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Ozone-Gravity Wave Interaction in the Upper Stratosphere/Lower Mesosphere

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Abstract. The increase in amplitudes of upward propagating gravity waves (GWs) with height due to decreasing density is usually described by exponential growth. Recent measurements indicate a stronger increase in the upper stratospheric/lower mesospheric gravity wave potential energy density (GWPED) during daylight than nighttime, which is unexplained up to
30 now. This paper suggests that ozone-gravity wave interaction might significantly contribute to this phenomenon. The coupling between ozone-photochemistry and temperature is particularly strong in the upper stratosphere where the time-mean ozone mixing ratio is decreasing with height; therefore, an initial ascent (or descent) of an air parcel must lead to a local increase (or decrease) in ozone and in the heating rate compared to the environment, and, hence, to an amplification of the initial wave perturbation. Standard solutions of upward propagating GWs with linear ozone-temperature coupling are
35 formulated suggesting local amplitude amplifications during daylight of 5 to 15% for low-frequency GWs (periods ≥ 4 hours), as a function of the intrinsic frequency which decreases if ozone-temperature coupling is included. Subsequently, for horizontal wavelengths larger than 500 km and vertical wavelengths smaller than 5 km, the cumulative amplification during the upward level-by-level propagation leads to much stronger amplitudes in the GW perturbations (factor of about 1.5 to 3) and in the GWPED (factor of about 3 to 9) at upper mesospheric altitudes. Conclusively, the identified process amplifies a
40 wide range of mesoscale GWs which are an important driver of the middle atmospheric circulation. The results open a new viewpoint for improving general circulation models with resolved or parameterized GWs.

1 Introduction

Atmospheric gravity waves (GWs), with horizontal wavelengths of 100 km to 2000 km, are produced in the troposphere and propagate vertically through the stratosphere and mesosphere, where gravity wave breaking processes are an important
45 driver of the middle atmospheric circulation (e.g., Andrews et al., 1986; Fritts and Alexander, 2003). Usually, upward propagating GWs are described by sinusoidal wave perturbations in a slowly varying background flow with an exponentially growing amplitude with height due to decreasing density ($\sim e^{z/2H}$, where H is the scale height). Recent Lidar measurements indicate that the growth of the GW amplitudes between middle stratosphere and lower mesosphere is obviously stronger during daylight than nighttime, which is unexplained up to now (Baumgarten et al., 2017). The aim of the present paper is to
50 examine whether ozone-gravity wave interaction can principally produce such an amplification.

Baumgarten et al. (2017) derived **monthly means** of the GWPED from full-day Lidar temperature measurements at northern mid-latitudes (54°N, 12°E), and found a **much stronger relative increase between 35-40 km and 55-60 km for full-day than nighttime observations during summer months**, but less pronounced differences during winter. Generally, measurements of the mesospheric GWPED are much more uncertain during summer than winter months (e.g., Kaifler et al., 2015; Ehard et al., 2015; Baumgarten et al., 2017). Taking the potential uncertainties of the analyzing methods into account (i.e., the temporal filtering methods used for the measured time series), Baumgarten et al. (2017) speculated that a change in the phase of long periodic waves (e.g., diurnal and semidiurnal tides) could change the filtering conditions for GWs. However, conclusively Baumgarten et al. (2017) assumed that the detected daylight-nighttime differences are of true geophysical origin, where an unequivocal explanation of this phenomenon remained open. Considering also that full-day observations of Baumgarten et al. (2018) during May 2016 showed pronounced GW activity particularly at altitudes between 42 km and 50 km, where the coupling between ozone and temperature is particularly strong, it seems to be worthwhile to examine whether ozone-gravity wave interaction could principally contribute to the indicated daylight-nighttime differences.

The coupling of temperature and ozone is particularly strong in the upper stratosphere due to the short photochemical lifetime of ozone (e.g., Brasseur and Solomon, 1995). Linear relationships for a change in the heating rate due to a change in ozone, and a change in photochemistry due to a change in temperature, were derived from basic theory or satellite observations, and have been introduced in standard equations of stratospheric dynamics to examine the effects on the stratospheric circulation, planetary-scale wave patterns and equatorial Kelvin waves (Dickinson, 1973; Douglass et al., 1985; Froidevaux et al., 1989; Cordero et al. 1998, 2000; Nathan et al., 2007; Ward et al., 2010; Gabriel et al., 2011a). Large-scale ozone-dynamic coupling processes show also significant effects in numerical weather prediction or general circulation models (Cariolle and Morcrette, 2006; Gabriel et al., 2007, 2011b; Gillet et al., 2009; Waugh et al., 2009; McCormack et al., 2011; Albers et al., 2013). However, possible effects of mesoscale ozone-gravity wave interaction in the upper stratosphere/lower mesosphere (USLM) have not been considered up to now.

The basic idea of the present paper can be summarized as follows. In the USLM, the time-mean ozone mixing ratio $\mu_0(z)$ is decreasing with height ($\partial\mu_0/\partial z < 0$). Therefore, a local **ascending** air parcel initially forced by an upward propagating **sinusoidal GW pattern (i.e., the wave crest with vertical velocity perturbation $w' > 0$)** must lead to a local increase $\partial\mu'/\partial t > 0$ by both transport (because $-w'\partial\mu_0/\partial z > 0$) and photochemistry (because the temperature-dependent ozone production increases in case of adiabatic cooling), and, hence, in the heating rate $Q'(\mu') > 0$, comparable to the latent heat release in the troposphere in case of condensation. Then, the induced perturbation $\Delta\theta' > 0$ (θ is potential temperature) reinforces the initial **ascent**, where the lapse rate $\partial(\theta_0 + \Delta\theta')/\partial z < \partial\theta_0/\partial z$ decreases ($\partial z = \text{constant}$) suggesting an effective *ozone adiabatic lapse rate* in the upper stratosphere **comparable** to the *moist adiabatic lapse rate* in the troposphere. **Analogously, a local descending air parcel (the wave trough where $w' < 0$) leads to a decrease $\partial\mu'/\partial t < 0$ and a corresponding change $Q'(\mu') < 0$, reinforcing the initial descent.** Overall, this process must lead to a significant local amplification of the initial GW amplitude and, hence, to a **successive amplification of the amplitude** during the upward level-by-level propagation through the USLM.

In Section 2, standard equations for GWs in a zonal mean background flow with and without linearized ozone-temperature coupling are formulated to quantify the local amplitude amplification at a specific altitude and latitude. Then, in section 3, the cumulative amplitude amplification during the propagation through the USLM is derived, based on an idealized approach of the upward level-by-level propagation of GWs with specific horizontal and vertical wavelengths. Section 4 concludes with summary and discussion.

90 2. Ozone-gravity wave interaction

In the following, ozone-gravity wave interaction is analysed based on standard equations describing GWs in a background atmosphere, where the solutions are illustrated for southern summer conditions. The background is prescribed by monthly and zonal mean temperature T_0 , ozone μ_0 and short-wave heating rate Q_0 of January 2001 (Figure 1, a-c) derived from a simulation with the high-altitude general circulation and chemistry model HAMMONIA (details of the model are given by Schmidt et al., 2010). The heating rate Q_0 (Figure 1c) is primarily due to the absorption of solar radiation by ozone and largely agrees with southern summer solar heating rates derived from satellite measurements by Gille and Lyjak (1986) but with somewhat smaller maximum values (in the order of $\sim 10\%$). Figure 1c shows that Q_0 is particularly strong in the upper stratosphere and lower mesosphere (USLM) where $\partial\mu_0/\partial z < 0$ (the dashed line in Figure 1b indicates $\partial\mu_0/\partial z = 0$). The HAMMONIA model includes 119 layers up to 250 km with increasing vertical resolution between ~ 0.7 km in the middle stratosphere and ~ 1.4 km in the middle mesosphere, with a horizontal resolution of 3.75° ; in the following, this grid is used to illustrate the analytic solutions of upward propagating GWs.

2.1 Local amplification of gravity wave amplitudes

2.1.1 Basic equations

105 Following Fritts and Alexander (2001), we consider standard equations (1)-(5) describing gravity wave propagation in a background flow, with linear gravity wave perturbations T' , θ' , u' , v' , w' , p' and ρ' (T' is temperature, $\theta' = T'(p_0/p)^{\kappa}$ is potential temperature, $p(z)$ is pressure, $p_0 = 1000$ hPa, z is altitude, u' , v' and w' are zonal, meridional and vertical wind perturbations, p' and ρ' are the perturbations in pressure and density). Additionally, we include an ozone-dependent heating rate perturbation $Q'(\mu')$ in the temperature equation (Eq. 5), and Eq. (6) for the ozone perturbation μ' with a temperature-dependent perturbation in ozone photochemistry $S'(T')$, where $a(\phi, z) > 0$ and $b(\phi, z) > 0$ are linear coupling parameters as a function of latitude ϕ and altitude z specified below ($\rho_0(z) = \rho_{00} \exp^{-(z-z_0)/H}$ is background density, $H \sim 7$ km is scale height, ρ_{00} is a reference value at altitude z_0 , u_0 is a zonal mean background wind, $\mathbf{d}_0/dt = \partial/\partial t + u_0\partial/\partial x + v_0\partial/\partial y$ where $\partial/\partial x$ and $\partial/\partial y$ denote

the derivations in longitude and latitude, g is the gravity acceleration, f is the Coriolis parameter; the background shear terms $w'\partial u_0/\partial z$ and $w'\partial v_0/\partial z$ are neglected because of the Wentzel-Kramers-Brillouin or WKB approximation):

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$$\frac{d_0 u'}{dt} + \frac{1}{\rho_0} \frac{\partial p'}{\partial x} = f v' \quad (1)$$

$$\frac{d_0 v'}{dt} + \frac{1}{\rho_0} \frac{\partial p'}{\partial y} = -f u' \quad (2)$$

