

12 April 2022

To  
The Editor, ACP

We are herewith submitting our revised manuscript #acp-2021-1039, entitled “Estimated regional CO2 flux and uncertainty based on an ensemble of atmospheric CO2 inversions” by Chandra et al.

We thank the reviewers for helping us greatly with very helpful comments and suggestions. We now have a huge confidence that the article contains useful information for the interests shown by the reviewers in the work. We have made our best effort to revise the manuscript.

Two paragraphs at the end of the Results and Discussion, Supplementary Figure S10, and the final paragraph of the Conclusions are deleted following the suggestions of the reviewers and taking in to account their concerns on the methodology. This deletion also helps us getting rid of some of the not-so-clear discussions and improves brevity of the text, without compromising on overall contents of the article. However, we still feel that the issues raised in these two paragraphs and Figure S10 are important, and will be followed up by dedicated studies in the future.

Thank you very much for allowing us to submit the revised manuscript.

Sincerely yours,

Naveen Chandra  
(on behalf of all coauthors)

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**Reply to reviewer#01's comments**

We sincerely thank the reviewer for carefully reading our manuscript and providing us important feedbacks. We have tried our best to address them. Please find our detailed replies in black to each comment in grey.

This manuscript presents inverse model estimates of global and regional CO<sub>2</sub> fluxes over the last two decades. The inverse model is based on a single transport model assimilating observations from 50 sites. A series of 16 model simulations is conducted by varying the prior fluxes and prior and observational errors. Results are evaluated against independent aircraft data. The authors found that the ensemble mean of 16 optimized fluxes outperformed individual model outputs. The spread of flux estimates from these 16 model simulations is considered as the uncertainty of the estimated fluxes.

General comments

The manuscript presents a detailed study focusing on the inverse model estimation (using a single model) of CO<sub>2</sub> fluxes on a global scale for two decades. Therefore, the paper is worthy of publication in ACP after addressing the concerns listed below.

Thank you very much for appreciating our study.

Authors should present the novel aspect of this manuscript. This study uses a single inverse model and conducts a series of model simulations by changing model components, keeping the same observational dataset. Many model intercomparison projects (TransCom and GOSAT and OCO-2 inverse model intercomparisons) address the same aspects by including different transport models but by changing individual model components. Calculating the ensemble mean and spread using a single transport model is not the right way of quantifying the mean and uncertainty in CO<sub>2</sub> flux estimates (by not accounting for transport errors).

The novelty of this work is to understand the impact of prior fluxes, and uncertainties (model data uncertainty and prior flux uncertainty) on the estimate of posterior fluxes at the global and regional scale. We agree that the single model transport is not ideal, but please note that this study does not aim to give a full flux estimation uncertainty range, including that due to model transport. We aim to estimate the best CO<sub>2</sub> flux with our transport and provide uncertainty on the best-estimated flux. The transport errors are already explored extensively in the TransCom, GOSAT, and OCO-2 model intercomparison projects. We evaluate fluxes using independent flux estimation such as RECCAP and compare the simulation of a posteriori fluxes with independent aircraft data like GCP. These are mentioned in the Abstract.

81 The MIROC4-ACTM model transport quality has been checked separately using multiple tracer simulations as  
82 discussed in the methods section. The performances for inter-hemispheric gradient and vertical transport in the  
83 upper troposphere and lower stratosphere are reasonable. Nevertheless, no uncertainty is given to our flux  
84 estimation system.

85 We have now revised the manuscript and do our best to highlight the novelty of the work.

86

87 To investigate the impact of different modeling components such as model transport, priors, and specification  
88 of uncertainties, there could be other systematic approaches, such as designing a series of simulations and  
89 quantitatively assessing the uncertainty components. For example, see Basu et al. (2018) and Philip et al. (2019).  
90 More rigorous experiments are required if this manuscript intends to assess the spread from priors and  
91 prior/observation uncertainties.

92

93 We agree approaches in Basu et al. (2018) and Philip et al. (2019) are good, but for full scale transport error  
94 uncertainty estimate. However, the uncertainty we estimate is different from that estimated in Basu et al. (2018)  
95 and Philip et al. (2019). Our aim is to estimate uncertainty due to choices of prior fluxes and representation of  
96 model data and flux uncertainties. It is impossible to estimate the role of inverse model input parameters without  
97 running a single model with a number of different choices of inverse model parameters (e.g., prior flux  
98 uncertainty, model data uncertainty etc.); hence we use a well-tested single transport model. As stated earlier  
99 we compare our estimated fluxes with regional fluxes from independent studies (RECCAP).

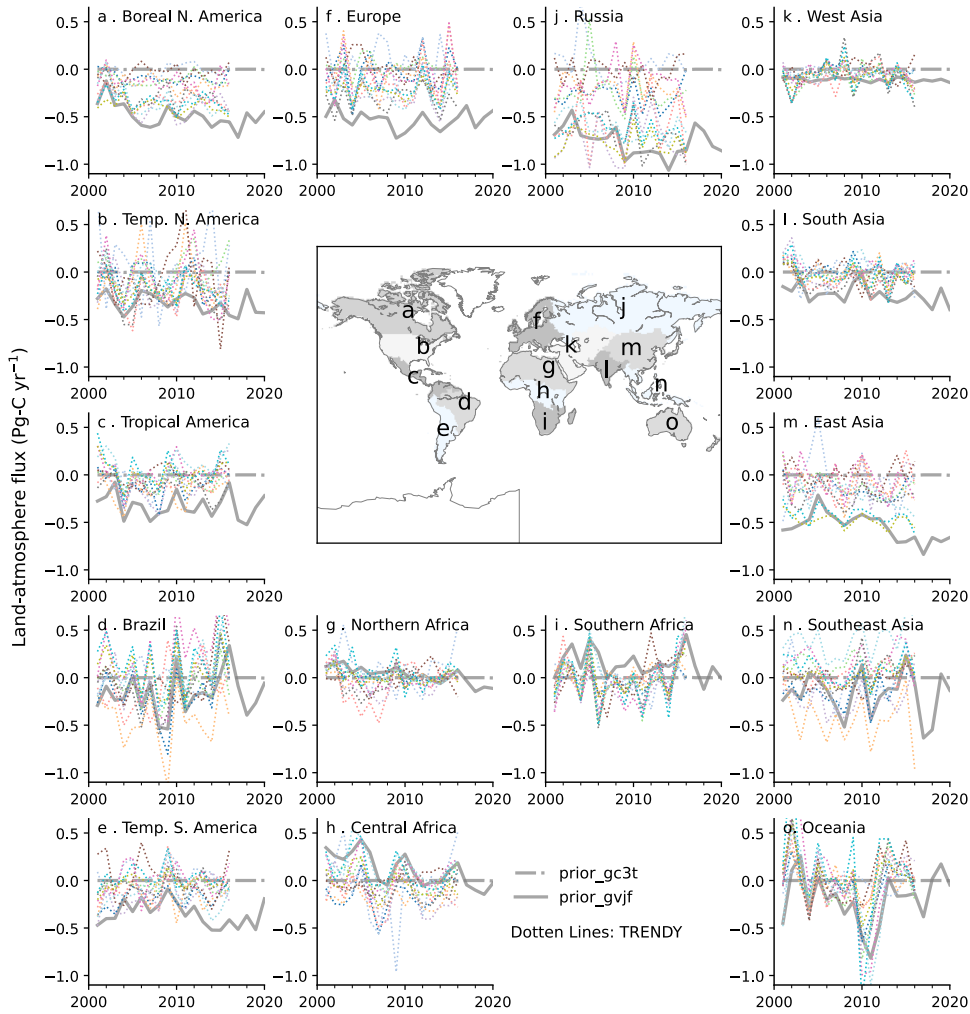
100

101 Randomly selecting two different terrestrial biosphere models (TBMs) or ocean models is insufficient.  
102 Otherwise, reconsider the focus of the manuscript. This study mainly tests land flux scenarios with and without  
103 interannual variability (IAV) (CASA versus VISIT). They should consider using different TBMs as priors  
104 (diagnostic/prognostic/with and without IAV etc.) with significant regional differences. That can lead to a  
105 reasonable spread in the optimized fluxes. Also, how about conducting a sensitivity test by artificially imposing  
106 zero net annual flux in the VISIT model?

107

108 While making choices on prior flux selection we did look in to the VISIT land and JMA ocean fluxes in  
109 comparison with typical DVGM simulations (GCP's TRENDY) and other ocean observation based flux  
110 products used in IPCC AR6, respectively. As you can see from the two plots below our Prior fluxes (CASA and  
111 VISIT; Takahashi and JMA) are fairly well encompassing the other available products. Therefore, we did not  
112 believe we needed more variety in our prior fluxes.

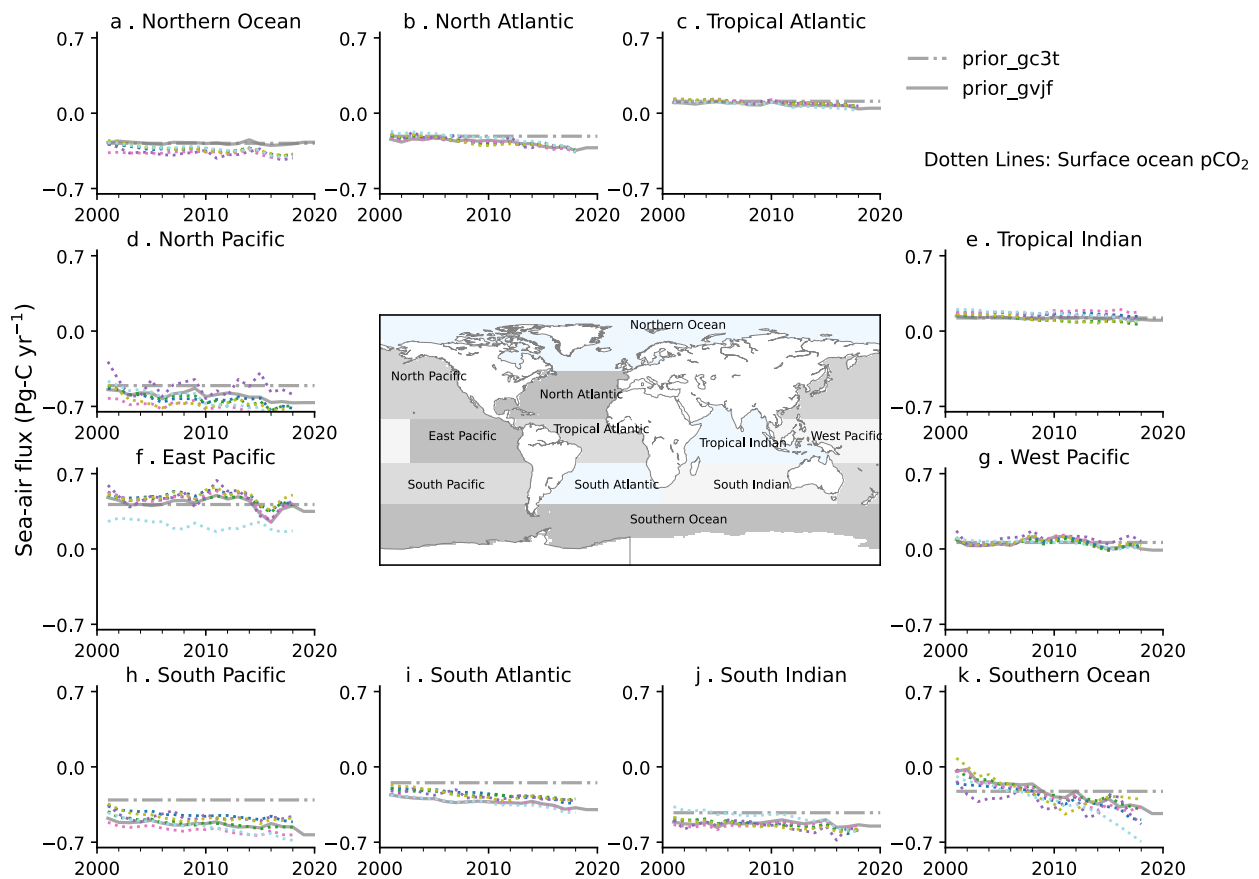
113 Figures 4, 5, 6 and 7 in the article are testimony that the inversions are able to bring a posteriori fluxes to a  
114 common value from both the prior flux extremes.



