



Simulating age of air and distribution of SF₆ in the stratosphere with SILAM model

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Abstract. The paper presents a comparative study of age of air (AoA) derived with several approaches: a widely used passive tracer accumulation method, the SF₆ accumulation, and a direct calculation of an “ideal age” tracer. The simulations have been performed with the Eulerian chemistry transport model SILAM driven with the ERA-Interim reanalysis for 1980-2018.

The Eulerian environment allowed for simultaneous application of several approaches within the same simulation, and interpretation of the obtained differences. A series of sensitivity simulations revealed the role of the vertical profile of turbulent diffusion in the stratosphere, destruction of SF₆ in the mesosphere, as well as the effect of gravitational separation of gases with strongly different molar masses.

The simulations reproduced well the main features of the SF₆ distribution in the atmosphere retrieved from the MIPAS satellite instrument. It was shown that the apparent very old air in the upper stratosphere derived from the SF₆ profile observations is a result of destruction and gravitational separation of this gas in the upper stratosphere and mesosphere. The effect of these processes add over 4 years to the actual AoA, which, according to our calculations, does not exceed 6-6.5 years.

The destruction of SF₆ and varying rate of emission make it unsuitable to reliably derive AoA or its trends. However, observations of SF₆ provide a very useful means for validation of stratospheric circulation in a model with properly implemented SF₆ loss.

15 1 Introduction

AoA is defined as the time spent by an air parcel in the stratosphere since its entry across the tropopause (Li and Waugh, 1999; Waugh, 2002). The distribution of the age of air (AoA) is controlled by the global atmospheric circulations, first of all, the Brewer-Dobson and the polar circulation. In particular, the temporal variation of AoA has been used as an indicator of long-term changes in the stratospheric circulation (Engel et al., 2009; Waugh, 2009). AoA has been extensively used to evaluate and compare general circulation and chemical transport models in the stratosphere (Waugh, 2002; Engel et al., 2009).

Simulations of the AoA according to the definition above have been performed with Lagrangian transport models (Eluszkiewicz et al., 2000; Waugh, 2002; Diallo et al., 2012). The trajectories are initiated with positions distributed in the stratosphere and integrated backwards until they cross the tropopause. The time elapsed since the initialization is attributed as age of air at the



point of initialization. Moreover, the distribution of the ages of particles originating from some location can be used to get the
25 age spectrum there.

The Eulerian simulations of AoA can be formulated in several different ways. The approaches with an accumulating tracer, mimicking the above-mentioned observational method were used in a comprehensive study by Krol et al. (2018) and several studies before (e.g. Eluszkiewicz et al., 2000; Monge-Sanz et al., 2012). Besides that, a special tracer that presents an analogy of Lagrangian clock has been used. The tracer appears in literature under names “clock-type tracer” (Monge-Sanz et al., 2012)
30 or “ideal age” (Waugh, 2002). The ideal age has constant rate of increasing of mixing ratio everywhere, except for the surface where it is continuously forced to zero. Similar tracers have been long used to simulate age of oceanic water (e.g. England, 1995; Thiele and Sarmiento, 1990).

Direct observations of the age of air, as it is defined above, are not possible, therefore AoA is usually derived from observed mixing ratios of various tracers. The tracers belong to one of two types: various tracers with known tropospheric mixing ratios
35 and lifetimes (Bhandari et al., 1966; Koch and Rind, 1998; Jacob et al., 1997; Patra et al., 2011), and long-living tracers with known trends in tropospheric mixing ratios. The studies published to-date used carbon dioxide CO₂ (Remsberg, 2015), nitrous oxide N₂O (Boering et al., 1996; Andrews et al., 2001), sulphur hexafluoride SF₆ (Waugh (2009); Stiller et al. (2012), methane CH₄ (Remsberg, 2015), and various fluorocarbons (Leedham Elvidge et al., 2018).

For accumulating tracers a mean AoA at some point in the stratosphere is calculated as a lag between the times when a
40 certain mixing ratio is observed near the surface and at that point. The lag time is equivalent to the mean AoA defined above only in the case of a strictly linear growth and uniform distribution of the tracer in the troposphere (Hall and Plumb, 1994).

In reality, there is no tracer whose mixing ratio in the troposphere grows strictly linearly. The violation of assumption of the linear growth leads to biases in the resulting AoA distribution and its trends. It has been pointed out that increasing growth rates of CO₂ and SF₆ lead to low-bias of AoA and its trends, and make these tracers ambiguous proxies for AoA (Garcia et al.,
45 2011). Various corrections have been applied in several studies (Hall and Plumb, 1994; Waugh, 2002; Engel et al., 2009; Stiller et al., 2012; Leedham Elvidge et al., 2018) to deduce the “true” AoA from observations of tracers with increasing growth rates. The effect of the correction method on AoA estimates has not been investigated and must be considered as source of uncertainty in resulting estimates (Garcia et al., 2011). Garcia et al. (2011) further conclude that accounting for the biases in trend estimates due to varying growth rates would likely require uniform and continuous knowledge of the evolution of trace
50 species, which is not available from any existing observational dataset. Recently Leedham Elvidge et al. (2018) have shown a minor sensitivity of AoA to the choice of particular correction method, however without detailed analysis of assumptions behind these methods.

Another major source of uncertainty in observational AoA is violation of conservation of a tracer due to sources and sinks, such as oxidation of carbon monoxide and methane for CO₂, or mesospheric destruction for SF₆. The mesospheric sink of SF₆
55 leads to an “over-aging”, especially pronounced in the area of polar vortices. The magnitude of the over-aging was estimated as 2 or more years (Waugh (2002)).

The simulations of SF₆ and AoA in the atmosphere with WACCM model (Kovács et al., 2017) have reproduced the effect of over-aging, but of much smaller magnitude than if inferred from SF₆ retrievals from the limb-viewing **MIPAS** instrument



operated on-board of the Envisat satellite in 2002-2012 (Stiller et al., 2012), and *in-situ* observations from the ER-2 aircraft
60 (Hall et al., 1999). Kovács et al. (2017) offered two possible scenarios for the discrepancy: either SF₆ loss is still underestimated
in WACCM, or MIPAS SF₆ is low biased above ~ 20km. Neither of the scenarios have been analysed in depth so far, which
leaves the status of MIPAS, the richest to date observational dataset for the stratospheric SF₆, unclear.

The aim of the present study is to provide consistent simulations simultaneously reproducing the spatio-temporal distribution
of AoA and the SF₆ mixing ratio in the stratosphere during last 39 years.

65 With these simulations we

- compare different methods of estimating the AoA and quantify inconsistencies in AoA and its trends arising from
violations of the underlying assumptions behind each method
- analyze the causes of the discrepancies in the upper stratosphere between different methods of deriving the AoA
- provide a solid basis for further studies of stratospheric circulation with observations of various trace gases and for
70 studies of climate effects of SF₆

The paper is organized as follows. Sec. 2 gives an overview of the modelling tools, and the modelling and observational
data used for the study. Sec. 3 describes the developments made for Silam in order to perform the simulations: vertical eddy
diffusivity parametrisation in stratosphere and lower mesosphere, and SF₆ destruction parametrization, as well as the mod-
elling setup. The sensitivity tests and evaluation of the simulations against MIPAS satellite retrievals, and stratospheric-balloon
75 measurements of SF₆ mixing ratios are given in Sec. 4. Sensitivity of AoA and its trends to the choice of the simulation setup
and AoA proxy is studied in Sec. 5. The findings of the whole study are summarised in Sec. 6.

2 Methods and input data

2.1 SILAM model

SILAM (System for Integrated modeLling of Atmospheric coMposition) is an off-line chemical-transport model. SILAM
80 features a mass-conservative and positive-definite advection scheme that makes the model suitable for long-term runs (Sofiev
et al., 2015). The model can be run at a range of resolutions starting from a kilometer scale in limited-area or in global mode.
The vertical structure of modelling domain consist of stacked layers starting from the surface. The layers can be defined either
in z- or hybrid sigma-pressure coordinates. The model can be driven with a variety of NWP- (numerical weather prediction) or
climate models.

85 In order to accurately model the AoA and needed tracers, the vertical diffusion part of the transport scheme of SILAM has
been refined to account for gravitational separation. In addition, several tracers with specific transformation procedures have
been implemented into the model. The specific setup used for the present study is described in Sec. 3.5



2.2 ECMWF ERA-interim reanalysis

The ERA-Interim reanalysis from the European Centre for Medium-range Weather Forecasts (ECMWF) had been used as a meteorological driver for our simulations. The data set has T255 spectral resolution and covers the whole atmosphere with 60 hybrid sigma-pressure levels (Dee et al., 2011), having the uppermost layer from 20 to 0 Pa with nominal pressure of 10 Pa. The reanalysis uses a 12-h data assimilation cycle, and the forecasts are stored with a 3-hour time step. We used the fields retrieved from the ECMWF's MARS archive on a lat-lon grid 500x250 points with step of 0.72 degrees. The four forecast times (+3h, +6h, +9 h and +12h) were used from every assimilation cycle to obtain a continuous dataset with 3-hour time step. To drive the dispersion model, the data for 1980-2015 were used.

The ERA-interim reanalysis has been used earlier for Lagrangian simulations of AoA (Diallo et al., 2012) and found to provide ages that agree with those inferred from in-situ observations in the lower stratosphere.

2.3 MIPAS observations of SF₆

To evaluate the results of SF₆ modelling we used the data from the MIPAS instrument operated on-board of Envisat satellite in 2002-2012. MIPAS was a limb-sounding Fourier transform spectrometer with a high spectral resolution measuring in the infrared. Due to its limb geometry, a good vertical resolution of the derived trace gas profiles and a high sensitivity to low-abundant species around the tangent point has been achieved. Along the orbit path, MIPAS measured a profile of atmospheric radiances about every 400 km with an altitude coverage, in its nominal mode, of about 6 – 70 km altitude. The vertical sampling was 1.5 km in the lower part of the stratosphere (up to 32 km) and 3 km above, with a vertical field of view covering 3 km at the tangent point. Over a day, about 1300 profiles along 14.4 orbits were measured, covering all latitudes up to the poles at sunlit and dark conditions. The vertical distributions of trace gases were derived from the radiance profiles by an inversion procedure, fitting simulated spectra to the measured ones while varying the atmospheric state parameters.

The retrieval of SF₆ is based on the spectral signature of this species in the vicinity of 10.55 μm wavelength and is in principle described in Stiller et al. (2008, 2012); Haenel et al. (2015). In this study here, we use an updated version of SF₆ data (compared to the one described in Haenel et al. (2015)) called V5H/R_SF6_21/224/225; the absorption cross-section data on SF₆ and a new CFC-11 band in the vicinity of the SF₆ signature provided by J. Harrison (pers. communication) has been used instead of the older cross section data by Varanasi et al. (1994). The updated version provides considerably higher SF₆ mixing ratios in the upper part of the stratosphere (above 30 km) than the versions before and is closer to independent reference data.

The retrieved profiles are sampled on an altitude grid spaced at 1 km, where as the actual resolution of the profiles is between 4 and 10 km for altitudes below 30 km. The retrievals are supplemented with averaging kernels and error covariance matrices describing uncertainties due to measurement noise, which is normally in the order of 10% of the retrieved value, and the correlations among the retrieved quantities. The error is uncorrelated between profiles, so, averaging makes it negligible in monthly zonal means.

