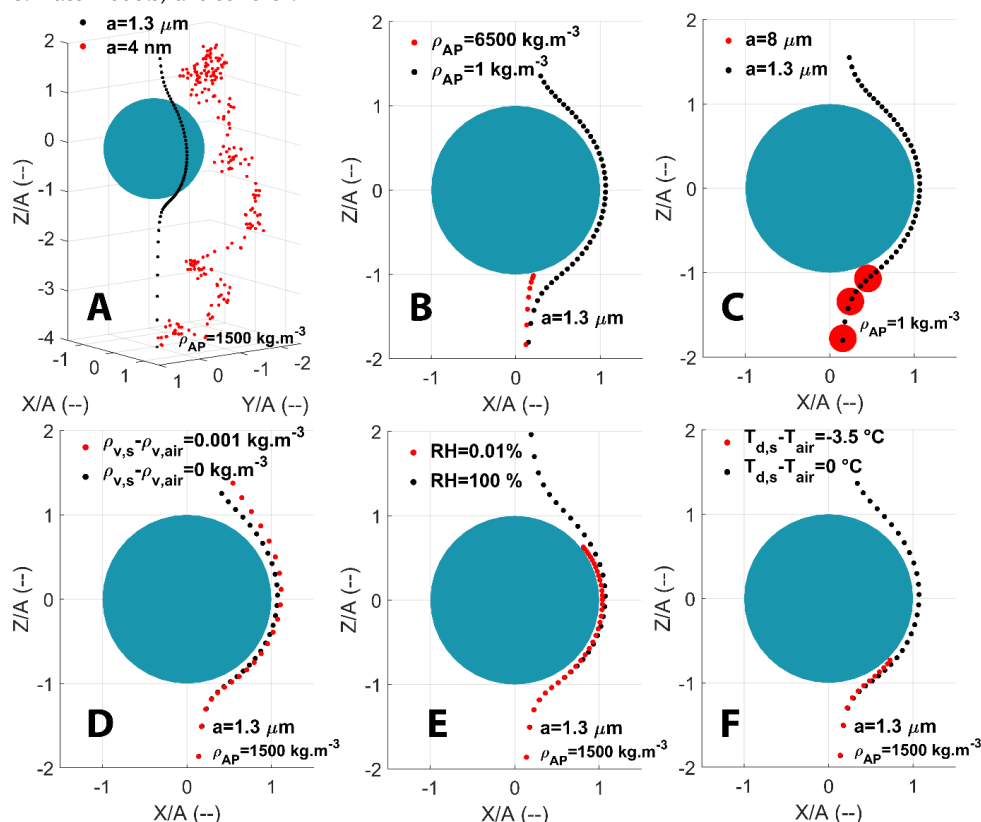




50 deposition. Flossmann (1998) numerically showed that the wet deposition is mainly induced by the
51 in-cloud AP collection since 70 % of the AP mass contained in raindrops reaching the soil comes from
52 the cloud. This result is consistent with the environmental measurements of Laguionie et al. (2014)
53 who evaluated the cloud contribution up to 60 % in the wet AP deposition. The in-cloud AP scavenging
54 is subdivided into two mechanisms - AP activation into cloud hydrometeors and AP collection by
55 clouds hydrometeors. The modelling of the in-cloud AP collection is therefore a fundamental climate,
56 weather and health issue. In most of current AP wet removal models - like DESCAM (Detailed
57 SCAvenging Model, Flossmann, 1985) - the AP collection is described through a microphysical
58 parameter called “collection efficiency” (CE) which quantifies the ability of a droplet to capture the
59 APs present in its surroundings during its fall.
60 Many microphysical effects influence this CE and their contribution is mainly depending on the AP
61 size. To be collected an AP has to leave the streamline that surrounds the falling droplet to make
62 contact with it. The nanometric AP’s motion is affected by the collisions with air molecules - referred
63 as the Brownian diffusion. It results in random movement patterns (see Figure 1, A) which tend to
64 increase the CE when the AP radius decreases. For massive APs, there is an increase of CE as they
65 retain an inertia strong enough to leave the streamline when it curves and to go straight toward the
66 droplet surface - phenomenon called inertial impaction (see Figure 1, B). When considering
67 intermediate AP size, the CE goes through a minimum value called the “Greenfield gap” (Greenfield,
68 1957) where the AP diffusion and inertia are weaker. In this gap, other microphysical effects can be
69 involved to make the droplet encounter the AP like the interception for instance. It is the collection
70 of APs following a streamline that approaches the droplet within a distance equivalent to the particle
71 radii (a) - see Figure 1, C. Note that the electrostatic forces can have a significant influence on the
72 CE (Tinsley and Zhou, 2015; Dépée et al., 2019). This effect will be discussed in a companion paper
73 (Dépée et al., 2020) of this work.
74 There are also thermophoretic and diffusiophoretic effects which can influence the CE. In clouds,
75 they shall favour the CE increase when evaporation occurs and decrease CE during condensation (due
76 to a thermal equilibrium between the droplet and the air). Thermophoresis exists when a thermal
77 gradient prevails between the air and the droplet. When the relative humidity is below 100 %, the
78 evaporating droplet’s surface temperature ($T_{d,s}$) is colder than the bulk air temperature (T_{air}). The
79 average kinetic energy of air molecules is then decreasing when approaching the droplet’s surface.
80 An AP is thus attracted by a thermophoretic force near the evaporating droplet (see Figure 1, F)
81 caused by the asymmetry in kinetic energy transferred during each collision. Diffusiophoresis occurs
82 in an environment where a gradient of vapor density in the air exists such as in the surrounding of an
83 evaporating droplet. In this case, water molecules diffuse toward the surrounding air meanwhile the
84 air molecules diffuse toward the droplet surface. In clouds, since the water molar mass is lower than
85 the air molar mass, there is an asymmetry in the momentum transferred to APs close to the
86 evaporating droplet produced by collisions with the molecules from the continuous phase. This
87 diffusion tends to attract the AP to the droplet. Nonetheless, in order to maintain a constant air
88 pressure at the droplet surface, a hydrodynamical flow directed toward the air is induced - this is
89 the Stefan flow. The hydrodynamical drag induced by the Stefan flow tends to repulse APs from an
90 evaporating droplet. The diffusiophoresis is the force resulting from both air and water vapour
91 diffusion, and the Stefan flow which is on average five times larger than the other two ones
92 (Santachiara et al., 2012). Finally, diffusiophoresis repulses APs from the evaporating droplet (see
93 Figure 1, D), decreasing the CE. Since, the thermophoretic process is on average twice larger than
94 the diffusiophoretic one (Tinsley et al., 2006), APs are ultimately attracted toward droplets in a
95 subsaturated air (see Figure 1, E). The coupling of the thermophoresis and diffusiophoresis entails
96 the CE increase when the relative humidity decreases.
97 The influence of the relative humidity on the CE is described by the well-known Wang et al. (1978)
98 model which is used in many cloud models like DESCAM (Flossmann, 1985). Since their model predicts
99 an important contribution of thermophoresis and diffusiophoresis on the CE for cloud droplet radii
100 ($A < 100 \mu\text{m}$) and submicron AP radii, it is mandatory to validate those theoretical CEs through
101 experiments. A review of available CE measurements can be found in Ardon-Dryer et al. (2015). The
102 only experimental study that tackles the influence of the relative humidity on the CE for cloud
103 droplets is the one of Ardon-Dryer et al. (2015), which tested two levels of relative humidity of 15
104 and 88 %. However, in their work they report that the measured electric charge on the droplets were
105 400 ± 400 elementary charges and on the APs were 1 elementary charge. Therefore, the electrostatic
106 forces should have had a significant influence on the measured CE for the droplet radius considered
107 ($A \approx 21.6 \mu\text{m}$) as numerically shown by Tinsley and Zhou (2015). Furthermore, there are no equivalent
108 measurements for other cloud droplet sizes neither for high levels of relative humidity as found in-
109 cloud.



110 The purpose of this work is to fill up the lack of data. Thus, a novel experiment has been developed
 111 in order to study the influence of the relative humidity on the CE to assess the magnitude of the
 112 thermophoretic and diffusiophoretic processes. With this experiment, the influence of electric
 113 charges can also be investigated and this is the object of a companion paper (Dépée et al., 2020).
 114 In the first section of this paper, the experimental setup is detailed while the experimental method
 115 to evaluate the CE is described in the second one. Finally, the third section is dedicated to the new
 116 CE measurements which are presented and compared to theoretical data from the Wang et al. (1978)
 117 Eulerian model. Another comparison is made in the last section to the newer Lagrangian model of
 118 Dépée et al. (2019) since it can model every microphysical effect involved in the AP collection by
 119 cloud droplets (like Brownian motion, inertial impaction, interception, etc.) and specially their
 120 coupling. As Dépée et al. (2019) are focusing on the electrostatic forces, the thermophoresis and the
 121 diffusiophoresis were not considered. Here, we extend the Dépée et al. (2019) model by adding these
 122 phoretic effects. Finally, this study experimentally validates the Dépée et al. (2019) model which
 123 provides consistent theoretical CEs for a convenient incorporation in cloud models, pollution models,
 124 climate models, and so forth.



