



A-Train estimates of the sensitivity of warm rain likelihood and efficiency to cloud size, environmental moisture, and aerosols

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Abstract. Precipitation efficiency has been found to play an important role in constraining the sensitivity of the climate through its role in controlling cloud cover, yet understanding of its controls are not fully understood. Here we use CloudSat observations to identify individual contiguous shallow cumulus cloud objects and compute the ratio of cloud water path to rain water path as a proxy for warm rain efficiency (WRE). Cloud objects are then conditionally sampled by cloud-top height, relative humidity, and aerosol optical depth (AOD) to analyze changes in WRE as a function of cloud size (extent). For a fixed cloud-top height, WRE increases with extent and environmental humidity following a double power-law distribution, as a function of extent. Similarly, WRE increases holding environmental moisture constant. There is surprisingly little relationship between WRE and AOD when conditioned by cloud-top height, suggesting that once rain drop formation begins, aerosols may not be as important for WRE as cloud size and depth. Consistent with prior studies, results show an increase in WRE with sea surface temperature. However, for a given depth and SST, WRE is also dependent on cloud size and becomes larger as cloud size increases. Given that larger objects become more frequent with increasing SST, these results imply that increasing precipitation efficiencies with SST are due not only to deeper clouds with greater cloud water contents, but also the propensity for larger clouds which may have more protected updrafts.

1 Introduction

Low cloud cover continues to be a dominant source of uncertainty in projecting future climate (e.g. Bony and Dufresne, 2005; Dufresne and Bony, 2008; Vial et al., 2013), with variations in shallow cumulus distributions explaining much of the differences in climate model-derived estimates of climate sensitivity (e.g. Wyant et al., 2006; Medeiros and Stevens, 2011; Nam et al., 2012). This stems from climate models' inability to simulate shallow cumulus and their impacts, due in part to the low temporal and spatial resolution of these models (e.g. Stevens et al., 2002), as well as the fact that small-scale processes important for cloud development, including turbulence and convection, must be parameterized (e.g. Tiedtke, 1989; Zhang and McFarlane, 1995; Bretherton et al., 2004). Studies have shown precipitation efficiency is a key parameter used to constrain cloud parameterizations within climate models (Rennó et al., 1994; Del Genio et al., 2005; Zhao, 2014; Lutsko and Cronin,



2018). Nam et al. (2012) hypothesized that shallow cumulus are too reflective in climate models, possibly because model
25 precipitation efficiencies are too weak. This results in excess cloud water which increases cloud optical depth and shallow
cumulus reflectance. Prior observational and modeling studies found the precipitation efficiency of shallow cumulus increases
as sea-surface temperature (SST) increases in response to climate change (Lau and Wu, 2003; Bailey et al., 2015; Lutsko and
Cronin, 2018). Factors including environmental moisture (e.g. Heus and Jonker, 2008; Schmeissner et al., 2015), entrainment
(e.g. Korolev et al., 2016; Pinsky et al., 2016b, a), and aerosols (e.g. Koren et al., 2014; Dagan et al., 2016; Jung et al., 2016b, a)
30 help regulate both thermodynamic and dynamical processes that promote favorable conditions important to not only warm rain
production, but also the efficiency of the conversion of cloud water to precipitation. To better constrain cloud parameterizations
of these processes and subsequently climate sensitivity to low cloud cover, more observations-based studies analyzing physical
processes influencing warm rain efficiencies are needed.

In an ideal shallow cumulus cloud, liquid water content increases adiabatically from cloud base to top. However, liquid water
35 content is generally only 50% - 80% of the adiabatic values due to entrainment (Gerber et al., 2008). Evaporation induced by
cloud-edge mixing not only impacts shallow cumulus updraft strength, but also the number and size of droplets within a
cloud (Lu et al., 2012), with increased evaporation potentially reducing the number and size of available droplets. Using a
large-eddy simulation (LES), Moser and Lasher-Trapp (2017) found the influence of entrainment decreases from cloud-edge
to center of individual shallow cumulus as they grow larger. This results in liquid water content at cloud center being closer to
40 adiabatic in larger clouds, because fewer droplets evaporate away at cloud-center. This implies that the collision-coalescence
process is more efficient at cloud center, because there is more cloud water available to be collected by large droplets. At
cloud edge, there are not only fewer droplets but also smaller droplets, potentially reducing collision-coalescence efficiencies
there. This is consistent with other LES results that found shallow cumulus updrafts are more insulated from entrainment as
they increase in size (e.g. Heus and Jonker, 2008; Burnet and Brenguier, 2010; Tian and Kuang, 2016). LES and limited field-
45 campaign observational studies have shown that cloud updrafts not only become more protected as cloud size increases, but
also as environmental moisture increases (Heus and Jonker, 2008; Schmeissner et al., 2015; Hernandez-Deckers and Sherwood,
2018). Romps (2014) used a cloud model to show that precipitation efficiency decreases as relative humidity decreases, because
precipitation evaporates more readily in a drier environment. Considering environmental moisture scales with temperature, this
is consistent with results found by Lau and Wu (2003) which show the efficiency of warm rain production increases as SSTs
50 increase using Tropical Rainfall Measuring Mission (TRMM) satellite observations. Given LES results showing that shallow
cumulus updrafts are more protected as clouds grow in size and/or environmental moisture increases, *we hypothesize larger
droplets will be evident closer to the cloud base and increase WRE in larger cloud objects, because the cloud-core of larger
cloud objects is more protected from entrainment.*

While perhaps not as important as organization (Minor et al., 2011) or cloud size (Jiang and Feingold, 2006), it is widely
55 understood that aerosol concentrations act to suppress warm rain production (Twomey, 1974; Albrecht, 1989) by increasing
the cloud droplet concentration and reducing cloud droplet sizes (Squires, 1958). Albrecht (1989) found that increasing precipi-
tation efficiency within a model is equivalent to decreasing the amount of cloud concentration nuclei (CCN), which reduces
the amount of cloud water. Similarly, Saleeby et al. (2015) used a cloud model to recently find both cloud water and rain drop



concentration decreases as cloud concentration nuclei increases. Lebsack et al. (2011) used CloudSat and Moderate Resolu-
60 tion Imaging Spectroradiometer (MODIS) observations to show that as drop size decreases, the ratio of rain water to cloud
water also decreases. Together, these studies suggest the number of large droplets able to fall at sufficient terminal velocities to
initiate collision-coalescence and continue growing to large enough sizes to fall out as rain decreases with increasing aerosol
concentrations, which would reduce warm rain efficiency (WRE).