115

116 Figure R1. Comparisons of VISIT and CASA prior cases with TRENDY DGVMs (Sitch et al., 2015;

117 <https://doi.org/10.5194/bg-12-653-2015>) for 15 land regions.



118

119 Figure R2. Comparisons of JMA and Takahashi prior cases with pCO<sub>2</sub> observation-based products (Fay et al.,  
 120 2021; <https://doi.org/10.5194/essd-13-4693-2021>) for 11 ocean regions.

121

122 The manuscript should be written more carefully, especially the introduction and conclusion sections. There are  
 123 many empty/loose sentences, no connection between paragraphs, introduction not providing any motivation of  
 124 the paper (it also discusses unrelated aspects), grammatical mistakes, etc., throughout the manuscript. See some  
 125 of the corrections in the technical-correction section below.

126

127 Thank you for pointing this out here and suggesting numerous corrections below. The reviewer#2 is also very  
 128 kind in reading the manuscript line by line and pointing us to all corrections that are needed. We have made our  
 129 best effort to incorporate all suggestions and revise the manuscript.

130

131 Specific comments

132

133 Line 17-21: These two sentences are not connected. You state that model errors and insufficient observations  
 134 lead to uncertainties in regional flux estimates. However, it is unclear how you address these with your  
 135 simulations using a single model. State clearly what uncertainty component you are addressing here in this  
 136 article.

137

138 We have revised the two sentences as

139 “However, the uncertainties in the regional flux distributions remain unconstrained due to the lack of high-  
140 quality measurements, uncertainties in model simulations, and representation of data and flux errors in the  
141 inversion systems. Here, we assess the representation of data and flux errors by using a suite of 16 inversion  
142 cases derived from a single transport model (MIROC4-ACTM) but different sets of a priori (bottom-up)  
143 terrestrial biosphere and oceanic fluxes, as well as prior flux and observational data uncertainties (50 sites) to  
144 estimate CO<sub>2</sub> fluxes for 84 regions over the period 2000-2020.”

145

146 Line 26-28: This is just a general statement. Need more clarity here: “Interannual variability and seasonal cycle  
147 in CO<sub>2</sub> fluxes are more consistently derived for different prior fluxes when a greater degree of freedom is given  
148 to the inversion System”.

149

150 We have slightly revised the sentence as

151 “Interannual variability and seasonal cycle in CO<sub>2</sub> fluxes are more consistently derived for two distinct prior  
152 fluxes when a greater degree of freedom (increased prior flux uncertainty) is given to the inversion system.”

153

154 Line 28-29: In line 261, you mention that fluxes are evaluated with aircraft observations. Are you using surface  
155 data as well? “...evaluated the inversion fluxes using independent aircraft and surface measurements not used  
156 in the inversion”.

157

158 Yes, surface data are also used, say in Fig. 12 (bottom row)

159

160 Line 28-29: Good if you can make it more quantitative, i.e., add some summary statistics or so: “which raises  
161 our confidence in the ensemble mean flux rather than an individual inversion”

162

163 We consider this remark and revised the sentence as

164 “We have further evaluated the inversion fluxes using meridional CO<sub>2</sub> distributions from independent (not used  
165 in the inversions) aircraft and surface measurements, suggesting that the ensemble mean flux (model-  
166 observation mean±1σ standard deviation = 0.3±3 ppm) best suited for global and regional CO<sub>2</sub> flux budgets  
167 than an individual inversion (model-observation 1σ standard deviation = 0.35±3.3 ppm).”

168

169 Line 31: It seems like an empty/loose sentence: “Differences between 5-year mean fluxes show promises and  
170 capability to track flux changes under ongoing and future CO<sub>2</sub> emission mitigation policies.”

171

172 We have slightly revised the sentence for clarity as:

173 “Using the ensemble mean fluxes and uncertainties for 15 land and 11 ocean regions at 5-year intervals, we  
174 show promises and capability to track flux changes toward supporting the ongoing and future CO<sub>2</sub> emission  
175 mitigation policies.”

176

177 Line 36-38: Cite IPCC report.

178

179 Canadell et al. is the referring to the Chapter of IPCC AR6 which has assessed the TCRE etc. Cited again in the  
180 next sentence, instead of this general sentence.

181

182 Line 44: Be very clear (solutions to ...?): “The sinks on the land and ocean constitute a major component of  
183 nature-based solutions”.

184

185 We modified the sentence as

186 “The sinks on the land and ocean constitute a major component of nature-based solutions to mitigate the rise in  
187 CO<sub>2</sub> concentration, as discussed in the IPCC AR6 (Canadell et al., 2021)”

188

189 Line 45-46: Cite proper references to support the statement.

190

191 The paragraph is rearranged and shifted to Line#57. We have added a reference to Kondo et al. (2020) for this  
192 sentence.

193

194 Line 45-53: In this paragraph, mention global flux uncertainty first, and then note the regional issues, with some  
195 additional details. That is, lines 45-46 should come after line 53.

196

197 Rearrangements of the text is done as per your suggestions.

198

199 Line 55-69: It is not clear why you need this paragraph. “However, the impacts of biases in FFC emissions on  
200 inversion estimated CO<sub>2</sub> fluxes remained relatively unexplored”. Are you exploring this aspect in this paper?  
201 Moreover, this paragraph is written poorly.

202

203 The aim of this introduction on FFC aliasing effect to give the background of the discussions related to the flux  
204 trends for East Asia; Fig. 6 and Fig. 10. Some revisions are now made based on reviewer#2’s suggestions and  
205 we have added some text in the previous paragraph to link the topics. Hope the paragraph reads better now.

206

207 Line 70-73: I don’t quite understand this statement! Who provides the metric, what is that metric? What’s the  
208 meaning of “metric for evaluation of regional fluxes should be evaluated”? Clarify.

209

210 We have now revised this paragraph. The 2<sup>nd</sup> sentence is deleted in the process. Hope the paragraph read well  
211 now.

212

213 Line 71-73: Is this something new? "...should be evaluated using a new transport model simulation of the  
214 predicted fluxes, not using the assimilated CO<sub>2</sub> field". Be clearer with sufficient details. Most evaluations in  
215 current published works are based on model simulation of optimized fluxes. For evaluation, using a different  
216 transport model than the one used in the inversion (as a forward model) is advantageous (not sure if this is what  
217 you mean here). Also, are you exploring this in this manuscript/study?

218

219 No, unfortunately this could not be explored in details and remained as a hypothesis. Thus, we have revised this  
220 paragraph by cleaning up texts.

221

222 Line 73-81: I'm lost here. From re-reading this, I understand that the assessment of the spread of optimized  
223 fluxes obtained by conducting multiple simulations using different model inputs is a better way of quantifying  
224 the uncertainty than simply evaluating the optimized CO<sub>2</sub> concentrations against independent measurement  
225 data. Revise the entire paragraph to be more apparent.

226

227 Thank you. We have revised the paragraph as a whole, and added at the end as discussed in previous comment  
228 (Line 70 – 73)

229 "Another way of improving our knowledge about uncertainties in regional flux estimations is to employ multiple  
230 types of datasets from both bottom-up and top-down modelling systems (Ciais et al., 2021; Kondo et al., 2020),  
231 which we have adapted here for checking the regional inversion fluxes, in addition to the GCP like evaluation  
232 using independent aircraft data."

233

234 Line 82-85: These uncertainty sources have been investigated previously. Cite some of those critical studies  
235 here.

236

237 We have cited : (Basu et al., 2018; Patra et al., 2005a; Philip et al., 2019; Qu et al., 2021; Wang et al., 2018).

238

239 Line 92-95: This statement is not correct: "Such intercomparisons used single inversion from different modeling  
240 groups and provided the range in CO<sub>2</sub> flux uncertainty due to differences in transport models.". These  
241 intercomparisons assessed uncertainty arising from different model components, not just the transport model  
242 differences. For example, see Crowell et al., 2019 and Peiro et al., 2022.

243

244 We are aware of these publications (Crowell et al. 2019 is already cited; Peiro et al. used fluxes for an extended  
245 period) which makes assessments of regional fluxes estimated by inversions using OCO-2 data but none of both  
246 give separate assessments of prior flux uncertainty vs data uncertainty on the inversion results, for example. In



247 fact, it is impossible to estimate the role of inverse model input parameters without running a single mode with  
248 a number of different choices of inverse model parameters (e.g., prior flux uncertainty, measurement data  
249 uncertainty etc.).

250  
251 Following your and Reviewer#2 suggestion we have modified the statement as

252 “Such intercomparisons used single inversions from different modelling groups and provided the range in total  
253 CO<sub>2</sub> flux uncertainty due to the choices of prior fluxes distribution, prior flux uncertainty, observational data  
254 uncertainty, and the model transport uncertainties.”

255

256

257 Line 123-124: This sentence is not clear to me.

258

259 The sentence is revised as

260 “Reasonably good model transport in MIROC4-ACTM enables us to use any mismatch between observation  
261 and simulations to estimate the land and oceanic fluxes using the inverse modelling technique (details in Section  
262 2.4).”

263

264 Line 128 and 129: Just “used” not “simulated” (?): “... is simulated using ...”

265

266 Corrected as per your suggestion.

267

268 Line 135: “...downscaled to 3-hourly time intervals...”: Mention how you downscaled; which variable used;  
269 and cite proper literature.

270

271 Thank you for pointing this out. The sentence is revised as “The CASA and VISIT monthly-mean fluxes are  
272 downscaled to 3-hourly time intervals by redistributing respiration and gross primary production (Olsen and  
273 Randerson, 2004) using JRA-55 meteorology, i.e., 2m air temperature and incoming solar radiation at the earth  
274 surface”

275

276 Line 136: Double-check if it is version 4.1? “...fire emissions are used from GFEDv4s (van der Werf et al.,  
277 2017...”.

278

279 Thank you for catching the mistake. Yes, we have used v4.1s

280

281 Line 145: Complex notations: gc3t and gvjf. What is “3” and “t” in gc3t?

282

283 Agreed, but we created a 4 lettered name to accommodate all 4 fluxes, as given in Eq. 1. We have slightly  
284 rearranged for better clarity about how the notations are formed: g: GridFED FFC, c3:CASA-3hr, v:VISIT,  
285 t:TT09 ocean, j: JMA ocean, and f: Fire

286

287 Line 149-150: Revise: “to evaluate the strength of MIROC4-ACTM simulations to derive fluxes consistently”.  
288 How do you evaluate the strength of simulation? Why did you mention “consistently” here? Fluxes will be  
289 derived using the inverse model, so how can you “evaluate the strength of forward simulation”?

290

291 Sorry for the unclear information. Our intent was to evaluation inversion strength. So, we have changed  
292 “simulations” by “inversions” for clarification. We stated both - consistently (or the lack of it)! We think  
293 transport model is key for the fluxes we derive, although CO<sub>2</sub> is an inert species and transport is linear. So, we  
294 thought of mentioning the model’s name.

