

1 **Core and margin in warm convective clouds. Part I: core types and evolution**  
2 **during a cloud's lifetime**

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17 **Abstract:**

18 The properties of a warm convective cloud are determined by the competition between  
19 the growth and dissipation processes occurring within it. One way to observe and follow  
20 this competition is by partitioning the cloud to core and margin regions. Here we look  
21 at three core definitions: positive vertical velocity ( $W_{core}$ ), supersaturation ( $RH_{core}$ ),  
22 and positive buoyancy ( $B_{core}$ ), and follow their evolution throughout the lifetime of  
23 warm convective clouds.

24 Using single cloud and cloud field simulations with bin-microphysics schemes, we  
25 show that the different core types tend to be subsets of one another in the following  
26 order:  $B_{core} \subseteq RH_{core} \subseteq W_{core}$ . This property is seen for several different  
27 thermodynamic profile initializations, and is generally maintained during the growing  
28 and mature stages of a cloud's lifetime. This finding is in line with previous works and  
29 theoretical predictions showing that cumulus clouds may be dominated by negative  
30 buoyancy at certain stages of their lifetime.

31 During its mature and growth stage, the cloud and its cores are centered at a similar  
32 location. During cloud dissipation the cores show less overlap, typically reduce in size,  
33 and migrate from the cloud centroid. In some cases, buoyancy cores can reemerge and  
34 often reside at the cloud periphery. Thus, the core-shell model of a positively buoyant  
35 center surrounded by negatively buoyant shell only applies to a fraction of the cloud  
36 lifetime.

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## 39 **1. Introduction**

40 Clouds are important players in the climate system (Trenberth et al., 2009), and  
41 currently constitute one of the largest uncertainties in climate and climate change  
42 research (IPCC, 2013). One of the reasons for this large uncertainty is the complexity  
43 created by opposing processes that occur at the same time but in different locations  
44 within a cloud. Although a cloud is generally considered as a single entity, physically,  
45 it can be partitioned to two main regions: i) a core region, where mainly cloud growth  
46 processes occur (i.e. condensation – accumulation of cloud mass), and ii) a margin  
47 region, where cloud suppression processes occur (i.e. evaporation - loss of cloud mass).  
48 Changes in thermodynamic or microphysical (aerosol) conditions impact the processes  
49 in both regions (sometimes in different ways), and thus the resultant total cloud  
50 properties (Dagan et al., 2015). To better understand cloud properties and their  
51 evolution in time, it is necessary to understand the interplay between physical processes  
52 within the core and margin regions (and the way they are affected by perturbations in  
53 the environmental conditions).

54 Considering convective clouds, there are several objective measures that have been  
55 used in previous works for separating a cloud's core from its margins (will be referred  
56 to as physical cores hereafter). In deep convective cloud simulations the core is usually  
57 defined by the updrafts' magnitude using a certain threshold, usually  $W > 1 \text{ m}\cdot\text{s}^{-1}$   
58 (Khairoutdinov et al., 2009; Kumar et al., 2015; Lebo and Seinfeld, 2011; Morrison,  
59 2012). Studies on warm cumulus clouds have defined the clouds' core as parts with  
60 positive buoyancy and positive updrafts (de Roode et al., 2012; Dawe and Austin, 2012;  
61 Heus and Jonker, 2008; Siebesma and Cuijpers, 1995) or solely regions with positively  
62 buoyancy (Heus and Seifert, 2013; Seigel, 2014). More recently, cloud partition to  
63 regions of supersaturation and sub-saturation has been used to define the cloud core in  
64 single cloud simulations (Dagan et al., 2015).

65 For simplicity, we focus on warm convective clouds (only contain liquid water),  
66 avoiding the additional complexity and uncertainties associated with mixed phase and  
67 ice phase microphysics. The common assumption when partitioning a convective cloud  
68 to its physical core and margin is that that the cloud core is at its geometrical center and  
69 the peripheral regions (i.e. edges) are the margin. Previous observational (Heus et al.,  
70 2009a; Rodts et al., 2003; Wang et al., 2009) and numerical (Heus and Jonker, 2008;

71 Jonker et al., 2008; Seigel, 2014) works have studied the gradients of cloud  
 72 thermodynamic properties from cloud center to edge, and suggest that a cloud is best  
 73 described by a core-shell model. This model assumes a core with positive vertical  
 74 velocity and buoyancy, surrounded by a shell with negative vertical velocity and  
 75 buoyancy. The shell is the region where mixing between cloudy and environmental air  
 76 parcels occurs, leading to evaporative cooling → decrease in buoyancy → decrease in  
 77 vertical velocity.

78 Based on previous findings, here we explore the partition of clouds to core and margin  
 79 using three different objective core definitions where the cloud core threshold is set to  
 80 be a positive value (of buoyancy, vertical velocity, or supersaturation). Cloud buoyancy  
 81 ( $B$ ) can be approximated by the following formula:

$$82 \quad B = g \cdot \left( \frac{\theta'}{\theta_0} + 0.61q'_v - q_l \right) \quad (1),$$

83 Where  $\theta_0$  represents the reference state potential temperature,  $q_v$  is the water vapor  
 84 mixing ratio, and  $q_l$  is the liquid water content. The ( $'$ ) stands for the deviation from the  
 85 reference state per height (Wang et al., 2009). Buoyancy is a measure for the vertical  
 86 acceleration and its integral is the convective potential energy. Latent heat release  
 87 during moist adiabatic ascent fuels positive buoyancy and clouds' growth, while  
 88 evaporation and subsequent cooling drives cloud decay (de Roode, 2008; Betts, 1973).  
 89 The prevalence of negatively buoyancy parcels at the cloud edges due to mixing and  
 90 evaporation is a well-known phenomenon (Morrison, 2017). Mixing diagrams have  
 91 been used to assess this effect (de Roode, 2008; Paluch, 1979; Taylor and Baker, 1991),  
 92 and are at the root of convective parameterization schemes (Emanuel, 1991; Gregory  
 93 and Rowntree, 1990; Kain and Fritsch, 1990) and parameterizations of entrainment and  
 94 detrainment in cumulus clouds (de Rooy and Siebesma, 2008; Derbyshire et al., 2011).

95 Neglecting cases of air flow near obstacles or air mass fronts, buoyancy is the main  
 96 source for vertical momentum in the cloud. In its simplest form, the vertical velocity  
 97 ( $w$ ) in the cloud can be approximated by the convective available potential energy  
 98 (CAPE) of the vertical column up to that height (Rennó and Ingersoll, 1996; Williams  
 99 and Stanfill, 2002; Yano et al., 2005):

$$100 \quad 0.5w^2(h) = \int_{h_0}^h B(z) dz = CAPE(h) \quad (2).$$

101 Here we define CAPE to be the vertical integral of buoyancy from the lowest level of  
 102 positive buoyancy ( $h_0$ , initiation of vertical velocity) to an arbitrary top height ( $h$ ).  
 103 Usually, the CAPE serves as a theoretical upper limit, and the vertical velocity is  
 104 smaller due to multiple effects (de Roode et al., 2012), most importantly the  
 105 perturbation pressure gradient force (which oppose the air motion) and mixing with the  
 106 environment (entrainment/detrainment) (de Roode et al., 2012; Morrison, 2016a;  
 107 Peters, 2016). Recent studies have shown that entrainment effects on vertical velocity  
 108 are of second order, and a rising thermal shows a balance between buoyancy and the  
 109 perturbation pressure gradient (Hernandez-Deckers and Sherwood, 2016; Romps and  
 110 Charn, 2015), the latter acting as a drag force on the updrafts. Nevertheless, initial  
 111 updraft and environmental conditions play a crucial role in determining the magnitude  
 112 of mixing effects on buoyancy, and thus also the vertical velocity profile in the cloud  
 113 (Morrison, 2016a, 2016b, 2017).

114 The supersaturation ( $S$ , where  $S=1$  is 100% relative humidity) core definition ( $S-1>0$  or  
 115  $RH>100\%$ ) partitions the cloud core and margin to areas of condensation and  
 116 evaporation. Since we consider hconvective clouds, the only driver of supersaturation  
 117 during cloud growth is upward vertical motion of air. Neglecting mixing with the  
 118 environment,  $S$  and  $w$  can be linked as follows:

$$119 \quad \frac{dS}{dt} = Q_1 w - Q_2 \frac{dq_l}{dt} \quad (3),$$

120 where  $Q_1, Q_2$  are thermodynamic factors (Rogers and Yau, 1989). The thermodynamic  
 121 factors are nearly insensitive to pressure for temperature above  $0^\circ\text{C}$ , and both weakly  
 122 decrease (less than 15% net change) with temperature increase between  $0^\circ\text{C}$  and  $30^\circ\text{C}$   
 123 (Pinsky et al., 2013). The first term on the right-hand side is related to the change in the  
 124 supersaturation due to adiabatic cooling or heating of the moist air (due to vertical  
 125 motion). The second term is related to the change in the supersaturation due to  
 126 condensation/evaporation of water vapor/drops. Hence, the supersaturation in a rising  
 127 parcel depends on the magnitude of the updraft and on the condensation rate of vapor  
 128 to drops (a sink term). The latter is proportional to the concentration of aerosols in the  
 129 cloud (Reutter et al., 2009; Seiki and Nakajima, 2014), which serve as cloud  
 130 condensation nuclei (CCN) for cloud droplets. In Part II of this work we demonstrate  
 131 some of the insights gained by investigating differences between the different cores  
 132 properties and their time evolution when changing the aerosol loading.

