19<sup>th</sup> August 2019

Object – Answers to the Reviewers for the paper: "Influence of the dry aerosol particle size distribution and morphology on the cloud condensation nuclei activation. An experimental and theoretical investigation", Ref. ACP-2019-172.

Dear Editor, dear Reviewers,

We would like to thank the Editorial Board for considering our paper «*Influence of the dry aerosol particle size distribution and morphology on the cloud condensation nuclei activation. An experimental and theoretical investigation*» for publication in ACP. We would also like to thank the Reviewers for the extensive amount of work that they clearly dedicated to our paper, we greatly appreciated their constructive comments and suggestions. We have carefully studied the comments, and the original paper has been thoroughly revised accordingly. In particular, as suggested by the Reviewers, the paper goal has been re-framed to focus on the effect of the particle morphology on activation and on the different response to chemical aging of soot having different properties. The data treatment has been updated to account for the multiple charges effect, the DMA transfer function has been used, a probability distribution of the parameter kappa has been introduced and one of the test distributions obtained with ammonium sulfate has been replaced with original results obtained on soot at 70 mm HAB. A detailed point-by-point rebuttal and a marked-up version of the revised manuscript can be found at the end of this document (all modifications are highlighted in blue font color and references to the Reviewers' comments are given in Microsoft Word Revision Mode).

With our best regards,

Dr. Alessandro Faccinetto on behalf of all Authors.

## Answers to anonymous Referee #1.

## Overview.

Wu et al. present laboratory data and theoretical modeling to treat the influence of particle morphology on CCN activation spectra. Size distribution data and the k-Kohler parameterization are combined to predict the CCN number concentration as a function of supersaturation. Fractal dimension inferred from single particle transmission electron microscopy experiments is folded into the analysis. The method is tested using ammonium sulfate and soot particles from a miniCAST burner. K-values for soot as a function of ozone exposure are presented. This manuscript is not suitable for publication in ACP, according to the journal standard to publish studies "with general implications for atmospheric science". The paper does not reach clear new conclusions, mostly focuses on methodology and would be more suitable for AMT. More importantly, the manuscript lacks context of a large body of published literature, needs additional analysis folding in DMA transfer function models, and will require significant rewriting to become acceptable for publication.

## Major comments.

(1) Eqs. (11) and (12), "the master equations" of the work are simply a cumulative size or supersaturation distributions that have been used in similar for decades in droplet activation schemes or closure studies (e.g. Abdul-Razzak and Gahn, 2000, Snider et al., 2003 and references therein).

Answer. We did our best to cover the most significant works in the field, and we thank the Reviewer for providing some examples of literature that we did not cited or that we missed. It is indeed true that the droplet activation of aerosol particles has been parameterized in the past by using a cumulative function of the lognormal distribution (Abdul-Razzak et al. 1998). The cumulative function has been used as well for predicting the type of the aerosol measured in the outdoor measurements (Snider et al. 2003). However, we would like to notice that especially in recent literature or in works more strictly related to combustion (our field) that investigate the activation of soot particles (Sullivan et al. 2009, Lambe et al. 2015; Tang et al. 2015), sigmoid function are still used for the determination of the critical supersaturation. Therefore, we believed this topic worthy to be discussed. Please notice that in response to this and to comments (2), (3), (4) and (6) the *Introduction, Theory* and *Results and Discussion* sections have been heavily updated or entirely rewritten: the more "tutorial-like" parts are reduced to the minimum required for presenting the research context (Eq. 2 in the *Introduction* and section 2.1), all the missing references are added and the paper is re-framed to focus on the effect of the morphology on soot activation.

(2) In general, the work herein can be interpreted either as a laboratory CCN closure experiment or an improvement to constrain laboratory inferred k-values from data. No studies in that context are cited. For example, it has long been recognized that k-values derived from CCN data are "effective" or "apparent" k-values that have folded in effects of surface tension, solubility, and particle morphology (e.g. Poschl et al., 2009, Sullivan et al., 2010). CCN closure experiments that take size distribution

data, composition and shape have been performed extensively on ambient aerosol. Studies that account for particle shape in the calibration of CCN instruments using DMAs and non-spherical particles are routine (e.g. Snider et al., 2006, Rose et al., 2008, Kuwata and Kondo, 2009). Using TEM to obtain particle shape may be novel here (this referee is not 100% sure), but the concepts described in Section 2 are well established.

Answer. In the original formulation of kappa-Köhler theory (Petters and Kreidenweis 2007), kappa is used to estimate the chemical activity of water in a multicomponent system. Indeed, an effective/apparent kappa has been defined and often used to account for surface tension, solubility and particle morphology effects as mentioned by the Reviewer. Furthermore, a shape factor has been considered to correct the difference between the experimental activation and simulated activation of irregular inorganic aerosol particles (Rose et al. 2008, Snider et al. 2006, Biskos et al. 2006). A similar approach has been used as well on the activation study of soot particles (Lambe et al. 2015), and in particular a volume equivalent diameter has been introduced to avoid the crossing of the Kelvin limit (Tritscher et al. 2011, Lambe et al. 2015). Please also see comment (16) for more details. Following this last approach, in our work we aim to provide a method for the estimation of the volume equivalent diameter  $d_{ve}$  of soot particles that accounts for the aggregate size and morphology rather than relegating all the deviations from the expected activation curves to the effective/apparent kappa. In our opinion, "de-coupling" the effective/apparent kappa and integrating size and morphology effects in  $d_{ve}$  has the potential advantage of preserving kappa as an indicator of the chemistry at the particle surface for instance. Please notice that in response to this comment, the old section 2 has been completely replaced with the derivation of the morphology-corrected  $d_{\rm ve}$ .

(3) The "master equation" (Eq. 11) cannot be applied to DMA distributions. The role of the DMA transfer function and of multiply charged particles needs to be taken into account (e.g. Petters, 2018). It is clear that the effect of multiply charge particles is not large as shown by the shoulder in Figure 6. However, the paper makes claims about kappa being a "Dirac delta distribution", i.e. a single value applied to a distribution. The question is whether the observed activation behavior is due to size distribution alone, or whether shape and composition heterogeneity increases the broadness. Therefore, Eq. (11) should be replaced with the DMA transfer function, including multiply charged particles, and the use unexplained discrepancies to identify the effect of shape and/or heterogeneity.

(4) The influences of size distribution heterogeneity and particle shape on the cumulative CCN spectrum have been discussed in the literature (e.g. Petters et al., 2009, Kuwata and Kondo, 2009, Su et al., 2010, Cerully et al., 2011). The work of Su et al. is particularly pertinent to this paper.

Answer. Being comments (3) and (4) strictly related, one comprehensive answer is provided. We acknowledge that this could have been better explained in our original manuscript, and we thank the Reviewer for providing the pertinent literature references. Indeed, in our original work we used a single value instead of a distribution to describe kappa, and we observed that the geometrical standard deviation ( $\sigma_g = 1.08$ ) of soot distribution recorded by SMPS is smaller than the value ( $\sigma_g = 1.16$ ) in Eq. (22) obtained by fitting experimental activation curves. This discrepancy was acknowledged but not explained. In response to these comments, in the revised version of the paper all calculations have been updated to take into account the DMA transfer function and the effect of multiply charged particles (the effect on the ammonium sulfate is important and cannot be

neglected, however the effect on soot is comparatively small). Furthermore, a distribution rather than a single kappa value was tested. As the Reviewer suggested, the updated  $\sigma_g$  values are now consistent, and therefore the kappa distribution (Su et al. 2010, Cerully et al. 2011) has been applied to all calculation and discussed in the revised version of the paper in the updated *Theory* and *Results and Discussion* sections.

(5) The aging studies of miniCAST soot are interesting. However, it is important to place these results in the context of several similar studies that have investigated the CCN activity of (chemically aged) soot.

Answer. We would like to emphasize that this work is not about miniCAST soot, but about the chemical aging of young and mature soot sampled from a laboratory turbulent jet flame supplied with liquid kerosene. Unlike miniCAST that provides only the soot that can be recovered in the exhausts, laboratory flames allow the generation of soot having controlled properties in terms of aggregate size distribution, morphology and surface chemical composition that are accessed by sampling the flame in the axis at different reaction time (or equivalently height above the burner, HAB). In a miniCAST burner there is no direct access to the flame, and therefore only the exhausts are routinely sampled that leads to several important limitations (contamination of the sampled soot with the exhaust gas phase, sampling of particles formed in very different conditions and mixed only at the end of the combustion process to name a few). Clarifications have been added to the Introduction, and the Results and Discussion section has been re-framed to focus on this aspect. To the best of our knowledge, the closest studies to our work are (Tritscher et al. 2011) and (Lambe et al. 2015), both referenced in the original paper, in which the approximated equation for kappa > 0.2is used. The implications on the use of such approximation for the interpretation of the activation curves were discussed in the original paper (old Figure 9), but rendered obsolete after revision. The Results and Discussion section has been updated to match.

(6) The framing around improving k-Kohler or Kohler theory in general is not justified. Kohler theory predicts the activation behavior of a single particle. If one applies that theory recursively to a size distribution with non-uniform composition, or a shaped particle, then those assumption need to be questioned, as it has been in previous studies. Statements that "[f]or all practical purposes, both theories operate under the hypothesis of Dirac delta distributions" don't really make sense in that context.

Answer. The particle size distribution (Snider et al. 2003) and the heterogeneity of kappa (Su et al. 2010) both influence the activation behavior and have been taken into account in the improved data treatment after revision. The hypothesis of Dirac delta distribution was initially proposed for a group of uniform size particles with constant morphology and chemical composition (for example ammonium sulfate). In our work, the comparison of  $\sigma_g$  obtained from experimental SMPS size distribution and from fitted activation spectra demonstrated that the modifications of the heterogeneity of aged soot particles is indeed a concern during the aging process. However, in the revised version of the paper, the main goals have been re-defined to focus on the role of the particle morphology on activation and on the difference in the behavior of young and mature soot. More

emphasis is given to original results rather than well established knowledge. For instance, one distribution on test ammonium sulfate has been replaced with a complete description of the results on soot at 70 mm HAB, and a more detailed discussion has been developed. The *Introduction, Theory* and *Results and Discussion* sections have been heavily updated or entirely rewritten. Overall, the paper has been made less pedagogic (removal of the "tutorial" section, focus from the very beginning on the morphology, removed some redundant text).

