Answer to Roland Eichinger's comments on "The advective Brewer-Dobson circulation in the ERA5 reanalysis: climatology, variability and trends" by Mohamadou Diallo et al.

Dear Editor-in-Chief, Peter H. Haynes,

We are submitting our revised article titled "The advective Brewer-Dobson circulation in the ERA5 reanalysis: climatology, variability and trends". We thank the two Reviewers for their detailed and well thought-out comments, which helped to significantly improve the paper. We have made substantial changes to the manuscript in order to thoroughly address the Reviewers' suggestions and comments. Main changes concern:

- The calculation of residual circulation from wave drag using the downward control principle, as suggested by Reviewer #1, a new figure showing these results and the related discussion.
- Addition of statistical significance using Student's t-test to the differences as suggested by Reviewer #1
- Addition of information related to S-RIP and references.
- Re-calculation of the RCTT using the w* instead of heating rates for 2010-2018.
- rephrasing of several paragraphs in order to clarify the manuscript.

With these changes, we are convinced that the paper has been significantly improved and is highly relevant for a wide-ranging journal like *Atmospheric Chemistry and Physics*. Please see below our answers point by point to all reviewers comments and suggestions.

Reviewers comments are in bold, followed by our respective replies. Changes in the manuscript are in blue, allowing them to be tracked easily.

Kind regards,

Mohamadou Diallo (on behalf of the co-authors)

Roland Eichinger, Reviewer #1 (Comments to Author):

Major issues:

1. P1L12-13 and P25L12-13: I did not believe this statement when I first read the abstract and I still dont do so having read the whole paper. Commonly the contribution of gravity waves on tropical upwelling is around 30% here (see Butchart et al. 2010). Stating that a weaker GW forcing reduces tropical upwelling by 40% does not go together with that. The statement seems to base on the sentence "The contribution of the planetary waves to the tropical upwelling differences is less evident" on P21L1-2 (and P26L23), which you use to entirely disregard any PW contribution or anything else. I think what could help to separate the contributions of planetary and GW waves here could be a downward control (Haynes et al. 1991) analysis, but on the basis of patchy Fig. 10, the statement seems adventurous to me. Moreover, how well do the troppauses fit together between ERAi and ERA5? The differences seem strongly altitude-dependent. This and also Fig. 2b made me think of a possible vertical shift between the reanalyses, that could contribute to the upwelling differences, too.

Thank you Roland for this comment and suggestion, which we followed further with carrying out the suggested downward control analysis, what significantly improved the paper! First of all, we agree that this strong contribution due to GWs seems somewhat inconsistent with Butchart et al 2010. However, the small-scale GWs depend largely on the models resolution and parameterizations. As both (resolution, GW parameterization) clearly differ between ERA5 and ERA-Interim, a significant effect on the reanalysis GWD can be expected. Furthermore, it is important to notice (Fig. 2b) that the 40% difference in the upwelling occurs only in a shallow layer between 15-17km, above the difference decreases with height.

The new statistical significance estimate Fig. 10 shows that the differences in GWD between the reanalysis in the lower stratosphere subtropics are indeed significant (at 95% level). Finally, our downward calculation indeed quantitatively proved that the difference in the upwelling between ERA5 and ERA-Interim is related to GW drag. The fact that PWD agrees much better between ERA5 and ERA-Interim makes sense to us because PWs are well resolved now in the reanalyses and climate models, therefore, differences between the reanalyses should only to a minor extent be caused by differences in the representation of PWs.

Regarding the potential effect of a tropopause difference between the reanalyses, we think that such an effect should be minor. The tropopause between the two reanalyses has already been compared by Tegtmeier et al (2020) that we already cited in the manuscript. They concluded that "there is good agreement between reanalysis estimates of tropical mean temperatures and radio occultation data, with relatively small cold biases for most data sets". Thanks again for this very good suggestion!

2. In all plots where you calculate the difference between ERA-interim and ERA5 you need to add the statistical significance of the differences. In some regions and/or for some variables, the variability may be so large that the mean differences are not meaningful or small differences might be overseen despite their significance. Please add significance to all those plots and revise your text accordingly. In many occasions (e.g. P26 L16,L24,31) you even mention significance, but it has never been shown.

Thank you Roland for this remark. We have added the statistical significance (t-test) of the differences in the figures and marked where results are significant. We revised the text where required.