133 The purpose of this part of the work (part I) is to compare and understand the differences  
134 between the three basic definitions of cloud core (i.e.  $W_{core}$ ,  $RH_{core}$ ,  $B_{core}$ ) throughout  
135 a convective cloud's lifetime, using both theoretical arguments and numerical  
136 simulations. It should be noted that the bin-microphysical schemes used here calculate  
137 saturation explicitly, by solving the diffusion growth equation, enabling super- and sub-  
138 saturation values in cloudy pixels. This is in contrary to many other works that used  
139 bulk-microphysical schemes which rely on saturation adjustment to 100% within the  
140 cloud (Khain et al., 2015). This difference may produce significant differences on the  
141 evolution of clouds and their cores. Specifically, we aim to answer questions such as:

- 142 • Which core type is largest? Which is smallest?
- 143 • How do the cores change during the lifetime of a cloud?
- 144 • Can different core types be used interchangeably without much effect on  
145 analysis results?
- 146 • Are the cores centered at the cloud's geometrical center, as expected from the  
147 core-shell model?

148 The differences between the cores' evolution in time shed new light on the competition  
149 of processes within a cloud in time and space. Moreover, such an understanding can  
150 serve as a guideline to all studies that perform the partition to cloud core and margin,  
151 and assist in determining the relevance of a given partition.

152

## 153 **2. Methods**

### 154 **2.1. Single cloud model**

155 For single cloud simulations we use the Tel-Aviv University axisymmetric, non-  
156 hydrostatic, warm convective single cloud model (TAU-CM). It includes a detailed  
157 (explicit) treatment of warm cloud microphysical processes solved by the multi-  
158 moment bin method (Feingold et al., 1988, 1991; Tzivion et al., 1989, 1994). The warm  
159 microphysical processes included in the model are nucleation, diffusion (i.e.  
160 condensation and evaporation), collisional coalescence, breakup and sedimentation (for  
161 a more detailed description, see (Reisin et al., 1996)).

162 Convection was initiated using a thermal perturbation near the surface. A time step of  
163 1 sec is chosen for dynamical computations, and 0.5 sec for the microphysical  
164 computations (e.g. condensation-evaporation). The total simulation time is 80 min.  
165 There are no radiation processes in the model. The domain size is 5x6 km, with an  
166 isotropic 50 m resolution. The model is initialized using a Hawaiian thermodynamic  
167 profile, based on the 91285 PHTO Hilo radiosonde at 00Z, 21 Aug, 2007. A typical  
168 oceanic size distribution of aerosols is chosen (Altaratz et al., 2008; Jaenicke, 1988),  
169 with a total concentration of  $500 \text{ cm}^{-3}$ . This concentration produced clouds that are non-  
170 to weakly- precipitating. In Part II additional aerosol concentrations are considered,  
171 including ones which produce heavy precipitation.

172

## 173 **2.2. Cloud field model**

174 Warm cumulus cloud fields are simulated using the System for Atmospheric Modeling  
175 (SAM) Model (version 6.10.3, for details see webpage:  
176 <http://rossby.msrc.sunysb.edu/~marat/SAM.html>) (Khairoutdinov and Randall, 2003)).  
177 SAM is a non-hydrostatic, anelastic model. Cyclic horizontal boundary conditions are  
178 used together with damping of gravity waves and maintaining temperature and moisture  
179 gradients at the model top. An explicit Spectral Bin Microphysics (SBM) scheme  
180 (Khain et al., 2004) is used. The scheme solves the same warm microphysical processes  
181 as in the TAU-CM single cloud model, and uses an identical aerosol size distribution  
182 and concentration (i.e.  $500 \text{ cm}^{-3}$ ) for the droplet activation process.

183 We use the BOMEX case study as our benchmark for shallow warm cumulus fields.  
184 This case simulates a trade-wind cumulus (TCu) cloud field based on observations  
185 made near Barbados during June 1969 (Holland and Rasmusson, 1973). This case study  
186 has a well-established initialization setup (sounding, surface fluxes, and surface  
187 roughness) and large scale forcing setup (Siebesma et al., 2003). It has been thoroughly  
188 tested in many previous studies (Grabowski and Jarecka, 2015; Heus et al., 2009b; Jiang  
189 and Feingold, 2006; Xue and Feingold, 2006). To check the robustness of the cloud  
190 field results, two additional case studies are simulated: (1) The same Hawaiian profile  
191 used to initiate the single cloud model, and (2) a continental shallow cumulus  
192 convection cases study (named CASS), based on long term observations taken at the  
193 ARM Southern Great Plains (SGP) site (Zhang et al., 2017).

194 The soundings, large scale forcing, and surface properties used to initialize the model  
195 are detailed in previous works (Heiblum et al., 2016a; Siebesma et al., 2003; Zhang et  
196 al., 2017). The domain size is 12.8 km x 12.8 km x 4 km for BOMEX, 12.8 km x 12.8  
197 km x 5 km for Hawaii, and 25.6 km x 25.6 km x 16 km for CASS. The grid size is set  
198 to 100 m in the horizontal direction and 40 m in the vertical direction for all simulations.  
199 For CASS, above a height of 5 km the vertical grid size gradually increases to 1km.  
200 The time step for computation is 1 s for all simulations, with a total runtime of 8 hours  
201 for BOMEX and Hawaii, and 12 hours for CASS. The initial temperature perturbations  
202 (randomly chosen within  $\pm 0.1^\circ\text{C}$ ) are applied near the surface, during the first time  
203 step.

204

### 205 **2.3. Physical and Geometrical Core definitions**

206 A cloudy pixel is defined here as a grid-box with liquid water amount that exceeds 0.01  
207  $\text{g kg}^{-1}$ . The physical core of the cloud is defined using three different definitions: 1)  
208  $RH_{core}$ : all grid boxes for which the relative humidity (RH) exceeds 100%, 2)  $B_{core}$ :  
209 buoyancy (see definition in Eq. (1)) above zero. The buoyancy is determined in each  
210 time step by comparing each cloudy pixel with the mean thermodynamic conditions for  
211 all non-cloudy pixels per vertical height, and 3)  $W_{core}$ : vertical velocity above zero.  
212 These definitions apply for both the single cloud and cloud field model simulations  
213 used here. We note that setting the core thresholds to positive values ( $>0$ ) may increase  
214 the amount of non-convective pixels which are classified as part of a physical core,  
215 especially for the  $W_{core}$ . Indeed, taking higher thresholds for the updrafts decreases the  
216  $W_{core}$  extent and reduces the variance. Nevertheless, any threshold taken is subjective  
217 in nature, while the positive vertical velocity definition is process based and objective.

218 The centroid (i.e. mean location in each of the axes) is used here to represent the  
219 geometrical location of the total cloud (i.e. cloud geometrical core) and its specific  
220 physical cores. The distances between the total cloud and its cores' centroids ( $D_{norm}$ ),  
221 as presented here, are normalized to cloud size to reflect the relative distance between  
222 the two centroids, where  $D_{norm} = 0$  indicates coincident physical and geometrical  
223 cores and  $D_{norm} = 1$  indicates a physical core located at the cloud boundary. The  
224 single cloud simulations rely on an axisymmetric model and thus all centroids are



225 horizontally located on the center axis while vertical deviations are permitted. For this  
226 model the distance is normalized by half the cloud's thickness. For the cloud field  
227 simulations both horizontal and vertical deviations are possible, therefore distances are  
228 normalized by the cloud's volume radius.

229

#### 230 **2.4. Center of gravity vs. Mass (CvM) phase space**

231 Recent studies (Heiblum et al., 2016a, 2016b) suggested the Center-of-Gravity vs. Mass  
232 (CvM) phase space as a useful approach to reduce the high dimensionality and to study  
233 results of large statistics of clouds during different stages of their lifetimes (such as seen  
234 in cloud fields). In this space, the Center-of-Gravity (COG) height and mass of each  
235 cloud in the field at each output time step (taken here to be 1 min) are collected and  
236 projected in the CvM phase space. This enables a compact view of all clouds in the  
237 simulation during all stages of their lifetimes, with the main disadvantage being the loss  
238 of grid-size resolution information on in-cloud dynamical processes. Although the  
239 scatter of clouds in the CvM is sensitive to the microphysical and thermodynamic  
240 settings of the cloud field, it was shown that the different subspaces in the CvM space  
241 correspond to different cloud processes and stages (Heiblum et al., 2016a, 2016b). The  
242 lifetime of a cloud can be described by a trajectory on this phase space.

