface alone but also on the difference to the value at TOA and surface, which

38 represents radiative heating within the atmosphere (Miller et al., 2004b; Yoshioka et al., 2007; Lau et al., 2009). The

39 large uncertainties in quantifying the dust RE in the models are mainly propagated from the large spatial heterogeneity

40 and temporal variability of mineral dust abundance and the physicochemical properties (e.g., size distribution, mineral

41 composition, and shape), as well as the ground surface characteristics and atmospheric properties (e.g., surface

42 reflectance, temperature, and atmospheric absorption) (Sicard et al., 2014; Lacagnina et al., 2015; Li and Sokolik,

43 2018). The model errors in dust size distribution and particle shape can lead to an overestimate of fine dust load after

44 the dust emissions in the models are scaled to match observed dust aerosol optical depth at 550 nm ($DAOD_{550}$). The

45 corresponding overestimate of SW cooling might be compensated for in models by using a refractive index that is too

46 absorbing (Di Biagio et al., 2019, 2020), which depends on the mineral composition of the dust. We regard "fine" and

47 "coarse" dust as dust particles with a diameter less than 2.5 µm (i.e., $PM_{2.5}$) and between 2.5 and 20 µm, respectively.

48 Below, we provide a brief discussion of the effects of the dust size distribution, particle shape, and mineral

49 composition on dust radiative effects.

50   First, there has been increased attention paid to the importance of accurately predicting the abundance of coarse

51 dust for the global energy balance (Kok et al., 2017; Song et al., 2018; Di Biagio et al., 2020; Adebiyi and Kok, 2020).

52 The coarser particles are expected to be more prevalent closer to the source regions, as they fall much faster than finer

53 particles (Mahowald et al., 2014). For instance, the lifetime of dust aerosols larger than 30 µm in diameter is less than

54 12 h in most cases except in large haboobs (Ryder et al., 2013). Current models, however, cannot accurately simulate

55 observed transport of coarse dust particles across the Atlantic (Weinzierl et al., 2017; Ansmann et al., 2017), although

56 several hypotheses have been proposed to explain measurements of giant dust particles (larger than 63 µm in diameter)

57 relatively far from source regions (van der Does et al., 2018). The potential mechanism for long-range transport of

58 giant dust particles is that the uplift events of coarse dust can be induced by a nocturnal low-level jet or cold pool

59 outflow from mesoscale convective systems (i.e., haboobs) (Rosenberg et al., 2014; Ryder et al., 2019). At higher

60 elevation, electrostatic forces might retard the settling of coarse and giant dust particles and thus may facilitate the

61 transport of these particles over longer distances (Harrison et al., 2018; Toth et al., 2019). Other missing processes

62 that affect the transport and deposition of giant particles would also need to be incorporated into the models to

63 reproduce the measurements of the size distribution over the open ocean (van der Does et al., 2018). The coarse dust

64 particles scatter and absorb both the solar and thermal radiation, causing a net warming effect at TOA. In contrast, the

65 fine dust particles principally scatter SW radiation, causing a net cooling effect. Since coarse dust tends to warm the

66 climate, the underestimation of the abundance of coarse dust causes Earth system models to underestimate the

67 warming near the dust source regions.

68   Second, previous studies have shown that the SW radiative effect of dust asphericity on climate simulations is

69   minor on a global scale, partly because the larger DAOD is compensated for by the larger asymmetry parameter of

70   aspherical dust, which reduces the amount of radiation scattered backward to space (Räisänen et al., 2013; Colarco et

71   al., 2014). Moreover, non-spherical calcium-rich dust particles can be converted to spherical particles, due to

72   heterogeneous reactions with nitrate and sulfate on these particles, especially over polluted regions (Laskin et al.,

73   2005; Matsuki et al., 2005). As the plumes move downwind to the oceans, the dust aerosols can be aggregated with

74   sea salt in the marine boundary layer, which leads to more spherical shapes and larger sizes (Zhang and Iwasaka,

75   2004). However, the assumption of spherical shape in models leads to a substantial underestimation of the extinction

76   efficiency and thus DAOD near the strong source regions, mainly because the assumption of sphericity causes an

77   underestimation of the surface-to-volume ratio compared to aspherical dust (Kok et al., 2017, 2021; Hoshyaripour et

78   al., 2019; Tuccella et al., 2020). Radiative effect efficiency is often used for the evaluation of the models and is defined

79   as the gradient of a linear least squares fit applied to AOD and dust radiative effect at each two-dimensional (2-D)

80   grid box (W·m^{-2} AOD^{-1}). Thus, the estimates of the dust radiative effect efficiency could be biased, in part, due to

81   large uncertainties associated with the spherical assumption on AOD retrieval (Zhou et al., 2020).

82   Third, the dust refractive index is often derived from measurements based on dust or individual mineral particles

83   (Bedidi and Cervelle, 1993; Long et al., 1993; Di Biagio et al., 2017, 2019; Stegmann & Yang, 2017). Indeed, most

84   dust particles are internal mixtures of various mineral compositions and irregular shapes (Reid, 2003; Wiegner et al.,

85   2009; Wagner et al., 2012). In desert soils, iron (Fe) oxides are generally hematite (α-Fe$_2$O$_3$) and goethite (FeOOH),

86   which cause soil-derived dust absorption at ultraviolet (UV) and visible wavelengths (Sokolik and Toon, 1999;

87   Balkanski et al., 2007). These two minerals have distinct optical properties, which might cause various intensities of

88   SW absorption and thus RE of dust aerosols (Lafon et al., 2016). The dust complex refractive index in the LW also

89   depends on the particle mineralogical composition (Sokolik et al., 1998). Di Biagio et al. (2017) found a linear

90   relationship between the magnitude of the imaginary refractive index at 7.0, 9.2, and 11.4 μm and the mass

91   concentration of calcite and quartz absorbing at these wavelengths. However, the speciation of dust into its mineral

92   components inherently comprises uncertainties on soil mineralogy, mineral content in size-segregated dust particles,

93   and refractive index of mineral, partly due to the differences in prescribed parameters such as the particle size. The

94   atmospheric aging of Fe-containing aerosols can further modulate the optical properties of Fe oxides (Ito et al., 2018)

95   and organic carbon (Al-Abadleh, 2021), while the photochemical transformation of Fe oxides from lithogenic sources

96   due to atmospheric processing is relatively limited (< 10%), compared to pyrogenic sources (Ito et al., 2019).

97   Here, we focus on the influence of the size-resolved abundance of aspherical dust on the aerosol radiative effects

98   in a coupled global chemical transport model (IMPACT) (Ito et al., 2020 and references therein) with a radiative

99   transfer module (RRTMG) (Iacono et al., 2008). We improve the accuracy of these simulations by correcting the bias

100   in size-resolved dust concentration with the Dust Constraints from joint Observational-Modelling-Experimental

101   analysis (DustCOMM) data set (Adebiyi et al., 2020), as well as by considering the aspherical shape (Huang et al.,

102   2020a, 20210b). We then explore the sensitivity to dust refractive index.

2 Methods

104   We examined the dust radiative effects using ten combinations of different numerical experiments that varied

105   (1) the simulated dust concentration and their size distribution, (2) particle shape, and (3) mineralogical composition

106   (Tables 1 and 2). Two experimentRRTMG calculations used the hourly averaged aerosoldust concentrations

107   calculated from the one IMPACT model simulationwith the finer dust size (E1 and E3) (denoted as "IMPACT"). The

108   two sensitivity experiments were handled in the RRTMG calculations performed with the distinction between

109   spherical and non-spherical dust and different refractive indices. We denoted "Sphere" when the RRTMG calculations

110   used the spherical assumption on the particle shape, while the IMPACT model considered asphericity in calculation

111   of gravitational settling velocities. On the other hand, we denoted "Asphere" when the dust asphericity was also

112   considered in the RRTMG calculations. Subsequently, the simulated dust concentration and the size distribution were

113   adjusted to the semi-observationally-based concentrations (Adebiyi and Kok, 2020) in another chemical transport

114   model simulation, which was performed with the other eightfive experimentRRTMG calculations (E4, E5, E6, E8,

115   and E9) with the coarser dust size (denoted as "DustCOMM"). The term "semi-observationally-based" is used for

116   DustCOMM, $DAOD_{550}$, and dust radiative effect efficiency when the estimates are based on the combination of

117   observations and models. Five sensitivity experiments were handled in the RRTMG calculations performed with

118   different refractive indices and hourly averaged aerosol concentrations with the two chemical transport model

119   simulations of "IMPACT" and "DustCOMM". We examined different refractive indices for the dust mineralogy to

120   represent the regional variations in refractive indices (denoted as "Mineral", "DB17", "DB19", "V83", "Less SW",

121   "More LW", "More SW", and "Less LW"). Thus, the other three experiments (E2, E7, and E10) were calculated from

122   the model output with a post-processor. DustCOMM-Asphere-DB19-V83 (E2) was obtained from combination of

123   DustCOMM-Asphere-DB19-DB17 (E4) for SW and DustCOMM-Asphere-Mineral-V83 (E6) for LW. DustCOMM-

124   Asphere-Less-More (E7) was obtained from combination of DustCOMM-Asphere-Less-Less (E8) for SW and

125   DustCOMM-Asphere-More-More (E9) for LW. DustCOMM-Asphere-More-Less (E10) was obtained from

126   combination of DustCOMM-Asphere-More-More (E9) for SW and DustCOMM-Asphere-Less-Less (E8) for LW.

127   Two simulations used the spherical assumption on the particle shape (denoted as "Sphere"), whereas the dust

128   asphericity was considered in the other eight experiments (denoted as "Asphere"). We then examined different

129   refractive indices for the dust mineralogy to represent the regional variations in refractive indices (denoted as

130   "Mineral", "DB17", "DB19", "V83", "Less SW", "More LW", "More SW", and "Less LW"). These sensitivity

simulations and their radiative effects are summarized in Tables 1 and 2, respectively, with more details below. In section 2.3, we describe the DustCOMM data set used to adjust (1) size-resolved abundance of dust concentration. In section 2.4, we describe the adjustment factor of (2) particle shape for spectral optical properties. In section 2.5, we describe differences in spectral refractive indices due to (3) different mineralogical compositions for the radiative flux calculation.

2.1   Aerosol chemistry transport model

This study used the Integrated Massively Parallel Atmospheric Chemical Transport (IMPACT) model (Ito et al., 2020 and references therein). Simulations were performed for the year 2016, using a horizontal resolution of $2.0°\times2.5°$ for latitude by longitude and 47 vertical layers. The chemical transport model was driven by the Modern Era Retrospective analysis for Research and Applications 2 (MERRA-2) reanalysis meteorological data from the National Aeronautics and Space Administration (NASA) Global Modeling and Assimilation Office (GMAO) (Gelaro et al., 2017). Thus, the radiative feedback of the dust aerosol on the climate was not considered in this study~~model simulation can be predicted by a separate version of the model (Penner et al., 2018)~~.