3. P7L26-27 and P25L13-14: "suggesting a stronger advective BDC" That statement seems much too general and in some sense even wrong, because you already showed, that in the tropics, the upwelling is weaker. Often tropical upwelling is used as a proxy for the advective BDC in the whole stratosphere. As the stronger downwelling is limited to the high latitudes, this might be related to the polar vortex strength, which has some impact on high latitude downwelling. But the polar vortex differences between ERAi and ERA5 are not discussed in the paper. I am not saying you should analyse it, and include plots, but there should be a discussion about it, separating the different regions. The topic only appears very briefly in the very last sentence of the paper. In my opinion this is much too late and too briefly discussed, it should be included properly in the analysis and discussion.

We agree that the formulation here was misleading. The upwelling is weaker compared to the fast ERA-I upwelling, but at the same time ERA5 does show a stronger downwelling of advective BDC in polar regions (Fig 1 and 2). The effect of polar vortex strength could indeed affect the downwelling differences, but would need a more detailed analysis beyond the scope of this paper. What is sure is that several things might be in play such as a higher resolution, higher model top, new non-orographic gravity wave parameterization scheme, and the progress made in the more realistic representation of the sponge layer in ERA5, which is presumably designed to damp upward propagating waves near the model top to avoid reflections from the upper boundary. Thus, we modified the text to clarify, and furthermore report what the analyses show and avoid any speculation about the polar vortex without background information. Further, we have improved the discussion.

4. The paper is quite long and not every analysis is really needed for the conclusions. I think some of the figures (or panels) do not contribute anything to the final conclusions. I therefore suggest to go through the paper starting from the back, analysing each conclusion with respect to which figures are really needed for that. The rest can be banished to a supplement, where I would also move the figures that now are in the appendix. For example: P25L14-18: If this is all the outcome from the seasonal climatologies, I think the analysis of the seasonal climatologies can be reduced drastically, and most of the figures can be moved to a supplement. Also, I am not sure if Fig. 3 is needed at all for the conclusions.

We agree that the paper is a bit long. However, as the ERA5 Thank you Roland for the suggestion. As the ERA5 reanalysis is new and this manuscript is the first paper looking at metrics of BDC for the S-RIP, we would like to present a complete analysis on the advective BDC representation in ERA5. Hence, we decided to keep all figures. However, we went through the text to streamline and shorten it, where possible.

5. Until section 4, the paper always focuses on the comparison between ERAi and ERA5. In section 4, at first only the ERA5 trends (streamfct and wave drag trends) are analysed, and then the mass flux trend is compared between ERA5 and ERAi again. I do not understand why you do not stick to the comparison between the reanalysis products, as it seemed to me that this is the focus of the paper. I suggest to include the ERA5-ERAi streamfct and wave drag comparison here as well, to keep the theme of the paper. Moreover, I suggest to reflect that theme also in the title of the

paper, maybe something like: "Comparison of the advective Brewer-Dobson circulation between ERA5 and ERAinterim reanalysis: climatology, variability and trends". And I particularly suggest to add "climatology", because that is what most of the paper deals with (annual and seasonal climatologies).

We do see the point that Fig. 11 is a bit different to the style of the other figures. However, as many authors have already discussed the effects of different wave types on BDC trends in ERA-Interim (e.g., Abalos et al., 2015) and repeating this here would add another 4 plot panels we decide to keep the figure as is. Nevertheless, we have improved the discussion and links toward previous studies. Also, we have added the term "climatology" into the title.

6. The discussion and conclusion section almost completely lacks the connection to literature and it also does not point out what the implications of the study are. I think both these points can easily be addressed. The literature is already outlined nicely in the introduction. The implications can include what the present study means for older conclusions about the BDC based on ERAi data (or model simulation results that are nudged or prescribed to ERAi dynamics), and what now can be assessed better, or more precisely, or differently with ERA5. This would be nice for closing remarks of the paper.

Thanks for this opinion! As we do not want to extend the conclusion section too much, we decided to address these points in section 4, which we modified accordingly. Now, we discuss the implications of our results for climate model simulations that are nudged to reanalysis meteorology and using reanalysis for validation.

