



1 The nature of ice-nucleating particles affects the radiative
2 properties of tropical convective cloud systems

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13

14 **Abstract**

15 Convective cloud systems in the maritime tropics play a critical role in global climate, but accurately representing
16 aerosol interactions within these clouds persists as a major challenge for weather and climate modelling. We quantify
17 the effect of ice-nucleating particles (INP) on the radiative properties of a complex Tropical Atlantic deep convective
18 cloud field using a regional model with an advanced double-moment microphysics scheme. Our results show that the
19 domain-mean daylight outgoing radiation varies by up to 18 W m⁻² depending on the bio- and physico-chemical
20 properties of INP. The key distinction between different INPs is the temperature dependence of ice formation, which
21 alters the vertical distribution of cloud microphysical processes. The controlling effect of the INP temperature
22 dependence is substantial even in the presence of secondary ice production, and the effects of secondary ice
23 formation depend strongly on the nature of the INP. Our results have implications for climate model simulations of
24 tropical clouds and radiation, which currently do not consider a link between INP particle type and ice water content.
25 The results also provide a challenge to the INP measurement community, since we demonstrate that INP
26 concentration measurements are required over the full mixed-phase temperature regime, which covers around 10
27 orders of magnitude in INP concentration.

28



29 **1. Introduction**

30 Deep convective clouds are important drivers of local, regional and global climate and weather (Arakawa, 2004;
31 Lohmann et al., 2016). They produce substantial precipitation (Arakawa, 2004) and the associated phase changes
32 release latent heat that helps to drive global atmospheric circulation (Fan et al., 2012). Convective clouds have a direct
33 impact on climate through interactions with incoming shortwave and outgoing longwave radiation (Lohmann et al.,
34 2016), for example by producing radiatively important long-lived cirrus clouds (Luo and Rossow, 2004). The clouds
35 extend from the warmer lower levels of the atmosphere where only liquid exists to the top of the troposphere where
36 only ice exists (Lohmann et al., 2016). Between these levels is the mixed-phase region where both liquid and ice
37 coexist and interact (Seinfeld and Spyros, 2006). Within the mixed-phase region, primary ice particles can form
38 heterogeneously through the freezing of cloud droplets by ice-nucleating particles (INP). The importance and relative
39 contribution of heterogeneous freezing to ice crystal number concentrations (ICNC) and resultant cloud properties,
40 such as cloud reflectivity, is very uncertain (Cantrell and Heymsfield, 2005; Kanji et al., 2017). This uncertainty stems
41 from the difficulty of predicting INP number concentrations (Kanji et al., 2017; Lacher et al., 2018) as well as the
42 difficulty of quantifying complex interactions between heterogeneous freezing and other ice production mechanisms
43 (Crawford et al., 2012; Huang et al., 2017; Phillips et al., 2005).

44 Understanding the effects of INP on convective clouds presents substantial challenges. Measurements indicate that
45 INP number concentrations can vary by as much as six orders of magnitude at any one temperature (DeMott et al.,
46 2010; Kanji et al., 2017), and large variability exists even in measurements of individual regions or aerosol populations
47 (Boose et al., 2016b; Kanji et al., 2017; Lacher et al., 2018). For example, there are four orders of magnitude variation
48 in summertime measurements of INP number concentrations in the Saharan Air Layer at -33°C (Boose et al., 2016b).
49 Even for particles of similar and known mineralogy, measurements of ice-nucleation efficiency can span several orders
50 of magnitude: The spread in laboratory measurements of ice nucleation active site densities (n_s) for different types of
51 feldspar spans seven orders of magnitude at -15°C (Atkinson et al., 2013; Harrison et al., 2016, 2019). Our ability to
52 understand and quantify such variability in INP concentrations has improved as more measurements have been made.
53 Although meteorological factors are not strong indicators of INP concentrations (Boose et al., 2016a; Lacher et al.,
54 2018), aerosol surface area (Lacher et al., 2018) and diameter (DeMott et al., 2015) provide some predictability and
55 global models based on known INP-active materials show reasonable skill in simulating global INP concentrations
56 (Vergara-Temprado et al., 2017).



57 It is known from model simulations that changes in INP number concentration affect the microphysical properties and
58 behaviour of deep convective clouds (Deng et al., 2018; Fan et al., 2010a, 2010b; Gibbons et al., 2018; Takeishi and
59 Storelvmo, 2018). However, in these model studies perturbations to INP number concentrations have predominantly
60 involved uniform increases in aerosol or INP concentrations with all simulations using the same INP parameterisation
61 (Carrió et al., 2007; Connolly et al., 2006; Deng et al., 2018; Ekman et al., 2007; Fan et al., 2010a; Gibbons et al., 2018;
62 van den Heever et al., 2006; Phillips et al., 2005). Where different INP parameterisations have been used (Eidhammer
63 et al., 2009; Fan et al., 2010b; Liu et al., 2018; Takeishi and Storelvmo, 2018), the results have in most cases been
64 interpreted in terms of the overall increase in INP number concentration (Fan et al., 2010b; Liu et al., 2018; Takeishi
65 and Storelvmo, 2018). However, there are important structural differences between different INP parameterisations
66 that have not yet been explored in detail. For example, currently available and regularly used parameterisations of INP
67 vary substantially in the dependence of INP activity on temperature. We hypothesise that the difference between
68 parameterisations will be particularly important for deep convective clouds because heterogeneous ice formation
69 occurs over a very wide temperature range from just below 0 to around -38°C in the mixed-phase region of these
70 clouds. For the same dust particle concentration, predicted INP concentrations can increase by up to three orders of
71 magnitude from -15 to -20°C (corresponding to approximately 1 km altitude change) using an INP parameterisation
72 with a steep temperature dependence (lower INP concentrations at high temperatures and higher INP concentrations
73 at low temperatures) (Atkinson et al., 2013), but by less than one order of magnitude using an INP parameterisation
74 with a shallower dependence (DeMott et al., 2010; Meyers et al., 1992). We hypothesise that such large differences in
75 ice production rates between INP parameterisations are likely to affect cloud properties. In simulations of deep
76 convective clouds over North America (Takeishi and Storelvmo, 2018) there were differences in the magnitude and
77 altitude of droplet depletion depending on INP parameterisation choice (Bigg, 1953; DeMott et al., 2010, 2015).

78 Uncertainty in mixed-phase cloud properties is compounded further by a lack of quantification of the interaction of
79 heterogeneous freezing with other ice production mechanisms. Ice crystals in the mixed-phase region can also be
80 formed by secondary ice production (SIP) from existing hydrometeors (Field et al., 2017) and droplets can freeze
81 homogeneously below around -33°C (Herbert et al., 2015). In observations of convective clouds with relatively warm
82 cloud-top temperatures (Fridlind et al., 2007; Heymsfield and Willis, 2014; Ladino et al., 2017; Lasher-Trapp et al.,
83 2016; Lawson et al., 2015), ICNC has frequently exceeded INP number concentrations by several orders of magnitude,
84 suggesting that secondary ice production is the dominant small-ice formation mechanism in mixed-phase regions
85 (Ladino et al., 2017). The importance of heterogeneous ice production relative to secondary and homogeneous



86 freezing has therefore been questioned (Ladino et al., 2017; Phillips et al., 2007) and it has been proposed that INP
87 concentrations may only be relevant up to a threshold needed to initiate SIP (Ladino et al., 2017; Phillips et al., 2007),
88 a value that may be as low as 0.01 L^{-1} (Crawford et al., 2012; Huang et al., 2017) for the Hallett Mossop process (Hallett
89 and Mossop, 1974). If this is the case, in clouds where SIP may also be initiated by the primary freezing of a few large
90 ($\sim 1 \text{ mm}$) droplets in a rising parcel (Field et al., 2017), INP number concentrations may be largely irrelevant to cloud
91 ice properties. The effect of INP and INP parameterisation on convective cloud properties must therefore be examined
92 with consideration for the presence of, and interactions with, SIP.

93 Here we explore how the choice of INP parameterisation affects the properties of a large and realistic cloud field
94 containing clouds at all levels as well as deep convective systems in the eastern Tropical Atlantic with a focus on the
95 top of atmosphere (TOA) outgoing radiation. The eastern Tropical Atlantic is an ideal location in which to examine the
96 role of INP concentrations in convective cloud systems because, owing to its position at the interface between the
97 Saharan Air Layer and the Inter Tropical Convergence Zone, it is subject to both high levels of convective activity and
98 high loadings of desert dust, a relatively well-defined INP type (DeMott et al., 2003; Niemand et al., 2012; Price et al.,
99 2018). First, we determine how the presence of INP alters the radiative properties of the cloud field. We then
100 examine how the properties of the simulated cloud field, including cloud shortwave reflectivity, cloud fraction and
101 anvil extent, depend on the choice of INP parameterisation. In particular, we examine the importance of the
102 dependence of INP number concentration on temperature, referred to as INP parameterisation slope herein, as a
103 major factor that determines cloud properties.

104

105 **2. Methods**

106 **2.1. Model set-up**

107 **2.1.1 Regional domain and initial conditions**

108 Simulations described in this article were performed using the Unified Model (UM) version 10.8 (GA6 configuration)
109 (Walters et al., 2017). The UM is a numerical weather prediction model developed by the UK Met Office. We use a
110 regional nest within the global model simulation, which has a grid spacing of 1 km (900×700 grid points) and 70
111 vertical levels. Meteorology of the driving global model is based on operational analysis data. Within the nested
112 domain, the Cloud AeroSol Interacting Microphysics scheme (CASIM) is employed to handle cloud microphysical



113 properties. The Met Office global model is used to initialise the nested simulation at 00:00 on the 21st of August 2015
114 and is used throughout the simulation for the boundary conditions.

