1	Estimating CCN number concentrations using aerosol optical properties:
2	Role of particle number size distribution and parameterization
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16	Abstract
17	The concentration of cloud condensation nuclei (CCN) is an essential parameter affecting
18	aerosol-cloud interactions within warm clouds. Long-term CCN number concentration (N_{CCN})
19	data are scarse, there are a lot more data on aerosol optical properties (AOPs). It is therefore
20	valuable to derive parameterizations for estimating $N_{\rm CCN}$ from AOP measurements. Such
21	parameterizations have been made earlier, and in the present work a new one is presented. The
22	relationships between $N_{\rm CCN}$, AOPs and size distributions were investigated based on in-situ
23	measurement data from six stations in very different environments around the world. The
24	relationships were used for deriving a parameterization that depends on the scattering Ångström
25	exponent (SAE), backscatter fraction (BSF) and total scattering coefficient (σ_{sp}) of PM10
26	particles. The analysis first showed that the dependence of $N_{\rm CCN}$ on supersaturation SS can be
27	described by a logarithmic fit in the range $SS < 1.1\%$, without any theoretical reasoning. The
28	relationship between $N_{\rm CCN}$ and AOPs was parameterized as: $N_{\rm CCN} \approx ((286 \pm 46) \text{SAE})$
29	$ln(SS/(0.093 \pm 0.006))(BSF - BSF_{min}) + (5.2 \pm 3.3))\sigma_{sp}$, where BSF_{min} is the minimum BSF, in
30	practice the 1 st percentile of BSF data at a site to be analyzed. At the lowest supersaturations of
	1

1 each site (SS $\approx 0.1\%$), the average bias, defined as the ratio of the AOP-derived and measured 2 N_{CCN} , varied from ~0.7 to ~1.9 at most sites except at the Himalayan site PGH where the bias 3 was > 4. At SS > 0.4% the average bias ranged from \sim 0.7 to \sim 1.3 at most sites. For the marineaerosol dominated site ASI the bias was higher, $\sim 1.4 - 1.9$. In other words, at SS > 0.4% N_{CCN} 4 5 was estimated with an average uncertainty of approximately 30% by using nephelometer data. 6 The biases were mainly due to the biases in the parameterization related to the scattering 7 Ångström exponent SAE. The squared correlation coefficients between the AOP-derived and 8 measured $N_{\rm CCN}$ varied from ~0.5 to ~0.8. To study the physical explanation of the relationships 9 between $N_{\rm CCN}$ and AOPs, lognormal unimodal particle size distributions were generated and 10 $N_{\rm CCN}$ and AOPs were calculated. The simulation showed that the relationships of $N_{\rm CCN}$ and 11 AOPs are affected by the geometric mean diameter and width of the size distribution and the 12 activation diameter. The relationships of $N_{\rm CCN}$ and AOPs were similar to those of the observed 13 ones.

14

15 **1. Introduction**

Aerosol-cloud interactions (ACI) are the most significant sources of uncertainty in estimating the radiative forcing of the Earth's climate system (e.g., Forster et al., 2007; Kerminen et al., 2012), which makes it more challenging to predict the future climate change (Schwartz et al., 2010). An essential parameter affecting ACI within warm clouds is the concentration of cloud condensation nuclei (CCN), i.e., the number concentration of particles capable of initiating cloud droplet formation at a given supersaturation. Determining CCN concentrations and their temporal and spatial variations is one of the critical aspects to reduce such uncertainty.

23

CCN number concentrations (N_{CCN}) have been measured at different locations worldwide (e.g., Twomey, 1959; Hudson,1993; Kulmala et al., 1993; Hämeri et al., 2001; Sihto et al., 2011; Pöhlker et al., 2016; Ma et al., 2014). However, the accessible data especially for long-term measurements are still limited in the past and nowadays due to the relatively high cost of instrumentation and the complexity of long-term operating. As an alternative to direct measurement, N_{CCN} can also be estimated from particle number size distributions and chemical composition using the Köhler equation. Several studies have investigated the relative 1 importance of the chemical composition and particle number distributions for the estimation of 2 N_{CCN} (Dusek et al., 2006; Ervens et al., 2007; Hudson, 2007; Crosbie et al., 2015). For the best 3 of our understanding, particle number size distributions are more important in determining N_{CCN} 4 than aerosol chemical composition. This makes particle number size distribution measurements 5 capable of serving as a supplement to direct CCN measurements.

6

7 Considering the tremendous spatiotemporal heterogeneity of atmospheric aerosol, neither 8 direct measurements of $N_{\rm CCN}$ nor the concentrations estimated from particle size distributions 9 are adequate for climate research. In order to overcome the limitation of current measurements, 10 many studies have attempted to estimate $N_{\rm CCN}$ using aerosol optical properties (AOPs) (e.g., Ghan et al., 2006; Shinozuka et al., 2009; Andreae, 2009; Jefferson, 2010; Liu et al., 2014; 11 12 Shinozuka et al., 2015; Tao et al., 2018). This approach would give both geographically wider 13 and temporally longer estimates of $N_{\rm CCN}$ than the available particle number size distribution and 14 direct CCN measurement data. For instance, on 20 June 2019 the WMO Global Atmosphere 15 Watch World Data Centre for Aerosols (GAW-WDCA) (http://ebas.nilu.no/) contained particle 16 number size distribution data sets from 22 countries altogether from 58 stations, but only 5 of 17 them were outside Europe. The CCN counter (CCNC) data were from 3 European sites. On the 18 other hand, in the same data base, the light scattering coefficients measured with a nephelometer 19 were from 31 countries and 103 stations located on all continents and also on some islands. The 20 temporal coverage data in the GAW-WDCA data base is such that the oldest nephelometer data, 21 those from Mauna Loa, start in 1974, whereas the oldest particle number size distribution data, 22 those from the SMEAR II station in Finland, start in 1993. Another easily available source for 23 data is the US Department of Energy Atmospheric Radiation Measurement (ARM) user facility 24 (https://www.arm.gov/data). On 20 June 2019 we found that the ARM research facility data 25 contained particle size distribution data from 7 permanent sites and light scattering coefficient 26 measured with a nephelometer from 20 sites. It is clear that there are other data sets of all of 27 these measured around the world, but those that can be found either from the GAW-WDCA or 28 the ARM data bases are quality controlled and readily available.

29

30 Most of the above-mentioned studies attempted to link $N_{\rm CCN}$ with extensive AOPs, such as the

1 aerosol extinction coefficient (σ_{ext}), aerosol scattering coefficient (σ_{sp}) and aerosol optical depth 2 (AOD). Both N_{CCN} and σ_{sp} are extensive properties that vary with a varying aerosol loading. 3 The most straightforward approach to estimate CCN is to utilize the ratio between CCN and one of the extensive AOPs (e.g. AOD, σ_{ext} , σ_{sp}). However, the ratio is not a constant. Previous 4 studies have also pointed out that the relationship between $N_{\rm CCN}$ and extensive AOPs are 5 6 nonlinear. On one hand, Andreae (2009) reported that the relationship between AOD at the 7 wavelength $\lambda = 500$ nm (AOD₅₀₀) and CCN number concentration at the supersaturation of 0.4% $(CCN_{0.4})$ can be written as $AOD_{500}=0.0027 \cdot (CCN_{0.4})^{0.640}$, which indicates that AOD and CCN 8 9 depend in a non-linear way on each other: for a larger AOD there are more CCN per unit change 10 in AOD. On the other hand, Shinozuka et al. (2015) indicated that the larger the extinction 11 coefficient σ_{ext} was, the fewer CCN were per unit change of σ_{ext} .

12

13 Some studies have also involved intensive aerosol optical properties, such as the scattering 14 Ångström exponent (SAE), hemispheric backscattering fraction (BSF) and single-scattering 15 albedo (SSA) to build up a bridge between the N_{CCN} and AOPs. Jefferson (2010) used BSF and SSA to parameterize the coefficients C and k in the relation $N_{\text{CCN}}(SS) = C \times (SS)^k$, where SS is 16 17 the supersaturation percent (Twomey, 1959) and the exponent k is a function of SSA which 18 means it depends both on the scattering and absorption coefficients. Liu and Li (2014) discussed 19 how different aerosol properties affect the ratio of $N_{\rm CCN}$ to $\sigma_{\rm sp}$, i.e., $R_{\rm CCN}/\sigma_{\rm sp}$ based on *in-situ* 20 and remote-sensing data. Shinozuka et al. (2015) used SAE and aerosol extinction coefficient 21 to estimate N_{CCN} . Tao et al. (2018) used a novel method to derive the ratio $R_{\text{CCN}}/\sigma_{sp}$ which they 22 named as AR_{sp}, based on SAE and aerosol hygroscopicity using a humidified nephelometer. 23 All the studies mentioned above noted that the particle number size distribution (PNSD) plays 24 an important role in estimating N_{CCN} from aerosol optical properties.

25

In this paper we will analyze the relationships between $N_{\rm CCN}$, aerosol optical properties and size distributions at six different types of sites around the world. The relationships obtained from the field sites will be used for developing a parameterization for calculating $N_{\rm CCN}$ using AOPs. We will also study the physical explanations of the relationships between $N_{\rm CCN}$ and AOPs by simulations.

1 **2. Methods**

2 2.1 Sites and measurements

In-situ measurements of AOPs, particle number size distributions (PNSDs), and N_{CCN} were conducted at SMEAR II in Finland, SORPES in China, and 4 ARM Climate Research Facility (ACRF) sites (Mather and Voyles, 2013). The locations and measurement periods are listed in Table 1.

7

8 The Station for Measuring Forest Ecosystem-Atmosphere Relations (SMEAR II) is located at 9 the Hyytiälä Forestry Field Station (61°51' N, 24°17' E, 181 m above sea level) of University 10 of Helsinki, 60 km north-east from the nearest city. The station represents boreal coniferous forest, which covers ~8 % of the Earth's surface. Total scattering coefficient (σ_{sp}) and 1112 hemispheric backscattering coefficient (σ_{bsp}) of sub-1 µm and sub-10 µm particles are measured 13 using a TSI-3563 3-wavelength integrating nephelometer at $\lambda = 450, 550, \text{ and } 700 \text{ nm}$. The 14 calibration, data processing and calculation of AOPs followed the procedure described by 15 Virkkula et al. (2011) and Luoma et al. (2019). $N_{\rm CCN}$ was measured at the supersaturations (SS) 16 of 0.1%, 0.2%, 0.3%, 0.5% and 1.0% using a DMT CCN-100 CCN counter, similar to Schmale 17 et al. (2017). A whole measurement cycle takes around 2 hours; data were interpolated to hourly 18 time resolution to compare with other measurements. PNSDs were measured with a custom-19 made Differential Mobility Particle Sizer (DMPS) system in size range 3-1000 nm (Aalto et 20 al., 2001). A more detailed description of CCN measurements and station operation can be 21 found in Sihto et al. (2011) and Paramonov et al. (2015).