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$$\frac{d_0 w'}{dt} + \frac{1}{\rho_0} \frac{\partial p'}{\partial z} = g \frac{\theta'}{\theta_0} \quad (3)$$

$$\frac{d_0 \rho'}{dt} + \frac{\partial u'}{\partial x} + \frac{\partial v'}{\partial y} + \frac{1}{\rho_0} \frac{\partial \rho_0 w'}{\partial z} = 0 \quad (4)$$

$$\frac{d_0 \theta'}{dt} + w' \frac{\partial \theta_0}{\partial z} = Q' \left(\frac{p_{00}}{p} \right)^\kappa = \frac{a}{\mu_0} \frac{d_0 \mu'}{dt} \quad (5)$$

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$$\frac{d_0 \mu'}{dt} + w' \frac{\partial \mu_0}{\partial z} = S' = -b \mu_0 \frac{d_0 \theta'}{dt} \quad (6)$$

Setting $Q'=0$, the dispersion relation for gravity waves results from Eqs. (1)-(5) by introducing sinusoidal perturbations $X_1' = X_{a0} \cdot \exp[i(k_1 x + l_1 y + m_1 z - \omega_1 t)] \cdot \exp^{(z-z_s)/2H}$, where X_1' denotes the perturbation quantities, X_{a0} the initial amplitude at
 130 altitude z_s at the lower boundary of the upper stratosphere, $\exp^{(z-z_s)/2H}$ the exponential growth of the amplitude due to decreasing density, k_1 and l_1 the horizontal and meridional wave number, $m_1 < 0$ the vertical wave number for upward propagating GWs with $|m_1| = 2\pi/L_{m1}$ and vertical wavelength L_{m1} , and ω_1 the frequency (here, the subscript 1 denotes the solutions for $Q'=0$). We focus on horizontal and vertical wavelengths $L_{h1} \geq 50$ km and $L_{m1} \leq 15$ km, where $k_{h1} = 2\pi/L_{h1}$ is the horizontal wave number given by $k_{h1} = (k_1^2 + l_1^2)^{1/2}$, therefore $(1 + k_{h1}^2/m_1^2) \approx 1$. Compressibility effects due to the vertical
 135 change in background density are excluded assuming $m_1^2 \gg 1/4H^2$, which is valid for vertical wavelengths $L_m \leq 30$ km. Then, the dispersion relation for the intrinsic frequency $\omega_{i1} = \omega_1 - k_1 u_0$ is given for the frequency range $N_0^2 > \omega_{i1}^2 > f^2$, where $N_0^2 = (g/\theta_0) \cdot \partial \theta_0 / \partial z$ denotes the Brunt-Vaisala frequency:

$$\omega_{i1}^2 = \frac{N_0^2 k_{h1}^2 + m_1^2 f^2}{k_{h1}^2 + m_1^2} \approx N_0^2 \frac{k_{h1}^2}{m_1^2} + f^2 \quad (7)$$

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2.1.2 Ozone-temperature coupling

For specifying the parameter b , we consider the vertical ascent $w'_1 > 0$ in the wave crest of an initial sinusoidal GW perturbation, related to an adiabatic cooling term $d_0\theta'_1/dt = -w'_1 \cdot \partial\theta_0/\partial z < 0$, which leads to an initial ozone perturbation $\mu'_1 > 0$ due to the induced increase $d_0\mu'_1/dt = -w'_1 \cdot \partial\mu_0/\partial z > 0$ via transport, and to a change in ozone photochemistry described by $S'(T'_1)$ (for the descent $w'_1 < 0$ in the wave trough, the formulations are analogously but with $\mu'_1 < 0$ and $d_0\theta'_1/dt = -w'_1 \cdot \partial\theta_0/\partial z > 0$). In the USLM region, ozone is very short lived and approximately in photochemical equilibrium (Brasseur and Solomon, 1995), i.e., for pure oxygen chemistry it is approximately given by

$$O_3 = \left(\frac{k_2}{k_3} M(O_2)^2 \frac{J_2(O_2)}{J_3(O_3)} \right)^{1/2} \quad (8)$$

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where $J_2(O_2)$ and $J_3(O_3)$ are photo-dissociation rates, and $k_2 = 6.0 \cdot 10^{-34} \cdot (300/T)^{2.3} \text{ cm}^6\text{s}^{-1}$ and $k_3 = 8.0 \cdot 10^{-12} \cdot \exp(-2060/T) \text{ cm}^3\text{s}^{-1}$ chemical reaction rates for ozone production, $O + O_2 + M \rightarrow O_3 + M$, and ozone loss, $O + O_3 \rightarrow 2O_2$ (Appendix C of Brasseur and Solomon, 1995; Table 2 of Schmidt et al., 2010). Accordingly, following Brasseur and Solomon (1995), a relative change in ozone $\Delta\mu_T/\mu_0 = \Delta O_3/O_3$ due to a change in temperature ΔT is given by

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$$\frac{\Delta\mu_T}{\mu_0} = \frac{1}{2} \frac{\Delta(k_2/k_3)}{(k_2/k_3)} = -\frac{1}{2} \left(\frac{2.3}{T_0} + \frac{2060}{T_0^2} \right) \Delta T \equiv -b_0(T_0) \Delta T \quad (9)$$

Then, defining $b = b_0 \cdot (p/p_{00})^k$ and introducing a total temperature change $\Delta T/\Delta t$ within a background flow described by $d_0T'/dt = (p/p_{00})^k \cdot d_0\theta'/dt$, the change S' is given by

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$$S' = \frac{\Delta\mu_T}{\Delta t} = \frac{\Delta\mu_T}{\Delta T} \frac{\Delta T}{\Delta t} = -\mu_0 b \frac{d_0\theta'}{dt} \quad (10)$$

which is the right-hand term of Eq. (6). Overall, the initial ascent $w'_1 > 0$ leads to a local increase in ozone via transport, and the related adiabatic cooling to an increase in ozone because of the induced change $S' > 0$; analogously, the initial descent $w'_1 < 0$ leads to a decrease in ozone via transport and an induced change $S' < 0$. The height-dependence of b is specified by considering that the ozone photochemistry of the USLM region is related to the spatial structure of Q_0 , which is characterized by a Gaussian-type height-dependence centered at the maximum of Q_0 and rapid decrease with latitude in the extra-tropical winter hemisphere (see Figure 1c). Therefore, b is multiplied with the normalized factor $hz = Q_0/Q_{00}$, where Q_{00} is the averaged profile of Q_0 over the summer hemisphere ($b \rightarrow b \cdot hz$, where $hz(z) \approx 1$ in the summer upper stratosphere at the

170 altitude where Q_0 reach maximum values). A similar approach of Gaussian-type height-dependence in ozone-temperature coupling was successfully used by Gabriel et al. (2011a) to analyze observed planetary-scale waves in the ozone distribution. Following previous works (e.g., Cordero and Nathan, 1998, 2000; Nathan et al., 2007; Ward et al., 2010; Gabriel et al., 2011a), the sensitivity of the upper stratospheric heating rate to a change in ozone is approximately described by the linear approach $\Delta Q_{\mu} \approx A \cdot \Delta \mu$, where $A = A(\rho, z)$ is a time-independent linear function. If we assume the same sensitivity for both the
 175 slowly varying background and the mesoscale GW perturbation propagating within the background flow, $Q_0 \approx A \cdot \mu_0$ and $Q' \approx A \cdot \mu'$, we may write $\Delta Q_{\mu} / \Delta \mu = Q_0 / \mu_0 = Q' / \mu'$. At a specific altitude z or pressure level $p(z)$, we consider a GW perturbation over the vertical scale of a vertical wavelength, $\Delta z = L_m$. Then, considering that $\partial \mu' / \partial z = i m \mu' = (\tau_i / L_m) \cdot (-i \omega_i \mu')$ with $\tau_i = 2\pi / \omega_i$, the first-order heating rate perturbation is given by

$$180 \quad Q' = L_m \frac{\partial Q'}{\partial z} \approx L_m \frac{\Delta Q_{\mu}}{\Delta \mu} \frac{\partial \mu'}{\partial z} = \tau_i \frac{Q_0}{\mu_0} \frac{d_0 \mu'}{dt} \quad (11)$$

which is the right-hand side of Eq. (5) when defining $a_0 = \tau_i Q_0$ and $a = a_0 \cdot (p_0/p)^{\kappa}$. Except in polar summer regions, the effect of Q' is limited by the length of daylight (here denoted by τ_{day}) in case of large wave periods; therefore, we set the time increment to $\tau_i = \tau_{\text{day}}$ in case of $\tau_i > \tau_{\text{day}}$, which reduces the effect of Q' during the time period of 24 hours (e.g., $\tau_i \leq 12$ hours
 185 over the equator). Overall, assuming again an initial ascent $w'_1 > 0$, the induced local increase in ozone $\mu' > 0$ at a pressure level $p(z)$ leads to a heating rate perturbation $Q' > 0$ at this level counteracting to the initial adiabatic cooling and therefore reinforcing the initial ascent. Analogously, an initial descent $w'_1 < 0$ is reinforced by inducing a perturbation $Q' < 0$.

Note here that the use of $\Delta z = L_m$ in Eq. (11) provides a suitable measure of the local effect of ozone-temperature coupling on the GW amplitudes over the vertical distance L_m . It is also possible to set a smaller vertical scale $\Delta z < L_m$ leading to smaller
 190 values $Q'_{\Delta z} = (\Delta z / L_m) \cdot Q'$ at a specific level, where Δz denotes, for example, the distances of a vertical grid used in a numerical model; this modification does not change the local effect over the vertical distance L_m but it provides better vertical resolution when calculating the cumulative amplitude amplification during the upward level-by-level propagation particularly in case of small vertical wavelengths or small vertical group velocities, as described in the next subsection.