The model simulated the emissions, chemistry, transport, radiation, and deposition of major aerosol species, including mineral dust, black carbon (BC), particulate organic matter (POM), sulfate, nitrate, ammonium, and sea spray aerosols, and their precursor gases. Dust emissions were dynamically simulated using a physically-based emission scheme (Kok et al., 2014; Ito and Kok, 2017) with the soil mineralogical map (Journet et al., 2014; Ito and Shi, 2016). Atmospheric processing of mineral dust aerosols, during transport, were projected for four distinct aerosol size bins (<1.26 µm, 1.26–2.5 µm, 2.5–5 µm, and 5–20 µm of diameter). In this version of the IMPACT model, two modes were used for sulfate aerosol (nuclei and accumulation mode), and two moments were predicted within each mode (sulfate aerosol number and mass concentration) (Liu et al., 2005). The surface coating of sulfate on dust aerosols occurred because of the condensation of sulfuric acid gas on their surfaces, coagulation with sulfate aerosol, and formation in aqueous reactions within cloudy regions of the atmosphere (Liu et al., 2005). The heterogeneous uptake of nitrate, ammonium, and water vapor by each aerosol for each size bin was interactively simulated in the model following a hybrid dynamical approach (Feng and Penner, 2007). Five types of aerosols (i.e., dust, nucleated sulfate, carbonaceous aerosols from fossil fuel combustion, carbonaceous aerosols from biomass burning, and sea salt) were assumed to be externally mixed in each size bin for the computation of spectral optical properties (Xu and Penner, 2012). ~~Dust emissions were dynamically simulated using a physically-based emission scheme (Kok et al., 2014; Ito and Kok, 2017) with the soil mineralogical map (Journet et al., 2014; Ito and Shi, 2016).~~ To derive atmospheric concentration of mineral composition for dust aerosol, "tagged" tracer was used for each size-resolved mineral source. The direct emissions of dust were evenly distributed in mixing ratio throughout the planetary boundary layer. The

162   global scaling factor of dust emission was determined from the comparison of the model results with ground-based

163   AOD measurements near the dust source regions prior to the adjustment to the DustCOMM (Kok et al., 2014; Ito and

164   Kok, 2017). In recent review papers, multi-model evaluations of aerosol iron concentrations and their solubilities have

165   been comprehensively summarized on global and regional scales (Myriokefalitakis et al., 2018; Ito et al., 2021).

166   To improve the accuracy of our simulations of mineral dust, we made several upgrades to the on-line emission

167   and gravitational settling schemes used in Ito et al. (2020). The dust emissions were extremely sensitive to soil

168   moisture, and thus the bias was adjusted with satellite observations (Ito and Kok, 2017). However, the satellite

169   measurements were only available every other day, depending on location. The Soil Moisture Active Passive (SMAP)

170   Level-4 Soil Moisture data product addressed these limitations by merging the satellite observations into a numerical

171   model of the land surface water and energy balance while considering the uncertainty of the observations and model

172   estimates (Reichle et al., 2019). In this work, we utilized the 3-hourly data of soil moisture derived from the SMAP

173   for barren and open shrublands separately (Reichle et al., 2018). To achieve this, we used the MODerate resolution

174   Imaging Spectroradiometer (MODIS) land cover map at 500 m resolution to calculate the fraction of barren and open

175   shrublands in each grand surface layer (Friedl et al., 2019)

176   Compared to the assumption on spherical shapes of aerosols, the dust asphericity increased aerodynamic drag

177   at a given volume and mass, and thus increased gravitational settling lifetime by about 20% (Huang et al., 2020a).

178   Here, we implemented a globally averaged asphericity factor of 0.87 (Huang et al., 2020a) to the gravitational settling

179   scheme for mineral dust. Nevertheless, the lifetime of the dust aerosol for the largest-size bin in the IMPACT model,

180   even after accounting for asphericity (1.4 days for 5–20 µm of diameter), was significantly shorter than an ensemble

181   of model results (2.1 ± 0.3 days for the mass mean diameter of 8.3 µm) (Kok et al., 2017). The impact of this

182   underestimate of atmospheric lifetime is explored using the DustCOMM data set, as was summarized in Table 2 (E3

183   – E4).

184   **2.2   Integration of IMPACT and RRTMG**

185   To improve the accuracy of our simulations of dust RE, we made upgrades to the radiative transfer calculations

186   (Ito et al., 2018 and references therein). In this study, we integrated the Rapid Radiative Transfer Model for GCMs

187   (RRTMG) online within the IMPACT model to calculate the radiative fluxes associated with atmospheric aerosols.

188   RRTMG is a radiative transfer code that calculates the SW and LW atmospheric fluxes (Iacono et al., 2008). Given

189   the size range of dust particles, scattering and absorption in the on-line model were described in terms of Mie theory.

190   Assuming homogeneous spherical particles, the spectral optical properties such as the mass extinction coefficient,

191   single scattering albedo, and asymmetry parameter were calculated using a look-up table as a function of refractive

192   index and size parameter (Xu and Penner, 2012). The impact of this spherical assumption is explored using aspherical

193   factor, as was summarized in Table 2 (E5 – E4).

194   The mineral dust particles were assumed to follow prescribed size distributions within each size bin (Liu et al.,

195   20~~10~~05). In applying the look-up table, the size spectrum for mineral dust was divided into 30 sub bins (Wang and

196   Penner, 2009). As for the SW, the particle size increased with the uptake of sulfate, nitrate, ammonium, and water by

197   the aerosols (Xu and Penner, 2012). These coating materials on aerosol cores were treated as internally mixed with

198   ~~dust~~ each aerosol core in each size bin. ~~and t~~Thus, the coating materials on dust only can reduce solar absorption of

199   mineral dust. Subsequently, these optical properties were used by the RRTMG to calculate RE based on dust mixing

200   ratio distributions in the IMPACT model. The dust RE was estimated as the difference in the calculated radiative

201   fluxes with all aerosols and with all aerosols except the dust aerosols coated with sulfate, nitrate, ammonium, and

202   water for each bin. As the LW scattering was not accounted for in the RRTMG, we multiplied the LW radiative fluxes

203   by the adjustment factors of 1.18 ± 0.01 and 2.04 ± 0.18 for the dry particles at the surface and TOA (Dufresne et al.,

204   2002), following Di Biagio et al. (2020). The larger adjustment factor at TOA reflects the fact that the upward LW

205   radiation emitted from the ground surface can be trapped through scattering and absorption compared to the surface.

206   The broadband direct and diffuse albedos for both the UV visible and visible IR were specified from the hourly

207   MERRA-2. The surface emissivity was based on the hourly MERRA-2. Long-lived greenhouse gas concentrations

208   were obtained from historical greenhouse gas concentrations for climate models (Meinshausen et al., 2017). Water

209   vapor concentrations were specified according to the MERRA-2. Cloud optical properties were calculated based on

210   the liquid and ice visible optical depths from the MERRA-2, prescribing effective radii of 10 μm for water droplets

211   and 25 μm for ice particles, respectively (Gettelman et al., 2010; Heald et al., 2014).

212   **2.3   DustCOMM dataset and sensitivity experiments to size-resolved dust concentration**

213   Dust Constraints from joint Observational-Modelling-experiMental analysis (DustCOMM) is a dataset of

214   three-dimensional (3-D) dust properties obtained by combining observational, experimental, and modeling constraints

215   on dust properties. While details can be found in Adebiyi et al. (2020) and Adebiyi and Kok (2020), we provide a

216   brief overview here. First, DustCOMM's constraint on the 3-D dust size distribution combines dozens of previously

217   published in-situ measurements of dust size distributions taken during several field campaigns, with an ensemble of

218   climate model simulations. The framework used those in-situ measurements first to constrain the globally averaged

219   size distribution (Adebiyi and Kok, 2020), which is used subsequently to adjust the bias in an ensemble of six global

220   model simulations (Adebiyi et al., 2020). The constraints on dust size distribution range from 0.2 μm to 20 μm in

221   diameter, where a generalized analytical function describes the sub-bin distribution based on brittle fragmentation

222   theory (Kok, 2011). The second DustCOMM product – atmospheric dust mass loading – combines the constraints on

dust size distribution with constraints on dust extinction efficiency and dust aerosol optical depth (Adebiyi et al., 2020). The constraints on dust extinction efficiency used the single-scattering database of Meng et al. (2010) and leveraged measurements of the dust index of refraction as well as accounts for the non-spherical shape of dust particles (Kok et al., 2017). For this, we approximate dust as tri-axial ellipsoidal particles described by the globally representative values of measured dust aspect ratio (the length-to-width ratio), and the height-to-width ratio (HWR) obtained from Huang et al. (2020a). Furthermore, the dust aerosol optical depth used to obtain the dust mass loading combines the semi-observationally-based dataset from Ridley et al. (2016) with information from four reanalysis products. This includes the MERRA-2, Navy Aerosol Analysis and Prediction System (NAAPS), Japanese Reanalysis for Aerosol (JRAero), and Copernicus Atmosphere Monitoring Service interim ReAnalysis (CAMSiRA) (Adebiyi et al., 2020). The aerosol RE of mineral dust strongly depends on both the magnitude of dust load and the dust size distribution (Tegen and Lacis, 1996; Liao and Seinfeld, 1998). The DustCOMM data set contains total column loading (X, Y) and concentration of mineral dust resolved by season (T) and particle size (S) (Adebiyi et al., 2020). To correct the bias in the seasonally averaged size-resolved dust emission in the IMPACT model, $E_{\text{IMPACT}}(X, Y, T, S)$, the sum of bin 1, bin 2, and bin 3 dust emission flux was scaled by the seasonal mean of the ratio of the sum of bin 1, bin 2, and bin 3 dust column loading between the model, $L_{\text{IMPACT}}(X, Y, T, S)$, and DustCOMM, $L_{\text{DustCOMM}}(X, Y, T, S)$, at each 2-D grid box. The bias correction factor, $L_{\text{bias}}(X, Y, T)$, between the IMPACT model and DustCOMM data set is given by:

$$L_{\text{bias}}(X, Y, T) = \sum_{S=1}^{3} L_{\text{DustCOMM}}(X, Y, T, S) \div \sum_{S=1}^{3} L_{\text{IMPACT}}(X, Y, T, S) \ (1).$$

When the source function was used for high-latitude dust in the Northern Hemisphere, this led to substantially high emissions and thus RE over there, likely due to the influences from long-range transported dust. Therefore, the direct emissions of dust from the nine major source regions only (Kok et al., 2021) were adjusted using the DustCOMM data (Fig. 1). To adjust the size bias in dust emissions, the mass fraction of emitted dust for each bin was prescribed according to the size-resolved total column loading of DustCOMM at each 2-D grid box. The mass fraction for each size bin, $S_{\text{DustCOMM}}(X, Y, T, S)$ is given by:

$$S_{\text{DustCOMM}}(X, Y, T, S) = L_{\text{DustCOMM}}(X, Y, T, S) \div \sum_{S=1}^{4} L_{\text{DustCOMM}}(X, Y, T, S) \ (2).$$

Thus, the dust emission flux after the adjustment, $E_{\text{DustCOMM}}(X, Y, T, S)$ is given by:

$$E_{\text{DustCOMM}}(X, Y, T, S) = L_{\text{bias}}(X, Y, T) \times S_{\text{DustCOMM}}(X, Y, T, S) \times E_{\text{IMPACT}}(X, Y, T) \ (3).$$

Overall, the IMPACT-simulated lifetime of the dust aerosol for the second-size bin (7.8 days 1.26–2.5 µm of diameter) was in good agreement with the ensemble of model results (8.5 ± 1.1 days for the mass mean diameter of 1.8 µm) (Kok et al., 2017). To correct the bias in the seasonally averaged 3-D dust size distribution after the transport, the mass fraction of dust concentration for each bin between 0.2 and 20.0 µm of diameter was scaled at each 3-D grid box prior

253   to calculating the radiative fluxes using the RRTMG by the ratio of mass concentration of $PM_{2.5}$ (i.e., the sum of bin

254   1 and bin 2) to each bin (Table 3).

2.4   Asphericity factor for optical properties and sensitivity experiments to particle shape

256   To account for the dust asphericity, an adjustment factor was applied to the spherical optical properties at each

257   dust size parameter and refractive index. The adjustment factors for the spectral optical properties of non-spherical

258   particles were calculated after Huang et al. (2021~~0b~~). The atmospheric aging of mineral dust can form a uniform

259   coating around the mineral core and therefore decrease particle asphericity during transport. This is implicitly

260   considered in the globally averaged shape distribution of dust (Huang et al., 2019). Specifically, Huang et al. (2021~~0b~~)

261   combined globally representative dust shape distributions (Huang et al., 2020~~a~~) with a shape-resolved single-scattering

262   database (Meng et al., 2010). This database combines four computational methods (Mie theory, T-matrix method,

263   discrete dipole approximation, and an improved geometric optics method) to compute the single-scattering properties

264   of non-spherical dust for a wide range of shape descriptors. Huang et al. (2021~~0b~~) provided the look-up table

265   containing optical properties of non-spherical dust as functions of size parameter and refractive index.