22

23 The Station for Observing Regional Processes of the Earth System (SORPES) is located in a 24 suburb of Nanjing, a megacity in the Yangtze River Delta municipal aggregation (32°07'14" N, 25118°57'10" E; ~40m a.s.l.). σ_{sp} and σ_{bsp} of total suspended particles (TSP) were measured with 26 an Ecotech Aurora-3000 3-wavelength integrating nephelometer at $\lambda = 450, 525$, and 635 nm 27 as described by Shen et al. (2018). N_{CCN} was measured using a CCN-200 dual column CCN 28 counter at 5 supersaturations: 0.1%, 0.2%, 0.4%, 0.6% and 0.8%. The two columns make the 29 same cycle simultaneously to cross-check with each other. Each cycle took 30 minutes. PNSDs 30 in the size range of 6 - 800 nm were measured with a DMPS built by University of Helsinki. 1 2 More details of the measurements at SORPES are given by, e.g., Ding et al. (2013, 2016) and Qi et al. (2015).

3

The US Atmospheric Radiation Measurement Mobile Facility (AMF) measures atmospheric 4 aerosol and radiation properties all over the world. The first AMF (AMF1) was deployed in 5 6 2005 with both a CCN counter and a nephelometer. Between 2011 and 2018, AMF1 was 7 operated at four locations: Ganges Valley (PGH) in the Himalayas, Cape Cod, Massachusetts 8 (PVC) in a coastal area of U.S., Manacapuru (MAO) downwind of the city of Manaus, Brazil, 9 and Ascension Island (ASI) on the South Atlantic Ocean downwind from Africa. Three of them 10 were accompanied by a scanning mobility particle sizer (SMPS; Kuang, 2016). The SMPS is 11 also part of the Aerosol Observing System (AOS) running side by side with AMF1 since 2012. Both PNSDs and AOPs are available simultaneously at PVC, MAO, and ASI. σ_{sp} and σ_{bsp} of 12 13 sub-1 µm and sub-10 µm particles are measured at all AMF1 locations by integrating 14 nephelometers (Uin, 2016a). The size range of the SMPS is around 11 – 465 nm with slightly 15 different ranges for different periods. $N_{\rm CCN}$ is measured at different supersaturations, with the 16 details given in Table 1. The supersaturations are typically calibrated before and after each 17 campaign at an altitude similar to measurement site according to the CCN handbook (Uin, 18 2016b). Detailed information about each dataset and measurement site can be found in the AOS 19 handbook (Jefferson, 2011) or ARM web site (http://www.arm.gov/) and references thereby.

20

Ganges Valley (PGH) is located in one of the largest and most rapidly developing sections of the Indian subcontinent. The aerosols in this region have complex sources, including coal combustion; biomass burning; automobile emissions; and dust. In monsoon seasons, dust dominates the aerosol mass due to transportation (Dumka et al., 2017; Gogoi et al., 2015).

25

PVC refers to the on-shore data set for the 'first column' of the Two-Column Aerosol Project
(TCAP) on Cape Cod, Massachusetts, USA. This is a coastal site but also significantly affected
by anthropogenic emissions (Berg et al., 2016).

29

30 MAO refers to Manacapuru in Amazonas, Brazil. It is a relatively clean site where Manaus

pollution plumes and biomass burning plumes impact the background pristine rainforest aerosol
 alternately (e.g., de Sá et al., 2019).

3

Ascension Island (ASI) is located in the southeast Atlantic where westward transport of biomass-burning aerosols from southern Africa may increase aerosol concentrations to high levels. Air mass at this site usually a mixture with aged biomass-burning plume and sea-salt aerosol. The aerosol loading can be very low when there is no pollution plume. In this case, there is a substantial uncertainty on the backscatter fraction.

9

10 The primary purpose of this study is to use as basic and readily accessible measurement data as 11 possible to estimate N_{CCN} . Aerosol optical properties are measured at different cutoff diameters, 12 usually 1 µm, 2.5 µm, 10 µm or TSP. At several stations there are two sets of AOPs using two 13 cutoff diameters. For this study we chose to use AOP data with the 10 µm cutoff (if data for 14 both 10 µm and 1 µm are available) that is more commonly used than smaller cutoff diameters. 15

16 **2.2 Data processing**

17 Regardless of the time resolution of raw data, all the data in this study were adjusted into hourly 18 averages before further analyses. Suspicious data within the whole dataset were removed 19 according to the following criteria:

20

1) for the size distributions, all the data with unexplainable spikes were removed manually;

22 2) for CCN measurements, insufficient water supply may cause underestimation of CCN,

- 23 especially at lower supersaturations (DMT, 2009). N_{CCN} reading at lower SS has a sudden drop
- a few hours before the similar sudden drop for higher SS under such conditions, so data from
 such periods were removed;
- 3) if any obvious inconsistencies between the AOPs and PNSD or between the N_{CCN} and PNSD were found on closure study, all the data in the same hour were removed.
- 28

29 Special treatments were carried out for the ASI dataset. There will inevitably be a considerable

30 uncertainty in the backscattering fraction if the zero point of either σ_{sp} or σ_{bsp} is inaccurate in

1 very clean conditions. The measured σ_{sp} was in agreement with that calculated from the PNSD 2 with the Mie model. However, in the data σ_{bsp} approaches 0.3 Mm⁻¹ whenever σ_{sp} approaches 3 0. Thus, we subtracted from back scattering coefficients a constant 0.3 Mm⁻¹ and no longer used 4 any data points with $\sigma_{sp} < 2$ Mm⁻¹ for this site to assure the data quality.

5

A more detailed description of the total number of available hourly-averaged data, accepted
data and removed data and the fractions of these are presented the supplement S1.

8

9 **2.3 Optical properties calculated from the nephelometer data**

10 The hemispheric backscatter fraction BSF was calculated from

11
$$BSF = \frac{\sigma_{bsp}}{\sigma_{sp}}$$
(1)

where σ_{sp} and σ_{bsp} are the total scattering coefficient and backscattering coefficient, respectively. BSF depends on both particle size and shape. For very small particles, BSF approaches the value of 0.5 and decreases with an increasing particle size (e.g., Wiscombe and Grams, 1976; Horvath et al., 2016; Shen et al., 2018). Jefferson (2010) used BSF as a proxy for the particle size for estimating CCN concentrations from in situ AOP measurements.

17

18 Scattering Ångström exponent (SAE) was calculated from total scattering coefficients σ_{sp} at 19 wavelengths λ_1 and λ_2 from

20
$$SAE = -\frac{\log(\sigma_{sp}(\lambda_1)) - \log(\sigma_{sp}(\lambda_2))}{\log(\lambda_1) - \log(\lambda_2)}$$
(2)

21 For those sites where the TSI 3563 nephelometer was used the wavelength pair was 450 nm 22 and 700 nm, for the Ecotech Aurora-3000 nephelometer the wavelength pair was 450 nm and 23 635 nm. SAE is typically considered to be associated with the dominating particle size. Its large 24 values (e.g. SAE>2) indicate a large contribution of small particles, whereas small values (e.g. 25 SAE<1) indicate a large contribution of large particles. SAE can be retrieved by remoting 26 sensing measurements and it serves as a proxy for particle size for satellite (e.g., Higurashi and 27 Nakajima, 1999; King et al., 1999; Liu et al., 2008) and sunphotometry (e.g., Holben et al., 28 2001; Gobbi et al., 2007) retrieval of aerosol optical properties, even though it is well known that this is just a crude approximation. Many studies found that this relationship is not unambiguous. Surface mean diameter (SMD) and volume mean diameter (VMD) correlate well with SAE while geometric mean diameter (GMD) correlates poorly with SAE according to Schuster et al. (2006), Virkkula et al. (2011) and Shen et al. (2018).

5

6 The reason for calculating both BSF and SAE in the present work is that they provide 7 information on the particle size distribution, yet being sensitive to slightly different particle size 8 ranges (e.g., Andrews et al., 2011; Collaud Coen et al., 2007). A detailed model analysis by 9 Collaud Coen et al., 2007) showed that BSF is more sensitive to small accumulation mode 10 particles, i.e., particles in the size range <400 nm whereas SAE is more sensitive to particles in 11 the size range of 500–800 nm.

12

13 **2.4 Light scattering calculated from the particle number size distributions**

14 Light scattering coefficients (both σ_{sp} and σ_{bsp}) were calculated using the Mie code similar to 15 Bohren and Huffman (1983). The refractive index was set to the average value of 1.517+0.019i 16 reported for SMEAR II by Virkkula et al. (2011). The wavelength for Mie modeling was set to 17550 nm, which is the same as in the measurements. The whole size range of the DMPS or the 18 SMPS, depending on the station, was used. BSF was calculated from (1) by using the modeled 19 σ_{sp} and σ_{bsp} . Both the size range and the selected constant refractive index create uncertainty 20 especially when the modeled scattering is compared with scattering of PM10 aerosols. However, 21the purpose of the modeled scattering was quality control and removal of inconsistent data.

22

23 **2.5 CCN number concentration calculated from the particle number size distribution**

24 The κ -Köhler theory uses a single parameter κ to describe the relationship between 25 hygroscopicity and water vapor saturation (Petters and Kreidenweis, 2007).

26
$$S(D) = \frac{D^3 - D_d^3}{D^3 - D_d^3(1 - \kappa)} exp\left(\frac{4\sigma_{s/a}M_w}{RT\rho_W D}\right)$$
(3)

Here *S*(D) is water vapor saturation, which equals to SS+100%, *D* is the diameter of the wet particle, D_d is particle dry diameter and κ is the hygroscopicity parameter. The rest of the

1 coefficients are usually set to constant, for instance in this study, $\sigma_{s/a} = 0.072 \text{ J/m}^2$ is the surface 2 tension of the solution/air interface, R = 8.314 J/mol is the universal gas constant, T = 298K is 3 temperature, $\rho_w = 1000 \text{kg/m}^3$ is the density of water, $M_w = 0.018 \text{kg/mol}$ is the molecular weight of water. At given κ and D_d , S(D) is a function of the wet diameter D, which is physically larger 4 5 than D_d . As a combination of the Kelvin effect and the Raoult effect, S(D) first increases and 6 then decreases as D increases, and there is a maximum value for S(D) in the S-D curve. Here, 7 we call the maximum value of S(D) and corresponding D as $S(D)_{max}$ and D_{max} respectively. 8 Physically, if $S(D)_{max}$ larger than the SS of the environment, the dry particle will reach a wet 9 diameter D between D_d and D_{max} ; while if $S(D)_{max}$ is smaller than the SS of the environment the 10 dry particle can grow to infinite sizes, which means it is a so-called activated particle. S(D)max 11 decreases monotonically as D_d increases. Thus we can iterate D_d until $S(D)_{max}$ equals to a given 12 SS. We call this D_d the critical diameter D_m . Particles with $D_d > D_m$ their $S(D)_{max} < SS$ and they 13 can be activated while the smaller particles cannot.