243 A schematic illustration of the CvM space is shown in Fig. 1. Most clouds are confined  
244 between the adiabat (curved dashed line) and the inversion layer base (horizontal  
245 dashed line). The adiabat curve corresponds to the theoretical evolution of a moist  
246 adiabat 1D cloud column in the CvM space. The large majority of clouds form within  
247 the growing branch (yellow shade) at the bottom left part of the space, adjacent to the  
248 adiabat. Clouds then follow the growing trajectory (grow in both COG and mass) to  
249 some maximal values. The growing branch deviates from the adiabat at large masses  
250 depending on the degree of sub-adiabaticity of the cloud field. After or during the  
251 growth stage of clouds, they may undergo the following processes: i) dissipate via a  
252 reverse trajectory along the growing one, ii) dissipate via a gradual dissipation  
253 trajectory (magenta shade), iii) shed off small mass cloud fragments (red shades), iv) in  
254 the case of precipitating clouds, they can shed off cloud fragments in the sub-cloudy  
255 layer (grey shade). The former two processes form continuous trajectories in the CvM  
256 space, while the latter two processes create disconnected subspaces.

## 257 **2.5. Cloud tracking**

258 To follow the evolution of individual clouds within a cloud field we use an automated  
259 3D cloud tracking algorithm (see (Heiblum et al., 2016a) for details). It enables tracking  
260 of Continuous Cloud Entities (CCEs) from formation to dissipation, even if interactions  
261 between clouds (splitting or merging) occur during that lifetime. A CCE initiates as a  
262 new cloud forming in the field, and is tracked on the condition that it retains the majority  
263 (>50%) of its mass during an interaction event if occurs. Thus, a CCE can terminate  
264 due to either cloud dissipation or cloud interactions.

265

## 266 **3. Theoretical estimations for different core sizes**

267 Here we propose simple physical considerations to evaluate the differences in cloud  
268 partition to core and margin using different definitions. The arguments rely on key  
269 findings from previous works (see Sect. 1) with aim to gain intuitive understanding of  
270 the potential differences between the core types. It is convenient to separate the analysis  
271 to an adiabatic case, and then add another layer of complexity and consider the effects  
272 of mixing of cloudy and non-cloudy air. In this theoretical derivation saturation  
273 adjustment to RH=100% is assumed for both cases, while in the other models used in  
274 this study, transient super- and sub-saturated cloudy parcels are treated (more realistic).

275

### 276 **3.1. Adiabatic case – no mixing**

277 Considering moist-adiabatic ascent, the excess vapor above saturation is  
278 instantaneously converted to liquid (saturation adjustment). Thus, the adiabatic cloud  
279 is saturated ( $S=1$ ) throughout its vertical profile, and only  $W_{core}$  and  $B_{core}$  differences  
280 can be considered. It is assumed that the adiabatic convective cloud is initiated by  
281 positive buoyancy initiating from the sub-cloudy layer. As long as the cloud is growing  
282 it should have positive CAPE and will experience positive  $w$  throughout the column  
283 even if the local buoyancy at specific height is negative. Eventually the cloud must  
284 decelerate due to negative buoyancy and reach a top height, where  $CAPE = 0$  and  $w =$   
285  $0$ . Hence, for the adiabatic column case,  $B_{core}$  is always a proper subset of  $W_{core}$   
286 ( $B_{core} \subset W_{core}$ ). These effects are commonly seen in warm convective cloud fields

287 where permanent vertical layers of negative buoyancy (but with updrafts) within clouds  
288 typically exist at the bottom and top regions of the cloudy layer (de Roode and  
289 Bretherton, 2003; Betts, 1973; Garstang and Betts, 1974; Grant and Lock, 2004; Heus  
290 et al., 2009b; Neggers et al., 2007).

291

### 292 **3.2. Cloud parcel entrainment model**

293 A mixing model between a saturated (cloudy) parcel and a dry (environment) parcel is  
294 used to illustrate the effects of mixing on the different core types. The details of these  
295 theoretical calculations are shown in Appendix A. The initial cloudy parcel is assumed  
296 to be saturated (part of  $RH_{core}$ ), have positive vertical velocity (part of  $W_{core}$ ), and  
297 experience either positive or negative buoyancy (part of  $B_{core}$  or  $B_{margin}$ ), as is seen  
298 for the adiabatic column case. Additionally, mixing is assumed to be isobaric, and in a  
299 steady environment where the average temperature of the environment per a given  
300 height does not change. The resultant mixed parcel will have lower humidity content  
301 and lower LWC as compared to the initial cloudy parcel, and a new temperature. In  
302 nearly all cases (beside in an extremely humid environment) the mixed parcel will be  
303 sub-saturated and evaporation of LWC will occur. Evaporation ceases when  
304 equilibrium is reached due to air saturation ( $S=1$ ) or due to complete evaporation of the  
305 droplets (which means  $S<1$ , and the mixed parcel is no longer cloudy since it has no  
306 liquid water content).

307 In addition to mixing between cloudy (core or margin) and non-cloudy parcels, mixing  
308 between core and margin parcels (within the cloud) also occurs. This mixing process  
309 can be considered as “entrainment-like” with respect to the cloud core. Considering the  
310 changes in the  $W_{core}$  and  $RH_{core}$ , there is no fundamental difference in the treatment of  
311 mixing of cloudy and non-cloudy parcels, or mixing between core and margin (because  
312 the margins and the environment are typically sub-saturated and experience negative  
313 vertical velocity). However, for the changes in the  $B_{core}$  after mixing, there exists a  
314 fundamental difference between mixing *with* the reference temperature/humidity state  
315 (in the case of mixing with the environment) and mixing *given* a reference  
316 temperature/humidity state (in mixing between  $B_{core}$  and  $B_{margin}$ ). Thus, it is  
317 interesting to check the effects of mixing between  $B_{core}$  and  $B_{margin}$  parcels on the

318 total extent of the  $B_{core}$  with respect to the other two core types. The details of this  
319 second case are shown in Appendix B.

320

### 321 **3.2.1. Effects of non-cloudy entrainment on buoyancy**

322 When mixed with non-cloudy air, the change in buoyancy of the initial cloudy parcel  
323 (which is a part of  $W_{core}$  and  $RH_{core}$  and either  $B_{core}$  or  $B_{margin}$ ) happens due to both  
324 mixing and evaporation processes. The theoretical calculations show that for all  
325 relevant temperatures ( $\sim 0^{\circ}\text{C}$  to  $30^{\circ}\text{C}$ , representing warm Cu), the change in the parcel's  
326 buoyancy due to evaporation alone will always be negative (see appendix A). It is  
327 because the negative effect of the temperature decrease outweighs the positive effects  
328 of the humidity increase and water loading decrease. Nevertheless, the total change in  
329 the buoyancy (due to both mixing and evaporation) depends on the initial temperature,  
330 relative humidity, and liquid water content of the cloudy and non-cloudy parcels.

331 In Fig. A1 a wide range of non-cloudy environmental parcels, each with their own  
332 thermodynamic conditions, are mixed with a saturated cloud parcel with either positive  
333 or negative buoyancy. The main conclusions regarding the effects of such mixing on  
334 the buoyancy are as follows:

- 335 i. To a first order, the initial buoyancy values are temperature dependent,  
336 where a cloudy parcel that is warmer (colder) by more than  $\sim 0.2^{\circ}\text{C}$  than  
337 the environment will be positively (negatively) buoyant for common  
338 values of cloudy layer environment relative humidity ( $\text{RH} > 80\%$ ).
- 339 ii. Parcels that are initially part of  $B_{core}$  may only lower their buoyancy  
340 due to entrainment, either to positive or negative values depending on  
341 the environmental conditions.
- 342 iii. The lower the environmental RH, the larger the probability for parcel  
343 transition from  $B_{core}$  to  $B_{margin}$  after entrainment.
- 344 iv. Parcels that are initially part of  $B_{margin}$  can either increase or decrease  
345 their buoyancy value, but never become positively buoyant. The former

346 case (buoyancy decrease) is expected be more prevalent since it occurs  
347 for the smaller range of temperature differences with the environment.

348 In summary, entrainment is expected to always have a net negative effect on  $B_{core}$   
349 extent and  $B_{margin}$  values, while evaporation feedbacks serve to maintain  $RH_{core}$  in  
350 the cloud. Thus, we can predict that  $B_{core}$  should be a subset of  $RH_{core}$  (i.e.  $B_{core} \subseteq$   
351  $RH_{core}$ ).

352

### 353 3.2.2. Effects of core and margin mixing on buoyancy

354 We consider the case of mixing between the  $B_{core}$  and  $B_{margin}$ , meaning positively  
355 buoyant and negatively buoyant cloud parcels. For simplicity, we assume both parcels  
356 are saturated ( $S=1$ , both included in the  $RH_{core}$ ). As seen above, such conditions exist  
357 in both the adiabatic case and in the case where an adiabatic cloud has undergone some  
358 entrainment with the environment. The buoyancy differences between the saturated  
359 parcels are mainly due to temperature differences, but also due to the increasing  
360 saturation vapor pressure with increasing temperature (see Appendix B for details).

361 In Fig. B1 is it shown that the resultant mixed parcel's buoyancy can be either positive  
362 or negative, depending on the magnitude of temperature difference of each parcel (core  
363 or margin) from that of the environment. However, in all cases the mixed parcel is  
364 supersaturated. This result can be generalized: given two parcels with equal RH but  
365 different temperature, the RH of the mixed parcel is always equal or higher than the  
366 initial value. Hence,  $B_{core}$  can either increase or decrease in extent, while the  $RH_{core}$   
367 can only increase due to mixing between saturated  $B_{core}$  and  $B_{margin}$  parcels. This  
368 again strengthens the assumption that  $B_{core}$  should be a subset of  $RH_{core}$ .