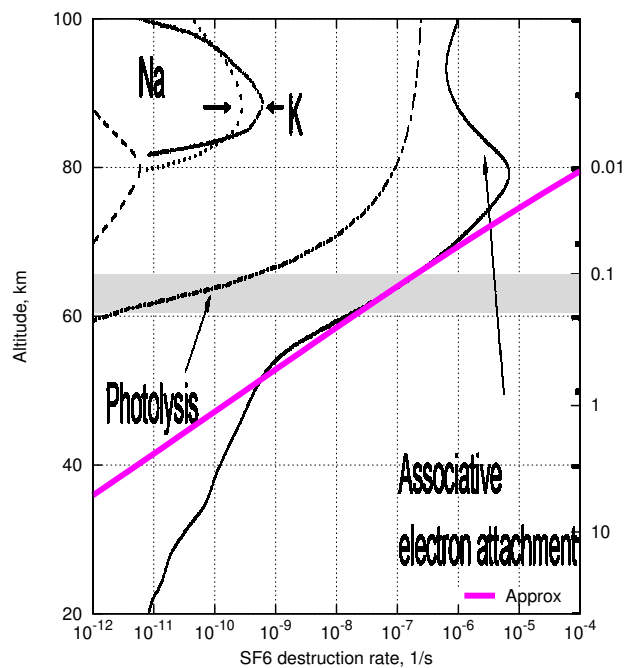


Figure 1. The vertical profiles of SF₆ destruction rate (after Totterdill et al., 2015) and its approximation in range of 55–75 km, given by Eq. (1).

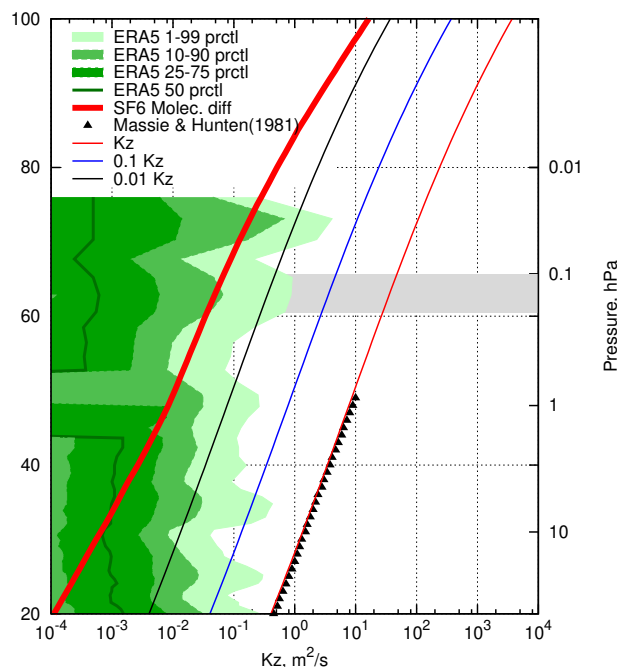


Figure 2. Vertical profiles of diffusion coefficients.

3 Silam developments

120 In this section we introduce a set of parametrizations implemented in Silam for this study.

3.1 SF₆ destruction

The destruction of atmospheric SF₆ occurs at altitudes over 60 km (Totterdill et al., 2015) that fall within the topmost layer of the ERA-Interim. The exchange processes in the upper stratosphere and lower mesosphere have to be adequately parameterized together with the destruction process.

125 Estimates of AoA from the SF₆ tracer rely on the assumption of it being a passive tracer. SF₆ is indeed essentially stable up to about 50 km altitudes. In the height range up to 100 km, the most pronounced destruction mechanism is associative electron attachment (Totterdill et al., 2015). The highest destruction rate of 10⁻⁵ s⁻¹ occurs at the altitude of 80 km (Fig. 1). An important feature of this profile is that the destruction rate becomes significant above the top of our modelling domain (10 Pa, 65 km). The ERA-Interim meteorological fields have the uppermost level at 10 Pa and do not resolve a vertical structure of
 130 the atmosphere above that level. In order to assess the loss of SF₆ due to destruction we have to parameterise the combined



effect of diffusion of SF₆ to the upper layers and its destruction there. Then the steady-state fluxes can be applied as the upper boundary condition to our simulations.

As an approximation to the vertical profile of the destruction rate in an altitude range of 50–80 km we have fitted a corresponding part of the curve in Fig. 9a of Totterdill et al. (2015) with a power function of pressure (magenta line in Fig. 1):

135

$$\frac{1}{\tau} = 3 \cdot 10^{-8} s^{-1} \left(\frac{20 \text{ Pa}}{p} \right)^3, \quad (1)$$

where τ is the lifetime of SF₆ at the altitude corresponding to pressure p .

3.2 Eddy diffusivity

Large variety of vertical profiles for eddy diffusivity in the stratosphere and lower mesosphere can be found in literature. In many studies in 1970-s – 1980-s the vertical profiles were derived from observed tracer concentrations neglecting the mean transport. Most studies suggested that the vertical eddy diffusion has a minimum of 0.2–0.5 m²/s (Pisso and Legras, 2008) at 15–20 km agreeing quite well to the ones derived from radar measurements in the range of 15–20 km Wilson (2004). Above that altitude K_z was suggested to gradually increases by about 1.5 orders of magnitude at 50 km due to breaking gravity waves (Lindzen, 1981).

145 The theoretical estimates of the effective exchange coefficients considering the layered and patchy structure of stratospheric turbulence suggest 0.5–2.5 m²/s for the upper troposphere and 0.015–0.02 m²/s for the lower stratosphere (Osman et al., 2016), which is about an order of magnitude lower than the estimates above.

The values of eddy exchange coefficient at heights of 10–20 km estimated from high-resolution balloon temperature measurements (Gavrilov et al., 2005) are ~ 0.01 m²/s with no noticeable vertical variation. It is not clear, however, how representative the derived values are for UTLS in general. We could not find any reliable observations of vertical diffusion in a range of 30–50 km.

The parameterisation for vertical eddy diffusivity above the boundary layer used in SILAM has been adapted from the IFS model of the European Centre for Medium-range Weather Forecasts (ECMWF, 2015). However, in the upper troposphere the predicted eddy diffusivity is nearly zero. For numerical reasons a lower limit of 0.01 m²/s is set for K_z in SILAM. Our sensitivity tests have shown that long-term simulations are practically insensitive to this limit as long as it is low enough (see results and discussion). The modelled K_z in the stratosphere is practically always set to the limiting value with relatively rare peaks, mostly in UTLS. Such scheme essentially turns off turbulent diffusion in the stratosphere. Same is true for recent ERA5 reanalysis dataset (Copernicus Climate Change Service (C3S), 2017) that provides the values of K_z among other model-level fields: the eddy diffusion practically always falls below the molecular diffusivity limit (Fig. 2), which is about two orders of magnitude lower than the estimates referenced above.

160 As a reference for this study, we took a tabulated profile of Hunten (1975), as it was quoted by Massie and Hunten (1981). The original profile covers the range up to 50 km, and the extrapolation up to 80 km matches well the theoretical estimates by (Lindzen, 1981) and by Allen et al. (1981). We approximate the profile as a function of pressure in the range of 100 – 0.01 hPa



(15 – 60 km):

$$165 \quad K_z(p) = 8 \text{ m}^2/\text{s} \left(\frac{100 \text{ Pa}}{p} \right)^{0.75}. \quad (2)$$

The approximated profile was stitched with the default Silam profile with a gradual transition within an altitude range of 10 – 15 km to keep the tropospheric dispersion intact. This profile gives values of K_z is 3 – 6 orders of magnitude higher than ones accepted in models (Fig. 2), and 1-2 orders of magnitude higher than more recent estimates (Legras et al., 2005). In order to cover the whole range of K_z , along with (2) we used two intermediate profiles whose upper part was scaled with factors
170 0.03 and 0.001 relative to the reference one. The three prescribed eddy-diffusivity profiles are hereinafter referred as “1Kz”, “0.03Kz”, and “0.001Kz” respectively. The dynamic eddy-diffusivity profile adopted from the ECMWF IFS model is referred to as “ECMWF Kz”. In all simulations the parameterization of K_z in the troposphere is the same, and linear transition from the SILAM K_z to the tabulated one occurs in the altitude range of 10 – 15 km.

3.3 Molecular diffusivity and gravity separation

175 In tropospheric and stratospheric CTMs gaseous admixtures are transported as tracers, i.e. advection and turbulent mixing do not depend on a species properties, whereas the molecular diffusion is negligible. Models that cover mesosphere, such as WACCM (Smith et al., 2011), account for molecular diffusion explicitly. Since some of the K_z parametrizations above often result in values below the molecular diffusivity, the parametrization of molecular diffusion has been implemented in SILAM.

The molecular diffusivity of SF_6 in the air at temperature $T_0 = 300 \text{ K}$ and pressure $p_0 = 1000 \text{ hPa}$, is $D_0 = 1 \times 10^{-5} \text{ m}^2 \text{ s}^{-2}$
180 (Marrero and Mason, 1972, Table 22). The diffusivity at a different temperature T and pressure p is given by:

$$D = D_0 \frac{p_0}{p} \left(\frac{T}{T_0} \right)^{3/2}, \quad (3)$$

see e.g. Cussler (1997). The vertical profile of molecular diffusivity in the US standard atmosphere (NOAA et al., 1976) is shown in (Fig. 2). Note that the value for the reference diffusivity of SF_6 used in this paper is about a half of the one used in simulations with WACCM by Kovács et al. (2017). The reason is that WACCM uses a universal parametrization (Smith et al.,
185 2011, Eq. 7 there) for all compounds. That parametrization relies solely on molecular mass of a tracer and does not account for e.g. the molecule collision radius. The latter is about twice larger for SF_6 molecule than for most of stratospheric tracers. Thus, for this study we use the value from Marrero and Mason (1972), which results from fitting laboratory data for diffusion of SF_6 in the air.

The vertical diffusion transport velocity of admixture with number concentration \tilde{n} and molecular mass $\tilde{\mu}$ in neutrally-
190 stratified media is given by (Mange, 1957):

$$w = -D \left[\frac{1}{\tilde{\mu}} \frac{\partial \tilde{\mu}}{\partial z} + \left(\frac{\tilde{\mu}}{\mu} - 1 \right) \frac{\mu g}{kT} \right], \quad (4)$$

where μ is molecular masses of air, g – acceleration due to gravity, k is the Boltzmann constant, and T is temperature. With ideal gas law $p = nkT$, in which p is pressure, and n is number concentration, and static law $dp/dz = -g\rho$, where $\rho = \mu n$ is



the air density, the equation (4) can be reformulated in terms of the admixture mixing ratio $\xi = \tilde{n}/n$ and pressure. Then the
195 vertical gradient of the equilibrium mixing ratio will be:

$$\frac{\partial \xi}{\partial p} = \left(\frac{\tilde{\mu}}{\mu} - 1 \right) \frac{\xi}{p}. \quad (5)$$

It is non-zero for an admixture of a molecular mass different from one of the air. Integrating the gradient (5) over vertical, one
can obtain that the equilibrium mixing ratios of the admixture at two layers are proportional to the corresponding pressures
taken to the power of $\tilde{\mu}/\mu - 1$. For heavy admixtures, such as SF₆ ($\tilde{\mu} = 0.146$ kg/mole) the equilibrium gradient of a mixing
200 ratio is substantial. For example, the difference of equilibrium mixing ratio of SF₆ in the atmosphere between 10 and 20 Pa is
a factor of 16.