Observationally, prior studies have used satellite observations to infer the relationship between precipitation efficiency and
65 both sea-surface temperature (Lau and Wu, 2003) and drop size (Lebsack et al., 2011). However, the relationship between
cloud water and precipitation as shallow cumulus grow larger, environmental moisture increases, and/or aerosol loading has
only been investigated using cloud models (e.g. Moser and Lasher-Trapp, 2017) and limited field-campaign observations (e.g.
Gerber et al., 2008). While these case and model studies provide insight into the physical processes, it is unclear how well they
70 represent the shallow cumulus clouds observed globally. Satellites can observe a large enough sample size of shallow cumulus
over different regions and during different stages of their lifecycle to gain a more holistic view of this relationship. Prior studies
have used TRMM and Global Precipitation Measurement Mission (GPM) observations to analyze warm rain production and
efficiency (e.g. Lau and Wu, 2003). Unfortunately, TRMM and GPM are precipitation radars operating at the Ku- and Ka-
bands not capable of observing the non-raining portions of clouds or light precipitation. Building off work in Smalley and
Rapp (2020) that analyzed the relationship between rain likelihood and cloud size, this study uses the higher sensitivity radar
75 of CloudSat in addition to MODIS observations to test the hypothesis that *WRE is higher in larger shallow cumulus and is
modulated by environmental moisture and aerosol loading.*

2 Data and Methods

To determine if larger shallow cumulus clouds are more efficient at producing warm rainfall, this study uses the CloudSat
Cloud Profiling Radar (CPR; Tanelli et al., 2008) to identify individual contiguous shallow cumulus cloud objects. The CPR is
80 a near-nadir pointing 94-GHz radar that can observe raining and non-raining cloud drops. It allows us to analyze the horizontal
distribution of cloud within a horizontal footprint of 1.4 x 1.8 km, and the vertical distributions of clouds within a 240 m bin
within each cloudsat pixel.

Contiguous cloudy regions are initially identified using the 2B-GEOPROF (Marchand et al., 2008) cloud mask confidence
values ≥ 20 , which removes orbit elements that may be influenced by ground clutter (Marchand et al., 2008). Before identifying
85 cloud objects, 2C-RAIN-PROFILE (Lebsack and L'Ecuyer, 2011) modeled reflectivity is mapped onto the two-dimensional
cloud mask field. As outlined by prior literature (e.g. L'Ecuyer and Stephens, 2002; Mitrescu et al., 2010; Lebsack and
L'Ecuyer, 2011), modeled reflectivity adjusts the raw reflectivity for multi-scattering and attenuation when it is raining. As
described by Smalley and Rapp (2020), we use a lower-tropospheric stability threshold of 18.55 K to separate cloud objects
occurring in environments favoring stratocumulus development from those occurring in environments favoring shallow cumu-
90 lus development. Shallow cumulus cloud objects are then identified using the methodology described by Smalley and Rapp
(2020) using the combined two-dimensional reflectivity field, with only single-layer cloud objects included. This study uses



2C-RAIN-PROFILE integrated precipitation water path (W_p) > 0 to identify raining cloud objects and does not consider non-raining objects. We then store the median cloud-top height and maximum along-track extent (hereby extent) of each cloud object for later analysis.

95 Although CloudSat 2B-CWC-RVOD (Austin et al., 2009) does provide a cloud water path (W_C) product, the rain drop size distribution used in 2B-CWC-RVOD is not the same as that used in 2C-RAIN-PROFILE. Additionally, Christensen et al. (2013) found that the 2B-CWC-RVOD algorithm struggles to filter out precipitation sized droplets in the presence of light precipitation and drizzle, which results in an overestimation of cloud water. This, coupled with differences in assumed drop size distributions by 2B-CWC-RVOD and 2C-RAIN-PROFILE, makes 2B-CWC-RVOD W_C not ideal for this study, so we
100 instead use MODIS W_C . While there are biases in MODIS shallow cumulus W_C , prior studies have found them to be small in comparison to other satellite retrievals (e.g. Lebsock and Su, 2014). W_C is then calculated for each CloudSat pixel by averaging the nearest nine MOD-06-1KM (Platnick et al., 2003) pixels, which have been previously matched to the CloudSat track in the MOD-06-1KM product (?). We then store and analyze the median W_C associated with each cloud object.

105 WRE of each shallow cumulus cloud object is calculated as $\frac{W_p}{W_C}$. Note, this is a proxy for true WRE, because mass flux of water in and out of a cloud cannot be determined without a model, however this ratio has been used by prior observational studies to analyze the amount of cloud water converted to rain water (e.g. Lebsock et al., 2011).

