

Smoke-charged vortices in the stratosphere generated by wildfires and their behaviour in both hemispheres : comparing Australia 2020 to Canada 2017

Hugo Lestrelin, Bernard Legras, Aurélien Podglajen, and Mikail Salihoglu

Laboratoire de Météorologie Dynamique, UMR CNRS 8539, IPSL, PSL-ENS/École Polytechnique/Sorbonne Université, Paris, France

Correspondence: Bernard Legras (bernard.legras@lmd.ipsl.fr)

Abstract. The two most intense wildfires of the last decade that took place in Canada in 2017 and Australia in 2019-2020 were followed by large injections of smoke in the stratosphere due to ~~pyroconvection~~^{pyro-convection}. It was discovered by Khaykin et al. (2020) and Kablick et al. (2020) that, after the Australian event, part of this smoke self-organized as anticyclonic confined 5 vortices that rose in the mid-latitude stratosphere up to 35 km. Based on CALIOP observations and the ERA5 reanalysis, this new study analyzes the Canadian case and ~~finds~~^{finds}, similarly, that a large plume penetrated the stratosphere by ~~12-12-13~~¹²⁻¹²⁻¹³ August 2017 and got trapped within a meso-scale anticyclonic structure which travelled across the Atlantic. It then broke into three offsprings that could be followed until mid-October performing three round the world journeys and rising up to 23 km. We analyze the dynamical structure of the vortices produced by these two wildfires and demonstrate how they are maintained 10 by the assimilation of data from instruments measuring the signature of the vortices in the temperature and ozone field. We propose that these vortices can be seen as bubbles of ~~low absolute small, almost vanishing~~^{low absolute small, almost vanishing}, potential vorticity and smoke carried vertically across the stratification from the troposphere inside the middle stratosphere by their internal heating, against the descending flux of the Brewer-Dobson circulation.

1 Introduction

15 A spectacular consequence of large summer wildfires in mid-latitude forests is the generation of ~~pyro-cumulus clouds~~^{pyro-cumulonimbus} (~~PyroCb~~) that can reach the lower stratosphere during extreme events (Fromm et al., 2010). The combustion products and accompanying tropospheric compounds (organic and black carbon, smoke aerosols, condensed water, carbon ~~monoxide~~^{monoxide}, low ozone, ...) that are lifted to the stratosphere can survive several months and be transported over considerable distances (Fromm et al., 2010; Yu et al., 2019; Kloss et al., 2019; Bourassa et al., 2019) filling the mid-latitude band and sometimes 20 reaching the tropics (Kloss et al., 2019). As black carbon is highly absorptive of the incoming solar radiation, the resulting heating produces buoyancy (~~Ditas et al., 2018~~)^(de Laat et al., 2012; Ditas et al., 2018) and an additional lift of the non diluted parts of the plume by several kilometers in the stratosphere (Khaykin et al., 2018; Yu et al., 2019). This effect enhances the dispersion and, by increasing the altitude, ensures a longer ~~life-time~~^{life-time} in the stratosphere (Yu et al., 2019), enhancing

the radiative effect on climate that has been estimated of comparable amplitude to moderate volcanic eruptions (Peterson et al., 2018; Khaykin et al., 2020).

The Australian ~~wildfire~~ wildfires of the summer season 2019-2020 have exceeded in magnitude all previously known events (Khaykin et al., 2020). A striking discovery has been the observation that a part of the stratospheric smoke plumes self-organized as anticyclonic vortices that persisted between one to three months ([Kablick et al., 2020](#); [Khaykin et al., 2020](#)) ([Kablick et al., 2020](#); [Khaykin et al., 2020](#); [Allen et al., 2020](#)) and, for the most intense one (nicknamed below as Koobor, following an aboriginal legend), rose up to 35 km (Khaykin et al., 2020), an altitude never reached by tropospheric aerosols since the Pinatubo eruption. It was conjectured by Khaykin et al. (2020) that aerosol heating was essential in maintaining the structure and providing the lift. In turn, the vortex created a confinement that preserved the embedded smoke cloud from being rapidly diluted within the environment.

[It is a natural extension to investigate](#) [Investigating](#) the occurrence of such vortices after previous wildfires, in particular over the last 15 years during which the required satellite instruments are available, [is a natural extension of](#) ([Khaykin et al., 2020](#)) . As the strongest previously recorded wildfire of the last decade is the 2017 Canadian event that took place in British Columbia (Hanes et al., 2019), this work is revisiting this case which has already been documented in several studies ([Khaykin et al., 2018](#); [Ansmann et al., 2018](#); [Khaykin et al., 2018](#); [Ansmann et al., 2018](#); [Peterson et al., 2018](#); [Yu et al., 2019](#); [Kloss et al., 2019](#); [Baars et al., 2019](#); [Torres et al., 2020](#)) . In particular, a stratospheric rise of up to 30 K day^{-1} was diagnosed based on satellite observation by Khaykin et al. (2018) who also [reports](#) [report](#) a compact smoke cloud at 19 km over the Haute-Provence observatory, Southern France, on 29 August 2017. An other goal of this study is to complement Khaykin et al. (2020) by expanding their diagnostics and interpretations on the 2020 case.

Section 2 describes the data and methods used in this work. Section 3 describes the new vortices found after the 2017 Canadian fire and their evolution. It includes a detailed discussion of previous results. Section 4 describes the structure of the vortices based on the 2017 [and Canadian case and the](#) 2020 [eases](#) [Australian case](#). Section 5 offers conclusions.

2 Data and methods

2.1 Satellite data from CALIOP

Launched in April 2006, the [CALIPSO Cloud-Aerosol Lidar and Infrared Path Satellite Observation \(CALIPSO\)](#) mission (Winker et al., 2010) took on board the Cloud-Aerosol Lidar with Orthogonal Polarization (CALIOP) which is a two-wavelength polarization lidar that performs global profiling of aerosols and clouds in the troposphere and lower stratosphere. We used the total attenuated 532 nm backscatter level 1 (L1) product in the latest available version V4.10 (Powell et al., 2009). The nominal along track horizontal and vertical resolutions are, respectively, 1 km / 60 m between 8.5 and 20.1 km and 1.667 km / 180 m between 20.1 and 30.1 km. The L1 product oversamples the layers above 8.5 km with an uniform horizontal resolution of 333 m. We computed the scattering ratio by dividing the total attenuated backscatter by the calculated molecular backscattering following Vernier et al. (2009) and Hostetler et al. (2006) using the meteorological metadata of the L1 product. To reduce the noise, an horizontal median filter with 40 km width (121 pixels) was applied to the data. In order to separate clouds from

aerosols, we also used the level 2 (L2) total scattering aerosol coefficient at 532 nm which is available at 5 km resolution. Both daytime and nighttime measurements have been used. Since the daytime measurements are noisier, they can only be used when the aerosol signal is strong enough, mainly during the first weeks after the release of the plume.

60 As in Khaykin et al. (2020), CALIOP inspection has been the first step in order to identify the potential vortices. The L1 sections have been systematically screened from 12 August to 15 October 2017, selecting those which contained isolated compact patterns above 11 km, identified as aerosols by the L2 product. The location and size of the retained patches were then determined by visually matching a rectangular box to the observation, as illustrated in Fig. A1. It is usually very easy to see the boundaries. At the next stage, the patches have been associated to the vortices detected as described below and a further 65 inspection has rejected cases (less than 20% of those retained at the first stage) that correspond to tails left behind by vortices.

Due to an increased solar activity, CALIOP operations have been suspended between 5 and 14 September. This has been an obstacle to establish a continuity based on CALIOP observations alone but the tracking of the vortices filled that gap as described below.

2.2 Meteorological data

70 2.2.1 Reanalysis

To track the stratospheric wildfire vortices and diagnose their dynamical structure, we used the ERA5 reanalysis (Hersbach et al., 2020) which is the last generation global atmospheric reanalysis of the European Center for Medium Range Weather Forecast (ECMWF). Khaykin et al. (2020) used instead the ECMWF operational analysis and forecast. Both are based on the ECMWF Integrated Forecast System (IFS). In the ERA5, the native horizontal resolution of the IFS model is about 31 km and 75 it has 137 levels in the vertical with spacing that varies from less than 400 m at 15 km to about 900 m at 35 km, within the relevant altitude range of this study. We used an extracted version of the ERA5 with 1° resolution in latitude and longitude, at full vertical resolution and 3-hourly resolution. This choice was dictated by practical considerations, and by the **fact that 1 is sufficient to describe evidence that this grid describes** synoptic-scale features and that vortices do not travel across more than a few grid points in 3 hours.

80 Khaykin et al. (2020) used temperature, ozone and vorticity to investigate the structure of the vortices. In this study, we also used potential vorticity (PV). PV is a Lagrangian invariant for inviscid and adiabatic flows (Ertel, 1942); furthermore, it provides a compact and complete picture of the balanced part of the flow (Hoskins et al., 1985). An interesting property of the ERA5 is that its dynamical core preserves PV much better than previous reanalyses (Hoffmann et al., 2019). Although ERA5 potential vorticity can be directly retrieved from the ECMWF archive on a given set of potential temperature levels, we instead 85 recalculated it from the retrieved vorticity, temperature and total horizontal wind fields on model levels, in order to benefit from the full vertical resolution offered by ERA5. For that purpose, we used the definition of PV for the primitive equations in spherical coordinates and model hybrid vertical coordinate η , which is given by :

$$P = \underline{\mathbf{g}} \left(\frac{\partial \theta}{\partial p} (f + \zeta_\eta) + \frac{1}{a} \left(\frac{\partial \theta}{\partial \phi} \bigg|_\eta \frac{\partial u}{\partial p} - \frac{1}{\cos \phi} \frac{\partial \theta}{\partial \lambda} \bigg|_\eta \frac{\partial v}{\partial p} \right) \right) \quad (1)$$

where a is the radius of the Earth, λ is the longitude, ϕ the latitude, g is the free-fall acceleration, ζ_η is the model level vertical component of the vorticity, f the Coriolis parameter, (u, v) the horizontal velocity, p the pressure and θ the potential temperature. The gradients are estimated using centered differences on the retrieved longitude-latitude- η grid. See Eq. (3.1.4) of Andrews et al. (1987) for an analogous formula in barometric altitude coordinate.

While the formulation of potential vorticity in Eq. (1) is the most commonly used, it bears the disadvantage of a large background vertical gradient, which proves inconvenient to track and characterize structures along their ascent. To overcome this issue, we used the alternative formulation of Lait (1994), discussed by Müller and Günther (2003):

$$\Pi = P \left(\frac{\theta}{\theta_0} \right)^{-\epsilon} \quad (2)$$

where P is the Ertel PV, $\epsilon = 4$ in the Australian case and $\epsilon = \frac{9}{2}$ in the Canadian case, and $\theta_0 = 420\text{K}$. Compared to P , Π is still an adiabatic invariant and exhibits a reduced vertical gradient, so that the vortices, characterized by anticyclonic Π anomalies, can be unambiguously distinguished during their ascent. In each of the two cases, the value of ϵ is chosen to nearly cancel the background vertical gradient of Π , and depends on the large-scale vertical temperature profile characterized by larger (more positive) $\frac{\partial \bar{T}}{\partial z}$ in the Australian case than in Canadian case (see Müller and Günther, 2003, for a discussion regarding the choice of ϵ)
 \vdots

2.2.2 Assimilation increment

The ERA5 is constrained by observations over repeated 12-hour assimilation cycles. The Over each cycle, the assimilation increment is defined ~~over each cycle~~ as the difference between the new analysis and the first guess provided as a final stage of a free forecast run of the model, initialized from the previous analysis 12 hours before. This definition can be applied to any of the basic variables of the model or to derived quantities like potential vorticity. In the ERA5, the assimilation increments can be calculated on each day at 6:00 and 18:00 UTC. In order to diagnose how the observations are forcing the vortices, we calculated the assimilation increments of temperature, vorticity, potential vorticity and ozone. Temperature and ozone determine the radiances that are measured by spaceborne instruments and are also directly accessible from in situ instruments. On the contrary, potential vorticity cannot be directly retrieved from any instrument and is indirectly constrained (see below). These three parameters are updated by the assimilation system in order to reduce the difference between observed quantities (typically radiances but also deviations of the GPS signal path) and simulated quantities (radiances that a satellite flying "above the model" would see). It is tempting to see the temperature assimilation increment as an additional heating but this is incorrect ~~as the~~. The increment is calculated from an adjusted state, resulting from the iterations of the assimilation, in which both temperature and motion respond to the forcing by the observations ~~that depend only on the temperature~~. As wind observations are much sparser than temperature observations, one would expect that winds, and wind related quantities like potential vorticity, are much less constrained and therefore much less accurate in the analysis than temperatures. This is true to a large extend in the tropics but not in the mid-latitudes where temperatures and winds are strongly related by the thermal wind relation. This equilibrium is enforced by the assimilation system which filters out the transient modes that deviate from it.

Neither the ECMWF operational analysis nor the ERA5 assimilate aerosol observations. The smoke plumes are hence totally missing in the IFS where stratospheric aerosols were only accounted by mean climatological distribution during the periods of investigation. The miracle of assimilation is that assimilating mainly the temperature signal of the smoke structure is enough to reconstruct the whole thermal and dynamical structure from the principle of balanced motion (McIntyre, 2015).