(7) It is not clear what the main finding of the work is. Equations are presented and somewhat successfully tested against experimental data, but that type of exercise has been presented before. The novelty of the work and the scientific findings contributed need to be better articulated.

Answer. All requested modifications are included in the revised version of the paper, please see answers to point (2), (5) and (6) for more details. Briefly, the main results include: "de-coupling" the particle morphology from the effective/apparent kappa and integrating size and morphology effects in  $d_{ve}$  to preserving kappa as an "all-chemistry" indicator; providing evidence that chemically aged young and mature soot behave very differently during activation experiments, and thus showing that the soot generation process is critically important for this kind of experiments; providing a lower limit for the validity of the model (kappa~5×10<sup>-6</sup>) by using chemically aged soot particles characterized by kappa values typically 2-3 orders of magnitude lower than typical inorganic aerosols used in activation experiments. The *Results and Discussion* sections have been heavily updated to focus on the main results.

(8) The writing of the manuscript needs to be improved significantly. Words are frequently used incorrectly. The writing lacks context of important prior literature. The framing of the work needs to be revised. Section 2 reads more like a tutorial than a scientific paper.

Answer. The manuscript has been thoroughly revised, and all the corrections suggested by the Reviewers implemented and/or discussed in detail. In particular, the *Introduction* and *Theory* sections have been entirely reworked to remove the feeling of "reading a tutorial" and to include and discuss the missing suggested literature. The *Discussion* section has been modified as well to account for the improved data treatment as suggested. Unfortunately, none of the Authors is a native English speaker. We did our best to keep up with the quality standards of ACP, and kindly thank the Reviewers for all the given suggestions aiming to improve the English level.

(9) The data availability is inconsistent with the journal policy. The data should be deposited in a publicly available repository.

Response: All corresponding data will be uploaded in a publicly available repository.

## Other comments.

(10) To my understanding Köhler theory isn't equivalent to "classical nucleation theory", which usually refers to homogeneous nucleation.

Answer. Corrected (this sentence has been removed in the re-framing process).

(11) The second part of the sentence isn't quite parsable. Is this talking about density profiles within a particle? Or differences in density and composition within a distribution. Given the context of the paper, it seems to be the latter. k-Köhler treats the activation of a single particle. It therefore does not make any assumptions about the heterogeneity of the size distribution."

Answer. Corrected (this sentence has been removed in the re-framing process).

(12) To the present day--please rephrase

Answer. Corrected.

(13) "internally mixed nature---internally mixed refers to a distribution property (i.e. two substances may be internally mixed or externally mixed across a distribution). A single particle is either pure or mixed. k-Köhler theory is one means to treat the activation of mixed particles."

Answer. Corrected (this sentence aimed to highlight the mixed nature of the single particle, and it been removed in the re-framing process).

(14) partially soluble---please change to sparingly soluble. The state of dissolution is determined by the water content. A substance may be "partially dissolved" but it has a strictly defined solubility value.

Answer. "Partially soluble" is a non-quantitative, descriptive locution commonly used in chemistry to indicate small but unknown solubility product constants  $K_{ps}$ .

(15) Response to comment: "neither the classical nor the k-Köhler theory account for the dry aerosol particle size distribution and morphology---this is not the objective of those theories. This is a problem on how it is applied in practice."

Answer. Corrected (this sentence has been removed in the re-framing process).

(16) more specifically, the crossing of the Kelvin limit has been reported in several instances---Please explain what is meant by that.

Answer. According to the kappa-Köhler theory, a non-soluble particle (kappa = 0) could be activated to form a water droplet by increasing the supersaturation up to the so-called Kelvin limit. However, soot particles are sometimes found beyond this limit if the mobility size or the volume equivalent size are used (Tritscher et al. 2011, Lambe et al. 2015). In the frame of kappa-Köhler theory, this leads to k < 0 that has no physical meaning. This point is now clarified in the *Introduction* and *Results and Discussion* sections of the revised paper in the context of the improved data treatment and interpretation suggested by the Reviewer in points (2), (3), (4) and (6).

(17) is the master equation of this work---this is an odd formulation

Answer. Corrected (this sentence has been removed in the re-framing process).

(18) geometric deviation---geometric standard deviation

Answer. Corrected.

(19) and the fitting is implicitly assumed not to carry any physically meaningful parameter. --- not true. See Cerrully et al. 2011, Figure 3.

Answer. A sigmoid curve is used in (Cerully et al. 2011). The slope of the sigmoid curve is explained by the degree of heterogeneity of activated particles. However, if the lognormal distribution of aerosol particles is used, figure 4d in the original paper clearly indicates that the activation curve is far from the sigmoid curve when  $\sigma_g$  increases. This point is now clarified in the *Introduction* in the context of the improved data treatment and interpretation suggested by the Reviewer in points (2), (3), (4) and (6).

(20) within 20% incertitude---within 20% uncertainty

Answer. Corrected.

(21) soot emissions are emblematic of human activities---please reword

Answer. Corrected.

(22) understanding the anthropogenic impact on the atmosphere---please reword

Answer. Corrected (this sentence has been removed in the re-framing process).

## (23) please specify what "very representative" means. Is there a metric for this?

Answer. The fractal dimension obtained for soot particles from 2D TEM analysis in this work spans the range 1.65-1.67 that is quite consistent with values in the range 1.61-1.82 typically found in the literature. Corrected.

## (24) univocally defined---is defined

Answer. Corrected.

# (25) Response to comment: "Young soot; mature soot---Soot aren't biological entities. Fresh soot and chemically aged soot would appear to be better terms."

Answer. "Young soot" and "mature soot" are well established descriptive terms used in the combustion community and related to the permanence time of soot inside the flame (or equivalently to the height above the burner, HAB). See for instance (Mitra et al. Combust. Flame 2019, Cain et al. PCCP 2014, Alfé et al. Proc. Combust. Inst. 2009). In a turbulent diffusion flame like the one investigated in this work, "young soot" refers to the condensed phase matter sampled at short reaction time (or low HAB) and characterized by high H/C ratio (typically H/C > 0.7) and small aggregates of 14-15 nm primary particles. On the other hand, "mature soot" refers to the matter sampled at long reaction time (or high HAB), characterized by low H/C ratio (typically < 0.4) that results in a much slower reactivity during the aging process. Furthermore, with respect to young soot, the aggregates are larger both in their number of primary particles per aggregate and in the size of the primary particles (16-17 nm). In other words, it is very well possible to have young fresh soot or young chemically aged soot, opposed to mature fresh soot or mature chemically aged soot. The different behavior of young and mature soot to chemical aging is actually one of the main points of our paper, and such investigation is mainly possible because of the precise control over the flame conditions allowed by the use of a laboratory flame rather than a commercial burner. A more accurate and detailed discussion has been added to the *Introduction*.

(26) k-Köhler theory is built around the idea that the soluble fraction only affects the heterogeneous nucleation---this is not strictly true. k-Köhler can be used to parameterize CCN activity descriptively, even if the underlying mechanism is incorrect. Such parameterizations have been termed "apparent k" or "effective k" in the literature.

Response: Corrected (a specific sentence has been added to the Introduction).

(27) k parameterizes all the information on the composition of the droplet approximated as an ideal water solution---this is incorrect. K is a one parameter activity coefficient model that explicitly models the non-ideality at the point of activation.

Response: Corrected. Please also see answers to point (2).

(28) Incidentally, the effect of the dry particle electrical charge on the activation is not considered in this work.---This is unclear what this means. As written, it suggests that particle charge itself affects activation. To my knowledge there is no evidence for such a claim. If it is meant that the effect of particle charge on selected size is not considered, this is correct and needs to be addressed (see major comment)."

Answer. Corrected (the effect of multiply charged particles is now taken into account in the data treatment, and a specific sentence has been added to the *Introduction*).

### Answers to anonymous Referee #2.

## Overview.

Wu et al. focus on the CCN activity of particles with irregular shape through a combination of theory and experimental data. Although the study contains interesting material, I feel it cannot be published in its current form and unfortunately must recommend rejection to provide the authors enough time to prepare a modified manuscript.

Overall this study contains a very large amount of material that is not wrong, but is "textbook", often without reference to any of the large body of published literature on the subject. I strongly recommend that the authors give appropriate credit to the published work, but also keep only what is absolutely necessary. Reviewer #1 presents a few references, I can add also the textbooks of Seinfeld & Pandis, Pruppacher and Klett, as well as review of state-of-the art mechanistic parameterizations (e.g., from the groups of Ghan or Nenes) – which normally adopt formulations that use lognormals (e.g., Fountoukis and Nenes, 2005). There is now a rich literature based upon CCN spectral analysis to constrain hygroscopicity – considering shape factors, multiple charging and DMA transfer function effects (e.g., Cerully et al., 2011 and references therein) – even for well established calibration aerosol like sodium chloride and ammonium sulfate.

#### Major comments.

(1) What I suggest is that the authors consider a resubmission, focusing on the results of the soot activation experiments, and also comparing them to existing literature. In their analysis it is nice that shape effects are considered, and even nicer that the fractal dimension is explicitly determined, because it allows then to explore other theories of activation such as adsorption-activation theory (e.g., Kumar et al., 2009; Laaksonen et al., 2016 and references therein) – alone or in combination with Kohler theory. It would be interesting to see how this other framework performs and if it can provide insight on the drivers of CCN activity for the particles studied.

