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Kesponse	to	reviewers

August 28, 2019

# **4** Summary:

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We thank both reviewers for their comments. As detailed in the point-by-point response below, we have done two
major modifications to the manuscript:

1. Now we explicitly take into account rain evaporation and horizontal advection in our model. These effects are described as simply as possible in the main text, and technical details are given in appendix. This allows us to rigorously quantify these effects on  $\delta D_0$  variations and to address all the related comments. This also simplifies the interpretation of  $r_{orig}$  variations. We also address explicitly the effect of rain evaporation and horizontal advection on  $z_{orig}$  estimates, and have modified our abstract and conclusion accordingly.

Now we better document and discuss the spatio-temporal variability of free tropospheric profiles. However,
 since this is not the core of the paper, and consistent with reviewer 1's suggestion, we have moved this
 discussion to the appendix.

## 15 1 Reviewer 1

16 We thank reviewer 1 for his/her comments.

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This paper presents an analytical steady state vertical mixing model to investigate the controls on the water 18 vapor isotopic composition in the subcloud layer over the tropical oceans. It is a nicely simple model that considers 19 the most important processes, which are surface evaporation and vertical mixing and predicts the subcloud layer 20 water vapour isotope composition from a combination of mass balance equations for all isotope species. I enjoyed 21 reading this paper very much, I particularly like the approach chosen for testing this analytical model, which 22 combines model simulation data and ship-based observations. The ideas presented in this paper are exciting and 23 very valuable for upcoming large field campaigns in which isotope observations are planned in different parts of the 24 lower troposphere. 25

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I thus recommend minor revisions with the following minor points:

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1) In the abstract it should be clearly stated that the proposed analytical model is a steady state formulation,
 which neglects horizontal gradients and thus the impact of horizontal advection.

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• Regarding the steady state formulation. Now we write in the abstract: "The model relies on the assumption that  $\delta D$  profiles are steeper than mixing lines, and that the SCL is at steady state, restricting its applications to time scales longer than daily."

• Regarding horizontal advection. Now we account for it explicitly. We write in the abstract: "We extend previous simple box models of the SCL by prescribing the shape of  $\delta D$  vertical profiles as a function of humidity profiles and by accounting for rain evaporation and horizontal advection effects."

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2) P. 1, L. 10: "When the air mixing into the SCL is lower in altitude it is moister": I think this is true most of
the time and certainly in a climatological sense, but of course when including differential advection elevated moist
layers can occur. I guess adding "it is generally moister" would make me very happy.

42 We modify as suggested.

- 3) P. 3, L. 4: Shouldn't cloud top cooling be mentioned here as well?
- We modify as: "driven by cloud-top radiative cooling, mixing and evaporative cooling of droplets"

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48 4) P. 5, L. 4: Neglecting the large-scale horizontal gradients in air properties, particularly in the trade wind
49 regions seems to me like a strong assumption. Given the sensitivity of dD to SST and the considerable SST gradient
50 across the North Atlantic, I find that this caveat could be discussed a bit more explicitly here.

<sup>52</sup> We agree that the neglect of horizontal advection was an important caveat. Therefore, now we rigorously <sup>53</sup> estimate the effect of horizontal advection of isotopic gradients on our results. This is detailed in section 2 in the <sup>54</sup> main text. Eq. (8) provides the new equation for  $R_0$  as a function of , the ratio of water vapor coming from <sup>55</sup> horizontal advection to that coming from surface evaporation, and  $\beta$ , the ratio of isotopic ratios of horizontal <sup>56</sup> advection to that of the SCL.

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Coming back to the effect of horizontal gradients in the North Atlantic: our figure 7h shows that the effect of horizontal advection is not stronger in the North Atlantic than elsewhere. But it is larger near the Saharan coast. A later comment from you can be used to explain this feature: section 4.1: "Horizontal advection is slightly enriching in deep convective regions and depleting in coastal regions (e.g. off the coasts of California, Peru, Mauritania, Namibia, India and Australia). For example, the Saharan layer in front of the North-Western African Coast leads to a strong effect of horizontal advection there ([Lacour et al., 2017]). "

5) P. 5, L. 20: "qs is the saturation specific humidity at SST"

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68 6) P. 6, L26: In the closure section and the discussion of the free tropospheric profile the role of horizontal 69 advection is again neglected. This is maybe a good assumption in the tropic but it should still be mentioned 70 explicitly.

<sup>71</sup> Now we account for the effect of horizontal advection on  $\delta D_0$  in our box model. However, our closure assumption <sup>72</sup> does not need to neglect horizontal advection. Horizontal advection effects are implicitely taken into account through <sup>73</sup> the  $\alpha_{eff}$ : we now clarify this: section 2.2: "Effects of horizontal advection and rain evaporation are encapsulated <sup>74</sup> into  $\alpha_{eff}$ . "

76 7) P. 8, L26: "Depending on microphysical details that are too complex to be addressed here", Graf et al. 2019 77 could be referenced here

We add this reference.

8) P. 9. Fig. 3: Which value was chosen for the SST? This could be mentioned in the caption as well as a reference to which equilibrium fractionation factor was used

We add this information in the caption: "For this illustrative purpose, we assume SST=30°C,  $h_0 = 0.8 \ \delta D_{oce} = 0\%$  and  $\phi = \eta = 0$ .". We also add it to Fig. 4.

9) P. 12, L. 2: "However, if the end member is defined below 500 hPa (e.g. 600 hPa), results are not always reasonable", why is this so?

Now we explain this in the text: section 3.3: "However, the end member should be defined above 500 hPa to ensure that it is well above boundary layer processes. If the end member is defined below 500 hPa (e.g. 600 hPa), there are a few cases where q increases with altitude  $(q_f > q_0)$  due to horizontal advection or convective detrainment from nearby moister regions. Meanwhile,  $\delta D$  decreases monotonically, leading to unrealistic values for  $\alpha_{eff}$ ."

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10) P. 12, L. 7: In my opinion, this makes it difficult to interpret rorig. But probably there are conditions when rorig and thus zorig are more physically meaningful than others. Could the authors maybe add a list with explicit and quantitatively expressed conditions in which they would argue that the assumptions involved in Eq. 9 are satisfied?

Now we explicitly account for rain evaporation and horizontal advection. Equations are given in the main text, so anyone can calculate these effects in their own cases. The contributions of these effects are plotted as maps in Fig. 7 g and h, and as composites as a function of  $\omega_{500}$  and EIS in Fig. 8. Table 2 compares the effect of  $r_{orig}$ if these effects are neglected or not. The effect of rain evaporation and horizontal advection on  $z_{orig}$  estimates are plotted in Fig. 14b.

Note that a list of conditions would not be easy, since the effect of rain evaporation depends on parameters  $\eta$ and  $\alpha_{evap}$  which are very difficult to estimate in nature, and horizontal advection depends on parameters  $\phi$  and  $\beta$ which are resolution-dependent and depend on several variables (wind, humidity and  $\delta D$  profiles in the SCL).

108 11) P. 13, L. 4-5: Is there a literature reference that the authors could indicated for this calculation of zi from 109 observations?

We now give several literature references and more explanation on this calculation method: section 3.4: "The 111 temperature inversion is an abrupt increase in temperature that caps the boundary layer. Therefore, a method 112 to automatically estimate its altitude is to detect a maximum in the vertical gradient of potential temperature 113 ([Stull, 1988, Oke, 1988, Sorbjan, 1989, Garratt, 1994, Siebert et al., 2000]). This method is sensitive to the res-114 olution of vertical profiles (Siebert et al., 2000, Seidel et al., 2010). Therefore, we adapted this method in order 115 to yield  $z_i$  values that best agree with what we would estimate from visual inspection of individual temperature 116 profiles. In LMDZ, we calculate  $z_i$  as the first level at which the vertical potential temperature gradient exceeds 117 3 times the moist-adiabatic lapse rate. In observations, we calculate  $z_i$  as the first level at which the vertical 118 potential temperature gradient exceeds 5 times the moist-adiabatic lapse rate, because radio-soundings are noisier 119 than simulated profiles. " 120

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## 122 12) P. 13, L. 15: I did not immediately understand what was meant by composites belonging to a given interval 123 of omega500, I was expecting a map. A reference to the results figure referred to here would have helped me.

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We now explain better how the composites are calculated, and we add a reference to Fig. 10 as an example. Section 3.5: "The type of clouds and mixing processes depends strongly on the large-scale velocity at 500 hPa ( $\omega_{500}$ , map shown in Fig. 6a), with shallow clouds in subsiding regions and deeper clouds in ascending regions (Fig. 1). Therefore, it is convenient to plot variables as composites as a function of  $\omega_{500}$  ([Bony et al., 2004]). To make such plots, we divide the  $\omega_{500}$  range from -30 to 50 hPa/d into intervals of 5 hPa/d. In each given interval, we average all seasonal-mean values at all locations over tropical oceans for which seasonal-mean  $\omega_{500}$  belongs to this interval (e.g. Fig. 10a will be an example).

The cloud cover strongly correlates with the inversion strength, which can be quantified by the Estimated Inversion Strength (EIS, [Wood and Bretherton, 2006], map shown in Fig. 6b) as a measure of inversion strength. We thus also plot variables as composites as a function of EIS. To make such plots, we divide the EIS range from -1 K to 9 K into intervals of 0.5K. In each given interval, we average all seasonal-mean values at all locations over tropical oceans for which seasonal-mean EIS belongs to this interval (e.g. Fig. 10b will be an example). "

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## 13) P. 13, L. 22: By how much (range of variability) were the four factors varied?

The four factors were varied from a control value to their simulated value.

Now we explain better the calculation with the contribution of  $r_{orig}$  as an example, and we give all equations 141 for other contributions in Table 1. Section 3.6: "To understand what controls the  $\delta D_0$  spatio-temporal variations, 142  $\delta D_0$  is decomposed into 4 contributions based on Eq. (8). First, we define  $r_{orig,bas} = 0.3$ ,  $\alpha_{eff,bas} = 1.09$ 143 ,  $SST_{bas}=25$ °C,  $h_{0,bas}=0.7$ ,  $\phi_{bas}=0$ ,  $\eta_{bas}=0$ ,  $\beta_{bas}=1$  and  $\alpha_{evap,bas}=1$  as a basic state. We call 144  $\delta D_{0,func}(r_{orig}, \alpha_{eff}, SST, h_0, \phi, \beta, \eta, \alpha_{evap})$  the function giving  $\delta D_0$  as a function of  $r_{orig}, \alpha_{eff}, SST, h_0, \phi, \beta, \eta$  and 145  $\alpha_{evap}$  following Eq. (8), and  $\delta D_{0,bas} = \delta D_{0,func}(r_{orig,bas}, \alpha_{eff,bas}, SST_{bas}, h_{0,bas}, \phi_{bas}, \beta_{bas}, \eta_{bas}, \alpha_{evap,bas})$ . The rel-146 ative contribution of  $r_{orig}$  to  $\delta D_0$  is estimated as  $\delta D_{0,func}(r_{orig}, \alpha_{eff,bas}, SST_{bas}, h_{0,bas}, \phi_{bas}, \beta_{bas}, \eta_{bas}, \alpha_{evap,bas}) - \delta D_0$ 147  $\delta D_{0,bas}$ . Similarly, the contributions of  $\alpha_{eff}$ , SST,  $h_0$ ,  $\phi$  and  $\eta$  are to  $\delta D_0$  are estimated as detailed in Table 1. All 148 the contributions have the same units as  $\delta D_0$  (‰).". 149 150

14) P. 14, Section 4.1: This section seemed very technical for me. I also see it more as a methodological aspect than a result. I would recommend to either shift it to a technical appendix (since the paper is quite long) or to the methods section.

We have now shifted this section to the appendix D.2. We have deeply modified this section to address comments from you and the other reviewer.

## 158 15) P. 15, Fig. 7: Mention that these are different random (?) grid points in the caption. I would have liked 159 a more general evaluation also describing the temporal and spatial variability in the vertical profiles simulation by 160 LMDZ.

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We have removed this figure, which was misleading, and replaced it by a more general documentation of the temporal and spatial variability in vertical profiles simulated by LMDZ, to address this comment and those from the other reviewer. This discussion is in appendix D: "LMDZ free tropospheric profiles". We add a figure showing maps of a parameter  $f = \frac{\delta D_{LMDZ} - \delta D_{Rayleigh}}{\delta D_{mix} - \delta D_{Rayleigh}}$  at 1000 m and 4000 m, representing how close is the simulated  $\delta D$ compared to the Rayleigh and mixing lines (Fig. 16b,d). This documents the spatial variability in the shape of  $\delta D$ profiles. To document the temporal variability, we add maps of the standard deviation of f (Fig. 16c,e).

## 16) P. 15, L. 3: could the authors mention the region where they think that alphaeff may also reflect horizontal advection effects?

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We now quantify the effect of horizontal advection on  $\delta D_0$ , i.e. in the SCL. However, the effect of horizontal advection on  $\alpha_{eff}$  is a completely different subject that is beyond the scope of this paper. Therefore, we only reply based on the litterature: in appendix D: "The pattern of  $\alpha_{eff}$  may also reflect horizontal advection effects, where strong isotopic gradients align with winds (e.g. from the Eastern to the Western Pacific, [Dee et al., 2018]). "

To clarify the scope of this paper, we start appendix D by stating: "The goal of this appendix is to document the spatio-temporal variability in the shape and steepness of simulated free tropospheric  $\delta D$  profiles. Note that a detailed interpretation of these profiles is beyond the scope of this paper. This paper aims at understanding  $\delta D_0$ , which is the first step towards understanding full tropospheric profiles. In turn, understanding full tropospheric profiles in future studies will help refine our model for  $\delta D_0$ ."

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17) P.16: I find it interesting that the mixing and Rayleigh lines have large biases in front of the eastern continental boundaries where the inversion is strongest and, where there is a strong decoupling between the FT and BL. In particular in these regions, I would expect horizontal advection to play a key role, (e.g. the SAL layer in front of the eastern North African Coast, see Lacour et al. 2017, ACP). Maybe the authors find a good way to shortly note this in the text.

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The map showing RMS errors was misleading. For example, if the simulated  $\delta D$  behaves smoothly and is halfway between Rayleigh lines and mixing lines, it will result in local maxima in RMS values, but when we plot the new parameter  $f = \frac{\delta D_{LMDZ} - \delta D_{Rayleigh}}{\delta D_{mix} - \delta D_{Rayleigh}}$ , representing how close is the simulated  $\delta D$  compared to the Rayleigh and mixing lines, nothing special emerges. This is the case in front of the Saharan coast. Therefore, we have not added this discussion here.

However, this comment is relevant for interpreting horizontal advection effects on  $\delta D_0$ : "Horizontal advection is slightly enriching in deep convective regions and depleting in coastal regions (e.g. off the coasts of California, Peru, Mauritania, Namibia, India and Australia). For example, the Saharan layer in front of the North-Western African Coast lead to a strong effect of horizontal advection ([Lacour et al., 2017])."

- 18) P. 17, L. 2: Maybe one could add oceanic upwelling and atmospheric deep convection. Jumping from upwelling to deep convection in the same sentence, I was not sure whether deep convection in the ocean or the atmosphere was meant here.
- 202 We modify as suggested.
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19) P. 17, L. 4: "Decreases as omega500 is more strongly ascending or descending" -> "with increasing vertical
 winds (omega500) of both signs"

We modify as suggested.

208 20) P. 17, L. 11: "in more ascending regions" -> a reference to Fig. 8d would have helped me here.

209 We add this reference

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- 21) P. 17, L. 25: "The fact that the effect..." I had difficulties to understand this sentence.
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We remove this sentence that was not so useful.

214 215 22) P. 17, L. 33:  $h_0$  (62%) is the largest explained fraction of all the variables considered and should thus be put 216 first. This could be a hint that large-scale horizontal advection plays an important role at the synoptic timescale 217 in these regions.

The numbers have changed because (1) we now account for rain evaporation and horizontal advection, and (2) we now add an additional condition to make our calculation: section 3.1: "to avoid numerical problems when estimating effect of horizontal advection and rain evaporation, only grid boxes and days where E > 0.5 mm/d are considered. This represents 99.7% of all tropical oceanic grid boxes."

With the new values, the effect of  $h_0$  is reduced and the effect of  $r_{orig}$  is enhanced (table 3). Section 4.1: "In subsiding regions, the effect of SST is muted due to its slow variability, and  $r_{orig}$  (82 %) becomes the main factor. "

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23) P. 19, Fig. 10: The bin sizes (number of data points per bin should be added).

We now add this information in Fig 8, and we write in the caption: "The number of samples in each bin is indicated on a logarithmic scale on the right-hand-side (dotted black line)."

If I understood correctly from the caption, the authors used the seasonal averaged fields from LMDZ. Why not
making these composites using the 6-hourly outputs? For me there is a timescale discrepancy between the processes
(mixing, evaporation) that the authors look at and the averaging timescale of the used fields.

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The composites are based on seasonal-mean EIS or  $\omega_{500}$  because this allows a better link with the large-scale 235 dynamical regime. Mixing and evaporation are processes that act at short time scales, but their relationship to the 236 large-scale circulation is best constrained by energetics at time scales longer than synoptic. Let's consider  $\omega_{500}$  for 237 example. It relates to convective activity and other diabatic processes through the conservation equation of moist 238 static energy. Adiabatic cooling by large-scale ascent balances latent heating by convection ([Yanai et al., 1973]). 239 or adiabatic heating by large-scale subsidence balances radiative cooling ([Emanuel et al., 1994]). The stationarity 240 in the conservation of moist static equation is most valid at time scales longer than synoptic, otherwise, the storage 241 term becomes important ([Masunaga and Sumi, 2017]). This is why in [Bony et al., 2004] and subsequent papers 242 (e.g. [Bony et al., 2013]) based on  $\omega_{500}$ , monthly-mean  $\omega_{500}$  is used, which yields similar results to seasonal-mean. 243 A similar rationale applies to EIS. This is why many papers on EIS use seasonal-mean values, notably the paper 244

defining this quantity ([Wood and Bretherton, 2006]).

We now explain this in section 3.5: "Note that such composites are done on seasonal-mean  $\omega_{500}$  because cloud processes and their associated diabatic heating are tied to the large-scale circulation through energetic constrains ([Yanai et al., 1973, Emanuel et al., 1994]) that are best valid at longer time scales (otherwise, the energy storage term may become significant, e.g. [Masunaga and Sumi, 2017]). This is why  $\omega_{500}$  is generally averaged over a month or longer (e.g. [Bony et al., 1997, Williams et al., 2003, Bony et al., 2004, Wyant et al., 2006, Bony et al., 2013]). In addition, we primarily focus on understanding the seasonal and spatial distribution of  $\delta D_0$ ."

and for EIS: "Using seasonal-mean values is consistent with [Wood and Bretherton, 2006] and with the better link at longer time scales between cloud processes and the large-scale dynamical regime.".