295

296 Line 159: Cite proper references: “WDCGG websites as appropriate”

297

298 Given as : GML/NOAA ([https://gml.noaa.gov/aftp/data/trace\\_gases/co2/flask/](https://gml.noaa.gov/aftp/data/trace_gases/co2/flask/)) and WDCGG  
299 (<https://gaw.kishou.go.jp/>) websites

300

301 Line 162: Is this the grid cell with the observation location? “...nearest grid of observation location at hourly  
302 intervals...”.

303

304 Revised as “the grid point nearest to the observation location” for clarity

305

306 Line 164: “These temporal data gaps (1-6 months) are filled using the curve fitting method based on the digital  
307 filtering technique”. Have you conducted simulations without using curve-fitted data? Why was this data filling  
308 necessary?

309

310 The matrix inversion system requires data every month of the inversion period. We have checked the fitting  
311 program works well when data gap is less than 6 months, as the seasonal cycle is derived by using 6 harmonics.

312

313 Line 200-210: How about conducting a simulation with “gpp\_v4” along with “ocean PFU = 0.5”? Explain the  
314 rationale for selecting different prior error scenarios you considered in this study.

315

316 We have stated the rationale as: (sorry without conducting the suggested simulation, we think a much greater  
317 number of model input parameters need to be tested and used in the future studies)

318 Selection of wide range of PFUs, in the range of 0.5 – 1.0 PgC yr<sup>-1</sup> the ocean regions and 0.2 – 4.0 PgC yr<sup>-1</sup> for  
319 the land regions allows us to understand about the stability of the inversion system as assess the range of a  
320 posteriori fluxes for aggregated sub-continental/basin regions or the land and ocean totals.

321

322 Line 234: “High values (FUR towards 100)”: If FUR is in percentage, then revise the equation in line 233.

323

324 Revised as per your suggestion.

325

326 Line 244: Not clear: “... indicative of the observational constraint regional fluxes...”

327 Line 245: “...we recommend that the spread of ensemble inversions provide more representative estimation of  
328 the regional CO<sub>2</sub> sources and sinks.”. “Spread” represents “a measure of uncertainty”, not a “representative  
329 estimation of...”. Why do you add “recommend” here?

330

331 This sentence is revised as

332 “As discussed later in this article, the FUR is only indicative of the observational constraint on the regional  
333 fluxes, the spread of ensemble inversions provides a measure of uncertainty of the regional CO<sub>2</sub> sources and  
334 sinks.”

335

336 Line 309 and 311: Revise this sentence: “Hence, the magnitude of biases and RMSE indicates predominantly  
337 the accuracy of the predicted fluxes.”. Model transport is one of the sources leading to uncertainties in the  
338 predicted fluxes.

339

340 As a remark. we have revised this sentence as

341 “Hence, the magnitude of biases and RMSE indicates predominantly the accuracy of the predicted fluxes (the  
342 errors due to model transport and measurement network are not explored in this study).”

343

344 Line 649: “CO<sub>2</sub> simulations are derived from three sets of prescribed fluxes: “gc3t”, “gvjf”, and “ensm”.”: I’m  
345 assuming that the evaluation is conducted for all 16 inversions (?).

346

347 All 16 sets are not simulated by model, but we used three representative cases, and part of this sentence is now  
348 revised for clarity as

349 “The CO<sub>2</sub> simulations are derived from three sets of prescribed fluxes: “gc3t” (case: ctl\_ux4\_gc3t in Table 2),  
350 “gvjf” (case: ctl\_ux4\_gvjf), and “ensm” (average of all 16 inversions).”

351

352 Lines 709-720: I’m not sure if these details (+ Figure S10) are required in this paper.

353

354 Thank you for this suggestion. Review#2 also expressed concerns on this part of the discussion.

355 We have removed this paragraph and the one before it, and Fig. S10.  
356 However, we still feel that the issues raised in these two paragraphs and Figure S10 are important, and will be  
357 followed up by dedicated studies in the future.  
358  
359 Line 775-782: Empty/loose sentences.  
360  
361 We have deleted this final paragraph of the Conclusions, as per your suggestion and also because lines 692-720  
362 in the submitted version are deleted following suggestions from you and Reviewer#2.  
363  
364 Technical corrections  
365 Line 14: Better add “atmospheric” here: “chemistry-transport model (ACTM)”.  
366 Line 16: Better avoid text in parenthesis: “regional flux (+ve: source to the atmosphere; -ve: sink on  
367 land/ocean)”.  
368 Line 21: Move the number of the sites (50) from here to the appropriate part of the sentences: “data uncertainties  
369 (50 sites)”.  
370 Line 24: Is this “22-33% and 16-18%” for land vs ocean? Not sure this is clear enough here.  
371 Line 25: Not clear what this approximate means here: “best estimations for (approx. 2000-2009)”.  
372 Line 52: Revise and add more clarity: “partitioning exists greatly in the ... release”.  
373 Line 55-56: Revise this sentence: “...because inversion calculations do not optimize...”.  
374 Line 90-91: You can write these in a better way: “inversions from ... for inversions using ... or for inversions”.  
375 Line 99: Revise: “observed and model data processing”.  
376 Line 100: Avoid capital letter: “the Results and discussion”.  
377 Line 155-156: Avoid repetition of “from”.  
378 Line 1120: Correct this: “lower panel (b)”.  
379 Line 242: Correct: “...West Asia, Northern Africa. The Tropical Indian Ocean...”.  
380 Line 252: Correct: “as per analysis”.  
381 Line 302-307: Use simple notations. For example, avoid “aircraft” from “x”.  
382 Line 308: Correct: “CO2 mixing ratios”.  
383 Line 317: Use the term “grid cells”.  
384 Line 336: Avoid “.”: “3.2. Global totals.”  
385 Line 346: Use “mean”: “Ensemble means land”.  
386  
387 We appreciate your help very much. All of the above corrections are made in the revised manuscript.  
388  
389 Line 563: Revise: “It is not easy for us to explain”.  
390 Thank you for the suggestion, we have further scrutinized the Yasunaka et al. paper and added

391 “It is not easy to put forward a hypothesis for the weaker sink in summer than in winter of Northern Ocean,  
392 while we can speculate that the atmospheric CO<sub>2</sub> decrease in polar air exceeds compared to the decrease that  
393 occur over the surface sea-water and reduced solubility of CO<sub>2</sub> in warmer water. Indeed, Yasunaka et al. (2018)  
394 have shown that the Greenland-Norwegian seas and Barents Sea are indeed acts as milder sink of CO<sub>2</sub> (flux = -  
395 4 to -5 mmol m<sup>-2</sup> day<sup>-1</sup>) during June-August compared to the October-March (flux = -10 to -15 mmol m<sup>-2</sup> day<sup>-1</sup>)  
396 <sup>1</sup>), and the Chukchi Sea and Arctic Ocean show strongest uptake in October. Thus, as whole the Northern Ocean  
397 of our study could act as the weakest sink in summer months.”

398

399 Line 763: Avoid “Please”.

400 Line 766: Correct: “is unanimously located”.

401 Figure 4: Choose a different font that is clearer.

402 Figure S2: Correct to CO<sub>2</sub>: “monthly-mean CO fluxes”

403

404 All of the above corrections are performed. We appreciate your help very much.

405

406 References

407 Basu, S., et al.: The impact of transport model differences on CO<sub>2</sub> surface flux estimates from OCO-2 retrievals  
408 of column average CO<sub>2</sub>, *Atmos. Chem. Phys.*, 18, 7189–7215, <https://doi.org/10.5194/acp-18-7189-2018>,  
409 2018.

410 Crowell, S., et al.: The 2015–2016 carbon cycle as seen from OCO-2 and the global in situ network, *Atmos.*  
411 *Chem. Phys.*, 19, 9797–9831, <https://doi.org/10.5194/acp-19-9797-2019>, 2019.

412 Peiro, H., et al.: Four years of global carbon cycle observed from the Orbiting Carbon Observatory 2 (OCO-2)  
413 version 9 and in situ data and comparison to OCO-2 version 7, *Atmos. Chem. Phys.*, 22, 1097–1130,  
414 <https://doi.org/10.5194/acp-22-1097-2022>, 2022.

415 Philip, S., et al.: Prior biosphere model impact on global terrestrial CO<sub>2</sub> fluxes estimated from OCO-2 retrievals,  
416 *Atmos. Chem. Phys.*, 19, 13267–13287, <https://doi.org/10.5194/acp-19-13267-2019>, 2019.

417

418 All of these references are cited in the revised manuscript

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429 **Reply to reviewer#02's comments**

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431 We sincerely thank the reviewer for carefully reading our manuscript and providing us important feedbacks.

432 We have tried our best to address them. Please find our detailed replies in black to each comment in grey.

433

434 This manuscript explores the sensitivity of a global CO<sub>2</sub> flux inversion using CO<sub>2</sub> mixing ratio measurements  
435 to the choices of prior flux, prior flux uncertainty, and measurement uncertainty assumed in the inversion. Gap-  
436 filled measurements from 50 globally-distributed sites are used and monthly fluxes across 2000-2020 are  
437 estimated for 84 emission regions (54 on land, 30 for the oceans). Given that the fluxes to be estimated are  
438 severely under-constrained by the data used here, especially in the tropics and southern hemisphere (SH) where  
439 the data are sparse, it is not surprising that the final estimate should depend strongly on the prior estimate  
440 assumed going in. The sensitivity to two different sets of prior fluxes are explored here: 1) annually-balanced  
441 CASA land biospheric fluxes paired with Takahashi (1999) ocean fluxes, a combination that results in too large  
442 of a trend of CO<sub>2</sub> in the atmosphere due to the lack of the realistic global land sink, and 2) land biospheric  
443 fluxes from the VISIT model that have too large of an global annual uptake, resulting in a too-small trend of  
444 CO<sub>2</sub> in the atmosphere, coupled with ocean fluxes from the JMA model. The bias in the global land+ocean  
445 uptake embodied in each of these sets of prior fluxes is reduced in the posterior flux estimates, but remains at a  
446 lower level, especially for individual regions instead of the global level. Since the two priors had errors in the  
447 trend of opposite signs, averaging results over the two cases results in lower errors with respect to the truth.

448

449 Besides varying the prior fluxes themselves, the authors explore the impact of assuming different values for the  
450 uncertainty on these prior fluxes as well as the uncertainty on the measurements (or model-measurement  
451 mismatches, to be more precise). One must assume some value for these uncertainties in the inversions, and  
452 these assumed values are always incorrect to some degree, since one never knows precisely what the true  
453 uncertainty ought to be: the larger the errors in these assumed values, the larger the error in the a posteriori  
454 estimate due to the bad assumptions; these errors tend to be systematic rather than random, so it is quite useful  
455 to know how large of an impact they have. In my view then, this study is worth publishing because it quantifies  
456 the impact of these mis-specified statistical assumptions, even if the global CO<sub>2</sub> flux inversion underpinning  
457 this work is far from being cutting edge. (Global CO<sub>2</sub> inversions of this sort using the in situ CO<sub>2</sub> measurement  
458 network have been done for over two decades, going back to the 1990s at least. There are now many more in  
459 situ measurement sites than the 50 used here, including tall towers on the continents and the routine aircraft  
460 profiles that have been used here for evaluation purposes. Furthermore, there are column-integrated CO<sub>2</sub>  
461 measurements from ground-based Fourier spectrometers looking at the sun, as well as the huge volume of  
462 column CO<sub>2</sub> data from satellites. These data are now used routinely to estimate fluxes for thousands of regions,  
463 instead of just the 84 used here.)