Being comments (1) and (6) strictly related, one comprehensive answer is provided. We would like to thank the Reviewer for the kind and constructive suggestions. A revised version of the paper has been prepared that includes all requested modifications, and indeed focuses on the results of the effect of the morphology on soot particles activation experiments. For a detailed explanation, please see the answers to points (5), (6) and (25) of Reviewer#1. The *Introduction* and *Results and Discussion* sections are particularly affected by the re-framing of the paper. Exploring other theories of activation, unfortunately, is beyond the scope of the present work that instead aims to further develop kappa-köhler theory to account for effects (morphology, and chemistry of soot) not yet fully understood. Nevertheless, we acknowledge this suggestion as an interesting research direction for future developments that we will certainly keep as a perspective for future work.

(2) The study also suffers from limitations that include the important DMA transfer function effects and multiple charging (although noted on Page 17 by the authors, they do not go through more indepth analysis), which is considered routine in established groups.

Answer. We would like to thank the Reviewer for the constructive suggestions and references. Indeed, including  $d_{ve}$ , multiple charges effects, DMA transfer function and kappa distribution is the proper way to treat the CCN activation data. In the revised version of the paper, the experimental data have been re-treated to account for the above mentioned effects, and a morphology-corrected  $d_{ve}$  is then calculated, using the data from TEM measurements. Furthermore, in the revised manuscript we updated the theory, the context of the presentation and all the figures. For more details on specific points, please see the answers to points (1), (2), (3), (4) and (6) of Reviewer#1.

#### Specific comments.

(3) Page 2, Line 6: k-Köhler is not just for partially soluble particles, it's to address chemical complexity (mixtures of solutes of a wide range of molar masses) – and can account for partial solubility as well.

Answer. Corrected.

(4) Page 2, Line 9: Kohler theory is formulate for a particle. It can (and is) extended to a size distribution easily, as mentioned in the above texts. I don't understand why the authors present this as an issue.

Answer: We acknowledge that this could have been explained in a different and more appropriate way, and we thank the Reviewer for providing the pertinent literature references. Please notice that in response to this comment and to comments (1), (2), (3) and (4) of Referee #1, the *Introduction* and *Theory* sections have been entirely rewritten.

(5) Page 2, Line 10: Sure, you can use - and is even elegant - to use Dirac functions to represent many particles of a given size as a size distribution. I understand where the authors come from when they

say that Kohler theory cannot be applied to a broad size distribution - but I also find it quite narrow because it is equivalent to saying that a size distribution with a finite particle width cannot be described with a monodisperse particle distribution (which is sort of an obvious statement)! On the other hand, Kohler theory can be applied to size distributions, even in the narrowest sense considered by the authors, because it defines the "size" above which all becomes droplets (this of course, assuming the soluble fraction is sufficient, with all that this implies). In this sense, a characteristic size is linked to a characteristic saturation - which is the basis of Kohler theory and the concept of a critical point that comes out of it.

Answer. We thank the Reviewer for this correction, in the revised version of the paper we updated the *Introduction* and *Theory* sections accordingly. Please also see answers to comments (3) and (4) of Reviewer#1.

(6) Page 2, Line 10: True, but then you need to use a theory that does not assume at least perfectly wettable particles. The work of Gorbunov, or adsorption activation theory can easily treat such situations – and is physically based. It would be nice if the authors actually refer to that work and consider it in their analysis.

Answer. Please see answer to comment (1).

(7) Figures: uncertainties are sometimes included in the activation plots, but they are not propagated later on in any of the analysis. This would be nice to see – and also include uncertainty from the DMA transfer function, shape factor, multiple charges, etc.

Answer. All missing uncertainties have been added to plots and tables.

(8) Page 19, line 30: I don't understand why nanoparticles will not be in equilibrium. The relevant timescale is extremely small – unless if I misunderstood the point raised by the authors.

Answer. Corrected. This sentence was not clear, and it has been removed.

## Influence of the dry aerosol particle size distribution and morphology on the cloud condensation nuclei activation. An experimental and theoretical investigation

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**Abstract.** Combustion and other high temperature processes frequently result in the emission of aerosols in the 10 form of polydisperse fractal-like aggregates made of condensed phase nanoparticles (soot for instance). If certain conditions are met, the emitted aerosol particles are known to evolve into important cloud condensation nuclei (CCN) in the atmosphere. In this work, the hygroscopic parameter  $\kappa$  of complex morphology aggregates is calculated from the supersaturation dependent activated fraction  $F_a = F_a(SS)$  in the frame of  $\kappa$ -Köhler theory. The particle size distribution is approximated with the morphology-corrected volume

- 15 equivalent diameter calculated from the electrical mobility diameter by taking into account the diameter of the primary particle and the fractal dimension of the aggregate experimentally obtained from transmission electron microscopy measurements. Activation experiments are performed in water supersaturation conditions using a commercial CCN-100 condensation nuclei counter. The model is tested in close-to-ideal conditions of size selected, isolated spherical particles (ammonium sulfate nanoparticles dispersed in nitrogen), then with
- 20 complex polydisperse fractal-like aggregates (soot particles activated by exposure to ozone with  $\kappa$  as low as  $5 \times 10^{-5}$ ) that represent realistic anthropogenic emissions in the atmosphere.

**Keywords**. *κ*-Köhler theory, cloud condensation nuclei (CCN), size distribution, morphology, hygroscopic parameter, soot.

**Comment [S1]:** Please notice that the *Abstract* has been updated to match the modifications required by the Reviewers.

#### 1. Introduction

Soot particles formed during the incomplete combustion of hydrocarbons and emitted in the exhausts are potentially important contributors to the radiative forcing of the atmosphere as they adsorb and scatter the solar radiation (direct effect), but can also act as cloud condensation nuclei (CCN) or ice nuclei (IN) and trigger

- 5 the formation of persistent clouds (indirect effect) (Bond et al., 2013). To date, estimations over the magnitude of the direct and indirect effects are subject to large uncertainty, and commonly accepted values span the range [+0.25, +1.09] W m<sup>-2</sup> for the direct effect and [-1.20, 0.00] W m<sup>-2</sup> for the indirect effect comprehensive of all aerosol-cloud interactions (Stocker et al., 2014). Such large uncertainties result from the combination of several difficult-to-predict behaviors of the soot particles in the atmosphere when compared to mineral and biogenic
- 10 aerosols. For instance, their small size and low density enable for a long lifetime in the atmosphere that can reach several weeks (Govardhan et al., 2017). Their complex morphology and large specific surface allow many possible surface interactions that can deeply affect their reactivity (Browne et al., 2015; Monge et al., 2010). Furthermore, their number concentration is subject to high geographic variability, and especially in polluted regions can be comparable to the typical number concentration of marine aerosols that provide the largest
- 15 contribution to the total mass of aerosols emissions (Rose et al., 2006; Sayer et al., 2012). To better understand the effect of soot particle on the radiative balance of the atmosphere, it is therefore important to understand how their size distribution, morphology, and surface composition impact their activity as CCN.

Soot formation in flame combustion is a complex process strongly affected, among other factors, by the fuel nature, the local fuel-air equivalence ratio and the flame temperature (D'Anna, 2009; Karatas and Gülder, 2012;

- 20 Wang, 2011). At short reaction time, or equivalently at low height above the burner (HAB), the oxidation of the fuel generates small radicals that quickly recombine to form larger and larger hydrocarbons, ions and radicals. Small polycyclic aromatic hydrocarbons (PAHs) and their derivatives are since long regarded as the most important soot molecular precursors (Richter and Howard, 2000). At longer reaction time, or equivalently at higher HAB, the soot molecular precursors react to form condensed phase nascent soot particles. In controlled,
- low sooting laboratory flames, nascent soot particles as small as 2 nm can be detected (Betrancourt et al., 25 2017). The dynamic equilibrium between the heterogeneous reactions at the particle surface (surface growth and oxidation) in parallel to coalescence and coagulation phenomena determine whether the newly formed particles increase their size or are re-oxidized into gas phase products. In sooting flames, nascent soot particles quickly evolve into primary soot particles having typical diameter in the range 5-30 nm (Apicella et al., 2015). If
- 30 their number concentration is sufficiently large, condensed phase particles at any reaction time can coalesce and coagulate into complex morphology aggregates that persist up to the flame exhausts (Kholghy et al., 2013).

A substantial body of literature exists on the characterization of the morphology of soot particles by electron microscopy. Young primary soot particles sampled at low HAB are well known to be characterized by an amorphous core surrounded by a highly structured series of concentric shells, often referred to as onion-like

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35 structure (Kholghy et al., 2016). On the other hand, mature soot particles sampled at high HAB tend to be extremely complex aggregates of hundreds to tens of thousands of primary particles (Kelesidis et al., 2017; Santamaría et al., 2007). The morphology of these aggregates is scale invariant over a relatively small range ("fractal-like" aggregates), so some concepts borrowed from fractal geometry can be applied to characterize them. In particular, the fractal dimension  $D_{\rm f}$  is considered to be an important descriptor of the soot particles 40 morphology that links the number of primary particles of an aggregate  $N_{\rm pp}$  to the diameter of the primary

particle  $d_{\rm pp}$  through the following power law (Eggersdorfer and Pratsinis, 2014; Sorensen, 2011):

$$N_{\rm pp} = k_{\rm f} \left(\frac{d_{\rm p}}{d_{\rm pp}}\right)^{D_{\rm f}}$$

Comment [S2]: Reviewer#1 (6) and (8). Reviewer#2 (1), (4) and (5).

This Introduction has been re-written as part of the re-framing of the paper

Comment [S3]: Reviewer#1 (5) and (25)

Eq. (1)

where  $k_{\rm f}$  is the exponential pre-factor and  $d_{\rm p}$  the equivalent particle diameter. Over the years, different approaches have been proposed to estimate  $d_{\rm p}$  with quantities easily accessible from experiments that include the diameter of gyration from angular light scattering measurements (Köylü et al., 1995; Sorensen et al., 1992) or the size of the aggregate projection from scanning electron microscopy (Colbeck et al., 1997) and transmission electron microscopy (Cai et al., 1995; Hu et al., 2003).