In most of the atmosphere, the effect of gravitational separation is insignificant due to overwhelming effect of other mixing
mechanisms, whereas in the upper stratosphere the molecular diffusivity may become significant. Thus in the upper stratosphere
heavy gases can no longer be considered as tracers and the molecular diffusion should be treated explicitly. The effect of
205 gravitational separation of nitrogen and oxygen isotopes in the stratosphere has been observed (Ishidoya et al., 2008, 2013;
Sugawara et al., 2018), however for isotopes the ratio of masses is relatively small, so the observed differences were also small
(up to 10^{-5}). For SF₆ the molecular mass difference is much larger.

In order to enable the gravitational separation in SILAM we have introduced a molecular diffusion mechanism that can
be enabled along with the turbulent vertical diffusion scheme. The exchange coefficients between the model layers are pre-
210 calculated according to Eq. (4) discretised for the given layer structure for each species according to its diffusivity and molar
mass. The US standard atmosphere (NOAA et al., 1976) was assumed for vertical profiles of temperature and air density during
pre-calculation.

3.4 Parametrization for destruction of SF₆ in the mesosphere

As it has been mentioned above, the topmost level of the ERA-Interim meteorological data set is located at 10 Pa, which
215 is below the layer where the destruction of SF₆ occurs. Therefore we have to put a boundary condition to our simulations
to account for the upward flux of SF₆ through the upper boundary of the simulation domain. For that we assume that SF₆
distribution above the computational domain is in equilibrium with destruction and vertical flux.

Assuming the profiles for $K_z(p)$ and the SF₆ lifetime $\tau(p)$ are given by (2) and (1), one can obtain a steady-state distribution
of mass-mixing ratio ξ of SF₆ due to destruction in the mesosphere at any point where both (2) and (1) are valid and vertical
220 advection is negligible. This requires a solution of a steady-state diffusion equation with a sink:

$$\frac{\partial \xi}{\partial t} = g^2 \frac{\partial}{\partial p} \left(\rho^2 K_z(p) \frac{\partial \xi}{\partial p} \right) - \frac{\xi}{\tau(p)} = 0, \quad (6)$$

where $\rho(p)$ is air density, and g is acceleration due to gravity. Solving the Eq. (6) one can express the steady-state upward flux
of SF₆ normalized with the mass mixing ratio at each pressure $\tilde{F}(p) = F(p)/\xi(p)$ as a function of p . The above equation was
solved numerically with a boundary conditions of unit mixing ratio at a height of 100 Pa and vanishing flux at $p = 0$. Indeed

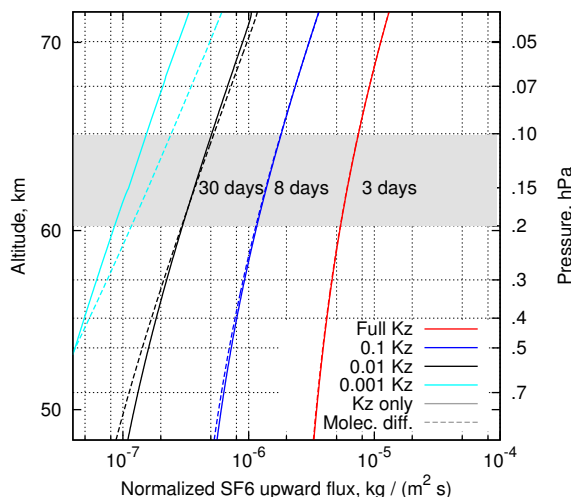


Figure 3. Vertical profiles of steady-state upward flux of SF₆ normalized with mass mixing ratio, for eddy diffusivity and lifetime profiles given by (2) and (1). The upper model layer of Silam and effective lifetimes of SF₆ there due to the destruction in the mesosphere for different K profiles are given.

225 for all considered cases the flux decreased by several orders of magnitude already at the level of a few Pa. The resulting $\tilde{F}(p)$ for four test profiles of K_z are shown in Fig. 3 with solid lines.

The effect of gravitational separation can be accounted for by introducing into Eq. (6) a term responsible for molecular diffusion and its equilibrium state (5):

$$\frac{\partial \xi}{\partial t} = g^2 \frac{\partial}{\partial p} \left(\rho^2 K_z(p) \frac{\partial \xi}{\partial p} + \rho^2 D(p) \left(\frac{\partial \xi}{\partial p} - \frac{\tilde{\mu} - \mu}{\mu} \frac{\xi}{p} \right) \right) - \frac{\xi}{\tau(p)} = 0. \quad (7)$$

230 The profiles of $\tilde{F}(p)$ resulting from this equation for SF₆ are given in Fig. 3 with dashed lines.

Accounting for molecular diffusion may either enhance or reduce the upward flux of SF₆ in the model. Along with setting the equilibrium state when the bulk of a heavy admixture is in the lower layers, molecular diffusion provides additional means for transport to the upper layers where the destruction occurs. For very low eddy diffusivities, the molecular diffusion is a sole mechanism of upward transport of SF₆ towards depletion layers. For higher eddy diffusivity the effect of molecular diffusion and gravitational separation becomes negligible.

235 For a model consisting of stacked well-mixed finite layers, the loss of SF₆ from the uppermost layer due to the steady upward flux would be proportional to the SF₆ mixing ratio in the layer. This loss of mass is equivalent to a linear decay of SF₆ in the layer at a rate $\tau^{-1} = g\tilde{F}(p)/\Delta p$, where Δp is a pressure drop in the layer.

240 For the upper layer of our simulations, the layer between 10 and 20 Pa (grey rectangle in Fig. 3) and $K_z(p)$ given with Eq. (2), the corresponding SF₆ lifetime τ in the layer is about 3 days. After scaling the $K_z(p)$ profile with factors of 0.1, 0.01, and 0.001 one gets the lifetimes of 8, 30, and 60 days respectively. Note that due to the molecular diffusion, the SF₆ lifetime in



the topmost model layer becomes insensitive to the exact profile of the eddy diffusivity. In particular, for the considered layer it can not be longer than 60 days.

3.5 Simulation setup

245 The simulations of atmospheric transport were performed with the SILAM model for 1980-2018 years on a 1.44x1.44 degree global grid with 60 hybrid sigma-pressure layers starting from surface, with the uppermost layer between pressures of 20 and 10 Pa. The model time step of 15 minutes was been used and the output of daily mean concentrations of tracers together with air density was arranged.

The simulations were driven with ERA-interim meteorology at 0.72-degree resolution, so the meteorological input for both cell-interface for winds, and cell mid-points for other parameters was available without further interpolation. The gridded ERA-interim fields are, however, a result of reprojection of the original meteorological fields from spherical harmonics. Moreover, differences in the representation of model vertical structure between IFS and SILAM make a vertical reprojection necessary. These reprojections together with a limited precision of the gridded fields and inevitable small differences in physical parametrizations between IFS and SILAM result in inconsistency between surface-pressure tendencies and vertically-integrated air-mass fluxes calculated from the meteorological fields in SILAM. Such inconsistencies cause spurious variations in wind-field divergence that on long-term run result in accumulation of errors in tracer mixing ratios, and consequently, in the simulated AoA. Therefore, horizontal wind fields were adjusted by distributing the residuals of pressure tendency and vertically-integrated horizontal air-mass fluxes as a correction to the horizontal winds following the procedure suggested by Heimann and Keeling (1989). The correction is normally comparable to the precision of the input wind fields. The vertical wind component was then re-diagnosed from a divergence of horizontal air-mass fluxes for individual SILAM layers as described in Sofiev et al. (2015).

SILAM performs 3D transport by means of a dimension split: transport along each dimension is performed separately as 1D transport. To minimize the inconsistency between the tracer transport and air-mass fluxes, caused by the dimension split at finite time step, the splitting sequence has been inverted at each time step to reduce the accumulation of errors. The residual inconsistency was resolved by using a separate “ones” tracer, which was initialized to the constant mass mixing ratio of 1 at the beginning of a simulation. If advection was perfect, the concentration of “ones” would be equivalent to air density (mixing ratio would stay equal to 1). The mixing ratios of simulated tracers were then evaluated as a ratio of a tracer mass in a cell to the mass of “ones”.

In order to assess the effects of gravitational separation and destruction on the atmospheric distribution of SF₆, we have used four tracers: SF₆ as a passive tracer “sf6pass”, SF₆ with gravitational separation but no destruction “sf6nochem” (no chemistry), SF₆ with destruction but no gravitational separation “sf6nograv”, and SF₆ with both gravitational separation and destruction in the upper model level “sf6”.

All SF₆ tracers had the same emission according to the SF₆ emission inventory (Rigby et al., 2010). The inventory covers 1970-2008, and was extrapolated with a linearly growing trend of 0.294 Gg/y until July 2016. The last 2.5 years were run without SF₆ emissions to evaluate its destruction rate.



Besides the four SF₆ tracers we have used a “passive” tracer emitted uniformly at the surface at constant rate during the whole simulation time and an “ideal age” tracer. The “ideal age” tracer is defined as a tracer whose mixing ratio ξ_{ia} obeys continuity equation (Waugh, 2002):

$$\frac{\partial \xi_{ia}}{\partial t} + \mathcal{L}(\xi_{ia}) = 1, \quad (8)$$

280 (where \mathcal{L} is an advection-diffusion operator), and boundary condition $\xi_{ia} = 0$ at the surface. The “ideal age” tracer is transported as a regular gaseous tracer, and to maintain consistency with other tracer mixing ratios, the ideal age is updated at every model time step Δt using the “ones” tracer:

$$M_{ia} \mapsto \begin{cases} 0, & \text{at lowest layer,} \\ M_{ia} + M_{ones} \Delta t, & \text{otherwise,} \end{cases} \quad (9)$$

where M_{ia} and M_{ones} are masses of “ideal age” tracer and of “ones” tracer in a grid cell. The mixing ratio of the “ideal age” tracer is a direct measure of the mean age of air in a cell, so the tracer is a direct Eulerian analogy of the time-tagged Lagrangian particles with clock reset at the surface.

A set of the simulations was performed with four settings for the eddy diffusivity profile, described in Sec. 3.2 and corresponding destruction rates of “sf6” and “sf6nograv” tracers in the uppermost model layer. All runs were initialized with the mixing ratios from the final state of a special initialization run performed with “0.001Kz” eddy diffusivity. The initialization simulation was started from zero fields for all tracers, except for “ones” tracer that was set to unity mixing ratio. The simulation was run with 1970-1979 emissions for SF₆ species, and driven by ERA-Interim meteorological fields for 1980-1989. The mixing ratios of all SF₆ tracers at the end of the initialization run were scaled to match the total SF₆ burden of 20.17 Gg in 1980 (Levin et al., 2010).