195 2.1.3 Local amplification of GW amplitudes

The parameterizations of Q' and S' provide a useful modification of the temperature tendency when introducing $d_0 \mu' / dt$ of Eq. (6) into (Eq. 5):

$$(1+ab) \frac{d_0 \theta'}{dt} + w' \left(\frac{\partial \theta_0}{\partial z} + \frac{a}{\mu_0} \frac{\partial \mu_0}{\partial z} \right) = 0 \quad (12)$$

Here, the amplification factor $1+ab$ (with $ab>0$) describes the feedback of the GW-induced ozone perturbation to the change in temperature, and $\partial\theta_0/\partial z+(a/\mu_0)\cdot\partial\mu_0/\partial z$ an *ozone adiabatic lapse rate* which is – in the USLM region – smaller than $\partial\theta_0/\partial z$ because of $\partial\mu_0/\partial z<0$. Alternatively, we may write:

$$205 \quad \frac{d_0}{dt} \left(\frac{g}{\theta_0} \theta' \right) + N_\mu^2 w' = 0 \quad (13)$$

with

$$N_\mu^2 = \frac{N_0^2 + N_c^2}{(1+ab)} \quad (14)$$

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where $N_c^2 = (g/\theta_0) \cdot (a/\mu_0) \cdot \partial\mu_0/\partial z$. Like for the lapse rate, N_μ^2 is smaller than N_0^2 because $N_c^2 < 0$ and $(1+ab) > 1$. If ozone-temperature coupling becomes weak, below and above the USLM region, N_μ^2 converges to N_0^2 .

Analogously to the standard solution given above, we introduce sinusoidal GW perturbations of the form $X_2' = X_{\mu 0} \cdot \exp[i(k_2 x + l_2 y + m_2 z - \omega_2 t)] \cdot \exp^{(z-z_s)/2H}$ in Eqs. (1)-(4) and (13) (here, the subscript 2 denotes the solutions with ozone-gravity wave coupling) which leads to the modified dispersion relation

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$$\omega_{i2}^2 = \frac{N_\mu^2 k_{h2}^2 + m_2^2 f^2}{k_{h2}^2 + m_2^2} \approx N_\mu^2 \frac{k_{h2}^2}{m_2^2} + f^2 \quad (15)$$

where $\omega_{i2} = \omega_2 - k_2 u_0$ and $k_{h2} = (k_2^2 + l_2^2)^{1/2}$.

220 Eq. (13) provides an evident measure of the local amplification of a GW amplitude at a specific altitude z or pressure level $p(z)$. On the one hand, introducing the same initial [adiabatic temperature perturbation](#) $d\theta'_1/dt$ either with or without ozone-temperature coupling leads to $w_2' = w_1' \cdot (N_0^2/N_\mu^2)$. Consistently, introducing the same initial [perturbation](#) $w_1' N_0^2$ leads to $d\theta'_2/dt = d\theta'_1/dt$ or $-i\omega_{i2}\theta_2' = -i\omega_{i1}\theta_1'$. Then, combining $-i\omega_{i2}\theta_2' = -N_\mu^2 w_2'$ and $-i\omega_{i1}\theta_1' = -N_0^2 w_1'$ suggests that the amplitude $\theta_\mu = \theta_{\mu 0} \cdot \exp^{(z-z_s)/2H}$ is stronger than $\theta_a = \theta_{a0} \cdot \exp^{(z-z_s)/2H}$ by the factor $\omega_{i1}/\omega_{i2} = N_0^2/N_\mu^2 \geq 1$:

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$$\theta_\mu = \theta_a \cdot (\omega_{i1}/\omega_{i2}) \quad (16)$$

Overall, the introduced process of ozone-temperature coupling leads to [a](#) decrease in the GW frequency and a corresponding amplification in the GW amplitude described by the factor ω_{i1}/ω_{i2} or N_0^2/N_μ^2 . Note that vertical variations in N_0^2 could affect

230 the increase in amplitude with height particularly in the summer upper mesosphere; therefore, N_0^2 is vertically averaged over

the USLM region (from 30 hPa to 0.03 hPa, or ~25 km to ~70 km altitude) to focus on the effects of ozone-gravity wave interaction only. Note also that the relation $\omega_{i1}/\omega_{i2}=N_0^2/N_\mu^2$ implies not only a change in amplitude but also a slight change in the relation of horizontal and vertical wavenumber described by $(k_{h2}/m_2)=(N_\mu^2/N_0^2)(k_{h1}/m_1)+f^2(N_\mu^2-N_0^2)/(N_0^2\cdot N_0^2)$, i.e., a slight change in the direction of upward propagating GWs which is perpendicular to the angle α of the phase lines defined by $\cos(\alpha)=\pm(k_h/m)$. However, as illustrated in the following, ozone-gravity wave interaction is particularly relevant for a range of wavelengths and periods where the induced changes in α are very small (for $L_{m1}/L_{kh1}<0.05$, or wave periods $\tau_i>2h$, the change in α is less than $1\cdot 10^{-4}$ degree).

2.1.4 Examples for local amplification of GW amplitudes

Figure 1d-f shows the factor $1+ab$ and the quotient N_0^2/N_μ^2 for a GW with horizontal and vertical wavelengths $L_k=500$ km and $L_m=5$ km, and the quotient N_0^2/N_μ^2 for a GW with $L_k=800$ km and $L_m=3$ km. In the first example, the factor $1+ab$ (Figure 1d) contributes to the local amplification of the GW amplitude by up to 6-8%, and the overall factor $N_0^2/N_\mu^2=(1+ab)\cdot N_0^2/(N_0^2+N_c^2)$ (Figure 1e) by up to 8-12% (including a decrease in the lapse rate of up to 3% described by $(N_0^2+N_c^2)/N_0^2$, here not shown). The second example (Figure 1f) shows that the factor N_0^2/N_μ^2 is larger in case of larger horizontal and smaller vertical wavelength, reaching local amplifications of up to 12% to 14% (shaded areas denote the latitudinal range where the amplification is reduced due to the length of daylight, i.e., where $\tau_i>\tau_{day}$).

For illustration of the induced local change in ozone (Figure 2 a-d), we assume an initial GW perturbation θ'_1 with exponentially growing amplitude $\theta_a=\theta_{a0}\cdot\exp^{(z-z_s)/2H}$, with an initial temperature amplitude T_{a0} of 1 K at $z_s\approx 35$ km ($p_s=6.28$ hPa) increasing to ~8 K at $z\approx 65$ km ($p=0.1$ hPa). In the present paper, we formulate the solutions for pressure levels p , i.e., the initial perturbation is alternatively described by $\theta_a=\theta_{a0}\cdot(p_s/p)^{1/2}$ assuming $p=p_s\cdot\exp^{(z-z_s)/H}$. Introducing the associated perturbation $w'_1=-(\partial\theta_0/\partial z)^{-1}\cdot d_0\theta'_1/dt$ in Eq. (6) leads to $d_0\mu'_1/dt=[(\partial\mu_0/\partial z)/(\partial\theta_0/\partial z)-b\mu_0]\cdot d_0\theta'_1/dt$, and, considering $d_0\mu'_1/dt=-i\omega_{i1}\mu'_1$ and $d_0\theta'_1/dt=-i\omega_{i1}\theta'_1$, to an initial ozone perturbation $\mu'_1=\theta'_1\cdot[(\partial\mu_0/\partial z)/(\partial\theta_0/\partial z)-b\mu_0]$. For the example of the ascent ($w'_1>0$) shown in Figure 2, we set $\theta'_1<0$ leading to $\mu'_1>0$. For $L_k=500$ km and $L_m=5$ km, the contributions $\mu'(TR)=\theta'_1\cdot[(\partial\mu_0/\partial z)/(\partial\theta_0/\partial z)]$ related to transport (Figure 2a) and $\mu'(CH)=-b\mu_0\theta'_1$ related to S' (Figure 2b) sum up to a total change of $\mu' \approx 0.2$ to 0.5 ppm (Figure 2c) or $\mu'/\mu_0 \approx 5$ to 10 % (Figure 2d) in the USLM region where the feedback to the heating rate is particularly strong.

The related local change in the heating rate (Figure 2e) is given by comparing Eq. (5) with and without ozone-temperature coupling. Assuming the same initial ascent or adiabatic cooling as above leads to $(w'_2-w'_1)(\partial\theta_0/\partial z)=Q'(\mu'_1)$, or, when introducing $w'_2=(\omega_{i1}/\omega_{i2})\cdot w'_1$, to $Q'(\mu'_1)=(\omega_{i1}/\omega_{i2}-1)(-\omega_{i1}\theta'_1)=a\omega_{i1}\mu'_1\mu_0^{-1}$ (where $Q'(\mu'_1)>0$ in case of $w'_1>0$). Figure 2e shows that $Q'(\mu'_1)$ reach values of 0.15 K hr⁻¹ over the tropics and 0.25 K hr⁻¹ at southern summer polar latitudes. Then, consistently with Eq. (16), we yield $\theta'_2-\theta'_1=(\omega_{i1}/\omega_{i2}-1)\cdot\theta'_1$ with $(\omega_{i1}/\omega_{i2}-1)=-a\mu_0^{-1}[(\partial\mu_0/\partial z)/(\partial\theta_0/\partial z)-b\mu_0]$ for the change in

the temperature perturbation, with values of 0.2 to 0.3 K in the USLM region (Figure 2f). In summary, analogously considering the corresponding change for the descent, we yield a local increase in the amplitude of the oscillating GW pattern by up to 5 to 10 % in ozone and 0.2 to 0.3 K in temperature.

265 For other initial wavelengths (or associated frequencies), the latitude-height dependence is very similar to those shown in Figure 1 (d-f) and Figure 2, whereas the magnitude of the amplification factor ω_{i1}/ω_{i2} becomes smaller in case of increasing vertical and decreasing horizontal wavelengths, or decreasing frequencies, as illustrated in Figure 3 for an altitude where ω_{i1}/ω_{i2} reach maximum values (1.156 hPa or ≈ 47 km altitude). Figure 3a shows values of $\omega_{i1}/\omega_{i2} > 1.02$ for wave periods of $\tau_i > 2$ h steadily increasing with increasing initial period up to values between 1.14 and 1.15. This value is limited, on the one
270 side, because of the increasing duration of nighttime with latitude towards equatorial and northern winter regions (denoted by shaded areas), and, on the other side, because of the increasing Coriolis force in southern summer mid- and polar regions (i.e., because of $\omega_{i1}^2 > f^2$).