From the chemical point of view, the gas-condensed phase conversion remains to date a poorly understood process (Wang, 2011). The molecular precursors participating to soot formation and found adsorbed on the surface of soot particles can be as small as PAHs containing 3-7 aromatic cycles, or as large as tens of aromatic cycles depending on the combustion conditions (Irimiea et al., 2019). The availability of surface hydrogen atoms

is considered to be a driving force of the surface growth process and is often described by the hydrogen abstraction/acetylene addition mechanism (Frenklach, 2002; Frenklach and Wang, 1990). At the particle surface, reactive young soot is generally rich of small PAHs characterized by high H/C ratio (> 0.7), in contrast to more inert mature soot that is characterized by low H/C ratio (< 0.4). Being PAHs thermodynamically stable compounds, they are often found adsorbed on the surface of the soot particles in the exhausts and give a significant contribution to the soot particles reactivity.</li>

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Such a large variability of size distribution, morphology and chemical composition strongly impacts the reactivity of soot particles in the atmosphere and their propensity to evolve into CCN. Several studies exist that characterize the CCN activity of soot particles generated in the exhausts of laboratory flames (Lambe et al., 2015) and commercial burners like the miniCAST (Friebel et al., 2019; Henning et al., 2012). Soot particle aging

- 20 experiments are often performed in laboratory conditions that simulate the atmosphere and make use of flow reactors (Kotzick et al., 1997; Lambe et al., 2015; Zuberi et al., 2005) or atmospheric simulation chambers (Grimonprez et al., 2018; Tritscher et al., 2011; Wittbom et al., 2014). The hygroscopic properties of soot are generally determined at supersaturation conditions provided by instruments such as variable supersaturation condensation nuclei counters (VSCNC) or cloud condensation nuclei counters (CCNc). Overall, freshly emitted
- 25 soot particles are generally considered as poor CCN. However, several studies demonstrate that photochemical aging (Tritscher et al., 2011) or chemical aging that includes exposition to OH radicals (Lambe et al., 2015; Zuberi et al., 2005), to O<sub>3</sub> (Grimonprez et al., 2018; Kotzick et al., 1997; Wittbom et al., 2014) or to NO<sub>3</sub> radicals (Zuberi et al., 2005) under atmospheric relevant conditions can efficiently turn soot particles into CCN.

Köhler theory is widely used to describe the formation process of liquid cloud droplets at supersaturation
 conditions. Köhler theory is entirely founded on equilibrium thermodynamics, and describes the change of the saturation vapor pressure of water induced by the curved surface of the nascent droplet and by the presence of solutes in the liquid phase. The internally mixed nature of many atmospheric aerosols is accounted for in a more modern approach, the so-called κ-Köhler theory (Petters and Kreidenweis, 2007), that combines the original theory and a single parameter (κ) representation of the CCN activity that takes into account the reduction of

35 the water activity due to the presence of partially soluble components. At thermodynamic equilibrium, the supersaturation over an aqueous solution droplet  $SS = SS(D, d_p, \kappa)$  as a function of the droplet diameter D, of the size of the seeding particle  $d_p$  and of the hygroscopic parameter  $\kappa$  is given by:

$$SS(D, d_{\rm p}, \kappa) = \frac{D^3 - d_{\rm p}^3}{D^3 - d_{\rm p}^3(1 - \kappa)} \exp\left(\frac{A}{D}\right) - 1, \qquad A = \frac{4M_{\rm w}\sigma_{\rm s/a}}{R T \rho_{\rm w}}$$
Eq. (2)

where  $M_w$  and  $\rho_w$  are the molar mass and density of water, respectively,  $\sigma_{s/a}$  is the surface tension at the solution/air interface, R is the ideal gas constant and T is the temperature.  $\sigma_{s/a}$  = 0.072 J m<sup>-2</sup> and T = 298 K are commonly used for calculations that lead to  $A \simeq 2.09 \times 10^{-9}$  m.

**Comment [S4]:** Reviewer#1 (5) and (25).

Comment [S5]: Reviewer#1 (1).

Explanation of the  $\kappa$ -Köhler theory is kept to a minimum.

 $\kappa$ -Köhler theory has been widely used to characterize the activity in supersaturation conditions of isolated non-spherical aerosol particles as a function of  $\kappa$  (Cerully et al., 2011; Su et al., 2010),  $d_p$  (Kuwata and Kondo, 2008), or *SS* (Sullivan et al., 2009; Tang et al., 2015). The particle size distribution has been proven to affect the CCN activation curves (Abdul-Razzak and Ghan, 2000). However, the (geometric) standard deviation of the particle size distribution alone is not sufficient to completely explain the slope of the CCN activation curves

5 particle size distribution alone is not sufficient to completely explain the slope of the CCN activation curves (Snider et al., 2006), and therefore a distribution of values of the parameter  $\kappa$  has been proposed to add the missing degree of freedom (Cerully et al., 2011; Su et al., 2010).

Only a few studies exist on the CCN activity of soot particles compared to non-aggregated aerosol particles (Grimonprez et al., 2018; Lambe et al., 2015; Tritscher et al., 2011; Wittbom et al., 2014). In these studies, a

- 10 corrected volume equivalent diameter based on the estimated mass density of the soot particles is used to parameterize the particle size. However, particles characterized by very low activity like fresh soot particles have been reported to have  $\kappa < 0$  ("apparent crossing of the Kelvin limit") in some instances (Grimonprez et al., 2018; Lambe et al., 2015; Tritscher et al., 2011). To avoid this problem,  $\kappa$  has been obtained from the fitting of the activation curve with generic sigmoid functions that do not take into account the particle size distribution or
- a distribution of values of  $\kappa$ . More specifically,  $\kappa$  has been calculated from the critical supersaturation (SS at  $F_a = 0.5$ ) by using an analytical approximation of Eq. (2) only valid for  $\kappa > 0.2$ , which is not always the case for soot particles.

In the above mentioned studies, both for non-aggregated and aggregated aerosol particles, the electrical mobility diameter, experimentally accessed by scanning mobility particle sizing (SMPS), has often been used to

20 measure the particle size distribution. In this case, the role of multiply charged particles needs to be taken into account (Petters, 2018).

The first main goal of this work is the quantification of the role of the particle morphology on the cloud condensation activity of soot particles in conditions that simulate atmospheric chemical aging. In practice, a morphology-corrected volume equivalent diameter  $d_{\rm ve}$  is calculated from the electrical mobility diameter  $d_{\rm m}$ 

- 25 by including the diameter of the primary particle  $d_{pp}$  and the fractal dimension  $D_f$  obtained from transmission electron microscopy (TEM).  $\kappa$  is calculated from the best fit of the experimental activation data  $F_a = F_a(SS)$ obtained in water supersaturation conditions using a commercial CCN-100 condensation nuclei counter. After including the contribution of the morphology in  $d_{ve}$ ,  $\kappa$  is considered to be only representative of the particle chemistry such as the modification of the surface composition or the formation of soluble compounds due to
- **30** the chemical aging. To account for the heterogeneity of the particle chemistry and to correct for the differences between experimental and calculated  $F_a = F_a(SS)$ ,  $\kappa$  is treated as a probability distribution rather than a single value. The second main goal of this work is to provide quantitative information on the evolution of  $\kappa$  during the chemical aging of soot particles characterized by different maturity, i.e. sampled at different HAB in a laboratory jet diffusion flame supplied with kerosene. The model is first tested in close-to-ideal conditions of size selected,
- 35 isolated spherical particles (ammonium sulfate nanoparticles dispersed in nitrogen), then in the complex case of polydisperse fractal-like aggregates (soot particles activated by exposure to ozone).

## 2. Theory

## **2.1.** Modification of $F_a(SS)$ to include a distributions of $d_p$ and $\kappa$

Probability density functions of  $d_p$  (Abdul-Razzak and Ghan, 2000; Snider et al., 2006) and  $\kappa$  (Cerully et al., 40 2011; Su et al., 2010) have been widely used in aerosol science and atmospheric research to describe the CCN Comment [S6]: Reviewer#1 (16).

#### Comment [S7]: Reviewer#1 (19).

Comment [S8]: Reviewer#1 (26).

**Comment [S9]:** Reviewer#1 (1), (3) and (4). Reviewer#2 (2), (4) and (5).

The content of this section now very briefly reviews the "practical approach" to fit the activated fraction curves that considers a distribution of  $\kappa$  values instead of a single value.

activity. By using lognormal distributions, and by treating  $d_p$  and  $\kappa$  as uncorrelated variables to avoid double integration (Su et al., 2010; Zhao et al., 2015), the activated fraction  $F_a(SS)$  can be calculated as:

$$F_{\rm a}(SS) = \sum_{\kappa=0}^{\infty} \left\{ \frac{1}{2} - \frac{1}{2} \operatorname{erf}\left[ \frac{\ln d_{\rm p}(\kappa, SS) - \ln \mu_{\rm p,mode} - \ln^2 \sigma_{\rm p,geo}}{\sqrt{2} \ln \sigma_{\rm p,geo}} \right] \right\} p(\kappa) \Delta \kappa$$
 Eq. (3)

where  $\mu_{p,mode}$  and  $\sigma_{p,geo}$  are the mode and the geometrical standard deviation of  $d_p$ .  $p(\kappa)$  is the probability density function of  $\kappa$ :

$$p(\kappa) = \frac{1}{\kappa \ln \sigma_{\kappa \sigma eo} \sqrt{2\pi}} e^{-\frac{\left[\ln \kappa - \ln \mu_{\kappa, \text{mode}} - \ln^2 \sigma_{\kappa, \text{geo}}\right]^2}{2\ln^2 \sigma_{\kappa, \text{geo}}}}$$
Eq. (4)

where  $\mu_{\kappa,\text{mode}}$  and  $\sigma_{\kappa,\text{geo}}$  are the mode and the geometrical standard deviation of  $\kappa$ .

