

1 **The Impact of Increasing Stratospheric Radiative Damping on the QBO Period**

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8

9 **Abstract.** Stratospheric radiative damping increases as atmospheric carbon dioxide concentration rises.

10 We use the one-dimensional mechanistic models of the QBO to conduct sensitivity experiments and

11 find that the simulated QBO period shortens due to the enhancing of radiative damping in the

12 stratosphere. This result suggests that increasing stratospheric radiative damping due to rising CO<sub>2</sub> may

13 play a role in determining the QBO period in a warming climate along with wave momentum flux

14 entering the stratosphere and tropical vertical residual velocity, both of which also respond to

15 increasing CO<sub>2</sub>.

16

17 **1. Introduction**

18 The quasi-biennial oscillation (QBO) dominates the variability of the equatorial middle and lower

19 stratosphere and is characterized by a downward propagating zonal wind regime that regularly changes

20 from westerlies to easterlies. The QBO period ranges from 22 to 34 months with its average being

21 slightly longer than 28 months. The QBO not only manifests itself in the equatorial zonal winds, but also

22 leaves an imprint on the temperature in both the tropics and extratropics (Baldwin et al., 2001 and

23 references therein).

24 The QBO has far-reaching implications for global weather and climate systems. First of all, the QBO  
25 exerts a marked influence on the distribution and transport of various chemical constituents such as  
26 ozone (O<sub>3</sub>) (e.g., Hasebe, 1994), water vapor (H<sub>2</sub>O) (e.g., Kawatani et al., 2014), methane (CH<sub>4</sub>), nitrous  
27 oxide (N<sub>2</sub>O), hydrogen fluoride (HF), hydrochloric acid (HCl), odd nitrogen species (NO<sub>y</sub>) (e.g.,  
28 Zawodny and McCormick, 1991), and volcanic aerosol (Trepte and Hitchman, 1992). Secondly, it is  
29 well appreciated that the QBO influences the extratropical circulation in the winter stratosphere, which  
30 is commonly known as the Holton–Tan effect (Holton and Tan, 1980; Labitzke, 1982). It has been noted  
31 that the effect of the QBO on the extratropical winter stratosphere impacts the severity of stratospheric  
32 ozone depletion (e.g., Lait et al., 1989). Furthermore, taking account of the QBO improves the simulation  
33 and predictability of the extratropical troposphere (e.g., Marshall and Scaife, 2009). Finally, through its  
34 modulation of temperature and vertical wind shear in the vicinity of the tropical tropopause, the QBO  
35 influences tropical moist convection (Collimore et al., 2003; Liess and Geller, 2012), the El Niño-  
36 Southern Oscillation (ENSO) (Gray et al., 1992; Huang et al., 2012; Hansen et al. 2016), the Hadley  
37 circulation (Hitchman and Huesmann, 2009), the tropospheric subtropical jet (Garfinkel and Hartmann,  
38 2011a, 2011b), the boreal summer monsoon (Giorgetta et al., 1999), and the Madden-Julian Oscillation  
39 (Yoo and Son, 2016). Intriguingly, the QBO is also reported to influence the activities of tropical  
40 cyclones (Gray et al., 1984; Ho et al., 2009), albeit this issue is still unsettled (Camargo and Sobel, 2010)  
41 and needs further study.

42 Efforts to understand and simulate the QBO have been ongoing ever since its discovery by Ebdon  
43 (1960) and Reed et al. (1961). Lindzen and Holton (1968) and Holton and Lindzen (1972) developed  
44 the classical theory of the QBO. Namely, as waves propagate upward, they are attenuated by thermal  
45 damping, encounter critical levels, and accelerate and decelerate the mean flow, providing momentum  
46 sources for both the westerly and easterly phases of the QBO.

47 Holton and Lindzen's (1972) model (hereafter referred to as HL model) was further simplified by  
48 Plumb (1977), the elegance of which made it a standard paradigm for the QBO. In Plumb's (1977)  
49 Boussinesq formulation, the QBO period is inversely dependent upon both the momentum flux and  
50 thermal dissipation rate. Hamilton (1981) further highlighted the role of the radiative damping rate on  
51 both the realistic vertical structure and the realistic period of the QBO.

91 By adopting higher vertical resolutions and incorporating various gravity wave parameterization  
92 schemes, many state-of-the-art climate models have shown the capability to self-consistently simulate  
93 the QBO (Scaife et al., 2000; Giorgetta et al., 2002, 2006; Rind et al., 2014, 2020; Geller et al., 2016a;  
94 Richter et al., 2020a, 2020b). Given the important implications of the QBO for the global climate system,  
95 it is natural to ask how the QBO will change in a warming climate.

96 Giorgetta and Doege (2005) showed a shortening of the QBO period in their doubled CO<sub>2</sub>  
97 experiments. They reasoned that both the weakening of the tropical upwelling and the prescribed  
98 increase of gravity wave sources lead to the reduction of the QBO period in a warming climate. However,  
99 most climate models project a strengthening rather than weakening of tropical upwelling in a warmer  
100 climate (Butchart et al., 2006; Butchart 2014; Li et al., 2008). Employing a model without any  
101 parametrized non-orographic gravity waves, Kawatani et al. (2011) demonstrated that the intensifying  
102 tropical upwelling in a warming climate dominates the counteracting effect of enhanced wave fluxes and  
103 consequently projected a lengthening of the QBO period. Using fixed sources of parametrized gravity  
104 waves, Watanabe and Kawatani (2012) also projected an elongation of the QBO period in a warming  
105 climate and ascribed it to the stronger tropical upwelling. Analyzing four Coupled Model  
106 Intercomparison Project phase 5 (CMIP5) models that could simulate a reasonable QBO, Kawatani and  
107 Hamilton (2013) found that the projected trends of the QBO period were inconsistent in sign. They  
108 further investigated the 60-year operational balloon-borne radiosonde observations provided by the Free

109 Berlin University and detected no significant trend in the QBO period. Richter et al. (2020b) investigated  
110 the response of the QBO to doubled and quadrupled CO<sub>2</sub> climates among eleven models that participated  
111 in Phase 1 of the Stratospheric-tropospheric Processes And their Role in Climate QBO-initiative (QBOi;  
112 Butchart et al., 2018), and found no consensus on how the QBO period would respond to a changing  
113 climate. Recently, Butchart et al. (2020) evaluated ten Coupled Model Intercomparison Project phase 6  
114 (CMIP6) models with realistic QBO in two Shared Socioeconomic Pathways (SSPs, Gidden et al., 2019)  
115 scenario simulations and surprisingly found that the QBO period shortens in seven of those ten models  
116 in both in both SSP3-7.0 and SSP5-8.5 scenarios although only two and three models show a significant  
117 shortening trend in the respective scenarios.

118 It is challenging to ascertain the trend of the QBO period in a warming climate. On one hand, a  
119 speeding-up of the Brewer-Dobson circulation in a warming climate leads to a lengthening of the QBO  
120 period in most climate models. On the other hand, there is a robust increase in the vertical component of  
121 the EP flux for both eastward and westward propagating waves (Richter et al., 2020b; Butchart et al.,  
122 2020), indicating that the QBO period shortens due to the enhanced wave driving in a warming climate.  
123 The competing effects between enhanced wave driving and a faster Brewer-Dobson circulation suggests  
124 that trends in the QBO period are likely to be small and difficult to detect due to the large cycle-to-cycle  
125 variability that is reproduced by climate models (Butchart et al., 2020). In addition, uncertainty in the  
126 representation of the parameterized gravity waves make it more elusive to detect the trend of the QBO  
127 period in a warming climate (Schirber et al., 2015; Richter et al., 2020b).

128 Given the fact that the QBO period is influenced by the radiative damping (Plumb 1977; Hamilton  
129 1981), a natural question to ask is whether it could play a role on the trend of the QBO in a warming  
130 climate. Fels (1985) estimated that the radiative damping time under a doubling of CO<sub>2</sub> would decrease

131 by about 23%. His estimate implies a shortening of the QBO period as the radiative damping rate  
132 increases.

