

Dear Reviewers and Editor,

We thank you for your helpful comments and corrections which were important to improve the article during a moderate or major revision.

(Reviewer comment is in blue,
our answer is in black,
manuscript change is in red)

Reviewer 1:

Point-to-point response:

1) However, the analysis is unfortunately not really done in a balanced way and I found most of the results to be speculative without any further analysis and explanation (see my major comments). The paper has a strong focus on the methodology of evaluating fluctuations in general (4.5 pages out of 6), whereas the interpretation of the fluctuations which is suggested by the title is rather very short.

We changed our analysis: Instead of specific kinetic energy fluctuations, we take the diurnal cycle of latent heat flux at Bern as provided by MERRA-2 reanalysis. So, we analyse and discuss the relation of a cause (diurnal cycle of latent heat flux) to the short-term variability of IWV. **Figure 6 and 7 are new and indicate that short-term variability of IWV is a consequence of the diurnal cycle in latent heat flux.**

- 2) First, I would like to mention the introduction. A complete motivation of the importance of water vapor and IWV with citation of the key papers is missing, e.g. Why is water vapor an important trace gas in the atmosphere (hydrological cycle etc.); Why is it important to understand IWV fluctuations? Open questions? The existing literature concerning IWV fluctuations is poorly cited and the work described here is not really put into the context. For example missing papers are: Ortiz de Trenberth et al. 1998, Galisteo et al. 2011, 2014, Vogelmann et al. 2015 and others. I recommend to revise the introduction and add a general part about water vapor, IWV and its importance.

We agree and added a paragraph about the role of atmospheric water vapour.

Atmospheric water vapour is the dominant greenhouse gas and acts like a warm mantle for the Earth. Global warming due to man-made CO₂ emissions is amplified by increase of the water vapour concentration in a warmer world. This amplification of global warming due to the so-called water vapour feedback is up to a factor of three (Held 2000). The electric dipole of the water molecule is responsible for the large latent heat of vaporization of water and for the strong interaction of electromagnetic waves with water vapour. Integrated water vapour (IWV) is the main contributor to the wet delay of signals of the Global Navigation Satellite System (GNSS) (Guerova 2016). Further, atmospheric water vapour is the reservoir gas for formation of cloud liquid water and precipitation such as snow, hail and rain which are relevant for weather and climate. The annual variation of integrated water vapour is rather strong at Bern (Switzerland) reaching from about 8 mm (or 8 kg m⁻²) in

winter to 24 mm in summer \citep{hocke2017}. \cite{ortiz2014} reported that IWV ranges from 14.5 mm to 20.0 mm in Spain. Long-term monitoring of IWV is essential for detection of regional and global trends of IWV \citep{morland2009,parracho2018}.

- 3) Second, the manuscript is not very balanced in general. The method part including the introduction is about 4.5 pages, whereas the results section is only about 1 page describing 7 figures in total with only a sparse discussion and explanation. I found much of this text to be poorly supported. I would recommend to split the results section into a more method based sub-section concerning how to extract the best amplitude spectrum (FFT, band-pass, moving SD) and a sub-section concerning correlation of turbulence with fluctuations of IWV. This would help to better underlay both parts of the analysis (method and turbulence) with more explanation and more extensive analysis. As an example, in the text to figure 2-4 mainly the behavior of the spectra in comparison to a power law is described, but no discussion about which power spectra is expected and why do the spectra behave like we see it in the Figures.

We agree and we structure the result sections into three subsections. We added a few sentences in the result section. However, the relation of the diurnal cycle of latent heat flux and the diurnal cycle of IWV fluctuation strength is quite basic and we think that a long discussion is not needed. The slope of the IWV spectra was not yet simulated or observed. Thus we cannot discuss our expectation or compare it to previous results. Our observational study can be regarded as a letter which presents a new result, namely the diurnal cycle of short-term IWV fluctuations.

Figure \ref{fig6} shows the diurnal cycle of the latent heat flux in winter, spring, summer and fall as derived from MERRA-2 reanalysis data close to Bern in the year 2010. As expected, the diurnal cycle of latent heat flux is strongest in summer.

The maximum latent heat flux is around 13:00 CET. That means the observed diurnal cycle of the short-term IWV fluctuations lags the diurnal cycle of latent heat flux by 1-2 hours. A numerical simulation by \cite{schlemmer2011} showed that the diurnal variation in solar short wave radiation leads the diurnal cycle of latent heat flux which is followed by the diurnal cycles of CAPE (convective available potential energy) and the convective mass flux. The maxima of the curves in CAPE and convective mass flux occurred in the afternoon and evening hours.

These observations and simulations suggest that the increase of short-term IWV fluctuations during daytime in summer is due to the diurnal cycle of latent heat flux which is a precondition for an increase of strong and variable convection cells in the afternoon. The up- and downdraft regions of the convection cells are passing the antenna beam of the TROWARA radiometer which consequently measures larger or smaller values of IWV in time distances of about 10 min. In addition, a convection cell is itself time variable: The lifetime of a convection cell is roughly between 30 and 60 minutes \citep{giaiotti2007}.

Figure \ref{fig7} compares the 3-day averages of SD of IWV (moving 10 min-window) in the upper panel with 3-day averages of MERRA-2 latent heat flux at Bern in the lower panel for the year 2010. The correlation coefficient r of SD(IWV) and the latent heat flux is equal to 0.82. Some of the peaks in the latent heat flux coincidentally appear in the SD curve of

short-term I WV variability in the upper panel, e.g., the double peak around June 2010. Figure \ref{fig7} suggests that the variability of the latent heat flux is a contributor to the short-term variability of I WV.

4) Third, there is a more detailed analysis missing to better understand the correlation of the I WV fluctuations and fluctuations of specific kinetic energy. It is obvious that the shape of both diurnal cycles is similar, but as you mentioned in the text the amplitude in different seasons is different. There are stronger fluctuations of specific kinetic energy in spring and you attributed this to stronger advection (page 6, line 15). This could be, but it is just speculation without any prove. From the diurnal cycle it is obvious that there are other processes involved influencing the I WV fluctuations. For example you could look into a connection between I WV and ILW fluctuations to determine the influence of clouds. This is also suggested by the cloud picture in Figure 1. Another example is that the I WV fluctuations in summer show also enhanced values during nighttime compared to other season, which is not reflected by the diurnal cycle of specific kinetic energy. In the end, I would like to have a more detailed discussion about possible other influencing factors like advection, cloud formation, precipitation, gravity waves etc.. All of this is not addressed at all in the manuscript.

We agree, the comparison of the diurnal cycle of short-term I WV fluctuations with specific kinetic energy (TKE) fluctuations was not so reasonable since TKE also includes the wind interaction with the surface which can be strong during equinox. In addition, small-scale turbulence may not induce significant changes in integrated water vapour. Thus, TKE fluctuations and I WV fluctuations are possibly not so much related. We argue now in a stronger manner that I WV fluctuations mainly depend on the spatio-temporal variability of convection cells and the amount of integrated water vapour in the updraft and downdraft regions. However, we added a sentence that other contributors to the I WV variability exist. One can see in the new Figure 7, that some peaks of SD(I WV) are not included in the annual curve of the latent heat flux. The relation of the diurnal cycles of various parameters are well discussed in the simulation study of Schlemmer et al. (2001). The diurnal cycle of latent heat flux in the reanalysis data agrees with this study. The phase lag of the diurnal cycle of SD(I WV) appears reasonable since the diurnal cycle in cloud liquid water (ILW) is also phase lagged with respect to the diurnal cycle of latent heat flux. Usually, ILW fluctuations have no influence on I WV but both, ILW fluctuations and I WV fluctuations, are connected to atmospheric convection.

Figure 6 and 7 are new. The discussion is now easier.

- Page 3, line 32: You mentioned the rotational transition line of water vapour centered at 22.232 GHz. Why does this effect your measurements, because the microwave channel at 21.4GHz has only a bandwidth of 100 MHz.

The pressure broadening of the 22 GHz line also influences the intensity at 21 GHz which is in the line wing

- Page 5, line 1: Which length of the Hamming window do you use? Maybe it is worth to mention this in the text.

We added a sentence that the size of the Hamming window is equal to the number of filter coefficients (three times of central period).