Considering reflectivity is a function of the drop size distribution to the sixth power, it is expected that the maximum reflectivity in non-raining cloud objects will occur near cloud-top, then shift downward as a cloud transitions from non-raining to raining. Wang et al. (2017) used the vertical reflectivity gradient (VGZ) to investigate warm rain onset. They found VGZ
110 (positive down) reverses sign (positive to negative) when clouds transition from non-raining to raining. Given previous studies and results shown in Smalley and Rapp (2020) finding rain is more likely as clouds grow larger in extent, it is hypothesized that the negative VGZ within individual raining cloud objects will increase in magnitude as cloud objects increase in extent. The methodology developed by Wang et al. (2017) is applied to find the VGZ for each pixel within every shallow cumulus cloud object. VGZ at cloud object center pixel (VGZ_{CP}) will then be compared to VGZ at cloud object edge pixel (VGZ_{EP}) to infer
115 the impact of mixing on cloud object cores as a function of cloud size and environmental moisture.

The influence of aerosols on the relationship between WRE and cloud object efficiency are determined using Aqua MODIS level-3 daily 550 nm aerosol optical depth (AOD) (Ruiz-Arias et al., 2013). Each cloud object is matched to the nearest $1^\circ \times 1^\circ$ gridbox AOD value. Note, this study does not consider the type of aerosol present in each environment, however this may also factor into the WRE.

120 Similar to Smalley and Rapp (2020), analysis is constrained to only marine shallow cumulus between between 60 N and 60 S. Measurements are constricted to June 2006 and December 2010 because CloudSat stopped taking night time measurements after 2010 due to a battery anomaly (Witkowski et al., 2012). Environmental moisture is classified using 6-hourly ECMWF-AUX (Cronk and Partain, 2017) average relative humidity below 3 km matched to each cloud object. Cloud-top height, environmental moisture, VGZ, and AOD are used to control and analyze the relationship between WRE and cloud object extent.



125 3 Warm rain relationship to extent

Similar to Smalley and Rapp (2020), The spatial distribution of W_P , W_C , WRE, AOD, and extent of raining shallow cumulus cloud objects is analyzed by binning them to a $2.5^\circ \times 2.5^\circ$ global grid.

Figure 1a shows the spatial distribution of W_P over the global ocean basins, with W_P increasing equatorward. This is consistent with prior literature that found raining shallow cumulus are most frequent within the tropics (e.g. Smalley and Rapp, 2020). W_P is largest near the Inter-Tropical Convergence Zone (ITCZ), South Pacific Convergence Zone (SPCZ), and tropical warm pool, with values exceeding 45 g m^{-2} . Deep convection is more frequent here (e.g. Waliser and Gautier, 1993), so some objects may be transitioning from raining shallow cumulus to deeper convection. The results likely include a mix of frequently occurring tropical raining shallow cumulus and the early stages of developing deep convection possibly resulting in large W_P over the tropics.

135 Spatial patterns in W_C (Figure 1b) within the tropics generally follow W_P , with values ranging between 110 g m^{-2} and 150 g m^{-2} in the tropics. Considering the tropics are more humid than the mid-latitude and polar regions, this is consistent with modeling studies that found less cloud water evaporates away in wetter environments (e.g. Hernandez-Deckers and Sherwood, 2018). Considering boundary layer depth scales with SST (e.g. Wood and Bretherton, 2004b), the boundary layer is generally deeper over the tropical oceans than the sub-tropical oceans. This supports deeper clouds (e.g. Short and Nakamura, 2000; Rauber et al., 2007; Smalley and Rapp, 2020) and could also help explain why W_C and W_P are largest in the tropics.

Figure 1c shows the spatial patterns in WRE follow spatial patterns in W_P , with values increasing equatorward. Shallow cumulus cloud object WRE is largest within the ITCZ, SPCZ, and tropical warm pool, with values > 0.35 . This is consistent with Lau and Wu (2003), who found precipitation efficiency is positively correlated with SST (e.g. Lau and Wu, 2003), and implies that WRE is higher in wetter environments.

145 Patterns in spatial extent shown in Figure 1d are similar to those found by Smalley and Rapp (2020), who used combined CloudSat/CALIPSO to define extent, with extent decreasing from the stratocumulus regions east into the trade cumulus regions and north into the ITCZ. Interestingly, Figure 1c shows WRE also peaks in the southeast Pacific stratocumulus region, implying that WRE is high in regions with relatively low SST. However, Figure 1e shows that fewer than 40 shallow cumulus objects are observed in a given gridbox over this region in a four-year period, reducing confidence in WRE here. Together, Figures 1c and 1d indicate that the relationship between WRE and extent is complicated and potentially depends on cloud depth (which increases in the tropics) and on environmental conditions including environmental moisture and aerosol loading.

To determine how WRE depends on cloud size, Figure 2 shows WRE as a function of cloud object extent. WRE follows a double power-law relationship, with $WRE < 0.25$ for cloud objects $< 8.3 \text{ km}$ and approaching 0.3 for cloud objects $> 8.3 \text{ km}$. Similar to these results, earlier studies have shown a double power-law distribution in shallow cumulus size (e.g. Benner and Curry, 1998; Trivej and Stevens, 2010), which will be discussed in further detail later.

155 To address the impact of environmental moisture and cloud depth on WRE, Figure 3 shows the relationship between WRE and cloud object extent conditioned using cloud-top height and $< 3 \text{ km}$ relative humidity. Holding environmental moisture constant, WRE depends strongly on cloud-top height with WRE nearly doubling for each 0.5km increase in cloud top height



for a given extent. For a given RH and top height, there is also an increase in WRE with extent. Holding top height constant, there is also an increase in WRE with increasing environmental moisture; however, increases in WRE are dominated by changing cloud size (depth and extent).

To support the hypothesis that larger shallow cumulus are able to sustain a larger droplet field within their cores to increase the precipitation efficiency, the variation in the VGZ across individual cloud objects is examined. We expect that VGZ will be a larger negative value near cloud center than cloud edge especially as cloud size increases. As an example, Figure 4a shows the change in median VGZ_{CP} to VGZ_{EP} for cloud objects with an extent of 10.2 km. VGZ decreases from 10 dBZ km^{-1} at cloud object edge to approximately -20 dBZ km^{-1} at cloud object center. This demonstrates that larger droplets are present near cloud base near cloud object center compared to the edge. This implies, at least for extents of 10.5 km, drops grow larger near cloud object centers and may be more protected from mixing.