464

465 The authors have done a nice job setting up their ensemble of runs (16 total, permutations of the 2 flux priors,  
466 2 different assumptions for the magnitude of measurement uncertainties assumed, and 4 different assumptions  
467 for the magnitude of a priori flux uncertainty assumed) and have done a careful job of analyzing the results from  
468 a variety of perspectives (global total, land/ocean totals, regional fluxes, annual means, interannual variability,  
469 seasonal variability, the estimation uncertainty versus the sensitivity of the estimate to the priors and assumed  
470 statistics, and errors evaluated by comparing to independent data). While the manuscript is quite long and may  
471 be daunting to some readers, I realize that there is a lot of ground to cover and am sympathetic that the length  
472 is not inappropriate. However, my main problem with the manuscript is with the writing: in many places, it is  
473 difficult to understand the points that are being made. As a result, I had difficulty understanding precisely what  
474 was done in this work, both in terms of the method used for the inversion and the methods used for the analysis,  
475 as well as the results obtained and the logic used to interpret those results. Therefore, before being published  
476 in ACP, I would like the authors to do a better job with their writing, making it clearer what was actually done  
477 and what the implications of their work really are. I think that they should also note that their setup here is more  
478 under-constrained by the data than most, and therefore the impact of the error sources that they examine is  
479 probably larger for this study than for inversions that use more data. Finally, when quantifying the uncertainty  
480 in the flux estimates, the authors need to do a better job explaining what error terms are quantified by their  
481 ensemble spread, and what are not (the authors note that transport model error is not quantified, since they only  
482 used a single transport model in this study, but they do not do a good job pointing out the difference between  
483 the estimation errors usually quantified by the inversion and the errors examined here in their sensitivity study,  
484 or the slight overlap between the two (due to the errors or differences in the prior fluxes)). I have noted below  
485 the places where the authors should clarify their text, and I have made numerous editorial corrections and  
486 suggestions for better wording that will hopefully make it easier for the reader to understand what is going on.  
487 I apologize for not breaking out the more-editorial comments separately from the more substantive ones: at the  
488 moment, they are all mixed together in rough line-number order.

489

490 We are overwhelmed by your efforts in reading the article so carefully. We have no words to appreciate or thank  
491 you enough. While revising the manuscript and writing replies we have felt that it requires immense patience  
492 and extraordinary helping nature to prepare such a review, for no credits.

493 We have revised whole manuscript as per your suggestions.

494

495 Detailed comments (line number indicated):

496

497 24: "without riverine export correction" -- I take this to mean that these are the actual fluxes inverted, and that  
498 if you corrected for 0.6, say, you would get  $1.6 + 0.6 = 2.2$  PgC/yr storage in the ocean. Please give more detail  
499 as to what making this correction would do to the results and how that relates to anthropogenic fluxes/storage.

500

501 We have added “The rivers carry about 0.6 PgC yr<sup>-1</sup> of land sink in to deep ocean, and thus the effective land  
502 and ocean partitioning is -2.3±0.3 and -2.2±0.3, respectively.”

503

504 29-30: "which raises our confidence in the ensemble mean flux rather than an individual inversion." Reword  
505 for clarity.

506

507 Revised as

508 “We have further evaluated the inversion fluxes using meridional CO<sub>2</sub> distributions from independent (not used  
509 in the inversions) aircraft and surface measurements, suggesting that the ensemble mean flux (model-  
510 observation mean±1σ standard deviation = -0.3± 3 ppm) best suited for global and regional CO<sub>2</sub> flux budgets  
511 than an individual inversion (model-observation 1σ standard deviation = -0.35±3.3 ppm).”

512

513 52: what does "greatly" indicate here? Reword for clarity.

514

515 The land and ocean sink uncertainty assessed in Canadell et al. is based on GCP CO<sub>2</sub> budget. We revised the  
516 sentence as

517 “The uncertainty in land and ocean sink partitioning of up to about 1 PgC yr<sup>-1</sup> in the IPCC AR6 are based on  
518 the Global Carbon Project (GCP)’s annual carbon budget”

519

520 56: It is not correct to say that inversions do not optimize the FFC emissions. They solve for corrections to the  
521 prior fluxes (including FFC ones), and then this correction must be partitioned between ocean, land biospheric,  
522 and FFC fluxes. Because the uncertainty on the prior FFC fluxes is thought to be much lower than that on the  
523 land biospheric fluxes, most of the correction should therefore be attributed to the land biospheric fluxes.  
524 However, a small part of it could also be attributed to the FFC ones. Usually this small amount is neglected and  
525 all of the correction over land is attributed to the land biospheric fluxes. However, this is a simplification.  
526 Inverse modelers could, without changing their inversions, choose to partition the correction differently between  
527 the two. As it is, they are very aware that some of the correction that they currently attribute to the land  
528 biospheric fluxes could also be due, in part, to errors in the initial FFC fluxes.

529

530 Following your suggestion, we have revised the later part of the first sentence for better clarity, as

531 “Top-down inverse models estimate residual natural or non-FFC CO<sub>2</sub> fluxes from land and ocean regions  
532 because inversion calculations do not explicitly optimise the FFC emissions, i.e., the FFC emissions are not  
533 revised, but the a priori land and ocean sinks are revised.”

534

535 64: reword "slower or faster" to "more slowly or quickly"; also add "and" before ")3"

536 66: change "on" to "from" in "on the IEA"

537 Both of the corrections are made.



538

539 70-81: While interesting, the authors need to do a better job later in the text of explaining why this new metric  
540 is needed (i.e. why one should get a different set of simulated measurements when doing a separate forward run  
541 than in the inversion itself).

542

543 We have updated/expanded the discussion here:

544 Evaluation of predicted fluxes from model-data differences may not be straightforward due to the underlying  
545 assumptions of a flux inversion system, e.g., for flux correlation lengths or the radius of influence for the  
546 measurements, observational data uncertainty, prior flux uncertainty (Baker et al., 2010; Chevallier et al., 2007;  
547 van der Laan-Luijkx et al., 2017; Miyazaki et al., 2011; Niwa et al., 2017; Rodenbeck et al., 2003), while the  
548 data assimilation system will fit the model concentrations to the observed values. Thus, good statistics for the  
549 validation metric using independent data and assimilated concentration field did not ensure good agreement  
550 between the estimated fluxes by different models, at the sub-hemispheric and sub-continental scales, or  
551 separately for land and ocean. For example, a model-observation difference within  $\pm 1$  ppm and/or vertical  
552 concentration gradient simulation within  $1-\sigma$  standard deviation of the observed gradient resulted in more than  
553  $1 \text{ PgC yr}^{-1}$  flux differences between models at regional or sub-hemispheric scales (Gaubert et al., 2019; Stephens  
554 et al., 2007; Thompson et al., 2016).

555

556 84: add "to" after "leading"; add "and" after "error,"

557 92: change to "single inversions"

558

559 Both the corrections are made.

560

561 93-95: What you are trying to say here is that none of these studies partition the inversion-group-based  
562 uncertainty between these three sources, but just give the total uncertainty. Try to reword it to bring out that  
563 point better.

564

565 Following your suggestion, two sentences are merged to one as

566 “Such intercomparisons used single inversions from different modelling groups and provided the range in total  
567 CO<sub>2</sub> flux uncertainty due to the choices of prior fluxes distribution, prior flux uncertainty, observational data  
568 uncertainty, and the model transport uncertainties.”

569

570 100: change to "Section 2" and "Discussion"

571 104: change to "Section 4"

572 112: remove "(" before "Bisht"

573 134: change "via" to "due to", for clarity; correct "on the net a large land sink" -- doesn't make sense now

574 144: add "fluxes" after "land"

575 Table 1, line 3: add a degree sign after the first "2.8"  
 576 155: change "The 38" to "Of these, 38"  
 577 156: "and 3"  
 578 162: reword to "sampled at the observation time and the grid box nearest to the observation location at hourly  
 579 intervals."  
 580 163: change "six months" to "six-month"

581  
 582 Thank you for these suggestions. All of the above corrections are made in the revised manuscript.  
 583

584 166: "with six harmonics by a cut-off length of 24 months for the digital filter."  
 585 It is not really clear how these six harmonics were chosen, given this wording. Please reword it to be clearer.  
 586 Sorry for the incorrect formulation. We revised the sentence as  
 587 "We fit the measured and simulated time-series at daily-weekly time intervals with six harmonics (extracts the  
 588 sinusoidal component, i.e., seasonal cycle) and Butterworth digital filter with a cut-off length of 24 months  
 589 (determines the long-term trends)"

590  
 591 169, Section 2.4: It is unclear what sort of Transcom-like inversion is being performed here. Is it the so-called  
 592 "cyclo-stationary" inversion, in which a single, typical seasonal cycle of flux is being solved for, then added  
 593 onto the prior? Or is it a fully time-dependent inversion in which the seasonal cycle for each year is optimized?  
 594 How many terms are in the state vector solved for? Is it a matrix-based inversion? How large is the matrix  
 595 actually inverted? How is the prior treated in this framework (i.e. what is the set of equations that is actually  
 596 solved, and where does the prior fit into that)? I note below that equations (1)-(3) do not seem to be written  
 597 correctly, in that S and D ought to be vectors, not matrices. In Figure S1 it is suggested that the basis functions  
 598 in the G matrix have only been run out for four months -- how is the impact of a flux represented for times after  
 599 those four months? Is the influence just ignored? Perhaps I am missing something here -- please describe what  
 600 you are doing more completely to make all this clearer.

601  
 602 Apologies for the poor construction of the equations and description. It is now revised as:  
 603

604 "In the Bayesian inversion, when the relation between model parameters and data parameters is linear ( $d = \mathbf{J}\vec{s}$ ),  
 605 the misfit function ( $\chi^2$ ) is constructed as (Rayner et al., 2008; Tarantola, 2005)

$$606 \chi^2 = \frac{1}{2} \left[ (\vec{s} - \vec{s}_0)^T \mathbf{C}(\vec{s}_0)^{-1} (\vec{s} - \vec{s}_0) + (\mathbf{J}\vec{s}_0 - \vec{d}_{obs})^T \mathbf{C}(\vec{d})^{-1} (\mathbf{J}\vec{s}_0 - \vec{d}_{obs}) \right] \quad (2)$$

607 Assuming that the elements of  $\mathbf{C}(\vec{d})$  are uncorrelated, the solutions for  $\vec{s}$  and  $\mathbf{C}(\vec{s})$  can then be written as

$$608 \langle \vec{s} \rangle = \vec{s}_0 + \left( \mathbf{J}^T \mathbf{C}(\vec{d})^{-1} \mathbf{J} + \mathbf{C}(\vec{s}_0)^{-1} \right)^{-1} \mathbf{J}^T \mathbf{C}(\vec{d})^{-1} (\vec{d}_{obs} - \vec{d}_{ACTM}) \quad (3)$$

609 and posterior error covariance

610 
$$\mathbf{C}(\vec{s}) = \left( \mathbf{J}^T \mathbf{C}(\vec{d})^{-1} \mathbf{J} + \mathbf{C}(\vec{s}_0)^{-1} \right)^{-1}$$

611

612 where  $\vec{s}_0$  is the prior source for the 84 regions and 288 months in 1998-2021,  $\mathbf{C}(\vec{s}_0)$  is the prior source error  
 613 covariance matrix,  $\vec{d}_{obs}$  is the measurement data at 50 sites for 288 months, and  $\mathbf{C}(\vec{d})$  is the data error  
 614 covariance matrix.  $\vec{d}_{ACTM} (\approx \mathbf{J}\vec{s}_0)$  is forward model simulation time series using a priori fluxes, run continuously  
 615 for the whole period of analysis, and sampled at the time and locations of the individual measurement before  
 616 calculating monthly means.  $\mathbf{J}$  is the Jacobian matrix of sensitivities of observations with respect to  $\vec{s}$ , calculated  
 617 using simulations of unitary pulse sources for a month for the 84 basis regions, and sampled at the 50  
 618 measurement sites. The unitary pulses are simulated for 4 years and originated for each month of year 2011 for  
 619 all regions (84 regions  $\times$  12 months = 1008 tracers per year; one set of  $\mathbf{J}$ -matrix is reused for all years). We have  
 620 shown in Fig. S1 and associated text that use of annually repeating  $\mathbf{J}$  does not affect the inversion results  
 621 significantly as majority of the spatial and temporal flux variabilities are coming from the a priori, which are  
 622 simulated using interannually varying meteorology. The elements in  $\vec{s}$  are the optimised CO<sub>2</sub> fluxes (referred to  
 623 as a posteriori or predicted flux) from 84 regions at monthly time intervals. The off-diagonal elements of  $\mathbf{C}(\vec{s}_0)$   
 624 are kept zero, assuming the a priori fluxes are uncorrelated to one another regions or time. The correction fluxes  
 625 ( $\vec{s} - \vec{s}_0$  in Eq. 3) is primarily determined by the term  $(\vec{d}_{ACTM} - \vec{d}_{obs})$ , scaled by the data/flux uncertainty.”

