

Supplement of

**Timescales of Secondary Organic Aerosols to Reach Equilibrium at
Various Temperatures and Relative Humidities**

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Contents of this file

Tables S1 to S2

Figures S1 to S5

Table S1. Temperature-dependent kinetic parameters used in the simulations.

| Parameter (Unit) | Description | Equation ^a |
|--|---|--|
| ω (cm s ⁻¹) | mean thermal velocity | $\omega(T) = (8RT/(\pi M))^{1/2}$ |
| D_g (cm ² s ⁻¹) | gas-phase diffusion coefficient | $D_g(T, P) = (T/T_{\text{standard}})^{1.75} (P_{\text{standard}}/P) D_g(T_{\text{standard}}, P_{\text{standard}})^b$ |
| D_b (cm ² s ⁻¹) | bulk diffusion coefficient | $D_b(T, RH) = kT/(6\pi a\eta(T, RH))$ |
| k_a (cm s ⁻¹) | first-order adsorption rate coefficient | $k_a(T) = \alpha_s \omega(T)/4$ |
| k_d (s ⁻¹) | first-order desorption rate coefficient | $k_d(T) = Ae^{-(E_{des}/(RT))}$ |
| $k_{ss,s}$ (cm s ⁻¹) | first-order rate coefficient for quasi-static-to-sorption layer transport | $k_{ss,s}(T, RH) = 2D_b(T, RH) / (\delta_{ss} + \delta_z)$ |
| $k_{s,ss}$ (s ⁻¹) | first-order rate coefficient for sorption-to-quasi-static surface transport | $k_{s,ss}(T, RH) = k_{ss,s}(T, RH)k_d(T)[Z]_{ss,eq} / (k_a(T)[Z]_{g,eq})$ |
| $k_{b1,ss}$ (cm s ⁻¹) | rate coefficient of bulk layer 1-to-quasi-static surface transport | $k_{b1,ss}(T, RH) = 2D_b(T, RH) / (\delta_{ss} + \delta(1))$ |
| $k_{ss,b1}$ (cm s ⁻¹) | rate coefficient of surface-to-bulk layer 1 transport | $k_{ss,b1}(T, RH) = k_{b1,ss}(T, RH)$ |
| $k_{b,b}$ (cm s ⁻¹) | rate coefficient of transport between bulk layers | $k_{b,b}(T, RH) = 2D_b(T, RH) / (\delta(k) + \delta(k + 1))$ |
| τ_d (s) | desorption lifetime | $\tau_d = k_d^{-1}$ |

^a Description and the values of the symbols shown in the equations are summarized in Table S2.

^b $D_g(T_{\text{standard}}, P_{\text{standard}})$ is calculated by the EPA on-line tools:

(<https://www3.epa.gov/ceampubl/learn2model/part-two/onsite/estdiffusion-ext.html>).

Table S2. Description and the values of the symbols in the equations of Table S1.

| Variable (Unit) | Description | Value |
|--|---|------------------------|
| R (J K ⁻¹ mol ⁻¹) | gas constant | 8.314 |
| T (K) | temperature | varied from 220 to 310 |
| RH (%) | relative humidity | varied from 0 to 100 |
| M (g mol ⁻¹) | molar mass of compound Z | 200 |
| T_0 (K) | room temperature | 298 |
| ρ (g cm ⁻³) | density of organic particles | 1.4 |
| T_{standard} (K) | sea level standard temperature | 288.15 |
| P_{standard} (Pa) | sea level standard atmospheric pressure | 101325 |
| K (J K ⁻¹) | Boltzmann constant | 1.38×10^{-23} |
| a (cm) | effective molecular radius | 10^{-8} |
| δ_z (cm) | effective molecular diameter | 2×10^{-8} |
| $\alpha_{s,0}$ | surface accommodation coefficient on free-substrate | 1 |
| A (s ⁻¹) | pre-exponential factor | 10^{12} |
| E_{des} (kJ mol ⁻¹) | desorption energy | 40 |
| $[Z]_{\text{g,eq}}$ (cm ⁻³) | equilibrium (saturation) number concentrations of Z in the gas phase | variable |
| $[Z]_{\text{ss,eq}}$ (cm ⁻²) | equilibrium (saturation) number concentrations of Z in the quasi-static surface layer | variable |
| δ_{ss} (cm) | thickness of the quasi-static surface layer | variable |
| $\delta(k)$ (cm) | thickness of the bulk layer k | variable |