125
 126
 127 Figure 1 APs trajectories computed with the extended Dépée et al. (2019) model for a 50 μm droplet
 128 radius (A) and AP with various radii (a) and densities (ρ_{AP}). The air temperature (T_{air}) and the air
 129 pressure (P_{air}) are respectively -17°C and 540 hPa. From Figure 1 A to F, the considered effects are
 130 the Brownian motion (A), the inertial impaction (B), the interception (C), the diffusiophoresis (D),
 131 the coupling of thermophoresis and diffusiophoresis (E) and the thermophoresis (F) are highlighted.
 132 In Figures 1 B, C, E and F - the red trajectories result in an AP collection. In Figure D, the differences
 133 in vapor density in the air at the droplet surface ($\rho_{v,s}$) and in the air ($\rho_{v,air}$), equal to 0 and 0.001 kg.m^{-3} ,
 134 represent an environment with a relative humidity of 100 and 0.01 % respectively. In Figure F, the
 135 differences between the temperature at the droplet surface ($T_{d,s}$) and in the environment (T_{air}),
 136 equal to 0 and to 3.5°C , represent a relative humidity of 100 and 0.01 % respectively.



137 1 EXPERIMENTAL SETUP

138

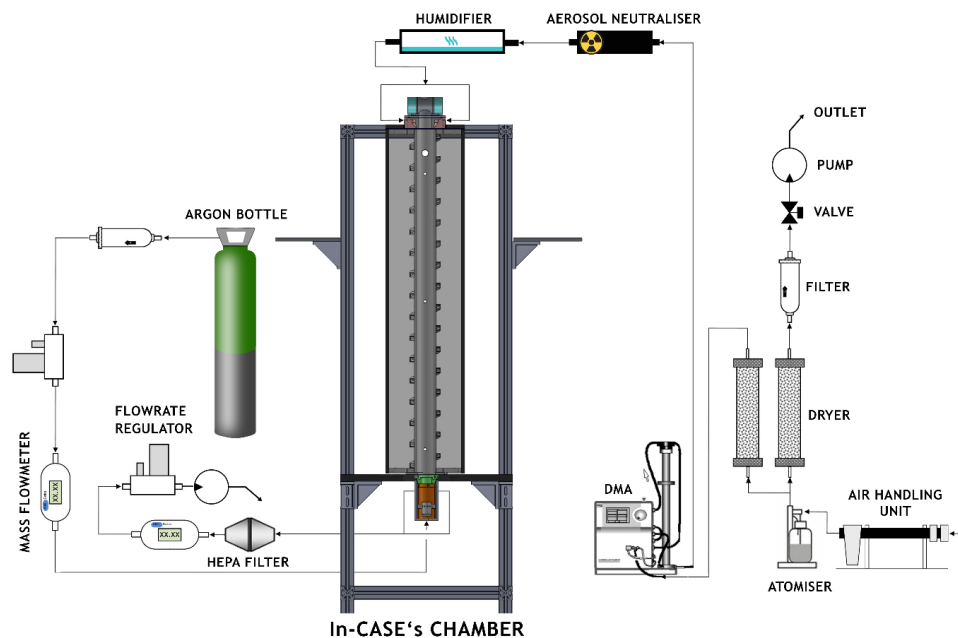
139

1.1 Overview

140 All measurements were conducted inside the In-Cloud Aerosol Scavenging Experiment (In-CASE).
141 Figure 2 shows the airflow diagram with the different parts of the experiment in order to study the
142 relative humidity influence on the CE. Note that this In-CASE setup is quite different from the other
143 configuration regarding the electric charges' influence described in the companion paper (D  p  e et
144 al., 2020). The major In-CASE's part is the collision chamber (Figure 2) where a laminar flow
145 containing APs interacts with a train of droplets falling at terminal velocity. In this chamber, the
146 droplet and AP size distributions are monodispersed and for this particular work the droplet and AP
147 electric charges are neutralised. In Figure 2, the right side of the diagram shows the AP generation
148 which is described in subsection 1.2. On the left side, an Argon flow is injected into the In-CASE
149 chamber's bottom part to separate droplets from the AP flow - this part is detailed in subsection
150 1.4.3.1 - meanwhile the AP flow leaves the chamber toward a High Efficiency Particulate Air (HEPA)
151 filter.

152 The relative humidity in the collision chamber is set through the temperature, this latter being
153 controlled via a cooling system. In the next sections, the droplets and AP characterisation as well as
154 the In-CASE's chamber are detailed.

155



156

157 Figure 2 In-CASE setup to study the influence of relative humidity.

158

159

1.2 AP generation

160

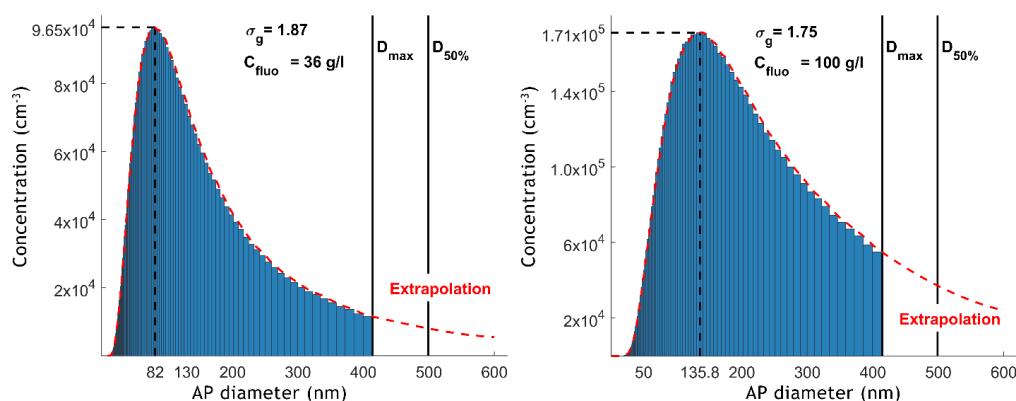
161

162 APs are generated by the atomisation (atomiser, TSI 3076) of a sodium fluorescein salt solution
163 ($C_{20}H_{10}Na_2O_5$). This molecule has been selected for its significant fluorescent properties, detectable
164 at very low concentrations (down to 10^{-10} g/l). Once atomised, the fine droplets go through a dry
165 diffuser to produce dry APs. In Figure 3, two AP size distributions are presented for two different
166 concentrations of the sodium fluorescein salt solution considered - 36 and 100 g/l - during the
167 experiments. Those two size distributions have been evaluated using a Scanning Mobility Particle
168 Sizer (SMPS). It was observed that the size distribution mode passes from 41 to 67.9 nm in radius
169 when the concentration is three times larger. Since the geometric standard deviation (σ_g) is above
170 1.75, a Differential Mobility Analyser (DMA; TSI 3080) is used between the atomiser and the In-CASE's



171 chamber to reduce the dispersion of the AP size distribution. After exiting the DMA, the AP flow goes
172 through a low-energy X-ray neutraliser (< 9.5 keV, TSI 3088) so that the AP charge distribution
173 entering the In-CASE's chamber is similar to a Boltzmann distribution. After the neutralisation, the
174 dry AP flow is humidified by a pure water container in order to get high relative humidity in the
175 collision chamber.
176

177 Note that, the DMA selects APs according to their electrical mobility - Z in equation (6) - assuming
178 that only single charged APs can leave the DMA. Actually, depending on the AP size distribution and
179 the AP flowrate in the DMA, larger AP radii carrying multiple charges than the one considered can
180 also be selected. Sometimes those multiple charged APs cannot be neglected as discussed in section
181 2.2.
182



183
184

185 Figure 3 Two typical AP size distributions obtained with a SMPS at the atomiser's outlet. The
186 concentration of the sodium fluorescein salt solution is 36 g/l (Left) and 100 g/l (Right). D_{max} and
187 $D_{50\%}$ are respectively the maximum diameter selected by the DMA and the cut-off diameter of the
188 impactor at the DMA inlet, at a given AP flowrate (0.6 l/min).
189

190 1.3 Droplet characterisation

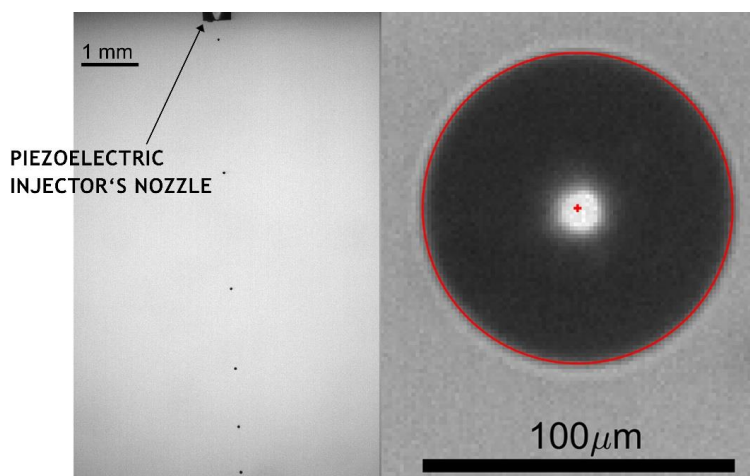
191 1.3.1 Droplet generation frequency and size measurement

192

193

194 The droplet generator used for these experiments is a piezoelectric injector provided by Microfab -
195 the MJ-ABL-01 model with an internal diameter of 150 μm . This model has been used for its stability
196 over time, since the experiments can last up to 5 hours. This piezoelectric injector generates droplets
197 - at a given frequency - above their terminal velocity. The distance between two following droplets
198 reduces when droplets fall away from the injector's nozzle since the droplet velocity decreases (see
199 Figure 4, left). It was highlighted during *ex situ* experiments that droplet generation frequencies
200 greater than 25 Hz induce droplet coalescence since the inter-droplet space becomes too short to
201 prevent droplets from aerodynamically disturbing each other. This agrees with Ardon-Dryer et al.
202 (2015) who observed droplet coalescence for droplet generation frequency larger than 30 Hz
203 operating a similar piezoelectric injector. Thus, droplets were generated at 25 Hz in all experiments
204 presented in this current paper.

