

Response to reviewers

August 28, 2019

Summary:

We thank both reviewers for their comments. As detailed in the point-by-point response below, we have done two major modifications to the manuscript:

1. Now we explicitly take into account rain evaporation and horizontal advection in our model. These effects are described as simply as possible in the main text, and technical details are given in appendix. This allows us to rigorously quantify these effects on δD_0 variations and to address all the related comments. This also simplifies the interpretation of r_{orig} variations. We also address explicitly the effect of rain evaporation and horizontal advection on z_{orig} estimates, and have modified our abstract and conclusion accordingly.
2. Now we better document and discuss the spatio-temporal variability of free tropospheric profiles. However, since this is not the core of the paper, and consistent with reviewer 1's suggestion, we have moved this discussion to the appendix.

1 Reviewer 1

We thank reviewer 1 for his/her comments.

This paper presents an analytical steady state vertical mixing model to investigate the controls on the water vapor isotopic composition in the subcloud layer over the tropical oceans. It is a nicely simple model that considers the most important processes, which are surface evaporation and vertical mixing and predicts the subcloud layer water vapour isotope composition from a combination of mass balance equations for all isotope species. I enjoyed reading this paper very much, I particularly like the approach chosen for testing this analytical model, which combines model simulation data and ship-based observations. The ideas presented in this paper are exciting and very valuable for upcoming large field campaigns in which isotope observations are planned in different parts of the lower troposphere.

I thus recommend minor revisions with the following minor points:

1) In the abstract it should be clearly stated that the proposed analytical model is a steady state formulation, which neglects horizontal gradients and thus the impact of horizontal advection.

- Regarding the steady state formulation. Now we write in the abstract: "The model relies on the assumption that δD profiles are steeper than mixing lines, and that the SCL is at steady state, restricting its applications to time scales longer than daily."
- Regarding horizontal advection. Now we account for it explicitly. We write in the abstract: "We extend previous simple box models of the SCL by prescribing the shape of δD vertical profiles as a function of humidity profiles and by accounting for rain evaporation and horizontal advection effects."

2) P. 1, L. 10: "When the air mixing into the SCL is lower in altitude it is moister": I think this is true most of the time and certainly in a climatological sense, but of course when including differential advection elevated moist layers can occur. I guess adding "it is generally moister" would make me very happy.

We modify as suggested.

43 3) P. 3, L. 4: Shouldn't cloud top cooling be mentioned here as well?

44
45 We modify as: "driven by cloud-top radiative cooling, mixing and evaporative cooling of droplets"

46
47
48 4) P. 5, L. 4: Neglecting the large-scale horizontal gradients in air properties, particularly in the trade wind
49 regions seems to me like a strong assumption. Given the sensitivity of dD to SST and the considerable SST gradient
50 across the North Atlantic, I find that this caveat could be discussed a bit more explicitly here.

51
52 We agree that the neglect of horizontal advection was an important caveat. Therefore, now we rigorously
53 estimate the effect of horizontal advection of isotopic gradients on our results. This is detailed in section 2 in the
54 main text. Eq. (8) provides the new equation for R_0 as a function of α , the ratio of water vapor coming from
55 horizontal advection to that coming from surface evaporation, and β , the ratio of isotopic ratios of horizontal
56 advection to that of the SCL.

57
58 Coming back to the effect of horizontal gradients in the North Atlantic: our figure 7h shows that the effect of
59 horizontal advection is not stronger in the North Atlantic than elsewhere. But it is larger near the Saharan coast. A
60 later comment from you can be used to explain this feature: section 4.1: "Horizontal advection is slightly enriching
61 in deep convective regions and depleting in coastal regions (e.g. off the coasts of California, Peru, Mauritania,
62 Namibia, India and Australia). For example, the Saharan layer in front of the North-Western African Coast leads
63 to a strong effect of horizontal advection there ([Lacour et al., 2017]). "

64
65 5) P. 5, L. 20: "qs is the saturation specific humidity at SST"
66 corrected

67
68 6) P. 6, L26: In the closure section and the discussion of the free tropospheric profile the role of horizontal
69 advection is again neglected. This is maybe a good assumption in the tropic but it should still be mentioned
70 explicitly.

71 Now we account for the effect of horizontal advection on δD_0 in our box model. However, our closure assumption
72 does not need to neglect horizontal advection. Horizontal advection effects are implicitly taken into account through
73 the α_{eff} : we now clarify this: section 2.2: "Effects of horizontal advection and rain evaporation are encapsulated
74 into α_{eff} . "

75
76 7) P. 8, L26: "Depending on microphysical details that are too complex to be addressed here", Graf et al. 2019
77 could be referenced here

78 We add this reference.

79
80 8) P. 9. Fig. 3: Which value was chosen for the SST? This could be mentioned in the caption as well as a
81 reference to which equilibrium fractionation factor was used

82
83 We add this information in the caption: "For this illustrative purpose, we assume SST=30°C, $h_0 = 0.8 \delta D_{oce} =$
84 0‰ and $\phi = \eta = 0$. ". We also add it to Fig. 4.

85
86 9) P. 12, L. 2: "However, if the end member is defined below 500 hPa (e.g. 600 hPa), results are not always
87 reasonable", why is this so?

88
89 Now we explain this in the text: section 3.3: "However, the end member should be defined above 500 hPa to
90 ensure that it is well above boundary layer processes. If the end member is defined below 500 hPa (e.g. 600 hPa),
91 there are a few cases where q increases with altitude ($q_f > q_0$) due to horizontal advection or convective detrainment
92 from nearby moister regions. Meanwhile, δD decreases monotonically, leading to unrealistic values for α_{eff} ."

93
94 10) P. 12, L. 7: In my opinion, this makes it difficult to interpret rorig. But probably there are conditions
95 when rorig and thus zorig are more physically meaningful than others. Could the authors maybe add a list with
96 explicit and quantitatively expressed conditions in which they would argue that the assumptions involved in Eq. 9
97 are satisfied?

99 Now we explicitly account for rain evaporation and horizontal advection. Equations are given in the main text,
 100 so anyone can calculate these effects in their own cases. The contributions of these effects are plotted as maps in
 101 Fig. 7 g and h, and as composites as a function of ω_{500} and EIS in Fig. 8. Table 2 compares the effect of r_{orig}
 102 if these effects are neglected or not. The effect of rain evaporation and horizontal advection on z_{orig} estimates are
 103 plotted in Fig. 14b.

104 Note that a list of conditions would not be easy, since the effect of rain evaporation depends on parameters η
 105 and α_{evap} which are very difficult to estimate in nature, and horizontal advection depends on parameters ϕ and β
 106 which are resolution-dependent and depend on several variables (wind, humidity and δD profiles in the SCL).

107
 108 11) P. 13, L. 4-5: Is there a literature reference that the authors could indicated for this calculation of zi from
 109 observations?

110
 111 We now give several literature references and more explanation on this calculation method: section 3.4: “The
 112 temperature inversion is an abrupt increase in temperature that caps the boundary layer. Therefore, a method
 113 to automatically estimate its altitude is to detect a maximum in the vertical gradient of potential temperature
 114 ([Stull, 1988, Oke, 1988, Sorbjan, 1989, Garratt, 1994, Siebert et al., 2000]). This method is sensitive to the res-
 115 olution of vertical profiles ([Siebert et al., 2000, Seidel et al., 2010]). Therefore, we adapted this method in order
 116 to yield z_i values that best agree with what we would estimate from visual inspection of individual temperature
 117 profiles. In LMDZ, we calculate z_i as the first level at which the vertical potential temperature gradient exceeds
 118 3 times the moist-adiabatic lapse rate. In observations, we calculate z_i as the first level at which the vertical
 119 potential temperature gradient exceeds 5 times the moist-adiabatic lapse rate, because radio-soundings are noisier
 120 than simulated profiles. ”

121
 122 12) P. 13, L. 15: I did not immediately understand what was meant by composites belonging to a given interval
 123 of omega500, I was expecting a map. A reference to the results figure referred to here would have helped me.

124
 125 We now explain better how the composites are calculated, and we add a reference to Fig. 10 as an example.
 126 Section 3.5: “The type of clouds and mixing processes depends strongly on the large-scale velocity at 500 hPa (ω_{500} ,
 127 map shown in Fig. 6a), with shallow clouds in subsiding regions and deeper clouds in ascending regions (Fig. 1).
 128 Therefore, it is convenient to plot variables as composites as a function of ω_{500} ([Bony et al., 2004]). To make such
 129 plots, we divide the ω_{500} range from -30 to 50 hPa/d into intervals of 5 hPa/d. In each given interval, we average
 130 all seasonal-mean values at all locations over tropical oceans for which seasonal-mean ω_{500} belongs to this interval
 131 (e.g. Fig. 10a will be an example). .

132 The cloud cover strongly correlates with the inversion strength, which can be quantified by the Estimated
 133 Inversion Strength (EIS, [Wood and Bretherton, 2006], map shown in Fig. 6b) as a measure of inversion strength.
 134 We thus also plot variables as composites as a function of EIS. To make such plots, we divide the EIS range from
 135 -1 K to 9 K into intervals of 0.5K. In each given interval, we average all seasonal-mean values at all locations over
 136 tropical oceans for which seasonal-mean EIS belongs to this interval (e.g. Fig. 10b will be an example). “

137
 138 13) P. 13, L. 22: By how much (range of variability) were the four factors varied?

139
 140 The four factors were varied from a control value to their simulated value.

141 Now we explain better the calculation with the contribution of r_{orig} as an example, and we give all equations
 142 for other contributions in Table 1. Section 3.6: “To understand what controls the δD_0 spatio-temporal variations,
 143 δD_0 is decomposed into 4 contributions based on Eq. (8). First, we define $r_{orig,bas} = 0.3$, $\alpha_{eff,bas} = 1.09$
 144 , $SST_{bas} = 25^\circ\text{C}$, $h_{0,bas} = 0.7$, $\phi_{bas} = 0$, $\eta_{bas} = 0$, $\beta_{bas} = 1$ and $\alpha_{evap,bas} = 1$ as a basic state. We call
 145 $\delta D_{0,func}(r_{orig}, \alpha_{eff}, SST, h_0, \phi, \beta, \eta, \alpha_{evap})$ the function giving δD_0 as a function of r_{orig} , α_{eff} , SST, h_0 , ϕ , β , η and
 146 α_{evap} following Eq. (8), and $\delta D_{0,bas} = \delta D_{0,func}(r_{orig,bas}, \alpha_{eff,bas}, SST_{bas}, h_{0,bas}, \phi_{bas}, \beta_{bas}, \eta_{bas}, \alpha_{evap,bas})$. The rel-
 147 ative contribution of r_{orig} to δD_0 is estimated as $\delta D_{0,func}(r_{orig}, \alpha_{eff,bas}, SST_{bas}, h_{0,bas}, \phi_{bas}, \beta_{bas}, \eta_{bas}, \alpha_{evap,bas}) -$
 148 $\delta D_{0,bas}$. Similarly, the contributions of α_{eff} , SST, h_0 , ϕ and η are to δD_0 are estimated as detailed in Table 1. All
 149 the contributions have the same units as δD_0 (%).”

150
 151 14) P. 14, Section 4.1: This section seemed very technical for me. I also see it more as a methodological aspect
 152 than a result. I would recommend to either shift it to a technical appendix (since the paper is quite long) or to the
 153 methods section.

155 We have now shifted this section to the appendix D.2. We have deeply modified this section to address comments
156 from you and the other reviewer.

157
158 15) P. 15, Fig. 7: Mention that these are different random (?) grid points in the caption. I would have liked
159 a more general evaluation also describing the temporal and spatial variability in the vertical profiles simulation by
160 LMDZ.

161
162 We have removed this figure, which was misleading, and replaced it by a more general documentation of the
163 temporal and spatial variability in vertical profiles simulated by LMDZ, to address this comment and those from
164 the other reviewer. This discussion is in appendix D: “LMDZ free tropospheric profiles”. We add a figure showing
165 maps of a parameter $f = \frac{\delta D_{LMDZ} - \delta D_{Rayleigh}}{\delta D_{mix} - \delta D_{Rayleigh}}$ at 1000 m and 4000 m, representing how close is the simulated δD
166 compared to the Rayleigh and mixing lines (Fig. 16b,d). This documents the spatial variability in the shape of δD
167 profiles. To document the temporal variability, we add maps of the standard deviation of f (Fig. 16c,e).

168
169 16) P. 15, L. 3: could the authors mention the region where they think that alphaeff may also reflect horizontal
170 advection effects?

171
172 We now quantify the effect of horizontal advection on δD_0 , i.e. in the SCL. However, the effect of horizontal
173 advection on α_{eff} is a completely different subject that is beyond the scope of this paper. Therefore, we only reply
174 based on the literature: in appendix D: “The pattern of α_{eff} may also reflect horizontal advection effects, where
175 strong isotopic gradients align with winds (e.g. from the Eastern to the Western Pacific, [Dee et al., 2018]). “

176 To clarify the scope of this paper, we start appendix D by stating: “The goal of this appendix is to document
177 the spatio-temporal variability in the shape and steepness of simulated free tropospheric δD profiles. Note that a
178 detailed interpretation of these profiles is beyond the scope of this paper. This paper aims at understanding δD_0 ,
179 which is the first step towards understanding full tropospheric profiles. In turn, understanding full tropospheric
180 profiles in future studies will help refine our model for δD_0 .”

181
182 17) P.16: I find it interesting that the mixing and Rayleigh lines have large biases in front of the eastern
183 continental boundaries where the inversion is strongest and, where there is a strong decoupling between the FT
184 and BL. In particular in these regions, I would expect horizontal advection to play a key role, (e.g. the SAL layer
185 in front of the eastern North African Coast, see Lacour et al. 2017, ACP). Maybe the authors find a good way to
186 shortly note this in the text.

187
188 The map showing RMS errors was misleading. For example, if the simulated δD behaves smoothly and is half-
189 way between Rayleigh lines and mixing lines, it will result in local maxima in RMS values, but when we plot the
190 new parameter $f = \frac{\delta D_{LMDZ} - \delta D_{Rayleigh}}{\delta D_{mix} - \delta D_{Rayleigh}}$, representing how close is the simulated δD compared to the Rayleigh and
191 mixing lines, nothing special emerges. This is the case in front of the Saharan coast. Therefore, we have not added
192 this discussion here.

193 However, this comment is relevant for interpreting horizontal advection effects on δD_0 : “Horizontal advection is
194 slightly enriching in deep convective regions and depleting in coastal regions (e.g. off the coasts of California, Peru,
195 Mauritania, Namibia, India and Australia). For example, the Saharan layer in front of the North-Western African
196 Coast lead to a strong effect of horizontal advection ([Lacour et al., 2017]).”

197
198 18)P. 17, L. 2: Maybe one could add oceanic upwelling and atmospheric deep convection. Jumping from
199 upwelling to deep convection in the same sentence, I was not sure whether deep convection in the ocean or the
200 atmosphere was meant here.

201
202 We modify as suggested.

203
204 19) P. 17, L. 4: “Decreases as omega500 is more strongly ascending or descending” -> “with increasing vertical
205 winds (omega500) of both signs”

206 We modify as suggested.

207
208 20) P. 17, L. 11: “in more ascending regions” -> a reference to Fig. 8d would have helped me here.

209 We add this reference

211 21) P. 17, L. 25: “The fact that the effect...” I had difficulties to understand this sentence.

212
213 We remove this sentence that was not so useful.

214
215 22) P. 17, L. 33: h_0 (62%) is the largest explained fraction of all the variables considered and should thus be put
216 first. This could be a hint that large-scale horizontal advection plays an important role at the synoptic timescale
217 in these regions.

218
219 The numbers have changed because (1) we now account for rain evaporation and horizontal advection, and
220 (2) we now add an additional condition to make our calculation: section 3.1: “to avoid numerical problems when
221 estimating effect of horizontal advection and rain evaporation, only grid boxes and days where $E > 0.5$ mm/d are
222 considered. This represents 99.7% of all tropical oceanic grid boxes.”

223 With the new values, the effect of h_0 is reduced and the effect of r_{orig} is enhanced (table 3). Section 4.1: “In
224 subsiding regions, the effect of SST is muted due to its slow variability, and r_{orig} (82 %) becomes the main factor.
225 “

226
227 23) P. 19, Fig. 10: The bin sizes (number of data points per bin should be added).

228 We now add this information in Fig 8, and we write in the caption: “The number of samples in each bin is
229 indicated on a logarithmic scale on the right-hand-side (dotted black line).”

230
231 If I understood correctly from the caption, the authors used the seasonal averaged fields from LMDZ. Why not
232 making these composites using the 6-hourly outputs? For me there is a timescale discrepancy between the processes
233 (mixing, evaporation) that the authors look at and the averaging timescale of the used fields.

234
235 The composites are based on seasonal-mean EIS or ω_{500} because this allows a better link with the large-scale
236 dynamical regime. Mixing and evaporation are processes that act at short time scales, but their relationship to the
237 large-scale circulation is best constrained by energetics at time scales longer than synoptic. Let’s consider ω_{500} , for
238 example. It relates to convective activity and other diabatic processes through the conservation equation of moist
239 static energy. Adiabatic cooling by large-scale ascent balances latent heating by convection ([Yanai et al., 1973]),
240 or adiabatic heating by large-scale subsidence balances radiative cooling ([Emanuel et al., 1994]). The stationarity
241 in the conservation of moist static equation is most valid at time scales longer than synoptic, otherwise, the storage
242 term becomes important ([Masunaga and Sumi, 2017]). This is why in [Bony et al., 2004] and subsequent papers
243 (e.g. [Bony et al., 2013]) based on ω_{500} , monthly-mean ω_{500} is used, which yields similar results to seasonal-mean.

244 A similar rationale applies to EIS. This is why many papers on EIS use seasonal-mean values, notably the paper
245 defining this quantity ([Wood and Bretherton, 2006]).

246
247 We now explain this in section 3.5: “Note that such composites are done on seasonal-mean ω_{500} because cloud
248 processes and their associated diabatic heating are tied to the large-scale circulation through energetic constrains
249 ([Yanai et al., 1973, Emanuel et al., 1994]) that are best valid at longer time scales (otherwise, the energy storage
250 term may become significant, e.g. [Masunaga and Sumi, 2017]). This is why ω_{500} is generally averaged over a month
251 or longer (e.g. [Bony et al., 1997, Williams et al., 2003, Bony et al., 2004, Wyant et al., 2006, Bony et al., 2013]).
252 In addition, we primarily focus on understanding the seasonal and spatial distribution of δD_0 .”

253 and for EIS: “Using seasonal-mean values is consistent with [Wood and Bretherton, 2006] and with the better
254 link at longer time scales between cloud processes and the large-scale dynamical regime.”

255
256 In addition, we do not look at the diurnal variations: the stationarity assumption in our simple model would be
257 violated. We now explain this in the abstract: “the steady-state assumption restricts the application of this model
258 to time scales longer than daily.” and in section 2.1: “We assume that the SCL is at steady state. For example, its
259 depth is constant. Since the SCL properties may exhibit a diurnal cycle ([Duynderke et al., 2004]), this hypothesis
260 restricts the application of this model to time scales longer than daily. “

261
262 24) P. 27, L. 28: a reference to a more technical paper such as Aemisegger et al. 2012 AMT, would be nice here.

263 We add this reference

264 Small technical comments:

265 1) P. 2, L. 22 : “suffers from a low bias”

- 266 2) P. 3, L. 28: “capturing **the** second-order...”
 267 3) P. 8, L. 26: no parenthesis after B)
 268 4) P. 12, L.7: “based” -> “biased”
 269 5) P. 15, L. 1: Figure 8d
 270 6) P. 15, L. 4: “Values **of** alphaeff...”
 271 7) P. 15, L. 5: using a fractionation coefficient alpha eq **as** a function of temperature”
 272 8) P. 17, L. 14: space missing between rorig and (
 273 9) P. 18, L. 1: “Overall, **the** results...”
 274 We correct all these mistakes.
 275 10) In general, the authors do not consistently use B15 for Benetti et al. (2015)
 276 We now use B15 consistently.
 277
 278 11) P. 21, L. 2: “with **the** strongest inversion”
 279 12) P. 27, L. 27: measurement errors
 280 13) P. 28, L. 2: “if **we** measure...”
 281 14) P. 29, L. 14: very precise
 282 15) P. 30, L. 11: **from** which altitude the air comes
 283 We correct all these mistakes.

284 2 Reviewer 2

285 We thank reviewer 2 for his/her comments.

286
 287 This paper presents a simple box model solving the water isotope budget in the sub-cloud layer to quantify the
 288 relative contributions of sea surface temperature, relative humidity, mid-tropospheric depletion, and the fraction
 289 of moisture from the free troposphere (r_{orig}) on the variability of δD in near-surface water vapor (δD_0). The
 290 contribution of r_{orig} is further separated into contributions of specific humidity at the surface, and the height
 291 (z_{orig}), relative humidity and temperature from which the free tropospheric air originates. z_{orig} is found to be an
 292 important factor explaining the seasonal-spatial and daily variations of δD_0 . This means that measurements of
 293 δD_0 , if precise enough, can potentially be used to estimate z_{orig} and distinguish between different mixing processes
 294 in the atmosphere.

295 The paper is interesting and well written, and it nicely demonstrates the use of measuring water vapor isotopes
 296 on short time scales. The box model’s theoretical framework is described in detail and its drawbacks are clearly
 297 identified by the authors. I only have a few comments about the methods, the rest are mainly ideas for clarifying
 298 the paper. I recommend that the paper be published after minor revisions.

299 General comments

300 1) I like the method for quantifying the contributions of different factors by linear regression. I see how this works
 301 when the contributing factors have the same units as the variable of interest, which was the case in the previous
 302 studies that used this method and are cited in this paper (Risi et al. 2010, Oueslati et al., 2016). Here the different
 303 factors all have different units, and the slope therefore depends on the units, or how much the components vary. I
 304 assume this was accounted for somehow, as the slopes in the tables are all unitless, but it is not clear from the text,
 305 and makes me a bit skeptical about the results. More explanation on that would be useful.

306
 307 The contributing factors have the same units as the variable of interest, i.e. permil. We now clarify this
 308 in the text. We also explain better the calculation with the contribution of r_{orig} as an example, and we give
 309 all equations for other contributions in Table 1. Section 3.6: “To understand what controls the δD_0 spatio-
 310 temporal variations, δD_0 is decomposed into 4 contributions based on Eq. (8). First, we define $r_{orig,bas} = 0.3$,
 311 $\alpha_{eff,bas} = 1.09$, $SST_{bas} = 25^\circ\text{C}$, $h_{0,bas} = 0.7$, $\phi_{bas} = 0$, $\eta_{bas} = 0$, $\beta_{bas} = 1$ and $\alpha_{evap,bas} = 1$ as a basic state. We call
 312 $\delta D_{0,func}(r_{orig}, \alpha_{eff}, SST, h_0, \phi, \beta, \eta, \alpha_{evap})$ the function giving δD_0 as a function of r_{orig} , α_{eff} , SST, h_0 , ϕ , β , η and
 313 α_{evap} following Eq. (8), and $\delta D_{0,bas} = \delta D_{0,func}(r_{orig,bas}, \alpha_{eff,bas}, SST_{bas}, h_{0,bas}, \phi_{bas}, \beta_{bas}, \eta_{bas}, \alpha_{evap,bas})$. The rel-
 314 ative contribution of r_{orig} to δD_0 is estimated as $\delta D_{0,func}(r_{orig}, \alpha_{eff,bas}, SST_{bas}, h_{0,bas}, \phi_{bas}, \beta_{bas}, \eta_{bas}, \alpha_{evap,bas}) -$
 315 $\delta D_{0,bas}$. Similarly, the contributions of α_{eff} , SST, h_0 , ϕ and η are to δD_0 are estimated as detailed in Table 1. All
 316 the contributions have the same units as δD_0 (‰).”.

317

2) As stated in the paper, the methods rely on the assumption that the δD profile follows a Rayleigh-like line, and that there is no effect of rain evaporation. Figures 7 and 8 show that the δD profile is often closer to a mixing line than a Rayleigh line, and the large contribution of r_{orig} mainly comes from ascending regions, where clouds are most likely precipitating. It would be nice to see some quantification of how this impacts the results. A possible way to do this is to remove days/locations where the RMSE of the mixing line is smaller than the RMSE of the Rayleigh line and where there is precipitation, then repeat the analysis for these new fields and add the results in brackets in Tables 1, 2 and as dotted lines in Figures 10, 12.