115 The 21st of August 2015 was chosen for simulation to coincide with flight b933 of the Ice in Clouds Experiment – Dust
116 (ICE-D) July-August 2015 field campaign that targeted convective clouds extending to and beyond the freezing level.
117 The aerosol profile measured during flight b933 (Fig. A1a) was used to derive the aerosol profiles prescribed over the
118 nested domain at the beginning of the simulation and are constantly applied at the boundaries. Model profiles were
119 calculated as follows: The UM vn 10.3 was used to simulate a domain comprising the entire Tropical Atlantic and West
120 Africa. This simulation was initiated on the 18th August 2015 with a grid spacing of 8 km using the UM operational one-
121 moment microphysics (i.e. not CASIM) and the CLASSIC aerosol scheme with a 6-bin dust model (Johnson et al.,
122 2015a). On the day of the b933 flight (21st August 2015), a dust layer was present between 2 and 3 km altitude.
123 Comparison to MODIS AOD data indicates agreement between the model and observations (not shown). This UM vn
124 10.3 simulation was used to calculate the average dust profile (mass and number concentration) over the CASIM
125 domain on the 21st of August 2015 and these dust profiles are applied in the nested domain as the insoluble aerosol
126 profiles (Fig. A1a). The approximate difference between the dust aerosol profile provided by the UM regional
127 simulation and the observed aerosol profile measured during flight b933 (comprising both insoluble and soluble
128 particles) is used as the soluble aerosol profile (Fig. A1a). The simulations are 24 hours in length.

129 **2.1.2. CASIM microphysics**

130 CASIM is a multi-moment bulk scheme, which is configured to be two-moment in this work. Both number
131 concentration and mass concentration for each of the five hydrometeor classes (cloud droplets, rain droplets, ice
132 crystals, graupel, snow) are prognostic variables. The model set-up is very similar to that used in Miltenberger et al.
133 (2018) including the parameter choices within CASIM. CASIM has been used and tested previously in simulations of
134 coastal mixed-phase convective clouds (Miltenberger et al., 2018), South-East Pacific stratocumulus clouds (Grosvenor
135 et al., 2017), Southern Ocean supercooled shallow cumulus (Vergara-Temprado et al., 2018), midlatitude cyclones
136 (McCoy et al., 2018) and CCN-limited Arctic clouds (Stevens et al., 2018).

137 Cloud droplet activation is parameterised according to (Abdul-Razzak and Ghan, 2000). The soluble accumulation
138 mode aerosol profile shown in Fig. A1a is used for cloud droplet activation and a simplistic CCN activation
139 parameterisation is included for the insoluble aerosol mode (Abdul-Razzak and Ghan, 2000) that assumes a 5% soluble
140 fraction on dust. Scavenging is not represented. Collision-coalescence, riming of ice crystals to graupel and



141 aggregation of ice crystals to snow is represented. Rain drop freezing is described using the parameterisation of Bigg
142 (1953). For reference, the modelled domain-mean out-of-cloud temperature and relative humidity are shown in Fig.
143 A1b. The model time-step is 5 seconds.

144 Heterogeneous ice nucleation is represented using 5 different parameterisations: Cooper (1986) (C86), Meyers et al.
145 (1992) (M92), DeMott et al. (2010b) (D10), Niemand et al. (2012) (N12) and Atkinson et al. (2013) (A13) (Fig. 1). C86
146 and M92 calculate a freezing rate based on temperature and are independent of aerosol concentration. D10
147 calculates an INP concentration from temperature and the concentration of insoluble aerosol with a diameter greater
148 than 0.5 μm . N12 and A13 calculate an INP concentration from the temperature dependent active surface site density
149 and the surface area of insoluble aerosol (n_s). For A13, a potassium-feldspar fraction of 0.25 is assumed. This is the
150 upper recommended fraction (Atkinson et al., 2013) which was deemed appropriate because of the study region's
151 exposure to Saharan dust outflow. M92 is described as a deposition and condensation freezing parameterisation
152 (Meyers et al., 1992) and is often used alongside an immersion freezing parameterisation in modelling studies (Deng
153 et al., 2018; Fan et al., 2010b, 2010a; Gibbons et al., 2018). However, the M92 parameterisation is based on aircraft
154 continuous flow diffusion chamber measurements and those measurements should capture all relevant nucleation
155 mechanisms (see Vali et al., 2015). To represent nucleation at conditions relevant for clouds with liquid water present,
156 we have set the saturation term in the M92 parameterisation to water saturation. One simulation is conducted with
157 no active heterogeneous ice nucleation representation (NoINP). The INP parameterisations inspect the conditions and
158 aerosol concentrations within a gridbox and use that information to predict an ice production rate via heterogeneous
159 freezing. The supercooled droplets are depleted by the freezing parameterisation, but scavenging of INPs is not
160 represented. Homogeneous freezing of cloud droplets is parameterised according to Jeffery and Austin (1997).

161 Secondary ice production (SIP) is represented using an approximation of the Hallett Mossop process which occurs
162 between -2.5 and -7.5°C. The efficiency of the Hallett Mossop process increases from -2.5 and -7.5°C to 100% at -5°C.
163 The rate of splinter production per rimed mass is prescribed with 350 new ice splinters produced per milligram of rime
164 at -5°C. The ice splinters produced by the representation of the Hallett Mossop process are the smallest allowable size
165 of ice in the model (i.e. 10^{-18} kg). The rate of splinter production by the Hallett Mossop process is based on the best
166 available estimate of the efficacy of the mechanism (Connolly et al., 2006; Hallett and Mossop, 1974; Mossop, 1985).
167 In-situ cloud observations have frequently observed ICNC that could be explained by the Hallett Mossop process, but
168 the mechanism underlying the Hallett Mossop process as well as the ice particle production rate remain uncertain and
169 not well quantified (Field et al., 2017). A maximum splinter production rate of 350 per milligram of rimed material has



170 been measured in a number of laboratory studies (Hallett and Mossop, 1974; Mossop, 1985) and has been applied as
171 the best estimate here and in previous modelling studies (Connolly et al., 2006), although other rates have also been
172 measured (Heymsfield and Mossop, 1984; Saunders and Hosseini, 2001). Uncertainties regarding the rate of splinter
173 production by Hallett Mossop are an important consideration that will be investigated in future work; this study
174 explores the structural uncertainty of the presence/absence of the Hallett Mossop process as currently understood.
175 Other mechanisms of SIP such as collision fragmentation, droplet shattering and sublimation fragmentation have
176 been proposed (Field et al., 2017), but are not represented in these simulations, in part because they are very poorly
177 defined and it is not clear how important they are. Other studies have attempted to model some of these additional
178 SIP processes (Phillips et al., 2018; Sullivan et al., 2018) but that was beyond the scope of this study.

179 **2.1.3. Cloud radiation**

180 The radiative processes are represented by the Suite of Community RAdiative Transfer codes based on Edwards and
181 Slingo (SOCRATES) (Edwards and Slingo, 1996; Manners et al., 2017), which considers cloud droplet number and mass,
182 as well as ice crystal and snow water paths for the calculation of cloud radiative properties. It does not respond to
183 changes in ice crystal or snow number concentration, or any changes to rain or graupel species. The cloud droplet
184 single scattering properties are calculated from the cloud droplet mass and effective radius in each gridbox using the
185 equations detailed in Edwards and Slingo (1996). Snow and ice are combined to form one ice category for the
186 purposes of the radiation calculations. The single scattering properties of this snow and ice category are calculated
187 from their combined mass and the ambient temperature. The parameterisation of bulk optical properties of snow and
188 ice used in the model is detailed in Baran et al. (2014).

189 The radiative properties (shortwave, longwave and total radiation) are calculated for daylight hours only, i.e. 10:00-
190 17:00 UTC. For all other modelled properties presented, except when plotted against a corresponding radiative
191 property, values are calculated for the last 14 hours of the simulation, i.e. from 10:00 - 24:00. The sensitivity of
192 analysis to time period selection was tested and found to have little impact.

193 Changes to outgoing radiation from cloudy regions and changes in cloud fraction both contribute to the total overall
194 change in outgoing radiation between two simulations. The contributions from changes in outgoing radiation from
195 cloudy regions and cloud fraction to the overall radiative differences between simulations were calculated separately
196 as described below. The cloudy regions contribution (ΔRad_{REFL}) to a domain radiative difference between two
197 simulations s and r ($s - r$) is calculated using Eq. (1).



$$\Delta Rad_{REFL} = c_{f_r} \times \Delta Rad_{cl} \quad (1)$$

199 where c_{f_r} is the cloud fraction of simulation r and ΔRad_{cl} is the change in outgoing radiation from cloudy areas only
200 between simulations ($s - r$). The cloud fraction contribution (ΔRad_{CF}) is calculated using Eq. (2).

$$\Delta Rad_{CF} = (Rad_{r,cl} - Rad_{r,cs}) \times \Delta cf \quad (2)$$

202 Where $Rad_{r,cl}$ is the mean outgoing radiation from cloudy regions in simulation r and $Rad_{r,cs}$ is the mean outgoing
203 radiation from clear sky regions in simulation r and Δcf is the difference in cloud fraction between simulations s and r
204 ($s-r$). There is interaction between the outgoing radiation from cloudy regions and cloud fraction changes (ΔRad_{INT})
205 which is calculated in Eq (3).

$$\Delta Rad_{INT} = \Delta Rad_{cl} \times \Delta cf + \Delta Rad_{cs} \times (1 - c_{f_s}) \quad (3)$$

207 Where ΔRad_{cs} is the change in mean outgoing radiation from clear sky areas between simulations s and r and c_{f_s} is
208 the cloud fraction of simulation s .

209 The total outgoing radiation difference between simulations s and r (ΔRad_{s-r}) is therefore as shown in Eq. (4).

$$\Delta Rad_{s-r} = Rad_s - Rad_r = \Delta Rad_{REFL} + \Delta Rad_{CF} + \Delta Rad_{INT} \quad (4)$$

211 The interaction term ΔRad_{INT} was found to be negligible and was therefore ignored for the purpose of this paper.

212 2.1.4. Model simulations

213 The conducted simulations are as follows:

- 214 - Five simulations with different heterogeneous ice nucleation parameterisations (C86, M92, D10, N12 and
215 A13) with a representation of the Hallett Mossop process (SIP_active).
- 216 - One simulation with no heterogeneous ice nucleation (NoINP), but with a representation of the Hallett
217 Mossop process (SIP_active).
- 218 - Five simulations with different heterogeneous ice nucleation parameterisations (C86, M92, D10, N12 and
219 A13) without a representation of the Hallett Mossop process (SIP_inactive).