133 It is well-known that enhanced wave fluxes entering the stratosphere and stronger tropical upwelling  
134 individually play a dominant role in determining the trends in the QBO period in a warming climate.  
135 Does the competing effect between them leave some room for increasing stratospheric radiative damping  
136 to exert an influence on the QBO period? In this paper, we use the HL model to isolate the effect of  
137 radiative damping on the QBO period by assuming that the momentum flux entering the stratosphere  
138 doesn't change in our experiments. Observational and modeling studies (Andrews et al., 1987; Kawatani  
139 et al., 2009, 2010, 2011; Richter et al., 2020b; Holt et al., 2020) showed that the wave forcing spectrum  
140 is similar to a discrete two-wave spectrum rather than red-noise or white-noise, all of which are  
141 illustrated in Saravanan (1990). Accordingly, the QBO is indeed sensitive to stratospheric radiative  
142 damping, and the HL model is suitable for us to conduct the sensitivity analysis.

143 The remainder of this paper is organized as follows. Section 2 investigates the sensitivity of the QBO  
144 period to the radiative damping using HL's original model. Section 3 explores the sensitivity of the QBO  
145 period to the radiative damping using a modified HL model where the semiannual forcing is removed.  
146 Discussion and conclusions are presented in Sections 4 and 5 respectively.

147

## 148 **2. Sensitivity of the QBO period to enhanced stratospheric radiative damping in the original HL** 149 **model**

150 In the HL model the governing equation of mean flow emerges after the primitive momentum  
151 equation is meridionally averaged over some suitable latitudinal belt over the equator.

$$152 \quad \frac{\partial \bar{u}}{\partial t} = -\frac{1}{\rho_0} \frac{\partial}{\partial z} \left[ \sum_{i=0}^1 \overline{F_i} \right] + K_z \frac{\partial^2 \bar{u}}{\partial z^2} + G \quad (1)$$

153 where  $\bar{u}$  is mean zonal wind,  $\rho_0$  is mean density,  $\bar{F}_i$  is the meridionally averaged vertical Eliassen-Palm  
 154 flux associated with wave  $i$ , the index  $i$  refers to the individual waves,  $K_z$  is a vertical eddy diffusion  
 155 coefficient,  $t$  is time,  $z$  is altitude, and  $G$  is semiannual forcing identical to that specified by HL.

156 The  $\bar{F}_i$  is are evaluated with Lindzen's (1971) WKB formalism for equatorial waves in shear. When  
 157 only infrared cooling acts to damp the waves the formulae for  $\bar{F}_i$  are

$$158 \quad \bar{F}_0(z) = A_0 \exp\left(-\int_{17km}^z \frac{\alpha N}{k(c - \bar{u})^2} dz\right) \quad (2)$$

159 for the Kelvin wave, and

$$160 \quad \bar{F}_1(z) = A_1 \exp\left[-\int_{17km}^z \frac{\alpha\beta N}{k^3(c - \bar{u})^3} \left(1 - \frac{k^2(\bar{u} - c)}{\beta}\right) dz\right] \quad (3)$$

161 for the mixed Rossby-gravity wave. As in HL, the wavenumber  $k$ , the phase speed  $c$ , and  $A_0$  are chosen  
 162 to be  $2\pi/(40,000 \text{ km})$ ,  $30 \text{ m s}^{-1}$ , and  $0.04 \text{ m}^2 \text{ s}^{-2} \rho_0(17 \text{ km})$ , respectively for the Kelvin wave while  
 163 they are equal to  $-2\pi/(10,000 \text{ km})$ ,  $-30 \text{ m s}^{-1}$ , and  $-0.04 \text{ m}^2 \text{ s}^{-2} \rho_0(17 \text{ km})$ , respectively for the  
 164 mixed Rossby-gravity wave. In Eq. (1),  $K_z = 0.3 \text{ m}^2 \text{ s}^{-1}$ , which is also the same as in HL. In addition,  
 165  $\beta = 2\Omega/a$ , where  $\Omega$  is earth's rotation rate, and  $a$  is earth's radius. HL's boundary conditions stipulated  
 166 that  $\bar{u} = 0$  at the lowest model level (17 km) and constrained  $\bar{u}$  to vary semiannually at the top level (35  
 167 km).

168 In our control run that is used to depict the present-day QBO all the model parameters are identical  
 169 to those used by HL in their original simulation. The Brunt-Väisälä frequency

$$170 \quad N = \sqrt{\frac{g}{T_0} \left( \frac{dT_0}{dz} + \frac{g}{c_p} \right)} \quad (4)$$

171 In Eq. (4),  $g$  is gravity,  $T_0$  is mean temperature, and  $c_p$  is specific heat of dry air at constant pressure.

172 HL set  $N$  in Eq. (4) to  $2.16 \times 10^{-2} \text{ s}^{-1}$  with a scale height  $H = 6 \text{ km}$ . In addition, the Newtonian

173 cooling profile in our control run, i.e.,  $\alpha(z)$  in Eqs. (2) and (3), is also identical to that in the original  
174 HL model and depicted in FIG. 1a as the black line. Namely,  $\alpha(z)$  in the control run increases from  
175  $(21 \text{ day})^{-1}$  at 17 km to  $(7 \text{ day})^{-1}$  at 30 km and is kept at  $(7 \text{ day})^{-1}$  between 30 km and 35 km. Fels  
176 (1985) explained why the magnitude of this radiative damping rate is suitable for simulating the QBO  
177 on the basis of the scale-dependent effect of radiative damping (Fels, 1982). Hamilton (1981)  
178 demonstrated that the proper choice of  $\alpha(z)$  is crucial in simulating a realistic vertical structure of the  
179 QBO.

180 Eq. (1) was integrated for 100 years using the forward-backward scheme (Matsuno, 1966). The  
181 vertical resolution was 250 m and identical to that in HL. The time step was 12 hr, i.e., one half of used  
182 in HL, because the 24-hr time step resulted in numerical instability in our integration.

183 FIG. 2a shows the time–height section of the monthly averaged mean zonal wind simulated over the  
184 first 20 years using the HL model. Both the QBO and the semiannual oscillation (SAO) are conspicuous.  
185 The fast Fourier transform (FFT) method is used to calculate the frequency power spectra. In order to  
186 more accurately derive the QBO period, the model was run for 100 years to increase the spectral  
187 resolution. Frequency–height sections of the power spectral densities (PSD) over zero to the Nyquist  
188 frequency, i.e., 0.5 cycle/month, depict two sharp lines (peaks) at  $\frac{1}{30}$  and  $\frac{1}{6}$  cycle/month, respectively  
189 (not shown). In order to better visualize the magnitudes of the PSD, we show two truncated frequency–  
190 height sections with FIG. 2b and FIG. 2c highlighting the QBO and the SAO respectively. FIG. 2b shows  
191 that the QBO dominates over the model domain. The peak frequency corresponds to the period of 30  
192 months. FIG. 2c shows the SAO dominates near the model top due to the fact a semiannual forcing was  
193 imposed in the altitudes from 28 to 35 km.

194 It is worth mentioning that the QBO period shown here is longer than 26.5 months reported in the HL  
195 paper (see their FIG. 1). Using the HL model parameters, the QBO period simulated by Plumb (1977)

196 was close to three years (refer to his FIG. 8a), which is longer than our simulated QBO period, i.e., 30.0  
 197 months. Although we could not explain why our simulated QBO period is longer than that simulated by  
 198 HL, we found that when the upper boundary condition is changed from  $\bar{u} = 14 \sin(\omega_a t)$  and  $\omega_a =$   
 199  $\frac{2\pi}{180} \text{ day}^{-1}$  used in the HL's original model (refer to their Eqs. (2)) to  $\frac{\partial \bar{u}}{\partial z} = 0$  used in Plumb (1977), the  
 200 simulated QBO period becomes 34.3 month (figure not shown). In other words, when we adopted the  
 201 stress-free upper boundary condition as in Plumb (1977), our simulated QBO period is comparable to  
 202 that simulated by him, which lends credence to our reconstruction of the HL model.