369 We note that an alternative option for mixing between the core and margin parcels that  
370 exist here, where either or both of the parcels are subsaturated so that the mixed parcel  
371 is subsaturated as well. In this case evaporation will also occur. As seen in Appendix  
372 A, this should further reduce the buoyancy value of the mixed parcel (while increasing  
373 the RH).

374

### 375 3.2.3. Effects of entrainment on vertical velocity

376 The vertical velocity equation dictates that buoyancy is the main production term (de  
377 Roode et al., 2012; Romps and Charn, 2015), and is balanced by perturbation pressure  
378 gradients and mixing (on grid and sub-grid scales). Thus, all changes of magnitude (and  
379 sign) in vertical velocity should lag the changes in buoyancy. This is the basis of  
380 convective overshooting and cumulus formation in the transition layer (see Sect. 3.1).  
381 It is interesting to assess the magnitude of this effect by quantifying the expected time  
382 lag between buoyancy and vertical velocity changes. The calculations in Appendix A  
383 indicates negative buoyancy values reaching  $-0.1 \text{ m/s}^2$  due to entrainment. However,  
384 measurements from within clouds show that the temperature deficiency of cloudy  
385 parcels with respect to the environment is generally restricted to less than  $1^\circ\text{C}$  for  
386 cumulus clouds (Burnet and Brenguier, 2010; Malkus, 1957; Sinkevich and Lawson,  
387 2005; Wei et al., 1998), and thus the negative buoyancy should be no more larger than  
388  $-0.05 \text{ m/s}^2$ . This value is closer to current and previous simulations and also  
389 observations that show negative buoyancy values within clouds to be confined between  
390  $-0.001$  and  $-0.01 \text{ m/s}^2$  (de Roode et al., 2012; Ackerman, 1956).

391 Given an initial vertical velocity of  $\sim 0.5 \text{ m/s}$ , the deceleration due to buoyancy (and  
392 reversal to negative vertical velocity) should occur within a typical time range of 1 - 10  
393 minutes. These timescales are much longer than the typical timescales of entrainment  
394 (mixing and evaporation that eliminate the  $B_{core}$ ) which range between 1 – 10 s  
395 (Lehmann et al., 2009). Moreover, the fact that a drag force typically balances the  
396 buoyancy acceleration (Romps and Charn, 2015) can also contribute to a time lag  
397 between effects on buoyancy and subsequent effects on vertical velocity. Therefore, the  
398 switching of sign for vertical velocity should occur with substantial delay compared to  
399 the reduction of buoyancy, and  $B_{core}$  should be a subset of  $W_{core}$  (i.e.  $B_{core} \subseteq W_{core}$ )  
400 during the growing and mature stages of a cloud's lifetime.

401

### 402 3.3. The relation between supersaturation and vertical velocity cores

403 Here we revisit the terms in Eq. 3. A rising parcel initially has no liquid water content,  
404 with its only source of supersaturation being the updraft  $w$ , and thus initially the  $RH_{core}$   
405 should always be a subset of  $W_{core}$ . In general, since the sink term  $\frac{dLWC}{dt}$  becomes a

406 source only when  $S < 1$  (the condition for evaporation), the only way for a convective  
407 cloud to produce supersaturation (i.e.  $S > 1$ ) is by updrafts during all stages of its lifetime.  
408 Once supersaturation is achieved, the sink term becomes positive  $\frac{dLWC}{dt} > 0$  and  
409 balances the updraft source term, so that supersaturation either increases or decreases.  
410 At any stage, if downdrafts replace the updrafts within a supersaturated parcel, the  
411 consequent change in supersaturation becomes strictly negative (i.e.  $\frac{dS}{dt} < 0$ ). This  
412 negative feedback limits the possibility to find supersaturated cloudy parcels with  
413 downdrafts. Hence, we can expect the  $RH_{core}$  to be smaller than  $W_{core}$  during the  
414 majority of a cloud's lifetime.

415

#### 416 **4. Results - Single cloud simulation**

417 The differences between the three types of core definitions are examined during the  
418 lifetime of a single cloud (Fig. 2), based on the Hawaiian profile. The cloud's total  
419 lifetime is 36 minutes (between  $t=7$  and  $t=43$  min of simulation). Each panel in Fig. 2  
420 presents vertical cross-sections of the three cores (magenta -  $W_{core}$ , green -  $RH_{core}$ , and  
421 yellow -  $B_{core}$ ) at four points in time (with 10-minute intervals). The cloud has an initial  
422 cloud base at 850m, and grows to a maximal top height of 2050 m. The condensation  
423 rates (red shades) increase toward the cloud center and the evaporation rates (blue  
424 shades) increase toward the cloud edges. Evaporation at the cloud top results in a large  
425 eddy below it that contributes to mixing and evaporation at the lateral boundaries of the  
426 cloud. Thus, a positive feedback is initiated which leads to cooling, negative buoyancy,  
427 and downdrafts. The dissipation of the cloud is accompanied with a rising cloud base  
428 and lowering of the cloud top.

429 During the growing stage ( $t=10, 20$  min), when substantial condensation still occurs  
430 within the cloud, all of the cores seem to be self-contained within one another, with  
431  $B_{core}$  being the smallest and  $W_{core}$  being the largest. During the final dissipation stages,  
432 when the cloud shows only evaporation ( $t=40$ ),  $W_{core}$  and  $RH_{core}$  disappear while there  
433 is still a small  $B_{core}$  near the cloud top. Further analysis (see Part II) shows that the  
434 entire dissipating cloud is colder and more humid than the environment but downdrafts  
435 from the cloud top (see arrows in Fig. 2) promote adiabatic heating, and by that increase  
436 the buoyancy in dissipating cloudy pixels, sometimes reaching positive values. These

437 buoyant pockets will be discussed further in Part II. The results indicate that the three  
438 types of physical cores of the cloud are not located around the cloud's geometrical core  
439 along the whole cloud lifetime. During cloud growth (i.e. (increase in mass and size)  
440 the three types of cores surround the cloud's center, while during late dissipation the  
441  $B_{core}$  is at offset from the cloud center.

442 For a more complete view of the evolution of the three core types in the single cloud  
443 case, time series of core fractions are shown in Fig. 3. Panels a and b show the core  
444 mass (core mass / total mass -  $f_{mass}$ ) and volume (core volume / total volume -  $f_{vol}$ )  
445 fractions out of the cloud's totals. The results are similar for both measures except for  
446 the fact that core mass fractions are larger than core volume fractions. This is due to  
447 significantly higher LWC per pixel in the cores compared to the margins, which skews  
448 the core mass fraction to higher values. Core mass fractions during the main cloud  
449 growing stage (between  $t=7$  and  $t=27$  min simulation time) are around 0.7 - 0.85 and  
450 core volume fractions are around 0.5 - 0.7. The time series show that as opposed to the  
451  $W_{core}$  and  $RH_{core}$  fractions which decrease monotonically with time,  $B_{core}$  shows a  
452 slight increase during stages of cloud growth. In addition, for most of the cloud's  
453 lifetime the  $B_{core}$  fractions are the smallest and the  $W_{core}$  fractions are the largest,  
454 except for the final stage of the clouds dissipation where downdrafts from the cloud top  
455 creates pockets of positive buoyancy. These pockets are located at the cloud's peripheral  
456 regions rather than near the cloud's geometrical center as is typically expected for the  
457 cloud's core. In the cloud's center (the geometrical core) the  $B_{core}$  is the first one to  
458 terminate (at  $t=32$  min) compared to both  $W_{core}$  and  $RH_{core}$  that decay together (at 36  
459 min).

460 For describing the locations of the physical cores, we examine the normalized distances  
461 ( $D_{norm}$ ) between the cloud's centroid and the cores' centroids. The evolution of these  
462 distances is shown in Fig. 3c. At cloud initiation ( $t=7$  min), when the cloud is very  
463 small, all cores' centroids coincide with the total cloud centroid location. The  $B_{core}$   
464 (and  $RH_{core}$  to a much lesser degree) centroid then deviates from the cloud centroid to  
465 a normalized distance of 0.27 ( $t=8$  min). As cloud growth proceeds,  $B_{core}$  grows and  
466 its centroid coincides with the cloud's centroid. All cores' centroids are located near the  
467 cloud centroid during the majority of the growing and mature stages of the cloud,  
468 showing normalized distances  $<0.1$ . During dissipation ( $t>27$  min), the cores' centroid



469 locations start to distance away from the cloud's geometrical core followed by a  
470 reduction in distances due to the rapid loss of cloud volume. As mentioned above, it is  
471 shown that the regeneration of positive buoyancy at the end of cloud dissipation (t=40  
472 min) takes place at the cloud edges, with normalized distance  $>0.5$ .

