

1 **Quantifying the nitrogen isotope effects during photochemical**
2 **equilibrium between NO and NO₂: implications for δ¹⁵N in**
3 **tropospheric reactive nitrogen**

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11 **Abstract.** Nitrogen isotope fractionations between nitrogen oxides (NO and NO₂) play a
12 significant role in determining the nitrogen isotopic compositions (δ¹⁵N) of atmospheric reactive
13 nitrogen. Both the equilibrium isotopic exchange between NO and NO₂ molecules and the isotope
14 effects occurring during the NO_x photochemical cycle are important, but both are not well
15 constrained. The nighttime and daytime isotopic fractionations between NO and NO₂ in an
16 atmospheric simulation chamber at atmospherically relevant NO_x levels were measured. Then, the
17 impact of NO_x level and NO₂ photolysis rate to the combined isotopic fractionation (equilibrium
18 isotopic exchange and photochemical cycle) between NO and NO₂ were calculated. It was found
19 that the isotope effects occurring during the NO_x photochemical cycle can be described using a
20 single fractionation factor, designated the Leighton Cycle Isotope Effect (LCIE). The results
21 showed that at room temperature, the fractionation factor of nitrogen isotopic exchange is
22 1.0275±0.0012, and the fractionation factor of LCIE (when O₃ solely controls the oxidation from
23 NO to NO₂) is 0.990±0.005. The measured LCIE factor showed good agreement with previous
24 field measurements, suggesting that it could be applied in ambient environment, although future
25 work is needed to assess the isotopic fractionation factors of NO + RO₂/HO₂ → NO₂. The results
26 were used to model the NO-NO₂ isotopic fractionations under several NO_x conditions. The model
27 suggested that isotopic exchange was the dominate factor when NO_x >20 nmol mol⁻¹, while LCIE
28 was more important at low NO_x concentrations (<1 nmol mol⁻¹) and high rates of NO₂ photolysis.
29 These findings provided a useful tool to quantify the isotopic fractionations between tropospheric
30 NO and NO₂, which can be applied in future field observations and atmospheric chemistry models.

31

32

33 1. Introduction

34 The nitrogen isotopic composition ($\delta^{15}\text{N}$) of reactive nitrogen compounds in the
35 atmosphere is an important tool in understanding the sources and chemistry of atmospheric NO_x
36 ($\text{NO}+\text{NO}_2$). It has been suggested that the $\delta^{15}\text{N}$ value of atmospheric nitrate (HNO_3 , nitrate
37 aerosols and nitrate ions in the precipitation and snow) imprints the $\delta^{15}\text{N}$ value of NO_x sources
38 (Elliott et al., 2009; Kendall et al., 2007) thus many studies have used the $\delta^{15}\text{N}$ values of
39 atmospheric nitrate to investigate NO_x sources (Chang et al., 2018; Felix et al., 2012; Felix &
40 Elliott, 2014; Gobel et al., 2013; Hastings et al., 2004, 2009; Morin et al., 2009; Park et al., 2018;
41 Walters et al., 2015, 2018). However, there remain questions about how isotopic fractionations
42 that may occur during photochemical cycling of NO_x could alter the $\delta^{15}\text{N}$ values as it partitions
43 into NO_y (NO_y = atmospheric nitrate, NO_3 , N_2O_5 , HONO , etc., Chang et al., 2018; Freyer, 1991;
44 Hastings et al., 2004; Jarvis et al., 2008; Michalski et al., 2005; Morin et al., 2009; Zong et al.,
45 2017). Similarly, other complex reactive nitrogen chemistry, such as nitrate photolysis and re-
46 deposition in ice and snow (Frey et al., 2009), may impact the $\delta^{15}\text{N}$ of NO_y and atmospheric nitrate.
47 The fractionation between NO and NO_2 via isotope exchange has been suggested to be the
48 dominant factor in determining the $\delta^{15}\text{N}$ of NO_2 and ultimately atmospheric nitrate (Freyer, 1991;
49 Freyer et al., 1993; Savarino et al., 2013; Walters et al., 2016). However, isotopic fractionations
50 occur in most, if not all, NO_x and NO_y reactions, while most of these are still unknown or, if
51 calculated (Walters and Michalski, 2015), unverified by experiments. Since the atmospheric
52 chemistry of NO_y varies significantly in different environments (e.g., polluted vs. pristine, night
53 vs. day), the isotopic fractionations associated with NO_y chemistry are also likely to vary in
54 different environments. These unknowns could potentially bias conclusions about NO_x source
55 apportionment reached when using nitrogen isotopes. Therefore, understanding the isotopic

56 fractionations between NO and NO₂ during photochemical cycling could improve our
57 understanding of the relative role of sources versus chemistry for controlling the δ¹⁵N variations
58 of atmospheric NO₂ and nitrate.

59 In general, there are three types of isotopic fractionation effects associated with NO_x
60 chemistry (Fig. 1A). The first type is the equilibrium isotopic effect (EIE), i.e., isotope exchange
61 between two compounds without forming new molecules (Urey, 1947, Bigeleisen and Mayer,
62 1947), which for nitrogen isotopes in the NO_x system is the $^{15}\text{NO} + ^{14}\text{NO}_2 \leftrightarrow ^{14}\text{NO} + ^{15}\text{NO}_2$
63 exchange reaction (Begun and Melton, 1956, Walters et al., 2016). The second type is the kinetic
64 isotopic effect (KIE) associated with difference in isotopologue rate coefficients during
65 unidirectional reactions (Bigeleisen & Wolfsberg, 1957). In the NO_x system this KIE would
66 manifest in the oxidation of NO into NO₂ by O₃/HO₂/RO₂. The third type is the photochemical
67 isotope fractionation effect (PHIFE, Miller & Yung, 2000), which for NO_x is the isotopic
68 fractionation associated with NO₂ photolysis. All three fractionations could impact the δ¹⁵N value
69 of NO₂, and consequently atmospheric nitrate, but the relative importance of each may vary.

70 The limited number of studies on the EIE in the NO_x cycle have significant uncertainties.
71 Discrepancies in the EIE for $^{15}\text{NO} + ^{14}\text{NO}_2 \leftrightarrow ^{14}\text{NO} + ^{15}\text{NO}_2$ have been noted in several studies.
72 Theoretical calculations predicted isotope fractionation factors (α) ranging from 1.035 to 1.042 at
73 room temperature (Begun & Fletcher, 1960; Monse et al., 1969; Walters & Michalski, 2015) due
74 to the different approximations used to calculate harmonic frequencies in each study. Likewise,
75 two separate experiments measured different room temperature fractionation factors of
76 1.028 ± 0.002 (Begun & Melton, 1956) and 1.0356 ± 0.0015 (Walters et al., 2016). A concern in both
77 experiments is that they were conducted in small chambers with high NO_x concentrations
78 (hundreds of μmol mol⁻¹), significantly higher than typical ambient atmospheric NO_x levels

79 (usually less than $0.1 \mu\text{mol mol}^{-1}$). Whether the isotopic fractionation factors determined by these
80 experiments are applicable in the ambient environment is uncertain because of possible wall effects
81 and formation of higher oxides, notably N_2O_4 and N_2O_3 at these high NO_x concentrations.

82 Even less research has examined the KIE and PHIFE occurring during NO_x cycling. The
83 KIE of $\text{NO} + \text{O}_3$ has been theoretically calculated (Walters and Michalski, 2016) but has not been
84 experimentally verified. The NO_2 PHIFE has not been experimentally determined or theoretically
85 calculated. As a result, field observation studies often overlook the effects of PHIFE and KIE.
86 Freyer et al. (1993) measured NO_x concentrations and the $\delta^{15}\text{N}$ values of NO_2 over a 1-year period
87 at Jülich, Germany and inferred a combined NO_x isotope fractionation factor (EIE+KIE+PHIFE)
88 of 1.018 ± 0.001 . Freyer et al. (1993) suggested that the NO_x photochemical cycle (KIE and PHIFE)
89 tends to diminish the equilibrium isotopic fractionation (EIE) between NO and NO_2 . Even if this
90 approach were valid, applying this single fractionation factor elsewhere, where NO_x , O_3
91 concentrations and actinic fluxes are different, would be tenuous given that these factors may
92 influence the relative importance of EIE, KIE and PHIFE (Hastings et al., 2004; Walters et al.,
93 2016). Therefore, to quantify the overall isotopic fractionations between NO and NO_2 at various
94 tropospheric conditions, it is crucial to know 1) isotopic fractionation factors of EIE, KIE and
95 PHIFE individually and 2) the relative importance of each factor under various conditions.

96 In this work, we aim to quantify the nitrogen isotope fractionation factors between NO and
97 NO_2 at photochemical equilibrium. First, we measure the N isotope fractionations between NO
98 and NO_2 in an atmospheric simulation chamber at atmospherically relevant NO_x levels. Then, we
99 provide mathematical solutions to assess the impact of NO_x level and NO_2 photolysis rate ($j(\text{NO}_2)$)
100 to the relative importance of EIE, KIE and PHIFE. Subsequently we use the solutions and chamber
101 measurements to calculate the isotopic fractionation factors of EIE, KIE and PHIFE. Lastly, using

102 the calculated fractionation factors and the equations, we model the NO-NO₂ isotopic
103 fractionations at several sites to illustrate the behavior of $\delta^{15}\text{N}$ values of NO_x in the ambient
104 environment.