220 The INP number concentration ([INP]) predicted by the five INP parameterisations (C86, M92, D10, N12, A13) are
221 compared with the available measurements from the study region (Price et al., 2018; Welte et al., 2018) in Fig. 1,



222 including those taken during the ICE-D field campaign (Price et al., 2018). All parameterisations are in reasonable
223 agreement with the measurements (and with each other) at around -17°C , but deviate strongly at higher and lower
224 temperatures. Importantly, the INP parameterisation slopes of the chosen parameterisations span the range used
225 within regional models (from a shallow $\text{dlog}_{10}[\text{INP}]/\text{dT} = -0.07$ in M92 (Meyers et al., 1992) to a steep $\text{dlog}_{10}[\text{INP}]/\text{dT} =$
226 -0.45 in A13 (Atkinson et al., 2013)).

227 When analysing the simulation output, cloudy grid boxes were classed as those containing more than $10^{-5} \text{ kg kg}^{-1}$
228 condensed water from cloud droplets, ice crystals, graupel and snow. Rain was not included to ensure analysis did not
229 include areas below cloud base. Other cloud thresholds were tested and found to have no notable effect on the
230 results. For cloud categorisation into low, mid and high clouds, model vertical columns containing cloudy grid boxes
231 were categorised by cloud altitude. Low cloud occurs below 4km, mid cloud between 4 and 9 km and high cloud above
232 9 km. Columns with cloudy grid boxes in two or more cloud categories were classified as mixed category columns
233 according to the vertical placement of the cloudy grid boxes, e.g. low/high for columns containing cloud below 4 km
234 and above 9 km. 4 and 9 km were chosen as the low/mid and mid/high division points because they are just below
235 two well-defined peaks in cloud base heights (not shown) and roughly correspond to the beginning of the
236 heterogeneous and homogeneous freezing regions, respectively.

237 **2.2. The observed case**

238 MODIS visible images of the 21st August 2015 are shown in Fig. 2 (a, b) alongside a time series of snapshots of the TOA
239 outgoing longwave radiation in our one of our simulations (c - h). The simulated cloud field has more cloud-free areas
240 than the satellite images but in general produces clouds similar to those shown in the satellite image and in
241 approximately the correct location. Overall the simulations produce a complex and realistic cloud field. Snapshots of
242 the simulated model TOA outgoing shortwave radiation are shown in Fig. A2.

243 In-situ measurements of cloud and aerosol properties were made using the UK FAAM Bae-146 research aircraft, which
244 was flown from Praia, Cape Verde Islands. An extensive suite of in-situ aerosol and cloud particle instruments were
245 operated onboard the aircraft and are described in detail in Lloyd et al. (2019). The aircraft penetrated the growing
246 convective clouds at a range of altitudes from just below the freezing level up to -20°C . In order to show that the
247 model reproduces the observed conditions, the observational data were compared to the conditions in modelled
248 clouds of similar size to those the aircraft flew in ($10 - 150 \text{ km}^2$) where a comparison was thought appropriate.
249 Comparisons of a selection of simulated cloud properties with aircraft data are shown in Fig. A3. In-cloud



250 measurements from the aircraft were selected using the same total water content threshold as for the model data
251 (10^{-5} kg kg⁻¹). Note that observational data only samples clouds along the 1D flight path, while model results include all
252 grid points inside the selected clouds.

253 The vertical wind and cloud droplet and ice number concentrations are shown Fig. A3. The vertical wind speeds from
254 the model and aircraft measurements agree well (Fig. A3a). The aircraft data exhibit less measurements of vertical
255 wind speeds above 10 m s⁻¹ but that is expected since the aircraft was purposefully not flow in very high updraft
256 speeds. The aircraft cloud droplet number concentration (CDNC), measured using a DMT cloud droplet probe, falls
257 predominantly in the regions of parameter space most highly populated by model data when plotted against vertical
258 wind speed (Fig. A3b). Note that the simulated points in Figure A1b represent values of CDNC and updraft speed in all
259 cloudy gridboxes, not just those at cloud base. The updraft speed is collocated with CDNC and therefore does not
260 necessarily represent the updraft speed at which the cloud droplets were activated. The higher CDNC values exhibited
261 in the model data may be due to the higher updraft speeds which were not measured by the aircraft. The observed
262 ICNC was derived from measurements using the DMT Cloud Imaging Probes (CIP-15 and CIP-100) and the SPEC
263 Stereoscopic optical array probe covering a size range from 10 to 6200 μ m using the SODA2 processing code to
264 reconstruct ice particle images that are fully contained within the probe sample volume. Because of uncertainties in
265 the optical array probe sample volume for very small images, only ice particle images greater than 100 μ m were
266 included. The aircraft ICNC fall almost entirely within the range of the model values (Fig. A3c).

267

268 **3. Results**

269 **3.1. Effect of INP and INP parameterisation on outgoing radiation**

270

271 We first examine the effect of INP parameterisation on the outgoing radiation relative to the simulation where the
272 only source of primary ice production was through homogeneous freezing (NoINP). When contrasting the effect of
273 different INP parameterisations in Sect 3.1-3.4, the Hallett Mossop process was always active. As stated in Sect. 2.1.3,
274 the radiation code is represented by the Suite Of Community RAdiative Transfer codes based on Edwards and Slingo
275 (SOCRATES) (Edwards and Slingo, 1996; Manners et al., 2017), and responds to changes in cloud droplet number and
276 cloud droplet, ice crystal and snow mass. The results detailed below relate to either the domain-wide properties or all



277 in-cloud regions within the domain. This means that the results describe the direct and indirect changes occurring due
278 to INP across all cloud present in the domain, including low-level liquid clouds, mixed-phase clouds without a
279 convective anvil and very deep convective clouds with an anvil. The effects of INP parameterisation and SIP on
280 convective anvils are discussed in Sect. 3.4.

281 Domain-mean TOA outgoing radiation (daylight hours, shortwave plus longwave) is enhanced by the inclusion of INP
282 in all cases (Fig. 3a). The enhancement in outgoing radiation varies between 2.6 W m^{-2} for D10 and 20.8 W m^{-2} for A13
283 relative to the NoINP simulation. There is a variation of up to 18.2 W m^{-2} depending on the chosen representation of
284 heterogeneous ice nucleation, which shows that the INP parameterisation can affect outgoing radiation as much as
285 excluding or including heterogeneous freezing altogether. Radiative changes from the NoINP simulation due to the
286 inclusion of INP are caused mainly by changes to outgoing shortwave radiation. The inclusion of INP enhances
287 outgoing shortwave radiation by between 5.3 W m^{-2} for D10 and 26.6 W m^{-2} for A13 (Fig. A4a). Differences in outgoing
288 longwave radiation are comparatively small (-2.7 W m^{-2} for D10 to -5.8 W m^{-2} for A13; Fig. A4b) due to similar cloud
289 top heights between simulations of these thermodynamically limited clouds. Bear in mind that SIP was active
290 (SIP_active) in the simulations summarised in Fig. 3a, indicating that these cloud systems are sensitive to INP even in
291 the presence of SIP. This is consistent with a comparatively small change in TOA radiation when SIP is active relative to
292 when it is inactive (Fig. 3b and 3c) (we discuss the role of SIP in more detail in Sect. 3.5).

293 The slope of the INP parameterisation is a key determinant of the outgoing radiation. There is a statistically significant
294 correlation between INP parameterisation slope and total TOA outgoing radiation ($r^2 = 0.75$, $p < 0.01$, $n = 10$) (Fig. 3c).
295 Changes in outgoing radiation due to the presence of INP are caused by a combination of changes to the outgoing
296 radiation from cloudy regions, caused by changes in cloud structure and microphysical properties, and changes to
297 domain cloud fraction, whose contributions to the total radiative difference are shown in Fig. 3a (left and centre). In
298 order to appreciate the reasons for these trends, we will now take a closer look at the effect of INP on outgoing
299 radiation from cloudy regions only, domain cloud fraction and cloud type.

300 **3.2. Effect of INP and INP parameterisation on outgoing radiation from cloudy regions**

301 Here we discuss the changes in outgoing radiation from cloudy regions only due to INP parameterisation choice.
302 Daytime outgoing radiation from cloudy regions increases due to INP for all but one INP parameterisation (Fig. 4a).
303 The absolute change in outgoing radiation from cloudy regions is between -0.8 (D10) and $+28.1$ (A13) W m^{-2} , and the
304 larger values are a result of large increases in reflected shortwave (up to $+37.2 \text{ W m}^{-2}$) and relatively moderate



305 decreases in outgoing longwave radiation (up to -11.1 W m^{-2}) from cloudy regions. The above absolute changes in
306 outgoing radiation from cloudy regions contribute between -0.7 and $+11.4 \text{ W m}^{-2}$ to the domain-mean change in
307 outgoing radiation due to the presence of INP (Fig. 3a, cloudy regions contribution).

308 The enhancement of outgoing radiation from cloudy regions due to INP is caused primarily by increases in cloud
309 condensate relative to the NoINP simulation (Fig. 4b). When INP are included in a simulation, snow and cloud droplet
310 water path are enhanced, causing increases in total cloud condensate, despite decreases (in all except A13) in ice
311 crystal water path. Snow, cloud droplets and ice crystals are the hydrometeors that affect outgoing radiation in CASIM
312 and the combined water path of these three species is significantly positively correlated with cloud shortwave
313 reflectivity ($r^2 = 0.62$, $p < 0.01$, $n = 11$) (Fig. 4c). The mechanism for this INP induced increase in cloud condensate and
314 consequently cloud shortwave reflectivity is as follows: When heterogeneous ice nucleation is active, liquid is
315 consumed in the warmer regions of mixed-phase clouds because of increased heterogeneous ice nucleation (Fig. 1)
316 and SIP (Fig. A5a). The resultant additional ice crystals in mixed-phase regions facilitate riming causing increases in
317 snow and graupel (Fig. A5c, d), increasing snow water path and reflectivity in mixed-phase and ice clouds. At the same
318 time, the enhanced production of relatively heavy snow and graupel increases precipitation which on evaporation
319 below 4 km, reduces out-of-cloud temperature and increases relative humidity (Fig. A6a, b). This leads to increases in
320 water path in low-level liquid clouds and thus an enhancement in their shortwave reflectivity.

