Hectometric scale simulations of a Mediterranean heavy precipitation event during HyMeX SOP1

Olivier Nuissier[1], Fanny Duffourg[2], Maxime Martinet[1], Véronique Ducrocq[1], and Christine Lac[1]

[1]CNRM (Météo-France & CNRS), 42 avenue G. Coriolis 31057 Toulouse Cédex
[2]CSG (CNES & Agence spatiale européenne)

Correspondence: Olivier Nuissier (olivier.nuissier@meteo.fr)

Abstract. Offshore convection occurred over the Mediterranean sea on 26 October 2012 and was well documented during the first Special Observation Period (SOP1) of the Hydrological cycle in the Mediterranean Experiment (HyMeX). This paper analyses the triggering and organizing factors involved in this convection case study, and examines how they are simulated and represented at hectometric resolutions. For that purpose, a Large Eddy Simulation (LES) of this real case study is carried out with a 150 m horizontal resolution over a large domain encompassing the convective systems, as well as the low level flow feeding convection over the sea. This LES is then compared to a reference simulation performed with a 450 m grid spacing in the heart of the so-called "grey zone" of turbulence modelling.

Increase of horizontal resolution from 450 m down to 150 m is unable to reduce significantly, for this case study, deficiencies of the simulation, more related to an issue of initial and lateral boundary conditions. Indeed, some of the triggering factors, such as a converging low level flow driven by a surface low pressure system, are simulated quite similarly for both simulations. However, differences for other mechanisms still exist since larger surface precipitation amounts are simulated at 450 m. It is found that the lack of a good representation of entrainment with a 450 m grid spacing along the edge of clouds causes a too quick triggering of deep convection at this resolution, associated with fast-track microphysical processes and enhanced dynamics. Furthermore, this first LES of a real Mediterranean precipitating case study highlights a convective organisation with very fine scale features within the converging low level flow, features that are definitively out of range of models with kilometric horizontal resolutions.

1   Introduction

Regularly during fall, Heavy Precipitation Events (HPEs) occur over the Northwestern Mediterranean basin and more particu-
larly over the mountainous coastal regions of France, Spain and Italy. In most cases, large amounts of precipitation are recorded
in less than one day (typically more than 200 mm in less than 24 h, and sometimes in only few hours) when a mesoscale
5   convective system (MCS) develops and stays over the same area for several hours (Nuissier et al., 2008; Buzzi et al., 2014;
Davolio et al., 2016; Duffourg et al., 2018, among others).

Several past case studies, especially in the framework of the HyMeX Special Observation Period (SOP1), have investigated
extensively the mechanisms and physical processes associated with such high-impact events, based on numerical experiments
with kilometric horizontal resolutions and dedicated observations (Ducrocq et al., 2016). Over the Western Mediterranean
10   region, HPEs evolve often within a favourable synoptic pattern, including an upper level trough centred over the Iberian Penin-
sula and/or high values of geopotential anchored over Central Europe, driving a persistent low-level moist and conditionally
unstable marine flow directed towards the coastal mountainous regions. Due to regional and local effects, the low level flow
is then deflected by neighbouring mountain ranges (Pyrénées, Massif Central and Alps) or islands such Corsica and Sardinia.
In order to trigger the deep convection, a lifting mechanism is needed to focus and finally release the conditional convective
15   instability at the same location. Orographic lifting of the conditionally unstable low level marine flow impinging the foothills
neighbouring the Western Mediterranean is a well-studied mechanism for renewing convection triggering at the same location
(Barthlott and Davolio, 2016; Duffourg et al., 2018). Lifting can also be due to local convergence in the low-level circulation
induced by the orography of the region (Barthlott et al., 2016; Buzzi et al., 2014; Scheffknecht et al., 2016) or lee cyclogeneses
(Jansa et al., 2001; Duffourg et al., 2016). A low-level cold pool, possibly forming under the MCS, can also lift the low-level
20   flow at its leading edge (Ducrocq et al., 2008) and/or modify the low-level circulation locally and enhance convergence areas
(Duffourg et al., 2016).

If various of these studies have also shown that a horizontal resolution of about one kilometer enables to simulate realistic
Mediterranean HPEs, as well as their associated key physical mechanisms, they have also some hard time to properly represent
the timing of triggering and organization of convection. The increase of horizontal resolution to sub-kilometric grid spacings
25   could be a way for improvement. Indeed, Verrelle et al. (2015) have shown, for an idealized convective case, that an increase of
horizontal resolution of 500 m simulates stronger updraught within convective cells associated with a larger cloudy coverage.
Hanley et al. (2015) and Fiori et al. (2017) carried out numerical simulation of HPE case study over Italy with grid spacings
ranging from 5 km to 200 m. Similarly with idealized studies, they found that smaller convective cells with a stronger intensity
are simulated with a horizontal resolution finer than 500 m. Scheffknecht et al. (2016) found that, when the horizontal grid
30   spacing is reduced to 500 m, precipitation is more widespread, maximum values are lower, and individual convective cells are
smaller. These previous studies concluded that surface precipitation amounts are enhanced and convective structures are better
represented at sub-kilometric scale.

Nevertheless, the increase in horizontal resolution may pose problems especially for the turbulence parameterization within
the so-called "grey zone" (GZ), typically in the range of horizontal resolution of about a few hundreds of kilometers and also

depending of the model's effective resolution (Wyngaard, 2004). Indeed, there are still uncertainties about how turbulence should be modeled at these resolutions. Past studies have investigated the impact of a one-dimensional (1D) versus a three-dimensional (3D) representation of the turbulence at sub-kilometric horizontal resolution. Verrelle et al. (2015) showed that a 3D turbulence leads to stronger mixing and larger cloud cover. Machado and Chaboureau (2015) carried out simulations using 1D turbulence which produced too many small cloud systems and rainy cells with a shorter lifespan. Additionally, Verrelle et al. (2017) compared kilometric deep convection simulations, up to 500m resolution, to LES and showed that subgrid turbulent kinetic energy at these resolutions was underestimated with eddy-diffusivity turbulence scheme, due to an underestimation of thermal turbulence production while resolved vertical velocities tend to be overestimated. Based on simulations carried out with 500 m grid spacings, Martinet et al. (2017) found that, for a specific case study of HyMeX SOP1 (IOP16a), not only cloud organisation but also the simulated environment and processes governing convection are strongly sensitive to the formulation of the mixing length. Indeed, when turbulent mixing is weak (i.e. weak subgrid turbulent kinetic energy), the resolved winds are increased, leading to larger low level moisture advection, higher hydrometeor contents, marked low level cold pools, and therefore more intense simulated convective systems.

This strong sensitivity obtained by Martinet et al. (2017) calls to adopt a Large Eddy Simulation (LES)-like approach, enabling a more suitable representation of turbulence within and at the edge of convective clouds and also within the atmospheric boundary layer. In a LES framework, eddies that contain most of the kinetic energy are resolved whereas smaller eddies, that carry less than 20% of the total kinetic energy, are represented by subgrid processes. Although several studies have demonstrated the need to use grid spacing of about 100 m to represent the convective flow correctly (Bryan et al., 2003; Petch, 2006; Stein et al., 2015; Zängl et al.; Dauhut et al., 2015, 2016, among others), most of these works were carried out using an idealized framework and/or using a small domain. To the author's knowledge no LES numerical simulation of a real case study of Mediterranean HPE over a large domain has already been performed. The purpose of this paper is to evaluate and analyse the impact of increasing horizontal resolution to LES in a numerical simulation of Mediterranean HPE, using a true topography in addition to truthful initial and forcing conditions. The present study goes further analysing how the physical mechanisms and convective organization are represented from sub-kilometric horizontal resolutions down to LES. For that purpose, a large domain encompassing the convective systems as well as the low level flow feeding convection over the sea is considered. The paper focuses on the same offshore convection case study described in Duffourg et al. (2016) and Martinet et al. (2017) (IOP16a), which took place on 26 October 2012 during the SOP1 of the HyMeX field programme (Ducrocq et al., 2014).

This article is organized as follows. A quick review of the case study and the involved mechanisms are provided in section 2. The numerical model and the simulation setup are presented in section 3. Both simulations with hectometric horizontal resolutions and LES, respectively, are compared in terms of rainfall field analysis and convection organization in section 4. The physical processes at cloud scale leading to very deep convection and convection organization are assessed in section 5. Finally, the study is summarized and conclusions are given in section 6, where perspectives for future work are also suggested.