125 2.2.3 Vortex tracking approach

Once we caught a first occurrence of an isolated bubble of aerosols with CALIOP, we searched the ERA5 data for the occurrence of a corresponding vortex that showed up as an isolated pattern in the Π and ozone maps. While Khaykin et al. (2020) used only relative vorticity to track the vortices for commodity, we used both Π defined from Eq. (2) and the ozone anomaly defined as the deviation with respect to the zonal mean at the same latitude and altitude. The tracking was made every six hour 130 hours by following a local extremum within a box of usually 12 degrees in longitude, 5 degrees in latitude and a range of at least 30 K of potential temperature in the vertical. Once a vortex was caught, the box was moved forward in time to the step $n + 1$ according to the vortex motion between steps $n - 1$ and n . In very few instances, the tracking was guided by reducing the size of the box. This was needed in particular at the birth-formation of a vortex, or when it split in two parts and in the final stage when one of the methods lost the track before the other.

135 3 A new occurrence : Canada 2017

3.1 General description

Although the 2017 Canadian fire started in June (Hanes et al., 2019), it is only by 12 August until early 13 August that the fire reached an intensity such that a large PyroCb developed and reached the lower stratosphere leaving a smoke plume that could be followed by satellite sensors (Khaykin et al., 2018; Peterson et al., 2018)(Khaykin et al., 2018; Peterson et al., 2018; Torres et al., 2020) 140 . From the inspection of scattering ratio along CALIPSO orbits, we found our first distinctly isolated cloud-smoke bubble on 16 August at 9:38 UTC and 12.6 km altitude, over the north of Canada at 63° N and 102° W, where the tropopause altitude was 11 km. This is two days after the first evidence of presence of smoke in the stratosphere (Peterson et al., 2018; Torres et al., 2020) In the following days and until the CALIOP interruption on 4 September, we could track this cloud, labelled as bubble O, and its offsprings almost every day. Figure 1 shows several typical patterns during that period.

145 As indicated by the longitudes on Fig. 1, the bubble O moved eastward across the Atlantic. During the early days, it was captured each day by at most two CALIPSO orbits (one day orbit and one night orbit), the adjacent orbits only showing filamentary non compact structures that could be easily distinguished. The bubble rose rapidly reaching 18 km by 25 August (i.e. an ascent rate larger than 0.5 km day^{-1}). One surprising feature is that once it reached the eastern-Atlantic-European coast by 27 August, several bubbles could be tracked on multiple close orbits, or even exceptionally, on the same orbit. As we shall 150 see in the following, this corresponds to the dissemination splitting of bubble O into several offsprings that we label as A, B1 and B2 for which several views are shown in Fig. 1. Another issue came soon after as CALIOP operations were suspended for

Aerosol scattering ratio 512

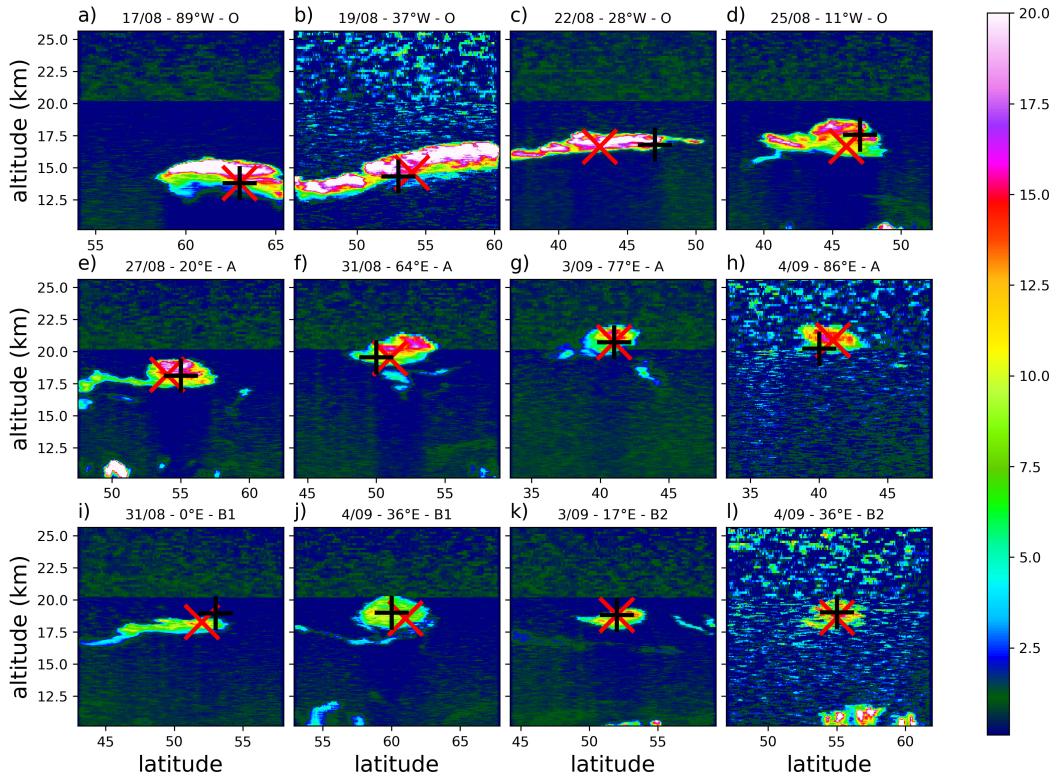


Figure 1. Selection of [along track sections of CALIOP scattering ratio profile profiles](#) during the first observation period until 4 September 2017. The upper row (a-d) shows sections of the [vortex-bubble](#) O at four times. The middle row (e-h) shows four sections of the [vortex-bubble](#) A after its separation from [vortex-bubble](#) O. The bottom row shows on the left (i-j) two sections of [vortex-bubble](#) B1 after its separation from [vortex-bubble](#) O and on the right (k-l) two views of [vortex-bubble](#) B2 that continues the track of [vortex-bubble](#) O after 1st September 2017. In each panel, the black [cross shows and red crosses show](#) the [orbital plane](#) projection of the [simultaneous location of the corresponding](#) vortex center according to, respectively, the [Lait PV II minimum onto the orbital plane from and](#) the [H tracking ozone trackings in the ERA5 data](#). On each panel, the longitude [indicated in the title](#) is that of the CALIPSO orbit at the center of the bubble.

the period 5 - 14 September due to increased solar activity. When CALIOP observations resumed after 14 September, the A, B1 and B2 bubbles that were now located at 20 km or above could be found again, over central Asia for A and over the Pacific for B1 and B2, and they were followed during their subsequent journey until mid October. Figure 2 shows a selection of views

155 during that period.

Aerosol scattering ratio 512

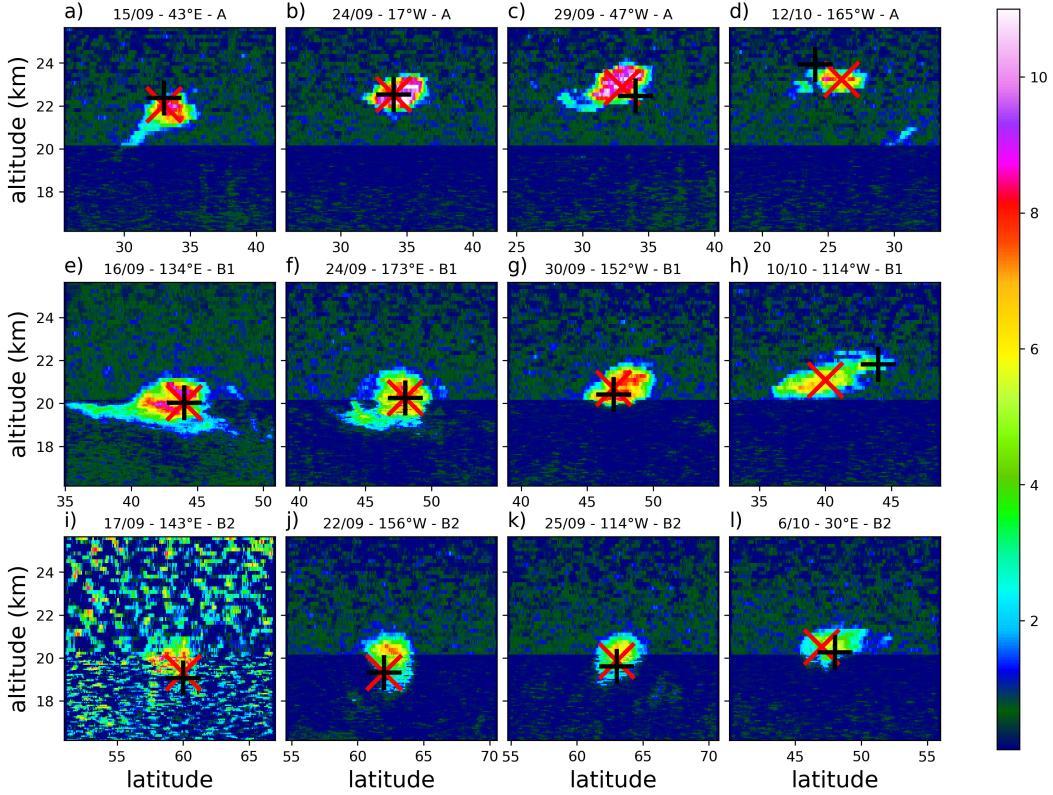


Figure 2. Same as Fig. 1 but during the second observation period after 15 September 2017 and showing, respectively, in the upper, middle and bottom rows, four sections of **vortices** **bubbles** A (a-d), B1(e-h) and B2 (i-l).

3.2 Early evolution

The smoke bubbles have been attributed to vortices based on the ERA5 reanalysis which were available during their whole life cycles. Starting on 14 August, a kernel of almost zero PV and low ozone could be found by 72° N and 115° W at an altitude of 12 km just above the tropopause. In the following days, this anomaly developed vertically and connected with the

160 bubble O location as identified from CALIOP (see animation in Sec. S2 of the Supplement). By 17 August, as it crossed the Hudson Bay, it exhibited a well developed intrusion that reached 14 km in the PV longitudinal and latitudinal section. As seen in the animation, this intrusion, while still rising, was subsequently stretched by the vertical shear and split by 19 August into an upper part isolated in the stratosphere at about 15 km while the lower part near the tropopause was further stretched and disappeared. The upper part which was associated with bubble O was tracked in ERA5 ozone and PV fields and from CALIOP 165 until the end of August (Fig. S1 of the Supplement). As it crossed the Atlantic, it got trapped inside a **thalweg** **trough** by 20 August and travelled with it until it reached the European coast. Due to the wind shear prevailing in the associated jet, the

vortex O elongated in latitude across the isentropes (see the animation) until it got ~~dissociated~~-split over western Europe into the three parts A, B1, B2, as described in the next section.

This early stage is also described in great details by Torres et al. (2020). These authors show that the whole smoke cloud is shaped, on 20 August, as a V by its passage in the trough resulting in a double maximum tilted pattern in the section by CALIOP. This pattern is recovered in the ERA5 PV pattern (freeze the animation in Sec. S2 of the Supplement as the same date) and our tracking is actually following the highest of the two maxima.

3.3 Horizontal and vertical ~~dissociation~~-splitting of vortex O into its offsprings

Figure 3 displays the series of ~~event that led to the dissociation of the vortex O events that led~~, over the period 22 August - 1st September, ~~to the splitting of the vortex O~~ into its three offsprings that were subsequently followed during one month and half. ~~The CALIPSO orbits which are displayed here are more numerous than those retained for the tracking of the vortices as we are also interested in the tails of PV patches a half. We display the CALIPSO orbits that intersect the vortex cores and also those that intersect their tails.~~ The presence of a smoke bubble ~~or patch~~ detected by CALIOP along an orbit is shown as a red segment. We see that on all orbits, there are bubbles ~~or patches~~ that match each of the intersections with the ~~low PV patches~~.

180 ~~tracked low PV regions.~~ The sequence begins, on 22 August (Fig. 3a) with the elongated structure of the vortex O that emerged at 420 K on the eastern flank of the ~~thalweg~~ trough within which it crossed the Atlantic. The elongation is due to the intense vertical shear in the jet stream. The ~~initiation~~-formation of vortex A is already visible as the wrapping up pattern on the north east end of vortex O. On 23 August (Fig. 3ab), the pattern of vortex A is lost at level 420 K but is now visible ~~on at~~ level 435 K. Two days later (Fig. 3c), the vortex A was a developed structure reaching 60° N at level 455 K which was ~~overpassed~~ 185 ~~overflowed~~ by CALIPSO (Fig. 4a). At the same time the vortex O maintained a core near 45° N (Fig. 1d). In the following days, on 26 and 27 August (Fig. 3d-e), the vortex A fully separated from vortex O as it moved eastward and rose (Fig. 1e). On 28 and 29 August (Fig. 3f-g), the vortex A moved away while the vortex O was ~~again elongated~~ ~~a new elongated~~, and started to split into a western part (Fig. 4b) and an eastern part (Fig. 4c). ~~The vertical structure of vortex A on 28 August in an other reanalysis is described in Fig. 16 of Allen et al. (2020).~~ On 30 and 31 August (Fig. 3h-i), the western part separated while the eastern part folded itself and separated in two more parts that provided vortex B1 as the north component (Fig. 1) and vortex B2 as the south component (essentially the continuation of the vortex O) which were both seen on the same CALIOP overpass of 1st September (Figs. 3j & 4d). The vortices B1 and B2 fully separated in the following days while rising and starting to move slowly eastward. The western component could also be followed until September 4, accompanied by patches seen by CALIOP. It remained ~~however~~, ~~however~~, below 460 K and could not be linked with certainty to any structure seen from CALIOP after 190 15 September.