## **2.2.** Definition of the morphology-corrected volume equivalent diameter $d_{ve}$

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In this section, we find an original relationship to derive  $d_{ve}$  from  $d_m$  for a fractal-like aggregate.  $d_{ve}$  is the diameter of a sphere having the same volume as the aggregate, and assuming the aggregate made of identical, spherical primary particles, is defined as:

$$d_{\rm ve} = d_{\rm pp} N_{\rm pp}^{\frac{1}{3}}$$
 Eq. (5)

10 where  $d_{pp}$  and  $N_{pp}$  are the diameter and number of primary particles per aggregate, respectively. It is worth to notice that often, for practical purposes, the value of  $d_{pp}$  used in calculations is the mass equivalent diameter of the primary particle distribution obtained from TEM measurements. On the other hand,  $d_m$  is directly linked to the aerodynamic force acting on the particle  $F_{drag}$  (Dahneke, 1973; Tritscher et al., 2011) and can be directly obtained from SMPS measurements:

$$F_{\rm drag} = \frac{3\pi \eta d_{\rm m} v_{\rm r}}{C_{\rm c}(d_{\rm m})}$$
 Eq. (6)

15 where  $\eta$  and  $v_r$  are the kinematic viscosity of the gas and the particle-gas relative velocity, and  $C_c$  is the Cunningham slip factor (Allen and Raabe, 1985):

$$C_{\rm c}(K_{\rm n}) = 1 + K_{\rm n} \left[ 1.142 + 0.558 \exp\left(-\frac{0.999}{K_{\rm n}}\right) \right]$$
 Eq. (7)

 $K_{\rm n} = 2\lambda_{\rm g}/d_{\rm m}$  is the Knudsen number and  $\lambda_{\rm g}$  is the gas mean free path. The drag force acting on an aggregate  $F_{\rm drag,agg}$  can be approximated using the drag force acting on each primary particle  $F_{\rm drag,pp}$ , which is considered as a sphere, using the relation (Yon et al., 2015):

$$F_{\rm drag,agg} = F_{\rm drag,pp} N_{\rm pp} \frac{\Gamma}{D_{\rm f}}$$
 Eq. (8)

20 The exponential factor  $\Gamma = \Gamma(d_{pp})$  has been empirically estimated as a function of the Knudsen number (Yon et al., 2015) for soot particles generated with a miniCAST commercial burner (propane-air diffusion flame). In the range 1.61 <  $D_{f}$  <1.79:

## **Comment [S10]:** Reviewer#1 (2) and (6). Reviewer#2 (1).

The content of this section corresponds to the section 4.2 of the original paper (mostly unchanged, except for minor English corrections). It has been moved here in compliance to the demands of Reviewer#1 of making the paper less pedagogic (2) and re-framing the main topic (6) to focus on the effect of the aggregate morphology on activation.

$$\Gamma = 1.378 \left[ \frac{1}{2} + \frac{1}{2} \operatorname{erf} \left( \frac{K_{n}(d_{pp}) + 4.454}{10.628} \right) \right]$$

Although the variability range of  $D_{\rm f}$  might seem quite restrictive, in practice it covers a region representative of soot aggregates (Kelesidis et al., 2017; Yon et al., 2015). Therefore, we make the additional hypothesis that Eq. (9) can be applied to a variety of experimental investigations including our case. Introducing Eq. (6) in Eq. (8) yields:

$$d_{\rm m} = \frac{C_{\rm c}(d_{\rm m})}{C_{\rm c}(d_{\rm pp})} \ d_{\rm pp} N_{\rm pp} \frac{\Gamma}{D_{\rm f}}$$
Eq. (10)

5 The dependence on  $N_{\rm pp}$  can be removed by using the definition of  $d_{\rm ve}$  in Eq. (5). Finally, Eq. (10) can be solved for  $d_{\rm ve}$  to yield:

$$d_{\rm ve}(d_{\rm pp}, D_{\rm f}, d_{\rm m}) = d_{\rm pp} \left[ \frac{d_{\rm m}}{d_{\rm pp}} \frac{C_{\rm c}(d_{\rm pp})}{C_{\rm c}(d_{\rm m})} \right]^{\frac{D_{\rm f}}{3\Gamma}}$$
Eq. (11)

 $d_{\rm ve} = d_{\rm ve}(d_{\rm pp}, D_{\rm f}, d_{\rm m})$  can be calculated once size distribution and morphology of the aerosol are known using Eq. (11).  $d_{\rm pp}$  and  $D_{\rm f}$  are obtained from TEM imaging as explained below, while  $d_{\rm m}$  is easy to access from SMPS measurements.

- 10 The functional analysis of Eq. (11) shown in Fig. 1 highlights the effect of the variability of (a)  $d_{pp}$  and (b)  $D_f$  on  $d_{ve}$  in a range important for soot particles. One of the DMA transfer functions obtained in this work (black solid line, see further below for details) is used as an example. In the cases investigated in this work,  $d_{ve} = d_{ve}(d_{pp}, D_f, d_m)$  (colored dashed and dotted lines) is always shifted to smaller values and narrower than the original DMA transfer function. Increasing  $d_{pp}$  from 10 nm up to 30 nm ( $D_f = 1.7$ ) results in the main mode of
- 15  $d_{ve}$  increasing from 82.0 nm up to 117.0 nm. Similarly, increasing  $D_{f}$  from 1.6 up to 1.8 ( $d_{pp}$  = 20 nm) results in  $d_{ve}$  increasing from 93.5 nm up to 113.3 nm.

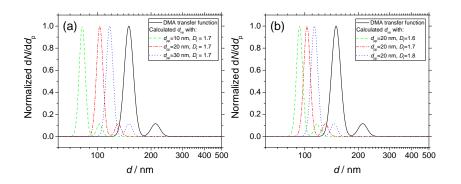


Fig. 1. Simulations of  $d_{ve} = d_{ve}(d_{pp}, D_f, d_m)$  of soot particles having complex morphology according to Eq. (11). The DMA transfer function (black solid line) results from the size selection at 150 nm of soot particles sampled from the kerosene jet diffusion flame at 130 mm HAB (see section 3 for details). For each series of simulations (colored dashed and dotted lines), (a)  $d_m$  and  $D_f$ , or alternatively (b)  $d_m$  and  $d_{pp}$  are set as constant and the remaining parameter is varied in the range indicated in the legend.

#### 3. Experimental approach

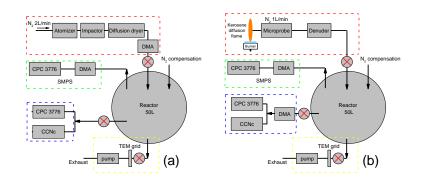
Eq. (9)

Comment [S11]: Reviewer#1 (23).

Comment [S12]: Reviewer#1 (6). Reviewer#2 (1).

This section (old section 4.2.3) has been integrated here as part of the re-framing of the paper.

In this section, the methodological approach is described. An overview of the experimental aerosol generation setup is shown in Fig. 2(a) for ammonium sulfate, and (b) for soot particles. Ammonium sulfate represents the simplest case that is well known in the literature (Rose et al., 2008) for the isolated, quasi-spherical particles that can be generated by atomization (section 3.1). Freshly generated ammonium sulfate aerosols are size selected then injected in a 50 L Pyrex glass static reactor. From the reactor, particles are sampled for activation experiments, size and morphology measurements. Soot particles are sampled from a jet diffusion flame supplied with kerosene, then chemically aged with ozone (section 3.2). All activation experiments are performed in a CCN-100 commercial nucleation chamber (section 3.3). The particle size and morphology are characterized by SMPS and TEM, respectively (section 3.4).



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Fig. 2. Overview of the experimental setup used for (a) ammonium sulfate and (b) soot. Aerosol injection system (red frame), size distribution measurement system (green frame), activated fraction measurements system (blue frame), and collection system for TEM grids (yellow frame).

#### 15 3.1. Ammonium sulfate aerosols generation

Ammonium sulfate aerosols are generated by atomization using a TSI aerosol generator 3076 loaded with  $0.1 \text{ gL}^{-1}$  concentration aqueous solution. Nitrogen is used for atomization, in the range 2-3 L min<sup>-1</sup> depending on the target aerosol concentration. The excess water is removed by flowing the aerosol in a 60 cm long diffusion dryer loaded with silica gel orange.

## 20 3.2. Soot aerosol generation, sampling and aging

A detailed description of the burner and sampling system is given in (Grimonprez et al., 2018). Briefly, a turbulent kerosene jet flame is stabilized on a Holthuis burner modified to allow the installation of a direct injection high efficiency nebulizer. The high speed spray of liquid fuel droplets at the exit of the nebulizer is ignited by a pilot methane flat flame on the outer ring of the modified burner, resulting in a turbulent diffusion flame approximately 21 cm high. All experiments are performed using kerosene fuel Jet A-1. Soot is extracted from the jet flame at 70 and 130 mm HAB. At 70 mm HAB the particle concentration is small and the gas phase is rich in condensable hydrocarbons. At higher HAB, the particle concentration increases and both the diameter

of the primary particles and the mobility diameter of the aggregates grow due to surface reaction and coagulation. This results in the increase of the soot volume fraction up to a peak at 130 mm HAB. Above
210 mm HAB all the particles are oxidized resulting in a non-smoking flame. Soot is sampled with a diluting quartz microprobe. The sampled flow is analyzed online by SMPS or deposited on Lacey grid for TEM analyses.

This setup allows a fast dilution of the sampled gas up to a factor  $3 \times 10^4$  that quenches most chemical reactions and limits particle coagulation and aggregation downstream in the sampling line. It is important to notice that the particle concentration in the sampling line has to be larger than the optical counters detection limit but low enough to limit post-sampling aggregation or agglomeration. To avoid the formation of secondary organic aerosol in the reactor, a parallel plate, activated carbon diffusion denuder is installed downstream the microprobe.