- Effect of rain evaporation. Now we explicitly account for the effect of rain evaporation. Equations are given in the main text. The contributions of this effect are plotted as maps in Fig. 7g, and as composites as a function of ω_{500} and EIS in Fig. 8. Table 2 compares the effect of r_{orig} if rain evaporation and horizontal advection are neglected or not. The effect of rain evaporation on z_{orig} estimates are plotted in Fig. 14b.
- Effect of the deviation of the δD profile from a Rayleigh distillation line. This is more difficult to quantify. Now we discuss this in detail in the discussion section: subsection 6.5 untitled “Rayleigh assumption for the shape of δD profiles”: “Finally, a fifth source of uncertainty comes the assumption that the δD profile follows a Rayleigh distillation line (section 2.2). However, both in LMDZ (appendix D) and nature ([Sodemann et al., 2017]), δD profiles are usually intermediate between Rayleigh and mixing lines. The precision of our z_{orig} estimate is maximum in the Rayleigh distillation case. When trying to directly find a numerical solution for z_{orig} from Eq. (6), a solution can be found only in 0.1 % of cases. This is because... However, it is possible that δD profiles simulated by LMDZ are closer to mixing lines than real profiles, since GCMs are known to overestimate vertical mixing through the troposphere ([Risi et al., 2012]) and to mix the lower free troposphere too frequently by deep convection in trade-wind regions ([Nuijens et al., 2015b, Nuijens et al., 2015a]). Therefore, the shape of δD profiles simulated by LMDZ is not a sufficient reason to reject the Rayleigh assumption. The uncertainty associated with this assumption is very difficult to quantify in LMDZ. More measurements of full δD profiles are very welcome to help quantify it.”

3) The paper presents the new box model as an extension of the model by Benetti et al. (2015), which is technically true, but can be a bit misleading because its application is different. Rather than predicting δD_0 from z_{orig} , it predicts z_{orig} from δD_0 and therefore requires δD_0 to be known. This means it cannot be applied to initialize Rayleigh models like the model by Benetti et al. (2015), which assumes constant z_{orig} . This could be written more clearly (e.g., from the abstract it seems like the model can be used to predict δD_0 , which is only possible if z_{orig} is known).

The model can be used both ways, either to predict δD_0 as a function of z_{orig} , or to estimate z_{orig} from δD_0 . We now clarify this:

- in the abstract: “The model express δD_0 as a function of z_{orig} , humidity and temperature profiles, surface conditions a parameter describing the steepness of the δD vertical gradient and a few parameters describing rain evaporation and horizontal advection effects.”
- in section 2.2: “If the goal is to predict R_0 from z_{orig} , we can apply Eq. (6) if we know the q and δD vertical profiles. Conversely, if the goal is to predict z_{orig} from R_0 , we can numerically solve Eq. (6) if we know the q and δD vertical profiles.”

4) Changing some of the colors and colormaps could make the figures easier to understand. For example, I think the contributions of different factors and how they add up in Figures 9 and 11 would be more intuitive with a perceptually uniform colormap going from light to dark colors. Also, the red and pink lines in Figures 3, 4, 7, 10, 12, 15 look very similar to each other. It would be good to use a different color for one of them.

- Now all maps are colored in shaded of blue for negative values and shaded of red for positive values.
- We now change the line color from pink to purple to distinguish it from red (Figures 3, 4, 5), or from red to dark red to distinguish it from pink (Figures 8, 10, 13).

368 Specific comments

369 P1 L13: [D]/[H] instead of [HDO]/[H2O]

370 We modify.

371

372 P2 L22: high bias instead of low bias?

373 Corrected.

374

375 P2 L30: Please introduce the abbreviation for LCL

376 Done.

377

378 P3 L4: pointed **out** the important role

379 Corrected.

380

381 P3 L15: “We do not call it entrained”: The word entrained/entrainment still appears a few times in the text
382 (e.g. in Fig. 2, the title of section 4.4)

383 We modify all the occurrences of “entrainment”, except when it really refers to entrainment.

384

385 P3 L23: during **a** field campaign, global outputs **of** an isotope-enabled GCM.

386 Corrected.

387

388 P3 L24: “at the global scale”: Really? There are no global maps. Are the numbers in Tables 1, 2 and the lines
389 in Figures 10, 12 from global output, or from the region shown on the maps?

390 We now modify by “in the Tropics”. We precise in the captions for these Tables and Figures: “All seasons and
391 locations over tropical oceans ($30^{\circ}N - 30^{\circ}S$, ocean fraction $> 80\%$) are considered.”

392

393 P3 L28: capturing **the** second-order parameter d-excess

394 Corrected.

395

396 P3 L32: “MJ79 already performs quite well for d-excess”: Pfahl and Wernli (2009) would probably disagree.

397 Now we modify as (section 1.3): “In addition, the need for an extension of MJ79 is more needed for δD than for d-
398 excess, since the effect of convective mixing is larger on δD than on d-excess ([Risi et al., 2010, Benetti et al., 2014]).”

399 This does not contradict Pfahl and Wernli (2009).

400

401 P5 L23: $r \rightarrow r_{orig}$

402 Corrected.

403

404 P6 L20: measurements

405 Corrected.

406

407 P6 L20: “Therefore, variations of δD_0 that are mediated by q_0 or h_0 do not interest us”: But δD in the FT is
408 prescribed as a function of q (confusing).

409 We remove this confusing sentence and we write (section 2.1): “We attempt to express neither h_0 as a function
410 of q_0 as in B15, and nor the q profile as a function of q_0 ”.

411

412 P8 L11: Refer to l’Hopital’s rule?

413 Now we add: “(L’Hopital’s rule was used to calculate this limit).” (section 2.2°

414

415 P8 L21: follows as mixing line

416 Corrected.

417

418 P9: Fig.3: $\alpha_{eff} = \alpha_{eq}$ instead of $\alpha_{eff} = 1/\alpha_{eq}$

419 Corrected.

420

421 P11 L25: “Only profiles during the ascending phase of the balloons are considered”: (Why?)

422

423 We now justify this choice: “Only profiles during the ascending phase of the balloon are considered, because the
424 descent phase is often located far away from the initial launch point ([McGrath et al., 2006, Seidel et al., 2011]). “
425 (section 3.2)

426
427 **P11 L27 (title): write somewhere that these results are based on LMDZ output (not observations)**

428 Now we write (section 3.3): “Here we explain how z_{orig} is estimated based on LMDZ outputs.”. Later in the
429 section, we write: “When estimating z_{orig} from observations, we follow the same methodology except that...”.

430
431 **P12 Fig. 5: Describe abbreviations (LCL, EIS, SCL) in caption.**

432 Done

433
434 **P12 L2: “if the end member is defined below 500hPa (e.g. 600hPa) results are not always reasonable”: In what
435 sense? Why?**

436 Now we write: “However, the end member should be defined above 500 hPa to ensure that it is well above
437 boundary layer processes. If the end member is defined below 500 hPa (e.g. 600 hPa), there are cases where q
438 increases with altitude ($q_f > q_0$) due to horizontal advection or convective detrainment from nearby moister regions;
439 meanwhile, δD decreases monotonically, leading to unrealistic values for α_{eff} .”

440
441 **P15 Fig. 7: What meteorological conditions do these examples represent? Would it be possible to show
442 all (/more) simulated profiles in the background, e.g. in some transparent color, to get a better feeling for the
443 variability? Also, I suggest adding markers to highlight where the levels are.**

444
445 We have removed this figure, because it was misleading. We replace it by Fig. 16 in appendix D to better docu-
446 ment the temporal and spatial variability in free tropospheric profiles. Maps show parameter $f = \frac{\delta D_{LMDZ} - \delta D_{Rayleigh}}{\delta D_{mix} - \delta D_{Rayleigh}}$
447 describing whether simulated δD is closer to Rayleigh line or a mixing line (Fig 16b,d). We also show maps for the
448 standard deviation of f to illustrate the temporal variability (Fig 16 c,e).

449 In addition, markers are added in Fig 16a to highlight the model levels.

450
451 **P15 L1: Figure 8d instead of 8c.**

452 Corrected

453
454 **P15 L5: α_{eq} as a function of temperature**

455 Corrected

456
457 **P16 Fig. 8: in boreal winters of all years**

458 Corrected

459
460 **P17 L22: “in the cold upwelling regions”: for example where?**

461 Now we add: “cold upwelling regions, for example off Peru or Namibia” (section 4.1)

462
463 **P17 L23: probably reflects**

464
465 This sentence was removed because r_{orig} cannot reflect rain evaporation any more.

466
467 **P17 L24: “the effect of r_{orig} can be seen on the composites as a function of EIS and not as a function of ω_{500} ”:**
468 **I don’t see this, please elaborate.**

469 This sentence was removed.

470
471 **P17 L30: followed by h_0 (23%), r_{orig} (16%), ...**

472 Corrected

473
474 **P18 Fig. 9: Are the correlations significant everywhere? Otherwise, add hatching where not significant?**

475
476 In this figure (now Fig. 7), we do not show the correlations, but rather the contributions to δD_0 on a ‰ scale.
477 We now explain better in the text how these contributions are calculated (section 3.6), and we add table 1 to give
478 the exact equations used to calculate each contribution.

479 The spatial-seasonal correlations are shown in Table 2. We now write between brackets when correlations are
480 not statistically significant at 99%. We write in the caption: “The threshold for the correlation coefficient to be
481 statistically significant at 99 % is 0.15 or lower in all cases. We write correlation coefficient and slope values between
482 brackets when they are not significant at 99%.”

483
484 P19 Fig.10: ω_{500} (hPa/d)
485 Corrected

486
487 P20 Tab. 2: q_0 seems to be important in Fig. 12, but the slope is 0.0 here, h_0 seems to be unimportant in Fig.
488 12 but slope is 0.91 here. Why is that?

489 We now explain this: section 4.2: “Note that this effect can be seen only in most stable regions, but when
490 considering all subsiding regions, the contribution is small (Table 2). “

491
492 P20 L1: “it would translate into a lower z_{orig} .”: Why?

493
494 For example, in case of deep convection with depleting rain evaporation, a larger r_{orig} is necessary to match the
495 depleted δD_0 , and a lower z_{orig} is necessary to match this large r_{orig} .

496 Now this sentence is removed, since we explicitly account for rain evaporation and horizontal advection. We
497 do not need this kind of rationale any more.

498
499 P22 Fig.12: ω_{500} (hPa/d)
500 Corrected

501
502 P25 L6: the cruises goes
503 Corrected

504
505 P25 L8: “when considering only the 6 data points when $z_{orig} < 2000\text{m}$ ”: Rationale behind this?

506
507 We now clarify what we mean: section 5: “Remarkably, there are 6 days when z_{orig} coincides with z_i with a root
508 means square error of 31‰ and correlation coefficient of 0.996 (Fig. 15c). This indicates that the air exactly comes
509 from the inversion layer. When recalling that z_{orig} and z_i are estimated from completely independent observations,
510 the coincidence is remarkable and lends support to the fact that on these days, our z_{orig} estimate is physical.
511 However, there remains 9 days when z_{orig} is much higher than z_i . This may reflect more penetrative downdrafts as
512 we approach deeper convective regimes. But it may also be an artifact of our neglect of horizontal advection. For
513 example, on these days which are characterized by lower h_0 , neglecting the advection of enriched water vapor from
514 nearby regions with higher h_0 could be mis-interpreted as lower r_{orig} and thus higher z_{orig} . ”.

515
516 P25 L14: ... at the seasonal-spatial and daily scale is the proportion of the water vapor in the SCL that is
517 originates from above
518 Corrected

519
520 P26 Fig. 15: $r \rightarrow r_{orig}$
521 Corrected

522
523 P27 L1: there \rightarrow they
524 Corrected

525
526 P27 L13: the **temporal** variability of α_{eff} . Is it possible to estimate the uncertainty from the spatial variability
527 of α_{eff} as well (in the vertical, i.e. how much the δ profile differs from a Rayleigh line with constant α_{eff})?

528
529 We now better document the spatio-temporal variability in the shape of free tropospheric δD profiles in the
530 appendix D.1. To address this specific comment, we now plot parameter $f = \frac{\delta D_{LMDZ} - \delta D_{Rayleigh}}{\delta D_{mix} - \delta D_{Rayleigh}}$ describing whether
531 simulated δD is closer to Rayleigh line or a mixing line. We show vertical profiles and maps of f at both 1000 m
532 and 4000 m (Fig 16 b,d).

533 We tried to compare the z_{orig} estimate with and without the assumption that the δD profile follows a Rayleigh
534 line. However, it didn’t work as well as expected. We now explain this when examining all errors on z_{orig} (section

535 6.5): “When trying to find a numerical solution for z_{orig} directly from Eq. (6), a solution can be found only in
536 0.1 % of cases.”. We explain why, and we also explain why it may work better in nature.

537

538 **P27 L21: estimating z_{orig} from δD_0 measurements on a daily basis (?)**

539

540 Now we write: “estimating z_{orig} from daily δD_0 measurements cannot be useful unless we measure δD profiles
541 on a daily basis as well.”

542

543 **P28 L2: and if we measure**

544 Corrected

545

546 **P28 L3: swap trade-wind cumulus and strato-cumulus clouds**

547 Corrected

548

549 **P29 L14: very precised estimates**

550 Corrected

551

552 **P29 L18: the altitude from which the air is originates, and is not to biased by**

553 Corrected

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Controls on the water vapor isotopic composition near the surface of tropical oceans and role of boundary layer mixing processes

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Abstract. Understanding what controls the water vapor isotopic composition of the sub-cloud layer (SCL) over tropical oceans (δD_0) is a first step towards understanding the water vapor isotopic composition everywhere in the troposphere. We propose an analytical model to predict δD_0 ~~as a function of sea surface conditions, humidity and temperature profiles, and the~~ motivated by the hypothesis that the altitude from which the free tropospheric air originates (z_{orig}) ~~. To do so, we extend previous studies by~~

5 ~~(1) is an important factor: when the air mixing into the SCL is lower in altitude, it is generally moister, and thus it depletes more efficiently the SCL. We extend previous simple box models of the SCL by~~ prescribing the shape of δD vertical profiles, and (2) linking δD_0 to z_{orig} as a function of humidity profiles and by accounting for rain evaporation and horizontal advection effects.

The model relies on the hypotheses assumption that δD profiles are steeper than mixing lines ~~and no clouds are precipitating,~~ and that the SCL is at steady state, restricting its applications to time scales longer than daily. The model express δD_0 as a function of z_{orig} , humidity and temperature profiles, surface conditions, a parameter describing the steepness of the δD vertical gradient and a few parameters describing rain evaporation and horizontal advection effects. We show that δD_0 does not depend on the intensity of entrainment, dampening hope that δD_0 measurements could help constrain this long-searched quantity.

Based on an isotope-enabled general circulation model simulation, we show that δD_0 variations are mainly controlled by mid-tropospheric depletion and rain evaporation in ascending regions, and by sea surface temperature and z_{orig} in subsiding regions. ~~When the air mixing into the SCL is lower in altitude, it is moister, and thus it depletes more efficiently the SCL.~~

In turn, could δD_0 measurements help estimate z_{orig} and thus discriminate between different mixing processes? Estimates that are accurate enough ~~For such isotope-based estimates of z_{orig} to be useful would be difficult to achieve in practice, requiring measuring daily,~~ we would need a precision of a few hundreds meters in deep convective regions and smaller than 20 m in strato-cumulus regions. To reach this target, we would need daily measurements of δD profiles, and measuring in the mid-troposphere and accurate measurements of δD_0 with an accuracy of (accuracy down to 0.1 ‰ and 0.4 ‰ in trade-wind cumulus and in the case of strato-cumulus clouds, which is currently difficult to obtain). We would also need information on the horizontal distribution of δD to account for horizontal advection effects, and full δD profiles to quantify the uncertainty associated with the assumed shape for δD profiles. Finally, rain evaporation is an issue in all regimes, even in strato-cumulus clouds ~~respectively.~~ Innovative techniques would need to be developed to quantify this effect from observations.

1 Introduction

1.1 What controls the water vapor isotopic composition?

The water vapor isotopic composition (e.g. $\delta D = (R/R_{SMOW} - 1) \times 1000$ expressed in ‰, where $R = HDO/H_2O$, R is the D/H ratio and SMOW is the Standard Mean Ocean Water reference) has been shown to be sensitive to a wide range of atmospheric processes (Galewsky et al., 2016), such as continental recycling (Salati et al., 1979; Risi et al., 2013), unsaturated downdrafts (Risi et al., 2008, 2010a), rain evaporation (Worden et al., 2007; Field et al., 2010), the degree of organization of convection (Lawrence et al., 2004; Tremoy et al., 2014), the convective depth (Lacour et al., 2017b), the proportion of precipitation that occurs as convective or large-scale precipitation (Lee et al., 2009; Kurita, 2013; Aggarwal et al., 2016), vertical mixing in the lower troposphere (Benetti et al., 2015; Galewsky, 2018a, b), mid-troposphere (Risi et al., 2012b) or upper-troposphere (Galewsky and Samuels-Crow, 2014), convective detrainment (Moyer et al., 1996; Webster and Heymsfield, 2003), ice microphysics (Bolot et al., 2013). It is therefore very challenging to quantitatively understand what controls the isotopic composition of water vapor.

A first step towards this goal is to understand what controls the water vapor isotopic composition in the sub-cloud layer (SCL) of tropical (30°S-30°N) oceans. Indeed, this water vapor is a an important source moistening air masses traveling to land regions (Gimeno et al., 2010; Ent and Savenije, 2013) and towards higher latitudes (Ciais et al., 1995; Delaygue et al., 2000). It is also ultimately the only source of water vapor in the tropical free troposphere, since water vapor in the free troposphere ultimately originates from convective detrainment (Sherwood, 1996), and convection ultimately feeds from the SCL air (Bony et al., 2008). Therefore, the water vapor isotopic composition in the SCL of tropical oceans serves as initial conditions to understand the isotopic composition in land waters and in the tropospheric water vapor everywhere on Earth. We focus here on the SCL because, by definition, there is no complication by cloud condensation processes.

The goal of this paper is thus to propose a simple analytical equation that allows us to understand and quantify the factors controlling the δD in the water vapor in the SCL of tropical oceans. So far, the most famous analytical equation for this purpose has been the closure equation developed by ~~Merlivat and Jouzel (1979)~~ Merlivat and Jouzel (1979) (MJ79). This closure equation can be derived by assuming that all the water vapor in the SCL air originates from surface evaporation. The water balance of the SCL can be closed by assuming a mass export at the SCL top (e.g. by convective mass fluxes) and a totally dry entrainment into the SCL to compensate this mass export. The MJ79 equation has proved very useful to capture the sensitivity of δD and second-order parameter d-excess to sea-surface conditions (~~Merlivat and Jouzel, 1979; Ciais et al., 1995; Risi et al., 2010d~~) Merlivat and Jouzel (1979); Ciais et al. (1995); Risi et al. (2010d). However, the δD calculated from this equation suffers a low from a high bias in tropical regions (~~Jouzel and Koster, 1996~~) Jouzel and Koster (1996). This bias can be explained by the neglect of vertical mixing between the SCL and air entrained from the free troposphere (FT). The MJ79 equation can better reproduce surface water vapor observation when extended to take into account this mixing (~~Benetti et al., 2015~~) Benetti et al. (2015), hereafter B15). ~~However, this~~ This extension requires to know the specific humidity (q) and water vapor δD of the entrained

air, ~~which are often unknown. In addition, they assumed. To get these values, they assume~~ that the air entrained into the boundary layer comes from a constant altitude, ~~which does not reflect. However, this does not reflect~~ the complexity of entrainment and mixing processes in marine boundary layers.

1.2 Entrainment and mixing mechanisms

5 Figure 1 summarizes our knowledge about these entrainment and mixing processes. In strato-cumulus regions, clouds are thin and the inversion is just above the LCL lifting condensation level (LCL). Air is entrained from the FT by cloud-top entrainment driven by radiative cooling or wind shear instabilities (Mellado, 2017), possibly amplified by evaporative cooling of droplets (Lozar and Mellado, 2015). Both Direct Numerical Simulations (Mellado, 2017) and observations of tracers (Faloona et al., 2005) and cloud holes (Gerber et al., 2005) show that air is entrained from a thin layer above the inversion, thinner than 80m
10 and as small as 5m. The boundary layer itself is animated by updrafts, downdrafts and associated turbulent shells that bring air from the cloud layer downward (Brient et al., 2019; Davini et al., 2017).

In trade-wind cumulus regions, the cloudy layer is a bit deeper. Observational studies and large-eddy simulations have pointed out the important role of thin subsiding shells around cumulus clouds, driven by cloud-top radiative cooling, mixing and evaporative cooling of droplets (Jonas, 1990; Rodts et al., 2003; Heus and Jonker, 2008; Heus et al., 2009; Park et al.,
15 2016). This brings air from the cloudy layer to the SCL. Subsiding shells may also cover overshooting plumes of the cumulus clouds, entraining FT air into the cloud layer (Heus and Jonker, 2008).

In deep convective regions, unsaturated downdrafts driven by rain evaporation (Zipser, 1977) are known to contribute significantly to the energy budget of the SCL (Emanuel et al., 1994). Large-eddy simulations show that subsiding shells, similar to those documented in shallow convection, also exist around deep convective clouds (Glenn and Krueger, 2014). In the clear-sky
20 environment between clouds, turbulent entrainment into the SCL may also play a significant role (Thayer-Calder and Randall, 2015).

Therefore, whatever the cloud regime, air entering the SCL from above may originate either from the cloud layer or from the free troposphere, depending on the mixing mechanism. Therefore, in this paper in contrast with ~~Benetti et al. (2015)~~ Benetti et al. (2015), we let the altitude from which the air originates, z_{orig} , be variable. We do not call it “entrained” air
25 because entrainment sometimes refer to mixing processes through an interface (e.g. ~~De Rooy et al. (2013); Davini et al. (2017)~~ De Rooy et al. (2013); Davini et al. (2017)), whereas air in the SCL may also enter through deep, coherent and penetrative structures such as unsaturated downdrafts. We do not call it FT air either, since it may originate from the cloudy layer.

1.3 Goal of the article

To acknowledge the diversity and complexity of mixing mechanisms, we extend the B15 framework in two several ways. First,
30 we assume that we know the ~~relationship between shape of δD and profiles as a function of q in the FT, which allows us to get rid of one unknown~~. Second, we write the specific humidity of the air originating from above the SCL as a function of z_{orig} .
Third, we account for rain evaporation and horizontal effects.

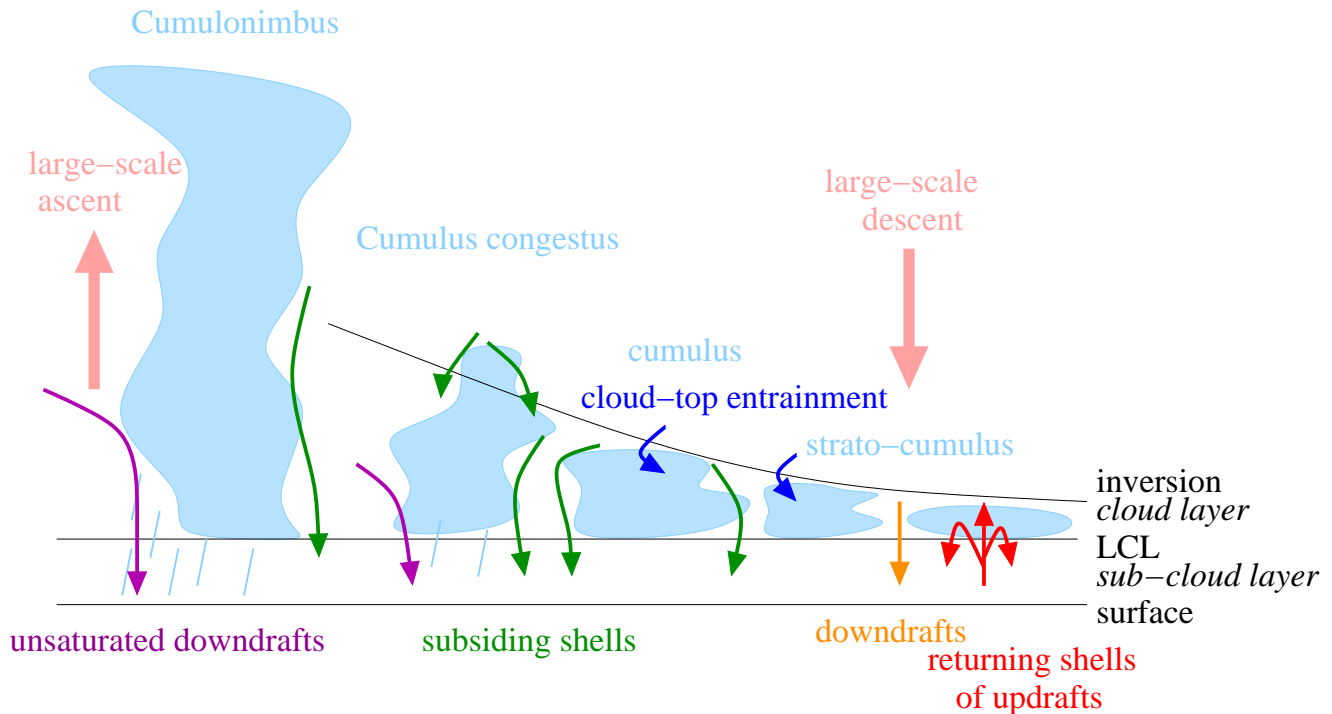


Figure 1. Schematics showing the different types of clouds and mixing processes as a function of the large-scale circulation.