3.4 Late evolution

During the observations period that followed the recovery of CALIOP after 15 September and until mid-October, almost all observations of compact smoke bubbles at 20 km and above could be attributed to one of the vortices A, B1 and B2. Those which were discarded are under the shape of filaments or tails at altitudes corresponding to the bottom of the bubbles. As in

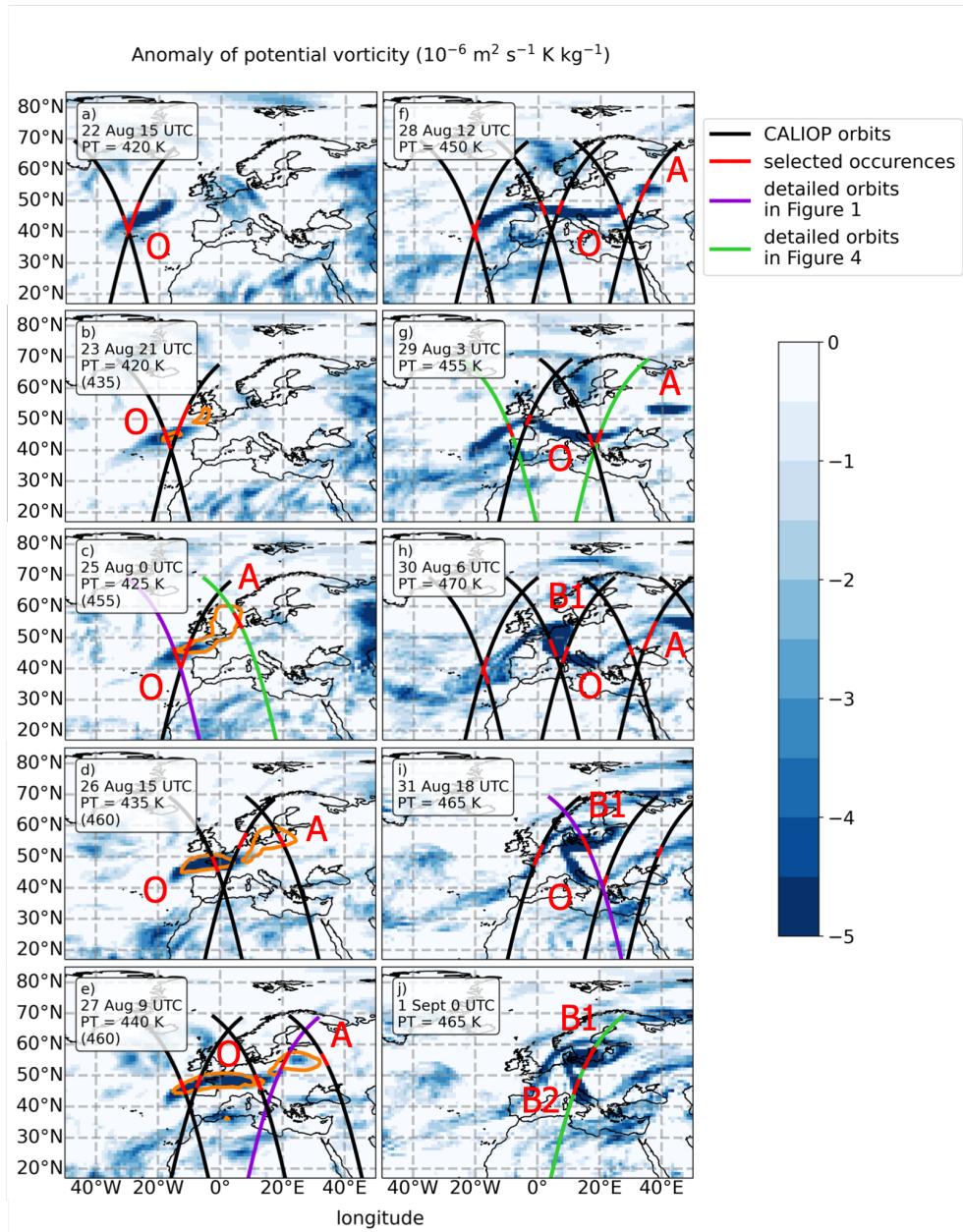


Figure 3. Sequence of PV charts showing the dissociation-splitting of vortex O into vortices A, B1 and B2. The map is plotted on the potential temperature surface corresponding to the core of vortex O or its continuation B2 in the ERA5 tracking. The orange lines are plotted at the isentropic level of vortex A, specified within parenthesis, and show the contour of -2 PVU ($1 \text{ PVU} = 10^{-6} \text{ Km}^2 \text{ kg}^{-1} \text{ s}^{-1}$) for vortex A. The black, green and purple lines show the intersecting orbits of CALIPSO and the red segments show the parts of the orbits occupied by the bubble (only the bubble core extent is displayed here). The maps are plotted at the hour matching best the selected CALIOP occurrences. The purple orbits are those corresponding to the sections shown in Fig. 1. The green orbits are those corresponding to the sections shown in Fig. 4. Day-time and night-time orbits are used, the day-time orbit are running from south-east to north-west while the night-time orbits are running from north-east to south-west. Starting from 1st September, the remaining of the vortex O is relabelled as B2.

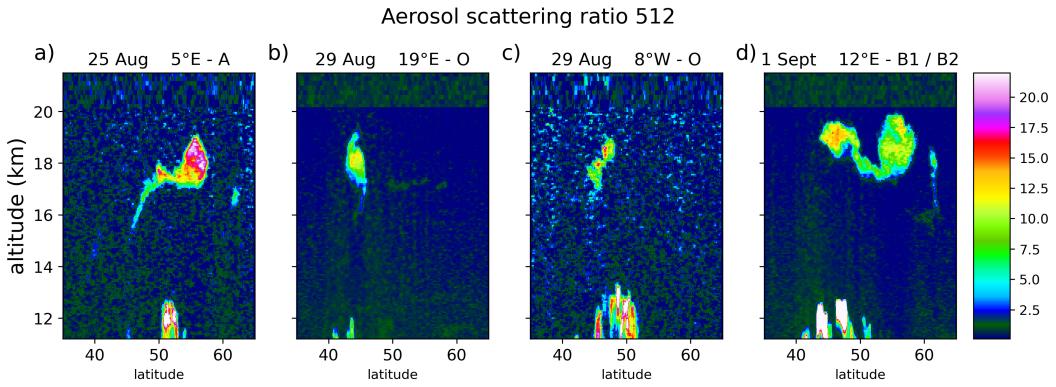


Figure 4. Selection of 4 CALIOP scattering ratio sections of the smoke bubbles along the orbits shown in green on Fig. 3. a) day-time section of bubble A on 25 August b-c) east night-time and west day-time sections of the elongated bubble O on 29 August d) night-time double section of bubbles B1 (at $\sim 55^\circ$ N) and B2 (at $\sim 45^\circ$ N) on 1st September

200 Fig. [Fig:CALIOPa 1](#), the location of the ERA5 vortex center is shown as a cross in each panel of [FigsFig. 2](#). In turn, the location
 of the smoke bubble centers are shown as square marks in Fig 5 which describes the trajectory of vortex A, and the bars indicate
 the latitude and altitude extent of the bubble. A perfect match of the horizontal location is not expected as there is no reason
 for CALIPSO orbit to cross every time the [bubble-vortex](#) by its center. Nevertheless, we see a very good agreement between
 205 the ERA5 trajectory and the location of the 27 smoke bubbles seen by CALIOP that are attributed to vortex A, and the same
 holds for the two other vortices B1 and B2 (Figs. S2 & S3 of the Supplement) with, both, 21 attributions. The evolution of
 vortices A, B1 and B2 is also available as animations in Sec. S3 of the Supplement. Vortex A was the first to separate from the
 mother [vortex](#) O by 22 August and moved first eastward until it reached central Asia by 1st September at a longitude of 60° E
 and a latitude of 55° N. It then got trapped into the region of slow motion that extends between the two centers of the Asian
 monsoon anticyclone (AMA), and started to drift slowly southward while staying at about the same longitude and maintaining
 210 its ascent rate. A week later it reached 35° N where it was caught into the easterly circulation and started to move westward
 crossing Africa and continuing its path which could be tracked until the west Pacific. Figure 6 shows a composite image of
 successive images of the localized ozone hole from the ERA5. It was easier to track the vortex using the ozone field than the
 PV. In particular the PV signal almost vanished as it passed over Africa (see the vortex A animation in the Supplement) while
 the ozone signature [WaS-was](#) always very clear. We attribute this vanishing to the strong infrared emissivity of the Sahara that
 215 limits the sensitivity of the IASI sounders which are important to sense the thermal signature of the vortex (Khaykin et al.,
 2020). [As ozone leaves also a signature in the ultra-violet seen by other assimilated](#) [The detection of ozone is less affected as it](#)
[uses also](#) instruments such as GOME-2 (Khaykin et al., 2020) [, it is less affected that operate in the ultraviolet range](#). The fact
 that the PV signature [reintensifies](#) [re-intensifies](#) as soon as the vortex is over the Atlantic supports this hypothesis. During the
 last stages of the vortex, by mid-October, we also see a premature loss of the PV signal while the ozone signal is still detectable
 220 [and can be detected beyond the end of our tracking](#). This pattern is shared by the two other vortices B1 and B2 and it differs

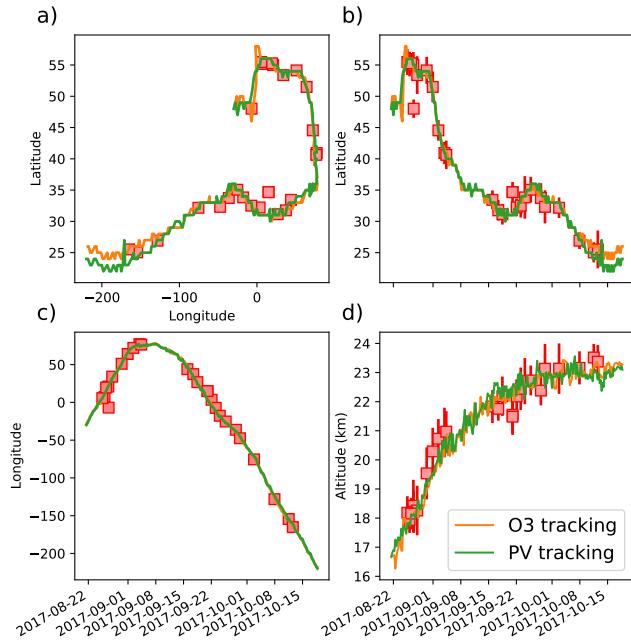


Figure 5. Trajectory of the vortex A tracked from the ERA5 fields of PV (orange) and ozone (green). a) Trajectory in the longitude-latitude plane; b, c, d respectively: latitude, longitude and altitude as a function of time. The [green curves are mostly masking the orange curves as they almost exactly coincide](#). The boxes show the location of smoke bubble according to CALIOP during CALIPSO overpasses and the bars indicate the range of the bubble in latitude and altitude.

from the 2020 case where such effect is not observed for any of the three vortices [studied by Khaykin et al. \(2020\)](#). Besides the increase of the IASI fleet from two to three instruments, we do not see any drastic change in the observation system between the two events.

While the vortex A was completing its transition to the tropics, the two other vortices B1 and B2 travelled eastward within 225 the westerly flow on the north side of the AMA reaching together the Pacific on 18 September. The vortex B1 crossed the Pacific at mid latitude and got lost near Hudson Bay after crossing most of North America by 14 October. The vortex B2 travelling at higher latitude completed a full round the globe travel during the same period, and got lost over central Asia by 11 October. Figure 7 summarized the trajectories of the vortices O, A, B1 and B2 from their [birth formation](#) to their loss. The total [recorded paths](#) of the four vortices are 13000, 42400, 28500 and 33400 km, respectively. They rose up to 23 km for vortex A 230 and to 21 km for vortices B1 and B2 ([altitudes of the core](#)).

[Trajectories of the vortices based on low ozone anomaly from the ERA5 analysis at 6-hour sampling. The colour gradient along each trajectory shows the time evolution of the vortices. We follow vortex O from 14 July 2017 until 31 August where it is relabelled as vortex B2 following its course until 11 October. Vortex A separates from vortex O on 22 August and is followed until 18 October. Vortex B1 separates from vortex O on 27 October and is followed until 14 October. The third panel shows](#)

235 the ascent both in altitude (left axis and lower set of curves) and potential temperature (right axis and upper set of curves). The crosses cover the part of each trajectory where CALIOP was not available.