Figure 4b shows the relationship between VGZ_{CP} and VGZ_{EP} as a function of extent and top height. For a constant cloud-top height, VGZ_{CP} again follows a double power-law distribution. Specifically, the magnitude of the VGZ_{CP} rapidly increases from approximately 10 dBZ km^{-1} to 20 dBZ km^{-1} as extent approaches 8.3 km, while it plateaus around 20 dBZ km^{-1} for extents > 8.3 km. Conversely, VGZ_{EP} decreases in magnitude, approaching 0 dBZ km^{-1} for the largest cloud object extents. However, it does not decrease as fast as VGZ_{CP} , implying that the change in vertical reflectivity gradient in the center of cloud is driving changes in differences from center to edge. Figure 4b also shows that the change in VGZ_{CP} depends on cloud-top height, with larger magnitudes for the tallest clouds. This is consistent with previous modeling studies that found larger shallow cumulus cloud cores are more insulated from entrainment (e.g. Burnet and Brenguier, 2010; Hernandez-Deckers and Sherwood, 2018), resulting in larger droplets (e.g. Moser and Lasher-Trapp, 2017) and a higher probability of rainfall (e.g. Smalley and Rapp, 2020) in observations.

To determine how VGZ_{CP} influences the relationship between WRE and extent, Figure 4c shows WRE as a function of extent conditioned by top height and VGZ_{CP} , with WRE increasing as the magnitude of VGZ_{CP} increases. This, coupled with Figure 4b, illustrates that as shallow cumulus grow deeper and wider, drops at the center of the cloud can grow larger and scavenge more available cloud water. This is consistent with larger shallow cumulus being more efficient at producing rainfall, perhaps in part because they are less influenced by environmental mixing.

Until this point, this paper has focused on how cloud size and environmental moisture impacts WRE. However, it is also understood that aerosol concentrations influence both the number and size of droplets within a cloud, with larger aerosol concentrations resulting in a greater number of smaller droplets (e.g. Twomey, 1974; Albrecht, 1989). As a result, we hypothesize increasing aerosol concentrations, which vary regionally (Figure 1f), increase the ratio of cloud droplets to rain drops, thus reducing WRE.

Figure 5a shows the relationship between WRE and AOD, conditioned by top height. On first glance, it appears that WRE increases as a function of AOD, which contradicts the expectation of a shift in drop size distribution towards fewer large drops to initiate collision-coalescence which would reduce the amount of cloud water converted to rain water. However, disentangling aerosol-cloud interactions from other meteorological variables is quite difficult, as increasing aerosol concentrations are often correlated with other environmental variables (e.g. Koren et al., 2014).



Given the strong dependence of WRE on top height, we further examine the relationship between AOD and top height
195 (Figure 5b), conditioned by extent. The curves shown in Figure 5a look similar to those shown in Figure 5b, suggesting the
positive correlation between aerosols and top height are responsible for the observed relationship between AOD and WRE.
Indeed, Figure 5c further supports this assertion. When conditioned by top height, WRE shows little dependence on AOD,
and suggests that the conversion from W_C to W_P is more sensitive to cloud depth than aerosols. While these results seem
counterintuitive, this analysis examines clouds in which precipitation has been detected. Examination of the likelihood of
200 precipitation shows the expected decrease with increasing AOD (not shown). These results imply that once the condensation-
coalescence is initiated, aerosol loading has a smaller impact on the conversion of cloud water to rain than other cloud or
environmental characteristics.

4 Summary and Discussion

This study uses the methodology described by Smalley and Rapp (2020) to classify a large global shallow cumulus cloud
205 object dataset from CloudSat and determine the relationship between WRE, cloud extent, environmental moisture, and aerosol
loading. We find that WRE increases as a function of cloud size (top height and extent) and environmental moisture. Benner
and Curry (1998) found a double-power law distribution in shallow cumulus thickness as a function of cloud diameter, and
Trivej and Stevens (2010) hypothesized that the shift from one power-law distribution to another results from small shallow
cumulus that can rapidly grow in size until reaching the trade inversion. We find a similar relationship between WRE and
210 extent, showing that one distribution exists with WRE increasing faster for extents < 8.3 km then slowly increasing above
this breakpoint. Trivej and Stevens (2010) also found that environmental factors, particularly environmental moisture, become
important once cloud-top height reaches the trade inversion. Our results show that WRE is most sensitive to environmental
moisture above an extent of 8.3 km, which we assume represents the average extent where cloud objects reach the trade
inversion.

215 Unexpectedly, we find that for a fixed cloud depth, WRE is fairly insensitive to AOD. One explanation may be that, although
high AOD values do occur over the global ocean basins, the majority of cloud objects being sampled still form in relatively
clean air, so the minority of cloud objects occurring over polluted regions have a small impact on the overall statistics. Another
explanation may be that this analysis only includes precipitating clouds, so once collision-coalescence is initiated, the amount
of cloud water converted to rain water is less influenced by aerosol concentrations.

220 Past studies conclude that precipitation efficiency increases as SST increases (Lau and Wu, 2003; Bailey et al., 2015; Lutsko
and Cronin, 2018). Considering warmer SSTs tend to result in deeper clouds (e.g. Wood and Bretherton, 2004a) and more
humid environments (e.g. Chen and Liu, 2016), it is reasonable to expect that WRE would increase in response (e.g. Lau and
Wu, 2003). Our results show that WRE is highest near the equator where SSTs are warmest. However, the general relationship
between cloud size (depth and extent), environmental moisture, and WRE suggests that WRE is more sensitive to cloud size
225 than environmental moisture. To directly address the SST dependence, Figure 6 shows the frequency distribution of extents
and the median WRE, both as a function of cloud-top height and SST. For a given cloud-top height, WRE does increase as



a function of SST. However, for a fixed SST, WRE also increases as extent increases. Additionally, Figure 6 shows that the frequency distribution of cloud object sizes shifts toward more frequent larger extents with increasing SST. Together, these suggest that increasing WRE with SST shown in past studies not only results from the deepening clouds but also the shift
230 towards more frequent larger clouds.