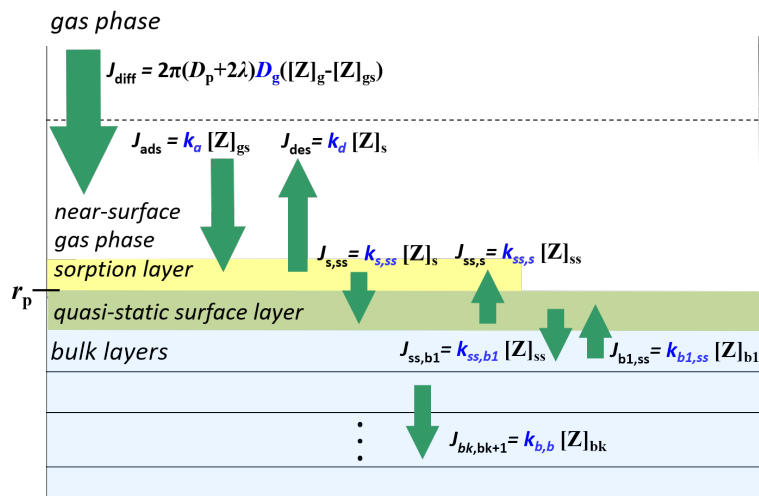


Figure S1. Temperature-dependent kinetic processes simulated in the KM-GAP model. Parameters in blue are treated as a function of temperature (Table S1). $[Z]$ are concentrations of species Z in the gas (g) and near-surface gas phases (gs), at the sorption layer (s) and in the surface (ss) and in the bulk (b) layers. J are the transport fluxes between each layer, including the gas-phase diffusion flux (J_{diff}), the adsorption (J_{ads}) and desorption (J_{des}) fluxes, surface–bulk exchange fluxes ($J_{s,ss}$, $J_{ss,s}$, $J_{ss,b1}$, $J_{b1,ss}$), and bulk diffusion fluxes ($J_{b,b}$).

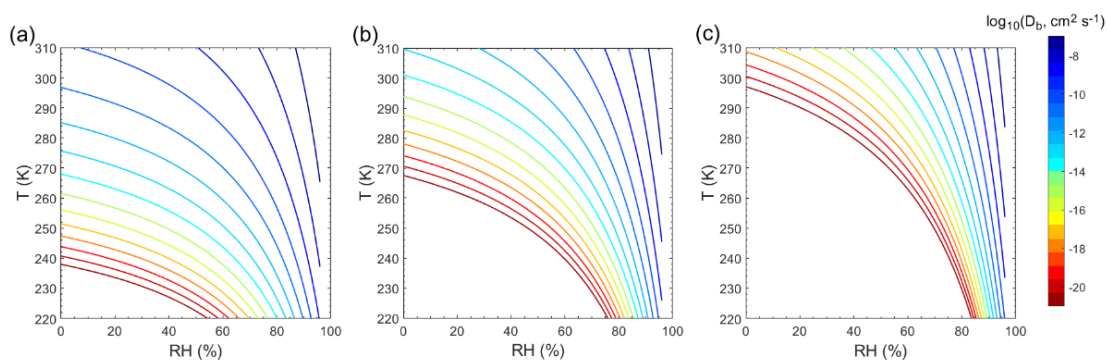


Figure S2. Bulk diffusion coefficient (D_b) in pre-existing particles as a function of temperature and relative humidity. The glass transition temperatures under dry conditions ($T_{g,\text{org}}$) are set to be (a) 240 K, (b) 270 K and (c) 300 K, respectively.