Minor issues:

1. P3L11: "the strength of the BDC". Do you mean the change of the strength here or really the strength? If the latter, I think the statement is out of place here, since you talk about trends in this paragraph.

We mean both: the strength and the trend. This is now stated more clearly in the revised manuscript.

2. P3L13: remove "reanalyses and for". There were no reanalyses analysed in that study.

We have rephrased the sentence.

3. P4L11-12: I assume that the ability to better resolve (macro-scale) meteorological features is mainly due to the higher resolution, and not "apart from that". Hence, please reformulate the sentence.

The sentence is talking about the improvement in ERA5 compared to ERA-Interim. In addition to higher resolution, there are additional important improvements as we mentioned in this paragraph. We have clarified it.

4. Sect. 2.2: Please consider the QJRMS paper by Eichinger and Sacha, (2020). You have to be very cautious with which w* you use for your analyses. As you do all your calculations in log-pressure coordinates, you may make a mistake when you calculate the w* trends because in log-pressure coordinates, the trends of the pressure levels (i.e. the temperature trends and thereby the trend in the scale-height, which you implicitly neglect using the log-pressure formulae) is not considered. In that paper, we propose using the goepotential coordinates. However, for your streamfunction trends, you should be fine, because the H cancels out when you use the log-pressure density (Sect. 4.2 of the paper). But you also calculate some w* trends at the end where it certainly matters. And I am not exactly sure if it is important for the variability calculations. Please make sure your analyses do not include the error.

We are aware of this study and conclusions. As both estimates are consistently calculated (e.i. literally saying Apple to Apple comparison). Any bias in one will be present in the other one. So multiplying our result by a constant (20%) will just shift the value but won't changes any pattern and variability differences between ERA5 and ERA-Interim. In addition, we have done the calculation on the original model levels for enabling comparisons to previous results that were obtained for reanalysis comparison S-RIP project as this article is part of the project.

5. P7L4: Remove the overbar over w^{*}, it is not zonal mean here. But throughout the paper, use the overbar when zonal mean is shown and no overbar if it is general. And note somewhere that the overbar stands for zonal mean.

In the regression, we use also the zonal mean w*bar as defined in equation (3).

6. Fig. 2: Why 15.σ? The 15 seems very arbitrary, can you explain why you chose it? And why not adding such a measure of uncertainty also to a,b,c? It would be helpful when interpreting the results (see also my major point about statistical significance)

The 15. σ was just for scaling the figure as the vertical profile are in percentage and sigma not. Anyway, we have replace the errorbar by the statistically significant value.

7. P10L9: But according to Fig. 2e, that is only true between 35 and 40 km, not everywhere above 20 km.

We have rephrased the sentence and added new ones.

8. P11L14-16: Note that ... polar regions. I do not understand what you try to say with that sentence. I suggest to remove it.

We are saying that there are differences in the upwelling and downwelling region like tropics, surf-zone and polar. We have rephrased it.

9. P11L19-24: The description of the differences is unclear to me: - In DJF, I only see a small negative patch in the UTLS and more negative fields in the SH mid to high latitudes. The conclusion in L21 therefore bases on wrong facts. - I also do not see the positive differences between 40S and 0, where are you there? Still in DJF? The differences generally barely exceed the tropopause, or are just much smaller in the stratosphere, as the mass streamfunction is much smaller there too. So the color bar is maybe not really suitable, and moreover, it would be very helpful here to see statistical significance. The statement that the residual circulation is stronger in ERA5 seems wrong. Firstly, you already showed that upwelling is weaker, secondly Fig. 4c shows the opposite. Please clarify and correct these points.

Thank you for this comments. Our apologies! We had made a mistake in indicating the right figure. The Fig. 4f and 4i clearly shows a blue area (negative difference) extending from the UTLS into the upper stratosphere during the DJF. Regarding the statistical significance, we have added and included the discussion in the revised version where it's needed.

10. P11L25-27: I do not understand what you mean by "horizontal shift" here. Can you elaborate on this please.

What we mean is that the circulation cell look like being southward shift in the UTLS during winter and northward shift during summer compared to ERA-Interim. We have rephrased it.

11. P14L23: "stronger westerly and easterly shear" I can not quite see that. Can you please describe where/guide the eye a bit?

We drop the term "shear". ERA5 exhibits stronger westerly and easterly QBO winds compared to the ERA-Interim as shown in the Fig. 6c (cross section) in the whole topical region. We have rephrased it.