266   The approximation of particles to spheres is evaluated by applying aspherical factors to the optical properties

267   of the mass extinction coefficient, single scattering albedo, and asymmetry parameter for SW, as well as absorption

268   fraction of extinction for the LW. At the same time, we maintained the consideration of asphericity on the gravitational

269   velocity and kept the dust concentrations unaltered between the spherical (denoted as "Sphere") and aspherical

270   (denoted as "Asphere") cases.

2.5   Spectral refractive index and sensitivity experiments to mineralogical compositions

272   The aerosol RE of mineral dust depends on mineralogical composition. For the sensitivity simulation to the

273   SW and LW refractive indices, we used the global mean of laboratory measurements of the refractive index from 19

274   natural soils from various source regions around the world in Di Biagio et al. (2019) (denoted as "DB19") and in Di

275   Biagio et al. (2017) (denoted as "DB17"), respectively. To illustrate the regional heterogeneity of refractive index, the

276   refractive index obtained from 19 samples was aggregated into 9 main source regions, and the arithmetic mean was

277   calculated for each source region (Di Biagio et al., 2017, 2019). The regionally averaged imaginary parts of the

278   refractive indices at the wavelength of 0.52 μm and 9.7 μm showed large differences in SW and LW absorptivity,

279   respectively, between different samples collected at various geographical locations (Fig. 1).

280   The optical properties from the measurements for dust samples generated from 19 natural soils suggested a

281   considerable role of Fe oxides in determining the SW absorption (Di Biagio et al., 2019). The refractive indices for

282   mineral components were used for hematite, goethite (Bedidi and Cervelle, 1993), silicate particle group, quarts,

283 gypsum (CaSO$_4$) (Stegmann & Yang, 2017), and calcite (CaCO$_3$) (Long et al., 1993) in the simulations denoted as

284 "Mineral". The hematite and goethite were treated separately according to the mineralogical map (Journet et al., 2014).

285 Consequently, hematite mass content averaged in the dust at emission (0.79% for fine and 0.50% for coarse from the

286 IMPACT simulation) was lower than goethite content (1.8% and 1.3%, respectively) on a global scale. In addition to

287 the primary emission of gypsum, CaSO$_4$ is secondarily formed due to the dissolution/precipitation of CaCO$_3$ in

288 thermodynamic equilibrium condition (Ito and Feng, 2010). To illustrate the difference in refractive index, the global

289 mean of the mineral composition was used for the comparison with DB19 (Fig. 1). The imaginary parts of the

290 refractive indices from mineralogical map were higher than DB19~~7~~, resulting in a stronger absorption over the SW

291 spectrum.

292   The mineral dust LW refractive index also depends on its mineralogical composition (Sokolik et al., 1998; Di

293 Biagio et al., 2017). The LW refractive index of Volz (1983) has been widely used in climate models and satellite

294 remote sensing algorithms and thus was examined here (denoted as "V83") (Song et al., 2018). The imaginary parts

295 of the refractive indices from V83 were higher than DB1~~7~~9, resulting in a stronger absorption over most of the LW

296 spectrum. To analyze the dependence of the results on less (more) absorptive SW and less (more) absorptive LW

297 refractive indices, we made further sensitivity simulations by varying the values of imaginary parts of the refractive

298 index within the range of values from Di Biagio et al. (2017, 2019) (10% or 90% percentiles for SW or LW,

299 respectively) (denoted as "Less" or "More"). The associated real parts with 10% or 90% percentile imaginary parts

300 for LW were calculated to account for the Kramers-Kronig relation (Lucarini et al., 2005).

301 **2.6   Semi-observationally-based dust SW and LW radiative effect efficiency**

302   To estimate dust radiative effect efficiency, aerosol and radiation remote sensing products have been used with

303 various methods (Table 4) (Zhang and Christopher 2003; Li et al. 2004; Christopher and Jones 2007; Brindley and

304 Russell 2009; Yang et al. 2009; Di Biagio et al. 2010; Hansell et al. 2010; Hansell et al. 2012; Song et al. 2018).

305   The instantaneous SW radiative effect efficiency at TOA is obtained from the linear regression of TOA

306 radiation flux versus AOD observations, although the values in low-dust periods can be substantially influenced by

307 other types of aerosols such as biomass burning (Li et al. 2004). This radiative effect efficiency corresponds to the

308 instantaneous value derived under the limited condition at the measurements (e.g., solar position, atmospheric

309 condition). From the extrapolation of the instantaneous value, the diurnal mean dust SW radiative effect efficiency at

310 the surface and TOA can be derived based on model calculations.

311   The LW radiative effect efficiency at TOA can be obtained from the linear regression of TOA radiation flux

312 versus AOD observations over the source regions (Brindley and Russell 2009). However, the observed outgoing LW

313 radiation is not only dependent on DAOD but also on other factors such as dust layer height, water vapor content, and

other types of aerosols. Thus, the LW radiative effect efficiency is estimated from the difference between observed

outgoing LW radiation and the dust-free outgoing LW radiation, which can be estimated using radiative transfer model

(Song et al., 2018).

Consequently, the semi-observationally-based estimates of the dust radiative effect efficiency could be biased,

in part, due to large uncertainties associated with the estimation method, the selection of cloud-free and dust-dominant

data, and dust physicochemical properties. To understand the sensitivity of the dust radiative effect efficiency to the

particle size distribution, asphericity, and refractive index of dust, radiative transfer computations have been carried

out in previous studies (Li et al., 2004; Song et al., 2018). Song et al. (2018) found that the combination of the coarser

dust particle size distribution and the more absorptive LW refractive index (V83) yielded the best simulation of the

dust LW radiative effect in comparison with the satellite flux observations (i.e., Clouds and the Earth's Radiant Energy

System (CERES)), compared to the less absorptive LW refractive index (DB17).

3.   Results and Discussions

We evaluate our results from the sensitivity simulations against semi-observationally-based estimates of

$DAOD_{550}$ in section 3.1 and radiative effect efficiency for SW and LW in section 3.2 and section 3.3, respectively.

We focus this evaluation on the North Africa and the North Atlantic in boreal summer (June, July, and August) partly

because that is the region and season for which most observational constraints on dust radiative effects are available.

The better agreement is obtained for the less absorptive SW (Di Biagio et al., 2019) and the more absorptive LW

(Volz, 1983) dust refractive indices with adjustments of size-resolved dust concentration and particle shape. Our

improved simulation from IMPACT-Sphere-Mineral-V83 (E1) to DustCOMM-Asphere-DB19-V83 (E2)

substantially reduces the model estimates of atmospheric radiative heating by mineral dust near the major source

regions even though it induces only a minor difference in RE at TOA on a global scale (section 3.4). To elucidate the

differences in dust radiative effects between different simulations, the results from the sensitivity simulations in

conjunction with previous modeling studies are analyzed in section 3.5.

3.1   Dust load and aerosol optical depth

We compared our model estimates of $DAOD_{550}$ against semi-observationally-based data in box plots and

Taylor diagrams (Taylor, 2001) for the evaluation of the various model experiments against semi-observationally-

based estimates (Ridley et al., 2016; Adebiyi et al., 2020) to provide a concise statistical summary of the bias,

correlation coefficient, root mean square errors, and the ratio of standard deviation (Fig. 2, Tables S1 and S2).

IMPACT-Sphere-Mineral-V83 (E1) simulations resulted in a significant underestimation of the global and annual

mean of $DAOD_{550}$ (0.023) (Fig. 2 and Table 3). ~~The lower DAOD~~$_{550}$ ~~from E2 than E1 was mostly found over East~~

Asia and Bodele/Sudan in winter (Fig. 2, Table S2). After considering the dust asphericity for spectral optical properties, we adjusted IMPACT-simulated dust loads against the constraints on dust load from the DustCOMM data set. This adjustment led the simulated total dust load to increase from 25 Tg (E1) to 32 Tg (E2), which addressed the issue of coarse dust underestimation and fine dust overestimation by the model (Fig. 3, Table 3). Consequently, the global and annual mean of $DAOD_{550}$ from DustCOMM-Asphere-DB19-V83 (E2) simulation (0.029) fell within the range in the semi-observationally-based estimate (0.030 ± 0.005) (Ridley et al., 2016) (Table 3). We found that the agreement in the median with the semi-observationally-based estimate (0.127) was improved from IMPACT-Sphere-Mineral-DB17 (0.049) to DustCOMM-Asphere-DB19-V83 (0.117) (solid line within the box mark in Fig. 2d). We also found improvementshigher $DAOD_{550}$ from E2 than E1 over East Asia and Bodele/Sudan in winter (Fig. 2, Table S2). The better agreement suggested that DustCOMM-Asphere-DB19-V83 (E2) simulation was reasonably constrained by the $DAOD_{550}$ (Ridley et al., 2016; Adebiyi et al., 2020).

3.2   Dust SW radiative effect efficiency

Modeled estimates of clear-sky dust SW radiative effect efficiencies ($W \cdot m^{-2} \ DAOD_{550}^{-1}$) at the surface (Table S3) and TOA (Table S4) were compared with estimates reported by regional studies based on satellite observations over the North Africa and the North Atlantic (Fig. 4). Comparisons for other regions and seasons were also included for SW in Figs. 4(g), 4(h), 4(i), and 4(j). Sensitivity simulations demonstrated that the radiative effect efficiency strongly depended on the particle size, refractive index, and particle shape (Fig. 4). The adjustment of size-resolved dust concentration and shape with the same refractive index led to overestimates of the SW radiative effect efficiencies against semi-observationally-based data at TOA (from E1 to E6 in Fig. 4h), because coarser dust absorbs more SW radiation efficiently than finer particles. Subsequently, the use of less absorptive SW refractive index with DustCOMM-Asphere-DB19-V83 (E2) simulations led to a better agreement (from E6 to E2 in Fig. 4). On the other hand, the use of much less (10% percentile) absorptive SW refractive index from DustCOMM-Asphere-Less-More (E7) simulation deteriorated the agreement due to the underestimate of cooling at the surface (Fig. 4g). In contrast, the use of a more absorptive SW refractive index from DustCOMM-Asphere-Mineral-V83 (E6) improved the agreement at the surface. However, the semi-observationally-based estimates of diurnally averaged radiative effect efficiency at the surface were derived from extrapolation of the instantaneous values, which would affect the comparison due to differences in the methodologies between dust models (section 2.6). The differences in the model-based estimates of radiative effect efficiency might arise from different data sets of the refractive index, size distribution, and particle shape (Song et al., 2018).

373 **3.3   Dust LW radiative effect efficiency**

374   Modeled estimates of clear-sky dust LW (Fig. 5) radiative effect efficiencies (W·m^{-2} DAOD$_{550}$$^{-1}$) at the surface

375 (Table S5) and TOA (Table S6) were compared with estimates reported by regional studies based on satellite

376 observations over North Africa and the North Atlantic. ~~Comparisons for other regions and seasons were also included~~

377 ~~for LW Figs. 5(g), 5(h), 5(i), and 5(j).~~ Sensitivity simulations demonstrated that the radiative effect efficiency strongly

378 depended on the particle size, refractive index, and particle shape (Fig. 5). Both the IMPACT-Sphere-Mineral-V83

379 (E1) and DustCOMM-Asphere-DB19-V83 (E2) simulations yielded better agreement with semi-observationally-

380 based data at the surface and TOA, compared to the less absorptive LW dust refractive indices (E3, E4, E5, and E7)

381 (Fig. 5). The relatively high LW radiative effect efficiencies over western Africa were also consistent with the semi-

382 observationally-based data. On the other hand, the relatively low LW radiative effect efficiencies were found over

383 eastern Africa. Moving toward the northeastern side of the region, however, the associated uncertainties in the semi-

384 observationally-based values increased (Brindley and Russell 2009). The dust LW radiative effect efficiency depends

385 strongly on the vertical profile of dust concentration, temperature, and water vapor, which would affect the comparison

386 due to a high variability in these factors (section 2.6).