14

Under the assumption of fully internally mixed particles, the CCN number concentration calculated from the particle number size distributions ($N_{CCN}(PNSD)$) is obtained by integrating the PNSD of particles larger than the critical dry particle diameter (D_m):

18
$$N_{CCN}(PNSD) = \int_{D_m}^{\infty} n(\log D_p) d\log D_p$$
(4)

19 at a given SS. All particles with a diameter larger than D_m can act as CCN. We calculated 20 $N_{CCN}(PNSD)$ at the supersaturations at which CCN were measured in the different stations (e.g., 21 0.1%, 0.2%, 0.3%, 0.5% and 1.0% for SMEAR II).

22

The accuracy of $N_{\text{CCN}}(\text{PNSD})$ is affected by the treatment of κ . In this study, we are not trying to achieve an accurate value of κ but instead want to illustrate that even an arbitrary setting of κ can yield reasonable CCN concentrations. This approach is named as 'unknown chemical approach' in (Kammermann et al., 2010) and as 'Prediction of N_{CCN} from the constant κ ' in Meng et al., (2014). Both of them give a detailed discussion of how this approach performs. Arbitrary κ is not performing as good as a proper κ when calculating N_{CCN} , yet we believe that it is good enough to be an alternative to measuring CCN in the empirical estimation of this study. Wang et al. (2010) also claimed that $N_{\text{CCN}}(\text{PNSD})$ may be successfully obtained by assuming an internal mixture and using bulk composition few hours after emissions. For SORPES, ASI and PVC, we simply set a global-average value of 0.27 for κ (Pringle et al., 2010; Kerminen et al., 2012). For the forest sites, SMEAR II and MAO, we set $\kappa = 0.12$, which is close to the value of κ for Aitken mode particles reported previously by studies at forest sites (Sihto et al., 2011; Hong et al., 2014). Here we used $N_{\text{CCN}}(\text{PNSD})$ for quality control and removal of inconsistent data.

8

9 2.6 Aerosol optical properties and CCN concentrations of simulated size distributions

10 For studying the relationships of particle size, N_{CCN} and AOPs, we generated unimodal particle 11 number size distributions n(GMD,GSD) with varying the geometric mean diameter (GMD) and 12 geometric standard deviation (GSD). For them we calculated the same AOPs with the Mie 13 model as were obtained from the real measurements from the stations σ_{sp} and σ_{bsp} and from 14 these the BSF at the wavelengths $\lambda = 550$ nm. N_{CCN} was calculated simply by integrating 15 number concentrations of particles larger than a critical diameter of 50 nm, 80 nm, 90 nm, 100 16 nm, and 110 nm, and 150 nm. When the global average hygroscopicity parameter $\kappa = 0.27$ is 17used this corresponds to a SS range of $\sim 0.14\% - 0.74\%$.

18

19 Using a unimodal size distribution for the simulation is an approximation. In the boundary layer, 20 particle number size distributions consist typically of an Aitken mode in the size range of ~25 21 -100 nm, an accumulation mode in the size range of 100 - 500 nm and, following atmospheric 22 new particle formation, also a nucleation mode in the size range of < 25 nm (e.g., Dal Maso et 23 al., 2005; Herrmann et al., 2015; Qi et al., 2015). While the particle number concentration is 24 dominated by the smaller modes, essentially all light scattering is due to the accumulation mode 25 and also coarse particles in the range of $1 - 10 \,\mu\text{m}$. For example, at SMEAR II the average 26 contribution of particles smaller than 100 nm to total scattering was ~ 0.2 % and even at the end 27 of new particle formation events it was no more than ~2% (Virkkula et al., 2011). Also most of 28 the CCN are in the accumulation mode size range, especially at low supersaturations (SS <29 0.2%); at higher SS also Aitken mode particles contribute to CCN (Sihto et al., 2011).

1 **3.** Relationships between *N*_{CCN} and AOPs

We first present general observations of the $N_{\rm CCN}$ and AOPs at all the six sites and investigate in more detail data from SMEAR II. Based on the relationships of AOPs and $N_{\rm CCN}$ at SMEAR II, we further use data from all the stations and develop a simple and general combined parameterization for estimating $N_{\rm CCN}$.

6

7 **3.1 Site-dependent** *N*_{CCN} - **AOP** relationships

8 The averages of AOPs of PM_{10} particles and N_{CCN} at four supersaturations during the analyzed 9 period for each site are presented in Table 2. In general all of them are cleaner than SORPES 10 and more polluted than SMEAR II, based on the average values of $\sigma_{\rm sp}$. The average values of 11 $N_{\rm CCN}$ are obviously higher in more polluted air as well as can be seen in the values presented in 12 Table 2. The dependence of $N_{\rm CCN}$ on SS is shown by plotting the averages of the measured N_{CCN} 13 at the six sites at the station-specific supersaturations of the CCN counters (Fig. 1). In all these 14 different types of environments a logarithmic function fits better to the data than the power 15 function $N_{\text{CCN}}(\text{SS}) = C \times (\text{SS})^k$. It is not a new observation that the power function is not perfect 16 for describing the $N_{\rm CCN}$ vs. SS relationship. Also other function types have been used in the 17 literature, for instance a product of the power function and the hypergeometric function (Cohard 18 et al., 1998; Pinsky et al., 2012), an exponential function (Ji and Shaw, 1998; Mircea et al., 19 2005; Deng et al., 2013) and the error function (e.g., Dusek et al., 2003 and 2006b; Pöhlker et 20 al., 2016). In the following analysis of the relationships between $N_{\rm CCN}$, AOPs and SS we will 21 use logarithmic fittings to the data without any theoretical reasoning.

22

Since there is obviously a positive correlation between the averages of $N_{\rm CCN}$ and $\sigma_{\rm sp}$ in Table 2, it is reasonable to study whether this is true also for the hourly-averaged data. A scatter plot shows that the correlation between $N_{\rm CCN}$ and $\sigma_{\rm sp}$ was weak at SMEAR II, especially for higher supersaturations (Fig 2). In spite of this, when the scatter plots are color-coded with respect to BSF, the relationship between $N_{\rm CCN}$ and $\sigma_{\rm sp}$ becomes clear: $N_{\rm CCN}$ grows almost linearly as a function of $\sigma_{\rm sp}$ for a narrow range of values of BSF. This indicates BSF can serve as a good proxy for describing the ratio between $N_{\rm CCN}$ and $\sigma_{\rm sp}$.

Hereafter, we will use the term $R_{CCN/\sigma} = N_{CCN}/\sigma_{sp}$ to describe the relationship between N_{CCN} and σ_{sp} , similar to Liu and Li (2014). Note that this same ratio was defined as AR_{scat} in Tao et al. (2018). $R_{CCN/\sigma}$ varies over a wide range of values, so a proper parameterization to describe it is of significance.

5

6 The first step in the development of the parameterization was to calculate linear regressions of 7 $R_{CCN/\sigma}$ vs BSF. $R_{CCN/\sigma}$ depends clearly on BSF (Fig. 3) as

$$\mathbf{R}_{\mathrm{CCN/\sigma}} = a \, \mathrm{BSF} + b \tag{5}$$

9 The correlation between BSF and $R_{CCN/\sigma}$ is strong when $\sigma_{sp} > 10 \text{ Mm}^{-1}$. At $\sigma_{sp} < 10 \text{ Mm}^{-1}$ the 10 uncertainty of the nephelometer is higher, which may at least partly explain the lower 11 correlation. Based on this we used $\sigma_{sp} > 10 \text{ Mm}^{-1}$ as the criterium for the data fitting.

12

Linear regressions of $R_{CCN/\sigma}$ vs BSF were applied to data from all the analyzed stations. For each dataset and individual supersaturation, *a* and *b*, i.e. the slope and offset of the linear regression, haves different value as presented in Table 3. The calculation of *a* and *b* are based on data with $\sigma_{sp} > 10 \text{ Mm}^{-1}$ only. The following discussion is based on the ordinary linear regression (OLR). In addition, we repeated the calculations with the Reduced Major Axis (RMA) regression, see supplement S2.

19

The parameterization gives the formula for calculating $N_{\text{CCN}}(\text{AOP})$, ie, N_{CCN} calculated from measurements of AOPs:

$$N_{\rm CCN}(\rm AOP_1) = (a_{\rm SS}BSF + b_{\rm SS}) \cdot \sigma_{\rm sp} \tag{6}$$

23 The subscript 1 for AOP₁ indicates the first set of parameterization.

24

Scatter plots of $N_{\text{CCN}}(\text{AOP}_1)$ vs $N_{\text{CCN}}(\text{meas})$ are presented for two supersaturations, high and low, at the six stations (Fig. 4). The correlation coefficient R^2 between $N_{\text{CCN}}(\text{AOP}_1)$ and $N_{\text{CCN}}(\text{meas})$ is higher at lower supersaturations than that at higher supersaturations in most of the scatter plots shown in Fig. 4. A reasonable explanation for this is that the higher the supersaturation is, the smaller are the particles that can act as CCN. And further, the smaller the particles are, the less they contribute to both total scattering and backscattering and the higher 1 is the relative uncertainty of both of them and thus also the uncertainty of $N_{\rm CCN}(\rm AOP_1)$.

