Response to editor comments

Dear Dr. Kaiser,

Thank you for your valuable input to this manuscript. Your suggestions significantly enhanced the overall quality of our paper. Please see below for a detailed point-by-point response.

1) Please integrate the supplement into the main text as appendix or appendices. The ACP manuscript guidelines require that "Supplementary material is reserved for items that cannot reasonably be included in the main text or as appendices. These may include short videos, very large images, maps, CIF files, as well as short computer codes such as matlab or python script. [...] Normal size figures, tables, as well as technical or theoretical developments that do not need to be included in the main text should be included as appendices."

Thanks for pointing this out. We moved the supplementary material into appendices and main text, now as Appendix A, B and C. We also numbered the figures and equations according to the format guideline.

2) Please remove the unnecessary approximations made in deriving equations 7 and 8, and make them consistent with Eq. 3. I have included the final steps of the calculation without approximation here (using the same δ and ε symbols as in the calculation I sent you during the discussion stage). Obviously, your steps up to the ratio R/R_2 are fine (except that I have used the inverse ratio, to simplify the final step of the calculation): Setting $A = 0$ (very fast isotope exchange) immediately reproduces Eq. 3 for verification.

Thanks for this advice and we agree removing the approximations will making Eq. 2 & 3 consistent with Eq. 7 &8. In Eq. 7 & 8, we get rid of the approximation that assuming $\delta(NO_2)-\delta(NO)=R(NO_2)/R(NO)$. The non-approximated equation became:

$$\delta(NO_2)-\delta(NO)=\frac{(\alpha_2-\alpha_1)\times A+(\alpha(NO_2-NO)-1)}{\alpha_1 A+1}(1+\delta(NO))$$

Here, when A=0, Eq. 7 become Eq. 2, therefore the two sets of equations are consistent.

However, we suggest the approximation that $\alpha_1*A+1=A+1$ can still be applied since it introduces very little error and will greatly simplify the equation by reducing the number of unknowns. We calculated the $\delta(NO_2)-\delta(NO)$ values before and after this approximation by assuming $\alpha_1=1.005$, which is an overestimation because our theoretical calculations show that it should only range from 1.0025 to 1.0029. Even under this assumption, we can calculate that the differences between approximation vs. non-approximation was less than 0.05‰ (with A ranging from 0.001 to 500). This difference is much smaller than the analytical uncertainty in many labs so it can be neglected. In the meantime, if we use this assumption ($\alpha_1*A=A$), we can mathematically reduce the number of unknowns from two ($\alpha_2-\alpha_1$ and α_1) to one (treating $\alpha_2-\alpha_1$ as one number). This approximation emphasized that the $\alpha_2-\alpha_1$ value, or the LCIE factor, acted as one important factor. Therefore, we suggest applying this approximation can simplify our model without bringing much uncertainty.

3) There is no need to repeat the reaction equations (R1 to R6, p. 5 of current supplement) or the definition of delta values (p. 6 of current supplement, lines from "Next, to calculate ..." to "$R_{NO2}/R_{NO} - 1$") in the Appendix.

In the appendix, we removed R1-R6 and referred the reactions to the main text. We also removed the delta definition equations.

4) Please remove unnecessary factors ("1000 ‰") from your mathematical equations (e.g. l. 180 and 182).

Revised as suggested.

5) Please also remove the unnecessary multiplication symbols (×). These make the equations unnecessarily difficult to read. Such multiplication symbols are rarely required outside scientific notation, e.g. $8 \times 10^{-14}\ cm^3\ s^{-1}$.

Revised as suggested.

6) L. 182: The quantity with the symbol ε should not be called "isotope enrichment factor" (which is a different kind of quantity). Please use the term "equilibrium isotopic fractionation" instead (as you do on l. 89 and elsewhere).

Thanks for pointing this out. In the text, we replaced all ε symbols with α-1 since we do not really need this extra symbol. Then, we name α “equilibrium fractionation factor”

7) L. 188 & 193: The quantities should be enclosed in parentheses so that the unit applies to value and uncertainty, e.g. "(–58.7±0.8) ‰"

Revised as suggested.

List of changes

1. The supplementary material now is merged into the main text or as appendices.

2. A more precise equation 7 is used in the main text.

3. Improvement was made in mathematical expressions, such as removing “1000‰”, “×”, and including uncertainties in brackets.

4. Replaced symbol “ε” with “α” to represent the equilibrium fractionation factor.

5. Reference list was updated to match the formatting requirement.

Quantifying the nitrogen isotope effects during photochemical equilibrium between NO and NO_2: implications for $\delta^{15}N$ in tropospheric reactive nitrogen

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Abstract. Nitrogen isotope fractionations between nitrogen oxides (NO and NO_2) play a significant role in determining the nitrogen isotopic compositions ($\delta^{15}N$) of atmospheric reactive nitrogen. Both the equilibrium isotopic exchange between NO and NO_2 molecules and the isotope effects occurring during the NO_x photochemical cycle are important, but both are not well constrained. The nighttime and daytime isotopic fractionations between NO and NO_2 in an atmospheric simulation chamber at atmospherically relevant NO_x levels were measured. Then, the impact of NO_x level and NO_2 photolysis rate to the combined isotopic fractionation (equilibrium isotopic exchange and photochemical cycle) between NO and NO_2 were calculated. It was found that the isotope effects occurring during the NO_x photochemical cycle can be described using a single fractionation factor, designated the Leighton Cycle Isotope Effect (LCIE). The results showed that at room temperature, the fractionation factor of nitrogen isotopic exchange is 1.0275±0.0012, and the fractionation factor of LCIE (when O_3 solely controls the oxidation from NO to NO_2) is 0.990±0.005. The measured LCIE factor showed good agreement with previous field measurements, suggesting that it could be applied in ambient environment, although future work is needed to assess the isotopic fractionation factors of NO + $RO_2/HO_2 \rightarrow NO_2$. The results were used to model the NO-NO_2 isotopic fractionations under several NO_x conditions. The model suggested that isotopic exchange was the dominate factor when NO_x >20 nmol mol^{-1}, while LCIE was more important at low NO_x concentrations (<1 nmol mol^{-1}) and high rates of NO_2 photolysis. These findings provided a useful tool to quantify the isotopic fractionations between tropospheric NO and NO_2, which can be applied in future field observations and atmospheric chemistry models.

1. Introduction

The nitrogen isotopic composition ($\delta^{15}N$) of reactive nitrogen compounds in the atmosphere is an important tool in understanding the sources and chemistry of atmospheric NO_x ($NO+NO_2$). It has been suggested that the $\delta^{15}N$ value of atmospheric nitrate (HNO_3, nitrate aerosols and nitrate ions in the precipitation and snow) imprints the $\delta^{15}N$ value of NO_x sources (Elliott et al., 2009; Kendall et al., 2007) thus many studies have used the $\delta^{15}N$ values of atmospheric nitrate to investigate NO_x sources (Chang et al., 2018; Felix et al., 2012; Felix & Elliott, 2014; Gobel et al., 2013; Hastings et al., 2004, 2009; Morin et al., 2009; Park et al., 2018; Walters et al., 2015, 2018). However, there remain questions about how isotopic fractionations that may occur during photochemical cycling of NO_x could alter the $\delta^{15}N$ values as it partitions into NO_y (NO_y = atmospheric nitrate, NO_3, N_2O_5, HONO, etc., Chang et al., 2018; Freyer, 1991; Hastings et al., 2004; Jarvis et al., 2008; Michalski et al., 2005; Morin et al., 2009; Zong et al., 2017). Similarily, other complex reactive nitrogen chemistry, such as nitrate photolysis and re-deposition in ice and snow (Frey et al., 2009), may impact the $\delta^{15}N$ of NO_y and atmospheric nitrate. The fractionation between NO and NO_2 via isotope exchange has been suggested to be the dominant factor in determining the $\delta^{15}N$ of NO_2 and ultimately atmospheric nitrate (Freyer, 1991; Freyer et al., 1993; Savarino et al., 2013; Walters et al., 2016). However, isotopic fractionations occur in most, if not all, NO_x and NO_y reactions, while most of these are still unknown or, if calculated (Walters and Michalski, 2015), unverified by experiments. Since the atmospheric chemistry of NO_y varies significantly in different environments (e.g., polluted vs. pristine, night vs. day), the isotopic fractionations associated with NO_y chemistry are also likely to vary in different environments. These unknowns could potentially bias conclusions about NO_x source apportionment reached when using nitrogen isotopes. Therefore, understanding the isotopic

fractionations between NO and NO_2 during photochemical cycling could improve our understanding of the relative role of sources versus chemistry for controlling the $\delta^{15}N$ variations of atmospheric NO_2 and nitrate.

In general, there are three types of isotopic fractionation effects associated with NO_x chemistry (Fig. 1A). The first type is the equilibrium isotopic effect (EIE), i.e., isotope exchange between two compounds without forming new molecules (Urey, 1947, Bigeleisen and Mayer, 1947), which for nitrogen isotopes in the NO_x system is the $^{15}NO + {}^{14}NO_2 \leftrightarrow {}^{14}NO + {}^{15}NO_2$ exchange reaction (Begun and Melton, 1956, Walters et al., 2016). The second type is the kinetic isotopic effect (KIE) associated with difference in isotopologue rate coefficients during unidirectional reactions (Bigeleisen & Wolfsberg, 1957). In the NO_x system this KIE would manifest in the oxidation of NO into NO_2 by $O_3/HO_2/RO_2$. The third type is the photochemical isotope fractionation effect (PHIFE, Miller & Yung, 2000), which for NO_x is the isotopic fractionation associated with NO_2 photolysis. All three fractionations could impact the $\delta^{15}N$ value of NO_2, and consequently atmospheric nitrate, but the relative importance of each may vary.

The limited number of studies on the EIE in the NO_x cycle have significant uncertainties. Discrepancies in the EIE for $^{15}NO + {}^{14}NO_2 \leftrightarrow {}^{14}NO + {}^{15}NO_2$ have been noted in several studies. Theoretical calculations predicted isotope fractionation factors (α) ranging from 1.035 to 1.042 at room temperature (Begun & Fletcher, 1960; Monse et al., 1969; Walters & Michalski, 2015) due to the different approximations used to calculate harmonic frequencies in each study. Likewise, two separate experiments measured different room temperature fractionation factors of 1.028±0.002 (Begun & Melton, 1956) and 1.0356±0.0015 (Walters et al., 2016). A concern in both experiments is that they were conducted in small chambers with high NO_x concentrations (hundreds of μmol mol^{-1}), significantly higher than typical ambient atmospheric NO_x levels

(usually less than 0.1 μmol mol^{-1}). Whether the isotopic fractionation factors determined by these experiments are applicable in the ambient environment is uncertain because of possible wall effects and formation of higher oxides, notably N_2O_4 and N_2O_3 at these high NO_x concentrations.