105

106 **2. Methods**

107 The experiments were conducted using a 10 m³ Atmospheric Simulation Chamber at the
108 National Center for Atmospheric Research (see descriptions in Appendix A and Zhang et al.
109 (2018)). A set of mass flow controllers was used to inject NO and O₃ into the chamber. NO was
110 injected at 1 L min⁻¹ from an in-house NO/N₂ cylinder (133.16 $\mu\text{mol mol}^{-1}$ NO in ultra-pure N₂),
111 and O₃ was generated by flowing 5 L min⁻¹ zero-air through a flow tube equipped with a UV Pen-
112 Ray lamp (UVP LLC., CA) into the chamber. NO and NO₂ concentrations were monitored in real
113 time by chemiluminescence with a detection limit of 0.5 ppb (model CLD 88Y, Eco Physics, MI)
114 as were O₃ concentrations using an UV absorption spectroscopy with a detection limit of 0.5 ppb
115 (model 49, Thermo Scientific, CO). In each experiment, the actual amounts of NO and O₃ injected
116 were calculated using measured NO_x and O₃ concentrations after steady state was reached (usually
117 within 1 h). The wall loss rate of NO₂ was tested by monitoring O₃ (29 nmol mol⁻¹) and NO_x (62
118 nmol mol⁻¹) over a 4-hour period. After the NO and NO₂ concentrations reached steady state, no
119 decrease in NO₂ concentrations was observed showing that chamber wall loss was negligible.

120 Two sets of experiments were conducted to separately investigate the EIE, KIE and PHIFE.
121 The first set of experiments was conducted in the dark. In each of these dark experiments, a range
122 of NO and O₃ ($[\text{O}_3] < [\text{NO}]$) was injected into the chamber to produce NO-NO₂ mixtures with
123 $[\text{NO}]/[\text{NO}_2]$ ratios ranging from 0.43 to 1.17. The N isotopes of these mixtures were used to
124 investigate the EIE between NO and NO₂. The second set of experiments was conducted under

125 irradiation of UV lights (300-500 nm, see Appendix A for irradiation spectrum). Under such
126 conditions, NO, NO₂ and O₃ reached photochemical steady state, which combined the isotopic
127 effects of EIE, KIE and PHIFE. In addition, three experiments were conducted to measure the δ¹⁵N
128 value of the tank NO. In each of these experiments, a certain amount of O₃ was first injected into
129 the chamber, then approximately the same amount of NO was injected into the chamber to ensure
130 100% of the NO_x was in the form of NO₂ with little O₃ (<3 nmol mol⁻¹) remaining in the chamber,
131 such that the O₃+NO₂ reaction was negligible. The NO₂ in the chamber was then collected and its
132 δ¹⁵N value measured, which equates to the δ¹⁵N value of the tank NO.

133 In all experiments, the concentrations of NO, NO₂ and O₃ were allowed to reach steady
134 state, and the product NO₂ was collected from the chamber using a honeycomb denuder tube. After
135 the NO, NO₂ and O₃ concentrations reached steady-state, well-mixed chamber air was drawn out
136 through a Norprene Thermoplastic tubing ~40 cm at 10 L min⁻¹ and passed through a honeycomb
137 denuder system (Chemcomb 3500, Thermo Scientific). Based on flow rate, the NO₂ residence time
138 in the was less than 0.5 second, thus in the light-on experiments where NO and O₃ coexisted, the
139 NO₂ produced inside the transfer tube through NO+O₃ reactions should be <0.03 ppb (using the
140 upper limit of NO and O₃ concentrations in our experiments). The honeycomb denuder system
141 consisted of two honeycomb denuder tubes connected in series. Each honeycomb denuder tube is
142 a glass cylinder of 38 mm long, 47 mm in diameter, and consist of 212 hexagonal tubes with inner
143 diameters of 2 mm. Before collecting samples, each denuder tube was coated with a solution of
144 10% KOH and 25% guaiacol in methanol and then dried by flowing N₂ gas through the denuder
145 tube for 15 seconds (Williams and Grosjean, 1990, Walters et al., 2016). The NO₂ reacted with
146 guaiacol coating and was converted into NO₂⁻ that was retained on the denuder tube wall (Williams
147 and Grosjean, 1990). NO was inert to the denuder tube coating: a control experiment sampled pure

148 NO using the denuder tubes, which did not show any measurable NO_2^- . The NO_2 collection
149 efficiency of a single honeycomb denuder tube was tested in another control experiment: air
150 containing 66 nmol mol^{-1} of NO_2 was drawn out of the chamber through a denuder tube, and the
151 NO_2 concentration at the exit of the tube holder was measured and found to be below the detection
152 limit ($<1 \text{ nmol mol}^{-1}$), suggesting the collection efficiency was nearly 100% when $[\text{NO}_2] < 66 \text{ nmol}$
153 mol^{-1} . Furthermore, when the denuder system consisted of two denuder tubes in series and NO_2^- in
154 the second denuder was below the detection limit indicating trivial NO_2 breakthrough. Each NO_2
155 collection lasted for 0.5-3 hours in order to collect enough NO_2^- for isotopic analysis ($\sim 300 \text{ nmol}$).
156 After collection, the NO_2^- was leached from each denuder tube by rinsing thoroughly with 10 ml
157 deionized water into a clean polypropylene container and stored frozen until isotopic analysis.
158 Isotopic analysis was conducted at Purdue Stable Isotope Laboratory. For each sample,
159 approximately 50 nmol of the NO_2^- extract was mixed with 2 M sodium azide solution in acetic
160 acid buffer in an air-tight glass vial, then shaken overnight to completely reduce all the NO_2^- to
161 $\text{N}_2\text{O}_{(g)}$ (Casciotti & McIlvin, 2007; McIlvin & Altabet, 2005). The product N_2O was directed into
162 a Thermo GasBench equipped with cryo-trap, then the $\delta^{15}\text{N}$ of the N_2O was measured using a
163 Delta-V Isotope Ratios Mass Spectrometer. Six coated denuders tubes that did not get exposed to
164 NO_2 were also analyzed using the same chemical procedure, which did not show any measurable
165 signal on the IRMS, suggesting the blank from both sampling process and the chemical conversion
166 process was negligible. The overall analytical uncertainty for $\delta^{15}\text{N}$ analysis was 0.5 ‰ (1σ) based
167 on replicate analysis of in house NO_2^- standards.

168

169 **3. Results and Discussions**

170 **3.1. Equilibrium Isotopic Fractionation between NO and NO_2**

171 The equilibrium isotope fractionation factor, $\alpha(\text{NO}_2\text{-NO})$, is the ^{15}N enrichment in NO_2
 172 relative to NO , and is expressed as the ratio of rate constants k_2/k_1 of two reactions:



175 where k_1 is the rate constant of the isotopic exchange, which was previously determined to be
 176 $8.14 \times 10^{-14} \text{ cm}^3 \text{ s}^{-1}$ (Sharma et al., 1970). The reaction time required for NO-NO_2 to reach isotopic
 177 equilibrium was estimated using the exchange rate constants in a simple kinetics box model
 178 (BOXMOX, Knote et al., 2015). The model predicts that at typical NO_x concentrations used during
 179 the chamber experiments ($7.7\text{-}62.4 \text{ nmol mol}^{-1}$), isotopic equilibrium would be reached within 15
 180 minutes (see Appendix B). Since the sample collection usually started 1 hour after NO_x was well
 181 mixed in the chamber, there was sufficient time to reach full isotope equilibrium. The isotope
 182 equilibrium fractionation factor ($\alpha(\text{NO}_2\text{-NO})$) is then calculated to be:

183
$$\alpha(\text{NO}_2 - \text{NO}) = \frac{[^{15}\text{NO}_2][^{14}\text{NO}]}{[^{14}\text{NO}_2][^{15}\text{NO}]} = \frac{R(\text{NO}_2)}{R(\text{NO})} \quad \text{Eq. (1)}$$

184 where $R(\text{NO}, \text{NO}_2)$ are the $^{15}\text{N}/^{14}\text{N}$ ratios of NO and NO_2 . By definition, the
 185 $\delta^{15}\text{N}(\text{NO}) = (R(\text{NO})/R(\text{reference}) - 1) \times 1000 \text{ ‰}$ and $\delta^{15}\text{N}(\text{NO}_2) = (R(\text{NO}_2)/R(\text{reference}) - 1) \times 1000 \text{ ‰}$,
 186 but hereafter, the $\delta^{15}\text{N}$ values of NO , NO_2 and NO_x will be referred as $\delta(\text{NO})$, $\delta(\text{NO}_2)$ and $\delta(\text{NO}_x)$,
 187 respectively. Eq. (1) leads to:

188
$$\delta(\text{NO}_2) - \delta(\text{NO}) = (\alpha(\text{NO}_2 - \text{NO}) - 1) (1 + \delta(\text{NO})) \quad \text{Eq. (2)}$$

189 Using Eq. (2) and applying NO_x isotopic mass balance ($\delta(\text{NO}_x) = f(\text{NO}_2)\delta(\text{NO}_2) + (1 - f(\text{NO}_2))\delta(\text{NO})$),
 190 $f(\text{NO}_2) = [\text{NO}_2]/([\text{NO}] + [\text{NO}_2])$ yields:

191
$$\frac{\delta(\text{NO}_2) - \delta(\text{NO}_x)}{1 + \delta(\text{NO}_2)} = \frac{\alpha(\text{NO}_2 - \text{NO}) - 1}{\alpha(\text{NO}_2 - \text{NO})} (1 - f(\text{NO}_2)) \quad \text{Eq. (3)}$$

192 Here, $\delta(\text{NO}_x)$ equals to the $\delta^{15}\text{N}$ value of the cylinder NO and $f(\text{NO}_2)$ is the molar fraction of NO_2
193 with respect to total NO_x . Three experiments (see descriptions in method section) that measured
194 $\delta(\text{NO}_x)$ showed consistent $\delta(\text{NO}_x)$ values of $(-58.7 \pm 0.8) \text{‰}$ ($n = 3$), indicating $\delta(\text{NO}_x)$ remained
195 unchanged throughout the experiments (as expected for isotope mass balance). Thus, the $\delta(\text{NO}_x)$
196 can be treated as a constant in Eq. (3), and the linear regression of $(\delta(\text{NO}_2) - \delta(\text{NO}_x)) / (1 + \delta(\text{NO}_2))$
197 versus $1 - f(\text{NO}_2)$ should have an intercept of 0 and a slope of $(\alpha(\text{NO}_2 - \text{NO}) - 1) / \alpha(\text{NO}_2 - \text{NO})$.