473 Finally, in Fig. 3d the fraction of pixels of each core contained within another core is  
474 shown. It can be seen that for the majority of cloud lifetime (up to t=33 min)  $B_{core}$  is  
475 subset (pixel fraction of 1) of  $RH_{core}$ , and the latter is a subset of  $W_{core}$ . As expected,  
476 the other three permutations of pixel fractions (e.g.  $W_{core}$  in  $B_{core}$ ) show much lower  
477 values. The cloudy regions that are not included within  $B_{core}$  but are included within  
478 the two other cores are exclusively at the cloud's boundaries (see Fig. 2). The same  
479 pattern is seen for cloudy regions that are included within  $W_{core}$  but not in  $RH_{core}$ .  
480 During the dissipation stage of the cloud its core subset property (i.e.  $B_{core} \subseteq RH_{core} \subseteq$   
481  $W_{core}$ ) breaks down. Similar temporal evolutions as shown here are seen for the other  
482 simulated clouds (with various aerosol concentrations) in part II of this work.

483

## 484 **5. Results - Cloud field simulations**

### 485 **5.1. Partition to different core types**

486 To test the robustness of the observed behaviors seen for a single cloud, it is necessary  
487 to check whether they also apply to large statistics of clouds in a cloud field. The  
488 BOMEX simulation is taken for the analyses here. We discard the first 3 hours of cloud  
489 field data, during which the field spins-up and its mean properties are unstable. In Fig.  
490 4 the volume ( $f_{vol}$ ) and mass ( $f_{mass}$ ) fractions of the three core types are compared for  
491 all clouds (at all output times – every 1 min) in the CvM space. As seen in Fig. 1, the  
492 location of specific clouds in the CvM space indicates their stage in evolution. Most  
493 clouds are confined to the region between the adiabat and the inversion layer base  
494 except for small precipitating (lower left region) and dissipating clouds (upper left  
495 region). The color shades of the clouds indicate whether a cloud is mostly core (red),  
496 mostly margin (blue), or equally divided to core and margin (white).

497 As seen for the single cloud, the core mass fractions tend to be larger than core volume  
498 fractions, for all core types. This is due to the fact that LWC values in the cloud core  
499 regions are higher than in margin regions, so that a cloud might be core dominated in

500 terms of mass while being margin dominated in terms of volume. Focusing on the  
501 differences between core types, the color patterns in the CvM space imply that  $B_{core}$   
502 definition yields the lowest core fractions (for both mass and volume), followed by  
503  $RH_{core}$  with higher values and  $W_{core}$  with the highest values. The absence of the  $B_{core}$   
504 is especially noticeable for small clouds in their initial growth stages after formation  
505 (COG  $\sim 550$  m and LWP  $< 1$  g m<sup>-2</sup>). Those same clouds show the highest core fractions  
506 for the other two core definitions. This large difference can be explained by the  
507 existence of the transition layer (as discussed in Sect. 3) near the lifting condensation  
508 level (LCL) in warm convective cloud fields which is the approximated height of a  
509 convective cloud base (Craven et al., 2002; Meerkötter and Bugliaro, 2009). Within  
510 this layer parcels rising from the sub-cloudy layer are generally colder than parcels  
511 subsiding from the cloudy layer. Thus, this transition layer clearly marks the lower edge  
512 of the buoyancy core as most convective clouds are initially negatively buoyant.

513 Generally, the growing cloud branch (i.e. the CvM region closest to the adiabat) shows  
514 the highest core fractions. The  $RH_{core}$  and  $W_{core}$  fractions decrease with cloud growth  
515 (increase in mass and COG height) while the  $B_{core}$  initially increases, shows the highest  
516 fraction values around the middle region of the growing branch and then decreases for  
517 the largest clouds. The transition from the growing branch to the dissipation branch is  
518 manifested by a transition from core dominated to margin dominated clouds (i.e.  
519 transition from red to blue shades). Mixed within the margin dominated dissipating  
520 cloud branch, a scatter of  $W_{core}$  dominated small clouds can be seen as well. These  
521 represent cloud fragments which shed off large clouds during their growing stages with  
522 positive vertical velocity. They are sometimes  $RH_{core}$  dominated as well but are strictly  
523 negatively buoyant. The few precipitating cloud fragments seen for this simulation  
524 (cloud scatter located below the adiabat) tend to be margin dominated, especially for the  
525  $RH_{core}$ .

526

## 527 **5.2. Subset properties of cores**

528 From Fig. 4 it is clear that  $W_{core}$  tends to be the largest and  $B_{core}$  tends to be the  
529 smallest. To what degree however, are the cores subsets of one another as was seen for  
530 the single cloud simulation? It is also interesting to check whether the different physical

531 cores are centered near the cloud's geometrical core. In Fig. 5 the pixel fraction ( $f_{pixel}$ )  
 532 of each core type within another core type is shown for all clouds in the CvM space. A  
 533  $f_{pixel}$  of 1 (bright colors) indicates that the pixels of the specific core in question  
 534 (labeled in each panel title) are a subset of the other core (also labeled in the panel title)  
 535 and a  $f_{pixel}$  of 0 (dark colors) indicates no intersection between the two cores in the  
 536 cloud. It is seen that  $B_{core}$  tends to be a subset of both other cores, with  $f_{pixel}$  around  
 537 0.75-1 for most of the growing branch area and large mass dissipating clouds which  
 538 still have some positive buoyancy. The pixel fractions are higher for  $B_{core}$  inside  $W_{core}$   
 539 compared with  $B_{core}$  inside  $RH_{core}$ , but both show decrease with increase in growing  
 540 branch cloud mass, meaning the chance for finding a proper subset  $B_{core}$  decreases in  
 541 large clouds.

542 The CvM space of  $RH_{core}$  inside  $W_{core}$  shows an even stronger relation between these  
 543 two core types. For almost all growing branch clouds, the  $RH_{core}$  is a subset of  $W_{core}$   
 544 (i.e.  $RH_{core} \subseteq W_{core}$ ). The decrease gradually with loss of cloud mass in the dissipation  
 545 branch. The other three permutations of  $f_{pixel}$  ( $W_{core}$  inside  $B_{core}$ ,  $W_{core}$   
 546 inside  $RH_{core}$ , and  $RH_{core}$  inside  $B_{core}$ ) give an indication of cores sizes and of which  
 547 cloud types show no overlap between different cores. As stated above, growing  
 548 (dissipation) clouds show higher (lower) overlap between the different core types. The  
 549  $W_{core}$  is almost twice as large as the  $B_{core}$  and 30% - 40% larger than the  $RH_{core}$  along  
 550 most of the growing branch. In conclusion, we see a strong tendency for the subset  
 551 property of cores ( $B_{core} \subseteq RH_{core} \subseteq W_{core}$ ) during the growth stages of clouds. This  
 552 property ceases for dissipating and precipitating clouds, especially for the smaller  
 553 clouds which show less overlap between core types.

554 In Fig. 6 the normalized distances ( $D_{norm}$ ) between the total cloud centroid and each  
 555 specific physical core centroid locations are evaluated. Along the growing branch the  
 556 cloud centroid and physical cores' centroids tend to be of close proximity, while during  
 557 cloud dissipation the cores' centroids tend to increase in distance from the cloud's  
 558 center. This type of evolution is most prominent for the  $W_{core}$ , which shows a clear  
 559 gradient of transition from small (dark colors) to large (bright colors) distances. The  
 560  $B_{core}$  shows a more complex transition, from intermediate distance values ( $\sim 0.5$ ) at  
 561 cloud formation, to near zeros values along the mature part of the growing branch, back  
 562 to large values in the dissipation branch. Along the growing branch  $RH_{core}$  shows

563 distances comparable to the  $W_{core}$  (except for large distances at cloud formation).  
564 However, compared to the other two core types,  $RH_{core}$  shows the smallest distances  
565 to the geometrical core during cloud dissipation. This is manifested by a relative  
566 absence of bright colors for dissipating clouds in Fig. 6.

567 The prevalence of cloud edge  $B_{core}$  pixels during dissipation can be explained by  
568 adiabatic heating due to weak downdrafts (see Sect. 4.2, Part II) which are expected at  
569 the cloud periphery. The fact that there is little overlap between  $B_{core}$  and both  $W_{core}$   
570 and  $RH_{core}$  pixels in dissipating clouds (see Fig. 5) serves to verify this assumption.  
571 The relative absence of isolated  $RH_{core}$  pixels at the cloud edges can be explained by  
572 the fact the pixels closest to the cloud's edge are most susceptible to mixing with non-  
573 cloudy air and evaporation, yielding subsaturation conditions. The innermost pixels are  
574 "protected" from such mixing and thus we can expect most  $RH_{core}$  pixels to be located  
575 near the geometrical core.

576 The  $W_{core}$  case is less intuitive. During cloud dissipation complex patterns of updrafts  
577 and downdrafts within the cloud can create scenarios where the  $W_{core}$  centroid is  
578 located anywhere in the cloud. However, the results show that most small dissipating  
579 clouds tend to have their  $W_{core}$  pixels concentrated at the cloud edges. Comparing Fig.  
580 6 with Figs. 4 and 5, we can see that these pixels comprise only a tiny fraction of the  
581 already small clouds and do not overlap with  $RH_{core}$  and  $B_{core}$  pixels and thus are not  
582 related to significant convection processes. Further analysis shows that the maximum  
583 updrafts in these clouds rarely exceed 0.5 m/s (i.e. 90% of clouds with normalized  
584 distance  $> 0.9$  have a maximum updraft of less than 0.5 m/s), and can thus be considered  
585 with near neutral vertical velocity.