Even less research has examined the KIE and PHIFE occurring during NO_x cycling. The KIE of NO + O_3 has been theoretically calculated (Walters and Michalski, 2016) but has not been experimentally verified. The NO_2 PHIFE has not been experimentally determined or theoretically calculated. As a result, field observation studies often overlook the effects of PHIFE and KIE. Freyer et al. (1993) measured NO_x concentrations and the $\delta^{15}N$ values of NO_2 over a 1-year period at Julich, Germany and inferred a combined NO_x isotope fractionation factor (EIE+KIE+PHIFE) of 1.018±0.001. Freyer et al. (1993) suggested that the NO_x photochemical cycle (KIE and PHIFE) tends to diminish the equilibrium isotopic fractionation (EIE) between NO and NO_2. Even if this approach were valid, applying this single fractionation factor elsewhere, where NO_x, O_3 concentrations and actinic fluxes are different, would be tenuous given that these factors may influence the relative importance of EIE, KIE and PHIFE (Hastings et al., 2004; Walters et al., 2016). Therefore, to quantify the overall isotopic fractionations between NO and NO_2 at various tropospheric conditions, it is crucial to know 1) isotopic fractionation factors of EIE, KIE and PHIFE individually and 2) the relative importance of each factor under various conditions.

In this work, we aim to quantify the nitrogen isotope fractionation factors between NO and NO_2 at photochemical equilibrium. First, we measure the N isotope fractionations between NO and NO_2 in an atmospheric simulation chamber at atmospherically relevant NO_x levels. Then, we provide mathematical solutions to assess the impact of NO_x level and NO_2 photolysis rate ($j(NO_2)$) to the relative importance of EIE, KIE and PHIFE. Subsequently we use the solutions and chamber measurements to calculate the isotopic fractionation factors of EIE, KIE and PHIFE. Lastly, using

the calculated fractionation factors and the equations, we model the NO-NO_2 isotopic fractionations at several sites to illustrate the behavior of $\delta^{15}N$ values of NO_x in the ambient environment.

2. Methods

The experiments were conducted using a 10 m^3 Atmospheric Simulation Chamber at the National Center for Atmospheric Research (see descriptions in Appendix A and Zhang et al. (2018)). A set of mass flow controllers was used to inject NO and O_3 into the chamber. NO was injected at 1 L min^{-1} from an in-house NO/N_2 cylinder (133.16 μmol mol^{-1} NO in ultra-pure N_2), and O_3 was generated by flowing 5 L min^{-1} zero-air through a flow tube equipped with a UV Pen-Ray lamp (UVP LLC., CA) into the chamber. NO and NO_2 concentrations were monitored in real time by chemiluminescence with a detection limit of 0.5 ppb (model CLD 88Y, Eco Physics, MI) as were O_3 concentrations using an UV absorption spectroscopy with a detection limit of 0.5 ppb (model 49, Thermo Scientific, CO). In each experiment, the actual amounts of NO and O_3 injected were calculated using measured NO_x and O_3 concentrations after steady state was reached (usually within 1 h). The wall loss rate of NO_2 was tested by monitoring O_3 (29 nmol mol^{-1}) and NO_x (62 nmol mol^{-1}) over a 4-hour period. After the NO and NO_2 concentrations reached steady state, no decrease in NO_2 concentrations was observed showing that chamber wall loss was negligible.

Two sets of experiments were conducted to separately investigate the EIE, KIE and PHIFE. The first set of experiments was conducted in the dark. In each of these dark experiments, a range of NO and O_3 ($[O_3]<[NO]$) was injected into the chamber to produce NO-NO_2 mixtures with $[NO]/[NO_2]$ ratios ranging from 0.43 to 1.17. The N isotopes of these mixtures were used to investigate the EIE between NO and NO_2. The second set of experiments was conducted under

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irradiation of UV lights (300-500 nm, see Appendix A for irradiation spectrum). Under such conditions, NO, NO_2 and O_3 reached photochemical steady state, which combined the isotopic effects of EIE, KIE and PHIFE. In addition, three experiments were conducted to measure the $\delta^{15}N$ value of the tank NO. In each of these experiments, a certain amount of O_3 was first injected into the chamber, then approximately the same amount of NO was injected into the chamber to ensure 100% of the NO_x was in the form of NO_2 with little O_3 (<3 nmol mol^{-1}) remaining in the chamber, such that the O_3+NO_2 reaction was negligible. The NO_2 in the chamber was then collected and its $\delta^{15}N$ value measured, which equates to the $\delta^{15}N$ value of the tank NO.

In all experiments, the concentrations of NO, NO_2 and O_3 were allowed to reach steady state, and the product NO_2 was collected from the chamber using a honeycomb denuder tube. After the NO, NO_2 and O_3 concentrations reached steady-state, well-mixed chamber air was drawn out through a Norprene Thermoplastic tubing ~40 cm at 10 L min^{-1} and passed through a honeycomb denuder system (Chemcomb 3500, Thermo Scientific). Based on flow rate, the NO_2 residence time in the was less than 0.5 second, thus in the light-on experiments where NO and O_3 coexisted, the NO_2 produced inside the transfer tube through NO+O_3 reactions should be <0.03 ppb (using the upper limit of NO and O_3 concentrations in our experiments). The honeycomb denuder system consisted of two honeycomb denuder tubes connected in series. Each honeycomb denuder tube is a glass cylinder of 38 mm long, 47 mm in diameter, and consist of 212 hexagonal tubes with inner diameters of 2 mm. Before collecting samples, each denuder tube was coated with a solution of 10% KOH and 25% guaiacol in methanol and then dried by flowing N_2 gas through the denuder tube for 15 seconds (Williams and Grosjean, 1990, Walters et al., 2016). The NO_2 reacted with guaiacol coating and was converted into NO_2^- that was retained on the denuder tube wall (Williams and Grosjean, 1990). NO was inert to the denuder tube coating: a control experiment sampled pure

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NO using the denuder tubes, which did not show any measurable NO_2^-. The NO_2 collection efficiency of a single honeycomb denuder tube was tested in another control experiment: air containing 66 nmol mol^{-1} of NO_2 was drawn out of the chamber through a denuder tube, and the NO_2 concentration at the exit of the tube holder was measured and found to be below the detection limit (<1 nmol mol^{-1}), suggesting the collection efficiency was nearly 100% when [NO_2] <66 nmol mol^{-1}. Furthermore, when the denuder system consisted of two denuder tubes in series and NO_2^- in the second denuder was below the detection limit indicating trivial NO_2 breakthrough. Each NO_2 collection lasted for 0.5-3 hours in order to collect enough NO_2^- for isotopic analysis (~300 nmol). After collection, the NO_2^- was leached from each denuder tube by rinsing thoroughly with 10 ml deionized water into a clean polypropylene container and stored frozen until isotopic analysis. Isotopic analysis was conducted at Purdue Stable Isotope Laboratory. For each sample, approximately 50 nmol of the NO_2^- extract was mixed with 2 M sodium azide solution in acetic acid buffer in an air-tight glass vial, then shaken overnight to completely reduce all the NO_2^- to $N_2O_{(g)}$ (Casciotti & McIlvin, 2007; McIlvin & Altabet, 2005). The product N_2O was directed into a Thermo GasBench equipped with cryo-trap, then the $\delta^{15}N$ of the N_2O was measured using a Delta-V Isotope Ratios Mass Spectrometer. Six coated denuders tubes that did not get exposed to NO_2 were also analyzed using the same chemical procedure, which did not show any measurable signal on the IRMS, suggesting the blank from both sampling process and the chemical conversion process was negligible. The overall analytical uncertainty for $\delta^{15}N$ analysis was 0.5 ‰ (1σ) based on replicate analysis of in house NO_2^- standards.

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3. Results and Discussions

3.1. Equilibrium Isotopic Fractionation between NO and NO_2

The equilibrium isotope fractionation factor, $\alpha(NO_2\text{-}NO)$, is the ^{15}N enrichment in NO_2 relative to NO, and is expressed as the ratio of rate constants k_2 / k_1 of two reactions:

$^{15}NO_2 + {}^{14}NO \rightarrow {}^{15}NO + {}^{14}NO_2$ R1, rate constant = k_1

$^{15}NO + {}^{14}NO_2 \rightarrow {}^{15}NO_2 + {}^{14}NO$ R2, rate constant = $k_2 = k_1 \alpha(NO_2\text{-}NO)$

where k_1 is the rate constant of the isotopic exchange, which was previously determined to be 8.14×10^{-14} cm^3 s^{-1} (Sharma et al., 1970). The reaction time required for NO-NO_2 to reach isotopic equilibrium was estimated using the exchange rate constants in a simple kinetics box model (BOXMOX, Knote et al., 2015). The model predicts that at typical NO_x concentrations used during the chamber experiments (7.7-62.4 nmol mol^{-1}), isotopic equilibrium would be reached within 15 minutes (see Appendix B). Since the sample collection usually started 1 hour after NO_x was well mixed in the chamber, there was sufficient time to reach full isotope equilibrium. The isotope equilibrium fractionation factor ($\alpha(NO_2\text{-}NO)$) is then calculated to be:

$$\alpha(NO_2 - NO) = \frac{[^{15}NO_2][^{14}NO]}{[^{14}NO_2][^{15}NO]} = \frac{R(NO_2)}{R(NO)} \quad \text{Eq. (1)}$$

where R(NO, NO_2) are the $^{15}N/^{14}N$ ratios of NO and NO_2. By definition, the $\delta^{15}N(NO)=(R(NO)/R(reference)-1)\times1000$ ‰ and $\delta^{15}N(NO_2)=(R(NO_2)/R(reference)-1)\times1000$ ‰, but hereafter, the $\delta^{15}N$ values of NO, NO_2 and NO_x will be referred as $\delta(NO)$, $\delta(NO_2)$ and $\delta(NO_x)$, respectively. Eq. (1) leads to:

$$\delta(NO_2) - \delta(NO) = (\alpha(NO_2 - NO) - 1)(1 + \delta(NO)) \quad \text{Eq. (2)}$$

Using Eq. (2) and applying NO_x isotopic mass balance ($\delta(NO_x)=f(NO_2)\delta(NO_2)+(1-f(NO_2))\delta(NO)$, $f(NO_2)=[NO_2]/([NO]+[NO_2])$) yields:

$$\frac{\delta(NO_2)-\delta(NO_x)}{1+\delta(NO_2)} = \frac{\alpha(NO_2-NO)-1}{\alpha(NO_2-NO)}\left(1 - f(NO_2)\right) \quad \text{Eq. (3)}$$

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$= \varepsilon(NO_2 - NO) \times (1 + \delta(NO))$

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Here, $\delta(NO_x)$ equals to the $\delta^{15}N$ value of the cylinder NO and $f(NO_2)$ is the molar fraction of NO_2 with respect to total NO_x. Three experiments (see descriptions in method section) that measured $\delta(NO_x)$ showed consistent $\delta(NO_x)$ values of (-58.7±0.8) ‰ (n = 3), indicating $\delta(NO_x)$ remained unchanged throughout the experiments (as expected for isotope mass balance). Thus, the $\delta(NO_x)$ can be treated as a constant in Eq. (3), and the linear regression of $(\delta(NO_2)-\delta(NO_x))/(1+\delta(NO_2))$ versus $1-f(NO_2)$ should have an intercept of 0 and a slope of $(\alpha(NO_2\text{-}NO)-1)/\alpha(NO_2\text{-}NO)$.