3.5 Comparison with previous studies

Several previous studies have discussed various stages of the smoke cloud evolution described above although none made the link with a PV structure. A number of comments are here in order:

240 – The ascent rate was the strongest during the initial stage of vortex O when it rose from its origin just above the tropopause. Previous studies based on CALIOP or limb sounding instruments reported an ascent rate using the upper envelop of the bubble. Yu et al. (2019) reported an ascent from 14 to 20 km from 15 to 24 ~~October~~ [August](#) and Khaykin et al. (2018) reported an ascent of 30 K of potential temperature per day, that is 3 km per day, between 16 and 18 August. We used the centroid of the PV and O3 anomalies to define the ascent and found (see Fig. S1 of the Supplement) that the vortex 245 O ascended from 12 to 17 km between 14 and 24 ~~October~~ [August](#) which is consistent with Yu et al. (2019) but we found no trace of a faster ascent. From 24 to 31 August, the two vortices O and A (see Fig. 5) climbed by 2 km and vortex A maintained this rate until 8 September where it reached 21 km. It took one more month to reach the maximum altitude of 23 km while B1 and B2 reached 21 km within the same time. [At the very initial stage, Torres et al. \(2020\) claim an ascent of 20 K day⁻¹ on 14 August when the smoke bubble is detected by the first time in the stratosphere by CALIOP.](#) 250 [However, the assumption of a tropopause crossing between 13 August and 14 August is questionable as the sections of CALIOP through the smoke cloud were on its periphery on 13 August, as shown by Fig. 1d of Torres et al. \(2020\) \(even adding the missing night orbit\). Therefore, it is equally plausible that the pyro-convective event has injected directly smoke in the stratosphere without need of a large internal radiative heating.](#)

255 – Peterson et al. (2018) noticed the [birth formation](#) of vortex O from CALIPSO and OMPS / SUOMI NPP overpasses on 14 August in north Canada. Both Khaykin et al. (2018) and Peterson et al. (2018) reported that the first smoke patches reached Europe by 19 August and they were observed by a ground lidar [stations station](#) in central Europe on 22 August (Ansmann et al., 2018) [\(Ansmann et al., 2018; Baars et al., 2019\)](#). These patches followed a northern route faster than that of vortex O and were seen as filamentary structures by CALIOP. Their forefront reached Asia by 24 August. By 260 29 August a thick layer of smoke with aerosol optical depth 0.04 was seen from a lidar in south east France at 19 km (Khaykin et al., 2018) corresponding to the passage of vortex O in the vicinity. According to our tracking, ~~it~~ the lidar saw the tail connecting vortex O to vortex B1 in course of separation (see Sect.3.3). Bourassa et al. (2019) noticed the southward motion of vortex A over Central Asia but interpreted it as a split of the plume over this region by 1st September while in fact the separation occurred one week before. It is tempting to see a trace of the vortex A in the OMPS signal at 30° N above 20 km during September in Fig.1 of Bourassa et al. (2019) and in the SAGE III low latitude signal above 265 20 km during October in Fig. 1d of Kloss et al. (2019). Bourassa et al. (2019) have been able to track smoke patches until January 2018 and the global signature at altitudes up [to](#) 24 km persisted until summer 2018 (Kloss et al., 2019).

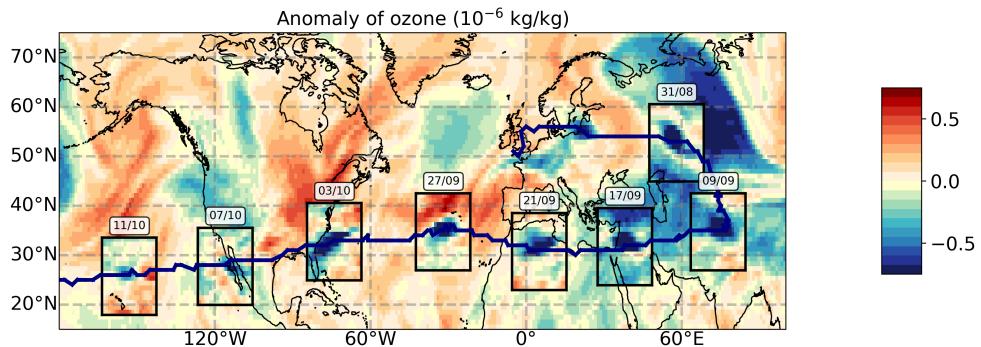


Figure 6. Sequence of ozone anomalies along the trajectory of vortex A for selected dates from 31 August to 11 October. The background is the mean ozone anomaly over this period at 460 K. For each selected day, the box shows the ozone anomaly on that day at 0:00 UTC at the level of the vortex centroid according to the ozone anomaly tracking, reported along the blue line.

270

275

280

- Kloss et al. (2019), using several satellite instruments and transport calculations, found transport of smoke patches to the tropics that is-was performed on the eastern southward branch of the AMA but they excluded transport across the AMA which is what we observe for vortex A. These authors focused their work on the events of the last week of August and on levels below 20 km. The transition of vortex A occurred in early September and it was already above 20 km. The smoke layer that Kloss et al. (2019) subsequently followed in the tropics includes the effect of vortex A.
- Baars et al. (2019) show interesting evidence of aerosol patches over Europe and the Mediterranean area reaching 23 km by mid September 2017 and again in mid December 2017. Although unstated, they do not expect the second patches to be the remnant of the first. They instead provide an explanation based on a circuit identified by Kloss et al. (2019), where smoke patches were injected into the tropics by early September. The smoke then rose slowly to higher levels in the tropics and came back to the mid latitudes carried by the Brewer-Dobson meridional circulation. There is, however, a hole in Baars et al. (2019) reasoning which is that the tropical rise is reported to reach 21 km by March 2018 while the aerosols supposedly blown away by the Brewer-Dobson are found at 23 km over Europe in December 2017. It is now clear that the missing piece of the puzzle is provided by vortex A which reached 23 km by late September (with a top at 24–25 km) leaving a tail along its path.

4 Structure of the vortices in 2020 and 2017

4.1 Composite analysis of the vortices in the ERA5

We investigate here the structure of the vortices by the mean of a composite analysis. The dynamical fields surrounding the vortex centroids were regridded regularly in Cartesian geometry in the horizontal and log-pressure altitude (Andrews et al., 1987) in the vertical, within a moving frame which follows the centroids ascent and meridional–horizontal displacement. As in

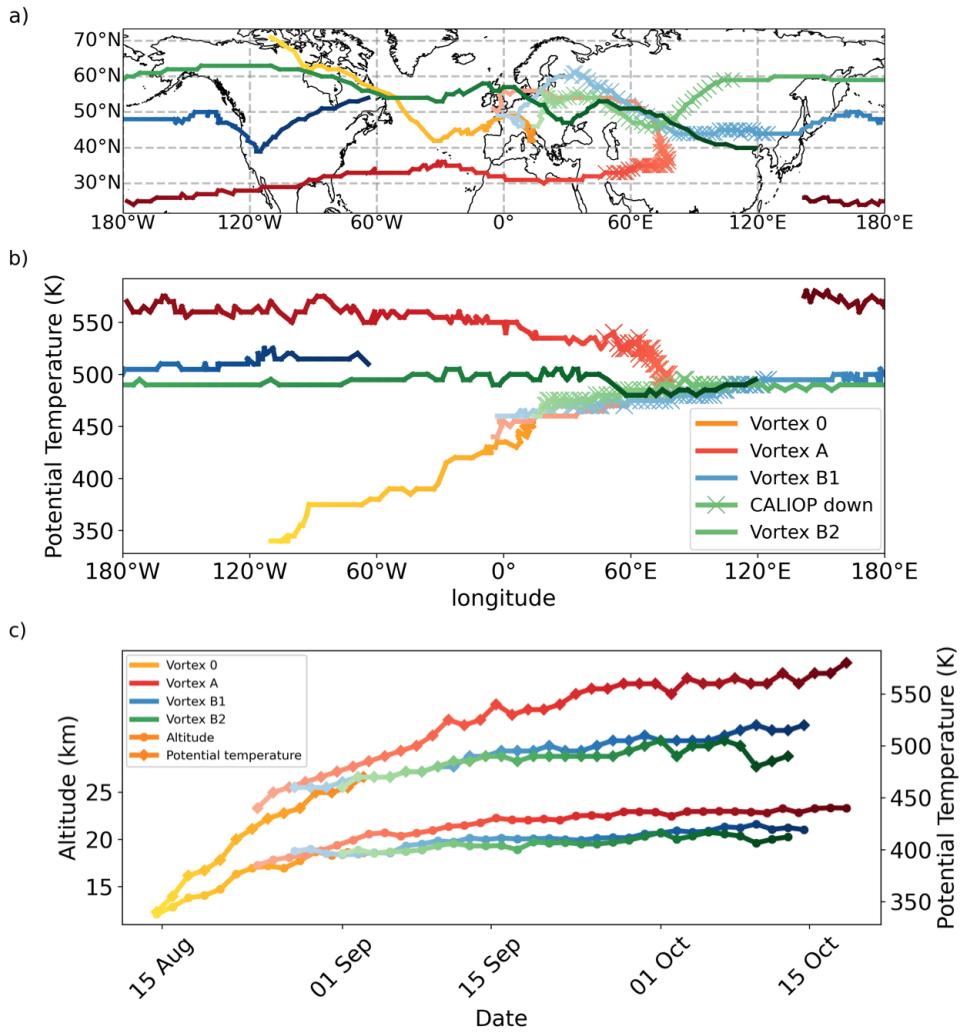


Figure 7. Trajectories of the vortices based on low-ozone anomaly from the ERA5 analysis at 6-hour sampling. The colour gradient along each trajectory shows the time evolution of the vortices. We follow vortex O from 14 July 2017 until 31 August where it is relabelled as vortex B2 following its course until 11 October. Vortex A separates from vortex O on 22 August and is followed until 18 October. Vortex B1 separates from vortex O on 27 October and is followed until 14 October. The third panel shows the ascent both in altitude (left axis and lower set of curves) and potential temperature (right axis and upper set of curves). The crosses cover the part of each trajectory where CALIOP was not available.

Khaykin et al. (2020), the composited model fields were then averaged in time to generate a composite analysis that filters out noise and ~~vacillations~~ variability unrelated to the vortices and emphasizes their mean structure.

This procedure also removes short-term vacillations (see Khaykin et al., 2020; Allen et al., 2020) which are a common property of vortices in shear flow (e.g. Tsang and Dritschel, 2015), thus enabling us to emphasize the mean structure of the

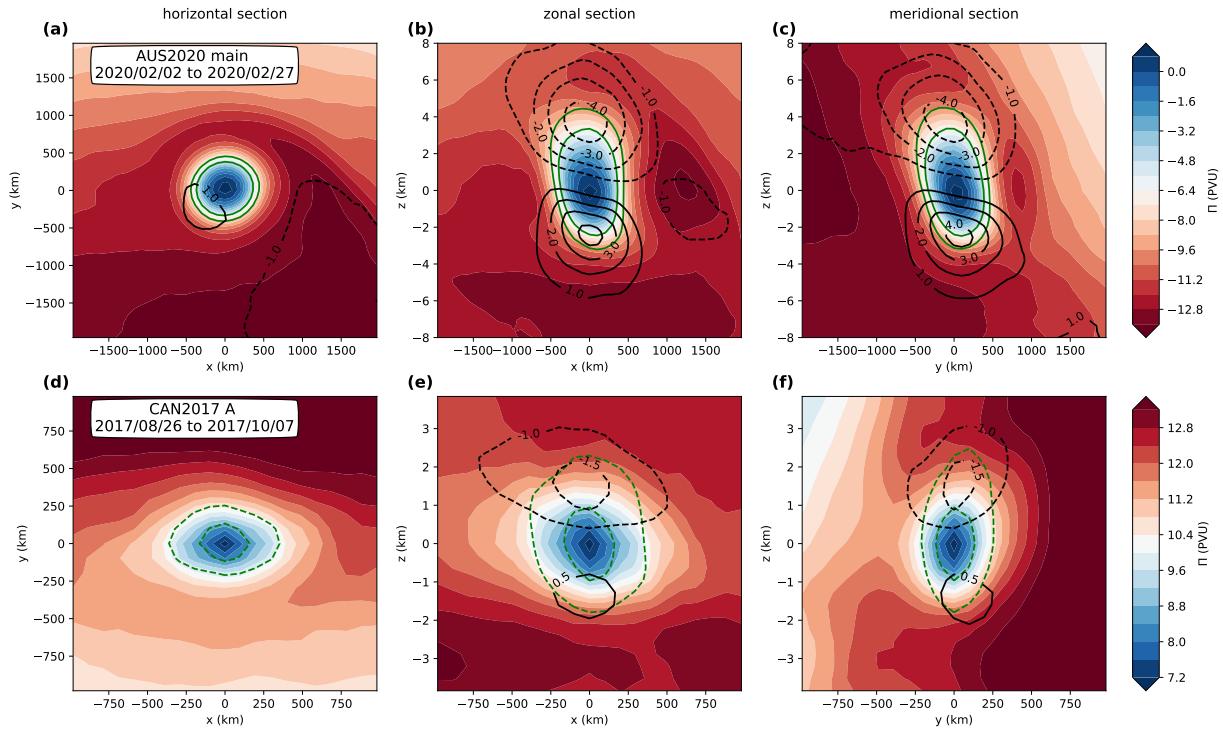


Figure 8. Time average composite sections of Lait PV II, in PVU ($1 \text{ PVU} = 10^{-6} \text{ Km}^2 \text{kg}^{-1} \text{s}^{-1}$), following two selected smoke charged vortices, the [major vortex](#)-[main Koobor vortex](#) from the 2020 Australian wildfires described in Khaykin et al. (2020) (a, b, c) and vortex A introduced in this paper (d, e, f). Panels a) and d), b) and e) and c) and f) are respectively horizontal, zonal and meridional sections through the centroid of the vortex. The green lines are contours of anticyclonic vertical vorticity (corresponding to $3 \cdot 10^{-5}$ and $5 \cdot 10^{-5} \text{ s}^{-1}$ for the top panels, and $-1.5 \cdot 10^{-5}$ and $-2.5 \cdot 10^{-5} \text{ s}^{-1}$ for the bottom panels). The black contours are temperature anomaly with respect to the zonal mean. Note that the displayed horizontal [range is and vertical ranges are](#) reduced by a factor of 2 for vortex A.