Consistently, the amplification factor is increasing with decreasing vertical and increasing horizontal wavelength (Figures 3b and 3c show examples for 70°S and 30°S), where the values are limited by the length of daylight in case of small relations L_m/L_k denoting the conditions where $\tau_i > \tau_{\text{day}}$ (Figure 3c, shaded area). Figure 3 also indicates that the examples with $L_k = 500$
275 km and $L_m = 5$ km (Figure 1e; Figure 2) and $L_k = 800$ km and $L_m = 3$ km (Figure 1f) represent scales where ozone-gravity wave interaction is particularly efficient.

Overall, Figures 1 (d-f), 2 and 3 illustrate the local amplification of GW amplitudes at a specific level and a specific time; as far as the GWs are continuously propagating upward through several levels where $\omega_{i1}/\omega_{i2} - 1 > 0$, the amplification will be
280 successively reinforced at each level. This cumulative amplification can lead to much stronger GW amplitudes at upper mesospheric altitudes in case with than without ozone-gravity wave interaction as demonstrated in the next subsection.

2.2 Upward propagating GWs in a background flow

2.2.1 Level-by-level amplification of GW amplitudes

285 In the following, a solution of the cumulative amplification during the vertical level-by-level propagation is derived, excluding – to a first guess – other effects like small-scale diffusion, wave breaking processes, interaction of the GWs with atmospheric tides, or so-called secondary gravity waves. Following Huygens principle, each point of a propagating wave front at a specific level is the source of a new wave at this level, i.e., a single upward propagating GW, which is amplified at a level z_{j-1} , is the initial perturbation amplified at the next level z_j . For illustration (Figure 4, a-c), we choose an initial GW
290 with horizontal and vertical wavelengths $L_m = 500$ km and $L_m = 5$ km as above, where the vertical distance between the levels z_{j-1} and z_j is set by the initial vertical wavelength $\Delta z = L_m$. First, we focus on polar latitudes during southern polar summer (70°S) with daylight conditions only, then we consider the modification for mid- and equatorial latitudes where GWs with weak vertical group velocities propagate through the USLM during both daylight and nighttime.

For orientation, Figure 4a shows the profiles ω_{i1}/ω_{i2} for $L_k=500$ km and $L_m=5$ km at 70°S (solid), and, for comparison, for
 295 $L_m=3$ km (dashed) and $L_m=9$ km (dotted), indicating the altitude range where ozone-temperature coupling is relevant (note
 that the depicted distance of pressure levels represents approximately a 5 km distance in altitude). Beginning with a first
 level at $z_s \approx 35$ km (6.28 hPa), the wave propagates through 8 layers between ≈ 35 km and ≈ 70 km (0.06 hPa) where the
 amplification of the amplitude is relevant. At each of these levels, denoted by $z_j = z_s + (j-1) \cdot \Delta z$ ($j=1, n$; here $n=8$), the
 amplitude will be amplified by the local factor $\omega_{i1}(z_j)/\omega_{i2}(z_j)$. Starting with an exponentially growing amplitude
 300 $T_a(z) = T_a(z_s) \cdot \exp^{(z-z_s)/2H}$ (where we set again $T_a(z_s) = 1$ K), we yield a new amplitude $T_{a1}(z_1) = T_a(z_1) \cdot \omega_{i1}(z_1)/\omega_{i2}(z_1)$ at the level
 z_1 defining a new exponentially growing amplitude $T_{\mu1}(z) = T_{a1}(z_1) \cdot \exp^{(z-z_1)/2H}$. Then, we yield $T_{a2}(z_2) = T_{\mu1}(z_2) \cdot \omega_{i1}(z_2)/\omega_{i2}(z_2)$ at
 the level z_2 defining $T_{\mu2}(z) = T_{a2}(z_2) \cdot \exp^{(z-z_2)/2H}$, and so on. Finally, the amplitude at the level z_n in the middle mesosphere is
 described by

$$305 \quad T_{\mu n}(z) = T_a(z) \cdot \prod_{j=1}^n \left[\frac{\omega_{i1}(z_j)}{\omega_{i2}(z_j)} \right], \quad (17)$$

where the product symbol $\prod_{j=1, n}$ denotes the multiplication with $\omega_{i1}(z_j)/\omega_{i2}(z_j)$ at each level $z_1 \leq z_j \leq z_n$. As mentioned above,
 the solutions are calculated on pressure levels, i.e., z represents the geopotential height, and the vertical distance Δz between
 the levels is given by $\Delta z = -(\rho_0 g)^{-1} \Delta p = -H(T_0) \cdot (\Delta p/p)$, where $H(T_0) = g/(RT_0)$ is the height-dependent scale height defined by
 310 the background; note here that using a constant scale height $H_0 = 7$ km instead of $H(T_0)$ leads only to second-order changes in
 the cumulative amplitude amplification (the sensitivity test is described below in Section 2.2.4), because $H(T_0)$ is varying
 only slightly in the USLM region (between ~ 7.5 km at summer stratopause altitudes and ~ 6.5 km at 70 km).

Figure 4b shows the initial amplitude T_a (blue line) and the series of the successively amplified amplitudes $T_{\mu1}, T_{\mu2}, \dots, T_{\mu n}$
 (from light blue towards red line), and Figure 4c the related series of constant relative values $T_{\mu1}/T_a, T_{\mu2}/T_a, \dots, T_{\mu n}/T_a$
 315 starting at the level z_j (solid lines) together with the previous values starting at z_{j-1} multiplied by the factor ω_{i1}/ω_{i2} (dotted
 lines), illustrating the **successively increasing** growth of the amplitude during the upward level-by-level propagation. Finally,
 the amplitudes converge to $T_{\mu n}(z)$ when reaching the upper mesosphere, where $T_{\mu n}(z)$ is stronger than $T_a(z)$ by a factor of
 ~ 1.47 . Figure 4c also shows the fitted relative increase of the amplitude T_{μ}/T_a (thick red line) describing the continuous
change in the growth rate of the amplitude, where $T_{\mu}(z)$, or $T_{\mu}(p)$, is defined by

$$320 \quad T_{\mu}(p) = h_s(p) \cdot T_a(p) + h_m(p) \cdot T_{\mu n}(p) \quad (18)$$

with weighting functions $hs=p_0^{1.5}/(p_0^{1.5}+p_m^{1.5})$ and $hm=1-hs$, where p_0 is the background pressure and $p_m(70^\circ\text{S})\approx 0.96$ hPa the level of the maximum of ω_{i1}/ω_{i2} (note that the height of this maximum is slightly decreasing from $p_m\approx 0.89$ hPa over the south pole to $p_m\approx 1.3$ hPa over the equator).

For mid- and equatorial latitudes, daylight-nighttime conditions are considered by setting the amplification factor to $F_d=\omega_{i1}/\omega_{i2}$ during daylight but to $F_d=1$ during nighttime over the vertical wave propagation distance of one full day. In detail, we define the parameter $L_{\text{day}}=(\tau_{\text{day}}-0.5\cdot\tau_0)/(0.5\cdot\tau_0)$, where $\tau_0=24$ hours and τ_{day} is the duration of daylight within 24 hours at the latitude φ (with $L_{\text{day}}=1$ during polar summer and $L_{\text{day}}=0$ at the equator). Further, considering the vertical group velocity $c_{gz}=\partial\omega_{i1}/\partial m_1=-(\omega_{i1}/m_1)\cdot(\omega_{i1}^2-f^2)/\omega_{i1}^2$ (with initial frequency ω_{i1} and vertical wavelength m_1 as first guess), the sinusoidal wave propagation structure between the middle stratosphere and middle mesosphere is described by $L_{\text{cgz}}=\cos(2\pi\tau_0\cdot(z-z_m)/c_{gz})$ changing periodically between 1 and -1 over one wavelength, where z and z_m are given in km and c_{gz} in km hr^{-1} , and where $L_{\text{cgi}}=1$ at the level p_m , or altitude $z_m(p_m)$. Then, the combined parameter $L_d=L_{\text{day}}+L_{\text{cgi}}$ separates the vertical propagation distance into daylight and nighttime fractions by defining a constant value $C_d=1$ in case of $L_d>1$ and $C_d=0$ in case of $L_d\leq 1$, where the factor $F_d=1+C_d\cdot((\omega_{i1}/\omega_{i2})-1)$ provides $F_d=\omega_{i1}/\omega_{i2}$ in case of daylight and $F_d=1$ in case of nighttime.

As an example, Figure 4d shows the profile of the resulting amplification factor F_d at 10°S for a GW with $L_k=500$ km and $L_m=5$ km as above, with an associated vertical group velocity c_{gz} of about 7 km per 12 hours, illustrating that we define $F_d(z_j)=\omega_{i1}(z_j)/\omega_{i2}(z_j)$ where z_j is located in the daylight region (red) but $F_d(z_j)=1$ where z_j is located in the nighttime region (blue). The indicated vertical wave propagation distance during daylight increases towards southern summer polar latitudes but decreases towards northern winter polar latitudes. Note here that, for vertical wavelengths examined in the present paper ($L_m\leq 15$ km), a vertical shift of the phase – as defined by the altitude z_m in the definition of L_{cgz} – does not have a significant impact on the cumulative amplification of the GW amplitudes because of the Gaussian-type structure of the profile of $F_d=\omega_{i1}/\omega_{i2}$, which has been verified by several test calculations with other levels than p_m , or other altitudes than z_m .

In the following, the fitted profiles T_μ are used for further examinations with different horizontal and vertical wavelengths, where the vertical level-by-level amplification is calculated by using the distances $\Delta z=\Delta z_H$ of the vertical grid of HAMMONIA instead of $\Delta z=L_m$. This includes a smaller amplification factor $F_\omega=\omega_{i1}/\omega_{i2}$ over the vertical distance Δz_H because of the smaller heating rate perturbation $Q'_{\Delta z_H}=(\Delta z_H/L_m)\cdot Q'$ (see Eq. (11 and related discussion); however, the resulting difference in the local amplification over the vertical distance L_m are nearly the same except some small differences of less than 0.5% due to the different vertical resolution (i.e., $F_\omega(\Delta z=L_m)\approx 1+(F_\omega(\Delta z=\Delta z_H)-1)\cdot(L_m/\Delta z_H)$). Also the resulting cumulative amplification in the upper mesosphere remains nearly unchanged ($T_{\mu n}(\Delta z=L_m)\approx T_{\mu nh}(\Delta z=\Delta z_H)$, where nh is the number of the HAMMONIA levels in the USLM), where small differences between $T_{\mu nh}$ and $T_{\mu n}$ of less than 10% occur only at mid- and equatorial latitudes in case of small vertical wavelengths (or small vertical group velocities) when considering the vertical propagation during both daylight and nighttime described below.