While B15 focused on observations during a field campaign, we also apply the extended equation to global outputs of an isotope-enabled general circulation model, with the aim to quantify the different factors controlling the δD variability at the global scale in the Tropics. The variable z_{orig} will emerge as an important factor. Therefore, we discuss the possibility that δD measurements at the near surface and through the lower FT could help estimate z_{orig} , and thus the mixing processes between the SCL and the air above.

Note that we focus on δD only. Results for $\delta^{18}O$ are similar. We do not aim at capturing the second-order parameter d-excess, because our model requires some knowledge about free tropospheric vertical profiles of isotopic composition. While δD is known to decrease with altitude (Ehhalt, 1974; Ehhalt et al., 2005; Sodemann et al., 2017), vertical profiles of d-excess are more diverse and less well understood (Sodemann et al., 2017). In addition, the need for an extension of MJ79 is more needed for δD than for d-excess anyway, since MJ79 already performs quite well for, since the effect of convective mixing is larger on δD than on d-excess (Risi et al., 2010d; Benetti et al., 2014).

2 Theoretical framework

2.1 Assumptions leading to the Benetti et al 2015 equation Box model and budget equations

In this section, we recall how the equation in Benetti et al. (2014) Building on Benetti et al. (2014) and B15 was derived and explicit all underlying assumptions.

We consider a simple box representing the SCL (Fig. 2). We assume that the air may come from above (M) or from the and from the incoming large-scale horizontal convergence ($D < 0$ advection (F_{adv}), and is exported through the SCL top (N , e.g. turbulent mixing or convective mass flux) or and by outgoing large-scale horizontal divergence ($D > 0$ advection ($F_{adv,out}$). We assume that the SCL is at steady state. In particular For example, its depth is constant. Since the SCL properties may exhibit a diurnal cycle (Duykerke et al., 2004), this hypothesis restricts the application of this model to time scales longer than daily. The air mass budget of the SCL thus writes:

$$M + F_{adv} = N + DF_{adv,out} \quad (1)$$

These fluxes also transport water vapor and isotopes. In addition, surface evaporation E imports and rain evaporation F_{evap} import water vapor and isotopes (Fig. 2). We neglect import of water vapor and isotopes by rain evaporation (Albrecht, 1993) and will test the sensitivity to this effect in appendix B.

Hereafter, to simplify equations, we use the isotopic ratio R instead of δD .

The SCL is usually well-mixed (Betts and Ridgway, 1989; Stevens, 2006; De Roode et al., 2016), so that we can. We thus assume that the humidity and isotopic properties are constant vertically and horizontally in the SCL. They are noted (q_0, R_0). The humidity and isotopic properties of the mass flux export N are thus also (q_0, R_0). In case of net horizontal divergence ($D > 0$), the The properties of the divergence flux are also (q_0, R_0). In case of net convergence ($D < 0$), we neglect large-scale flux M are noted (q_{orig}, R_{orig}). The properties of the incoming air by horizontal advection are noted (q_{adv}, R_{adv}). For simplicity we neglect here the effect of horizontal gradients in air properties, so that the properties of the convergence flux are also (q_0, R_0). The properties of the flux M are noted (q_{orig}, R_{orig}) humidity (i.e. $q_{adv} = q_0$), assuming that the main effect of horizontal advection on δD_0 arises from horizontal gradients in δD . Appendix C explains how R_{adv} can be calculated. At steady state, the water budget of the SCL writes:

$$M \cdot q_{orig} + E + F_{evap} + F_{adv} \cdot q_0 = (N + DF_{adv,out}) \cdot q_0 \quad (2)$$

This model is consistent with SCL water budgets that have already been derived in previous studies (Bretherton et al., 1995), except that we consider steady state. This equation can be solved for q_0 :

$$q_0 = q_{orig} + \frac{E + F_{evap}}{M} \quad (3)$$

The SCL humidity q_0 is thus sensitive to M , justifying that it can be used to estimate the mixing intensity or the entrainment velocity “entrainment velocity” $w_e = M/\rho_0$ (ρ being the air volumic mass) (Bretherton et al., 1995).

At steady state, the water isotope budget of the SCL writes:

$$M \cdot q_{orig} \cdot R_{orig} + E \cdot R_E + \underbrace{F_{evap} \cdot R_{evap} + F_{adv} \cdot q_0 \cdot R_{adv}} = (N + \underbrace{DF_{adv,out}}) \cdot q_0 \cdot R_0 \quad (4)$$

where R_E is the isotopic composition of the surface evaporation. It is assumed to follow the [Craig and Gordon \(1965\)](#) [Craig and Gordon \(1965\)](#) equation:

$$5 \quad R_E = \frac{R_{oce}/\alpha_{eq} - h_0 \cdot R_0}{\alpha_K \cdot (1 - h_0)} \quad (5)$$

where R_{oce} is the isotopic ratio in the surface ocean water, α_{eq} is the equilibrium fractionation calculated at the ocean surface temperature (SST) (Majoube, 1971), α_K is the kinetic fractionation coefficient (MJ79) and h_0 is the relative humidity normalized at the SST ($h_0 = q_0/q_s(SST, P_0)$ where q_s is the [saturation](#) specific humidity at [saturation-function-SST](#) and P_0 is the surface pressure).

10 [We write the isotopic composition of the rain evaporation, \$R_{evap}\$, as:](#)

$$\underbrace{R_{evap} = \alpha_{evap} \cdot R_0}$$

[where \$\alpha_{evap}\$ is an effective fractionation coefficient. For example, if droplets are formed near the cloud base, some of them precipitate and evaporate totally into the SCL \(e.g. in non-precipitating shallow cumulus clouds\), then \$\alpha_{evap} = \alpha\(T_{cloudbase}\)\$. In contrast, if droplets are formed in deep convective updrafts after total condensation of the SCL vapor, and then a very small fraction of the rain is evaporated into a very dry SCL, then \$\alpha_{evap} = 1/\alpha\(T_{SCL}\)/\alpha_K\$ \(Stewart, 1975\).](#)

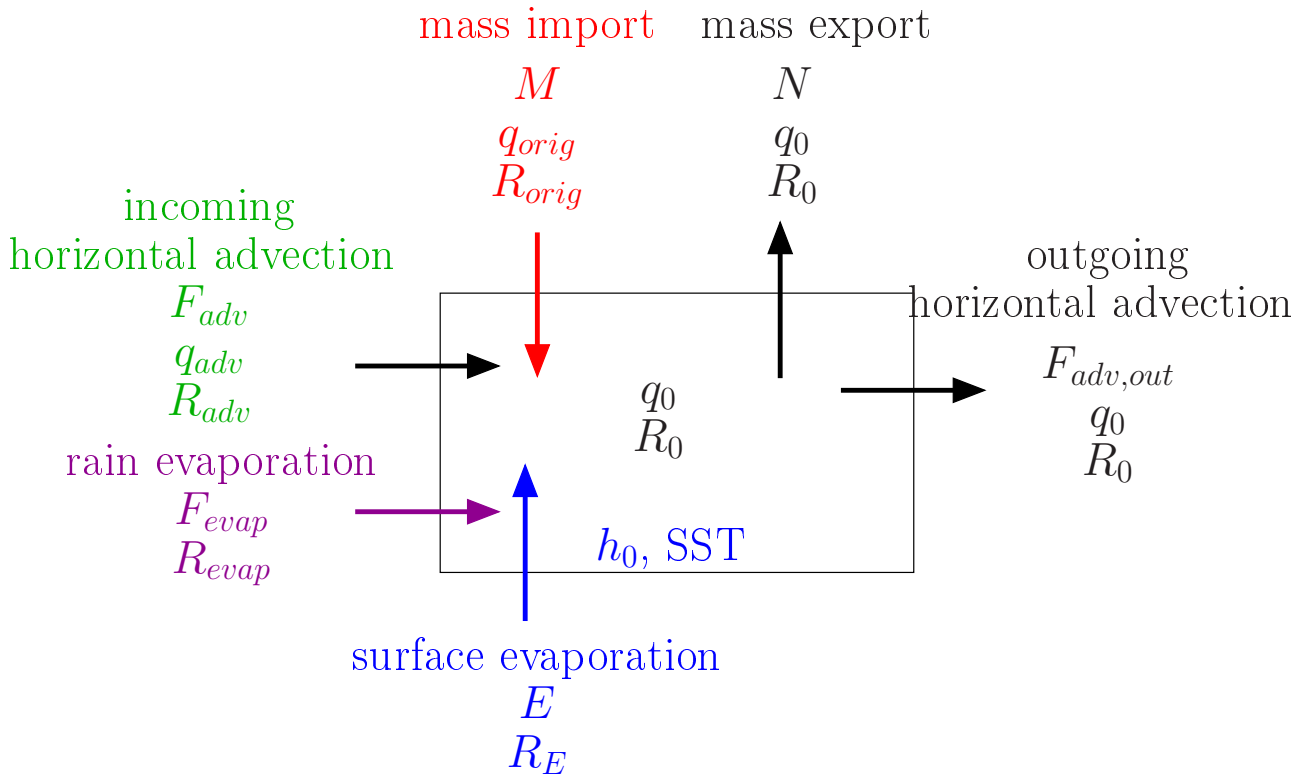
15 [We note \$\eta = F_{evap}/E\$ the ratio of water vapor coming from rain evaporation to that of surface evaporation, and \$\phi = F_{adv} \cdot q_{adv}/E\$ the ratio of water vapor coming from horizontal advection to that coming from surface evaporation. We note \$\beta = R_{adv}/R_0\$ the ratio of isotopic ratios of horizontal advection to that of the SCL.](#)

20 [Note that in all our equations, we assume that temperature and humidity profiles and all basic surface meteorological variables are known. We attempt to express neither \$h_0\$ as a function of \$q_0\$ as in B15, nor the \$q\$ profile as a function of \$q_0\$. Our ultimate goal is to assess the added value of \$\delta D\$ assuming that meteorological measurements are already routinely done.](#)

By combining all these equations, we get:

$$R_0 = \frac{(1 - r_{orig}) \cdot R_{oce}/\alpha_{eq} + \alpha_K \cdot (1 - h_0) \cdot r \cdot R_{orig}}{(1 - r_{orig}) \cdot h_0 + \alpha_K \cdot (1 - h_0)} \frac{(1 - r_{orig}) \cdot R_{oce}/\alpha_{eq} + \alpha_K \cdot (1 - h_0) \cdot r_{orig} \cdot (1 + \eta) \cdot R_{orig}}{(1 - r_{orig}) \cdot h_0 + \alpha_K \cdot (1 - h_0) \cdot (1 + \eta + (1 - r_{orig}) \cdot (\phi \cdot (1 - \beta) - \eta \cdot \alpha_{evap}))} \quad (6)$$

where $r_{orig} = q_{orig}/q_0$ is the proportion of the water vapor in the SCL that originates from above.



Equation-

Figure 2. Schematics showing the simple box model on which the theoretical framework is based, and illustrating the main notations.

An intriguing aspect of this equation is that the sensitivity to M disappears. In contrast to q_0 , R_0 is not sensitive to M . Therefore, it appears illusory to promise that water vapor isotopic measurements could help constrain the entrainment velocity that many studies have ~~strived~~ striven to estimate (Nicholls and Turton, 1986; Khalsa, 1993; Wang and Albrecht, 1994; Bretherton et al., 1995; Faloon et al., 2005; Gerber et al., 2005, 2013). The lack of sensitivity of R_0 to M is explained physically by the fact that for a given q_0 and q_{orig} , if M increases, then $\underline{E - E + F_{evap}}$ increases in the same proportion to maintain the water balance. Therefore, the relative proportion of the water vapor originating from surface ~~evaporation and~~ and rain evaporation to that coming from above, to which R_0 is sensitive, remains constant. Rather, since q and R vary with altitude, R_0 is sensitive to the altitude from which the air originates, ~~as argued in the next paragraph.~~

2.2 Two additional assumptions to close the equation

10 2.2 Closure if δD profile follows a Rayleigh distillation line

Eq. (6) requires to know q_{orig} and R_{orig} . B15 ~~closed it by taking the values of q_{orig} and R_{orig}~~ take these values from GCM outputs at 700 hPa ~~from GCM outputs. We modify this in two ways.~~

First, we want to. In contrast, here we acknowledge the diversity and complexity of mixing mechanisms by taking keeping the possibility to take q_{orig} and R_{orig} at a variable altitude z_{orig} .

$$q_{orig} = h(z_{orig}) \cdot q_s(\bar{T}(z_{orig}) + \delta T(z_{orig}), P(z_{orig}))$$

where $\bar{T}(z_{orig}) + \delta T(z_{orig}) = T(z_{orig})$ is the temperature at altitude z_{orig} , \bar{T} is the tropical ocean mean temperature profiles, $h(z_{orig})$ we can apply Eq. (6) if we know the q and $P(z_{orig})$ are the relative humidity and pressure at δD vertical profiles. Conversely, if the goal is to predict z_{orig} , and $\delta T(z_{orig})$ is the temperature perturbation compared to \bar{T} . Therefore, from R_0 , we can numerically solve Eq. (6) if we know the q and δD vertical profiles. No analytical solution exists in the unknown q_{orig} is replaced by the unknown general case, but a numerical solution can be searched for z_{orig} based on Eq. (6). However, the existence and unicity of the solution is not warranted for all kinds of profiles (e.g. appendix A).

Note that in all our equations, we assume that temperature and humidity profiles and all basic surface meteorological variables are known. We make no attempt to express h_0 as a function of q_0 as in B15. Our ultimate goal is to assess the added value of δD assuming that meteorological measurement are already routinely done. Therefore, variations of δD_0 that are mediated by q_0 or h_0 do not interest us.

Second, to deal with R_{orig} in Eq. (6) and get an analytical solution, we assume. In practice, full isotopic profiles are costly to measure. In addition, our goal is to develop an analytical model. Therefore, in the following we simplify the problem by assuming that the vertical profile of R follows a known relationship as a function of q . Measured vertical profiles of δD are usually bounded by two curves when plotted in a $(q, \delta D)$ diagram (Sodemann et al., 2017): Rayleigh distillation curve and mixing line. We explore these two extreme cases in the next section and in appendix A respectively.

Schematics showing the simple box model on which the theoretical framework is based, and illustrating the main notations.

2.3 Closure if the tropospheric profile follows a Rayleigh line

Here we assume that R_{orig} is uniquely related to q_{orig} by Rayleigh distillation. First, we explore the case of a Rayleigh distillation curve (Dansgaard, 1964), as in Galewsky and Rabanus (2016) Galewsky and Rabanus (2016):

$$R_{orig} = R_0 \cdot r_{orig}^{\alpha_{eff}-1} \quad (7)$$

where α_{eff} is an effective fractionation coefficient. Typically, q decreases with altitude, so R also decreases with altitude. However, in observations and models, vertical profiles of R can be very diverse (Bony et al., 2008; Sodemann et al., 2017). The water vapor may be more (Worden et al., 2007) or less (Sodemann et al., 2017) depleted than predicted by Rayleigh curve using a realistic fractionation factor that depends on local temperature. Therefore, here we let α_{eff} be a free parameter larger than 1. Rather than assuming a true Rayleigh curve, we simply assume that R and q are logarithmically related. Effects of horizontal advection and rain evaporation on tropospheric profiles are encapsulated into α_{eff} .

Injecting Eq. (7) into Eq. (6), we get:

$$R_0 = \frac{R_{oce}}{\alpha_{eq}} \cdot \frac{1}{h_0 + \alpha_K \cdot (1 - h_0) \cdot \left((1 + \eta) \cdot \frac{1 - r_{orig}^{\alpha_{eff}}}{1 - r_{orig}} - \eta \cdot \alpha_{evap} + \phi \cdot (1 - \beta) \right)} \quad (8)$$

A simpler form can be found if neglecting horizontal advection and rain evaporation effects ($\phi = \eta = 0$):

$$R_0 = \frac{R_{oce}}{\alpha_{eq}} \cdot \frac{1}{h_0 + \alpha_K \cdot (1 - h_0) \cdot \frac{1 - r_{orig}^{\alpha_{eff}}}{1 - r_{orig}}} \quad (9)$$

5 As a consistency check, in the limit case where the air coming from above is totally dry ($r_{orig} = 0$), we find Eq. (9) becomes the MJ79 equation:

$$R_0 = \frac{R_{oce}}{\alpha_{eq}} \cdot \frac{1}{h_0 + \alpha_K \cdot (1 - h_0)} \quad (10)$$

Equation (98) tells us that whenever $\alpha_{eff} > 1$, R_0 decreases as r_{orig} increases (Fig. 3 red), i.e. as q_{orig} is moister. Therefore, R_0 decreases as z_{orig} is lower in altitude. This result may be counter-intuitive, but can be physically interpreted as follows. If z_{orig} is high, mixing brings air with very depleted water vapor, but since the air is dry, the depleting effect is small. In contrast, if z_{orig} is low, mixing brings air with water vapor that is not very depleted, but since the air is moist, the depleting effect is large (Fig. 4a).

Figure 3 (red) shows that the range of possible δD values is restricted to -70 ‰ to -85 ‰. This explains why in quiescent conditions near the sea level in tropical ocean locations, the water vapor δD varies little [Benetti et al. \(2014\)](#) ([Benetti et al. \(2014\)](#), [F. Vimeux pers. comm.](#)). In the limit case where $r_{orig} \rightarrow 1$ (i.e. the air comes from the SCL top), $R_0 \rightarrow \frac{R_{oce}}{\alpha_{eq}} \cdot \frac{1}{h_0 + \alpha_K \cdot (1 - h_0) \cdot \alpha_{eff}}$ (L'Hopital's rule was used to calculate this limit). This lower bound is not so depleted compared to the more depleted water vapor observed in regions of deep convection (e.g. [Lawrence et al. \(2002\)](#); [Lawrence et al. \(2004\)](#); [Kurita \(2013\)](#) [Lawrence et al. \(2002\)](#); [Lawrence et al. \(2004\)](#); [Worden et al. \(2007\)](#)) can further decrease R_0 (appendix B).

Figure 3 (green) shows that the sensitivity to α_{eff} is relatively small but cannot be neglected. Therefore, predicting water vapor $\delta D - \delta D_0$ requires to have some knowledge about the steepness of the isotopic profiles in the FT. Rain evaporation and horizontal advection can have either an enriching or depleting effect, but do not qualitatively change the results (Fig. 3 purple and blue).

25 Assuming a Rayleigh shape for the δD profile allows us to find a good-looking analytical solution, but our Now we consider the case of a mixing line. Detailed calculation in appendix A show that the sensitivity to r_{orig} is lost. An infinity of FT end members can lead to the same δD_0 when mixed with the surface evaporation, as illustrated in Fig. 4b and analytically

demonstrated in appendix A. Our main results (more depleted δD_0 as r_{orig} increases, restricted range of δD_0 variations, relationship with z_{orig}) would hold for any hold only for δD profile that is steeper than the profiles that are steeper than a mixing line. If the profile follows as This is the case for profiles that are intermediate between a Rayleigh and a mixing line, however, our results would not hold any more, because no single end member can be identified, as illustrated in Fig. 4b and analytically demonstrated in appendix A. Therefore, in the remaining of the paper, we will assume that R follows a logarithmic line. We will assess the validity of this assumption in section D1, as is usually the case in nature (Sodemann et al., 2017) or in a general circulation model (appendix D1).

An important assumption that led to Eq. (9) is the neglect of SCL moistening by rain evaporation. We propose an extended equation including rain evaporation in appendix B. Rain evaporation can have a depleting or enriching effect (e.g. pink and blue curves in Fig. 3), depending on microphysical details that are too complex to be addressed here. Therefore, we neglect rain evaporation effects and our results will be valid only in regions covered by non-precipitating clouds, e.g. subsiding regions covered by non-precipitating trade-wind cumulus, strato-cumulus or stratus clouds.

3 Model simulations, observations and methods

3.1 LMDZ simulations

We use an isotope-enabled general circulation model (GCM) as a laboratory to test our hypotheses and investigate isotopic controls what controls the isotopic composition. We use the LMDZ5A version of LMDZ (Laboratoire de Météorologie Dynamique Zoom), which is the atmospheric component of the IPSL-CM5A coupled model (Dufresne et al., 2012) that took part in CMIP5 (Coupled Model Intercomparison Project, Taylor et al. (2012) Taylor et al. (2012)). This version is very close to LMDZ4 (Hourdin et al., 2006). Water isotopes are implemented the same way as in its predecessor LMDZ4 (Risi et al., 2010c). We use 4 years (2009-2012) of an AMIP (Atmospheric Model Intercomparison Project)-type simulation (Gates, 1992) that was initialized in 1977. The winds are nudged towards ERA-40 reanalyses (Uppala et al., 2005) to ensure a more realistic simulation. Such a simulation has already been described and extensively validated for isotopic variables in both precipitation and water vapor (Risi et al., 2010c, 2012a). The ocean surface water δD_{oce} is assumed constant and set to 4 ‰. The resolution is 2.5° in latitude \times 3.75° in longitude, with 39 vertical levels. Over the ocean, the first layer extends up to 64 m, and a typical SCL extending up to 600 m is resolved by 6 layers. Around 2500 m, a typical altitude for the inversion for trade-wind cumulus clouds, the resolution is about 500 m.

For our calculations, we only use tropical grid boxes (30°S - 30°N) over tropical oceans (>80% ocean fraction in the grid box). In addition, to avoid numerical problems when estimating effect of horizontal advection and rain evaporation, only grid boxes and days where $E > 0.5$ mm/d are considered. This represents 99.7% of all tropical oceanic grid boxes.

Specific diagnostics for horizontal advection and rain evaporation are detailed in appendix B and C.