Prior literature has shown that modeled shallow cumulus cores become more adiabatic as they grow larger (Moser and Lasher-Trapp, 2017), potentially resulting in larger drops. Figure 6 and our analysis of the relationship between VGZCP, extent, and WRE suggest drop growth is being enhanced near the base at the center of larger cloud objects, potentially resulting in more cloud water being scavenged by larger droplets and more efficient autoconversion and accretion processes. Most
235 climate models parameterize autoconversion and accretion as functions of cloud and precipitation properties (e.g. Lohmann and Roeckner, 1996; Liu and Daum, 2004; Morrison et al., 2005; Lim and Hong, 2010; Lee and Baik, 2017), but recently enhancement factors that depend on variations and covariations in WC and WP have been introduced to correct for biases due to subgrid-scale W_c and W_p inhomogeneity (e.g. Lebsock et al., 2013; Boutle et al., 2014; Witte et al., 2019). Presumably, the dependence of these enhancement factors on W_c variability would capture the increase in WRE with cloud depth shown here,
240 however it is unclear if these enhancement factors based on the variance in W_c and W_p capture the effects of cloud extent on WC and WP, and subsequently WRE. Our dataset provides an opportunity for a future analysis that could focus on investigating the relationship between subgrid-scale variability in WC, WP, WRE, and extent, which could help improve our understanding and simulation of precipitating shallow cloud processes in climate models.

Data availability. All CloudSat/MODIS data products used in this analysis were acquired from the CloudSat Data Processing Center and
245 can be accessed at <http://www.cloudsat.cira.colostate.edu>.

Code and data availability. Please contact the authors for access to any dataset created by the analysis and/or the code used to process the CloudSat/MODIS data..

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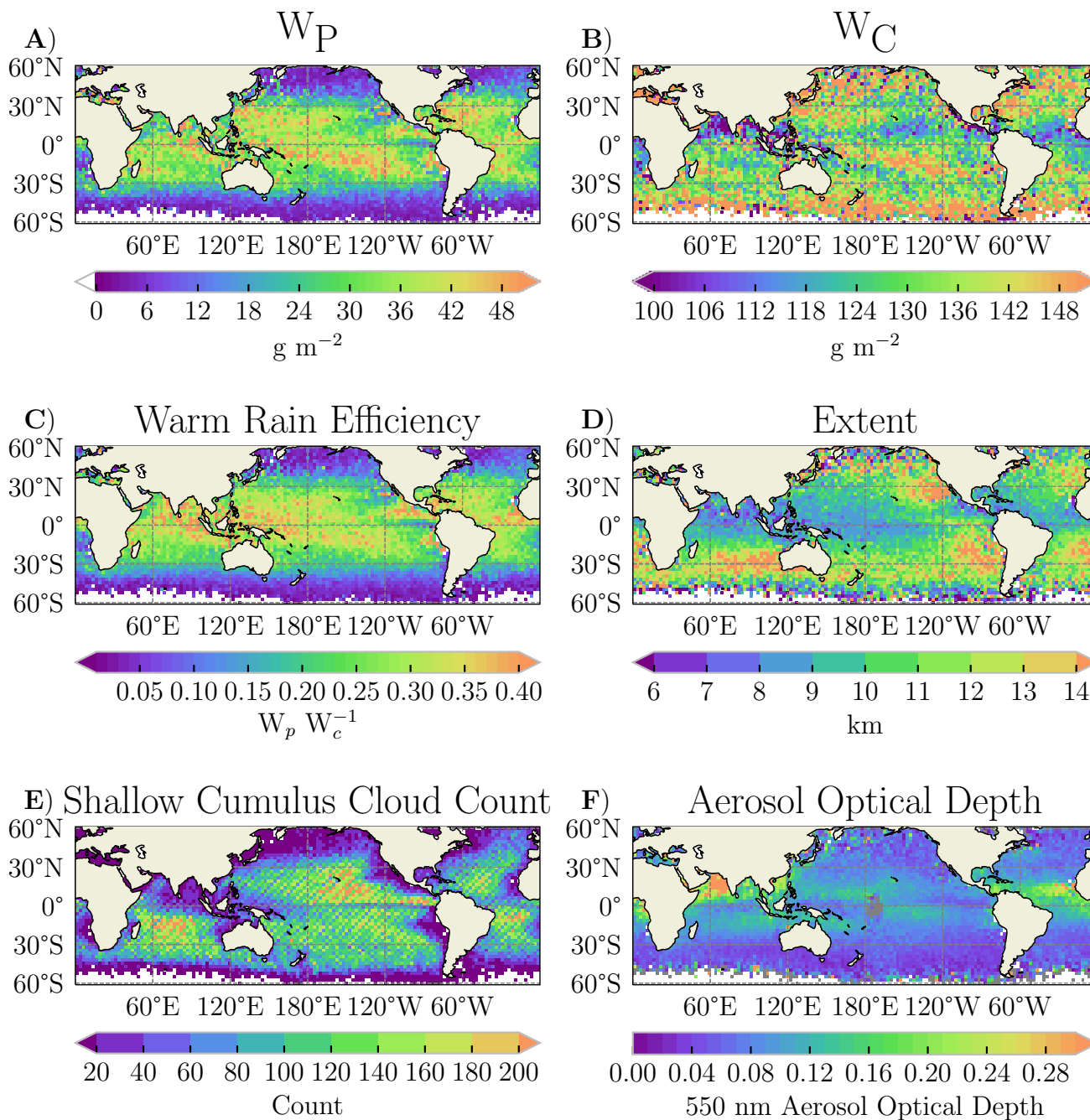


Figure 1. The spatial distribution of integrated precipitation water path (W_p), cloud water path (W_c), warm rain efficiency, extent, number of shallow cumulus cloud objects, and aerosol optical depth are shown in panels A), B), C), D), E), and F) respectively. Cloud objects are binned onto a $2.5^\circ \times 2.5^\circ$ spatial grid, and any grid box containing no data is white.