4 Sensitivity and validation of SF₆ simulations

295 4.1 Gravitational separation and mesospheric depletion

To evaluate the relative importance of gravitational separation and mesospheric depletion and their effect on the SF₆ concentrations we have compared the simulations for various SF₆ tracers and evaluated the relative reduction of SF₆ content in the stratosphere due to these processes. As a conservative estimate of the reduction, we evaluated the relative differences between the tracers in the latitude belt of 70-85S, since both processes have the most pronounced effect in southern polar vortex, where the downdraught of Brewer-Dobson circulation is the strongest.

Hereafter we quantify the effect of a relative difference between atmospheric contents of two SF₆ tracers “X” and “Y” defined as:

$$\Delta(\text{“X”}, \text{“Y”}) = 2 \frac{\xi_X - \xi_Y}{\xi_X + \xi_Y} \cdot 100\% \quad (10)$$

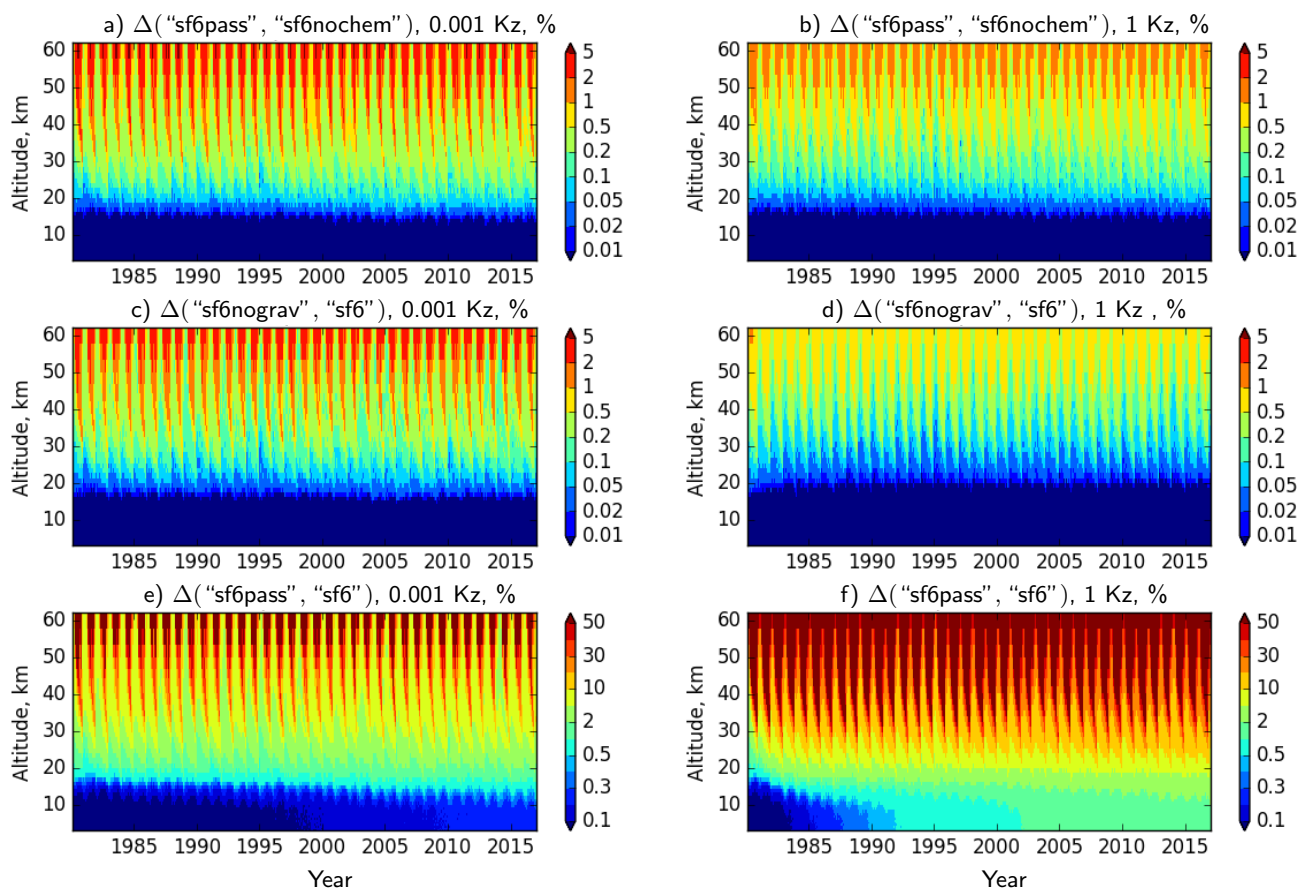


Figure 4. The relative reduction of SF₆ content (in %) at 70-85S due to gravitational separation with (a, b) and without (c, d) depletion, and due to combined effect of depletion and separation (e, f) at two extreme K_z cases. Note different color scales for e) and f).

The relative differences for the SF₆ tracers in the Southern polar region simulated with two extreme models for K_z is given in Fig. 4 as a function of time and altitude. Noteworthy, every 5% of decrease of SF₆ with respect to its passive counterpart correspond to about one year of a positive bias in AoA derived from SF₆ mixing ratios.

The reduction of SF₆ content due to gravitational separation if the mesospheric depletion is disabled is given by the relative difference of "sf6nochem" and "sf6pass" (Fig. 4ab). Expectedly, the effect of gravitational separation is most pronounced for the case of low eddy diffusivity ("0.001 Kz"), and the reduction of SF₆ in the altitude range of 30–50 km reaches 2 – 5%. In the case of strong mixing, the effect of separation is about 1%.

The reduction of SF₆ content due to gravitational separation in presence of stratospheric depletion given by the relative difference of "sf6nograv" and "sf6" tracers. The effect of the separation for low K_z is very similar between depletion and no-depletion case (Fig. 4c vs. Fig. 4a). Depletion reduces the effect of the gravitational separation for high K_z (Fig. 4b vs Fig. 4d).



Tracer/ Kz scheme	removal rate, 10^3 mol/year	lifetime, years
passive, any Kz	0	∞
SF ₆ , ECMWF Kz	440	2900
SF ₆ , 0.001 Kz	480	2600
SF ₆ , 0.01 Kz	760	1700
SF ₆ , 0.03 Kz	800	1540
SF ₆ , 0.1 Kz	960	1300
SF ₆ , 1 Kz	2160	590

Table 1. SF₆ destruction rate after stopping emissions. Mid-2011 atmospheric burden of SF₆ of $1.27 \cdot 10^9$ moles is used as reference for the lifetime estimate

315 Regardless depletion, stronger K_z reduces the effect of the gravitational separation, however the latter is still non-negligible if
precisions of order of a month for AoA are required.

The combined effect of depletion and gravitational separation is seen in the relative difference of “sf6pass” and “sf6” tracers
(Fig. 4e and 4f). For both K_z cases the effect of depletion is by more than an order of magnitude stronger than one of gravity
separation. Regardless the used K_z profiles, the reduction exceeds 50 %, which roughly corresponds to 10 years of an offset
320 in the apparent AoA. The reduction has a noticeable inter-annual variability that poses substantial difficulties on applying a
consistent correction to the apparent AoA. Contrary to the former two comparisons, stronger eddy mixing leads to stronger
reduction of SF₆ since it intensifies the transport to the depletion layers, and thus enhances the depletion rate.

Since the simulations for different K_z have been initialized with the same state matching the total amount of SF₆, the
simulations with “0.01 Kz” showed relaxation of the SF₆ vertical distribution during the first few years of the simulations. For
325 “1 Kz” case (4f) the gradual increase of the difference between SF₆ and its passive version in the troposphere can be seen.
The rate of this increase is about 0.5% per 39 years of simulations. This rate should not be confused with the depletion rate of
SF₆ in the atmosphere since the difference is a combined effect of depletion and growth of emission rate, despite the latter is
exactly the same for both tracers.

The above comparison indicates that the depletion has the stronger effect on the distribution of the SF₆ mixing ratio in
330 the upper stratosphere than gravitational separation and molecular diffusion. However, the important role of the molecular
diffusion is that it maintains the upward flux towards the mesosphere in the simulations even if the eddy diffusivity ceases.

Further in this paper only the “sf6pass” and “sf6” tracers will be used.

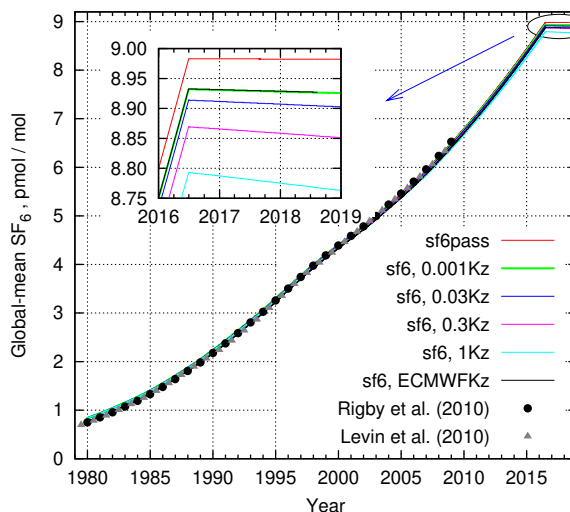


Figure 5. The time series of mean mixing ratio of SF₆ in the atmosphere simulated with emissions stopped in July 2016. The total burden by Levin et al. (2010) and by Rigby et al. (2010) are shown for comparison.

4.2 Lifetime of SF₆ in the atmosphere

In order to estimate the atmospheric lifetime of SF₆ we turned off the emission of all simulated SF₆ tracers in July 2016 and
335 let the model run until the end of 2018 without emissions (Fig. 5). The decrease of the simulated SF₆ burden after the emission stop can be used to estimate the SF₆ removal rate from the atmosphere.

Time series of the total burden of SF₆ in the atmosphere in the simulations are given in Fig. 5. For easier comparison to
observed mixing ratios the burden has been normalised with $1.78 \cdot 10^{20}$ moles – the total amount of air in the atmosphere –
to get the mean mixing ratio. The tabulated values for the atmospheric burden of SF₆ from Levin et al. (2010) and Rigby
340 et al. (2010) are given for comparison. Since the removal of SF₆ from the atmosphere is mostly controlled by the transport towards the depletion layer, the vertical exchange is a key controlling factor. In all simulated cases, the removal of SF₆ from the atmosphere is very slow, so the relative difference between the cases is small.