- Page 6: Did you analysed the spectrum of the specific kinetic energy fluctuations ? The time resolution is of course lower than of the IWV fluctuations, but you could compare the slope of the spectra in comparison to the spectra of the IWV fluctuations for time window length larger than 10 min.

The new manuscript version do not consider the specific kinetic energy fluctuations.

Thank you for the Technical components which we included in the new version!

Reviewer 3:

Point-to-point response:

1) Most critical I see the conclusion, “ that the diurnal cycle of the short-term IWV fluctuations is caused by turbulence associated with large convective heating during daytime in summer” from the comparison in this work, because:
- The diurnal cycles are not very similar (e.g. for JJA Figure 5 shows the maximum between 12 and 14h, Figure 6 after 16h.)

We agree. When we submitted the paper we were also not happy about the weak correlation between turbulence (TKE fluctuations) and IWV fluctuation strength. After your comments, we got the idea that the diurnal cycle of latent heat flux as provided by MERRA-2 reanalysis is the cause of the observed diurnal cycle of SD(IWV). Both curves must be not in phase. The study of Schlemmer et al. (2001) shows for example that the maximum of latent heat flux occurs around noon while the cloud liquid water and precipitation peaks in the afternoon and early evening hours. This is possibly due to the ascent time of water vapour.

Fig. 6 and 7 are new. We found a strong correlation of the annual curves of latent heat flux and SD(IWV). We changed the discussion.

I would expect a more detailed analysis of this connection, looking into more detail than the seasonal mean of the diurnal cycle. How is the correlation between them (for single days and/or do days with strong (week) short-term IWV fluctuations show also strong (weak) fluctuations of the specific kinetic energy)?

- What about spring and autumn?

- How large is the variability of the diurnal cycles shown in Figure 5 and 6?

Thank you for your fruitful comments which we considered in the revision.

Figure 7 gives an overview on the variability of 3-day averages of latent heat flux and SD(IWV). We emphasize that single peaks in latent heat flux coincidentally appear in the observed SD(IWV).

We show the error of the mean in Figures 5 and 6 for the season JJA.

Figure \ref{fig6} shows the diurnal cycle of the latent heat flux in winter, spring, summer and fall as derived from MERRA-2 reanalysis data close to Bern in the year 2010. As expected, the diurnal cycle of latent heat flux is strongest in summer.

The maximum latent heat flux is around 13:00 CET. That means the observed diurnal cycle of the short-term IWV fluctuations lags the diurnal cycle of latent heat flux by 1-2 hours. A numerical simulation by \cite{schlemmer2011} showed that the diurnal variation in solar short wave radiation leads the diurnal cycle of latent heat flux which is followed by the diurnal cycles of CAPE (convective available potential energy) and the convective mass flux. The maxima of the curves in CAPE and convective mass flux occurred in the afternoon and evening hours.

These observations and simulations suggest that the increase of short-term IWV fluctuations during daytime in summer is due to the diurnal cycle of latent heat flux which is a precondition for an increase of strong and variable convection cells in the afternoon. The up- and downdraft regions of the convection cells are passing the antenna beam of the TROWARA radiometer which consequently measures larger or smaller values of IWV in time distances of about 10 min. In addition, a convection cell is itself time variable: The lifetime of a convection cell is roughly between 30 and 60 minutes \citep{giaiotti2007}.

Figure \ref{fig7} compares the 3-day averages of SD of IWV (moving 10 min-window) in the upper panel with 3-day averages of MERRA-2 latent heat flux at Bern in the lower panel for the year 2010. The correlation coefficient r of SD(IWV) and the latent heat flux is equal to 0.82. Some of the peaks in the latent heat flux coincidentally appear in the SD curve of short-term IWV variability in the upper panel, e.g., the double peak around June 2010. Figure \ref{fig7} suggests that the variability of the latent heat flux is a contributor to the short-term variability of IWV.

The results and discussion part is rather short and should be extended.

We added several sentences. The discussion is now easier since latent heat flux and SD(IWV) are related. So, the discussion can be kept short. We refer to the study of Schlemmer et al. (2001). Finally, we like that the manuscript is more like a letter.

Why is the method of the moving standard deviation chosen to analyse the diurnal cycle, what is its advantage compared to the band pass filter?

We added a sentence:

In the following, we focus on the third method (SD values) since the standard deviation is most common for the characterization of the variability of a time series.

What are the potential benefits for modelling studies from these measurements? In the introduction more literature concerning this topic should be mentioned.

A potential benefit is that high resolution atmosphere modelling may produce a similar diurnal cycle of short-term IWV fluctuation strengths as we observed. This would be a confirmation that atmospheric convective processes are well represented in the model world. We added the following paragraph at the end of the manuscript:

Thus, we suggest that the diurnal cycle of the short-term IWV fluctuations is mainly caused by the diurnal cycle of latent heat flux which is a precondition for strong and variable convection cells in the afternoon during summer. The spatio-temporal variability of the convection cells induces the diurnal cycle of short-term IWV fluctuations as observed by the TROWARA radiometer at Bern in summer. However, other sources such as eddies in the lower troposphere may also contribute to the short-term variability of IWV. High resolution modelling of the diurnal cycle of short-term IWV fluctuations could be compared to the TROWARA observations so that one can estimate how good convective processes are represented by the model. Generally, we think that the high resolution IWV observations of TROWARA can contribute to research on the atmospheric boundary layer.

Page 2, line 33: "...height of the atmospheric boundary layer" instead of "...height level of the atmospheric boundary layer"?

We agree and we changed it

Page 4, line 19: 11 seconds or 10 seconds as mentioned at page 2 line 1?

Now, we keep 10 seconds.

The link between the short term fluctuations of the specific kinetic energy and the turbulent kinetic energy could be explained in more detail.

we do not need this link in the new version.

Why does Figure 7 use the climatology and not the 2010 data as the rest of the paper?

Figure 7 is replaced by a different figure.

Thank you for your review!

Diurnal cycle of short-term fluctuations of integrated water vapour above Switzerland

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Abstract. The TROpospheric WAter RAdiometer (TROWARA) continuously measures integrated water vapour (IWV) with a time resolution of 6 seconds at Bern in Switzerland. During summer, we often see that IWV has temporal fluctuations during daytime while the night-time data are without fluctuations. The data analysis is focused on the year 2010 where TROWARA has a good data quality without data gaps. We derive the spectrum of the IWV fluctuations in the period range from about 1 to 100 min. The FFT spectrum with a window size of 3 months leads to a serious underestimation of the spectral amplitudes of the fluctuations. Thus, we apply a band pass filtering method to derive the amplitudes as a function of period T_p . The amplitudes are proportional to $T_p^{0.5}$. Another method is the ~~computation~~ calculation of the moving standard deviation with time window lengths from about 1 to 100 min. Here, we get similar results as for the band pass filtering method. At all periods, the IWV fluctuations are strongest during summer while they are smallest during winter. We derive the diurnal variation of the short-term IWV fluctuations by applying a moving standard deviation with a window length of 10 min. The daily cycle is strongest during the summer season with standard deviations up to 0.22 mm at about 14:00 CET. The diurnal cycle disappears during winter time. ~~Using the meteorological weather station at Bern, we derive the~~ A similar seasonal behaviour is observed in the diurnal cycle of latent heat flux as provided by the Modern-Era Retrospective Analysis for Research and Applications, version 2 (MERRA-2 reanalysis) at Bern. Further, the 3-day averages of the latent heat flux and the magnitude of the short-term ~~fluctuations of the specific kinetic energy e_k . Since these data have a temporal resolution of 10 min, we apply a 20 min-moving standard deviation. The derived short-term e_k fluctuations can be regarded as a proxy of turbulent kinetic energy (TKE). During summer time, the 20 min-moving standard deviation of e_k increases during daytime and has a similar diurnal cycle like the short-term-IWV fluctuations. variability show a strong correlation (r of 0.82) at Bern in 2010.~~ Thus, we ~~conclude~~ suggest that the diurnal cycle of ~~the short-term IWV fluctuations~~ is caused by turbulence associated with at Bern is mainly caused by large convective heating during daytime in summer.

Copyright statement.