321 However, increases in total cloud condensate alone cannot account for the differences in outgoing radiation from
322 cloudy regions between simulations using different INP parameterisations, which are caused by a combination of
323 cloud microphysical responses. We find that outgoing radiation from cloudy regions is significantly negatively
324 correlated with INP parameterisation slope ($r^2 = 0.63$, $p < 0.01$, $n = 10$) (Fig. 5a), i.e. simulations using a steep INP
325 parameterisation have a higher outgoing radiation from cloudy regions. This result makes sense when we consider the
326 relationships between INP parameterisation slope and a multitude of cloud microphysical properties affecting cloud
327 radiative properties. In particular, a steep INP parameterisation results in a mixed-phase cloud region characterised by
328 a higher ice crystal water path aloft ($r^2 = 0.80$, $p < 0.01$, $n = 10$; Fig. 5b) and higher cloud droplet number
329 concentrations at the bottom of the mixed-phase region ($r^2 = 0.89$, $p < 0.01$, $n = 10$; Fig. 5c) when compared to
330 shallower parameterisations. A steeper INP parameterisation slope allows increased transport of liquid to upper cloud
331 levels due to lower rates of heterogeneous freezing (Fig. 1) and SIP at high temperatures (Fig. A5a). This, combined
332 with higher INP concentrations at low temperatures (Fig. 1), increases ICNC at upper mixed-phase altitudes, as well as



333 enhancing the lifetime of liquid cloud droplets at lower altitudes in the mixed-phase region when compared to
334 shallower INP parameterisations.

335 **3.3. Effect of INP and INP parameterisation on cloud fraction**

336 Overall cloud fraction is increased by INP for all INP parameterisations and these increases in cloud fraction contribute
337 about as much to changes in domain-mean radiation as the changes in outgoing radiation from cloudy regions (Fig. 3a,
338 cloud fraction contribution). Increases in domain cloud fraction due to INP are driven by cloud cover increases in the
339 warm and mixed-phase regions of the cloud (~ 4 -6 km), offset somewhat by decreases in the homogeneous freezing
340 regime (~ 10 - 14 km) (Fig. 6a). Cloud fraction increases at mid-levels occur because heterogeneous ice nucleation
341 induces an increase in precipitation-sized particles (snow and graupel) which sediment to lower levels and moisten the
342 atmosphere by evaporation (Fig. A6a, b). This increases new cloud formation and may prolong the lifetime of existing
343 cloud cells. Additionally, increased droplet freezing and riming in the mixed-phase cloud region releases latent heat
344 and invigorates cloud development with increases in updraft speed just above 4 km (Fig. A6c). The increased cloud
345 fraction at mid-levels due to INP are partially offset by a reduced cloud fraction above 10 km (Fig. 6a) which is caused
346 by an INP induced enhancement in freezing and riming in the mixed-phase region reducing moisture transport to the
347 homogeneous freezing regime.

348 The effects of INP on the altitude profile of cloud fraction are strongest for shallow INP parameterisation slopes, which
349 have a freezing profile most different to that of the NoINP simulation (Fig. 6a). At 5 km, the shallowest
350 parameterisation (M92) causes the largest increase in cloud fraction, while the steepest parameterisation (A13)
351 causes the smallest ($r^2 = 0.83$, $p < 0.05$, $n = 5$). At 12 km, the order is reversed, and steep parameterisations exhibit the
352 highest cloud fraction ($r^2 = 0.94$, $p < 0.01$, $n = 5$). The largest cloud fraction-induced increases in outgoing radiation
353 relative to the NoINP simulation (Fig. 3a) are seen in simulations using steeper INP parameterisations because these
354 simulations exhibit higher cloud fractions at high altitudes (~12 km), translating into the higher total cloud fraction.
355 These slope dependent changes in cloud fraction are explained by a relationship between cloud fraction and several
356 microphysical properties affecting cloud fraction. For example, steeper INP parameterisations produce higher ICNC at
357 the top of the mixed-phase region (10 km) as well as higher ratios of ice crystal mass to snow and graupel mass within
358 the homogeneous freezing region (12 km) (Fig. 6b, c). A higher number and mass of ice crystals relative to those of
359 larger precipitation-sized hydrometeors with the steepest parameterisations results in lower frozen hydrometeor
360 sedimentation, a longer cloud lifetime and a higher cloud fraction.



361 **3.4. Effect of INP and INP parameterisation on cirrus anvils**

362 Our results show that the INP parameterisation affects the properties and spatial extent of cirrus anvils. We define
363 cirrus anvils to be regions where cloud is present above 9 km only (further details available in Sect. 2.1.4). 2D aerial
364 images of cloud categorisation (Fig. 7a-f) show well-defined regions of anvil cloud (light blue - H) surrounding a large
365 convective system containing clouds at a range of altitudes from <4 km to >9 km. There are clearly differences in the
366 extent and position of cloud categories between simulations (Fig. 7a -f).

367 The presence of INP reduces convective anvil extent by between 2.1 and 4.1% of the domain area depending on the
368 choice of INP parameterisation (Fig. 7 g), corresponding to a decrease in anvil cloud of between 22 and 53% relative to
369 the NoINP simulation (not shown). The reduction in anvil extent in the presence of INP is caused by increased liquid
370 consumption at all mixed-phase levels, due to heterogeneous freezing, enhanced SIP and increased graupel and snow
371 production, reducing the availability of cloud droplets for homogeneous freezing (Fig. A5b), reducing ICNC at cloud-
372 top, and reducing cloud anvil extent (Fig. 7g).

373 Reductions in anvil extent caused by INP are somewhat offset by the overall increases in cloud fraction across the
374 domain (Fig. 7g). However, it is possible that the effect of INP and INP parameterisation choice on anvil cloud fraction,
375 and the contribution of anvil cloud to overall cloud fraction and radiative changes, would become larger with a longer
376 analysis period. This is because detrained convective anvils can persist longer in the atmosphere than the convective
377 core that creates them (Luo and Rossow, 2004; Mace et al., 2006), but this is beyond the scope of the current study.

378 **3.5. Importance of secondary ice production**

379 It has been argued that primary ice particle production rate is unimportant for convective cloud properties when
380 secondary ice production (SIP) is active (Fridlind et al., 2007; Heymsfield and Willis, 2014; Ladino et al., 2017; Lawson
381 et al., 2015) because primary ice crystal concentrations are often overwhelmed by ice crystals formed via SIP (Field et
382 al., 2017). However, the results shown in Fig. 3a (in which the simulations included SIP) do not support this argument.
383 We find that the microphysical and radiative properties of the cloud field depend strongly on the properties of the INP
384 even with SIP (Hallett-Mossop process) occurs. Furthermore, the effect of including SIP on daylight domain-mean
385 outgoing radiation varies between -2.0 W m^{-2} and $+6.6 \text{ W m}^{-2}$ (Fig. 3b), showing that SIP has a smaller effect than the
386 INP parameterisation. Furthermore, the effect of SIP depends on the INP parameterisation. Therefore, rather than
387 primary ice being simply overwhelmed by SIP, it actually determines how SIP affects cloud microphysics.



388 The effect of SIP on the radiative properties of the cloud field is dependent on INP parameterisation choice, both in
389 magnitude and sign of change (Fig. 3b). SIP makes the clouds more reflective independent of the chosen
390 parameterisation (Fig. 3b, cloudy regions contribution) due to increases in snow and cloud droplet water path. N12
391 and A13 have the largest overall radiative response to SIP because changes to the radiative forcing from cloudy
392 regions and cloud fraction contributions act to increase outgoing radiation (Fig. 3b). However, the cloud fraction
393 response to SIP is opposite for C86, M92 and D10 meaning the cloudy regions and cloud fraction contributions act in
394 opposite directions, reducing the total radiative forcing.

395 The different response of the domain cloud fraction to the presence of SIP is caused by substantial variation between
396 simulations in the anvil cloud extent (Fig. 7h), from an increase of 10% (+0.9% of the domain area) in N12 to a
397 decrease of 40% (-3.6% of the domain area) in M92 (Fig. 7h). These non-uniform changes in cloud fraction and
398 outgoing radiation can be explained by differences in the response of cloud freezing profiles to SIP due to variations in
399 INP parameterisation slope. For all INP parameterisations, SIP reduces the availability of liquid at higher altitudes. For
400 shallower parameterisations such as M92 this causes a reduction in the amount of cloud droplets reaching the
401 homogeneous freezing regime and thereby reduces ICNC and cloud anvil spatial extent. However, in simulations using
402 a steep parameterisation, almost all available droplets are frozen heterogeneously before they reach the
403 homogeneous regime (see reduced homogeneous ice production rates in N12 and A13 in Fig. A5b). Therefore, in
404 simulations using a steeper parameterisation, such as N12, a reduction in liquid availability due to SIP occurs at the
405 top of the heterogeneous freezing regime, reducing the availability of liquid for riming, causing a reduction in frozen
406 hydrometeor size at high altitudes, a reduction in hydrometeor sedimentation and an increase in anvil extent. Overall,
407 our simulations show that INP parameterisation choice and slope is an important determinant of cloud field micro-
408 and macrophysical properties, even when SIP is active, and that choice of INP parameterisation affects the cloud field
409 response to SIP.

410

411 **4. Limitations of this modelling study**

412 The lack of consideration of ice and snow particle number by the SOCRATES radiation scheme is an important
413 limitation of the results presented here. Changes to ICNC, without a co-occurring change in ice crystal mass
414 concentrations, will not be reflected in modelled radiative fluxes. However, our results are still very relevant for



415 climate model simulations as climate models do not typically represent ICNCs and have frequently been shown to
416 poorly represent ice crystal mass concentrations (Baran et al., 2014; Waliser et al., 2009). The SOCRATES
417 representation of radiation with a dependence on ice mass is a more accurate and realistic representation of radiation
418 than is seen in many climate models which often derive bulk optical properties using empirically derived deterministic
419 relationships between ice particle size and environmental temperature and/or ice water content (Baran et al., 2014;
420 Edwards et al., 2007; Fu et al., 1999; Gu et al., 2011). However, the effect of INP parameterisation on deep convective
421 clouds radiative properties using a radiation code that considers ice particle number should be explored in future
422 studies. The sensitivity of the cloud field to the chosen INP parameterisation and SIP indicates the importance of
423 accurately representing ice water content in climate models and linking this ice water content to ice-nucleating
424 particle type.