355 2.2.2 Cumulative amplitude amplification for representative examples

Figure 4e illustrates the dependence of the amplitude amplification on the horizontal and vertical wavelengths L_k and L_m at 70°S , where it is not affected by nighttime conditions. In comparison to the example of $L_k=500$ km and $L_m=5$ km leading to a cumulative amplification of ~ 1.47 (red, solid line), a larger vertical wavelength of $L_m=9$ km leads to a smaller value of ~ 1.15 (red, dotted line), but a smaller vertical wavelength of $L_m=3$ km to a larger value of ~ 2.27 (red, dashed line), because
 360 the induced increase in the ozone perturbation μ' produces a heating rate perturbation Q' within a shorter (in case of $L_m=9$ km) or larger (in case of $L_m=3$ km) time increment τ_i . For the same reason, the amplification is generally larger if the horizontal wavelength L_k is larger, e.g., in case of $L_k=800$ km, the final amplification in the upper mesospheric amplitudes amounts to ~ 1.22 for $L_m=9$ km (purple, dotted line), ~ 1.63 for $L_m=5$ km (purple, solid line), and ~ 2.56 for $L_m=3$ km (purple, dashed line).

365 The related gravity wave potential energy density (GWPED, here denoted by E) is derived following Kaifler et al. (2015):

$$E = \frac{1}{2} \left(\frac{g}{N} \right)^2 \left(\frac{T'}{T_0} \right)^2 \quad (19)$$

Introducing $T'=T_2'$ and $N=N_\mu$, or $T'=T_1'$ and $N=N_0$, leads to the case with (E_μ) or without (E_a) ozone-gravity wave
 370 interaction. Figure 4f shows the relative amplitudes E_μ/E_a related to Figure 4e. In case of $L_k=500$ km (red lines), the final amplification reach values of ~ 1.32 for $L_m=9$ km (dotted), ~ 2.17 for $L_m=5$ km (solid), and ~ 5.21 for $L_m=3$ km (dashed), and in case of $L_k=800$ km (purple) values of ~ 1.50 for $L_m=9$ km (dotted), ~ 2.70 for $L_m=5$ km (solid), and ~ 6.62 for $L_m=3$ km (dashed). Overall, these factors provide a first-order estimate of the effect of ozone-gravity wave coupling at 70°S during
 375 amplifications in the upper mesosphere in the order of ~ 1.5 to ~ 2.5 in the temperature perturbations and in the order of ~ 3 to ~ 7 in the related GWPED.

2.2.3 Cumulative amplitude amplification depending on latitude

For the GW with $L_k=500$ km and $L_m=5$ km, Figure 5 shows the latitudinal dependence of the cumulative amplification of the
 380 temperature perturbation (indicated by T_μ/T_a , Figure 5a) and the related GWPED (indicated by E_μ/E_a , Figure 5b). The values decrease from $T_\mu/T_a \approx 1.5$ and $E_\mu/E_a \approx 2.4$ over southern summer polar latitudes towards $T_\mu/T_a \approx 1.2$ and $E_\mu/E_a \approx 1.4$ at lower mid-latitudes (40°S), and then less rapidly towards $T_\mu/T_a \approx 1.1$ and $E_\mu/E_a \approx 1.2$ at 20°N . Overall, although the amplification of the GW amplitudes decreases rapidly with the decrease in the length of daylight, it is still quite strong at mid-latitudes.

Figure 6 shows the relations T_μ/T_a (Figure 6a) and E_μ/E_a (Figure 6b) at upper mesospheric levels (0.01 hPa, ~ 80 km) for
 385 different horizontal and vertical wavelengths as used for Figures 4e and 4f. For both $L_k=500$ km (red) and $L_k=800$ km

(purple), the amplifications of the temperature perturbations and of the related GWPED are strongest for $L_m=3$ km (dashed lines), at polar latitudes with values between 2.5 to 3 in T_μ/T_a and 7 to 9 in E_μ/E_a , and at mid- and equatorial latitudes between 1.5 to 1.8 in T_μ/T_a and 2.4 to 3.5 in E_μ/E_a . These values decrease with increasing vertical wavelength, i.e., when changing to $L_m=5$ km (solid lines) or $L_m=9$ km (dotted lines) roughly to ~ 1.7 or ~ 1.25 in T_μ/T_a and ~ 3.0 or ~ 1.5 in E_μ/E_a at polar latitudes, and roughly to ~ 1.25 or ~ 1.2 in T_μ/T_a and ~ 1.5 or ~ 1.25 in E_μ/E_a at mid- and equatorial latitudes. Overall, for the mesoscale GWs with small vertical and large horizontal wavelengths, the cumulative amplification due to ozone-gravity wave coupling leads to much stronger amplitudes at upper mesospheric altitudes during daylight than nighttime, in the GW perturbations by a factor between ~ 1.5 at summer mid-latitudes and ~ 3 for polar day conditions, and in the GWPED by a factor between ~ 3 at summer mid-latitudes and ~ 9 for polar day conditions.

Note here that vertical momentum flux terms $F_{GW}=\rho_0(u'w')$ can be derived from local profiles T' if the background is known, i.e. by $F_{GW}=\rho_0E\cdot(k/m)$ (Ern et al., 2004). Therefore, the amplification of the GW amplitudes must lead to the same amplification of the flux term F_{GW} and, if the GWs do not break at lower levels, of the associated gravity wave drag $GWD=-\rho_0^{-1}\partial F_{GW}/\partial z$ in the upper mesosphere, suggesting an important effect of ozone-gravity wave interaction on the meridional mass circulation particularly at polar latitudes. However, more detailed investigations need extensive numerical model simulations with a spectrum of resolved GWs which is beyond the scope of the present paper.

2.2.4 Sensitivity to varying conditions

In the following, we estimate the sensitivity of the GW amplitude amplification on non-linear processes and background conditions which could modulate the first-guess results described above. For example, the decrease in the frequency towards $\omega_{i2}<\omega_{i1}$ includes a slight decrease in the vertical group velocity towards $c_{gz2}<c_{gz1}$, which can additionally strengthen the process of amplitude amplification because the wave propagates somewhat more slowly through the ULSM region. However, this effect is at least one order smaller than the first-order process described above as derived from test calculations including this effect. For example, for $L_k=500$ km and $L_m=5$ km, c_{gz2} is smaller than c_{gz1} by 15% to 20% at southern summer polar latitudes and 5% to 10% at mid- and equatorial latitudes. Subsequently, the local amplification factor $F_d(c_{gz2})$ is stronger than $F_d(c_{gz1})$ by 2% to 3% at polar latitudes and less than 1% at mid- and equatorial latitudes. Including this change into the successive level-by-level propagation leads to a weak successive increase in the cumulative amplifications by $\sim 5\%$ at 1 hPa to $\sim 10\%$ at 0.01 hPa at polar summer latitudes, and by only $\sim 1\%$ at 1 hPa to $\sim 2\%$ at 0.01 hPa at mid- and equatorial latitudes.

We also estimate the sensitivity of the amplitude amplification on the ozone background μ_0 , considering the observed long-term changes in upper stratospheric ozone in the order of up to -8% per decade (e.g., Sofieva et al., 2017; WMO, 2018), and the uncertainty in the maximum of the heating rate Q_0 which is smaller in the used HAMMONIA data in the order of $\sim 10\%$ compared to those derived from satellite measurements, as mentioned above. In case of a 10%-reduction in ozone, the

cumulative amplification in the upper mesospheric GW amplitudes is weaker by about 5% for the example with $L_m=5$ km and 10% for $L_m=3$ km (i.e., at 70°S , we yield a cumulative amplification of ~ 1.4 to ~ 2.25 instead of ~ 1.5 to ~ 2.5), and the related amplification of the GWPED is weaker by about 10% for $L_m=5$ km and 20% for $L_m=3$ km (at 70°S , a cumulative amplification of ~ 2.7 to ~ 7.2 instead of ~ 3 to ~ 9). Analogously, in case of an increase in Q_0 by 10%, the cumulative amplification is stronger by 5% or 10% in the GW amplitudes and by 10% or 20% in the related GWPED amplitudes.

Another question arises on the sensitivity of the effect of ozone-gravity wave coupling to atmospheric tides or the diurnal cycle in stratospheric ozone, which are planetary-scale processes changing the background conditions for the local propagation of the mesoscale GW perturbations. For example, Schranz et al. (2018) observed stronger amplitudes in upper stratospheric ozone during daylight than nighttime in the order of 5% (summer solstice) to 8% (May). Such a difference would correspond to a change in the cumulative amplification of the upper mesospheric GW amplitudes or GWPED in the order of 5% to 10% or 10% to 20%, as follows from the sensitivity of the effect on the prescribed long-term change in stratospheric ozone derived above.

Baumgarten and Stober (2019) derived amplitudes of tides in the order of up to 0.5 K in the middle stratosphere (~ 35 km) increasing up to 2 K at ~ 50 km and ~ 4 K at 70 km, which would correspond to a change in the lapse rate in the order of up to 0.1 K km^{-1} , or in the Brunt-Vaisala frequency N_0^2 in the order of 1%. As follows from Eq. (14), a change in the amplification factor $F_d=N_0^2/N_\mu^2$ due to a relative change $\Delta N_0^2/N_0^2$ is given by the factor $[1+(\Delta N_0^2/N_0^2)]/[1+(\Delta N_0^2/N_0^2)(N_0^2/N_\mu^2)(1+ab)^{-1}]$; therefore, for wavelengths $L_k \geq 500$ km and $L_m \leq 5$ km, a relative increase (decrease) of 1% in N_0^2 would lead to a relative decrease (increase) in the amplification factor of up to 0.035% at stratopause altitudes, which is much less than the effects of the changes in the vertical group velocity or in ozone described above. Moreover, even if a relative change $\Delta N_0^2/N_0^2$ would be much larger (10% to 50%), it does not change the local amplification factor by more than 1% to 3%, and, hence, the cumulative amplification of the GW amplitudes in the upper mesosphere by more than 5 to 10%.