1 Introduction

~~The spatio-temporal variability of integrated water vapour~~

5 Atmospheric water vapour is the dominant greenhouse gas and acts like a warm mantle for the Earth. Global warming due to man-made CO₂ emissions is amplified by increase of the water vapour concentration in a warmer world. This amplification of global warming due to the so-called water vapour feedback is up to a factor of three (Held and Soden, 2000). The electric dipole of the water molecule is responsible for the large latent heat of vaporization of water and for the strong interaction of electromagnetic waves with water vapour. Integrated water vapour (IWV) is the main contributor to the wet delay of signals of the Global Navigation Satellite System (GNSS) (Guerova et al., 2016). Further, atmospheric water vapour is the reservoir gas for formation of cloud liquid water and precipitation such as snow, hail and rain which are relevant for weather and climate. The annual variation of integrated water vapour is rather strong at Bern (Switzerland) reaching from about 8 mm (or 8 kg m⁻²) in winter to 24 mm in summer (Hocke et al., 2017). Ortiz de Galisteo et al. (2014) reported that IWV ranges from 14.5 mm to 20.0 mm in Spain. Long-term monitoring of IWV is essential for detection of regional and global trends of IWV (Morland et al., 2009; Parracho et al., 2018).

15 The spatio-temporal variability of IWV on scales of less than 10 km and hours was assessed by Steinke et al. (2015) using various instruments and atmospheric numerical simulations. The model runs showed IWV variabilities of the order of 0.4 mm (or kg m⁻²) for differences in space of 3-4 km or time of 10-15 min during the presence of a boundary layer. Passive microwave radiometry can provide a high temporal resolution of 10 seconds for IWV measurements. Steinke et al. (2015) reported about standard deviations of IWV observed by microwave radiometers exceeding 1 mm even at short time scales of a few minutes. To our knowledge there are no other studies on the IWV variability at very short scales from 1 to 20 min. Since the short-term IWV fluctuations are likely connected with atmospheric waves and turbulence, we expect a seasonal and diurnal variation of the IWV variability which was not investigated by Steinke et al. (2015) and others. However, Steinke et al. (2015) suggested that the short-term IWV variability at time scales of 15 min or less is induced by atmospheric turbulence which was simulated by their high-resolution model.

20 The TROpospheric WAter RAdiometer (TROWARA) has measured continuously integrated water vapour (IWV) with a time resolution of 6 seconds at Bern in Switzerland since 2009. In the time from 1994 to 2008 the temporal resolution was 10 seconds. Thus, it is no problem to analyse the IWV variability at Bern on time scales from 1 to 100 min as function of local time and season. The short-term IWV variability is possibly connected with the growth of the atmospheric boundary layer during daytime in summer. Convective heating and associated turbulence generate variable vertical winds and circulation cells leading to a variable vertical water vapour flux during daytime. We expect that IWV can significantly change during daytime if the antenna beam of the radiometer transects an updraft or downdraft region in the lower troposphere.

30 ? simulated the atmospheric convection over land in summer at mid-latitudes. They found diurnal cycles in surface net shortwave radiation, latent heat flux, sensible heat flux, convective mass flux, convective available potential energy (CAPE), specific cloud water content, and surface precipitation. These diurnal cycles have maxima around noon or in the afternoon and early evening hours. Numerical simulations (Stull, 1988; Yamada and Mellor, 1975) show that the turbulent kinetic energy (TKE) has a strong diurnal cycle with increases of TKE from 0.05 J kg⁻¹ at night-time to about 1 J kg⁻¹ at daytime. The maximum occurs at a height of about 300 m above the surface. This increase of TKE is associated with the presence of a

convective mixed layer during daytime reaching from the surface to 1.5 km or higher. Lüdi and Magun (2002) determined turbulence parameters in the lower troposphere by analyzing the scintillations of a microwave link between a transmitter and a receiver.

The diurnal cycle in IWV over Bern was described by Hocke et al. (2017) using hourly data of the TROWARA radiometer.

5 The diurnal cycle in IWV goes from about -0.5 mm (relative to the daily mean value) in the morning hours to about +0.5 mm during the evening hours. This IWV variation is less than 5%, and it can be assumed that the diurnal cycle in IWV has no direct influence on the diurnal cycle of short-term IWV variability. Nevertheless, the diurnal cycle in IWV can be understood as a residual upward flux of tropospheric water vapour during daytime so that the accumulation of IWV achieves a maximum in the evening hours.

10 Using observations of wind profilers, radiometers and lidars, Collaud Coen et al. (2014) derived the climatology of the atmospheric boundary layer at Payerne which is closely located to Bern in the Swiss plateau. They also compared the observed height of the boundary layer to the modeled height. The regional weather model predicted a boundary layer height of about 1800 m during summer from May to August while the observations indicated a boundary layer height of about 1500 m or less. During winter the boundary layer height decreased to about 500 m where the model gave slightly lower values than
15 the observations. Generally, vertical profiles of specific humidity or relative humidity can be used to determine the height of the atmospheric boundary layer as described by Seidel et al. (2010). The boundary layer is assumed to be moister than the free troposphere so that the vertical gradient of humidity becomes minimal (extreme) at the height ~~level~~ of the atmospheric boundary layer. This vertical gradient method of humidity also shows that there is a connection between IWV and the moist boundary layer.

20 The aim of the present study is to ~~give~~ provide mean values of the amplitudes of the short-term IWV fluctuations in the period range from 1 to 100 min. These mean values may guide modeling studies about water vapour convection and circulation cells in the lower troposphere. Further, we derive the dependence of the short-term IWV variability on the season and the local time. Section 2 describes the TROWARA radiometer and the weather station of the University of Bern. Section 3 explains the data analysis to obtain the amplitudes or the moving standard deviation of the IWV variability. Section 4 presents the results
25 on the short-term IWV variability and ~~the standard deviation of the specific kinetic energy where the latter is derived from the horizontal wind speed measurements of the weather station~~ its relation to the latent heat flux at Bern. Concluding remarks are given in section 5.

2 Measurement instruments and retrieval

2.1 TROWARA

30 Our study is focused on the IWV observations of the TROpospheric WAtER RAdiometer (TROWARA). TROWARA is a dual-channel microwave radiometer, and its design and construction were described by Peter and Kämpfer (1992) and Morland (2002). Two ferrite circulator switches at each frequency channel of the radiometer perform the change from the antenna to the noise diodes. The noise diodes serve as hot and cold reference loads. The developed radiometer model considers the mea-

measurements of the reflection and transmission coefficients of all radiometer components including the ferrite switches (Morland, 2002). In addition, a tipping curve calibration is performed by using the variable brightness temperature of the clear sky at different elevation angles of the antenna. The instrument is very stable so that the tipping curve calibration is only required 2 or 3 times per year.

- 5 TROWARA measures the vertically-integrated water vapour (IWV) which is also known as precipitable water vapour. Further, TROWARA provides the vertically-integrated cloud liquid water (ILW), also known as liquid water path. The instrument is operated inside a temperature-controlled room on the roof of the building for Exakte Wissenschaften (EXWI) of the University of Bern (46.95°N, 7.44°E, 575 m a.s.l.). The antenna receives the atmospheric radiation inside the room through a microwave transparent window. This indoor operation of TROWARA allows the measurement of IWV even during rainy periods.
- 10 The antenna beam of TROWARA has a full width at half power of 4° and is pointing the sky at an zenith angle of 50° towards south-east. At 1 km above surface, the horizontal diameter of the sounding volume of TROWARA is about 170 m. The view direction is constant, so that short-term temporal variations of the brightness temperature, IWV and ILW are well monitored with a time resolution of 6 seconds. TROWARA's IWV measurement has nearly all-weather capability during day and night-time. The ILW measurement cannot be carried out in presence of rain droplets. Thus, the ILW measurement is restricted to
- 15 cloud droplets (ILW < 0.4 mm). Details of the TROWARA instrument and the retrieval technique are provided by Cossu et al. (2015) and Mätzler and Morland (2009).

In the following, we briefly explain the measurement principle and the retrieval. The microwave channel of TROWARA at 21.4 GHz has a bandwidth of 100 MHz, and the microwave channel at 31.5 GHz has a bandwidth of 200 MHz. The frequency channel at 31.5 GHz is more sensitive to microwaves from atmospheric liquid water, while the frequency channel at 21.4 GHz

20 is more sensitive to microwaves from water vapour since there is a rotational transition line of water vapour centered at 22.235 GHz.