203 In order to rigorously quantify the relationship of the Newtonian cooling coefficient at any altitude  $z$   
 204 between the reference and doubled  $\text{CO}_2$ , we follow Dickinson (1973) in using a radiative transfer model  
 205 to calculate  $Q_1(T)$  for a reference temperature profile  $T(z)$  and  $Q_1(T + \delta)$  for  $T(z) + \delta$ , where a small  
 206 perturbation  $\delta T = 0.1 \text{ K}$  with  $T(z)$  being the 1976 U.S. standard atmosphere. Our radiative transfer  
 207 computations use the MODTRAN gas absorption database with  $0.1 \text{ cm}^{-1}$  spectral resolution (Jin et al.  
 208 2019; Berk et al. 2008). We then repeat the computations with the doubled  $\text{CO}_2$  to yield  $Q_2(T)$  and  
 209  $Q_2(T + \delta)$ . It follows that  $\frac{\alpha_2}{\alpha_1} = \frac{Q_2(T+\delta) - Q_2(T)}{Q_1(T+\delta) - Q_1(T)}$ , where  $\alpha_1(z)$  and  $\alpha_2(z)$  stand for the Newtonian cooling  
 210 coefficient at any altitude  $z$  for the reference and doubled  $\text{CO}_2$ , respectively. In FIG. 1b the black line  
 211 depicts the ratio for the broadband longwave radiation ( $5 \mu\text{m} - 100 \mu\text{m}$ ) and the red line delineates the  
 212 ratio for the  $\text{CO}_2$  absorption band ( $12 \mu\text{m} - 18 \mu\text{m}$ ). The ratio calculated over the broadband is  
 213 conspicuously smaller than that for the  $\text{CO}_2$  absorption band, because the changes in cooling rate from  
 214 the temperature perturbation are larger over a wider spectral band. It is worth mentioning that the ratios  
 215 calculated over the broadband in the middle stratosphere are close to 1.3 and comparable to what Fels  
 216 (1985) estimated, i.e., about 23% decrease of the radiative damping time under a doubling of  $\text{CO}_2$ .

217 Returning to the 1D HL model, we synthesize those findings by prescribing  $\alpha_2(z)$  in our  
 218 experimental runs for the doubled  $\text{CO}_2$  as follows: an increase of 30% between 30 and 35 km, no change



219 below 24 km, and linear interpolation between 24 and 30 km. The resulting increase of radiative damping  
220 rate from the control runs is depicted as the red line in FIG. 1a. This increase is reasonable based on our  
221 results shown in FIG. 1b.

222 FIG. 3a shows the time–height section of the monthly averaged mean zonal wind simulated over the  
223 first 20 years for the doubled CO<sub>2</sub> run, where the increased  $\alpha(z)$  depicted as the red line in FIG. 1a was  
224 employed while all other parameters are identical to those in the control run. Obviously, the QBO  
225 dominates below 28 km while the semiannual oscillation (SAO) dominates above 31 km. Like FIG. 2b  
226 and FIG. 2c, we only show two truncated frequency–height sections with FIG. 3b highlighting the QBO  
227 and FIG. 3c highlighting the SAO. FIG. 3b also shows that the QBO prevails over the model domain. The  
228 peak frequency corresponds to the period of 27.9 months. FIG. 3c shows the SAO dominates near the  
229 model top due to the same imposed semiannual forcing as that in the control run.

230 In summary, using the original HL model we found that the increased radiative damping due to the  
231 doubling of CO<sub>2</sub> shortens the QBO period by 7% (i.e., decreases from 30 months to 27.9 months).

232

### 233 **3. Sensitivity of the QBO period to enhanced stratospheric radiative damping in the modified HL** 234 **model without the semiannual forcing**

235 HL pointed out that the imposed semiannual oscillation was not essential for their QBO theory.  
236 Applying  $\frac{\partial \bar{u}}{\partial z} = 0$  as the upper boundary condition, Plumb (1977) showed a simulated QBO without  
237 resorting to the semiannual momentum source (refer to his FIG. 8b). In the following control run, all  
238 parameters are identical to those used in the previous control run in Section 2 except that  $G$  in Eq. (1) is  
239 set to zero with  $\frac{\partial \bar{u}}{\partial z}$  also being set to zero at  $z = 35$  km. Hereafter we refer to it as the Plumb model<sup>1</sup>. FIG.

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<sup>1</sup> Strictly speaking, it is the HL model modified by Plumb (1977). In this paper, we don't use his eponymous model, i.e., the simplest possible model of the QBO, where Boussinesq fluids with uniform mean density were employed, because the HL model and its variant are considerably more realistic.

240 4a shows the time–height section of the monthly averaged mean zonal wind simulated over the first 20  
241 years using the Plumb model. As expected, the QBO emerges without any trace of SAO since  $G = 0$  in  
242 Eq. (1). FIG. 4b shows that the QBO dominates over the whole model domain. The peak frequency  
243 corresponds to the period of 37.5 months, which is comparable to that simulated by Plumb (1977) shown  
244 in his FIG. 8b. Apparently, the QBO period from the Plumb model, i.e., 37.5 months shown in FIG. 4b,  
245 is longer than that from the HL model, i.e., 30.0 months shown in FIG. 2b. This is partly because the  
246 additional forcing  $G$  in Eq. (1) was removed in the Plumb model.

247 In the following experimental run, all parameters are identical to those used in the previous  
248 experimental run in Section 2 except that  $G$  in Eq. (1) is set to zero with  $\frac{\partial \bar{u}}{\partial z}$  also being set to zero at  $z =$   
249 35 km. In other words, the following experimental run using the Plumb model employed the same  
250 parameters as the afore-mentioned control run using the Plumb model except that the increased  $\alpha(z)$   
251 shown as the red line in FIG. 1a was used in the following experimental run while  $\alpha(z)$  shown as the  
252 black line in FIG. 1a was used in the above control run. FIG. 5a shows the time–height section of the  
253 monthly averaged mean zonal wind simulated over the first 20 years for the doubled CO<sub>2</sub> run. It is natural  
254 that only the QBO emerges. A comparison of FIG. 4a and FIG. 5a shows that the QBO period shortens  
255 when the infrared damping increases in response to the doubled CO<sub>2</sub>. FIG. 5b shows that the QBO  
256 dominates over the whole model domain. The peak frequency corresponds to the period of 31.6 months.

257 Using the Plumb model, we found that the increased radiative damping due to the doubling of CO<sub>2</sub>  
258 shortens the QBO period by 15.7% (i.e., decreases from 37.5 months to 31.6 months).

259

#### 260 4. Discussion

261 Dunkerton (1997) showed that in the presence of tropical upwelling it was gravity waves rather than  
262 large-scale Kelvin and mixed Rossby-gravity waves that contributed the bulk of QBO forcing.

263 Consequently, Geller et al. (2016a, 2016b) pointed out that enough gravity wave momentum flux is  
264 required to model the QBO in a self-consistent manner in climate models and that the magnitude of the  
265 subgrid-scale gravity wave momentum flux plays a crucial role in determining the QBO period. Since  
266 there is no tropical upwelling in either the HL model or the Plumb model, it is natural that planetary-  
267 scale Kelvin and mixed Rossby-gravity waves largely determine the QBO periods shown in Sections 2  
268 and 3 due to the fact that the specified  $G$  is significantly weaker than that in the terrestrial stratosphere.  
269 We conducted another sensitivity test where all parameters are identical to those in the HL model except  
270 that  $G$  in both the control and experimental runs is twice as large as that used by HL. As the radiative  
271 damping profile changes from the black line to the red line above 24 km shown in FIG. 1a, our simulated  
272 QBO period decreases from 28.6 months to 27.3 months (figures not shown). This smaller percentage  
273 decrease of 4.5% is not unexpected because  $G$  is not sensitive to the radiative damping at all and the  
274 greater specified  $G$  reduces the fraction of the total wave forcing arising from the planetary waves.