198 The plot of $(\delta(\text{NO}_2) - \delta(\text{NO}_x)) / (1 + \delta(\text{NO}_2))$ as a function of $1 - f(\text{NO}_2)$ values from five
199 experiments yields an $\alpha(\text{NO}_2 - \text{NO})$ value of 1.0275 ± 0.0012 at room temperature (Fig. 1B). This
200 fractionation factor is comparable to previously measured values but with some differences. Our
201 result agrees well with the $\alpha(\text{NO}_2 - \text{NO})$ value of 1.028 ± 0.002 obtained by Begun and Melton (1956)
202 at room temperature. However, Walters et al., (2016) determined the $\alpha(\text{NO}_2 - \text{NO})$ values of NO-
203 NO_2 exchange in a 1-liter reaction vessel, which showed a slightly higher $\alpha(\text{NO}_2 - \text{NO})$ value of
204 1.035. This discrepancy might originate from rapid heterogeneous reactions on the wall of the
205 reaction vessel at high NO_x concentrations and the small chamber size used by Walters et al. (2016).
206 They used a reaction vessel made of Pyrex, which is known to absorb water (Do Remus et al.,
207 1983; Takei et al., 1997) that can react with NO_2 forming HONO, HNO_3 and other N compounds.
208 Additionally, previous studies have suggested that Pyrex walls enhance the formation rate of N_2O_4
209 by over an order of magnitude (Barney & Finlayson-Pitts, 2000; Saliba et al., 2001), which at
210 isotopic equilibrium is enriched in ^{15}N compared to NO and NO_2 (Walters & Michalski, 2015).
211 Therefore, their measured $\alpha(\text{NO}_2 - \text{NO})$ might be slightly higher than the actual $\alpha(\text{NO}_2 - \text{NO})$ value.
212 In this work, the 10 m^3 chamber has a much smaller surface to volume ratio relative to Walters et
213 al. (2016) which minimizes wall effects, and the walls were made of Teflon that minimize NO_2
214 surface reactivity, which was evidenced by the NO_2 wall loss control experiment. Furthermore,

215 the low NO_x mixing ratios in our experiments minimized N₂O₄ and N₂O₃ formation. At NO and
216 NO₂ concentrations of 50 nmol mol⁻¹ the steady state concentrations of N₂O₄ and N₂O₃ were
217 calculated to be 0.014 and 0.001 pmol mol⁻¹, respectively (Atkinson et al., 2004). Therefore, we
218 suggest our measured $\alpha(\text{NO}_2\text{-NO})$ value (1.0275±0.0012) may better reflect the room temperature
219 (298 K) NO-NO₂ EIE in the ambient environment.

220 Unfortunately, the chamber temperature could not be controlled so we were not able to
221 investigate the temperature dependence of the EIE. Hence, we speculate that the $\alpha(\text{NO}_2\text{-NO})$
222 follows a similar temperature dependence pattern calculated in Walters et al. (2016). Walters et al.
223 (2016) suggested that, the $\alpha(\text{NO}_2\text{-NO})$ value would be 0.0047 higher at 273 K and 0.002 lower at
224 310 K, relative to room temperature (298 K). Using this pattern and our experimentally determined
225 data, we suggest the $\alpha(\text{NO}_2\text{-NO})$ values at 273 K, 298 K and 310 K are 1.0322±0.0012,
226 1.0275±0.0012 and 1.0255±0.0012, respectively. This 0.0067 variation at least partially contribute
227 to the daily and seasonal variations of $\delta^{15}\text{N}$ values of NO₂ and nitrate in some areas (e.g., polar
228 regions with strong seasonal temperature variation). Thus, future investigations should be
229 conducted to verify the EIE temperature dependence.

230

231 **3.2. Kinetic isotopic fractionation of Leighton Cycle**

232 The photochemical reactions of NO_x will compete with the isotope exchange fractionations
233 between NO and NO₂. The NO-NO₂ photochemical cycle in the chamber was controlled by the
234 Leighton cycle: NO₂ photolysis and the NO + O₃ reaction. This is because there were no VOCs in
235 the chamber so no RO₂ was produced, which excludes the NO + RO₂ reaction. Likewise, the low
236 water vapor content (RH<10%) and the minor flux of photons < 310 nm results in minimal OH
237 production and hence little HO₂ formation and subsequently trivial amount of NO₂ would be

238 formed by NO + HO₂. Applying these limiting assumptions, the EIE between NO and NO₂ (R1-
 239 R2) were only competing with the KIE (R3-R4) and the PHIFE in R5-R6:



244 In which $j(\text{NO}_2)$ is the NO₂ photolysis rate ($1.4 \times 10^{-3} \text{ s}^{-1}$ in these experiments), k_5 is the rate constant
 245 for the NO+O₃ reaction ($1.73 \times 10^{-14} \text{ cm}^3 \text{ s}^{-1}$, Atkinson et al., 2004), and $\alpha_{1,2}$ are isotopic
 246 fractionation factors for the two reactions. Previous studies (Freyer et al., 1993; Walters et al.,
 247 2016) have attempted to assess the competition between EIE (R1-R2), KIE and PHIFE (R3-R6),
 248 but none of them quantified the relative importance of the two processes, nor were α_1 or α_2 values
 249 experimentally determined. Here we provide the mathematical solution of EIE, KIE and PHIFE to
 250 illustrate how R1-R6 affect the isotopic fractionations between NO and NO₂.

251 First, the NO₂ lifetime with respect to isotopic exchange with NO (τ_{exchange}) and photolysis
 252 (τ_{photo}) was determined:

253
$$\tau_{\text{exchange}} = \frac{1}{k_1 [\text{NO}]}$$
 Eq. (4)

254
$$\tau_{\text{photo}} = \frac{1}{j(\text{NO}_2)}$$
 Eq. (5)

255 We then define an A factor:

256
$$A = \begin{cases} \frac{\tau_{\text{exchange}}}{\tau_{\text{photo}}} & \text{when } j(\text{NO}_2) \neq 0 \\ 0 & \text{when } j(\text{NO}_2) = 0 \end{cases}$$
 Eq. (6)

257 Using R1-R6 and Eq. (1)-(6), we solved steady-state $\delta(\text{NO}_2)$ and $\delta(\text{NO})$ values (see calculations
 258 in Appendix C). Our calculations show that the $\delta(\text{NO}_2)$ - $\delta(\text{NO})$ and $\delta(\text{NO}_2)$ - $\delta(\text{NO}_x)$ values at steady
 259 state can be expressed as functions of α_1 , α_2 , $\alpha(\text{NO}_2\text{-NO})$ and A:

$$260 \quad \delta(\text{NO}_2) - \delta(\text{NO}) = \frac{(\alpha_2 - \alpha_1)A + (\alpha(\text{NO}_2\text{-NO}) - 1)}{A + 1} (1 + \delta(\text{NO})) \quad \text{Eq. (7)}$$

$$261 \quad \delta(\text{NO}_2) - \delta(\text{NO}_x) = \frac{(\alpha_2 - \alpha_1)A + (\alpha(\text{NO}_2\text{-NO}) - 1)}{A + 1} (1 + \delta(\text{NO}))(1 - f(\text{NO}_2)) \quad \text{Eq. (8)}$$

262 Equation (7) shows the isotopic fractionation between NO and NO₂ ($\delta(\text{NO}_2)$ - $\delta(\text{NO})$) is determined
 263 by A, the EIE factor ($\alpha(\text{NO}_2\text{-NO})-1$) and the $(\alpha_2-\alpha_1)$ factor assuming $(1+\delta(\text{NO}))$ is close to 1. This
 264 $(\alpha_2-\alpha_1)$ represents a combination of KIE and PHIFE, suggesting they act together as one factor;
 265 therefore, we name the $(\alpha_2-\alpha_1)$ factor Leighton Cycle Isotopic Effect, i.e., LCIE. Using measured
 266 $(\delta(\text{NO}_2)-\delta(\text{NO}))/ (1+\delta(\text{NO}))$ values, A values, and the previously determined EIE factor, we
 267 calculated that the best fit for the LCIE factor was $(-10 \pm 5) \text{‰}$ (showing the lowest Rooted Mean
 268 Square Error, RMSE, of 1.1‰, Fig. 1C). The uncertainties in the LCIE factor are relatively higher
 269 than that of the EIE factor, mainly because of the accumulated analytical uncertainties at low NO_x
 270 and O₃ concentrations, and low A values (0.10-0.28) due to the relatively low $j(\text{NO}_2)$ value
 271 ($1.4 \times 10^{-3} \text{ s}^{-1}$) under the chamber irradiation conditions.