2

3 3.2 Site-independent relationships between N_{CCN}, AOPs and supersaturations

The relationships between $N_{\rm CCN}$ and AOPs are obviously different for each site and 4 5 supersaturation. We next try to find a way to combine them into a site-independent form. First, 6 the slopes and offsets obtained from the linear regression (Table 3) were plotted as a function 7 of SS (Fig 5). The data obviously depend logarithmically on SS, so that (6) becomes

8
$$N_{CCN}(AOP_2) = (a_{ss}BSF + b_{ss})\sigma_{sp} = ((a_1 \ln(SS) + a_0)BSF + b_1 \ln(SS) + b_0)\sigma_{sp}$$
(7)

9 The coefficients a_0 , a_1 , b_0 and b_1 obtained from the regression of $a_{SS} = a_1 \ln(SS) + a_0$ and $b_{SS} =$ 10 $b_1 \ln(SS) + b_0$ vs. the supersaturations SS for each station are presented in Table 4.

11

12 Note that also a power function of SS of the form SS^k was used for fitting the data (Fig 5). This 13is the dependence on SS assumed for instance in the parameterization by Jefferson (2010). It is 14 obvious that the power function fitting is not as good as the logarithm of SS. This is in line with 15 the fittings to N_{CCN} vs. SS (Fig. 1) and the related discussion in section 3.1.

16

17 The relationships of the coefficients in Table 4 are next used to get a combined, more general 18 parameterization. Obviously the a_0 vs. a_1 , b_0 vs. b_1 , a_1 vs. b_1 and b_0 vs. b_0 pairs from all stations 19 follow very accurately the same lines (Fig 6). Linear regressions yielding $a_0 = (2.38 \pm 0.06)a_1$, $b_0 = (2.33 \pm 0.03)b_1$, and $b_1 = (-0.096 \pm 0.013)a_1 + (6.0 \pm 5.9)$ were used, after the simple algebra 20

21in the supplement S3, to get

$$N_{CCN}(AOP_2) \approx \left(\ln(SS) + (2.38 \pm 0.06) \right) \left(a_1(BSF - (0.096 \pm 0.013)) + (6.0 \pm 5.9) \right) \sigma_{sp}$$
$$\approx \ln \left(\frac{SS}{0.093 \pm 0.006} \right) \left(a_1(BSF - (0.096 \pm 0.013)) + (6.0 \pm 5.9) \right) \sigma_{sp}$$

(8)

where both the coefficient a_1 and the constant 6.0 ± 5.9 have units of $[N_{\rm CCN}]/[\sigma_{\rm sp}] = \text{cm}^{-3}/\text{Mm}^{-1}$. 23 24 This is the general formula for the parameterization. In both (7) and (8) the only unquantified 25 coefficient is now a₁. However, we can find some ways to quantify also it.

26

27 The above derivation of the combined parameterization by using the logarithms of SS was fairly 28 straightforward. In the error-function parameterizations of Dusek et al. (2003) and Pöhlker et

1 al. (2016) there are adjustable parameters that affect the argument of the error function. In the 2 parameterization of Ji and Shaw (1998) there is an exponential function where the argument 3 contains the power function of SS and the parameterization of by Cohard et al. (1998) is a 4 product of the power function and the hypergeometric function. If these functions were used 5 for fitting the N_{CCN}(AOP, SS) data it would be would be more complicated to combine the site-6 dependent parameterizations into a general equation analogous to Eq. (8). The simplicity of the 7 logarithmic fitting makes it most suitable for our approach. The disadvantage of Eq. (8) is that 8 it predicts no upper limit for N_{CCN} at high supersaturations. This is not correct since N_{CCN} cannot 9 be larger than the total particle number concentration and therefore it has to be emphasized that 10 the parameterization presented here is only valid in the range of SS < 1.1%.

11

For a given station, if there are simultaneous data of $N_{\text{CCN}}(\text{meas})$ and σ_{sp} for some reasonably long period, (8) can be adjusted. To estimate what is a reasonably long period, we added an analysis in the supplement S5. It shows that when the number of hourly samples is > ~1000, the uncertainty in BSF_{min} is low enough. Instead of subtracting (0.096 ± 0.013) from BSF, the minimum BSF = BSF_{min} in the data set will be used. Further, when BSF = BSF_{min} the factor $a_1(\text{BSF}-\text{BSF}_{\text{min}}) = 0$ and $N_{\text{CCN}}(\text{AOP}_2) \approx R_{\text{min}} \cdot \sigma_{\text{sp}}$ where R_{min} is the minimum $R_{\text{CCN}/\sigma}$ in the data set. It follows that

19
$$N_{CCN}(AOP_2) \approx \left(a_1 \ln\left(\frac{SS}{0.093 \pm 0.006}\right)(BSF - BSF_{\min}) + R_{\min}\right)\sigma_{sp}$$
(9)

The derivation of (9) is shown in the supplement S4. In the data processing the 1st percentiles of both BSF and $R_{\text{CCN/}\sigma}$ are used as BSF_{min} and R_{min} , respectively. Here the free parameters are a_1 , BSF_{min} and R_{min} .

23

The coefficient a_1 is positively correlated with SAE. The linear regressions of a_1 and the average and median scattering Ångström exponent of PM₁₀ particles (SAE) (Table 4) at the 6 sites in the analyzed periods yield $a_1 \approx (298 \pm 51)$ SAE cm⁻³/Mm⁻¹ and $a_1 \approx (286 \pm 46)$ SAE cm⁻³/Mm⁻¹, respectively (Fig. 7). The uncertainties are large, but the main point is that the correlations show that a_1 and thus $N_{CCN}(AOP_2)$ is higher for higher values of SAE. If we consider the a_1 values in Table 4 as the accurate station-specific values, then using $a_1 = 286$ ·SAE overestimates or 1 underestimates a_1 by +37%, +30%, -20%, -32%, -20% and +251% for SMEAR II, SORPES, 2 PGH, PVC, MAO and ASI, respectively. These values were calculated from 100%(286·SAE – 3 $a_1)/a_1$. The effect of the biases of a_1 to the biases of N_{CCN}(AOP₂) are discussed in more detail in 4 the supplement S6. Nevertheless, we found that SAE is the only parameter that is positively 5 correlated with a_1 and that can easily be obtained from nephelometer measurements. Searching 6 for a more suitable proxy for a_1 would be an important part of follow up studies.

7

8 R_{\min} of (9) was estimated by calculating the 1st percentile of $R_{CCN/\sigma}$ at each site at each SS. The 9 average and standard deviation of R_{\min} was 5.2 ± 3.3 cm⁻³/Mm⁻¹. Consequently, the 10 parameterization becomes

 $N_{CCN}(AOP_2) \approx \left((286 \pm 46) \text{SAE} \cdot \ln \left(\frac{\text{SS}}{0.093 \pm 0.006} \right) (BSF - BSF_{\min}) + (5.2 \pm 3.3) \right) \sigma_{sp}$ (10)

12 The parameterization suggests that at any supersaturation and constant scattering coefficient, 13 N_{CCN} is the higher the smaller the particles are because both SAE and BSF are roughly inversely 14 correlated with the particle size. A qualitative explanation to this is that to keep σ_{sp} constant 15 even if the dominating particle size decreases – which means that both SAE and BSF increase 16 - the number of particles has to increase. The analysis also shows that neither SAE nor BSF 17 alone is enough for obtaining a good estimate of $N_{\rm CCN}$ from AOP measurements. This is again 18 in line with the model study of Collaud Coen et al. (2007) which showed that SAE and BSF are 19 sensitive to variations in somewhat different size ranges.

20

21 The parameterization in Eq (10) was applied to the data of the 6 stations and $N_{CCN}(AOP_2)$ was 22 compared with the $N_{\rm CCN}$ (meas) at the supersaturations used in the respective CCN counters. 23 The results are presented as scatter plots of $N_{CCN}(AOP_2)$ vs. $N_{CCN}(meas)$ (Fig 8a and 8b), the 24 bias of the parameterization calculated as $N_{\rm CCN}(\rm AOP_2)/N_{\rm CCN}(\rm meas)$ (Fig 8c) and the squared 25 correlation coefficient R^2 of the linear regression of $N_{\text{CCN}}(\text{AOP}_2)$ vs. $N_{\text{CCN}}(\text{meas})$ (Fig 8d). The 26 $N_{\rm CCN}(\rm AOP_2)$ values used for the statistics shown in Fig. 8 were calculated by using the SAE of 27 hourly-averaged scattering coefficients. The problem with that is that when SAE < 0 it is very 28 probable that also $N_{\text{CCN}}(\text{AOP}_2)$ is negative if BSF > BSF_{min}, as can be seen from Eq. (10). For 29 this reason the data with SAE < 0 were not used. The fraction of negative SAE hourly values

1 varied from 0.0% at SMEAR II and SORPES to 6% at MAO (Supplement S6, Table TS3). To 2 reduce the number of rejected data, we also calculated $N_{CCN}(AOP_2)$ by using the site-specific 3 median SAE shown in Table 4 and the hourly BSF values. The results are shown in the 4 supplement S6.

5

6 At the site-specific lowest values of SS, the scatter plots of $N_{CCN}(AOP_2)$ vs. $N_{CCN}(meas)$ of data 7 from most stations clustered along the 1:1 line, but for the Himalayan site PGH the 8 parameterization yielded significantly higher concentrations (Fig 8a). The bias varied from 0.7 9 to > 4 (Fig 8c) (Table TS3). At PGH at the lowest SS, the bias was > 4 but decreased to ~ 1.1 -10 1.2 at SS = 0.4% and even closer to 1 at higher SS. At SS > 0.4%, the average bias varied 11 between ~0.7 and ~1.3, which means N_{CCN} was estimated with an average uncertainty of 12 approximately 30% by using nephelometer data. For ASI the bias was higher, in the range of 13 \sim 1.4 – 1.9. For the US coastal site PVC, the parameterization constantly underestimated the CCN concentrations by about 30%. Since $N_{CCN}(AOP_2) \approx (a_1 \ln(SS/0.093)(BSF - BSF_{min}) +$ 14 15 R_{min}) σ_{sp} , it is obvious that biases of a_1 affect the bias of N_{CCN}(AOP₂). As it was written above, 16 the parameterization of $a_1 = 286$ SAE overestimates or underestimates a_1 . For most stations the 17bias of N_{CCN}(AOP₂) can be explained by the bias of a_1 : when a_1 is underestimated so is 18 $N_{CCN}(AOP_2)$, and when a_1 is overestimated so is $N_{CCN}(AOP_2)$. A detailed analysis of the effect 19 of the bias of a_1 on the bias of N_{CCN}(AOP₂) is presented in the supplement S6.

20

The correlation coefficient of $N_{\text{CCN}}(\text{AOP}_2)$ vs. $N_{\text{CCN}}(\text{meas})$ is higher at higher CCN concentrations (not shown in the figure). One possible reason for this is that when CCN concentration is lower, the aerosol loading is usually lower and also the relative uncertainties of both N_{CCN} and AOPs are higher than at high concentrations.