387 **3.4   ~~Less A~~atmospheric radiative heating by dust due to the synergy of coarser size and aspherical shape**

388   The Saharan dust cools the ground surface by reducing the solar radiation reaching the surface and warms the

389 atmosphere by absorbing solar radiation (Fig. 6). On the other hand, thermal emission by dust warms the surface and

390 cools the atmosphere (Fig. 7). Our sensitivity simulations showed that the annually averaged net instantaneous

391 radiative effect due to mineral aerosol (NET) ranged from –0.48 (DustCOMM-Asphere-Less-Less) to +0.25

392 (DustCOMM-Asphere-Mineral-V83) W·m^{-2} at TOA (Table 5). The net RE from both the IMPACT-Sphere-Mineral-

393 V83 (–0.00 W·m^{-2}) and DustCOMM-Asphere-DB19-V83 (–0.08 W·m^{-2}) simulations resulted within 98%

394 confidential interval of DustCOMM data set (–0.27 to 0.14 W·m^{-2}).

395   The SW RE by dust outweighs the LW warming effect at the surface in the IMPACT-Sphere-Mineral-V83

396 (E1) simulation (Fig. 8). Consequently, the highly absorbing dust could play an important role in the aerosol radiative

397 forcing for the climate models to alter the West African monsoon, with the radiative heating concentrated in the dust

398 layer (Miller et al., 2004b; Lau et al., 2009). Our model results of dust RE from DustCOMM-Asphere-DB19-V83

399 (E2) simulation, however, suggested that the surface warming was substantially enhanced near the strong dust source

400 regions (−0.23 W·m^{-2} on a global scale) (Fig. 8), compared to the IMPACT-Sphere-Mineral-V83 simulation (−0.60

401 W·m^{-2} on a global scale). Thus, our results demonstrated that the atmospheric radiative heating by mineral dust was

402 substantially reduced for DustCOMM-Asphere-DB19-V83 (E2) simulation (0.15 W·m^{-2}), compared to the IMPACT-

403 Sphere-Mineral-V83 (E1) simulation (0.59 W·m^{-2}).

3.5 ~~Synergy of coarser size and aspherical shape~~Variability of dust radiative effect in different simulations

To elucidate the differences in dust radiative effects between the IMPACT-Sphere-Mineral-V83 (E1) and DustCOMM-Asphere-DB19-V83 (E2) simulations and to explore the variability in different previous model estimates (Fig. 9), the differences in annually averaged radiative effects of mineral dust from DustCOMM-Asphere-DB19-DB17 (E4) simulation were shown in Fig. 10. A slope of one in Fig. 10 represented an identical change in both the surface and TOA and thus corresponded to no change in radiative heating within the atmosphere. The distances from the DustCOMM-Asphere-DB19-DB17 (E4) simulation demonstrated that large uncertainties existed for the size distribution and spectral optical properties. Our sensitivity simulations revealed that the DustCOMM-Asphere-DB19-V83 (E2) simulation led to a similar net RE at TOA to the IMPACT-Sphere-Mineral-V83 (E1) simulation but resulted in less cooling at the surface (Fig. 9). This revision can be divided into (1) the size-resolved abundance (black hexagons, E3 – E4, in Fig. 10), (2) SW refractive index (red diamonds, E6 – E4, in Fig. 10 ~~and triangles~~), and (3) particle shape (red circles, E5– E4, in Fig. 10). Additionally, we show the sensitivity of dust RE to LW refractive index (DB17), which was used by both Di Biagio et al. (2020) and Balkanski et al. (2021).

First, at TOA, the SW RE was more sensitive to the size-resolved abundance (–0.17 W·m^{-2} at the vertical axis of black hexagon in Fig. 10a), compared to LW (0.00 W·m^{-2} at the vertical axis of black hexagon in Fig. 10b). Second, this less SW cooling effect with coarser dust (E3 – E4) was partially compensated for by more SW cooling with the use of~~by~~ the less absorptive SW refractive index (E4: –0.32 W·m^{-2}) than E6 (0.02 W·m^{-2})~~(0.34 W·m^{-2} at the vertical axis of red diamond in Fig. 10a)~~. Thirdly, the sensitivity of SW RE to dust asphericity was rather minor (0.04 W·m^{-2} at the vertical axis of red circle in Fig. 10a), partly because the lower DAOD was compensated for by the lower asymmetry parameter of spherical dust, which enhanced the amount of radiation scattered backward to space (Räisänen et al., 2013; Colarco et al., 2014). The partial compensation led to a small enhancement of SW RE for the IMPACT-Sphere-Mineral-V83 (E1) simulation and thus the resulting similar net RE to DustCOMM-Asphere-DB19-V83 (E2) at TOA (Fig. 9).

In contrast, at the surface, our sensitivity simulations demonstrated substantially different responses in the RE, mostly because of LW warming effects (Fig. 9). The enhanced LW warming by coarser dust (–0.08 W·m^{-2} at the horizontal axis of black hexagon in Fig. 10b) was accompanied by the asphericity (–0.15 W·m^{-2} at the horizontal axis of red circle in Fig. 10b), because the enhancement of the absorption fraction of extinction due to asphericity was larger at coarser size. The enhanced LW warming effects of each as well as the synergy was further amplified using the more absorptive LW dust refractive index (Volz, 1983) (at the horizontal axis of red diamond in Fig. 10b). As a result, our sensitivity simulations revealed that substantially less dust absorption at LW due to the underestimation of the coarse dust load and the assumption of the spherical shape (IMPACT-Sphere-Mineral-V83) contributed to the less surface warming, compared to DustCOMM-Asphere-DB19-V83 (Fig. 9).

A relatively good agreement of net RE by dust at TOA with both Di Biagio et al. (2020) (–0.06 W·m^{-2}) and Balkanski et al. (2021) (–0.02 W·m^{-2}) could be obtained from both the IMPACT-Sphere-Mineral-V83 (E1: –0.00 W·m^{-2}) and DustCOMM-Asphere-DB19-V83 (E2: –0.08 W·m^{-2}) simulations (Fig. 9 and Table 5). On the other hand, our modeled dust net RE at the surface from DustCOMM-Asphere-DB19-V83 (E2: –0.23 W·m^{-2}) ~~was~~ indicated much less cooling~~larger~~ than Di Biagio et al. (2020) (–0.63 W·m^{-2}), Balkanski et al. (2021) (–1.01 W·m^{-2}), and IMPACT-Sphere-Mineral-V83 (E1: –0.60 W·m^{-2}). The synergy of coarser size and aspherical dust could contribute to the less surface ~~warming~~ cooling of the DustCOMM-Asphere-DB19-V83 (E2), because of enhanced LW warming. At the same time, both Di Biagio et al. (2020) and Balkanski et al. (2021) used DB17 and considered dust with diameters more than 20 μm. Thus, the more absorptive LW dust refractive index (V83, E6 for LW: 1.00 W·m^{-2}) than DB17 (E4 for LW: 0.58 W·m^{-2}) (E6 – E4 for LW: 0.42 W·m^{-2} at the horizontal axis of red diamond in Fig. 10b) could also contribute to the less surface ~~warming~~cooling, which might be partially compensated for in our model by the omission of dust with diameters ~~in excess of~~more than 20 μm. Consequently, our estimate of atmospheric radiative heating by dust from DustCOMM-Asphere-DB19-V83 (E2: 0.15 W·m^{-2}) was lower than Di Biagio et al. (2020) (0.63 W·m^{-2}), Balkanski et al. (2021) (0.98 W·m^{-2}), and IMPACT-Sphere-Mineral-V83 (E1: 0.59 W·m^{-2}). Additionally, the hot and dry climate over brighter desert surface exaggerates differences in RE at the surface between the models (Miller et al., 2014). The low humidity allows dust particles to absorb LW radiation with reduced competition from water vapor, while high temperatures within the boundary layer increase downward thermal emission by dust (Liao and Seinfeld, 1998). The reduction of fine dust load after the adjustment leads to underestimates of the SW cooling at TOA. To improve agreement against semi-observationally-based estimate of the radiative effect efficiency at TOA, the less absorptive SW dust refractive index is required for coarser aspherical dust. Thus, uncertainties in the size-resolved dust concentration, particle shape, and refractive index contribute to the diversity in the simulated dust RE at the surface.

4.   Conclusions

Accurate estimates of the size-resolved dust abundance, their spectral optical properties, and their seasonality in regional and vertical scales provide a step towards a more reliable projection of the climatic feedback of mineral aerosols. The radiative effect efficiency depends on numerous variables in model simulations, including the spatial distribution and temporal variation of size-resolved dust concentrations, the mass extinction coefficient, single scattering albedo, and asymmetry parameter of dust. Since the models typically underestimate the coarse dust load and overestimate the fine dust load, the sensitivity to the aerosol absorptivity might be considerably different from previous studies. Thus, the model results should be re-evaluated against semi-observationally-based estimate of the DAOD$_{550}$ and dust radiative effect efficiency.

467   We improved the accuracy of the simulations by adjusting the bias in size-resolved aspherical dust

468   concentration with the DustCOMM data set. Alternatively, dust mineralogy might contribute to the underestimation

469   of modeled aerosol absorption compared to satellite observations (Lacagnina et al., 2015). This enhanced aerosol

470   absorption was examined by specifying the mineralogy with varying amounts of light-absorbing Fe oxides for SW.

471   The better agreement with the semi-observationally-based data of dust radiative effect efficiency was obtained using

472   the less absorptive SW ~~and the more absorptive LW~~ dust refractive indices after the adjustments of dust sizes and

473   shapes.

474   The diversity of modeled dust net RE at the surface (–1.7~~6~~4 W·m^{-2} to –0.20 W·m^{-2}) is much larger than at

475   TOA (–0.01 W·m^{-2} to –0.60~~1~~ W·m^{-2}), partly because the refractive index is optimized to obtain reasonable agreement

476   against satellite observations of TOA radiation flux (e.g., CERES). The uncertainties in the size-resolved dust

477   concentration, particle shape, and refractive index contribute to the model diversity at the surface. DustCOMM-

478   Asphere-DB19-V83 (E2) simulation resulted in less cooling at the surface by the synergy of coarser size and aspherical

479   shape, compared to IMPACT-Sphere-Mineral-V83 (E1) simulation (–0.23 vs. –0.60~~88~~ W·m^{-2} on a global scale).

480   Consequently, the atmospheric heating due to mineral dust was substantially reduced for the DustCOMM-Asphere-

481   DB19-V83 (E2) simulation (0.15 W·m^{-2}), compared to the intensified atmospheric heating from the IMPACT-Sphere-

482   Mineral-V83 (E1) simulation (0.59 W·m^{-2}). The less intensified atmospheric heating due to mineral dust could

483   substantially modify the vertical temperature profile in Earth system models and thus has important implications for

484   the projection of dust feedback near the major source regions in the past and future climate changes (Kok et al., 2018).

485   More accurate estimates of semi-observationally-based dust SW and LW radiative effect efficiencies over strong dust

486   source regions are needed to narrow the uncertainty in the RE.