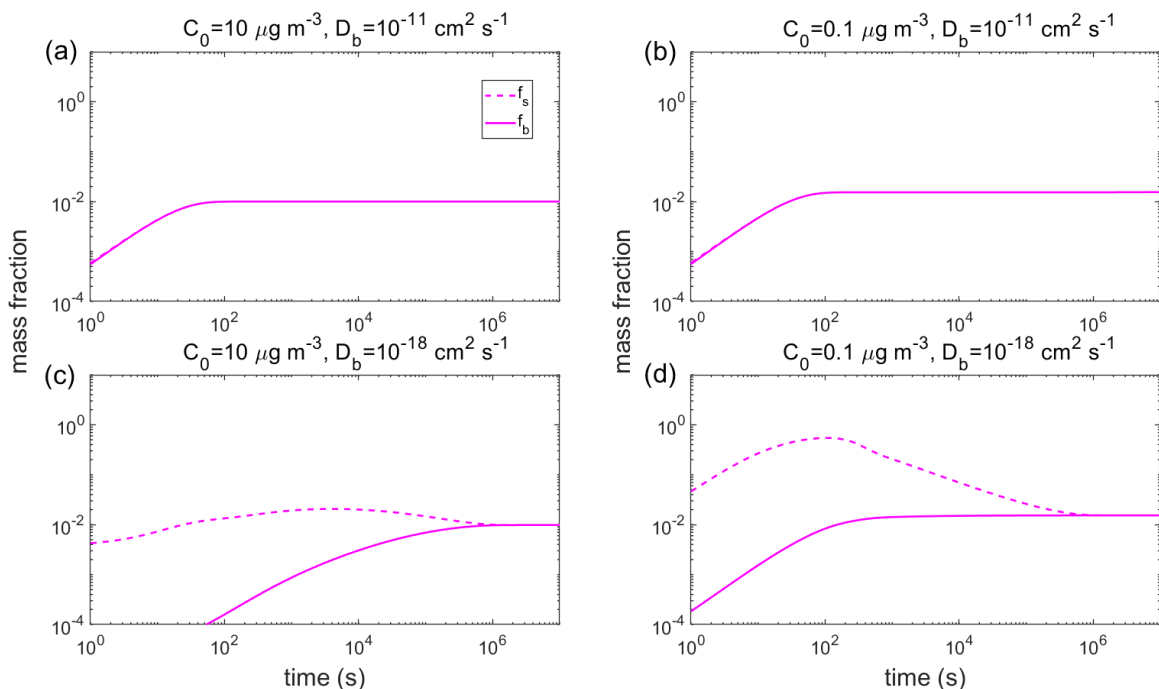


Figure S3. Temporal evolution of the mass fraction of Z in the near-surface bulk (f_s), and the average fraction of Z in the entire bulk (f_b). RH = 60% and T is (a, b) 298 K and (c, d) 250 K. The C_0 of Z is (a, c) $10 \mu\text{g m}^{-3}$ and (b, d) $0.1 \mu\text{g m}^{-3}$. The glass transition temperature of pre-existing particles under dry conditions ($T_{g,\text{org}}$) is set to be 270 K, which leads to D_b of (a, b) $10^{-11} \text{cm}^2 \text{s}^{-1}$ and (c, d) $10^{-18} \text{cm}^2 \text{s}^{-1}$. The initial mass concentration of pre-existing particles is assumed to be $20 \mu\text{g m}^{-3}$ with the number concentrations of $3 \times 10^4 \text{cm}^{-3}$ and the initial particle diameter of 100 nm.