Assuming exponential growth of the amplitudes ($\sim e^{(z-z_s)/2H}$) between two levels, the usual approach of a constant scale height (e.g., $H \sim 7$ km) instead of a height-dependent scale height $H(T_0)=g/(RT_0)$ can principally lead to significant differences in the GWPED profiles (e.g., Reichert et al., 2021). For estimating the relevance of a change in H on the cumulative amplitude amplification, the solutions are also calculated for an initial GW perturbation $\theta_a=\theta_{a0}\cdot\exp^{(z-z_s)/2H}$ with a prescribed scale height $H_0=7$ km instead of $\theta_a=\theta_{a0}\cdot(\text{ps}/\text{p})^{1/2}$, and a related vertical distance $\Delta z=-H_0\cdot(\Delta\text{p}/\text{p})$ instead of $\Delta z=-H(T_0)\cdot(\Delta\text{p}/\text{p})$ (note that $H(T_0)$ varies in the USLM region between ~ 7.5 km at summer stratopause altitudes and ~ 6.5 km at 70 km). Compared to the values shown in Figures 5 and 6, the cumulative amplification of the upper mesospheric GW amplitudes is weaker by about 5% ($L_m=5$ km) to 10% ($L_m=3$ km) over the summer south pole, and weaker by about 1% ($L_m=5$ km) to 3% ($L_m=3$ km) at summer mid-latitudes; correspondingly, the related GWPED values are weaker by about 7.5% ($L_m=5$ km) to 20% ($L_m=3$ km) over the summer south pole, and 1.5% ($L_m=5$ km) to 5% ($L_m=3$ km) at summer mid-latitudes. Overall, these differences are smaller than the first-order effect of ozone-gravity wave coupling by approximately one order, where the use of $H(T_0)$ instead of H_0 at the levels of relevant amplification leads to somewhat stronger amplitude amplifications particularly over the

summer south pole, because of the difference between the high background temperatures in the summer stratopause region and the low background temperatures in the summer mesosphere (see Figure 1a).

3 Summary and conclusions

455 The present paper shows that ozone-gravity wave interaction in the upper stratosphere/lower mesosphere (USLM) leads to a stronger increase of gravity wave (GW) amplitudes with height during daylight than nighttime, particularly during polar summer. The results include information on both the local amplification of the GW amplitudes and the cumulative increase of the amplitudes during the upward propagation of the wave from middle stratosphere to upper mesosphere.

In a first step, standard equations describing upward propagating GWs with and without linearized ozone-gravity wave
460 coupling are formulated, where an initial sinusoidal GW perturbation in the vertical ozone transport and temperature-dependent ozone photochemistry produces a heating rate perturbation as a function of the initial intrinsic frequency, which determines the local duration of the perturbation over the distance of the initial vertical wavelength. The solution reveals a
465 [local amplification of the ascending and descending perturbations of the sinusoidal GW pattern, i.e.](#), a decrease of the intrinsic frequency due to both [the induced changes](#) in the lapse rate (or Brunt-Vaisala frequency) and the positive feedback of the coupling on the initial GW perturbation, and an associated local increase of the GW amplitude by a factor $\omega_{i1}/\omega_{i2} \geq 1$ defined by the relation of the intrinsic frequencies without (ω_{i1}) and with (ω_{i2}) ozone-gravity wave coupling. This amplitude amplification is dependent on the horizontal and vertical wavelengths, L_k and L_m , where the effect is most efficient for GWs with $L_k \geq 500$ km and $L_m \leq 5$ km, or initial frequencies $\tau_i \geq 4$ hours, representing [mesoscale](#) GWs forced by cyclones or fronts, or by the orography of mountain ridges [like the Rocky Mountains, Andes or Norwegian Caledonides](#). For southern summer
470 conditions, strongest local amplitude amplifications of about 5% to 15% over the perturbation distance of one vertical wavelength are located near the stratopause, with peak values over the equator and over summer polar latitudes.

In a second step, an analytic approach of the upward level-by-level propagation of the GW perturbations with and without ozone-gravity wave interaction reveals the cumulative amplitude amplification, where the wave is propagating upward with the vertical group velocity defined by the initial GW parameters, and where daylight-nighttime conditions at mid- and
475 equatorial regions are considered. Representative examples with different initial wavelengths illustrate that the [successive](#) increase of both the GW amplitudes and the related gravity wave potential energy density (GWPED) converge to much stronger amplitudes in the upper mesosphere during daylight than nighttime. This effect is strongly decreasing with latitude between summer polar and mid-latitudes because of the decrease in the length of daylight, nearly constant at equatorial latitudes, and decreasing again with latitude towards insignificant values in the winter extra-tropics. For [the](#) GWs with
480 horizontal wavelengths between $L_k = 500$ km and $L_k = 800$ km, and a vertical wavelength of $L_m = 3$ km, the amplitudes of the GWPED in the upper mesosphere are stronger during daylight than nighttime by a factor ~ 2.5 to ~ 3.5 at summer mid-latitudes, and by a factor ~ 7 to ~ 9 at summer polar latitudes.

The variety of horizontal and vertical wavelengths used in the present paper are representative for mesoscale GWs in the USLM region. Observations suggest characteristic vertical wavelengths of GWs between ~2-5 km in the lower stratosphere increasing to ~10-30 km in the upper mesosphere, but also the existence of large vertical wavelengths greater than 10 km in the ULSM region particularly above convection in equatorial regions or over southernmost Argentina (e.g., Alexander, 1998; McLandress et al., 2000; Fritts and Alexander, 2003; Hocke et al., 2016; Baumgarten et al., 2018; Reichert et al., 2021). The results of the present paper suggest that the effect of ozone-gravity wave coupling decreases with increasing vertical wavelengths $L_m \geq 9$ km but strongly increases with decreasing vertical wavelengths $L_m \leq 5$ km. The latter could lead to more pronounced gravity wave breaking and dissipation processes in the upper stratosphere during daylight than nighttime, and – subsequently – to more prominent GWs with larger vertical wavelengths of $L_m \geq 5$ km, which would be consistent with the observed GW characteristics at these altitudes presented by Baumgarten et al. (2018).

At summer mid-latitudes, for single GWs with wavelengths $L_k \geq 500$ km and $L_m \leq 5$ km, the increase in the GWPED with height is stronger with than without ozone-gravity wave coupling up to a factor ~1.5 to ~3 at upper mesospheric altitudes. This is in the order of the daylight-nighttime differences suggested by Baumgarten et al. (2017), where the increase in GWPED with height is stronger for full-day than night-time measurements by a factor of more than ~2, or, assuming roughly a half-day-half-night relation of the effect of a related process, stronger during daylight than nighttime by a factor ~4. In addition, considering the observed power spectral density of the GWPED (e.g., Baumgarten et al., 2018), ozone-gravity wave coupling is particularly effective for GWs within a range of wave periods ≥ 4 hours (related to the wavelengths $L_k \geq 500$ km and $L_m \leq 5$ km) where the power spectral density is large. Conclusively, this process might significantly contribute to the daylight-nighttime differences in the GWPED at summer mid-latitudes. However, an unequivocal quantification of this contribution to the total GWPED profiles needs more investigations – for example, based on GW resolving model simulations with interactive ozone-photochemistry –, which is beyond the scope of the present paper.

The largest effect of ozone-gravity wave coupling is found for polar day or polar summer conditions, with an amplification of the GWPED amplitudes by a factor between ~3 and ~9 at upper mesospheric altitudes. Conclusively, this process might also contribute to observed polar day-polar night differences in the GWPED, and, hence, to its seasonal cycle as far as daylight measurements are included. For comparison, Kaifler et al. (2015) derived GWPED values from full-day Lidar temperature measurements at southern polar latitudes (69°S, 78°E) indicating that the relative increase in the GWPED between middle stratosphere (30-40 km) and upper mesosphere (85-95 km) is stronger during polar summer than winter by a factor between ~3.5 (December, February) and ~8 (January), where the GWPED in the middle stratosphere is weaker during polar summer than winter by a factor of about ~5. In addition, Kaifler et al. (2015) also observed a range of wave periods between 4 to 10 hours, i.e., a range where ozone-gravity wave coupling is particularly effective. However, Kaifler et al. (2015) did not analyze the GWPED for daylight and nighttime separately in a similar way as Baumgarten et al. (2017), and the variety of important processes contributing to the observed monthly mean GWPED cannot be separated easily.

515 For example, the largest portion of the seasonal cycle in the middle atmospheric GW activity might be related to the seasonal
cycle in critical level filtering by the zonal wind (e.g., Andrews et al., 1987; Fritts and Alexander, 2001; Kaifler et al., 2015).
Also, atmospheric tides (e.g., Baumgarten et al., 2017, 2018; Baumgarten and Stober, 2019), or specific GWs generated by
convection and propagating towards polar latitudes (Chen et al., 2019), or so-called secondary gravity waves produced in the
mesosphere by dissipating primary GWs (Becker and Vadas, 2018), are important factors which have to be considered when
520 deriving reliable polar summer GWPED values from measured time series. In addition, except the unexpected strong
GWPED value at southern polar latitudes for January shown by Kaifler et al. (2015), the seasonal cycle of the GWPED
seems to be somewhat less pronounced in the upper mesosphere than in the levels below, as also reported by Reichert et al.
(2021) for night-time GWPED measurements at southern high mid-latitudes (53.7°, 67.7°W); in combination with the strong
seasonal cycle in the stratospheric GW sources, this could indicate a source of GWs in the mesosphere independent from the
525 GWs at lower levels, and would also lead to an enhanced relative increase between stratospheric and mesospheric GWPED
values during polar summer compared to winter. However, as in case of summer mid-latitudes, the effect of ozone-gravity
wave coupling on the GWPED at polar summer latitudes is remarkably strong for mesoscale GWs within the important
range of wave periods between 4 to 10 hours; conclusively, it might also give a relevant contribution to the polar summer
GWPED. As above, more investigations based on observations and model simulations are needed to fully understand the
530 potential contribution of this process to the total GWPED profiles.