2   The IOP16a case study

2.1   Meteorological conditions
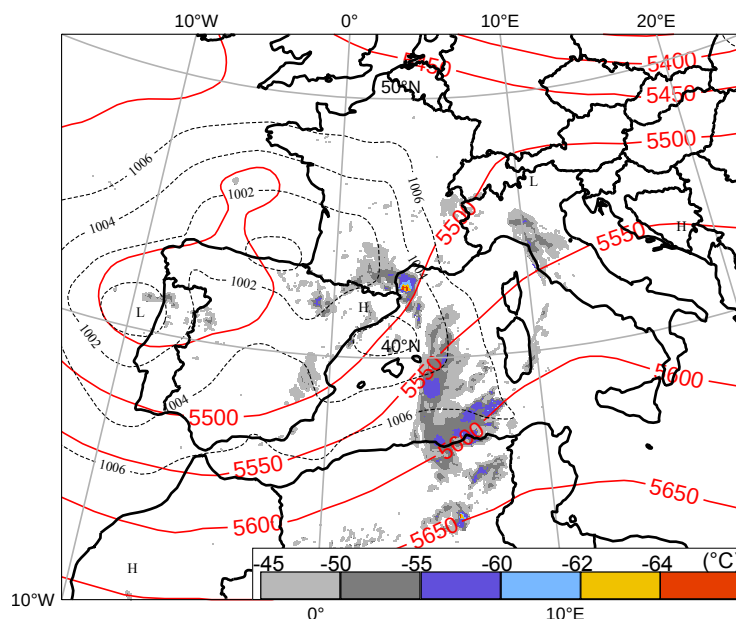
Figure 1. ARPEGE analysis for IOP16a in terms of 500 hPa geopotential height (solid line, every 50 dam) and mean sea level pressure (dashed line, hPa) and Meteosat Second Generation infrared brightness temperature (°C) (coloured areas) valid at 0600 UTC on 26 October 2012.

This section presents the HPE observed on 26 October 2012 and well documented during the HyMeX SOP1. During this event, a large part of the Northwestern Mediterranean was concerned by intense precipitation which locally led to flash flooding.

5   Figure 1 shows the synoptic scale situation, valid at 0600 UTC on 26 October 2012. The synoptic situation was characterized by a large deep upper-level low centred over Spain. A short-wave trough along with an associated potential vorticity anomaly (not shown) circulated ahead of the main system (i.e. offshore intense convective systems), passing over southeastern Spain, France and then Italy. Moreover, a large low is also anchored over Spain as seen with the mean sea level pressure (Figure 1).

At low levels, Figure 2 shows that deep convection was embedded within a very moist flow all along the system life-cycle.

10   A surface low pressure formed and strengthened downstream of the Iberian mountainous regions, between Spain and Balearic Islands. It was strongly associated with the eastward propagation of the upper level trough.

Such favourable meteorological conditions described above led to the generation of several convective systems over the Mediterranean Sea. The first convective cells appeared just East of the Spanish coast around 0600 UTC on 26 October. Convection started to organize while moving northeastwards and forming an intense south-north oriented line (marked CS1) (Figure

15   2b). It appeared that, in addition to offshore convection, the meteorological situation was also favourable to some orographic

forcing over the southern slopes of the Massif Central throughout the day on 26 October 2012. The southermost cells behind CS1 also developed and organized into a second mesoscale convective system (marked CS2), which headed eastnortheastwards towards the southeastern coastal regions of France. In the afternoon of 26 October 2012, CS2 crossed the region with surface rainfall amounts of about 150 mm in 24h causing two casualties.
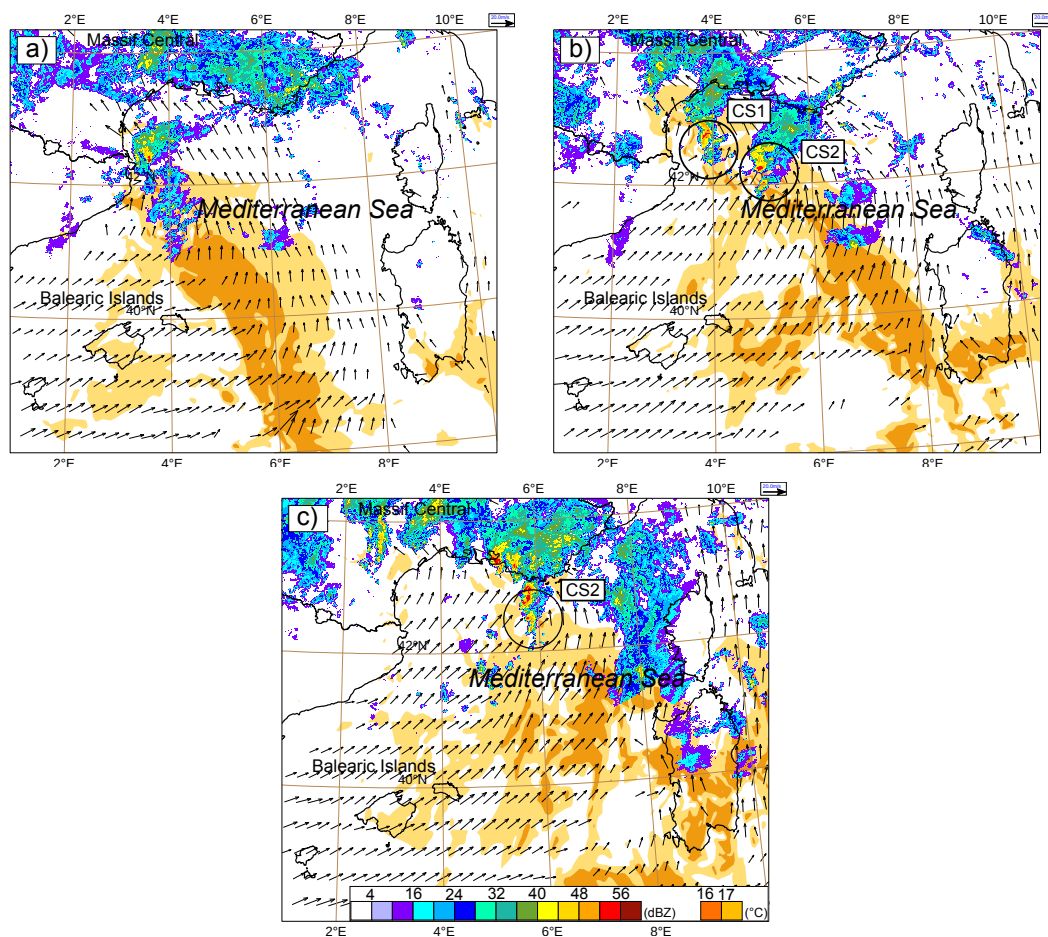
Figure 2. Observed radar reflectivity (colour scale, dBZ) superimposed to AROME analysis for IOP16a in terms of adiabatic wet-bulb potential temperature (coloured areas) and horizontal winds larger than 20 m s^{-1} (arrows) at 925 hPa valid at, **(a)** 0600 UTC, **(b)** 0900 UTC and **(c)** 1200 UTC on 26 October 2012.

2.2 Triggering mechanisms

An exhaustive evaluation of Meso-NH simulations for the convective systems involved in IOP16a can be found either in Duffourg et al. (2016) or Martinet et al. (2017) at 2.5 km and 500 m horizontal resolution, respectively.
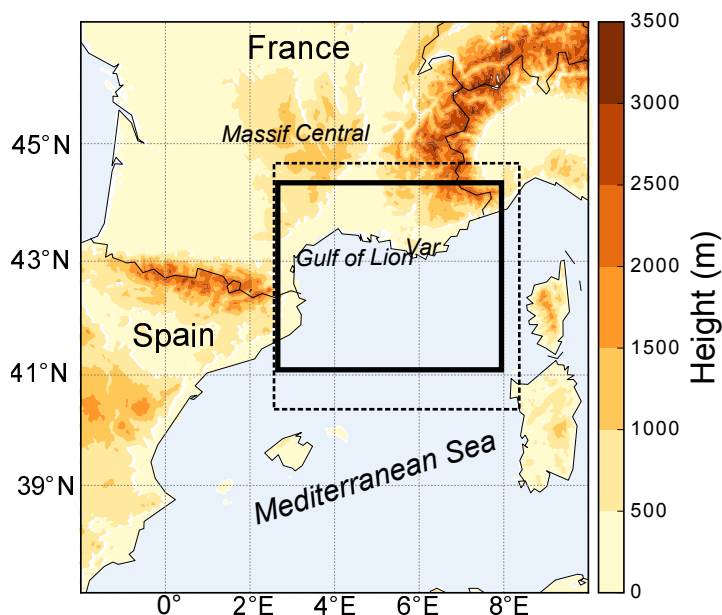
Figure 3. Computational domains used for the outer/coarser domain (900m, dashed rectangle) and for the inner/finer domain (450m or 150m, thick solid rectangle), respectively (see text for more explanation). The model orography (m) is shown in shading.

The numerous dedicated airborne and ground-based observations during the HyMeX SOP1 (suites of water vapour lidars, wind profilers, radiosoundings and boundary-layer drifting balloons, among others) over the sea and along the coast of the northwestern Mediterranean offered an unique framework for validating the convective systems simulated over the sea by kilometric scale numerical models initialized and driven by kilometric resolution analyses. Indeed, Duffourg et al. (2016)

5   showed that these convective systems during IOP16a were fed during their evolution over the sea by moist and conditionnaly unstable air masses. A southwest to southeasterly converging low level flow over the sea is the main triggering mechanism acting to continually initiate and maintain the renewal of convective cells, contributing to the back-building systems CS1 and CS2. Lifting is also partly due to evaporative low level cooling. In addition it appears that this low level cooling also controls the organization into a mesoscale convective system.