425 Another limitation of the SOCRATES radiation code is its lack of consideration of rain and graupel particles. The effects
426 of these hydrometeors are expected to be less than that of ice, snow and cloud droplets as they precipitate faster and
427 therefore have a shorter lifetime. Furthermore, the effect of graupel on the tropical longwave radiative effect has
428 been found to be negligible and dwarfed by that of snow (Chen et al., 2018). The global radiative effect of rain has also
429 been found to be small in the vast majority of cases even at high temporal and spatial resolution (Hill et al., 2018). The
430 effect of the incorporation of these hydrometeors into radiative transfer parameterisations should however be tested
431 in future studies.

432 The use of both aerosol-dependent (D10, N12, A13) and solely-temperature dependent (C86, M92) parameterisations
433 in this study means that we have examined the radiative sensitivity of a complex cloud field to a larger variety of INP
434 parameterisations used in weather and climate models than if we had exclusively used parameterisations that
435 consider aerosol concentration. However, this experimental design has limitations. For example, due to the lack of
436 aerosol dependence of the C86 and M92 schemes a 'presumed' dust concentration is implicitly present in these two
437 cases and remains uniform throughout the simulation period. The effect of INP parameterisation choice on convective
438 cloud field properties should also be examined with the inclusion of aerosol scavenging but this was beyond the scope
439 of this study.

440 This study utilised our best estimate of ice production by the Hallett Mossop process (Connolly et al., 2006; Hallett and
441 Mossop, 1974; Mossop, 1985), the most well-studied SIP mechanism, to try and understand the effect of the process,
442 as currently understood, on deep convective cloud properties. However, this rate of ice production is very uncertain



443 and other mechanisms of SIP have also been proposed (Field et al., 2017). Future work will attempt to overcome the
444 above caveats by using statistical emulation (Johnson et al., 2015b) to examine the interacting effects of dust number
445 concentration, INP parameterisation slope and SIP in an idealised deep convective cloud.

446

447 5. Conclusions

448 We quantified the effect of INP parameterisation choice on the radiative properties of a deep convective cloud field
449 using a regional model with advanced double-moment capabilities. The simulated domain exceeds 600,000 km² and
450 therefore captures the effects of INP and INP parameterisation on a typical large, complex and heterogeneous
451 convective cloud field. The presence of INP increases domain-mean daylight TOA outgoing radiation by between 2.6
452 and 20.8 W m⁻² and the choice of INP parameterisation can have as large an effect on cloud field properties as the
453 inclusion or exclusion of INP. These effects are evident even in the presence of SIP, refuting the hypothesis that INP is
454 irrelevant beyond a minimum concentration needed to initiate SIP (Crawford et al., 2012; Ladino et al., 2017; Lawson
455 et al., 2015; Phillips et al., 2007). Furthermore, the effects of SIP on the cloud field properties are strongly dependent
456 on INP parameterisation choice. Both the magnitude and direction of change in cloud fraction and total outgoing
457 radiation due to SIP varies according to INP parameterisation choice. Microphysical alterations to cloud properties are
458 important contributors to radiative differences between simulations, in agreement with previous studies documenting
459 the effect of aerosol-cloud interactions to the radiative forcing by deep convective clouds (Fan et al., 2013). For
460 example, increasing cloud condensation nuclei concentrations, with no perturbations to INP, was shown to increase
461 cloud albedo and cloud fraction, deepen clouds and increase TOA outgoing radiation by 2-4 W m⁻² (Fan et al., 2013).
462 Here we find that even for the same aerosol and CCN concentrations, just altering the relationship between aerosol
463 concentration and ice-nucleating ability can cause changes in daylight TOA outgoing radiation of up to 18.2 W m⁻² in
464 our domain.

465 Our results indicate that the slope of the INP parameterisation with respect to temperature ($d\log[\text{INP}]/dT$) is
466 particularly important: Outgoing total radiation, along with many cloud field and microphysical properties affecting
467 radiation, were significantly correlated with INP parameterisation slope. Best practise for accurately representing INP
468 number concentrations based on current knowledge is to utilise parameterisations that link aerosol number and
469 particle size to INP number concentration (e.g. D10, N12, A13) but that is not enough without also using a



470 parameterisation in which the temperature dependence of the INP number concentrations matches reality; the
471 largest differences in domain outgoing radiation existed in this study between simulations using aerosol dependent
472 parameterisations (D10 and A13). These large variations in outgoing radiation between simulations using different
473 aerosol dependent INP parameterisations justifies investment in observational campaigns to more effectively
474 constrain the range of expected INP concentrations and parameterisation slopes in the Saharan dust outflow region,
475 and other regions dominated by maritime deep convective activity.

476 The significance of the slope of the INP parameterisation indicates the potential importance of accounting for
477 differences in aerosol composition in modelling studies. For example, INP derived from marine organics (Wilson et al.,
478 2015) have a shallower slope than mineral dust INP (Atkinson et al., 2013; Niemand et al., 2012). Furthermore, real-
479 world INP concentrations are known to have complex temperature dependencies with biological INP, such as soil
480 borne fungus and plant related bacteria, making significant contributions at the warmest temperatures and mineral
481 components being more important at lower temperatures (O'Sullivan et al., 2018). The work here suggests that the
482 presence of biological INP might be to reduce liquid water transport to the upper levels of the cloud, reducing cirrus
483 anvil extent, but also to increase low cloud fraction. Nevertheless, measurements in the eastern tropical Atlantic
484 indicate that biological INP in the Saharan dust plumes is at most a minor contribution and that the parameterisations
485 with shallow slope in Fig. 1 produce too much glaciation at warm temperatures.

486 The results presented here also present a new framework for understanding the effect of SIP by identifying a potential
487 relationship between the effect of the Hallett Mossop process and INP parameterisation slope. The significance of INP
488 parameterisation slope also highlights the importance of characterising the INP concentration across the entirety of
489 the mixed-phase temperature range rather than just at one temperature, or in a narrow temperature range, as is
490 common in many field campaigns. For example, in the ICE-D field campaign, INP concentrations at temperatures
491 above -7 and below -27°C were not measurable due to experimental and sampling constraints (Price et al., 2018).
492 Measuring INP over the entire mixed-phase temperature range, throughout which deep convective clouds extend,
493 conceivably covering around 10 orders of magnitude in INP number concentration, represents a major experimental
494 challenge. This issue is compounded by the fact that INP spectra cannot reliably be extrapolated to higher or lower
495 temperatures since our underpinning physical understanding of what makes an effective nucleation site is lacking
496 (Holden et al., 2019). This work demonstrates the importance of solving these problems and measuring INP number
497 concentrations across the entirety of the mixed-phase temperature spectrum.



498 **Data Availability**

499 The datasets generated and analysed in this study are available from the corresponding author on reasonable request.

500 **Author Contributions**

501 REH, AKM, KSC, PRF and BJM contributed to the design, development and direction of the study. REH and AKM set up
502 and ran the UM-CASIM simulations presented in the paper. REH processed and analysed the UM-CASIM datasets.
503 JMW, AAH and BJS built and maintained the Met-Office CASIM model used to run the simulations. ZC and RJC
504 provided processed aircraft data from the ICE-D b933 flight and helped with the comparison of model data with
505 aircraft measurements. REH, AKM, JMW, AAH, ZC, RJC, KSC, PRF and BJM edited the manuscript.

506 **Competing interests**

507 The authors declare no competing interests.
508

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514 Reflectance images from the NASA Worldview website (<https://worldview.earthdata.nasa.gov/>). Airborne
515 measurements were obtained from the ICE-D field campaign and specifically the b933 flight on the 21st August 2015.
516 The ICE-D campaign used the BAe-146-301 Atmospheric Research Aircraft which is operated by Directflight Ltd (now
517 Airtask) and managed by the Facility for Airborne Atmospheric Measurements (FAAM). At the time of the
518 measurements FAAM was a joint entity of NERC and the UK Met Office. We thank all the people involved in the ICE-D
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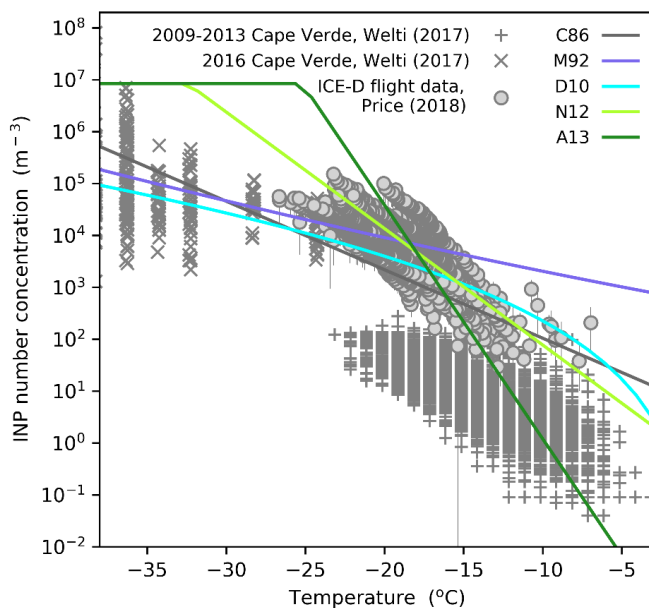
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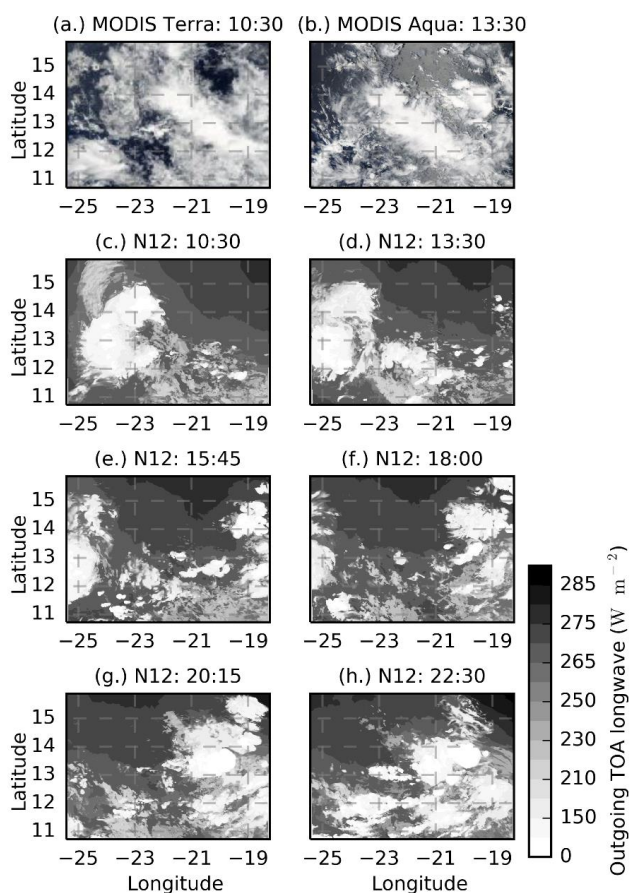
746 **Figures**