In addition, we do not look at the diurnal variations: the stationarity assumption in our simple model would be violated. We now explain this in the abstract: "the steady-state assumption restricts the application of this model to time scales longer than daily." and in section 2.1: "We assume that the SCL is at steady state. For example, its depth is constant. Since the SCL properties may exhibit a diurnal cycle ([Duynkerke et al., 2004]), this hypothesis restricts the application of this model to time scales longer than daily. "

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262 24) P. 27, L. 28: a reference to a more technical paper such as Aemisegger et al. 2012 AMT, would be nice here.
263 We add this reference

## 264 Small technical comments:

265 1) P. 2, L. 22 : "suffers from a low bias"

- 266 2) P. 3, L. 28: "capturing the second-order..."
- 3) P. 8, L. 26: no parenthesis after B)
- 268 4) P. 12, L.7: "based" -> "biased"
- 269 5) P. 15, L. 1: Figure 8d
- 270 6) P. 15, L. 4: "Values of alphaeff..."
- 7) P. 15, L. 5: using a fractionation coefficient alpha eq as a function of temperature
- 8) P. 17, L. 14: space missing between rorig and (
- 273 9) P. 18, L. 1: "Overall, the results..."
- 274 We correct all these mistakes.
- 10) In general, the authors do not consistently use B15 for Benetti et al. (2015)
- We now use B15 consistently.
- 11) P. 21, L. 2: "with the strongest inversion"
- 279 12) P. 27, L. 27: measurement errors
- 280 13) P. 28, L. 2: "if we measure..."
- 281 14) P. 29, L. 14: very precise
- 15) P. 30, L. 11: from which altitude the air comes
- We correct all these mistakes.

## 284 2 Reviewer 2

<sup>285</sup> We thank reviewer 2 for his/her comments.

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This paper presents a simple box model solving the water isotope budget in the sub-cloud layer to quantify the 287 relative contributions of sea surface temperature, relative humidity, mid-tropospheric depletion, and the fraction 288 of moisture from the free troposphere (rorig) on the variability of  $\delta D$  in near-surface water vapor ( $\delta D_0$ ). The 289 contribution of  $r_{orig}$  is further separated into contributions of specific humidity at the surface, and the height 290  $(z_{orig})$ , relative humidity and temperature from which the free tropospheric air originates. Zorigis found to be an 291 important factor explaining the seasonal-spatial and daily variations of  $\delta D_0$ . This means that measurements of 292  $D\delta 0$ , if precise enough, can potentially be used to estimate  $z_{orig}$  and distinguish between different mixing processes 293 in the atmosphere. 294

The paper is interesting and well written, and it nicely demonstrates the use of measuring water vapor isotopes on short time scales. The box model's theoretical framework is described in detail and its drawbacks are clearly identified by the authors. I only have a few comments about the methods, the rest are mainly ideas for clarifying the paper. I recommend that the paper be published after minor revisions.

## **299** General comments

1) I like the method for quantifying the contributions of different factors by linear regression. I see how this works
when the contributing factors have the same units as the variable of interest, which was the case in the previous
studies that used this method and are cited in this paper (Risi et al. 2010, Oueslati et al., 2016). Here the different
factors all have different units, and the slope therefore depends on the units, or how much the components vary. I
assume this was accounted for somehow, as the slopes in the tables are all unitless, but it is not clear from the text,
and makes me a bit skeptical about the results. More explanation on that would be useful.

The contributing factors have the same units as the variable of interest, i.e. permil. We now clarify this 307 in the text. We also explain better the calculation with the contribution of  $r_{orig}$  as an example, and we give 308 all equations for other contributions in Table 1. Section 3.6: "To understand what controls the  $\delta D_0$  spatio-309 temporal variations,  $\delta D_0$  is decomposed into 4 contributions based on Eq. (8). First, we define  $r_{orig,bas} = 0.3$ , 310  $\alpha_{eff,bas} = 1.09$ ,  $SST_{bas} = 25$ °C,  $h_{0,bas} = 0.7$ ,  $\phi_{bas} = 0$ ,  $\eta_{bas} = 0$ ,  $\beta_{bas} = 1$  and  $\alpha_{evap,bas} = 1$  as a basic state. We call 311  $\delta D_{0,func}(r_{orig}, \alpha_{eff}, SST, h_0, \phi, \beta, \eta, \alpha_{evap})$  the function giving  $\delta D_0$  as a function of  $r_{orig}, \alpha_{eff}, SST, h_0, \phi, \beta, \eta$  and 312  $\alpha_{evap}$  following Eq. (8), and  $\delta D_{0,bas} = \delta D_{0,func}(r_{orig,bas}, \alpha_{eff,bas}, SST_{bas}, h_{0,bas}, \phi_{bas}, \beta_{bas}, \eta_{bas}, \alpha_{evap,bas})$ . The rel-313 ative contribution of  $r_{orig}$  to  $\delta D_0$  is estimated as  $\delta D_{0,func}(r_{orig}, \alpha_{eff,bas}, SST_{bas}, h_{0,bas}, \phi_{bas}, \beta_{bas}, \eta_{bas}, \alpha_{evap,bas})$  – 314  $\delta D_{0,bas}$ . Similarly, the contributions of  $\alpha_{eff}$ , SST,  $h_0$ ,  $\phi$  and  $\eta$  are to  $\delta D_0$  are estimated as detailed in Table 1. All 315 the contributions have the same units as  $\delta D_0$  (‰).". 316

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2) As stated in the paper, the methods rely on the assumption that the  $\delta D$  profile follows a Rayleigh-like line, and that there is no effect of rain evaporation. Figures 7 and 8 show that the  $\delta D$  profile is often closer to a mixing line than a Rayleigh line, and the large contribution of  $r_{orig}$  mainly comes from ascending regions, where clouds are most likely precipitating. It would be nice to see some quantification of how this impacts the results. A possible way to do this is to remove days/locations where the RMSE of the mixing line is smaller than the RMSE of the Rayleigh line and where there is precipitation, then repeat the analysis for these new fields and add the results in brackets in Tables 1, 2 and as dotted lines in Figures 10, 12.

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• Effect of rain evaporation. Now we explicitly account for the effect of rain evaporation. Equations are given in the main text. The contributions of this effect are plotted as maps in Fig. 7g, and as composites as a function of  $\omega_{500}$  and EIS in Fig. 8. Table 2 compares the effect of  $r_{orig}$  if rain evaporation and horizontal advection are neglected or not. The effect of rain evaporation on  $z_{orig}$  estimates are plotted in Fig. 14b.

• Effect of the deviation of the  $\delta D$  profile from a Rayleigh distillation line. This is more difficult to quantify. Now 330 we discuss this in detail in the discussion section: subsection 6.5 untitled "Rayleigh assumption for the shape of 331  $\delta D$  profiles": "Finally, a fifth source of uncertainty comes the assumption that the  $\delta D$  profile follows a Rayleigh 332 distillation line (section 2.2). However, both in LMDZ (appendix D) and nature ([Sodemann et al., 2017]), 333  $\delta D$  profiles are usually intermediate between Rayleigh and mixing lines. The precision of our  $z_{orig}$  estimate is 334 maximum in the Rayleigh distillation case. When trying to directly find a numerical solution for  $z_{orig}$  from Eq. 335 (6), a solution can be found only in 0.1 % of cases. This is because... However, it is possible that  $\delta D$  profiles 336 simulated by LMDZ are closer to mixing lines than real profiles, since GCMs are known to overestimate vertical 337 mixing through the troposphere ([Risi et al., 2012]) and to mix the lower free troposphere too frequently by 338 deep convection in trade-wind regions ([Nuijens et al., 2015b, Nuijens et al., 2015a]). Therefore, the shape of 339  $\delta D$  profiles simulated by LMDZ is not a sufficient reason to reject the Rayleigh assumption. The uncertainty 340 associated with this assumption is very difficult to quantify in LMDZ. More measurements of full  $\delta D$  profiles 341 are very welcome to help quantify it." 342

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3) The paper presents the new box model as an extension of the model by Benetti et al. (2015), which is technically true, but can be a bit misleading because its application is different. Rather than predicting  $\delta D_0$  from zorig, it predicts  $z_{orig}$  from  $\delta D_0$  and therefore requires  $\delta D_0$  to be known. This means it cannot be applied to initialize Rayleigh models like the model by Benetti et al. (2015), which assumes constant zorig. This could be written more clearly (e.g., from the abstract it seems like the model can be used to predict  $\delta D_0$ , which is only possible if  $z_{orig}$  is known).

The model can be used both ways, either to predict  $\delta D_0$  as a function of  $z_{orig}$ , or to estimate  $z_{orig}$  from  $\delta D_0$ . We now clarify this:

• in the abstract: "The model express  $\delta D_0$  as a function of  $z_{orig}$ , humidity and temperature profiles, surface conditions a parameter describing the steepness of the  $\delta D$  vertical gradient and a few parameters describing rain evaporation and horizontal advection effects.".

• in section 2.2: "If the goal is to predict  $R_0$  from  $z_{orig}$ , we can apply Eq. (6) if we know the q and  $\delta D$  vertical profiles. Conversely, if the goal is to predict  $z_{orig}$  from  $R_0$ , we can numerically solve Eq. (6) if we know the qand  $\delta D$  vertical profiles."

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4) Changing some of the colors and colormaps could make the figures easier to understand. For example, I think the contributions of different factors and how they add up in Figures 9 and 11 would be more intuitive with a perceptually uniform colormap going from light to dark colors. Also, the red and pink lines in Figures 3, 4, 7, 10, 12, 15 look very similar to each other. It would be good to use a different color for one of them.

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- Now all maps are colored in shaded of blue for negative values and shaded of red for positive values.

• We now change the line color from pink to purple to distinguish it from red (Figures 3, 4, 5), or from red to dark red to distinguish it from pink (Figures 8, 10, 13).

# 368 Specific comments

369 370	P1 L13: [D]/[H] instead of [HDO]/[H2O] We modify.
371 372 373	P2 L22: high bias instead of low bias? Corrected.
374 375 376	P2 L30: Please introduce the abbreviation for LCL Done.
377 378 379	P3 L4: pointed <b>out</b> the important role Corrected.
380 381 382	P3 L15: "We do not call it entrained": The word entrained/entrainment still appears a few times in the text (e.g. in Fig. 2, the title of section 4.4)
383	We modify all the occurences of "entrainment", except when it really refers to entrainment.
385 386	P3 L23: during <b>a</b> field campaign, global outputs <b>of</b> an isotope-enabled GCM. Corrected.
387 388 389 390 391	P3 L24: "at the global scale": Really? There are no global maps. Are the numbers in Tables 1, 2 and the lines in Figures 10, 12 from global output, or from the region shown on the maps? We now modify by "in the Tropics". We precise in the captions for these Tables and Figures: "All seasons and locations over tropical oceans $(30^{\circ}N - 30^{\circ}S)$ , ocean fraction>80%) are considered."
392 393 394	P3 L28: capturing <b>the</b> second-order parameter d-excess Corrected.
395 396 397 398 399	P3 L32: "MJ79 already performs quite well for d-excess": Pfahl and Wernli (2009) would probably disagree. Now we modify as (section 1.3): "In addition, the need for an extension of MJ79 is more needed for $\delta D$ than for d-excess, since the effect of convective mixing is larger on $\delta D$ than on d-excess ([Risi et al., 2010, Benetti et al., 2014]).". This does not contradict Pfahl and Wernli (2009).
4 00 4 01 4 02	P5 L23: $r \rightarrow r_{orig}$ Corrected.
4 03 4 04 4 05	P6 L20: measurements Corrected.
4 06 4 07 4 08	P6 L20: "Therefore, variations of $\delta D_0$ that are mediated by $q_0$ or $h_0$ do not interest us": But $\delta D$ in the FT is prescribed as a function of q (confusing).
409 410 411	We remove this confusing sentence and we write (section 2.1): "We attempt to express neither $h_0$ as a function of $q_0$ as in B15, and nor the $q$ profile as a function of $q_0$ ".
412 413	P8 L11: Refer to l'Hopital's rule? Now we add: "(L'Hopital's rule was used to calculate this limit)." (section 2.2°
414 415 416 417	P8 L21: follows as mixing line Corrected.
418 419 420	P9: Fig.3: $\alpha_{eff} = \alpha_{eq}$ instead of $\alpha_{eff} = 1/\alpha_{eq}$ Corrected.
421	P11 L25: "Only profiles during the ascending phase of the balloons are considered": (Why?)

We now justify this choice: "Only profiles during the ascending phase of the balloon are considered, because the descent phase is often located far away from the initial launch point ([McGrath et al., 2006, Seidel et al., 2011]). " (section 3.2)

## P11 L27 (title): write somewhere that these results are based on LMDZ output (not observations)

Now we write (section 3.3): "Here we explain how  $z_{orig}$  is estimated based on LMDZ outputs.". Later in the section, we write: "When estimating  $z_{orig}$  from observations, we follow the same methodology except that...".

<sup>431</sup> P12 Fig. 5: Describe abbreviations (LCL, EIS, SCL) in caption.

432 Done

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P12 L2: "if the end member is defined below 500hPa (e.g. 600hPa) results are not always reasonable": In what sense? Why?

Now we write: "However, the end member should be defined above 500 hPa to ensure that it is well above boundary layer processes. If the end member is defined below 500 hPa (e.g. 600 hPa), there are cases where qincreases with altitude ( $q_f > q_0$ ) due to horizontal advection or convective detrainment from nearby moister regions; meanwhile,  $\delta D$  decreases monotically, leading to unrealistic values for  $\alpha_{eff}$ ."

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P15 Fig. 7: What meteorological conditions do these examples represent? Would it be possible to show all (/more) simulated profiles in the background, e.g. in some transparent color, to get a better feeling for the variability? Also, I suggest adding markers to highlight where the levels are.

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We have removed this figure, because it was misleading. We replace it by Fig. 16 in appendix D to better document the temporal and spatial variability in free tropospheric profiles. Maps show parameter  $f = \frac{\delta D_{LMDZ} - \delta D_{Rayleigh}}{\delta D_{mix} - \delta D_{Rayleigh}}$ describing whether simulated  $\delta D$  is closer to Rayleigh line or a mixing line (Fig 16b,d). We also show maps for the standard deviation of f to illustrate the temporal variability (Fig 16 c,e).

In addition, markers are added in Fig 16a to highlight the model levels.

- <sup>451</sup> P15 L1: Figure 8d instead of 8c.
- 452 Corrected
- 454 P15 L5:  $\alpha_{eq}$  as a function of temperature
- 455 Corrected
- <sup>457</sup> P16 Fig. 8: in **boreal** winters of all years
- 458 Corrected
- <sup>460</sup> P17 L22: "in the cold upwelling regions": for example where?
- Now we add: "cold upwelling regions, for example off Peru or Namibia" (section 4.1)
- 463 P17 L23: probably reflects
- This sentence was removed because  $r_{orig}$  cannot reflect rain evaporation any more.

P17 L24: "the effect of  $r_{orig}$  can be seen on the composites as a function of EIS and not as a function of  $\omega_{500}$ ": I don't see this, please elaborate.

- This sentence was removed.
- 470
- 471 P17 L30: followed by  $h_0$  (23%),  $r_{orig}$  (16%), ...
- 472 Corrected
- 473474 P18 Fig. 9: Are the correlations significant everywhere? Otherwise, add hatching where not significant?
- 4 7 5

In this figure (now Fig. 7), we do not show the correlations, but rather the contributions to  $\delta D_0$  on a % scale. We now explain better in the text how these contributions are calculated (section 3.6), and we add table 1 to give the exact equations used to calculate each contribution.

The spatial-seasonal correlations are shown in Table 2. We now write between brackets when correlations are 479 not statistically significant at 99%. We write in the caption: "The threshold for the correlation coefficient to be 480 statistically significant at 99 % is 0.15 or lower in all cases. We write correlation coefficient and slope values between 4 81 brackets when they are not significant at 99%." 482 483 P19 Fig.10:  $\omega_{500}$  (hPa/d) 4 84 Corrected 485 486 P20 Tab. 2:  $q_0$  seems to be important in Fig. 12, but the slope is 0.0 here,  $h_0$  seems to be unimportant in Fig. 487 12 but slope is 0.91 here. Why is that? 488 We now explain this: section 4.2: "Note that this effect can be seen only in most stable regions, but when 489 considering all subsiding regions, the contribution is small (Table 2). " 490 4 91 P20 L1: "it would translate into a lower zorig.": Why? 492 493 For example, in case of deep convection with depleting rain evaporation, a larger  $r_{orig}$  is necessary to match the 4 94 depleted  $\delta D_0$ , and a lower  $z_{orig}$  is necessary to match this large  $r_{orig}$ . 495 Now this sentence is removed, since we explicitly account for rain evaporation and horizontal advection. We 496 do not need this kind of rationale any more. 497 498 P22 Fig.12:  $\omega_{500}(hPa/d)$ 499 Corrected 500 5 01 P25 L6: the cruises goes 502 Corrected 503 5 04 P25 L8: "when considering only the 6 data points when  $z_{orig} < 2000$ m": Rationale behind this? 5 0 5 506 We now clarify what we mean: section 5: "Remarkably, there are 6 days when  $z_{orig}$  coincides with  $z_i$  with a root 507 means square error of 31% and correlation coefficient of 0.996 (Fig. 15c). This indicates that the air exactly comes 508 from the inversion layer. When recalling that  $z_{orig}$  and  $z_i$  are estimated from completely independent observations, 509 the coincidence is remarkable and lends support to the fact that on these days, our  $z_{orig}$  estimate is physical. 510 However, there remains 9 days when  $z_{orig}$  is much higher than  $z_i$ . This may reflect more penetrative downdrafts as 511 we approach deeper convective regimes. But it may also be an artifact of our neglect of horizontal advection. For 512 example, on these days which are characterized by lower  $h_0$ , neglecting the advection of enriched water vapor from 513 nearby regions with higher  $h_0$  could be mis-interpreted as lower  $r_{orig}$  and thus higher  $z_{orig}$ .". 514 515 P25 L14: ... at the seasonal-spatial and daily scale is the proportion of the water vapor in the SCL that is 516 originates from above 517 Corrected 518 519 P26 Fig. 15:  $r \rightarrow r_{orig}$ 520 Corrected 521 522 P27 L1: there  $\rightarrow$  they 523 Corrected

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<sup>526</sup> P27 L13: the **temporal** variability of  $\alpha_{eff}$ . Is it possible to estimate the uncertainty from the spatial variability <sup>527</sup> of  $\alpha_{eff}$  as well (in the vertical, i.e. how much the  $\delta$  profile differs from a Rayleigh line with constant  $\alpha_{eff}$ )?

528

We now better document the spatio-temporal variability in the shape of free tropospheric  $\delta D$  profiles in the appendix D.1. To address this specific comment, we now plot parameter  $f = \frac{\delta D_{LMDZ} - \delta D_{Rayleigh}}{\delta D_{mix} - \delta D_{Rayleigh}}$  describing whether simulated  $\delta D$  is closer to Rayleigh line or a mixing line. We show vertical profiles and maps of f at both 1000 m and 4000 m (Fig 16 b,d).

<sup>533</sup> We tried to compare the  $z_{orig}$  estimate with and without the assumption that the  $\delta D$  profile follows a Rayleigh <sup>534</sup> line. However, it didn't work as well as expected. We now explain this when examining all errors on  $z_{orig}$  (section <sup>535</sup> 6.5): "When trying to find a numerical solution for  $z_{orig}$  directly from Eq. (6), a solution can be found only in <sup>536</sup> 0.1 % of cases.". We explain why, and we also explain why it may work better in nature.