626

627 173: change "lands" to "land"

628 178: usually, you would give the cost function a symbol, like: "J = (D-Gs)T ... etc."

629 The equations are modified for cost function like symbols.

630

631 Note on equations: These need to be cleaned up a bit to conform with standard notation. Vectors should be  
 632 lower case and bold. Matrices should be upper case and bold. Change this both in the equations and text. At  
 633 the moment, you have the fluxes being put into a 2-degree matrix, S, whereas they are usually put into a 1-  
 634 degree vector, s. Why do you have it as a matrix? Are you putting the vectors for multiple inversion cases all  
 635 together into one big matrix and doing the inversion all together at the same time across all cases? (If so, the  
 636 equations given are not correct.) If not, the fluxes should be put in vectors s.

637

638 We follow the equations from Rayner et al. (2008) and Tarantola (2005). They are now written in the notations  
 639 you suggest. The vectors and matrix are shown in small letters with arrow on top and capital letters, respectively.

640

641 187-188: A word about how you order the monthly fluxes into vector s (not matrix S) would be useful: the 84  
 642 measurements for month 1, followed by the 84 for month 2, etc...?

643

644 The inversion code is made available on github, which was first developed by Peter Rayner, Rachel Law et al.  
645 at CSIRO, and later distributed through TransCom inversion activities by Kevin Gurney, Rachel Law et al. We  
646 have revised some of the codes and functionalities, e.g., we are using  $(d - d_{ACTM})$  as input the inversions instead  
647 of originally  $d$  and  $d_{ACTM}$  separately. The  $C_D$  and  $C_{S0}$  and other infrastructures are also changed vastly. Part of  
648 the code is given below for 's'

649

```
650     Kount2 = 0
651     do l=1,lreg1           ! for number of regions, 84 in this case
652         write(chl2,'(i2)') l
653         do m=1,mtot1       ! for months
654             do n=firstsrc,lastsrc ! for years: firstsrc = 1998, lastsrc=2021
655                 kount2 = kount2 + 1
656                 ntime = nfirst + (n-firstsrc)*mtot1 +m-1
657                 src(kount2) = stemp3(l,ntime,1)
658             enddo
659         enddo
660     enddo
```

661

662 191: Similarly, what you have at the moment as matrices  $D_{obs}$  and  $D_{ACTM}$  should actually be vectors  
663  $d_{obs}$  and  $d_{ACTM}$ , right?

664 183: change "prior source covariance matrix" to "prior source error covariance matrix"

665 184: change "data covariance matrix" to "data error covariance matrix"

666

667 All corrections are done

668

669 183-187: Some more detail needs to be given about how these Green's functions are created. Apparently, you  
670 are solving for monthly fluxes. Are you also averaging all the measurements together into blocks of one month,  
671 as well? Or are they treated at a finer temporal resolution? How far out in time are the Green's functions run?  
672 All 23 years, or across a shorter span? If truncated, how is the effect after that handled? Are the fluxes inside  
673 each emission region divided by the flux uncertainty before being run through the transport model (so that the  
674 spatial distribution of the uncertainty inside the region is captured)? Or after the fact (i.e. uncertainty for the  
675 region as a whole)?

676

677 Replied above for the comment "169, Section 2.4:" The revised texts clarified these issues.

678

679 193: usually one uses the term "model data error" or "model data mismatch" to indicate that much of the error  
680 here is due to the model itself being unable to represent the data, as distinguished from a pure measurement  
681 error. That is not captured by your term "measurement data uncertainty".

682

683 Thank you for this suggestion. We have changed this to "model data uncertainty" here and all places in the  
684 manuscript.

685

686 Table 2 caption, line 2: change "Every PFU and MDU cases are" to "Each PFU and MDU combination case is"

687

688 Corrections are made

689

690 206-207: if you are multiplying by 3 and 4 in place of 2, shouldn't the ranges then become 0.3-3.0 and 0.4-4.0  
691 PgC/yr? That is not what you give at the moment. Why do you change the lower bounds?

692

693 We stated the "maximum allowed" values. However, we agree with you that it is better to give the range, as  
694 given in the Table 2 already. Revised accordingly.

695

696 211: add a comma before "are used"

697 215: reword to "added these to an"

698

699 Corrected.

700 Figure 2: what does the subscript "pred" indicate? Are these the a posteriori results? Maybe something like  
701 "post" would be better...

702

703 233-234: Again, "posterior" or "a posteriori" would be more easy to understand in this context than "predicted",  
704 which could just as easily be thought to indicate the prior.

705

706 We had used "pred" for predicted flux. Following your suggestion all is changed to "post". This is now clarified  
707 in the Figure 2 caption. Thank you

708

709 In general, "FUR" is not a great statistic, since it depends heavily on the prior uncertainty, which can be made  
710 arbitrarily large and not change the final uncertainty much, at least in cases where most of the information is  
711 coming from the data rather than the prior.

712

713 Yes, we tend to agree with you, but we haven't been able to come up with anything different. So, we continue  
714 to use FUR.

715

716 201: Here you say that the PFU for the oceans in the control case is 1.0 PgC/yr, the same as it is in the fourth  
717 case, gpp\_v4. However, in the left column of Figure 3, they appear to be different colors. Was the PFU for the  
718 oceans in the control case not 1.0 PgC/yr?

719

720 Apologies for this mistake. The PFU for the oceans in the control case is 0.75 PgC/yr. Text and Table 2 revised.

721

722 240: not the South Pacific -- a 1-5% reduction in uncertainty is not "good", I think.

723

724 We have removed South Pacific now. However, we think any measurable FUR change is a positive sign.

725

726 242: after "Northern", change "Africa. The Tropical" to "'Africa, and The Tropical"

727 244: add "on the" before "regional fluxes"? Otherwise, the meaning is not clear, so please clarify

728 249: reword "into 1o x 1o spatial resolutions" to "to the 1o x 1o spatial resolution"

729

730 All of the above corrections are made in the revised manuscript.

731

732 253-254: You assert that the ensemble mean of the 16 different cases is the "best estimate", but how do you  
733 really know that this is the case? Maybe one of the looser prior cases is the best, because it allows the estimate  
734 to go closer to what the data indicate. Or maybe one of the tighter prior cases is the best because it damps down  
735 the dipoles caused by the generally underconstrained nature of these inversions. What criterion do you use to  
736 make this assertion?

737

738 We have now stated our criterion as (which is later shown in Fig. 5) :

739 The best estimate criterion is based on closest agreement of the global total (FFC emissions + land and ocean  
740 sinks) fluxes with the global mean growth rate (section 3.2).

741

742 There is no other observable quantity to validate inversion fluxes in a strict sense, and also used in GCP CO<sub>2</sub>  
743 budgeting process.

744

745 256-257: You should indicate what portion of the total uncertainty this ensemble-based measure pertains to.  
746 In particular, since you use a matrix inversion-based inverse method, you can presumably get a full-rank  
747 covariance matrix pertaining to the flux estimate (for each ensemble member). The uncertainties derived from  
748 this covariance would give you that portion of the total flux uncertainty due to the uncertainty in the  
749 measurements (the random error part) plus the uncertainty in the prior fluxes. The spread across the ensemble  
750 quantifies other errors -- say here what you think those are.

751

752 Yes, we have the full covariance matrix, but the regional fluxes we are analysing here do not conform with the  
753 inversion model regions. However, we have checked the a posteriori flux uncertainty for the TransCom sized  
754 regions are well over 2 PgC/yr. It is also clear from FUR statistics that the uncertainty for 84 inverse model  
755 regions is not very large. Since we start with large a priori uncertainties (say, compared to TransCom Level 2  
756 inversions), our a posteriori uncertainties are large.

757

758 That's one of the reasons we have performed an ensemble of inversion to assess the physically meaningful (can  
759 be questioned) uncertainties for regional fluxes. We have added these sentences in the article for clarification.  
760 "The regional and global land/ocean flux uncertainties estimated from the 16 ensemble members cover those  
761 arise from priori flux distributions, PFU, MDU. The uncertainties due to data coverage and model transport  
762 errors are not assessed here."

763

764 260: reword "3-dimensional CO2 observations" to "3-dimensional CO2 mixing ratio fields"?

765 Because you don't have an observation at each point in the full 3-d field.

766

767 Corrected.

768

769 262: You need to give a reference to the source of this data. In the References, you have a Schuldt et al reference  
770 pointing to obspack\_co2\_1\_GLOBALVIEWplus\_v7.0\_2021-08-18. Does that pertain to this? Which did you  
771 use, v6.1 or v7.0? Please clarify.

772

773 Sorry, for missing the citation. Schuldt et al., 2021 is added for v6.1. The reference list is corrected accordingly.

774

775 271: "latitude intervals"?

776

777 279: Please indicate the total number of routine NOAA aircraft profile sites or time series you use. Table S4  
778 seems to indicate that more than just these three sites were used. Maybe point to this Table S4 here in the text.

779 308: subscript "CO2"

780

781 Corrections and additions are made. We use 16 routine NOAA aircraft profile sites.

782

783 309: What errors do you mean to include in the term "uncertainties in the predicted flux"? Just those due to  
784 random errors (since uncertainty usually pertains to those errors)? If you mean to say "errors" instead of  
785 "uncertainties", then wouldn't some of those errors already be due to transport errors?

786

787 Yes, some errors would come from transport error, but as we have mentioned in the previous sentence the  
788 MIROC4-ACTM transport is validated for inter-hemispheric transport and transport of species in the upper

789 troposphere and lower stratosphere using multiple tracers. Thus, we believe the biases and RMSEs will decipher  
790 mostly about flux errors.

791

792 We have revised this sentence as “Model transport is one of the sources leading to uncertainties in the predicted  
793 fluxes, but the simulations of SF<sub>6</sub> and age of air confirm the low transport error in MIROC4-ACTM (Bisht et  
794 al., 2021; Patra et al., 2018). Hence, the magnitude of biases and RMSE indicates predominantly the accuracy  
795 of the predicted fluxes (the errors due to model transport and measurement network are not explored in this  
796 study).”

797

798 321: "though" -- is this the word you want? The sentence, as it is written now, is unclear. Are you trying to say  
799 that the posterior results make reasonable corrections regardless of which prior they start from? Please reword  
800 so that this is clearer.

801

802 The sentence is revised as “The a posteriori results make reasonable corrections regardless of which a priori  
803 fluxes they start from, e.g., the gc3t case with net-zero annual flux or the ‘gvjf’ case with strong sink.”

804

805 333: "However, the degree of freedom of our inversions is similar to the gridded inversions when spatial flux  
806 correlations of greater than 1000 km are assumed (Peylin et al., 2013)."