275 We further conducted two sensitivity tests where all parameters are identical to those in the HL model  
276 except that  $G$  in the first test is half as large as that used by HL and is equal to zero in the second test.  
277 Surprisingly, as the radiative damping profile changes from the black line to the red line above 24 km  
278 shown in FIG. 1a, our simulated QBO periods decreases from 30.0 months to 28.6 months both for  $G$   
279 being decreased by 50% and for  $G = 0$  (figures not shown). This 4.7% decrease in the QBO period is  
280 smaller than the 7% reduction obtained from the sensitivity test presented in Section 2 when  $G$  is the  
281 same as that used by HL. It is surprising because the model atmosphere is expected to be more sensitive  
282 to the changes in the radiative damping as  $G$  becomes smaller and smaller. Note that when our control  
283 runs adopt the black radiative damping profile shown in FIG. 1a the simulated QBO periods are not  
284 sensitive to the imposed semiannual forcing provided that  $G$  does not exceed the values employed by  
285 HL. Similarly, when our experimental runs adopt the red radiative damping profile above 24 km shown

286 in FIG. 1a the simulated QBO periods are also not sensitive to the imposed semiannual forcing provided  
287 that  $G$  does not exceed 50% of the values adopted in HL. The question naturally arises: what is  
288 responsible for this unexpected behavior?

289 In Section 2, the simulated QBO periods are equal to 30 and 34.3 months when we adopted the no-  
290 slip and stress-free upper boundary condition respectively with all other parameters being identical to  
291 those used by HL. The results implicate the upper boundary conditions in the inconsistency. Plumb (1977)  
292 pointed out that the upper boundary in HL was undesirably low and implied that raising the lid to an  
293 additional 50% would be adequate for the robustness in his model. Here, we carry out a series of  
294 sensitivity tests by raising the model lid gradually from 35 km to 55 km with the one-kilometer increment.  
295 we will demonstrate how the behavior of the HL model with  $G = 0$  converges with that of the Plumb  
296 model. The modified HL model, i.e., the HL model with  $G = 0$  is identical to the Plumb model except  
297 that the former has the no-slip upper boundary condition while the latter has the stress-free upper  
298 boundary condition. Both models share the same governing equation (5). Note that we set the radiative  
299 damping rate above the 35 km level to its value at the 35 km level shown in FIG. 1a.

300 For the radiative damping profile corresponding to the reference CO<sub>2</sub>, FIG. 6 shows that when the  
301 model lid is placed at the 35 km level the simulated QBO period of 30.0 months with the no-slip upper  
302 boundary condition (solid black line) is apparently shorter than that of 37.5 months with the stress-free  
303 upper boundary condition (dashed black line). FIG. 6 also shows that as the model lid is raised  
304 incrementally from the 35 km level to the 46 km level, the discrepancies between the simulated QBO  
305 periods due to the different upper boundary conditions decrease monotonically. No matter whether we  
306 adopt the no-slip or stress-free upper boundary condition, the simulated QBO period is 32.4 months for  
307 the reference radiative damping profile provided that the model top is at or above the 46 km level.

308 Similarly, for the radiative damping profile corresponding to the doubled CO<sub>2</sub>, FIG. 6 demonstrates  
309 that when the model lid is placed at the 35 km level the simulated QBO period of 28.6 months with the  
310 no-slip upper boundary condition (solid red line) is obviously shorter than that of 31.6 months with the  
311 stress-free upper boundary condition (dashed red line). FIG. 6 also exhibits that as the model lid is raised  
312 gradually from the 35 km level to the 40 km level, the discrepancies between the simulated QBO periods  
313 due to the different upper boundary conditions decrease monotonically. No matter whether we adopt the  
314 no-slip or stress-free upper boundary condition, the simulated QBO period for the enhanced infrared  
315 cooling due to the doubled CO<sub>2</sub> is 30.0 months provided that the model top is at or above the 40 km level.  
316 It is apparent that the required model top is lower when the radiative damping is augmented due to the  
317 doubling of CO<sub>2</sub> because the planetary waves dissipate more steeply with height in presence of the  
318 enhanced infrared cooling rates.

319 FIG. 6 suggests that when the model lid is sufficiently high the QBO period in response to the  
320 enhanced radiative damping due to the increasing CO<sub>2</sub> will decrease from 32.4 to 30.0 months. This  
321 7.4% decrease in the QBO period is independent of the upper boundary condition. Note that the relative  
322 uncertainty in the ratio  $\frac{\alpha_2}{\alpha_1}$  calculated over the broadband (refer to the black line shown in FIG. 1b) ranges  
323 from 5% to 10% in the lower stratosphere and from 10 to 15% in the middle and upper stratosphere.  
324 Thus, the relative uncertainty in the calculated ratio is 15% at a liberal estimate in the stratosphere. Using  
325 the HL model with its top at the 48 km level, we further conducted two experiments by adopting  $G = 0$   
326 in Eq. (1) and increasing the radiative damping corresponding to the doubled CO<sub>2</sub> between 30 km and  
327 48 km by  $30\% - 30\% * 15\% = 25.5\%$  and  $30\% + 30\% * 15\% = 34.5\%$  respectively relative to that  
328 in the control run. The simulated QBO periods are 30.3 and 29.7 months respectively. Therefore, when  
329 the model lid is sufficiently high the QBO period in response to the enhanced radiative damping due to  
330 the doubled CO<sub>2</sub> will decrease by approximately  $7.4\% \pm 0.9\%$ .

331 Jonsson et al. (2004) showed that the doubled CO<sub>2</sub> induces a substantial cooling throughout most of  
332 the middle atmosphere, which in turn increases the ozone mixing ratio by 15–20% in the upper  
333 stratosphere and by 10–15% in the lower mesosphere (refer to their Figure 6). Incorporating this increase  
334 into the ozone profile for the doubled CO<sub>2</sub>, we recalculated the ratio of  $\alpha_2$ , the Newtonian cooling  
335 coefficient for the doubled CO<sub>2</sub>, to  $\alpha_1$ , the Newtonian cooling coefficient for the reference CO<sub>2</sub>. Our  
336 calculated  $\alpha_2/\alpha_1$  is only slightly increased as compared with that shown FIG. 1b no matter whether the  
337 CO<sub>2</sub> absorption band is  $5\ \mu\text{m} - 100\ \mu\text{m}$  or  $12\ \mu\text{m} - 18\ \mu\text{m}$  (figure not shown). It is not unexpected  
338 because the infrared radiative cooling by ozone is significantly smaller than that by CO<sub>2</sub> (refer to Fig. 1  
339 in Dickinson 1973) and, as a result, the 15–20% increases in the ozone mixing ratio will not make a  
340 noticeable difference. Since the monthly and zonal mean 2-D ozone concentrations are specified in about  
341 80% of CMIP5 models (Cionni et al., 2011) and the monthly mean 3-D ozone data are employed in  
342 many CMIP6 models (Keeble et al., 2020), it is expected that the change in the radiative damping due  
343 to the increase in ozone in response to the doubled CO<sub>2</sub> only marginally impacts the QBO periods in  
344 those models that do not include an interactive chemistry. However, the 15–20% increases in the ozone  
345 mixing ratio in response to the doubled CO<sub>2</sub> do contribute the shortening of the QBO period due to its  
346 role in strengthening the tropical upwelling in the stratosphere (Bushell et al., 2010).

347 The real atmosphere involves the complex interactions among dynamics, chemistry, and radiation  
348 (Andrews et al., 1987). First of all, the dynamical QBO goes hand in hand with the ozone QBO (Hasebe,  
349 1994). Shibata and Deushi (2005) pointed out that the radiative heating related to the ozone QBO could  
350 modify the secondary meridional circulation associated with the QBO, and consequently could modify  
351 how the QBO westerlies move down faster than the QBO easterlies, leading to the elongation of the  
352 QBO period in the chemically interactive models as compared with the chemically non-interactive  
353 models. However, it is difficult to fathom how the intensity of the secondary meridional circulation

354 associated with the QBO could change the QBO period due to the fact that any speedup or slowdown of  
355 the descending westerly shear zones is roughly compensated by the concurrent slowdown or speedup of  
356 the descending easterly shear zones. Furthermore, due to the increase of the zonal mean temperatures  
357 and ozone concentrations with the altitude in the lower stratosphere, the motion, ozone, and thermal  
358 waves are closely coupled. Pawson et al. (1992) found that the net linearized cooling coefficient from  
359 CO<sub>2</sub> (Newtonian cooling) was more than compensated in the lower equatorial atmosphere arising from  
360 absorption by the 9.6  $\mu\text{m}$  bands of ozone (see their figure 8). This reduced or negative radiative damping  
361 in the lower stratosphere acts to lengthen the QBO period in presence of the increased ozone due to the  
362 doubling of the CO<sub>2</sub> concentrations. Finally, taking into account the short-wave heating of eddy ozone,  
363 Cordero et al. (1998) used a mechanistic model with a one-dimensional representation for mean flow  
364 and a three-dimensional depiction for Kelvin and Rossby-gravity waves to demonstrate that the ozone  
365 distribution, which maximizes in the middle stratosphere, leads to the local radiative damping decreases  
366 by up to 15% below 35 km and its increases by up to 20%. They concluded that ozone feedbacks  
367 lengthen the QBO period by about 2 months. Cordero and Nathan (2000) further developed a more  
368 sophisticated mechanistic model with a two-dimensional representation for mean flow and a three-  
369 dimensional depiction for Kelvin and Rossby-gravity waves, and surprisingly found that ozone  
370 feedbacks had little influence on the QBO period. We believe that more studies should be conducted to  
371 fully understand how to put together those various effects of interactive ozone on the QBO period.