205 The droplet generator is placed at the top of the In-CASE's collision chamber, within an injection
206 head (see Figure 6). Few times during an experiment, droplet pictures are recorded by optical
207 shadowgraphy through two facing portholes in the injection head (see Figure 6). A circle Hough
208 transform is then applied to evaluate the droplet radii in the recorded pictures. An example is given
209 in Figure 4 (right) for a 49.7 μm droplet radius. Note that the size distributions of the droplets
210 generated by the piezoelectric injector are considered monodispersed since the droplet size
211 dispersion is very low ($\sigma \sim 1\%$).
212
213
214



215
216 Figure 4 (Left) Droplet train at the piezoelectric injector's outlet obtained by optical shadowgraphy
217 - the droplet generating frequency is 200 Hz. (Right) A droplet picture obtained by optical
218 shadowgraphy - the droplet radius and centre are detected thanks to a circle Hough transform (red
219 cross and line).

220 221 1.3.2 Droplet charge neutralisation

222
223 It is well-known that the piezoelectric droplet generator produces highly electrically charged droplets.
224 With a similar device, Ardon-Dryer et al. (2015) measured up to 10^4 elementary charges on the
225 generated droplets. Since this paper focused only on the relative humidity influence, the droplets,
226 as well as APs, must be neutralised.

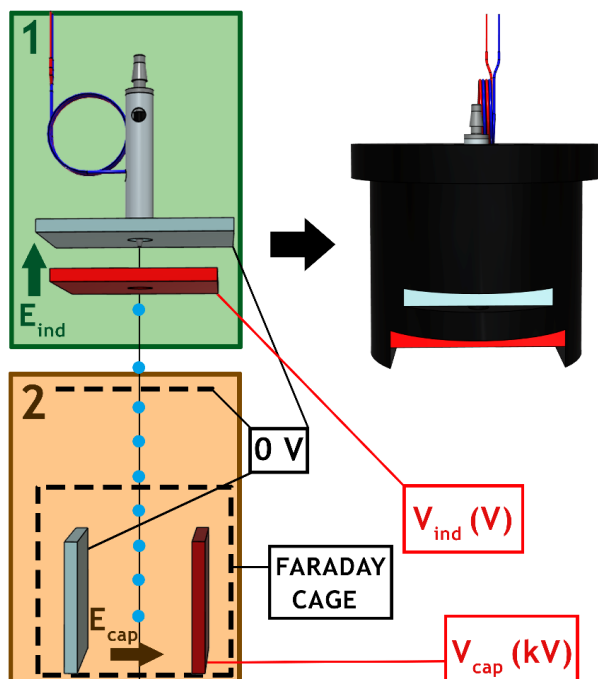
227 To do so, an electrostatic inductor was built following Reischl et al. (1977). Two parallel metal plate
228 are placed at the droplet generator's nozzle - this is the electrostatic inductor shown in Figure 5
229 (labelled 1, left). One plate is connected to a potential (V_{ind}) while the other is connected to the
230 neutral potential - as presented in Figure 5 - in order to induce an electric field ($E_{ind} \sim 10^2\text{-}10^3$ V/m).
231 Sodium chloride is added to the pure water that feeds the piezoelectric injector. According to the
232 generated electric field polarity, the system can selectively attract negative or positive ions toward
233 the nozzle where the droplet is formed. If V_{ind} is positive, the negative chloride ions (Cl^-) migrate
234 toward the nozzle and the positive sodium ions (Na^+) are repulsed from the nozzle and inversely if
235 the potential is negative. Following the electric field amplitude - through V_{ind} - the ion quantity can
236 be set. This system can conclusively control the droplet charge. Note that the sodium chloride
237 concentration has no effect on the principle of induction used here since the ion number is large
238 enough for the entire experiment period (Reischl et al., 1977) - 3.3 g/l has been considered.

239 To evaluate the droplet charge and then, neutralise the droplets, an *ex situ* experiment has been
240 conducted where the droplet train passed through a capacitor (labelled 2, Figure 5, left). One
241 capacitor's plate is connected to the neutral whereas the other is connected to a high potential (V_{cap})
242 - inducing an electric field ($E_{cap} \sim 10^5\text{-}10^6$ V/m). A Faraday cage surrounding the capacitor and a plate
243 maintained at a neutral potential are set in order to prevent the electric field at the capacitor (E_{cap})
244 from disturbing the electric field at the inductor (E_{ind}) which could change the droplet charge.
245 Finally, the potential V_{ind} which electrically neutralises the droplet is found by selecting for the V_{ind}
246 value which minimises the droplet train deflection.

247 Actually, this system can also be used to precisely evaluate the electric charges on the droplets (for
248 both polarities), this method is applied and presented in Dépée et al. 2020.

249 Note that, the droplet charge induced by the piezoelectric injector has been calculated to
250 -8,400 elementary charges - in line with Ardon-Dryer et al. (2015) using a similar generator. Moreover,
251 after the droplet neutralisation, an uncertainty of 600 elementary charges was evaluated.

252



253

254

255 Figure 5 (Left) 1 - Electrostatic inductor set at the piezoelectric injector's nozzle to electrically

256 neutralise the droplets. 2 - Capacitor used to check the droplet deviation caused by the electric field

257 in the capacitor (E_{cap}). (Right) 3D printing containing the piezoelectric injector and the electrostatic

258 inductor, set in the injection head (see Figure 6).

259

260 1.4 In-CASE chamber

261

262 The In-CASE chamber (see Figure 2) is subdivided into three stages - the injection head, the collision

263 chamber and the In-CASE chamber's bottom part. These three parts will be detailed in the next

264 subsections.

265

266 1.4.1 Injection head

267

268 The injection head is composed of two parts - the droplets and the APs injection. The upper part is

269 used to inject the droplets while the APs are inserted in the second part about 10 cm below. This

270 distance is required to measure the droplet size through the two facing portholes (see section 1.3.1)

271 but also to let droplets decelerate and reach their terminal velocity.

272 The droplet train is injected through a 3D printing set at the top of the droplet injector (see Figure 6).

273 This 3D printing has been constructed to precisely place the droplet generator and the electrostatic

274 inductor together (see Figure 5, right). Indeed, the electrostatic inductor has to keep the same

275 position relative to the droplet generator to prevent changes in the electric field E_{ind} which in turn,

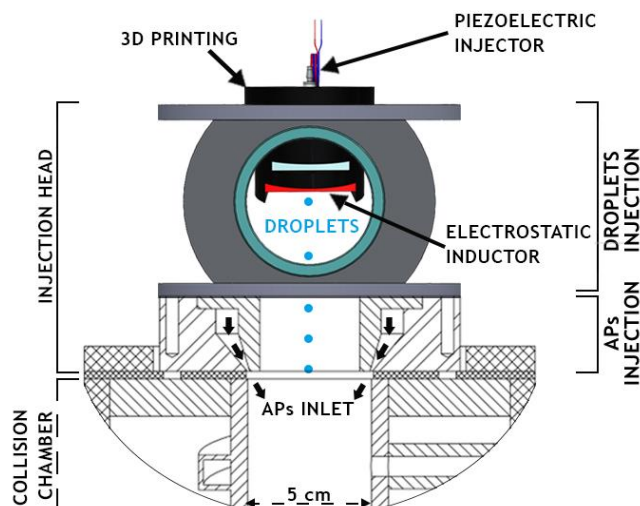
276 can disturb the droplet charge and stop the neutralisation.

277 The APs are inserted from the sides of the entire circumference through a kind of flat torus. This

278 injection principle is based on the CLINCH experiment (CoLision Ice Nucleation Chamber, Ladino et

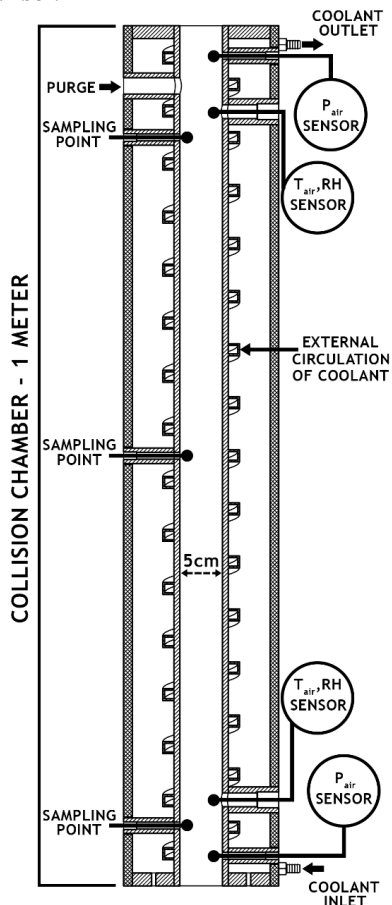
279 al., 2011) which ensures a laminar flow and a great spatial APs mixture in the collision chamber inlet.

280



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283

Figure 6 View of the In-CASE chamber's top with the injection head where APs and droplets are injected into the collision chamber.



284
285

Figure 7 In-CASE collision chamber - 2D section plane.



286 1.4.2 Collision chamber

287

288 The collision chamber is a one-meter stainless steel cylinder with an inner diameter of 5 cm (see
289 Figure 7). The collision chamber's temperature is controlled through a coolant which spirally
290 circulates outside the chamber, from the bottom to the top of the collision chamber. The pressure
291 (P_{air}), temperature (T_{air}) and relative humidity (RH) are measured at the top and the bottom by
292 sensors. To clean the chamber, water or compressed dried air are injected via a purge. Three
293 sampling points are available but were not used for these experiments.

294 The temperature and the relative humidity discrepancies between top and bottom were respectively
295 less than 1 °C and 4 % in all the CE measurements - the mean values are then considered for the both
296 parameters.