The decrease of the atmospheric SF₆ content after the emission stop, is given at the zoom panel of Fig. 5. As expected,
after July 2016 the content of passive SF₆ stays constant, while depleting SF₆ start to fall down at a rate that depends on
345 the transport properties of the stratosphere in the simulations, with faster removal for stronger eddy diffusivity. The removal rate is driven by the SF₆ content in the upper stratosphere, which is not in equilibrium with total atmospheric SF₆ content. A typical delay between SF₆ mixing ratio in the troposphere, where most of SF₆ resides, and the upper stratosphere, from where SF₆ escapes further to the depletion layers, is about 5-6 years. Hence, to estimate the SF₆ lifetimes we used the total amount of atmospheric SF₆ 5 years before the emission stop, i.e. 1.23×10^9 mol, which corresponds to mean mixing ratio of about
350 7 pmol/mol. Dividing the destruction rate with the reference amount one gets the range of corresponding simulated SF₆ life

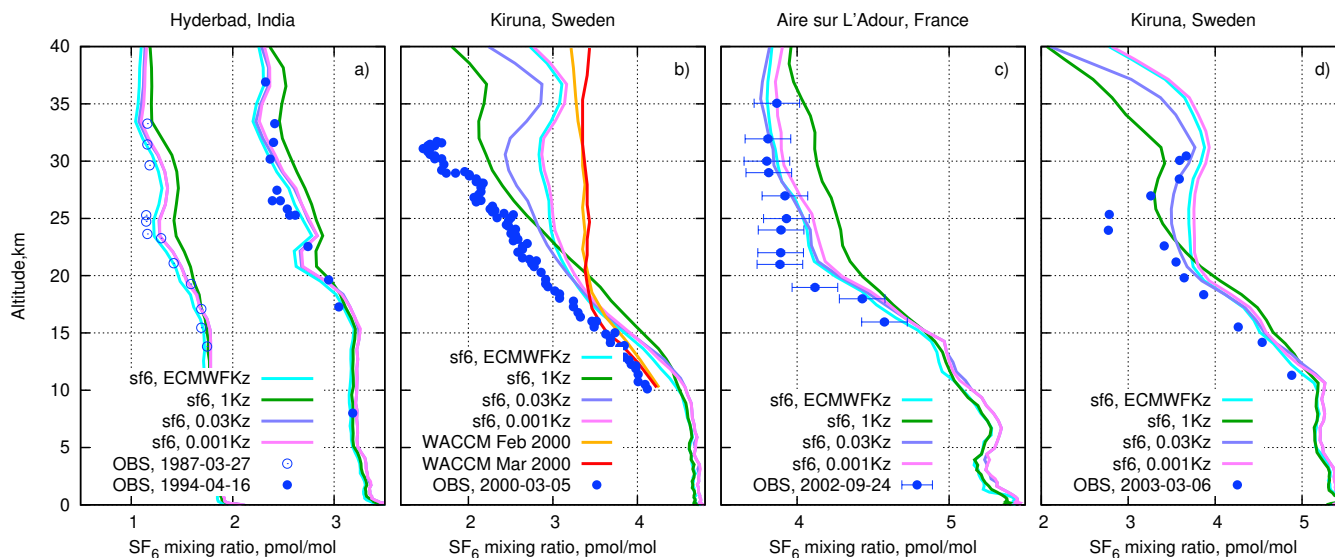


Figure 6. Observed SF_6 balloon profiles and corresponding daily-mean SILAM profiles for the date of observations. The observational data obtained from Patra et al. (1997), Ray et al. (2017), Ray et al. (2014), and Engel et al. (2006) for panels a–d correspondingly. The model profiles from WACCM model are from Ray et al. (2017).

times in the atmosphere: 600 to 2900 years. Despite the range of assumed diffusivities is three orders of magnitude, the decay rate of SF_6 varies only within a factor of five (Table 1).

The range of the SF_6 life times meets the ranges suggested by earlier studies. It is in a good agreement with results of Kovács et al. (2017), who obtained 1120 – 1475 years, and within the range of 800 – 3200 years, that one can find from model studies (Ravishankara et al., 1993; Morris et al., 1995), and 580–1400 years estimated from observational data (Ray et al., 2017).

4.3 Evaluation against balloon profiles

The tropospheric concentrations of SF_6 in our simulations have been practically insensitive to the way and rate of SF_6 destruction or to the choice of the eddy diffusivity profile. The difference in the modelled profiles can however be seen above the tropopause. For comparison we took the simulations with prescribed eddy diffusivity in stratosphere (1Kz, 0.03Kz, and 0.001Kz, see Sec. 3.2), and with dynamic eddy diffusivity “ECMWF Kz”. The simulations were matched with stratospheric balloon observations we have found in a literature (Fig. 6).

Two balloon profiles observed at Hyderabad (17.5N,78.6E) in 1987 and 1994 by Patra et al. (1997) indicate an increase of SF_6 content during the time between the soundings (Fig. 6a). Both profiles have a clear transition layer from tropopause at ~ 17 km to undisturbed upper stratosphere above ~ 25 km. The simulated profiles agree quite well to the observed profiles, except for the most diffusive case that gave notably smoother profiles and somewhat overstated SF_6 mixing ratios due to too strong exchange through the tropopause.



The profile in Fig. 6b has been obtained from Kiruna (68N, 21E) in early spring 2000 during the SAGE III Ozone Loss and Validation Experiment, SOLVE, (Ray et al., 2002) with the Lightweight Airborne Chromatograph (Moore et al., 2003). The profile is affected by the polar vortex and clearly indicates a strong reduction of SF₆ with height with a pronounced local minimum at 32 km. The corresponding SILAM profiles tend to overestimate the SF₆ vmr. The “ECMWF Kz” profile practically coincides to “0.001Kz”, since vertical mixing is negligible in both cases. The most diffusive profile “1Kz” has the strongest depletion in the upper part, but the largest deviation from the observations below 20 km. The intermediate-diffusion profile (“0.03Kz”) is almost as close to observations as the non-diffusive profile. Moreover, the “0.03Kz” profile has a minimum at the same altitude as the observed one, albeit the modelled minimum is substantially less deep.

For comparison, Fig. 6b also contains monthly-mean profiles from the WACCM simulations of Ray et al. (2014) along with the observation data. The WACCM profiles match very well the observations below 17 km, but turn nearly constant above, thus under-representing the depletion of SF₆ inside the polar vortex. Monthly-mean SILAM profiles (not shown) were much closer to plotted daily profiles than to monthly WACCM ones.

For the mid-latitude profile in Fig. 6c from Aire-sur-l’Adour, France (43.7N,0.3W), all SILAM profiles except for “1Kz” practically fall within the observational error bars provided together with the data by Ray et al. (2017). Similar to the Kiruna case in Fig. 6b, the SILAM profiles are much smoother than the observed ones and are unable to reproduce the sharp transition at 20 km.

Another profile from within the polar vortex (Fig. 6d) was observed at the same Kiruna site as one in Fig. 6b, but three years later. The observed profile also has a minimum that is much deeper than in the modelled profiles. Similar to the case in Fig. 6b, the “0.03Kz” profile is the only one that has a pronounced minimum at the same altitude as the observed one.

In all above cases, the “1Kz” profile is clearly far too diffusive and is an outlier that is furthest from the observations. The “ECMWF Kz” profiles practically coincide to “0.001Kz”, since vertical mixing is negligible in both cases. The “0.03Kz” profiles appear to be most realistic out of the four considered simulations: they are close to observed ones and have local minima at right altitudes for both Kiruna profiles.

4.4 Evaluation of SF₆ against MIPAS data

The MIPAS observations provide the richest observational dataset for stratospheric SF₆. However, each individual observation has a substantial noise error, which is noticeably larger than the difference between observation and any of the SILAM simulations. The largest diversity of the modelled SF₆ profiles was observed in polar regions, therefore below we show the mean profiles for each season in southern and northern polar areas. Besides that, we consider statistics of the model performance against MIPAS measurements in lower and upper stratosphere separately. For simplicity, we do not show the statistics for the “ECMWF Kz” runs, since it is very similar to one for “0.001Kz”.

For the comparison, the daily mean model profiles have been collocated to the observed ones, and then, an averaging kernel of the corresponding MIPAS profile was applied to the SILAM profile. For the comparison we took only the data points with all the following criteria met:

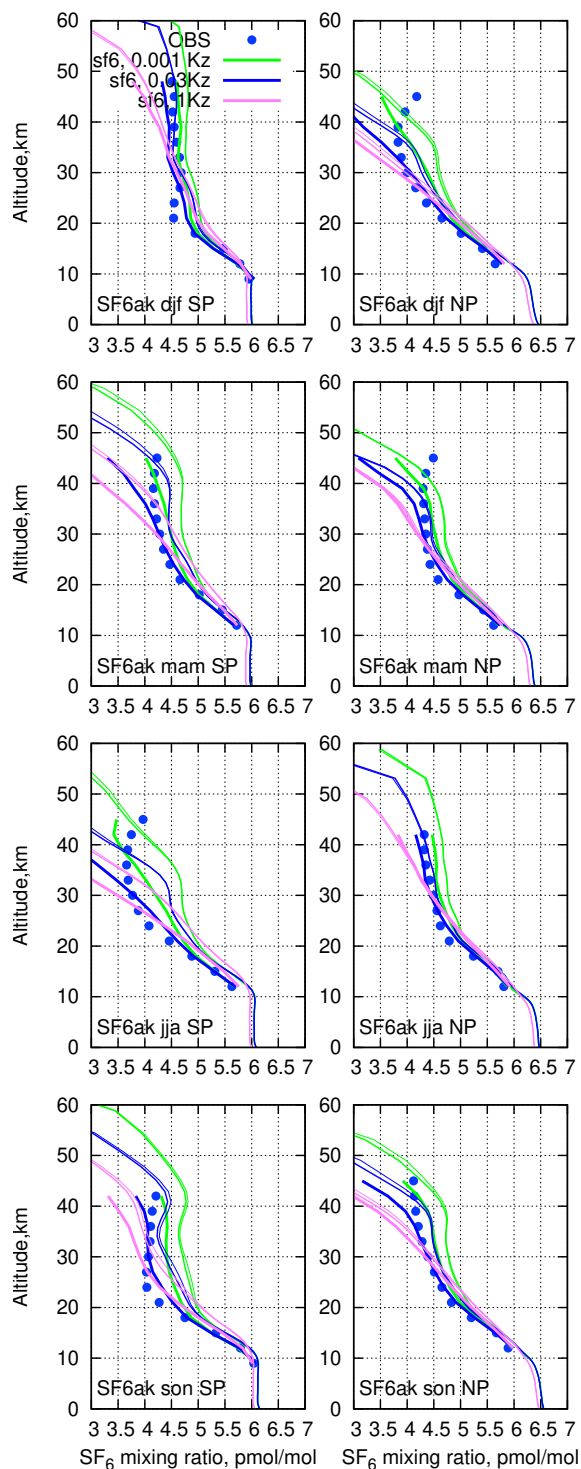


Figure 7. Seasonal mean collocated SILAM SF₆ and MIPAS profiles for 2007, for southern and northern polar regions



- 400 – MIPAS visibility flag equals 1
- MIPAS Averaging kernel diagonal elements exceed 0.01
- MIPAS retrieval vertical resolution, i.e. full-width at half-maximum of the row of the averaging kernel, is better than 20 km
- MIPAS volume mixing ratio noise error of SF₆ is less than 3 pmol/mol

405 The mean seasonal profiles of the SF₆ mixing ratio for southern and northern polar regions derived from the MIPAS observations and SILAM simulations for 2007 are given in Fig. 7. In order to facilitate the comparison of our evaluation with earlier study by Kovács et al. (2017) we have chosen the same year and same layout of the panels as Fig. 3 there. The main differences between Kovács et al. (2017) and current evaluation are:

- 410 – We used averages of collocated model profiles (bold lines). The non-collocated seasonal- and area-mean model profiles are given with thin lines for comparison.
- we use a newer version of MIPAS SF₆ data with considerably larger values in the upper stratosphere, compared to the version that was used by Kovács et al. (2017).
- We do not put error bars for the observed data, since the statistical uncertainty of the averaged values in the scale of the plots is smaller than a data point size. In Kovács et al. (2017) the bars are standard deviations of the observed values, rather than uncertainties of the mean.
- 415 – We use 3-km vertical bins for the profiles to make the points in MIPAS profiles distinguishable

First of all, note a substantial difference between collocated and non-collocated model profiles. The difference is caused by uneven sampling of the atmosphere by the satellite both in space and time. In particular, MIPAS, being a polar-orbiting instrument, makes more profiles per unit area closer to a pole than further away. The difference gets somewhat reduced if one uses equal weights for all model grid cells instead of area-weighted averaging, especially for wide latitude belts. The major difference comes probably from the inability of MIPAS to retrieve SF₆ profiles in presence of polar stratospheric clouds that clutter lower layers of the stratosphere and make the sampling of polar regions quite uneven both in time and in vertical. This hypothesis agrees with fact that the difference is most pronounced for the winter pole, especially for the south pole in JJA, and practically negligible at a summer pole.