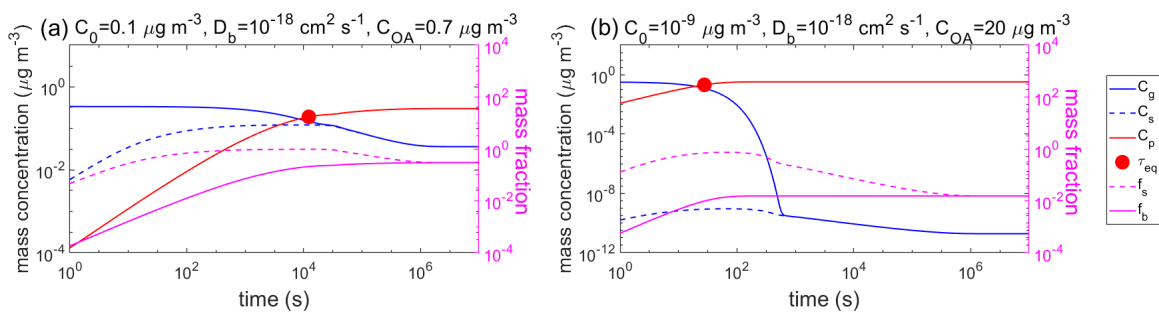


Figure S4. Temporal evolution of mass concentrations of the condensing compound Z in the gas phase (C_g), just above the particle surface (C_s), and in the particle phase (C_p). The mass fraction of Z in the near-surface bulk (f_s), and the average fraction of Z in the entire particle bulk (f_b) are also shown. D_b is $10^{-18} \text{cm}^2 \text{s}^{-1}$. The C_0 of Z is (a) $0.1 \mu\text{g m}^{-3}$ and (b) $10^{-9} \mu\text{g m}^{-3}$. The initial mass concentration of pre-existing particles is set to be (a) $0.7 \mu\text{g m}^{-3}$ and (b) $20 \mu\text{g m}^{-3}$. τ_{eq} is marked with the red circle. τ_{eq} (~ 28 s) in (b) is consistent with the inverse of the condensation sink (29 s).

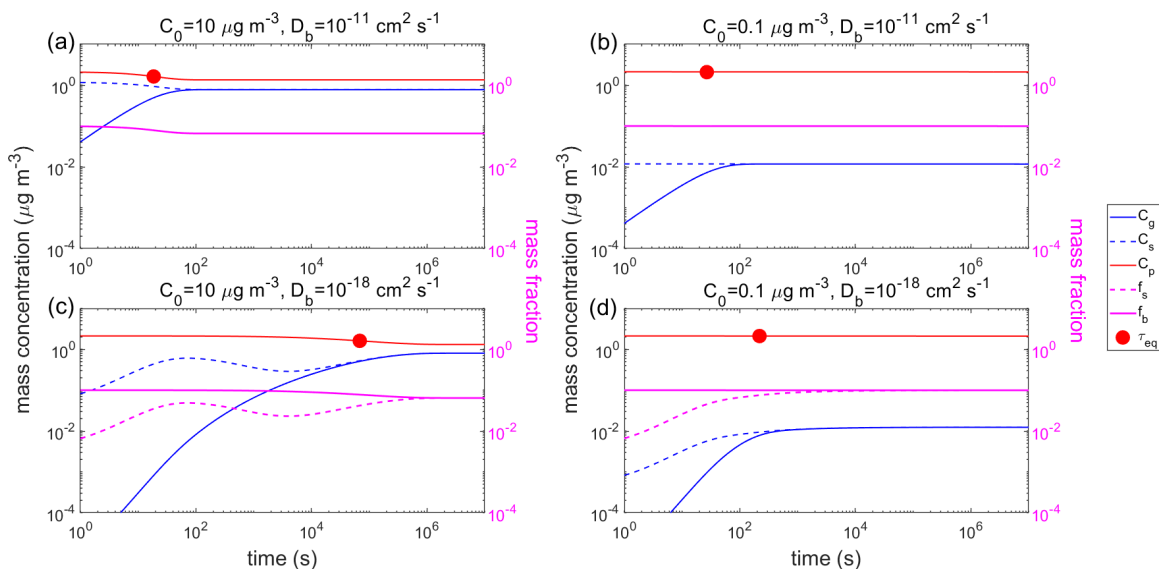


Figure S5. Temporal evolution of mass concentrations of the condensing compound Z in the gas phase (C_g), just above particle surface (C_s), in the particle phase (C_p), the mass fraction of Z in the near-surface bulk (f_s), and the average fraction of Z in the entire particle bulk (f_b). τ_{eq} are marked with red circles. RH = 60% and T is (a–b) 298 K and (c–d) 250 K. The C_0 of the condensing compound is (a, c) $10 \mu\text{g m}^{-3}$ and (b, d) $0.1 \mu\text{g m}^{-3}$. The glass transition temperature of pre-existing particles under dry conditions ($T_{g,org}$) is set to be 270 K, which leads to D_b of (a, b) $10^{-11} \text{ cm}^2 \text{ s}^{-1}$ and (c, d) $10^{-18} \text{ cm}^2 \text{ s}^{-1}$. The initial mass concentration of pre-existing non-volatile particles (C_{OA}) is assumed to be $20 \mu\text{g m}^{-3}$ with the number concentrations of $3 \times 10^4 \text{ cm}^{-3}$ and the initial particle diameter of 100 nm.