25

1 4. Analyses of size distribution effects on N_{CCN}-AOP relationships

Below we will first present effects of simulated size distributions on the relationships between N_{CCN} and aerosol optical properties and then compare the simulations with field data.

4

5

4.1 N_{CCN}–AOP relationships of simulated particle size distributions

We generated lognormal unimodal size distributions as explained in section 2.6. GMD was
given logarithmically evenly-spaced values from 50 nm to 1600 nm and GSD was given two
values: 1.5 representing a relatively narrow size distribution and 2.0 a wide size distribution.
We then calculated AOPs, N_{CCN} and R_{CCN/σ} for these size distributions.

10

11 The reasoning for the approach of estimating N_{CCN} from σ_{sp} and BSF can easily be explained 12 by the qualitatively similar variations of $R_{CCN/\sigma}$ and BSF as function of GMD (Fig. 9). $R_{CCN/\sigma}$ is 13 the highest for the smallest particles, i.e. for GMD = 50 nm and it decreases with an increasing 14 GMD as also BSF. Note that the width of the size distribution has very strong effects on R_{CCN/σ}: 15 for the wide size distribution it is approximately an order of magnitude lower than for the 16 narrow size distribution. Note also that the values of $R_{CCN/\sigma}$ of the wide size distributions are 17plotted twice (Fig. 9a): the black symbols and line use the left axis to emphasize the big 18 difference in the magnitudes of the wide and narrow size distributions; the red symbols and line 19 use the right axis to show that the shape of the $R_{CCN/\sigma}$ size distribution is very similar to the one 20 calculated for the narrow size distributions. The simulation also shows a potential source of 21 uncertainty of the method: in the GMD range of \sim 500 – 800 nm, the BSF of the narrow size 22 distribution actually increases, although very little with an increasing value of GMD (Fig. 9b). 23 This phenomenon is due to Mie scattering and it is even stronger for single particles. When the 24 size parameter $x = \pi D_p / \lambda$ of non-absorbing and weakly-absorbing spherical particles grows 25 from ~3 to ~8, their BSF increases and then decreases again as can be shown by Mie modeling 26 (Wiscombe and Grams, 1976). For the wavelength $\lambda = 550$ nm this corresponds to a particle 27 diameter range of ~525 to ~1400 nm.

28

29 The decrease of $R_{CCN/\sigma}$ and BSF with the increasing GMD was used for estimating particle sizes

1 with a stepwise linear regression. An example is given by the linear regressions of $R_{CCN/\sigma}$ vs. 2 BSF calculated for 5 consecutive size distributions, first for those that have their GMDs from 3 50 nm to 100 nm and the second for those that have their GMDs from 100 nm to 200 nm (Fig. 10). Note that it is obvious that linear regressions are applicable for short intervals but not well 4 for the whole size range. It is also obvious that an exponential fit would be perfect to explain 5 6 the relationship between $R_{CCN/\sigma}$ and BSF. But this is not what we are looking for. We are looking for the slopes and offsets in the relationship $R_{CCN/\sigma} = aBSF + b$ that was used for fitting 7 8 the field measurement data. So, physically it would mean that N_{CCN} would increase linearly as 9 a function of BSF even though this is not exactly correct.

10

11 The absolute values of the slopes and offsets are clearly lower for the larger particle size range. 12 Here, we define the particle size used for describing the size range of each regression as the 13 equivalent geometric mean diameter GMD_e, the geometric mean of the range of the GMDs of 14 the unimodal size distributions used for each regression. other In words, $GMD_e = \sqrt{GMD_{low}GMD_{high}}$, where GMD_{low} and GMD_{high} are the smallest GMD and the largest 15 16 GMD of the range, respectively. Two examples of the regressions were given above, one 17 calculated for the GMD range from 50 nm to 100 nm and the other for the GMD range from 18 100 nm to 200 nm. The GMDes of these two size ranges are 70.7 nm and 141.4 nm, respectively. 19 It will be shown below that GMD_e is a mathematical concept that helps to explain the observed 20 relationships, not an actual GMD of the particle size distribution at the sites.

21

For a wide size distribution, the slopes and offsets of the regressions of $R_{CCN/\sigma}$ vs. BSF decrease and increase, respectively, monotonically with an increasing value of GMD_e in the whole size range studied here (Fig. 11). For a narrow size distribution, the slope decreases until GMD_e \approx 300 nm and then increases, which means that there is no unambiguous relationship between them. The reason is, as discussed above related to Fig 9b, that in the GMD range of ~500 – 800 nm the BSF of narrow size distributions increases slightly with an increasing GMD.

28

29 Note also that the ranges of the absolute values of the slopes and offsets of the narrow and wide

size distributions are very different. For instance, when $GMD_e = 100 \text{ nm}$ the slope $a \approx 4000 \text{ cm}^{-3}/\text{Mm}^{-1}$ and $a \approx 1600 \text{ cm}^{-3}/\text{Mm}^{-1}$ for the narrow and wide size distribution, respectively. Since $N_{CCN}(AOP) = R_{CCN/\sigma} \cdot \sigma_{sp} = (aBSF + b)\sigma_{sp}$ this means that the $N_{CCN}(AOP)$ of narrow size distributions is more sensitive to variations in mean particle size than the $N_{CCN}(AOP)$ of wide size distributions.

6

We plotted the offset vs. slope of the unimodal size distributions and those obtained from the linear regressions of the field data at the supersaturatios presented in Table 3 and below it the GMD_e vs. the slopes of the regressions of the unimodal size distributions (Fig 12). In Fig. 12 also the effect of the choice of the activation diameters of 50 nm, 80 nm, 110 nm, and 150 nm is shown.

12

13 Several observations can be made in Fig. 12. First, for the simulated wide size distributions the 14 relationship between the offset and slope is unambiguous, while this is not the case for the 15 narrow size distributions at sizes $GMD_e > \sim 200$ nm (Fig 12b). Second, the field data points roughly follow the lines of the simulations. This suggests that the slopes and offsets of the linear 16 regressions of $R_{CCN/\sigma}$ vs. BSF yield information on the dominating particle sizes just as they do 17 18 for the simulated size distributions. For instance, the PVC data point corresponding to the 19 highest supersaturation has the highest slope (1970 cm⁻³/Mm⁻³, Table 3) and it is close to the 20 wide size distribution line with the activation diameter of 50 nm (Fig. 12a). This corresponds 21 to the GMD_e of ~150 nm (Fig. 12b). The SMEAR II high SS offset vs. slope fits best with the 22 corresponding lines of the narrow unimodal size distributions with activation diameters in the 23 range of $\sim 50 - 110$ nm and the corresponding GMD_e $\approx 150 - 200$ nm.

24

At the lowest SS, the offset vs. slope points of all stations agree well with the lines derived from the unimodal modes. This is actually in line with the higher correlation coefficients (\mathbb{R}^2) of the regressions of N_{CCN} (AOP₁) vs. N_{CCN} (meas) at the lowest SS (Fig. 4). This can be explained by that at low SS small particles do not get activated and unimodal size distributions in the accumulation mode are mainly responsible for CCN. For ASI the slopes and offsets of the lowest and highest SS are especially close to each other, closer than at any other station (Fig. 1 12a), and the corresponding $GMD_e \approx 750$ nm and 400 nm, respectively, when the GMD_e vs. a 2 relationship of any of the distributions is used (Fig. 12b). This is in line with that ASI is an 3 island site dominated by marine aerosols. For PGH at the lowest SS, the slope is actually 4 negative which is not obtained from the simulations at all so no GMD_e can be given for it.

5

6 **4.2 Aerosol size characteristics of the sites**

As it was shown above, particle size distributions affect the relationships between N_{CCN} and AOPs. It is therefore discussed here how the size distributions vary at the six sites of the study and whether they support the interpretations presented above. The size distributions are discussed using the particle number size distribution data and the ratios of σ_{sp} of PM₁ and PM₁₀ size ranges from those stations where they are available.

12

13 **4.2.1 Diurnal variation of particle number size distribution**

Fig. 13a shows the averaged diurnal cycle of PNSD at the sites where either a DMPS or SMPS is available. New particle formation (NPF) events are a significant source of uncertainty in the prediction of N_{CCN} (Kerminen et al., 2012; Ma et al., 2016). Complete NPF events start from a burst of sub-10 nm particles followed by a continuous growth up to a few hundred nanometers. As a result, the size distribution varies significantly. NPF is one possible explanation of the poor N_{CCN} - σ_{sp} correlation.

20

21 SMEAR II and SORPES are reported to have an appreciable frequency of NPF (Kulmala et al., 22 2004; Dal Maso et al., 2005; Sihto et al., 2006; Qi et al., 2015). A continuous growth of particle 23 size at SORPES can usually last for several days after NPF (Shen et al. 2018). Similar growth 24 patterns have also been observed in the Two-Column Aerosol Project (TCAP; 25 http://campaign.arm.gov/tcap/; refers as PVC in this study) according to Kassianov et al. (2014). 26 NPF is rarely observed in the Amazon forest, as reported by Wang et al. (2016). However, it 27does take place at MAO as is shown in the diurnal cycle of PNSD. The reason is probably that 28 the MAO site was measuring aerosol downwind of the City Manaus. At ASI, there no evidence 29 of NPF according to the PNSD diurnal cycle.

These observations of the NPF are compared with the bias and correlation coefficients of the parameterization discussed in section 4.1 (Fig. 8). The correlation coefficient of N_{CCN} (AOP₂) vs. N_{CCN} (meas) is the highest, $\mathbb{R}^2 > 0.85$ at all SS at ASI where no NPF takes place and clearly lower at the other sites (Fig 8d). For the bias NPF appears not to have a clear influence: for both SMEAR II and SORPES bias varies from ~1.1 to ~1.4 at SS > 0.1%. As it was stated above (section 3.2), for most stations the bias of $N_{\text{CCN}}(\text{AOP}_2)$ can be explained by the bias of a_1 in $N_{\text{CCN}}(\text{AOP}_2) \approx (a_1 \ln(\text{SS}/0.093)(\text{BSF} - \text{BSF}_{min}) + \mathbb{R}_{min})\sigma_{\text{sp}}$.