272 This LCIE factor determined in our experiments is in good agreement with theoretical
 273 calculations. Walters and Michalski (2016) previously used an *ab initio* approach to determine an
 274 α_2 value of 0.9933 at room temperature, 0.9943 at 237 K and 0.9929 at 310 K. The total variation
 275 of α_2 values from 273 K to 310 K is only 1.4 ‰, significantly smaller than our experimental
 276 uncertainty ($\pm 5 \text{‰}$). The α_1 value was calculated using a ZPE shift model (Miller & Yung, 2000)
 277 to calculate the isotopic fractionation of NO₂ by photolysis. Briefly, this model assumes both
 278 isotopologues have the same quantum yield function and the PHIFE was only caused by the
 279 differences in the ¹⁵NO₂ and ¹⁴NO₂ absorption cross-section as a function of wavelength, thus α_1

280 values do not vary by temperature. The $^{15}\text{NO}_2$ absorption cross-section was calculated by shifting
281 the $^{14}\text{NO}_2$ absorption cross-section by the $^{15}\text{NO}_2$ zero-point energy (Michalski et al., 2004). When
282 the ZPE shift model was used with the irradiation spectrum of the chamber lights, the resulting α_1
283 value was 1.0023. Therefore, the theoretically predicted $\alpha_2-\alpha_1$ value should be -0.0090, i.e., (-
284 9.0 ± 0.7) ‰ when temperature ranges from 273 K to 310 K. This result shows excellent agreement
285 with our experimentally determined room temperature $\alpha_2-\alpha_1$ value of (-10 ± 5) ‰.

286 This model was then used to evaluate the variations of α_1 value to different lighting
287 conditions. The TUV model (TUV5.3.2, Madronich & Flocke, 1999) was used to calculate the
288 solar wavelength spectrum at three different conditions: early morning/late afternoon (solar zenith
289 angle=85 degree), mid-morning/afternoon (solar zenith angle=45 degree), noon (solar zenith
290 angle=0 degree). These spectrums were used in the ZPE shift model to calculate the α_1 values,
291 which are 1.0025, 1.0028, and 1.0029 at solar zenith angles of 85, 45 and 0 degree, respectively.
292 These values, along with the predicted α_1 value in the chamber, showed a total span of 0.6‰
293 (1.0026 ± 0.0003), which is again significantly smaller than our measured uncertainty. Therefore,
294 we suggest that our experimentally determined LCIE factor ((-10 ± 5) ‰) can be used in most
295 tropospheric solar irradiation spectrums.

296 The equations can also be applied in tropospheric environments to calculate the combined
297 isotopic fractionations of EIE and LCIE for NO and NO_2 . First, the NO_2 sink reactions (mainly
298 NO_2+OH in the daytime) are at least 2-3 orders of magnitude slower than the Leighton cycle and
299 the NO- NO_2 isotope exchange reactions (Walters et al., 2016), therefore their effects on the $\delta(\text{NO}_2)$
300 should be minor. Second, although the conversion of NO into NO_2 in the ambient environment is
301 also controlled by $\text{NO} + \text{RO}_2$ and HO_2 in addition to $\text{NO}+\text{O}_3$ (e.g., King et al., 2001), Eq. (7) still
302 showed good agreement with field observations in previous studies. Freyer et al. (1993)

303 determined the annual average daytime $\delta(\text{NO}_2)$ - $\delta(\text{NO})$ at Julich, Germany along with average
304 daytime NO concentration (9 nmol mol^{-1} , similar to our experimental conditions) to be
305 $(+18.03 \pm 0.98) \text{ ‰}$. Using Eq. (7), assuming the daytime average $j(\text{NO}_2)$ value throughout the year
306 was $(5.0 \pm 1.0) \times 10^{-3}$, and a calculated A value from measured NO_x concentration ranged from 0.22-
307 0.33, the average NO- NO_2 fractionation factor was calculated to be $(+18.8 \pm 1.4) \text{ ‰}$ (Fig. 1C), in
308 excellent agreement with the measurements in the present study. This agreement suggests the
309 $\text{NO} + \text{RO}_2/\text{HO}_2$ reactions might have similar fractionation factors as $\text{NO} + \text{O}_3$. Therefore, we suggest
310 Eq. (7) and (8) can be used to estimate the isotopic fractionations between NO and NO_2 in the
311 troposphere.

312

313 **3.3 Calculating nitrogen isotopic fractionations of NO- NO_2**

314 First, Eq. (7) was used to calculate the $\Delta(\text{NO}_2\text{-NO}) = \delta(\text{NO}_2) - \delta(\text{NO})$ at a wide range of
315 NO_x concentrations, $f(\text{NO}_2)$ and $j(\text{NO}_2)$ values (Fig. 2A-D), assuming $(1 + \delta(\text{NO})) = 1$. $j(\text{NO}_2)$
316 values of 0 s^{-1} (Fig. 2A), $1.4 \times 10^{-3} \text{ s}^{-1}$ (Fig. 2B), $5 \times 10^{-3} \text{ s}^{-1}$ (Fig. 2C) and $1 \times 10^{-2} \text{ s}^{-1}$ (Fig. 2D) were
317 selected to represent nighttime, dawn (as well as the laboratory conditions of our experiments),
318 daytime average and noon, respectively. Each panel represented a fixed $j(\text{NO}_2)$ value, and the
319 $\Delta(\text{NO}_2\text{-NO})$ values were calculated as a function of the A value, which was derived from NO_x
320 concentration and $f(\text{NO}_2)$. The A values have a large span, from 0 to 500, depending on the $j(\text{NO}_2)$
321 value and the NO concentration. When $A=0$ ($j(\text{NO}_2)=0$) and $f(\text{NO}_2) < 1$ (meaning NO- NO_2 coexist
322 and $[\text{O}_3]=0$), Eq. (7) and (8) become Eq. (2) and (3), showing the EIE was the sole factor, the
323 $\Delta(\text{NO}_2\text{-NO})$ values were solely controlled by EIE which has a constant value of $+27.5 \text{ ‰}$ at 298K
324 (Fig. 2A). When $j(\text{NO}_2) > 0$, the calculated $\Delta(\text{NO}_2\text{-NO})$ values showed a wide range from -10.0 ‰
325 (controlled by LCIE factor: $\alpha_2 - \alpha_1 = -10 \text{ ‰}$) to $+27.5 \text{ ‰}$ (controlled by EIE factor: $\alpha(\text{NO}_2\text{-NO}) - 1 =$

326 +27.5 ‰). Fig. 2B-D display the transition from a LCIE-dominated regime to an EIE-dominated
327 regime. The LCIE-dominated regime is characterized by low $[\text{NO}_x]$ ($<50 \text{ pmol mol}^{-1}$), representing
328 remote ocean areas and polar regions (Beine et al., 2002; Custard et al., 2015). At this range the A
329 value can be greater than 200, thus Eq. (7) can be simplified as: $\Delta(\text{NO}_2\text{-NO}) = \alpha_2 - \alpha_1$, suggesting
330 the LCIE almost exclusively controls the NO-NO₂ isotopic fractionation. The $\Delta(\text{NO}_2\text{-NO})$ values
331 of these regions are predicted to be $<0 \text{ ‰}$ during most time of the day and $< -5 \text{ ‰}$ at noon. On the
332 other hand, the EIE-dominated regime was characterized by high $[\text{NO}_x]$ ($>20 \text{ nmol mol}^{-1}$) and low
333 $f(\text{NO}_2)$ (< 0.6), representative of regions with intensive NO emissions, e.g., near roadside or stack
334 plumes (Clapp & Jenkin, 2001; Kimbrough et al., 2017). In this case, the τ_{exchange} are relatively
335 short (10-50 s) compared to the τ_{photo} (approximately 100 s at noon and 1000 s at dawn), therefore
336 the A values are small (0.01-0.5). The EIE factor in this regime thus is much more important than
337 the LCIE factor, resulting in high $\Delta(\text{NO}_2\text{-NO})$ values ($>20 \text{ ‰}$). Between the two regimes, both
338 EIE and LCIE are competitive and therefore it is necessary to use Eq. (7) to quantify the $\Delta(\text{NO}_2\text{-}$
339 NO) values.

340 Fig. 2 also implies that changes in the $j(\text{NO}_2)$ value can cause the diurnal variations in
341 $\Delta(\text{NO}_2\text{-NO})$ values. Changing $j(\text{NO}_2)$ would affect the value of A and consequently the NO-NO₂
342 isotopic fractionations in two ways: 1) changes in $j(\text{NO}_2)$ value would change the photolysis
343 intensity, therefore the τ_{photo} value; 2) in addition, changes in $j(\text{NO}_2)$ value would also alter the
344 steady state NO concentration, therefore changing the τ_{exchange} (Fig. 2C). The combined effect of
345 these two factors on the A value varies along with the atmospheric conditions, and thus needs to
346 be carefully calculated using NO_x concentration data and atmospheric chemistry models.