807

808 A gridded inversion with a correlation length of ~1000 km would have, say, 36x15=480 independent regions  
809 being estimated, more or less, compared to 84 in your case. This is not really comparable. I would agree,  
810 maybe, if you said ~2000 km. But what gridded inversions are using ~2000 km resolution? Please reword this  
811 to make your meaning clearer.

812

813 Revised as “The degree of freedom of our inversions is a few times smaller than the gridded inversions when  
814 spatial flux correlations of 1000-2000 km are assumed”.

815

816 340: "two combinations": It appears that all 16 combinations of priors/prior uncertainties are shown in Figure  
817 5 -- who do you say only two?

818

819 Revised for better clarity as

820 “Figure 5 shows the trends and interannual variability in the global fossil fuel (FF) emissions (used as input for  
821 the inverse model), land-biosphere, ocean, and annual atmospheric CO<sub>2</sub> growth rate for 16 inversion ensemble  
822 members based on two combinations of land-biosphere and ocean prior fluxes (VISIT and CASA for land-  
823 atmosphere, and TT09 and JMA for sea-air) and eight combinations of prior flux/data uncertainties (PFU and  
824 MDU)”

825



826 349-350: If you say that the uncertainties for the global land and ocean fluxes are 1.4 and 0.7 ppm, respectively,  
827 it makes me wonder whether you have accounted for the correlations (the off-diagonal terms) in the a posteriori  
828 covariance matrix properly in computing the uncertainties for those two regions. Other global inversions of in  
829 situ CO<sub>2</sub> data have found the uncertainty for the global land flux to be down around 0.5 PgC/yr. Do you  
830 consider the off-diagonal terms in the a posteriori covariance matrix when calculating these uncertainty values  
831 on the global land and ocean regions?

832

833 Yes, the off-diagonal terms are included. Note that our a priori flux uncertainties are much greater than those  
834 used in TransCom studies for example. We use flat 2 PgC/yr for land and 0.75 PgC/yr for oceans in the control  
835 case.

836

837 Figure 5 caption, line 150: "brackets"

838

839 Corrected.

840

841 Figure 5 caption, line 150: "Numbers in the bracket in the legend are budget imbalance between inversions and  
842 observed CO<sub>2</sub> growth rate." The description given here and in the text (lines 360-361) does not make it clear  
843 how these values were calculated. Do they measure the difference in `_trend_` across the twenty years? (I.e.,  
844 the difference in the beginning and ending values, divided by the number of years.) Or is it not the trend but  
845 rather the absolute offset that you are calculating? Or is it the RMS difference between individual annual  
846 values? Or monthly values? What are the units? Please do a better job describing this quantity in both places.

847

848 Mean of absolute offsets are given in PgC yr<sup>-1</sup>. We have clarified it at both places as per your suggestion

849

850 373: "-induced changes": this doesn't work with a long parenthetical expression squeeze in between the original  
851 word ("La Nina") and this phrase. Please put the information inside the parentheses elsewhere (maybe in the  
852 caption to Fig. 5).

853

854 We have revised as per your suggestion. Parenthetical expression moved to Figure caption. Thank you.

855

856 377: "generally showing an increased ocean sink during strong El Niño events (e.g., during 2015-2016)".  
857 But your Figure 5c does not show this: it has an increased ocean sink at the end of 2016/beginning of 2017 and  
858 a reduced ocean sink in 2015. The 2015/2016 El Niño began in mid-2015 (or earlier) and was well over by  
859 mid-2016. The increased uptake, due to the capping of the thermocline in the East Pacific that occurs during  
860 the El Niño, should therefore be seen a full year before it is seen in Figure 5c. Please remove this or do a better  
861 job explaining what you mean.

862

863 We have deleted this part of the sentence. Such inconsistency arises from the lack of sufficient measurements  
864 in the Tropical Eastern Pacific region.

865

866 382: reword "caused by increasing pCO<sub>2</sub> between the" to "caused by the increasing CO<sub>2</sub> difference between  
867 the"

868

869 Done.

870

871 384: "and the gradual sink increase...": Wait, if you remove the strong increase in sink lasting up to 2012,  
872 possibly caused by the incorrect reporting of Chinese FFC use, then there is no increase in sink after that, but  
873 rather a decrease in sink (after 2012). Which effect do you want to argue for most -- the FFC effect or the CO<sub>2</sub>  
874 fertilization effect? (It does not seem that you can have it both ways...)

875

876 Practically both are happening here. The FFC error is affecting flux estimation for a short period of 2001-2009,  
877 while the CO<sub>2</sub> fertilisation is slow but lasting process. We have made the specific period of FFC effect clear in  
878 the manuscript.

879

880 Figure 5d: With your sign convention for land and ocean fluxes, the quantity plotted here should be labeled  
881 "FF + (land+ocean)" -- i.e. change the minus sign to a plus sign.

882

883 Done.

884

885 398-402: This is really worded poorly and makes it difficult to understand what point is trying to be made.  
886 Really you are first giving the values the VISIT prior has for certain regions, followed by what the final predicted  
887 values are. However, it reads as if you are first giving the difference between the VISIT and predicted values  
888 (actually, it is not clear at all what the values in parentheses refer to). Please reword it to say: here is what the  
889 VISIT prior says the values should be, then here is what the predicted value is, then say where the final uptake  
890 is more or less than the prior. I.e., reword it for clarity.

891

892 Thank you very much for suggestion. We have revised the sentences as "Significant differences are seen in  
893 between a priori VISIT fluxes and a posteriori fluxes over Russia, East Asia and Europe. The VIST prior suggest  
894 the mean values of land uptake -0.76, -0.55 and -0.54 PgC yr<sup>-1</sup>, respectively for Russia, East Asia and Europe;  
895 however the ensemble inversion suggest the ranges of fluxes from -0.33 to -0.37, -0.42 to -0.57 and 0.08 to -  
896 0.09 PgC yr<sup>-1</sup>, respectively. In general, the inversions suggest substantial uptakes ..."

897

898 406: "neighborhood"

899 408: "less certainly"

900 409: "groups"

901

902 Corrected.

903

904 411: since a sink of -0.18 PgC/yr could also be considered "mild", maybe change the wording here from "show  
905 a mild carbon sink" to "show almost no carbon sink"

906

907 Done.

908

909 412: Why do you mention that the VISIT prior has strong sinks over all three South American regions? Are  
910 you contrasting it to something? Not clear why you mention it.

911

912 Revised as "VISIT prior consists of strong sinks over all three South America regions, and for all the regions  
913 the inversions moderated the sinks and thus producing fluxes closer to the inversions using CASA prior even  
914 though the regions have no measurement sites"

915

916 418-419: It is not clear why you tie the trend towards increasing sink in East Asia to the trend in increasing FFC  
917 values there. If you are implying that the prior FFC numbers are overestimated there, please say that, to be  
918 clear.

919

920 Revised as "The predicted land carbon sink over East Asia tends to increase is tied to a rapid increase in FFC",  
921 and further explanations are given in the next sentences.

922

923 420-422: "Because the atmospheric data constrain the total net surface flux, the rapid increase in fossil fuel  
924 emissions is required to be compensated by increasing the natural land uptake of similar magnitude through  
925 inversion." This compensation is only required if the atmospheric CO<sub>2</sub> amount is not increasing to take up the  
926 fossil fuel added. There is no requirement for local land uptake in areas of increasing fossil fuel input, since the  
927 winds can blow the input around across the globe quickly. Please reword this to make your argument clearer.

928

929 Following your suggestions, we have revised this sentence as "Because the atmospheric data constrain the total  
930 net surface flux regionally when fluxes are constrained by observations, a biased high increase in fossil fuel  
931 emissions is required to be compensated by a biased high increase in the natural land uptake by inversion. If  
932 absolutely no constraints by observations, the compensation will occur in the regions where the biased FFC  
933 signals are transported by the prevailing winds."

934

935 428: "support"

936 430-431: reword "while the prior flux consisted no" to ", starting from a prior flux that has no"

937 435: change "due to" to "given by" or "caused by the assumed"?

938 437: add "in the" before "gvjf inversions"

939

940 Thank you very much for pointing out these corrections. All corrections are made.

941

942 437-442: In order for this discussion to be understood better by the reader, you should mention that the  
943 incomplete measurement constraint in the inversions permits "dipoles" of flux errors to appear between  
944 neighboring regions (compensating errors of opposite sign due to the inability of the measurements to  
945 completely localize the source or sink in the right place), and that that is what is likely being seen here.

946

947 Thank you. We have borrowed your words and added a sentence here "These features appear likely because of  
948 the incomplete measurement constraint in the inversions permits "dipoles" of flux errors to appear between the  
949 neighbouring regions (compensating errors of opposite sign due to the inability of the measurements to  
950 completely localise the source or sink in the right place)."

951

952 443: replace "two-fold" with "a two-fold higher"

953 444: replace "Inversion largely follows" with "The inversion results largely follow"

954 446: replace "as" with "is"

955 447: replace "of" with "off"

956 448: "is also known to have" -- what, "occurred"? Please reword so that this makes some sense.

957 448-449: replace "tighter constrain by" with "a tighter constraint due to the"

958 450: replace "; while, we have" with ", even though we have"

959 Figure 8 caption: it is unclear what "TDI calculation" refers to -- please spell out "TDI" and describe better  
960 what is meant by it here.

961

962 All corrections are made, and "TDI calculation" is replaced by "inversions" in Figure 8 caption.

963

964 462-465: This sentence needs to be reworded for clarity. It is only dimly clear what point is trying to be made,  
965 at the moment.

966

967 Revised and one sentence is added for clarity,

968 "The correlations were less than 0.3 between "gc3t" inversion and "gvjf" prior, which can be inferred as only  
969 some of the interannual variabilities were present in the gvjf prior, and the interannual flux variability for gvjf  
970 inversions are significantly different from gvjf prior. These results imply that the VISIT land ecosystem fluxes  
971 and GFEDv4s fire emissions inadequately represent CO<sub>2</sub> flux signals that are observed at the 50 measurement  
972 sites in our inversion."

973

974 474 and Table S3 caption: subscript "CO2"

975 Table S3: You need to give some more detail here on what ENSO index you are using when doing this  
976 correlation.

977

978 Corrected and ENSO index information given

979

980 470-471: "The CO2 flux anomalies in the tropical regions are strongly correlated with the ENSO index, while  
981 temperate and boreal regions are weakly correlated". This is an overly-generous characterization of the  
982 correlations you show in Table S3: there are only a couple regions that might at all be considered to have  
983 "strong" correlations with the ENSO index (Southeast Asia at +0.61, Western Pacific at -0.62), and this is only  
984 because that correlated variability was present in the prior at a slightly stronger level. Notably, the other set of  
985 priors did not give posterior estimates for these regions with a correlation stronger than 0.3. You are blithely  
986 twisting your narrative well beyond what the data justify.

987

988 Correlations are about 0.3 or greater for Brazil, Temp S America, Northern and Central Africa and Southeast  
989 Asia, as given in Table S3, for the gc3t inversion case which had no interannual variability in the prior flux,  
990 both for land and ocean. Also for these regions and gvjf inversion case, the correlation between MEI and  
991 posterior fluxes remained similar or slightly increased compared to MEI and prior fluxes.

992

993 We have now provided P-values as a significance test of the correlation coefficients in Table S3.

994

995 476: Russia is not one of the regions given in Table S3 -- maybe change to "North Asia"?

996

997 This was an overlook. Yes, North Asia – now changed to Russia

998

999 483: Figure 7 refers to ocean fluxes. Do you mean to point to Figure 6 or 8?