10   Martinet et al. (2017) found that the mechanisms mentionned above, as well as the dynamics of the convective systems, are sensitive to the mixing length formulation used in turbulence parameterization, at horizontal resolution of 500m. These elements motivate an increase of the horizontal resolution up to LES scale in this present study to assess how the involved physical mechanisms are represented

3 Description on the numerical experiments

3.1 The Meso-NH model

The French non-hydrostatic mesoscale numerical model Meso-NH (Lac et al., 2018) was used for the simulation of the IOP16a case study. The Gal-Chen and Somerville (1975) vertical coordinate is used with 140 vertical levels. The vertical grid is

5 streched with a spacing not varying continuously with altitude, from 10 m close to the surface to 250 m aloft. The top of the domain is at 20 km altitude, and a Rayleigh damping is progressively applied above 15 km altitude to the perturbations of the wind components and the thermodynamical variables with respect to their large-scale values, in order to prevent spurious reflections from the upper boundary.

The prognostic variables are the three Cartesian components of velocity, the dry potential temperature, the different water

10 mixing ratios and the turbulent kinetic energy. Pressure perturbations are determined by solving the elliptic equation obtained by combining air mass continuity and momentum conservation equations. The transport scheme for momentum variables is the Weighted Essentially NonOscillatory (WENO) scheme (Shu and Osher, 1988) of the 5th order combined with the fourth order Runge-Kutta time-splitting method (Lunet et al., 2017), while other 20 variables are transported with the Piecewise Parabolic Method (PPM) scheme (Colella and Woodward, 1984). A bulk one-moment mixed microphysical scheme (Caniaux et al.,

15 1994; Pinty and Jabouille, 1998) governs the equations of the six water species: water vapour, cloud water, rain water, primary ice, snow aggregates, and graupel. The turbulence parametrization is based on a 1.5-order closure (Cuxart et al., 2000) and the calculation of the turbulent flow is performed through a three dimensional (3D) scheme for horizontal resolution below kilometric grid spacings. For horizontal resolution of about a few hundred meters and coarser grids, the mixing length follows the method of Bougeault and Lacarrère (1989) whereas for LES resolution, the mixing length formulation follows the one

20 proposed by Deardorff (1972), which is directly proportional to the grid volume.

3.2 Simulation design

In this present study a LES of the IOP16a case study is carried out with the Meso-NH model. As in Duffourg et al. (2016) or Martinet et al. (2017), the initial and lateral boundary conditions of the simulations are provided by the AROME-WMED

25 analyses (Fourrié et al., 2015). Since it is not suitable to initialize and drive the LES simulation using directly the AROME-WMED analyses due to a too large horizontal resolution gap, an intermediate domain with a coarser grid is used, through the nesting technique in a two-way interactive mode (Stein et al., 2000). The coarser grid provides the lateral boundary conditions to the finer one, while the variables of the coarser grid are relaxed with a short relaxation time toward the finer grid's values in the overlapping area. Vertical grids are the same. For this present study, two nested domains in the horizontal plane with

30 horizontal grid spacings of 900 m and 150 m (hereafter **HR150**) was retained. An other control simulation (hereafter **LR450**) is carried out with horizontal grid spacings of 900 m and 450 m, respectively (Figure 3). The simulation domains cover nearly the same regions as in Martinet et al. (2017), i.e. the southeastern France and the northwestern Mediterranean, encompassing the precipitating systems and their marine low level moisture supplying flow (see Figure 3).

The simulations are initialized at 0000 UTC on 26 October 2012 and run untill 1200 UTC. At 0000 UTC and for a 3h- period only the coarser domain with a grid spacing of 900m (dashed rectangle in Figure 3) is started . The finer domains (450m or 150m) are activated at 0300 UTC and for the rest of the simulation period.

4   Overview of the numerical simulations

5   This section aims at assessing the impact of increasing horizontal resolution by comparing both simulations over the same spatial scale. For that purpose the reference LES fields are upscaled at a coarser horizontal resolution of 450 m (hereafter **LR150**). The fields are thus coarse grained by averaging the LES fields as in Verrelle et al. (2017) or Honnert et al. (2011). We focus on the life-cycle of heavy precipitation occurring over sea mainly in the morning of 26 October 2012, with a mature phase happening between 0600 UTC and 1200 UTC. It allows to better understand and model the triggering mechanisms within the

10   convective systems.

4.1   Comparaison between LR450 and LR150 simulations

4.1.1   Precipitation field analysis
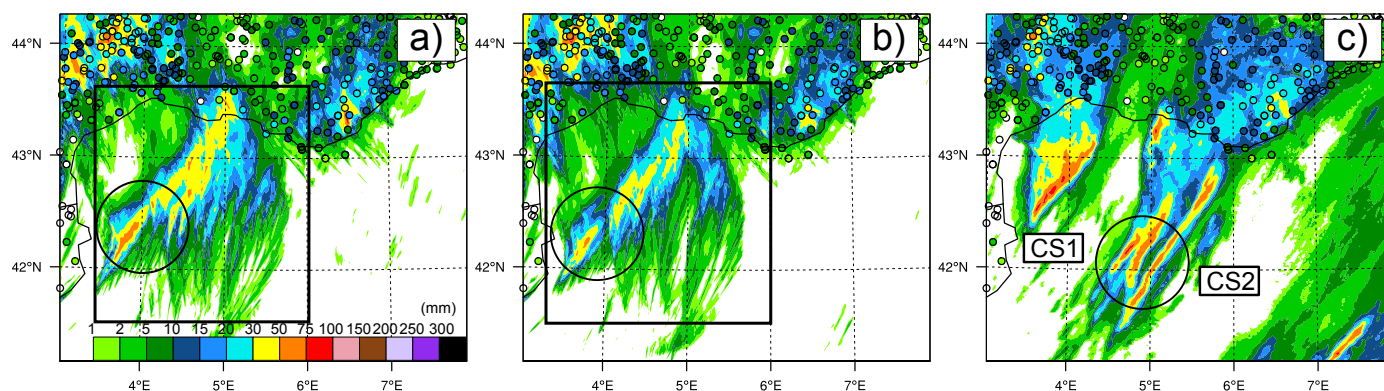
Figure 4. 6-h accumulated simulated and observed surface precipitation from, **(a)** **LR450** experiment, **(b)** **LR150** experiment, and **(c)** radar estimates, respectively between 0600 UTC and 1200 UTC on October 2012. The small circles on panels represent the raingauge observations whereas the largest ones highlight the surface precipitation associated with CS2.

Figure 4 represents the surface rainfall accumulated between 0600 UTC and 1200 UTC on 26 October 2012. Both **LR450**

15   and **LR150** fairly simulate the areas of strong precipitation over Southeastern France. The surface rainfall over land is well reproduced in terms of magnitude and location over the Var region and over the southeastern part of the Massif Central, compared to observations (Figure 4).

As for precipitation over sea, it is worth mentioning that radar quantitative precipitation estimation is impacted by large uncertainties, and in any case should be viewed cautiously. Nevertheless, two areas of strong accumulated surface rainfall are observed over sea in Figure 4c; a first one located near 4°E and a second one a few tens of kilometers southwest near 5°E. These large surface precipitation are induced by the convective systems CS1 and CS2 mentioned earlier. Although only one

5 convective system is simulated (i.e. CS2), its evolution over sea is well simulated by both **LR450** and **LR150**, except for a location too far west and stronger offshore rainfall just east of Spanish coast (see area circled in Figure 4). This precipitation pattern is explained by a former convective system triggered earlier in the simulation and not dissipating in time. But, the spatial distribution and magnitude of precipitation appear stronger for **LR450** compared to **LR150**. The results presented here for **LR450** are fairly comparable to those obtained by Martinet et al. (2017) with a 500 m horizontal resolution. Differences