347 We then calculated the differences of $\delta^{15}\text{N}$ values between NO₂ and total NO_x, e.g. $\Delta(\text{NO}_2\text{-}$
348 NO_x) = $\delta(\text{NO}_2) - \delta(\text{NO}_x)$ in Fig. 2E-H. Since $\Delta(\text{NO}_2\text{-NO}_x)$ are connected through the observed $\delta^{15}\text{N}$

349 of NO₂ (or nitrate) to the δ¹⁵N of NO_x sources, this term might be useful in field studies (e.g.,
350 Chang et al., 2018; Zong et al., 2017). The calculated Δ(NO₂-NO_x) values (Fig. 2E-H) also showed
351 a LCIE-dominated regime at low [NO_x] and an EIE-dominated regime at high [NO_x]. The Δ(NO₂-
352 NO_x) values were dampened by the 1-*f*(NO₂) factor comparing to Δ(NO₂-NO), as shown in Eq.
353 (3) and (8): Δ(NO₂-NO_x) = Δ(NO₂-NO) (1-*f*(NO₂)). At high *f*(NO₂) values (>0.8), the differences
354 between δ(NO₂) and δ(NO_x) were less than 5 ‰, thus the measured δ(NO₂) values were similar to
355 δ(NO_x), although the isotopic fractionation between NO and NO₂ could be noteworthy. Some
356 ambient environments with significant NO emissions or high NO₂ photolysis rates usually have
357 *f*(NO₂) values between 0.4-0.8 (Mazzeo et al., 2005; Vicars et al., 2013). In this scenario, the
358 Δ(NO₂-NO_x) values in Fig. 2F-H showed wide ranges of -4.8 ‰ to +15.6 ‰, -6.0 ‰ to +15.0 ‰,
359 and -6.3 ‰ to +14.2 ‰ at *j*(NO₂)=1.4×10⁻³ s⁻¹, 5×10⁻³ s⁻¹, 1×10⁻² s⁻¹, respectively. These significant
360 differences again highlighted the importance of both LCIE and EIE (Eq. (7) and (8)) in calculating
361 the Δ(NO₂-NO_x). In the following discussion, we assume 1) the α₁ value remain constant (see
362 discussion above), 2) the NO+RO₂/HO₂ reactions have the same fractionation factors (α₂) as
363 NO+O₃, and 3) both EIE and LCIE do not display significant temperature dependence, then use
364 Equations (7) and (8) and this laboratory determined LCIE factor (-10 ‰) to calculate the nitrogen
365 isotopic fractionation between NO and NO₂ at various tropospheric atmospheric conditions.

366

367 4. Implications

368 The daily variations of Δ(NO₂-NO_x) values at two roadside NO_x monitoring sites were
369 predicted to demonstrate the effects of NO_x concentrations to the NO-NO₂ isotopic fractionations.
370 Hourly NO and NO₂ concentrations were acquired from a roadside site at Anaheim, CA
371 (<https://www.arb.ca.gov>) and an urban site at Evansville, IN (<http://idem.tx.sutron.com>) on July

372 25, 2018. The hourly $j(\text{NO}_2)$ values output from the TUV model (Madronich & Flocke, 1999) at
373 these locations was used to calculate the daily variations of $\Delta(\text{NO}_2\text{-NO}_x)$ values (Fig. 3A, B) by
374 applying Eq. (8) and assuming $(1+\delta(\text{NO}))=1$. Hourly NO_x concentrations were 12-51 nmol mol^{-1}
375 at Anaheim and 9-38 nmol mol^{-1} at Evansville and the $f(\text{NO}_2)$ values at both sites did not show
376 significant daily variations (0.45 ± 0.07 at Anaheim and 0.65 ± 0.08 at Evansville), likely because
377 the NO_x concentrations were controlled by the high NO emissions from the road (Gao, 2007). The
378 calculated $\Delta(\text{NO}_2\text{-NO}_x)$ values using Eq. (8) showed significant diurnal variations. During the
379 nighttime, the isotopic fractionations were solely controlled by the EIE, the predicted $\Delta(\text{NO}_2\text{-NO}_x)$
380 values were $(+14.5\pm 2.0)$ ‰ and $(+8.7\pm 2.1)$ ‰ at Anaheim and Evansville, respectively. During
381 the daytime, the existence of LCIE lowered the predicted $\Delta(\text{NO}_2\text{-NO}_x)$ values to $(+9.8\pm 1.7)$ ‰ at
382 Anaheim and $(+3.1\pm 1.5)$ ‰ at Evansville while the $f(\text{NO}_2)$ values at both sites remained similar.
383 The lowest $\Delta(\text{NO}_2\text{-NO}_x)$ values for both sites $(+7.0)$ ‰ and $(+1.7)$ ‰ occurred around noon when
384 the NO_x photolysis was the most intense. In contrast, if one neglects the LCIE factor in the daytime,
385 the $\Delta(\text{NO}_2\text{-NO}_x)$ values would be $(+12.9\pm 1.5)$ ‰ and $(+10.0\pm 1.6)$ ‰ respectively, an
386 overestimation of 3.1 ‰ and 6.9 ‰. These discrepancies suggested that the LCIE played an
387 important role in the NO- NO_2 isotopic fractionations and neglecting it could bias the NO_x source
388 apportionment using $\delta^{15}\text{N}$ of NO_2 or nitrate.

389 The role of LCIE was more important in less polluted sites. The $\Delta(\text{NO}_2\text{-NO}_x)$ values
390 calculated for a suburban site near San Diego, CA, USA, again using the hourly NO_x
391 concentrations (<https://www.arb.ca.gov>, Fig. 3C) and $j(\text{NO}_2)$ values calculated from the TUV
392 model. NO_x concentrations at this site varied from 1 to 9 nmol mol^{-1} and assuming $(1+\delta(\text{NO}))=1$.
393 During the nighttime, NO_x was in the form of NO_2 ($f(\text{NO}_2)=1$) because O_3 concentrations were
394 higher than NO_x , thus the $\delta(\text{NO}_2)$ values should be identical to $\delta(\text{NO}_x)$ ($\Delta(\text{NO}_2\text{-NO}_x)=0$). In the

395 daytime a certain amount of NO was produced by direct NO emission and NO₂ photolysis but the
396 $f(\text{NO}_2)$ was still high (0.73 ± 0.08). Our calculation suggested the daytime $\Delta(\text{NO}_2\text{-NO}_x)$ values
397 should be only ($+1.3 \pm 3.2$) ‰ with a lowest value of -1.3 ‰. These $\Delta(\text{NO}_2\text{-NO}_x)$ values were
398 similar to the observed and modeled summer daytime $\delta(\text{NO}_2)$ values in West Lafayette, IN
399 (Walters et al., 2018), which suggest the average daytime $\Delta(\text{NO}_2\text{-NO}_x)$ values at $\text{NO}_x = (3.9 \pm 1.2)$
400 nmol mol^{-1} should range from +0.1 ‰ to +2.4 ‰. In this regime, we suggest the $\Delta(\text{NO}_2\text{-NO}_x)$
401 values were generally small due to the significant contribution of LCIE and high $f(\text{NO}_2)$.

402 The LCIE should be the dominant factor controlling the NO-NO₂ isotopic fractionation at
403 remote regions, resulting in a completely different diurnal pattern of $\Delta(\text{NO}_2\text{-NO}_x)$ compared with
404 the urban-suburban area. Direct hourly measurements of NO_x at remote sites are rare, thus we used
405 total NO_x concentration of 50 pmol mol^{-1} , daily O₃ concentration of 20 nmol mol^{-1} at Summit,
406 Greenland (Dibb et al., 2002; Hastings et al., 2004; Honrath et al., 1999; Yang et al., 2002), and
407 assumed $(1 + \delta(\text{NO})) = 1$ and the conversion of NO to NO₂ was completely controlled by O₃ to
408 calculate the NO/NO₂ ratios. Here the isotopes of NO_x were almost exclusively controlled by the
409 LCIE due to the high A values (>110). The $\Delta(\text{NO}_2\text{-NO}_x)$ values displayed a clear diurnal pattern
410 (Fig. 3D) with highest value of -0.3 ‰ in the “nighttime” (solar zenith angle >85 degree) and
411 lowest value of -5.0 ‰ in the mid-day. This suggest that the isotopic fractionations between NO
412 and NO₂ were almost completely controlled by LCIE at remote regions, when NO_x concentrations
413 were $<0.1 \text{ nmol mol}^{-1}$. However, since the isotopic fractionation factors of nitrate-formation
414 reactions ($\text{NO}_2 + \text{OH}$, $\text{NO}_3 + \text{HC}$, $\text{N}_2\text{O}_5 + \text{H}_2\text{O}$) are still unknown, more studies are needed to fully
415 explain the daily and seasonal variations of $\delta(\text{NO}_3^-)$ at remote regions.

416 Nevertheless, our results have a few limitations. First, currently there are very few field
417 observations that can be used to evaluate our model, therefore, future field observations that

418 measure the $\delta^{15}\text{N}$ values of ambient NO and NO_2 should be carried out to test our model. Second,
419 more work, including theoretical and experimental studies, is needed to investigate the isotope
420 fractionation factors occurring during the conversion from NO_x to NO_y and nitrate: in the NO_y
421 cycle, EIE (isotopic exchange between NO_2 , NO_3 and N_2O_5), KIE (formation of NO_3 , N_2O_5 and
422 nitrate) and PHIFE (photolysis of NO_3 , N_2O_5 , HONO and sometimes nitrate) may also exist and
423 be relevant for the $\delta^{15}\text{N}$ of HNO_3 and HONO. In particular, the N isotope fractionation occurring
424 during the $\text{NO}_2 + \text{OH} \rightarrow \text{HNO}_3$ reaction needs investigation. Such studies could help us modeling
425 the isotopic fractionation between NO_x emission and nitrate, and eventually enable us to analyze
426 the $\delta^{15}\text{N}$ value of NO_x emission by measuring the $\delta^{15}\text{N}$ values of nitrate aerosols and nitrate in wet
427 depositions. Third, our discussion only focuses on the reactive nitrogen chemistry in the
428 troposphere, however, the nitrogen chemistry in the stratosphere is drastically different from the
429 tropospheric chemistry, thus future studies are also needed to investigate the isotopic fractionations
430 in the stratospheric nitrogen chemistry. Last, the temperature dependence of both EIE and LCIE
431 needs to be carefully investigated, because of the wide range of temperature in both troposphere
432 and stratosphere. Changes in temperature could alter the isotopic fractionation factors of both EIE
433 and LCIE, as well as contribute to the seasonality of isotopic fractionations between NO_x and NO_y
434 molecules.