The radiative transfer equation of a non-scattering atmosphere is

$$T_{B,i} = T_c e^{-\tau_i} + T_{mean,i} (1 - e^{-\tau_i}), \quad (1)$$

where τ_i is the opacity of the i -th frequency channel (e.g., 21 GHz) along the line of sight of the radiometer. $T_{B,i}$ is the

25 observed brightness temperature, and T_c is the brightness temperature of the cosmic microwave background. $T_{mean,i}$ denotes the effective mean temperature of the troposphere (Ingold et al., 1998; Mätzler and Morland, 2009).

The equation 1 can be solved for the opacities

$$\tau_i = -\ln \left(\frac{T_{B,i} - T_{mean,i}}{T_c - T_{mean,i}} \right) \quad (2)$$

where the TROWARA observations yield the radiances $T_{B,i}$.

- 30 In a plane-parallel atmosphere, the opacity is linearly related to IWV and ILW

$$\tau_i = a_i'' + b_i'' IWV + c_i'' ILW, \quad (3)$$

where the coefficients a'' and b'' partly depend on air pressure. Mätzler and Morland (2009) showed that the coefficients can be statistically derived by means of coincident measurements of radiosondes and fine-tuned at times of periods with a

clear atmosphere. The coefficient c'' indicates the mass absorption coefficient of cloud water. c'' depends on temperature (and frequency), but not on pressure. It is derived from the physical expression of Rayleigh absorption by clouds (Mätzler and Morland, 2009). After determination of the coefficients, the opacity measurements at 21 and 31 GHz yield the desired parameters IWV and ILW in equation 3.

5 TROWARA provides a time series of IWV since 1994 with a time resolution of ~~11~~10 seconds until end of 2009 and 6 seconds afterwards. The IWV time series have been used for trend analysis (Morland et al., 2009; Hocke et al., 2011). Hocke et al. (2017) analysed diurnal cycles in IWV, ILW and cloud fraction by using all informations of TROWARA which also has an infrared radiometer channel at 9.5 -11.5 μm . The present study only uses the IWV measurements of the year 2010 when the performance of TROWARA was very good.

10 **2.2 Weather station**~~The weather station is located on the roof of the building Exakte Wissenschaften of the University of Bern. The coordinates of the weather station are 46.95~~MERRA-2 reanalysis data

The Modern-Era Retrospective Analysis for Research and Applications, version 2 (MERRA-2) is an atmospheric reanalysis provided by NASA's Global Modeling and Assimilation Office (GMAO) (Gelaro et al., 2017). The MERRA-2 variable used in the present study is the latent heat flux (or total latent energy flux) at the grid point (47°N, 7.447.5°E, 575 m a.s.l. It is a

15 ~~Vaisala Milos 500 station, and the observed parameters are temperature, relative humidity, precipitation, pressure, wind speed, and wind direction. The temporal-~~ which is close to Bern. The time resolution of the weather data is 10 min., and the data have been stored since 1997. In 2017, a new weather station of the model Vaisala WXT 536 began the operation~~latent heat flux is one hour. The grid resolution of MERRA-2 is 0.5° in latitude and 0.625° in longitude.~~

3 Data analysis

20 The amplitude spectra of the temporal IWV fluctuations are computed by three different methods. Firstly, the fast Fourier Transform (FFT) spectrum of the summer 2010 is calculated. The arithmetic mean is removed from the time series of IWV. Then, the FFT spectrum is obtained by folding the IWV time series of summer 2010 with a Hamming window and by applying zero padding at the beginning and end of the time series. The FFT spectrum does not take into account the intermittency of the short wave trains of the IWV fluctuations.

25 A better method is the band pass filtering of the IWV time series with a digital non-recursive, finite impulse response (FIR) band pass filter performing zero-phase filtering by processing the time series in forward and reverse directions. The number of filter coefficients corresponds to a time window of three times the central period, and a Hamming window of equal length has been selected for the filter. Thus, the band pass filter has a fast response time to temporal changes in the data series. The variable choice of the filter order permits the analysis of wave trains with a resolution that matches their scale. The bandpass cutoff frequencies are at $f_c = f_p \pm 10\%f_p$, where f_p is the central frequency. More details about the bandpass filtering are given by Studer et al. (2012).

30

The third method for the estimation of the strength of the IWV fluctuations is a moving standard deviation where the time window length is subsequently changed from 0.5 min to 90 min.

4 Results and discussion

5 The main effect investigated in the present study is that short-term IWV fluctuations occur at daytime in summer (June - August) while they disappear at night. Figure 1a shows a convective cloud system which appears near to Bern in the afternoon of 28 June 2010. We assume that water vapour convection, turbulence and convection cells induce the short-term fluctuations of IWV. Figure 1b shows the IWV time series for six days in summer 2010 observed by the TROWARA radiometer. It is obvious that the short-term IWV fluctuations are enhanced during daytime. This main effect can be better shown if the IWV series is
10 band pass filtered at a period of 15 min. Figure 1c depicts the mean amplitude of the IWV fluctuations in the period range from 10 to 20 min. The amplitude of the 15 min-IWV fluctuations is four times greater during daytime than at night.

4.1 Spectra of IWV fluctuations

Figure 2 shows the amplitude spectra derived by FFT analysis (blue) and by the band pass filtering method (black) of the IWV series during summer 2010. It is obvious that the FFT method underestimates the amplitude of the IWV fluctuations by 1-2
15 magnitudes. Further, the exponent of the power law is -2 for the FFT spectrum and -1 for the band pass filter method. Since the FFT method does not take into account the intermittency of the IWV wave trains, the results of the band pass filter method are better than those of the FFT method.

Figure 3 depicts the seasonal variations of the amplitude spectra of the IWV fluctuations in 2010. As expected the summer spectrum (June - August, black line) is the strongest one. The spectra of spring and fall (red and blue) are close together while
20 the winter spectrum (green) is below the other spectra at periods greater than 2 min. At periods > 7 min the four power spectra fulfill the power law $P \sim f^{-1}$ which is indicated by the magenta line.

Another method to characterize the IWV fluctuations is the moving standard deviation with a variable time window length. The time window length is a bit similar to the period. The four seasonal spectra of the standard deviation SD are shown as function of the time window length in Fig. 4. Using the SD method, we find a similar power law $P \sim f^{-1}$ as indicated by the
25 magenta line. The SD values in Fig. 4 are about two times larger than the amplitude values in Fig. 3. In the following, we only present results derived by the SD method. The SD values in Fig. 4 are in a good agreement with those of Fig. 8 in Steinke et al. (2015). In the following, we focus on the third method (SD values) since the standard deviation is most common for the characterization of the variability of a time series.

4.2 Seasonal variation of IWV fluctuations and relation to latent heat flux

30 Figure 5 shows the diurnal variation of SD for a time window length of 10 min and for the different seasons in 2010. It is obvious that the IWV fluctuations are strongest during summer and weakest during winter. During spring, summer and fall there is a maximum of SD during the afternoon hours (around 14:00 -15:00 CET). During winter (green), there is no clear

maximum or minimum of SD. In addition, there is a noise floor in summer since the SD of the IWV fluctuations does not vanish during nighttime. The noise floor is higher during summer than in winter.

The weather station at University of Bern is used to investigate if the diurnal variation of SD of IWV is related to the seasonal variation of the diurnal cycle of the short-term fluctuations of specific kinetic energy e_k . Such a relationship is likely since the IWV fluctuations is possibly related to the annual variation in solar heating of the Earth's surface during daytime in summer. Surface heating leads to increased turbulence, convection, and upward water vapour flux during daytime. The increased water vapour flux is possibly associated with short-term IWV fluctuations observed by TROWARA.

We derive e_k by assuming $e_k(t) \sim 0.5(u(t)^2 + v(t)^2)$ where we neglect the small vertical wind component since the weather station measures the horizontal wind speed. The moving standard deviation of e_k is computed with a time window of 20 min. Figure 6 shows the results. It is obvious that the curves have their daily maxima in the afternoon hours. Figure 6 shows the diurnal cycle of the latent heat flux in winter, spring, summer and fall as derived from MERRA-2 reanalysis data close to Bern in the year 2010. As expected, the diurnal cycle of latent heat flux is strongest in summer. The maximum latent heat flux is around 14:13:00 CET. In so far, the CET. That means the observed diurnal cycle of the short-term IWV fluctuations of specific kinetic energy e_k might be the cause for the lags the diurnal cycle of latent heat flux by 1-2 hours. A numerical simulation by Schlemmer et al. (2011) showed that the diurnal variation in solar short wave radiation leads the diurnal cycle of latent heat flux which is followed by the diurnal cycles of CAPE (convective available potential energy) and the convective mass flux. The maxima of the curves in CAPE and convective mass flux occurred in the afternoon and evening hours.