10 are probably due to both different initial conditions and numerical schemes in both simulations.
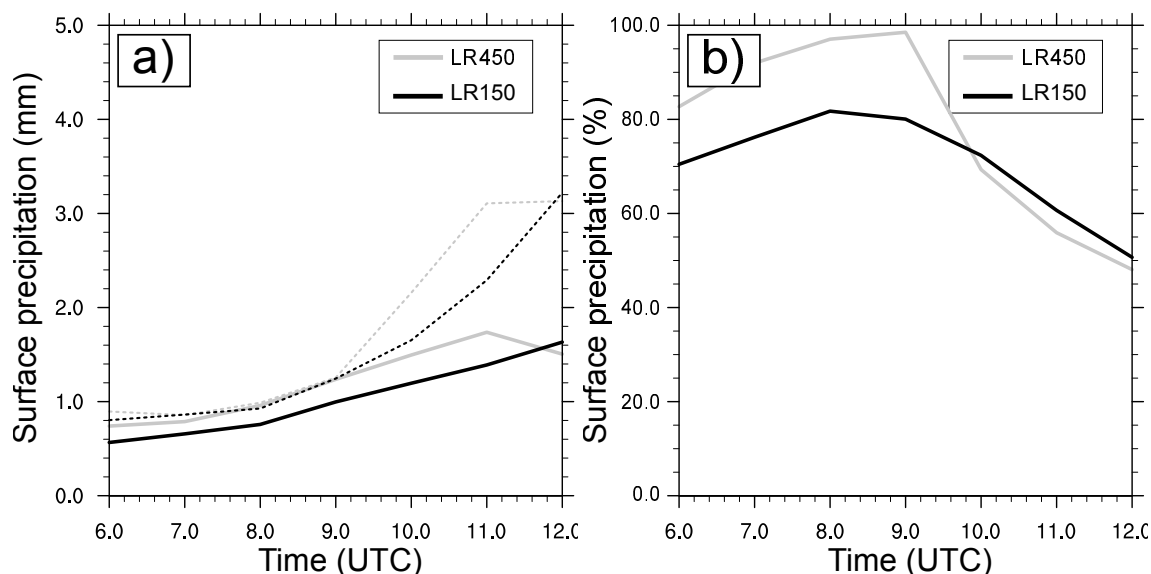
Figure 5. (a) Time series of the hourly surface precipitation (mm) for **LR450** and **LR150** experiment, averaged over the whole subdomain seen in Figure 4 (solid lines) and averaged over an area where surface precipitation exceeding 0.1 mm h^{-1} (dashed lines). **(b)** Time series of spatial coverage (%) of the hourly surface precipitation exceeding the threshold of 0.1 mm h^{-1} over the same subdomain.

In order to assess the consistency of these results along all the simulation period, time series of surface precipitation, averaged over the subdomain represented in Figure 4, are calculated. This domain enables to encompass the evolution of the convective system over sea, not considering here mainland precipitation. Figure 5 shows the surface precipitation averaged over the whole subdomain, as well as averaged over an area where surface precipitation exceeding 0.1 mm h^{-1}.

15 One can remark that the surface precipitation simulated by **LR450** is larger than **LR150** from 0600 untill near 1100 UTC on 26 October 2012 (Figure 5a). However, it must be emphasized that the largest surface rainfall in **LR450** from 0600 UTC untill 0900 UTC are mainly due to more spatially widespread precipitation, whereas between 0900 UTC and 1100 UTC stronger

rainfall rates contribute more to the largest precipitation for **LR450**. The sensitivity of these results to precipitation threshold has also been examined (not shown). Indeed, higher precipitation thresholds (> 20 mm h^{-1}) confirm that **LR450** simulates stronger rainfall over a larger spatial area after 0900 UTC.

These results with more simulated precipitation with a horizontal resolution of 450m, compared to the LES, are somewhat
5   different than those obtained by Fiori et al. (2017) or Hanley et al. (2015) for instance, who found that the largest surface rainfall amounts are simulated at the finest scale. Nevertheless around 1200 UTC, the surface rainfall simulated by **LR150** becomes larger (Figure 5a).
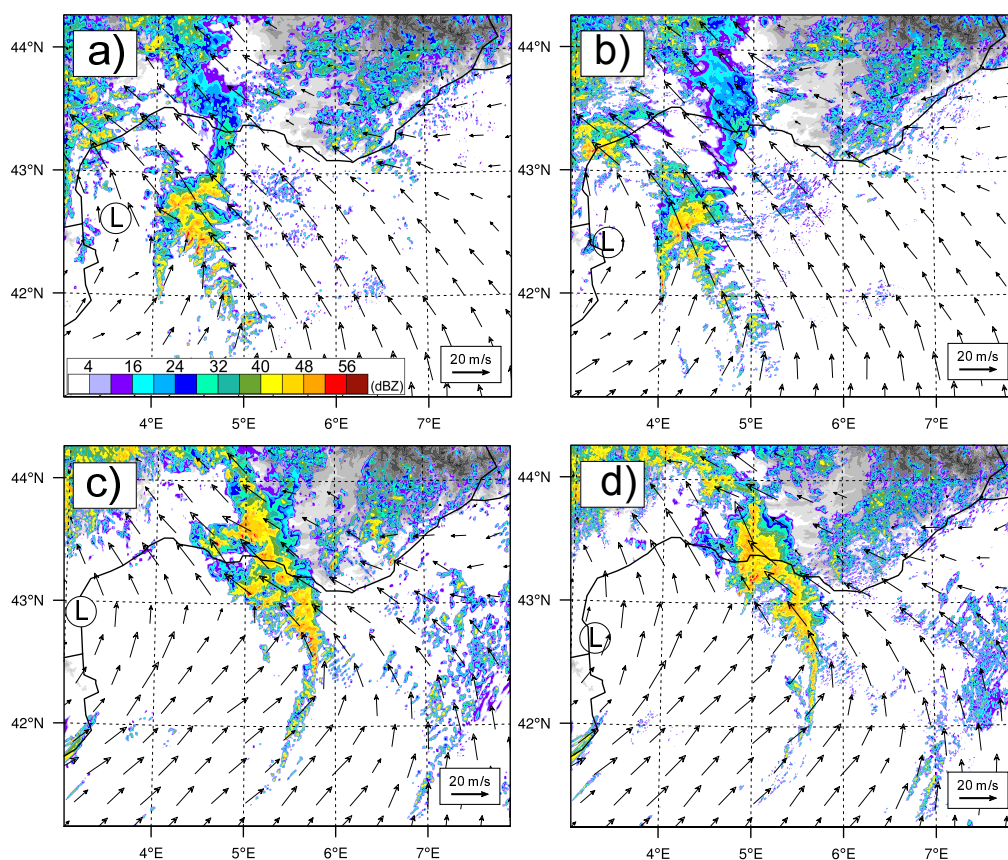
Figure 6. Simulated radar reflectivities (dBZ) at 850 hPa and horizontal winds (m s^{-1}) at 950 hPa from : **(a)** LR450 and **(b)** LR150 at 0900 UTC on 26 October 2012, respectively. Panels **(c)** and **(d)** are the same except for 1200 UTC. The symbol L marks the location of the surface low pressure system.

Both **LR450** and **LR150** are now compared by analysing the time evolution of the convection over the sea. It is worth
10   mentioning that a convective system is triggered earlier shortly after the beginning of the simulation and was maintained in the simulation for a too long time, essentially due to the lateral boundary conditions imposed by AROME-WMED analysis. This

former convective system is responsible for the large surface precipitation accumulation just east tip of Spain (Figure 4). The first convective cells of interest are actually triggered a bit late in both simulations near 0700 UCT on 26 October 2012 (not shown), leading to a different behaviour and evolution during the triggering stage compared to observations.

Figure 6 represents the simulated radar reflectivities at 0900 UTC and 1200 UTC at 850 hPa, respectively, as well as hori-

5   zontal winds at 950 hPa. As mentionned previously, the circulation, in which the convective system evolves, was characterized by strong low level convergence, controlled by a surface low pressure located between Spain and Balearic Islands. This pattern enhances locally convergence in the southwesterly to southeasterly low level flow. This surface low pressure is simulated quite similarly in both **LR450** and **LR150** (Figure 6b et d). The mature stage is characterized by continual renewal of convective cells along the low level convergence around 0900 UTC as shown in Figure 6a and b. It appears that the convective system develops

10   faster in **LR450** whith convection extending more northeastwards. As a matter of fact, when comparing both simulations at upper level, i.e. analysing the infrared brightness temperature, one can see a more spatially extended convective system with a more pronounced cloudy anvil in **LR450** (Figure 7a and b). As the surface low pressure moves east-northeastwards, the low level flow strengthens and convergence increases, organising in a very pronounced line. Near 1200 UTC on 26 October 2012, differences between both **LR450** and **LR150** become barely discernable and precipitating structures are more comparable

15   (Figure 6c and d). Both simulations show at this time a convective system tilting along a slight southwest-northeast axis that is fairly comparable with the observed radar reflectivities (Figure 2).

In summary, increase of horizontal resolution from 450 m untill 150 m for this case does not significantly improve some deficiencies of the simulation, probably more driven by initial and lateral boundary conditions. Indeed, the low level convergence is closely controlled by the surface low pressure, and both **LR450** and **LR150** handle its strengthening very similarly.

20   Moreover, only a single convective system is simulated in both **LR450** and **LR150** instead of two compared to observations, and too strong surface rainfall is simulated just east of Spanish coast. Nevertheless, significant differences appear between both simulations during the mature stage of the convective systems, especially in terms of accumulation of surface precipitation, spatial extent of the simulated systems, intensity (between 0900 UTC and 1100 UTC) and development evolution of convection over the Mediterranean Sea.