12. P14L25: "into the troposphere below the tropopause does not propagate that far downward" I can not see that. Only some seasonal pattern is stronger in the upper troposphere in ERA5. Can you please explain this more precisely, and/or rephrase the sentence.

We have rephrased it.

13. P14L29-30: Halting, complicated sentence, please rephrase.

We have rephrase it as following "In the ERA5, the use of a new non-orographic gravity wave drag parameterization, which is different from the ERA-Interim, is likely the cause of the observed differences (Orr et al., 2010; Scaife et al., 2002; Lott et al., 2012; Richter et al., 2014)."

14. P17L6-7: Can you rephrase this sentence please, I think this is important, but I do not understand it.

We have rephrased it.

15. P19L1: Why competing? Both these points are accelerating the BDC, right?

Competing in the sense which one has a predominant effect for instance on mid-latitude ozone, i.e. global warming versus strong El niño. However in term of acceleration, they both led to BDC strengthening. We have rephrased it and be more explicit.

16. P19L4-5: According to what I can see from the figures, this statement is probably right, but why do you not show the differences figures in that case, as you do for all other figures? (see also my major point on that)

Thank you for the suggestion. As the difference is clearly visible, therefore, we don't think it is necessary showing an additional panel.

17. **P20L7:** "less evident, but stronger" How can that be? That does not seem right to me. It would be clearer if you would show the differences.

We mean that the ENSO-induced change in the deep branch is much stronger in ERA5 than in ERA-i even though they are not as clear as in the shallow and transition branches. We rephrased the sentence.

18. **P20L22:** ... can induce meridional wind "changes". (provide a citation for this please, maybe Holton et al. 1995. Also for line 25-27)

In this sentence "contribution" and "changes" are inter-changeable. We keep it. We have added the citation.

19. P20L30: this description is not clear to me, please rephrase it.

We have rephrase it.

20. **P20L31-33:** Please rephrase this sentence, it is confusing. Why planetary and gravity wave together in the second part of the sentence? Did you not want to separate the two forcings here?

What we mean is "in the UTLS GW drag is dominant while in the upper stratosphere both GW and PW drag contribute. We have rephrased it.

21. P22L4-5: "the difference in the net forcing..." This sentence seems obsolete to me, that is what you analyse here, not a result.

The net forcing is shown in fig 10 and is calculated as (PW+GW-dudt). We have rephrased it.

22. **P22L15-33:** Figures that are not shown should not be described in detail and analysed in detail as here. As the paper is quite long already, I do not ask you to show the figures, but rather to move the description and the figures to the supplement and write in the main text only the most important outcome of these figures with a quick reference to the supplement.

Due to the importance of the figure and the discussion, we have chosen this compromised solution. Therefore, the discussion will stand for itself. Reference to the figures in the Appendix is only given for completeness.

23. **P23L7-8:** The trend around the tropopause seems like being caused by the tropopause rise (which is part of stratospheric shrinking). The circulation moves upward. Please reformulate, keep the Sacha citation, but add for example OberInder-Hayn et al. (2016) and Vallis et al. (2015).

We have added the references, as suggested. However, we would like to keep the word "probably", as further investigation of the strength of this process is still needed for ERA5. We have added the references and rephrased it.

24. **P23L29:** Provide an uncertainty range of the trend (e.g. 1σ)

We have include uncertainty range.

25. P23L23: "not significant", what test did you perform? Significant on what level?

We use a student t-test with two tail distribution and the level of significant is 95%. We have added in the text.

26. **P23L32-34:** please rephrase, it does not disappear, it is simply not present in ERA5, in contrast to ERAi. This is indeed a very important point, because it has been standing in contrast to what GCMs simulate. It should be described/ discussed with references in the last section.

We have rephrased it and added references.

27. Fig. 11: Panel a: Please do not show these white (undefined) areas in the troposphere, instead, modify the colour bar such that it includes -inf and +inf, so that at least the sign can clearly be seen. Panels b-d: What are the contour lines here? Add an estimate of the significance of the trends, and the units to the colour bars.

Thank you for the suggestion. We have included these white (undefined) areas in the troposphere. We did not add statistical significant values as it is not significant at 95%. It does not make sense. The contour lines are zonal wind and we have added to the captions. For aesthetical reasons of the figures, we just put the units in the captions.