These observations and simulations suggest that the increase of short-term IWV fluctuations during daytime in summer is due to the diurnal cycle of latent heat flux which is a precondition for an increase of strong and variable convection cells in the afternoon. The up- and downdraft regions of the convection cells are passing the antenna beam of the TROWARA radiometer which consequently measures larger or smaller values of IWV in time distances of about 10 min. In addition, a convection cell is itself time variable: The lifetime of a convection cell is roughly between 30 and 60 minutes (Gaiotti et al., 2007).

Figure 7 compares the 3-day averages of SD of IWV (moving 10 min-window) in the IWV fluctuations.

It is obvious that the spring curve (red) is larger than the summer curve (black) in Fig. 6. This effect can be due to stronger advection in spring than in summer. We can show that the specific kinetic energy is larger during the spring months than during the summer months. Figure 7 shows the climatologies of e_k and SD of e_k which are maximal during the spring months. This is in agreement with the order of curves in Fig. 6. However, since the annual maximum of IWV is in upper panel with 3-day averages of MERRA-2 latent heat flux at Bern in the summer months, the maximal water vapour convection occurs during summer and not during spring. The daily cycle of the lower panel for the year 2010. The correlation coefficient r of SD(IWV) and the latent heat flux is equal to 0.82. Some of the peaks in the latent heat flux coincidentally appear in the SD curve of short-term fluctuations of e_k explains the daily cycle of the IWV variability in the upper panel, e.g., the double peak around June 2010. Figure 7 suggests that the variability of the latent heat flux is a contributor to the short-term IWV fluctuations variability of IWV.

5 Conclusions

During summer, we often see that IWV has temporal fluctuations during daytime while the night-time data ~~are without have~~ smaller fluctuations. We derive the spectrum of the IWV fluctuations in the period range from about 1 to 100 min. The FFT spectrum with a window size of 3 months leads to a serious underestimation of the spectral amplitudes of the fluctuations. Thus, we apply a band pass filtering method to derive the amplitudes as a function of period T_p . The amplitudes are proportional to $T_p^{0.5}$ corresponding to a power law $P \sim f^{-1}$ where f is the frequency. Another method is the ~~computation calculation~~ of the moving standard deviation (SD) with time window lengths from about 1 to 100 min. Here, we get similar results as for the band pass filtering method. At all periods, the IWV fluctuations are strongest during summer while they are smallest during winter. However, the mean SD value is smaller than 0.5 mm for time window lengths less than 90 min. We derive the diurnal variation of the short-term IWV fluctuations by applying a moving standard deviation with a window length of 10 min. The daily cycle is strongest during the summer season with standard deviations up to 0.22 mm at about 14:00 CET. The diurnal cycle disappears during winter time. ~~Using the meteorological weather station at Bern, we derive~~ A similar seasonal behaviour is obvious in the diurnal cycle of latent heat flux at Bern as provided by MERRA-2 reanalysis. Further, the curves of SD(IWV) and the latent heat flux yield a correlation coefficient r of 0.82 at Bern in 2010.

~~Thus, we suggest that~~ the diurnal cycle of the short-term ~~fluctuations of the specific kinetic energy e_k . Since these data have~~ a temporal resolution of 10 min, we apply a 20 min-moving standard deviation. The derived IWV fluctuations is mainly caused by the diurnal cycle of latent heat flux which is a precondition for strong and variable convection cells in the afternoon during summer. The spatio-temporal variability of the convection cells induces the diurnal cycle of short-term ~~e_k fluctuations can be regarded as a proxy of turbulent kinetic energy (TKE). During summer, IWV fluctuations as observed by the TROWARA radiometer at Bern in summer. However, other sources such as eddies in the lower troposphere may also contribute to the~~ 20 min-moving standard deviation of e_k increases during daytime and has a similar diurnal cycle like the short-term ~~IWV fluctuations. Thus, we conclude that~~ variability of IWV. High resolution modelling of the diurnal cycle of ~~the~~ short-term IWV fluctuations ~~is caused by turbulence associated with large convective heating during daytime in summer. The observed behaviour of the short-term IWV fluctuations is useful for modeling studies on water vapour convection in~~ could be compared to the TROWARA observations so that one can estimate how good convective processes are represented by the model. Generally, we think that the high resolution IWV observations of TROWARA can contribute to research on the atmospheric boundary layer.

Code availability. Programs are available from KH upon request.

5 *Data availability.* High resolution IWV data of TROWARA are available upon request. Data of the EXWI weather station are provided by the startwave H2O database (<http://www.iapmw.unibe.ch/research/projects/STARTWAVE/>).

Author contributions. KH performed the data analysis. All authors contribute to the interpretation of the results.

Competing interests. We have no competing interests.

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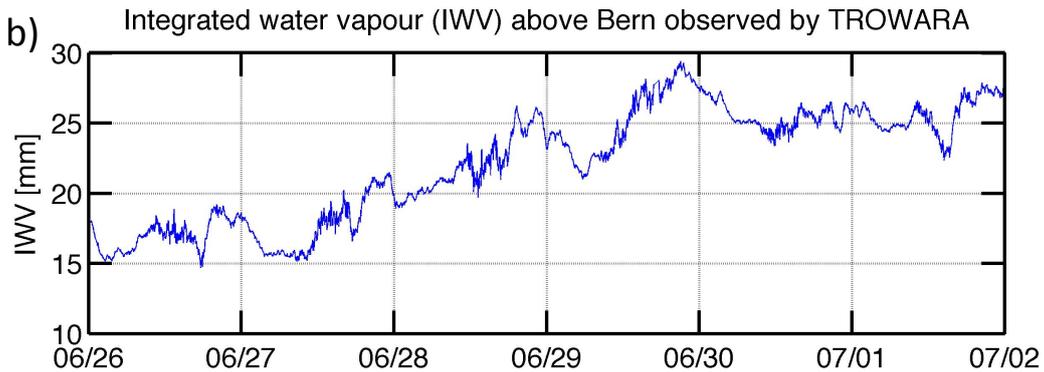
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a)



b)



c)

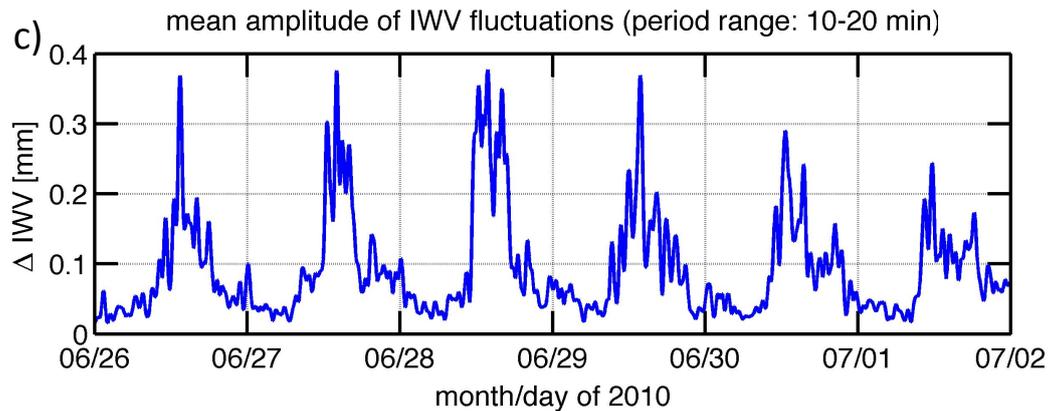


Figure 1. a) The convection cell built up within 45 minutes in the south of Bern on June, 28 2010 (picture was taken at 16:36 UT). b) Integrated water vapour (IWV) as function of time (month/day) observed by the Tropospheric Water Radiometer (TROWARA) at Bern. IWV fluctuations regularly occurred between 10 and 18 UT. ~~The high-frequency fluctuations are likely associated to the onset of thermal convective activity.~~ c) Mean amplitudes of the bandpass-filtered IWV fluctuations (period range 10 to 20 min) show a strong diurnal variation. Day ticks are at 0:00 UT.