297

298 1.4.2.1 Thermodynamic conditions

299

300 All the experiments were conducted at atmospheric pressure. To get comparable CE measurements,
301 the temperature has been set to 0.58 ± 0.50 °C - as constant as possible between experiments. Three
302 levels of relative humidity (RH) were considered - 71.1, 82.4 and 93.5 %. To increase the relative
303 humidity at a given collision chamber temperature, the temperature of the pure water in the
304 humidifier (Figure 2) was increased. The relative humidity level of 71.1 % was obtained by completely
305 removing the humidifier to get the driest AP flow possible at the collision chamber inlet. At lab
306 temperature (about 22 °C), the relative humidity of the dry AP flow ranged from 10 to 20 % at the In-
307 CASE's chamber inlet.

308 Note that the AP flow before the injection head is also thermally set to inject APs with the same
309 temperature as in the collision chamber.

310

311 1.4.2.2 Droplet evaporation

312

313 The change in droplet radius due to vaporisation in the collision chamber is calculated according to
314 the section 13.2 of Pruppacher and Klett (1997). The corresponding terminal velocity is computed
315 from Beard (1976). The residence time of the droplet in the chamber is computed considering these
316 two changes. Since the droplet radius only decreases around 3 % by evaporation with the lower
317 relative humidity considered in the experiments (71.1 %), the droplet evaporation in the collision
318 chamber is neglected.

319

320 1.4.2.3 AP hygroscopicity

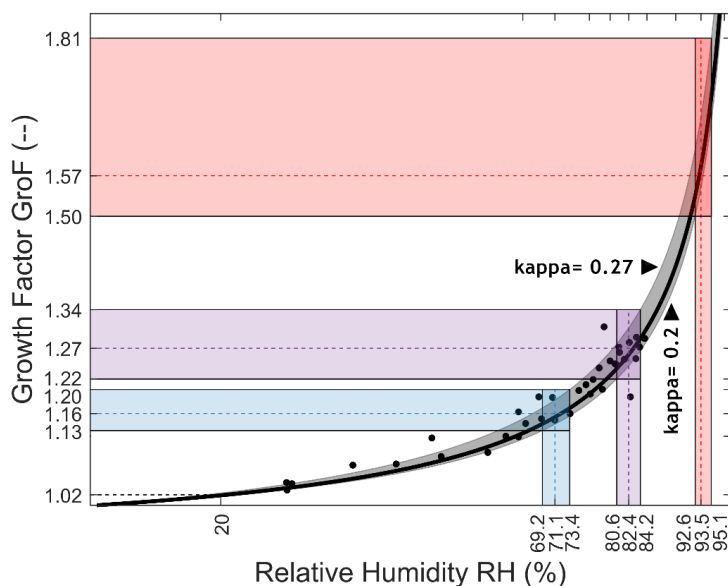
321

322 The APs are composed of pure sodium fluorescein salt which is a high hygroscopic chemical
323 compound. The APs inside the collision chamber then grow to reach their equilibrium size with the
324 relative humidity (RH). In order to evaluate the increase of size by humidification, the AP growth
325 factor ($GroF$) measured in Qu  rel et al. (2014) was considered. The growth factor is defined as the
326 ratio of the size of the humid AP over the size of the dry AP. Since their data are limited to relative
327 humidity levels below 90 %, the kappa-theory described in Petters and Kreidenweis (2007) is used to
328 extrapolate to the required values. To fit the measurements of Qu  rel et al. (2014) with the kappa-
329 theory, only their data with a relative humidity level less than 85 % were considered. Figure 8 shows
330 the AP growth factor related to the relative humidity for a kappa value of 0.23 and two extreme
331 values of 0.2 and 0.27 - fitting to the sodium fluorescein salt hygroscopicity.

332 Thus, for relative humidity levels of 71.1 %, 82.4 % and 93.5 % studied here, a dry AP radius of 50 nm
333 selected by the DMA grows with a growth factor ($GroF$) of 1.16, 1.27 and 1.57, respectively.
334 Consequently, the CE measured are applied for size of respectively 58.0, 63.5 and 78.5 nm AP radii.
335 Note that the AP density is not the one of sodium fluorescein salt ($\rho_{fluorescein} = 1580$ kg.m⁻³) since
336 APs contain water. Indeed, the water density (ρ_{water}) should be considered in the AP density (ρ_p)
337 calculation. At a given relative humidity (RH), the AP density inside the chamber is then deduced by
338 the equation (1):

$$\rho_p(RH) = \frac{\rho_{fluorescein} + \rho_{water} \times [GroF(RH)^3 - 1]}{GroF(RH)^3} \quad (1)$$

339 Since the relative humidity after the dryer (see Figure 2) ranges from 10 to 20 %, the AP growth factor
340 is less than 1.02 (see Figure 8) in the DMA. APs are then considered dry when exiting the DMA.



341
342

343 Figure 8 Growth factor ($GroF$) as function of the given relative humidity (RH). Data points (dots)
344 from Qu  rel et al. (2014) and fittings (lines) with the kappa-theory (Petters and Kreidenweis, 2007).
345

346 1.4.3 In-CASE's bottom stage

347

348 The CE is calculated from the AP mass collected by the droplets during an experiment and the average
349 AP mass concentration in the collision chamber. To obtain these quantities, the droplet train must
350 be separated from the interstitial APs (which were not collected).

351

352 1.4.3.1 APs and droplets separation

353

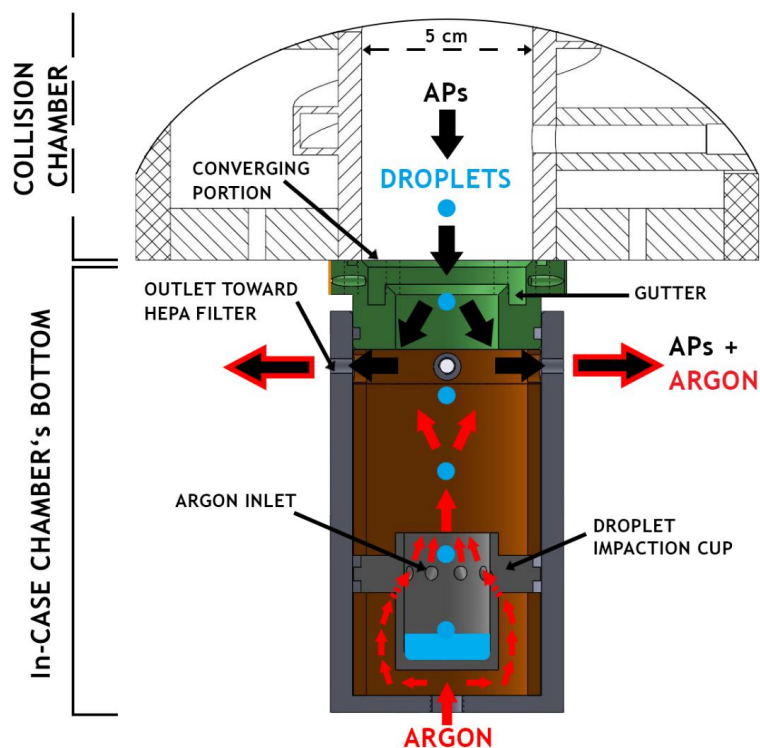
354 The system developed to separate the droplet train from the AP flow is presented in Figure 9. It is
355 composed of a converging portion (from 5 to 3 cm in diameter) where a gutter is inserted to prevent
356 the water condensed on the wall from entering to the In-CASE's chamber bottom. The APs are directly
357 vacuumed toward a HEPA filter (see Figure 2) at the upper part of the separator through four outlets
358 while the droplets - containing collected APs - are impacted into a cup at the separator's lower part.
359 To prevent AP pollution in the droplet impaction cup, a counter-flow is injected below the In-CASE's
360 chamber and passes through the droplet impaction cup from nine holes set on its entire
361 circumference. Since the counter-flow is injected at the laboratory temperature and the APs
362 downward flow is colder, Argon - denser than the air - was selected to avoid any Rayleigh-Taylor
363 instability (Sharp, 1983).

364

365 Argon is injected at 0.4 l/min. The diameter of the nine holes is 4 mm and the top of the droplet
366 impaction cup is 2.5 cm. Thus, the upward Argon flow is injected at 5.9 and 1.4 cm/s, through the
367 nine holes and the top of the impaction cup, respectively. Because the droplet velocity is about 25
368 cm/s (for the 50 μm droplet radius studied) and the AP terminal velocity is about 10^{-2} cm/s, APs can
369 not settle into the impaction cup whereas droplets are impacted without undue disruption.

370

371



372
373 Figure 9 View of the In-CASE chamber's bottom - APs and droplets separation.
374
375

376
377 1.4.3.2 Validation
378

379 The droplets and APs separation were verified with two tests. First, In-CASE was run under usual
380 experimental conditions except no droplets were generated. After five hours of experiment, a
381 spectrometry analysis was performed in the droplet impactation cup and no fluorescein was detected.
382 Thus, no AP had settled on the droplet impactation cup during the experiment.

383 The second test was to ensure that droplets were collected by the impactation cup. Then, In-CASE was
384 again run like a typical experiment except the flow passing through the In-CASE chamber was clean
385 air without any AP. Droplets were tracked by adding sodium fluorescein salt in the water supplying
386 the piezoelectric injector. Since the concentration of sodium fluorescein salt in the water, the
387 droplet generation frequency, the droplet size and the experiment time were known, the goal was
388 to check if the expected fluorescein mass in the droplets and the actual measured fluorescein mass
389 were equal. After five hours (= 450,000 injected droplets), a discrepancy of 2 % between expected
390 and measured fluorescein mass was obtained. Therefore, all droplets are considered impacted in the
391 impactation cup.