28. caption Fig. 12: replace "trend" with "linear regression lines" (both times).

For consistency with the discussion in our regression section, and to be more accurate, we replaced "trend" with "linear trend".

29. *P26L28: Please provide a citation for ERA5 here. Also, remove the last part of the sentence (from ", which is" onward) or clarify what was done there and make it more precise*

We have added citations.

30. **P26L32:** But this acceleration has not been observed! Observations show a non-significant deceleration (Engel eta. 2009, 2017). The acceleration has been shown in model simulations.

Here, we were explained the observed temperature trends in the lower stratosphere from the findings of Thompson and Solomon, 2005 as well Fu and Qu, 2014 all agreed in the acceleration of the BDC upwelling. The Engel et al 2017 only look at a very localized area in the NH upper stratosphere, which is remote from the tropical upwelling and not significant. The previous papers look at observations in the most relevant area, including the tropical upwelling region. We have precise what we mean by rephrasing the sentence.

Minor issues:

- 1. *P1L7: The comparison of shows very good....* We have rephrased it.
- 2. P1L9: ...and in the...

Our original wording and that suggested are both correct. We decided to keep the wording as is.

3. P1L13: ...due to weaker gravity wave forcing at....

We have rephrased it.

- 4. *P1L20: ...(BDC, e.g. ...* We have rephrased it.
- 5. P1L21: ... has received a lot of interest ...

We have rephrased it

6. P2L2: remove "most effectively"

We decided to keep the wording as is.

- P2L7: (the so-called surf zone) We decided to keep the wording as is.
- 8. P2L16: ... and small-scale waves

We rephrased it.

- P2L23: greenhouse gas ozone depleting substances We rephrased it.
- P2L24-26: ... variability, QBO and ENSO, which affecting the temperature structure and thus the tropical upwelling and extratropical downwelling in the stratosphere
 We decided to keep the wording as is.

- 11. *P2L27: ... in wave propagation...* We have rephrased it.
- 12. P2L31: remove "would".

We have rephrased it.

13. P2L32: ...negative stratospheric temperature...

We have rephrased it to the suggested text by Reviewer 2.

14. P4L5and6: change better to higher

We decided to keep as it is because we mean better as "higher" is already illustrated by brackets "(6-hourly versus 1-5hourly)".

15. P4L8: ... for the 2000...

We have rephrased it.

16. P4L18: I guess you mean UTC here.

We have rephrased it.

- 17. *P4L28: ps (small letter)* We have rephrased it.
- 18. P4L29: velocity

We have rephrased it.

- P5L3: ... is the Lagrangian...
 We rephrased it following Reviewer 2 suggestion.
- 20. *P5L17:* θ *is the potential...* We have rephrased it.
- 21. *P6L10: ... to maintain steady ...* We decided to keep the wording as is.
- 22. *P6L10-11: brackets around citations (use citep)* We have rephrased it.
- 23. **P6L17: I guess this should be** $\phi(z')$

It is $\phi(z)$ as z' is just a substitute to z for notation sake in the integral. We decided to keep the wording as is.

24. P6L24: Used as a ...

We have rephrased it.

- P7L1: ... in detail and applied in numerous...
 We have rephrased it
- 26. P7L8: ... which are the...

We have rephrased it.

27. **P7L17:** ... seasonal means of ... This appears also below (P7L28 and caption Fig. 1, maybe more.)

We decided to keep the wording as is.

- P7L27: 0.5 mm.s1. (The dot between mm and s!). And that wrong dot appears many times again in the paper, e.g. P7L31, Fig. 2, Fig. 4, please correct throughout the paper We have replaced the dot by the common way ("cdot").
- 29. For a quick look at the figures, I would appreciate the units of the variable attached to each color bar, rather than (only) in the caption.

Instead of overloading the plots with information we decided to state the units in the captions.

30. *caption fig. 1: black*

We have corrected it.

31. Fig. 2 overbar over w

With the matlab version that we have, it is not possible to put the overbar.

- caption Fig. 2: ... the differences of w* between relative to the annual mean We have rephrased it.
- 33. caption Fig. 3: Monthly mean w* at 70 hPa as function of latitude and time.