Fresh kerosene soot particles are characterized by extremely low  $\kappa$ . In this work, the reaction of freshly sampled soot with ozone is used to increase  $\kappa$ , i.e. to lower  $SS_c$ , following the experimental procedure detailed in our past work (Grimonprez et al., 2018). The experimental variable used to control the surface oxidation of soot particle is the so called ozone exposure, defined as the product of the ozone concentration and the residence

- 10 particle is the so called ozone exposure, defined as the product of the ozone concentration and the residence time in the reactor. Briefly, the reactor is first pumped to reduce the background particle count below the lower detection limit of the CPC, and then is filled with nitrogen and ozone generated by photolysis of oxygen with a UVP SOG-2 lamp. To inject the soot aerosol, the pressure in the reactor is set to a slightly lower value than the sampling line ( $\Delta p \simeq -20$  mbar). Therefore, a net sample flow (estimated around 2-5 mL min<sup>-1</sup>) enters the probe
- from the flame, is immediately mixed with the nitrogen dilution flow (1-8 L min<sup>-1</sup>), passes through the denuder and finally arrives to the reactor. The time origin for the calculation of ozone exposure starts 10 s after the end of soot injection. During injections, the SMPS is disconnected from the reactor to avoid acquiring data outside the recommended pressure range, and reconnected after the pressure has been raised again up to p = 1 bar.

#### 3.3. Activation experiments

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- 20 Activation experiments aim to measure  $F_a = F_a(SS)$  and are performed by means of a commercial Droplet Measurement Technologies Cloud Condensation Nuclei counter CCNc-100 installed in parallel to a TSI condensation particle counter CPC 3776. To study the effect of the particle size distribution on  $F_a$ , two different protocols are adopted for ammonium sulfate and soot. Ammonium sulfate particles are size selected by a DMA, pass through the reactor and then are injected in the CCNc-100. Soot particles are first sampled from the flame
- and injected in the reactor in which they are aged with ozone (section 3.2). A TSI differential mobility analyzer DMA 3081 is installed immediately downstream the reactor so that only aerosol particles with a selected electrical mobility and geometric deviation are injected in the CCNc-100. Additional verifications of the size distribution are performed by SMSP at regular time intervals to rule out the presence of coagulation during the aging experiments. More in detail, a 0.8 L min<sup>-1</sup> particle-laden flow is sampled from the reactor, split and used
- to supply the CCNc (0.5 L min<sup>-1</sup>) and the CPC (0.3 L min<sup>-1</sup>) in parallel that record the concentration of nucleated water droplets and aerosol particles at different supersaturations, respectively, required to plot  $F_a = F_a(SS)$ . The total flow sampled by the CPC and the CCN is balanced with nitrogen injected directly into the reactor, and all concentrations are corrected for dilution during measurements. Samples on TEM grids are also collected to get information on the morphology and primary particle size distribution of the test aerosol. All activation
- 35 experiments were taken from our previous work (Grimonprez et al., 2018).

#### 3.4. Diagnostics

SMPS measurements are performed to measure the aerosol electrical mobility diameter  $d_m$  using a TSI 3091 SMPS that consists of a TSI 3080 DMA upstream a TSI 3776 CPC operated with 0.3 L min<sup>-1</sup> aerosol flow rate and 1:10 sample/sheath flow ratio. The DMA can be used independently to select aerosol particles of the desired mobility.

40 mobility

TEM is used to measure  $d_{\rm pp}$  and  $N_{\rm pp}$  from which  $D_{\rm f}$  is calculated (section 4.2). All parameters are estimated from the TEM images by using ImageJ freeware software. TEM measurements are performed on the FEI Tecnai G2 20 microscope (200 kV acceleration voltage) available at the center for electron microscopy of Lille University. All samples are deposited on Lacey carbon meshes.

## 5 4. Results and discussion

## 4.1. Isolated, spherical particles: test with ammonium sulfate

Ammonium sulfate is well known for the quasi-spherical particles that can be generated by atomization of aqueous solution, and for this very reason is often used as a reference material for activation experiments (Petters and Kreidenweis, 2007; Rose et al., 2008), and in this work to test the validity of Eq. (3) before moving

10 to complex morphology aggregates. An example of TEM image of the ammonium sulfate particles obtained after size selection is shown in Fig. 3(a), while the corresponding particle projection (TEM) and electrical mobility (SMPS) distributions are shown in Fig. 3(b) and (c), respectively. The lognormal fitting functions of  $d_p$ (black dashed line) and  $d_m$  (red solid line) are also shown in the figures. The fitting function of  $d_m$  is the sum of two lognormal distributions corresponding to +1 (dotted blue line) and +2 (dashed green line) net particle charge (Kuwata and Kondo, 2008)

$$\frac{\mathrm{d}N(d_{\mathrm{p}})}{\mathrm{d}d_{\mathrm{p}}} = \sum_{i=1}^{2} \frac{N_{i}}{d_{\mathrm{p}}\ln\sigma_{\mathrm{p,geo,i}}\sqrt{2\pi}} e^{-\frac{\left[\ln d_{\mathrm{p}} - \ln\mu_{\mathrm{p,mode,i}} - \ln^{2}\sigma_{\mathrm{p,geo,i}}\right]^{2}}{2\ln^{2}\sigma_{\mathrm{p,geo,i}}}}$$

For isolated, spherical and homogeneous particles,  $d_{ve} = d_m = d_p$  (Eggersdorfer and Pratsinis, 2014; Sorensen, 2011). Although Fig. 3 shows a particularly favorable case, in this work it is found that  $d_m = d_p$  is always true within 20% uncertainty. A summary of the parameters of the distributions is given in Table 1.

Comment [S13]: Reviewer#1 (3), (4) and (28). Reviewer#2 (2).

Multiple charges and the DMA transfer function are now considered in the calculations.

Eq. (12)

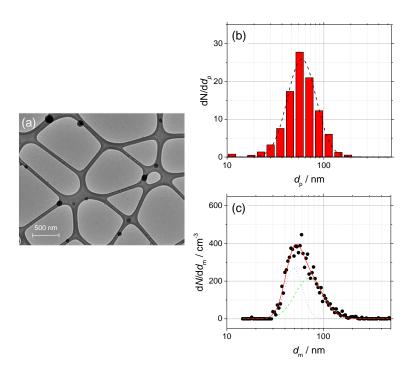


Fig. 3. (a) TEM image of size selected ammonium sulfate particles (black quasi-spherical particles) deposited on a Lacey mesh, 6500 magnification. (b) diameter of the particle projection  $d_p$  obtained from TEM measurements (red bars) and fitting function (black dashed line). (c) electrical mobility diameter  $d_m$  obtained from SMPS measurements (black dots). The contributions of +1 (blue dotted line) and +2 (green dashed line) charged particles to the fitting function (red solid line) are also shown.

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The experimental activation data (black data points) and the calculated activation curves are shown in Fig. 4(a):  $\mu_{p,mode}$  and  $\sigma_{p,geo}$  are used as input parameters and obtained independently from SMPS ( $d_m$ , red solid line) and TEM ( $d_p$ , black dashed lines) measurements as shown in Fig. 3. Globally, the experimental data are in good agreement with the calculated curves. Fig. 4(b) shows  $p(\kappa)$  obtained from the fitting in the two cases ( $\mu_{\kappa,mode}$ and  $\sigma_{\kappa,geo}$  are set as free parameters). The calculations from the independently obtained  $d_m$  and  $d_p$  result in very close  $p(\kappa)$  having geometric mean  $\kappa_{SMPS} = 0.60$  and  $\kappa_{TEM} = 0.61$ , both in excellent agreement with  $\kappa = 0.61$  found in the literature (Petters and Kreidenweis, 2007).

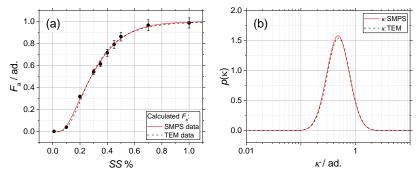




Fig. 4. Dry ammonium sulfate particles: (a) activation data obtained from CCNc experiments (black dots) and calculated  $F_a = F_a(SS)$  using SMPS (red solid line) and TEM (black dashed lines) data as  $d_{ve}$ . (b) corresponding  $p(\kappa)$  distributions.

<i>d</i> <sub>m</sub> / nm (mode, SMPS)	d <sub>p</sub> / nm (mode, TEM)	$d_{\rm m}/d_{\rm p}$ (expected: 1.0)	$\kappa_{\text{SMPS}}$ / ad. (geometric mean)	$\kappa_{\text{TEM}}$ / ad. (geometric mean)
57.3±0.6	59.2±0.8	0.97	0.60±0.02	0.61±0.02

Table 1. Parameters of the lognormal distributions used in the activation experiments of ammonium sulfate particles and shown in Fig. 3. The uncertainties are calculated from the lognormal fitting of the distributions. The table also shows the comparison of  $\kappa_{\text{SMPS}}$  and  $\kappa_{\text{TEM}}$ .

#### 4.2. Characterization of the soot particles morphology

As mentioned above,  $d_{pp}$  and  $D_f$  of soot aggregates are obtained at the same time from the analysis of TEM images. It is important to notice that Eq. (8) is derived for the mass equivalent diameter and not for the diameter of the projected image (Yon et al., 2015). However, if the soot particles can be considered homogeneous, the mass equivalent diameter and the diameter of the projected image only differ by a scale factor that is easily accounted for.

In this work,  $d_{pp}$  is directly obtained by manual counting of the projected images of the soot primary particles.