25   **4.1.2   Triggering mechanisms**

In this section, the differences highlighted in terms of simulated surface precipitation patterns, convective organization and intensity are explained by analysing the environment and the mechanisms associated with the convective systems. It has been shown in the previous section that the mature stage is simulated differently by both **LR450** and **LR150**. The system of interest is triggered around 0700 UTC just east of an other decaying one, offshore of Balearic Islands, slowly moving east-northeastwards

30   over sea. This convective system developed within a warm and moist environment and high values of conditional convective instability (not shown) along a low level convergence line, as discussed already. These triggering mechanisms are quite similar than those found by Duffourg et al. (2016) and Martinet et al. (2017) with a 2.5 km or 500 m horizontal resolution, albeit with a slight time lag.
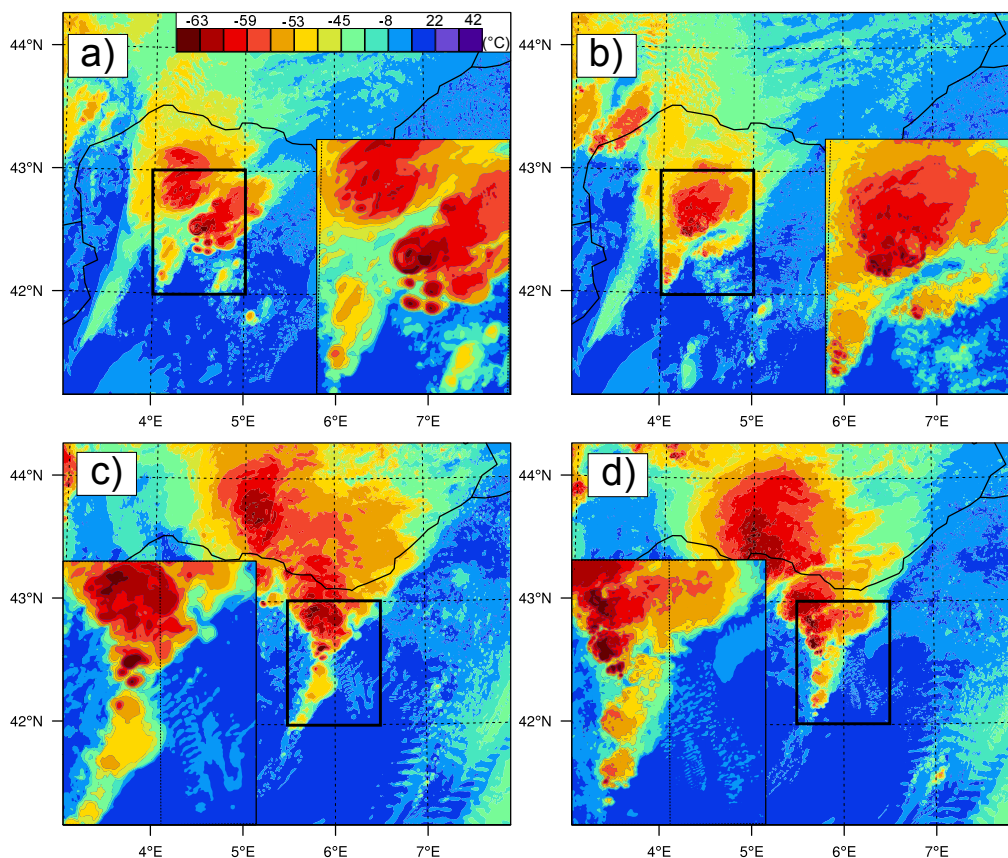
Figure 7. Same as Figure 6 except for simulated infrared brightness temperature (°C).

Thereafter and as also discussed previously, the systems simulated in both simulations adopt different behaviours during their mature stage. Figure 8 shows the low level moisture flux integrated in the first 3000 m of the troposphere, the virtual potential temperature at near 40 m AGL (third model level), as well as updraught with magnitude larger than 3 m s^{-1} at 500 m height, simulated for both **LR450** and **LR150** around the mature stage. The spatial distribution of the low level moist flux

5 is simulated differently in both simulations. Indeed around 0900 UTC, **LR150** simulates stronger values downstream of the convective system, whereas intense values of low level moisture flux are located in the vicinity of the precipitating event for **LR450**, with a maximum value reaching near 500 kg m^{-2} s^{-1} (Figure 8a and b). Near 1200 UTC on 26 October 2012, the low level moisture flux becomes stronger and more uniform for **LR150**, throughout the convective system (Figure 8d), with locally stronger fluxes than **LR450**. Strong and pronounced updraught are simulated for both simulations at the leading edge of the

10 area of low level convergence, thus evidencing the lifting of conditionally unstable air masses triggering deep convection. This area of low level convergence and high moisture flux appears slightly northeast for **LR150**.

An other mechanism responsible for lifting is also present and competes with the low level convergence. Indeed, both simulations reproduce a low level cold pool (LLCP) underneath the convective system. However, the cooling is more spatially
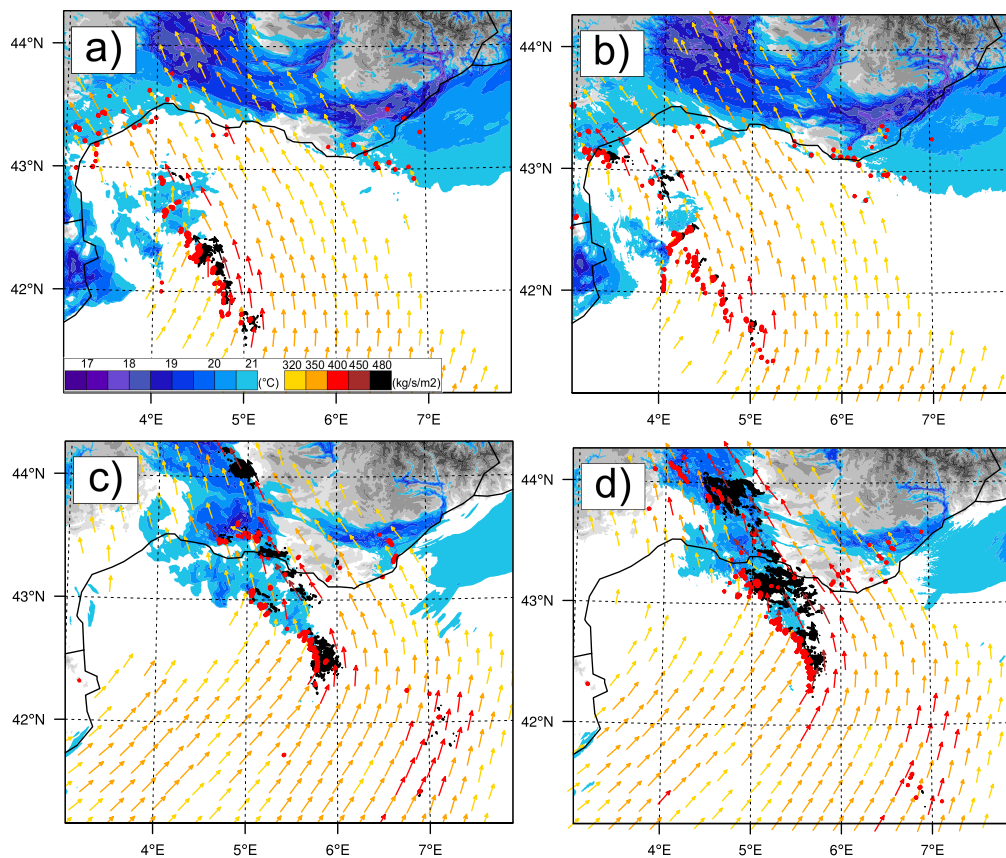
Figure 8. Same as Figure 6 except for virtual potential temperature at the third model level (near 40 m AGL) (°C, blue areas), water vapour horizontal flux integrated over the lowest 3000 m ASL (kg m^{-2} s^{-1}, arrows) and vertical velocity exceeding 3 m s^{-1} at 500 m ASL (red isolines). Black areas denote values of moisture flux exceeding 480 kg m^{-2} s^{-1}.

widespread with stronger horizontal gradients larger than 2°C for **LR450**, favouring lifting more easily. The LLCP interacts with the low level flow and also enhance locally the area of convergence, as shown in Duffourg et al. (2016) with their simulations at 2.5 km horizontal resolution. The less intense LLCP for **LR150** probably leads to a less deflected flow, stronger moisture advection and triggering of convection downstream compared to the system simulated by **LR450**.