537

<sup>538</sup> P27 L21: estimating  $z_{orig}$  from  $\delta D_0$  measurements on a daily basis (?)

Now we write: "estimating  $z_{orig}$  from daily  $\delta D_0$  measurements cannot be useful unless we measure  $\delta D$  profiles on a daily basis as well."

542 P28 L2: and if we measure 543 Corrected 544 545 P28 L3: swap trade-wind cumulus and strato-cumulus clouds 546 Corrected 547 548 P29 L14: very precised estimates 549 Corrected 550 551 P29 L18: the altitude from which the air is originates, and is not to biased by 552

553 Corrected

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# Controls on the water vapor isotopic composition near the surface of tropical oceans and role of boundary layer mixing processes

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Abstract. Understanding what controls the water vapor isotopic composition of the sub-cloud layer (SCL) over tropical oceans  $(\delta D_0)$  is a first step towards understanding the water vapor isotopic composition everywhere in the troposphere. We propose an analytical model to predict  $\delta D_0$  as a function of sea surface conditions, humidity and temperature profiles, and the motivated by the hypothesis that the altitude from which the free tropospheric air originates  $(z_{orig})$ . To do so, we extend previous studies by

- 5 (1) is an important factor: when the air mixing into the SCL is lower in altitude, it is generally moister, and thus it depletes more efficiently the SCL. We extend previous simple box models of the SCL by prescribing the shape of  $\delta D$  vertical profiles , and (2) linking  $\delta D_0$  to  $z_{orig}$  as a function of humidity profiles and by accounting for rain evaporation and horizontal advection effects. The model relies on the hypotheses assumption that  $\delta D$  profiles are steeper than mixing linesand no clouds are precipitating, and that the SCL is at steady state, restricting its applications to time scales longer than daily. The model express  $\delta D_0$  as a
- 10 function of  $z_{orig}$ , humidity and temperature profiles, surface conditions, a parameter describing the steepness of the  $\delta D$  vertical gradient and a few parameters describing rain evaporation and horizontal advection effects. We show that  $\delta D_0$  does not depend on the intensity of entrainment, dampening hope that  $\delta D_0$  measurements could help constrain this long-searched quantity.

Based on an isotope-enabled general circulation model simulation, we show that  $\delta D_0$  variations are mainly controlled by mid-tropospheric depletion and rain evaporation in ascending regions, and by sea surface temperature and  $z_{orig}$  in subsiding regions. When the air mixing into the SCL is lower in altitude, it is moister, and thus it depletes more efficiently the SCL.

In turn, could  $\delta D_0$  measurements help estimate  $z_{orig}$  and thus discriminate between different mixing processes? Estimates that are accurate enough For such isotope-based estimates of  $z_{orig}$  to be useful would be difficult to achieve in practice, requiring measuring daily, we would need a precision of a few hundreds meters in deep convective regions and smaller than 20 m in strato-cumulus regions. To reach this target, we would need daily measurements of  $\delta D$  profiles, and measuring in the

20 mid-troposphere and accurate measurements of  $\delta D_0$  with an accuracy of (accuracy down to 0.1 ‰ and 0.4 ‰ in trade-wind cumulus and in the case of strato-cumulus clouds, which is currently difficult to obtain). We would also need information on the horizontal distribution of  $\delta D$  to account for horizontal advection effects, and full  $\delta D$  profiles to quantify the uncertainty associated with the assumed shape for  $\delta D$  profiles. Finally, rain evaporation is an issue in all regimes, even in strato-cumulus cloudsrespectively. Innovative techniques would need to be developed to quantify this effect from observations. Copyright statement.

#### **1** Introduction

#### 1.1 What controls the water vapor isotopic composition?

The water vapor isotopic composition (e.g.  $\delta D = (R/R_{SMOW} - 1) \times 1000$  expressed in ‰, where  $R = HDO/H_2O$  R is

- 5 the D/H ratio and SMOW is the Standard Mean Ocean Water reference) has been shown to be sensitive to a wide range of atmospheric processes (Galewsky et al., 2016), such as continental recycling (Salati et al., 1979; Risi et al., 2013), unsaturated downdrafts (Risi et al., 2008, 2010a), rain evaporation (Worden et al., 2007; Field et al., 2010), the degree of organization of convection (Lawrence et al., 2004; Tremoy et al., 2014), the convective depth (Lacour et al., 2017b), the proportion of precipitation that occurs as convective or large-scale precipitation (Lee et al., 2009; Kurita, 2013; Aggarwal et al., 2016), vertical
- 10 mixing in the lower troposphere (Benetti et al., 2015; Galewsky, 2018a, b), mid-troposphere (Risi et al., 2012b) or uppertroposphere (Galewsky and Samuels-Crow, 2014), convective detrainment (Moyer et al., 1996; Webster and Heymsfield, 2003), ice microphysics (Bolot et al., 2013). It is therefore very challenging to quantitatively understand what controls the isotopic composition of water vapor.
- A first step towards this goal is to understand what controls the water vapor isotopic composition in the sub-cloud layer (SCL) of tropical (30°S-30°N) oceans. Indeed, this water vapor is a an important source moistening air masses traveling to land regions (Gimeno et al., 2010; Ent and Savenije, 2013) and towards higher latitudes (Ciais et al., 1995; Delaygue et al., 2000). It is also ultimately the only source of water vapor in the tropical free troposphere, since water vapor in the free troposphere ultimately originates from convective detrainment (Sherwood, 1996), and convection ultimately feeds from the SCL air (Bony et al., 2008). Therefore, the water vapor isotopic composition in the SCL of tropical oceans serves as initial
- 20 conditions to understand the isotopic composition in land waters and in the tropospheric water vapor everywhere on Earth. We focus here on the SCL because, by definition, there is no complication by cloud condensation processes.

The goal of this paper is thus to propose a simple analytical equation that allows us to understand and quantify the factors controlling the  $\delta D$  in the water vapor in the SCL of tropical oceans. So far, the most famous analytical equation for this purpose has been the closure equation developed by Merlivat and Jouzel (1979)-Merlivat and Jouzel (1979). This closure equa-

- 25 tion can be derived by assuming that all the water vapor in the SCL air originates from surface evaporation. The water balance of the SCL can be closed by assuming a mass export at the SCL top (e.g. by convective mass fluxes) and a totally dry entrainment into the SCL to compensate this mass export. The MJ79 equation has proved very useful to capture the sensitivity of  $\delta D$  and second-order parameter d-excess to sea-surface conditions (Merlivat and Jouzel, 1979; Ciais et al., 1995; Risi et al., 2010d) Merlivat and Jouzel (1979); Ciais et al. (1995); Risi et al. (2010d). However, the  $\delta D$  calculated from this equation suffers a low
- 30 from a high bias in tropical regions (Jouzel and Koster, 1996)Jouzel and Koster (1996). This bias can be explained by the neglect of vertical mixing between the SCL and air entrained from the free troposphere (FT). The MJ79 equation can better reproduce surface water vapor observation when extended to take into account this mixing (Benetti et al., 2015)(Benetti et al. (2015) , hereafter B15). However, this This extension requires to know the specific humidity (q) and water vapor  $\delta D$  of the entrained

air, which are often unknown. In addition, they assumed. To get these values, they assume that the air entrained into the boundary layer comes from a constant altitude, which does not reflects. However, this does not reflect the complexity of entrainment and mixing processes in marine boundary layers.

#### 1.2 Entrainment and mixing mechanisms

- 5 Figure 1 summarizes our knowledge about these entrainment and mixing processes. In strato-cumulus regions, clouds are thin and the inversion is just above the LCL lifting condensation level (LCL). Air is entrained from the FT by cloud-top entrainment driven by radiative cooling or wind shear instabilities (Mellado, 2017), possibly amplified by evaporative cooling of droplets (Lozar and Mellado, 2015). Both Direct Numerical Simulations (Mellado, 2017) and observations of tracers (Faloona et al., 2005) and cloud holes (Gerber et al., 2005) show that air is entrained from a thin layer above the inversion, thinner than 80m
- 10 and as small as 5m. The boundary layer itself is animated by updrafts, downdrafts and associated turbulent shells that bring air from the cloud layer downward (Brient et al., 2019; Davini et al., 2017).

In trade-wind cumulus regions, the cloudy layer is a bit deeper. Observational studies and large-eddy simulations have pointed <u>out</u> the important role of thin subsiding shells around cumulus clouds, driven by <u>cloud-top radiative cooling</u>, mixing and evaporative cooling of droplets (Jonas, 1990; Rodts et al., 2003; Heus and Jonker, 2008; Heus et al., 2009; Park et al., 2016). This beinge air from the elevely layer to the SCL. Subsiding shells mere also serve successes a substantian relevance of the survey layer.

15 2016). This brings air from the cloudy layer to the SCL. Subsiding shells may also cover overshooting plumes of the cumulus clouds, entraining FT air into the cloud layer (Heus and Jonker, 2008).

In deep convective regions, unsaturated downdrafts driven by rain evaporation (Zipser, 1977) are known to contribute significantly to the energy budget of the SCL (Emanuel et al., 1994). Large-eddy simulations show that subsiding shells, similar to those documented in shallow convection, also exist around deep convective clouds (Glenn and Krueger, 2014). In the clear-sky

20 environment between clouds, turbulent entrainment into the SCL may also play a significant role (Thayer-Calder and Randall, 2015).

Therefore, whatever the cloud regime, air entering the SCL from above may originate either from the cloud layer or from the free troposphere, depending on the mixing mechanism. Therefore, in this paper in contrast with Benetti et al. (2015). Benetti et al. (2015), we let the altitude from which the air originates,  $z_{orig}$ , be variable. We do not call it "entrained" air because entrainment sometimes refer to mixing processes through an interface (e.g. De Roov et al. (2013); Davini et al. (2017)

25 because entrainment sometimes refer to mixing processes through an interface (e.g. De Rooy et al. (2013); Davini et al. (2017) De Rooy et al. (2013); Davini et al. (2017)), whereas air in the SCL may also enter through deep, coherent and penetrative structures such as unsaturated downdrafts. We do not call it FT air either, since it may originate from the cloudy layer.

#### **1.3** Goal of the article

To acknowledge the diversity and complexity of mixing mechanisms, we extend the B15 framework in two several ways. First,

30 we assume that we know the relationship between shape of  $\delta D$  and profiles as a function of *q* in the FT, which allows us to get rid of one unknown. Second, we write the specific humidity of the air originating from above the SCL as a function of  $z_{orig}$ . Third, we account for rain evaporation and horizontal effects.



Figure 1. Schematics showing the different types of clouds and mixing processes as a function of the large-scale circulation.

While B15 focused on observations during a field campaign, we also apply the extended equation to global outputs of an isotope-enabled general circulation model, with the aim to quantify the different factors controlling the  $\delta D$  variability at the global scale in the Tropics. The variable  $z_{orig}$  will emerge as an important factor. Therefore, we discuss the possibility that  $\delta D$ measurements at the near surface and through the lower FT could help estimate  $z_{orig}$ , and thus the mixing processes between the SCL and the air above.

5

Note that we focus on  $\delta D$  only. Results for  $\delta^{18}O$  are similar. We do not aim at capturing the second-order parameter dexcess, because our model requires some knowledge about free tropospheric vertical profiles of isotopic composition. While  $\delta D$  is known to decrease with altitude (Ehhalt, 1974; Ehhalt et al., 2005; Sodemann et al., 2017), vertical profiles of d-excess are more diverse and less well understood (Sodemann et al., 2017)). In addition, the need for an extension of MJ79 is more

needed for  $\delta D$  than for d-excess<del>anyway, since MJ79 already performs quite well for</del>, since the effect of convective mixing is 10 larger on  $\delta D$  than on d-excess (Risi et al., 2010d; Benetti et al., 2014).

#### **Theoretical framework** 2

#### Assumptions leading to the Benetti et al 2015 equationBox model and budget equations 2.1

In this section, we recall how the equation in Benetti et al. (2014) Building on Benetti et al. (2014) and B15was derived and explicit all underlying assumptions.

We, we consider a simple box representing the SCL (Fig. 2). We assume that the air may come comes from above (M) or from the and from the incoming large-scale horizontal convergence (D < 0 advection ( $F_{adv}$ ), and is exported through the SCL

5 top (N, e.g. turbulent mixing or convective mass flux) or and by outgoing large-scale horizontal divergence (D > 0 advection ( $F_{adv,out}$ ). We assume that the SCL is at steady state. In particularFor example, its depth is constant. Since the SCL properties may exhibit a diurnal cycle (Duynkerke et al., 2004), this hypothesis restricts the application of this model to time scales longer than daily. The air mass budget of the SCL thus writes:

$$M + \underline{F}_{adv} = N + \underline{D} \underline{F}_{adv,out} \tag{1}$$

10 These fluxes also transport water vapor and isotopes. In addition, surface evaporation E imports and rain evaporation  $F_{evap}$ import water vapor and isotopes (Fig. 2). We neglect import of water vapor and isotopes by rain evaporation (Albrecht, 1993) and will test the sensitivity to this effect in appendix B.

Hereafter, to simplify equations, we use the isotopic ratio R instead of  $\delta D$ .

- The SCL is usually well-mixed (Betts and Ridgway, 1989; Stevens, 2006; De Roode et al., 2016), so that we can . We 15 thus assume that the humidity and isotopic properties are constant vertically and horizontally in the SCL. They are noted ( $q_0$ ,  $R_0$ ). The humidity and isotopic properties of the mass flux export N are thus also ( $q_0$ ,  $R_0$ ). In case of net horizontal divergence (D > 0), the The properties of the divergence flux are also ( $q_0$ ,  $R_0$ ). In case of net convergence (D < 0), we neglect large-scale flux M are noted ( $q_{orig}$ ,  $R_{orig}$ ). The properties of the incoming air by horizontal advection are noted ( $q_{adv}$ ,  $R_{adv}$ ). For simplicity we neglect here the effect of horizontal gradients in air properties, so that the properties of the convergence flux
- 20 are also  $(q_0, R_0)$ . The properties of the flux M are noted  $(q_{orig}, R_{orig})$  humidity (i.e.  $q_{adv} = q_0$ ), assuming that the main effect of horizontal advection on  $\delta D_0$  arises from horizontal gradients in  $\delta D$ . Appendix C explains how  $R_{adv}$  can be calculated. At steady state, the water budget of the SCL writes:

$$M \cdot q_{orig} + E + F_{evap} + F_{adv} \cdot q_0 = (N + \underline{D}F_{adv,out}) \cdot q_0 \tag{2}$$

This model is consistent with SCL water budgets that have already been derived in previous studies (Bretherton et al., 1995), 25 except that we consider steady state. This equation can be solved for  $q_0$ :

$$q_0 = q_{orig} + \underline{E/M} \frac{E + F_{evap}}{M}$$
(3)

The SCL humidity  $q_0$  is thus sensitive to M, justifying that it can be used to estimate the mixing intensity or the entrainment velocity "entrainment velocity"  $w_e = M/\rho_0$  ( $\rho$  being the air volumic mass) (Bretherton et al., 1995).

At steady state, the water isotope budget of the SCL writes:

$$M \cdot q_{orig} \cdot R_{orig} + E \cdot R_E + F_{evap} \cdot R_{evap} + F_{adv} \cdot q_0 \cdot R_{adv} = (N + \underline{D}F_{adv,out}) \cdot q_0 \cdot R_0$$
(4)

where  $R_E$  is the isotopic composition of the surface evaporation. It is assumed to follow the Craig and Gordon (1965) Craig and Gordon (1965) equation:

5 
$$R_E = \frac{R_{oce}/\alpha_{eq} - h_0 \cdot R_0}{\alpha_K \cdot (1 - h_0)}$$
(5)

where  $R_{oce}$  is the isotopic ratio in the surface ocean water,  $\alpha_{eq}$  is the equilibrium fractionation calculated at the ocean surface temperature (SST) (Majoube, 1971),  $\alpha_K$  is the kinetic fractionation coefficient (MJ79) and  $h_0$  is the relative humidity normalized at the SST ( $h_0 = q_0/q_s(SST, P_0)$ ) where  $q_s$  is the <u>saturation</u> specific humidity at <u>saturation function SST</u> and  $P_0$  is the surface pressure).

10 We write the isotopic composition of the rain evaporation,  $R_{e\mu qp}$ , as:

 $R_{evap} = \alpha_{evap} \cdot R_0$ 

20

where  $\alpha_{evap}$  is an effective fractionation coefficient. For example, if droplets are formed near the cloud base, some of them precipitate and evaporate totally into the SCL (e.g. in non-precipitating shallow cumulus clouds), then  $\alpha_{evap} = \alpha(T_{cloudbase})$ . In contrast, if droplets are formed in deep convective updrafts after total condensation of the SCL vapor, and then a very small

15 fraction of the rain is evaporated into a very dry SCL, then  $\alpha_{evap} = 1/\alpha(T_{SCL})/\alpha_K$  (Stewart, 1975).

We note  $\eta = F_{evap}/E$  the ratio of water vapor coming from rain evaporation to that of surface evaporation, and  $\phi = F_{adv} \cdot g_{adv}/E$ the ratio of water vapor coming from horizontal advection to that coming from surface evaporation. We note  $\beta = R_{adv}/R_0$  the ratio of isotopic ratios of horizontal advection to that of the SCL.

Note that in all our equations, we assume that temperature and humidity profiles and all basic surface meteorological variables are known. We attempt to express neither  $h_0$  as a function of  $q_0$  as in B15, nor the q profile as a function of  $q_0$ . Our ultimate goal is to assess the added value of  $\delta D$  assuming that meteorological measurements are already routinely done.

By combining all these equations, we get:

$$R_{0} = \frac{(1 - r_{orig}) \cdot R_{oce} / \alpha_{eq} + \alpha_{K} \cdot (1 - h_{0}) \cdot r \cdot R_{orig}}{(1 - r_{orig}) \cdot h_{0} + \alpha_{K} \cdot (1 - h_{0})} \frac{(1 - r_{orig}) \cdot R_{oce} / \alpha_{eq} + \alpha_{K} \cdot (1 - h_{0}) \cdot r_{orig} \cdot (1 + \eta) \cdot R_{orig}}{(1 - r_{orig}) \cdot h_{0} + \alpha_{K} \cdot (1 - h_{0})} \frac{(1 - r_{orig}) \cdot R_{oce} / \alpha_{eq}}{(1 - r_{orig}) \cdot h_{0} + \alpha_{K} \cdot (1 - h_{0}) \cdot r_{orig} \cdot (1 + \eta) \cdot R_{orig}}$$

(6)

where  $r_{orig} = q_{orig}/q_0$  is the proportion of the water vapor in the SCL that originates from above.



Equation-

Figure 2. Schematics showing the simple box model on which the theoretical framework is based, and illustrating the main notations.