Current state-of-the-art general circulation models (GCMs) usually use a variety of prescribed tropospheric sources and
tuning parameters in the parameterized gravity wave drag (GWD) parameterizations forcing the middle atmospheric
circulation (e.g., McLandress et al., 1998; Fritts and Alexander, 2003; Garcia et al., 2017), where the extreme low
temperatures observed in the summer upper mesosphere provide an important benchmark for the quality of the upwelling
535 branch and the associated adiabatic cooling produced by the models. Including ozone-gravity wave interaction into the
GCMs might lead to a substantial improvement of the used GWDs and the associated processes driving the summer
mesospheric circulation, because the related increase in the GWPED must lead to a similar increase in the vertical
momentum flux term determining the GWD. However, the incorporation of ozone-gravity wave interaction in a state-of-the-
art GCM using a GWD, or in a numerical model with resolved GWs, needs extensive test simulations, which is beyond the
540 scope of the present paper.

Current GCMs particularly indicate significant changes in the time-mean circulation of the upper mesosphere due to the
stratospheric ozone loss over Antarctica during southern spring and early summer via the induced changes in the GWD
(Smith et al., 2010; Lossow et al., 2012; Lubi et al., 2016). Long-term changes in upper stratospheric ozone of up to -8% per
decade derived from satellite measurements (e.g., Sofieva et al., 2017; WMO, 2018) could also affect the mesospheric
545 circulation in the stratosphere and mesosphere by modulating the GW amplitudes and, hence, the GWD. Based on the
idealized approach of the present paper, we estimate the sensitivity of the amplification of the GW amplitudes in the upper
mesosphere on changes in the ozone background μ_0 and the ozone-related heating rate $Q_0(\mu_0)$, revealing that, for horizontal
and vertical wavelengths $L_k \geq 500$ km and $L_m \leq 5$ km, a change of $\pm 10\%$ in μ_0 or Q_0 results in a change of $\pm 10\%$ to $\pm 20\%$ in

the upper mesospheric GWPED. Conclusively, the summer mesospheric upwelling might be much more sensitive to the
550 long-term changes in upper stratospheric ozone as has been suggested by the GCMs up to now.

Also, the diurnal cycle in stratospheric ozone and atmospheric tides can principally modulate the effect of ozone-gravity
wave coupling by changing the planetary-scale background conditions for the propagation of the mesoscale GWs. The
sensitivity calculations of the present paper suggest that the related changes are smaller than the first-order effect of ozone-
gravity wave coupling by approximately one order. Further test calculations have shown that the use of a height-dependent
555 scale height $H(T_0)$ instead of a constant scale height H_0 at the levels of relevant amplification leads to stronger amplitude
amplifications particularly over the summer south pole, because of the high temperatures in the stratopause region and the
very low temperatures in the upper mesosphere, where the related differences are also smaller than the first-order process
(e.g., in the GWPED, for vertical wavelengths between $L_m=5$ km and $L_m=3$ km, between about 7.5% to 20% at summer
polar latitudes and less than 5% at summer mid-latitudes).

560 The results of the present paper might stimulate further daytime-nighttime observations of GW activity particularly at
specific measurement sites where the GWs are usually characterized by specific horizontal and vertical wavelengths, e.g.,
downwind of specific mountain ridges (east of Rocky Mountains, Southern Andes or Norwegian Caledonides), which could
be helpful to better understand of how ozone-gravity wave coupling is operating in situ.

565 **Data Availability**

Background data and programs visualizing the presented analytic solutions are available at the IAP archive under
<ftp://ftp.iap-kborn.de/data-in-publications/Gabriel/ACP2021/>.

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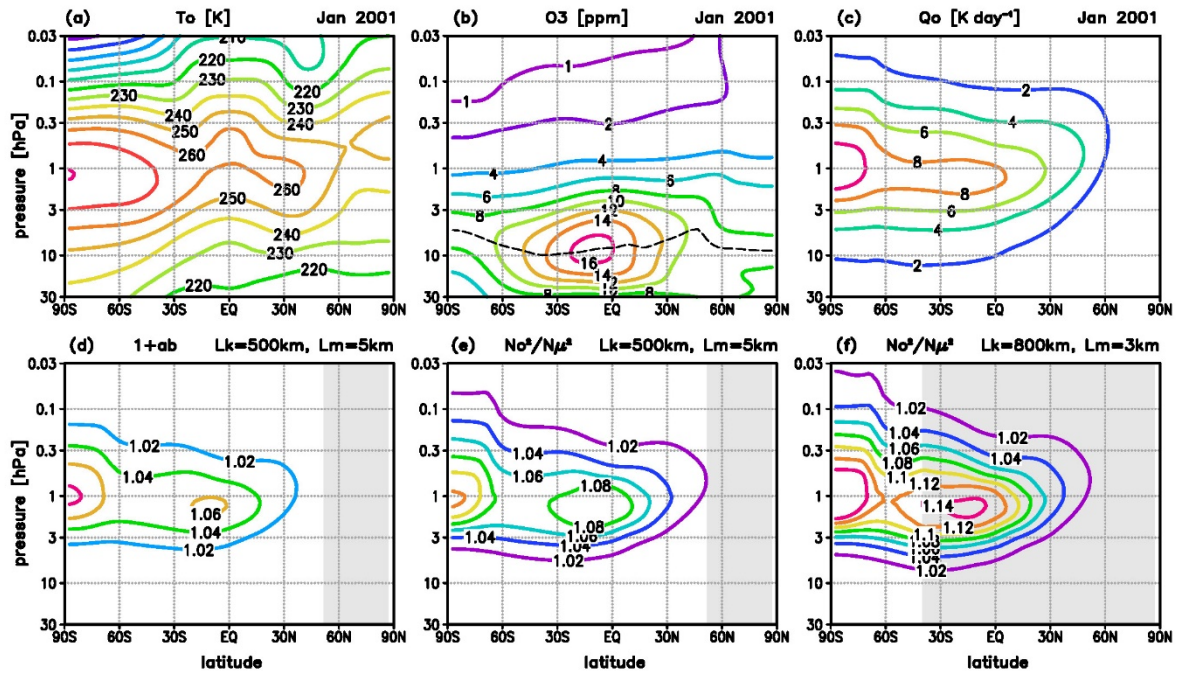
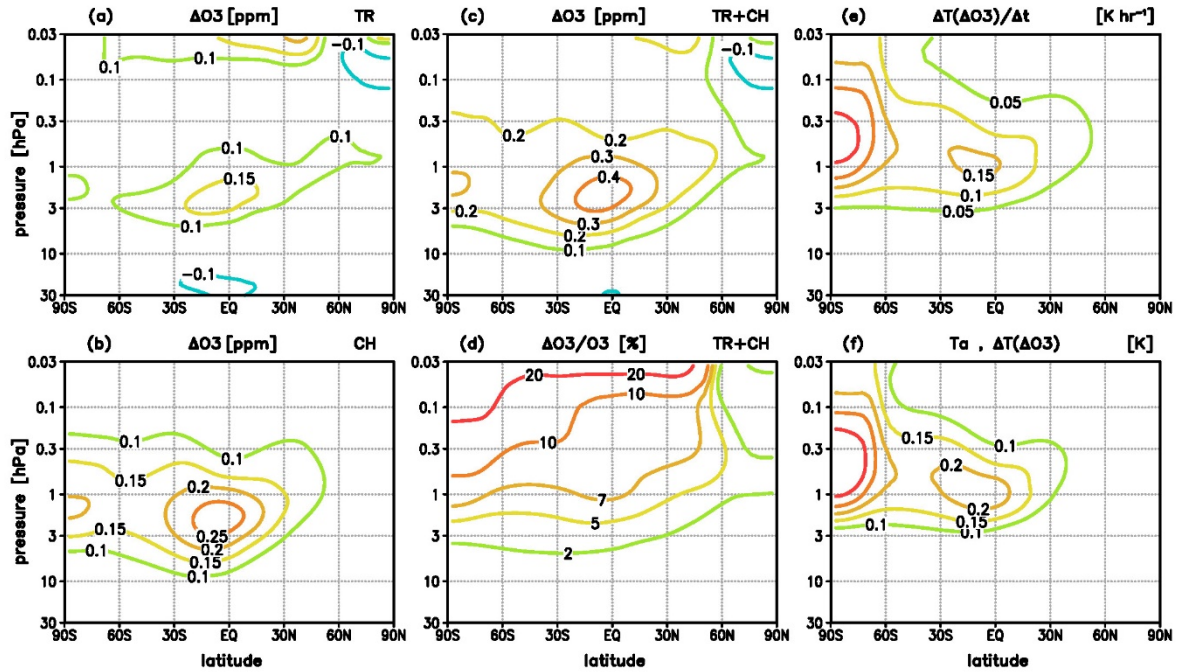


Figure 1: (a-c) Zonal and monthly mean background, (a) temperature T_0 , (b) ozone mixing ratio O_3 (the dashed line denotes where $\partial O_3 / \partial z = 0$) and (c) ozone heating rate Q_0 , January 2001, extracted from a simulation with the circulation and chemistry model HAMMONIA; (d-f) amplification factors (d) $1+ab$ and (e) N_0^2/N_μ^2 for a GW with horizontal and vertical wavelengths $L_k=500$ km and $L_m=5$ km, and (f) N_0^2/N_μ^2 for a GW with $L_k=800$ km and $L_m=3$ km; shaded areas denote the latitudes where the amplification is limited by the length of daylight ($\tau_i > \tau_{day}$).



685 **Figure 2:** Local changes due to ozone-temperature coupling induced by an initial GW perturbation with horizontal and vertical wavelengths $L_k=500$ km and $L_m=5$ km, and with exponential increase in amplitude with height (initial temperature amplitude $T_a(z_s)=1$ K at $z_s \approx 35$ km ($p=6.28$ hPa)); (a) change in ozone due to vertical transport, (b) change in ozone due to photochemistry, (c) total change in ozone, (d) relative change in ozone, (e) change in the heating rate, (f) change in the temperature perturbation.