5   In order to assess how these differences on mechanisms impact the dynamics of the simulated convective systems, Figure 9 presents time series of the mixing ratios for the precipitating hydrometeors as well as the strongest updraught, averaged over the whole subdomain shown in Figure 4. Precipitating hydrometeors (rain, graupel and snow aggregates) contents and updraught are increasing throughout the morning of 26 October 2012 untill 1200 UTC, showing a strengthening of the convective system with intense dynamics. Hydrometeors contents and vertical motions are systematically larger for **LR450**, exceeding sometimes

10   by nearly 50 % more the values for **LR150** (Figure 9b).
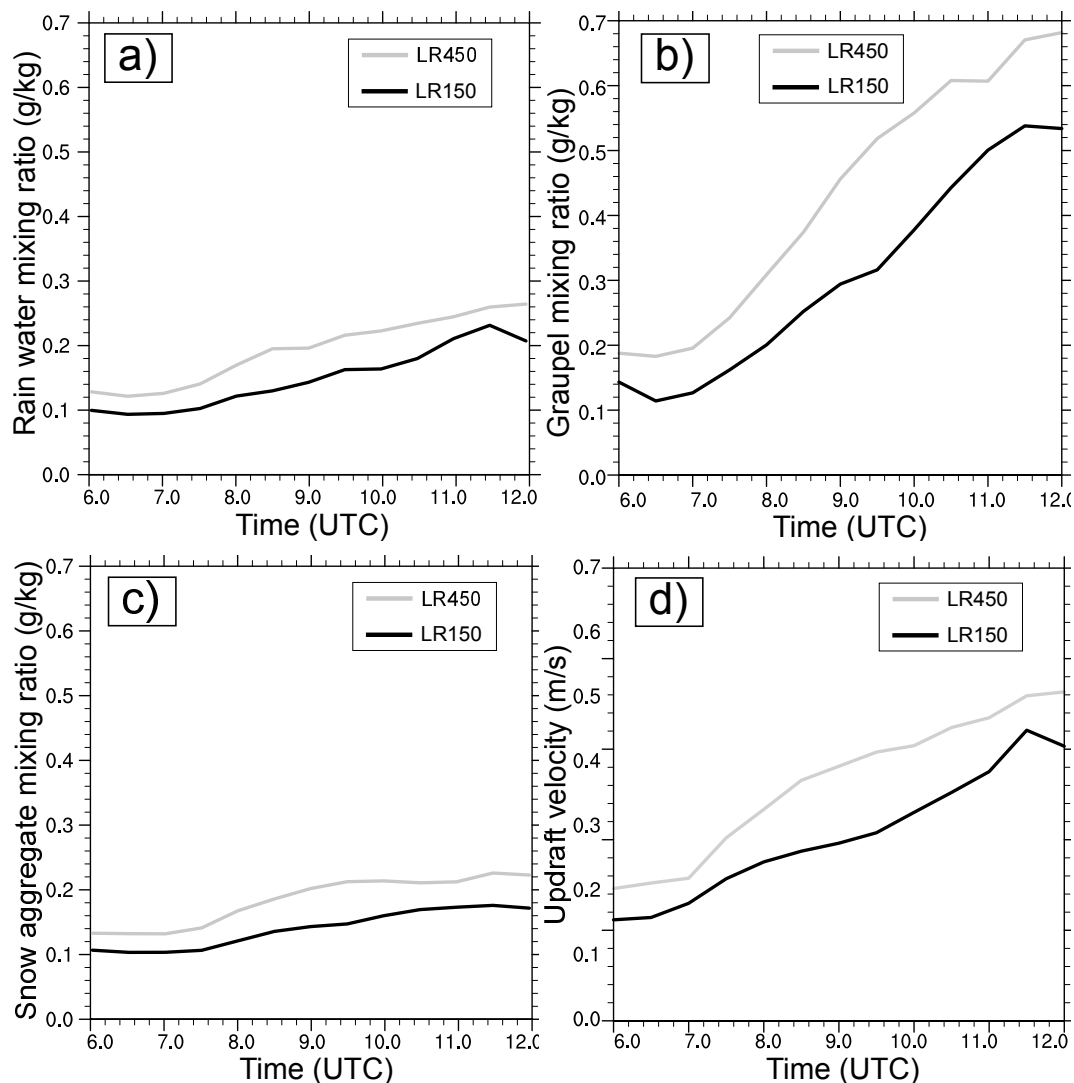
Figure 9. Time series of : **(a)** rain water mixing ratio, **(b)** graupel mixing ratio, **(c)** snow aggregate mixing ratio, and **(d)** the 90th percentile of vertical velocities, for **LR450** and **LR150** experiments respectively, averaged over the whole subdomain seen in Figure 4.

Dynamics of the convective system and the hydrometeor contents, leading to the LLCP and more surface precipitation, appear thus much larger in the simulation with a horizontal resolution of 450m compared to the LES. However, when horizontal winds and water vapour contents are examined, the low level environment for both simulations appear quite similar, even with a slightly weaker low level flow for **LR450** (not shown). Therefore, one can argue that, for this specific IOP16a case study, the

5 largest surface precipitation obtained for the simulation with a horizontal resolution of 450m could be partly explained by the

manner in which dynamics and microphysics are represented within the convective system and its interactions with the near surrounding air.

5 Very fine-scale convective organization
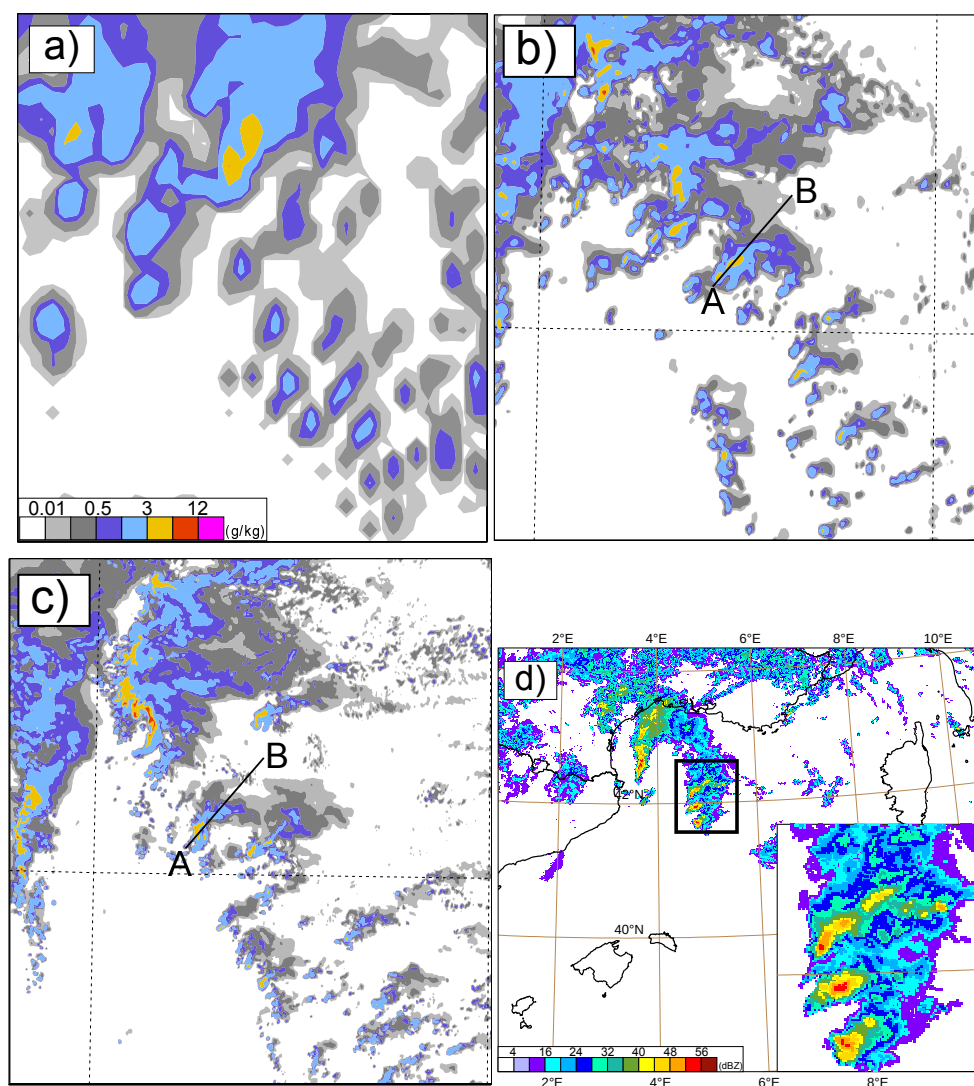
Figure 10. Zoomed view of the spatial distribution of warm microphysical species (sum of rain and cloud water mixing ratio) at 1500 m height for : **(a)** Duffourg et al. (2016)'s simulation at 2.5 km horizontal resolution, **(b) LR450**, and **(c) HR150**, respectively. Panel **(d)** shows the observed radar reflectivities at 0900 UTC on 26 October 2012.

In previous section 4, both simulations were compared by upscaling the LES at the same resolution than **LR450**. It has been shown that the increase in horizontal resolution does not modify in depth the environment of the precipitating system. The triggering mechanisms, such as the low level convergence, are not modified significantly, except for the LLCP which is strengthened by possible enhancement of rainfall evaporation under the convective system.