435

436 **5. Conclusions**

437 The effect of NO_x photochemistry on the nitrogen isotopic fractionations between NO and
438 NO_2 was investigated. We first measured the isotopic fractionations between NO and NO_2 and
439 provided mathematical solutions to assess the impact of NO_x level and NO_2 photolysis rate ($j(\text{NO}_2)$)
440 to the relative importance of EIE and LCIE. The EIE and LCIE isotope fractionation factors, at

441 room temperature, were determined to be 1.0275 ± 0.0012 and 0.990 ± 0.005 , respectively. These
442 calculations and measurements can be used to determine the steady state $\Delta(\text{NO}_2\text{-NO})$ and $\Delta(\text{NO}_2\text{-}$
443 $\text{NO}_x)$ values at room temperature. Subsequently we applied our equations to polluted, clean and
444 remote sites to model the daily variations of $\Delta(\text{NO}_2\text{-NO}_x)$ values. We found that the $\Delta(\text{NO}_2\text{-NO}_x)$
445 values could vary from over +20 ‰ to less than -5 ‰ depending on the environment: in general,
446 the role of LCIE becoming more important at low NO_x concentrations, which tend to decrease the
447 $\Delta(\text{NO}_2\text{-NO}_x)$ values. Our work provided a mathematical approach to quantify the nitrogen isotopic
448 fractionations between NO and NO_2 that can be applied to many tropospheric environments, which
449 could help interpret the measured $\delta^{15}\text{N}$ values of NO_2 and nitrate in field observation studies.

450

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457 **Data Availability**

458 Data acquired from this study was deposited at Open Sciences Framework (Li, 2019,
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460 **Author contribution**

461 J. Li and G. Michalski designed the experiments, X. Zhang and J. Li conducted the
462 experiments. X. Zhang, G. Michalski, J. Orlando and G. Tyndall helped J. Li in interpreting the

463 results. The manuscript was written by J. Li and all the authors have contributed during the revision
464 of this manuscript.

465 **Competing interest**

466 The authors declare no competing interest.

467

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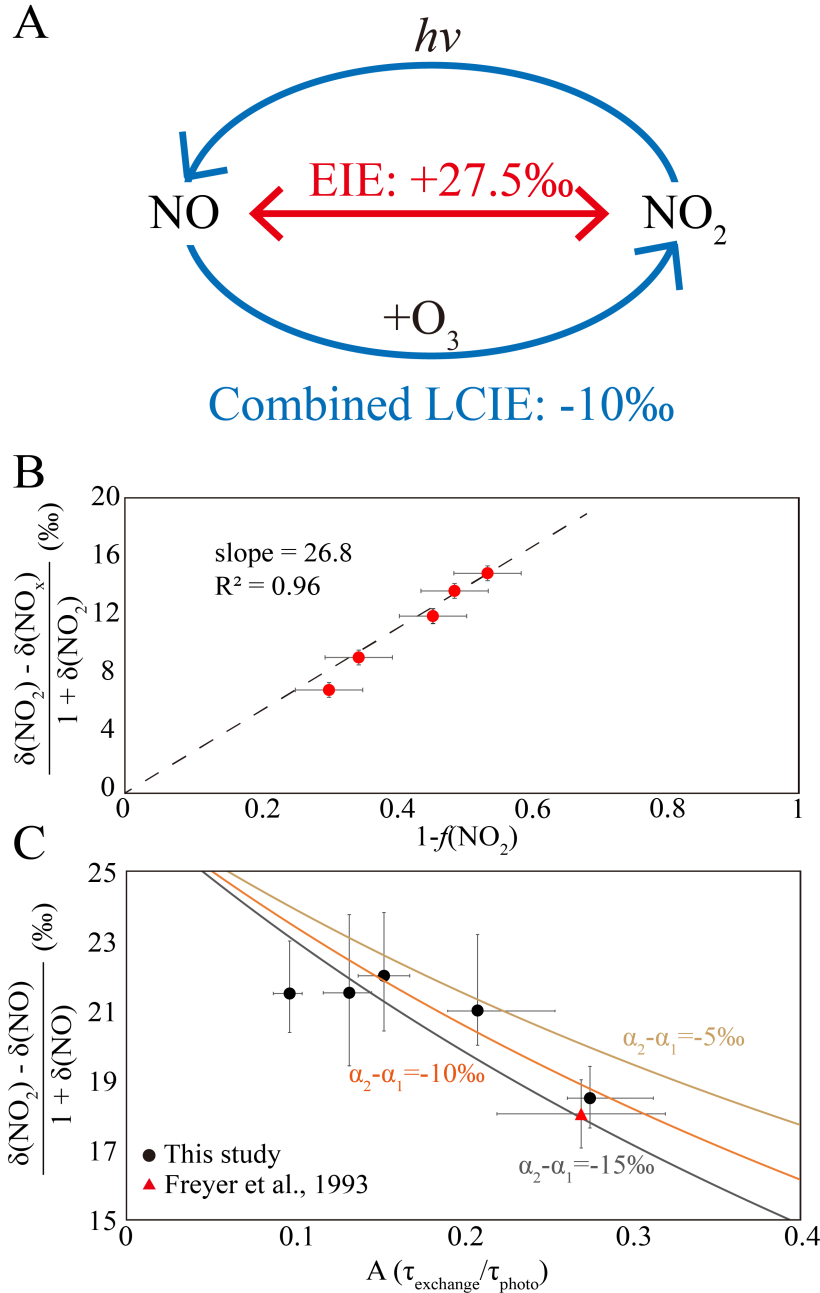
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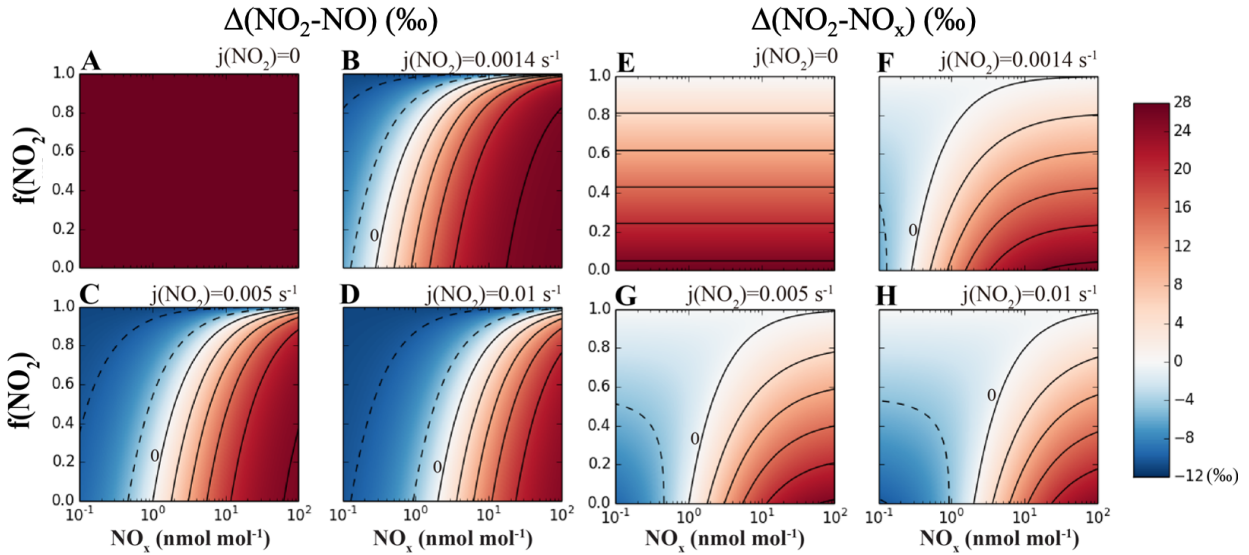
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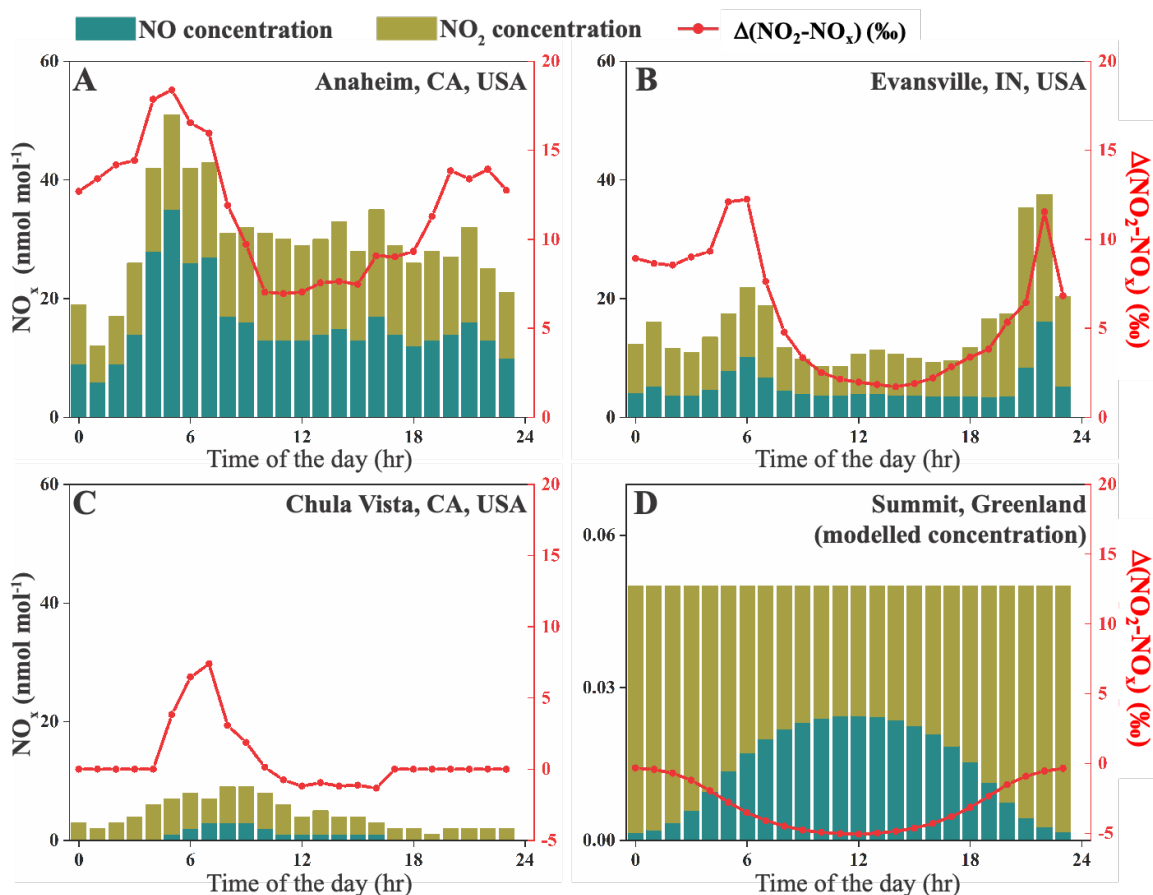