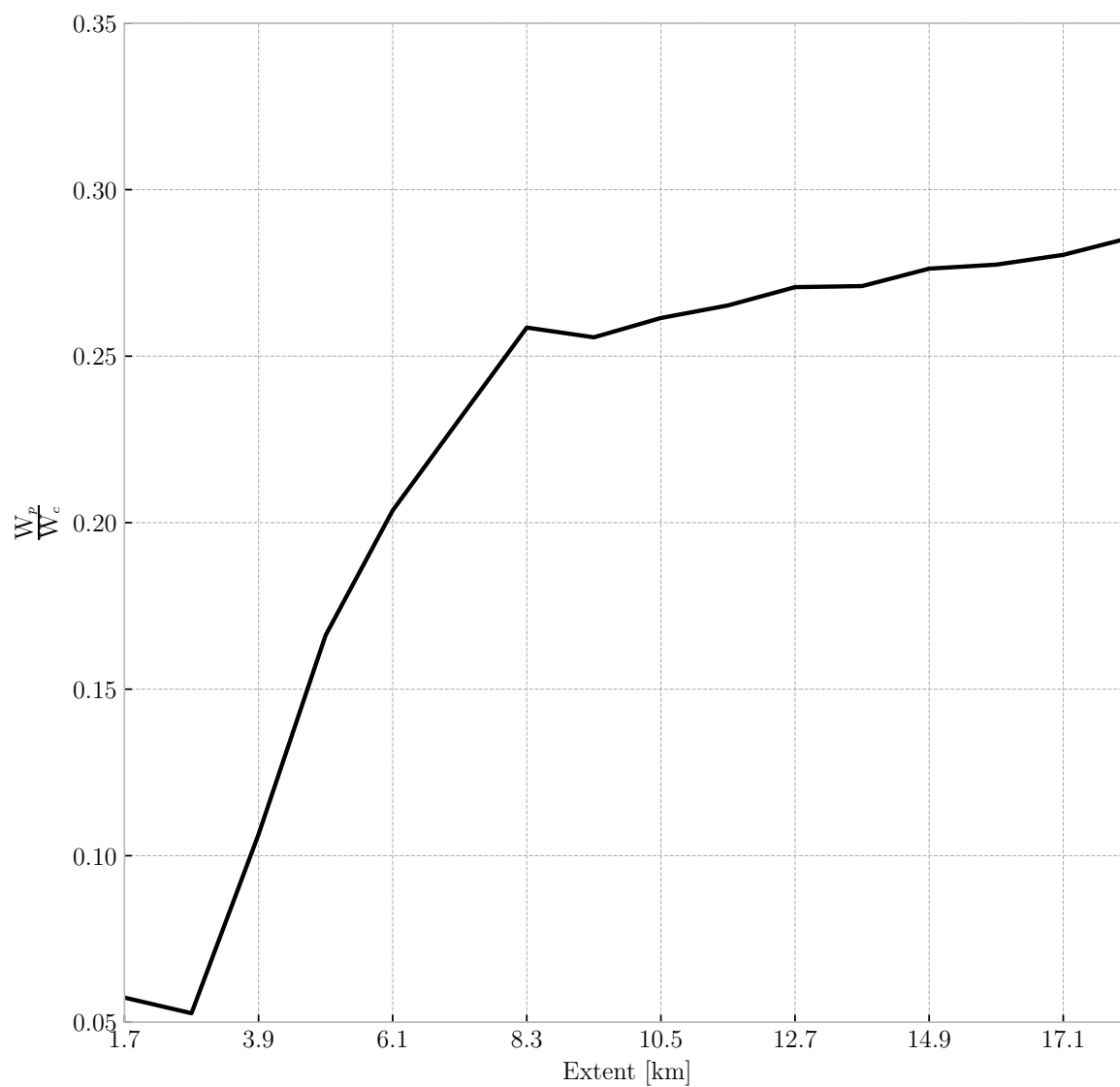


Figure 2. The median warm rain efficiency $\left(\frac{W_p}{W_c}\right)$ at a given median size (extent).