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 $D_{\rm f}$  has been obtained in the past by using at least three different experimental techniques: angular light scattering (Sorensen et al., 1992), scanning electron microscopy (Colbeck et al., 1997) and transmission electron microscopy (Cai et al., 1995; Hu et al., 2003; Köylü and Faeth, 1992). In this work, we follow an approach to estimate  $D_{\rm f}$  from the images of soot aggregates that requires measuring the maximum length of the aggregate projection  $L_{\rm 2D}$  (Cai et al., 1995; Köylü et al., 1995):

$$\ln(N_{\rm pp}) = \ln(k_{\rm g}) + D_{\rm f} \ln\left(\frac{L_{\rm 2D}}{d_{\rm pp}}\right)$$
 Eq. (13)

where  $k_g$  is the coefficient of the maximum length of the aggregate projection that is treated as a free parameter. As a faster alternative to manual counting, it is possible to estimate  $N_{pp}$  from the same set of data used to measure  $D_f$  with Eq. (13) by also measuring the total surface of the aggregate projection  $A_{2D}$  (Köylü et al., 1995):

$$\ln(N_{\rm pp}) = \ln(k_{\rm a}) + \alpha \ln\left(\frac{4A_{\rm 2D}}{\pi d_{\rm pp}^2}\right)$$
 Eq. (14)

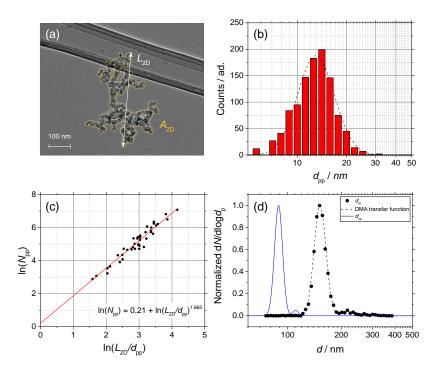
where  $k_a$  and  $\alpha$  are the coefficient and exponent of the projection area, respectively, that for soot fractal aggregates can be either calculated (Medalia, 1967) or measured (Köylü et al., 1995; Samson et al., 1987).  $D_f$  of fresh soot particles measured by following this approach (1.665 at 70 mm HAB and 1.647 at 130 mm HAB) is consistent with typical values found in the literature (Cai et al., 1995; Köylü et al., 1995; Samson et al., 1987; Sorensen and Roberts, 1997; Tian et al., 2006). The analysis of TEM images of soot aggregates before and after exposure to ozone confirms that the fractal dimension does not change significantly during the chemical aging process.

30 The complete characterization of the size and morphology of young soot particles sampled at 70 mm HAB and mature soot particles sampled at 130 mm are shown in Fig. 5 and Fig. 6, respectively. (a) TEM pictures of one

**Comment [S14]:** Reviewer#1, (3) and Reviewer#2, (1), (4) and (5).

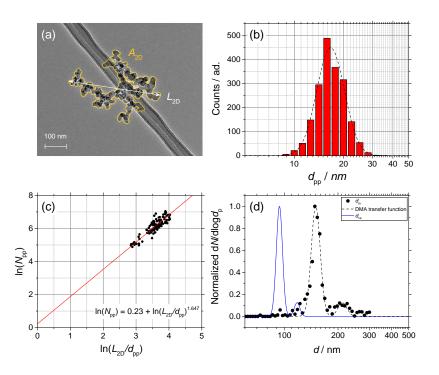
This section is clarified and re-organized to match the revised paper structure, however the content is unchanged with respect to the original paper.

aggregate; (b)  $d_{\rm pp}$  size distributions; (c) ln ( $N_{\rm pp}$ ) vs. ln ( $L_{\rm 2D}/d_{\rm pp}$ ) plots from which  $D_{\rm f}$  is obtained according to Eq. (13); (d) SMSP data (black points) and DMA transfer function (black dashed line) after particle size selection, and morphology-corrected  $d_{\rm ve}$  (blue solid line) calculated using Eq. (11).



5 Fig. 5. Soot sampled from the turbulent jet flame supplied with liquid kerosene at 70 mm HAB. (a) TEM picture of a soot aggregate showing  $L_{2D}$  and  $A_{2D}$ . (b)  $d_{pp}$  size distribution (red bars) and lognormal fit (black dashed line),  $d_{pp} = 13.0$  nm (mass equivalent  $d_{pp} = 14.1$  nm). (c) ln  $(N_{pp})$  vs. ln  $(L_{2D}/d_{pp})$  plot from which  $D_f$  is obtained (42 projections). (d) normalized SMPS data after size selection at 150 nm (black data points and dashed line) and morphology-corrected  $d_{ve}$  calculated using Eq. (11) (blue solid line).

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Fig. 6. Soot sampled from the turbulent jet flame supplied with liquid kerosene at 130 mm HAB. (a) TEM picture of a soot aggregate showing  $L_{2D}$  and  $A_{2D}$ . (b)  $d_{pp}$  size distribution (red bars) and lognormal fit (black dashed line),  $d_{pp} = 16.7$  nm (mass equivalent  $d_{pp} = 17.7$  nm). (c) ln  $(N_{pp})$  vs. ln  $(L_{2D}/d_{pp})$  plot from which  $D_f$  is obtained (100 projections). (d) normalized SMPS data after size selection at 150 nm (black data points and dashed line) and morphology-corrected  $d_{
m ve}$ calculated using Eq. (11) (blue solid line).

## 4.3. CCN activity of soot particles

In this section, the data obtained from CCNc activation experiments are used to validate the approach based on the morphology-corrected  $d_{ve}$  and to determine  $p(\kappa)$ . The activation data are reproduced from our past investigation (Grimonprez et al., 2018). Soot is collected from the kerosene jet flame at two HABs to show the different behavior of young and reactive soot (70 mm HAB) and of mature and more inert soot (130 mm HAB) during the chemical aging. The morphology-corrected  $d_{ve} = d_{ve}(d_{pp}, D_f, d_m)$  is considered as representative of both the soot particle size distribution ( $d_{\rm m}$ ) and morphology ( $d_{\rm pp}$  and  $D_{\rm f}$ ) and used as  $d_{\rm p}$  in Eq. (3).  $p(\kappa)$  is obtained from the fitting of  $F_a = F_a(SS)$  with Eq. (3) and Eq. (4) with  $\mu_{\kappa,mode}$  and  $\sigma_{\kappa,geo}$  treated as free

15 parameters.

> Fig. 7 shows the activation data obtained after chemical aging with ozone and used to quantify  $p(\kappa)$  at different ozone exposure (data points). The activation curves (lines) are calculated in four different scenarios, with each individual plot representing one unique combination of  $d_{\rm m}$  or  $d_{\rm ve}$  with  $\kappa$  or  $p(\kappa)$ : to represent the particle size distribution, the DMA transfer function (left column) or alternatively the morphology-corrected  $d_{\rm ve}$  (right

column) is used. To represent the particle hygroscopic activity, a single  $\kappa$  value (top row) or a probability 20 distribution  $p(\kappa)$  (bottom row) is used in the fitting function.

Comment [S15]: Reviewer#1 (6), (7) and (8). Reviewer#2 (4) and (5)

This section has been entirely re-written to comply with the requested re-framing of the paper: the focus of the paper has been moved to the effect of the particle morphology and of the soot maturity on the activation (6), and the goals are explained more clearly and directly (7).

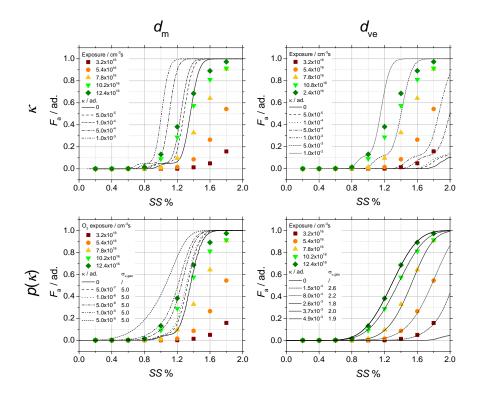


Fig. 7. Soot sampled from the turbulent jet flame supplied with liquid kerosene at 70 mm HAB. CCNc activation curves of the soot particles obtained after chemical aging with ozone, comparison of the experimental data (data points) to activation curves calculated under four different hypotheses (lines): single  $\kappa$  value (top row),  $p(\kappa)$  (bottom row), DMA transfer function (left column), and the morphology-corrected  $d_{ve}$  (right column).

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As shown in the figure, the calculations based on  $d_{\rm m}$  consistently result in the shift of the activation curves to low *SS*, and as a consequence many activation data are found below the Kelvin limit ( $\kappa = 0$ , black solid line). Although using  $p(\kappa)$  instead of  $\kappa$  has a clear effect on the slope of the activation curves as  $\sigma_{\kappa,geo}$  introduces one additional degree of freedom in the fitting function, this effect is not large enough to compensate for the shift.

10 On the other hand, the calculations based on  $d_{ve}$  result in a significant shift of the Kelvin limit to high *SS*. The additional degree of freedom of the fitting function obtained by using  $p(\kappa)$  instead of  $\kappa$  further improves the quality of the fitting, and the activation data can now be very convincingly reproduced by the calculated curves. In conclusion, in order to correctly reproduce the activation behavior of soot particles, their fractal-like morphology must be taken into account, and a morphology-corrected  $d_{ve}$  is a relatively simple and convenient 15 approach.

The activation data obtained after chemical aging of mature soot at different ozone exposure (data points) are shown in Fig. 8. Unlike the previous case, the activation curves (lines) are directly calculated using the morphology-corrected  $d_{ve}$  and a probability distribution  $p(\kappa)$ . As shown in the figure, the chemical aging with ozone of mature soot particles with exposure below ~10<sup>15</sup> cm<sup>-3</sup>s produces particles that are only activated at

20 very high SS, andthe plateau of the activation curves is reached outside the dynamic range of the CCNc. Although it is evident that a weak but consistent activation occurs at high SS, this behavior is poorly reproduced by Eq. (3) and cannot be distinguished from the limit case of ideal non-interacting water vapor and soot particles.

Comment [S16]: Reviewer#1 (16).

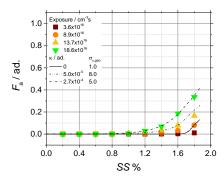


Fig. 8. Soot sampled from the turbulent jet flame supplied with liquid kerosene at 130 mm HAB. CCNc activation curves of the soot particles obtained after chemical aging with ozone, comparison of the experimental data (data points) to activation curves (lines) calculated by using  $p(\kappa)$  the and morphology-corrected  $d_{ve}$ .