747

748 **Figure 1.** Dependence of INP number concentration on temperature ($d[INP]/dT$) for the five heterogeneous freezing
749 parameterisations simulated in this study (C86, M92, D10, N12, A13) compared to INP number concentrations measured
750 in the eastern Tropical Atlantic (Price et al., 2018; Welti et al., 2018). Parameterisations are shown for the aerosol
751 concentrations at approximately the first freezing level in our simulations ($\sim 8 \text{ cm}^{-3}$). D10, N12 and A13 are dependent on
752 aerosol concentrations, while C86 and M92 are not dependent on aerosol concentration. For the correlation analysis
753 where model outputs were plotted against parameterisation slope ($d\log_{10}[INP]/dT$), a straight line was fitted to the
754 D10 parameterisation between -3 and -37°C to obtain an approximate INP parameterisation slope. Other
755 temperature ranges were tested and were found to have no notable effect on results.

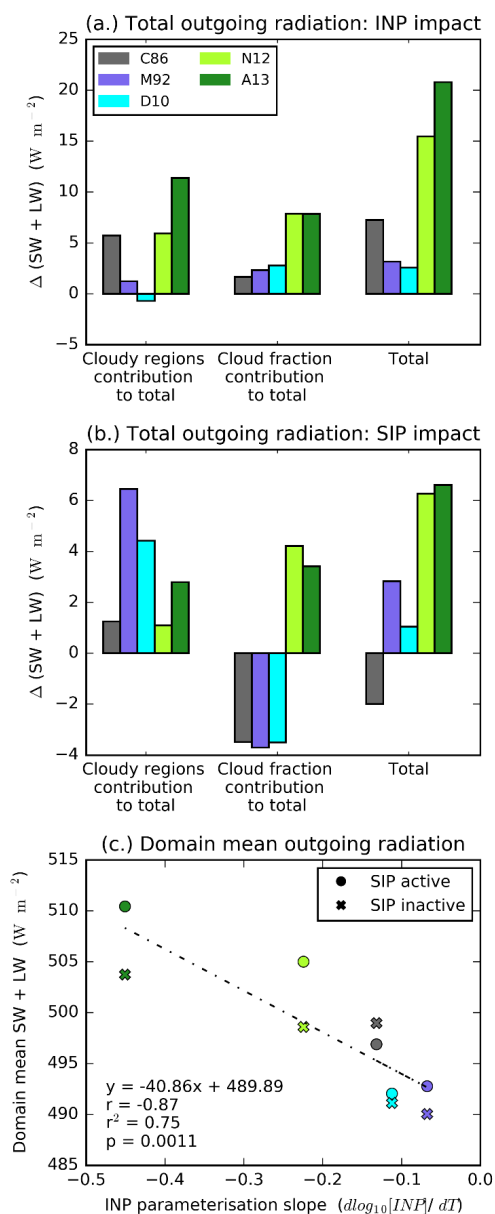
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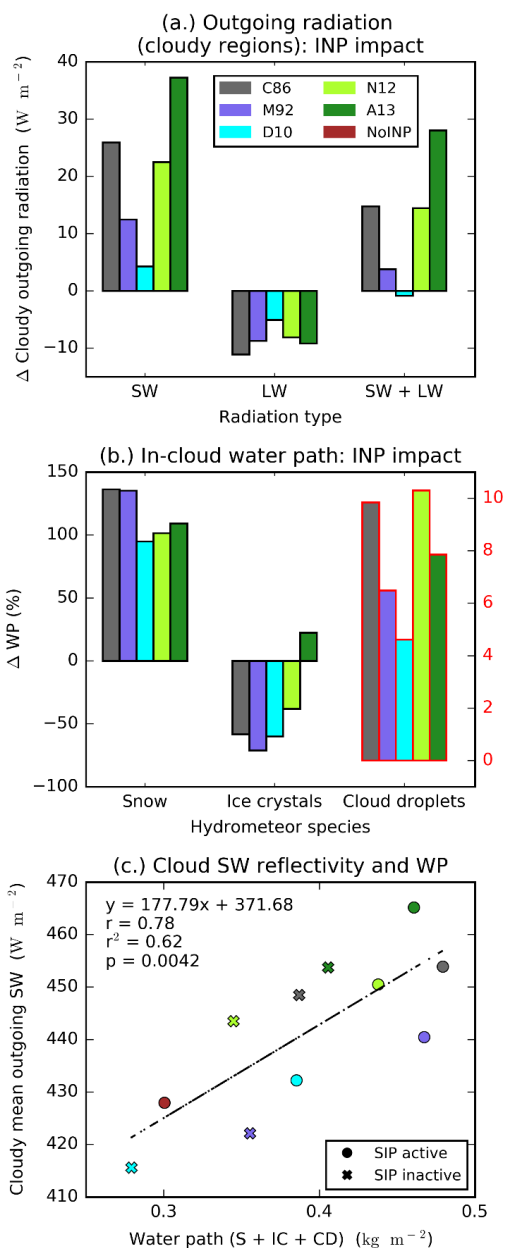
758 **Figure 2. Cloud field evolution. MODIS Terra (a) and Aqua (b) corrected reflectance images of the modelled domain for the**
759 **21st of August 2015 and the simulated top of atmosphere outgoing longwave radiation for the N12 simulation throughout**
760 **the study period (c-h). Note that the colour bar relates to panels c-h only. Images shown in (a) and (b) are moderate**
761 **resolution imaging spectroradiometer (MODIS) Corrected Reflectance imagery produced using the MODIS Level 1B**
762 **data and downloaded from the NASA Worldview website.**

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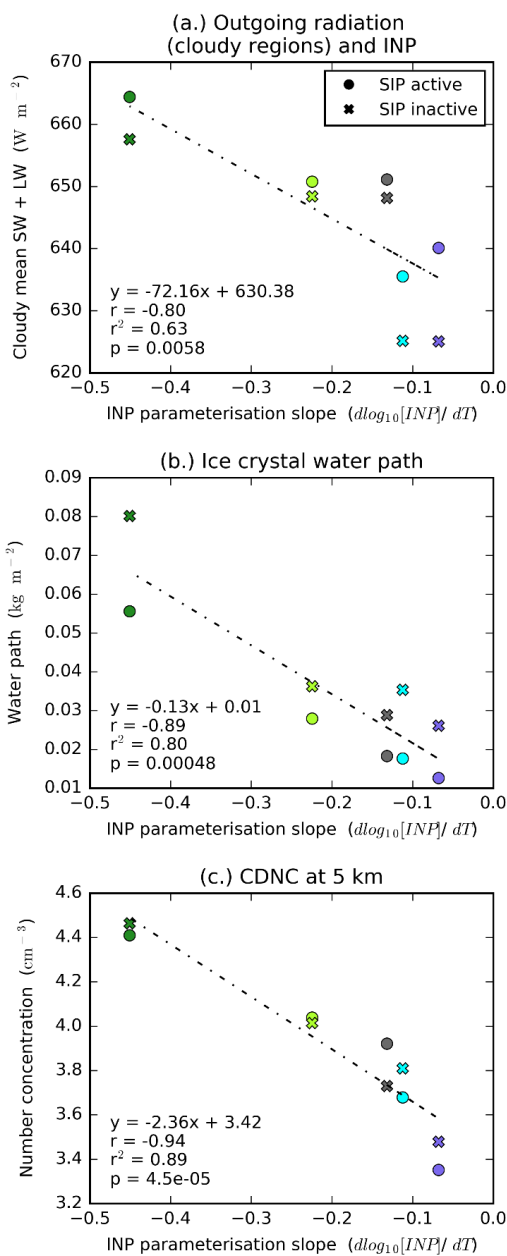
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765 **Figure 3. Effect of INP and secondary production on top of atmosphere (TOA) outgoing radiation. Effect of INP**
 766 **parameterisation (a) and SIP (a representation of the Hallett Mossop process) (b) on domain-mean daytime TOA outgoing**
 767 **radiation and total domain-mean daytime TOA outgoing radiation plotted against INP parameterisation slope (c). In (a),**
 768 **the change from the NoINP simulation is shown (INP - NoINP) with SIP active. In (b), the change from SIP_active to**
 769 **SIP_inactive is shown (SIP_active – SIP_inactive). A positive value indicates more outgoing radiation when INP or SIP are**
 770 **active. In (a) and (b), the relative contributions of changes in outgoing radiation from cloudy regions (left) and cloud**
 771 **fraction (middle) to the total radiative forcing (right) are shown (calculation described in Sect. 2.1.3). In addition to the**
 772 **simulated values, a regression line (n=10) is shown in (c) along with its associated statistical descriptors.**