000

001 Yes, it should be Fig. 8 (or Fig. 6). Fig. 8 is now cited.

002

003 492: In your discussion of the large IAV seen in Oceania, you do not mention that this is all coming from the  
004 gvjf prior and not from the data. This is because the a priori flux uncertainty for that region is quite tight,  
005 according to Figure 3a (except for the control case -- why is the uncertainty in the control case so much higher  
006 there than for the other prior cases? Is this an error in Figure 3a?). Because the fluxes for the two different  
007 prior models (gc3t and gvjf) are so different, it would have been more reasonable to have used a looser prior for  
008 this region, reflecting the disagreement between the two actual prior timeseries that you used. I like your  
009 discussion of the variability in the GFED prior, but it is unfortunate that you did not leave the fluxes for this  
010 region loose enough to test whether this prior is in fact in agreement with the available CO2 data.

011

012 We actually have the inversion cases of `ctl_ux2_gvjf` & `ctl_ux4_gvjf`, which are clearly suggesting some  
013 differences from the prior by the inversions (Fig. 6o). But some part of the Australian landmass is weakly  
014 constrained by observations (Fig. 3). In general, our inversion suggests some consistency in the CO<sub>2</sub> flux IAV  
015 for `gc3t` and `gvjf` inversions ( $r=0.43$ ), but the flux variabilities are much weaker for `gc3t` compared to those for  
016 `gvjf` prior or predicted fluxes.

017

018 why is the uncertainty in the control case so much higher there than for the other prior cases? :

019 In the control case we used fixed 2 PgC/yr PFU for all land regions, but in the `gpp_v*` cases the PFU are  
020 proportional to GPP of the region, which is low for Australia due to the lack of dense biosphere.

021

022 We believe more targeted research is needed to answer all the important questions you have raised. Thus, we  
023 are not changing the discussions here, for not to be too speculative.

024

025 500: You seem to be contrasting the `gc3t` and `gvjf` priors here -- please add something like "The `gc3t`" at the  
026 beginning of the sentence to indicate that you are talking about that case first, before switching to talk about the  
027 `gvjf` case.

028

029 Thank you. Done

030

031 502-504: "The oceanographic observations indicate that sea surface temperature and pCO<sub>2</sub> in the equatorial  
032 warm pool areas (5°N–5°S, west of the dateline) are not sensitive to El Niño conditions (Takahashi et al.,  
033 2003)." If that is the case, how do you explain the "strong" correlation in the West Pacific in the `gvjf` case, both  
034 in the prior and final estimate? What about the JMA model is correlated with ENSO if not SST and pCO<sub>2</sub>?

035

036 We have added this discussion here:

037 "The oceanographic observations indicate that sea surface temperature and pCO<sub>2</sub> in the equatorial warm pool  
038 areas (5°N–5°S, west of the dateline) are not sensitive to El Niño conditions (Takahashi et al., 2003), but a  
039 strong correlation is found for the West Pacific region in the case of JMA ocean prior that is driven by pCO<sub>2</sub>  
040 measurements and sea-surface temperature. The `gc3t` inversions did not produce expected (negative) correlation  
041 for CO<sub>2</sub> fluxes and ENSO index for the both East and West Pacific regions, due to the lack of observational  
042 coverage. Patra et al. (2005a) showed that the global ocean flux variability is significantly underestimated or  
043 even produced opposite phase for strong El Niño of 1997/1998, if the Pacific Ocean Cruise data are not used in  
044 inversions."

045

046 521-522: reword this first sentence so it is clear that the CASA model is the one with the July peak.

047

048 We have revised the sentence now as “Seasonal cycle amplitude for CASA prior flux for land total is 33.6 PgC  
049 yr<sup>-1</sup>, and that for VISIT is weaker at 23.8 PgC yr<sup>-1</sup>, and the peak of the growing season (when the net flux is  
050 most negative) occurred in July for CASA that is one month after the VISIT (Fig. 9, top-left panel)”.

051

052 524: reword this to make it clear that it is the a posteriori, or predicted, estimates for the gc3t case that you are  
053 comparing to the prior.

054 527: It appears that you are still discussing the total land flux at this point, which is not shown in Fig 9a, but  
055 rather the figure to the left of that one -- please fix this reference here.

056

057 We have made several small corrections for clarity, based on these 2 comments.

058

059 534: change to "Northern land fluxes drive"

060 539: change "are" to "is"

061

062 Corrected.

063

064 539-542: You have described why the prior fluxes agree or disagree here, but not why the posterior fluxes do  
065 so. For the posterior fluxes, they do not converge well in the tropics mainly because of the general sparseness  
066 of data there, or rather data that constrain the fluxes there. Perhaps noting that, as well, would be useful.

067

068 We have added a sentence : “Posterior fluxes for the tropical regions also do not converge well mainly because  
069 of the general sparseness of CO<sub>2</sub> data (Patra et al., 2013)”

070

071 547: add "adjoining" before "neighborhoods" to indicate that it is observations in the surrounding area that are  
072 providing the constraint.

073 552: add "and" before "East Asia"

074 560: add a comma before "caused"

075

076 All corrections are made.

077

078 563: "It is not easy for us to explain the mechanism for the Northern Ocean to be a weaker sink in summer than  
079 in winter." One possibility is simply the reduced solubility of CO<sub>2</sub> in warmer waters leading to an outgassing  
080 of CO<sub>2</sub> then.

081

082 Thank you for the suggestion, we have further scrutinized the Yasunaka et al. paper and added  
083 “It is not easy to put forward a hypothesis for the weaker sink in summer than in winter of Northern Ocean,  
084 while we can speculate that the atmospheric CO<sub>2</sub> decrease in polar air exceeds compared to the decrease that

085 occur over the surface sea-water and reduced solubility of CO<sub>2</sub> in warmer water. Indeed, Yasunaka et al. (2018)  
086 have shown that the Greenland-Norwegian seas and Barents Sea are indeed acts as milder sink of CO<sub>2</sub> (flux = -  
087 4 to -5 mmol m<sup>-2</sup> day<sup>-1</sup>) during June-August compared to the October-March (flux = -10 to -15 mmol m<sup>-2</sup> day<sup>-1</sup>)  
088 <sup>1</sup>), and the Chukchi Sea and Arctic Ocean show strongest uptake in October. Thus, as whole the Northern Ocean  
089 of our study could act as the weakest sink in summer months.”

090

091 568: add a comma after "Overall"

092 Figure 10 caption, 2nd line: replace "Each inversion cases" with "The different inversion cases"

093 Table S4 caption: change "is" to "are"; Also you need to say how you calculate the differences that are being  
094 plotted: is it model-observation? Is it the average of the a posteriori fluxes for all 16 cases that make up the  
095 modeled value?

096

097 Corrections and clarifications are made.

098

099 590-593: It is not clear what distinction you are making between the 25 and 75 percent error bounds. Aren't  
100 these just the two sides of the mean (i.e. 25% on either side of the mean, given by the bounds of the boxes in  
101 Figure 10)? When talking about the 25% results, do you really mean the 5%/95% bounds (given by the  
102 whiskers)? Not clear as currently written...

103

104 We revised this text as “Flux estimates for all the land regions remain quite uncertain, as seen from the 5 to 95  
105 percentiles range of the 16-inversion ensemble (whiskers) at about 0.3 PgC yr<sup>-1</sup> for the land regions and typically  
106 less than 0.2 PgC yr<sup>-1</sup> for the ocean regions. The fluxes at 25 to 75 percentiles range show slightly reduced  
107 uncertainties – a large reduction is not seen compared to the 5 to 95 percentiles range because the two a priori  
108 models often formed two different sets of CO<sub>2</sub> flux values”

109

110 595: This lack of reduction for the larger regions makes me wonder again whether you have properly accounted  
111 for the off-diagonal terms in the a posteriori covariance matrix when grouping regions.

112

113 We have followed the TransCom formulation for this calculation. Usually, we have about 5 regions in one  
114 aggregated region. Here are the posteriori flux uncertainties for the TransCom regions (except that the  
115 Temperate Asia is broken in to South and East Asia):

116 Region name	Flux_Correction	Flux_Uncertainty
117 Boreal N. America	-0.16	2.13
118 Temperate North America	-0.96	2.79
119 Tropical America	0.43	3.20
120 South America	-0.01	3.18
121 Northern Africa	-0.09	3.22



122	Southern Africa	-0.07	2.78
123	Boreal Eurasia	-0.22	3.09
124	West Asia	-0.43	3.81
125	East Asia	-0.26	2.63
126	Tropical Asia	-0.13	3.32
127	Australia	-0.30	2.38
128	Europe	-0.04	3.00
129	North Pacific	-0.11	1.29
130	West Pacific	0.00	1.00
131	East Pacific	0.20	0.91
132	South Pacific	-0.09	1.08
133	Northern Oean	0.13	0.85
134	North Atlantic	-0.12	0.92
135	Tropical Atlantic	0.03	0.93
136	South Atlantic	-0.02	0.97
137	Southern Ocean	-0.06	0.83
138	Tropical Indian Ocean	-0.12	1.41
139	South Indian Ocean	0.03	0.84
140	total	-2.39	8.38
141	total-land	-2.26	8.20
142	total-ocean	-0.13	3.38

143

144 We have now revised the sentence as “each of the 15 land analysis regions have predicted flux uncertainties in  
145 range of 2.1 (Boreal North America) to 3.8 (West Asia) PgC yr<sup>-1</sup> for the control gc3t case, as the reduction from  
146 prior flux uncertainties were small by inversion for most region (Fig. 3)”

147

148 Sorry for not being precise in the submitted manuscript.

149

150 615: "hosts" and "and hence is"

151 624: it is not clear what you mean by "at a higher magnitude" -- please reword for clarity.

152 626: put the wiggle on the n in "El Nino"

153 633: "unanimously" doesn't seem to be used correctly here -- remove it?

154 636: subscript "CO<sub>2</sub>"

155 640: "is in the North Pacific,"

156 641: instead of "CO<sub>2</sub> uptake rate", say "change in CO<sub>2</sub> uptake", since it is not very clear that by "uptake rate"  
157 you mean the time derivative of uptake.

158 644: the Long et al reference is missing from the Reference list -- add it

159  
160 Thank you very much for these suggestions. All the corrections are made.

161  
162 646. This new section should presumably be numbered "6.", not "4.", since it follows "5.", and the Conclusion  
163 section later as "7.", not "5."

164  
165 All the sub-sections in the Results and Discussion section are numbered as 3.x for simplicity, and the  
166 Conclusions as '4'.

167  
168 649: You need to define how you came up with these three sets of fluxes: 'gc3t', 'gvjf', and 'ensm' – are they  
169 created from the average of the 8 gc3t and 8 gvjf ones, and the average of all 16? If so, say so.

170  
171 We have revised the text as “three sets of prescribed fluxes: “gc3t” (case: ctl\_ux4\_gc3t in Table 2), “gvjf” (case:  
172 ctl\_ux4\_gvjf), and “ensm” (average of all 16 inversions).”

173  
174 651, 653: "ATom"  
175 Fig 11 caption, line 1: "meridional"

176  
177 Thank you. Corrections are incorporated in the revised manuscript.

178  
179 Fig 11 caption: you should indicate which quantity is subtracted from which when computing the biases -- it is  
180 not clear from the figure.

181  
182 “model-observation bias” is now mentioned.

183  
184 664: "Most of the aircraft data over these latitude bands are available over the continental regions, and this  
185 comparison suggests a higher sink than the estimated sink by inversion."

186  
187 It is not clear whether the aircraft data that you refer to here are the ATom and HIPPO data that you were  
188 discussing in the previous sentence, or other data. Since the sign of the observation-model difference has  
189 changed, this implies that you are discussing some other set of data. Please clarify this. If the data is still the  
190 HIPPO and ATom data, then the two sentences seem to contradict each other. Please reword these sentences  
191 so that your meaning is clear. Also, in the final sentence in this paragraph, why do you say that the models  
192 seem to do a good job in terms of the mean CO2 level when in the previous two sentences you have just pointed  
193 out that they do not do a good job (i.e. they are biased), at least in the north?