- 5 κ of chemically aged soot particles is typically 2-3 orders of magnitude lower than typical inorganic aerosols used in activation experiments (Petters and Kreidenweis, 2007). Therefore, the activation experiments with chemically aged mature soot are particularly interesting as they offer a unique opportunity to estimate the lower limit of validity of Eq. (3). The activation data shown in Fig. 8 are well reproduced by Eq. (3) only for exposure larger than about 13×10<sup>-16</sup> cm<sup>-3</sup>s and yield κ values in the range of 10<sup>-5</sup>-10<sup>-4</sup>, while exposure lower than about 9×10<sup>-16</sup> cm<sup>-3</sup>s result in activation data very close to or below the Kelvin limit. From the comparison of the two situations, it can be estimated that Eq. (3) is only valid for κ > 5×10<sup>-6</sup>.
  - The data on the size distribution and morphology of the tested young and mature soot particles are summarized and compared to the activation data obtained at different ozone exposure in Table 2.

HAB / mm	d <sub>pp</sub> / nm (mode, TEM)	$D_{\rm f}$ / ad.	d <sub>m</sub> / nm (mode, SMPS)	d <sub>ve</sub> / nm (mode)	Exposure / 10 <sup>16</sup> cm <sup>-3</sup> s	$\mu_{\kappa, mode} / 10^{-4}$ (geo. mean)	$\sigma_{ m \kappa,geo}$ / ad. (geo. st. dev.)
70 13.0±0.:		1.665±0.005	152.1±0.9		3.2	3.7 [3.2, 4.5]	2.6
				89.0±0.5	5.4	15 [14, 17]	2.2
	13.0±0.5				7.8	37 [34, 41]	1.8
					10.2	60 [57, 65]	2.0
					12.4	74 [69, 80]	1.9
130		1.647±0.005	150.0±0.9	93.8±0.5	3.6	/	/
	16.7±0.5				8.9	/	/
	10.7±0.5				13.7	0.5 [0.4, 0.6]	8.0
					18.6	2.7 [2.6, 3.6]	5.0

15 Table 2. Size and morphology parameters  $(d_{pp}, D_f, d_m)$  used for calculating the morphology-corrected  $d_{ve}$  of young (70 mm HAB) and mature (130 mm HAB) soot particles. Comparison with the activation data at different ozone exposure,  $\mu_{\kappa,mode}$  and  $\sigma_{\kappa,geo}$  are calculated from the best fit (the variability range of  $\mu_{\kappa,mode}$  is provided in brackets).

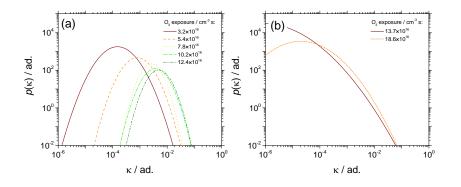


Fig. 9. Evolution of  $p(\kappa)$  vs. ozone exposure of (a) young soot particles sampled at 70 mm HAB, and (b) mature soot particles sampled at 130 mm HAB.

Fig. 9 shows the effect of the chemical aging on  $p(\kappa)$ . In the literature,  $\kappa$  is often treated as an effective value that folds in all information not explicitly accounted for in the theory, like the change of the water surface tension due to the presence of solutes or the particle morphology for instance. The main advantage of using a morphology-corrected  $d_{ve}$  is that the effects of the particle size and morphology on activation are de-coupled from the particle chemistry, and therefore  $\kappa$  is preserved as a "chemistry-only" indicator.

As shown in Fig. 9(a), and (b) to a lesser extent, as the ozone exposure increases  $p(\kappa)$  shifts to the right ( $\mu_{\kappa,mode}$ 

- 10 increases) and becomes progressively narrower ( $\sigma_{\kappa,geo}$  decreases). The increasing  $\mu_{\kappa,mode}$  is strong evidence that the (surface) chemical composition of the soot particles changes significantly against the ozone exposure time. The PAHs adsorbed at the surface of soot particles are likely candidates to explain the difference in the particle reactivity. Small PAHs typically found adsorbed on the surface of young soot particles have large H/C ratio, and therefore large surface concentration of hydrogen atoms available for abstraction reactions.
- 15 Conversely, large PAHs typically found on mature soot are characterized by lower H/C ratio that can explain the overall lower reactivity of mature soot particles. An early discussion based on the analysis of  $F_a$  at fixed SS can be found in our previous work (Grimonprez et al., 2018). It is also noteworthy that  $\sigma_{\kappa,geo}$  decreases as the ozone exposure increases. A possible interpretation is that the (surface) chemical composition of the soot particles becomes more homogeneous after chemically aging, likely as a consequence of the PAHs oxidation process that results in the formation of water soluble compounds (ketones, aldehydes) at the particle surface.
  - The comparison of Fig. 9(a) and (b) clearly shows that young and mature soot particles behave very differently to chemical aging and activation experiments. Similar ozone exposure in the range  $12 14 \times 10^{-16}$  cm<sup>-3</sup>s result in  $\kappa$  being over two orders of magnitude larger at 70 mm HAB ( $74 \times 10^{-4}$ ) than at 130 mm HAB ( $0.5 \times 10^{-4}$ ). The soot generation process is therefore critically important for aging/activation experiments and must be taken into account to obtain reliable and reproducible data.

25

- As a concluding remark, it is important to remember that  $\kappa$ -Köhler theory is a classical theory entirely founded on equilibrium thermodynamics, and for this very reason it is possibly not adapted to describe nanoscale phenomena. The work presented herein remains a simple extension of  $\kappa$ -Köhler theory that despite not requiring detailed chemical knowledge of the aerosol particles still manages produce rather accurate predictions of the activated fraction of soot particles characterized by complex morphology without adding any
- **30** predictions of the activated fraction of soot particles characterized by complex morphology without adding any ad-hoc hypothesis. A more sophisticated approach is probably required to explain the existence of activation data below the Kelvin limit (adsorption-activation theory for instance). Furthermore,  $d_{ve}$  is obviously not the only diameter that can be used to parameterize the particle activation but only a very convenient one.

Comment [S17]: Reviewer#1 (26).

Potentially viable alternatives include the aerodynamic or the gyration diameter for instance, however a systematic verification goes beyond the scope of this paper.

#### 5. Conclusions

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- Soot particles having fractal-like morphology are well known to become, if certain conditions are met, important cloud condensation nuclei (CCN) in the atmosphere. In this work, in order to determine the probability distribution  $p(\kappa)$  of the hygroscopic parameter  $\kappa$  of soot particles, a morphology-corrected volume equivalent diameter  $d_{ve}$  is defined and used to parameterize the particle diameter in  $\kappa$ -Köhler theory. The morphology-corrected  $d_{ve}$  is calculated from the particle electrical mobility  $d_m$  and folds in two important descriptors of the particle morphology that are the primary particle diameter  $d_{pp}$  and the fractal dimension
- 10  $D_{\rm f}$ . In practice,  $d_{\rm m}$  is measured by scanning mobility particle sizing (SMPS), while  $d_{\rm pp}$  and  $D_{\rm f}$  are obtained from the analysis of the projections of soot particles from transmission electron microscopy images (TEM).

This simple model, first tested with isolated, quasi-spherical ammonium sulfate particles, well reproduces the activation experiments and provides  $\kappa$  in excellent agreement with the literature. Then, the model is used to determine  $p(\kappa)$  of soot particles sampled at different reaction time, or equivalently at different height above

- 15 the burner (HAB), from a laboratory jet flame supplied with kerosene. To increase their hygroscopic activity, soot particles are chemically aged with ozone beforehand. The experimental activation data are compared to the activation curves calculated using all combinations of  $d_{\rm m}$  or  $d_{\rm ve}$  with  $\kappa$  or  $p(\kappa)$ . The best fitting of the activation data is obtained by using  $p(\kappa)$  along with the morphology-corrected  $d_{\rm ve}$ . This important conclusion proves that the particle morphology are shown to plays a non negligible role on the activation of soot particles
- 20 and has to be taken into account. Furthermore, using the morphology-corrected  $d_{ve}$  effectively de-couples the effect of the particle morphology on the activation, potentially preserving  $p(\kappa)$  as an indicator of the particle chemistry only.

Young soot particles sampled at 70 mm HAB are more reactive than mature soot particles sampled at 130 mm HAB, resulting in their activation data to be shifted by a significant amount to lower *SS*. The predictive capability of the model is very satisfying in the case of young soot particles that are efficiently converted into CCN after exposure to ozone ( $\kappa \sim 3.7 - 74 \times 10^{-4}$ ). At similar ozone exposure, mature soot particles show a much slower reactivity with ozone ( $\kappa \sim 0.5 - 2.7 \times 10^{-4}$ ) that results in the plateau of the activation curves being reached outside the dynamic range of the CCN counter. This approach proved to be viable for  $\kappa > 5 \times 10^{-6}$ .

30 *Data availability.* The data used in this study are stored in the University of Lille servers and are available on request from the corresponding author (alessandro.faccinetto@univ-lille.fr).

Author contributions. JW provided the initial version of the model. JW, SG and SB carried out the research and performed the data analysis. JW, AF, JY, PD and DP improved and refined the model. JW and AF wrote the manuscript with contributions from all authors. All authors have given approval to the final version of the manuscript.

Competing interests. The authors declare that they have no conflict of interest.

**Comment [S18]:** Please notice that the *Conclusions* have been updated to match the modifications required by the Reviewers. Acknowledgments. This work was supported by the Agence Nationale de la Recherche through the LABEX CAPPA (ANR-11-LABX-0005), the Ministry of Higher Education and Research, Hauts-de-France Regional Council, the European Regional Development Fund (ERDF) through the Contrat de Projets Etat-Region (CPER CLIMIBIO) and the MERMOSE project sponsored by the French Civil Aviation Authority (DGAC).

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