The plot of $(\delta(NO_2)-\delta(NO_x))/(1+\delta(NO_2))$ as a function of $1-f(NO_2)$ values from five experiments yields an $\alpha(NO_2\text{-}NO)$ value of 1.0275±0.0012 at room temperature (Fig. 1B). This fractionation factor is comparable to previously measured values but with some differences. Our result agrees well with the $\alpha(NO_2\text{-}NO)$ value of 1.028±0.002 obtained by Begun and Melton (1956) at room temperature. However, Walters et al., (2016) determined the $\alpha(NO_2\text{-}NO)$ values of NO-NO_2 exchange in a 1-liter reaction vessel, which showed a slightly higher $\alpha(NO_2\text{-}NO)$ value of 1.035. This discrepancy might originate from rapid heterogeneous reactions on the wall of the reaction vessel at high NO_x concentrations and the small chamber size used by Walters et al. (2016). They used a reaction vessel made of Pyrex, which is known to absorb water (Do Remus et al., 1983; Takei et al., 1997) that can react with NO_2 forming HONO, HNO_3 and other N compounds. Additionally, previous studies have suggested that Pyrex walls enhance the formation rate of N_2O_4 by over an order of magnitude (Barney & Finlayson-Pitts, 2000; Saliba et al., 2001), which at isotopic equilibrium is enriched in ^{15}N compared to NO and NO_2 (Walters & Michalski, 2015). Therefore, their measured $\alpha(NO_2\text{-}NO)$ might be slightly higher than the actual $\alpha(NO_2\text{-}NO)$ value. In this work, the 10 m^3 chamber has a much smaller surface to volume ratio relative to Walters et al. (2016) which minimizes wall effects, and the walls were made of Teflon that minimize NO_2 surface reactivity, which was evidenced by the NO_2 wall loss control experiment. Furthermore,

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237 the low NO_x mixing ratios in our experiments minimized N_2O_4 and N_2O_3 formation. At NO and
238 NO_2 concentrations of 50 nmol mol^{-1} the steady state concentrations of N_2O_4 and N_2O_3 were
239 calculated to be 0.014 and 0.001 pmol mol^{-1}, respectively (Atkinson et al., 2004). Therefore, we
240 suggest our measured $\alpha(NO_2\text{-}NO)$ value (1.0275±0.0012) may better reflect the room temperature
241 (298 K) NO-NO_2 EIE in the ambient environment.

242 Unfortunately, the chamber temperature could not be controlled so we were not able to
243 investigate the temperature dependence of the EIE. Hence, we speculate that the $\alpha(NO_2\text{-}NO)$
244 follows a similar temperature dependence pattern calculated in Walters et al. (2016). Walters et al.
245 (2016) suggested that, the $\alpha(NO_2\text{-}NO)$ value would be 0.0047 higher at 273 K and 0.002 lower at
246 310 K, relative to room temperature (298 K). Using this pattern and our experimentally determined
247 data, we suggest the $\alpha(NO_2\text{-}NO)$ values at 273 K, 298 K and 310 K are 1.0322±0.0012,
248 1.0275±0.0012 and 1.0255±0.0012, respectively. This 0.0067 variation at least partially contribute
249 to the daily and seasonal variations of $\delta^{15}N$ values of NO_2 and nitrate in some areas (e.g., polar
250 regions with strong seasonal temperature variation). Thus, future investigations should be
251 conducted to verify the EIE temperature dependence.
252
253 **3.2. Kinetic isotopic fractionation of Leighton Cycle**

254 The photochemical reactions of NO_x will compete with the isotope exchange fractionations
255 between NO and NO_2. The NO-NO_2 photochemical cycle in the chamber was controlled by the
256 Leighton cycle: NO_2 photolysis and the NO + O_3 reaction. This is because there were no VOCs in
257 the chamber so no RO_2 was produced, which excludes the NO + RO_2 reaction. Likewise, the low
258 water vapor content (RH<10%) and the minor flux of photons < 310 nm results in minimal OH
259 production and hence little HO_2 formation and subsequently trivial amount of NO_2 would be

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formed by NO + HO_2. Applying these limiting assumptions, the EIE between NO and NO_2 (R1-R2) were only competing with the KIE (R3-R4) and the PHIFE in R5-R6:

$^{14}NO_2 \rightarrow {}^{14}NO + O$ R3, rate constant=$j(NO_2)$

$^{15}NO_2 \rightarrow {}^{15}NO + O$ R4, rate constant=$j(NO_2)\ \alpha_1$

$^{14}NO + O_3 \rightarrow {}^{14}NO_2 + O_2$ R5, rate constant=k_5

$^{15}NO + O_3 \rightarrow {}^{15}NO_2 + O_2$ R6, rate constant=$k_5\ \alpha_2$

In which $j(NO_2)$ is the NO_2 photolysis rate (1.4×10^{-3} s^{-1} in these experiments), k_5 is the rate constant for the $NO+O_3$ reaction (1.73×10^{-14} cm^3 s^{-1}, Atkinson et al., 2004), and $\alpha_{1,2}$ are isotopic fractionation factors for the two reactions. Previous studies (Freyer et al., 1993; Walters et al., 2016) have attempted to assess the competition between EIE (R1-R2), KIE and PHIFE (R3-R6), but none of them quantified the relative importance of the two processes, nor were α_1 or α_2 values experimentally determined. Here we provide the mathematical solution of EIE, KIE and PHIFE to illustrate how R1-R6 affect the isotopic fractionations between NO and NO_2.

First, the NO_2 lifetime with respect to isotopic exchange with NO ($\tau_{exchange}$) and photolysis (τ_{photo}) was determined:

$$\tau_{exchange} = \frac{1}{k_1[NO]} \quad \text{Eq. (4)}$$

$$\tau_{photo} = \frac{1}{j(NO_2)} \quad \text{Eq. (5)}$$

We then define an A factor:

$$A = \begin{cases} \frac{\tau_{exchange}}{\tau_{photo}} & \text{when } j(NO_2) \neq 0 \\ 0 & \text{when } j(NO_2) = 0 \end{cases} \quad \text{Eq. (6)}$$

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Using R1-R6 and Eq. (1)-(6), we solved steady-state $\delta(NO_2)$ and $\delta(NO)$ values (see calculations in Appendix C). Our calculations show that the $\delta(NO_2)$-$\delta(NO)$ and $\delta(NO_2)$-$\delta(NO_x)$ values at steady state can be expressed as functions of α_1, α_2, $\alpha(NO_2\text{-}NO)$ and A:

$$\delta(NO_2) - \delta(NO) = \frac{(\alpha_2-\alpha_1)\,A+(\alpha(NO_2-NO)-1)}{A+1}(1+\delta(NO)) \quad \text{Eq. (7)}$$

$$\delta(NO_2) - \delta(NO_x) = \frac{(\alpha_2-\alpha_1)\,A+(\alpha(NO_2-NO)-1)}{A+1}(1+\delta(NO))(1-f(NO_2)) \quad \text{Eq. (8)}$$

Equation (7) shows the isotopic fractionation between NO and NO_2 ($\delta(NO_2)$-$\delta(NO)$) is determined by A, the EIE factor ($\alpha(NO_2\text{-}NO)$-1) and the (α_2-α_1) factor assuming (1+δ(NO)) is close to 1. This (α_2-α_1) represents a combination of KIE and PHIFE, suggesting they act together as one factor; therefore, we name the (α_2-α_1) factor Leighton Cycle Isotopic Effect, i.e., LCIE. Using measured ($\delta(NO_2)$-$\delta(NO)$)/(1+δ(NO)) values, A values, and the previously determined EIE factor, we calculated that the best fit for the LCIE factor was (-10±5) ‰ (showing the lowest Rooted Mean Square Error, RMSE, of 1.1‰, Fig. 1C). The uncertainties in the LCIE factor are relatively higher than that of the EIE factor, mainly because of the accumulated analytical uncertainties at low NO_x and O_3 concentrations, and low A values (0.10-0.28) due to the relatively low $j(NO_2)$ value (1.4×10^{-3} s^{-1}) under the chamber irradiation conditions.

This LCIE factor determined in our experiments is in good agreement with theoretical calculations. Walters and Michalski (2016) previously used an *ab initio* approach to determine an α_2 value of 0.9933 at room temperature, 0.9943 at 237 K and 0.9929 at 310 K. The total variation of α_2 values from 273 K to 310 K is only 1.4 ‰, significantly smaller than our experimental uncertainty (±5 ‰). The α_1 value was calculated using a ZPE shift model (Miller & Yung, 2000) to calculate the isotopic fractionation of NO_2 by photolysis. Briefly, this model assumes both isotopologues have the same quantum yield function and the PHIFE was only caused by the differences in the $^{15}NO_2$ and $^{14}NO_2$ absorption cross-section as a function of wavelength, thus α_1

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values do not vary by temperature. The $^{15}NO_2$ absorption cross-section was calculated by shifting the $^{14}NO_2$ absorption cross-section by the $^{15}NO_2$ zero-point energy (Michalski et al., 2004). When the ZPE shift model was used with the irradiation spectrum of the chamber lights, the resulting α_1 value was 1.0023. Therefore, the theoretically predicted α_2-α_1 value should be -0.0090, i.e., (-9.0±0.7) ‰ when temperature ranges from 273 K to 310 K. This result shows excellent agreement with our experimentally determined room temperature α_2-α_1 value of (-10±5) ‰.