194  
195 Sorry for the unclear discussions. The text is revised now as

196 “The NOAA aircraft observations show a high bias during boreal summer throughout the troposphere over the  
197 US and Canada, implying possible seasonally dependent errors in posterior fluxes over these latitude regions  
198 (Fig. S7). When the aircraft data is over the high latitude continental regions, model-observation comparison  
199 suggests a stronger surface CO<sub>2</sub> sink is estimated by inversion compared to what is suggested by vertical profile  
200 gradients. HIPPO for the month of July also show negative model-observation mismatches near the surface (Fig.  
201 S6). But the mismatches turn positive in the higher altitudes, above about 1 km, and thus the model and  
202 observations averaged over 0-2 km are in much closer agreements (Fig. 11c). Based on these comparisons, the  
203 simulations from the ensemble mean of 16 inversion cases (“ensm”) show lowest mean bias, in comparison  
204 with gc3t or gvjf inversions, and suggested to be most suitable flux estimation for quantifying the global land  
205 and ocean carbon sink on the timescale of annual mean and its decadal trend.”

206

207 673: "The inversions underestimate"

208

209 Done

210

211 693: It is not clear what the broken lines are meant to indicate in Fig 12d-f. Are these what you get using the  
212 prior fluxes, and the solid lines what you get using the predicted fluxes? Please reword this both in the text and  
213 in the caption to Fig 12, so that this is clear.

214

215 **Figure caption and text revised according to your suggestions.**

216

217 694-697: "In the case of predicted data, the inversion fits the observation well due to minimisation of prior  
218 model-observation differences, but when the simulations are run using predicted fluxes, the (small) systematic  
219 biases produce a (large) cumulative effect over the model integration period."

220

221 This is NOT a general feature of flux inversion models, but rather a peculiarity of your inversion setup. In most  
222 inversion models, when you do a forward run with the optimized fluxes, you get the same modeled  
223 measurements as the inversion would give (unless for some reason you choose to run the model at a different  
224 resolution than what was used in the inversion). What is it about your inversion setup that causes this not to be  
225 the case? One possibility that comes to mind is that you have not extended your Green's functions runs out in  
226 time long enough: how long do you run them for? How do you handle the influence of a Green's function after  
227 this (i.e. after the end of your run)? You must provide more discussion on why you get different modeled  
228 measurements from what you assume in the inversion when you run the optimized fluxes forward through the  
229 model.

230

231 It is now given clearly in the Inverse method (section 2.4) that the Green's functions are run for 4 years. We  
232 have checked that the pulse signals are homogeneously distribution at the end of 48 months, and we believe

233 further extension of the simulations are not needed. But it is something we should test in the future by running  
234 the Green's functions well beyond 4 years.

235

236 However, following suggestions from you and reviewer#1, we have deleted lines 692-720 from the submitted  
237 version of the manuscript. Also deleted are Supplementary Figure S10, and the final paragraph from the  
238 Conclusions. We hope these actions will get rid of much of the confusions, as mentioned here and in the  
239 comments below.

240

241 “..when you do a forward run with the optimized fluxes, you get the same modeled ...”

242

243 “You must provide more discussion on why you get different modeled measurements”

244

245 Fig 12 caption and legend: it is not clear what the dashed lines labeled 'gc3t' and 'gvjf' indicate -- are these the  
246 modeled measurements given by these two priors? Please say in the caption what they are. If they are the  
247 modeled measurements given by the priors, why do you not also plot these lines for the top panels?

248

249 699: "We speculate that MIROC4-ACTM produces stronger sinks in the high northern latitudes":

250

251 stronger than what? Please reword this to make the meaning clear.

252

253 697-707: "It is also interesting to note that the meridional gradients in biases for independent aircraft  
254 observations (Fig. 12a,b,c) and sites used in inversion (Fig. 12d,e,f) show opposite phases, i.e., most negative  
255 and most positive at 25oN, respectively. We speculate that MIROC4-ACTM produces stronger sinks in the high  
256 northern latitudes (negative model-observation bias at surface sites over 75oN or HIPPO/ATOM latitude-  
257 altitude plots in Fig. S5, S6), which can arise from the model's inability to simulate the sites over the land  
258 because of the coarse horizontal resolution. Thus, resulting in a weaker sink or a stronger source in the northern  
259 tropics and subtropical (25oN) regions, respectively. The tropical source is then transported to the mid-high  
260 latitudes, which is captured by the aircraft observations, as a positively biased concentration. This experience  
261 suggests a need for new forward model simulations using inversion fluxes, not the optimised atmospheric CO2  
262 fields during data assimilation, should be used for evaluating inversion fluxes with the help of independent  
263 observations."

264

265 This discussion is not clear and makes no sense to me. Why should 75 deg N be an important inflection point  
266 for the surface data (there being very few surface sites that far north, anyway)? If there is a stronger sink than  
267 there should be in the northern extratropics, then yes, there could be a balancing stronger source south of that.  
268 But how could the positive perturbation in atmospheric CO2 then jump over the negative perturbation to the  
269 north of it to then somehow cause the positive model-obs differences seen in the far north (Figure 12 and S5)?

270 And even if this were a plausible explanation, how does this relate to running the optimized fluxes back through  
271 the forward model? An alternate explanation would be too-weak mixing during the summer and too-strong  
272 mixing during the winter in the north, causing overestimation of the summer drawdown and underestimation of  
273 the winter accumulation of CO<sub>2</sub> in the PBL.

274  
275 710 and Figure S10: If the same transport model is being used for the forward run as was used in the inversion,  
276 and run at the same resolution, then why would you expect that it would give a different simulation of the 3-D  
277 CO<sub>2</sub> field than was obtained in the inversion? What is the underlying reason? (I can think of one possibility:  
278 that the Green's functions used in the inversion were not run out far enough in time, driving basis function time  
279 truncation errors in the inversion. Is this the reason?) Please do a better job describing why you think doing a  
280 final forward run would give different modeled CO<sub>2</sub> fields, if this is a perfect model situation and the same  
281 model is being used for the forward run as in the inversions.

282  
283 711-720: This whole discussion also makes no sense to me. For CO<sub>2</sub>, a model with weaker interhemispheric  
284 transport causes a stronger N/S gradient when forced with NH-dominant fossil fuel emissions. When compared  
285 to the weaker observed N/S CO<sub>2</sub> gradient, this then requires a stronger NH CO<sub>2</sub> sink than a model that gives a  
286 weaker N/S CO<sub>2</sub> gradient. It is not very complicated and "complex interactions" need not be invoked. I agree  
287 that one should not use the assimilated data as a test, but rather comparison against independent data. But you  
288 do compare against independent data here (HIPPO, ATom), so why do you need this whole paragraph in the  
289 first place. Please do a better job with your argument, so that the reader can understand your point.

290  
291 We believe the final two paragraphs are not clear and appearing to confuse even the expert readers. With that  
292 in mind we have decided to delete these two paragraphs, Supplementary Fig. 10, and the final paragraph in this  
293 revised manuscript. However, we still feel that the issues raised in these two paragraphs and Figure S10 are  
294 important, and will be followed up by dedicated studies in the future.

295  
296 Regarding the final paragraph before Conclusions (lines 709-720), it is nice that we have a general agreement  
297 on how the inversion estimated fluxes are to be tested, i.e., by comparison against independent data. As the  
298 reviewer has kindly pointed out we have already done both comparisons with independent flux results from  
299 RECCAP and aircraft observations to assess our inversion results, and this paragraph and Figure S10 are  
300 redundant.

301  
302 723: You should be more specific and say that the land and ocean absorb 53% of the FFC fluxes, not of the total  
303 anthropogenic fluxes, because if you add in deforestation (which is an anthropogenic flux), it is no longer 53%.

304  
305 This sentence is revised as "The terrestrial biosphere (2.58 PgC yr<sup>-1</sup>) and ocean (1.54 PgC yr<sup>-1</sup>) absorb about  
306 46% of the emissions due to fossil fuel and cement production (8.9 PgC yr<sup>-1</sup>) in the period 2001-2020."

307

308 730: add a comma before "and two"

309 734: replace "resultant" with "result"

310

311 Corrected.

312

313 735-736: "The spread between the ensemble members provides us a reasonable measure of the inversion  
314 estimated flux uncertainty but lacks the quantification of transport model uncertainty."

315

316 It seems to me that the spread in the ensemble results should quantify the variability due to only those things  
317 that are varied across the ensemble: prior fluxes, prior flux uncertainty, and characterization of the MDU. It  
318 should not be expected to capture the usual estimation uncertainty due to errors in the measurements and errors  
319 in the prior flux (why? because the spread across the ensemble only quantifies the effect of mis-characterizing  
320 or changing the assumed statistics for those quantities, but does not capture the uncertainty due to those errors  
321 themselves). Therefore, in addition to the errors due to transport, you should also add on these usual estimation  
322 uncertainties to get the total errors. This would be a good place to mention that additional error source.

323

324 This sentence is revised as "...but lacks in quantification of the roles of transport model uncertainty or the  
325 inherent errors in the measurements and the prior fluxes."

326

327 742: replace "extratropical" with "extratropical southern", since you are focusing only on the south not the north

328

329 Done

330

331 743: "The ensemble of inversions splits into a "near-neutral" group and a "strong-source" group based on the  
332 priors."

333

334 It is unclear what feature in the flux results you are referring to here, with this statement. Please say what flux  
335 feature you are discussing -- global total? global land total? global ocean total?

336

337 We have revised this as "The ensemble of inversions splits into a "near-neutral" group and a "strong-source/sink"  
338 group based on the priors for the tropical and extratropical southern land regions."

339

340 750 remove the comma before "in less agreement"

341 752: "ATom"

342 766: what do you mean by "unanimously"? That it is true across all 16 cases?

343 772: "North Pacific"

344

345 Thank you for these suggesting these corrections. All of the above corrections are made in the revised  
346 manuscript.

347

348 772: What do you mean by "the most considerable CO<sub>2</sub> uptake"? The uptake in the Southern Ocean that you  
349 discuss here is not as large as the uptake in the land regions you just mentioned. Do you mean "the most  
350 considerable CO<sub>2</sub> uptake in the oceans"?

351

352 Revised as "North Pacific with a mean flux of  $-0.55 \pm 0.05$  PgC yr<sup>-1</sup>, and also considerable CO<sub>2</sub> uptake is  
353 estimated for Southern Ocean, where CO<sub>2</sub> uptake increased from  $-0.12 \pm 0.07$  PgC yr<sup>-1</sup> in 2001-2009 to -  
354  $0.33 \pm 0.06$  PgC yr<sup>-1</sup> in 2010-2019"

355

356 778-779: "There is no doubt that this set of results is unique because they close the year-to-year budget of  
357 decadal CO<sub>2</sub> changes in the atmosphere."

358

359 Almost all inversions close the year-to-year budget in decadal CO<sub>2</sub> change, due to the strong observability of  
360 the fossil fuel input minus atmospheric increase. Given that, why is your set of results unique? I have the little  
361 doubt that it is not. Please reword to make your point clearer.

362

363 779-780: "The bottom-up inventory or other modelling system still has limitations in closing year-to-year  
364 budgets."

365

366 You have used two sets of priors here that make no attempt to satisfy the long-term CO<sub>2</sub> trend in the atmosphere  
367 by trying to model an appropriate global land biospheric uptake. That does not point to a limitation in the  
368 modelling systems but rather a deliberate choice that you have made in the work you present here.

369

370 We have deleted the final paragraph of Conclusions in the revised manuscript, following these comments from  
371 you and Reviewer#1

372