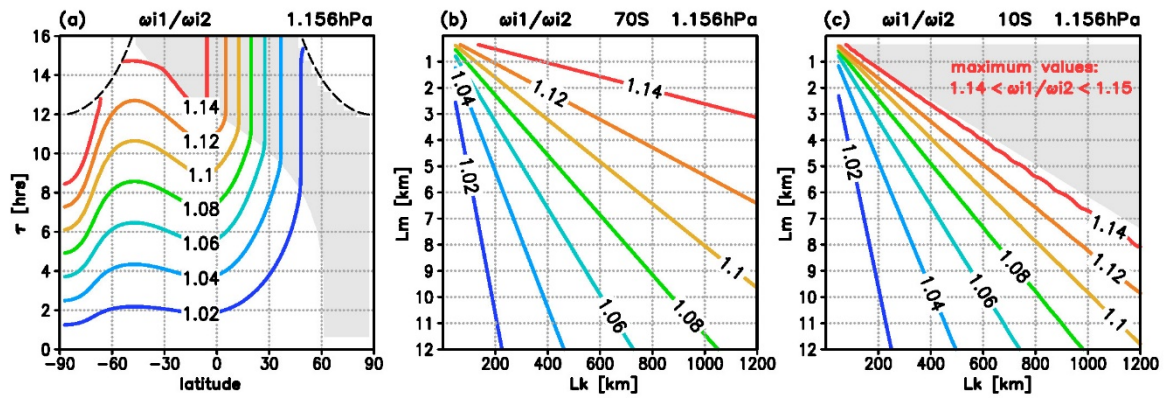


Figure 3: Amplification factor ω_{i1}/ω_{i2} at a level of the maximum values of ω_{i1}/ω_{i2} (1.156 hPa) illustrating the decrease of the intrinsic frequency with (ω_{i2}) compared to without (ω_{i1}) ozone-temperature coupling (compare with Figure 1e-f), (a) latitudinal distribution of ω_{i1}/ω_{i2} as a function of the initial wave period τ_i [in hours], and (b-c) dependence of ω_{i1}/ω_{i2} on the horizontal and vertical wavelengths L_k and L_m [in km] at (b) 70° S and (c) 10° S; shaded areas denote where the amplification is limited by the length of daylight ($\tau_i > \tau_{\text{day}}$).

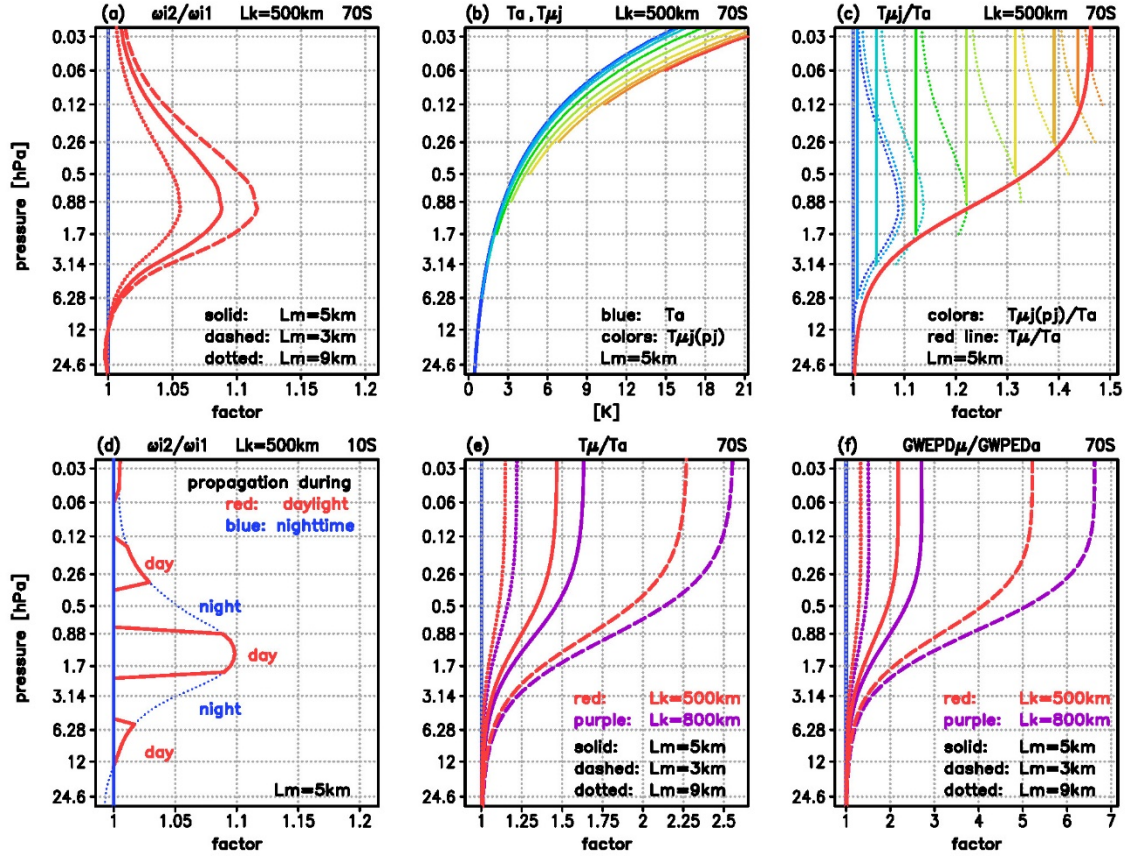
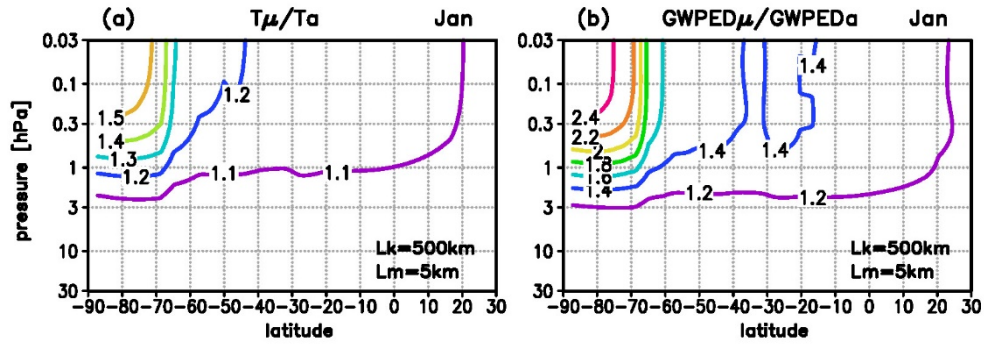


Figure 4: Illustration of the successive amplification of GW amplitudes during the upward level-by-level propagation, (a) amplification factor ω_{i2}/ω_{i1} at 70° S for a GW with horizontal wavelength $L_k=500$ km and vertical wavelength $L_m=5$ km (red solid line), and, for comparison, $L_m=3$ km (dashed) and $L_m=9$ km (dotted); (b) temperature amplitudes for the GW with $L_k=500$ km and $L_m=5$ km, depicting the initial perturbation T_a (blue) and the successively amplified amplitudes $T_{\mu j(z_j)}|_{j=1,n}$ (light blue towards red; here, $n=8$ for $L_m=5$ km), (c) same as (b) but for the relative amplitudes $T_{\mu j(z_j)}/T_a$ (solid lines) together with the profiles of the previous level multiplied by ω_{i1}/ω_{i2} (i.e., $T_{\mu j-1(z_{j-1})} \cdot (\omega_{i1}/\omega_{i2})$), dashed lines) and a fitted approach T_μ (thick red solid line, defined by Eq. 18), (d) same as (a) for the case $L_k=500$ km and $L_m=5$ km but at 10° S including the limitation due to the length of night-time conditions, (e) relative values T_μ/T_a at 70° S for different horizontal (red: $L_k=500$ km, purple: $L_k=800$ km) and vertical (dashed: $L_m=3$ km, solid: $L_m=5$ km, dotted: $L_m=9$ km) wavelengths, (f) same as (e) but for the relative values E_μ/E_a of the related gravity wave potential energy density (GWPED, defined by Eq. 19).



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Figure 5: Cumulative amplification of the GW amplitude during the upward level-by-level propagation for a GW with $L_k=500 \text{ km}$ and $L_m=5 \text{ km}$, (a) cumulative increase in the temperature amplitudes described by T_μ/T_α , (b) related increase in the gravity wave potential energy density (GWPED) described by E_μ/E_α ; background conditions: January 2001.

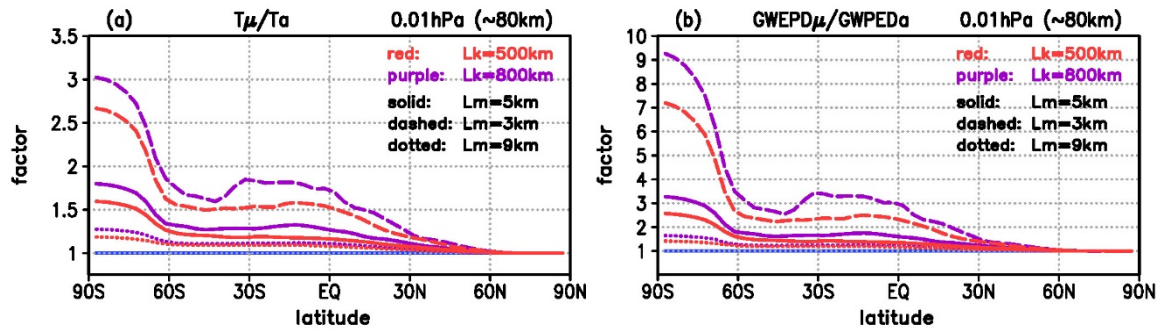


Figure 6: Cumulative amplification of the GW amplitudes similar as in Figure 5 but at upper mesospheric levels (0.01 hPa, ~80 km) for different horizontal and vertical wavelengths L_k (red: 500 km, purple: 800 km) and L_m (dotted: 9 km, solid: 5 km, dashed: 3 km), (a) T_{μ}/T_a , (b) E_{μ}/E_a .