290 [vortex](#). Figure 8 depicts the composite of Lait PV II (defined in Eq. (2)) and temperature anomaly following vortex A (bottom panels) and the main [vortex](#)-[Koobor Koobor vortex](#) (top panels) generated by the 2020 Australian fires and tracked by Khaykin et al. (2020). In the natural coordinates, without expanding the vertical direction, both vortices appear as isolated pancakes of anomalous anticyclonic Lait PV (i.e., negative in the northern hemisphere and positive in the southern one). The analysed temperature anomaly consists in a vertical dipole surrounding the PV with negative temperature anomaly above and positive 295 temperature below it, where the centers are located on the upper and lower edges of the Lait PV distribution. As noted by Khaykin et al. (2020), this relationship between temperature stratification and vorticity is qualitatively consistent with the thermal wind balance, and characteristic of anticyclonic vortices in the quasi-geostrophic (QG) equations (Dritschel et al., 2004), but also of balanced anticyclones in the full primitive equations (e.g. Hoskins et al., 1985). In the case of the smoke-charged vortices investigated here, it turns out that their intensity is slightly beyond that of the typical geostrophic flow. The

300 typical Rossby number of the structure can be expressed as follows:

$$Ro = \frac{U}{f L_h} \simeq \frac{\bar{\zeta}}{f}, \quad (3)$$

with U the maximum horizontal wind speed, L_h the horizontal length scale (defined as the diameter of the ring of local wind speed maximum at the altitude of the centroid and estimated in the West-East direction) and $\bar{\zeta} = U/L_h$ the average relative vorticity. Ro is about 0.06 in the 2017 case and 0.35 for 2020. While in 2020 the Rossby number is beyond the typical
305 QG regime ($Ro < 0.1$), the aspect ratio α , defined as

$$\alpha = \frac{L_z}{L_h} \simeq 5 \cdot 10^{-3}, \quad (4)$$

(L_z being the vertical extent of the vorticity contour contour of vorticity at maximum wind speed at the horizontal location of the vortex centroid) obeys the stratified QG scaling $\alpha \simeq \frac{f}{N}$ in both cases, despite the 2017 vortex A being about 8-2.3 times smaller in volume than its gigantic 2020 counterpart.

310 To investigate further the dynamical regime in which the identified vortices evolve (or their representation in the IFS), Table 1 presents their typical sizes, amplitude characterized by the Rossby number Ro and the Froude number:

$$Fr = \frac{U}{L_z N} \quad (5)$$

as well as the absolute vorticity amplitude at the vortex centroid normalized by f :

$$\frac{\zeta_a}{f} = \frac{\zeta + f}{f} \quad (6)$$

315 which measures the inertial (in)stability of the flow. It should be noted that despite the similarity, $\frac{\zeta_a}{f}$ is not redundant with Ro defined in Eq. 3 and characterizes the extremum rather than the structure average of the vorticity.

Keeping in mind the limited vertical and horizontal resolution of the IFS, it can be noticed that the Froude and Rossby numbers are always of the same order, leading to a Burger number $Bu \sim 1$ as typically encountered in geophysical flows. Furthermore, most vortices in Table 1 obey the QG aspect ratio, so that they are quasi-spherical (see Fig. 8) when the vertical
320 coordinate is stretched by a factor $\frac{N}{f}$. This observation is consistent with numerical studies of ellipsoidal vortices, which have demonstrated that the higher stability of quasi-spherical vortices (Dritschel et al., 2005) and the tendency of aspherical vortices to relax towards sphericity in the stretched coordinate system $[x, y, \frac{N}{f} z]$ (Tsang and Dritschel, 2015).

Contrary to its aspect ratio, the magnitude of the vortex perturbation is case-dependent and does not necessarily fit in the classical QG scaling, thereby contrasting with the synoptic scale circulation. Indeed, typical vortex-averaged Rossby numbers
325 range from 0.06 up to 0.35, a range similar to observed mesoscale and submesoscale oceanic eddies (e.g. Le Vu et al., 2017). For the intense 2020 Koobor vortex, the maximum vorticity in the vortex core is on the verge of inertial instability or even slightly beyond its threshold for linear flows (Hoskins, 1974), as can be seen from the positive Π values in Fig. 8 (see also the small negative values of $\frac{\zeta_a}{f}$ in Table 1). This property was maintained over one month and half from the birth-formation of the Koobor vortex to its first breaking (see Fig. S4 of the [supplement](https://www.overleaf.com/project/603224684e539beef9522ffe)). Although it is not clear how realistic the ECMWF vortices are, their amplitude is likely underestimated since they

Table 1. Characteristics (horizontal diameter L_h , vertical depth L_z , aspect ratio α , QG aspect ratio imposed by the environment f/N , Rossby number, Froude number and maximum vorticity $\frac{\zeta_a}{f}$) of the six smoke charged pancake vortices originating from the Canadian (2017) and Australian (2020) wildfires. The [main vortex from 2020 Koobor vortex](#) was long-lasting and is here decomposed into two periods.

| name | geographic origin | considered period | L_h (km) | L_z (km) | $10^3 \alpha$ | $10^3 \frac{f}{N}$ | Ro | Fr | $\frac{\zeta_a}{f}$ |
|------------|-------------------|--------------------------|---------------|---------------|---------------|--------------------|------|------|---------------------|
| Koobor | Australia | 2020/01/07 to 2020/01/27 | 784 | 6.1 | 7.8 | 6.6 | 0.35 | 0.30 | 0.03 |
| Koobor | Australia | 2020/02/02 to 2020/02/27 | 784 | 6.1 | 7.8 | 5.8 | 0.33 | 0.25 | -0.09 |
| 2nd Vortex | Australia | 2020/01/18 to 2020/01/27 | 588 | 3.8 | 6.5 | 6.6 | 0.35 | 0.35 | -0.12 |
| 3rd Vortex | Australia | 2020/01/20 to 2020/02/07 | 588 | 7.7 | 13.1 | 7.9 | 0.10 | 0.06 | 0.72 |
| Vortex A | Canada | 2017/08/26 to 2017/10/07 | 686 | 3.5 | 5.1 | 4.8 | 0.06 | 0.06 | 0.6 |
| Vortex B1 | Canada | 2017/08/27 to 2017/10/07 | 588 | 4.5 | 7.6 | 6.2 | 0.12 | 0.10 | 0.56 |
| Vortex B2 | Canada | 2017/09/01 to 2017/10/07 | 490 | 3.8 | 7.8 | 7.0 | 0.11 | 0.09 | 0.6 |

are forced by data assimilation and the standalone model does not simulate them. We can therefore not generally conclude on the amplitude of the perturbations, in particular the smaller [NH Northern Hemisphere](#) vortices. Nevertheless, the 2020 cases demonstrate that the vorticity anomaly may reach the threshold for inertial instability at which it likely saturates.

Related to their different magnitudes, the vortices also have distinct impacts on their immediate surroundings, as can be identified in Fig. 8. While the 2020 Koobor vortex was strong enough to generate a significant cyclonic PV anomaly eastward of the vortex centroid which rolls up around it on its northern edge, no such signature can be distinguished around vortex A. In a zonal plane, the 2020 negative PV patch has diameter comparable to the [main Koobor](#) vortex but reduced magnitude. The existence of this negative anomaly can be attributed to the equatorward advection of [cyclonic](#) PV on the eastern flank of [the main vortex Koobor](#) and is likely responsible for the equatorward [beta-drift undergone by the main vortex beta-drift](#) ([Sai-Lap Lam and Dritschel, 2001](#)) [undergone by Koobor](#) during its ascent.

Finally, for completeness, two further remarks should be made. First, note that the vertical temperature dipole is slightly asymmetric with larger magnitude of the negative temperature anomaly. Second, panel (c) of Fig. 8 shows that the vertical axis of Koobor exhibits on average a small tilt with altitude, being slanted along the South-North direction, which is perpendicular to the prevailing background shear. This property is a common characteristic of vortices undergoing shear ([Tsang and Dritschel, 2015](#)) and related to the temporal vacillations of Koobor described by [Allen et al. \(2020\)](#) and also seen in Fig. 6 of [Khaykin et al. \(2020\)](#).

4.2 Diagnosing diabatic tendencies

By comparing the [main 2020 smoke-charged Koobor](#) vortex in ECMWF analyses and model forecasts, [Khaykin et al. \(2020\)](#) have shown two systematic shortcomings of the free-running model with respect to the analysis, namely:

- a failure to reproduce the observed ascent of the structure at about 6 K/day in potential temperature: on the contrary, the modeled anticyclones tend to remain at constant θ ;
- a decay of the vorticity anomaly within one week, while the observed vortex survives for more than 3 months.

355 This suggests that data assimilation of observed temperature and ozone profiles is a necessary ingredient to both ascent and the maintenance of the vortex in the model, while some physical or spurious processes act to dissipate the structure. In the atmosphere, it is assumed that the forcing is exerted by radiative heating through solar absorption by black carbon aerosols within the smoke (Yu et al., 2019). Increments are thus expected to play substitute in the analysis system for the diabatic tendency maintaining the vortices, as the wildfires smoke is missing in the model.

4.2.1 Temperature and vorticity tendencies

360 Figure 9 (a, d) depicts the average composite of the ERA 5 total heating due to physics calculated over the forecast. This field is dominated by the ~~long-wave~~ longwave radiative heating component since the ~~short-wave~~ shortwave absorption by the smoke is missing from the IFS. The dominant feature shown by Fig. 9 is a damping of the temperature anomaly T' with respect to radiative equilibrium temperature which can be cast into a Newtonian relaxation as:

$$\frac{DT'}{Dt} \simeq -\frac{T'}{\tau_{rad}} \quad (7)$$

365 where τ_{rad} is the radiative damping rate. Figure 9 suggests $\tau_{rad} \simeq 6 - 7$ days. This is consistent with the ~~life-time~~ life-time of the structure in the ECMWF forecast which is about one week (Khaykin et al., 2020), suggesting that radiative dissipation plays a major role in the decay of the vortex in the model but also in the real atmosphere.

370 However, since the model itself cannot sustain the vortices, it comes to data assimilation to maintain the structure. It was demonstrated by Khaykin et al. (2020) that the IFS extracts information from the thermal signature and the ozone anomaly detected by satellite instruments. The temperature increments are shown in Fig. 9 (b, e). In contrast with the heating rates, which are instantaneous forcing of the temperature by physical processes, the temperature increments result from the balanced dynamical response of the temperature field to the forcing induced by the discrepancy of measured radiances with respect to their estimated values in the assimilation procedure. Hence, the temperature pattern does not match the observed aerosol bubble ~~collocated~~ collocated with the vortex which would be expected for the ~~SW~~ shortwave aerosol absorption. It rather exhibits a multipolar structure, essentially oriented vertically. In the 2017 case with limited vertical ascent rate, the ~~T~~ T increment vertical dipole mainly cancels the radiative damping. In 2020, it is rather a dipole which enables the maintenance but also the ascent of the dipolar temperature anomaly structure.

380 Due to this dynamical adjustment, temperature is not the only field incremented via data assimilation. Figure 9 (c, ~~ef~~) shows the increments of relative vorticity ζ . They contribute again to the maintenance (2017 case) and ascent and maintenance (2020 case) of the vortices. Moreover, similarly to the composite vortex, the composite vorticity and temperature increment tendencies exhibit the structure of a balanced vortex: the 2017 anticyclonic ζ tendency monopole is sandwiched between the two extrema of temperature increment dipole whereas in 2020 the dipole of ~~T~~ T increment alternates with the two layers of

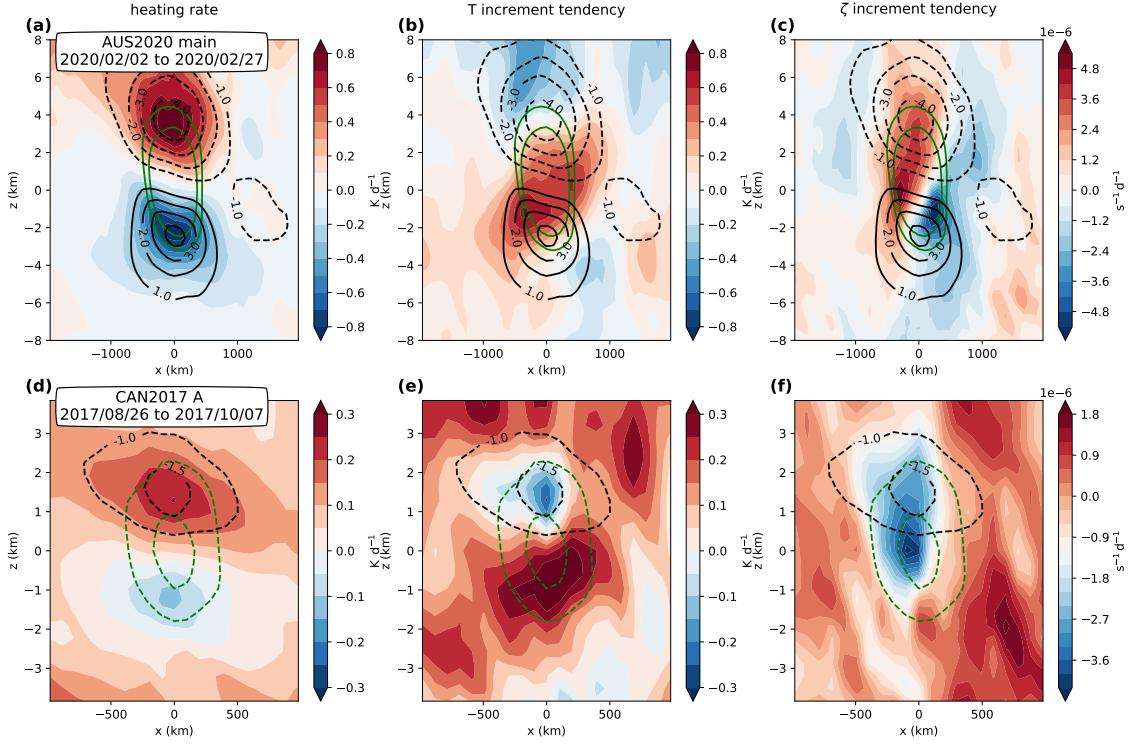


Figure 9. Time average composite sections of ERA 5 total heating rate (a, c), increment-induced temperature (b, e) and vorticity tendency (c, f) following two selected smoke charged vortices, the major vortex from the 2020 Australian wildfires described in Khaykin et al. (2020) (a, b, c) and vortex A (d, e, f). The green lines are contours of anticyclonic vertical vorticity (corresponding to $3 \cdot 10^{-5}$ and $5 \cdot 10^{-5} \text{ s}^{-1}$ for the top panels, and $-1.5 \cdot 10^{-5}$ and $-2.5 \cdot 10^{-5} \text{ s}^{-1}$ for the bottom panels). The black contours are temperature anomaly with respect to the zonal mean. Note that the displayed horizontal range is reduced by a factor of 2 for vortex A.

vorticity anomalies. Overall, the F-T and ζ patterns of the 2020 assimilation increment are qualitatively consistent with the expected effect of a localized heating in a rotating atmosphere (as sketched in fig.10 of Hoskins et al., 2003).