8

9 4.2.2 Distributions of geometric mean diameters

10 Figure 13b presents the normalized distributions of the geometric mean diameters at SMEAR II, SORPES, PVC, MAO and ASI. They vary from 20 nm to 200 nm at all sites, with the most 11 12 frequent GMD between \sim 70 nm and \sim 120 nm depending on the site. This shows clearly that 13 the above-presented equivalent geometric mean diameter GMD_e calculated assuming a 14 unimodal size distribution is not a quantitative GMD of the size distribution, it is a mathematical 15 concept that explains partially the relationships of $R_{CCN/\sigma}$ and BSF. However, the GMD of the 16 measured size distribution and GMD_e are not quite comparable also for another reason. The 17 simulations were made by using unimodal size distributions, so that GMDe varied in the range 18 70 nm - 1100 nm (Fig. 11) while the GMDs were calculated from DMPS and SMPS data that 19 also contained the nucleation and Aitken modes that often dominate the total particle number 20 concentration.

21

The frequency distribution of GMD at SMEAR II is the widest among the five sites with PNSD data available, followed by SORPES and PVC. At MAO the frequency distribution of GMD has two peaks in this study. The lower peak is possibly due to the burst of sub-20 nm particles, since these these particles have little chance to grow to sizes where they can serve as CCN. The second peak at around 100 nm possibly represents the GMD without the burst of sub-20 nm particles and it is distinctly narrower than at SMEAR II, SORPES and PVC.

28

A comparison of the correlation coefficients of N_{CCN} (AOP₂) vs. N_{CCN} (meas) (Fig. 8d) and the widths of the GMD frequency distributions (Fig. 13b) do not show any clear relationships, except in ASI. The frequency distribution of GMD is the narrowest at ASI, indicating that the average particle size does not change much throughout the whole period. This is in line with the low variation of the slope and offset of the R_{CCN} vs BSF of ASI (Fig 12a). At ASI also the correlation coefficient of N_{CCN} (AOP₂) vs. N_{CCN} (meas) is the highest, R² ≈ 0.8 at all SS.

5

6 **4.3.3 Contribution of light scattering by sub-μm particles**

7 There is one more measure related to particle size distribution, the ratio between σ_{sp} of sub-1 8 μ m and sub-10 μ m aerosol ($\sigma_{sp}(PM_1)/\sigma_{sp}(PM_{10})$). At SMEAR II, the contribution of submicron 9 particles usually varies within a range of $\sim 0.8 \sim 0.9$ and it is the highest among all sites in this 10 study. PVC has two peaks in the $\sigma_{sp}(PM_1)/\sigma_{sp}(PM_{10})$ distribution, the peak around 0.2 corresponding to air masses from the sea, with a very low scattering coefficient and $N_{\rm CCN}$. By 11 12 ignoring the cleanest air masses (σ_{sp} <5 Mm⁻¹), the fraction of σ_{sp} (PM₁)/ σ_{sp} (PM₁₀) is usually 13 around 0.8, which is just slightly lower than at SMEAR II. At PGH and MAO, the distribution 14 of the ratio is wider, and the peak position is at about 0.65. The overall contribution of sub-µm 15 particle light scattering at PGH is moderate among the sites in this study. At ASI, 16 $\sigma_{sp}(PM_1)/\sigma_{sp}(PM_{10})$ is the lowest among all sites in this study, indicating that particles larger 17than 1 µm contribute a considerable fraction of total light scattering. For SORPES 18 $\sigma_{sp}(PM_1)/\sigma_{sp}(PM_{10})$ is not available.

19

20 Among those five sites, when $\sigma_{sp}(PM_1)/\sigma_{sp}(PM_{10})$ decreases, the correlation between BSF and 21 $R_{CCN/\sigma}$ decreases (not shown in a scatter plot). At some sites (e.g., ASI) the BSF of PM₁₀ is often 22 even larger than that of PM_1 , which can be an error in the measurements but it may also be due 23 to a real phenomenon. As discussed in section 4.1, for single spherical particles Mie modeling 24 shows that in the particle diameter range of ~525 to ~1400 nm BSF increases with an increasing 25 D_b. Mugnai and Wiscombe (1986) simulated scattering by non-spherical particles and found 26 that BSF increases when the size parameter x grows from ~ 8 to ~ 15 , which corresponds to the 27particle diameter range of ~1400 nm to ~2600 nm at $\lambda = 550$ nm. Therefore it is obvious that 28 large and non-spherical particles like sea salt and dust will blur the correlation between BSF 29 and R_{CCN/o}. In such a case the increase in the amount of large particles sometimes leads to an

1 increase of BSF and a decrease of $R_{CCN/\sigma}$, which is opposite to the usual positive correlation 2 between BSF and $R_{CCN/\sigma}$ in this study. This may be at least part of the explanation of the highest 3 bias at high values of SS in ASI (Fig 8c), the site dominated by marine aerosol. Thus, the lower 4 $\sigma_{sp}(PM_1)/\sigma_{sp}(PM_{10})$ may in principle result in a poor performance of our method. However, a comparison of the correlation coefficients and the $\sigma_{sp}(PM_1)/\sigma_{sp}(PM_{10})$ frequency distributions 5 of each site shows the opposite. At the highest SS of each site, the R^2 in a decreasing order is 6 7 ASI, PGH, MAO, SORPES, SMEAR II, and PVC (Fig. 8d). The peaks, i.e. modes of the 8 frequency distribution of $\sigma_{sp}(PM_1)/\sigma_{sp}(PM_{10})$ are, in a growing order, ASI: 0.375, PGH: 0.625, 9 MAO: 0.65, PVC: 0.825, SMEAR II: 0.875. Note that at SORPES there is only one size range 10 measured. Of these the R² of only PVC and SMEAR II are not in the same order (Fig 8d). This 11 suggests that $N_{\rm CCN}$ can be estimated better from the aerosol optical properties for sites 12 dominated by large particles than for sites dominated by small particles. This further suggests 13 that the ambient size distributions were so wide that the non-monotonous relationship between 14 particle size and BSF discussed above did not play an important role. On the other hand, the 15 bias at the highest SS has no clear relationship with $\sigma_{sp}(PM_1)/\sigma_{sp}(PM_{10})$.

16

There is also an additional observation that can be made. The above-mentioned order of the modes of the frequency distribution of $\sigma_{sp}(PM_1)/\sigma_{sp}(PM_{10})$ is almost the same as the order of the slopes and offsets and GMD_es in Fig. 12. Only for SMEAR II and PVC the order is not the same. This further supports the interpretation that the slopes and offsets of the linear regression of R_{CCN} vs BSF depend on the dominating particle size of particle size distribution.

- 22
- 23
- 24

25 **5. Conclusions**

The relationships between aerosol optical properties, CCN number concentrations (N_{CCN}) and particle number size distributions were investigated based on in-situ measurement data from six stations in very different environments around the world. The goals were to find physical explanations of the relationships and to find a parametrization to obtain N_{CCN} from sites where AOPs are measured but no CCN counter is available. There are many previous parameterizations for doing just the same. As a starting point we used the parameterization presented by Jefferson (2010). That one needs also absorption measurements since it includes single-scattering albedo. We instead studied how the parameterization would look like if only total scattering and backscattering data were available.

5

The basic idea for the parameterization is that $N_{\rm CCN}$ is proportional to $\sigma_{\rm sp}$ and a function of the 6 7 backscatter fraction (BSF), i.e., $N_{CCN}(AOP) = (aBSF + b)\sigma_{sp}$ as is also in the parameterization 8 of Jefferson (2010). In the study of the physical explanation of the relationships between $N_{\rm CCN}$ 9 and AOPs, we found that the slope a and offset b in $N_{\text{CCN}}(\text{AOP}) = (\text{aBSF} + b)\sigma_{\text{sp}}$ depend clearly 10 on the dominating particle size and on the width of the size distributions. This was shown first 11 by simulations and then by comparisons of the simulations with field data. The analyses showed 12 that the sensitivity of $N_{\text{CCN}}(\text{AOP})$ to variations of BSF increases with a decreasing particle size. 13 As a result, sites dominated by supermicron aerosol particles, such as ASI that is dominated by 14 marine aerosol, have a small value of the slope a in the above formula, which means that it is 15 not very sensitive to variations in BSF. Sites dominated by small aerosol particles are clearly 16 more sensitive. For instance for the coastal site PVC that is significantly affected by 17 anthropogenic emissions, the slope a in the above formula is an order of magnitude higher than 18 at the marine site.

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A logarithmic function was fitted to the N_{CCN} vs. supersaturation SS data in the range SS < 1.1%. For $N_{CCN}(AOP)$ the fitting yielded a logarithmic dependence on SS: $N_{CCN}(AOP) \approx$ (286:SAE·ln(SS/0.093)(BSF – BSF_{min}) + (5.2 ± 3.3)) σ_{sp} . Actually this result is qualitatively in line with the relationship between AOD and CCN reported by Andreae (2010). The derived $N_{CCN}(AOP)$ depends on σ_{sp} , SAE and BSF. The analysis shows that neither SAE nor BSF alone is enough for obtaining a good estimate of N_{CCN} from AOP measurements.

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At the lowest supersaturations of each site (SS $\approx 0.1\%$), the average bias, defined as the ratio of the AOP-derived and measured N_{CCN} , varied from ~0.7 to ~1.9 at most sites except at the Himalayan site PGH where the bias was > 4. At SS > 0.4% the average bias ranged from ~0.7 to ~1.3 at most sites. For the marine-aerosol dominated site ASI the bias was higher, ~1.4 – 1.9. 1 In other words, at SS > 0.4% N_{CCN} was estimated with an average uncertainty of approximately 2 30% by using nephelometer data. The biases were mainly due to the biases in the 3 parameterization related to the scattering Ångström exponent SAE.

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6 Author contributions

7 YS carried out measurements at SORPES in China, analyzed and visualized data of all sites, 8 and wrote the original draft. AV contributed to data analysis and visualization, writing and 9 editing the original draft, and supervised the work of YS in Finland. AD provided funding for 10 the measurements and research at SORPES in China, acquired funding for YS in China, and 11 supervised the work of YS. KL, HK and PA carried out measurements, data collection and 12 maintenance of measurement data of SMEAR II in Finland. YS, XC, XQ, WN and XH carried 13 out measurements, data collection and maintenance of measurement data of SORPES in China. MK and TP provided the funding for YS in Finland. MK provided funding for the 14 15 measurements and research at SMEAR II in Finland. TP and VMK formulated the goals of the 16 research and supervised it.