5   In the LES, the precipitating structures are simulated and represented at a finer scale. It offers the possibility of analysing more precisely dynamics and the convective organization down to the cell scale. Therefore, in the rest of the paper, the LES simulation will be presented at the native horizontal resolution (**HR150**). Figure 10 highlights the spatial distribution of the rain and cloud mixing ratios at 1500 m height for both **LR450** and **HR150**, which are compared to the Duffourg et al. (2016)'s simulation at 2.5 km horizontal resolution. If the kilometric simulation develops a convective structure within the low level

10   convergence, it is unable to organize small convective cells, as depicted at hectometric resolution (Figure 10a compared to Figure 10b,c). This simulated organisation with trains of very small convective cells are also depicted and confirmed thanks to radar observations (Figure 10d).

Within the southernmost part of the precipitating system, one can see intense convective cell trains, oriented southwest to northeast, triggered and organised along the low level convergence. Figure 11 shows a vertical crossection along a convective

15   cell between 0745 UTC and 0815 UTC (A-B axis in Figure 10), in both **LR450** and **HR150**, of the simulated precipitating hydrometeor contents (rain, graupel and snow aggregate contents) and the non precipitating (cloud and ice) water contents. Vertical motions (updraught and downdraught) are also represented. At the beginning of the developing stage at 0745 UTC, the non precipitating hydrometeors depict for **LR450** a rather shallow cloud with a base below 500 m ASL (Above Sea Level). There are some mixed hydrometeor contents appearing at 0800 UTC but they are limited to 5-6 km height (Figure 11c). Very

20   quickly - 15 min later - at 0815 UTC, strong upward motions are simulated within the cell, associated with large graupel contents up to 9 km height (Figure 11e). When reaching the top of troposphere, a cloudy anvil forms and fans out downstream of the upper level southwesterly flow.

However, the cloud appearance is quite different and especially more realistic for **HR150**. Indeed, the structure is still organized with pronounced hydrometeor amounts advected upwards within convective updraught but, in this case, there are stronger

25   gradients of vertical velocity located all along the edge of the convective cell, i.e. downward motions in the environment neighbouring and abuting strong updraught at the edge cloud. Moreover in **HR150**, the cloud takes a clearly discernible cumuliform appearance throughout all the period of the developing stage, that might be an indication of stronger entrainment and therefore a better representation, at this scale, of horizontal turbulent mixing between the cloud and its environment (Figure 11b,d and f). The results obtained in this present study confirm the need to use horizontal grid spacing of about a hundred of meters to re-

30   solve properly these eddies containing most of the kinetic energy and thus to better represent in particular the different stages of convection. Indeed, an assessment of the vertical structure of the southernmost convective cells along the low level convergence in **LR450** (not shown) indicates rather low and shallow cumulus clouds with only weak mixed hydrometeor contents above the freezing level. It appears thus that **LR450** triggers deep convection, in a too abruptly manner, with enhanced microphysical processes, an issue arising from a lack of entrainment and exchange between the convective plume and its environment. As a
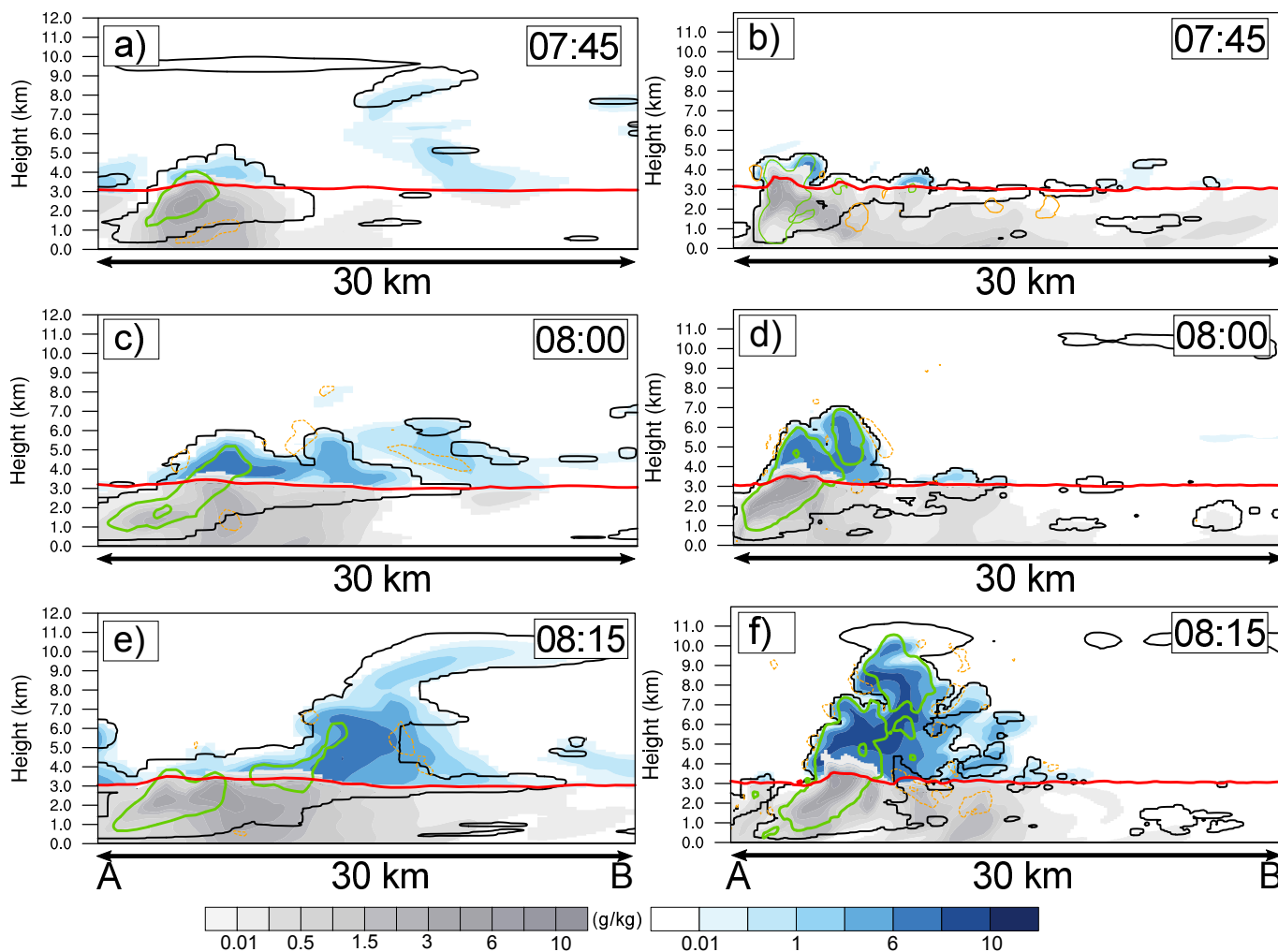
Figure 11. Vertical crossection along a convective cell for : **(a) LR450**, and **(b) HR150** at 0745, 0800 and 0815 UTC, respectively. Rain water contents (g kg^{-1}) are represented in grey, whereas mixed precipitating hydrometeor (graupel and snow aggregate) contents (g kg^{-1}) are highlighted in blue. The black solid line delineates the cloud boundaries (threshold of cloud and ice water contents > 0.001 g kg^{-1}). Updraught (green lines) and downdraught (orange dashed lines) are represented with a threshold of about 5 m s^{-1} and -2 m s^{-1}, respectively. The red solid line stands for the freezing level.

matter of fact, these results might explain why **LR450** simulates larger surface precipitation amounts between 0600 and 1100 UTC, before results of both simulations converge later.