This model was then used to evaluate the variations of α_1 value to different lighting conditions. The TUV model (TUV5.3.2, Madronich & Flocke, 1999) was used to calculate the solar wavelength spectrum at three different conditions: early morning/late afternoon (solar zenith angle=85 degree), mid-morning/afternoon (solar zenith angle=45 degree), noon (solar zenith angle=0 degree). These spectrums were used in the ZPE shift model to calculate the α_1 values, which are 1.0025, 1.0028, and 1.0029 at solar zenith angles of 85, 45 and 0 degree, respectively. These values, along with the predicted α_1 value in the chamber, showed a total span of 0.6‰ (1.0026±0.0003), which is again significantly smaller than our measured uncertainty. Therefore, we suggest that our experimentally determined LCIE factor ((-10±5) ‰) can be used in most tropospheric solar irradiation spectrums.

The equations can also be applied in tropospheric environments to calculate the combined isotopic fractionations of EIE and LCIE for NO and NO_2. First, the NO_2 sink reactions (mainly NO_2+OH in the daytime) are at least 2-3 orders of magnitude slower than the Leighton cycle and the NO-NO_2 isotope exchange reactions (Walters et al., 2016), therefore their effects on the $\delta(NO_2)$ should be minor. Second, although the conversion of NO into NO_2 in the ambient environment is also controlled by NO + RO_2 and HO_2 in addition to NO+O_3 (e.g., King et al., 2001), Eq. (7) still showed good agreement with field observations in previous studies. Freyer et al. (1993)

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354 determined the annual average daytime $\delta(NO_2)$-$\delta(NO)$ at Julich, Germany along with average
355 daytime NO concentration (9 nmol mol^{-1}, similar to our experimental conditions) to be
356 (+18.03±0.98) ‰. Using Eq. (7), assuming the daytime average $j(NO_2)$ value throughout the year
357 was (5.0±1.0)×10^{-3}, and a calculated A value from measured NO_x concentration ranged from 0.22-
358 0.33, the average NO-NO_2 fractionation factor was calculated to be (+18.8±1.4) ‰ (Fig. 1C), in
359 excellent agreement with the measurements in the present study. This agreement suggests the
360 NO+RO_2/HO_2 reactions might have similar fractionation factors as NO+O_3. Therefore, we suggest
361 Eq. (7) and (8) can be used to estimate the isotopic fractionations between NO and NO_2 in the
362 troposphere.
363
364 **3.3 Calculating nitrogen isotopic fractionations of NO-NO_2**
365 First, Eq. (7) was used to calculate the $\Delta(NO_2\text{-}NO) = \delta(NO_2)\text{-}\delta(NO)$ at a wide range of
366 NO_x concentrations, $f(NO_2)$ and $j(NO_2)$ values (Fig. 2A-D), assuming $(1+\delta(NO))=1$. $j(NO_2)$
367 values of 0 s^{-1} (Fig. 2A), 1.4×10^{-3} s^{-1} (Fig. 2B), 5×10^{-3} s^{-1} (Fig. 2C) and 1×10^{-2} s^{-1} (Fig. 2D) were
368 selected to represent nighttime, dawn (as well as the laboratory conditions of our experiments),
369 daytime average and noon, respectively. Each panel represented a fixed $j(NO_2)$ value, and the
370 $\Delta(NO_2\text{-}NO)$ values were calculated as a function of the A value, which was derived from NO_x
371 concentration and $f(NO_2)$. The A values have a large span, from 0 to 500, depending on the $j(NO_2)$
372 value and the NO concentration. When A=0 ($j(NO_2)$=0) and $f(NO_2)$<1 (meaning NO-NO_2 coexist
373 and $[O_3]$=0), Eq. (7) and (8) become Eq. (2) and (3), showing the EIE was the sole factor, the
374 $\Delta(NO_2\text{-}NO)$ values were solely controlled by EIE which has a constant value of +27.5 ‰ at 298K
375 (Fig. 2A). When $j(NO_2)$>0, the calculated $\Delta(NO_2\text{-}NO)$ values showed a wide range from -10.0 ‰
376 (controlled by LCIE factor: α_2-α_1=-10 ‰) to +27.5 ‰ (controlled by EIE factor: $\alpha(NO_2\text{-}NO)$-1 =

+27.5 ‰). Fig. 2B-D display the transition from a LCIE-dominated regime to an EIE-dominated regime. The LCIE-dominated regime is characterized by low [NO_x] (<50 pmol mol^{-1}), representing remote ocean areas and polar regions (Beine et al., 2002; Custard et al., 2015). At this range the A value can be greater than 200, thus Eq. (7) can be simplified as: $\Delta(NO_2\text{-}NO) = \alpha_2\text{-}\alpha_1$, suggesting the LCIE almost exclusively controls the NO-NO_2 isotopic fractionation. The $\Delta(NO_2\text{-}NO)$ values of these regions are predicted to be <0 ‰ during most time of the day and < -5 ‰ at noon. On the other hand, the EIE-dominated regime was characterized by high [NO_x] (>20 nmol mol^{-1}) and low $f(NO_2)$ (< 0.6), representative of regions with intensive NO emissions, e.g., near roadside or stack plumes (Clapp & Jenkin, 2001; Kimbrough et al., 2017). In this case, the $\tau_{exchange}$ are relatively short (10-50 s) compared to the τ_{photo} (approximately 100 s at noon and 1000 s at dawn), therefore the A values are small (0.01-0.5). The EIE factor in this regime thus is much more important than the LCIE factor, resulting in high $\Delta(NO_2\text{-}NO)$ values (>20 ‰). Between the two regimes, both EIE and LCIE are competitive and therefore it is necessary to use Eq. (7) to quantify the $\Delta(NO_2\text{-}NO)$ values.

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Fig. 2 also implies that changes in the $j(NO_2)$ value can cause the diurnal variations in $\Delta(NO_2\text{-}NO)$ values. Changing $j(NO_2)$ would affect the value of A and consequently the NO-NO_2 isotopic fractionations in two ways: 1) changes in $j(NO_2)$ value would change the photolysis intensity, therefore the τ_{photo} value; 2) in addition, changes in $j(NO_2)$ value would also alter the steady state NO concentration, therefore changing the $\tau_{exchange}$ (Fig. 2C). The combined effect of these two factors on the A value varies along with the atmospheric conditions, and thus needs to be carefully calculated using NO_x concentration data and atmospheric chemistry models.

We then calculated the differences of $\delta^{15}N$ values between NO_2 and total NO_x, e.g. $\Delta(NO_2\text{-}NO_x) = \delta(NO_2)\text{-}\delta(NO_x)$ in Fig. 2E-H. Since $\Delta(NO_2\text{-}NO_x)$ are connected through the observed $\delta^{15}N$

of NO_2 (or nitrate) to the $\delta^{15}N$ of NO_x sources, this term might be useful in field studies (e.g., Chang et al., 2018; Zong et al., 2017). The calculated $\Delta(NO_2\text{-}NO_x)$ values (Fig. 2E-H) also showed a LCIE-dominated regime at low $[NO_x]$ and an EIE-dominated regime at high $[NO_x]$. The $\Delta(NO_2\text{-}NO_x)$ values were dampened by the $1\text{-}f(NO_2)$ factor comparing to $\Delta(NO_2\text{-}NO)$, as shown in Eq. (3) and (8): $\Delta(NO_2\text{-}NO_x) = \Delta(NO_2\text{-}NO)\cdot(1\text{-}f(NO_2))$. At high $f(NO_2)$ values (>0.8), the differences between $\delta(NO_2)$ and $\delta(NO_x)$ were less than 5 ‰, thus the measured $\delta(NO_2)$ values were similar to $\delta(NO_x)$, although the isotopic fractionation between NO and NO_2 could be noteworthy. Some ambient environments with significant NO emissions or high NO_2 photolysis rates usually have $f(NO_2)$ values between 0.4-0.8 (Mazzeo et al., 2005; Vicars et al., 2013). In this scenario, the $\Delta(NO_2\text{-}NO_x)$ values in Fig. 2F-H showed wide ranges of -4.8 ‰ to +15.6 ‰, -6.0 ‰ to +15.0 ‰, and -6.3 ‰ to +14.2 ‰ at $j(NO_2)$=1.4×10^{-3} s^{-1}, 5×10^{-3} s^{-1}, 1×10^{-2} s^{-1}, respectively. These significant differences again highlighted the importance of both LCIE and EIE (Eq. (7) and (8)) in calculating the $\Delta(NO_2\text{-}NO_x)$. In the following discussion, we assume 1) the α_1 value remain constant (see discussion above), 2) the $NO+RO_2/HO_2$ reactions have the same fractionation factors (α_2) as $NO+O_3$, and 3) both EIE and LCIE do not display significant temperature dependence, then use Equations (7) and (8) and this laboratory determined LCIE factor (-10 ‰) to calculate the nitrogen isotopic fractionation between NO and NO_2 at various tropospheric atmospheric conditions.

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4. Implications

The daily variations of $\Delta(NO_2\text{-}NO_x)$ values at two roadside NO_x monitoring sites were predicted to demonstrate the effects of NO_x concentrations to the $NO\text{-}NO_2$ isotopic fractionations. Hourly NO and NO_2 concentrations were acquired from a roadside site at Anaheim, CA (https://www.arb.ca.gov) and an urban site at Evansville, IN (http://idem.tx.sutron.com) on July

25, 2018. The hourly $j(NO_2)$ values output from the TUV model (Madronich & Flocke, 1999) at these locations was used to calculate the daily variations of $\Delta(NO_2\text{-}NO_x)$ values (Fig. 3A, B) by applying Eq. (8) and assuming $(1+\delta(NO))=1$. Hourly NO_x concentrations were 12-51 nmol mol^{-1} at Anaheim and 9-38 nmol mol^{-1} at Evansville and the $f(NO_2)$ values at both sites did not show significant daily variations (0.45±0.07 at Anaheim and 0.65±0.08 at Evansville), likely because the NO_x concentrations were controlled by the high NO emissions from the road (Gao, 2007). The calculated $\Delta(NO_2\text{-}NO_x)$ values using Eq. (8) showed significant diurnal variations. During the nighttime, the isotopic fractionations were solely controlled by the EIE, the predicted $\Delta(NO_2\text{-}NO_x)$ values were (+14.5±2.0) ‰ and (+8.7±2.1) ‰ at Anaheim and Evansville, respectively. During the daytime, the existence of LCIE lowered the predicted $\Delta(NO_2\text{-}NO_x)$ values to (+9.8±1.7) ‰ at Anaheim and (+3.1±1.5) ‰ at Evansville while the $f(NO_2)$ values at both sites remained similar. The lowest $\Delta(NO_2\text{-}NO_x)$ values for both sites (+7.0 ‰ and +1.7 ‰) occurred around noon when the NO_x photolysis was the most intense. In contrast, if one neglects the LCIE factor in the daytime, the $\Delta(NO_2\text{-}NO_x)$ values would be (+12.9±1.5) ‰ and (+10.0±1.6) ‰ respectively, an overestimation of 3.1 ‰ and 6.9 ‰. These discrepancies suggested that the LCIE played an important role in the NO-NO_2 isotopic fractionations and neglecting it could bias the NO_x source apportionment using $\delta^{15}N$ of NO_2 or nitrate.