An intriguing aspect of this equation is that the sensitivity to M disappears. In contrast to  $q_0$ ,  $R_0$  is not sensitive to M. Therefore, it appears illusory to promise that water vapor isotopic measurements could help constrain the entrainment velocity that many studies have strived striven to estimate (Nicholls and Turton, 1986; Khalsa, 1993; Wang and Albrecht, 1994; Bretherton et al., 1995; Faloona et al., 2005; Gerber et al., 2005, 2013). The lack of sensitivity of  $R_0$  to M is explained physically by the fact that for a given  $q_0$  and  $q_{orig}$ , if M increases, then  $E = E \pm F_{evap}$  increases in the same proportion to maintain the water balance. Therefore, the relative proportion of the water vapor originating from surface evaporation and and rain evaporation to that coming from above, to which  $R_0$  is sensitive, remains constant. Rather, since q and R vary with altitude,  $R_0$  is sensitive to the altitude from which the air originates, as argued in the next paragraph.

#### 2.2 Two additional assumptions to close the equation

5

## 10 2.2 Closure if $\delta D$ profile follows a Rayleigh distillation line

Eq. (6) requires to know  $q_{orig}$  and  $R_{orig}$ . B15 closed it by taking the values of  $q_{orig}$  and  $R_{orig}$  take these values from GCM outputs at 700 hPafrom GCM outputs. We modify this in two ways.

First, we want to. In contrast, here we acknowledge the diversity and complexity of mixing mechanisms by taking keeping the possibility to take  $q_{orig}$  and  $R_{orig}$  at a variable altitude  $z_{orig}$ .

 $q_{orig} = h(z_{orig}) \cdot q_s(\bar{T}(z_{orig}) + \delta T(z_{orig}), P(z_{orig}))$ 

where T
(z<sub>orig</sub>) + δT(z<sub>orig</sub>) = T(z<sub>orig</sub>) is the temperature at altitude If the goal is to predict R<sub>0</sub> from z<sub>orig</sub>, T
is the
tropical ocean mean temperature profiles, h(z<sub>orig</sub>) we can apply Eq. (6) if we know the q and P(z<sub>orig</sub>) are the relative humidity and pressure at δD vertical profiles. Conversely, if the goal is to predict z<sub>orig</sub>, and δT(z<sub>orig</sub>) is the temperature perturbation compared to T
. Therefore, from R<sub>0</sub>, we can numerically solve Eq. (6) if we know the q and δD vertical profiles. No analytical solution exists in the unknown q<sub>orig</sub> is replaced by the unknown general case, but a numerical solution can be searched for z<sub>orig</sub>. based on Eq. (6). However, the existence and unicity of the solution is not warranted for all kinds of profiles (e.g. appendix
10 A).

Note that in all our equations, we assume that temperature and humidity profiles and all basic surface meteorological variables are known. We make no attempt to express  $h_0$  as a function of  $q_0$  as in B15. Our ultimate goal is to assess the added value of  $\delta D$  assuming that meteorological measurement are already routinely done. Therefore, variations of  $\delta D_0$  that are mediated by  $q_0$  or  $h_0$  do not interest us.

- 15 Second, to deal with  $R_{orig}$  in Eq. (6) and get an analytical solution, we assume In practice, full isotopic profiles are costly to measure. In addition, our goal is to develop an analytical model. Therefore, in the following we simplify the problem by assuming that the vertical profile of R follows a known relationship as a function of q. Measured vertical profiles of  $\delta D$  are usually bounded by two curves when plotted in a  $(q, \delta D)$  diagram (Sodemann et al., 2017): Rayleigh distillation curve and mixing line. We explore these two extreme cases in the next section and in appendix A respectively.
- 20 Schematics showing the simple box model on which the theoretical framework is based, and illustrating the main notations.

#### 2.3 Closure if the tropospheric profile follows a Rayleigh line

Here we assume that  $R_{orig}$  is uniquely related to  $q_{orig}$  by Rayleigh distillation First, we explore the case of a Rayleigh distillation curve (Dansgaard, 1964), as in Galewsky and Rabanus (2016)Galewsky and Rabanus (2016):

$$R_{orig} = R_0 \cdot r_{orig}^{\alpha_{eff} - 1} \tag{7}$$

where α<sub>eff</sub> is an effective fractionation coefficient. Typically, q decreases with altitude, so R also decreases with altitude. However, in observations and models, vertical profiles of R can be very diverse (Bony et al., 2008; Sodemann et al., 2017). The water vapor may be more (Worden et al., 2007) or less (Sodemann et al., 2017) depleted than predicted by Rayleigh curve using a realistic fractionation factor that depends on local temperature. Therefore, here we let α<sub>eff</sub> be a free parameter larger than 1. Rather than assuming a true Rayleigh curve, we simply assume that R and q are logarithmically related. Effects of horizontal advection and rain evaporation on tropospheric profiles are encapsulated into α<sub>eff</sub>.

Injecting Eq. (7) into Eq. (6), we get:

$$R_{0} = \frac{R_{oce}}{\alpha_{eq}} \cdot \frac{1}{h_{0} + \alpha_{K} \cdot (1 - h_{0}) \cdot \left((1 + \eta) \cdot \frac{1 - r_{orig}^{\alpha_{eff}}}{1 - r_{orig}} - \eta \cdot \alpha_{evap} + \phi \cdot (1 - \beta)\right)}$$
(8)

A simpler form can be found if neglecting horizontal advection and rain evaporation effects ( $\phi = \eta = 0$ ):

$$R_0 = \frac{R_{oce}}{\alpha_{eq}} \cdot \frac{1}{h_0 + \alpha_K \cdot (1 - h_0) \cdot \frac{1 - r_{orig}^{\alpha_{eff}}}{1 - r_{orig}}}$$
(9)

5 As a consistency check, in the limit case where the air coming from above is totally dry ( $r_{orig} = 0$ ), we find Eq. (9) becomes the MJ79 equation:

$$R_0 = \frac{R_{oce}}{\alpha_{eq}} \cdot \frac{1}{h_0 + \alpha_K \cdot (1 - h_0)} \tag{10}$$

Equation (98) tells us that whenever α<sub>eff</sub> > 1, R<sub>0</sub> decreases as r<sub>orig</sub> increases (Fig. 3 red), i.e. as q<sub>orig</sub> is moister. Therefore, R<sub>0</sub> decreases as z<sub>orig</sub> is lower in altitude. This result may be counter-intuitive, but can be physically interpreted as follows. If
z<sub>orig</sub> is high, mixing brings air with very depleted water vapor, but since the air is dry, the depleting effect is small. In contrast, if z<sub>orig</sub> is low, mixing brings air with water vapor that is not very depleted, but since the air is moist, the depleting effect is large (Fig. 4a).

Figure 3 (red) shows that the range of possible  $\delta D$  values is restricted to -70 ‰ to -85 ‰. This explains why in quiescent conditions near the sea level in tropical ocean locations, the water vapor  $\delta D$  varies little Benetti et al. (2014) (Benetti et al. (2014).

- 15 F. Vimeux pers. comm.). In the limit case where r<sub>orig</sub> → 1 (i.e. the air comes from the SCL top), R<sub>0</sub> → R<sub>oce</sub>/α<sub>eq</sub> · 1/(h<sub>0</sub>+α<sub>K</sub>·(1-h<sub>0</sub>)·α<sub>eff</sub>)
  (L'Hopital's rule was used to calculate this limit). This lower bound is not so depleted compared to the more depleted water vapor observed in regions of deep convection (e.g. Lawrence et al. (2002); Lawrence et al. (2004); Kurita (2013)Lawrence et al. (2002); Lawrence et al. (2002); Lawrence et al. (2004); Kurita (2013)Lawrence et al. (2002); Lawrence et al. (2002); Lawrence et al. (2004); Kurita (2013)Lawrence et al. (2002); Lawrence et al. (2002); Lawrence et al. (2004); Kurita (2013)Lawrence et al. (2002); Lawrence et al. (2004); Kurita (2013)Lawrence et al. (2002); Lawrence et al. (2004); Kurita (2013)Lawrence et al. (2002); Lawrence et al. (2004); Kurita (2013)Lawrence et al. (2002); Lawrence et al. (2004); Kurita (2013)Lawrence et al. (2002); Lawrence et al. (2004); Kurita (2013)Lawrence et al. (2002); Lawrence et al. (2004); Kurita (2013)Lawrence et al. (2002); Lawrence et al. (2004); Kurita (2013)Lawrence et al. (2002); Lawrence et al. (2004); Kurita (2013)Lawrence et al. (2002); Lawrence et al. (2004); Kurita (2013)Lawrence et al. (2002); Lawrence et al. (2004); Kurita (2013)Lawrence et al. (2002); Lawrence et al. (2004); Kurita (2013)Lawrence et al. (2002); Lawrence et al. (2004); Kurita (2013)Lawrence et al. (2002); Lawrence et al. (2004); Kurita (2013)Lawrence et al. (2002); Lawrence et al. (2004); Kurita (2013)Lawrence et al. (2014); Kurita (2014); Kurita (2014); Kurita
- or liquid-vapor exchanges (Lawrence et al., 2004; Worden et al., 2007) can further decrease  $R_0$  (appendix B).

Figure 3 (green) shows that the sensitivity to  $\alpha_{eff}$  is relatively small but cannot be neglected. Therefore, predicting water vapor  $\delta D$ - $\delta D_0$  requires to have some knowledge about the steepness of the isotopic profiles in the FT. Rain evaporation and horizontal advection can have either an enriching or depleting effect, but do not qualitatively change the results (Fig. 3 purple and blue).

25 Assuming a Rayleigh shape for the  $\delta D$  profile allows us to find a good-looking analytical solution, but our Now we consider the case of a mixing line. Detailed calculation in appendix A show that the sensitivity to  $r_{orig}$  is lost. An infinity of FT end members can lead to the same  $\delta D_0$  when mixed with the surface evaporation, as illustrated in Fig. 4b and analytically demonstrated in appendix A. Our main results (more depleted  $\delta D_0$  as  $r_{orig}$  increases, restricted range of  $\delta D_0$  variations, relationship with  $z_{orig}$ ) would hold for any hold only for  $\delta D$  profile that is steeper than the profiles that are steeper than a mixing line. If the profile follows as This is the case for profiles that are intermediate between a Rayleigh and a mixing line, however, our results would not hold any more, because no single end member can be identified, as illustrated in Fig. 4b and

5 analytically demonstrated in appendix A. Therefore, in the remaining of the paper, we will assume that *R* follows a logarithmic line. We will assess the validity of this assumption in section D1. as is usually the case in nature (Sodemann et al., 2017) or in a general circulation model (appendix D1).

An important assumption that led to Eq. (9) is the neglect of SCL moistening by rain evaporation. We propose an extended equation including rain evaporation in appendix B). Rain evaporation can have a depleting or enriching effect (e.g. pink and

10 blue curves in Fig. 3), depending on microphysical details that are too complex to be addressed here. Therefore, we neglect rain evaporation effects and our results will be valid only in regions covered by non-precipitating clouds, e.g. subsiding regions covered by non-precipitating trade-wind cumulus, strato-cumulus or stratus clouds.

#### 3 Model simulations, observations and methods

#### 3.1 LMDZ simulations

- 15 We use an isotope-enabled general circulation model (GCM) as a laboratory to test our hypotheses and investigate isotopic controls what controls the isotopic composition. We use the LMDZ5A version of LMDZ (Laboratoire de Météorologie Dynamique Zoom), which is the atmospheric component of the IPSL-CM5A coupled model (Dufresne et al., 2012) that took part in CMIP5 (Coupled Model Intercomparison Project, Taylor et al. (2012)Taylor et al. (2012)). This version is very close to LMDZ4 (Hourdin et al., 2006). Water isotopes are implemented the same way as in its predecessor LMDZ4 (Risi et al.,
- 20 2010c). We use 4 years (2009-2012) of an AMIP (Atmospheric Model Intercomparison Project)-type simulation (Gates, 1992) that was initialized in 1977. The winds are nudged towards ERA-40 reanalyses (Uppala et al., 2005) to ensure a more realistic simulation. Such a simulation has already been described and extensively validated for isotopic variables in both precipitation and water vapor (Risi et al., 2010c, 2012a). The ocean surface water  $\delta D_{oce}$  is assumed constant and set to 4 ‰. The resolution is 2.5° in latitude × 3.75° in longitude, with 39 vertical levels. Over the ocean, the first layer extends up to 64 m, and a typical
- 25 SCL extending up to 600 m is resolved by 6 layers. Around 2500 m, a typical altitude for the inversion for trade-wind cumulus clouds, the resolution is about 500 m.

For our calculations, we only use tropical grid boxes ( $30^{\circ}$ S- $30^{\circ}$ N) over tropical oceans (>80% ocean fraction in the grid box). In addition, to avoid numerical problems when estimating effect of horizontal advection and rain evaporation, only grid boxes and days where E > 0.5 mm/d are considered. This represents 99.7% of all tropical oceanic grid boxes.

30 Specific diagnostics for horizontal advection and rain evaporation are detailed in appendix B and C.



Figure 3.  $\delta D_0$  as a function of  $r_{orig}$  according to Eq. (9), with  $\alpha_{eff} = \alpha_{eq}$  as an example (red). For this illustrative purpose, we assume SST=30°C,  $h_0 = 0.8$ ,  $\delta D_{occ} = 0\%$  and  $\phi = \eta = 0$ . The sensitivity to the effective fractionation factor  $\alpha_{eff}$  (green) is shown. In case of If rain evaporation fractionation 25% of surface evaporation ( $\eta = 0.25$ ), the solid pink and blue curves show the sensitivity to the effective fractionation factor  $\alpha_{re}$  (see appendix B)  $\alpha_{evaR}$ . If the incoming water vapor by horizontal advection is shown 25% of surface evaporation (pink $\phi = 0.25$ ), the dashed pink and blue ) curves show the sensitivity to the isotopic gradient quantified by  $\beta$ .



Figure 4. Idealized  $q - \delta D$  diagrams showing how the SCL water vapor  $\delta D$  is set. For this illustrative purpose, we assume SST=30°C,  $h_0 = 0.8$ ,  $\delta D_{acc} = 0$ , and and  $\phi = \eta = 0$ . (a) If  $\delta D$  profiles follow Rayleigh distillation. The red curve shows the Rayleigh profile starting from the SCL and the pink curve shows the mixing line connecting the air coming from above to the surface evaporation, in the case  $r_{orig} = q_{orig}/q_0 = 0.7$ . The green curve shows the the Rayleigh profile starting from the SCL and the blue curve shows the mixing line connecting the air coming from above to the surface evaporation, in the case  $r_{orig} = q_{orig}/q_0 = 0.5$ . One can visually see that when  $r_{orig}$  is lower, the mixing line is more curved, leading to more enriched values. (b) If  $\delta D$  profiles follow a mixing line. The pink-purple curve joins the SCL air and the air at all altitudes above the SCL. One can see that different values for  $r_{orig}$  can lead to the same value of  $\delta D$  in the SCL.

#### 3.2 STRASSE observations

We also apply our theoretical framework to observations during the STRASSE (subtropical Atlantic surface salinity experiment) cruise that took place in the Northern subtropical ocean in August and September 2012 (Benetti et al., 2014). This campaign accumulates several advantages that are important for our analysis: (1) continuous  $\delta D_0$  measurements in the surface

- 5 water vapor (17m) at a high temporal frequency during one month (Benetti et al., 2014, 2015, 2017b), (2) associated surface meteorological measurements, including SST and  $h_0$ , (3) 22 radio-soundings relatively well distributed over the campaign period and providing vertical profiles of altitude, temperature, relative humidity and pressure, (4) ocean surface water  $\delta D_{oce}$ measurements (Benetti et al., 2017a), (5) a variety of conditions ranging from quiescent weather to convective conditions, (6) on many vertical profiles, a well defined temperature inversion allows to calculate the inversion altitude.
- We use  $\delta D_0$  measurements on a 15-minute time step. The measurements in ocean water were interpolated on the same time steps using a Gaussian filter with a width of 3 days. The radio-soundings are used together with all water vapor isotopic measurements that are within 30 minutes of the radio-sounding launch. Only profiles during the ascending phase of the balloon are considered, because the descent phase is often located far away from the initial launch point (McGrath et al., 2006; Seidel et al., 2011)

## 15 3.3 Estimating the altitude from which the air originates

First,  $\alpha_{eff}$  is estimated assuming that Here we explain how  $z_{orig}$  is estimated based on LMDZ outputs. First, we assume that the q and  $\delta D$  at 500 hPa ( $q_f$ ,  $\delta D_f$ ) at 500hPa follows belong to a Rayleigh distillation line starting from the surface with effective fractionation  $\alpha_{eff}$ :

$$\alpha_{eff} = 1 + \frac{\ln(R_f/R_0)}{\ln(q_f/q_0)}$$

In a real field campaign, this assumption means that we do not need to measure the full vertical profile of  $\delta D$ , but only  $\delta D_f$  at a given free tropospheric altitude (e.g. 500 hPa).

We checked that results are similar when defining the end member at 400 hPa rather than 500 hPa. However, if the end member is should be defined above 500 hPa to ensure that it is well above boundary layer processes. If the end member is defined below 500 hPa (e.g. 600 hPa), results are not always reasonable there are a few cases where q increases with altitude ( $q_f > q_0$ )

25 due to horizontal advection or convective detrainment from nearby moister regions; meanwhile,  $\delta D$  decreases monotonically, leading to unrealistic values for  $\alpha_{off}$ .

Second,  $r_{orig}$  is estimated based on Eq. (9), using  $\alpha_{eff}$ ,  $\alpha_{eq}$ ,  $\alpha_K$ ,  $\delta D_{oce}$ ,  $h_0$  and  $\delta D_0$  simulated by LMDZ.

Third, the altitude  $z_{orig}$  is estimated from  $r_{orig}$ . Using the q vertical profile, we find  $z_{orig}$  so that  $q(z_{orig}) = r_{orig} \cdot q_0$  (Fig. 5, red).

30 Note that When estimating  $z_{orig}$  from observations, we follow the same methodology except that in absence of measurements for  $q_f$  and  $\delta D_f$  we assume a constant  $\alpha_{eff} = 1.07$  based on LMDZ simulation, and that  $\alpha_{eq}$ ,  $\alpha_K$ ,  $\delta D_{oce}$ ,  $h_0$  and  $\delta D_0$  come from surface observations.



Figure 5. Schematics illustrating the typical structure of tropical marine boundary layers. The sub-cloud layer (SCL) extends from the surface to the lifting condensation level (LCL) and the cloud layer extends from the LCL to the inversion  $(z_i)$ . EIS stands for the estimated inversion strength. Left: shape of the vertical profile in q (black) and  $q_s$  (green). Right: shape of the vertical profile in potential temperature  $\theta$ , inspired by Wood and Bretherton (2006) (Wood and Bretherton, 2006). The LCL,  $z_{orig}$ ,  $z_{orig,r_{orig}=0.6}$  and  $z_i$  altitudes defined in section 3.4 are indicated.

Note that  $r_{orig}$  and  $z_{orig}$  are not direct diagnostics from the simulation, but rather a-posteriori estimates to match the simulated  $\delta D_0$ . Therefore, if assumptions underlying Eq. (9) are violated, then the estimate of  $r_{orig}$ , and subsequently  $z_{orig}$ , will be basedbiased. The estimate of  $r_{orig}$  encapsulates the effect of mixing processes, but also all other processes that have been neglected in our theoretical framework, such as temporal variations in SCL depth,  $q_0$  or  $\delta D_0$ , horizontal gradients in or

5 vertical variations of  $g_0$  or  $\delta D_0$ , or rain evaporation. For example, in case of deep convection, depleting rain evaporation will reflect into an artificially larger  $r_{orig}$  and lower  $z_{orig}$ . We have to keep this in mind when interpreting the results within the SCL.