425 The comparison in Fig. 7 shows that the profiles from the SILAM simulations agree quite well to the observations in the altitude range below 20 – 25 km, with the most diffusive “1Kz” slightly overstating the SF₆ mixing ratios. In the range above 25 km, the ‘1Kz’ profiles indicate too fast decrease of SF₆ with altitude. The “0.03Kz” profiles give the best results up to ~ 40 km, except for south pole in JJA and North pole in DJF.

430 None of the model setups is capable of reproducing adequately the observations above 40 km. Wintertime poles also pose a problem to the model. The disagreement indicates a deficiency in the model representation of air flows in the upper part of



the domain caused by insufficient vertical resolution of ERA-Interim in the upper stratosphere and lower mesosphere, and lack of pole-to-pole circulation. This discrepancy is in line with the comparisons in Fig. 6 for polar regions. The model tends to overstate the SF₆ content in the lower part of a polar vortex, and understate it above 40 km.

As more extensive verification of the SILAM simulations we computed statistical scores of the simulated SF₆ mixing ratios for each month of the MIPAS mission. The statistics were computed separately for the altitude range of 10 – 35 km (Fig. 8) and 30 – 60 km (Fig. 9). As the difference in statistical scores of the three selected simulations is quite minor, in addition to the aforementioned selection criteria for MIPAS data, we have selected only observations with the retrieval target noise error below 1 pmol mol⁻¹.

The root-mean square error of is mostly controlled by the bias, and does not allow for clear distinction between the simulated cases. In order to disentangle the effect of bias, we have calculated the standard deviation of model-measurement difference (STD), absolute bias, and normalised mean bias. The latter is given by

$$\text{NMB}(\%) = 2 \left\langle \frac{M - O}{M + O} \right\rangle \cdot 100\%, \quad (11)$$

where M and O are modelled and observed values, respectively, and $\langle \cdot \rangle$ denotes averaging over the selected model-observation pairs for the given range of times and altitudes. Along with the STD, we have plotted the RMS error of the observations due to retrieval noise in the original MIPAS data.

In the altitude range of 10 – 35 km, the STD of model-measurement difference is practically uniform in time with minor peaks in August-September (Fig. 8). The level of the noise error constitutes about 85 % of the total model-measurement difference. Application of averaging kernel to the model profiles reduces the STD. The intermediate-diffusivity case “0.03Kz” clearly shows the least STD uniformly over the whole observation period, the same case indicates the least absolute bias.

In the range of 30 – 60 km altitudes (Fig. 9) the level of retrieval noise is noticeably higher than for the lower stratosphere. Unlike in the lower stratosphere, the least biased case is “1Kz”, which has the largest STD. The STDs of “0.03Kz” and “0.001Kz” are practically on pair, however the latter has the strongest biases. Thus for the upper troposphere the intermediate-diffusivity case also shows the best performance.

5 Simulations of AoA

5.1 Eddy diffusivity and simulated AoA

The effect of the vertical eddy diffusivity on AoA in the stratosphere was evaluated with the same set of three prescribed K_z profiles and one dynamic K_z profile, as for SF₆ simulations. An example of annual-mean distributions of AoA for the same year is given in Fig. 10. The Hunten (1975) K_z profile (Fig. 10a) gives AoA in the stratosphere of about 3.5 years. It is much shorter than available estimates of stratospheric AoA (e.g. Waugh, 2009; Engel et al., 2009) from the observations of various tracers. Three other profiles of K_z result in practically identical distribution of AoA with typical stratospheric AoA of 5.5 years, which agrees quite well with the experimental estimates. Since “0.03Kz” profiles result in most realistic distribution of SF₆ in our simulations, in the current section we will use simulated distributions of tracers with “0.03Kz” eddy diffusivity.



5.2 Age-of-Air and apparent SF₆ AoA

The constant-rate emission of the “passive” tracer in our simulations resulted in practically linear growth of the near-surface
465 mixing ratio of the tracer after a decade of spin-up. The latter makes the age derived from the “passive” tracer equivalent to the
age derived from the ideal-age tracer. The resulting distributions of “passive” and ideal-age AoA are indeed very close to each
other (Fig. 11 a and b). The agreement confirms the self-consistency of the transport procedure since the tracers have opposite
sensitivity to the advection errors: higher mixing ratios correspond to younger air for the accumulating tracers, while for the
ideal-age tracer higher mixing ratios correspond to older air. The remaining differences are caused by spatial inhomogeneities
470 of near-surface mixing ratio of “passive” due to variations in the near-surface air density.

The distribution of the AoA derived from “sf6pass” (Fig. 11c) is partly similar to the ideal-age one, however one can see
substantial differences. The negative AoA in northern troposphere for the “sf6pass” tracer is caused by the predominant location
of the sources in the northern hemisphere, so the concentrations there exceed global-mean levels. The growing rate of the SF₆
emissions leads to the greater than linear increase of near-surface mixing ratios, which leads to a slight old bias of the “sf6pass”
475 AoA. This old bias has been one of the drawbacks of the SF₆ AoA pointed by Garcia et al. (2011).

The ages shown in Fig. 11a – c agree well with the ages derived from *in-situ* observations of SF₆ and CO₂ at the 25 km
altitude by Waugh (2002). They also agree quite well with earlier simulations with five climate models that give annual mean
ages in the upper stratosphere between 4.5 and 5.5 years (Butchart et al., 2010), and with Lagrangian simulations of (Diallo
et al., 2012) driven by the same ERA-Interim meteorological fields as used for the present study. A substantial disagreement,
480 however, exists with the ages derived from the MIPAS satellite observations (Stiller et al., 2012; Haenel et al., 2015), who
calculated ages exceeding 10 years in polar areas and in the upper stratosphere. The reason for the disagreement follows from
the above analysis: SF₆ can neither be considered as a passive tracer nor its mixing ration in the troposphere grows linearly
with time. Denoting the AoA derived from the SF₆ profiles as “apparent AoA” (Waugh, 2002), we calculated it from the
SILAM-predicted SF₆ profiles, which, as shown above, agree well with AoA derived from MIPAS. The resulting model-based
485 apparent AoA (Fig. 11d) is indeed much older than the “ideal-age” AoA and pretty close to the values derived from MIPAS
profiles by Stiller et al. (2012); Haenel et al. (2015).

The effect of apparent over-aging in the stratosphere due to the subsidence of the mesospheric air was estimated by Stiller
et al. (2012) to be a fraction of a year in the upper stratosphere. In our simulations, the over-aging due to the SF₆ depletion and
other factors discussed in previous sections is much stronger and affects practically the whole stratosphere. Recently Sugawara
490 et al. (2018) also pointed that SF₆ AoA clearly deviates from AoA obtained from CO₂ already above 25 km.

5.3 Trends in apparent AoA

Changes in AoA have been used in many studies as an indicator of changes in the atmospheric circulation. In order to evaluate
the effect of the way AoA is evaluated on trends in AoA we have calculated trends in apparent AoA at different altitudes and
latitudes for 2002-2012. This period roughly covers the MIPAS mission time and allows for comparison with trends reported
495 by Haenel et al. (2015).



The zonal-mean vertical profiles of the AoA trends during 2002-2012 are shown in Fig. 12 for five latitudinal belts. The presented variable is a slope of the linear fit of the AoA time series for each tracer, averaged over the corresponding latitudinal belt and model layer. The fit was made with the ordinary least-squares method for each tracer. The error-bars show 95-% confidence intervals, calculated as if a model of linear trend with uncorrelated Gaussian noise was applicable to the time series.

500 The trends of the apparent AoA for the non-passive SF₆ species have a clear increase with height in the upper part of the profiles. The increase is the largest at high latitudes. Such a behaviour of trends agrees well with the AoA trends of Haenel et al. (2015, Fig. 7) obtained from the MIPAS observations. The over-aging due to the mesospheric depletion of SF₆ has been discussed and estimated by Haenel et al. (2015); Kovács et al. (2017). However, Fig. 12 shows that the mesospheric depletion of SF₆ also affects its trend: the over-aging increases with time. The reason is that depletion is proportional to the SF₆ load,

505 which grows with time.

The apparent AoA derived with passive SF₆ tracer “sf6pass” indicates a negative trend of about 0.5 years/decade. The trend is caused by the temporal variation of SF₆ emissions. In order to get unbiased AoA estimate from a passive tracer, one needs the mixing ratio at the surface increasing linearly with time. A steady growth of emission rate at the surface leads to faster-than-linear increase of near-surface mixing ratio and, thus, low-bias of AoA since younger (i.e. more rich with SF₆) air gets

510 more weight when two volumes of different age mix. According to the inventory (Levin et al., 2010) used in this study, the SF₆ emission rate was growing in 1997–2000 about twice slower than after 2005. Consequently, the negative bias of apparent AoA has increased resulting in negative trend if AoA in the stratosphere.

The AoA trends derived from the “ideal age” and “passive” tracers agree through the whole range of altitudes and latitudes indicating internal consistency of our simulations. The main common feature of the profiles is the negative tendency of about

515 –0.5 year/decade in the altitude range of 15-30 km. We suspect it to be a feature of the non-uniformity of the ERA-Interim dataset, which was produced with assimilation of an inhomogeneous set of the observations. During that period, the amount of the assimilated data on the upper-air temperatures was by an order of magnitude higher than before 2000 and two orders of magnitude higher than after 2010 (Dee et al., 2011). It had a clear impact on the patterns of analysis increments in ERA-Interim and, consequently, on the predicted stratospheric circulation. Due to such inhomogeneities, ERA-Interim was not recommended

520 for climatological studies. Therefore we do not draw any conclusion here on the actual trends of AoA but highlight that the trends of apparent AoA are completely determined by the method of its calculation.

6 Conclusions

Eulerian simulations of the tropospheric and stratospheric transport of several tracers were performed with SILAM model driven by ERA-Interim reanalysis for 1980-2018. The simulations included several species representing SF₆ under different

525 assumptions, a passive tracer emitted uniformly at the surface, and an “ideal age” tracer directly comparable with Lagrangian simulations of a particle residence time. To our best knowledge this is the first systematic evaluation of AoA derived from several different tracers within the same simulation over several decades, combined with extensive evaluation against MIPAS and balloon SF₆ observations.