Together with the apparently balanced vortex structure of the increments, the similarity with the theoretical response in
385 Hoskins et al. (2003) suggests that potential vorticity (or Lait PV) is the appropriate field to consider for a more straightforward interpretation of the increments in terms of missing diabatic processes. This is the focus of the next subsection.

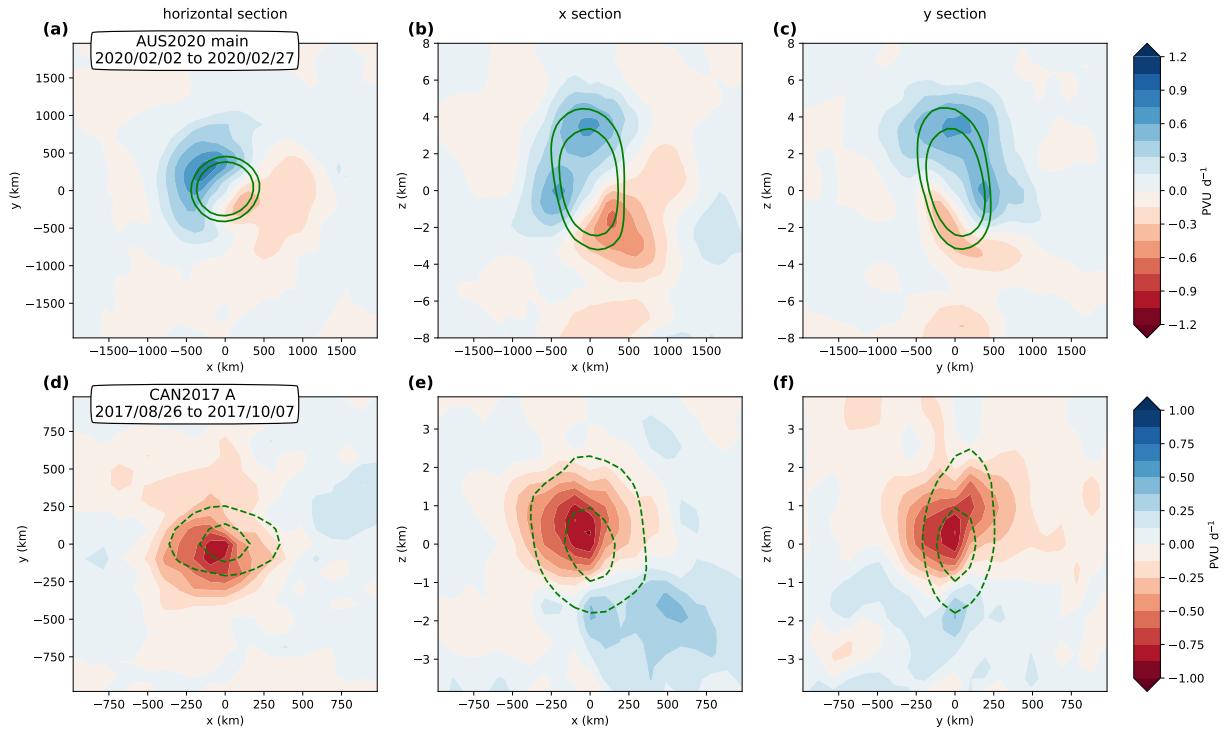


Figure 10. Same as Figure 8, but for Lait PV increments.

4.2.2 Lait PV and ozone tendencies due to assimilation increments

Composite time average increments of Lait PV Π are presented in Fig. 10. As stressed above, Π increments result from a combination of both temperature and vorticity and appear due to the implicit incorporation of temperature observations into an approximately dynamically-balanced response by the 4D-Var scheme used in the ERA5.

Contrary to the mean vortex structure in Fig. 8, we notice a stark contrast between the NH and SH Northern and Southern Hemisphere vortices. In the 2017 case, the Π increment shows a dominant monopole structure whose extremum is slightly shifted upward (by about 500 m) with respect to the Π extremum (Fig. 8). The effect of the increment is thus mainly to reinforce the existing Π anomaly and, secondarily, to drive its ascent. In contrast, the 2020 case shows essentially a vertical dipole structure which forces an ascent of the Π center. The dipole is furthermore tilted along a north-west to south-east axis. A qualitative analysis (Appendix B) shows that the observed westward tilt of the increment dipole emerges as a consequence of the negative zonal wind shear encountered by the main-2020 Koobor vortex along its ascent. More precisely, it is the combination of this shear and the distribution of the increment tendency over the 12 hours analysis time window which is responsible for the tilt. This feature may also be seen in other periods of Koobor lifetime during which the structure was drifting eastward, such as in the middle of January 2020 (see Fig. B1), emphasizing that the inclination of the increment dipole is due to the background wind shear rather than the local wind at the altitude of the vortex.

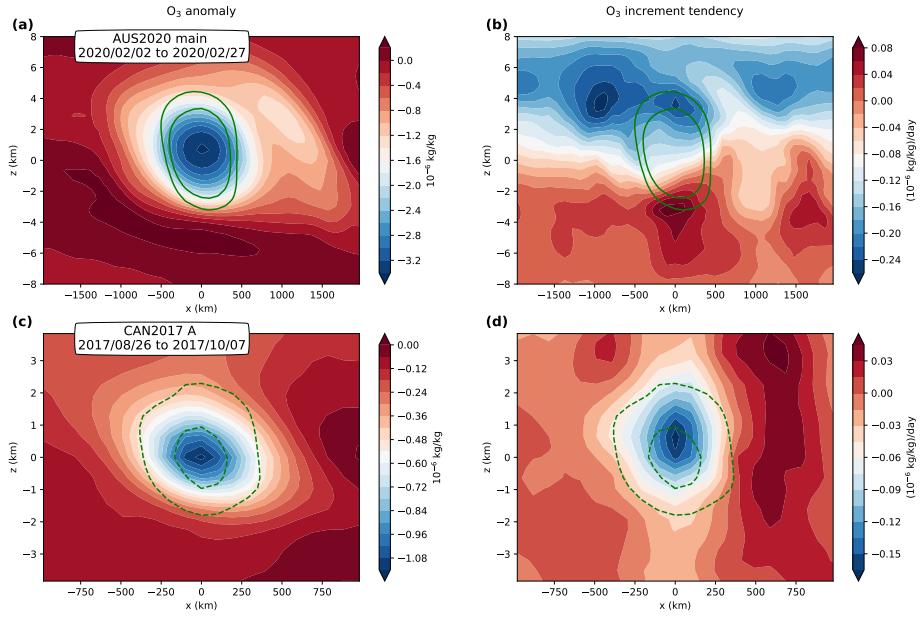


Figure 11. Same as Figure 9, but for ozone anomalies from the zonal mean ((a), (c)) and ozone increments ((b), (d)).

The different patterns of Lait PV II (Fig. 8) and its increment (Fig. 10) around the vortex are mimicked in the ozone field, as shown in Fig. 11. As described above, the ascending anticyclonic vorticity anomalies are accompanied by negative ozone anomalies (Fig. 11 a and c). Compared with Figs. 8 and 10, Fig. 11 shows that the patterns of the ozone anomaly bubble and its increment are very similar to those of II. We note that the magnitude of the increments may vary depending on the period chosen for the composite, for instance due to the different ascent speed of the vortex in log-pressure altitude coordinate (250 m/day in January versus 150 m/day in February for Koobor). However, the monopole and tilted dipole structures shown in Fig. 10 and Fig. 11 are representative of the typical situation found. Overall, model increments tend to (i) counter the dissipation and (ii) drive a cross-isentropic vertical motion of PV and ozone anomalies.

At this point, it is tempting to interpret the low ozone, low absolute PV anticyclones as resulting from the vertical advection of smoke-charged tropospheric air bubbles conserving both their low absolute PV and their tropospheric tracer content during their ascent in the stratosphere. In the case of the main-2020 plumeKoobor vortex, this perception is broadly consistent with the behavior of PV and PV anomaly at the center of the vortex, which respectively remain constant or exhibit a steady increase related to the large vertical gradient of PV within the stratosphere (Fig. S4 of the supplement). It is also consistent with our analysis of the developing stage of the mother vortex O in Sec. 3.2. We note, however, that the analogy between inert tracer and PV transport arises from their Lagrangian conservation in the adiabatic inviscid case and breaks in the presence of diabatic processes (Haynes and McIntyre, 1987). The maintenance of this relationship hence calls for dedicated theoretical and numerical investigations.

5 Conclusions

420 The generation of smoke-charged vortices rising in the southern stratosphere was discovered following the Australian ~~wildfires~~
~~wildfires~~ at the turn of 2019 (Khaykin et al., 2020). We find here that similar events took place in 2017 in the northern
stratosphere after the British Columbia ~~wildfires~~
~~wildfires~~ that culminated in early August 2017 when a large plume of smoke
and of low potential vorticity air has been injected in the lower stratosphere on 12 August 2017. We show that soon after, a
vortical structure developed in the plume and started to rise in the stratosphere. During the following days this smoke vortex
425 became an isolated bubble and was transported eastward across the Atlantic while getting elongated by the wind shear and
reaching 19 km in altitude at its top. Subsequently, that structure ~~dissociated~~
~~was split~~ over western Europe into three separate
vortices that could be followed until the middle of October 2017. Two of them kept moving eastward in the middle latitudes
and performed a round the globe travel, rising up to a potential temperature of 530 K (21 km). The third one has transited to
the subtropics across the Asian monsoon anticyclone and moved eastward until Asia. It also rose higher, to 570 K (23 ~~km~~km).
430 Our study demonstrates again the ability of the advanced assimilation system used at the ECMWF which is the basis of the
ERA5 to exploit the signature left by smoke vortices in the temperature and ozone fields and reconstruct the balanced vortical
structure. The balance is produced during the iterations of the assimilation and therefore the assimilation increment reflects this
balance by providing an increment on the wind as well as on the temperature. The increment is consistent with the expected
effect of a localized heating due to the radiative absorption of the smoke. It fights the ~~long-wave~~
~~longwave~~ radiative dissipation
435 and moves the vortices upward. It is quite likely, however, that the detection of vortices by the assimilation system is limited
by the sensitivity of the satellite instruments to the disturbances in the temperature and ozone fields. There are also detection
limits in CALIOP and limited chances to overpass small-scale structures if they are sparse enough. It is therefore possible that
a number of small-scale vortices escape the direct methods used in this study. It is also possible that dynamical constrains, like
the ambient shear, limit the existence of such vortices. It is thus difficult to conclude from our study what is the generality of
440 such structures and their global impact. It is however quite clear that they provide an effective way for smoke plumes to stay
compact and concentrated inducing a rise of the order of 10 km or more in the stratosphere that, in turns, increases the ~~life~~
~~time~~
~~life-time~~ and the radiative impact mentioned in previous studies (Ditas et al., 2018) from months to years knowing the
character of the Brewer Dobson circulation (e.g. Butchart, 2014).

445 Long lived anticyclones dubbed as "frozen-in-anticyclones" (FrIAC) by Manney et al. (2006) have already been reported
in the Arctic stratosphere. They share a long life span with the smoke anticyclones but they differ in many other respects.
The FrIAC are deep barotropic structures extending from 550 K to 1300 K and are observed in the polar region after the
breaking of the winter polar vortex. They are generated by the isentropic intrusion of low latitude air with low PV (Allen et al.,
2011; Thiéblemont et al., 2011). Instead, the smoke vortices exhibit a strong baroclinic structure with a vertical temperature
dipole and are propelled through the layers of the stratosphere by their internal heating bringing tropospheric air to the middle
450 stratosphere at latitudes where the Brewer circulation does the opposite (Butchart, 2014).