#### 3.4 Boundary layer structure diagnostics

Figure 5 illustrates the structure of a typical tropical marine boundary layer covered by strato-cumulus or cumulus clouds
(Betts and Ridgway, 1989; Wood, 2012; Wood and Bretherton, 2004; Neggers et al., 2006; Stevens, 2006). The cloud base corresponds to the lifting condensation level (LCL). Below is the well-mixed SCL. Above is the cloud layer, topped by a temperature inversion. Above the inversion is the FT.

The LCL is calculated as the altitude at which the specific humidity near the surface equals the specific humidity at saturation of a parcel that is lifted following a dry adiabat (Fig. 5). In LMDZ, the inversion-

The temperature inversion is an abrupt increase in temperature that caps the boundary layer. Therefore, a method to automatically estimate its altitude  $z_i$  is calculated to detect a maximum in the vertical gradient of potential temperature (Stull, 1988; Oke, 1988; Sorbjan, 1). This method is sensitive to the resolution of vertical profiles (Siebert et al., 2000; Seidel et al., 2010). Therefore, we adapted this method in order to yield  $z_i$  values that best agree with what we would estimate from visual inspection of individual

- 5 temperature profiles. In LMDZ, we calculate  $z_i$  as the first level at which the vertical potential temperature gradients-gradient exceeds 3 times the moist-adiabatic lapse rate. In observations, we calculate  $z_i$  is calculated as the first level at which the vertical potential temperature gradients-gradient exceeds 5 times the moist-adiabatic lapse rate, because radio-soundings are noisier than simulated profiles. These estimates are consistent with what we would estimate from visual inspection of vertical profiles.
- Finally, we calculate  $z_{orig,r_{orig}=0.6}$ , which is the  $z_{orig}$  altitude if  $r_{orig}$  is set to 0.6. This usually coincides with the altitude of strong humidity decrease near the inversion (Fig. 5).

#### 3.5 Averages and composites

All calculations are done on daily values for LMDZ, and on 15-minute values for observations.

For LMDZ, when analyzing spatial and seasonal variability, seasonal averages are calculated at each grid box <u>over tropical</u>
15 <u>oceans</u> by averaging all days of all years that belong to each season. Seasons are defined as boreal winter (December-January-February), spring (March-April-May), summer (June-July-August) and fall (September-October-November). For illustration purpose, all maps are plotted for boreal winter. Standard deviations are also calculated among all days of all years for each season.

The type of clouds and mixing processes depends strongly on the large-scale velocity at 500 hPa ( $\omega_{500}$ , map shown

- 20 in Fig. 6a), with shallow clouds in subsiding regions and deeper clouds in ascending regions ((Bony et al., 2004), Fig. 1). Therefore, composites are calculated by averaging-it is convenient to plot variables as composites as a function of  $\omega_{500}$ (Bony et al., 2004). To make such plots, we divide the  $\omega_{500}$  range from -30 to 50 hPa/d into intervals of 5 hPa/d. In each given interval, we average all seasonal-mean values at all locations that belong to a given interval of over tropical oceans for which seasonal-mean  $\omega_{500}$  belongs to this interval (e.g. Fig. 8a will be an example). Note that such composites are done
- 25 on seasonal-mean  $\omega_{500}$  because cloud processes and their associated diabatic heating are tied to the large-scale circulation through energetic constrains (Yanai et al., 1973; Emanuel et al., 1994) that are best valid at longer time scales (otherwise, the energy storage term may become significant, e.g. Masunaga and Sumi (2017)). This is why  $\omega_{500}$  is generally averaged over a month or longer (e.g. Bony et al. (1997); Williams et al. (2003); Bony et al. (2004); Wyant et al. (2006); Bony et al. (2013)). In addition, we primarily focus on understanding the seasonal and spatial distribution of  $\delta D_0$ .
- 30 The cloud cover strongly depends on correlates with the inversion strength, with increasing cloud fraction as inversion strength increases. We use which can be quantified by the Estimated Inversion Strength (EIS) (Wood and Bretherton, 2006) (, Wood and Bretherton (2006), map shown in Fig. 6b) as a measure of inversion strength. Composites as We thus also plot variables as composites as a function of EISare calculated by averaging. To make such plots, we divide the EIS range from -1 K to 9 K into intervals of 0.5K. In each given interval, we average all seasonal-mean values at all locations that belong



**Figure 6.** Maps of winter-mean  $\omega_{500}$  (a) and EIS (b) simulated by LMDZ.

to a given interval of EIS.over tropical oceans for which seasonal-mean EIS belongs to this interval (e.g. Fig. 8b will be an example). Using seasonal-mean values is consistent with Wood and Bretherton (2006) and with the better link at longer time scales between cloud processes and the large-scale dynamical regime.

#### **3.6** Decomposition method for $\delta D_0$

5 To understand what controls the  $\delta D_0$  spatio-temporal variations,  $\delta D_0$  is decomposed into 4 contributions based on Eq. (9). The 4 factors,  $r_{orig}$  S. First, we define  $r_{orig,bas} = 0.3$ ,  $\alpha_{eff} \alpha_{eff,bas} = 1.09$ , SST and  $h_0$ , are alternatively varied each one at a time, assuming that all other factors are constant ( $r_{orig} = 0.6$ ,  $\alpha_{eff} = 1.09$ , SST  $SST_{bas} = 25^{\circ}$ C,  $h_0 = 0.8$ ). This yields 4 components  $h_{0,bas} = 0.7$ , representing the effects of the variability of  $\phi_{bas} = 0$ ,  $\eta_{bas} = 0$ ,  $\beta_{bas} = 1$  and  $\alpha_{evap,bas} = 1$  as a basic state. We call  $\delta D_{0,func}(r_{orig}, \alpha_{eff}, SST, h_0, \phi, \beta, \eta, \alpha_{evap})$  the function giving  $\delta D_0$  as a function of  $r_{orig}$ ,  $\alpha_{eff}$ , SST and , SST,  $h_0$  on

10  $\delta D_0$ ,  $\phi$ ,  $\beta$ ,  $\eta$  and  $\alpha_{evap}$  following Eq. (8), and  $\delta D_{0,bas} = \delta D_{0,func}(r_{orig,bas}, \alpha_{eff,bas}, SST_{bas}, h_{0,bas}, \phi_{bas}, \beta_{bas}, \eta_{bas}, \alpha_{evap,bas})$ . The relative contribution of  $r_{orig}$  to  $\delta D_0$  is estimated as  $\delta D_{0,func}(r_{orig}, \alpha_{eff,bas}, SST_{bas}, h_{0,bas}, \phi_{bas}, \beta_{bas}, \eta_{bas}, \alpha_{evap,bas}) - \delta D_{0,bas}$ . Similarly, the contributions of  $\alpha_{eff}$ , SST,  $h_0$ ,  $\phi$  and  $\eta$  are to  $\delta D_0$  are estimated as detailed in table 1. All the contributions have the same units as  $\delta D_0$  (‰). The sum of these components yields a quantity that is very close to the simulated  $\delta D_0$ , which confirms the validity of this linear decomposition. These components and their sum can be plotted as maps: Fig. 7 provides an

15 <u>example</u>.

The relative contribution contributions of each of these effects components to the  $\delta D$  variability is are quantified by performing a linear regression of each of the components as a function of  $\delta D_0$ . If the correlation coefficient is significant for a given factor, then the slope quantifies the contribution of this factor to the variability of  $\delta D_0$ . The sum of all contributions may not always be 1 due to non-linearity. Such a method has already been applied in previous studies (e.g. Risi et al. (2010b); Oueslati et al. (2016)

20 Risi et al. (2010b); Oueslati et al. (2016)). The contributions to the seasonal-spatial variability of  $\delta D_0$  can be quantified by performing the regression among all locations and seasons. The contributions to the daily variability of  $\delta D_0$  can be quantified by performing the regression among all days of a given season at a given location.

	Calculation	Physical meaning
roria	$\delta D_{0,tunc}(r_{orige} \alpha_{ett,bas}, SST_{bas}, h_{0,bas}, \phi_{bas}, eta_{bas}, \eta_{bas}, \alpha_{evap,bas}) - \delta D_{0,bas}$	Altitude from which the air originates
Qett.	$\delta D_{0,tuuc}(r_{aria,bas}, \alpha_{ett}, SST_{bas}, h_{0,bas}, \phi_{bas}, eta_{bas}, M_{bas}, lpha_{evap,bas}) = \delta D_{0,bas}$	Steepness of the $\delta D$ vertical gradient in the FT
SST	$\delta D_{0.func}(r_{erig.bas.}lpha_{eff.bas.}SST,h_{0.bas.}\phi_{bas.}eta_{bas.}\eta_{bas.}lpha_{evar.basic}) - \delta D_{0.bas.}$	SST
ho	$\delta D_{0.func}(r_{orig.bas,}lpha_{ef.f.bas,}SST_{bas,}h_{0,}\phi_{bas,}eta_{bas,}M_{bas,}lpha_{ev.ap.bas})-\delta D_{0.bas}$	he
¢	$\delta D_{0.func}(r_{orig.bas.} \alpha_{eff.bas.} SST_{bas.} h_{0.bas.} \phi_{.} \beta_{.} \eta_{bas.} \alpha_{evap.bas}) = \delta D_{0.bas.}$	Horizontal advection through horizontal $\delta D$ gradients
n. Table 1. Equations 1	$\delta D_{0.tunc}(r_{erig.bas.} \alpha_{ef.f.bas.} SST_{bas.} h_{0.bas.} \phi_{bas.} \beta_{bas.} \eta_{.} \alpha_{ever}) - \delta D_{0.bas.}$	Rain evaporation in the SCL

Table 1. Equations to calculate the relative contributions of  $r_{orig}$ ,  $\alpha_{eff}$ , SS1,  $h_0$ ,  $\phi$  and  $\eta$  to  $\delta D_0$ , and the physical meaning of these contributions.

## **3.7** Decomposition method for $r_{orig}$

To understand what controls  $r_{orig}$ , a similar method as for the decomposition of  $\delta D_0$  can be applied, based on Eq. (??). We can write  $r_{orig}$  as:

$$r_{orig} = \frac{h(z_{orig}) \cdot q_s(\bar{T}(z_{orig}) + \delta T(z_{orig}), P(z_{orig}))}{q_0} \tag{11}$$

5 where  $\overline{T}(z_{orig}) + \delta T(z_{orig}) = T(z_{orig})$  is the temperature at altitude  $z_{orig}$ ,  $\overline{T}$  is the tropical-ocean-mean temperature profiles,  $h(z_{orig})$  and  $P(z_{orig})$  are the relative humidity and pressure at  $z_{orig}$ , and  $\delta T(z_{orig})$  is the temperature perturbation compared to  $\overline{T}$ . Therefore, the variability of  $r_{orig}$  is decomposed into the effect of 4 factors:  $q_0$ ,  $z_{orig}$ ,  $h(z_{orig})$  and  $\delta T(z_{orig})$ . In practice,  $r_{orig}$  and  $z_{orig}$  are calculated following section 3.3, then Eq. (11) is applied.

## 4 Results from LMDZ

## 10 4.1 Does the tropospheric profile follow a mixing or Rayleigh line?

First, we test whether the  $\delta D$  vertical profiles simulated by LMDZ follow a Rayleigh or mixing curve as a function of q. For the Rayleigh curve,  $\alpha_{eff}$  is estimated as explained in section 3.3. For the mixing line, the end member  $(q_f, R_f)$  is also taken at 500 hPa. Examples of vertical  $\delta D$  profiles simulated by LMDZ and predicted by the Rayleigh and mixing lines are plotted in Fig. ??. We can see that simulated profiles are usually bounded by these two extreme lines, consistent with observations

5 (Sodemann et al., 2017). Profiles are however much smoother than in observations, due to the coarse vertical resolution of the model. The coarse vertical resolution is a limitation to keep in mind when discussing the shape of vertical profiles.-

When assuming a Rayleigh or mixing curve, the root mean square error (RMSE) on the  $\delta D$  profile from the surface to 500hPa ranges from 5 to 30 ‰ (Fig. D1a-b). In average, RMSE are slightly larger for Rayleigh, but this depends on the location and no generic curve fits perfectly well the vertical profiles. This is consistent with the diversity of observed profile

10 shapes (Sodemann et al., 2017). In the following, we will assume that the Rayleigh curve is a good first order approximation. Our method of  $z_{orig}$  estimate remains valid even if  $\delta D$  vertical profiles do not follow Rayleigh, as long they follow a curve that is steeper than mixing. This is the case in LMDZ (Fig. ??).

Figure D1c shows the estimated  $\alpha_{eff}$ . It is maximum in regions of deep convection. This is consistent with the maximum depletion simulated in deep convective regions in the mid-troposphere simulated by models (Bony et al., 2008), leading to steeper  $\delta D$  profiles. The pattern of  $\alpha_{eff}$  may also reflect horizontal advection effects (Dee et al., 2018).

Values  $\alpha_{eff}$  are of the same order of magnitude as real fractionation factors, but the spatial variations do not reflect those predicted if using a fractionation coefficient  $\alpha_{eq}$  a function of temperature T (Fig. D1f). Rayleigh curves using  $\alpha_{eq}(T)$  poorly predict vertical profiles of  $\delta D$  (Fig. D1c), with RMSE values exceeding 20 ‰ at most locations.

- Examples of vertical profiles simulated by LMDZ (red), predicted by a Rayleigh curve with  $\alpha_{eff}$  estimated to fit the 20 simulated  $\delta D$  at 500 hPa (section 3.3, green), and predicted by a mixing line with the dry end member at 500 hPa (pink). Three examples are given: (a) the simulated profile is closed to a mixing line, (b) the simulated profile is closed to a Rayleigh line, and (c) the simulated profile deviates both from a mixing and a Rayleigh line (c). The RMS values indicate the RMS difference between simulated profile and mixing line (pink) or Rayleigh curve (green).
- a) Root mean square error (RMSE) between the simulated δD profile and a δD profile that would follow a mixing curve
  between the surface and 500 hPa. b) Same as a but for a profile that would follow a Rayleigh curve between the surface and 500 hPa, with α<sub>eff</sub> determined based on simulated δD at 500 hPa. c) Same as b but for a profile that would follow a Rayleigh curve using equilibrium fractionation calculated as a function of temperature, α<sub>eq</sub>(T). d) α<sub>eff</sub> 1, where α<sub>eff</sub> is the effective fractionation coefficient, expressed in ‰. e) Standard deviation of α<sub>eff</sub> among all days in winter of all years, expressed in ‰. f) α<sub>eq</sub>(T) 1 expressed in ‰. For a-d and f, all daily values are averaged over all days in winters of all years.

## 30 4.1 Decomposition of $\delta D_0$ variability

15

The spatial variations of  $\delta D_0$  simulated by LMDZ (Fig. 7a) are characterized by depleted values near mid-latitudes and in dry subsiding regions (e.g. off the coast of Peru and over other upwelling regions ) and in deep convective regions regions of oceanic upwelling) and regions of atmospheric deep convection (e.g. Maritime Continent). Consistently,  $\delta D_0$  values exhibit a maximum for weakly ascending or subsiding regions:  $\delta D_0$  decreases as  $\omega_{500}$  is more strongly ascending or descending with

increasing vertical velocity of both signs (Fig. 8a black);  $\delta D_0$  decreases as EIS increases reflecting more stable, subsiding conditions (Fig. 8b black). This pattern is consistent with previous studies (e.g. Good et al. (2015))Good et al. (2015)). For the first time, we propose a theoretical framework to interpret this pattern, decomposing it into 4-6 contributions:  $r_{orig}$ ,  $\alpha_{eff}$ , SSTand,  $h_0$ , rain evaporation and horizontal advection effects (section 3.6). We check that the reconstructed  $\delta D_0$  from the

5 sum of its 4 contributions is very similar to the simulated  $\delta D_0$  (Fig. 7b, 8 dashed black).

In ascending regions, the main contribution explaining the more depleted  $\delta D_0$  in deep convective regions is that of  $\alpha_{eff}$  (Fig. 7d, 8a red).  $\alpha_{eff}$  is higher in more ascending regions – (Fig. D1d). This means that the main factor depleting  $\delta D_0$  in deep convective regions is the fact that the mid-troposphere is more depleted. This leads to a steeper gradient (higher  $\alpha_{eff}$ ), and thus a more efficient depletion by vertical mixing. This is consistent with deep convection depleting the water vapor most

- 10 efficiently in the mid-troposphere (Bony et al. (2008))(Bony et al., 2008). The second main contribution is that associated with  $r_{orig}$  (Fig. 7c, 8a green).  $r_{orig}$  is larger in deep convective regions . However, we recall that Eq. (9) does not consider rain evaporation, which is a significant source of water vapor in deep convective regions (Worden et al. (2007)). Rain evaporation in deep convective regions is expected to deplete the water vapor (section B), so that neglecting rain evaporation leads to an over-estimate of  $r_{orig}$  in these regions. Therefore, the stronger  $r_{orig}$  in deep convective regions could be partially an artifact
- 15 reflecting the effect of rain evaporation. (as explained in section 4.2).

In subsidence regions, the main factor explaining the more depleted  $\delta D_0$  as subsidence is stronger, or as EIS increases, is the cold SST (Fig. 7e, 8a pink), leading to larger  $\alpha_{eq}$ , and to a lesser extent the dry  $h_0$  (Fig. 7f, 8a purple). The contribution of  $r_{orig}$  is also a significant contribution to the depletion of  $\delta D_0$  in the cold upwelling regions, for example off Peru or Namibia (Fig. 7c). In subsidence regions,  $r_{orig}$ , is unlikely to be an artifact of rain evaporation there, and probably really reflect the

20 importance of mixing processes. The shallower boundary layer there are associated with higher  $r_{orig}$ . The fact that the effect of  $r_{orig}$  can be seen on the composites as a function of EIS-

The contribution of rain evaporation on  $\delta D_0$  is minor compared to other contributions, except in the deepest convective regions (Fig. 8b, green) and not as a function of  $\omega_{500}$  may reflect the fact that EIS reflects more faithfully the cloud and mixing processes in dry, stable regions than  $\omega_{500}$  does (Wood and Bretherton, 2006)7g). Rain evaporation has a slightly depleting

- 25 effect in regions of strong deep convection and a slightly enriching effect in regions of moderate deep convection. When the fraction of raindrops that evaporate is small, isotopic fractionation favors evaporation of the lighter isotopologues. Therefore in convective, moist regions, rain evaporation has a depleting effect on the SCL (Worden et al., 2007). In contrast, in drier regions, rain evaporates almost totally. The evaporation flux thus has almost the same composition as the initial rain, which is more enriched than the water vapor.
- 30 The contribution of horizontal advection to  $\delta D_0$  is significant only where isotopic gradients are the largest (Fig. C1h). Horizontal advection has slightly enriching in deep convective regions and depleting in coastal regions (e.g. off the coasts of California, Peru, Mauritania, Namibia, India and Australia). For example, the Saharan layer in front of the North-Western African Coast leads to a strong effect of horizontal advection (Lacour et al., 2017a).