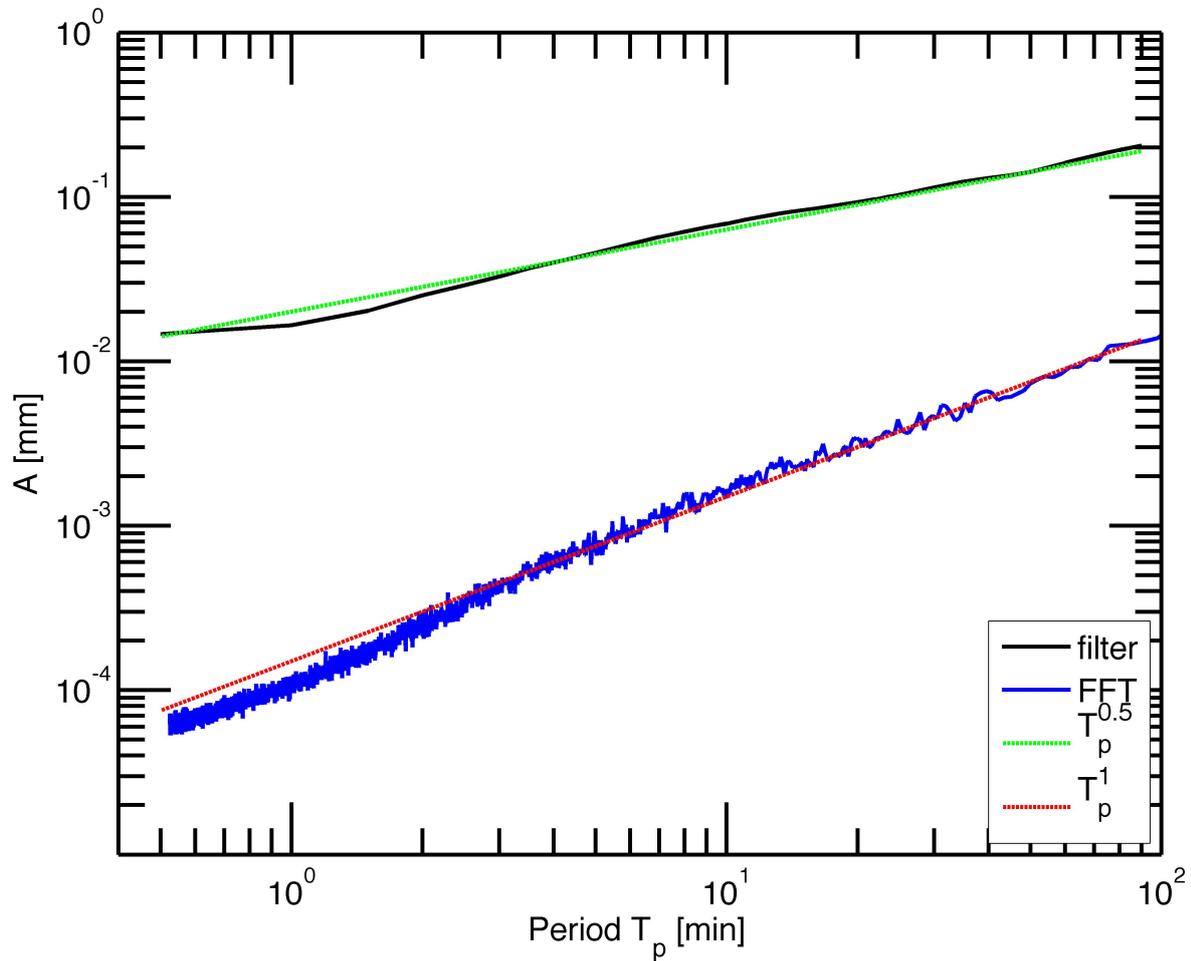


Figure 2. Amplitude spectra of IWV fluctuations observed at Bern in summer 2010. The solid black line is obtained by a band pass filtering method. The green line shows the inclination for $A \sim T_p^{0.5}$ where T_p is the period. The corresponding power law is given by $P \sim f^{-1}$ where f is the frequency. The blue line is obtained by a Fast Fourier Transform of the complete summer 2010 time interval. The red line shows the inclination for $A \sim T_p^1$ (or power $P \sim f^{-2}$). The FFT method underestimates the amplitudes and overestimates the steepness of the inclination.

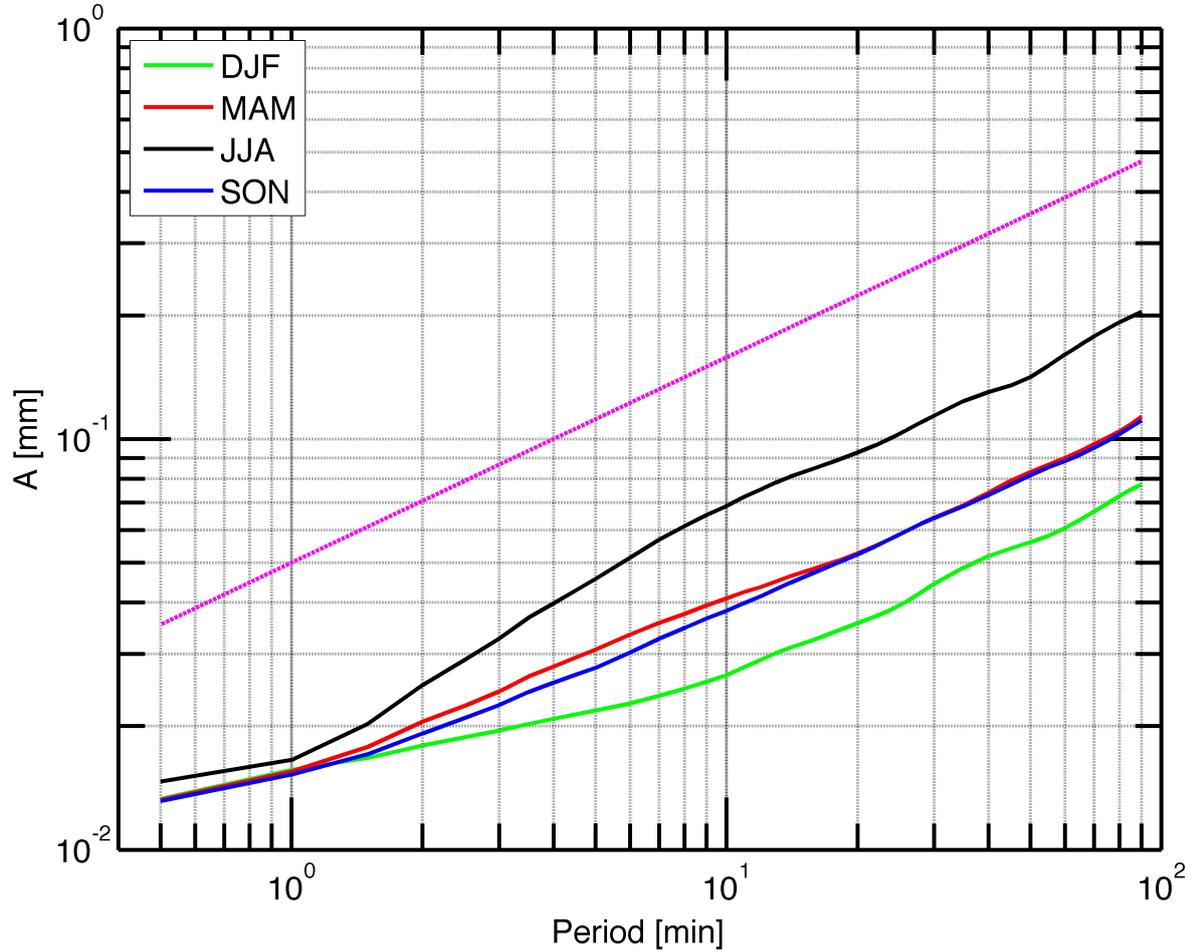


Figure 3. Amplitude spectra of IWV fluctuations observed at Bern for the four seasons of the year 2010. The green, red, blue and black line is obtained by a band pass filtering method for winter, spring, autumn and summer respectively. The magenta line shows the inclination for $A \sim T_p^{0.5}$ (or power $P \sim f^{-1}$) where f is the frequency and T_p is the period.