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1 Tables

2

3 Table 1. Site and data description

Dataset	Description	Location Perio	р · 1	CCN		Size distrubtion		AOPs	
			Period	Instrument	SS	Instrument	size range	Instrument	inlet
SMEAR II	Boreal Forest, Finland	61°51' N, 24°17' E, 179m	2016.1.1- 2016.12.31	CCN-100	0.1%, 0.2%, 0.5% and 1.0%	DMPS custom-made	3-1000nm	Nephelometer TSI-3563	PM1, PM10
SORPES	Urban agglomerations, China	32°07' N, 118°56'E, 40m	2016.06.01- 2017.05.31	CCN-200	0.1%, 0.2%, 04%, and 0.8%	DMPS custom-made	6-800nm	Nephelometer Aurora-3000	TSP
PGH ^a	Ganges Valley, India	29°22' N, 79°27' E, 1936m	2011.11.01- 2013.03.25	CCN-100	0.12%, 0.22%, 0.48% and 0.78%	NA	NA	Nephelometer TSI-3563	PM1, PM10
PVC ^b	Cape Cod, USA	42°2' N, 70°3' W, 43m	2012.07.16- 2012.09.30	CCN-100	0.15%, 0.25%, 0.4% and 1.0%	SMPS TSI-3936	11-465nm*	Nephelometer TSI-3563	PM1, PM10
MAO ^c	Downwind Manaus City, Brazil	3°13' S, 60°36 W, 50m	2014.01.29- 2014.12.31	CCN-100	0.25%, 0.4%, 0.6% and 1.1%	SMPS TSI-3936	11-465nm*	Nephelometer TSI-3563	PM1, PM10
ASI ^d	Ascension Island, Atlantic Ocean	7°58' S, 14°21' W, 341m	2016.06.01- 2017.10.19	CCN-100	0.1%, 0.2%, 0.4%, and 0.8%	SMPS TSI-3936	11-465nm*	Nephelometer TSI-3563	PM1, PM10

^a use products: aipavg1ogrenM1.c1., and aosccnavgM1.c2.

^b use products: aipavg1ogrenM1.s1., noaaaosccn100M1.b1., and aossmpsS1.a1.

^c use products: aip1ogrenM1.c1., aosccn1colM1.b1., and aossmpsS1.a1.

 $^{\rm d}$ use products: aosnephdryM1.b1., aosccn2colaavgM1.b1., and aossmpsM1.a1. * vary slightly

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5

6 Table 2. Descriptive statistics of AOPs of PM10 aerosol and N_{CCN} at the different sites. σ_{sp} :

7 total scattering coefficient of green light ($\lambda = 550$ nm or 525 nm), in Mm⁻¹; BSF: backscatter

8 fraction of green light; SAE: scattering Ångström exponent between blue and red light. The

9 $N_{\rm CCN}$ statistics in # cm⁻³ are presented for four supersaturations (SS) at each site. The numbers

10 are the averages and standard deviations.

		AOPs				С	CN	
	σ_{sp}	BSF	SAE		#1	#2	#3	#4
SMEAR II	R II 14±14	0.15±0.03	2.11±0.67	SS:	0.10%	0.20%	0.50%	1.00%
SMEAR II				N _{CCN} :	129±99	303±229	514 ± 388	740±511
SORPES	270 . 199	0.11+0.02 1.45+	1 45 0 22	SS:	0.10%	0.20%	0.40%	0.80%
SORPES	270±188	0.11±0.02	±0.02 1.43±0.33	$N_{\rm CCN}$:	974 ± 632	2377±1244	4199±1915	5363±2245
PGH	020.015	0.07±0.01 0.53±0.30	0.52+0.20	SS:	0.12%	0.22%	0.48%	0.78%
РОП	239±213		$N_{\rm CCN}$:	325 ± 296	935±621	2359±1391	2882±1707	
PVC	27+22	0.13±0.03 1.	1 70 1 0 52	SS:	0.15%	0.25%	0.40%	1.00%
PVC	/C 2/±22			$N_{\rm CCN}$:	515 ± 361	864±603	1163 ± 774	1766±1020
MAO	AO 24±19	0.14±0.02 1.00±0.5	1.00 0.55	SS:	0.25%	0.40%	0.60%	1.10%
MAU			1.00±0.55	N _{CCN} :	448±377	783±693	1034 ± 923	1251±1068
ACT	ASI 20±13	0.14±0.01 0.7	0.72+0.41	SS:	0.10%	0.20%	0.40%	0.80%
ASI			0.75 ± 0.41	N _{CCN} :	113±79	234±175	271±199	319±203

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14

1 Table 3. The slopes and offsets of ordinary linear regressions of $R_{CCN/\sigma}$ vs. BSF at the different

2 supersaturation SS at the studied sites. s.e.: standard error of the respective coefficient obtained

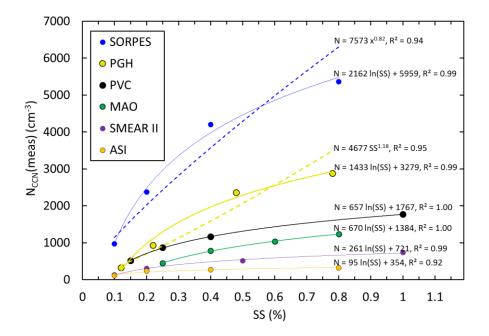
3	from the linear regressions.	The unit of the coefficients	is $[N_{\rm CCN}]/[\sigma_{\rm sp}] = {\rm cm}^{-3}/{\rm Mm}^{-1}$.
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		R _{CCN/s} =	aBSF + b
	SS (%)	a ± s.e.	b ± s.e.
SMEAR II	0.10	91 ± 3	-2.9 ±0.4
	0.20	433 ± 5	-38.6 ±0.7
	0.50	867 ±10	-86.4 ± 1.5
	1.00	1155 ± 17	-115.8 ± 2.5
SORPES	0.10	62 ± 2	-2.6 ± 0.2
	0.20	266 ± 4	-18.4 ± 0.4
	0.40	531 ± 7	-39.1 ±0.8
	0.80	738 ±11	-55.9 ± 1.2
PGH	0.12	-18 ±1	2.6 ± 0.1
	0.22	24 ± 3	2.8 ± 0.2
	0.48	244 ± 12	-4.4 ± 0.8
	0.78	344 ± 14	-8.3 ± 1.0
PVC	0.15	417 ± 9	-30.2 ± 1.1
	0.25	793 ±17	-61.7 ± 2.1
	0.40	1176 ± 25	-95.3 ± 3.1
	1.00	1945 ± 43	-161.4 ± 5.3
MAO	0.25	273 ± 5	-19.0 ± 0.7
	0.40	544 ± 8	-42.9 ±1.2
	0.60	678 ±13	-50.9 ± 1.8
	1.10	868 ± 32	-58.3 ± 4.3
ASI	0.10	22 ± 2	2.2 ± 0.2
	0.20	105 ± 3	-3.6 ±0.5
	0.40	127 ± 4	-5.0 ± 0.6
	0.80	136 ± 4	-4.0 ± 0.6

Table 4. The coefficients a_0 , a_1 , b_0 and b_1 obtained from the fitting of $a = a_1 \ln(SS) + a_0$ and $b = b_1 \ln(SS) + b_0$ with the data in Table 3. The unit of the coefficients is $[N_{CCN}]/[\sigma_{sp}] = \text{cm}^{-3}/\text{Mm}^{-1}$. s.e.: standard error of the respective coefficient obtained from the regressions. SAE: scattering Ångström exponent of PM10 aerosol.

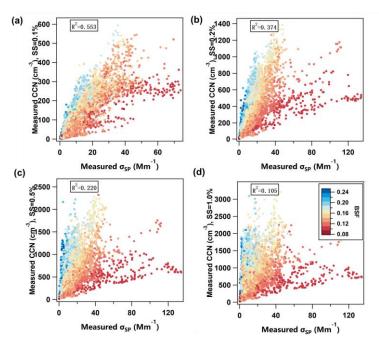
	R _{CCN/σ} =	SAE				
SITE	a ₁ ± s.e.	$a_0 \pm s.e.$	$b_1 \pm s.e.$	$b_0 \pm s.e.$	average ± std	median
SMEAR II	464 ± 11	1170 ± 16	-49 ± 1.5	-118 ± 2.1	2.11 ± 0.67	2.22
SORPES	331 ± 12	817 ± 18	-26 ± 0.9	-62 ± 1.4	1.45 ± 0.33	1.50
PGH	205 ± 30	385 ± 41	-6.3 ± 1.5	-9.1 ± 2.0	0.53 ± 0.30	0.57
PVC	810 ± 17	1933 ± 21	-70 ± 1.7	-160 ± 2.1	1.79 ± 0.52	1.91
MAO	393 ± 45	858 ± 40	-25 ± 6.6	-60 ± 5.8	1.00 ± 0.55	1.09
ASI	52 ± 17	164 ± 26	-2.9 ± 1.6	-6.3 ± 2.3	0.73 ± 0.41	0.64

1 FIGURES



2

- 3 Figure 1. Averages of the measured N_{CCN} at the six sites at the station-specific supersaturations
- 4 of the CCN counters and a logaritmic fitting to the data.



6 Figure 2. Measured CCN number concentration N_{CCN} (meas) vs. PM₁₀ scattering coefficient σ_{sp}

- 7 at λ = 550 nm at SMEAR II at four supersaturations (SS): a) 0.1 %, b) 0.2 %, c) 0.5 % and d) 1.0 %.
- 8 Colorcoding: backscatter fraction (BSF) at λ = 550 nm.
- 9

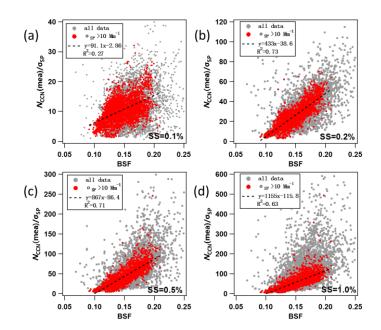
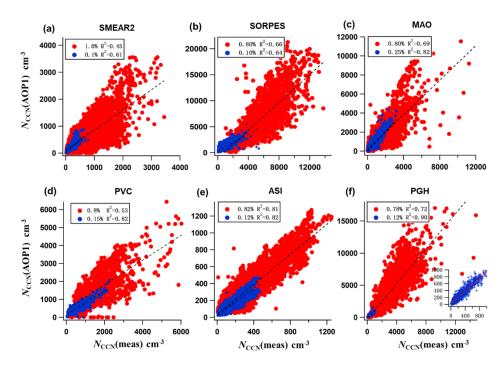
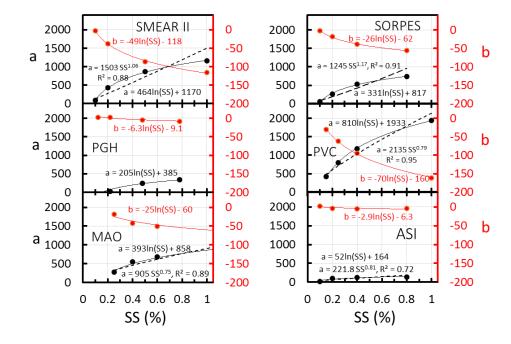


Figure 3. Relationship between $R_{CCN/\sigma}$ (= N_{CCN} (meas)/ σ_{sp}) and BSF at SMEAR II at four supersaturations (SS): a) 0.1 %, b) 0.2 %, c) 0.5 % and d) 1.0 %. Grey symbols: all data, red symbols: data at $\sigma_{sp} > 10 \text{ Mm}^{-1}$. Both σ_{sp} and BSF were measured at $\lambda = 550 \text{ nm}$.