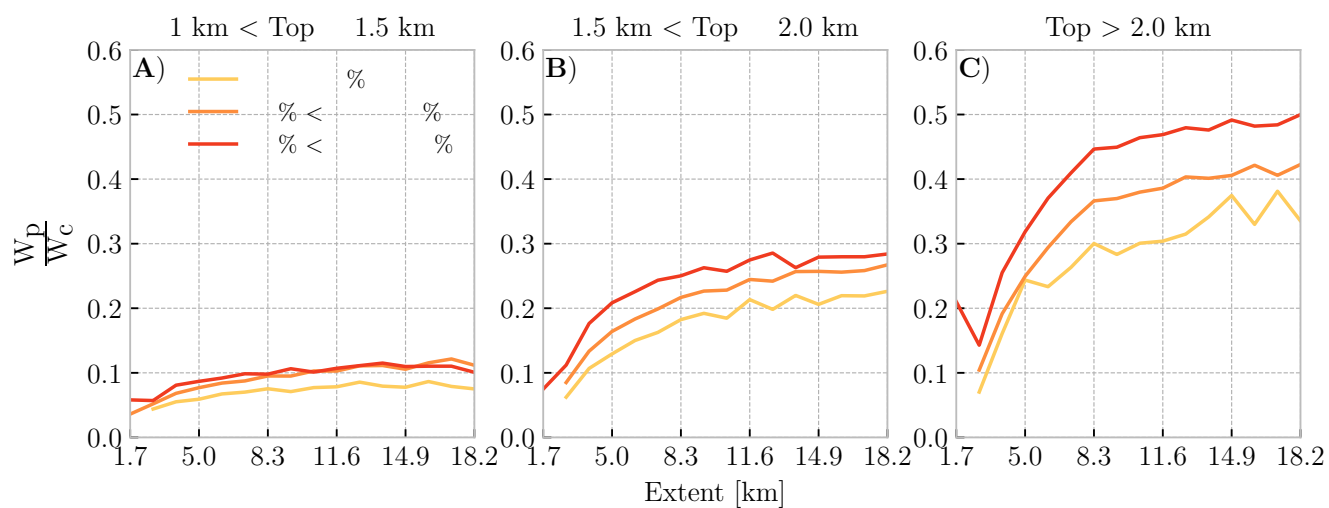


Figure 3. The median warm rain efficiency $\left(\frac{W_p}{W_c}\right)$ at a given median size (extent). The different line colors represent cloud objects separated by environmental moisture (< 3 km relative humidity).

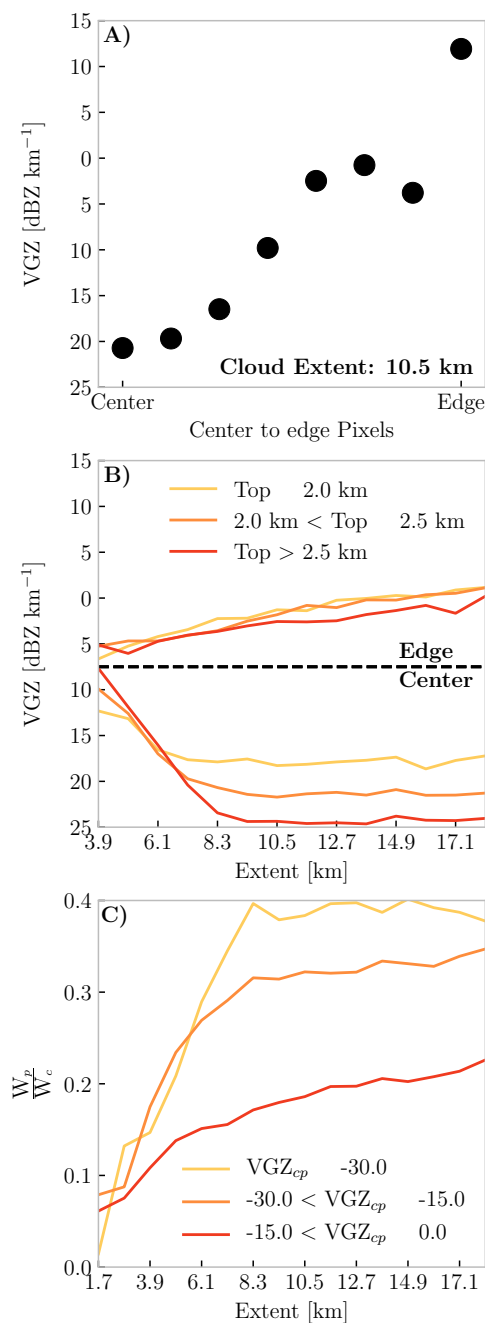


Figure 4. Panel A) shows the median change in the vertical reflectivity (VGZ) from the center to edge of all cloud objects with an extent of 10.5 km. Panel B) shows the median vertical reflectivity gradient (VGZ) at the center (red) and edge (blue) of different sized (extent) raining cloud objects. Different lines represent cloud objects separated by top height. Panel C) shows the median warm rain efficiency ($\frac{W_p}{W_c}$) at a given median size (extent). The different line colors represent cloud objects separated by the vertical reflectivity gradient on the center pixel (VGZ_{cp}) of all cloud objects.