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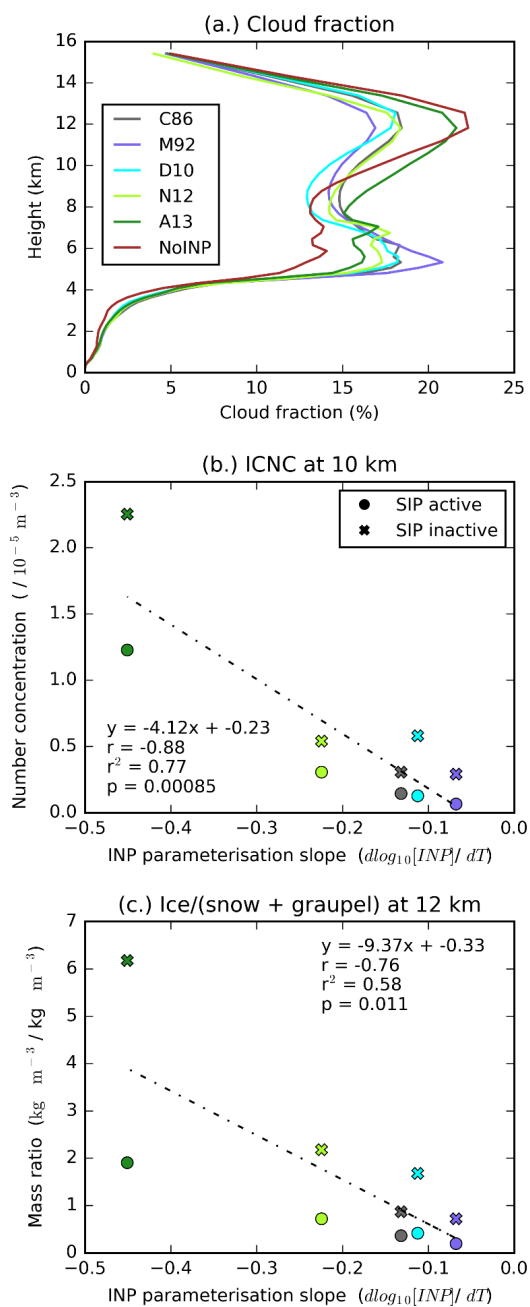
774 **Figure 4.** INP and outgoing radiation from cloudy regions. Absolute change in outgoing shortwave, longwave and total
 775 radiation from cloudy regions relative to the NoINP simulation (a), the percentage change in water path (WP) associated
 776 with snow (S), ice crystals (IC) and cloud droplets (CD) relative to the NoINP simulation (b), and mean daytime outgoing
 777 shortwave from cloudy regions plotted against the sum of S, IC and CD water paths (c). Note different scale for CD water
 778 path in (b). In addition to the simulated values, a regression line (n=11) is shown in (c) along with its associated statistical
 779 descriptors.



780

781 **Figure 5.** Outgoing radiation from cloudy regions and INP parameterisation slope. Scatter plots of INP parameterisation
782 slope and total daytime outgoing radiation from cloudy regions (a), in-cloud mean ice crystal water path (b), and in-cloud
783 cloud droplet number concentrations at the start of the mixed-phase region (5 km) (c). Also shown are the respective
784 regression lines ($n=10$) and associated statistical descriptors.

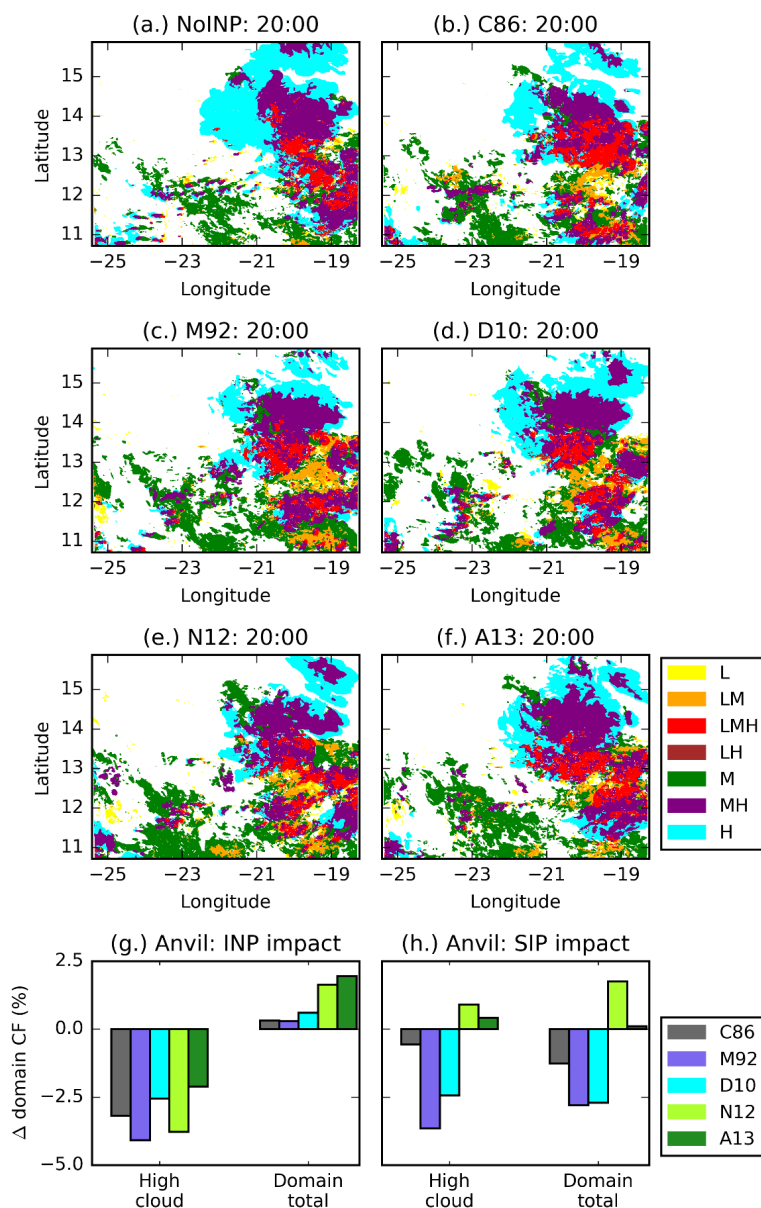
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787 **Figure 6. Cloud fraction and INP parameterisation slope. Domain-mean cloud fraction profile (a), INP parameterisation**
 788 **slope plotted against ice crystal number concentration at 10 km (b) and mass ratio of ice crystals to snow plus graupel at**
 789 **12 km (c). Also shown in (b) and (c) are the respective regression lines (n=10) and associated statistical descriptors.**

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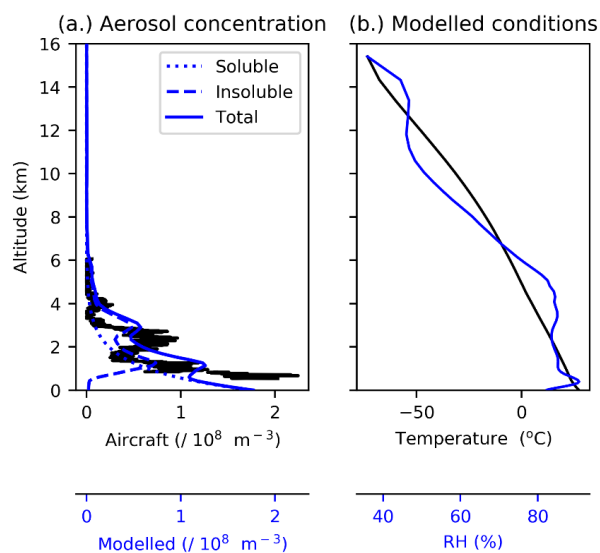
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792 **Figure 7. Vertical composition of cloud. 2D distribution of cloud type at 20:00 for all six SIP_active simulations (a-f), as**
 793 **well as anvil and domain cloud fraction change due to INP (g) and due to SIP (h). Clouds are categorised according to their**
 794 **altitude into low (L, <4 km), mid (M, 4-9 km) and high (H, >9 km) levels and mixed category columns if cloud (containing**
 795 **more than 10^{-5} kg kg⁻¹ condensed water from cloud droplets, ice crystals, snow and graupel) was present in more than one**
 796 **of these levels (a more detailed description can be found in Sect. 2.1.4). A positive value in (g) or (h) indicates higher**
 797 **values when INP (g) or SIP (h) are active.**

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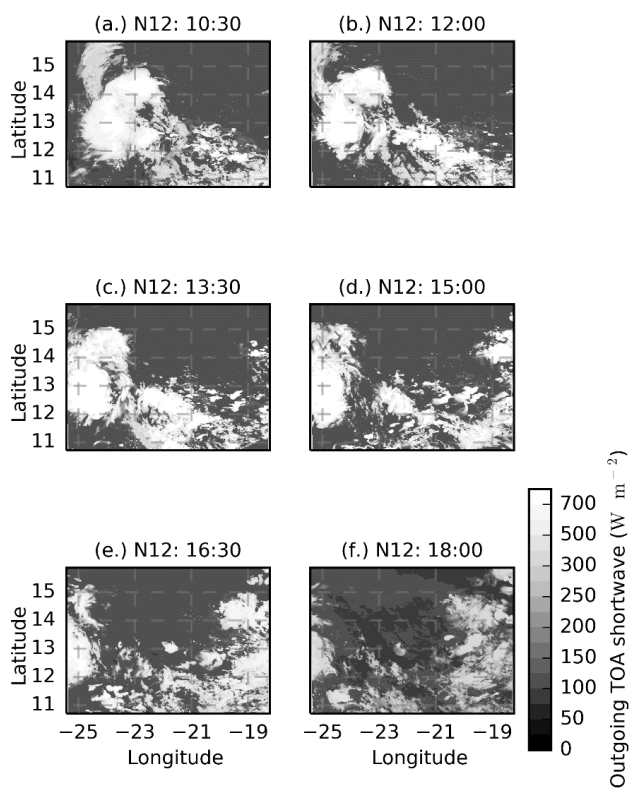
799 **Appendix A**