392 Finally, this indicates that the AP mass detected in the droplet impactation cup after an experiment
393 results effectively from scavenging events in the In-CASE collision chamber.
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403 2 DATA ANALYSIS

404

405 2.1 Definition of the collection efficiency

406

407 At the end of an experiment, the collection efficiency (CE) is calculated from the equation (2):

$$CE(a, A, HR) = \frac{m_{AP,d}}{m_{AP,available}} \quad (2)$$

408 Where the AP mass collected by all droplets ($m_{AP,d}$) is directly measured by spectrometry analysis in
409 the droplet impaction cup (see Figure 9) while the mass of available APs in the volume swept by the
410 droplets ($m_{AP,available}$) is given by the equation (3) :

$$m_{AP,available} = \pi(A + GroF(RH) \times a)^2 \times F_d \times \Delta t \times H_{eff} \times C_{m,AP} \quad (3)$$

411 F_d and Δt are respectively the droplet generation frequency and the experiment duration - the
412 product of those two quantities is the number of droplets injected during an experiment. Note that
413 a is the AP dry radius corrected by the growth factor ($GroF$) which depends on the relative humidity
414 (see section 1.4.2.3). H_{eff} is the effective height of interaction between droplets and APs. Since the
415 APs are also falling in the In-CASE collision chamber, this height is not the In-CASE collision chamber's
416 height ($H_{In-CASE}$) but is equal to the equation (4):

$$H_{eff} = \frac{U_{A,\infty}}{U_{A,\infty} + V_Q} H_{In-CASE} \quad (4)$$

417 However, as the droplet terminal velocity ($U_{A,\infty}$) is about 25 cm/s and the maximum AP flow velocity
418 (V_Q) considered in the In-CASE collision chamber during the experiment is 5 mm/s (for an AP flowrate
419 of 0.6 l/min), these both heights are thus considered equal ($H_{eff} \sim H_{In-CASE}$).

420

421 In equation (3), $C_{m,AP}$ is the mean AP mass concentration in the In-CASE collision chamber, estimated
422 from the fluorescence spectrometry analysis of the HEPA filter though the equation (5):

$$C_{m,AP} = \frac{m_{AP,tot}}{\Delta t \times Q_{In-CASE,c}} \quad (5)$$

423 $Q_{In-CASE,c}$ is the AP flowrate within the In-CASE collision chamber.

424

425

426

427

428 2.2 DMA selection - multiple charged AP's principle

429

430 As previously stated, the AP flow travels through a DMA to select the particles according to their
431 electrical mobility (Z) which is defined by the equation (6):

$$Z = \frac{n e C_u}{6 \pi \eta_{air} a} \quad (6)$$

432 Where n , C_u , η_{air} are respectively the number of elementary charge (e), the Cunningham correction
433 coefficient and the air dynamic viscosity (expressed here in poise).

434

435 Thus, for an AP radius selected by the DMA, all particles with the same $\frac{n C_u}{a}$ ratio are actually
436 selected. For example, when an AP with a radius of 50 nm is selected (single charged), the AP radii
437 of 75.8 nm (double charged) and 98.2 nm (triple charged) will also be selected and progress into the
438 In-CASE collision chamber since they have the same electrical mobility. In this paper, "multiple
439 charged APs" are referred as the APs with the same electrical mobility as the ones (single charged)
440 selected by the DMA.

441



442 At the DMA inlet, an aerodynamic impactor is placed to prevent the heaviest APs from entering into
443 the DMA. Thus, for a given AP flowrate in the DMA, the multiple charged APs can be impacted at the
444 DMA inlet and can then be neglected at the DMA outlet. To evaluate this case, the cut-off radius of
445 the impactor at the DMA inlet must be considered (referred as $D_{50\%}/2$). This radius is defined as the
446 one where 50 % of the APs are impacted. The Table 1 shows this parameter for every AP flowrate
447 used during the experiment and for a given selected AP radius. The double charged AP radius with
448 the same electrical mobility as the selected AP radius (single charged) is also indicated - when this
449 latter size is large enough compared to the cut-off radius, it is assumed that there is no contribution
450 of the multiple charged APs in the CE measurement. This is the case for a selected AP radius of 200
451 or 250 nm where the AP size distribution at the DMA outlet can be considered purely monodispersed.

452
453 However, for a selected AP radius of 50 or 150 nm, according to Table 1, the multiple charged AP
454 radii cannot be neglected. Different experiments were run to perform a deconvolution of their
455 respective contributions in the final CE calculation. This method is presented in Appendix A.

456
457

Table 1 AP selection parameters

Selected AP radius by the DMA (single charged)	Double charged AP radius with the same electrical mobility	AP flowrate in the DMA	Cut-off radius of the impactor at the DMA inlet ($D_{50\%}/2$)
50 nm	75.8 nm	0.6 l/min	213 nm
150 nm	253.7 nm	0.6 l/min	213 nm
200 nm	348.3 nm	0.6 l/min	213 nm
250 nm	444.3 nm	0.4 l/min	268.5 nm

458
459

460 2.3 Uncertainty evaluations

461
462

463 2.3.1 AP radius uncertainty

464
465

466 The first AP radius uncertainty is related to the AP selection by the DMA. Nevertheless, this
467 uncertainty has been neglected since the spectral bandwidth of the DMA is quite small compared to
468 the AP radius uncertainty addressed below.

469
470

471 Indeed, the only significant AP radius uncertainty results from the effective AP radius inside the In-
472 CASE collision chamber due to the hygroscopicity of the APs. For the relative humidity levels studied
473 (71.1, 82.4 or 93.5 %), the extreme relative humidity levels measured in all experiments are
474 considered - for 71.1 %, the minimum and maximum values are 69.2 % and 73.4 %, respectively. As a
475 reminder, the kappa-value is assumed from the Qu  rel et al. (2014) data and ranges from 0.2 to 0.27
476 (see Figure 8). The low uncertainty for the AP radius is then evaluated by considering the minimum
477 growth factor ($GroF$) in Figure 8 for the lower level of relative humidity measured and the lower
478 kappa value determined - respectively 69.2 % and 0.2. Similarly, for the same example ($RH= 71.1$ %),
479 the high uncertainty for the AP radius is estimated by evaluating the maximum growth factor - for
480 the maximum level of relative humidity observed and the maximum kappa value assumed -
481 respectively 73.4 % and 0.27. In this example, for a dry AP radius of 50 nm selected by the DMA, its
482 wet radius in the In-CASE collision chamber is likely to be 58 nm ($GroF= 1.16$) ranging from 56.5 nm
483 ($GroF= 1.13$) to 60 nm ($GroF= 1.20$) resulting from the respective low and high uncertainties.

484
485

486 2.3.2 Uncertainty of the collection efficiency

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488

489 Since the method of CE evaluation differs in the presence of multiple charged APs, the uncertainty
490 calculation is also different depending on the situations. The method is described in the Appendix B.

491
492

493 When there are no multiple charged APs in the AP flow, the CE is directly estimated through the
494 equation (3) which can be rewritten as the equation (7):



$$CE(a, A, RH) = \frac{m_{AP,d}}{\pi(A+a)^2 \times N_d \times H_{eff} \times C_{m,AP}} \approx \frac{m_{AP,d}}{\pi A^2 \times N_d \times H_{In-CASE} \times C_{m,AP}} \quad (7)$$

488
 489 Where N_d is the number of injected droplets during the experiment. The relative CE uncertainty (u_{CE})
 490 is then evaluated according to Lira (2003) and summarised by the equation (8):
 491

$$u_{CE} = \sqrt{u_A^2 + u_{H_{In-CASE}}^2 + u_{N_d}^2 + u_{m_{AP,d}}^2 + u_{C_{m,AP}}^2} \quad (8)$$

492
 493 With:

- 494 • The relative uncertainty related to the droplet radius measurement (u_A) which is the ratio
 495 between the standard-deviation and the mean droplet radius on 200 pictures obtained by
 496 optical shadowgraphy. This relative uncertainty is about 1 %;
- 497 • The relative uncertainty of the In-CASE collision chamber's height ($u_{H_{In-CASE}}$) which is 1 %;
- 498 • The relative uncertainty of the number of droplets (u_{N_d}) which can be correlated to the
 499 droplet number effectively impacted on the droplet impaction cup. This relative uncertainty
 500 was evaluated during the validation of APs and droplet train separation (section 1.4.3.2) and
 501 is about 2 %;
- 502 • The relative uncertainty of the detected AP mass in the droplet impaction cup ($u_{m_{AP,d}}$) which
 503 takes into account the relative uncertainty related to the spectrometry analysis ($u_{fluorimeter}$)
 504 and the one caused by the dilution ($u_{dilution}$) - equation (9). Indeed, at the end of an
 505 experiment the water contained in the droplet impaction cup is dried and the residual AP
 506 mass is then dissolved in 2 ml volume of ammonia water.

$$u_{m_{AP,d}} = \sqrt{u_{fluorimeter}^2 + u_{dilution}^2} \quad (9)$$

- 507 $u_{dilution}$ is estimated at 1 % meanwhile $u_{fluorimeter}$ is the main source of uncertainty. In fact,
 508 when the mass of AP collected by the droplet is close to the detection limit of the fluorimeter
 509 (about 10^{-15} kg in the droplet sample volume analyzed), $u_{fluorimeter}$ is up to 30 %.
- 510 • The relative uncertainty of the mean AP mass concentration in the In-CASE collision chamber
 511 ($u_{C_{m,AP}}$) which can be evaluated, according to the equation (5), by the equation (10):

$$\begin{cases} u_{C_{m,AP}} = \sqrt{u_{m_{AP,tot}}^2 + u_{Q_{In-CASE,c}}^2 + u_{\Delta t}^2} \approx \sqrt{u_{m_{AP,tot}}^2 + u_{Q_{In-CASE,c}}^2} \\ u_{m_{AP,tot}} = \sqrt{u_{fluorimeter}^2 + u_{dilution}^2} \end{cases} \quad (10)$$

512 Where the relative uncertainty of the detected AP mass on the HEPA filter ($u_{m_{AP,tot}}$) depends
 513 on the one on the fluorimeter ($u_{fluorimeter}$) and the one on the dilution ($u_{dilution} \sim 1\%$). In fact,
 514 the spectrometry analysis is performed by diluting the AP mass on the HEPA filter in a 100 ml
 515 ammonia water solution at the end of an experiment. The relative uncertainty of the AP
 516 flowrate in the In-CASE collision chamber ($u_{Q_{In-CASE,c}}$) is given by the datasheet of the
 517 constructor - about 1 %. Note that the relative uncertainty on the experiment time ($u_{\Delta t}$) is
 518 neglected since the error is approximately one second on a experiment that can last more
 519 than 5 hours.