372 Using the NASA Goddard Institute for Space Studies (GISS) Model E2.2-AP (Rind et al. 2020; Orbe  
373 et al. 2020), DallaSanta et al. (2021), to the great extent, isolated the overall effect on the QBO period  
374 of the increase in ozone due to the doubled CO<sub>2</sub>. They first used a chemically non-interactive (NINT)  
375 model to conduct two CMIP6 experiments: the preindustrial (pi) control run, and the doubled CO<sub>2</sub> (2X)  
376 run. The two experiments only differ in the CO<sub>2</sub> concentration with the latter being two times the former.

377 Any other specification of these two experiments is the same, e.g., the ozone concentrations in the two  
378 runs are identical. Their Figure 5 shows that the doubling of CO<sub>2</sub> in the NINT model shortens the QBO  
379 period from 29.1 to 25 months. In other words, the doubling of CO<sub>2</sub> shortens the QBO period by 14%.  
380 DallaSanta et al. (2021) then employed a chemically interactive CMIP6 model with a mass-based scheme  
381 (Bauer et al., 2020), called One-Moment Aerosol (OMA), to conduct the pi control run and the 2X run.  
382 The ozone concentrations simulated by the OMA model increase by 10-15% in response to the doubling  
383 of CO<sub>2</sub> (figure not shown), which is consistent with the results of Jonsson et al. (2004). Figure 5 in  
384 DallaSanta et al. (2021) indicates that the doubling of CO<sub>2</sub> in the OMA model shortens the QBO period  
385 from 31.7 to 26.6 months. Namely, the doubling of CO<sub>2</sub> shortens the QBO period by 16%. In short, the  
386 results of DallaSanta et al. (2021) appear to suggest that three-way interactions among dynamics,  
387 chemistry, and radiation tend to slightly amplify the shortening of the QBO period in response to the  
388 doubling of CO<sub>2</sub>.

389 Note that  $N$ , the Brunt-Väisälä frequency, in Eqs. (2) and (3) also changes with increasing CO<sub>2</sub>.  
390 Richter et al. (2020b) showed that  $N^2$  would be decreased by ~5% in the stratosphere when CO<sub>2</sub> is  
391 doubled (refer to their Figure 2c). We used the HL model to conduct a sensitivity test by adopting  $G = 0$   
392 in Eq. (1) with the radiative damping profile corresponding to the doubled CO<sub>2</sub> and the top of the models  
393 at the 48 km level. The rest of parameters in this sensitivity test are identical to those in all the previous  
394 runs except that the Brunt-Väisälä frequency in this experimental run was 2.5% smaller than that in the  
395 control run. The models were run for 1000 years to further increase the spectral resolution. We found  
396 that when the Brunt-Väisälä frequency was decreased by 2.5%, the simulated QBO period was slightly  
397 lengthened from 30 months to 30.2 months (figure not shown). In other words, the impact of decreasing  
398 stratospheric buoyancy frequency on the QBO period is almost negligible.



399 Analyzing eleven CCM1-1 REF-C2 climate–chemistry simulations, Eichinger and Šácha (2020)  
400 showed that the scale height in the stratosphere decreases by 2.3% per century. Accordingly, we used  
401 the HL model to conduct another sensitivity test by adopting  $G = 0$  in Eq. (1) with the radiative damping  
402 profile corresponding to the doubled  $\text{CO}_2$  and the top of the models at the 48 km level. The rest of  
403 parameters in this sensitivity test are identical to those in all the previous control runs except that the  
404 scale height in this experimental run was 2.3% smaller than that in the control run. The model was also  
405 run for 1000 years for the sake of higher spectral resolution. We found that when the scale height was  
406 decreased by 2.3%, the simulated QBO period was also shortened by about 2.3%, i.e., from 30 months  
407 to 29.3 months (figure not shown). Apparently, the shortening of the QBO period due to the warming  
408 climate is ascribed less to the shrinkage of the scale height in the stratosphere than to the enhancing of  
409 the stratospheric radiative damping. Together, the shrinking scale height and the increasing radiative  
410 damping shorten the QBO period by about 9.6%.

411

## 412 **5. Conclusions**

413 Plumb (1977) envisioned that stratospheric climate change would give rise to long-term changes in  
414 the QBO period due to changes in radiative damping and the Brunt-Väisälä frequency. Using one-  
415 dimensional (1D) models and taking into account the uncertainty due to the radiative damping rate, we  
416 found that the enhanced radiative damping arising from the doubling of  $\text{CO}_2$  leads to the shortening of  
417 the QBO period by about  $7.4\% \pm 0.9\%$  provided that the model top is higher than the 46 km level.  
418 Furthermore, when we incorporated both the 2.3% shrinkage of the scale height and the enhanced  
419 radiative damping, the QBO period is shortened by about 9.6%. In addition, the impact of decreasing  
420 stratospheric buoyancy frequency is marginal. While the increased ozone in response to the doubling of  
421  $\text{CO}_2$  appears to slightly further shorten the QBO period, more research needs to be done for the

422 appreciation of the underlying mechanisms. Note that our 1D models include neither gravity waves nor  
423 tropical upwelling and assume that there are no changes in wave fluxes entering the equatorial  
424 stratosphere.

425 From a comprehensive model perspective, Richter et al. (2020b) showed that the changes in period  
426 of the QBO in warming climate simulations varied quite significantly among these models. Some models  
427 projected longer mean periods and some shorter mean periods for the QBO in a future warmer climate.  
428 They argue that uncertainty in the representation of the parameterized gravity waves is the most likely  
429 cause of the spread among the QBOi models in the QBO's response to climate change.

430 In addition, CO<sub>2</sub> increases in the NASA GISS Model E2.2-AP lead to a decrease of both QBO period  
431 and QBO amplitude (DallaSanta et al., 2021). The period decrease is mostly associated with increases  
432 in lower stratospheric momentum fluxes (related to parameterized convection), a finding consistent with  
433 Geller et al. (2016a, 2016b) and Richter et al. (2020b). The amplitude decrease is mainly associated with  
434 a strengthened residual mean circulation, also consistent with the literature, although the vertical  
435 structure of the circulation response is nontrivial. It is worth mentioning that horizontal momentum flux  
436 divergences could also play an important role in weakening the QBO (Match and Fueglistaler, 2019,  
437 2020).

438 Our 1D models only explored how the QBO period responds to the enhancing radiative damping of  
439 planetary waves, the shrinking scale height in the stratosphere, and the decreasing stratospheric  
440 buoyancy frequency due to the increasing CO<sub>2</sub> concentration. In order to investigate how those factors  
441 affect gravity waves which play an even more important role in determining the QBO period than  
442 planetary waves, high-resolution models such as those used by Kawatani et al. (2011, 2019) are desirable  
443 to further our understanding. Ultimately, how the QBO period changes in response to the increasing CO<sub>2</sub>  
444 will be determined by the combined effects of the strengthening of tropical upwelling, the increasing of

445 wave fluxes entering the equatorial stratosphere, the enhancing of radiative damping, and the shrinking  
446 of the scale height in the stratosphere, which warrants further research.