The role of LCIE was more important in less polluted sites. The $\Delta(NO_2\text{-}NO_x)$ values calculated for a suburban site near San Diego, CA, USA, again using the hourly NO_x concentrations (https://www.arb.ca.gov, Fig. 3C) and $j(NO_2)$ values calculated from the TUV model. NO_x concentrations at this site varied from 1 to 9 nmol mol^{-1} and assuming $(1+\delta(NO))=1$. During the nighttime, NO_x was in the form of NO_2 ($f(NO_2) = 1$) because O_3 concentrations were higher than NO_x, thus the $\delta(NO_2)$ values should be identical to $\delta(NO_x)$ ($\Delta(NO_2\text{-}NO_x) = 0$). In the

449 daytime a certain amount of NO was produced by direct NO emission and NO_2 photolysis but the
450 $f(NO_2)$ was still high (0.73±0.08). Our calculation suggested the daytime $\Delta(NO_2\text{-}NO_x)$ values
451 should be only (+1.3±3.2) ‰ with a lowest value of -1.3 ‰. These $\Delta(NO_2\text{-}NO_x)$ values were
452 similar to the observed and modeled summer daytime $\delta(NO_2)$ values in West Lafayette, IN
453 (Walters et al., 2018), which suggest the average daytime $\Delta(NO_2\text{-}NO_x)$ values at NO_x = (3.9±1.2)
454 nmol mol^{-1} should range from +0.1 ‰ to +2.4 ‰. In this regime, we suggest the $\Delta(NO_2\text{-}NO_x)$
455 values were generally small due to the significant contribution of LCIE and high $f(NO_2)$.

456 The LCIE should be the dominant factor controlling the NO-NO_2 isotopic fractionation at
457 remote regions, resulting in a completely different diurnal pattern of $\Delta(NO_2\text{-}NO_x)$ compared with
458 the urban-suburban area. Direct hourly measurements of NO_x at remote sites are rare, thus we used
459 total NO_x concentration of 50 pmol mol^{-1}, daily O_3 concentration of 20 nmol mol^{-1} at Summit,
460 Greenland (Dibb et al., 2002; Hastings et al., 2004; Honrath et al., 1999; Yang et al., 2002), and
461 assumed (1+δ(NO))=1 and the conversion of NO to NO_2 was completely controlled by O_3 to
462 calculate the NO/NO_2 ratios. Here the isotopes of NO_x were almost exclusively controlled by the
463 LCIE due to the high A values (>110). The $\Delta(NO_2\text{-}NO_x)$ values displayed a clear diurnal pattern
464 (Fig. 3D) with highest value of -0.3 ‰ in the "nighttime" (solar zenith angle >85 degree) and
465 lowest value of -5.0 ‰ in the mid-day. This suggest that the isotopic fractionations between NO
466 and NO_2 were almost completely controlled by LCIE at remote regions, when NO_x concentrations
467 were <0.1 nmol mol^{-1}. However, since the isotopic fractionation factors of nitrate-formation
468 reactions (NO_2+OH, NO_3+HC, N_2O_5+H_2O) are still unknown, more studies are needed to fully
469 explain the daily and seasonal variations of $\delta(NO_3^-)$ at remote regions.

470 Nevertheless, our results have a few limitations. First, currently there are very few field
471 observations that can be used to evaluate our model, therefore, future field observations that

472 measure the $\delta^{15}N$ values of ambient NO and NO_2 should be carried out to test our model. Second,
473 more work, including theoretical and experimental studies, is needed to investigate the isotope
474 fractionation factors occurring during the conversion from NO_x to NO_y and nitrate: in the NO_y
475 cycle, EIE (isotopic exchange between NO_2, NO_3 and N_2O_5), KIE (formation of NO_3, N_2O_5 and
476 nitrate) and PHIFE (photolysis of NO_3, N_2O_5, HONO and sometimes nitrate) may also exist and
477 be relevant for the $\delta^{15}N$ of HNO_3 and HONO. In particular, the N isotope fractionation occurring
478 during the $NO_2 + OH \rightarrow HNO_3$ reaction needs investigation. Such studies could help us modeling
479 the isotopic fractionation between NO_x emission and nitrate, and eventually enable us to analyze
480 the $\delta^{15}N$ value of NO_x emission by measuring the $\delta^{15}N$ values of nitrate aerosols and nitrate in wet
481 depositions. Third, our discussion only focuses on the reactive nitrogen chemistry in the
482 troposphere, however, the nitrogen chemistry in the stratosphere is drastically different from the
483 tropospheric chemistry, thus future studies are also needed to investigate the isotopic fractionations
484 in the stratospheric nitrogen chemistry. Last, the temperature dependence of both EIE and LCIE
485 needs to be carefully investigated, because of the wide range of temperature in both troposphere
486 and stratosphere. Changes in temperature could alter the isotopic fractionation factors of both EIE
487 and LCIE, as well as contribute to the seasonality of isotopic fractionations between NO_x and NO_y
488 molecules.
489
490 **5. Conclusions**
491 The effect of NO_x photochemistry on the nitrogen isotopic fractionations between NO and
492 NO_2 was investigated. We first measured the isotopic fractionations between NO and NO_2 and
493 provided mathematical solutions to assess the impact of NO_x level and NO_2 photolysis rate ($j(NO_2)$)
494 to the relative importance of EIE and LCIE. The EIE and LCIE isotope fractionation factors, at

room temperature, were determined to be 1.0275±0.0012 and 0.990±0.005, respectively. These calculations and measurements can be used to determine the steady state $\Delta(NO_2\text{-}NO)$ and $\Delta(NO_2\text{-}NO_x)$ values at room temperature. Subsequently we applied our equations to polluted, clean and remote sites to model the daily variations of $\Delta(NO_2\text{-}NO_x)$ values. We found that the $\Delta(NO_2\text{-}NO_x)$ values could vary from over +20 ‰ to less than -5 ‰ depending on the environment: in general, the role of LCIE becoming more important at low NO_x concentrations, which tend to decrease the $\Delta(NO_2\text{-}NO_x)$ values. Our work provided a mathematical approach to quantify the nitrogen isotopic fractionations between NO and NO_2 that can be applied to many tropospheric environments, which could help interpret the measured $\delta^{15}N$ values of NO_2 and nitrate in field observation studies.

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Data Availability

Data acquired from this study was deposited at Open Sciences Framework (Li, 2019, DOI 10.17605/OSF.IO/JW8HU).

Author contribution

J. Li and G. Michalski designed the experiments, X. Zhang and J. Li conducted the experiments. X. Zhang, G. Michalski, J. Orlando and G. Tyndall helped J. Li in interpreting the

results. The manuscript was written by J. Li and all the authors have contributed during the revision of this manuscript.

Competing interest

The authors declare no competing interest.

References:

Atkinson, R., Baulch, D. L., Cox, R. A., Crowley, J. N., Hampson, R. F., Hynes, R. G., Jenkin, M. E., Rossi, M. J., and Troe, J. (2004). Evaluated kinetic and photochemical data for atmospheric chemistry: Volume I-gas phase reactions of O_x, HO_x, NO_x and SO_x. Atmospheric chemistry and physics, 4(6), 1461-1738. https://doi.org/10.5194/acp-4-1461-2004, 2004

Barney, W. S., & Finlayson-Pitts, B. J. (2000). Enhancement of N_2O_4 on porous glass at room temperature: A key intermediate in the heterogeneous hydrolysis of NO_2? The Journal of Physical Chemistry A, 104(2), 171–175. https://doi.org/10.1021/jp993169b

Begun, G. M., & Fletcher, W. H. (1960). Partition function ratios for molecules containing nitrogen isotopes. The Journal of Chemical Physics, 33(4), 1083–1085. https://doi.org/10.1063/1.1731338

Begun, G. M., & Melton, C. E. (1956). Nitrogen isotopic fractionation between NO and NO_2 and mass discrimination in mass analysis of NO_2. The Journal of Chemical Physics, 25(6), 1292–1293. https://doi.org/10.1063/1.1743215

Beine, H. J., Honrath, R. E., Dominé, F., Simpson, W. R., & Fuentes, J. D. (2002). NO_x during background and ozone depletion periods at Alert: Fluxes above the snow surface. Journal of Geophysical Research: Atmospheres, 107(D21), ACH-7. https://doi.org/10.1029/2002JD002082

Bigeleisen, J., & Mayer, M. G. (1947). Calculation of equilibrium constants for isotopic exchange reactions. The Journal of Chemical Physics, 15(5), 261-267. https://doi.org/10.1063/1.1746492

Bigeleisen, J., & Wolfsberg, M. (1957). Theoretical and experimental aspects of isotope effects in chemical kinetics. Advances in Chemical Physics, 15–76. https://doi.org/10.1002/9780470143476.ch2

Casciotti, K. L., & McIlvin, M. R. (2007). Isotopic analyses of nitrate and nitrite from reference mixtures and application to Eastern Tropical North Pacific waters. Marine Chemistry, 107(2), 184–201. https://doi.org/10.1016/j.marchem.2007.06.021

Chang, Y., Zhang, Y., Tian, C., Zhang, S., Ma, X., Cao, F., et al. (2018). Nitrogen isotope fractionation during gas-to-particle conversion of NO_x to NO_3^- in the atmosphere–implications for

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isotope-based NO_x source apportionment. Atmospheric Chemistry and Physics, 18(16), 11647–11661. https://doi.org/10.5194/acp-18-11647-2018, 2018.

Clapp, L. J., & Jenkin, M. E. (2001). Analysis of the relationship between ambient levels of O_3, NO_2 and NO as a function of NO_x in the UK. Atmospheric Environment, 35(36), 6391–6405. https://doi.org/10.1016/S1352-2310(01)00378-8

Custard, K. D., Thompson, C. R., Pratt, K. A., Shepson, P. B., Liao, J., Huey, L. G., Orlando, J. J., Weinheimer, A. J., Apel, E., Hall, S. R., Flocke, F., Mauldin, L., Hornbrook, R. S., Pöhler, D., General, S., Zielcke, J., Simpson, W. R., Platt, U., Fried, A., Weibring, P., Sive, B. C., Ullmann, K., Cantrell, C., Knapp, D. J., and Montzka, D. D.: The NOx dependence of bromine chemistry in the Arctic atmospheric boundary layer, Atmos. Chem. Phys., 15, 10799–10809, https://doi.org/10.5194/acp-15-10799-2015, 2015.