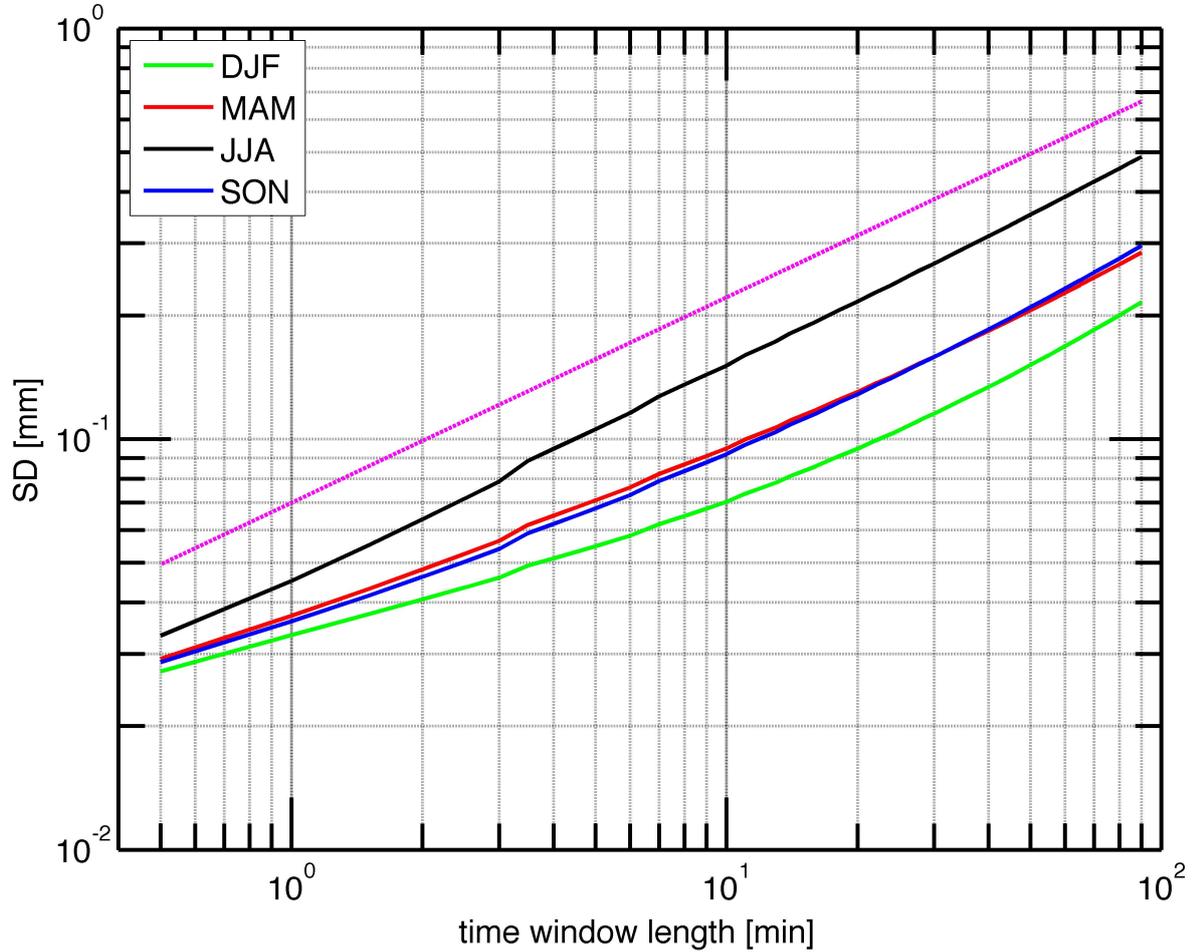


Figure 4. Spectra of IWV fluctuations observed at Bern for the four seasons of the year 2010. The green, red, black and blue line is obtained by a moving standard deviation (SD) with a variable time window length for winter, spring, summer and autumn respectively. The magenta line shows the inclination for $A \sim T_p^{0.5}$ (or power $P \sim f^{-1}$) where f is the frequency and T_p is the period.

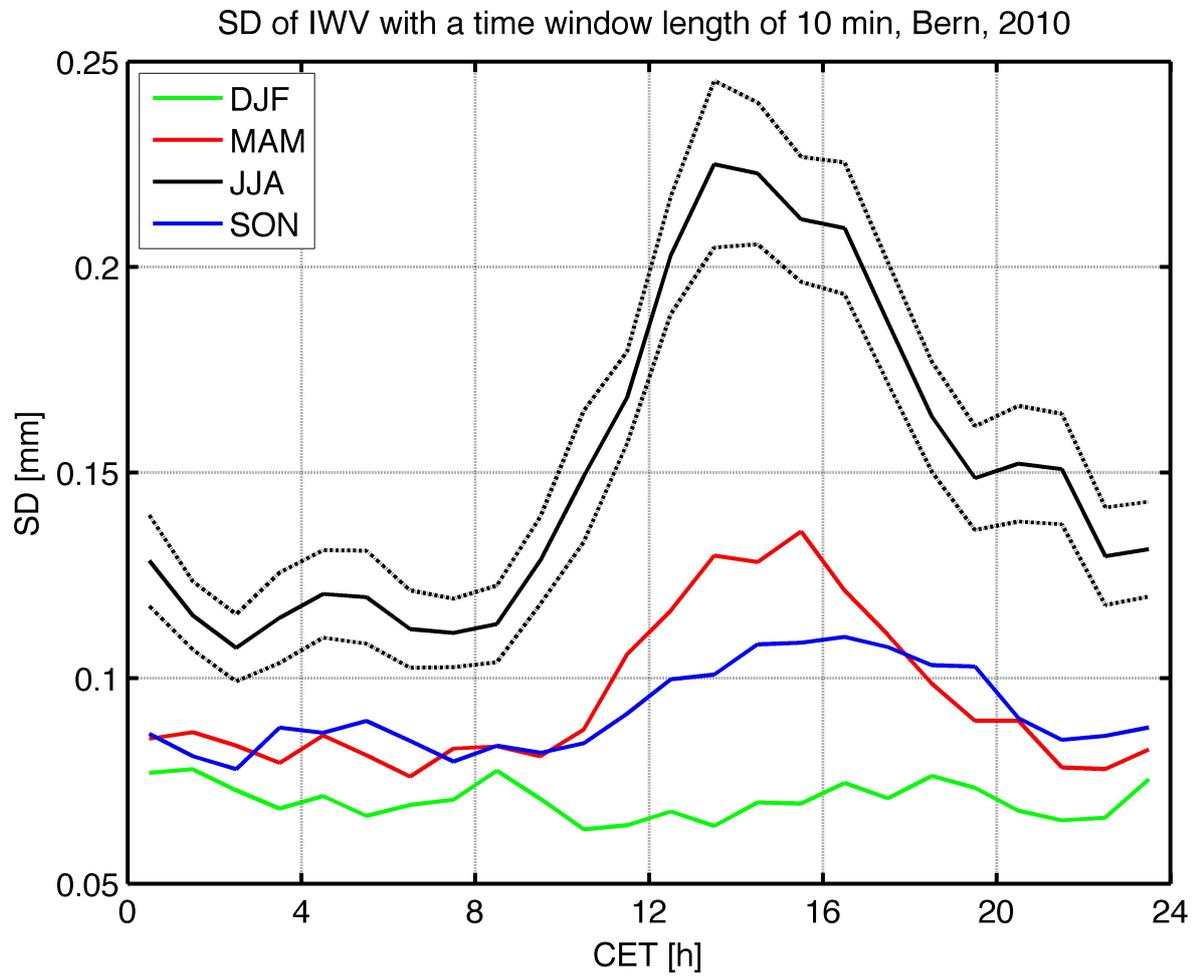


Figure 5. Diurnal cycle of IWV fluctuations observed at Bern for the four seasons of the year 2010 (moving standard deviation SD with time window length of 10 min). The green, red, blue and black line is for winter, spring, autumn and summer respectively. CET stands for Central European Time (Universal Time +1 hour). The error of the mean (for hourly averages) is shown for the summer season (JJA) by the dashed black lines.