487   Currently, the model did not include dust particles above 20 μm, but a substantial fraction of airborne dust near

488   source regions may be above this threshold (Ryder et al., 2019). Moreover, such large particles can be transported to

489   higher altitudes and longer distances than the model prediction. The higher the dust layer resides, the larger the dust

490   LW RE at TOA is estimated under the clear-sky conditions (Liao and Seinfeld, 1998). Marine sediment traps, which

491   are located underneath the main Saharan dust plume in the Atlantic Ocean, suggest that giant particles are dominated

492   by platy mica and rounded quartz particles (van der Does et al., 2016). Thus, mineral composition of the giant particles

493   could be different from the aerosol samples generated from soils in the laboratory by Di Biagio et al. (2017), which

494   may reflect less absorbing LW refractive index of DB17 than V83. Indeed, the dust sample was collected for V83

495   from rainwater after strong wind. On the other hand, the contribution of the LW scattering might be underestimated

496   in the models, as Di Biagio et al. (2020) noted that the adjustment factor was estimated for dust of diameter less than

497   10 μm and thus might be a lower approximation of the LW scattering by coarse dust. Therefore, a better understanding

498   of the effect of such large particles beyond 20 μm and mineralogical composition on radiation balance remains a topic

499   of active research, given their potential to amplify the warming of the climate system. In such an extreme case as the

500   "Godzilla" dust storm over the North Africa and the tropical Atlantic in June 2020 (Francis et al., 2020), the dust

501   loading could be larger than that examined for this study, and our estimates of the warming effects might be

502   conservative during such events. However, to keep the giant particles in the atmosphere, the modeled deposition fluxes

503   should be reduced from the current model. Therefore, models should improve their ability to capture the evolution of

504   the dust size distribution as the plumes move downwind of the source regions.

505   **Code availability.**

506   The source code of the RRTMG has been obtained from the website at https://github.com/AER-RC/RRTMG_LW and

507   https://github.com/AER-RC/RRTMG_SW. The source code of the Kramers-Kronig relations has been obtained from

508   the website at https://www.mathworks.com/matlabcentral/fileexchange/8135-tools-for-data-analysis-in-optics-

509   acoustics-signal-processing. The source code of the Taylor diagram has been obtained from the web site at

510   https://www.mathworks.com/matlabcentral/fileexchange/20559-taylor-diagram.

511   **Data availability.**

512   SMAP data have been obtained from the website at https://nsidc.org/data/smap/smap-data.html. MODIS land data

513   have been retrieved from the website at https://ladsweb.modaps.eosdis.nasa.gov/. MERRA-2 data have been provided

514   by the Global Modeling and Assimilation Office (GMAO) at NASA Goddard Space Flight Center

515   (https://disc.gsfc.nasa.gov/datasets/). The DustCOMM data are available at https://dustcomm.atmos.ucla.edu/. The

516   datasets supporting the conclusions of this article are included within the article and its supplement file.

517   **Supplement.**

518   The supplement related to this article is available online at:

519   **Author contributions.**

520   AI and JFK initiated the modeling collaboration with semi-observationally-based data sets. AI carried out the

521   modeling study. AAA, YH, JFK contributed semi-observationally-based data sets of DustCOMM and asphericity

522   factor. All authors read and approved the final manuscript.

523   **Competing interests.**

524   The authors declare that they have no competing interests.

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538   **References**

539   Adebiyi, A. A., Kok, J. F., Wang, Y., Ito, A., Ridley, D. A., Nabat, P., and Zhao, C.: Dust Constraints from joint

540   Observational-Modelling-experiMental analysis (DustCOMM): comparison with measurements and model

541   simulations, Atmos. Chem. Phys., 20, 829–863, https://doi.org/10.5194/acp-20-829-2020, 2020.

542   Adebiyi, A. A. and Kok, J. F.: Climate models miss most of the coarse dust in the atmosphere, Sci. Adv., 6, eaaz9507,

543   https://doi.org/10.1126/sciadv.aaz9507, 2020.

544   Al-Abadleh, H. A.: Aging of atmospheric aerosols and the role of iron in catalyzing brown carbon formation. Environ.

545   Sci.: Atmos., 1, 297–345, https://doi.org/10.1039/D1EA00038A, 2021.

546   Albani, S., Mahowald, N. M., Perry, A. T., Scanza, R. A., Heavens, N. G., Zender, C. S., Maggi, V., Kok, J. F., and

547   Otto-Bliesner, B. L.: Improved dust representation in the Community Atmosphere Model. J. Adv. Model.

548   Earth Syst., 6, 541–570, https://doi.org/10.1002/2013MS000279, 2014.

549   Ansmann, A., Rittmeister, F., Engelmann, R., Basart, S., Jorba, O., Spyrou, C., Remy, S., Skupin, A., Baars, H., Seifert,

550   P., Senf, F., and Kanitz, T.: Profiling of Saharan dust from the Caribbean to western Africa – Part 2:

551   Shipborne   lidar   measurements   versus   forecasts,   Atmos.   Chem.   Phys.,   17,   14987–15006,

552   https://doi.org/10.5194/acp-17-14987-2017, 2017.

553   Balkanski, Y., Schulz, M., Claquin, T., and Guibert, S.: Reevaluation of Mineral aerosol radiative forcings suggests a

554   better agreement with satellite and AERONET data, Atmos. Chem. Phys., 7, 81–95,

555   https://doi.org/10.5194/acp-7-81-2007, 2007.

556   Balkanski, Y., Bonnet, R., Boucher, O., Checa-Garcia, R., and Servonnat, J.: Better representation of dust can improve

557   climate models with too weak an African monsoon, Atmos. Chem. Phys., 21, 11423–11435,

558   https://doi.org/10.5194/acp-21-11423-2021, 2021.

559   Bedidi, A. and Cervelle, B.: Light scattering by spherical particles with hematite and goethitelike optical properties:

560   effect of water impregnation, J. Geophys. Res., 98, 11941–11952, 1993, https://doi.org/10.1029/93JB00188.

561   Brindley, H. E. and Russell, J. E.: An assessment of Saharan dust loading and the corresponding cloud-free longwave

562   direct radiative effect from geostationary satellite observations, J. Geophys. Res.-Atmos., 114, D23201,

563   https://doi.org/10.1029/2008jd011635, 2009.

564   Colarco, P. R., Nowottnick, E. P., Randles, C. A., Yi, B. Q., Yang, P., Kim, K. M., Smith, J. A., and Bardeen, C. G.:

565   Impact of radiatively interactive dust aerosols in the NASA GEOS-5 climate model: Sensitivity to dust

566   particle shape and refractive index, J. Geophys. Res.-Atmos., 119, 753–786,

567   https://doi.org/10.1002/2013JD020046, 2014.

568   Christopher, S. A. and Jones, T.: Satellite-based assessment of cloud-free net radiative effect of dust aerosols over the

569   Atlantic Ocean, Geophys. Res. Lett., 34, L02810, doi:10.1029/2006GL027783, 2007.

570   Di Biagio, C., di Sarra, A., and Meloni, D.: Large atmospheric shortwave radiative forcing by Mediterranean aerosol

571   derived from simultaneous ground-based and spaceborne observations, and dependence on the aerosol type

572   and single scattering albedo, J. Geophys. Res., 115, D10209, https://doi.org/10.1029/2009JD012697, 2010.

573   Di Biagio, C., Formenti, P., Balkanski, Y., Caponi, L., Cazaunau, M., Pangui, E., Journet, E., Nowak, S., Caquineau,

574   S., Andreae, M. O., Kandler, K., Saeed, T., Piketh, S., Seibert, D., Williams, E., and Doussin, J.-F.: Global

575   scale variability of the mineral dust long-wave refractive index: a new dataset of in situ measurements for

576   climate modeling and remote sensing, Atmos. Chem. Phys., 17, 1901–1929, https://doi.org/10.5194/acp-17-

577   1901-2017, 2017.

578   Di Biagio, C., Formenti, P., Balkanski, Y., Caponi, L., Cazaunau, M., Pangui, E., Journet, E., Nowak, S., Andreae, M.

579   O., Kandler, K., Saeed, T., Piketh, S., Seibert, D., Williams, E., and Doussin, J.-F.: Complex refractive

580   indices and single-scattering albedo of global dust aerosols in the shortwave spectrum and relationship to

581   size and iron content, Atmos. Chem. Phys., 19, 15503–15531, https://doi.org/10.5194/acp-19-15503-2019,

582   2019.

583 Di Biagio, C., Balkanski, Y., Albani, S., Boucher, O., and Formenti, P.: Direct radiative effect by mineral dust aerosols
584   constrained by new microphysical and spectral optical data. Geophys. Res. Lett., 47, e2019GL086186,
585   https://doi.org/10.1029/2019GL086186, 2020.

586 Dufresne, J., Gautier, C., Ricchizzi, P., and Fouquart, Y.: Longwave scattering effects of mineral aerosols, J. Atmos.
587   Sci., 59(12), 1959–1966, 2002, https://doi.org/10.1175/1520-0469(2002)059<1959:LSEOMA>2.0.CO;2.

588 Feng, Y. and Penner, J. E.: Global modeling of nitrate and ammonium: Interaction of aerosols and tropospheric
589   chemistry, J. Geophys. Res., 112, D01304, doi:10.1029/2005JD006404, 2007.

590 Francis, D., Fonseca, R., Nelli, N., Cuesta, J., Weston, M., Evan, A., and Temimi, M.: The atmospheric drivers of the
591   major Saharan dust storm in June 2020. Geophys. Res. Lett., 47, e2020GL090102,
592   https://doi.org/10.1029/2020GL090102, 2020.

593 Friedl, M. and Sulla-Menashe, D.: MCD12Q1 MODIS/Terra+Aqua Land Cover Type Yearly L3 Global 500m SIN
594   Grid V006 [Data set]. NASA EOSDIS Land Processes DAAC,
595   https://doi.org/10.5067/MODIS/MCD12Q1.006, 2019.

596 Gelaro, R., McCarty, W., Suárez, M. J., Todling, R., Molod, A., Takacs, L., Randles, C. A., Darmenov, A., Bosilovich,
597   M. G., Reichle, R., Wargan, K., Coy, L., Cullather, R., Draper, C., Akella, S., Buchard, V., Conaty, A., da
598   Silva, A. M., Gu, W., Kim, G.-K., Koster, R., Lucchesi, R., Merkova, D., Nielsen, J. E., Partyka, G., Pawson,
599   S., Putman,W., Rienecker, M., Schubert, S. D., Sienkiewicz, M., and Zhao, B.: The Modern-Era
600   Retrospective Analysis for Research and Applications, Version 2 (MERRA-2), J. Climate, 30, 5419–5454
601   https://doi.org/10.1175/JCLI-D-16-0758.1, 2017,.

602 Gettelman, A., Liu, X., Ghan, S. J., Morrison, H., Park, S., Conley, A. J., Klein, S. A., Boyle, J., Mitchell, D. L., and
603   Li, J. L. F.: Global simulations of ice nucleation and ice supersaturation with an improved cloud scheme in
604   the Community Atmosphere Model, J. Geophys. Res., 115, D18216, https://doi.org/10.1029/2009jd013797,
605   2010.

606 Harrison, R. G., Nicoll, K. A., Marlton, G. J., Ryder, C. L., and Bennett, A. J.: Saharan dust plume charging observed
607   over the UK, Environ. Res. Lett., 13, 054018, https://doi.org/10.1088/1748-9326/aabcd9, 2018.

608 Hansell, R. A., Tsay, S., Hsu, N. C., Ji, Q., Bell, S.W., Brent, N. H., Welton, E. J., Roush, T. L., Zhang, W., Huang,
609   J., Li Z. Q., and Chen, H.: An assessment of the surface longwave direct radiative effect of airborne dust in
610   Zhangye, China, during the Asian Monsoon Years field experiment (2008), J. Geophys. Res., 117, D00K39,
611   https://doi.org/10.1029/2011JD017370, 2012.