586

### 587 **5.3. Consistency of the cloud partition to core types**

588 The results for cloud fields are summarized in Fig. 7 that presents the evolution of core  
589 fractions of continuous cloud entities (CCEs, see Sect. 2.5 for details) from formation  
590 to dissipation. Only CCEs that undergo a complete life cycle are averaged here. These  
591 CCEs fulfill the following four conditions: i) form near the LCL, ii) live for at least 10  
592 minutes, ii) reach maximum cloud mean LWP values above  $10 \text{ g m}^{-2}$ , and iv) terminate  
593 with mass value below  $10 \text{ g m}^{-2}$ . As a test of generality, we performed this analysis for

594 Hawaiian and CASS warm cumulus cloud field simulations in addition to the BOMEX  
595 one. For each simulation, hundreds of CCEs are collected (see panel titles) and their  
596 core volume fractions are averaged according to their normalized lifetimes ( $\tau$ ).

597 Consistent results are seen for all three simulations. Clouds initiate with a  $W_{core}$   
598 fraction of  $\sim 1$ ,  $RH_{core}$  fraction of  $\sim 0.8$ , and  $B_{core}$  fraction of  $\sim 0 - 0.1$ . The former two  
599 core types' volume fraction decreases monotonically with lifetime, while the latter core  
600 type's volume fraction increases up to 0.15 - 0.35 at  $\tau \sim 0.25$ , and then monotonically  
601 decreases for increasing  $\tau$ . The continental (CASS) simulation consistently shows lower  
602 buoyancy volume fractions than the oceanic simulations. This can be attributed to lower  
603 RH in the CASS cloudy layer (60% - 80%) compared with the oceanic simulations  
604 (85% - 95%). The lower RH increases entrainment and reduces buoyancy. The fact that  
605 clouds end their life cycle with non-zero volume fractions may indicate that some of  
606 the CCE terminate not because of full dissipation but rather because of significant  
607 splitting or merging events.

608 Normalized distances ( $D_{norm}$ ) between core centroid and total cloud centroid (Fig. 7,  
609 middle column) tend to monotonically increase for  $RH_{core}$  and  $W_{core}$  with CCE  
610 lifetime for all simulations. The gradient of increase is larger at the later stages of CCE  
611 lifetime. Initially the  $W_{core}$  is closer to the geometrical core but at later stages of CCE  
612 lifetime (typically  $\tau > 0.5$ ) this switches and  $RH_{core}$  remains the closest. As seen above,  
613 for the first (second) half of CCE lifetime, the distance between  $B_{core}$  centroid and  
614 cloud centroid decreases (increases), starting at normalized distances above 0.4 for all  
615 simulations. The physical cores stay closer to the geometrical core ( $D_{norm} < 0.5$ ) for  
616 the majority of their lifetimes for the three cases. However, the assumption that a  
617 cloud's core (by any definition) is also indicative of the cloud's centroid only applies  
618 to a fraction of that lifetime. Taking the value  $D_{norm} = 0.25$  as a threshold for physical  
619 cores centered near the cloud centroid, Bomex, Hawaii, and CASS simulation CCEs'  
620  $W_{core}$  cross this threshold at  $\tau = 0.8, 0.6, \text{ and } 0.65$ , respectively. Thus, the core-shell  
621 geometrical model is mostly true for the first two-thirds of a typical cloud's lifetime.

622 The analysis of core subset properties (Fig. 7, right column) shows that the assumption  
623  $B_{core} \subseteq RH_{core} \subseteq W_{core}$  is true for the initial formation stages of a cloud. Although the  
624 corresponding pixel fractions decrease slightly during the lifetime of the CCE, they  
625 remain above 0.9 (e.g.  $B_{core}$  is 90% contained within  $RH_{core}$ ). A sharp decrease in

626 pixel fractions is seen for  $\tau > 0.8$  ( $\tau > 0.5$  for the CASS simulation), as the overlaps  
627 between the different cores is reduced during dissipation stages of the cloud. For all  
628 simulations, the highest pixel fraction values are seen for the  $B_{core}$  inside  $W_{core}$  pair,  
629 followed by  $RH_{core}$  inside  $W_{core}$  pair, and  $B_{core}$  inside  $RH_{core}$  pair showing lower  
630 values. In addition, it can be seen that the variance of average pixel fraction (per  $\tau$ )  
631 increases with increase in  $\tau$ . This is due to the fact the all CCEs initiate with almost  
632 identical characteristics but may terminate in very different ways. In part II of this work  
633 we show that this variance is highly influenced from precipitation which contributes to  
634 more significant interactions between clouds (Heiblum et al., 2016b).

635

## 636 **6. Summary**

637 In this paper we study the partition of warm convective clouds to core and margin  
638 according to three different definitions: i) positive vertical velocity ( $W_{core}$ ), ii) relative  
639 humidity supersaturation ( $RH_{core}$ ), and iii) positive buoyancy ( $B_{core}$ ), with emphasis  
640 on the differences between those definitions. Using theoretical considerations of both  
641 an adiabatic cloud column and a simple two parcel mixing model (see appendix A and  
642 B), we support our simulated results as we show that the  $B_{core}$  is expected to be the  
643 smallest of the three. This finding is in line with previous works that showed that  
644 negative buoyancy is prevalent in cumulus clouds for a wide range of thermodynamic  
645 conditions (de Roode, 2008; Paluch, 1979; Taylor and Baker, 1991). This is due to the  
646 fact that entrainment into the core (i.e. mixing with non-cloudy environment or mixing  
647 with the margin regions of the cloud) may result in sub-saturation, followed by  
648 evaporation that always has a negative net effect on buoyancy. The same process has  
649 an opposing effect on the relative humidity of the mixed parcel and acts to reach  
650 saturation. Entrainment (or mixing) also acts to decrease vertical velocity, but at slower  
651 manner compared to the time scales of changes in the buoyancy and relative humidity.  
652 In addition, the supersaturation equation (Eq. (3)) predicts that it is unlikely to maintain  
653 supersaturation in a cloudy volume with negative vertical velocity. Hence,  $W_{core}$  can  
654 be expected to be the largest of the three cores.

655 Using numerical simulations of both a single cloud and cloud fields of warm cumulus  
656 clouds, we show that during most stages of clouds' lifetime,  $W_{core}$  is indeed the largest

657 of the three and  $B_{core}$  the smallest. In addition to the differences in their sizes, the three  
658 cores tend to be subsets of one another (and located around the cloud geometrical  
659 center), in the following order:  $B_{core} \subseteq RH_{core} \subseteq W_{core}$ . This property is most valid  
660 for a cloud at its initial stages and breaks down gradually during a cloud's lifetime. The  
661 warm convective cloud fields simulated here typically have a transition layer near the  
662 lifting condensation level (LCL). Thus, the lower parts of the clouds are negatively  
663 buoyant or even lack a  $B_{core}$  at formation. After cloud formation internal growth  
664 processes (i.e. condensation and latent heat release) increase the  $B_{core}$  until dissipation  
665 processes become dominant and the  $B_{core}$  decreases quickly due to entrainment. In  
666 contrast, clouds are initially dominated by the  $W_{core}$  and  $RH_{core}$  (fractions close to 1).  
667 The fractions of these cores then decrease monotonically with cloud lifetime.

668 During dissipation stages, the clouds are mostly margin dominated, such that most of  
669 the small mass dissipation cloud fragments are entirely coreless. However, several  
670 small mass dissipating cloud fragments which shed off large cloud entities (with large  
671 COG height) may be core dominated, especially using the  $RH_{core}$  definition. The same  
672 is observed for small precipitating cloud fragments which reside below the convective  
673 cloud base. We note that the results here are similar for both volume and mass core  
674 fractions out the cloud's totals, with the core mass fractions being larger due to a skewed  
675 distribution of cloud LWC which favors the core regions. Moreover, we show that these  
676 results are consistent for various levels of aerosol concentrations (will be seen in Part  
677 II) and different thermodynamic profiles used to initialize the models.

678 With respect to cloud morphology, it is shown that during cloud growth, which  
679 comprises the majority of a warm cloud lifetime, the physical cores are centered near  
680 the cloud's geometrical core, as is intuitively expected from a cloud's core. This  
681 matches the convective cloud core-shell model. An exception to this is the initial growth  
682 stages, where the  $B_{core}$  centroid can be located far from the cloud's centroid. During  
683 dissipation (i.e. approximately the last third of a cloud's lifetime), the core-shell model  
684 no longer applies to the clouds, as the cores decouple from the geometrical core and  
685 often comprise just a few isolated pixels at the cloud's edges. The  $W_{core}$  and  $B_{core}$   
686 pixels tend to be more peripheral than  $RH_{core}$  during dissipation (see Sect. 5.2).  
687 Downdraft induced adiabatic heating at the clouds' edge (see more in Part II) promote  
688 positive buoyancy while decreasing the chance for supersaturation. During dissipation

689 the overlap between different core types also decreases rapidly, implying that minor  
 690 local effects enable core existence rather than cloud convection. Thus, only during  
 691 mature growth stages can all three cores types can be considered interchangeable. In  
 692 Part II of this work we use the insights gained here to understand aerosol effects on  
 693 warm convective clouds, as are reflected by a cloud's partition to its core and margin.