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Fig. 1 **A.** a sketch of the isotopic fractionation processes between NO and NO₂, both fractionation factors are determined in this work. **B.** Results from five dark experiments yielded a line with slope of 0.0268 and an $\alpha(\text{NO}_2\text{-NO})$ value of 1.0275; **C.** Results from five UV irradiation experiments (black points) and a previous field study (red triangle). The three lines represent different $(\alpha_2 - \alpha_1)$ values: the $(\alpha_2 - \alpha_1) = -10$ ‰ line showed the lowest RMSE to our experimental data as well as the previous field observation. The error bars in panels B and C represented the combined uncertainties of NO_x concentration measurements and isotopic analysis.



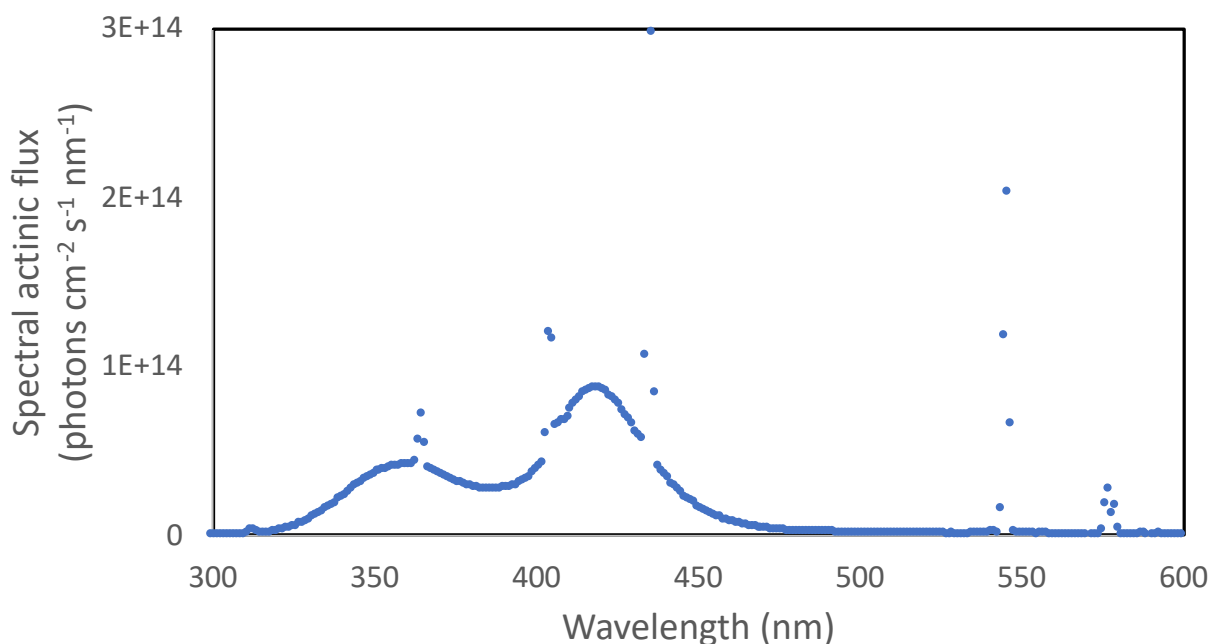
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 709 **Fig. 2** Calculating isotopic fractionation values between NO-NO₂ ($\Delta(\text{NO}_2\text{-NO})$, **A-D**) and NO_x-
 710 NO₂ ($\Delta(\text{NO}_2\text{-NO}_x)$, **E-H**) at various $j(\text{NO}_2)$, NO_x level and $f(\text{NO}_2)$ using Eq. (7) and (8). Each
 711 panel represents a fixed $j(\text{NO}_2)$ value (showing on the upper right side of each panel), and the
 712 fractionation values are shown by color. Lines are contours with the same fractionation values, at
 713 an interval of 5‰, the contour line representing 0‰ was marked on each panel except for A and
 714 E.



715
 716 **Fig. 3** NO_x concentrations and calculated $\Delta(\text{NO}_2-\text{NO}_x)$ values at four sites. Stacked bars show the
 717 NO and NO₂ concentrations extracted from monitoring sites (A-C) or calculated using 0-D box
 718 model (D); the red lines are $\Delta(\text{NO}_2-\text{NO}_x)$ values at each site. Note that the NO_x concentration (left-
 719 y) axis on panel D is different from the rest.
 720

721 **Appendix A. Chamber descriptions**

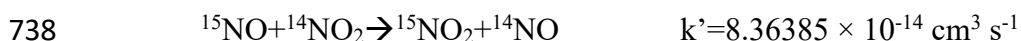
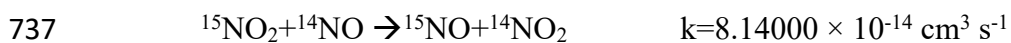
722 The chamber is a 10 m³ Teflon bag equipped with several standard instruments including
723 temperature and humidity probe, NO_x monitor and O₃ monitor. 128 wall-mounted blacklight tubes
724 surrounded the chamber to mimic tropospheric photochemistry and the photolysis rate of NO₂
725 ($j(\text{NO}_2)$) when all lights are on have been previously determined to be $1.4 \times 10^{-3} \text{ s}^{-1}$, similar to a
726 $j(\text{NO}_2)$ coefficient at an 81-degree solar zenith angle. The irradiation spectrum of the blacklights
727 are shown in Figure A1. The chamber was kept at room temperature and one atmospheric pressure.
728 Before each experiment, the chamber was flushed with zero air at 40 L min⁻¹ for at least 12 hours
729 to ensure the background NO_x, O₃ and other trace gases were below detection limit.
730



731
732 Figure A1 Spectral actinic flux versus wavelengths of the UV light source used in our experiments.
733

734 **Appendix B. Box model assessing the time needed for NO-NO₂ to reach isotopic equilibrium**

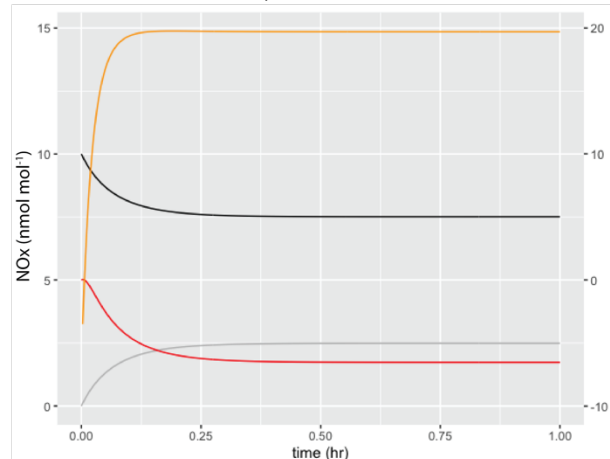
735 The time needed to reach NO-NO₂ isotopic equilibrium during light-off experiments were
736 assessed using a 0-D box model. This box model contains only two reactions:



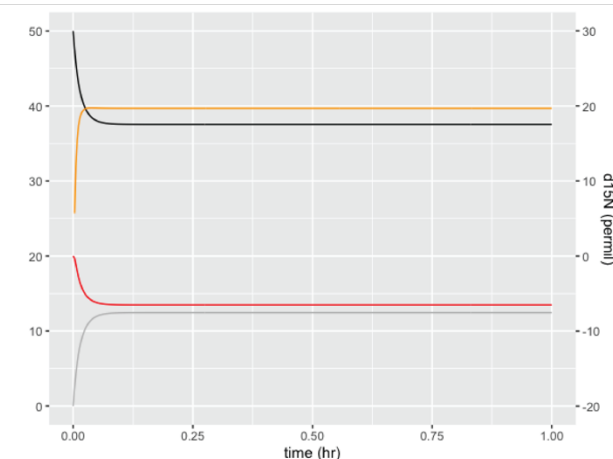
739 Where k and k' are rate constants of the reactions. The differences in rate constants were calculated
740 by assuming an $\alpha(\text{NO}_2\text{-NO})$ value of 1.0275. Six simulations were conducted at various initial NO
741 (with $\delta^{15}\text{N}=0\%$) and O₃ levels that were similar to our experiment. Then the $\delta^{15}\text{N}$ values of NO
742 and NO₂ during the simulation were calculated from the model and were shown in Figure B1,
743 suggesting that in our experimental condition, all systems should reach isotopic equilibrium within
744 1 hr.