522 3 RESULTS AND DISCUSSIONS

523 3.1 Extension of the Dépée et al. (2019) model

524
 525 In all experiments, the droplet charge is 0 ± 600 elementary charges with a radius of about 50 μm .
 526 Since the AP charge distribution is similar to a Boltzmann distribution, an AP charge of more than
 527 5 elementary charges is thus highly unlikely. Consequently, it is assumed that the contribution of the
 528 electrostatic forces on the CE is of second order and these effects were then neglected. Indeed,
 529 Dépée et al. (2019) numerically evaluated the contribution of the electrostatic forces on the CE for
 530



531 a droplet of 50 μm radius with 1000 elementary charges and 5 elementary charges on the AP. For
 532 these extreme values, they shown that the electrostatic forces increase the CE by a maximum of 42 %
 533 in the AP size range considered during the experiments (actually for an AP radius of 50 nm where the
 534 electrical mobility is the largest).

535
 536 To extend the Dépée et al. (2019) model for the thermophoretic (F_{th}) and diffusiophoretic forces
 537 (F_{df}), the resulting velocity at the AP location ($U_{f@p^*}$) given by the authors (in Equation 6) is replaced
 538 by the equation (11):

$$U_{f@AP}^*(t) = U_{f@AP}(t) + \frac{\tau_p}{m_p} (F_{buoy} + F_{df} + F_{th}) \quad (11)$$

539 Where all the terms are defined in Dépée et al. (2019), except the thermophoresis and the
 540 diffusiophoresis which are given by Brock (1962) and Waldmann and Schmitt (1966), respectively,
 541 summarised in the Equations (12):

$$\begin{cases} F_{df} = -6\pi\eta_{air}a \frac{0,74D_vM_{air}}{C_uM_{water}\rho_{air}} \times \frac{\textcircled{1}}{Ar^{*2}} f_v \mathbf{u}_r \\ F_{th} = -\frac{12\pi\eta_{air}a}{5P_{air}} \frac{(k_{air} + 2,5k_{AP}K_n)k_{air}}{(1 + 3K_n)(2k_{air} + k_{AP} + 5k_{AP}K_n)} \times \frac{\textcircled{2}}{Ar^{*2}} (T_{air} - T_{d,s})f_h \mathbf{u}_r \end{cases} \quad (12)$$

542 With \mathbf{u}_r - the unit vector in the radial direction from the droplet centre to the AP centre, r^* - the
 543 distance between the AP and droplet centres normalised by the droplet radius A , D_v - the diffusivity
 544 of vapor, K_n - the Knudsen number, M_{air} and M_{water} - the respective air and water molar masses, k_{air}
 545 and k_{AP} - the respective air and AP thermal conductivities. Note that the thermal conductivity of the
 546 sodium fluorescein salt is considered for k_{AP} - equal to 0.43 $\text{m.kg.s}^{-3}.\text{K}^{-1}$ (Al-Azzawi et Owen, 1984).

547
 548 In equations (12), the terms $\textcircled{1}$ and $\textcircled{2}$ represent the gradient of vapor density in the air and the
 549 thermal gradient, respectively. These two gradients are computed under the assumption that the
 550 temperature and vapor density profiles are spherically symmetric around the droplet (Wang et al.,
 551 1978). Because the droplet is falling in the air, f_v and f_h - which are the ventilation coefficient for
 552 the vapor and the heat respectively (Beard and Pruppacher, 1971) - correct the gradients since the
 553 profiles are actually disturbed by the airflow.

554
 555

3.2 Collection efficiency measurements and analysis

556
 557 In Figure 9, the CEs are presented for the three levels of relative humidity studied - 71.1, 82.4 and
 558 93.5 % - and 6 dry AP radii ranging from 50 to 250 nm. As a reminder, all experiments were conducted
 559 with an air temperature of $0.58 \pm 0.50^\circ\text{C}$ at the atmospheric pressure, the AP charge distribution is
 560 similar to a Boltzmann distribution and the droplet charge is 0 ± 600 elementary charges. The droplet
 561 radius is $49.6 \pm 1.3 \mu\text{m}$. Note that the experimental conditions vary a little for the CE measurements
 562 at a given relative humidity level. On figure 9, the measurements are compared to computed
 563 efficiencies using the models described in Wang et al. (1978) (bottom) as well as the extended version
 564 of Dépée et al. (2019) (top). The envelopes are computed by considering the extreme conditions in
 565 all experiments - the droplet radius A , the relative humidity RH , the air temperature T_{air} -
 566 maximizing (dashed line) and minimizing (dotted line) the CE and the mean conditions (solid line).
 567 The experimental conditions presented in Figure 9 are summarised in Table 2. The wet AP radii are
 568 evaluated with the mean experimental conditions as well as the AP density (ρ_{AP}) which is calculated
 569 with (1). The CE measurements are summarised in Table 3.

570
 571 Regarding the experimental results, it can be noted that the influence of the relative humidity via
 572 the thermophoresis and diffusiophoresis contribution on the CE is of first order. For the larger AP
 573 radii studied, the CE increases by a factor of 4 when the relative humidity passes from 93.5 to 71.1 %
 574 - filling up the Greenfield gap as the models predicts. A slight decline of the contribution of these
 575 two phoretic effects is observed when the AP radius decreases - the previous factor of 4 reducing to
 576 a factor of 3 for the smaller AP radii and for the same relative humidity range (from 93.5 to 71.1 %).
 577 Although this decrease is weak, it is in line with the theory. Indeed, when the AP radius decreases
 578 the contribution of the Brownian motion on the CE increases and starts dominating the
 579



580 thermophoretic and the diffusiophoretic forces. Consequently, the influence of the relative humidity
 581 on the CE is negligible for nanometric AP radii.
 582 Moreover, the impact of the AP size is lower than the influence of the relative humidity for the
 583 experimental conditions considered. Indeed, between the larger and the smaller AP radii, the CE is
 584 only increased by a factor of 1.61, 1.59 and 2.03 for the respective relative humidity levels of 71.1,
 585 82.4 and 93.5 %. A decrease of the AP size effect on the CE is noticeable when the thermophoresis
 586 and the diffusiophoresis contributions intensify - in other words when the relative humidity declines.
 587 This observation is in line with the modelling of the CE when a threshold is more and more visible as
 588 the relative humidity decreases, for the submicron AP radii studied.
 589 Finally, for the AP sizes and the droplet radius studied, both models describe relatively well the
 590 observed CE variations when changing relative humidity. For the two lowest levels of relative
 591 humidity (71.1 and 82.4 %), the CE modelling is really close between both models since the
 592 thermophoresis and diffusiophoresis dominate the influence on the CE. Nevertheless, some significant
 593 discrepancies appear for the highest relative humidity (93.5 %), where the Dépée et al. (2019)
 594 extended model gives higher CE values. These differences result from the Wang et al. (1978) model
 595 which does not consider dynamic effects such as AP inertia, AP weight and interception, in contrast
 596 to the extended model of Dépée et al. (2019) which offers a complete description of the
 597 microphysical effects involved in-cloud.
 598
 599