447

448 **Data availability**

449 Any data used in this paper can be made available from the corresponding author upon request.

450

451 **Author contributions**

452 All authors made equal contributions to this work.

453

454 **Competing interests**

455 The authors declare that they have no conflict of interest.

456

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463

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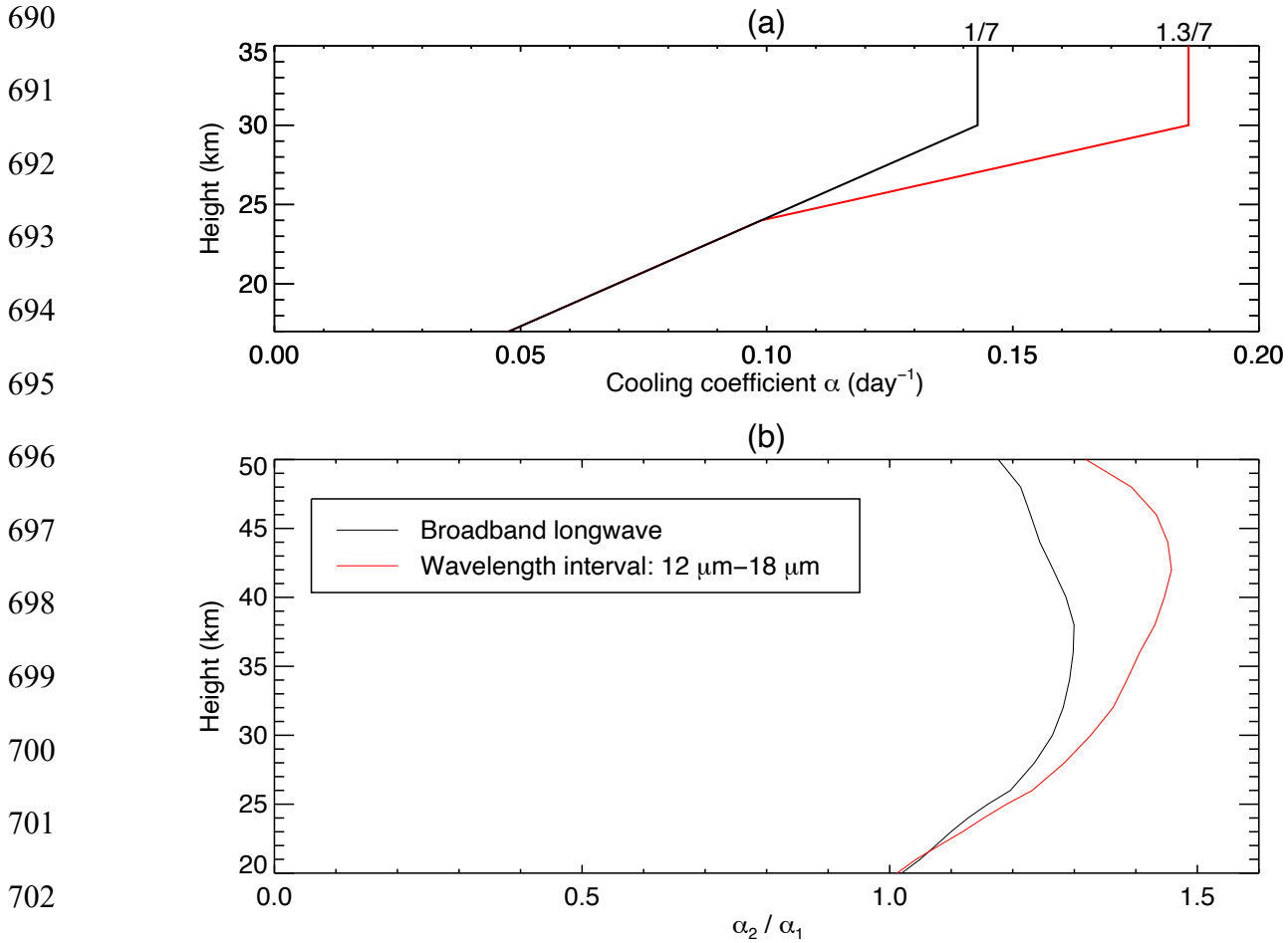
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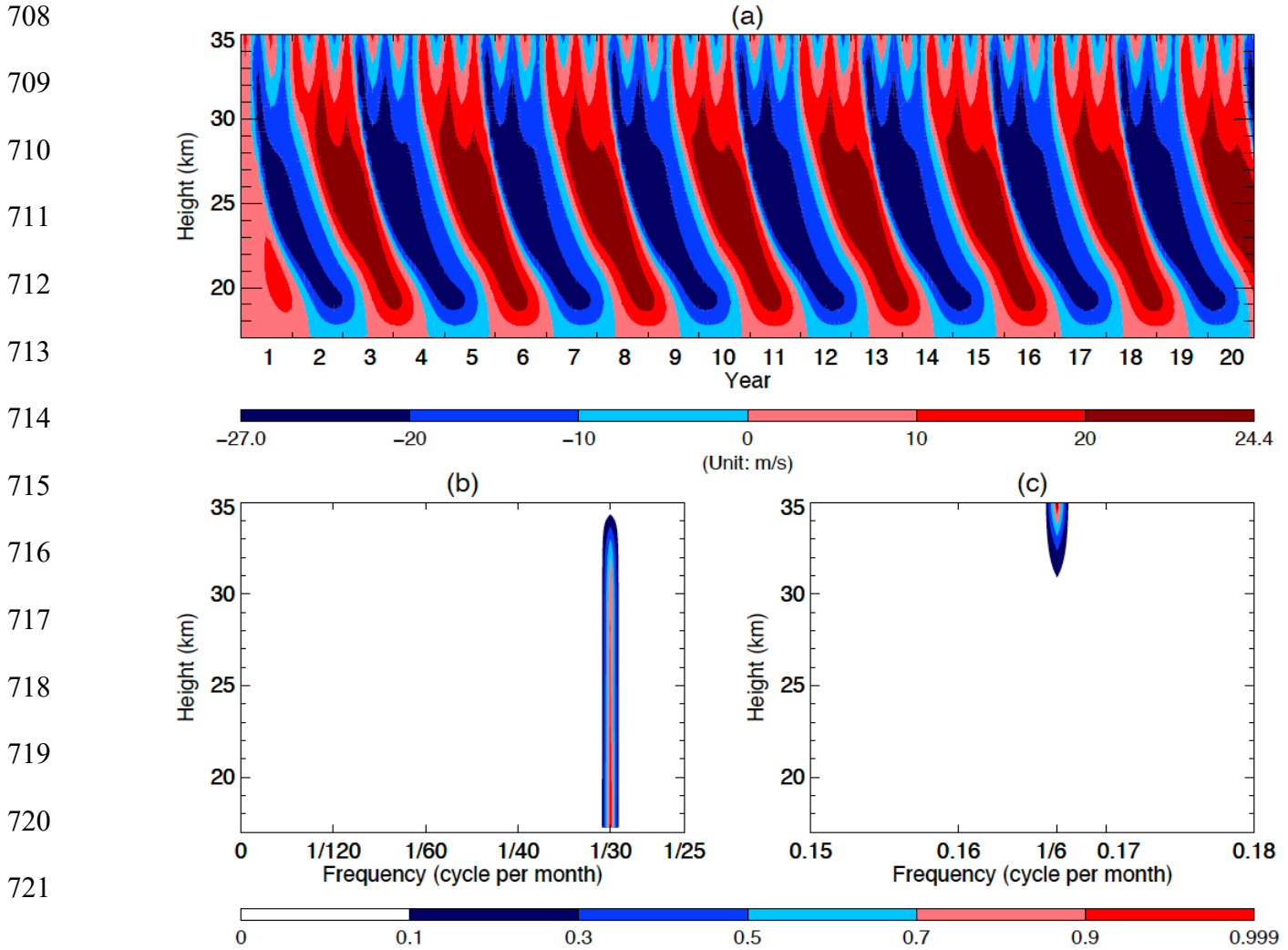
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703 **FIG. 1:** (a) Profiles of Newtonian cooling coefficients: The smaller values (black line) are used for the  
 704 control runs while the larger values (red line) are used for the experimental runs. (b) Profiles of the  
 705 ratio of  $\alpha_2$  to  $\alpha_1$ , where  $\alpha_1$  and  $\alpha_2$  denote the Newtonian cooling coefficient for the reference CO<sub>2</sub> and  
 706 the doubled CO<sub>2</sub>, respectively. The black line depicts the ratio for the broadband longwave (5  $\mu\text{m}$  –  
 707 100  $\mu\text{m}$ ) and the red line delineates that for the CO<sub>2</sub> absorption band (12  $\mu\text{m}$  – 18  $\mu\text{m}$ ).