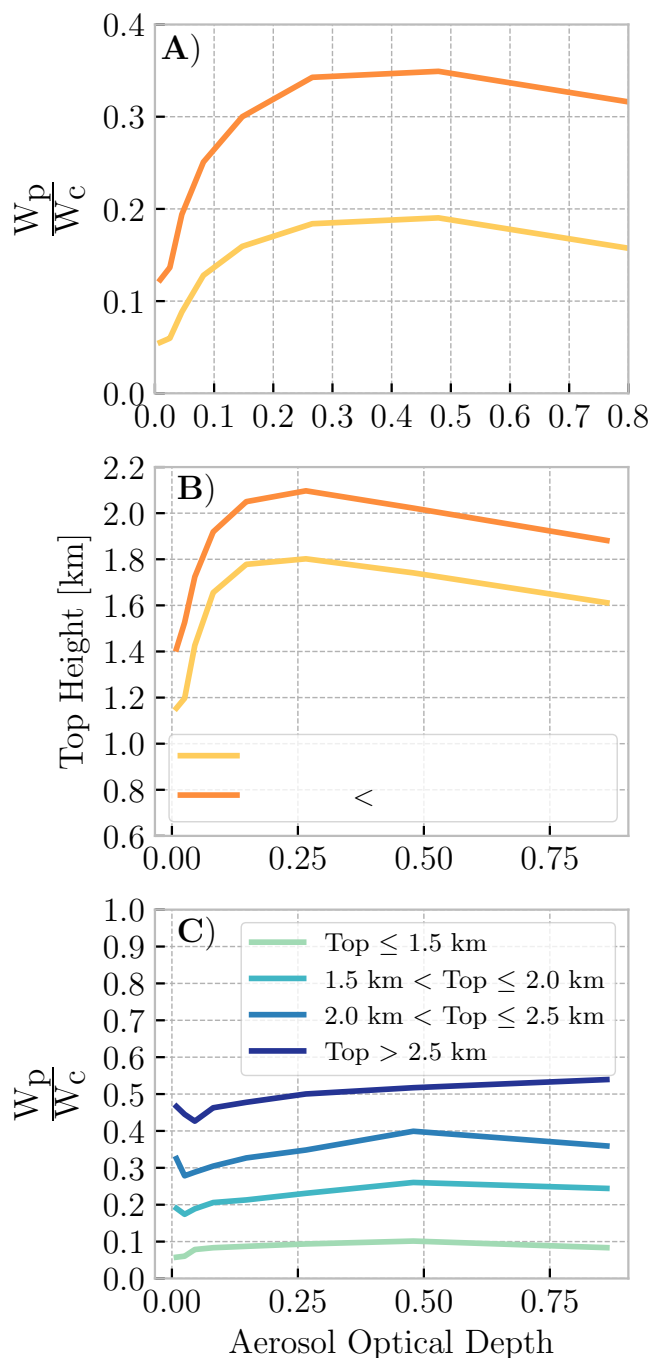


Figure 5. Panel A) shows the relationship between median warm rain efficiency as MODIS 550 nm aerosol optical depth. Panel B) shows the relationship between median cloud-top height and aerosol optical depth. Panel C) shows the relationship between warm rain efficiency ($\frac{W_p}{W_c}$) and aerosol optical depth. Line colors in panels A) and B) represent cloud objects separated by extent, while line colors in panel C) represent cloud objects separated by top height.

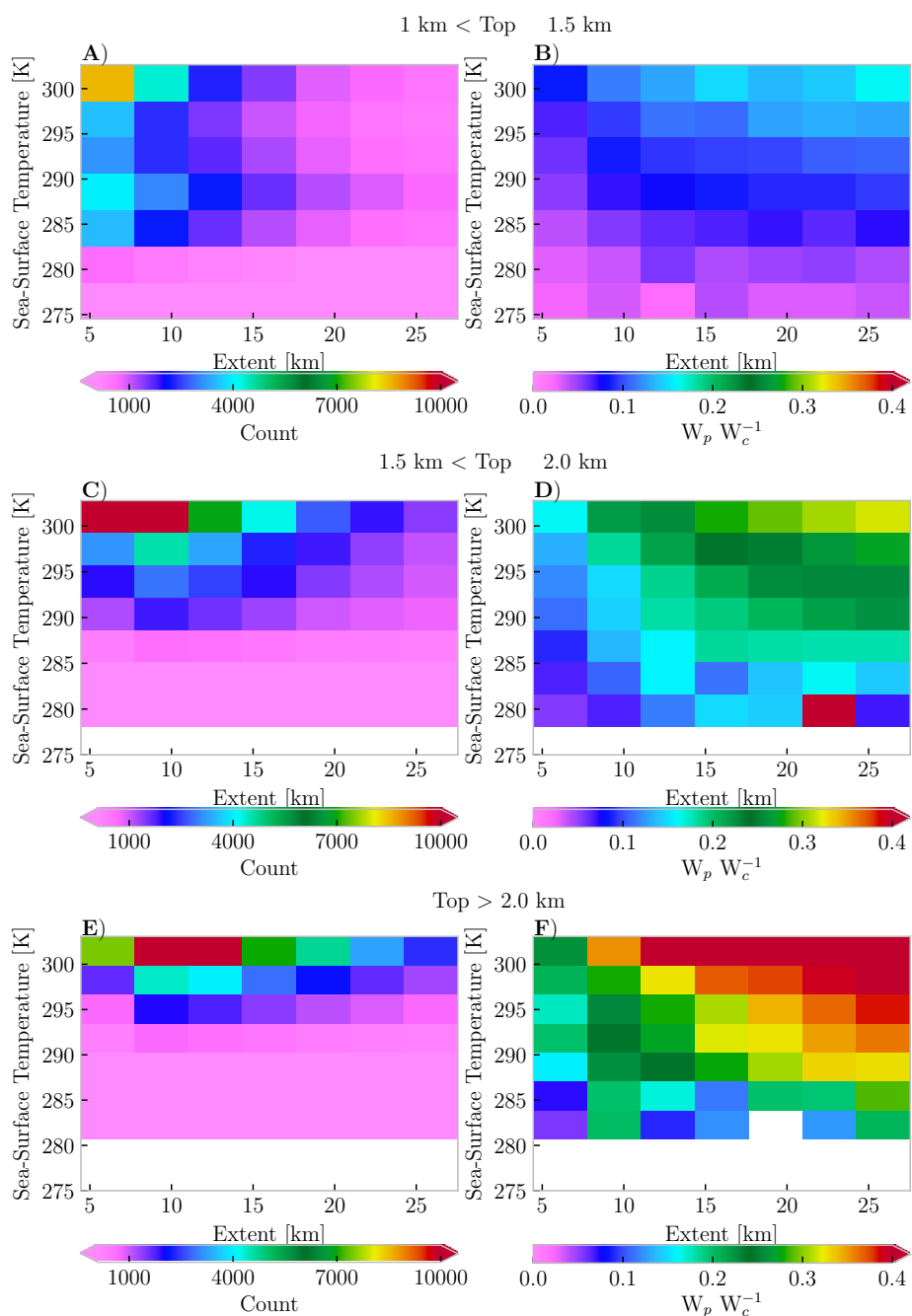


Figure 6. The two-dimensional distribution of extent as a function of sea-surface temperature, conditioned by cloud-top height, is shown in panels A), C), and E) respectively. The median warm rain efficiency ($W_p W_c^{-1}$) as a function of Extent and sea-surface temperature are shown in panels B), D), and F) respectively.