Dibb, J. E., Arsenault, M., Peterson, M. C., & Honrath, R. E. (2002). Fast nitrogen oxide photochemistry in Summit, Greenland snow. Atmospheric Environment, 36(15–16), 2501–2511. https://doi.org/10.1016/S1352-2310(02)00130-9

Do Remus, R. H., Mehrotra, Y., Lanford, W. A., & Burman, C. (1983). Reaction of water with glass: influence of a transformed surface layer. Journal of Materials Science, 18(2), 612–622. https://doi.org/10.1007/BF00560651

Elliott, E. M., Kendall, C., Boyer, E. W., Burns, D. A., Lear, G. G., Golden, H. E., Harlin, K., Bytnerowicz, A., Butler, T. J., and Glatz, R. (2009). Dual nitrate isotopes in dry deposition: Utility for partitioning NO_x source contributions to landscape nitrogen deposition. Journal of Geophysical Research: Biogeosciences, 114(G4), G04020. https://doi.org/10.1029/2008JG000889

Felix, J. D., & Elliott, E. M. (2014). Isotopic composition of passively collected nitrogen dioxide emissions: Vehicle, soil and livestock source signatures. Atmospheric Environment, 92, 359–366. https://doi.org/10.1016/j.atmosenv.2014.04.005

Felix, J. D., Elliott, E. M., & Shaw, S. L. (2012). Nitrogen isotopic composition of coal-fired power plant NO_x: influence of emission controls and implications for global emission inventories. Environmental Science & Technology, 46(6), 3528–3535. https://doi.org/10.1021/es203355v

Frey, M. M., Savarino, J., Morin, S., Erbland, J., & Martins, J. M. F. (2009). Photolysis imprint in the nitrate stable isotope signal in snow and atmosphere of East Antarctica and implications for reactive nitrogen cycling. Atmos. Chem. Phys, 9, 8681-8696. https://doi.org/10.5194/acp-9-8681-2009, 2009.

Freyer, H. D. (1991). Seasonal variation of $^{15}N/^{14}N$ ratios in atmospheric nitrate species. Tellus B, 43(1), 30–44. https://doi.org/10.1034/j.1600-0889.1991.00003.x

Freyer, H. D., Kley, D., Volz-Thomas, A., & Kobel, K. (1993). On the interaction of isotopic exchange processes with photochemical reactions in atmospheric oxides of nitrogen. Journal of Geophysical Research: Atmospheres, 98(D8), 14791–14796. https://doi.org/10.1029/93JD00874

Deleted: Custard, K. D., Thompson, C. R., Pratt, K. A., Shepson, P. B., Liao, J., Huey, L. G., et al. (2015). The NO_x dependence of bromine chemistry in the Arctic atmospheric boundary layer. Atmospheric Chemistry and Physics, 15(18), 10799–10809.¶

Deleted: Elliott, E. M., Kendall, C., Boyer, E. W., Burns, D. A., Lear, G. G., Golden, H. E., et al. (2009).

Gao, H. O. (2007). Day of week effects on diurnal ozone/NO_x cycles and transportation emissions in Southern California. Transportation Research Part D: Transport and Environment, 12(4), 292–305. https://doi.org/10.1016/j.trd.2007.03.004

Gobel, A. R., Altieri, K. E., Peters, A. J., Hastings, M. G., & Sigman, D. M. (2013). Insights into anthropogenic nitrogen deposition to the North Atlantic investigated using the isotopic composition of aerosol and rainwater nitrate. Geophysical Research Letters, 40(22), 5977–5982. https://doi.org/10.1002/2013GL058167

Hastings, M G, Jarvis, J. C., & Steig, E. J. (2009). Anthropogenic impacts on nitrogen isotopes of ice-core nitrate. Science, 324(5932), 1288. DOI: 10.1126/science.1170510

Hastings, M G, Steig, E. J., & Sigman, D. M. (2004). Seasonal variations in N and O isotopes of nitrate in snow at Summit, Greenland: Implications for the study of nitrate in snow and ice cores. Journal of Geophysical Research: Atmospheres, 109(D20). https://doi.org/10.1029/2004JD004991

Honrath, R. E., Peterson, M. C., Guo, S., Dibb, J. E., Shepson, P. B., & Campbell, B. (1999). Evidence of NO_x production within or upon ice particles in the Greenland snowpack. Geophysical Research Letters, 26(6), 695–698. https://doi.org/10.1029/1999GL900077

Jarvis, J. C., Steig, E. J., Hastings, M. G., & Kunasek, S. A. (2008). Influence of local photochemistry on isotopes of nitrate in Greenland snow. Geophysical Research Letters, 35(21). https://doi.org/10.1029/2008GL035551

Kendall, C., Elliott, E. M., & Wankel, S. D. (2007). Tracing anthropogenic inputs of nitrogen to ecosystems. Stable Isotopes in Ecology and Environmental Science, 2, 375–449. https://doi.org/10.1002/9780470691854.ch12

Kimbrough, S., Owen, R. C., Snyder, M., & Richmond-Bryant, J. (2017). NO to NO_2 conversion rate analysis and implications for dispersion model chemistry methods using Las Vegas, Nevada near-road field measurements. Atmospheric Environment, 165, 23–34. https://doi.org/10.1016/j.atmosenv.2017.06.027

King, M. D., Canosa-Mas, C. E. and Wayne R. P. (2001). Gas-phase reactions between RO_2 and NO, HO_2 or CH_3O_2: correlations between rate constants and the SOMO energy of the peroxy (RO_2) radical. Atmospheric Environment 35.12 (2001): 2081-2088. https://doi.org/10.1016/S1352-2310(00)00501-X

Knote, C., Tuccella, P., Curci, G., Emmons, L., Orlando, J. J. Madronich, S., Baró, R., Jiménez-Guerrero, P., Luecken, D., Hogrefe, C., Forkel, R., Werhahn, J., Hirtl, M., Pérez, J. L., San José, R., Giordano, L., Brunner, D., Yahya, K., Zhang, Y., Influence of the choice of gas-phase mechanism on predictions of key gaseous pollutants during the AQMEII phase-2 intercomparison. Atmospheric Environment 115 (2015): 553-568. https://doi.org/10.1016/j.atmosenv.2014.11.066.

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Li, J. (2019). Quantifying the nitrogen equilibrium and photochemistry-induced kinetic isotopic effects between NO and NO_2. Retrieved from osf.io/jw8hu

Madronich, S., & Flocke, S. (1999). The role of solar radiation in atmospheric chemistry. In Environmental photochemistry (pp. 1–26). The Handbook of Environmental Chemistry (Reactions and Processes), vol 2 / 2L. Springer, Berlin, Heidelberg, https://doi.org/10.1007/978-3-540-69044-3_1

Mazzeo, N. A., Venegas, L. E., & Choren, H. (2005). Analysis of NO, NO_2, O_3 and NO_x concentrations measured at a green area of Buenos Aires City during wintertime. Atmospheric Environment, 39(17), 3055–3068. https://doi.org/10.1016/j.atmosenv.2005.01.029

McIlvin, M. R., & Altabet, M. A. (2005). Chemical conversion of nitrate and nitrite to nitrous oxide for nitrogen and oxygen isotopic analysis in freshwater and seawater. Analytical Chemistry, 77(17), 5589–5595. https://doi.org/10.1021/ac050528s

Michalski, G., Jost, R., Sugny, D., Joyeux, M., & Thiemens, M. (2004). Dissociation energies of six NO_2 isotopologues by laser induced fluorescence spectroscopy and zero-point energy of some triatomic molecules. The Journal of Chemical Physics, 121(15), 7153–7161. https://doi.org/10.1063/1.1792233

Michalski, G., Bockheim, J. G., Kendall, C., & Thiemens, M. (2005). Isotopic composition of Antarctic Dry Valley nitrate: Implications for NO_y sources and cycling in Antarctica. Geophysical Research Letters, 32(13). https://doi.org/10.1029/2004GL022121

Miller, C. E., & Yung, Y. L. (2000). Photo-induced isotopic fractionation. Journal of Geophysical Research: Atmospheres, 105(D23), 29039–29051. https://doi.org/10.1029/2000JD900388

Monse, E. U., Spindel, W., & Stern, M. J. (1969). Analysis of isotope-effect calculations illustrated with exchange equilibria among oxynitrogen compounds. Rutgers-The State Univ., Newark, NJ. DOI: 10.1021/ba-1969-0089.ch009

Morin, S., Savarino, J., Frey, M. M., Domine, F., Jacobi, H.-W., Kaleschke, L., & Martins, J. M. F. (2009). Comprehensive isotopic composition of atmospheric nitrate in the Atlantic Ocean boundary layer from 65°S to 79°N. J. Geophys. Res, 114. https://doi.org/10.1029/2008JD010696

Park, Y.-M., Park, K.-S., Kim, H., Yu, S.-M., Noh, S., Kim, M.-S., Kim, J.-Y., Ahn, J.-Y., Lee, M.-D., Seok, K.-S., Kin, Y.-H., (2018). Characterizing isotopic compositions of TC-C, NO_3^--N, and NH_4^+-N in PM2.5 in South Korea: Impact of China's winter heating. https://doi.org/10.1016/j.envpol.2017.10.072

Saliba, N. A., Yang, H., & Finlayson-Pitts, B. J. (2001). Reaction of gaseous nitric oxide with nitric acid on silica surfaces in the presence of water at room temperature. The Journal of Physical Chemistry A, 105(45), 10339–10346. https://doi.org/10.1021/jp012330r

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Savarino, J., Morin, S., Erbland, J., Grannec, F., Patey, M. D., Vicars, W., Alexander, B., Achterberg, E. P., (2013). Isotopic composition of atmospheric nitrate in a tropical marine boundary layer. Proceedings of the National Academy of Sciences, 110(44), 17668–17673. https://doi.org/10.1073/pnas.1216639110

Sharma, H. D., Jervis, R. E., & Wong, K. Y. (1970). Isotopic exchange reactions in nitrogen oxides. The Journal of Physical Chemistry, 74(4), 923–933. https://doi.org/10.1021/j100699a044

Takei, T., Yamazaki, A., Watanabe, T., & Chikazawa, M. (1997). Water adsorption properties on porous silica glass surface modified by trimethylsilyl groups. Journal of Colloid and Interface Science, 188(2), 409–414. https://doi.org/10.1006/jcis.1997.4777