We decided to keep the wording as is as "Monthly" and "latitudinal" are equivalent to "as a function of latitude and time"

34. P10L3: of w*

We decided to keep the wording as is.

- 35. P10L5: and L16: in w* (please correct that throughout the paper) We decided to keep the wording as is.
- P11L20: ... between 0 and ...
 We have rephrased it.
- P11L21: ... and is consistent...
 We have rephrased it.
- P11L25: You mean "Fig. 4g-i" We have rephrased it.
- 39. *P11L28: the two reanalysis in Fig. 5,...*We decided to keep the wording as is.
- 40. *P11L32: ...between ERA5 and... (remove the here, and please do that throughout the paper)* We have rephrased it.
- 41. *Caption Fig. 4: boreal winter / boreal summer* We have rephrased it.

42. Caption Fig. 4: You describe differences in contour lines, but I do not see any difference in the colour bar, so what do you mean?

We decided to keep the wording as is.

- Caption Fig. 5: boreal winter / boreal summer We have rephrased it.
- 44. **P14L3: years**

We have rephrased it.

- 45. *P14L7: average* We have rephrased it.
- 46. *P14L8: ...for the full..* We decided to keep the wording as is.
- 47. *P14L: ... major modes of ...* We have rephrased it.
- 48. *P14L15 interannual time-scales* We have rephrased it.
- 49. *P15L1: driving of the* We have rephrased it.
- 50. *P16L11: i.e.* We have corrected it.
- 51. *P16L15: of the secondary* We have rephrased it.
- 52. *Caption Fig. 7. Missing full stop after (10)* We have corrected it
- 53. *caption Fig. 8: I guess the common abbreviation for standard deviation is std* We have corrected it as ACP imposed this abbreviation.
- 54. *P18L1: remove "regions of"* We have rephrased it
- 55. *P18L2: while the QBO* We have rephrased it.

- 56. *P18L2: remove "again"* We have deleted it
- 57. *P18L3: altitudes* We have rephrased it.
- 58. *P18L9: conditions* We have rephrased it.
- 59. *P20L8: stream-function* We have rephrased it.
- 60. *P20L13-14: ...with less ...* We have rephrased it.
- 61. *P20L15: remove out* We have rephrased it.
- 62. *P20L19: driving of the* We have rephrased it.
- 63. *Assuming zonal momentum...* We decided to keep the wording as is.
- 64. *P20L23: ... the meridional residual wind...* We decided to keep the wording as is.
- 65. *P22L11:... the non-orographic gravity wave ...* We have rephrased it.
- 66. P22L11: So ERA5 does... please rephrase the sentence We have rephrased it.
- 67. *P22L15: seaonal differences* We decided to keep the wording as is.
- 68. *P23L9: ...trend provides an...* We have rephrased it.
- 69. *P23L10: remove in ERA5 (that is the case not only in ERA5)* We are talking about our result. We decided to keep the wording as is.

- 70. *P23L15: planetary wave breaking* We have rephrased it.
- 71. *P23L18: remove we also note that* We have rephrased it.
- 72. *P23L22: ERA-Interim shows a ...* We have rephrased it.
- P23L32: the Does not apply anymore. This text was generally revised.
- 74. *P25L4: replace including with in particular* We have rephrased it.
- 75. P25L10: induced modulations

Does not apply anymore. This text was generally revised.

76. P25L16: seasonal mean

We decided to keep the wording as is.

Anonymous Referee #2:

General comments:

1. - While the detailed comparison between ERA5 and ERA-interim is very useful, it would also help to have some discussion linking how these reanalyses compare to other reanalyses. It is briefly mentioned that previous work has shown ERA-interim to be to have too strong upwelling, but it would be nice to know more. Since this paper is part of the S-RIP special issue, it would the authors better tie their work in with the other S-RIP work on the BDC. I'm not sure if the authors are contributors to the S-RIP BDC chapter, but I would recommend they get in touch with the authors of that chapter and have some content on the broader context of reanalysis representations of the BDC.

We thank the Reviewer for this thoughtful suggestions. We are involved in several S-RIP chapter, including the S-RIP BDC chapter 5. We have enhanced the discussion about the comparison to other reanalyses, about the too strong upwelling in ERA-Interim and the S-RIP work on the BDC at needed places in the manuscript (page 4, lines 26-30 and section 4).