Due to the limited vertical coverage and resolution of ERA-Interim in the upper stratosphere, the SILAM simulation domain
530 had a lid at 10 Pa, which is below the altitude of the SF₆ destruction. In order to perform realistic simulations of SF₆ in our
setup, the eddy diffusion in the upper stratosphere and lower mesosphere had to be parameterised, along with the mesospheric
sink of SF₆.

A set of simulations with different parameterisations for the vertical eddy diffusion showed that published profiles derived
with no account for advection (see e.g. Massie and Hunten, 1981, and references therein) overestimate the eddy diffusivity.
535 On other hand, the eddy-diffusivity profiles for scalars calculated from ERA-Interim fields according to the IFS procedures
ECMWF (2015)), or readily available from ERA5 reanalysis, appear to be of no relevance for the upper stratosphere, since
they fall below the molecular diffusivity. Evaluation of our simulations against satellite and balloon observations indicated that
the best agreement between simulated and observed SF₆ mixing ratios is achieved for the tabulated eddy-diffusivity profile of
Hunten (1975) scaled down with a factor of 30. It is not clear, however, if this conclusion is valid beyond the specific setup.
540 Thus, the question on the importance and magnitude of the eddy diffusivity in the upper stratosphere and lower mesosphere
remains open. Our simulations indicate that the diffusivities of 0.1 m/s² or less can be used in the upper stratosphere, until the
molecular diffusivity takes over.

The mesospheric sink of SF₆ has a major impact on the mixing ratios above 20 km. The depletion impact is especially strong
in wintertime polar areas due to the downdraft within a polar vortex. The sensitivity tests have shown that molecular diffusion
545 and gravitational separation of SF₆ are responsible for up to a few percent of further reduction in SF₆ mixing ratios in the
upper stratosphere.

A good agreement of simulated SF₆ distribution to the MIPAS observations up to the altitudes of 30-40 km and to available
balloon profiles was shown. The standard deviation between MIPAS and modelled SF₆ mixing ratios is up to 80 % controlled
by noise error of the satellite retrievals. The results of the comparison also underline the importance of accurate collocation of
550 model and observed data in terms of space, time and vertical averaging of observed data.

The lifetime of SF₆ in the atmosphere estimated from the best-performing setup is about 1500 years, in a good agreement
with previous studies.

Our simulations were able to reproduce both AoA obtained in other model studies, and apparent SF₆ AoA derived from
MIPAS observations. Having all tracers within the same simulations we were able to trace the differences in the estimated
555 AoA to the peculiarities of each tracer. A good agreement of passive-tracer and “ideal-age” AoA indicates a consistency of the
simulations, since these two methods have opposite sign of sensitivity to errors of the transport scheme.

The mesospheric sink has severe implications on the AoA derived from SF₆. The apparent over-aging introduced by the
sink is large and variable in space and season. Moreover, the over-aging due to the sink increases as the atmospheric burden
of SF₆ grows. All this makes SF₆ unsuitable to infer AoA above ~ 20 km. Even in for the fully-passive SF₆ tracer there are
560 deviations of apparent AoA from the “ideal-age” AoA caused by variable rate of the emissions. These deviations appear as
long-term trends in the apparent AoA that differ from trends in the “ideal-age AoA”, and have little relation to actual trends in
the atmospheric circulation.



565 Procedures used to derive AoA from observations of various tracers in the atmosphere are inevitably based on assumptions and idealisations that have limited and often unknown area of applicability. The resulting uncertainties in AoA are large enough to preclude the use of apparent AoA and its trends for evaluation of changes in atmospheric circulation or for validation of atmospheric models. Observations of the tracers themselves, however, have quite well quantified uncertainties, so direct comparisons of simulated tracers to the observed ones are a very promising means for the atmospheric model evaluation. AoA in turn is a convenient means for model inter-comparison if a protocol of AoA derivation is well specified.

570 *Code and data availability.* The SILAM source code as well as the simulation results used for this study are available from MS or RK on request. The MIPAS observational data available from GS on request. ERA-Interim and ERA5 reanalyses data sets are available from the European Center for Medium-range weather forecast <http://www.ecmwf.int>.

Author contributions. RK performed the simulations and data analyses, prepared text and illustrations. MS and JV inspired the study and helped with discussions on content and structure of the study. GS provided MIPAS data and wrote sections about MIPAS observations. All authors participated in the final preparation of the text.

575 *Competing interests.* The authors declare no competing interests.

Acknowledgements. The authors acknowledge the support of projects: EU FP7-MarcoPolo (ID: 606953), ESA-ATILA (contract no. 4000105828/12/F/MO) and ASTREX of Academy of Finland (grant 139126).

580 The SF₆ and mean age-of-air distributions from MIPAS observations were generated within the project STI 210/5-3 of the CAWSES priority program, funded by the German Research Foundation (DFG), and the project BDCHANGE (01LG1221B), funded by the German Federal Ministry of Education and Research (BMBF) within the “ROMIC” program.

The authors are grateful to Viktoria Sofieva (Finnish Meteorological institute) for reading the manuscript and providing useful comments, to Florian Haenel and Michael Kiefer (Karlsruhe Institute of Technology) for technical assistance in handling MIPAS SF₆ data.



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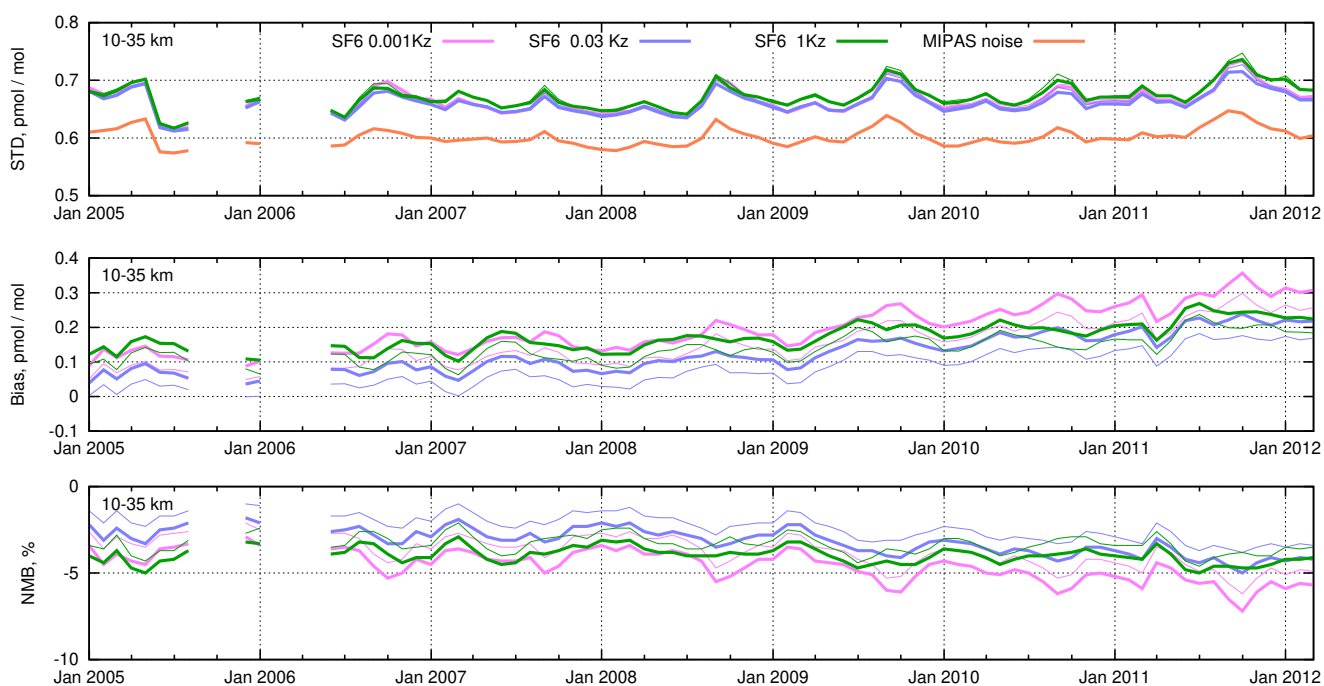


Figure 8. The time series of monthly scores for the SILAM-simulated SF₆ mixing ratios for the whole period of MIPAS observations in the altitude range of 10 – 35 km. The statistics are: de-biased RMSE, absolute bias and normalised mean bias. The statistics of model mixing ratios extracted at nominal MIPAS altitudes are given in thin lines.

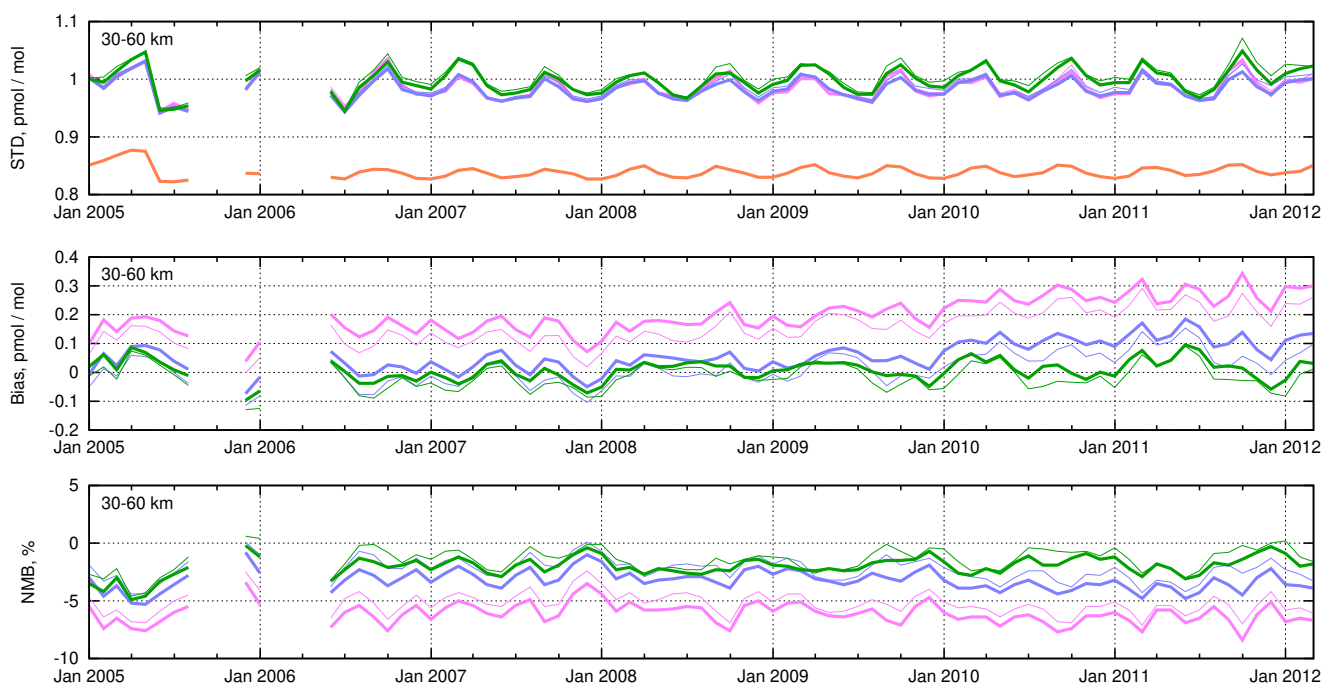


Figure 9. Same as in Fig. 8, but for the MIPAS altitude range of 30 – 60 km.