745

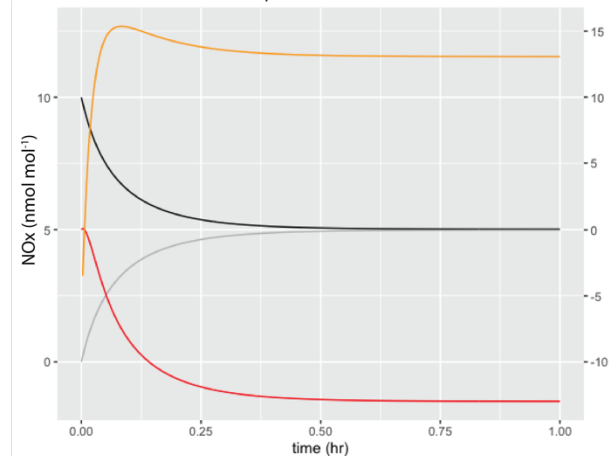
Initial NO=10 nmol mol⁻¹, O3=2.5 nmol mol⁻¹



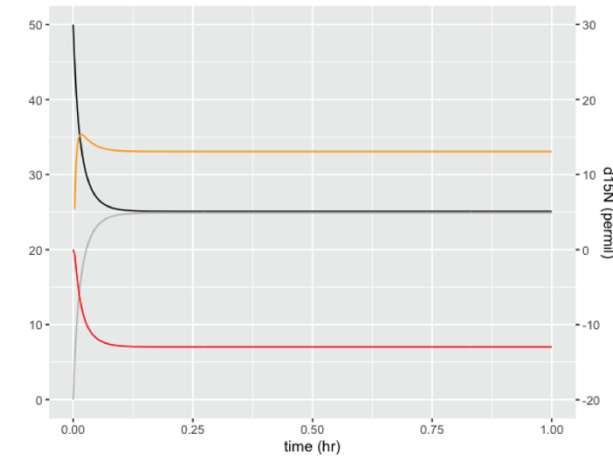
Initial NO=50 nmol mol⁻¹, O3=12.5 nmol mol⁻¹



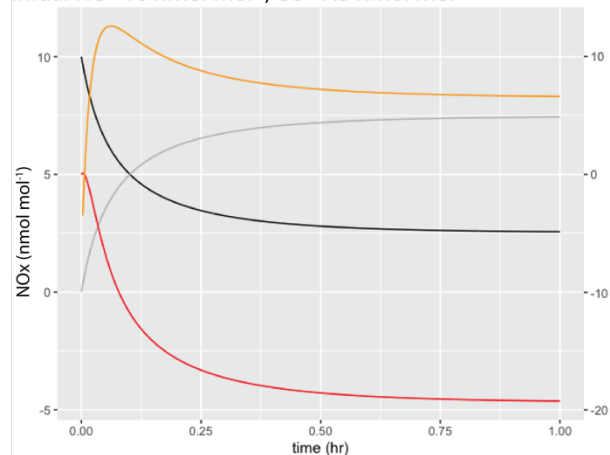
Initial NO=10 nmol mol⁻¹, O3=5 nmol mol⁻¹



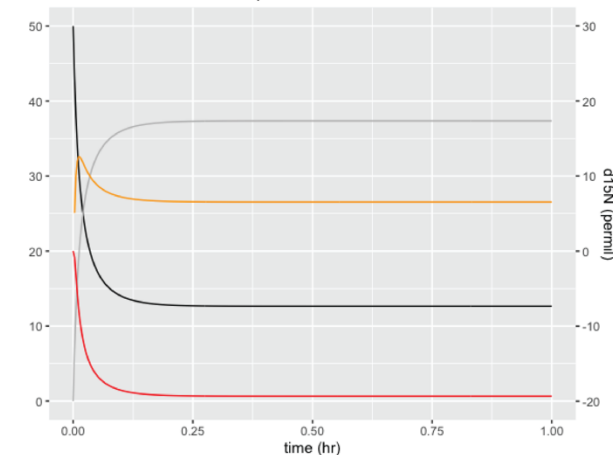
Initial NO=50 nmol mol⁻¹, O3=25 nmol mol⁻¹



Initial NO=10 nmol mol⁻¹, O3=7.5 nmol mol⁻¹



Initial NO=50 nmol mol⁻¹, O3=37.5 nmol mol⁻¹



746 — NO concentration — NO₂ concentration — δ(NO₂) — δ(NO)

747 Figure B1 Simulated NO-NO₂ isotopic equilibrium process in the chamber at various NO and O₃
748 concentrations.

749 **Appendix C. Deriving Equations 7 and 8**

750 When the system (R1-R6) reaches steady-state, we have:

751
$$d[^{15}\text{NO}_2]/dt=0 \quad \text{Eq. (C1)}$$

752 Therefore, using R1-R6:

753
$$k_1 [^{15}\text{NO}_2][^{14}\text{NO}] + j(\text{NO}_2)\alpha_1 [^{15}\text{NO}_2] =$$

754
$$k_5\alpha_2 [^{15}\text{NO}][\text{O}_3] + k_1\alpha(\text{NO}_2-\text{NO}) [^{15}\text{NO}][^{14}\text{NO}_2] \quad \text{Eq. (C2)}$$

755 From here we refer $^{14}\text{NO}_2$ and ^{14}NO as NO_2 and NO for convenience, rearrange the above equation,
756 we get:

757
$$\frac{[^{15}\text{NO}_2]}{[^{15}\text{NO}]} = \frac{k_5\alpha_2[\text{O}_3] + k_1\alpha(\text{NO}_2-\text{NO}) [\text{NO}_2]}{j_{\text{NO}_2}\alpha_1 + k_1[\text{NO}]} \quad \text{Eq. (C3)}$$

758 Meantime, since the Leighton cycle reaction still holds for the majority isotopes (NO and NO_2),
759 we have:

760
$$j_{\text{NO}_2}[\text{NO}_2] = k_5[\text{NO}][\text{O}_3] \quad \text{Eq. (C4)}$$

761 Thus,

762
$$\frac{[\text{NO}_2]}{[\text{NO}]} = \frac{k_5 \times [\text{O}_3]}{j_{\text{NO}_2}} \quad \text{Eq. (C5)}$$

763 From the text, when $j_{\text{NO}_2} > 0$, we defined $A = \tau_{\text{exchange}}/\tau_{\text{photo}} = j_{\text{NO}_2}/(k_1 \times [\text{NO}])$. Using the above
764 equations, we know:

765
$$\frac{j_{\text{NO}_2}}{[\text{NO}]} = \frac{k_5[\text{O}_3]}{[\text{NO}_2]} = Ak_1 \quad \text{Eq. (C6)}$$

766
$$\frac{j_{\text{NO}_2}}{k_1[\text{NO}]} = \frac{k_5[\text{O}_3]}{k_1[\text{NO}_2]} = A \quad \text{Eq. (C7)}$$

767 Next, to calculate $\delta(\text{NO}_2) - \delta(\text{NO})$, we use the definition of delta notation:

768
$$\delta(\text{NO}_2) - \delta(\text{NO}) = R_{\text{NO}_2}/R_{\text{std}} - R_{\text{NO}}/R_{\text{std}} = (R_{\text{NO}_2}/R_{\text{NO}} - 1)(1 + \delta(\text{NO})) \quad \text{Eq. (C8)}$$

769

770
$$\frac{R_{NO_2}}{R_{NO}} = \frac{[^{15}NO_2][NO]}{[^{15}NO][NO_2]} = \frac{k_5\alpha_2[O_3][NO]+k_1\alpha(NO_2-NO)[NO_2][NO]}{j_{NO_2}\alpha_1[NO_2]+k_1[NO][NO_2]}$$
 Eq. (C9)

771 Divide both side by $k_1[NO][NO_2]$:

772
$$\frac{R_{NO_2}}{R_{NO}} = \frac{\frac{k_5\alpha_2[O_3]}{k_1[NO_2]}+\alpha(NO_2-NO)}{\frac{j_{NO_2}\alpha_1}{k_1[NO]}+1}$$
 Eq. (C10)

773 Rearrange and substitute $\frac{k_5[O_3]}{k_1[NO_2]}$ and $\frac{j_{NO_2}}{k_1[NO]}$ with A:

774
$$\frac{R_{NO_2}}{R_{NO}} = \frac{\alpha_2 \times A + \alpha(NO_2 - NO)}{\alpha_1 \times A + 1}$$
 Eq. (C11)

775
$$\frac{R_{NO_2}}{R_{NO}} - 1 = \frac{(\alpha_2 - \alpha_1) \times A + (\alpha(NO_2 - NO) - 1)}{\alpha_1 \times A + 1}$$
 Eq. (C12)

776 Thus,

777
$$\delta(NO_2) - \delta(NO) = \frac{(\alpha_2 - \alpha_1) \times A + (\alpha(NO_2 - NO) - 1)}{\alpha_1 \times A + 1} (1 + \delta(NO))$$
 Eq. (C13)

778 Since $\alpha_1 \approx 1$, $\alpha_1 \times A + 1 \approx 1 + A$ this equation can be further simplified to Eq. 7:

779
$$\delta(NO_2) - \delta(NO) = \frac{(\alpha_2 - \alpha_1) \times A + \alpha(NO_2 - NO) - 1}{A + 1} (1 + \delta(NO))$$
 Eq. (C14)

780 Then, using mass balance:

781
$$\delta(NO_2) f(NO_2) + \delta(NO) (1 - f(NO_2)) = \delta(NO_x)$$
 Eq. (C15)

782 We can derive Eq. 8:

783
$$\delta(NO_2) - \delta(NO_x) = \frac{(\alpha_2 - \alpha_1) \times A + \alpha(NO_2 - NO) - 1}{A + 1} (1 + \delta(NO)) (1 - f(NO_2))$$
 Eq. (C16)