As volcanic plumes in the stratospheric are usually made of secondary sulfuric acid aerosols that are considerably less
absorbing than the black carbon, raising compact plumes are not expected to be seen in the stratosphere after extratropical

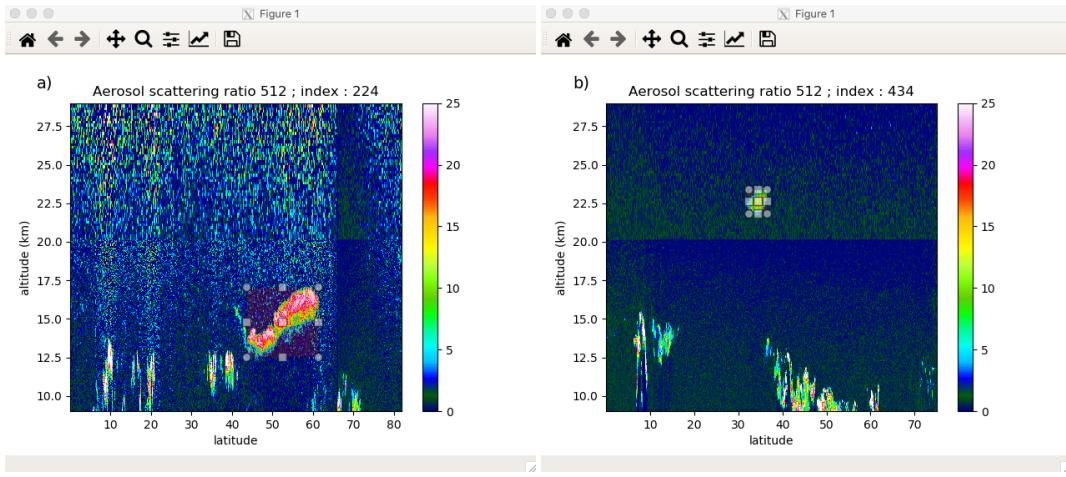


Figure A1. CALIOP sections with the superimposed box showing how the tracking is performed a) day-time orbit over bubble O on 19 August, b) night-time orbit over bubble A on 24 September.

volcanic eruptions. Such a case, however, has been reported after the 2019 eruption of the Raikoke (Chouza et al., 2020; Muser et al., 2020). This event which displays a slow rise and is not associated with a vortex in the ERA5 might fall below the 455 detection limit but opens the question of the possible role of heating by volcanic aerosols.

The conditions to maintain the stability of the smoke vortices and those leading to their final dilution are also not yet understood and this work is only opening a path to be explored.

Appendix A: Tracking of the smoke bubbles

Figure A1 shows two screenshots as examples of the interactive tracking of the smoke bubbles in CALIOP sections of the 460 scattering ratio. The first case (Fig. A1a) is taken from bubble O on 19 August when it was elongated within the Atlantic ~~thalweg~~trough. The second case (Fig. A1b) is taken from bubble A on 24 September while it was moving westward over the Atlantic. The interactive method used to perform the tracking is displayed in ~~a~~ an animation in Sec. S1 of the Supplement.

Appendix B: Increment structure around the ascending vortex in a sheared background wind

The average composite of Lait PV increment for the 2020 anticyclone (Fig. 10) exhibits a tilted dipole structure, whose inclination 465 by far exceeds the slight dip observed for the vortex axis and figured by the green vorticity contours in Fig. 10 **b**. This tilt causes the dipole to appear not only in vertical panes but also in the horizontal one (Fig. 10 **a**). The existence of the tilt is not related to the direction of the drift of the vortex: in January, when Koobor is drifting eastward due to the prevailing Westerlies, we observe the same general orientation of the increment dipole, as shown in Fig. B1.

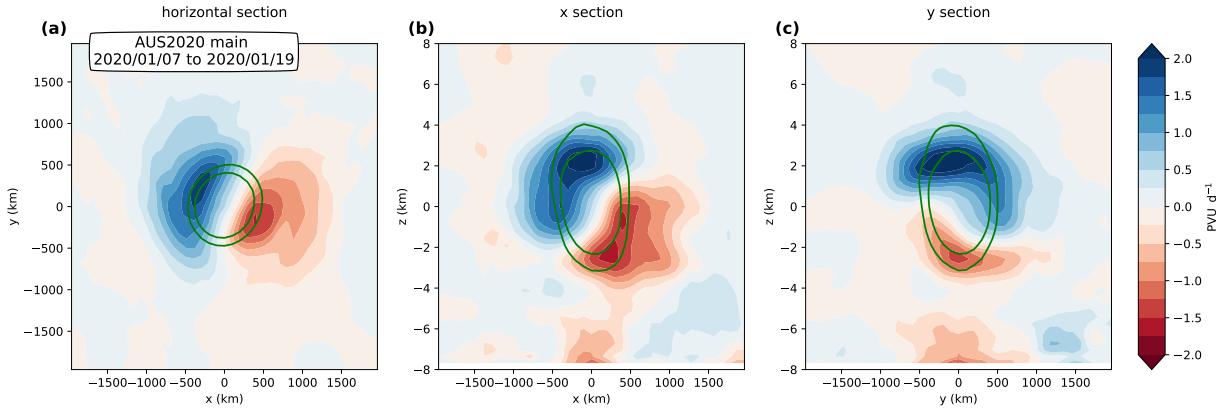


Figure B1. Same as Figure 10, but for Koobor Lait PV increments during the 2020/01/07–2020/01/19 time period. Note the different colorbar compared to Fig. 10. The different magnitude of the increments is due to the different ascent speed of the vortex in log-pressure altitude coordinate (250 m/day in January versus 150 m/day in February).

From a purely kinematic point of view, the dipolar structure of the increment shows that the forecast model systematically 470 underestimates both upward and westward motions (as well as northward in Fig. B1). While it is unlikely that the ECMWF forecast model underestimates zonal wind magnitude over such a long period, this missing westward displacement filled by the increments may be attributed to missing vertical ascent in an easterly sheared background wind.

This can be grasped by comparing trajectories advected by a sheared flow (wind profile $U(z) = U_0 + \Lambda z$ where Λ is the shear) with or without an ascent. The two situations are contrasted for a simplified case in Tab. B1. Over the finite analysis 475 time window Δt , the vertical velocity ascent rate W causes the parcel (here, the vortex) to be advected in a region of different mean wind and drift away from its non-ascending cousin. Hence, the additional motion brought by the ascent has both vertical and horizontal components, which can be expressed as:

$$(\dot{X}, \dot{Z})_{incr} = \left(\frac{\Lambda W}{2} \Delta t, W \right) \quad (B1)$$

The tendency of Π associated with a translation at speed $(\dot{X}, \dot{Z})_{incr}$ is:

$$480 \quad \partial_t \Pi = -\dot{X}_{incr} \partial_x \Pi - \dot{Z}_{incr} \partial_z \Pi \quad (B2)$$

If we consider the isolated bubble of maximum potential vorticity anomaly P_{max} and length scales L_x and $L_z = \alpha L_x$, the magnitude of the tendency required to translate it along x and z are then:

$$\begin{aligned} \partial_t \Pi|_{x=0} &= -W \frac{2\Pi_{max}}{L_z} \\ \partial_t \Pi|_{z=0} &= -\Lambda W \frac{\Delta t}{2} \frac{2\Pi_{max}}{L_x} \end{aligned} \quad (B3)$$

and their ratio γ is:

$$485 \quad \gamma = \frac{\partial_t \Pi(z=0)}{\partial_t \Pi(x=0)} = \alpha \Lambda \frac{\Delta t}{2} \quad (B4)$$

Table B1. Analytical trajectory of a bubble in an idealized sheared wind profile: $U(z) = U_0 + \Lambda z$ with (forecast) or without (analysis) vertical ascent, and resulting average speed.

| | forecast | analysis (atmosphere) |
|--|-----------------------------------|--|
| vertical velocity | $\dot{Z} = 0$ | $\dot{Z} = W$ |
| horizontal velocity | $\dot{X} = U_0$ | $\dot{X} = U_0 + \Lambda Z$ |
| vertical trajectory | $Z(t) = Z_0$ | $Z(t) = Z_0 + Wt$ |
| horizontal trajectory | $X(t) = X_0 + U_0 t$ | $X(t) = X_0 + U_0 t + \frac{\Lambda W}{2} t^2$ |
| averaged vertical velocity over Δt | $\frac{\Delta Z}{\Delta t} = 0$ | $\frac{\Delta Z}{\Delta t} = W$ |
| averaged horizontal velocity over Δt | $\frac{\Delta X}{\Delta t} = U_0$ | $\frac{\Delta X}{\Delta t} = U_0 + \frac{\Lambda W}{2} \Delta t$ |

In the case of the 2020 vortex, $\alpha \simeq 7.8 10^{-3}$, $\Lambda \simeq 3.10^{-3} \text{ s}^{-1}$ and the background shear Λ estimated in a 8 km layer around the vortex varies from $\simeq -3.10^{-3} \text{ s}^{-1}$ in January 7-19 to $\simeq -2.10^{-3} \text{ s}^{-1}$ in February 2-27. With those values and the assimilation window is $\Delta t = 0.5$ day so that $\gamma \simeq 0.5$, that $|\gamma|$ is of the order of 0.3 to 0.5, which is quantitatively consistent with Fig. 10, panel b) and Fig. B1. When the shear is properly taken into account, the westward drift induced by the increments can thus be reconciled with the idea that the ascent is the main process lacking from the model. Note that this reasoning also applies to ozone.

Author contributions. The four authors performed together the analysis. HL, BL and AP wrote the manuscript. All authors contributed to the final version.

Competing interests. We declare that no competing interest are present.

495 *Acknowledgements.* CALIOP data were provided by the ICARE/AERIS data centre. ERA-5 data were provided by Copernicus Climate Change Service Information. This work was supported the TTL-Xing ANR-17-CE01-0015 project of Agence Nationale de la Recherche.

References

Allen, D. R., Douglass, A. R., Manney, G. L., Strahan, S. E., Krosschell, J. C., Trueblood, J. V., Nielsen, J. E., Pawson, S., and Zhu, Z.: Modeling the Frozen-In Anticyclone in the 2005 Arctic Summer Stratosphere, *Atmospheric Chemistry and Physics*, 11, 4557–4576, 500 https://doi.org/10.5194/acp-11-4557-2011, 2011.

Allen, D. R., Fromm, M. D., Kablick III, G. P., and Nedoluha, G. E.: Smoke with Induced Rotation and Lofting (SWIRL) in the Stratosphere, *Journal of the Atmospheric Sciences*, 77, 4297–4316, https://doi.org/10.1175/JAS-D-20-0131.1, 2020.

Andrews, D., Holton, J., and Leovy, C.: *Middle Atmosphere Dynamics.*, Academic Press, 1987.

Ansmann, A., Baars, H., Chudnovsky, A., Mattis, I., Veselovskii, I., Haarig, M., Seifert, P., Engelmann, R., and Wandinger, U.: Extreme 505 Levels of Canadian Wildfire Smoke in the Stratosphere over Central Europe on 21–22 August 2017, *Atmospheric Chemistry and Physics*, 18, 11 831–11 845, https://doi.org/10.5194/acp-18-11831-2018, 2018.

Baars, H., Ansmann, A., Ohneiser, K., Haarig, M., Engelmann, R., Althausen, D., Hanssen, I., Gausa, M., Pietruczuk, A., Szkop, A., Stach- 510 lewska, I. S., Wang, D., Reichardt, J., Skupin, A., Mattis, I., Trickl, T., Vogelmann, H., Navas-Guzmán, F., Haefele, A., Acheson, K., Ruth, A. A., Tatarov, B., Müller, D., Hu, Q., Podvin, T., Goloub, P., Veselovskii, I., Pietras, C., Haeffelin, M., Fréville, P., Sicard, M., Comerón, A., Fernández García, A. J., Molero Menéndez, F., Córdoba-Jabonero, C., Guerrero-Rascado, J. L., Alados-Arboledas, L., Bortoli, D., Costa, M. J., Dionisi, D., Liberti, G. L., Wang, X., Sannino, A., Papagiannopoulos, N., Boselli, A., Mona, L., D'Amico, G., Romano, S., Perrone, M. R., Belegante, L., Nicolae, D., Grigorov, I., Gialitaki, A., Amiridis, V., Soupiona, O., Papayannis, A., Mamouri, 515 R.-E., Nisantzi, A., Heese, B., Hofer, J., Schechner, Y. Y., Wandinger, U., and Pappalardo, G.: The Unprecedented 2017–2018 Stratospheric Smoke Event: Decay Phase and Aerosol Properties Observed with the EARLINET, *Atmospheric Chemistry and Physics*, 19, 15 183–15 198, https://doi.org/10.5194/acp-19-15183-2019, 2019.

Bourassa, A. E., Rieger, L. A., Zawada, D. J., Khaykin, S., Thomason, L. W., and Degenstein, D. A.: Satellite Limb Observations of Unprecedented Forest Fire Aerosol in the Stratosphere, *Journal of Geophysical Research: Atmospheres*, 124, 9510–9519, 520 https://doi.org/10.1029/2019JD030607, 2019.

Butchart, N.: The Brewer-Dobson Circulation, *Reviews of Geophysics*, 52, 157–184, https://doi.org/10.1002/2013RG000448, 2014.