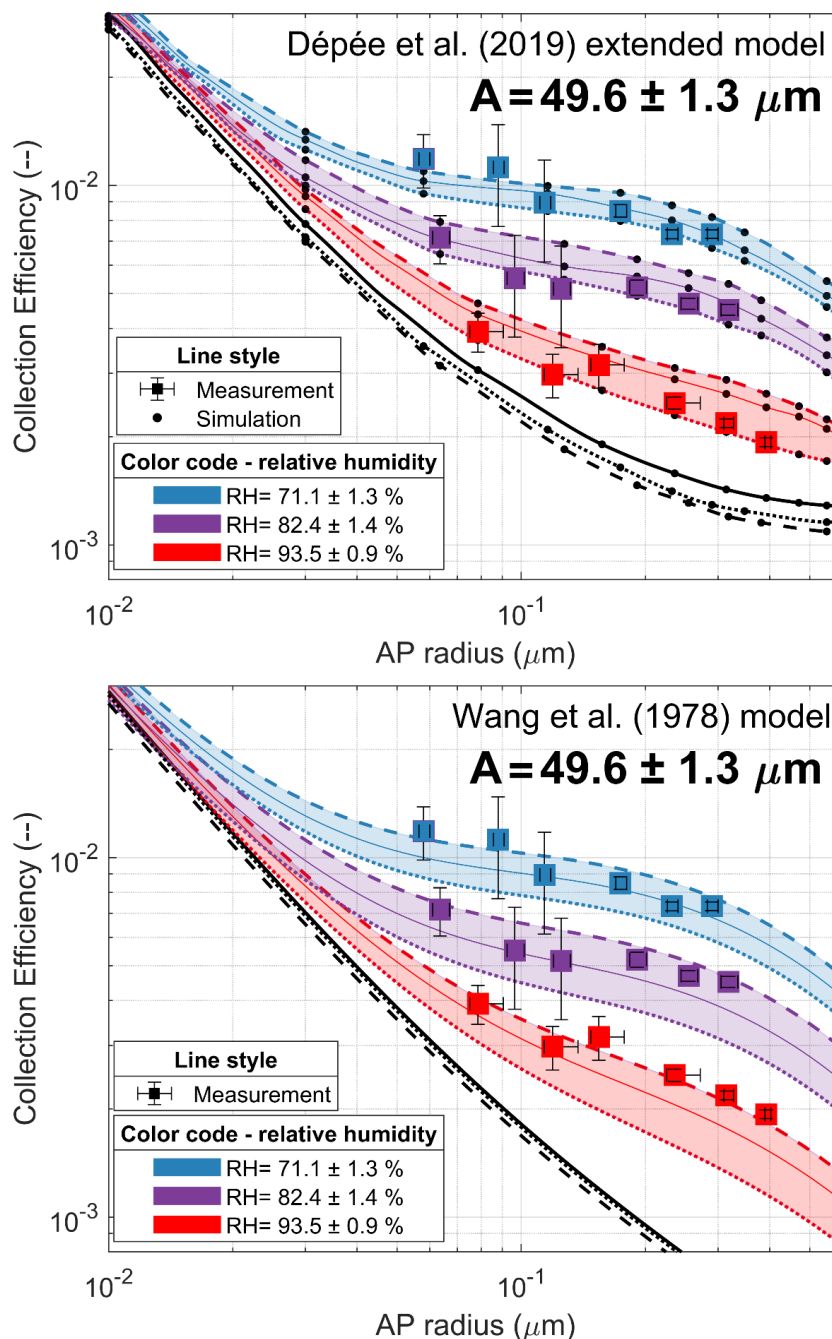
600 Table 2 Mean experimental conditions (solid line) and extreme experimental conditions maximizing
 601 (dashed line) and minimizing (dotted line) the CE.

Line style	$A(\mu\text{m})$	$RH(\%)$	$T(^{\circ}\text{C})$	$\rho_{AP}(\text{kg}\cdot\text{m}^{-3})$
.....	50.4	95.1	0.75	1150
————	48.8	93.5	1.20	1150
- - - - -	47.6	92.6	1.60	1150
————	48.8	100.0	1.20	1150
.....	53.0	84.2	0.03	1282
————	50.8	82.4	0.27	1282
- - - - -	48.6	80.6	0.59	1282
- - - - -	50.8	100.0	0.27	1282
.....	50.6	73.4	0.14	1372
————	49.3	71.1	0.27	1372
- - - - -	48.0	69.2	0.37	1372
.....	49.3	100.0	0.27	1372

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Table 3 CE measurements for the three levels of relative humidity (RH) and the wet AP radii (a).
 The droplet radius is $49.6 \pm 1.3 \mu\text{m}$.

$RH = 93.5 \%$		$RH = 82.4 \%$		$RH = 71.1 \%$	
a (nm)	CE (—)	a (nm)	CE (—)	a (nm)	CE (—)
79	3.92×10^{-3}	64	7.15×10^{-3}	58	1.18×10^{-2}
119	2.98×10^{-3}	96	5.52×10^{-3}	88	1.12×10^{-2}
154	3.17×10^{-3}	125	5.16×10^{-3}	114	8.94×10^{-3}
235	2.48×10^{-3}	191	5.20×10^{-3}	174	8.50×10^{-3}
314	2.18×10^{-3}	254	4.69×10^{-3}	232	7.31×10^{-3}
393	1.93×10^{-3}	318	4.51×10^{-3}	290	7.32×10^{-3}



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Figure 9 CE measurements for three levels of relative humidity - 71.1, 82.4 and 93.5 % - compared to the extended model of Dépée et al. (2019) (top) and the Wang et al. (1978) model (bottom). Squares are the CE measurements summarised in Table 3 while lines are the CE modelling resulting from the experimental conditions found in Table 2.



614 CONCLUSIONS

615 In-CASE (In-Cloud Aerosol Scavenging Experiment) was built to conduct a set of experiments
616 quantifying the contribution of any microphysics effects involved in the AP collection by falling cloud
617 droplets. For this purpose, all parameters influencing the collection efficiency (CE) are controlled -
618 i.e. the AP and droplet sizes, the AP and droplet electric charges and the relative humidity.

619 This study focused on the influence of relative humidity since the literature lacks baseline data
620 validating the theoretical models of CE implemented in cloud, climate and pollution models. Indeed,
621 only the work of Ardon-Dryer et al. (2015) is dedicated to check the CE variation for two levels of
622 relative humidity and cloud droplet sizes ($A \leq 100 \mu\text{m}$). Nevertheless, for the droplet radius
623 considered, the authors conclude that the electrostatic forces could have played a key role on their
624 CE measurements, since the AP and droplet are charged, however slightly.

625 In the new measured CE dataset that is presented here, the APs and droplets are neutralised. There
626 is no significant remaining electrostatic effect considering the maximum residual AP and droplet
627 charges for the droplet radius examined ($A = 49.6 \pm 1.3 \mu\text{m}$), twice larger than the one studied by
628 Ardon-Dryer et al. (2015). Here, three levels of relative humidity were investigated - 71.1, 82.4 and
629 93.5 % which are typical in-cloud conditions.

630 From the measurements obtained, it is clear that the relative humidity - through the thermophoretic
631 and diffusiophoretic forces - significantly impacts the CE. Indeed, an increase by a factor of 4 was
632 observed for the CE when the relative humidity level declines from 93.5 to 71.1 %. Thus, it is quite
633 important to consider these effects in cloud model since the levels of relative humidity are
634 comparable from those used in this study. It was also shown that for the AP size considered in the
635 present study, the impact of the AP size on the CE is a second order dependency. In fact, only a
636 doubling of the CE was highlighted - for a relative humidity of 93.5 % - from the larger to the smaller
637 AP radius considered. This impact of the AP size decreased when the influence of the relative
638 humidity increases.

639 The CE computed with the well-established model of Wang et al. (1978) as well as the new Lagrangian
640 model described in Dépée et al. (2019) and extended to phoretic effects were compared to the
641 measurements. The agreement was good. Nevertheless, significant discrepancies between both
642 models were revealed for high relative humidity (in a subsaturated air) where the relative humidity
643 influence is weak. This can be attributed to the fact that the model of Wang et al. (1978) disregards
644 some microphysics effects such as AP weight, AP inertia and interception which have a significant
645 contribution near the Greenfield gap (Greenfield, 1957). Thus, the extended Lagrangian model of
646 Dépée et al. (2019) offers a more appropriate estimation of the CE.

647 In this study, the electrostatic effects were not considered. However, Dépée et al. (2019) have shown
648 an impact of several orders of magnitude on the CE, especially considering the electric charges of
649 cloud droplets and radioactive APs. Then, it is essential to investigate the AP collection by clouds
650 due to the electrostatic forces - referred as "electroscavenging". Up to now, the analytical expression
651 of the electrostatic forces - based on the image charge theory developed by Jackson (1999) - has
652 never been experimentally validated or at least emphasised. Consequently, In-CASE was also used to
653 study the influence of the droplet and AP charge on CE which is addressed in a second paper (Dépée
654 et al., 2020).

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672 Appendix A - Evaluation method of the collection efficiency in the 673 presence of multiple charged APs

674 This appendix presents the method used to evaluate the CE when the selected AP radius by the DMA
 675 is 50 or 150 nm - when the multiple charged APs can not be neglected (see section 2.2).
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 677

678 A.1 Ratio of multiple charged APs

679 A.1.1 Selected AP radius of 50 nm

680 Before the AP selection, the DMA charges the APs following a known charging law (Wiedensohler,
 681 1988) with an energy X-ray neutraliser (not presented in Figure 2).
 682

683 The first step is to estimate the number and mass ratios of multiple charged APs in the mean AP mass
 684 concentration measured in the In-CASE collision chamber ($C_{m,AP}$). For this purpose, the size
 685 distribution of the APs produced by the atomiser is measured just before the DMA selection (Figure
 686 3). The AP number concentration at the single (50 nm), double (75.8 nm), triple (98.2 nm), quadruple
 687 (119.1 nm) and quintuple (139.1 nm) charged radii are deduced from the size distribution.
 688

689 Those AP number concentrations are the total concentrations at a given multiple charged AP radius.
 690 From those total concentrations, a fraction will be actually carrying the correct charge number to
 691 have the exact electrical mobility selected by the DMA (1 charge for 50 nm, 2 charge for 75.8 nm, 3
 692 charges for 98.2 nm, etc.). This fraction number ($F_{N,n}$) of an AP radius (a) carrying n elementary
 693 charge(s) can be estimated through the APs charging law imposed by the energy X-ray neutraliser -
 694 defined by Wiedensohler (1988). This similar Boltzmann distribution is defined in the equations (13):
 695
 696
 697

$$\left. \begin{aligned}
 & F_{N,n}(a) = 10^{\left[\sum_{i=1}^6 c_i(n) \left(\log \left(\frac{2a}{10^{-9}} \right) \right)^{i-1} \right]} \quad \text{if } n < 3 \\
 & F_{N,n}(a) = \frac{e}{\sqrt{8\pi^2 \varepsilon_0 a k_b T_{air}}} \exp \left[\frac{n \frac{4\pi \varepsilon_0 a k_b T_{air} \ln \left(\frac{Z_{i+}}{Z_{i-}} \right)}{e^2}}{2 \frac{4\pi \varepsilon_0 a k_b T_{air}}{e^2}} \right] \quad \text{if } n \geq 3
 \end{aligned} \right\} \begin{cases}
 c_{i \in [1,6]}(1) = \begin{bmatrix} -2,3484 \\ 0,6044 \\ 0,4800 \\ 0,0013 \\ -0,1553 \\ 0,0320 \end{bmatrix} \\
 c_{i \in [1,6]}(2) = \begin{bmatrix} -44,4756 \\ 79,3772 \\ -62,8900 \\ 26,4492 \\ -5,7480 \\ 0,5049 \end{bmatrix}
 \end{cases}$$

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Where ε_0 , k_b and $T_{air}=295.15$ K are the vacuum permittivity, the Boltzmann's constant and the lab temperature. The ion mobility ratio ($\frac{Z_{i+}}{Z_{i-}}$) is assumed to be equal to 0.875 (Wiedensohler, 1988).