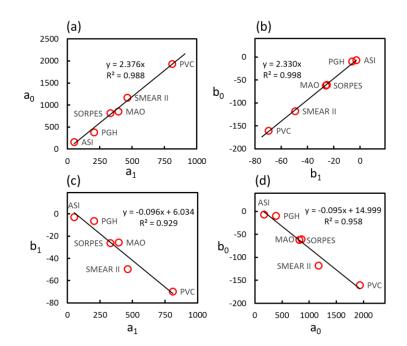


6 Figure 4. N_{CCN} (AOP₁) vs. N_{CCN} (meas) at a) SMEAR II, b) SORPES, c) MAO, d) PVC, e) ASI and f) 7 PGH. N_{CCN} (AOP) was calculated by using the slopes and offsets a and b of the linear regressions 8 R_{CCN/ σ} = aBSF + b in Table 3 for two supersaturations (blue symbols: low SS, red symbols: high 9 SS).



1

Figure 5. The the slopes and offsets a and b of the linear regressions $R_{CCN/\sigma} = aBSF + b$ of each station (Table 3) as a function of supersaturation SS. Two types of functions, a logarithmic and a power fuction were fitted to the coefficient a, to coefficient b only a logaritmic function. The squared correlation coefficients R² are shown only for the power function fittings, for the logarithmic fittings they were all > 0.99.



8

9 Figure 6. Relationship between the coefficients a_0 , a_1 , b_0 and b_1 of Equation (7) for each station

10 presented in Table 4 for the 6 stations. a) $a_0 vs. a_1$, b) $b_0 vs. b_1$, c) $b_1 vs. a_1$, d) $b_0 vs. a_0$.

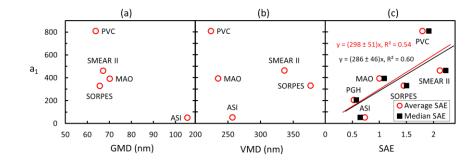


Figure 7. Relationship of the a_1 coefficient in Equation (8) with the average a) geometric mean diameter of the PNSD data size ranges of the sites, b) volume mean diameter of the same size

4 range, and c) PM₁₀ scattering Ångström exponent (SAE).

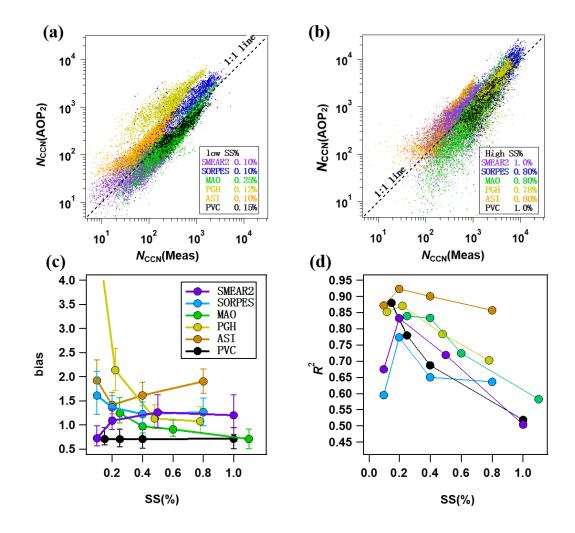
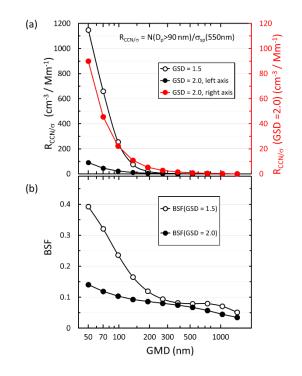




Figure 8. Statistics of $N_{CCN}(AOP_2)$ from parameterization in Eq. (10). $N_{CCN}(AOP_2)$ vs. $N_{CCN}(meas)$ at different sites at relatively (a) low and (b) high supersaturations, (c) bias = $N_{CCN}(AOP_2)/N_{CCN}$ (meas) at different sites and supersaturations, and (d) R^2 of the linear regression of $N_{CCN}(AOP_2)$ ys. N_{CCN} (meas) at different sites and supersaturations.





3 Figure 9. Size distribution of a) R_{CCN/ σ} and b) backscatter fraction BSF (λ = 550 nm) of simulated narrow (GSD = 1.5) and wide (GSD = 2.0) unimodal size distributions. GMD: geometric mean 4 5 diameter, GSD: geometric standard deviation. Note: in a) the $R_{CCN/\sigma}$ of the wide size 6 distributions are plotted twice: the black symbols and line use the left axis to emphasize the 7 big difference in the magnitudes of the wide and narrow size distributions; the red symbols 8 and line use the right axis to show that the shape of the $R_{CCN/\sigma}$ size distribution is very similar 9 to the one calculated for thew narrow size distributions. $R_{\text{CCN}/\sigma}$ was calculated assuming 10 particles larger than 90 nm get activated.

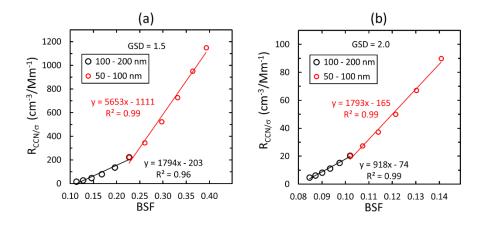
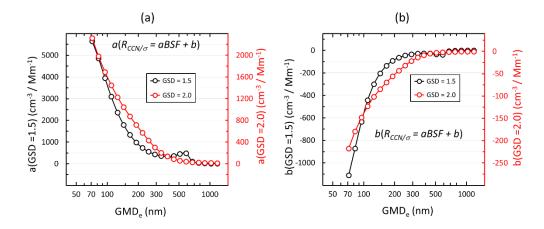


Figure 10. Linear regressions of $R_{CCN/\sigma}$ vs backscatter fraction BSF (λ = 550 nm) of simulated unimodal a) narrow (GSD = 1.5) and b) wide (GSD = 2.0) size distributions. The regressions were calculated assuming that the data consist of size distributions with GMD ranging from 50 to 100 nm and 100 to 200 nm. $R_{CCN/\sigma}$ was calculated assuming particles larger than 90 nm get activated.



8

9 Figure 11. Size distributions of the coefficients of the linear regressions of $R_{CCN/\sigma}(\lambda = 550 \text{ nm})$ 10 vs backscatter fraction BSF ($\lambda = 550 \text{ nm}$) of narrow and wide size distributions. a) slopes of 11 $R_{CCN/\sigma}$ vs. BSF, b) offsets of $R_{CCN/\sigma}$ vs. BSF. $R_{CCN/\sigma}$ was calculated assuming particles larger than 12 90 nm get activated. The regressions were calculated for 5 consequtive size distributions. 13 GMD_e is the geometric mean of the range of the unimodal size distributions used for the 14 regressions.

- 15
- 16

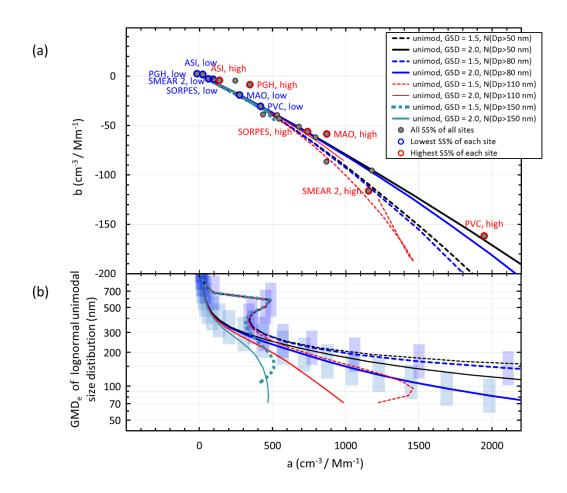
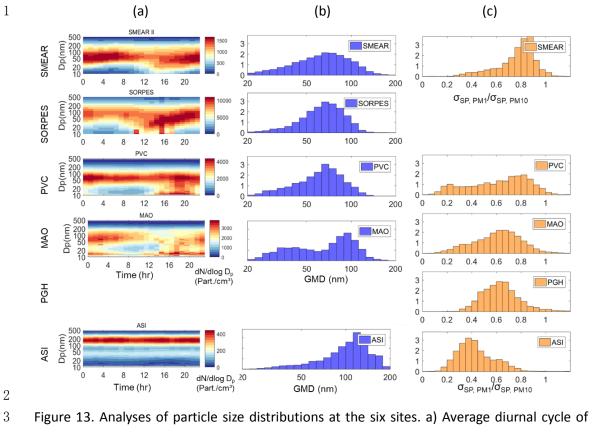


Figure 12. a) Relationships of the slopes and offsets of the linear regressions of $R_{CCN/\sigma} = aBSF +$ b vs. BSF of the simulated unimodal narrow (GSD = 1.5) and wide (GSD = 2.0) size distributions and those obtained from the similar regressions of the station data (Table 3). b) Equivalent geometric mean diameter (GMD_e) of the unimodal modes used for the linear regression vs. the slope of the linear regression of $R_{CCN/\sigma}$ vs. BSF. The vertical error bars show the ranges of the GMDs of the unimodal size distributions used in the respective linear regressions. $R_{CCN/\sigma}$ was calculated for the activation diameters of 50 nm, 80 nm, 110nm, and 150 nm.

9



PNSD and b) normalized size distribution of GMD at SMEAR II, SORPES, PVC, and ASI, c) normalized frequency distribution of $\sigma_{sp}(PM_1)/\sigma_{sp}(PM_{10})$ at SMEAR II, PVC, MAO, PGH and ASI.