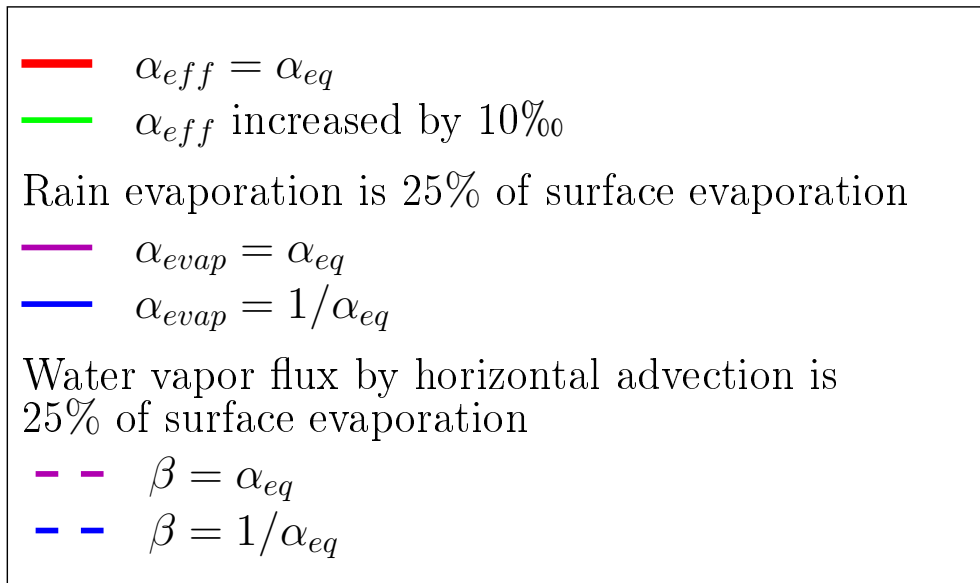
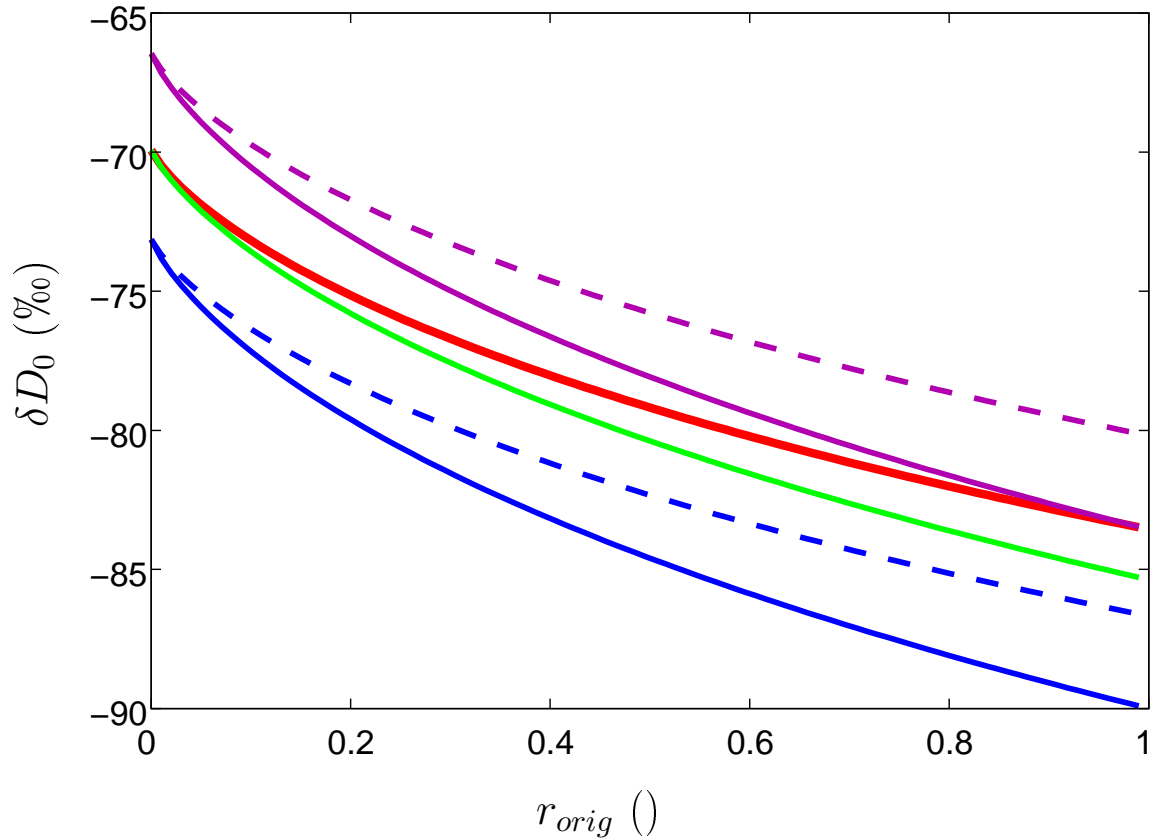


Figure 3. δD_0 as a function of r_{orig} according to Eq. (9), with $\alpha_{eff} = \alpha_{eq}$ as an example (red). For this illustrative purpose, we assume SST=30°C, $h_0 = 0.8$, $\delta D_{oce} = 0‰$ and $\phi = \eta = 0$. The sensitivity to the effective fractionation factor α_{eff} (green) is shown. In case of If rain evaporation fractionation is 25% of surface evaporation ($\eta = 0.25$), the solid pink and blue curves show the sensitivity to the effective fractionation factor α_{evap} (see appendix B). If the incoming water vapor by horizontal advection is shown 25% of surface evaporation (pink $\phi = 0.25$), the dashed pink and blue curves show the sensitivity to the isotopic gradient quantified by β .

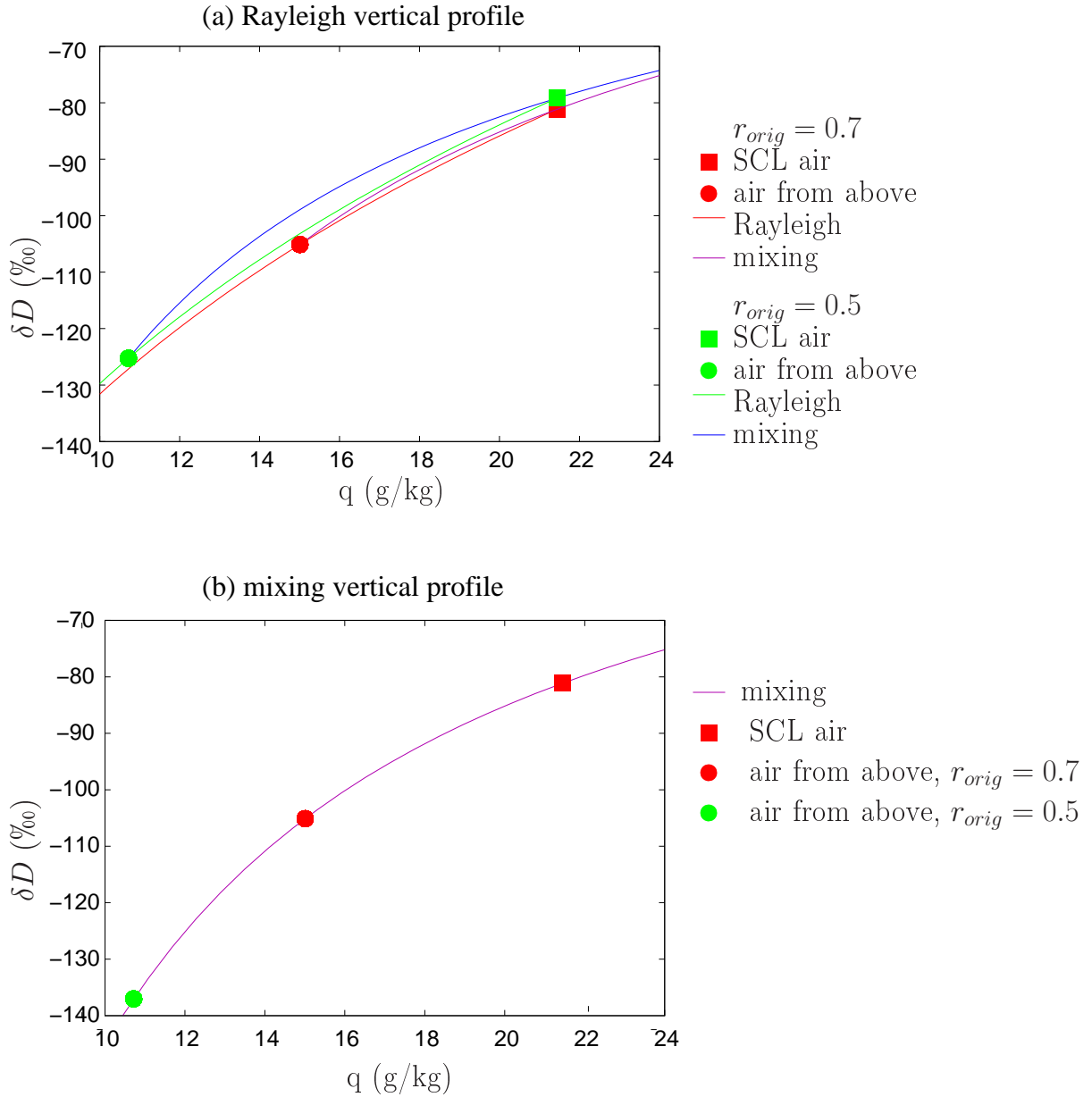


Figure 4. Idealized $q - \delta D$ diagrams showing how the SCL water vapor δD is set. [For this illustrative purpose, we assume SST=30°C, \$h_0 = 0.8\$, \$\delta D_{sea} = 0\text{‰}\$ and \$\phi = \eta = 0\$.](#) (a) If δD profiles follow Rayleigh distillation. The red curve shows the Rayleigh profile starting from the SCL and the pink curve shows the mixing line connecting the air coming from above to the surface evaporation, in the case $r_{orig} = q_{orig}/q_0 = 0.7$. The green curve shows the the Rayleigh profile starting from the SCL and the blue curve shows the mixing line connecting the air coming from above to the surface evaporation, in the case $r_{orig} = q_{orig}/q_0 = 0.5$. One can visually see that when r_{orig} is lower, the mixing line is more curved, leading to more enriched values. (b) If δD profiles follow a mixing line. The pink-purple curve joins the SCL air and the air at all altitudes above the SCL. One can see that different values for r_{orig} can lead to the same value of δD in the SCL.

3.2 STRASSE observations

We also apply our theoretical framework to observations during the STRASSE (subtropical Atlantic surface salinity experiment) cruise that took place in the Northern subtropical ocean in August and September 2012 (Benetti et al., 2014). This campaign accumulates several advantages that are important for our analysis: (1) continuous δD_0 measurements in the surface water vapor (17m) at a high temporal frequency during one month (Benetti et al., 2014, 2015, 2017b), (2) associated surface meteorological measurements, including SST and h_0 , (3) 22 radio-soundings relatively well distributed over the campaign period and providing vertical profiles of altitude, temperature, relative humidity and pressure, (4) ocean surface water δD_{oce} measurements (Benetti et al., 2017a), (5) a variety of conditions ranging from quiescent weather to convective conditions, (6) on many vertical profiles, a well defined temperature inversion allows to calculate the inversion altitude.

We use δD_0 measurements on a 15-minute time step. The measurements in ocean water were interpolated on the same time steps using a Gaussian filter with a width of 3 days. The radio-soundings are used together with all water vapor isotopic measurements that are within 30 minutes of the radio-sounding launch. Only profiles during the ascending phase of the balloon are considered, because the descent phase is often located far away from the initial launch point (McGrath et al., 2006; Seidel et al., 2011).

3.3 Estimating the altitude from which the air originates

~~First, α_{eff} is estimated assuming that~~ Here we explain how z_{orig} is estimated based on LMDZ outputs. First, we assume that the q and δD at 500 hPa ($q_f, \delta D_f$) at 500hPa follows belong to a Rayleigh distillation line starting from the surface with effective fractionation α_{eff} :

$$\alpha_{eff} = 1 + \frac{\ln(R_f/R_0)}{\ln(q_f/q_0)}$$

In a real field campaign, this assumption means that we do not need to measure the full vertical profile of δD , but only δD_f at a given free tropospheric altitude (e.g. 500 hPa).

We checked that results are similar when defining the end member at 400 hPa rather than 500 hPa. However, ~~if~~ the end member ~~is~~ should be defined above 500 hPa to ensure that it is well above boundary layer processes. If the end member is defined below 500 hPa (e.g. 600 hPa), results are not always reasonable there are a few cases where q increases with altitude ($q_f > q_0$) due to horizontal advection or convective detrainment from nearby moister regions; meanwhile, δD decreases monotonically, leading to unrealistic values for α_{eff} .

Second, r_{orig} is estimated based on Eq. (9), using $\alpha_{eff}, \alpha_{eq}, \alpha_K, \delta D_{oce}, h_0$ and δD_0 simulated by LMDZ.

Third, the altitude z_{orig} is estimated from r_{orig} . Using the q vertical profile, we find z_{orig} so that $q(z_{orig}) = r_{orig} \cdot q_0$ (Fig. 5, red).

Note that When estimating z_{orig} from observations, we follow the same methodology except that in absence of measurements for q_f and δD_f we assume a constant $\alpha_{eff} = 1.07$ based on LMDZ simulation, and that $\alpha_{eq}, \alpha_K, \delta D_{oce}, h_0$ and δD_0 come from surface observations.

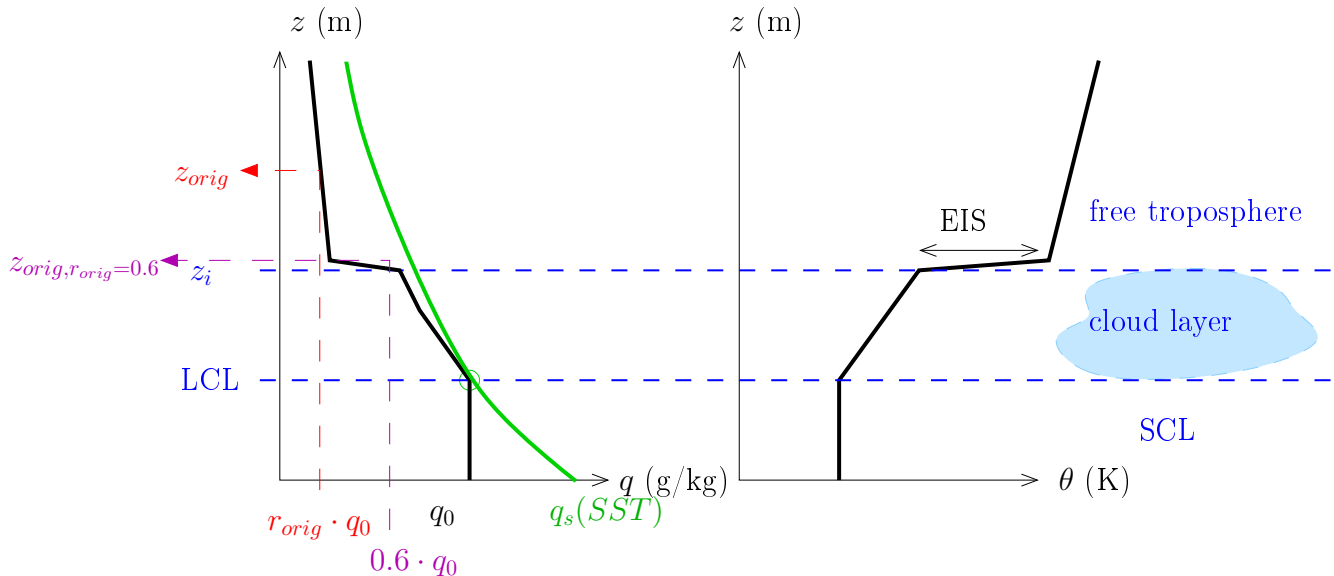


Figure 5. Schematics illustrating the typical structure of tropical marine boundary layers. The sub-cloud layer (SCL) extends from the surface to the lifting condensation level (LCL) and the cloud layer extends from the LCL to the inversion (z_i). EIS stands for the estimated inversion strength. Left: shape of the vertical profile in q (black) and q_s (green). Right: shape of the vertical profile in potential temperature θ , inspired by Wood and Bretherton (2006) (Wood and Bretherton, 2006). The LCL, z_{orig} , $z_{orig, r_{orig}=0.6}$ and z_i altitudes defined in section 3.4 are indicated.

Note that r_{orig} and z_{orig} are not direct diagnostics from the simulation, but rather a-posteriori estimates to match the simulated δD_0 . Therefore, if assumptions underlying Eq. (9) are violated, then the estimate of r_{orig} , and subsequently z_{orig} , will be biased. The estimate of r_{orig} encapsulates the effect of mixing processes, but also all other processes that have been neglected in our theoretical framework, such as temporal variations in SCL depth, q_0 or δD_0 , horizontal gradients in or vertical variations of q_0 or δD_0 , or rain evaporation. For example, in case of deep convection, depleting rain evaporation will reflect into an artificially larger r_{orig} and lower z_{orig} . We have to keep this in mind when interpreting the results within the SCL.

3.4 Boundary layer structure diagnostics

Figure 5 illustrates the structure of a typical tropical marine boundary layer covered by strato-cumulus or cumulus clouds (Betts and Ridgway, 1989; Wood, 2012; Wood and Bretherton, 2004; Neggers et al., 2006; Stevens, 2006). The cloud base corresponds to the lifting condensation level (LCL). Below is the well-mixed SCL. Above is the cloud layer, topped by a temperature inversion. Above the inversion is the FT.

The LCL is calculated as the altitude at which the specific humidity near the surface equals the specific humidity at saturation of a parcel that is lifted following a dry adiabat (Fig. 5). In LMDZ, the inversion

The temperature inversion is an abrupt increase in temperature that caps the boundary layer. Therefore, a method to automatically estimate its altitude z_i is ~~calculated~~ to detect a maximum in the vertical gradient of potential temperature (Stull, 1988; Oke, 1988; Sorbjan, 1989). This method is sensitive to the resolution of vertical profiles (Siebert et al., 2000; Seidel et al., 2010). Therefore, we adapted this method in order to yield z_i values that best agree with what we would estimate from visual inspection of individual temperature profiles. In LMDZ, we calculate z_i as the first level at which the vertical potential temperature ~~gradients~~-gradient exceeds 3 times the moist-adiabatic lapse rate. In observations, ~~we calculate~~ z_i ~~is calculated~~ as the first level at which the vertical potential temperature ~~gradients~~-gradient exceeds 5 times the moist-adiabatic lapse rate, because radio-soundings are noisier than simulated profiles. ~~These estimates are consistent with what we would estimate from visual inspection of vertical profiles.~~

Finally, we calculate $z_{orig, r_{orig}=0.6}$, which is the z_{orig} altitude if r_{orig} is set to 0.6. This usually coincides with the altitude of strong humidity decrease near the inversion (Fig. 5).

3.5 Averages and composites

All calculations are done on daily values for LMDZ, and on 15-minute values for observations.

For LMDZ, when analyzing spatial and seasonal variability, seasonal averages are calculated at each grid box ~~over tropical oceans~~ by averaging all days of all years that belong to each season. Seasons are defined as boreal winter (December-January-February), spring (March-April-May), summer (June-July-August) and fall (September-October-November). For illustration purpose, all maps are plotted for boreal winter. Standard deviations are also calculated among all days of all years for each season.

The type of clouds and mixing processes depends strongly on the large-scale velocity at 500 hPa (ω_{500} , ~~map shown in~~ Fig. 6a), with shallow clouds in subsiding regions and deeper clouds in ascending regions (~~Bony et al., 2004~~, Fig. 1). Therefore, ~~composites are calculated by averaging~~ it is convenient to plot variables as composites as a function of ω_{500} (~~Bony et al., 2004~~). To make such plots, we divide the ω_{500} range from -30 to 50 hPa/d into intervals of 5 hPa/d. In each given interval, we average all seasonal-mean values at all locations ~~that belong to a given interval of over tropical oceans~~ for which seasonal-mean ω_{500} belongs to this interval (e.g. Fig. 8a will be an example). Note that such composites are done on seasonal-mean ω_{500} because cloud processes and their associated diabatic heating are tied to the large-scale circulation through energetic constrains (Yanai et al., 1973; Emanuel et al., 1994) that are best valid at longer time scales (otherwise, the energy storage term may become significant, e.g. Masunaga and Sumi (2017)). This is why ω_{500} is generally averaged over a month or longer (e.g. Bony et al. (1997); Williams et al. (2003); Bony et al. (2004); Wyant et al. (2006); Bony et al. (2013)). In addition, we primarily focus on understanding the seasonal and spatial distribution of δD_0 .

The cloud cover strongly ~~depends on~~ ~~correlates with~~ the inversion strength, ~~with increasing cloud fraction as inversion strength increases.~~ We use ~~which can be quantified by the~~ Estimated Inversion Strength (EIS) (~~Wood and Bretherton, 2006~~) (~~Wood and Bretherton (2006), map shown in~~ Fig. 6b) as a measure of inversion strength. ~~Composites as~~ We thus also plot variables as composites as a function of EIS ~~are calculated by averaging~~. To make such plots, we divide the EIS range from -1 K to 9 K into intervals of 0.5K. In each given interval, we average all seasonal-mean values at all locations ~~that belong~~

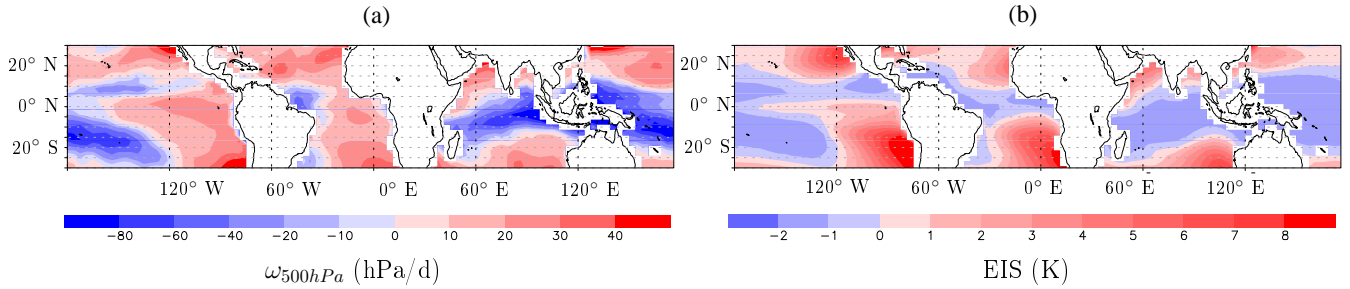


Figure 6. Maps of winter-mean ω_{500} (a) and EIS (b) simulated by LMDZ.

to a given interval of EIS over tropical oceans for which seasonal-mean EIS belongs to this interval (e.g. Fig. 8b will be an example). Using seasonal-mean values is consistent with Wood and Bretherton (2006) and with the better link at longer time scales between cloud processes and the large-scale dynamical regime.

3.6 Decomposition method for δD_0

- 5 To understand what controls the δD_0 spatio-temporal variations, δD_0 is decomposed into 4 contributions based on Eq. (9). The 4 factors, r_{orig} (8). First, we define $r_{orig,bas} = 0.3$, $\alpha_{eff,bas} = 1.09$, $SST_{bas} = 25^\circ\text{C}$ and $h_0 = 0.8$, assuming that all other factors are constant ($r_{orig} = 0.6$, $\alpha_{eff} = 1.09$, $SST_{bas} = 25^\circ\text{C}$, $h_0 = 0.8$). This yields 4 components $h_0,bas = 0.7$, representing the effects of the variability of $\phi_{bas} = 0$, $\eta_{bas} = 0$, $\beta_{bas} = 1$ and $\alpha_{evap,bas} = 1$ as a basic state. We call $\delta D_{0,func}(r_{orig}, \alpha_{eff}, SST, h_0, \phi, \beta, \eta, \alpha_{evap})$ the function giving δD_0 as a function of r_{orig} , α_{eff} , SST and h_0 on δD_0 , ϕ , β , η and α_{evap} following Eq. (8), and $\delta D_{0,bas} = \delta D_{0,func}(r_{orig,bas}, \alpha_{eff,bas}, SST_{bas}, h_0,bas, \phi_{bas}, \beta_{bas}, \eta_{bas}, \alpha_{evap,bas})$. The relative contribution of r_{orig} to δD_0 is estimated as $\delta D_{0,func}(r_{orig}, \alpha_{eff,bas}, SST_{bas}, h_0,bas, \phi_{bas}, \beta_{bas}, \eta_{bas}, \alpha_{evap,bas}) - \delta D_{0,bas}$. Similarly, the contributions of α_{eff} , SST , h_0 , ϕ and η are to δD_0 are estimated as detailed in table 1. All the contributions have the same units as δD_0 (‰). The sum of these components yields a quantity that is very close to the simulated δD_0 , which confirms the validity of this linear decomposition. These components and their sum can be plotted as maps: Fig. 7 provides an example.

- The relative contribution contributions of each of these effects components to the δD variability is are quantified by performing a linear regression of each of the components as a function of δD_0 . If the correlation coefficient is significant for a given factor, then the slope quantifies the contribution of this factor to the variability of δD_0 . The sum of all contributions may not always be 1 due to non-linearity. Such a method has already been applied in previous studies (e.g. Risi et al. (2010b); Oueslati et al. (2016) Risi et al. (2010b); Oueslati et al. (2016)). The contributions to the seasonal-spatial variability of δD_0 can be quantified by performing the regression among all locations and seasons. The contributions to the daily variability of δD_0 can be quantified by performing the regression among all days of a given season at a given location.