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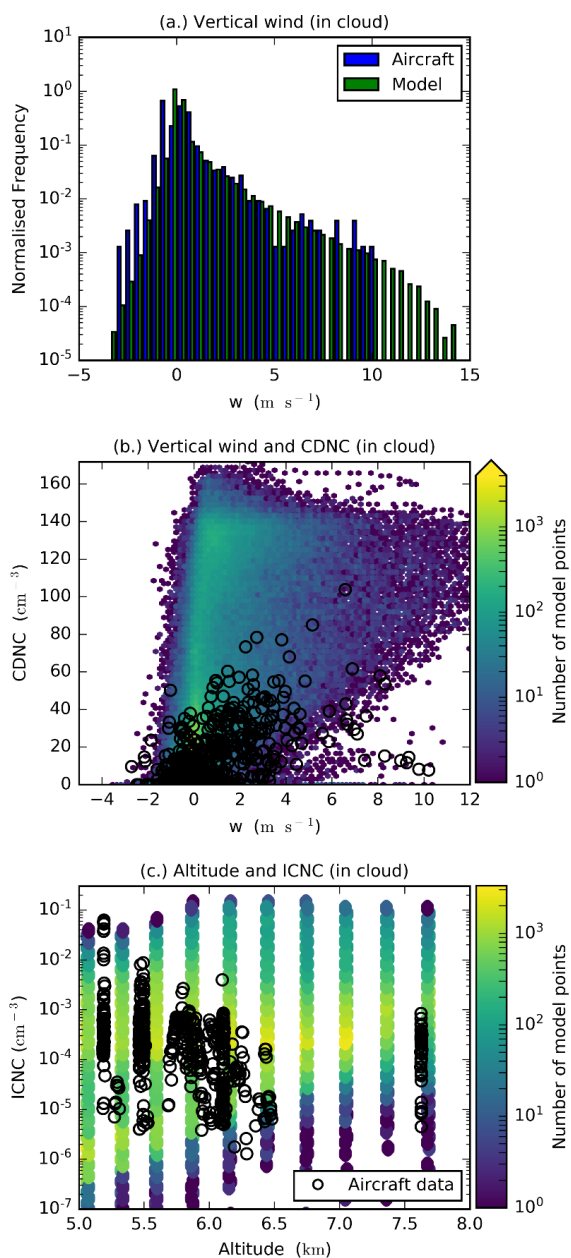
801 **Figure A1. Observed (black line) and modelled (blue lines) aerosol concentrations (a), and modelled domain mean**
802 **temperature and relative humidity profiles (b). INP concentrations in the D10, N12 and A13 simulations are linked to the**
803 **insoluble aerosol profile shown.**

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805

806 **Figure A2.** Cloud field evolution. Simulated top of atmosphere outgoing shortwave radiation for the N12 simulation in the
807 daylight hours throughout the study period (a-f).



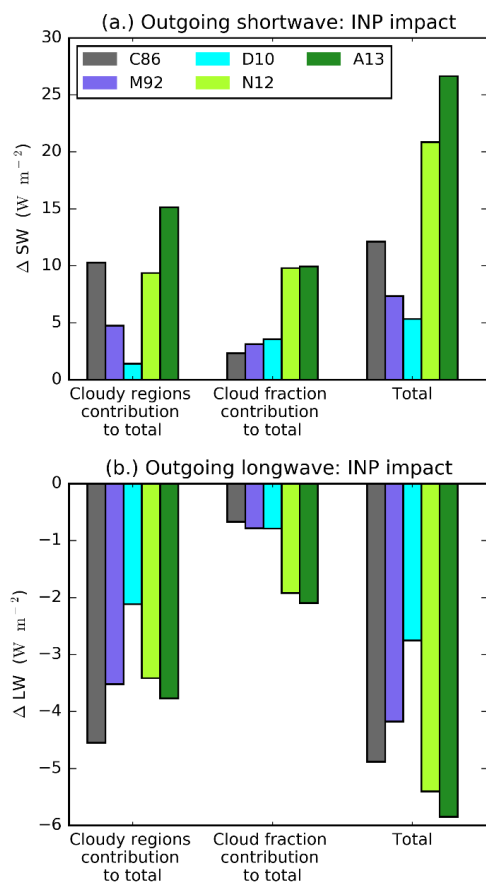
808

809 **Figure A3.** Comparison of observed conditions from the b933 ICED field campaign flight on the 21st August 2015 and the
810 modelled conditions. Vertical wind speed from the model and aircraft data (a), a 2D histograms of modelled vertical wind
811 against cloud droplet number concentration (CDNC) (b) and altitude plotted against ice crystal number concentration
812 (ICNC) (c) with the aircraft data overlaid. Modelled values are selected from clouds between 10 and 150 km² in size from
813 the N12 simulation.

814



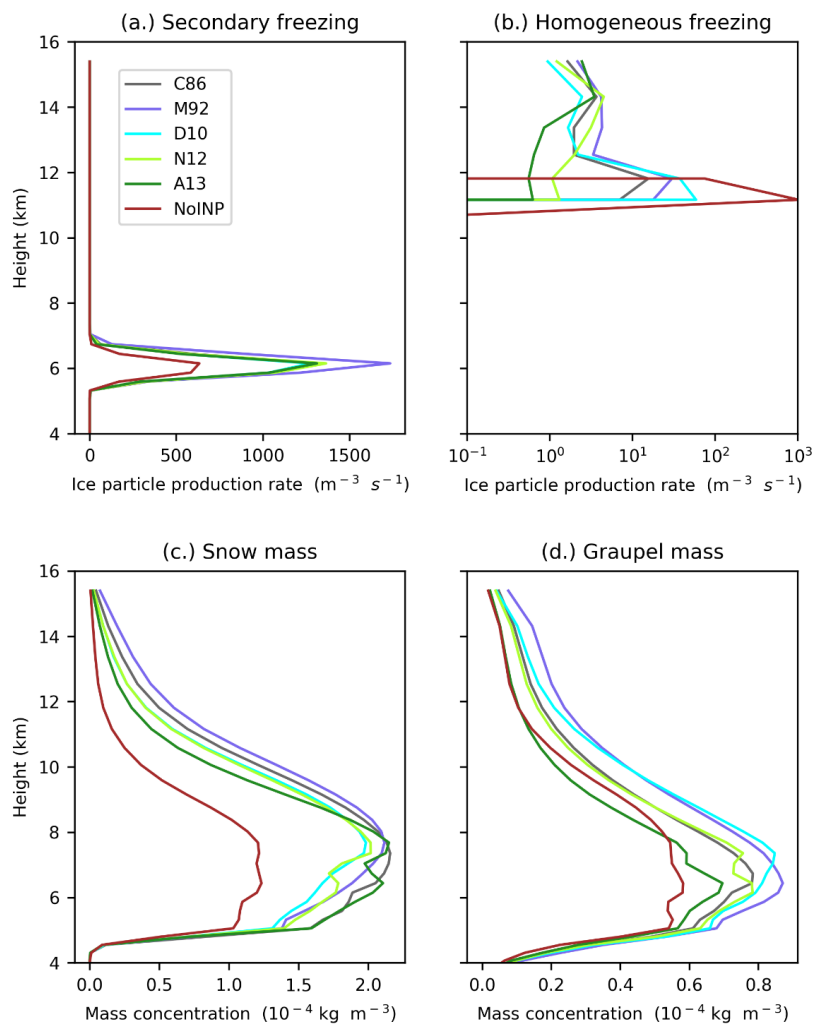
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816

817 **Figure A4.** Effect of INP on domain mean daytime outgoing TOA shortwave and longwave radiation. The change from the
 818 **NoINP** simulation is shown (**INP - NoINP**). A positive value indicates more outgoing radiation when INP are present. The
 819 **contributions of changes in outgoing radiation from cloudy regions (left) and cloud fraction (middle) to the total radiative**
 820 **forcing (right) are also shown.**

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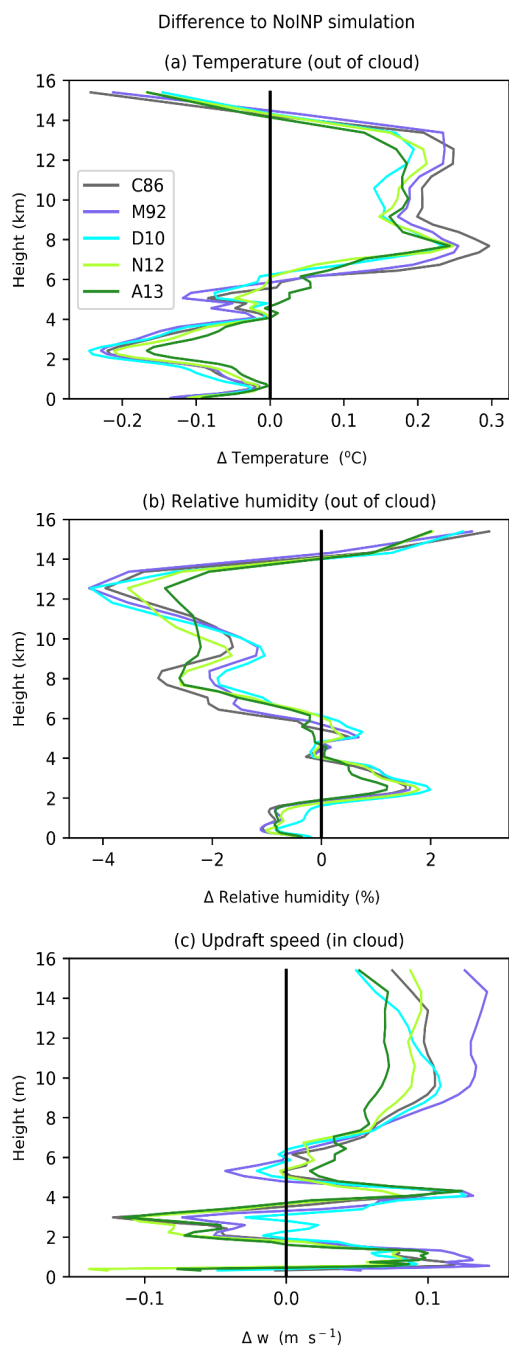
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823 **Figure A5. Profiles of some microphysical properties of the simulated clouds. Mean in-cloud ice particle production rates**
824 **from secondary (b) and homogeneous (c) freezing, snow mass concentration (c) and graupel mass concentration (d).**

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828 **Figure A6.** Effect of INP on domain mean out of cloud temperature (a) and relative humidity (b), and in cloud updraft
829 speed (c). The difference from the NoINP simulation is shown, a positive value indicates a higher value when INP is
830 present.