722 **FIG. 2:** (a) Time–height section of the monthly averaged mean zonal wind over the first 20 years from  
 723 the HL’s original model. (b) and (c) Frequency–height section of the power spectral densities (PSD) of  
 724 the standardized monthly averaged mean zonal wind of the 100 years. Note that in order to better  
 725 visualize the PSD in (b) and (c), we trimmed off the blank segments for the frequencies ranging from  
 726  $\frac{1}{25}$  to 0.15 cycle per month and those ranging from 0.18 to 0.5 cycle per month.

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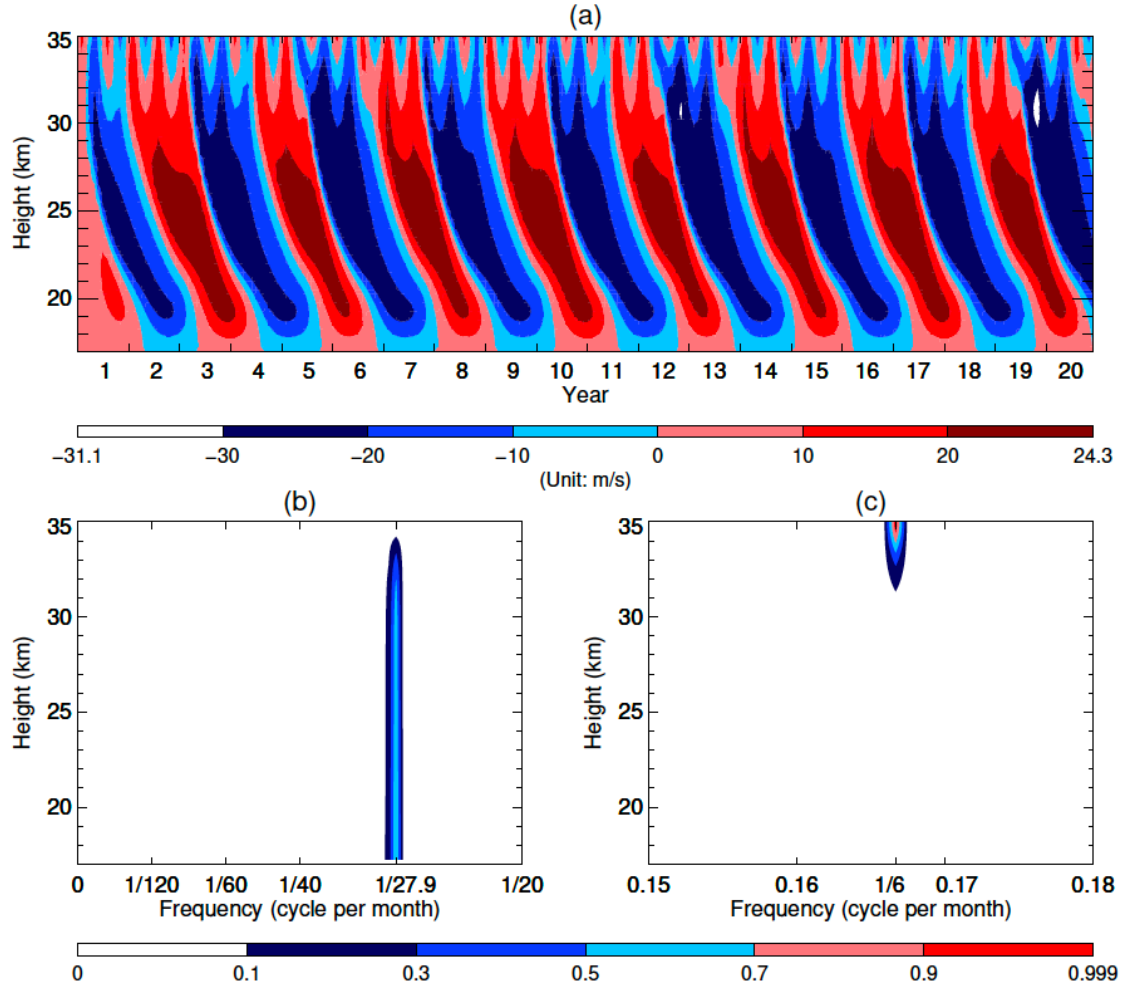
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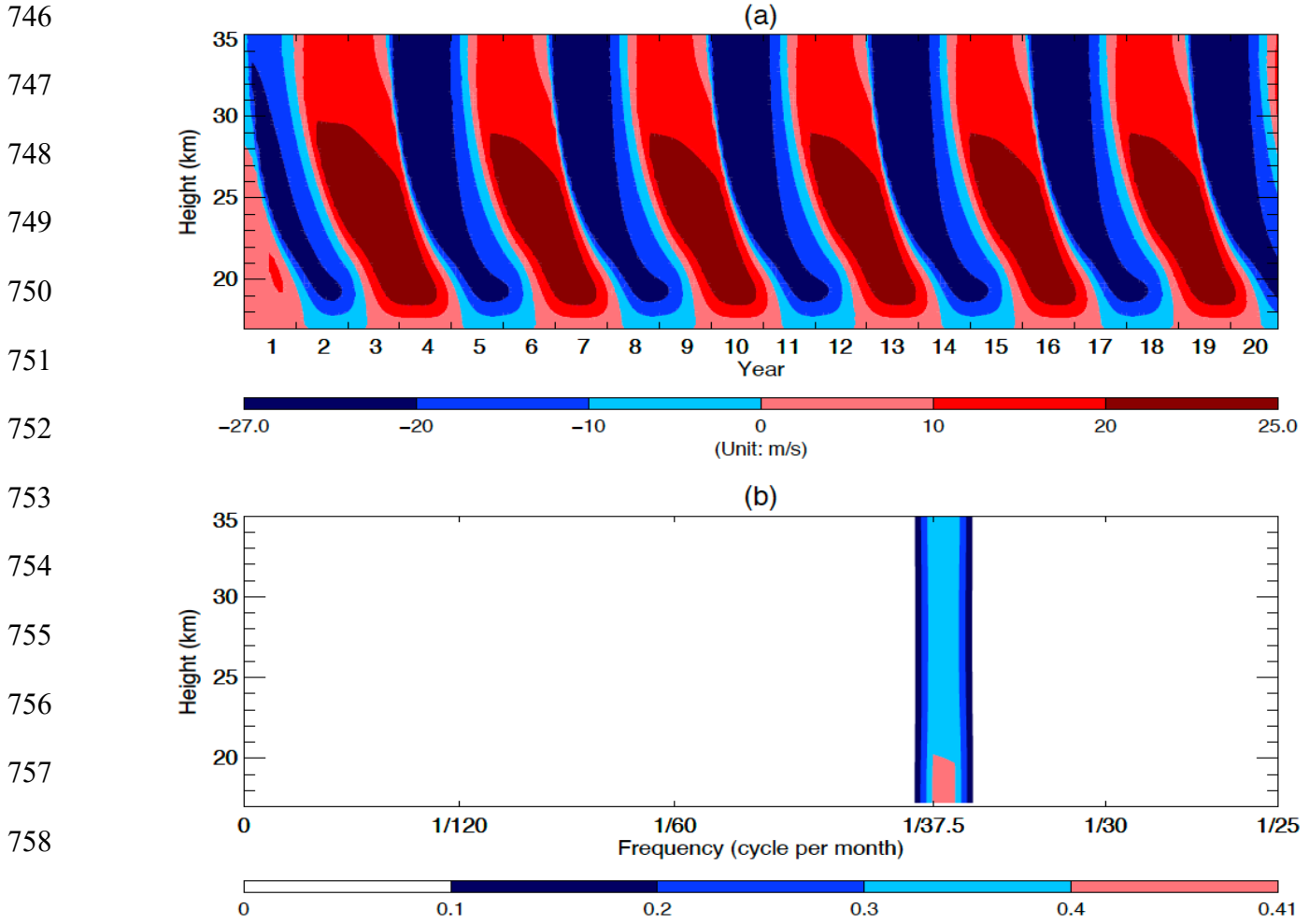
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**FIG. 3:** (a) Same as FIG. 2a, but with the enhanced  $\alpha(z)$  depicted as the red line in FIG. 1a. (b) and (c) Frequency–height section of the power spectral densities (PSD) of the standardized monthly averaged mean zonal wind of the 100 years. Note that in order to better visualize the PSD in (b) and (c), we trimmed off the blank segments for the frequencies ranging from  $\frac{1}{20}$  to 0.15 cycle per month and those ranging from 0.18 to 0.5 cycle per month.