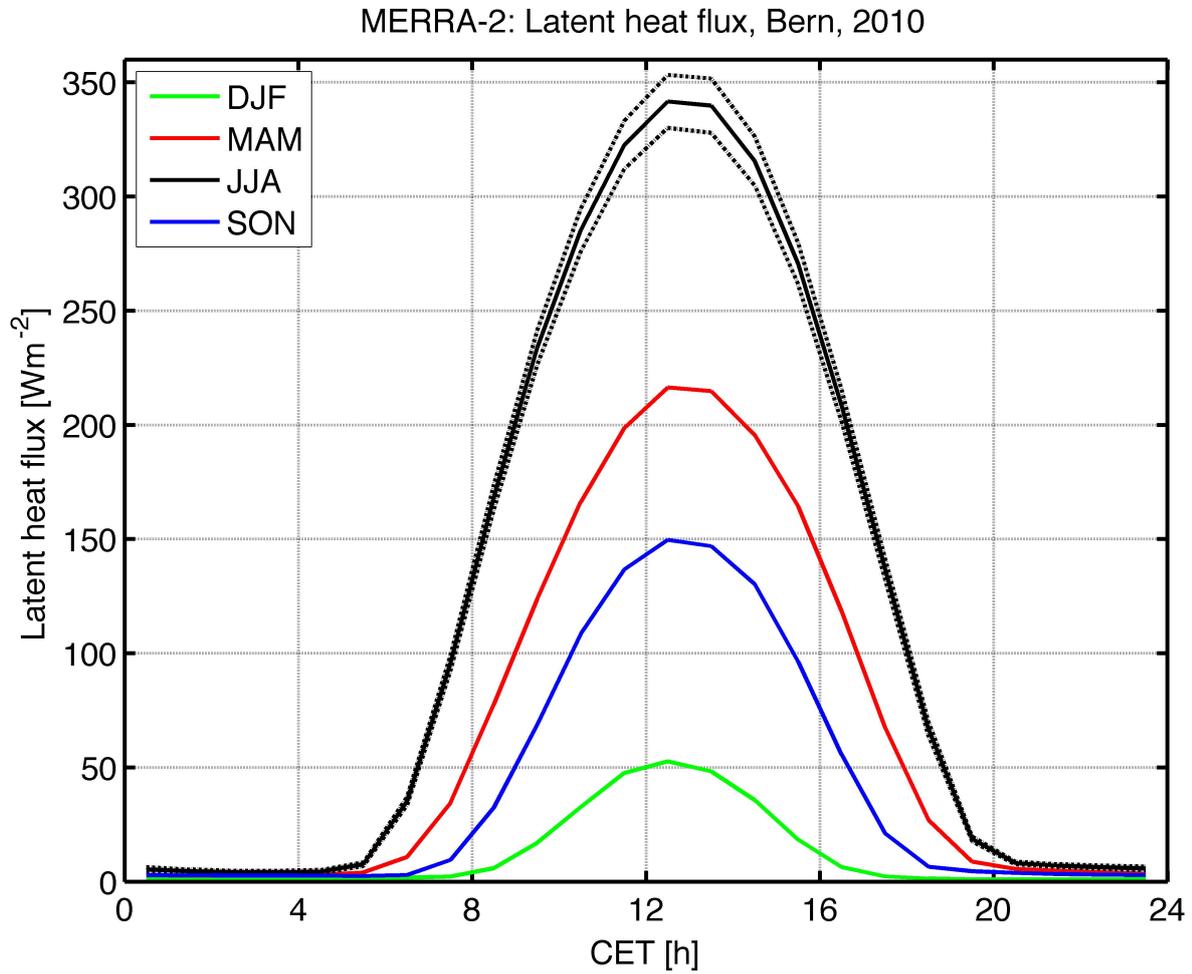


Figure 6. Diurnal cycle of short-term fluctuations of specific kinetic energy e_k latent heat flux near to Bern for different seasons as derived from MERRA-2 reanalysis data. The moving standard deviation error of the mean (SD for hourly averages) of e_k was computed with a time window of 20 min. e_k was estimated is shown for the summer season (JJA) by using the horizontal wind speed measurements with a temporal resolution of 10 min from the weather station on the roof of the university building at Bern dashed black lines.

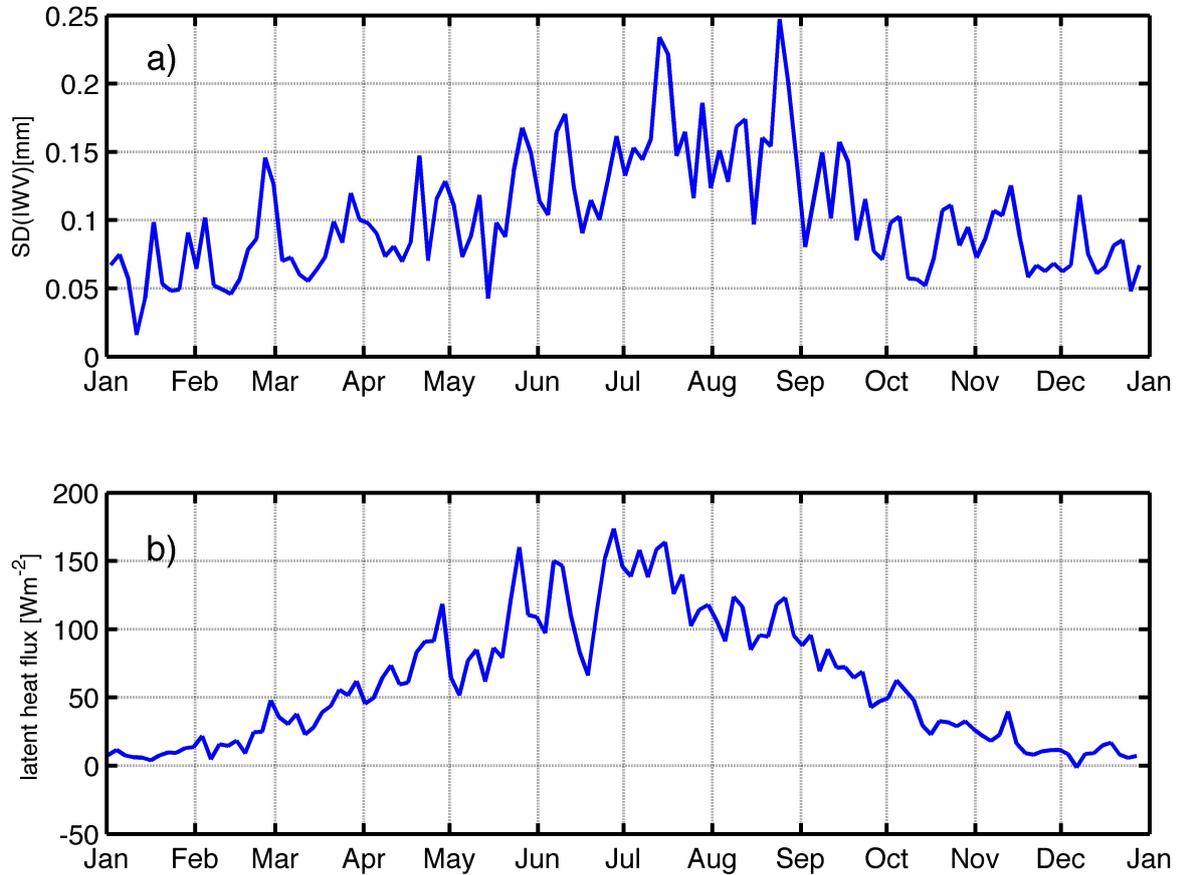


Figure 7. Mean annual cycle of specific kinetic energy e_k (lower panel) and standard deviation 3-day averages of e_k (upper panel) at the weather station magnitude of University of Bern. The standard deviation the short-term IWV variability (moving SD) of e_k was computed IWV with a moving time window of 20-10 min. Both curves are averaged window) observed by a 30-day moving average. Data TROWARA at Bern in 2010. 3-day averages of the time interval from 1997 latent heat flux near to 2018 were taken for the climatology. Bern derived from MERRA-2 reanalysis data in 2010.