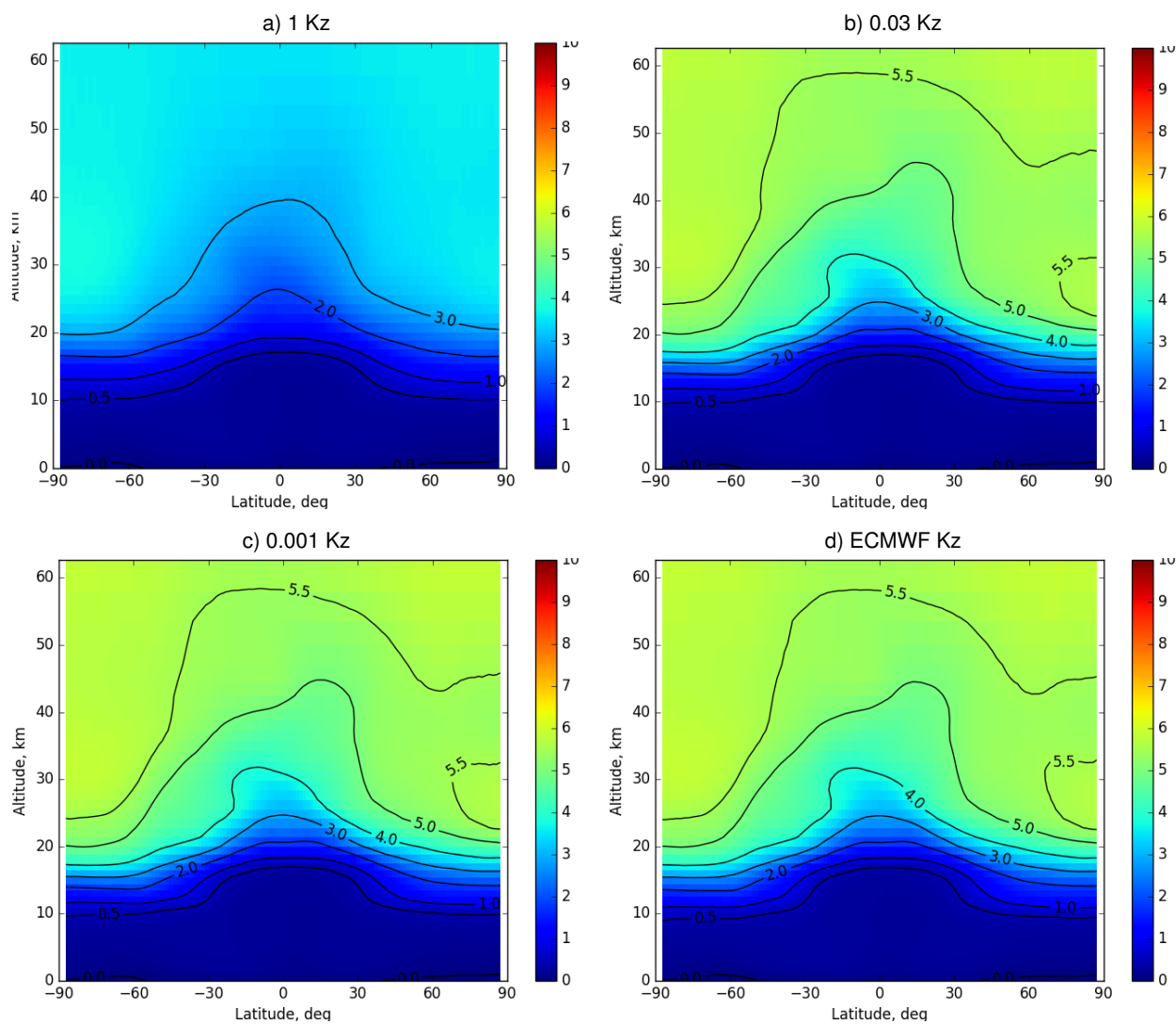


Figure 10. The zonal-mean spatial distribution of the ideal-age AoA for 2011 calculated for different eddy-diffusivity profiles.

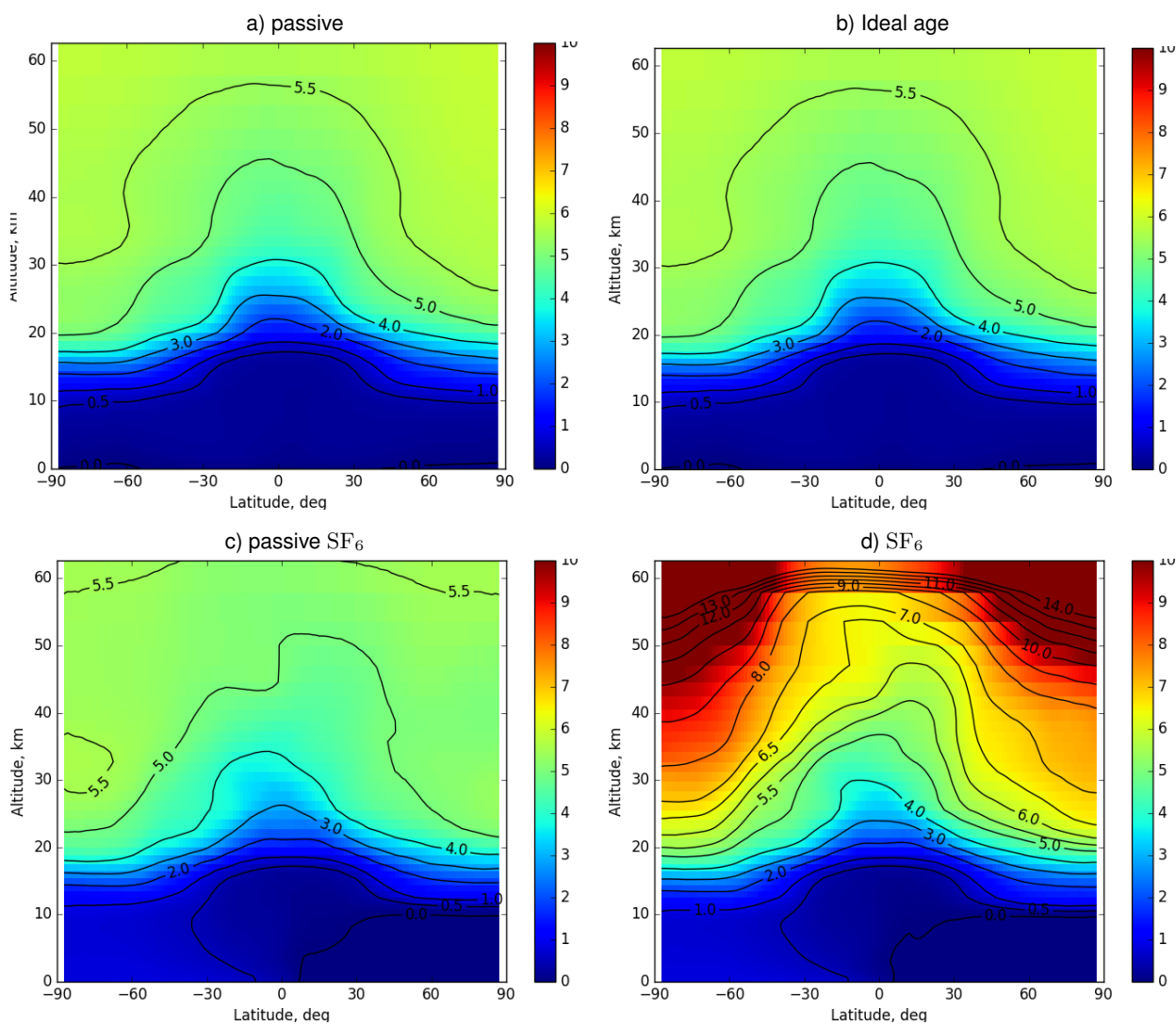


Figure 11. Zonal-mean distributions of atmospheric AoA simulated with “passive”, ideal-age, and two SF₆ tracers, average for 2012.

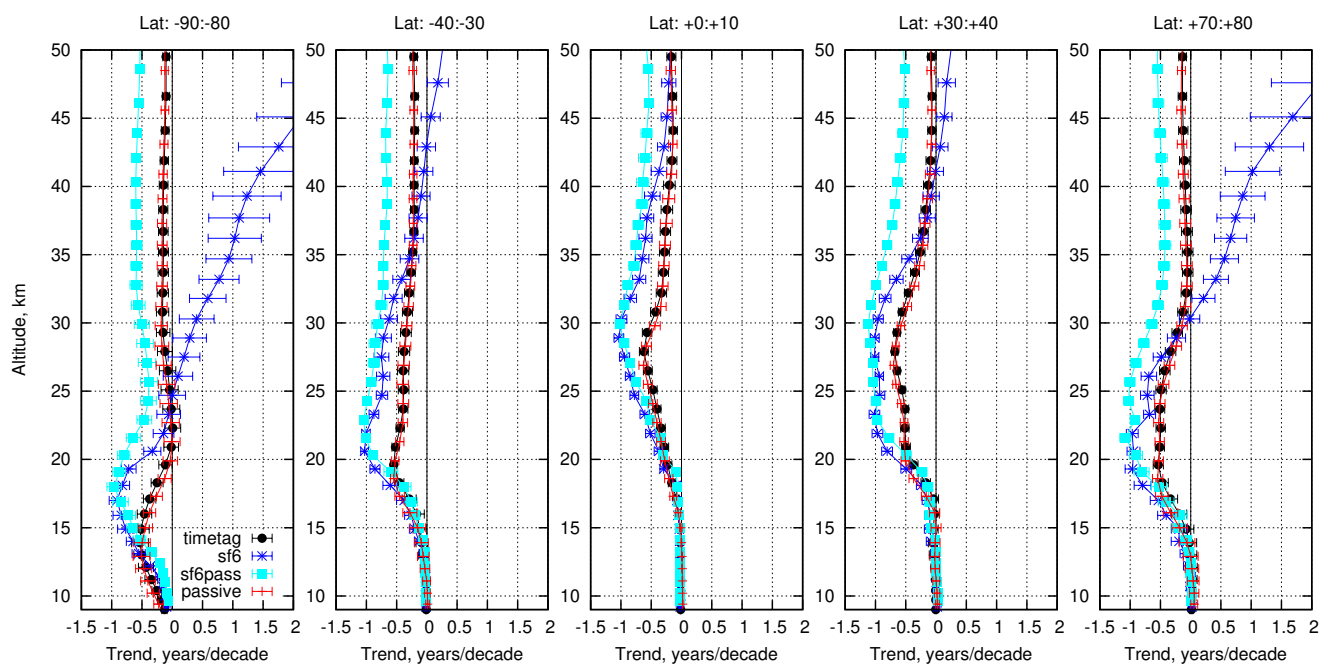


Figure 12. Vertical profiles of the simulated age of air linear trends over 2002-2012 for example latitude belts.