2. - I found some of the discussion of the regression modeling confusing, and would appreciate if the authors could make some of this clearer. The most unclear part is the discussion of things like QBO amplitude variability that is plotted in figures 7 through 9. This is not really well defined in the paper. I'm guessing it might be the QBO coefficient in the regression fit, or it might be something like the RMS of the QBO timeseries for the fit. Also, the authors regress things like the zonal wind field against zonal wind defined at a specific level (i.e., the QBO defined as zonal wind at 50 hPa), which is a bit odd and requires a bit more nuanced interpretation. When doing something like this, the correlations at a higher level (at, say, 30 hPa) aren't really "caused" by the QBO wind at 50 hPa, but rather reflect the climatological structure of how the equatorial zonal winds propagate downward as part of the QBO. I think the discussion around these figures (7-9) results could be clarified on this point.

We thanks the Reviewer for pointing this out. The simplified description of the regression model was motivated by the fact that the regression model is well described in our previous studies (e.g. Diallo et al.

2018, 2019). Our regression model uses a lag term, therefore, allowing us to use only one QBO proxy at any given level. With the lag term, we can reconstruct the propagation of the QBO signal, therefore preventing us using two QBO proxies as classical linear regressions do. Regarding the figures 7 through 9, the Reviewer is right as the QBO "amplitude variability" is the QBO coefficient in the regression fit normalized by the standard deviation of the QBO proxy for all plots except for the temperatures and zonal mean wind figure. Now, we have clarified the description of the regression model and enhanced the discussion of the regression results.

Specific comments:

1. **Pg 1, line 21: gain** – > **gained**

We have rephrased it.

- Pg 1, line 22: distributions -> distribution
 We have rephrased it.
- 3. Pg 2, line 6: ascent > ascend

We have rephrased it.

4. Pg 2, lines 31-32: "strengthen the BDC, consistent with negative temperature trends" Do you mean negative temperature trends in the tropical lower stratosphere? Please clarify this statement

We thank the Reviewer for precision. Yes indeed, we mean the negative temperature trends in the tropical lower stratosphere as shown in previous studies (Thompson and Solomon, 2005; Fu et al., 2019). We have rephrased the sentences.

5. *Pg 2, line 34: e.i.* – > *i.e.*

We have rephrased it.

6. Pg 2-3: I'm a bit confused by the statement that reanalyses show BDC lower branch strengthening whereas figures like Fig 12 seem to indicate a slowdown (at least in ERAinterim). Are the reanalyses actually consistent on this, or is it just some of them? This comment ties in with my general comment about placing the ECMWF results within the broader context.

We apologize for the confusion. Overall, all reanalysis data sets except CFSR agreed in a robust strengthening shallow branch of the BDC from several different diagnostics such age of air, age spectrum and TEM (Diallo et al. 2012; Abalos et al. 2015; Chabrillat et al. 2018; Ploeger et al. 2019). The negative trend in ERA-interim w* calculated using the standard TEM formula is only present in the ERA-Interim as we have mentioned it in the manuscript following the previous studies (Seviour et al 2011; Abalos et al 2015). Abalos et al 2015 using different ways (standard, momentum and thermodynamic balance) of estimating w*, show that only the standard formula exhibits that behavior. In figure 12, we re-evaluated and highlighted that this strange behavior in ERA-interim w* calculated using the standard TEM formula vanishes in ERA5. Thus, this allows our scientific community to use ERA5 w* estimated with the standard TEM formula as a proxy for climate model inter-comparison, which were not recommended for ERA-Interim w* estimated using the standard TEM formula.

7. Pg 4: Both ERA5 and ERA-Interim use a hybrid vertical coordinate system. Are the authors using model level data for both calculations, or the lower vertical resolution pressure-gridded data typically provided by reanalysis centers? If using model level data, please state so explicitly. Also, it would be helpful to have some mention what kind of error in the TEM calculations would be induced by using data that is not strictly on pressure levels. Related to this, what is the lowest level (i.e., highest pressure value) at which the model levels are pure pressure levels (i.e., where b=0 for a vertical coordinate system where $p = a + b^*PS$), and is this different between ERA-Interim and ERA5? This might impact the discussion of the residual circulation below 20 km.