Urey, H. C. (1947). The thermodynamic properties of isotopic substances. Journal of the Chemical Society (Resumed), 562-581. https://doi.org/10.1039/JR9470000562

Vicars, W. C., Morin, S., Savarino, J., Wagner, N. L., Erbland, J., Vince, E., Martins, J. M. F., Lerner, B. M., Quinn, P. K., Coffman, D. J., Williams, E. J., Brown, S. S., (2013). Spatial and diurnal variability in reactive nitrogen oxide chemistry as reflected in the isotopic composition of atmospheric nitrate: Results from the CalNex 2010 field study. Journal of Geophysical Research: Atmospheres, 118(18), 10–567. https://doi.org/10.1002/jgrd.50680

Walters, W. W., & Michalski, G. (2015). Theoretical calculation of nitrogen isotope equilibrium exchange fractionation factors for various NO_y molecules. Geochimica et Cosmochimica Acta, 164, 284–297. https://doi.org/10.1016/j.gca.2015.05.029

Walters, W. W., Goodwin, S. R., & Michalski, G. (2015). Nitrogen stable isotope composition ($\delta^{15}N$) of vehicle-emitted NO_x. Environmental Science & Technology, 49(4), 2278–2285. https://doi.org/10.1021/es505580v

Walters, W. W., & Michalski, G. (2016). Ab initio study of nitrogen and position-specific oxygen kinetic isotope effects in the $NO+O_3$ reaction. The Journal of chemical physics, 145(22), 224311. https://doi.org/10.1063/1.4968562

Walters, W. W., Simonini, D. S., & Michalski, G. (2016). Nitrogen isotope exchange between NO and NO_2 and its implications for $\delta^{15}N$ variations in tropospheric NO_x and atmospheric nitrate. Geophysical Research Letters, 43(1), 440–448. https://doi.org/10.1002/2015GL066438

Walters, W. W., Fang, H., & Michalski, G. (2018). Summertime diurnal variations in the isotopic composition of atmospheric nitrogen dioxide at a small midwestern United States city. Atmospheric Environment, 179, 1–11. https://doi.org/10.1016/j.atmosenv.2018.01.047

Williams, E. L., & Grosjean, D. (1990). Removal of atmospheric oxidants with annular denuders. Environmental Science & Technology, 24(6), 811–814. https://doi.org/10.1021/es00076a002

Yang, J., Honrath, R. E., Peterson, M. C., Dibb, J. E., Sumner, A. L., Shepson, P. B., Frey, M., Jacobi, H.-W., Swanson, A., Blake, N., (2002). Impacts of snowpack emissions on deduced levels

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of OH and peroxy radicals at Summit, Greenland. Atmospheric Environment, 36(15–16), 2523–2534. https://doi.org/10.1016/S1352-2310(02)00128-0

Zhang, X., Ortega, J., Huang, Y., Shertz, S., Tyndall, G. S., & Orlando, J. J. (2018). A steady-state continuous flow chamber for the study of daytime and nighttime chemistry under atmospherically relevant NO levels. Atmospheric Measurement Techniques, 11(5), 2537–2551. https://doi.org/10.5194/amt-11-2537-2018

Zong, Z., Wang, X., Tian, C., Chen, Y., Fang, Y., Zhang, F., Li, C., Sun, J., Li, J., Zhang, G., (2017). First assessment of NO_x sources at a regional background site in North China using isotopic analysis linked with modeling. Environmental Science & Technology, 51(11), 5923–5931. https://doi.org/10.1021/acs.est.6b06316

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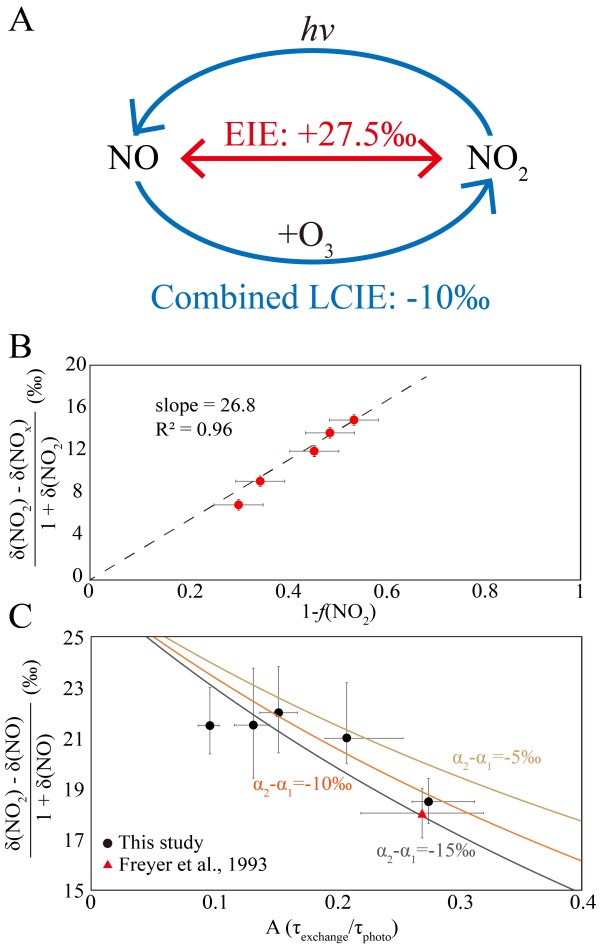

Fig. 1 A. a sketch of the isotopic fractionation processes between NO and NO_2, both fractionation factors are determined in this work. **B.** Results from five dark experiments yielded a line with slope of 0.0268 and an $\alpha(NO_2\text{-}NO)$ value of 1.0275; **C.** Results from five UV irradiation experiments (black points) and a previous field study (red triangle). The three lines represent different (α_2-α_1) values: the (α_2-α_1)=-10 ‰ line showed the lowest RMSE to our experimental data as well as the previous field observation. The error bars in panels B and C represented the combined uncertainties of NO_x concentration measurements and isotopic analysis.

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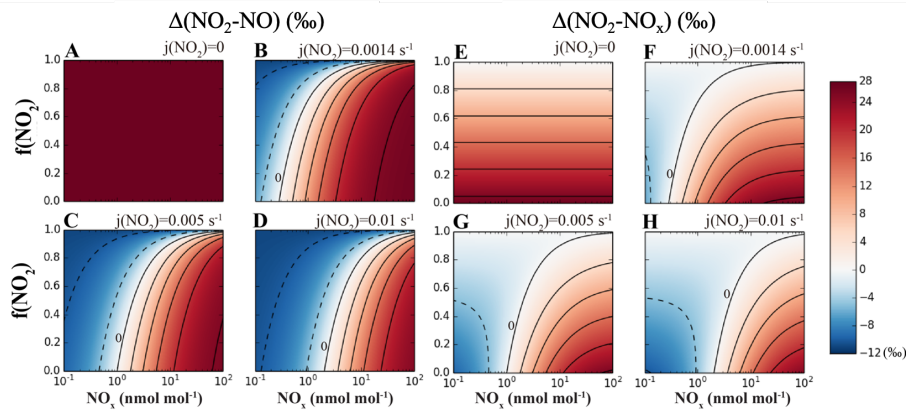

Fig. 2 Calculating isotopic fractionation values between NO-NO_2 ($\Delta(NO_2\text{-}NO)$, **A-D**) and NO_x-NO_2 ($\Delta(NO_2\text{-}NO_x)$, **E-H**) at various $j(NO_2)$, NO_x level and $f(NO_2)$ using Eq. (7) and (8). Each panel represents a fixed $j(NO_2)$ value (showing on the upper right side of each panel), and the fractionation values are shown by color. Lines are contours with the same fractionation values, at an interval of 5‰, the contour line representing 0‰ was marked on each panel except for A and E.

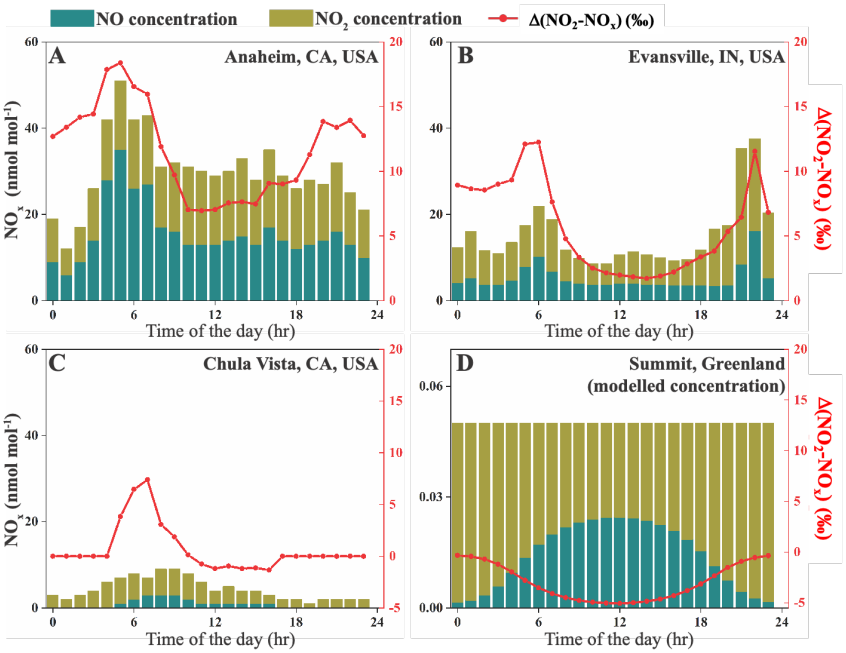

Fig. 3 NO_x concentrations and calculated $\Delta(NO_2\text{-}NO_x)$ values at four sites. Stacked bars show the NO and NO_2 concentrations extracted from monitoring sites (A-C) or calculated using 0-D box model (D); the red lines are $\Delta(NO_2\text{-}NO_x)$ values at each site. Note that the NO_x concentration (left-y) axis on panel D is different from the rest.

Appendix A. Chamber descriptions

The chamber is a 10 m^3 Teflon bag equipped with several standard instruments including temperature and humidity probe, NO_x monitor and O_3 monitor. 128 wall-mounted blacklight tubes surrounded the chamber to mimic tropospheric photochemistry and the photolysis rate of NO_2 ($j(NO_2)$) when all lights are on have been previously determined to be 1.4×10^{-3} s^{-1}, similar to a $j(NO_2)$ coefficient at an 81-degree solar zenith angle. The irradiation spectrum of the blacklights are shown in Figure A1. The chamber was kept at room temperature and one atmospheric pressure. Before each experiment, the chamber was flushed with zero air at 40 L min^{-1} for at least 12 hours to ensure the background NO_x, O_3 and other trace gases were below detection limit.