<u>Contribution</u>	<u>Calculation</u>	<u>Physical meaning</u>
r_{orig}	$\delta D_{0,func}(r_{orig,bas}, \alpha_{eff,bas}, SST_{bas}, h_{0,bas}, \phi_{bas}, \beta_{bas}, \eta_{bas}, \alpha_{evap,bas}) - \delta D_{0,bas}$	<u>Altitude from which the air originates</u>
α_{eff}	$\delta D_{0,func}(r_{orig,bas}, \alpha_{eff,bas}, SST_{bas}, h_{0,bas}, \phi_{bas}, \beta_{bas}, \eta_{bas}, \alpha_{evap,bas}) - \delta D_{0,bas}$	<u>Steepness of the δD vertical gradient in the FT</u>
<u>SST</u>	$\delta D_{0,func}(r_{orig,bas}, \alpha_{eff,bas}, SST_{bas}, h_{0,bas}, \phi_{bas}, \beta_{bas}, \eta_{bas}, \alpha_{evap,bas}) - \delta D_{0,bas}$	<u>SST</u>
h_0	$\delta D_{0,func}(r_{orig,bas}, \alpha_{eff,bas}, SST_{bas}, h_{0,bas}, \phi_{bas}, \beta_{bas}, \eta_{bas}, \alpha_{evap,bas}) - \delta D_{0,bas}$	h_0
ϕ	$\delta D_{0,func}(r_{orig,bas}, \alpha_{eff,bas}, SST_{bas}, h_{0,bas}, \phi_{bas}, \beta_{bas}, \eta_{bas}, \alpha_{evap,bas}) - \delta D_{0,bas}$	<u>Horizontal advection through horizontal δD gradients</u>
η	$\delta D_{0,func}(r_{orig,bas}, \alpha_{eff,bas}, SST_{bas}, h_{0,bas}, \phi_{bas}, \beta_{bas}, \eta_{bas}, \alpha_{evap,bas}) - \delta D_{0,bas}$	<u>Rain evaporation in the SCL</u>

Table 1. Equations to calculate the relative contributions of r_{orig} , α_{eff} , SST, h_0 , ϕ and η to δD_0 , and the physical meaning of these contributions.

3.7 Decomposition method for r_{orig}

To understand what controls r_{orig} , a similar method as for the decomposition of δD_0 can be applied, ~~based on Eq. (??)~~. We can write r_{orig} as:

$$r_{orig} = \frac{h(z_{orig}) \cdot q_s(\bar{T}(z_{orig}) + \delta T(z_{orig}), P(z_{orig}))}{q_0} \quad (11)$$

- 5 where $\bar{T}(z_{orig}) + \delta T(z_{orig}) = T(z_{orig})$ is the temperature at altitude z_{orig} . \bar{T} is the tropical-ocean-mean temperature profiles, $h(z_{orig})$ and $P(z_{orig})$ are the relative humidity and pressure at z_{orig} , and $\delta T(z_{orig})$ is the temperature perturbation compared to \bar{T} . Therefore, the variability of r_{orig} is decomposed into the effect of 4 factors: q_0 , z_{orig} , $h(z_{orig})$ and $\delta T(z_{orig})$. In practice, r_{orig} and z_{orig} are calculated following section 3.3, then Eq. (11) is applied.

4 Results from LMDZ

10 4.1 Does the tropospheric profile follow a mixing or Rayleigh line?

First, we test whether the δD vertical profiles simulated by LMDZ follow a Rayleigh or mixing curve as a function of q . For the Rayleigh curve, α_{eff} is estimated as explained in section 3.3. For the mixing line, the end member (q_f, R_f) is also taken at 500 hPa. Examples of vertical δD profiles simulated by LMDZ and predicted by the Rayleigh and mixing lines are plotted in Fig. ??.

We can see that simulated profiles are usually bounded by these two extreme lines, consistent with observations (Sodemann et al., 2017). Profiles are however much smoother than in observations, due to the coarse vertical resolution of the model. The coarse vertical resolution is a limitation to keep in mind when discussing the shape of vertical profiles.

When assuming a Rayleigh or mixing curve, the root mean square error (RMSE) on the δD profile from the surface to 500hPa ranges from 5 to 30 ‰ (Fig. D1a-b). In average, RMSE are slightly larger for Rayleigh, but this depends on the location and no generic curve fits perfectly well the vertical profiles. This is consistent with the diversity of observed profile shapes (Sodemann et al., 2017). In the following, we will assume that the Rayleigh curve is a good first order approximation. Our method of z_{orig} estimate remains valid even if δD vertical profiles do not follow Rayleigh, as long they follow a curve that is steeper than mixing. This is the case in LMDZ (Fig. ??).

Figure D1c shows the estimated α_{eff} . It is maximum in regions of deep convection. This is consistent with the maximum depletion simulated in deep convective regions in the mid-troposphere simulated by models (Bony et al., 2008), leading to steeper δD profiles. The pattern of α_{eff} may also reflect horizontal advection effects (Dee et al., 2018).

Values α_{eff} are of the same order of magnitude as real fractionation factors, but the spatial variations do not reflect those predicted if using a fractionation coefficient α_{eq} a function of temperature T (Fig. D1f). Rayleigh curves using $\alpha_{eq}(T)$ poorly predict vertical profiles of δD (Fig. D1e), with RMSE values exceeding 20 ‰ at most locations.

Examples of vertical profiles simulated by LMDZ (red), predicted by a Rayleigh curve with α_{eff} estimated to fit the simulated δD at 500 hPa (section 3.3, green), and predicted by a mixing line with the dry end member at 500 hPa (pink). Three examples are given: (a) the simulated profile is closed to a mixing line, (b) the simulated profile is closed to a Rayleigh line, and (c) the simulated profile deviates both from a mixing and a Rayleigh line (c). The RMS values indicate the RMS difference between simulated profile and mixing line (pink) or Rayleigh curve (green).

a) Root mean square error (RMSE) between the simulated δD profile and a δD profile that would follow a mixing curve between the surface and 500 hPa. b) Same as a but for a profile that would follow a Rayleigh curve between the surface and 500 hPa, with α_{eff} determined based on simulated δD at 500 hPa. c) Same as b but for a profile that would follow a Rayleigh curve using equilibrium fractionation calculated as a function of temperature, $\alpha_{eq}(T)$. d) $\alpha_{eff} - 1$, where α_{eff} is the effective fractionation coefficient, expressed in ‰. e) Standard deviation of α_{eff} among all days in winter of all years, expressed in ‰. f) $\alpha_{eq}(T) - 1$ expressed in ‰. For a-d and f, all daily values are averaged over all days in winters of all years.

30 4.1 Decomposition of δD_0 variability

The spatial variations of δD_0 simulated by LMDZ (Fig. 7a) are characterized by depleted values near mid-latitudes and in dry subsiding regions (e.g. off the coast of Peru and over other upwelling regions) and in deep convective regions regions of oceanic upwelling and regions of atmospheric deep convection (e.g. Maritime Continent). Consistently, δD_0 values exhibit a maximum for weakly ascending or subsiding regions: δD_0 decreases as ω_{500} is more strongly ascending or descending with

5 increasing vertical velocity of both signs (Fig. 8a black); δD_0 decreases as EIS increases reflecting more stable, subsiding conditions (Fig. 8b black). This pattern is consistent with previous studies (e.g. [Good et al. \(2015\)](#)[Good et al. \(2015\)](#)). For the first time, we propose a theoretical framework to interpret this pattern, decomposing it into 4-6 contributions: r_{orig} , α_{eff} , SST and h_0 , rain evaporation and horizontal advection effects (section 3.6). We check that the reconstructed δD_0 from the sum of its 4 contributions is very similar to the simulated δD_0 (Fig. 7b, 8 dashed black).

In ascending regions, the main contribution explaining the more depleted δD_0 in deep convective regions is that of α_{eff} (Fig. 7d, 8a red). α_{eff} is higher in more ascending regions ~~(Fig. D1d)~~. This means that the main factor depleting δD_0 in deep convective regions is the fact that the mid-troposphere is more depleted. This leads to a steeper gradient (higher α_{eff}), and thus a more efficient depletion by vertical mixing. This is consistent with deep convection depleting the water vapor most efficiently in the mid-troposphere ([Bony et al. \(2008\)](#))[\(Bony et al., 2008\)](#). The second main contribution is that associated with r_{orig} (Fig. 7c, 8a green). r_{orig} is larger in deep convective regions ~~However, we recall that Eq. (9) does not consider rain evaporation, which is a significant source of water vapor in deep convective regions (Worden et al. (2007)). Rain evaporation in deep convective regions is expected to deplete the water vapor (section B), so that neglecting rain evaporation leads to an over-estimate of r_{orig} in these regions. Therefore, the stronger r_{orig} in deep convective regions could be partially an artifact reflecting the effect of rain evaporation. (as explained in section 4.2).~~

In subsidence regions, the main factor explaining the more depleted δD_0 as subsidence is stronger, or as EIS increases, is the cold SST (Fig. 7e, 8a pink), leading to larger α_{eq} , and to a lesser extent the dry h_0 (Fig. 7f, 8a purple). The contribution of r_{orig} is also a significant contribution to the depletion of δD_0 in the cold upwelling regions, for example off Peru or Namibia (Fig. 7c). ~~In subsidence regions, r_{orig} , is unlikely to be an artifact of rain evaporation there, and probably really reflect the importance of mixing processes.~~ The shallower boundary layer there are associated with higher r_{orig} . ~~The fact that the effect of r_{orig} can be seen on the composites as a function of EIS~~

The contribution of rain evaporation on δD_0 is minor compared to other contributions, except in the deepest convective regions (Fig. 8b, green)~~and not as a function of ω_{500} may reflect the fact that EIS reflects more faithfully the cloud and mixing processes in dry, stable regions than ω_{500} does (Wood and Bretherton, 2006)7g)~~. Rain evaporation has a slightly depleting effect in regions of strong deep convection and a slightly enriching effect in regions of moderate deep convection. When the fraction of raindrops that evaporate is small, isotopic fractionation favors evaporation of the lighter isotopologues. Therefore in convective, moist regions, rain evaporation has a depleting effect on the SCL (Worden et al., 2007). In contrast, in drier regions, rain evaporates almost totally. The evaporation flux thus has almost the same composition as the initial rain, which is more enriched than the water vapor.

30 The contribution of horizontal advection to δD_0 is significant only where isotopic gradients are the largest (Fig. C1h). Horizontal advection has slightly enriching in deep convective regions and depleting in coastal regions (e.g. off the coasts of California, Peru, Mauritania, Namibia, India and Australia). For example, the Saharan layer in front of the North-Western African Coast leads to a strong effect of horizontal advection (Lacour et al., 2017a).

From a quantitative point of view, we can decompose the δD_0 seasonal-spatial variations into these different effects (section 3.6). In regions of large-scale ascent, α_{eff} is the main factor explaining the δD_0 seasonal-spatial variations (37-33%), followed

Regime	ascending		Subsiding	
	correlation coefficient	slope	correlation coefficient	slope
r_{orig}	0.71 <u>0.59</u>	0.17 <u>0.19</u>	0.50 <u>0.52</u>	0.16 <u>0.29</u>
α_{eff}	0.75 <u>0.73</u>	0.37 <u>0.33</u>	0.36 <u>0.26</u>	0.14 <u>0.10</u>
SST	-0.20 <u>-0.23</u>	-0.06	0.89	0.54
h_0	0.09 <u>(0.06)</u>	0.03 <u>(0.01)</u>	0.35 <u>0.28</u>	0.23 <u>0.13</u>
<u>rain evaporation</u>	<u>0.67</u>	<u>0.20</u>	<u>-0.36</u>	<u>-0.05</u>
<u>horizontal advection</u>	<u>-0.26</u>	<u>-0.12</u>	<u>(0.10)</u>	<u>(0.04)</u>
<u>r_{orig} if rain evaporation and horizontal advection are neglected</u>	<u>0.69</u>	<u>0.30</u>	<u>0.58</u>	<u>0.34</u>

~~Decomposition of the spatial and seasonal variation in δD_0 into its 4 contributions: effect of~~

Table 2. ~~Decomposition of the spatial and seasonal variation in δD_0 into its 6 contributions: effect of r_{orig} , α_{eff} , SST, h_0 , rain evaporation and horizontal advection. For each contribution, we show the correlation coefficient of the linear regression of the contribution as a function of δD_0 . The analysis is done separately for ascending and subsiding regimes. All seasons and locations over tropical oceans ($30^\circ N - 30^\circ S$, ocean fraction > 80%, surface evaporation > 0.5 mm/d) are considered. The threshold for the correlation coefficient to be statistically significant at 99 % is 0.15 or lower in all cases. We write correlation coefficient and slope values between brackets when they are not significant at 99%.~~

~~by rain evaporation (20%) and r_{orig} (47.19 %) and (Table 2). In regions of large-scale descent, SST is the main factor explaining the seasonal-spatial variations (54 %), followed by r_{orig} (16.29 %) h_0 (13%), and α_{eff} (14.10 %) (table-Table 2). Note that the contribution of r_{orig} would be similar if we neglect rain evaporation and horizontal advection effects (Table 2).~~

The decomposition method can also be applied to decompose the δD_0 variability at the daily time scale at each location and
5 for each season (Table 3). On average, in ascending regions, r_{orig} is the main factor (49.52 %), followed by rain evaporation (48%) and α_{eff} (39.35 %). In subsiding regions, the effect of SST is muted due to its slow variability, and r_{orig} (59.82 %) ; ~~α_{eff} (49 %) and h_0 (62 %) become the main factors~~becomes the main factor.

Overall, the results highlight the importance of r_{orig} as one of the main factors controlling the spatio-temporal variability of δD_0 .

10 4.2 Decomposition of r_{orig} variability

Given the importance of r_{orig} in controlling the δD_0 variations, we now decompose r_{orig} into its 4 contributions: q_0 , z_{orig} , h_{orig} and δT_{orig} (section 3.6). Spatially, r_{orig} is maximum in regions of strong large-scale ascent (Fig. 10a) such as the Maritime continent (Fig. 9a), and in very stable regions (Fig. 10b) such as upwelling regions (Fig. 10a). We check that the reconstructed r_{orig} from the sum of its 4 contributions is very similar to the simulated r_{orig} (Fig. 9b, 10 dashed black).

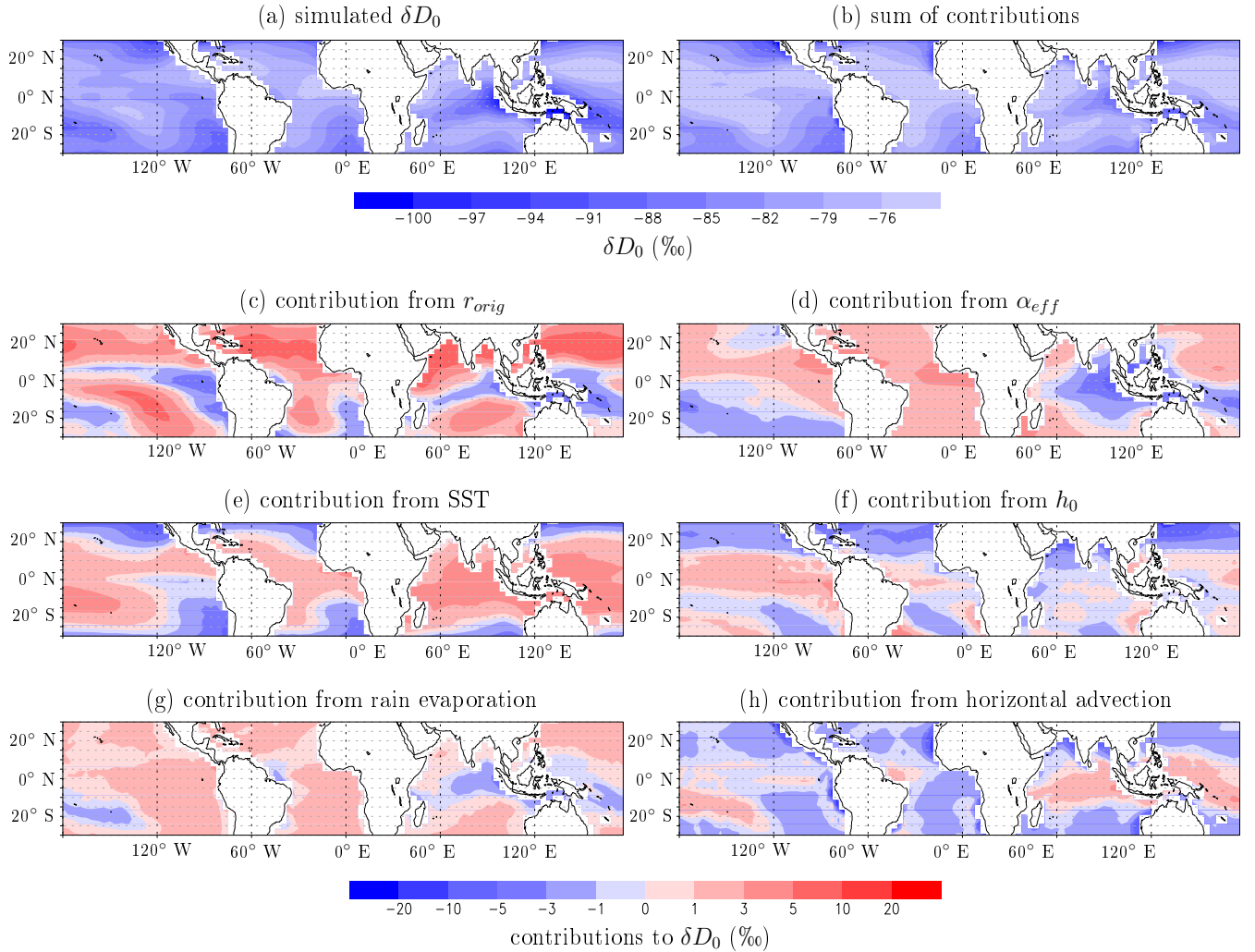


Figure 7. a) Map of winter-mean δD_0 simulated by LMDZ. b) Map of winter-mean δD_0 reconstructed as the sum of the 4 contributions. **Note that to focus on variations only and to get values of the same order of magnitude as the simulated Tropical-mean δD_0 field, we subtracted the mean of the 4 contributions and was added the mean of simulated δD_0 to compare with a on the reconstructed δD_0 field same color scale.** c) Map of the contribution of r_{orig} on winter-mean δD_0 calculated from Eq. (9) **if only r_{orig} varies** (see section 3.6). d) Same as b but **of only for α_{eff} varies**. e) Same as b but **if only for SST varies**. f) Same as b but **if only for h_0 varies**.

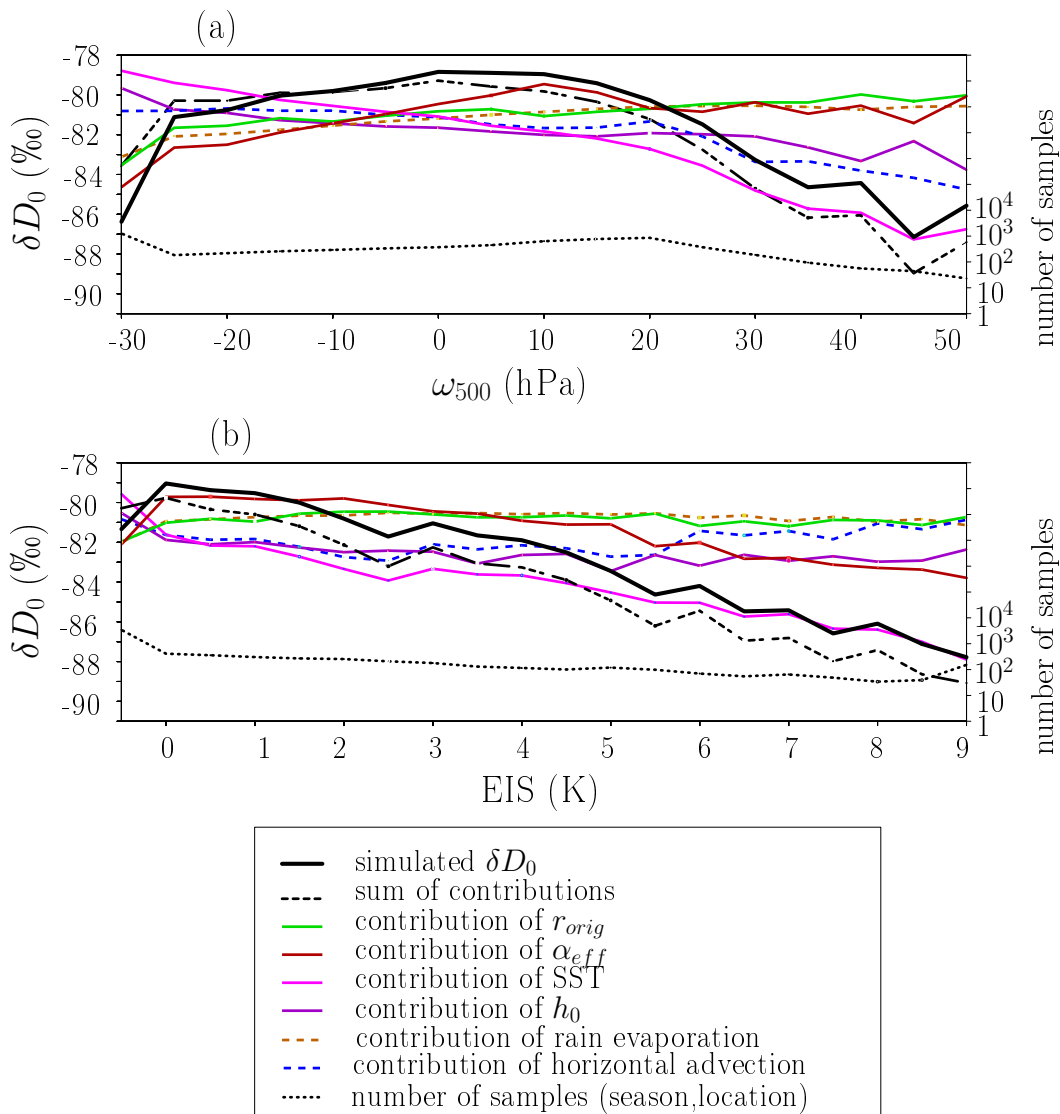


Figure 8. Composites as a function of ω_{500} (a) and of EIS (b) of the seasonal averages of δD_0 simulated by LMDZ over all tropical ocean locations (black). Same for the sum of the contributions (black dashed) and for each individual contribution to δD_0 : r_{orig} varies (green), α_{eff} (dark red), SST (pink) and h_0 (purple), rain evaporation (dashed brown) and horizontal advection (dashed blue). The tropical mean δD_0 was added to each contribution to plot on the same scale as simulated δD_0 . The number of samples in each bin is indicated on a logarithmic scale on the right-hand-side (dotted black line).

<u>Regime</u>	Ascending		Subsiding	
	<u>correlation coefficient</u>	<u>slope</u>	<u>correlation coefficient</u>	<u>slope</u>
r_{orig}	<u>0.46</u>	<u>0.52</u>	<u>0.42</u>	<u>0.82</u>
α_{eff}	<u>0.34</u>	<u>0.35</u>	<u>0.14</u>	<u>0.40</u>
SST	<u>-0.12</u>	<u>-0.01</u>	<u>0.25</u>	<u>0.22</u>
h_0 variations	<u>0.06</u>	<u>0.26</u>	<u>0.15</u>	<u>0.39</u>
rain evaporation	<u>0.49</u>	<u>0.48</u>	<u>0.19</u>	<u>0.20</u>
horizontal advection	<u>-0.26</u>	<u>-0.24</u>	<u>-0.15</u>	<u>-0.31</u>

Table 3. As in table 4 but at the correlation coefficient of the linear regression of the contribution as a function of δD_0 daily scale. The threshold for the correlation coefficient to be statistically significant at 99% is 0.15 or lower in coefficients and slopes are averaged over all cases. The analysis is done seasons and locations over tropical oceans ($30^\circ N - 30^\circ S$, ocean fraction > 80%), separately for ascending and subsiding regimes. All seasons and tropical oceans locations are considered.