612 Hansell, R. A., Tsay, S. C., Ji, Q., Hsu, N. C., Jeong, M. J.,Wang, S. H., Reid, J. S., Liou, K. N., and Ou, S. C.: An
613   assessment of the surface longwave direct radiative effect of airborne saharan dust during the NAMMA field
614   campaign, J. Atmos. Sci. 67, 1048–1065, doi:10.1175/2009JAS3257.1, 2010.

Heald, C. L., Ridley, D. A., Kroll, J. H., Barrett, S. R. H., Cady-Pereira, K. E., Alvarado, M. J., and Holmes, C. D.: Contrasting the direct radiative effect and direct radiative forcing of aerosols, Atmos. Chem. Phys., 14, 5513–5527, https://doi.org/10.5194/acp-14-5513-2014, 2014.

Huang, Y., Kok, J. F., Kandler, K., Lindqvist, H., Nousiainen, T., Sakai, T., Adebiyi, A., and Jokinen, O.: Climate Models and Remote Sensing Retrievals Neglect Substantial Desert Dust Asphericity, Geophys. Res. Lett., 47, e2019GL086592, https://doi.org/10.1029/2019GL086592, 2020~~a~~.

Huang, Y., Adebiyi, A. A., Formenti, P., and Kok, J. F. ~~2020b,~~: Linking the different diameter types of aspherical desert dust indicates that models underestimate coarse dust emission, Geophys. Res. Lett.~~American Geophysical Union~~, 48~~Fall Meeting 2020~~, e2020GL092054~~abstract A007-0016~~, https://doi.org/10.1029/2020GL092054, 2021~~doi: 10.1002/essoar.10504925.1~~.

Hoshyaripour, G. A., Bachmann, V., Förstner, J., Steiner, A., Vogel, H., Wagner, F., Walter, C., and Vogel, B.: Effects of Particle Nonsphericity on Dust Optical Properties in a Forecast System: Implications for Model-Observation Comparison, J. Geophys. Res.-Atmos., 124, 2018JD030228, https://doi.org/10.1029/2018JD030228, 2019.

Iacono, M. J., Delamere, J. S., Mlawer, E. J., Shephard, M. W., Clough, S. A., and Collins, W. D.: Radiative forcing by long-lived greenhouse gases: Calculations with the AER radiative transfer models, J. Geophys. Res., 113, D13103, https://doi.org/10.1029/2008JD009944, 2008.

Ito, A. and Feng, Y.: Role of dust alkalinity in acid mobilization of iron, Atmos. Chem. Phys., 10, 9237–9250, https://doi.org/10.5194/acp-10-9237-2010, 2010.

Ito, A. and Shi, Z.: Delivery of anthropogenic bioavailable iron from mineral dust and combustion aerosols to the ocean, Atmos. Chem. Phys., 16, 85–99, https://doi.org/10.5194/acp-16-85-2016, 2016.

Ito, A. and Kok, J. F.: Do dust emissions from sparsely vegetated regions dominate atmospheric iron supply to the Southern Ocean?, J. Geophys. Res.-Atmos., 122, 3987–4002, https://doi.org/10.1002/2016JD025939, 2017.

Ito, A., Lin, G., and Penner, J. E.: Radiative forcing by lightabsorbing aerosols of pyrogenetic iron oxides, Sci. Rep.-UK, 8, 7347, https://doi.org/10.1038/s41598-018-25756-3, 2018.

Ito, A., Myriokefalitakis, S., Kanakidou, M., Mahowald, N. M., Scanza, R. A., Hamilton, D. S., Baker, A. R., Jickells, T., Sarin, M., Bikkina, S., Gao, Y., Shelley, R. U., Buck, C. S., Landing, W. M., Bowie, A. R., Perron, M. M. G., Guieu, C., Meskhidze, N., Johnson, M. S., Feng, Y., Kok, J. F., Nenes, A., and Duce, R. A.: Pyrogenic iron: The missing link to high iron solubility in aerosols, Sci. Adv., 5, eaau7671, https://doi.org/10.1126/sciadv.aau7671, 2019.

Ito, A., Perron, M. M. G., Proemse, B. C., Strzelec, M., Gault-Ringold, M., Boyd, P. W., and Bowie, A. R.: Evaluation of aerosol iron solubility over Australian coastal regions based on inverse modeling: implications of bushfires

on bioaccessible iron concentrations in the Southern Hemisphere, Prog. Earth Planet. Sci., 7, 42, https://doi.org/10.1186/s40645-020-00357-9, 2020.

Ito, A., Ye, Y., Baldo, C., and Shi, Z.: Ocean fertilization by pyrogenic aerosol iron, npj Clim. Atmos. Sci., 4, 30, https://doi.org/10.1038/s41612-021-00185-8, 2021.

Journet, E., Balkanski, Y., and Harrison, S. P.: A new data set of soil mineralogy for dust-cycle modeling, Atmos. Chem. Phys., 14, 3801–3816, https://doi.org/10.5194/acp-14-3801-2014, 2014.

Kok, J. F.: A scaling theory for the size distribution of emitted dust aerosols suggests climate models underestimate the size of the global dust cycle, P. Natl. Acad. Sci. USA, 108, 1016–1021, https://doi.org/10.1073/pnas.1014798108, 2011.

Kok, J. F., Parteli, E. J. R., Michaels, T. I., and Karam, D. B.: The physics of wind-blown sand and dust, Rep. Prog. Phys., 75, 106901, doi:10.1088/0034-4885/75/10/106901, 2012.

Kok, J. F., Mahowald, N. M., Fratini, G., Gillies, J. A., Ishizuka, M., Leys, J. F., Mikami, M., Park, M.-S, Park, S.-U., Van Pelt, R. S., and Zobeck, T. M.: An improved dust emission model – Part 1: Model description and comparison against measurements, Atmos. Chem. Phys., 14, 13023–13041, https://doi.org/10.5194/acp-14-13023-2014, 2014.

Kok, J. F., Ridley, D. A., Zhou, Q., Miller, R. L., Zhao, C., Heald, C. L., Ward, D. S., Albani, S., and Haustein, K.: Smaller desert dust cooling effect estimated from analysis of dust size and abundance, Nat. Geosci., 10, 274–278, https://doi.org/10.1038/ngeo2912, 2017.

Kok, J. F., Ward, D. S., Mahowald, N. M., and Evan, A. T.: Global and regional importance of the direct dust-climate feedback, Nat. Commun., 9, 241, https://doi.org/10.1038/s41467-017-02620-y, 2018.

Kok, J. F., Adebiyi, A. A., Albani, S., Balkanski, Y., Checa-Garcia, R., Chin, M., Colarco, P. R., Hamilton, D. S., Huang, Y., Ito, A., Klose, M., Leung, D. M., Li, L., Mahowald, N. M., Miller, R. L., Obiso, V., Pérez García-Pando, C., Rocha-Lima, A., Wan, J. S., and Whicker, C. A.: Improved representation of the global dust cycle using observational constraints on dust properties and abundance, Atmos. Chem. Phys., 21, 8127–8167, https://doi.org/10.5194/acp-21-8127-2021, 2021.

Lacagnina, C., Hasekamp, O. P., Bian, H., Curci, G., Myhre, G., van Noije, T., Schulz, M., Skeie, R. B., Takemura, T., and Zhang, K.: Aerosol single-scattering albedo over the global oceans: Comparing PARASOL retrievals with AERONET, OMI, and AeroCom models estimates, J. Geophys. Res., 120, 9814–9836, https://doi.org/10.1002/2015JD023501, 2015.

Laskin, A., Iedema, M. J., Ichkovich, A., Graber, E. R., Taraniukb, I., and Yinon, R.: Direct observation of completely processed calcium carbonate dust particles, Faraday Discuss., 130, 453–468, https://doi.org/10.1039/B417366J, 2005.

679   Lau, K. M., Kim, K. M., Sud, Y. C., and Walker, G. K.: A GCM study of the response of the atmospheric water cycle

680   of West Africa and the Atlantic to Saharan dust radiative forcing, Ann. Geophys., 27, 4023–4037,

681   https://doi.org/10.5194/angeo-27-4023-2009, 2009.

682   Li, F., Vogelmann, A. M., and Ramanathan, V.: Dust aerosol radiative forcing measured from space over the Western

683   Africa,   J.   Climate,   17(13),   2558–2571,   https://doi.org/10.1175/1520-

684   0442(2004)017<2558:SDARFM>2.0.CO;2, 2004.

685   Li, L., and Sokolik, I. N.: The dust direct radiative impact and its sensitivity to the land surface state and key minerals

686   in the WRF-Chem-DuMo model: A case study of dust storms in Central Asia, J. Geophys. Res.-Atmos., 123,

687   4564–4582, https://doi.org/10.1029/2017JD027667, 2018.

688   Liao, H. and Seinfeld, J.: Radiative forcing by mineral dust aerosols: sensitivity to key variables, J. Geophys. Res.,

689   103, 31637–31645, https://doi.org/10.1029/1998JD200036, 1998.

690   Liu, X. H., Penner, J. E. and Herzog, M.: Global modeling of aerosol dynamics: Model description, evaluation, and

691   interactions   between   sulfate   and   nonsulfate   aerosols,   J.   Geophys.   Res.,   110,   D18206,

692   doi:10.1029/2004jd005674, 2005.

693   Long, L. L., Querry, M. R., Bell, R. J., and Alexander, R. W.: Optical properties of calcite and gypsum in crystalline

694   and   powdered   form   in   the   infrared   and   far-infrared,   Infrared   Phys.,   34,   191–201,

695   https://doi.org/10.1016/0020-0891(93)90008-U, 1993.

696   Lucarini, V., Saarinen, J. J., Peiponen, K.-E., and Vartiainen, E. M.: Kramers-Kronig relations in optical materials

697   research, vol. 110, Switzerland: Springer Science & Business Media, 2005.

698   Mahowald, N., Albani, S., Kok, J. F., Engelstaeder, S., Scanza, R., Ward, D. S., and Flanner, M. G.: The size

699   distribution of desert dust aerosols and its impact on the Earth system, Aeolian Res., 15, 53–71, 2014,

700   https://doi.org/10.1016/j.aeolia.2013.09.002, 2014.

701   Matsuki, A., Iwasaka, Y., Shi, G., Zhang, D., Trochkine, D., Yamada, M., Kim, Y.-S., Chen, B., Nagatani, T.,

702   Miyazawa, T., Nagatani, M., and Nakata, H.: Morphological and chemical modification of mineral dust:

703   Observational insight into the heterogeneous uptake of acidic gases, Geophys. Res. Lett., 32, L22806,

704   https://doi.org/10.1029/2005gl024176, 2005.

705   Meinshausen, M., Vogel, E., Nauels, A., Lorbacher, K., Meinshausen, N., Etheridge, D. M., Fraser, P. J., Montzka, S.

706   A., Rayner, P. J., Trudinger, C. M., Krummel, P. B., Beyerle, U., Canadell, J. G., Daniel, J. S., Enting, I. G.,

707   Law, R. M., Lunder, C. R., O'Doherty, S., Prinn, R. G., Reimann, S., Rubino, M., Velders, G. J. M., Vollmer,

708   M. K., Wang, R. H. J., and Weiss, R.: Historical greenhouse gas concentrations for climate modelling

709   (CMIP6), Geosci. Model Dev., 10, 2057–2116, https://doi.org/10.5194/gmd-10-2057-2017, 2017.

Meng, Z., Yang, P., Kattawar, G. W., Bi, L., Liou, K. N., and Laszlo, I.: Single-scattering properties of tri-axial ellipsoidal mineral dust aerosols: a database for application to radiative transfer calculations, J. Aerosol Sci., 41, 501–512, https://doi.org/10.1016/j.jaerosci.2010.02.008, 2010.