759 **FIG. 4:** (a) Time–height section of the monthly averaged mean zonal wind over the first 20 years from  
 760 the HL’s model without the semiannual forcing. (b) Frequency–height section of the power spectral  
 761 densities (PSD) of the standardized monthly averaged mean zonal wind of the 100 years. Note that in  
 762 order to visualize the PSD, we trimmed off the blank segment for the frequencies ranging from  $\frac{1}{25}$   
 763 to 0.5 cycle per month.

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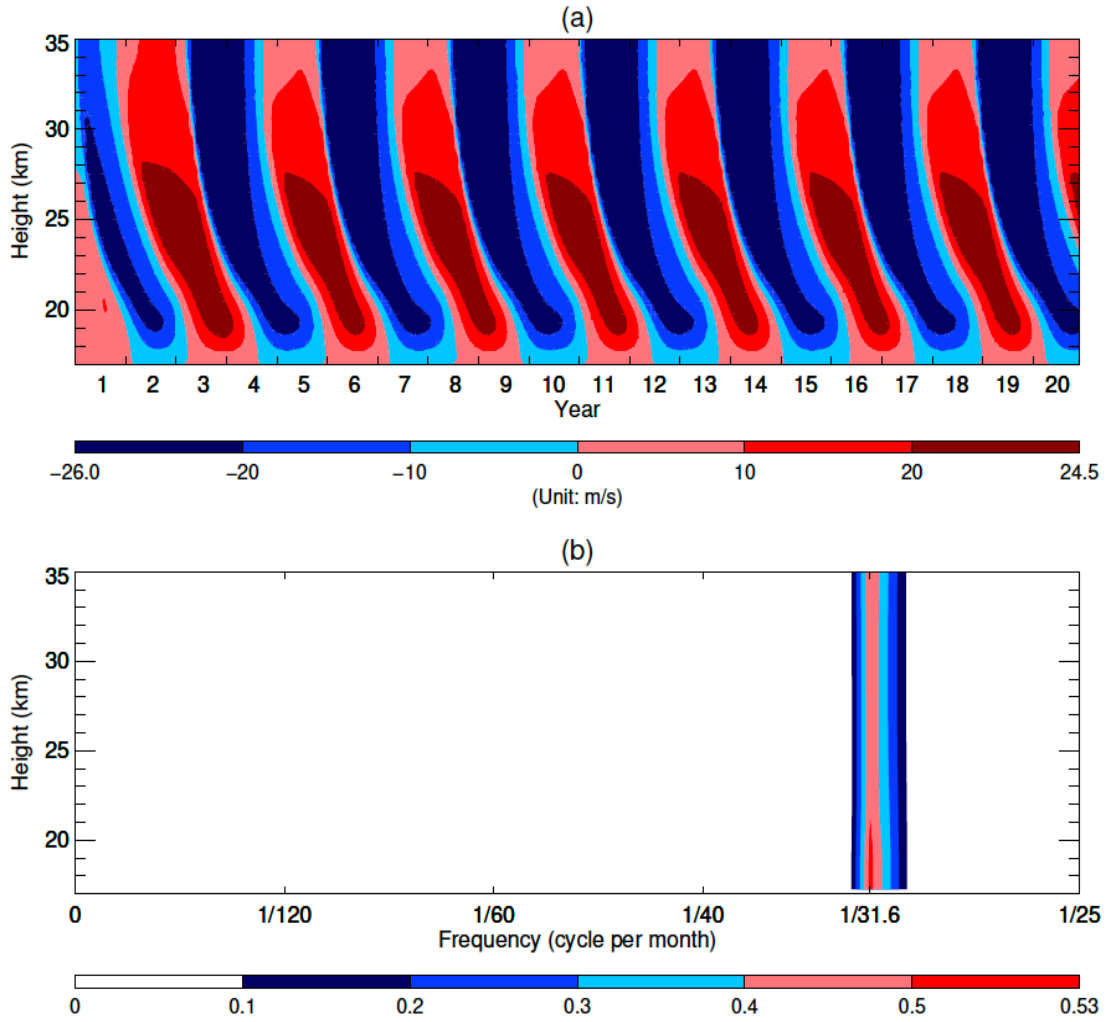
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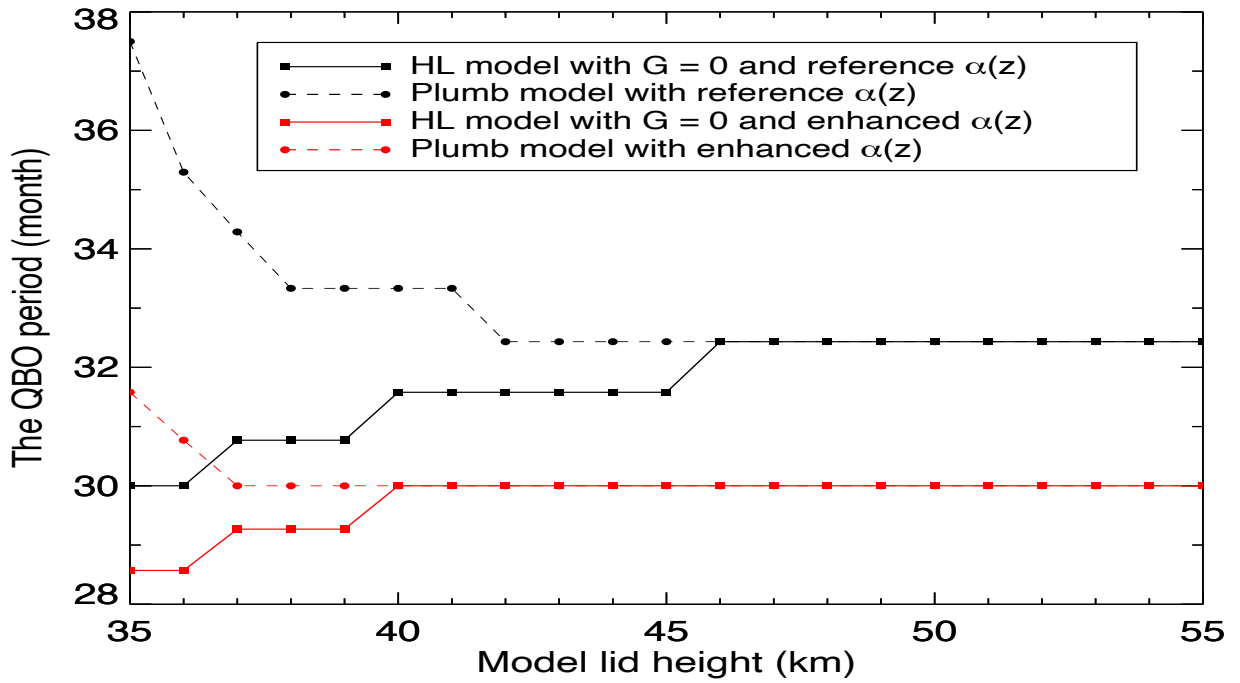
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**FIG. 5:** (a) Same as FIG. 4a, but with the enhanced  $\alpha(z)$  depicted as the red line in FIG. 1a. (b) Same as FIG. 4b, but for the doubled CO<sub>2</sub> Run.

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790 **FIG. 6:** The relationship between the simulated QBO period with the height of the model lid. Black and  
791 red lines depict the results from using the reference radiative damping and the enhanced radiative  
792 damping respectively while solid and dashed lines delineate the results from the HL model with  $G = 0$   
793 and the Plumb model respectively.