In regions of strong large-scale ascent, r_{orig} is larger mainly because h_{orig} is larger (Fig. 9e, 10a pink). This suggests that even though the effect of rain evaporation may artificially bias high the estimate of r_{orig} , a substantial part of the r_{orig} signal is actually physical. Indeed, if the large r_{orig} was purely an artifact of the neglect of rain evaporation, it would translate totally into a lower z_{orig} . Physically, the is because the moister the FT, the higher the contribution of vapor coming from above to the vapor of the SCL, and thus the higher r_{orig} and the more depleted δD_0 . This mechanism through which a moister FT leads to a more depleted δD_0 is consistent with that argued in B15. z_{orig} damps this effect: when convection is stronger and the FT moister, convection is also deeper, so the air originates from higher in altitude where the air is drier.

In very stable regions, r_{orig} is larger mainly because q_0 is small larger (Fig. 9c, 10b green), consistent with the drier conditions in these regions of large-scale descent, and. Note that this effect can be seen only in most stable regions, but when considering all subsiding regions, the contribution is small (Table 2). r_{orig} is larger also because z_{orig} is lower in altitude (Fig. 9d, 10b red), consistent with the shallower boundary layers as EIS increases. Physically, the lower in altitude the. As EIS increases, the boundary layers are shallower, the air comes from the higher lower in altitude, r_{orig} and the more depleted is higher and thus δD_0 is more depleted. This mechanism was not considered in Benetti et al. (2015) B15 but our decomposition shows that it is a key mechanism driving r_{orig} and thus δD_0 variations in stable regions.

Quantitatively, in ascending regions, the main factors factor controlling the seasonal-spatial variations in r_{orig} are is h_{orig} (94.182%) and, dampened by z_{orig} (61-67%) (Table 4). Similarly, in descending regions, the main factors are factor is also h_{orig} (91.96%) and, followed by z_{orig} (72.41%) (Table 4). At the daily scale, the same two factors dominate the variability of r_{orig} : h_{orig} and z_{orig} contribute to 67.78% and 76.39% of r_{orig} variations in average over ascending regions, and to 40.4118% and 73.39% in average over descending regions (Table 5).

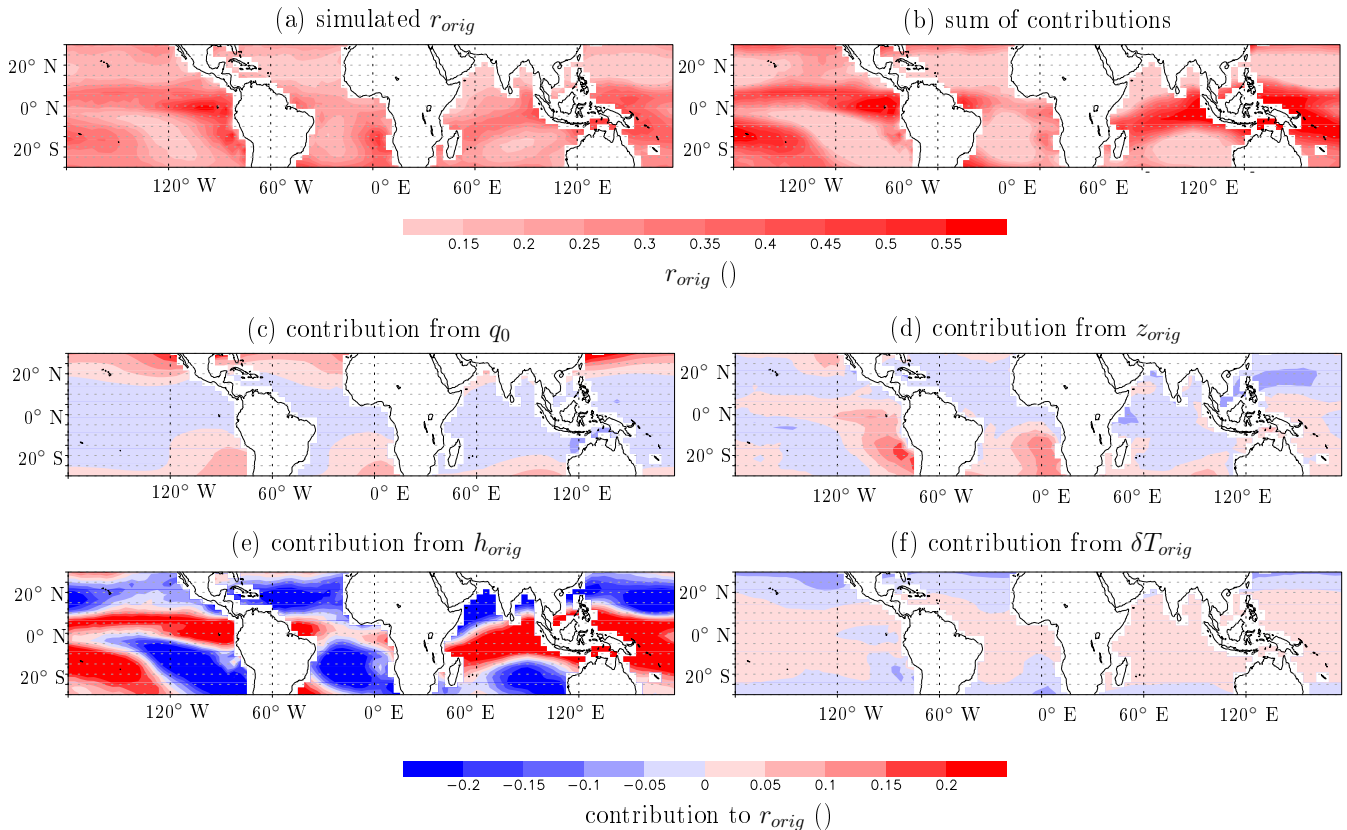


Figure 9. a) Map of winter-mean r_{orig} simulated by LMDZ. b) Map of winter-mean r_{orig} reconstructed as the sum of the 4 contributions. Tropical-mean r_{orig} was added to compare with a with the same color scale. c) Map of winter-mean r_{orig} calculated from Eq. (11) if only q_0 varies (see section 3.6). d) Same as b but of only z_{orig} varies. e) Same as b but if only $h(z_{orig})$ varies. f) Same as b but if only δT_{orig} varies.

4.3 Entrainment Estimating altitude estimate z_{orig} .

Estimated altitude z_{orig} is minimum in dry subsiding regions, especially in upwelling regions (Fig. 11a, Fig. 12), corresponding to regions with the strongest inversion (Fig. 11). This contributes to the depleted δD_0 in these regions.

As explained in 3.3, our estimate of z_{orig} may be artificially biased due to the neglect of some processes in our theoretical framework. Ideally, to check whether z_{orig} really physically represents the altitude from which the air originates, additional model experiments where water vapor from different levels are tagged (Risi et al., 2010b) would be needed. While we leave this for future work, in the meanwhile we check whether z_{orig} estimates are consistent with what we expect based on what we know about mixing processes in the marine boundary layers. We expect that in strato-cumulus regions, air is entrained originates from a very shallow (a few tens of meters) layer above the inversion, whereas the mixing processes may be more diverse, and possibly deeper in the FT, as the boundary layer deepens (Fig. 1).

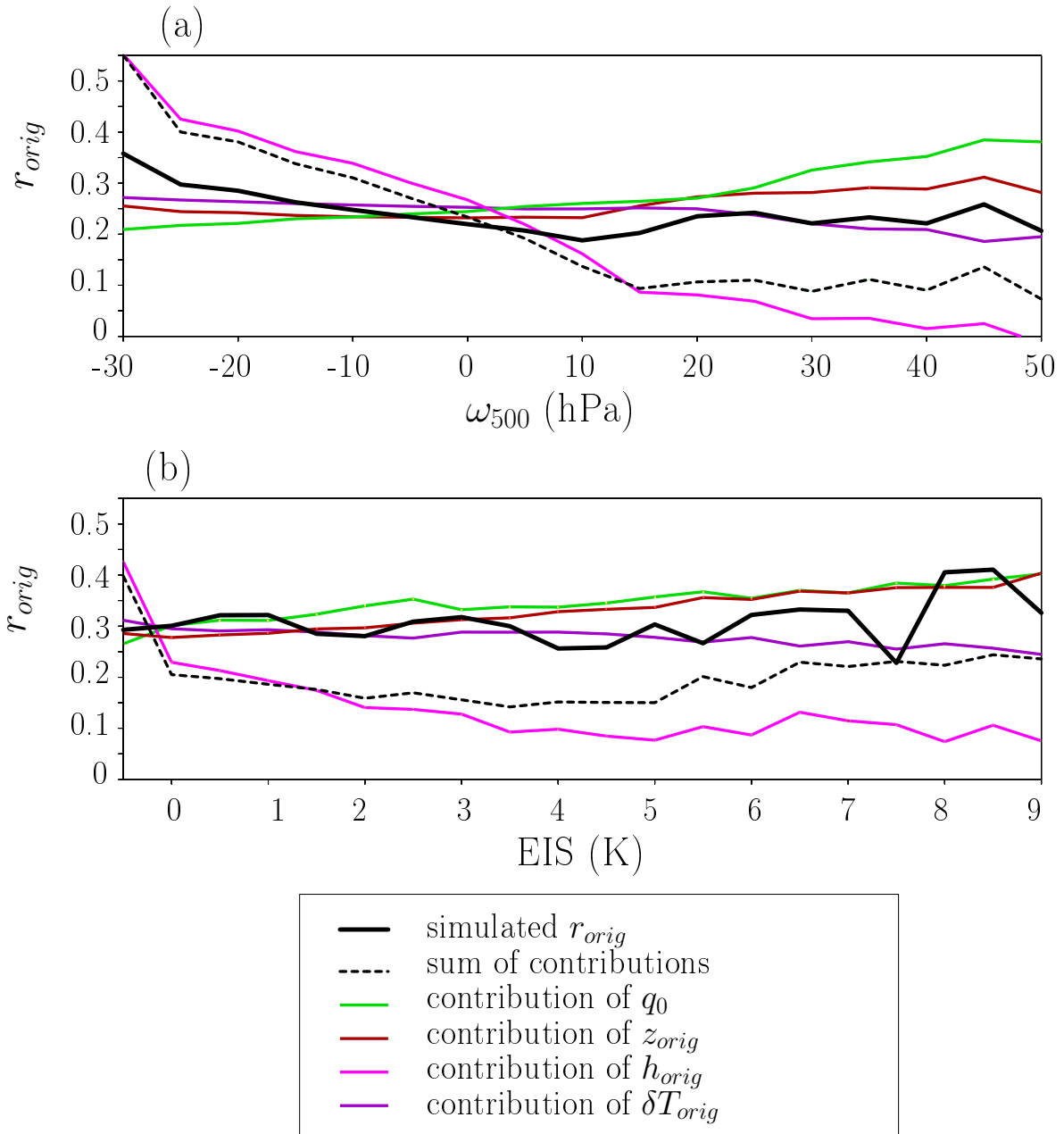


Figure 10. Composites as a function of ω_{500} (a) and of EIS (b) of the seasonal averages of r_{orig} simulated by LMDZ over all tropical ocean locations (black). Same for the sum of the contributions (black dashed) and for each individual contribution to r_{orig} : q_0 varies (green), z_{orig} (dark red), $h(z_{orig})$ (pink) and δT_{orig} (purple). [The number of samples in each bin is indicated on a logarithmic scale on the right-hand-side as bars.](#)

Regime	Ascending		Subsiding	
	correlation coefficient	slope	correlation coefficient	slope
q_0	-0.24 -0.82	0.0 -0.33	0.09-0.21	0.00-0.12
z_{orig}	0.88-0.91	0.61-0.67	0.65-0.77	0.72-0.41
h_{orig}	0.75-0.98	0.94-1.82	0.53	0.91-0.96
δT_{orig}	0.33-0.55	0.12-0.06	-0.34-0.37	-0.27-0.12

~~Decomposition of the spatial-seasonal variation in r_{orig} into its 4 contributions: effect of-~~

Table 4. ~~Decomposition of the spatial-seasonal variation in r_{orig} into its 4 contributions: effect of q_0 , z_{orig} , h_{orig} and δT_{orig} variations. For each contribution, we show the correlation coefficient of the linear regression of the contribution as a function of r_{orig} . The analysis is done separately for ascending and subsiding regimes. All seasons and locations over tropical oceans ($30^\circ N - 30^\circ S$, ocean fraction > 80%) are considered. The threshold for the correlation coefficient to be statistically significant is 0.15 or lower in all cases. We write correlation coefficient and slope values between brackets when they are not significant at 99%.~~

Regime	Ascending		Subsiding	
	correlation coefficient	slope	correlation coefficient	slope
q_0 -	-0.37	-0.04	-0.23	-0.07
z_{orig} -	0.91	0.39	0.80	0.39
h_{orig} and-	0.58	0.78	0.58	1.18
δT_{orig} variations. For each contribution, we show-	-0.14	0.01	-0.23	-0.12

Table 5. ~~As in table 4 but at the correlation coefficient of the linear regression of the contribution as a function of r_{orig} daily scale. The threshold for the correlation coefficient to be statistically significant is 0.15 or lower in coefficients and slopes are averaged over all cases. The analysis is done seasons and locations over tropical oceans ($30^\circ N - 30^\circ S$, ocean fraction > 80%), separately for ascending and subsiding regimes. All seasons and tropical oceans locations are considered.~~

To check whether estimated z_{orig} is consistent with this picture, we compare z_{orig} to $z_{orig, r_{orig}=0.6}$ (z_{orig} that we would estimate if r_{orig} was set constant to 0.6) and z_i (section 3.4), which are measures of the altitude of the humidity drop and temperature inversion respectively. As expected from Fig. 1, they are minimum in dry upwelling regions, intermediate in trade-wind regions, and maximum values in convective regions (Fig. 11c-d, 12 green, blue). Therefore, the low z_{orig} in upwelling regions reflects the low z_i . Consistently, in subsiding regions, z_{orig} correlates well with $z_{orig, r_{orig}=0.6}$ (correlation coefficient of 0.52, statistically significant beyond 99 %). If we focus on very stable regions only (EIS > 7 K), z_{orig} correlates well with both $z_{orig, r_{orig}=0.6}$ and z_i (correlation coefficient of 0.58 and 0.52 respectively, statistically significant beyond 99 %). The altitude z_{orig} is a few meters above the inversion in strato-cumulus regions, and up to 1km above the inversion in cumulus and deep convective regions (Fig. 12), consistent with our expectations from Fig. 1. This lends support to the fact that at least in subsiding regions, our isotope-based z_{orig} estimate effectively ~~reflect~~ reflects the origin of air coming from above.

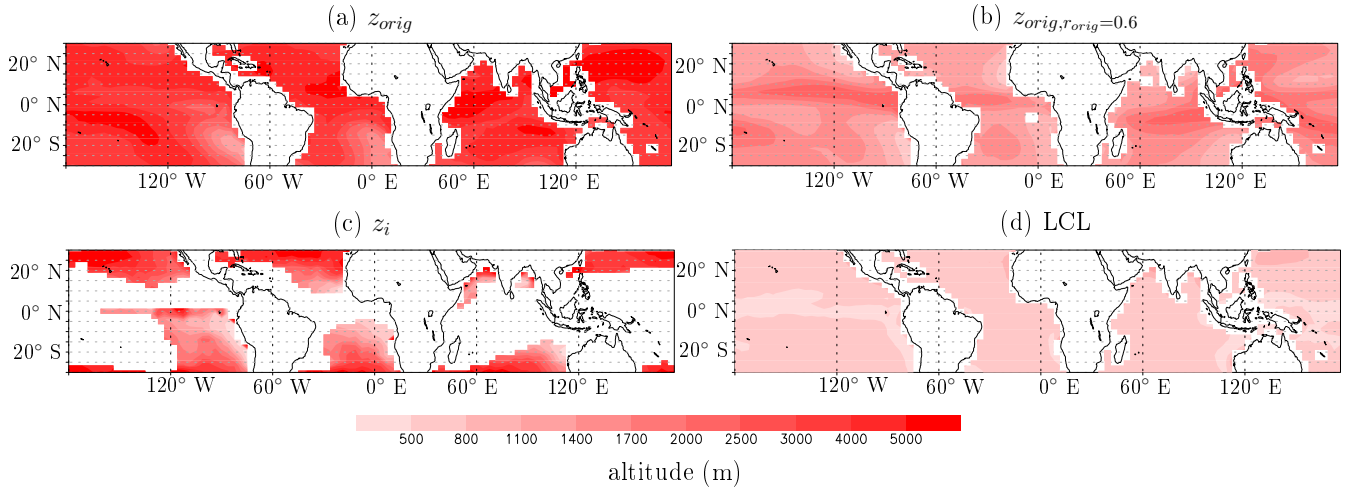


Figure 11. a) Map of winter-mean z_{orig} estimated from δD_0 simulated by LMDZ. b) Same as a but z_{orig} that we would estimate if r_{orig} was constant set to 0.6 ($z_{orig,r_{orig}=0.6}$). c). Same as a but for z_i simulated from LMDZ. Only days when $EIS > 2$ K are considered, otherwise z_i is difficult to estimate. d) Same as a but for LCL simulated by LMDZ.

In ascending regions, in contrast, z_{orig} does not correlate significantly with $z_{orig,r_{orig}=0.6}$ or z_i . This may indicate either that our z_{orig} estimate is biased by neglected processes such as rain evaporation, or that in deep convective regions, the origin of FT air into the SCL is very diverse due to the variety of mixing processes (1).

5 Results from observations

- 5 To check whether our results obtained with LMDZ are realistic, we apply our methods to the measurements gathered during the STRASSE campaign. ~~In the absence of measured δD profiles, we assume that α_{eff} is 1.07 based on LMDZ simulation~~ For simplicity and in absence of all necessary measurements, here we neglect the effects of rain evaporation and horizontal advection.

Throughout the cruise, δD_0 shows a large variability, ranging from around -75 ‰ in quiescent conditions to -120 ‰ during
 10 the two convective conditions (Benetti et al., 2014) (Fig. 13a red). Variability in r_{orig} is the major factor contributing to this variability (58 %) (Fig. 13a green, Table 6). This crucial importance of mixing processes is consistent with B15.

During the two convective events, the estimated r_{orig} saturates at 1 (Fig. 13b). This proves that r_{orig} estimated in these conditions is biased high because it encapsulates the effect of neglected processes, i.e. depletion by rain evaporation. Equation (9) is not valid in this case. In addition, at the scale of a few hours, the steady-state assumptions may be violated. Rain
 15 evaporation may strongly deplete the SCL before surface evaporation has the time to play its dampening role, hence the possibility to reach very low δD_0 that cannot be predicted even when considering rain evaporation (appendix B).

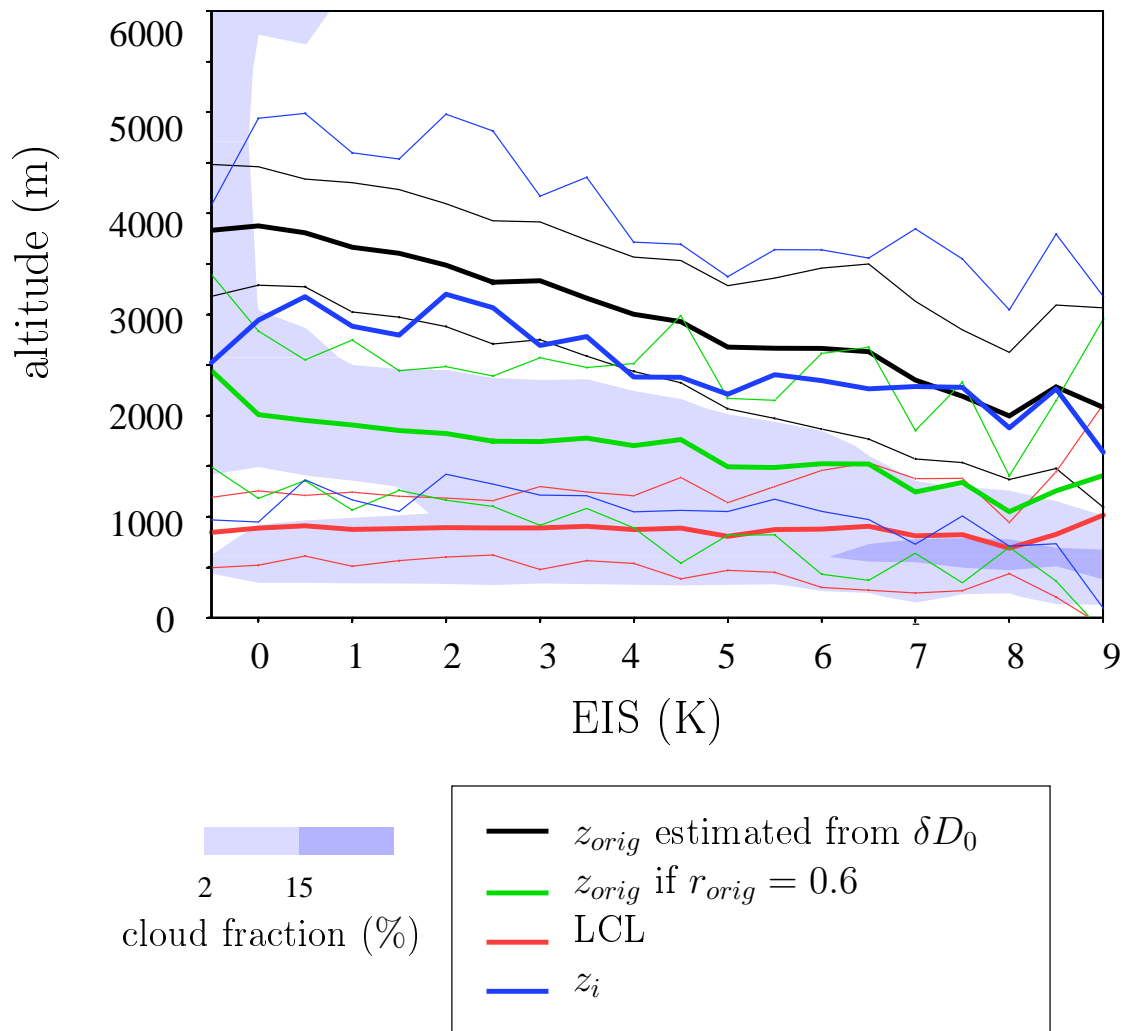


Figure 12. Composites as a function of EIS of seasonal-mean of z_{orig} (black), $z_{orig, r_{orig}=0.6}$ (green), z_i (blue) and LCL (red). The composite profiles of cloud cover are also shown, showing deep clouds when EIS is close to 0 and shallowest clouds when EIS is largest.

contributions to δD_0	correlation coefficient	slope
r_{orig}	0.77	0.58
SST	0.57	0.16
h_0	0.40	0.48

Table 6. Same as Table 2 but for the STRASSE observations. Linear regressions are calculated among 1977 data points.

contributions to r_{orig}	correlation coefficient	slope
q_0	-0.46	-1.49
z_{orig}	0.66	0.90
h_{orig}	0.81	0.70
δT_{orig}	-0.36	-0.91

Table 7. Same as Table 4 but for the STRASSE observations. Linear regressions are calculated among 55 data points, so that correlation coefficients above 0.35 are statistically significant at 99 %.

During the rest of the cruise, the main factors controlling the r_{orig} variability are z_{orig} (90 %) and h_{orig} (70 %). The importance of FT humidity in controlling r_{orig} was already highlighted in B15. However, in their paper, the variability in z_{orig} was neglected, whereas it appears here as the main factor.