Furthermore, the LES simulation also enables to emphasize the spatial and temporal convective organization at cell scale within the precipitating system. Figure 12 illustrates a 3D rendering of the convective cell simulated by **HR150** between 0900 UTC and 0940 UTC. One can see at 0900 UTC a well developed cumulus cloud, and forming a well simulated arcus cloud
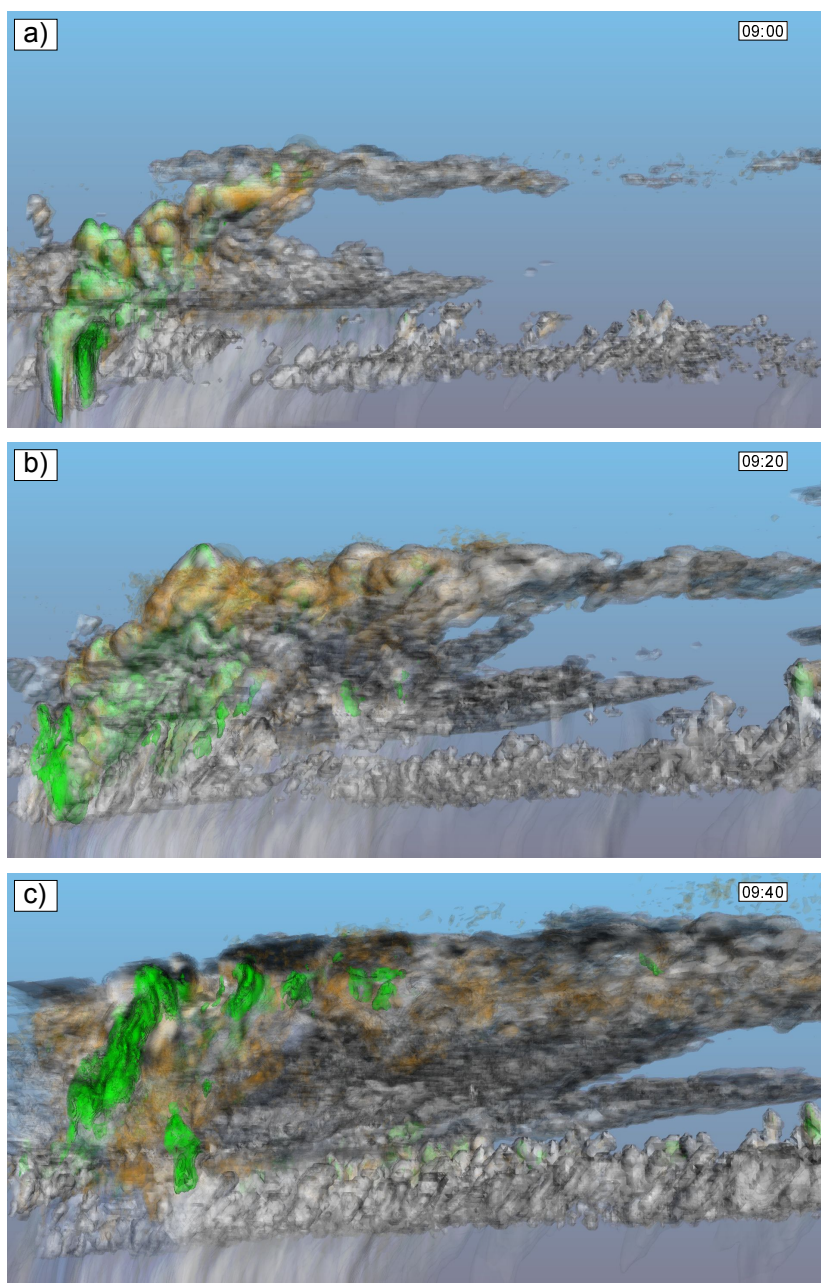
Figure 12. 3D rendering of the simulated convective cell from **HR150** between 0900 and 1000 UTC. Panels also show updraught exceeding 5 m s^{-1} (green colour) and downdraught stronger than 2 m s^{-1} (orange colour), respectively.

just front of very intense rainfall underneath the storms (Figure 12a). It is possible to track the cell across the following ten minutes. It continues to expand spatially and vertically in the following ten minutes while developing a stratiform part and
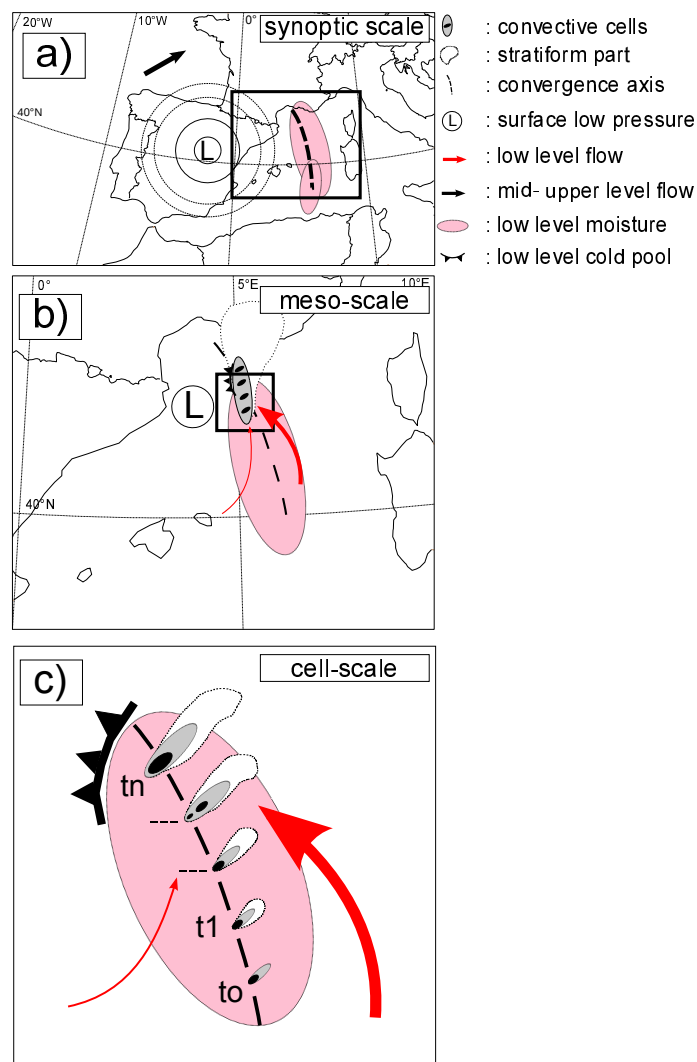
Figure 13. Schematic drawings of the precipitation structures of the convective systems and triggering ingredients observed during HyMeX IOP16a on 26 October 2012, at : **(a)** synoptic scale, **(b)** mesoscale, and **(c)** cell scale, respectively.

stronger subsidence downstream (Figure 12b). Finally around 0940 UTC, the convective cell reaches its mature stage (Figure 12c), before loosing its identity and it is no longer discernible as it merges gradually with the rest of the precipitating system (not shown) .

An animation of this 3D rendering performed with very high temporal resolution (every one minute) is very useful to better
5 understand the 3D circulation within the precipitating system. The animation is available at https://doi.org/10.6096/mistrals-hymex.1540 (Nuissier, 2019). The southwest to southeasterly low level flow initiates convective cells just at the inner edge of the resulting strong convergence that, hereafter, propagate northwards while developing in the southwesterly upper level flow.

6   Conclusions

This study examines the impact of increasing horizontal resolution to Large Eddy Simulation (LES) in a numerical simulation of a real case study of Mediterranean HPE. For that purpose and for the first time, a large domain encompassing the convective systems, as well as the low level flow feeding convection over the Mediterranean sea, is considered. The goal here was to

5   assess precisely how the physical mechanisms and convective organization are represented from sub-kilometric scale down to LES horizontal resolution. The paper focuses on an offshore convection case study, which took place on 26 October 2012 during the HyMeX SOP1. Figure 13 summarises the precipitation structures of the convective systems as well as the triggering mechanisms analysed during this HyMeX case study.

The convective systems observed during IOP16a were fed all along their evolution over sea by moist and conditionally unsta-

10   ble air masses. A southwest to southeasterly converging low level flow is the main triggering mechanism acting to continually initiate and maintain the renewal of convective cells, contributing to a back-building-shaped system (Figure 13b). The low level convergence was enhanced strongly by a surface low pressure located between Spain and Balearic Islands (Figure 13a).

First, a LES carried out at 150 m horizontal resolution is compared, at the same scale, to an other simulation performed with a 450 m grid spacing. On one hand, the increase of horizontal resolution from 450 m untill 150 m is not able to im-

15   prove significantly, for this case study, deficiencies of the simulation. Indeed, the simulated converging low level flow is quite similar in both simulations and only a single convective system is represented by both simulations instead of two compared to observations. This might be related to an issue of initial and lateral boundary conditions. There were numerous dedicated observations, in particular over Mediterranean sea, during HyMeX SOP1 that captured fairly the wind and moisture spatial and vertical features of the upstream flow heading towards the French Mediterranean coastal regions (Duffourg et al., 2016).

20   A posteriori assimilation of these field research observations could improve the quality of kilometric scale analyses arising from AROME-WMED for example. As a matter of fact, a reanalysis, including HyMeX observations, was carried out recently with AROME-WMED (Fourrié et al., 2019). New initial and lateral boundary conditions providing by this reanalysis may help improve the representation of the mesoscale flow over sea for this case study.

On the other hand, the increase of horizontal resolution modifies the representation of some of triggering and organizing

25   mechanisms controlling the precipitating system. More intense low level cold pools are simulated with a horizontal resolution of 450 m, probably related to evaporation of larger falling precipitation at least at the beginning of the simulation. However, an assessment of convective features at cell scale shows more realistic features, such as cumuliform appearance, strong horizontal gradients of vertical winds at the edge of the cloud, that might be an indication of stronger entrainment and therefore a better representation, at this scale, of exchange between the cloud and its environment. It appears therefore that deep convection could

30   be is triggered too quickly with a 450 m grid spacing, leading to enhanced microphysical processes and amplified mechanisms (stronger low level cold pools).

Obviously, the results presented here need to be confirmed by using more statistical approaches combining and mixing more convective case studies. However, this first LES of a real Mediterranean precipitating case study highlighted an organization in fast-propagating and developing cell trains within the converging low level flow (Figure 13), features that are definitively out

of range of the kilometric resolution. In a general way, the goal of ongoing and future works is to better represent in the models at hectometric scales the key processes, such as turbulence and microphysics, that are crucial to progress in heavy precipitation forecasts.

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