From a quantitative point of view, we can decompose the  $\delta D_0$  seasonal-spatial variations into these different effects (section 35 3.6). In regions of large-scale ascent,  $\alpha_{eff}$  is the main factor explaining the  $\delta D_0$  seasonal-spatial variations (37-33%), followed

Regime	ascending		Subsiding	
	correlation coefficient	slope	correlation coefficient	slope
$r_{orig}$	<del>0.71-0.59</del>	<del>0.17-0.19</del>	<del>0.50 <u>0.52</u></del>	<del>0.16</del> 0.29
$lpha_{eff}$	<del>0.75-</del> 0.73	<del>0.37 <u>0.33</u></del>	<del>0.36</del> <u>0.26</u>	<del>0.14</del> 0.10
SST	<del>-0.20</del> -0.23	-0.06	0.89	0.54
$h_0$	<del>0.09 (0.06)</del>	<del>0.03 (0.01)</del>	<del>0.35 0.28</del>	<del>0.23</del> 0.13
rain evaporation	0.67	0.20	-0.36	-0.05
horizontal advection	-0.26	-0.12	.(0.10)~	(0.04)
<i>r<sub>ovig</sub></i> if rain evaporation and horizontal advection are neglected	0.69	0.30	0.58	0.34

Decomposition of the spatial and seasonal variation in  $\delta D_0$  into its 4 contributions: effect of

**Table 2.** Decomposition of the spatial and seasonal variation in  $\delta D_0$  into its 6 contributions: effect of  $r_{orig}$ ,  $\alpha_{eff}$ , SST,  $h_0$ , rain evaporation and horizontal advection. For each contribution, we show the correlation coefficient of the linear regression of the contribution as a function of  $\delta D_0$ . The analysis is done separately for ascending and subsiding regimes. All seasons and locations over tropical oceans ( $30^\circ N - 30^\circ S$ , ocean fraction>80%, surface evaporation>0.5 mm/d) are considered. The threshold for the correlation coefficient to be statistically significant at 99 % is 0.15 or lower in all cases. We write correlation coefficient and slope values between brackets when they are not significant at 99%.

by rain evaporation (20%) and  $r_{orig}$  (1719%) and (Table 2). In regions of large-scale descent, SST is the main factor explaining the seasonal-spatial variations (54%), followed by  $r_{orig}$  (1629%)  $h_0$  (13%), and  $\alpha_{eff}$  (1410%) (table-Table 2). Note that the contribution of  $r_{orig}$  would be similar if we neglect rain evaporation and horizontal advection effects (Table 2).

The decomposition method can also be applied to decompose the  $\delta D_0$  variability at the daily time scale at each location and for each season (Table 3). On average, in ascending regions,  $r_{orig}$  is the main factor (4952 %), followed by rain evaporation (48%) and  $\alpha_{eff}$  (3935 %). In subsiding regions, the effect of SST is muted due to its slow variability, and  $r_{orig}$  (5982 %),  $\alpha_{eff}$  (49%) and  $h_0$  (62%) become the main factors becomes the main factor.

Overall, the results highlight the importance of  $r_{orig}$  as one of the main factors controlling the spatio-temporal variability of  $\delta D_0$ .

#### 10 4.2 Decomposition of $r_{orig}$ variability

5

Given the importance of  $r_{orig}$  in controlling the  $\delta D_0$  variations, we now decompose  $r_{orig}$  into its 4 contributions:  $q_0$ ,  $z_{orig}$ ,  $h_{orig}$  and  $\delta T_{orig}$  (section 3.6). Spatially,  $r_{orig}$  is maximum in regions of strong large-scale ascent (Fig. 10a) such as the Maritime continent (Fig. 9a), and in very stable regions (Fig. 10b) such as upwelling regions (Fig. 10a). We check that the reconstructed  $r_{orig}$  from the sum of its 4 contributions is very similar to the simulated  $r_{orig}$  (Fig. 9b, 10 dashed black).



Figure 7. a) Map of winter-mean  $\delta D_0$  simulated by LMDZ. b) Map of winter-mean  $\delta D_0$  reconstructed as the sum of the 4 contributions. Note that to focus on variations only and to get values of the same order of magnitude as the simulated Tropical-mean  $\delta D_0$  field, we subtracted the mean of the 4 contributions and was added the mean of simulated  $\delta D_0$  to compare with a on the reconstructed  $\delta D_0$  fields and color scale. c) Map of the contribution of  $r_{orig}$  on winter-mean  $\delta D_0$  calculated from Eq. (9) if only  $r_{orig}$  varies (see section 3.6). d) Same as b but of only for  $\alpha_{eff}$  varies. e) Same as b but if only for SST varies. f) Same as b but if only for  $h_0$  varies.



**Figure 8.** Composites as a function of  $\omega_{500}$  (a) and of EIS (b) of the seasonal averages of  $\delta D_0$  simulated by LMDZ over all tropical ocean locations (black). Same for the sum of the contributions (black dashed ) and for each individual contribution to  $\delta D_0$ :  $r_{orig}$  varies (green),  $\alpha_{eff}$  (dark red), SST (pink) and ,  $h_0$  (purple), rain evaporation (dashed brown) and horizontal advection (dashed blue), the tropical mean  $\delta D_0$  was added to each contribution to plot on the same scale as simulated  $\delta D_0$ . The number of samples in each bin is indicated on a logarithmic scale on the right-hand-side (dotted black line).

	Ascending		Subsiding	
Regime				-
	correlation coefficient	slope	correlation coefficient	slope
$r_{orig}$ ,	0.46	0.52	0.42	0.82
$\alpha_{eff}$ ,	0.34	0.35	0.14	0.40
SST <del>and</del>	-0.12	-0.01	0.25	0.22
$h_0$ variations. For each	0.06	0.26	0.15	0.39
contribution, we show-				
	0.49	0.48	0.19	0.20
rain evaporation				
horizontal advection	-0.26	-0.24	-0.15	-0.31
~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~				

**Table 3.** As in table 4 but at the correlation coefficient of the linear regression of the contribution as a function of  $\delta D_0$  daily scale. The threshold for the correlation coefficient to be statistically significant at 99 % is 0.15 or lower in coefficients and slopes are averaged over all cases. The analysis is done seasons and locations over tropical oceans ( $30^\circ N - 30^\circ S$ , ocean fraction>80%), separately for ascending and subsiding regimes. All seasons and tropical oceans locations are considered.

In regions of strong large-scale ascent,  $r_{orig}$  is larger mainly because  $h_{orig}$  is larger (Fig. 9e, 10a pink). This suggests that even though the effect of rain evaporation may artificially bias high the estimate of  $r_{orig}$ , a substantial part of the  $r_{orig}$  signal is actually physical. Indeed, if the large  $r_{orig}$  was purely an artifact of the neglect of rain evaporation, it would translate totally into a lower  $z_{orig}$ . Physically, the is because the moister the FT, the higher the contribution of vapor coming from above to the vapor of the SCL, and thus the higher  $r_{orig}$  and the more depleted  $\delta D_0$ . This mechanism through which a moister FT leads to a more depleted  $\delta D_0$  is consistent with that argued in B15.  $z_{orig}$  damps this effect: when convection is stronger and the FT

moister, convection is also deeper, so the air originates from higher in altitude where the air is drier.

5

In very stable regions,  $r_{orig}$  is larger mainly because  $q_0$  is small\_larger (Fig. 9c, 10b green), consistent with the drier conditions in these regions of large-scale descent, and. Note that this effect can be seen only in most stable regions, but when

- 10 considering all subsiding regions, the contribution is small (Table 2).  $r_{orig}$  is larger also because  $z_{orig}$  is lower in altitude (Fig. 9d, 10b red), consistent with the shallower boundary layers as EIS increases. Physically, the lower in altitude the . As EIS increases, the boundary layers are shallower, the air comes from , the higher lower in altitude,  $r_{orig}$  and the more depleted is higher and thus  $\delta D_0$  is more depleted. This mechanism was not considered in Benetti et al. (2015) B15 but our decomposition shows that it is a key mechanism driving  $r_{orig}$  and thus  $\delta D_0$  variations in stable regions.
- 15 Quantitatively, in ascending regions, the main factors factor controlling the seasonal-spatial variations in  $r_{orig}$  are is  $h_{orig}$ (94182 %)and, dampened by  $z_{orig}$  (61-67 %) (Table 4). Similarly, in In descending regions, the main factors are factor is also  $h_{orig}$  (9196 %)and, followed by  $z_{orig}$  (7241 %) (Table 4). At the daily scale, the same two factors dominate the variability of  $r_{orig}$ :  $h_{orig}$  and  $z_{orig}$  contribute to 6778 % and 7639 % of  $r_{orig}$  variations in average over ascending regions, and to 104118 % and 7339 % in average over descending regions (Table 5).



**Figure 9.** a) Map of winter-mean  $r_{orig}$  simulated by LMDZ. b) Map of winter-mean  $r_{orig}$  reconstructed as the sum of the 4 contributions. <u>Tropical-mean  $r_{orig}$  was added to compare with a with the same color scale</u>. c) Map of winter-mean  $r_{orig}$  calculated from Eq. (11) if only  $q_0$  varies (see section 3.6). d) Same as b but of only  $z_{orig}$  varies. e) Same as b but if only  $h(z_{orig})$  varies. f) Same as b but if only  $\delta T_{orig}$  varies.

## 4.3 Entrainment Estimating altitude estimatezoria

Estimated altitude  $z_{orig}$  is minimum in dry subsiding regions, especially in upwelling regions (Fig. 11a, Fig. 12), corresponding to regions with the strongest inversion (Fig. 11). This contributes to the depleted  $\delta D_0$  in these regions.

- As explained in 3.3, our estimate of  $z_{orig}$  may be artificially biased due to the neglect of some processes in our theoretical framework. Ideally, to check whether  $z_{orig}$  really physically represents the altitude from which the air originates, additional model experiments where water vapor from different levels are tagged (Risi et al., 2010b) would be needed. While we leave this for future work, in the meanwhile we check whether  $z_{orig}$  estimates are consistent with what we expect based on what we know about mixing processes in the marine boundary layers. We expect that in strato-cumulus regions, air is entrained originates from a very shallow (a few tens of meters) layer above the inversion, whereas the mixing processes may be more
- 10 diverse, and possibly deeper in the FT, as the boundary layer deepens (Fig. 1).



Figure 10. Composites as a function of  $\omega_{500}$  (a) and of EIS (b) of the seasonal averages of  $r_{orig}$  simulated by LMDZ over all tropical ocean locations (black). Same for the sum of the contributions (black dashed) and for each individual contribution to  $r_{orig}$ :  $q_0$  varies (green),  $z_{orig}$  (dark red),  $h(z_{orig})$  (pink) and  $\delta T_{orig}$  (purple). The number of samples in each bin is indicated on a logarithmic scale on the right-hand-side as bars.

Regime	Ascending		Subsiding	
	correlation coefficient	slope	correlation coefficient	slope
$q_0$	<del>-0.24</del> - <u>0.82</u>	<del>0.0</del> - <u>0.33</u>	0.09-0.21	<del>0.00.12</del>
$z_{orig}$	<del>0.88</del> - <u>0.91</u>	<del>0.61_0.67</del>	<del>0.65-</del> 0.77	<del>0.720.41</del>
horig	<del>0.75-</del> 0.98	<del>0.94</del> -1 <u>.82</u>	0.53	<del>0.910.96</del>
$\delta T_{orig}$	<del>0.33 <u>0</u>.55</del>	<del>0.12-</del> 0.06	<del>-0.34</del> - <u>0.37</u>	- <del>0.27</del> -0.12
Decommon	ition of the smotial season	al moniation in	m into ito 4 contributi	and affaat of

Decomposition of the spatial-seasonal variation in rorig into its 4 contributions: effect of

**Table 4.** Decomposition of the spatial-seasonal variation in  $r_{orig}$  into its 4 contributions: effect of  $q_0$ ,  $z_{orig}$ ,  $h_{orig}$  and  $\delta T_{orig}$  variations. For each contribution, we show the correlation coefficient of the linear regression of the contribution as a function of  $r_{orig}$ . The analysis is done separately for ascending and subsiding regimes. All seasons and locations over tropical oceans  $(30^{\circ}N - 30^{\circ}S)$ , ocean fraction>80%) are considered. The threshold for the correlation coefficient to be statistically significant is 0.15 or lower in all cases. We write correlation coefficient and slope values between brackets when they are not significant at 99%.

Regime	Ascending		Subsiding	
	correlation coefficient	slope	correlation coefficient	slope
$q_0$ –	-0.37	-0.04	-0.23	-0.07
$z_{orig}$ ,	0.91	0.39	0.80	0.39
$h_{orig}$ and	0.58	0.78	0.58	1.18
$\delta T_{orig}$ variations. For each contribution, we show-	-0.14	0.01	-0.23	-0.12

**Table 5.** As in table 4 but at the correlation coefficient of the linear regression of the contribution as a function of  $r_{orig}$  daily scale. The threshold for the correlation coefficient to be statistically significant is 0.15 or lower in coefficients and slopes are averaged over all cases. The analysis is done seasons and locations over tropical oceans ( $30^{\circ}N - 30^{\circ}S$ , ocean fraction>80%), separately for ascending and subsiding regimes. All seasons and tropical oceans locations are considered.

To check whether estimated  $z_{orig}$  is consistent with this picture, we compare  $z_{orig}$  to  $z_{orig,r_{orig}=0.6}$  ( $z_{orig}$  that we would estimate is  $r_{orig}$  was set constant to 0.6) and  $z_i$  (section 3.4), which are measures of the altitude of the humidity drop and temperature inversion respectively. As expected from Fig. 1, they are minimum in dry upwelling regions, intermediate in tradewind regions, and maximum values in convective regions (Fig. 11c-d, 12 green, blue). Therefore, the low  $z_{orig}$  in upwelling

5 regions reflects the low  $z_i$ . Consistently, in subsiding regions,  $z_{orig}$  correlates well with  $z_{orig,r_{orig}=0.6}$  (correlation coefficient of 0.52, statistically significant beyond 99 %). If we focus on very stable regions only (EIS>7 K),  $z_{orig}$  correlates well with both  $z_{orig,r_{orig}=0.6}$  and  $z_i$  (correlation coefficient of 0.58 and 0.52 respectively, statistically significant beyond 99 %). The altitude  $z_{orig}$  is a few meters above the inversion in strato-cumulus regions, and up to 1km above the inversion in cumulus and deep convective regions (Fig. 12), consistent with our expectations from Fig. 1. This lends support to the fact that at least in subsiding regions, our jectore based  $z_{orig}$  actimate effectively reflect reflects the origin of air coming from above



**Figure 11.** a) Map of winter-mean  $z_{orig}$  estimated from  $\delta D_0$  simulated by LMDZ. b) Same as a but  $z_{orig}$  that we would estimate if  $r_{orig}$  was constant set to 0.6 ( $z_{orig,r_{orig}=0.6}$ ). c). Same as a but for  $z_i$  simulated from LMDZ. Only days when EIS>2 K are considered, otherwise  $z_i$  is difficult to estimate. d) Same as a but for LCL simulated by LMDZ.

In ascending regions, in contrast,  $z_{orig}$  does not correlate significantly with  $z_{orig,r_{orig}=0.6}$  or  $z_i$ . This may indicate either that our  $z_{orig}$  estimate is biased by neglected processes such as rain evaporation, or that in deep convective regions, the origin of FT air into the SCL is very diverse due to the variety of mixing processes (1).

#### 5 Results from observations

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5 To check whether our results obtained with LMDZ are realistic, we apply our methods to the measurements gathered during the STRASSE campaign. In the absence of measured  $\delta D$  profiles, we assume that  $\alpha_{eff}$  is 1.07 based on LMDZ simulation. simplicity and in absence of all necessary measurements, here we neglect the effects of rain evaporation and horizontal advection.

Throughout the cruise, δD<sub>0</sub> shows a large variability, ranging from around -75 ‰ in quiescent conditions to -120 ‰ during
the two convective conditions (Benetti et al., 2014) (Fig. 13a red). Variability in r<sub>orig</sub> is the major factor contributing to this variability (58 %) (Fig. 13a green, Table 6). This crucial importance of mixing processes is consistent with B15.

During the two convective events, the estimated  $r_{orig}$  saturates at 1 (Fig. 13b). This proves that  $r_{orig}$  estimated in these conditions is biased high because it encapsulates the effect of neglected processes, i.e. depletion by rain evaporation. Equation (9) is not valid in this case. In addition, at the scale of a few hours, the steady-state assumptions may be violated. Rain evaporation may strongly deplete the SCL before surface evaporation has the time to play its dampening role, hence the

possibility to reach very low  $\delta D_0$  that cannot be predicted even when considering rain evaporation (appendix B).



**Figure 12.** Composites as a function of EIS of seasonal-mean of  $z_{orig}$  (black),  $z_{orig,r_{orig}=0.6}$  (green),  $z_i$  (blue) and LCL (red). The composite profiles of cloud cover are also shown, showing deep clouds when EIS is close to 0 and shallowest clouds when EIS is largest.

contributions to $\delta D_0$	correlation coefficient	slope
$r_{orig}$	0.77	0.58
SST	0.57	0.16
$h_0$	0.40	0.48

Table 6. Same as Table 2 but for the STRASSE observations. Linear regressions are calculated among 1977 data points.

contributions to $r_{orig}$	correlation coefficient	slope
$q_0$	-0.46	-1.49
$z_{orig}$	0.66	0.90
$h_{orig}$	0.81	0.70
$\delta T_{orig}$	-0.36	-0.91

 Table 7. Same as Table 4 but for the STRASSE observations. Linear regressions are calculated among 55 data points, so that correlation coefficients above 0.35 are statistically significant at 99 %.

During the rest of the cruise, the main factors controlling the  $r_{orig}$  variability are  $z_{orig}$  (90 %) and  $h_{orig}$  (70 %). The importance of FT humidity in controlling  $r_{orig}$  was already highlighted in B15. However, in their paper, the variability in  $z_{orig}$  was neglected, whereas it appears here as the main factor.

- Through September, the eruises cruise goes from a shallow boundary layer in early September to deeper boundary layers 5 with higher inversions, before reaching the convective conditions (Fig. 13c). Consistently with this deepening boundary layer, the air is entrained originates from increasingly higher in altitude. When considering only the Remarkably, there are 6 data points when  $z_{orig} < 2000$  m, days when  $z_{orig}$  coincides almost exactly with  $z_i$  with a root means square error of 31% and correlation coefficient of 0.996 (Fig. 13c; the correlation coefficient between  $z_{orig}$  and  $z_i$  is 0.996). This indicates that the air is entrained into the SCL exactly exactly comes from the inversion layer. Even if the number of sample is small, the coincidence
- 10 is remarkable, especially when When recalling that  $z_{orig}$  and  $z_i$  are estimated from completely independent observations. This, the coincidence is remarkable and lends support to the fact that on these days, our  $z_{orig}$  estimate is physical. However, there remains 9 days when  $z_{orig}$  is much higher than  $z_i$ . This may reflect more penetrative downdrafts as we approach deeper convective regimes. But it may also be an artifact of our neglect of horizontal advection. For example, on these days which are characterized by lower  $h_0$ , neglecting the advection of enriched water vapor from nearby regions with higher  $h_0$  could be
- 15 mis-interpreted as lower  $r_{orig}$  and thus higher  $z_{orig}$ .