Through September, the ~~eruises-cruise~~ goes from a shallow boundary layer in early September to deeper boundary layers with higher inversions, before reaching the convective conditions (Fig. 13c). Consistently with this deepening boundary layer, the air ~~is entrained-originate~~s from increasingly higher in altitude. ~~When considering only the Remarkably, there are 6 data points when $z_{orig} < 2000$ m, days when z_{orig} coincides almost exactly with z_i with a root means square error of 31% and correlation coefficient of 0.996 (Fig. 13c; the correlation coefficient between z_{orig} and z_i is 0.996).~~ This indicates that the air ~~is entrained into the SCL exactly exactly comes~~ from the inversion layer. ~~Even if the number of sample is small, the coincidence is remarkable, especially when~~ ~~When~~ recalling that z_{orig} and z_i are estimated from completely independent observations. ~~This, the coincidence is remarkable and~~ lends support to the fact that ~~on these days,~~ our z_{orig} estimate is physical. ~~However, there remains 9 days when z_{orig} is much higher than z_j . This may reflect more penetrative downdrafts as we approach deeper convective regimes. But it may also be an artifact of our neglect of horizontal advection. For example, on these days which are characterized by lower h_0 , neglecting the advection of enriched water vapor from nearby regions with higher h_0 could be mis-interpreted as lower r_{orig} and thus higher z_{orig} .~~

6 Discussion: what can we learn from water isotopes on mixing processes?

We have shown in the previous section that one of the main factors controlling δD_0 at the seasonal-spatial and daily scale are the proportion of the water vapor in the SCL that ~~is~~-originates from above (r_{orig}), and that one of the main factor controlling r_{orig} is the altitude from which the air originates (z_{orig}). In turn, could we use water vapor isotopic measurements to constrain

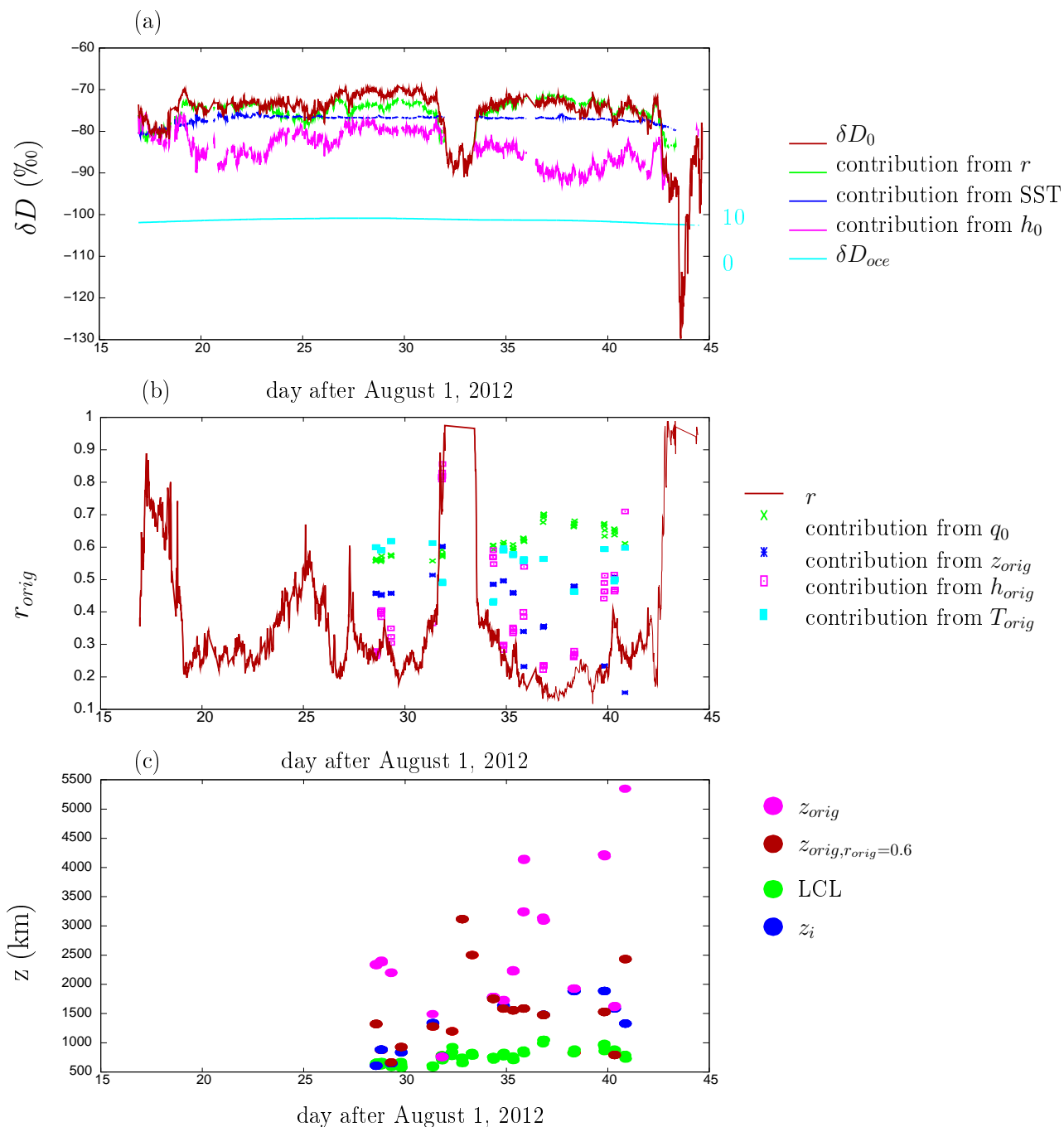


Figure 13. a) Time series of δD_0 observed during the STRASSE cruise, together with its 4 contributions. The δD of the surface ocean water is also plotted with the scale on the right. b) Time series of r_{orig} estimated from observations during the STRASSE campaign, together with its 4 contributions. c) Times series of z_{orig} , $z_{orig,r_{orig}=0.6}$, LCL and z_i estimated from the STRASSE observations.

z_{orig} ? This would open the door to discriminating between different mixing processes at play (Fig. 1). Since mixing processes are crucial to determine the sensitivity of cloud fraction to SST (Sherwood et al., 2014; Bretherton, 2015; Vial et al., 2016), such a prospect would allow us to improve our knowledge of cloud feedbacks, and hence of climate sensitivity.

With this in mind, we assess the errors associated with z_{orig} estimates from δD_0 measurements, and discuss whether ~~there~~ ~~they~~ are small enough for z_{orig} estimates to be useful. In strato-cumulus clouds where the air is believed to ~~be entrained~~ ~~originate~~ from the first few tens of meters above cloud top (Faloona et al., 2005; Mellado, 2017), z_{orig} estimates are not useful if the errors are larger than a few tens of meters, e.g. 20 m. In cumulus clouds where mixing processes are more diverse and possibly deeper (Fig. 1), z_{orig} estimates may be useful if errors are of the order of 80 m.

Let's assume that we have a field campaign where we measure δD_0 , surface meteorological variables, temperature and humidity profiles (e.g. radio-soundings), and a few δD profiles (e.g. by aircraft). This is what we can expect for example from the future EUREC4A (Elucidating the role of clouds-circulation coupling in climate) campaign to study trade-wind cumulus clouds (Bony et al., 2017). Below we quantify the effects of five sources of uncertainty on z_{orig} estimates.

6.1 Measurement errors

The first source of uncertainty ~~that we have highlighted in this article is the effect of rain evaporation. As long as the~~ ~~microphysical processes and associated isotopic fractionation processes are not well constrained~~ are measurement errors. We re-calculate z_{orig} assuming an error of 0.4 ‰ on δD_0 (typical of what we can measure with in-situ laser instruments, Aemisegger et al. (2012); Benetti et al. (2014)) and 1 ‰ on δD_f (larger errors due to lower humidity and the increased complexity of measurements in altitude). The averaged errors on z_{orig} and their standard deviations are plotted as a function of EIS in Fig. 14a. Whereas errors on δD_f lead to errors on z_{orig} of the order of 20 m (Fig. 14a, green), errors on δD_0 lead to errors on z_{orig} of the order of 80 m (Fig. 14a, red). Yet in strato-cumulus, none expects the air to originate from a higher altitude than 80 m above the inversion. Therefore, δD_0 measurements would need to be more accurate than usual to be useful in strato-cumulus regions, i.e. 0.1 ‰ to yield a 20 m precision on z_{orig} . In trade-wind cumulus regions, the precision of 0.4 ‰ is enough for z_{orig} to be useful.

6.2 Neglecting rain evaporation

The second source of uncertainty is associated with neglecting rain evaporation. This effect can be quantified in a model, but it is very difficult to quantify in nature because it is complicated and uncertain to measure η (Rosenfeld and Mintz, 1988), and it is even more complicated to measure or predict α_{evap} . Rain evaporation can have a depleting or enriching effect depending on microphysical details that are too complex to be addressed here (Graf et al., 2019). Neglecting rain evaporation leads to an error of the order of 500 m in regions of low EIS and 250 m in regions of strong EIS (Fig. 14b, brown). In regions of strato-cumulus regions, rain evaporation is a significant source of error in spite of the relatively small amount of precipitation available to evaporate. This is because total evaporation of the rain efficiently enriches the SCL, and easily modifies δD_0 by more than the 0.1‰ targeted precision explained above. However, it is ~~safer to restrain z_{orig} estimates to non-precipitating clouds~~ possible that LMDZ overestimates this source of error in trade-wind cumulus and strato-cumulus regions. LMDZ is one of the GCMs

producing the strongest rain in srato-cumulus regions (Zhang et al., 2013), and GCMs are known to trigger convection to often in trade-wind cumulus regions (Nuijens et al., 2015a, b).

~~The second-~~

6.3 Neglecting horizontal advection

- 5 ~~The third~~ source of uncertainty is ~~the~~ associated with horizontal advection. In nature, ϕ can be estimated from meteorological analyzes and β can be estimated from near-surface isotopic measurements at several locations (e.g. sounding arrays during typical field campaigns). In absence of these additional measurements, neglecting this effect leads to an error of the order of 800 m (Fig. 14b, purple). This limits the usefulness of z_{orig} estimates for all cloud regimes.

6.4 Daily variability in the steepness of δD profiles

- 10 ~~The fourth~~ source of uncertainty arises from the daily variability in α_{eff} ~~-Measuring daily-~~ (appendix D2). Estimating α_{eff} requires to measure δD_f at 500 hPa. Satellite measurements are available but are affected by random errors that are too large for our application (Worden et al., 2011, 2012; Lacour et al., 2015). Precise in-situ measurements of water vapor δD profiles ~~is-in altitude are~~ costly and difficult (Sodemann et al., 2017).

- Let's assume that we have only one ~~profile~~ δD_f value that represents the seasonal-average at a given location. ~~The daily~~ standard deviation of α_{eff} ($\sigma_{\alpha_{eff}}$) for a given season ranges from 5‰ in the Central Atlantic to 40‰ near the Maritime Continent (Fig. D1d). To estimate the resulting error on z_{orig} , we re-estimate z_{orig} every day and at each location using $\alpha_{eff}^- + \sigma_{\alpha_{eff}}$ and $\alpha_{eff}^- - \sigma_{\alpha_{eff}}$. The error on z_{orig} is calculated as $(z_{orig}(\alpha_{eff}^- - \sigma_{\alpha_{eff}}) - z_{orig}(\alpha_{eff}^- + \sigma_{\alpha_{eff}})) / 2$. The averaged error and its standard deviation is plotted as a function of EIS in Fig. 14c (black). It is of the order of 400m, and rarely below 200m. If we attempt to estimate α_{eff} as the fractionation coefficient as a function of local temperature, errors would be even more dissuasive (Fig. 14c, blue).

- Therefore, estimating z_{orig} from ~~daily~~ δD_0 measurements cannot be useful unless we measure ~~daily δD profiles~~ δD_f on a ~~daily basis as well~~. Practically, we could imagine measuring FT properties (δD_f) at the top of a mountain while we measure δD_0 at the sea level (e.g. on Islands such as Hawaii or La Réunion, Galewsky et al. (2007); Bailey et al. (2013); Guilpart et al. (2017) ~~)-We could also imagine retrieving α_{eff} from daily~~ Galewsky et al. (2007); Bailey et al. (2013); Guilpart et al. (2017) ~~).~~

25 6.5 Rayleigh assumption for the shape of δD profiles

- Finally, a fifth source of uncertainty comes the assumption that the δD profiles ~~retrieved from space by IASI (Infrared Atmospheric Sounding Interferometer, Lacour et al. (2012, 2015))~~, but this would be associated with additional errors whose estimate is beyond the scope of this paper profile follows a Rayleigh distillation line (section 2.2). However, both in LMDZ (appendix D1) and nature (Sodemann et al., 2017), δD profiles are usually intermediate between Rayleigh and mixing lines.
- 30 ~~The precision of our z_{orig} estimate is maximum in the Rayleigh distillation case.~~

The third source of uncertainty are measurements errors. We recalculate z_{orig} assuming an error of 0.4 ‰ on δD_0 (typical of what we can measure with in-situ laser instruments, Benetti et al. (2014)) and 1 ‰ on δD_f (larger errors due to lower humidity and the increased complexity of measurements in altitude). Whereas errors on δD_f lead to errors on z_{orig} directly from Eq. (6), a solution can be found only in 0.1 % of cases. This is because simulated δD profiles are often close to a mixing line in the lower troposphere (appendix D1). Whatever z_{orig} of the order of 20 m (Fig. 14, green), errors on δD_0 lead to errors on z_{orig} calculated from Eq. (6) is nearly constant because the δD profile is close to a mixing line (appendix A, Fig. 4b). Whatever z_{orig} of the order of 80 m. This is higher than the upper bound for the expected entrainment altitude in strato-cumulus. Therefore, in the middle troposphere, the δD_0 measurements would need to be more accurate than usual to be useful in strato-cumulus regions, i.e. 0.1 ‰ to yield a 20 m precision on z_{orig} . In the lower troposphere, the δD_0 lead to errors on z_{orig} calculated from Eq. (6) is also nearly constant because r_{orig} there is very small. So whatever z_{orig} in the lower troposphere, the δD calculated from Eq. (6) is nearly constant, and the numerical solution fails.

However, it is possible that δD profiles simulated by LMDZ are closer to mixing lines than real profiles, since GCMs are known to overestimate vertical mixing through the troposphere (Risi et al., 2012b) and to mix the lower free troposphere too frequently by deep convection in trade-wind cumulus regions, the precision is enough for z_{orig} to be useful. regions (Nuijens et al., 2015a, b). Therefore, the shape of δD profiles simulated by LMDZ is not a sufficient reason to reject the Rayleigh assumption. The uncertainty associated with this assumption is very difficult to quantify in LMDZ. More measurements of full δD profiles are very welcome to help quantify it.

To summarize, δD_0 measurements could potentially be useful to estimate z_{orig} with a useful precision in cumulus and strato-cumulus clouds, but only if we are able to measure daily δD_f in the mid-troposphere, if the shape of δD profiles and if can be better documented, if we measure δD_0 at different places to quantify the effect of horizontal advection, and if we can invent innovative techniques to better quantify the effect of rain evaporation. In addition in strato-cumulus clouds, we need to measure δD_0 with an accuracy of 0.1 ‰ and 0.4 ‰ in trade-wind cumulus and strato-cumulus clouds respectively.

7 Conclusion

We propose an analytical model to predict the water vapor isotopic composition δD_0 of the sub-cloud layer (SCL) over tropical oceans. Benetti et al. (2015) extended the Merlivat and Jouzel (1979) This model relies on the hypothesis that the altitude from which the air originates, z_{orig} , is an important factor. We build on Benetti et al. (2015) who extended the Merlivat and Jouzel (1979) closure equation to make explicit the link between δD_0 and FT entrainment mixing processes. We further extend the Benetti et al. (2015) equation in two ways: first, we assume that we know the shape of their equation: we assume a shape for the δD vertical profiles, and second, we let the altitude from which the air originates, z_{orig} , vary as a function of q , and we account for horizontal advection and rain evaporation effects.

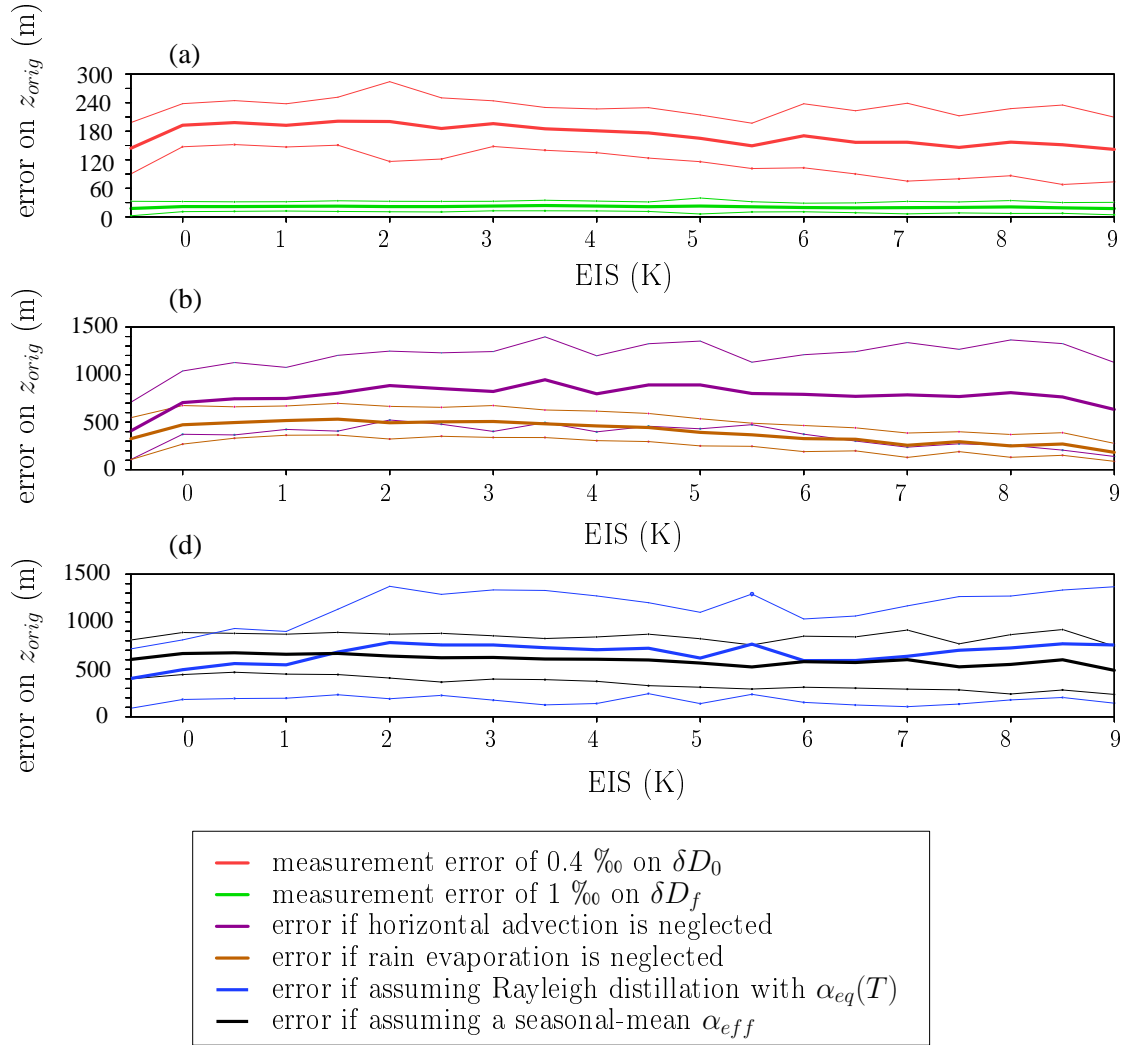


Figure 14. Errors when estimating z_{orig} from δD_0 observations, as a function of EIS, as predicted by LMDZ: ~~error if one uses α_{eq} as a function of local temperature to estimate α_{eff} , error if one uses the seasonal-mean profile instead of the daily profile to estimate α_{eff} (black), error we would make if δD_0 is measured with a 1‰ error (red), and error we would make if δD_f is measured with a 1‰ error (green). b) error we would make if we neglect horizontal advection effects (purple) and rain evaporation effects (brown). c) Error if one uses α_{eq} as a function of local temperature to estimate α_{eff} (blue), error if one uses the seasonal-mean profile instead of the daily profile to estimate α_{eff} (black). The standard deviations among all daily errors estimated in each bin of EIS are also shown.~~

The resulting equation highlights the fact that δD_0 is not sensitive to the intensity of ~~entrainment~~mixing processes. Therefore, it is unlikely that water vapor isotopic measurements could help estimate the entrainment velocity that many studies have ~~strived~~striven to estimate (Bretherton et al., 1995). In contrast, δD_0 is sensitive to the altitude from which the air originates. Based on a simulation with LMDZ and observations during the STRASSE cruise, we show that z_{orig} is an important factor
5 explaining the seasonal-spatial and daily variations in δD_0 , especially in subsidence regions. In turn, could δD_0 measurements, combined with vertical profiles of humidity, temperature and δD , help estimate z_{orig} and thus discriminate between different mixing processes? ~~This should rely on a good knowledge of the δD vertical profiles. We find that for~~ For such isotope-based estimates of z_{orig} to be useful, we would need ~~frequent vertical profiles of a precision of a few hundreds meters in deep convective regions and smaller than 20 m in strato-cumulus regions. To reach this target, we would need daily measurements~~
10 of δD in the mid-troposphere and very accurate measurements of δD_0 , which are currently difficult to obtain. ~~In precipitating clouds and deep convection~~ We would also need information on the horizontal distribution of δD to account for horizontal advection effects, and full δD profiles to quantify the uncertainty associated with the assumed shape for δD profiles. Finally, rain evaporation is ~~too large a source of uncertainty, whereas in an issue in all regimes, even for strato-cumulus regions, very precised estimates of z_{orig} (no larger than 20 m) would be needed to be useful. Therefore, it is in regions of shallow~~
15 cumulus clouds that such isotope-based estimates of z_{orig} would be most useful. ~~clouds. Innovative techniques would need to be developed to quantify this effect from observations.~~

This study is preliminary in many respects. First, it would be safe to check using water tagging experiments in LMDZ that z_{orig} estimates really ~~represents~~represent the altitude from which the air ~~is~~ originates, and is not ~~to biases~~biased by our simplifying assumptions. Second, the coarse vertical resolution of LMDZ, and the simplicity of mixing parameterizations
20 (e.g. cloud top entrainment is not represented) are a limitation of this study. Ideally, the relationship between δD_0 , z_{orig} and the type of mixing processes should be investigated in isotope-enabled Large Eddy Simulations (LES) (Blossey et al., 2010; Moore et al., 2014). Artificial tracers and structure detection methods (Park et al., 2016; Brient et al., 2019), combined with conditional sampling methods (Couvreux et al., 2010), could help detect the different kinds of mixing structures, estimate their contributions to vertical transport, and describe their isotopic signature. This would allow us to confirm, or infirm, many of
25 the hypotheses and conclusions in this paper. Finally, if the sensitivity of δD_0 to the type of mixing processes is confirmed, paired isotopic simulations of single-column model (SCM) versions of general circulation models (GCM) and LES, forced by the same forcing, could be very useful to help evaluate and improve the representation of mixing and entrainment processes in GCMs, as is routinely the case for non-isotopic variables (Randall et al., 2003; Hourdin et al., 2013; Zhang et al., 2013).

Code and data availability. LMDZ can be downloaded from <http://lmdz.lmd.jussieu.fr/>. Program codes used for the analysis are available
30 on https://prodn.idris.fr/thredds/catalog/ipsl_public/r1md698/article_mixing_processes/d_pgmf/catalog.html.

Isotopic measurements from STRASSE can be downloaded from <http://cds-espri.ipsl.fr/isowvdataatlantic/>. All other datasets and processed files are available on https://prodn.idris.fr/thredds/catalog/ipsl_public/r1md698/article_mixing_processes/catalog.html.

Appendix A: Closure if the tropospheric profile follows a mixing line

For simplicity, we neglect here horizontal advection and rain evaporation effects, but results would be similar otherwise. If we assume that R_{orig} is uniquely related to q_{orig} through a mixing line between the SCL air and a dry end-member (q_f, R_f):

$$q_{orig} = a \cdot q_0 + (1 - a) \cdot q_f \quad (A1)$$

5 and

$$R_{orig} = a \cdot q_0 \cdot R_0 + (1 - a) \cdot q_f \cdot R_f \quad (A2)$$

Reorganizing Eq. (A1), we get $a = \frac{r-p}{1-p}$ with $p = q_f/q_0$. Since $q_f \leq q_{orig} \leq q_0$, $p \leq r_{orig}$. Injecting Eq. (A2) into 6, we get:

$$R_0 = \frac{R_{oce}/\alpha_{eq} + p/(1-p) \cdot R_f \cdot \alpha_K \cdot (1 - h_0)}{h_0 + \alpha_K \cdot (1 - h_0)/(1 - p)} \quad (A3)$$

As a consistency check, in the limit case where the end-member is totally dry ($p = 0$), we find the MJ79 equation, i.e. Eq. 10 (10).