Thank you for for these comments and suggestions about the lowest level (b=0). We use model level data interpolated to log-pressure levels for both calculations. Fortunately, the ERA5 and ERA-interim shows almost the same lowest level (i.e., highest pressure value) at which the model levels are pure pressure levels (i.e., where b=0 for a vertical coordinate system where $p = a + b^*PS$). This level is about 18 km. For ERA-Interim, the coefficient b is equal to zero where the coefficient a is equal to 7306.63000 Pa and for ERA5 b is equal to zero where a is equal to 7311.869141 Pa.

8. Pg 4, line 19: What do the authors mean as the ERA5 dynamical fields are archived as tendencies over one hour? I assume fields like u,v,T are either archived as averages over some period (e.g., 1 hour) or are instantaneous quantities.

We have rephrase it.

9. *Pg 4, line 29: Omega is introduced here, but is not used until f is defined in the following sentence. I recommend to define omega in the sentence defining f.*

We have moved the definition of omega at suggested place.

- Pg 5, line 3: is a the -> is a We have rephrased it.
- Pg 6, line 10-11: references need proper parentheses. We have rephrased it.
- 12. Pg 7, line 8: "which the" > "which are the"

We have rephrased it.

13. *Pg 9, Fig 2: I believe the lower row of plots is showing ERA5 minus ERA-Interim, expressed as a percent difference. Please make this more clear in the caption.*

Yes indeed, the ERA5 minus ERA-Interim, expressed as a percent difference is actually the relative difference in percentage. We have rephrased it.

14. Pg 10, line 9: I don't really see ERA5 being stronger than ERA-Interim above 20 km in general. It does appear to be stronger from about 35 to 40 km (Fig. 2e).

Yes, that's correct. We have corrected it.

15. Pg 10, line 11: The use of a 15 sigma error bar strikes me as odd. Please justify the use of this quantity.

This use of 15 sigma was just for scaling issues as the differences were plotted in percentage. We have now added as errorbar the statistical significance of the differences, which highlight better the areas where the differences between the two reanalyses are significant.

16. Pg 10, line 11-12: I don't see what the authors are pointing out here. It looks to me like the variance increases with height.

We have rephrased it.

17. Pg 14, line 7-8: Why is only a 2 year period used? Regarding the period used, I assume the 2017-2018 period is somewhat of a best case scenario given that there are more/better observations constraining the reanalysis in this period than, say, in the earliest part of the record. Pg 14, line 14: mode – > modes.

We used two 2 years of mean RCTT because that's what we had at that time. Now, we replaced the RCTT calculated from diabatic heating rates for these 2 years by RCTTs calculated from (v^*,w^*) TEM residual circulation over the much longer period 2010-2018. The result is still consistent with fact ERA5 is be slower than ERA-interim.. The respective text passages are changed accordingly.

18. Pg 14, line 32: For those of us not intimately familiar with non-orographic gravity wave drag parameterizations, could the authors give some brief information on the difference between the schemes?

We have added brief information about the schemes.

19. Pg 17, line 10: Fig 8c,d should be Fig8 a,b.

We have corrected it.

- 20. *Pg 18, line 5: Fig 8a,b should be Fig8 c,d.* We have corrected it.
- 21. *Pg 22, line 33: awkward wording. Maybe the authors mean "therefore" instead of "there"?* We have rephrased it.

22. Pg 24, Fig 11a. I dont understand why the authors are showing the streamfunciton here instead of w*

The mass streamfunction and w^* are equivalent. The advantage using the streamfunction is that we can distinguish the BDC cells, and therefore discuss the different BDC branches (e.g., shallow vs. deep branch).

23. Pg 24, line 3 and Fig 12: The authors should show the uncertainties on these trends. Does the ERA5 trend use the ERA5 v5.1 data for the period 2002-2007? It would be really helpful to include both ERA5 and 5.1 in the timeseries plot, trend numbers, and discussion. It may not matter, but it's not obvious whether or not that is the case.

We have added the uncertainties to these trends. Yes, we use the ERA5 v5.1 in the study as we state in the section of description of the reanalyses.

24. *Pg 26, line 22: Could the authors be more specific about resolved vs. unresolved GW forcing in the discussion here, and elsewhere in the manuscript?*

We have rephrased it.

25. *Pg 26, line 24: large* -> *larger* We have rephrased it.