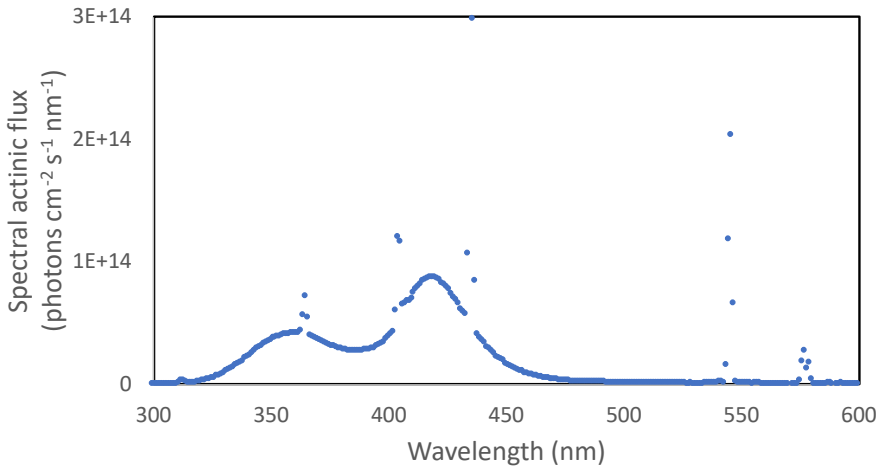

Figure A1 Spectral actinic flux versus wavelengths of the UV light source used in our experiments.

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Appendix B. Box model assessing the time needed for $NO-NO_2$ to reach isotopic equilibrium

The time needed to reach $NO-NO_2$ isotopic equilibrium during light-off experiments were assessed using a 0-D box model. This box model contains only two reactions:

$^{15}NO_2 + {}^{14}NO \rightarrow {}^{15}NO + {}^{14}NO_2$ $k = 8.14000 \times 10^{-14}$ cm^3 s^{-1}

$^{15}NO + {}^{14}NO_2 \rightarrow {}^{15}NO_2 + {}^{14}NO$ $k' = 8.36385 \times 10^{-14}$ cm^3 s^{-1}

Where k and k' are rate constants of the reactions. The differences in rate constants were calculated by assuming an $\alpha(NO_2\text{-}NO)$ value of 1.0275. Six simulations were conducted at various initial NO (with $\delta^{15}N = 0‰$) and O_3 levels that were similar to our experiment. Then the $\delta^{15}N$ values of NO and NO_2 during the simulation were calculated from the model and were shown in Figure B1, suggesting that in our experimental condition, all systems should reach isotopic equilibrium within 1 hr.

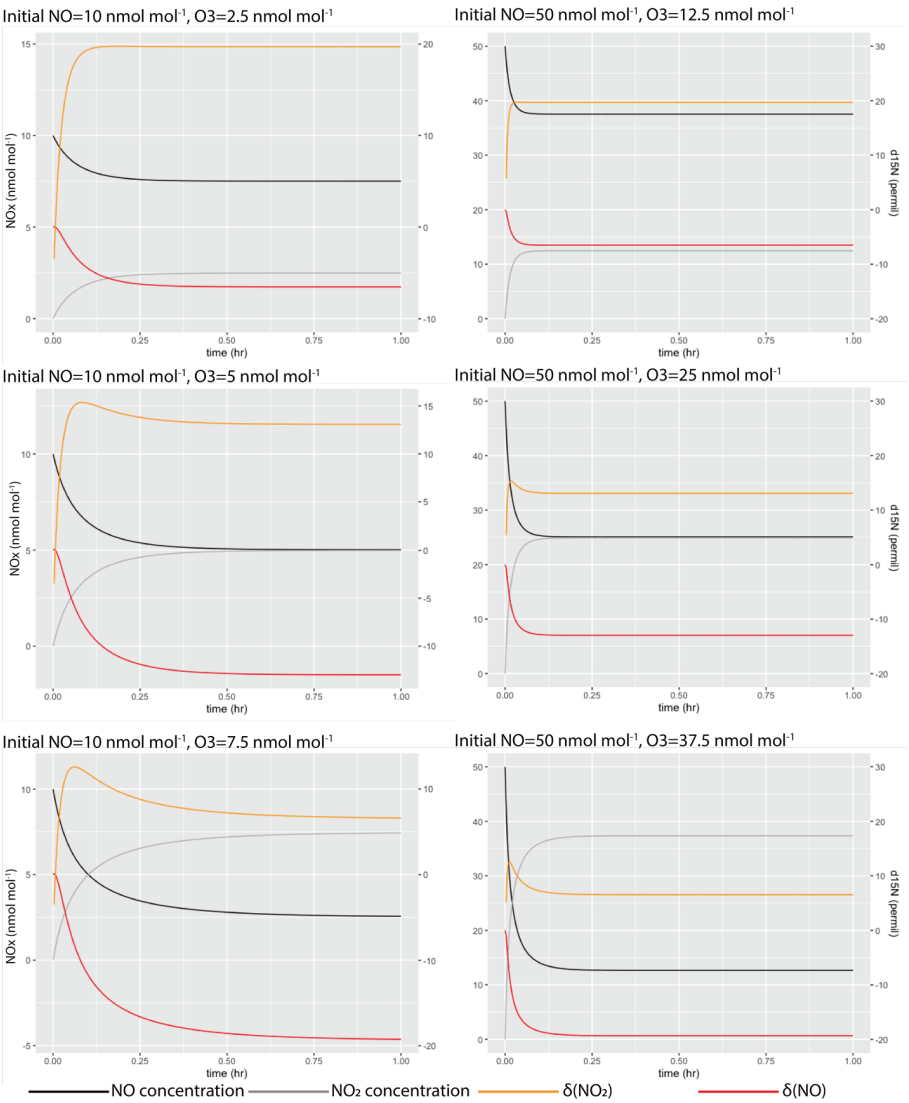

Figure B1 Simulated NO-NO_2 isotopic equilibrium process in the chamber at various NO and O_3 concentrations.

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Appendix C. Deriving Equations 7 and 8

When the system (R1-R6) reaches steady-state, we have:

$$d[^{15}NO_2]/dt=0 \quad \text{Eq. (C1)}$$

Therefore, using R1-R6:

$$k_1 [^{15}NO_2][^{14}NO]+j(NO_2)\alpha_1[^{15}NO_2]=$$

$$k_5\alpha_2[^{15}NO][O_3]+ k_1\alpha(NO_2\text{-}NO) [^{15}NO][^{14}NO_2] \quad \text{Eq. (C2)}$$

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From here we refer $^{14}NO_2$ and ^{14}NO as NO_2 and NO for convenience, rearrange the above equation, we get:

$$\frac{[^{15}NO_2]}{[^{15}NO]} = \frac{k_5\alpha_2[O_3]+k_1\alpha(NO_2-NO)\,[NO_2]}{j_{NO2}\alpha_1+k_1[NO]} \quad \text{Eq. (C3)}$$

Meantime, since the Leighton cycle reaction still holds for the majority isotopes (NO and NO_2), we have:

$$j_{NO2}[NO_2]= k_5[NO][O_3] \quad \text{Eq. (C4)}$$

Thus,

$$\frac{[NO_2]}{[NO]} = \frac{k_5\times[O_3]}{j_{NO2}} \quad \text{Eq. (C5)}$$

From the text, when $j_{NO2}>0$, we defined $A=\tau_{exchange}/\tau_{photo}=j_{NO2}/(k_1\times[NO])$. Using the above equations, we know:

$$\frac{j_{NO2}}{[NO]} = \frac{k_5[O_3]}{[NO_2]} = Ak_1 \quad \text{Eq. (C6)}$$

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$$\frac{j_{NO2}}{k_1[NO]} = \frac{k_5[O_3]}{k_1[NO_2]} = A \quad \text{Eq. (C7)}$$

Next, to calculate $\delta(NO_2)$-$\delta(NO)$, we use the definition of delta notation:

$$\delta(NO_2)\text{-}\delta(NO) = R_{NO2}/R_{std}\text{-}\ R_{NO}/R_{std} = (R_{NO2}/R_{NO}\text{-}1)(1+\delta(NO)) \quad \text{Eq. (C8)}$$

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$$\frac{R_{NO2}}{R_{NO}} = \frac{[^{15}NO_2][NO]}{[^{15}NO][NO_2]} = \frac{k_5\alpha_2[O_3][NO]+k_1\alpha(NO_2-NO)[NO_2][NO]}{j_{NO2}\alpha_1[NO_2]+k_1[NO][NO_2]} \quad \text{Eq. (C9)}$$

Divide both side by $k_1[NO][NO_2]$:

$$\frac{R_{NO2}}{R_{NO}} = \frac{\frac{k_5\alpha_2[O_3]}{k_1[NO_2]}+\alpha(NO_2-NO)}{\frac{j_{NO2}\alpha_1}{k_1[NO]}+1} \quad \text{Eq. (C10)}$$

Rearrange and substitute $\frac{k_5[O_3]}{k_1[NO_2]}$ and $\frac{j_{NO2}}{k_1[NO]}$ with A:

$$\frac{R_{NO2}}{R_{NO}} = \frac{\alpha_2\times A+\alpha(NO_2-NO)}{\alpha_1\times A+1} \quad \text{Eq. (C11)}$$

$$\frac{R_{NO2}}{R_{NO}} - 1 = \frac{(\alpha_2-\alpha_1)\times A+(\alpha(NO_2-NO)-1)}{\alpha_1\times A+1} \quad \text{Eq. (C12)}$$

Thus,

$$\delta(NO_2)-\delta(NO)=\frac{(\alpha_2-\alpha_1)\times A+(\alpha(NO_2-NO)-1)}{\alpha_1\times A+1}(1+\delta(NO)) \quad \text{Eq. (C13)}$$

Since $\alpha_1 \approx 1$, $\alpha_1\times A+1 \approx 1+A$ this equation can be further simplified to Eq. 7:

$$\delta(NO_2)-\delta(NO)=\frac{(\alpha_2-\alpha_1)*A+\alpha(NO_2-NO)-1)}{A+1}(1+\delta(NO)) \quad \text{Eq. (C14)}$$

Then, using mass balance:

$$\delta(NO_2)\, f(NO_2)+\delta(NO)(1- f(NO_2)) = \delta(NO_x) \quad \text{Eq. (C15)}$$

We can derive Eq. 8:

$$\delta(NO_2)-\delta(NO_x)=\frac{(\alpha_2-\alpha_1)\times A+\alpha(NO_2-NO)-1)}{A+1}(1+\delta(NO))\,(1- f(NO_2)) \quad \text{Eq. (C16)}$$

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