Miller, R. L. and Tegen, I.: Climate response to soil dust aerosols, J. Climate, 11, 3247–3267, https://doi.org/10.1175/1520-0442(1998)011<3247:CRTSDA>2.0.CO;2, 1998.

Miller, R. L., Perlwitz, J., and Tegen, I.: Feedback upon dust emission by dust radiative forcing through the planetary boundary layer, J. Geophys. Res., 109, D24209, doi:10.1029/2004JD004912, 2004a.

Miller, R. L., Tegen, I., and Perlwitz, J.: Surface radiative forcing by soil dust aerosols and the hydrologic cycle, J. Geophys. Res., 109, D04203, https://doi.org/10.1029/2003JD004085, 2004b.

Miller, R. L., Knippertz, P., Pérez García-Pando, C., Perlwitz, J. P., and Tegen, I.: Impact of dust radiative forcing upon climate, in: Mineral Dust: A Key Player in the Earth System, edited by: Knippertz, P. and Stuut, J.-B. W., Springer, 327–357, doi:10.1007/978-94-017-8978-3_13, 2014.

Myriokefalitakis, S., Ito, A., Kanakidou, M., Nenes, A., Krol, M. C., Mahowald, N. M., Scanza, R. A., Hamilton, D. S., Johnson, M. S., Meskhidze, N., Kok, J. F., Guieu, C., Baker, A. R., Jickells, T. D., Sarin, M. M., Bikkina, S., Shelley, R., Bowie, A., Perron, M. M. G., and Duce, R. A.: Reviews and syntheses: the GESAMP atmospheric iron deposition model intercomparison study, Biogeosciences, 15, 6659–6684, https://doi.org/10.5194/bg-15-6659-2018, 2018.

~~Penner, J. E., Zhou, C., Garnier, A., and Mitchell, D. L.: Anthropogenic aerosol indirect effects in cirrus clouds. J. Geophys. Res., 123, 11,652–11,677. https://doi.org/10.1029/2018JD029204, 2018.~~

Penner, J.: Soot, sulfate, dust and the climate—Three ways through the fog. Nature, 570, 158–159, https://doi.org/10.1038/d41586-019-01791-6, 2019.

Perlwitz, J., Tegen, I., and Miller, R.: Interactive soil dust aerosol model in the GISS GCM 1. Sensitivity of the soil dust cycle to radiative properties of soil dust aerosols, J. Geophys. Res., 106(D16), 18,167–18,192, https://doi.org/10.1029/2000JD900668, 2001

Räisänen, P., Haapanala, P., Chung, C. E., Kahnert, M., Makkonen, R., Tonttila, J., and Nousiainen, T.: Impact of dust particle nonsphericity on climate simulations, Q. J. Roy. Meteor. Soc., 139, 2222–2232, https://doi.org/10.1002/qj.2084, 2013.

Reichle, R. H., de Lannoy, G., Koster, R. D., Crow, W. T., Kimball, J. S., and Liu, Q.: SMAP L4 global 3-hourly 9 km EASE-grid surface and root zone soil moisture geophysical data, version 4. NASA National Snow and Ice Data Center Distributed Active Archive Center, https://doi.org/10.5067/kpjnn2gi1dqr, 2018.

Reichle, R. H., Liu, Q., Koster, R. D., Crow, W. T., De Lannoy, G. J. M., Kimball, J. S., Ardizzone, J. V., Bosch, D., Colliander, A., Cosh, M., Kolassa, J., Mahanama, S. P., Prueger, J., Starks, P., and Walker, J. P.: Version 4

742 of the SMAP Level-4 Soil Moisture algorithm and data product. J. Adv. Model Earth Syst., 11, 3106–3130,

743 https://doi.org/10.1029/2019MS001729, 2019.

744 Reid, E. A., Reid, J. S., Meier, M. M., Dunlap, M. R., Cliff, S. S., Broumas, A., Perry, K., and Maring, H.:

745 Characterization of African dust transported to Puerto Rico by individual particle and size segregated bulk

746 analysis, J. Geophys. Res., 108, 8591, https://doi.org/10.1029/2002JD002935, D19, 2003.

747 Ridley, D. A., Heald, C. L., Kok, J. F., and Zhao, C.: An observationally constrained estimate of global dust aerosol

748 optical depth, Atmos. Chem. Phys., 16, 15097–15117, https://doi.org/10.5194/acp-16-15097-2016, 2016.

749 Rosenberg, P. D., Parker, D. J., Ryder, C. L., Marsham, J. H., Garcia-Carreras, L., Dorsey, J. R., Brooks, I. M., Dean,

750 A. R., Crosier, J., McQuaid, J. B., andWashington, R.: Quantifying particle size and turbulent scale

751 dependence of dust flux in the Sahara using aircraft measurements, J. Geophys. Res.-Atmos., 119, 7577–

752 7598, https://doi.org/10.1002/2013JD021255, 2014.

753 Ryder, C. L., Highwood, E. J., Lai, T. M., Sodemann, H., and Marsham, J. H.: Impact of atmospheric transport on the

754 evolution of microphysical and optical properties of Saharan dust, Geophys. Res. Lett., 40, 2433–2438,

755 https://doi.org/10.1002/grl.50482, 2013.

756 Ryder, C. L., Highwood, E. J., Walser, A., Seibert, P., Philipp, A., and Weinzierl, B.: Coarse and giant particles are

757 ubiquitous in Saharan dust export regions and are radiatively significant over the Sahara, Atmos. Chem.

758 Phys., 19, 15353–15376, https://doi.org/10.5194/acp-19-15353-2019, 2019.

759 Sicard, M., Bertolín, S., Mallet, M., Dubuisson, P., and Comerón, A.: Estimation of mineral dust long-wave radiative

760 forcing: sensitivity study to particle properties and application to real cases in the region of Barcelona, Atmos.

761 Chem. Phys., 14, 9213–9231, https://doi.org/10.5194/acp-14-9213-2014, 2014.

762 Sokolik, I. N., Toon, O. B., and Bergstrom, R. W.: Modeling the radiative characteristics of airborne mineral aerosols

763 at infrared wavelengths, J. Geophys. Res., 103, 8813–8826, https://doi.org/10.1029/98JD00049, 1998.

764 Sokolik, I. N. and Toon, O. B.: Incorporation of mineralogical composition into models of the radiative properties of

765 mineral aerosol from UV to IR wavelengths, J. Geophys. Res., 104(D8), 9423–9444,

766 https://doi.org/10.1029/1998JD200048, 1999.

767 Song, Q., Zhang, Z., Yu, H., Kato, S., Yang, P., Colarco, P., Remer, L. A., and Ryder, C. L.: Net radiative effects of

768 dust in the tropical North Atlantic based on integrated satellite observations and in situ measurements, Atmos.

769 Chem. Phys., 18, 11303–11322, https://doi.org/10.5194/acp-18-11303-2018, 2018.

770 Stegmann, P. G. and Yang, P.: A regional, size-dependent, and causal effective medium model for Asian and Saharan

771 mineral dust refractive index spectra, J. Aerosol Sci., 114, 327–341,

772 https://doi.org/10.1016/j.jaerosci.2017.10.003, 2017.

773 Takemura, T., Egashira, M., Matsuzawa, K., Ichijo, H., O'ishi, R., and Abe-Ouchi, A.: A simulation of the global
774   distribution and radiative forcing of soil dust aerosols at the Last Glacial Maximum, Atmos. Chem. Phys., 9,
775   3061–3073, https://doi.org/10.5194/acp-9-3061-2009, 2009.

776 Tanaka, T. Y., Aoki, T., Takahashi, H., Shibata, K., Uchiyama, A., and Mikami, M.: Study of the sensitivity of optical
777   properties of mineral dust to the direct aerosol radiative perturbation using a global aerosol transport model,
778   SOLA, 3, 33–36, https://doi.org/10.2151/sola.2007-009, 2007.

779 Taylor, K.E., 2001. Summarizing multiple aspects of model performance in a single diagram. Journal of Geophysical
780   Research-Atmospheres 106, 7183-7192.

781 Tegen, I. and Lacis, A.: Modeling of particle size distribution and its influence on the radiative properties of mineral
782   dust aerosol, J. Geophys. Res., 101, 19237–19244, https://doi.org/10.1029/95JD03610, 1996.

783 Toth III, J. R., Rajupet, S., Squire, H., Volbers, B., Zhou, J., Xie, L., Sankaran, R. M., and Lacks, D. J.: Electrostatic
784   forces alter particle size distributions in atmospheric dust, Atmos. Chem. Phys., 20, 3181–3190,
785   https://doi.org/10.5194/acp-20-3181-2020, 2020.

786 Tuccella, P., Curci, G., Pitari, G., Lee, S., and Jo, D. S.: Direct radiative effect of absorbing aerosols: sensitivity to
787   mixing state, brown carbon and soil dust refractive index and shape, J. Geophys. Res.-Atmos., 125,
788   e2019JD030967, https://doi.org/10.1029/2019JD030967, 2020.

789 van der Does, M., Korte, L. F., Munday, C. I., Brummer, G.-J. A., and Stuut, J.-B. W.: Particle size traces modern
790   Saharan dust transport and deposition across the equatorial North Atlantic, Atmos. Chem. Phys., 16, 13697–
791   13710, https://doi.org/10.5194/acp-16-13697-2016, 2016.

792 van der Does, M., Knippertz, P., Zschenderlein, P., Giles Harrison, R., and Stuut, J.-B. W.: The mysterious long-range
793   transport of giant mineral dust particles, Sci. Adv., 4, eaau2768, https://doi.org/10.1126/sciadv.aau2768,
794   2018.

795 Volz, F.: Infrared optical constants of aerosols at some locations, Appl. Optics, 22, 23, 3690–3700,
796   https://doi.org/10.1364/AO.11.000755, 1983.

797 Wagner, R., Ajtai, T., Kandler, K., Lieke, K., Linke, C., Müller, T., Schnaiter, M., and Vragel, M.: Complex refractive
798   indices of Saharan dust samples at visible and near UV wavelengths: a laboratory study, Atmos. Chem. Phys.,
799   12, 2491–2512, https://doi.org/10.5194/acp-12-2491-2012, 2012.

800 Wan, Z., Hook, S., and Hulley, G.: MOD11C2 MODIS/Terra Land Surface Temperature/Emissivity 8-Day L3 Global
801   0.05Deg   CMG   V006   [Data   set].   NASA   EOSDIS   Land   Processes   DAAC,
802   https://doi.org/10.5067/MODIS/MOD11C2.006, 2015.

803 Wang, M. and Penner, J. E.: Aerosol indirect forcing in a global model with particle nucleation, Atmos. Chem. Phys.,
804   9, 239–260, https://doi.org/10.5194/acp-9-239-2009, 2009.

805   Wiegner, M., Gasteiger, J., Kandler, K., Weinzierl, B., Rasp, K., Esselborn, M., Freudenthaler, V., Heese, B.,

806   Toledano, C., Tesche, M., and Althausen, D.: Numerical simulations of optical properties of Saharan dust

807   aerosols with emphasis on lidar applications, Tellus B, 61, 180–194, https://doi.org/10.1111/j.1600-

808   0889.2008.00381.x, 2009.

809   Xu, L. and Penner, J. E.: Global simulations of nitrate and ammonium aerosols and their radiative effects, Atmos.

810   Chem. Phys., 12, 9479–9504, https://doi.org/10.5194/acp-12-9479-2012, 2012.

811   Yang, E.-S., Gupta, P., and Christopher, S. A.: Net radiative effect of dust aerosols from satellite measurements over

812   Sahara, Geophys. Res. Lett., 36, L18812, https://doi.org/10.1029/2009GL039801, 2009.

813   Yoshioka, M., Mahowald, N., Conley, A. J., Collins, W. D., Fillmore, D.W., Zender, C. S., and Coleman, D. B.:

814   Impact of desert dust radiative forcing on Sahel precipitation: relative importance of dust compared to sea

815   surface temperature variations, vegetation changes and greenhouse gas warming, J. Climate, 16, 1445–1467,

816   https://doi.org/10.1175/JCLI4056.1, 2007.