#### 6 Discussion: what can we learn from water isotopes on mixing processes?

We have shown in the previous section that one of the main factors controlling  $\delta D_0$  at the seasonal-spatial and daily scale are the proportion of the water vapor in the SCL that is originates from above  $(r_{orig})$ , and that one of the main factor controlling  $r_{orig}$  is the altitude from which the air originates  $(z_{orig})$ . In turn, could we use water vapor isotopic measurements to constrain



Figure 13. a) Time series of  $\delta D_0$  observed during the STRASSE cruise, together with its 4 contributions. The  $\delta D$  of the surface ocean water is also plotted with the scale on the right. b) Time series of  $r_{orig}$  estimated from observations during the STRASSE campaign, together with its 4 contributions. c) Times series of  $z_{orig}$ ,  $z_{orig,r_{orig}=0.6}$ , LCL and  $z_i$  estimated from the STRASSE observations.

 $z_{orig}$ ? This would open the door to discriminating between different mixing processes at play (Fig. 1). Since mixing processes are crucial to determine the sensitivity of cloud fraction to SST (Sherwood et al., 2014; Bretherton, 2015; Vial et al., 2016), such a prospect would allow us to improve our knowledge of cloud feedbacks, and hence of climate sensitivity.

- With this in mind, we assess the errors associated with  $z_{orig}$  estimates from  $\delta D_0$  measurements, and discuss whether there they are small enough for  $z_{orig}$  estimates to be useful. In strato-cumulus clouds where the air is believed to be entrained originate from the first few tens of meters above cloud top (Faloona et al., 2005; Mellado, 2017),  $z_{orig}$  estimates are not useful if the errors are larger than a few tens of meters, e.g. 20 m. In cumulus clouds where mixing processes are more diverse and possibly deeper (Fig. 1),  $z_{orig}$  estimates may be useful if errors are of the order of 80 m.
- Let's assume that we have a field campaign where we measure  $\delta D_0$ , surface meteorological variables, temperature and 10 humidity profiles (e.g. radio-soundings), and a few  $\delta D$  profiles (e.g. by aircraft). This is what we can expect for example from the future EUREC4A (Elucidating the role of clouds-circulation coupling in climate) campaign to study trade-wind cumulus clouds (Bony et al., 2017). Below we quantify the effects of five sources of uncertainty on  $z_{orig}$  estimates.

## 6.1 Measurement errors

The first source of uncertainty that we have highlighted in this article is the effect of rain evaporation. As long as the

- 15 microphysical processes and associated isotopic fractionation processes are not well constrained are measurement errors. We re-calculate  $z_{orig}$  assuming an error of 0.4 ‰ on  $\delta D_0$  (typical of what we can measure with in-situ laser instruments, Aemisegger et al. (2012); Benetti et al. (2014)) and 1 ‰ on  $\delta D_f$  (larger errors due to lower humidity and the increased complexity of measurements in altitude). The averaged errors on  $z_{orig}$  and their standard deviations are plotted as a function of EIS in Fig. 14a. Whereas errors on  $\delta D_f$  lead to errors on  $z_{orig}$  of the order of 20 m (Fig. 14a, green), errors on  $\delta D_0$  lead to errors on  $z_{orig}$
- 20 of the order of 80 m (Fig. 14a, red). Yet in strato-cumulus, none expects the air to originate from a higher altitude than 80 m above the inversion. Therefore,  $\delta D_0$  measurements would need to be more accurate than usual to be useful in strato-cumulus regions, i.e. 0.1 % to yield a 20 m precision on  $z_{orig}$ . In trade-wind cumulus regions, the precision of 0.4 % is enough for  $z_{orig}$  to be useful.

## 6.2 Neglecting rain evaporation

- 25 The second source of uncertainty is associated with neglecting rain evaporation. This effect can be quantified in a model, but it is very difficult to quantify in nature because it is complicated and uncertain to measure  $\eta$  (Rosenfeld and Mintz, 1988), and it is even more complicated to measure or predict  $\alpha_{evap}$ . Rain evaporation can have a depleting or enriching effect depending on microphysical details that are too complex to be addressed here (Graf et al., 2019). Neglecting rain evaporation leads to an error of the order of 500 m in regions of low EIS and 250 m in regions of strong EIS (Fig. 14b, brown). In regions of strato-cumulus
- 30 regions, rain evaporation is a significant source of error in spite of the relatively small amount of precipitation available to evaporate. This is because total evaporation of the rain efficiently enriches the SCL, and easily modifies  $\delta D_0$  by more than the 0.1% targeted precision explained above. However, it is safer to restrain  $z_{orig}$  estimates to non-precipitating clouds that LMDZ overestimates this source of error in trade-wind cumulus and strato-cumulus regions. LMDZ is one of the GCMs

producing the strongest rain in srato-cumulus regions (Zhang et al., 2013), and GCMs are known to trigger convection to often in trade-wind cumulus regions (Nuijens et al., 2015a, b).

The second-

15

## 6.3 Neglecting horizontal advection

5 The third source of uncertainty is the associated with horizontal advection. In nature,  $\phi$  can be estimated from meteorological analyzes and  $\beta$  can be estimated from near-surface isotopic measurements at several locations (e.g. sounding arrays during typical field campaigns). In absence of these additional measurements, neglecting this effect leads to an error of the order of 800 m (Fig. 14b, purple). This limits the usefulness of  $z_{orig}$  estimates for all cloud regimes.

## 6.4 Daily variability in the steepness of $\delta D$ profiles

10 The fourth source of uncertainty arises from the daily variability in  $\alpha_{eff}$ . Measuring daily (appendix D2). Estimating  $\alpha_{eff}$  requires to measure  $\delta D_f$  at 500 hPa. Satellite measurements are available but are affected by random errors that are too large for our application (Worden et al., 2011, 2012; Lacour et al., 2015). Precise in-situ measurements of water vapor  $\delta D$  profiles is in altitude are costly and difficult (Sodemann et al., 2017).

Let's assume that we have only one profile  $\delta D_f$  value that represents the seasonal-average at a given location. The daily standard deviation of  $\alpha_{eff}$  ( $\sigma_{\alpha_{eff}}$ ) for a given season ranges from 5‰ in the Central Atlantic to 40‰ near the Maritime Continent (Fig. D1d). To estimate the resulting error on  $z_{orig}$ , we re-estimate  $z_{orig}$  every day and at each location using  $\alpha_{eff} + \sigma_{\alpha_{eff}}$  and  $\alpha_{eff} - \sigma_{\alpha_{eff}}$ . The error on  $z_{orig}$  is calculated as  $(z_{orig}(\alpha_{eff} - \sigma_{\alpha_{eff}}) - z_{orig}(\alpha_{eff} + \sigma_{\alpha_{eff}}))/2$ . The averaged error and its standard deviation is plotted as a function of EIS in Fig. 14c (black). It is of the order of 400m, and rarely below 200m. If we attempt to estimate  $\alpha_{eff}$  as the fractionation coefficient as a function of local temperature, errors would be

20 even more dissuasive (Fig. 14<u>c</u>, blue).

Therefore, estimating  $z_{orig}$  from daily  $\delta D_0$  measurements cannot be useful unless we measure daily  $\delta D$  profiles  $\delta D_f$  on a daily basis as well. Practically, we could imagine measuring FT properties ( $\delta D_f$ ) at the top of a mountain while we measure  $\delta D_0$  at the sea level (e.g. on Islands such as Hawaii or La Réunion, Galewsky et al. (2007); Bailey et al. (2013); Guilpart et al. (2017)). We could also imagine retrieving  $\alpha_{eff}$  from daily Galewsky et al. (2007); Bailey et al. (2013); Guilpart et al. (2017)).

## 25 6.5 Rayleigh assumption for the shape of $\delta D$ profiles

Finally, a fifth source of uncertainty comes the assumption that the  $\delta D$  profiles retrieved from space by IASI (Infrared Atmospheric Sounding Interferometer, Lacour et al. (2012, 2015)), but this would be associated with additional errors whose estimate is beyond the scope of this paperprofile follows a Rayleigh distillation line (section 2.2). However, both in LMDZ (appendix D1) and nature (Sodemann et al., 2017),  $\delta D$  profiles are usually intermediate between Rayleigh and mixing lines.

30 The precision of our *z<sub>orig</sub>* estimate is maximum in the Rayleigh distillation case.

The third source of uncertainty are measurements errors. We recalculate When trying to find a numerical solution for  $z_{orig}$  assuming an error of 0.4 ‰ on  $\delta D_0$  (typical of what we can measure with in-situ laser instruments, Benetti et al. (2014))and 1 ‰ on  $\delta D_f$  (larger errors due to lower humidity and the increased complexity of measurements in altitude). Whereas errors on  $\delta D_f$  lead to errors on directly from Eq. (6), a solution can be found only in 0.1 % of cases. This is because simulated  $\delta D$ 

- 5 profiles are often close to a mixing line in the lower troposphere (appendix D1). Whatever  $z_{orig}$  of the order of 20 m (Fig. 14, green), errors on in the lower troposphere, the  $\delta D_0$  lead to errors on calculated from Eq. (6) is nearly constant because the  $\delta D$ profile is close to a mixing line (appendix A, Fig. 4b). Whatever  $z_{orig}$  of the order of 80 m. This is higher than the upper bound for the expected entrainment altitude in strato-cumulus. Therefore, in the middle troposphere, the  $\delta D_0$  measurements would need to be more accurate than usual to be useful in strato-cumulus regions, i.e. 0.1 ‰ to yield a 20 m precision on calculated
- 10 from Eq. (6) is also nearly constant because  $r_{orig}$  there is very small. So whatever  $z_{orig}$ . In , the  $\delta D$  calculated from Eq. (6) is nearly constant, and the numerical solution fails.

However, it is possible that  $\delta D$  profiles simulated by LMDZ are closer to mixing lines than real profiles, since GCMs are known to overestimate vertical mixing through the troposphere (Risi et al., 2012b) and to mix the lower free troposphere too frequently by deep convection in trade-wind cumulus regions, the precision is enough for  $z_{orig}$  to be useful. regions

15 (Nuijens et al., 2015a, b). Therefore, the shape of  $\delta D$  profiles simulated by LMDZ is not a sufficient reason to reject the Rayleigh assumption. The uncertainty associated with this assumption is very difficult to quantify in LMDZ. More measurements of full  $\delta D$  profiles are very welcome to help quantify it.

To summarize,  $\delta D_0$  measurements could potentially be useful to estimate  $z_{orig}$  with a useful precisionin cumulus and strato-cumulus clouds, but only if we are able to measure daily, but if we measure daily  $\delta D_f$  in the mid-troposphere, if

the shape of  $\delta D$  profiles and if can be better documented, if we measure  $\delta D_0$  at different places to quantify the effect of horizontal advection, and if we can invent innovative techniques to better quantify the effect of rain evaporation. In addition in strato-cumulus clouds, we need to measure  $\delta D_0$  with an accuracy of 0.1 ‰ and 0.4 ‰ in trade-wind cumulus and strato-cumulus clouds respectively.

## 25 7 Conclusion

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We propose an analytical model to predict the water vapor isotopic composition  $\delta D_0$  of the sub-cloud layer (SCL) over tropical oceans. Benetti et al. (2015) extended the Merlivat and Jouzel (1979) This model relies on the hypothesis that the altitude from which the air originates,  $z_{orig}$ , is an important factor. We build on Benetti et al. (2015) who extended the Merlivat and Jouzel (1979) closure equation to make explicit the link between  $\delta D_0$  and FT entrainmentmixing processes. We further extend the Benetti et al. (2015)

30 equationin two ways: first, we assume that we know the shape of their equation: we assume a shape for the  $\delta D$  vertical profiles , and second, we let the altitude from which the air originates,  $z_{orig}$ , varyas a function of q, and we account for horizontal advection and rain evaporation effects.



Figure 14. Errors when estimating  $z_{orig}$  from  $\delta D_0$  observations, as a function of EIS, as predicted by LMDZ: error if one uses  $\alpha_{eq}$  as a function of local temperature to estimate  $\alpha_{eff}$ , error if one uses the seasonal-mean profile instead of the daily profile to estimate  $\alpha_{eff}$  (black), error Error we would make if  $\delta D_0$  is measured with a 1% error (red), and error we would make if  $\delta D_f$  is measured with a 1% error (green). b) error we would make if we neglect horizontal advection effects (purple) and rain evaporation effects (brown). c) Error if one uses  $\alpha_{eq}$  as a function of local temperature to estimate  $\alpha_{eff}$  (blue), error if one uses the seasonal-mean profile instead of the daily profile to estimate  $\alpha_{eff}$  (blue). The standard deviations among all daily errors estimated in each bin of EIS are also shown.

The resulting equation highlights the fact that  $\delta D_0$  is not sensitive to the intensity of entrainmentmixing processes. Therefore, it is unlikely that water vapor isotopic measurements could help estimate the entrainment velocity that many studies have strived striven to estimate (Bretherton et al., 1995). In contrast,  $\delta D_0$  is sensitive to the altitude from which the air originates. Based on a simulation with LMDZ and observations during the STRASSE cruise, we show that  $z_{orig}$  is an important factor

- 5 explaining the seasonal-spatial and daily variations in  $\delta D_0$ , especially in subsidence regions. In turn, could  $\delta D_0$  measurements, combined with vertical profiles of humidity, temperature and  $\delta D$ , help estimate  $z_{orig}$  and thus discriminate between different mixing processes? This should rely on a good knowledge of the  $\delta D$  vertical profiles. We find that for For such isotope-based estimates of  $z_{orig}$  to be useful, we would need frequent vertical profiles of a precision of a few hundreds meters in deep convective regions and smaller than 20 m in strato-cumulus regions. To reach this target, we would need daily measurements
- 10 of  $\delta D$  in the mid-troposphere and very accurate measurements of  $\delta D_0$ , which are currently difficult to obtain. In precipitating clouds and deep convection We would also need information on the horizontal distribution of  $\delta D$  to account for horizontal advection effects, and full  $\delta D$  profiles to quantify the uncertainty associated with the assumed shape for  $\delta D$  profiles. Finally, rain evaporation is too large a source of uncertainty, whereas in an issue in all regimes, even for strato-cumulus regions, very precised estimates of  $z_{orig}$  (no larger than 20 m) would be needed to be useful. Therefore, it is in regions of shallow
- 15 cumulus clouds that such isotope-based estimates of *z<sub>orig</sub>* would be most useful. clouds. Innovative techniques would need to be developed to quantify this effect from observations.

This study is preliminary in many respects. First, it would be safe to check using water tagging experiments in LMDZ that  $z_{orig}$  estimates really represents represent the altitude from which the air is originates, and is not to biases biased by our simplifying assumptions. Second, the coarse vertical resolution of LMDZ, and the simplicity of mixing parameterizations

- 20 (e.g. cloud top entrainment is not represented) are a limitation of this study. Ideally, the relationship between  $\delta D_0$ ,  $z_{orig}$  and the type of mixing processes should be investigated in isotope-enabled Large Eddy Simulations (LES) (Blossey et al., 2010; Moore et al., 2014). Artificial tracers and structure detection methods (Park et al., 2016; Brient et al., 2019), combined with conditional sampling methods (Couvreux et al., 2010), could help detect the different kinds of mixing structures, estimate their contributions to vertical transport, and describe their isotopic signature. This would allow us to confirm, or infirm, many of
- 25 the hypotheses and conclusions in this paper. Finally, if the sensitivity of  $\delta D_0$  to the type of mixing processes is confirmed, paired isotopic simulations of single-column model (SCM) versions of general circulation models (GCM) and LES, forced by the same forcing, could be very useful to help evaluate and improve the representation of mixing and entrainment processes in GCMs, as is routinely the case for non-isotopic variables (Randall et al., 2003; Hourdin et al., 2013; Zhang et al., 2013).

*Code and data availability.* LMDZ can be downloaded from http://lmdz.lmd.jussieu.fr/. Program codes used for the analysis are available on https://prodn.idris.fr/thredds/catalog/ipsl\_public/rlmd698/article\_mixing\_processes/d\_pgmf/catalog.html.

Isotopic measurements from STRASSE can be downloaded from http://cds-espri.ipsl.fr/isowvdataatlantic/. All other datasets and processed files are available on https://prodn.idris.fr/thredds/catalog/ipsl\_public/rlmd698/article\_mixing\_processes/catalog.html.

#### Appendix A: Closure if the tropospheric profile follows a mixing line

For simplicity, we neglect here horizontal advection and rain evaporation effects, but results would be similar otherwise. If we assume that  $R_{orig}$  is uniquely related to  $q_{orig}$  through a mixing line between the SCL air and a dry end-member ( $q_f$ ,  $R_f$ ):

$$q_{orig} = a \cdot q_0 + (1 - a) \cdot q_f \tag{A1}$$

5 and

$$R_{orig} = a \cdot q_0 \cdot R_0 + (1-a) \cdot q_f \cdot R_f \tag{A2}$$

Reorganizing Eq. (A1), we get  $a = \frac{r-p}{1-p}$  with  $p = q_f/q_0$ . Since  $q_f \le q_{orig} \le q_0$ ,  $p \le r_{orig}$ . Injecting Eq. (A2) into 6, we get:

$$R_0 = \frac{R_{oce}/\alpha_{eq} + p/(1-p) \cdot R_f \cdot \alpha_K \cdot (1-h_0)}{h_0 + \alpha_K \cdot (1-h_0)/(1-p)}$$
(A3)

As a consistency check, in the limit case where the end-member is totally dry (p = 0), we find the MJ79 equation, i.e. Eq. 10 (10).

It is intriguing to realize that  $r_{orig}$  has disappeared from Eq. (A3). This can be understood physically: if the vertical profile follows a mixing line, it does not matter at from which altitude the air comesfrom: ultimately, what matters is how much dry air has been mixed directly or indirectly into the SCL. This can be visualize in Fig. 4b. Therefore, if  $R_{orig}$  follows a mixing line, we lose the sensitivity to  $z_{orig}$ .

#### 15 Appendix B: Modification in case of Diagnostics for rain evaporation in LMDZ

An important assumption that led to Eq. (9)is the neglect of SCL moistening by rain evaporation. Here we test the sensitivity to this assumption by adding a rain evaporation component. The new water vapor Rain evaporation can be accounted for in equation 8 if we can quantify  $\eta$ , the ratio of water vapor originating from rain evaporation to that originating from surface evaporation, and  $\alpha_{evap}$ , the ratio of isotopic ratio in the rain evaporation flux to  $R_0$ .