Chouza, F., Leblanc, T., Barnes, J., Brewer, M., Wang, P., and Koon, D.: Long-Term (1999–2019) Variability of Stratospheric Aerosol over 525 Mauna Loa, Hawaii, as Seen by Two Co-Located Lidars and Satellite Measurements, *Atmospheric Chemistry and Physics*, 20, 6821–6839, https://doi.org/10.5194/acp-20-6821-2020, 2020.

de Laat, A. T. J., Stein Zweers, D. C., Boers, R., and Tuinder, O. N. E.: A Solar Escalator: Observational Evidence of the Self-Lifting of Smoke and Aerosols by Absorption of Solar Radiation in the February 2009 Australian Black Saturday Plume: OBSERVATIONS 530 OF SELF-LIFTING AEROSOLS, *Journal of Geophysical Research: Atmospheres*, 117, n/a–n/a, https://doi.org/10.1029/2011JD017016, 2012.

Ditas, J., Ma, N., Zhang, Y., Assmann, D., Neumaier, M., Riede, H., Karu, E., Williams, J., Scharffe, D., Wang, Q., Saturno, J., Schwarz, J. P., Katich, J. M., McMeeking, G. R., Zahn, A., Hermann, M., Brenninkmeijer, C. A. M., Andreae, M. O., Pöschl, U., Su, H., and Cheng, Y.: Strong Impact of Wildfires on the Abundance and Aging of Black Carbon in the Lowermost Stratosphere, *Proceedings of the National Academy of Sciences*, 115, E11 595–E11 603, https://doi.org/10.1073/pnas.1806868115, 2018.

Dritschel, D. G., Reinaud, J. N., and McKIVER, W. J.: The quasi-geostrophic ellipsoidal vortex model, *Journal of Fluid Mechanics*, 505, 201–223, https://doi.org/10.1017/S0022112004008377, 2004.

Dritschel, D. G., Scott, R. K., and Reinaud, J. N.: The Stability of Quasi-Geostrophic Ellipsoidal Vortices, *Journal of Fluid Mechanics*, 536, 401–421, <https://doi.org/10.1017/S0022112005004921>, 2005.

535 Ertel, H.: Ein neuer hydrodynamischer Erhaltungssatz, *Die Naturwissenschaften*, 30, 543–544, <https://doi.org/10.1007/BF01475602>, 1942.

Fromm, M., Lindsey, D. T., Servranckx, R., Yue, G., Trickl, T., Sica, R., Doucet, P., and Godin-Beekmann, S.: The Untold Story of Pyrocumulonimbus, *Bulletin of the American Meteorological Society*, 91, 1193–1210, <https://doi.org/10.1175/2010BAMS3004.1>, 2010.

Hanes, C. C., Wang, X., Jain, P., Parisien, M.-A., Little, J. M., and Flannigan, M. D.: Fire-regime changes in Canada over the last half century, *Canadian Journal of Forest Research*, 49, 256–269, <https://doi.org/10.1139/cjfr-2018-0293>, 2019.

540 Haynes, P. H. and McIntyre, M. E.: On the Evolution of Vorticity and Potential Vorticity in the Presence of Diabatic Heating and Frictional or Other Forces, *Journal of the Atmospheric Sciences*, 44, 828–841, [https://doi.org/10.1175/1520-0469\(1987\)044<0828:OTEVOVA>2.0.CO;2](https://doi.org/10.1175/1520-0469(1987)044<0828:OTEVOVA>2.0.CO;2), 1987.

Hersbach, H., Bell, B., Berrisford, P., Hirahara, S., Horányi, A., Muñoz-Sabater, J., Nicolas, J., Peubey, C., Radu, R., Schepers, D., Simmonds, A., Soci, C., Abdalla, S., Abellán, X., Balsamo, G., Bechtold, P., Biavati, G., Bidlot, J., Bonavita, M., Chiara, G. D., Dahlgren, 545 P., Dee, D., Diamantakis, M., Dragani, R., Flemming, J., Forbes, R., Fuentes, M., Geer, A., Haimberger, L., Healy, S., Hogan, R. J., Hólm, E., Janisková, M., Keeley, S., Laloyaux, P., Lopez, P., Lupu, C., Radnoti, G., Rosnay, P. d., Rozum, I., Vamborg, F., Vil- laume, S., and Thépaut, J.-N.: The ERA5 global reanalysis, *Quarterly Journal of the Royal Meteorological Society*, 146, 1999–2049, <https://doi.org/10.1002/qj.3803>, 2020.

Hoffmann, L., Günther, G., Li, D., Stein, O., Wu, X., Griessbach, S., Heng, Y., Konopka, P., Müller, R., Vogel, B., and Wright, J. S.: 550 From ERA-Interim to ERA5: The Considerable Impact of ECMWF's next-Generation Reanalysis on Lagrangian Transport Simulations, *Atmospheric Chemistry and Physics*, 19, 3097–3124, <https://doi.org/10.5194/acp-19-3097-2019>, 2019.

Hoskins, B., Pedder, M., and Jones, D. W.: The Omega Equation and Potential Vorticity, *Quart. J. Roy. Met. Soc.*, 129, 3277–3303, <https://doi.org/10.1256/qj.02.135>, 2003.

Hoskins, B. J.: The Role of Potential Vorticity in Symmetric Stability and Instability, *Quarterly Journal of the Royal Meteorological Society*, 555 100, 480–482, <https://doi.org/10.1002/qj.49710042520>, 1974.

Hoskins, B. J., McIntyre, M. E., and Robertson, A. W.: On the Use and Significance of Isentropic Potential Vorticity Maps, *Quarterly Journal of the Royal Meteorological Society*, 111, 877–946, <https://doi.org/10.1002/qj.49711147002>, 1985.

Hostetler, C. A., Liu, Z., Reagan, J. A., Vaughan, M., Winker, D., Osborn, M., Hunt, W. H., Powell, K. A., and Trepte, C.: CALIOP Algorithm Theoretical Basis Document. Calibration and Level 1 Data Products, Tech. Rep. Doc. PS-SCI-201, NASA Langley Res. Cent., Hampton, 560 VA, 2006.

Kablick, G. P., Allen, D. R., Fromm, M. D., and Nedoluha, G. E.: Australian PyroCb Smoke Generates Synoptic-Scale Stratospheric Anti-cyclones, *Geophysical Research Letters*, 47, e2020GL088101, <https://doi.org/10.1029/2020GL088101>, 2020.

Khaykin, S., Legras, B., Bucci, S., Sellitto, P., Isaksen, L., Tence, F., Bekki, S., Bourassa, A., Rieger, L., Zawada, D., Jumelet, J., and Godin-Beekmann, S.: The 2019–2020 Australian wildfires generated a persistent smoke-charged vortex rising up to 35 km altitude, *Communications Earth and Environment*, 1, 22, <https://doi.org/10.1038/s43247-020-00022-5>, 2020.

565 Khaykin, S. M., Godin-Beekmann, S., Hauchecorne, A., Pelon, J., Ravetta, F., and Keckhut, P.: Stratospheric Smoke With Unprecedentedly High Backscatter Observed by Lidars Above Southern France, *Geophysical Research Letters*, 45, 1639–1646, <https://doi.org/10.1002/2017GL076763>, 2018.

Kloss, C., Berthet, G., Sellitto, P., Ploeger, F., Bucci, S., Khaykin, S., Jégou, F., Taha, G., Thomason, L. W., Barret, B., Le Flochmoen, E.,
570 von Hobe, M., Bossolasco, A., Bègue, N., and Legras, B.: Transport of the 2017 Canadian wildfire plume to the tropics via the Asian monsoon circulation, *Atmospheric Chemistry and Physics*, 19, 13 547–13 567, <https://doi.org/10.5194/acp-19-13547-2019>, 2019.

Lait, L. R.: An Alternative Form for Potential Vorticity, *Journal of the Atmospheric Sciences*, 51, 1754–1759, [https://doi.org/10.1175/1520-0469\(1994\)051<1754:AAFFPV>2.0.CO;2](https://doi.org/10.1175/1520-0469(1994)051<1754:AAFFPV>2.0.CO;2), 1994.

Le Vu, B., Stegner, A., and Arsouze, T.: Angular Momentum Eddy Detection and Tracking Algorithm (AMEDA) and Its Application to
575 Coastal Eddy Formation, *Journal of Atmospheric and Oceanic Technology*, 35, 739–762, <https://doi.org/10.1175/JTECH-D-17-0010.1>, 2017.

Manney, G. L., Livesey, N. J., Jimenez, C. J., Pumphrey, H. C., Santee, M. L., MacKenzie, I. A., and Waters, J. W.: EOS Microwave Limb Sounder Observations of “Frozen-in” Anticyclonic Air in Arctic Summer, *Geophysical Research Letters*, 33, L06 810, <https://doi.org/10.1029/2005GL025418>, 2006.

580 McIntyre, M.: DYNAMICAL METEOROLOGY | Balanced Flow, in: *Encyclopedia of Atmospheric Sciences*, pp. 298–303, Elsevier, <https://doi.org/10.1016/B978-0-12-382225-3.00484-9>, 2015.

Müller, R. and Günther, G.: A Generalized Form of Lait’s Modified Potential Vorticity, *Journal of the Atmospheric Sciences*, 60, 2229–2237, [https://doi.org/10.1175/1520-0469\(2003\)060<2229:AGFOLM>2.0.CO;2](https://doi.org/10.1175/1520-0469(2003)060<2229:AGFOLM>2.0.CO;2), 2003.

Muser, L. O., Hoshayaripour, G. A., Bruckert, J., Horvath, A., Malinina, E., Peglow, S., Prata, F. J., Rozanov, A., and Vogel, B.: Particle Aging
585 and Aerosol–Radiation Interaction Affect Volcanic Plume Dispersion: Evidence from Raikoke Eruption 2019, *Atmos. Chem. Phys. Disc.*, <https://doi.org/10.5194/acp-2020-370>, 2020.

Peterson, D. A., Campbell, J. R., Hyer, E. J., Fromm, M. D., Kablyk, G. P., Cossuth, J. H., and DeLand, M. T.: Wildfire-driven thunderstorms cause a volcano-like stratospheric injection of smoke, *npj Climate and Atmospheric Science*, 1, 1–8, <https://doi.org/10.1038/s41612-018-0039-3>, 2018.

590 Powell, K. A., Hostetler, C. A., Vaughan, M. A., Lee, K.-P., Trepte, C. R., Rogers, R. R., Winker, D. M., Liu, Z., Kuehn, R. E., Hunt, W. H., and Young, S. A.: CALIPSO Lidar Calibration Algorithms. Part I: Nighttime 532-nm Parallel Channel and 532-nm Perpendicular Channel, *Journal of Atmospheric and Oceanic Technology*, 26, 2015–2033, <https://doi.org/10.1175/2009JTECHA1242.1>, <https://journals.ametsoc.org/jtech/article/26/10/2015/3468/CALIPSO-Lidar-Calibration-Algorithms-Part-I>, 2009.

Sai-Lap Lam, J. and Dritschel, D. G.: On the Beta-Drift of an Initially Circular Vortex Patch, *Journal of Fluid Mechanics*, 436, 107–129,
595 <https://doi.org/10.1017/S0022112001003974>, 2001.

Thiéblemont, R., Huret, N., Orsolini, Y. J., Hauchecorne, A., and Drouin, M.-A.: Frozen-in Anticyclones Occurring in Polar Northern Hemisphere during Springtime: Characterization, Occurrence and Link with Quasi-Biennial Oscillation, *Journal of Geophysical Research*, 116, D20 110, <https://doi.org/10.1029/2011JD016042>, 2011.

Torres, O., Bhartia, P. K., Taha, G., Jethva, H., Das, S., Colarco, P., Krotkov, N., Omar, A., and Ahn, C.: Stratospheric Injection of Massive
600 Smoke Plume From Canadian Boreal Fires in 2017 as Seen by DSCOVR-EPIC, CALIOP, and OMPS-LP Observations, *Journal of Geophysical Research: Atmospheres*, 125, <https://doi.org/10.1029/2020JD032579>, 2020.

Tsang, Y.-K. and Dritschel, D. G.: Ellipsoidal Vortices in Rotating Stratified Fluids: Beyond the Quasi-Geostrophic Approximation, *Journal of Fluid Mechanics*, 762, 196–231, <https://doi.org/10.1017/jfm.2014.630>, 2015.

Vernier, J. P., Pommereau, J. P., Garnier, A., Pelon, J., Larsen, N., Nielsen, J., Christensen, T., Cairo, F., Thomason, L. W., Leblanc, T.,
605 and McDermid, I. S.: Tropical Stratospheric Aerosol Layer from CALIPSO Lidar Observations, *Journal of Geophysical Research*, 114, D00H10, <https://doi.org/10.1029/2009JD011946>, 2009.

Winker, D. M., Pelon, J., Jr, J. A. C., Ackerman, S. A., Charlson, R. J., Colarco, P. R., Flamant, P., Fu, Q., Hoff, R. M., Kittaka, C., Kubar, T. L., Treut, H. L., McCormick, M. P., Mégie, G., Poole, L., Powell, K., Trepte, C., Vaughan, M. A., and Wielicki, B. A.: The CALIPSO mission: A Global 3D View of Aerosols and Clouds, *Bulletin of the American Meteorological Society*, 91, 1211–1230, 2010.

610 Yu, P., Toon, O. B., Bardeen, C. G., Zhu, Y., Rosenlof, K. H., Portmann, R. W., Thornberry, T. D., Gao, R.-S., Davis, S. M., Wolf, E. T., de Gouw, J., Peterson, D. A., Fromm, M. D., and Robock, A.: Black carbon lofts wildfire smoke high into the stratosphere to form a persistent plume, *Science*, 365, 587–590, <https://doi.org/10.1126/science.aax1748>, 2019.