Finally, the effective AP numbers for the respective multiple charged AP radii have been evaluated in the AP flow at the DMA's outlet (corresponding to the AP flow going into the In-CASE collision chamber). Thus, the mass fractions ($F_{m,n}$) for the single, double..., quintuple charged AP radii were estimated. It was found that the quadruple and quintuple charged AP radii can be neglected since their weight less than 6 % in the mean AP mass concentration in the In-CASE collision chamber ($C_{m,AP}$). Moreover, since their number concentrations are really poor (less than 50 cm⁻³) compared to the



711 single, double and triple charged radius ($\sim 10^3\text{-}10^4 \text{ cm}^{-3}$), the likelihood of those APs to be collected
 712 by a droplet in the collision chamber is extremely unlikely.

713

714 A.1.2 Selected AP radius of 150 nm

715

716 For a selected AP radius of 150 nm, only the double charged APs are considered since the triple
 717 charged APs are assumed to be stopped by the impactor at the DMA inlet (triple charged radius =
 718 353.4 nm and $D_{50\%}/2 = 213 \text{ nm}$, Table 1). The mass fractions ($F_{m,n}$) of the single and double charged
 719 are evaluated in the same way as a 50 nm selected AP radius.

720

721 A.2 Deduction of the collection efficiency

722

723 A.2.1 Selected AP radius of 50 nm

724

725 As explained in section 2.2, when the selected AP radius by the DMA is 50 nm, the AP mass collected
 726 at the In-CASE's chamber bottom ($m_{AP,d}$) is actually the sum of the masses of the single (50 nm),
 727 double (75.8 nm) and triple (98.2 nm) charged AP collected by the droplet train. This can also be
 728 defined as the linear combination of the collection efficiencies ($CE_i(a_i, A, RH)$) and the available AP
 729 mass in the volume swept by the droplets ($m_{AP,available}(a_i)$) at a given multiple charged dry AP radius
 730 (a_i) - equation (14):

$$m_{AP,d} = m_{50 \text{ nm},d} + m_{75.8 \text{ nm},d} + m_{98.2 \text{ nm},d} = \sum_{i=1}^3 CE_i(a_i, A, RH) \times m_{AP,available}(a_i) \quad (14)$$

731

732 Where the respective available AP masses in the volume swept by the droplets are defined by the
 733 equation (15):

$$m_{AP,available}(a_i) = \pi(A + GroF(RH) \times a_i)^2 \times F_d \times \Delta t \times H_{eff} \times C_{m,AP} \times F_{m,n}(a_i) \quad (15)$$

734

735 All the parameters given in equation (8) are either measured or initially known, except the collection
 736 efficiencies (CE_i) for the single, double and triple charged AP dry radius. To deduce those three
 737 unknown parameters, a set of j linearly independent experiments ($j \geq 3$) has been performed by
 738 varying the ratio of the multiple charged APs (by changing the AP size distribution mode in Figure 3).
 739 The matrix system is then described through the equation (16):

$$M_{collected \ mass} = M_{available} \otimes M_{CE} \quad (16)$$

740

741 Where the one-dimension matrix of the collected mass ($M_{collected \ mass}$) for the set of j experiment is
 742 noted as the equation (17):

$$M_{collected \ mass} = \begin{bmatrix} m_{AP,d,1} \\ \vdots \\ m_{AP,d,j} \end{bmatrix} \quad (17)$$

743

744 The two-dimension matrix of the available AP masses in the volume swept by the droplet ($M_{available}$)
 745 for the single (a_1), double (a_2) and triple (a_3) charged is defined as the equation (18):

$$M_{available} = \begin{bmatrix} m_{AP,available,1}(a_1) & m_{AP,available,1}(a_2) & m_{AP,available,1}(a_3) \\ \vdots & \vdots & \vdots \\ m_{AP,available,j}(a_1) & m_{AP,available,j}(a_2) & m_{AP,available,j}(a_3) \end{bmatrix} \quad (18)$$

746

747 The one-dimension matrix containing all the unknown CEs (M_{CE}) is the equation (19):

$$M_{CE} = \begin{bmatrix} CE_1 \\ CE_2 \\ CE_3 \end{bmatrix} \quad (19)$$

748

749 Finally, this matrix system (16) is numerically solved by the quasi-Newton method. The uniqueness
 750 of the solution was verified - the initial value was changed in the solving method, giving the same
 751 solution vector.



752 A.2.2 Selected AP radius of 150 nm

753

754 Like the same principle as before, the AP mass collected by the whole droplets ($m_{AP,d}$) is the linear
755 combination of the single (150 nm) and double charged (253.7 nm), defined as the equation (20):

$$m_{AP,d} = m_{150\text{ nm},d} + m_{253.7\text{ nm},d} = \sum_{i=1}^2 CE_i(a_i, A, RH) \times m_{AP,available}(a_i) \quad (20)$$

756

757 Nevertheless, to avoid additional experiments and numerically reverse a similar matrix system as
758 (10), it was assumed that the CE of a dry AP radius of 253.7 nm is equivalent to the one for a dry AP
759 radius of 250 nm. Then, the CE for a 150 nm dry AP radius is deduced by the equation (21):

$$CE_1(150\text{ nm}, A, RH) = \frac{m_{AP,d} - CE_2(253.7\text{ nm}, A, RH) \times m_{AP,available}(253.7\text{ nm})}{m_{AP,available}(150\text{ nm})} \quad (21)$$
$$\approx \frac{m_{AP,d} - CE(250\text{ nm}, A, RH) \times m_{AP,available}(253.7\text{ nm})}{m_{AP,available}(150\text{ nm})}$$

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761 The right term in equation (21) has no unknown since the CE of a 250 dry AP radius
762 ($CE_2(250\text{ nm}, A, RH)$) has been previously calculated with the method developed in section 2.1.

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801 Appendix B - Uncertainty of the collection efficiency in the presence 802 of multiple charged APs

803 This appendix presents the method used to evaluate the CE uncertainty when the selected AP radius
804 by the DMA is 50 or 150 nm - when the multiple charged APs can not be neglected (see section 2.2).

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806

807 B.1 With a selected dry AP radius of 150 nm

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809 Since the CE of a selected dry AP radius of 150 nm ($CE(150 \text{ nm}, A, RH)$) is calculated through the CE
810 of a selected dry AP radius of 250 nm ($CE(250 \text{ nm}, A, RH)$) - equation (21) - the uncertainty on the CE
811 for the 150 nm ($u_{CE(150 \text{ nm}, A, RH)}$) is evaluated by propagating the uncertainty on the CE for 250 nm
812 ($u_{CE(250 \text{ nm}, A, RH)}$). It means the term $u_{CE(250 \text{ nm}, A, RH)}$ is added in equation (8) to deduce $u_{CE(150 \text{ nm}, A, RH)}$.

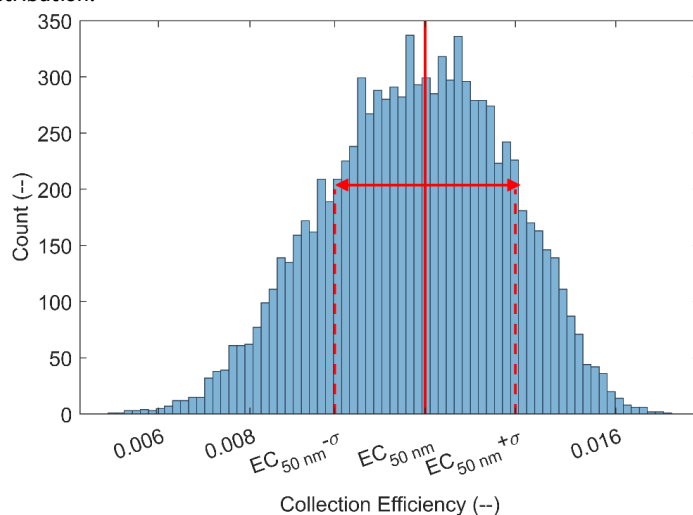
813

814 B.2 With a selected dry AP radius of 50 nm

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816 When the selected dry AP radius is 50 nm, the matrix system (16), solved by a quasi-Newton method,
817 is composed of parameters each with their relative uncertainties. The relative CE uncertainties of
818 the single (50 nm), double (75.8 nm) and triple (98.2 nm) charged dry AP radius are then deduced by
819 randomly perturbing the terms of the matrix $M_{collected \text{ mass}}$ and $M_{available}$ in equation (16) within the
820 limits of their respective experimental relative uncertainties. 10,000 perturbed matrix systems were
821 generated by the Monte-Carlo method and solved with the quasi-Newton method. From the 10,000
822 solution vectors - shaped like the equation (17) - the ones with negative CEs were removed since they
823 have no physical meaning. The Figure 10 shows the set of the solutions for a relative humidity level
824 of 71.1 % and a single charged dry AP radius (50 nm).

825 Finally, the relative uncertainty of the CE is given by the standard deviation (σ) of the solution
826 distribution.



827

828 Figure 10 Distribution of 10,000 solutions (negative values were removed) for a relative humidity
829 level of 71.1 % and a single charged dry AP radius (50 nm)

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