817   Zhang, D., and Iwasaka, Y.: Size change of Asian dust particles caused by sea salt interaction: Measurements in

818   southwestern Japan, Geophys. Res. Lett., 31, L15102, https://doi.org/10.1029/2004GL020087, 2004.

819   Zhang, J. and Christopher, S. A.: Longwave radiative forcing of Saharan dust aerosols estimated from MODIS, MISR,

820   and CERES observations on Terra, Geophys. Res., Lett., 30(23), 2188,

821   https://doi.org/10.1029/2003GL018479, 2003.

822   Zhao, C., Chen, S., Leung, L. R., Qian, Y., Kok, J. F., Zaveri, R. A., and Huang, J.: Uncertainty in modeling dust mass

823   balance and radiative forcing from size parameterization, Atmos. Chem. Phys., 13, 10733–10753,

824   https://doi.org/10.5194/acp-13-10733-2013, 2013.

825   Zhou, Y., Levy, R. C., Remer, L. A., Mattoo, S., and Espinosa, W. R.: Dust aerosol retrieval over the oceans with the

826   MODIS/VIIRS dark target algorithm: 2. Nonspherical dust model, Earth Space Sci., 7, e2020EA001222,

827   https://doi.org/10.1029/2020EA001222, 2020.

	Figure captions

829	Figure 1.	Imaginary part of the refractive index at (a) 0.52 µm, (b) SW, (c) 9.7 µm, and (d) LW for the nine

830	main source regions and the global mean for others. The refractive index obtained from 19 samples was

831	aggregated into 9 main source regions and the arithmetic mean was calculated for each source region (Di

832	Biagio et al., 2017, 2019). The global mean is used for others. The coordinates of the nine source regions

833	were: (S1) western North Africa (20°W – 7.5°E; 18°N – 37.5°N), (S2) eastern North Africa (7.5°E – 35°E;

834	18°N – 37.5°N), (S3) the Sahel (20°W – 35°E; 0°N – 18°N), (S4) Middle East / Central Asia (30°E – 70°E

835	for 0°N – 35°N, and 30°E – 75°E for 35°N – 50°N), (S5) East Asia (70°E – 120°E; 35°N – 50°N), (S6) North

836	America (130°W – 80°W; 20°N – 45°N), (S7) Australia (110°E – 160°E; 10°S – 40°S), (S8) South America

837	(80°W – 20°W; 0°S – 60°S), and (S9) Southern Africa (0°E – 40°E; 0°S – 40°S).

838	Figure 2.	The model better reproduced semi-observationally-based data of $DAOD_{550}$ after adjusting the size-

839	resolved dust load with DustCOMM and considering the dust asphericity. (a) semi-observationally-based

840	estimates of the $DAOD_{550}$ were averaged over 2004–2008 (Ridley et al., 2016; Adebiyi et al., 2020). The

841	annually averaged model results were shown for (b) DustCOMM-Asphere-DB19-V83 (E2) and (c) the

842	differences between IMPACT-Sphere-Mineral-V83 (E1) and E2 simulations. (d) Comparison of seasonally

843	averaged $DAOD_{550}$ for semi-observationally-based (SOB) data, E1, E2, IMPACT-Asphere-DB19-DB17

844	(E3), and DustCOMM-Sphere-DB19-DB17 (E5). The square symbol represents the mean. The solid line

845	within the box mark shows the median. The boundaries of the box mark the 25th and 75th percentiles. The

846	whiskers above and below the box indicate the $1.5 \times$ interquartile range, and the points indicate the outside

847	of the range. (e) Taylor diagram summarizing the statistics of the comparison against the seasonally averaged

848	regional $DAOD_{550}$ for the different experiments. The horizontal axis shows the standard deviation of the data

849	set or model prediction, the curved axis shows the correlation, and the green dashed lines denote the root-

850	mean-squared errors between the semi-observationally-based data and the model predictions. As such, the

851	distance between the semi-observationally-based data and the model predictions is a measure of the model's

852	ability to reproduce the spatiotemporal variability in the semi-observationally-based data. The coordinates of

853	the fifteen regions were: (A1) Mid Atlantic (4° 40°N, 50° 20°W), (A2) African West Coast (10° 34°N,

854	20° 5°W), (A3) Northern Africa (26° 40°N, 5°W 30°E), (A4) Mali/Niger (10° 26°N, 5°W 10°E), (A5)

855	Bodele/Sudan (10° 26°N, 10° 40°E), (A6) Northern Middle East (26° 40°N, 30° 50°E), (A7) Southern

856	Middle East (0° 26°N, 40° 67.5°E), (A8) Kyzyl Kum (26° 50°N, 50° 67.5°E), (A9) Thar (20° 50°N,

857	67.5° 75°E), (A10) Taklamakan (30° 50°N, 75° 92.5°E), (A11) Gobi (36° 50°N, 92.5° 115°E), (A12)

858	North America (20° 45°N, 80° 130°W), (A13) South America (0° 55°S, 80° 55°W), (A14) Southern

859	Africa (10° 35°S, 10° 40°E), and (A15) Australia (10° 40°S, 110° 160°E). and Tthe values of $DAOD_{550}$ at

860 the 15 regions (marked in Fig. 3a) in summer were listed in Table S1. The comparison for other seasons was

861 presented in Table S2.

862 Figure 3. Model-simulated dust loads at fine (smaller than 2.5 µm of diameter) and coarse size ranges (larger

863 than 2.5 µm of diameter) before and after adjusting the size-resolved dust load with DustCOMM. Results

864 were shown for (a) fine dust from DustCOMM, (b) fine dust from IMPACT-Sphere-Mineral-V83 (E1), (c)

865 fine dust from DustCOMM-Asphere-DB19-V83 (E2), (d) coarse dust from DustCOMM, (e) coarse dust from

866 E1, and (f) coarse dust from E2 simulations. The parentheses represented the global dust burden (Tg). The

867 values of dust load at each bin were listed in Table 3.

868 Figure 4. Dust clear-sky SW radiative effect efficiency (W·m^{-2} DAOD^{-1}). Semi-observationally-based data

869 at (a) the surface and (b) TOA were based on satellite observations (Yang et al. 2009; Li et al., 2004: Song

870 et al., 2018; Christopher and Jones, 2007). The model results were shown for (c) and (d) IMPACT-Sphere-

871 Mineral-V83 (E1), and (e) and (f) DustCOMM-Asphere-DB19-V83 (E2) simulations at the surface and TOA,

872 respectively. (g) Comparison of seasonally averaged SW radiative effect efficiency for semi-observationally-

873 based (SOB) data and the different experiments at (g) the surface and (h) TOA. The square symbol represents

874 the mean. The solid line within the box mark shows the median. The boundaries of the box mark the 25th

875 and 75th percentiles. The whiskers above and below the box indicate the 1.5 × interquartile range, and the

876 points indicate the outside of the range. (h) Taylor diagram summarizing the statistics of the comparison

877 against the seasonally averaged regional SW radiative effect efficiency for the different experiments at (i)

878 the surface and (j) TOA. The horizontal axis shows the standard deviation of the data set or model prediction,

879 the curved axis shows the correlation, and the green dashed lines denote the root-mean-squared errors

880 between the semi-observationally-based data and the model predictions. As such, the distance between the

881 semi-observationally-based data and the model predictions is a measure of the model's ability to reproduce

882 the spatiotemporal variability in the semi-observationally-based data. The regionally averaged values were

883 listed in Tables S3 and S4 at the surface and TOA, respectively.

884 Figure 5. Dust clear-sky LW radiative effect efficiency (W·m^{-2} DAOD^{-1}). Semi-observationally-based

885 estimates at (a) surface and (b) TOA were based on satellite observations (Song et al., 2018; Christopher and

886 Jones, 2007; Zhang and Christopher, 2003; Brindley and Russell, 2009; Yang et al., 2009). The model results

887 were shown for (c) and (d) IMPACT-Sphere-Mineral-V83 (E1), and (e) and (f) DustCOMM-Asphere-DB19-

888 V83 (E2) simulations at the surface and TOA, respectively. (g) Comparison of seasonally averaged LW

889 radiative effect efficiency for semi-observationally-based (SOB) data and the different experiments at (g) the

890 surface and (h) TOA. The square symbol represents the mean. The solid line within the box mark shows the

891 median. The boundaries of the box mark the 25th and 75th percentiles. The whiskers above and below the

892 box indicate the 1.5 × interquartile range, and the points indicate the outside of the range. ~~(h)~~ Taylor diagram

893 summarizing the statistics of the comparison against the seasonally averaged regional SW radiative effect

894 efficiency for the different experiments at (i) the surface and (j) TOA. The horizontal axis shows the standard

895 deviation of the data set or model prediction, the curved axis shows the correlation, and the green dashed

896 lines denote the root-mean-squared errors between the semi-observationally-based data and the model

897 predictions. As such, the distance between the semi-observationally-based data and the model predictions is

898 a measure of the model's ability to reproduce the spatiotemporal variability in the semi-observationally-based

899 data. The regionally averaged values were listed in Tables S5 and S6 at the surface and TOA, respectively.

900 Figure 6. Dust SW radiative effect (W·m^{-2}) and radiative heating of the atmosphere (i.e., the subtraction of

901 radiative effects from TOA to the surface in unit of W·m^{-2}). The model results were shown for the simulations

902 for (a) IMPACT-Sphere-Mineral-V83 (E1) at the surface, (b) DustCOMM-Asphere-DB19-V83 (E2) at the

903 surface, (c) E1 in atmospheric column, (d) E2 in atmospheric column, (e) E1 at TOA, and (f) E2 simulations

904 at TOA. The numbers in parentheses represented the global mean.

905 Figure 7. Dust LW radiative effect (W·m^{-2}) and radiative heating of the atmosphere (i.e., the subtraction of

906 radiative effects from TOA to the surface in unit of W·m^{-2}). The model results were shown for the simulations

907 for (a) IMPACT-Sphere-Mineral-V83 (E1) at the surface, (b) DustCOMM-Asphere-DB19-V83 (E2) at the

908 surface, (c) E1 in atmospheric column, (d) E2 in atmospheric column, (e) E1 at TOA, and (f) E2 simulations

909 at TOA. The numbers in parentheses represented the global mean.

910 Figure 8. Dust net radiative effect (W·m^{-2}) and radiative heating of the atmosphere (i.e., the subtraction of

911 radiative effects from TOA to the surface in unit of W·m^{-2}). The model results were shown for the simulations

912 for (a) IMPACT-Sphere-Mineral-V83 (E1) at the surface, (b) DustCOMM-Asphere-DB19-V83 (E2) at the

913 surface, (c) E1 in atmospheric column, (d) E2 in atmospheric column, (e) E1 at TOA, and (f) E2 simulations

914 at TOA. The numbers in parentheses represented the global mean.

915 Figure 9. Variability of dust R~~r~~adiative effect (W·m^{-2}) ~~of mineral dust due to~~in different model

916 simulations~~studies~~ at the surface and TOA for (a) total dust SW, (b) total dust LW, and (c) total dust NET.

917 The annually averaged values were listed in Table 5.

918 Figure 10. Radiative effect (W·m^{-2}) of mineral dust due to various aerosol absorptivity at the surface and TOA

919 for (a) total dust SW, (b) total dust LW, and (c) total dust NET. The annually averaged values were listed in

920 Table 5. The dashed line represented a 1 : 1 correspondence and corresponded to no change in radiative

921 heating within the atmosphere.