It is intriguing to realize that r_{orig} has disappeared from Eq. (A3). This can be understood physically: if the vertical profile follows a mixing line, it does not matter at from which altitude the air comes from: ultimately, what matters is how much dry air has been mixed directly or indirectly into the SCL. This can be visualize in Fig. 4b. Therefore, if R_{orig} follows a mixing line, we lose the sensitivity to z_{orig} .

15 Appendix B: **Modification in case of** Diagnostics for rain evaporation in LMDZ

~~An important assumption that led to Eq. (9) is the neglect of SCL moistening by rain evaporation. Here we test the sensitivity to this assumption by adding a rain evaporation component. The new water vapor~~ Rain evaporation can be accounted for in equation 8 if we can quantify η , the ratio of water vapor originating from rain evaporation to that originating from surface evaporation, and α_{evap} , the ratio of isotopic ratio in the rain evaporation flux to R_0 .

20 B1 Equations

In LMDZ, two parameterization schemes can produce rain evaporation: the convective scheme and the large-scale condensation scheme. Their respective precipitation evaporation tendencies, $(dq/dt)_{evap,conv}$ and isotopic budgets of the SCL write $(dq/dt)_{evap,lsc}$, are given in $kg_{water} \cdot kg_{air}^{-1} \cdot s^{-1}$ and are used to calculate F_{evap} in $kg_{water} \cdot m^{-2} \cdot s^{-1}$:

$$\underline{M \cdot q_{orig} + F + E = (N + D) \cdot q_0}$$

$$F_{evap} = \sum_{k=1}^{k_{LCL}} \left((dq/dt)_{evap,conv} + (dq/dt)_{evap,lsc} \right) \cdot \frac{\Delta P_k}{g}$$

$$M \cdot q_{orig} \cdot R_{orig} + F \cdot R_F + E \cdot R_E = (N + D) \cdot q_0 \cdot R_0$$

5 where F is the rain evaporation flux where k_{LCL} is the last layer below the LCL, ΔP_k is the depth of layer k in pressure coordinate and g is gravity.

The isotopic equivalent of this flux, $F_{evap,iso}$, is used to calculate $R_{evap} = F_{evap,iso}/F_{evap}$. We note $F = \eta \cdot E$. We write the isotopic composition of the rain evaporation, R_F , as

Only grid boxes and days where $F_{evap} > 0.05$ mm/d are considered to calculate α_{evap} . This represents 94.0% of all tropical oceanic grid boxes.

10 B2 Results

Consistent with the larger amount of precipitation available for evaporation, η is maximum in regions of deep convection, reaching 30% around the Maritime continent (Fig. C1a). It is minimal over the dry descending regions, reaching 5% off the coasts of Mauritania, Peru or Namibia. The rain evaporation is more depleted than the SCL in regions of strong deep convection, by as much as 70‰ around the Maritime continent (Fig. C1b). When the fraction of raindrops that evaporate is small, as is the case in such moist regions, isotopic fractionation favors evaporation of the lighter isotopologues. In these regions, rain evaporation has a depleting effect on the SCL, consistent with Worden et al. (2007). In contrast, in other regions, rain evaporation has an enriching effect on the SCL, up to 70‰ in dry regions. This is because in dry regions, rain evaporates almost totally, so that the evaporation flux has almost the same composition as the initial rain, which is more enriched than the water vapor.

20 Appendix C: Diagnostics for horizontal advection in LMDZ

We can account for horizontal advection in Eq. (8) if we can quantify parameters $\phi = \frac{F_{adv} \cdot q_{adv}}{E}$, the ratio of water vapor coming from horizontal advection to that coming from surface evaporation, and $\beta = R_{adv}/R_0$, the ratio of isotopic ratios of horizontal advection to that of the SCL.

C1 Equations

Let's assume that the box representing the SCL has a zonal extent Δy , a meridional extent Δx and is composed of k_{LCL} layers of vertical extent Δz_k . The quantity $F_{adv} \cdot q_{adv}$ represents the mass flux of water entering the grid box by horizontal advection per surface area, expressed in $kg_{water} \cdot s^{-1} \cdot m^{-2}$. Assuming an upstream advection scheme, it can be expressed as:

$$F_{adv} \cdot q_{adv} = \frac{\sum_{k=1}^{k_{LCL}} (\rho_k \cdot |u_k| \cdot q_{uk} \cdot \Delta y \cdot \Delta z_k + \rho_k \cdot |v_k| \cdot q_{vk} \cdot \Delta x \cdot \Delta z_k)}{\Delta x \cdot \Delta y} \quad (C1)$$

- 5 where u_k and v_k are the zonal and meridional wind components at layer k , ρ_k is the volumic mass of air at layer k , and q_{uk} and q_{vk} are the humidities of the incoming air from zonal and meridional advection at layer k . When $u_k > 0$, q_{uk} is the humidity in the grid box to the West. When $u_k < 0$, q_{uk} is the humidity in the grid box to the East. When $v_k > 0$, q_{vk} is the humidity in the grid box to the South. When $v_k < 0$, q_{vk} is the humidity in the grid box to the North.

- 10 Applying the hydrostatic equation at each layer ($\Delta P_k = \rho_k \cdot g \cdot \Delta z_k$, where g is gravity and ΔP_k is the vertical extent of the layer k in pressure coordinate), we get:

$$F_{adv} \cdot q_{adv} = \sum_{k=1}^{k_{LCL}} \frac{\Delta P_k}{g} \cdot \left(\frac{|u_k| \cdot q_{uk}}{\Delta x} + \frac{|v_k| \cdot q_{vk}}{\Delta y} \right)$$

The quantity F_{adv} represents the incoming air mass flux by horizontal advection, and q_{adv} represents the humidity of the incoming air. We can thus write them as:

$$F_{adv} = \sum_{k=1}^{k_{LCL}} \left(\frac{|u_k|}{\Delta x} + \frac{|v_k|}{\Delta y} \right) \cdot \frac{\Delta P_k}{g}$$

- 15 and

$$q_{adv} = \frac{\sum_{k=1}^{k_{LCL}} \left(\frac{|u_k|}{\Delta x} \cdot q_{uk} + \frac{|v_k|}{\Delta y} \cdot q_{vk} \right) \cdot \frac{\Delta P_k}{g}}{\sum_{k=1}^{k_{LCL}} \left(\frac{|u_k|}{\Delta x} + \frac{|v_k|}{\Delta y} \right) \cdot \frac{\Delta P_k}{g}}$$

The same budget as in Eq. C1 can be written for water isotopes:

$$F_{adv} \cdot q_{adv} \cdot R_{adv} = \frac{\sum_{k=1}^{k_{LCL}} (\rho_k \cdot |u_k| \cdot q_{uk} \cdot R_{uk} \cdot \Delta y \cdot \Delta z_k + \rho_k \cdot |v_k| \cdot q_{vk} \cdot R_{vk} \cdot \Delta x \cdot \Delta z_k)}{\Delta x \cdot \Delta y}$$

where R_{adv} represents the isotopic ratio of the incoming water vapor:

$$20 \quad R_{adv} = \frac{\sum_{k=1}^{k_{LCL}} \left(\frac{|u_k|}{\Delta x} \cdot q_{uk} \cdot R_{uk} + \frac{|v_k|}{\Delta y} \cdot q_{vk} \cdot R_{vk} \right) \cdot \frac{\Delta P_k}{g}}{\sum_{k=1}^{k_{LCL}} \left(\frac{|u_k|}{\Delta x} \cdot q_{uk} + \frac{|v_k|}{\Delta y} \cdot q_{vk} \right) \cdot \frac{\Delta P_k}{g}}$$

Note that the upstream advection scheme assumed here overestimates the effect of advection compared to the Van Leer (1977) advection scheme used in LMDZ. We thus estimate here an upper bound for the advection effect.

In practice, rather than calculating $\beta = R_{adv}/R_0$, we calculate $\beta = R_{adv}/R_{SCL}$ where R_{SCL} is the isotopic ratio in average through the SCL:

$$R_{F_{SCL}} = \frac{\alpha_{re} \cdot R_0 \sum_{k=1}^{k_{LCL}} q_k \cdot R_k \frac{\Delta P_k}{g}}{\sum_{k=1}^{k_{LCL}} q_k \frac{\Delta P_k}{g}}$$

where α_{re} is an effective fractionation coefficient. For example, if droplets are formed near the cloud base, some of them precipitate and evaporate totally in the SCL (e. g. in non-precipitating shallow cumulus clouds), then $\alpha_{re} = \alpha(T_{cloudbase})$. In contrast, if droplets are formed in deep convective updrafts after total condensation of the SCL vapor, and then a very small fraction of the rain is evaporated in a very dry SCL, then $\alpha_{re} = 1/\alpha(T_{SCL})/\alpha_K$ (Stewart, 1975). This prevents the advected water vapor to be systematically more depleted when the mixed-layer hypothesis is not exactly verified.

Combining all equations, in the case of a logarithmic δD profile, we get:-

C2 Results

$$R_0 = \frac{R_{oce}}{\alpha_{eq}} \cdot \frac{1}{h_0 + \alpha_K \cdot (1 - h_0) \cdot \frac{1 - r_{orig}^{\alpha_{eff}}}{1 - r_{orig}} + \eta \cdot \alpha_K \cdot (1 - h_0) \cdot (1 - \alpha_{re})}$$

Parameter ϕ is maximum where winds are maximum, such as near the extra-tropics or in the North Atlantic (Fig. C1a). Horizontal advection has an enriching effect in deep convective regions (probably because water vapor comes from nearby drier regions that have been less depleted by deep convection), and a depleting effect near the coasts (probably because of winds bringing vapor from the nearby land that is depleted by the continental effect) (Fig. C1b).

Rain evaporation can have a depleting or enriching effect depending on the sign of $1 - \alpha_{re}$ (Fig. Note that in this formulation, parameters ϕ and β are resolution-dependent. For example, in a finer resolution, ϕ would be larger and β would be closer to 1, but $F_{adv} \cdot q_{adv} \cdot R_{adv}$ and thus the contribution of horizontal advection in Eq. (8) would remain the same.

Appendix D: LMDZ free tropospheric profiles

The goal of this appendix is to document the spatio-temporal variability in the shape (section D1) and steepness (section D2) of simulated free tropospheric δD profiles. Note that a detailed interpretation of these profiles is beyond the scope of this paper. This paper aims at understanding δD_0 , which is the first step towards understanding full tropospheric profiles. In turn, understanding full tropospheric profiles in future studies will help refine our model for δD_0 . 3-pink, blue). In the paper, we thus well neglect rain evaporation effects, to avoid dealing with such an unknown parameter as α_{re} .

D1 Shape of tropospheric profiles

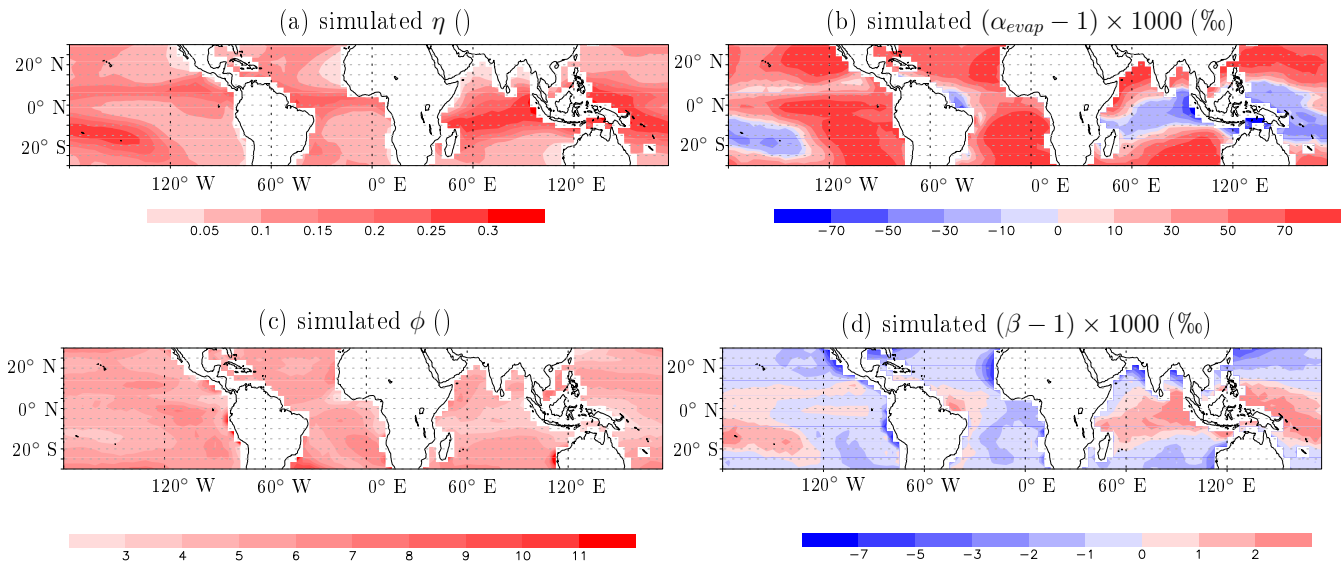


Figure C1. a) Ratio η of water in the SCL coming from rain evaporation to that coming from surface evaporation. b) Effective fractionation coefficient α_{evap} between the SCL water vapor and the rain evaporation. c) Ratio ϕ of water in the SCL coming from horizontal advection to that coming from surface evaporation. d) Effective fractionation coefficient β between the SCL water vapor and the water vapor coming from horizontal advection.

First, we test whether the δD vertical profiles simulated by LMDZ follow a Rayleigh or mixing line as a function of q . For the Rayleigh curve, α_{eff} is estimated as explained in section 3.3. For the mixing line (appendix A), the end member (q_f, R_f) is also taken at 500 hPa.

The tropical-mean vertical δD profiles simulated by LMDZ is bounded by Rayleigh and mixing lines (Fig. D1a). To better document the spatial variability in the shape of δD profiles, we plot parameter $f = \frac{\delta D_{LMDZ} - \delta D_{Rayleigh}}{\delta D_{mix} - \delta D_{Rayleigh}}$ describing how close is the simulated δD (δD_{LMDZ}) to the Rayleigh ($\delta D_{Rayleigh}$) and mixing (δD_{mix}) lines. We have $f = 0$ in case of a Rayleigh line, $f = 1$ in case of a mixing line, and $f > 1$ if δD is more enriched than a mixing line. In the lower-troposphere, δD_{LMDZ} is close to a mixing line (and sometimes even more enriched) in deep convective regions (Indian Ocean, South Pacific Convergence Zone, Atlantic ITCZ), probably because deep convection efficiently mixes the lower troposphere. Elsewhere, δD_{LMDZ} is intermediate between the two lines (Fig D1e). In the middle troposphere, δD_{LMDZ} is relatively closer to Rayleigh everywhere (Fig D1b).

The daily variability of f is large everywhere and at all levels (Fig D1c,e), with standard deviation of 0.23 and 0.44 on tropical average at 1000 m and 4000 m respectively. A large daily variability in the shape of profiles is also observed in nature (Sodemann et al., 2017).

15 D2 Steepness of tropospheric profiles

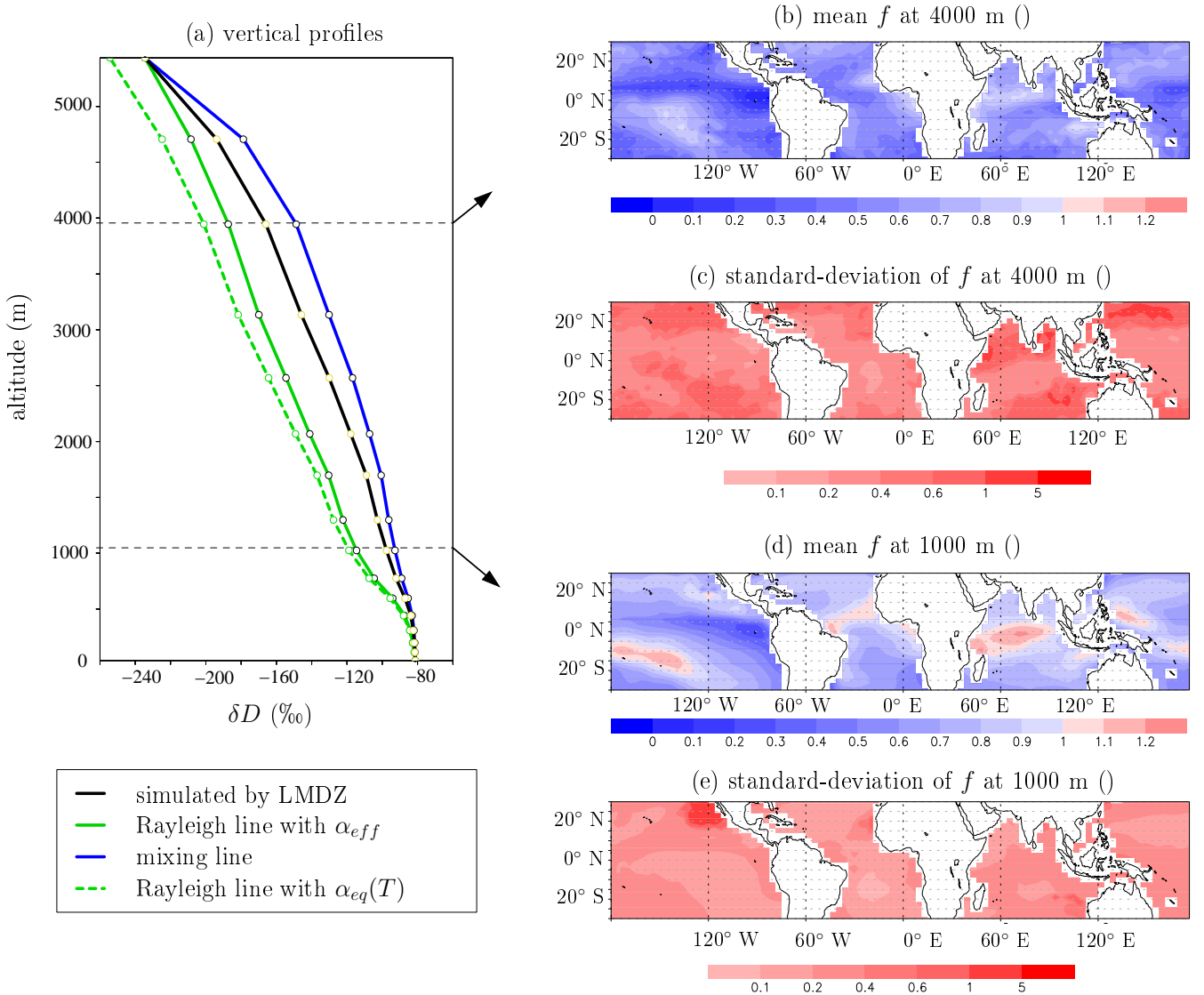


Figure D1. a) Vertical profiles of water vapor δD simulated by LMDZ (black), calculated if assuming a Rayleigh-type curve with α_{eff} estimated from $(q_f, \delta D_f)$ at 500 hPa (green), calculated if assuming a Rayleigh-type curve with $\alpha_{eq}(T)$ (dashed green) and calculated if assuming a mixing curve between the first layer and $(q_f, \delta D_f)$ at 500 hPa (blue), in average over all tropical oceanic locations and days. b) Winter-mean map of parameter $f = \frac{\delta D_{LMDZ} - \delta D_{Rayleigh}}{\delta D_{mix} - \delta D_{Rayleigh}}$ at 4000 m, i.e. slightly below 500 hPa where q_f and δD_f are taken. Parameter f describes how close is the simulated δD (δD_{LMDZ}) to the Rayleigh ($\delta D_{Rayleigh}$) and mixing lines (δD_{mix}): $f = 0$ in case of a Rayleigh line, $f = 1$ in case of a mixing line, and $f > 1$ if δD is more enriched than a mixing line. c) Standard deviation of parameter f among all days in winter of all years, at 4000 m. d) Same as b but at 1000 m, i.e. slightly above the LCL. e) Same as c but at 1000 m. To avoid numerical problems, only days and locations where $|\delta D_{mix} - \delta D_{Rayleigh}| > 5\%$ are used in the calculations.

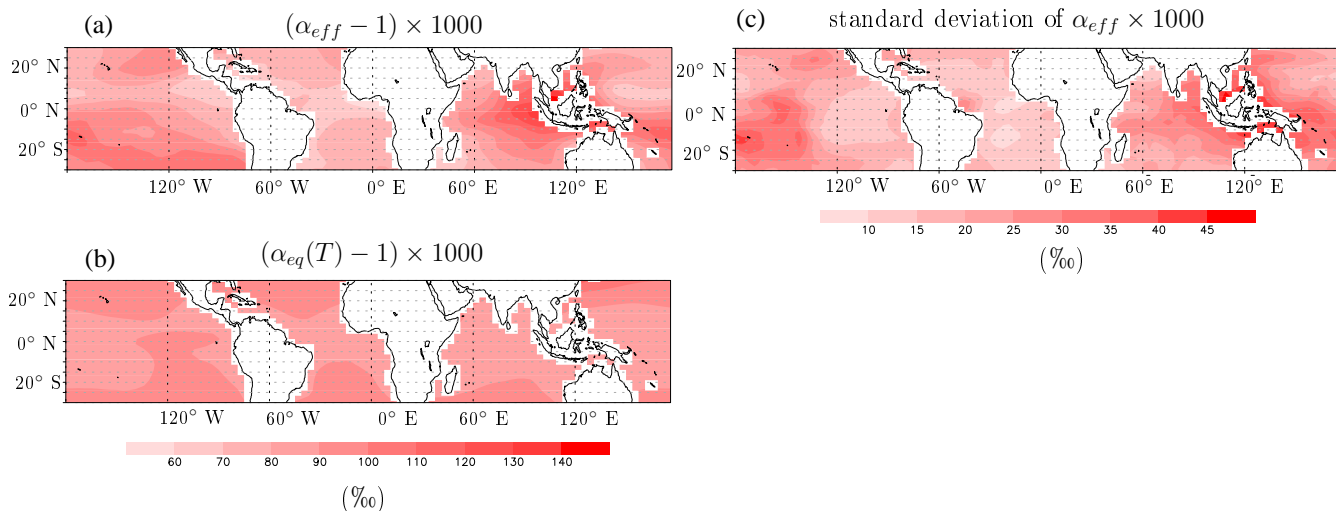


Figure D2. a) $\alpha_{eff} - 1$, where α_{eff} is the effective fractionation coefficient, expressed in ‰. b) $\alpha_{eq}(T) - 1$ expressed in ‰. All daily values are averaged over all days in winters of all years. c) Standard deviation of α_{eff} among all days in winter of all years, expressed in ‰.

The steepness of the δD gradient from the surface to the middle troposphere is described by the parameter α_{eff} . It is maximum in regions of deep convection, for example around the Maritime Continent (Fig. D2a). This is consistent with the maximum depletion simulated in deep convective regions in the mid-troposphere simulated by models (Bony et al., 2008), leading to steeper δD profiles. The pattern of α_{eff} may also reflect horizontal advection effects, where strong isotopic gradients align with winds (e.g. from the Eastern to the Western Pacific, Dee et al. (2018)).

Values of α_{eff} are of the same order of magnitude as real fractionation factors, but the spatial variations do not reflect those predicted if using a fractionation coefficient α_{eq} as a function of temperature T (Fig. D2b).

The daily standard deviation of α_{eff} ($\sigma_{\alpha_{eff}}$) for a given season ranges from 5‰ in the Central Atlantic to 40‰ near the Maritime Continent (Fig. D2c). On average over all seasons and locations, daily $\alpha_{eff} - 1$ at a given location varies within $\pm 25\%$ of its seasonal-mean mean value.

Author contributions. CR thought about the equations, ran the LMDZ simulations, made the analysis and wrote the manuscript. JG initiated the discussion on the subject and discussed regularly about the results. GR provided the STRASSE radiosoundings. FB provided insight and references about cloud processes. JG, GR and FB all gave comments on the manuscript.

Competing interests. The authors declare that they have no conflict of interest.

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