## 20 B1 Equations

In LMDZ, two parameterization schemes can produce rain evaporation: the convective scheme and the large-scale condensation scheme. Their respective precipitation evaporation tendencies,  $(dq/dt)_{evap,conv}$  and isotopic budgets of the SCL write  $(dq/dt)_{evap,lsc}$ , are given in  $kg_{water} \cdot kg_{air}^{-1} \cdot s^{-1}$  and are used to calculate  $F_{evap}$  in  $kg_{water} \cdot m^{-2} \cdot s^{-1}$ :

 $M \cdot q_{orig} + F + E = (N+D) \cdot q_0$ 

$$F_{evap} = \sum_{k=1}^{k_{LCL}} \left( (dq/dt)_{evap,conv} + (dq/dt)_{evap,lsc} \right) \cdot \frac{\Delta P_k}{g}$$

$$M \cdot q_{orig} \cdot R_{orig} + F \cdot R_F + E \cdot R_E = (N+D) \cdot q_0 \cdot R_0$$

where F is the rain evaporation flux where  $k_{LCL}$  is the last layer below the LCL,  $\Delta P_k$  is the depth of layer k in pressure coordinate and q is gravity.

The isotopic equivalent of this flux,  $F_{svap,ise}$ , is used to calculate  $R_{svap} = F_{svap,ise}/F_{svap}$ . We note  $F = \eta \cdot E$ . We write the isotopic composition of the rain evaporation,  $R_F$ , as

Only grid boxes and days where  $F_{evap} > 0.05$  mm/d are considered to calculate  $\alpha_{evap}$ . This represents 94.0% of all tropical oceanic grid boxes.

## 10 B2 Results

5

Consistent with the larger amount of precipitation available for evaporation,  $\eta$  is maximum in regions of deep convection, reaching 30% around the Maritime continent (Fig. C1a). It is minimal over the dry descending regions, reaching 5% off the coasts of Mauritania, Peru or Namibia. The rain evaporation is more depleted than the SCL in regions of strong deep convection, by as much as 70‰ around the Maritime continent (Fig. C1b). When the fraction of raindrops that evaporate

15 is small, as is the case in such moist regions, isotopic fractionation favors evaporation of the lighter isotopologues. In these regions, rain evaporation has a depleting effect on the SCL, consistent with Worden et al. (2007). In contrast, in other regions, rain evaporation has a enriching effect on the SCL, up to 70‰ in dry regions. This is because in dry regions, rain evaporates almost totally, so that the evaporation flux has almost the same composition as the initial rain, which is more enriched than the water vapor.

## 20 Appendix C: Diagnostics for horizontal advection in LMDZ

We can account for horizontal advection in Eq. (8) if we can quantify parameters  $\phi = \frac{F_{adv} \cdot q_{adv}}{E}$ , the ratio of water vapor coming from horizontal advection to that coming from surface evaporation, and  $\beta = R_{adv}/R_0$ , the ratio of isotopic ratios of horizontal advection to that of the SCL.

## C1 Equations

Let's assume that the box representing the SCL has a zonal extent  $\Delta y$ , a meridional extent  $\Delta x$  and is composed of  $k_{LCL}$  layers of vertical extent  $\Delta z_k$ . The quantity  $F_{adv} \cdot g_{adv}$  represents the mass flux of water entering the grid box by horizontal advection per surface area, expressed in  $kg_{water} \cdot s^{-1} \cdot m^{-2}$ . Assuming an upstream advection scheme, it can be expressed as:

$$F_{adv} \cdot q_{adv} = \frac{\sum_{k=1}^{k_{LCL}} \left(\rho_k \cdot |u_k| \cdot q_{uk} \cdot \Delta y \cdot \Delta z_k + \rho_k \cdot |v_v| \cdot q_{vk} \cdot \Delta x \cdot \Delta z_k\right)}{\Delta x \cdot \Delta y} \tag{C1}$$

5 where  $u_k$  and  $v_k$  are the zonal and meridional wind components at layer k,  $\rho_k$  is the volumic mass of air at layer k, and  $q_{uk}$  and  $q_{vk}$  are the humidities of the incoming air from zonal and meridional advection at layer k. When  $u_k > 0$ ,  $q_{uk}$  is the humidity in the grid box to the West. When  $u_k < 0$ ,  $q_{uk}$  is the humidity in the grid box to the South. When  $v_k < 0$ ,  $q_{uk}$  is the humidity in the grid box to the South. When  $v_k < 0$ ,  $q_{uk}$  is the humidity in the grid box to the North.

Applying the hydrostatic equation at each layer ( $\Delta P_k = \rho_k \cdot g \cdot \Delta z_k$ , where g is gravity and  $\Delta P_k$  is the vertical extent of the 10 layer k in pressure coordinate), we get:

$$F_{adv} \cdot q_{adv} = \sum_{k=1}^{k_{LCL}} \frac{\Delta P_k}{g} \cdot \left(\frac{|u_k| \cdot q_{uk}}{\Delta x} + \frac{|v_k| \cdot q_{vk}}{\Delta y}\right)$$

The quantity  $F_{adv}$  represents the incoming air mass flux by horizontal advection, and  $q_{adv}$  represents the humidity of the incoming air. We can thus write them as:

$$F_{adv} = \sum_{k=1}^{k_{LCL}} \left( \frac{|u_k|}{\Delta x} + \frac{|v_k|}{\Delta y} \right) \cdot \frac{\Delta P_k}{g}$$

15 and

$$q_{adv} = \frac{\sum_{k=1}^{k_{LCL}} \left( \frac{|u_k|}{\Delta x} \cdot q_{uk} + \frac{|v_k|}{\Delta y} \cdot q_{vk} \right) \cdot \frac{\Delta P_k}{g}}{\sum_{k=1}^{k_{LCL}} \left( \frac{|u_k|}{\Delta x} + \frac{|v_k|}{\Delta y} \right) \cdot \frac{\Delta P_k}{g}}$$

The same budget as in Eq. C1 can be written for water isotopes:

$$F_{adv} \cdot q_{adv} \cdot R_{adv} = \frac{\sum_{k=1}^{k_{LCL}} \left( \rho_k \cdot |u_k| \cdot q_{uk} \cdot R_{uk} \cdot \Delta y \cdot \Delta z_k + \rho_k \cdot |v_v| \cdot q_{vk} \cdot R_{vk} \cdot \Delta x \cdot \Delta z_k \right)}{\Delta x \cdot \Delta y}$$

where  $R_{adv}$  represents the isotopic ratio of the incoming water vapor:

$$\mathbf{20} \quad R_{adv} = \frac{\sum_{k=1}^{k_{LCL}} \left( \frac{|u_k|}{\Delta x} \cdot q_{uk} \cdot R_{uk} + \frac{|v_k|}{\Delta y} \cdot q_{vk} \cdot R_{vk} \right) \cdot \frac{\Delta P_k}{g}}{\sum_{k=1}^{k_{LCL}} \left( \frac{|u_k|}{\Delta x} \cdot q_{uk} + \frac{|v_k|}{\Delta y} \cdot q_{vk} \right) \cdot \frac{\Delta P_k}{g}}$$

Note that the upstream advection scheme assumed here overestimates the effect of advection compared to the Van Leer (1977) advection scheme used in LMDZ. We thus estimate here an upper bound for the advection effect.

In practice, rather than calculating  $\beta = R_{adv}/R_0$ , we calculate  $\beta = R_{adv}/R_{SCL}$  where  $R_{SCL}$  is the isotopic ratio in average through the SCL:

5 
$$R_{\underline{F}SCL} = \underline{\alpha_{re} \cdot R_0} \frac{\sum_{k=1}^{k_{LCL}} q_k \cdot R_k \frac{\Delta P_k}{g}}{\sum_{k=1}^{k_{LCL}} q_k \frac{\Delta P_k}{g}}$$

where  $\alpha_{re}$  is an effective fractionation coefficient. For example, if droplets are formed near the cloud base, some of them precipitate and evaporate totally in the SCL (e. g. in non-precipitating shallow cumulus clouds), then  $\alpha_{re} = \alpha(T_{cloudbase})$ . In contrast, if droplets are formed in deep convective updrafts after total condensation of the SCL vapor, and then a very small fraction of the rain is evaporated in a very dry SCL, then  $\alpha_{re} = 1/\alpha(T_{SCL})/\alpha_K$  (Stewart, 1975). This prevents the advected

10 water vapor to be systematically more depleted when the mixed-layer hypothesis is not exactly verified.

Combining all equations, in the case of a logarithmic  $\delta D$  profile, we get:

## C2 Results

20

$$R_0 = \frac{R_{oce}}{\alpha_{eq}} \cdot \frac{1}{h_0 + \alpha_K \cdot (1 - h_0) \cdot \frac{1 - r_{orig}^{\alpha_{eff}}}{1 - r_{orig}} + \eta \cdot \alpha_K \cdot (1 - h_0) \cdot (1 - \alpha_{re})}$$

Parameter φ is maximum where winds are maximum, such as near the extra-tropics or in the North Atlantic (Fig. C1a).
Horizontal advection has an enriching effect in deep convective regions (probably because water vapor comes from nearby drier regions that have been less depleted by deep convection), and a depleting effect near the coasts (probably because of winds bringing vapor from the nearby land that is depleted by the continental effect) (Fig. C1b).

Rain evaporation can have a depleting or enriching effect depending on the sign of  $1 - \alpha_{re}$  (Fig Note that in this formulation, parameters  $\phi$  and  $\beta$  are resolution-dependent. For example, in a finer resolution,  $\phi$  would be larger and  $\beta$  would be closer to 1, but  $F_{adv} \cdot g_{adv} \cdot R_{adv}$  and thus the contribution of horizontal advection in Eq. (8) would remain the same.

## Appendix D: LMDZ free tropospheric profiles

The goal of this appendix is to document the spatio-temporal variability in the shape (section D1) and steepness (section D2) of simulated free tropospheric  $\delta D$  profiles. Note that a detailed interpretation of these profiles is beyond the scope of this paper. This paper aims at understanding  $\delta D_0$ , which is the first step towards understanding full tropospheric profiles. In turn,

- 25 understanding full tropospheric profiles in future studies will help refine our model for  $\delta D_0$ . 3 pink, blue). In the paper, we thus well neglect rain evaporation effects, to avoid dealing with such an unknown parameter as  $\alpha_{re}$ .
  - D1 Shape of tropospheric profiles



Figure C1. a) Ratio  $\eta$  of water in the SCL coming from rain evaporation to that coming from surface evaporation. b) Effective fractionation coefficient  $\alpha_{erap}$  between the SCL water vapor and the rain evaporation. c) Ratio  $\phi$  of water in the SCL coming from horizontal advection to that coming from surface evaporation. d) Effective fractionation coefficient  $\beta$  between the SCL water vapor and the water vapor coming from horizontal advection.

First, we test whether the  $\delta D$  vertical profiles simulated by LMDZ follow a Rayleigh or mixing line as a function of q. For the Rayleigh curve,  $\alpha_{eff}$  is estimated as explained in section 3.3. For the mixing line (appendix A), the end member  $(q_f, R_f)$  is also taken at 500 hPa.

The tropical-mean vertical  $\delta D$  profiles simulated by LMDZ is bounded by Rayleigh and mixing lines (Fig. D1a). To better 5 document the spatial variability in the shape of  $\delta D$  profiles, we plot parameter  $f = \frac{\delta D_{LMDZ} - \delta D_{Rayleigh}}{\delta D_{max} - \delta D_{Rayleigh}}$ , describing how close is the simulated  $\delta D$  ( $\delta D_{LMDZ}$ ) to the Rayleigh ( $\delta D_{Rayleigh}$ ) and mixing ( $\delta D_{mix}$ ) lines. We have f = 0 in case of a Raleigh line, f = 1 in case of a mixing line, and f > 1 if  $\delta D$  is more enriched than a mixing line. In the lower-troposphere,  $\delta D_{LMDZ}$  is close to a mixing line (and sometimes even more enriched) in deep convective regions (Indian Ocean, South Pacific Convergence Zone, Atlantic ITCZ), probably because deep convection efficiently mixes the lower troposphere. Elsewhere,

10  $\delta D_{LMDZ}$  is intermediate between the two lines (Fig D1e). In the middle troposphere,  $\delta D_{LMDZ}$  is relatively closer to Rayleigh everywhere (Fig D1b).

The daily variability of f is large everywhere and at all levels (Fig D1c,e), with standard deviation of 0.23 and 0.44 on tropical average at 1000 m and 4000 m respectively. A large daily variability in the shape of profiles is also observed in nature (Sodemann et al., 2017).

## 15 D2 Steepness of tropospheric profiles



**Figure D1.** a) Vertical profiles of water vapor  $\delta D$  simulated by LMDZ (black), calculated if assuming a Rayleigh-type curve with  $\alpha_{eff}$  estimated from  $(q_f, \delta D_f)$  at 500 hPa (green), calculated if assuming a Rayleigh-type curve with  $\alpha_{eff}(T)$  (dashed green) and calculated if assuming a mixing curve between the first layer and  $(q_f, \delta D_f)$  at 500 hPa (blue), in average over all tropical oceanic locations and days. b) Winter-mean map of parameter  $f = \frac{\delta D_{LMDZ} - \delta D_{Rayleigh}}{\delta D_{Rayleigh}}$  at 4000 m, i.e. slightly below 500 hPa where  $q_f$  and  $\delta D_f$  are taken. Parameter f describes how close is the simulated  $\delta D$  ( $\delta D_{LMDZ}$ ) to the Rayleigh ( $\delta D_{Rayleigh}$ ) and mixing lines ( $\delta D_{mix}$ ): f = 0 in case of a Raleigh line, f = 1 in case of a mixing line, and f > 1 if  $\delta D$  is more enriched than a mixing line. c) Standard deviation of parameter f among all days in winter of all years, at 4000 m, d) Same as b but at 1000 m, i.e. slightly above the LCL. e) Same as c but at 1000 m. To avoid numerical problems, only days and locations where  $|\delta D_{mix} - \delta D_{Rayleigh}| > 5\%$  are used in the calculations.



Figure D2. a)  $\alpha_{eff} = 1$ , where  $\alpha_{eff}$  is the effective fractionation coefficient, expressed in  $\infty$ . b)  $\alpha_{eg}(T) = 1$  expressed in  $\infty$ . All daily values are averaged over all days in winters of all years. c) Standard deviation of  $\alpha_{eff}$  among all days in winter of all years, expressed in  $\infty$ .

The steepness of the  $\delta D$  gradient from the surface to the middle troposphere is described by the parameter  $\alpha_{eff}$ . It is maximum in regions of deep convection, for example around the Maritime Continent (Fig. D2a). This is consistent with the maximum depletion simulated in deep convective regions in the mid-troposphere simulated by models (Bony et al., 2008), leading to steeper  $\delta D$  profiles. The pattern of  $\alpha_{eff}$  may also reflect horizontal advection effects, where strong isotopic gradients align with winds (e.g. from the Eastern to the Western Pacific, Dee et al. (2018)).

Values of  $\alpha_{eff}$  are of the same order of magnitude as real fractionation factors, but the spatial variations do not reflect those predicted if using a fractionation coefficient  $\alpha_{eq}$  as a function of temperature T (Fig. D2b).

The daily standard deviation of α<sub>eff</sub> (σ<sub>αeff</sub>) for a given season ranges from 5‰ in the Central Atlantic to 40‰ near the Maritime Continent (Fig. D2c). On average over all seasons and locations, daily α<sub>eff</sub> - 1 at a given location varies within
 ±25 % of its seasonal-mean mean value.

*Author contributions.* CR thought about the equations, ran the LMDZ simulations, made the analysis and wrote the manuscript. JG initiated the discussion on the subject and discussed regularly about the results. GR provided the STRASSE radiosoundings. FB provided insight and references about cloud processes. JG, GR and FB all gave comments on the manuscript.

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# Response to Co-editor report

## September 5, 2019

• P1, L8-10: These two sentence are quite difficult to follow and I would suggest to rephrase these. Do you mean "In the model delD0 is expressed as....."? What do you mean with "dampening hope"? I guess the sentence is not complete and thus confusing.

We now write: "In the model,  $\delta D_0$  is expressed as a function of  $z_{orig}$ , humidity and temperature profiles, surface conditions, a parameter describing the steepness of the  $\delta D$  vertical gradient and a few parameters describing rain evaporation and horizontal advection effects. We show that  $\delta D_0$  does not depend on the intensity of entrainment, in contrast to several previous studies that had hoped that  $\delta D_0$  measurements could help estimate this quantity."

• P1, L15: This paragraph should be combined with the previous paragraph.

 $\operatorname{Done}$ 

• P1: Since you do not have any copyright statement this line is obsolete and can be deleted.

OK

• P3, 6-7: Space between number and unit is missing. This should be corrected throughout the manuscript.

 $\operatorname{Done}$ 

• P3, L20: Here you should use the abbreviation "B15" you introduced before.

Done

• P11, Fig 4 caption: "If delD profiles follow a Rayleigh distillation....." Not entirely clear. I understand that this is the figure for the case where the delD profiles follow a Rayleigh distillation. I would clearly state that and write here e.g.: " (a) For the case where the delD profiles follow the Rayleigh distillation". Same holds than for the figure caption of (b).

Now we clarify by writing: "for the case where the tropospheric  $\delta D$  profile follow Rayleigh distillation (a) or a mixing line (b)."

• P13, Fig 5 caption: "\citetet" instead of "\citep" should be used here.

Done

• P13, L5: strato-cumulus -> stratocumulus (?)

OK, replaced everywhere

• P15, L2: table 1 -> Table 1

OK, replaced everywhere

• P15, L10: To avoid the double parentheses you should use in latex: \citep[e.g.][]{ref1,ref2} for the references.

Done

• P15, L7: Same here.

Done

• P17, L33: from higher in altitude -> from higher altitudes

Done

• P18, Fig 7 caption: For better readability I suggets the following changes a) -> (a) and in the text then instead of just a -> (a), Same holds for panel (b).

Corrected here and everywhere

• P19, Fig 8 legend: add a space between "season" and "location" so that it reads "(season, location)".

Done

• P19, Fig. 8: Why is the y-axes labelling at the right axes not done for all ticks?

Because the number of samples doesn't go beyond  $10^4$ . But we have now added all the tick labels.

• P20, Table 2: ascending -> Ascending

Corrected here and everywhere

• P24, Fig 11: Same here as for Foig 7.

OK

• Further, the writing of the z\_orig is a bit confusing. I would not write the r\_orig = 0.6 as subscript. I would suggest to write in parentheses z\_orig (r\_orig = 0.6).

Done everywhere

• P26, L14: increasingly higher in altitude -> increasingly higher altitudes

Done

• P29, L7: to -> too

Done

• P29, L25: space between parentheses and delD\_f obsolete.

 $\operatorname{Done}$ 

• P29, L26: use write the text first and then give the citations wit  $(e.g. on Islands such as ... (citep{ref1, ref2, ref3}))$ 

We now write: "(e.g. on Islands such as Hawaii or La Réunion: Galewsky et al., 2007; Bailey et al., 2013; Guilpart et al., 2017)."

We have improved the citation format everywhere.

• P29, L28: Finally, as fifth -> Finally, as a fifth

Done

• P30, L4: appendix -> Appendix

Done here and everywhere

• P30, L19: Benetti et al. (2015) -> B15

Done

• P30, L19: make explicit the -> make the explicit

Done

• P30, L28: hundreds -> hundred

Done

• P33, L3: visualize -> visualized. Further, I would rather write has been than can be since you have done it and shown in Fig. 4.

We write: "...into the SCL (Fig. 4b)."

• Fig C1 and D1: There are lost parentheses without content in the figure titles.

This was to mean there was no unit. Now we remove these parentheses, here and everywhere.