694

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698

699

### 700 **Appendix A: Buoyancy changes due to mixing of cloudy and non-cloudy parcels**

701 Here we present a simple model for entrainment mixing between a cloudy parcel (either  
 702 part of  $B_{core}$  or  $B_{margin}$ ) and a dry environmental parcel. Entrainment mixes the  
 703 momentum, heat, and humidity of the two parcels. We consider the mixing of a unit  
 704 mass of cloud parcel which is defined by two criteria:

$$705 \begin{aligned} S_1 &\geq 1 \\ B_1 &> 0 \text{ or } B_1 < 0 \end{aligned}$$

706 with a unit mass of dry environment parcel, defined by:

$$707 S_2 < 1$$

708 and explore the properties of the resulting mixed parcel.

709 Assume that  $T_1, T_2, T_3$  are the initial temperatures of the cloudy, environmental, and  
 710 resulting mixed parcel, respectively.  $q_{v1}, q_{v2}, q_{v3}, \theta_1, \theta_2, \theta_3$ , and  $q_{l1}, q_{l2}, q_{l3}$  are their  
 711 respective vapor mixing ratios, potential temperatures, and liquid water contents  
 712 (LWC).

713 The change in buoyancy due to mixing will be:

$$714 dB_{mix} = g * \left( \frac{\theta_3 - \theta_1}{\theta_2} + 0.61(q_{v3} - q_{v1}) - (q_{l3} - q_{l1}) \right) \quad (A1),$$

715 with



716  $T_3 = \mu_1 \cdot T_1 + \mu_2 \cdot T_2$  (A2),

717  $q_{v3} = \mu_1 \cdot q_{v1} + \mu_2 \cdot q_{v2}$  (A3),

718  $q_{l3} = \mu_1 \cdot q_{l1} + \mu_2 \cdot q_{l2}$  (A4),

719 where  $\mu_1$  and  $\mu_2$  are the corresponding mixing fractions. We assume that the mixed  
 720 parcel is at the same height as the cloudy and environmental parcels, and that the mean  
 721 environmental temperature at that height stays the same after mixing. The potential  
 722 temperature ( $\theta$ ) is calculated using its definition.

723 After the mixing process, the resultant mixed parcel may be subsaturated ( $S_3 < 1$ ), and  
 724 cloud droplets start to evaporate. The evaporation process increases the humidity of the  
 725 parcel. ((Korolev et al., 2016), Eq. (A8)) calculated the amount of the required liquid  
 726 water for evaporation, in order to reach  $S=1$  again:

727 
$$\delta q = \frac{C_p R_v T_3^2}{L^2} \ln \left( \frac{1 + \frac{e_s(T_3) R_a L^2}{P C_p R_v^2 T_3^2}}{1 + S_3 \frac{e_s(T_3) R_a L^2}{P C_p R_v^2 T_3^2}} \right)$$
 (A5),

728 Where  $C_p$  is a specific heat at constant pressure,  $e_s(T_3)$  is the saturated vapor pressure  
 729 for the mixed temperature,  $P$  is pressure,  $L$  is latent heat,  $R_v, R_a$  are individual gas  
 730 constants for water vapor and dry air, respectively. If the mixed parcel contains  
 731 sufficient LWC to evaporate  $\delta q$  amount of water, the mixed parcel will reach  
 732 saturation. We note that Eq. (A5) holds for cases where  $|T_1 - T_2| < 10^\circ C$ , which is  
 733 well within the range seen in our simulations of warm clouds.

734 Assuming the average environmental temperature stays the same after evaporation, the  
 735 buoyancy after evaporation is calculated using the following formulas:

736 
$$dB_{evap} = g \cdot \left( \frac{d\theta'_{evap}}{\theta_2} + 0.61 dq_{v_{evap}} - dq_{l_{evap}} \right)$$
 (A6),

737 
$$d\theta'_{evap} = dT_{evap}$$
 (A7),

738 From the first law of thermodynamics:

739 
$$C_p \cdot dT_{evap} = -L \cdot dq_{v_{evap}}$$
 (A8).

740 The water vapor is the amount of liquid water lost by evaporation:

741  $dq_{v_{evap}} = -dq_{l_{evap}} = \delta q$  (A9),

742 From the above we get:

743  $dB_{evap} = g \cdot \delta q \left( 1.61 - \frac{L}{c_p \theta_2} \right)$  (A10).

744 For a wide temperature range between  $200 < \theta_2 < 300[K]$ ,  $dB_{evap}$  is always  
 745 negative. This result is not trivial because evaporation both decreases the T and  
 746 increases the  $q_v$  which have opposite effects. The total change in buoyancy is taken as  
 747 the sum of  $dB_{evap}$  and  $dB_{mix}$ .

748 Figure A1 presents a phase space of possible changes in cloudy pixel buoyancy due to  
 749 mixing with outside air, for various thermodynamic conditions, and a mixing fraction  
 750 of 0.5. The initial cloudy parcel is chosen to be saturated ( $S=1$ ) and includes a LWC of  
 751  $1 \text{ g kg}^{-1}$ . The pressure is assumed to be 850 mb, and the temperature  $15^\circ\text{C}$ . However,  
 752 we note that the conclusions here apply to all atmospherically relevant values of  
 753 pressure, temperature, supersaturation (values of  $RH > 100\%$ ), and LWC in warm  
 754 clouds. The X-axis in Fig. A1 spans a range of non-cloudy environment relative  
 755 humidity values ( $60\% < RH < 100\%$ ), and the Y-axis spans a temperature difference  
 756 range between the cloud and the environment parcels ( $-3^\circ < dT < 3^\circ$ ). The initial ( $B_i$ )  
 757 and final ( $B_f$ , after entrainment) buoyancy values, and the differences between them  
 758 can be either positive or negative. The regions of  $B_i > 0$  ( $B_i < 0$ ) in fact illustrate the effects  
 759 of entrainment on  $B_{core}$  ( $B_{margin}$ ) parcels.

760

761

762 **Appendix B: Buoyancy changes due to mixing of core and margin parcels**

763 Following the notations of appendix A, we now consider the mixing of two cloudy  
 764 parcels, one part of  $B_{core}$  and one part of  $B_{margin}$ . For simplicity, we choose the case  
 765 where both parcels are saturated and have the same LWC of  $0.5 \text{ g kg}^{-1}$ :

766 
$$\begin{aligned} S_{core} &= S_{margin} = S_{cloud} = 1 \\ q_{l_{core}} &= q_{l_{margin}} = q_{l_{cloud}} = 0.5 \end{aligned} \quad (\text{B1}).$$

767 The buoyancy of each cloudy parcel is determined in reference to the environmental  
 768 temperature and humidity,  $T_{env}$ ,  $q_{v_{env}}$ , so that:

$$769 \quad B_{cloud} = g * \left( \frac{\theta_{cloud} - \theta_{env}}{\theta_{env}} + 0.61(q_{v_{cloud}} - q_{v_{env}}) - q_{l_{cloud}} \right) \quad (B2).$$

770 As mentioned in the main text, we take a temperature range of  $T_{env} - 3^\circ C < T_{cloud} <$   
 771  $T_{env} + 3^\circ C$ . Each cloudy parcel's temperature also dictates its saturation vapor pressure  
 772  $e_s(T_{cloud})$  and therefore also its humidity content,  $q_{v_{cloud}}$ . Plugging these into Eq. (B2),  
 773 one can associate each temperature/humidity pair with the  $B_{core}$  or  $B_{margin}$ :

$$774 \quad \begin{aligned} T_{core} &= T_{cloud}(B_{cloud} > 0), q_{v_{core}} = q_{v_{cloud}}(B_{cloud} > 0) \\ T_{margin} &= T_{cloud}(B_{cloud} < 0), q_{v_{margin}} = q_{v_{cloud}}(B_{cloud} < 0) \end{aligned} \quad (B3).$$

775 The core and margin parcels can then be mixed (see appendix A) yielding a mixed  
 776 parcel temperature and humidity content, and thus a new relative humidity. The  
 777 buoyancy of the mixed parcel is obtained by inserting these parameters in Eq. (B2).

778 In Fig. B1 the resultant buoyancy values and RH values after the mixing of  $B_{core}$   
 779 parcels with  $B_{margin}$  parcels are shown. As defined in Appendix A, temperature  
 780 differences between the parcels and the environment are confined to  $\pm 3^\circ C$ . The  
 781 reference environmental temperature, pressure, and RH are taken to be  $15^\circ C$ , 850 mb,  
 782 and 90%, respectively. We note the main differences between this section and  
 783 Appendix A are the absence of evaporation and the fact that the core and margin  
 784 thermodynamic variables are the ones that vary while the reference environmental ones  
 785 are kept constant.

786 It can be seen that all negatively buoyant parcels are colder than the environment and  
 787 nearly all positively buoyant parcels are warmer than the environment, except for a  
 788 small fraction that are slightly colder but positively buoyant due to the increased  
 789 humidity. The transition from  $B_f > 0$  to  $B_f < 0$  near the 1 to 1 line indicates that  $B_f$  is  
 790 approximately linearly dependent on the temperature differences with respect to the  
 791 environment. In other words, if  $|T_{core} - T_{env}| > |T_{margin} - T_{env}|$ , the mixed parcel is  
 792 expected to be part of the  $B_{core}$  (i.e.  $B_f > 0$ ). The exponential increase in saturation vapor  
 793 pressure with temperature is demonstrated by the results of the mixed parcel final RH,  
 794 which all show supersaturation values. Additional sensitivity tests were performed for

795 this analysis, showing only weak dependencies on environmental parameter values,  
796 while maintaining the main conclusions.

797

798

799

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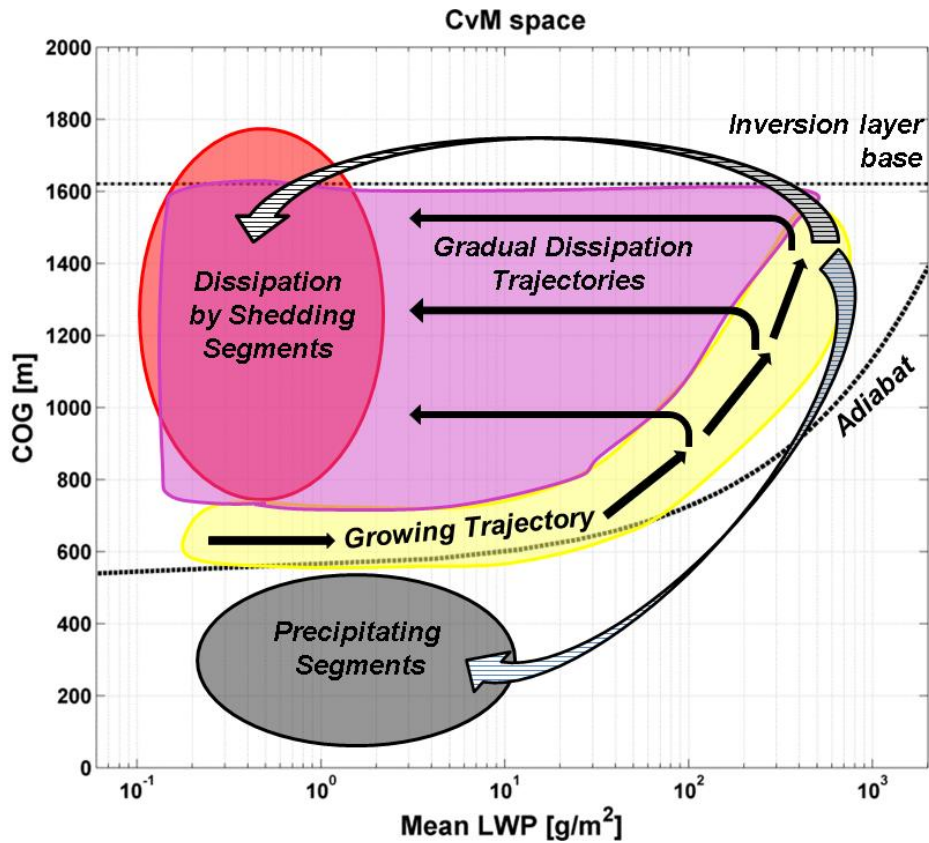
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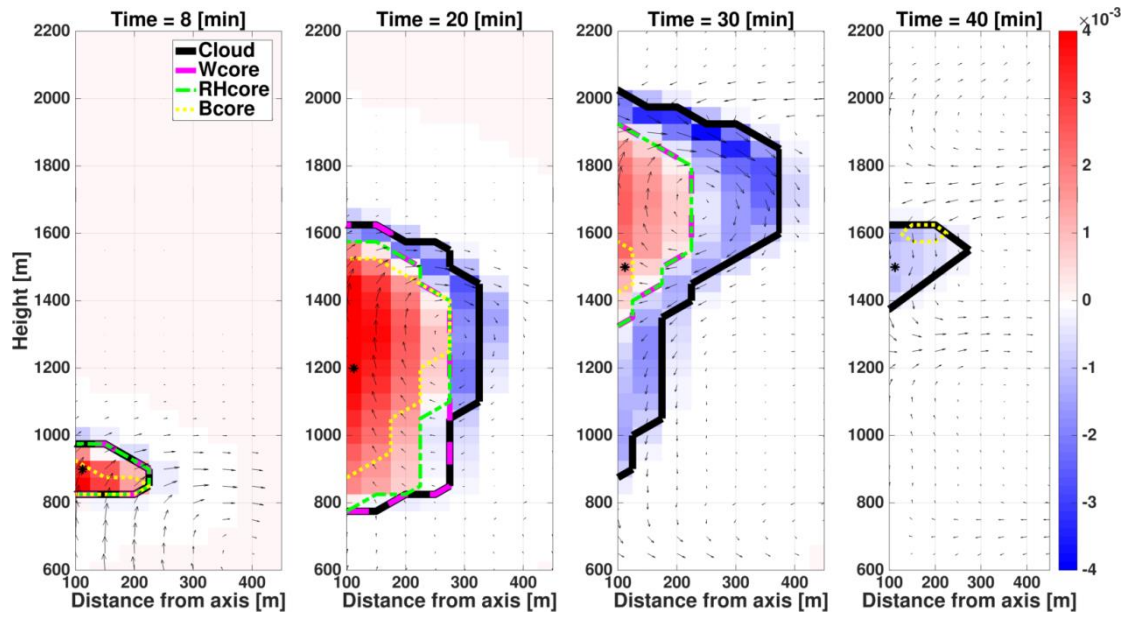
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1009

1010 *Figure 1. A schematic representation of a cloud field Center-of-gravity height (Y-Axis)*  
 1011 *vs. Mass (X-Axis) phase space (CvM in short). The majority of clouds are confined to*  
 1012 *the region between the adiabatic approximation (curved dashed line) and the inversion*  
 1013 *layer base height (horizontal dashed line). The yellow, magenta, red, and grey shaded*  
 1014 *regions represent cloud growth, gradual dissipation, cloud fragments which shed off*  
 1015 *large clouds, and cloud fragments which shed off precipitating clouds, respectively.*  
 1016 *The black arrows represent continuous trajectories of cloud growth and dissipation.*  
 1017 *The hatched arrows represent two possible discontinuous trajectories of cloud*  
 1018 *dissipation where clouds shed segments.*

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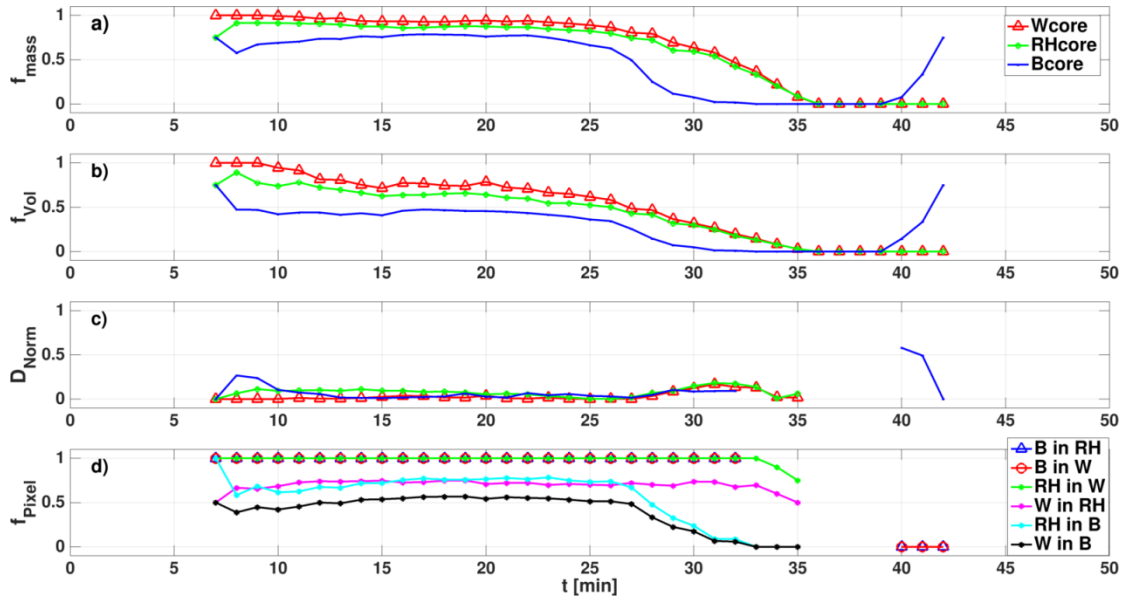


1020

1021 *Figure 2. Four vertical cross-sections (at  $t=8, 20, 30, 40$  minutes) during the single*  
 1022 *cloud simulation. Y-axis represents height [m] and X-axis represents the distance from*  
 1023 *the axis [m]. The black, magenta, green and yellow lines represent the cloud,*  
 1024  *$W_{core}$ ,  $RH_{core}$  and  $B_{core}$ , respectively. The black arrows represent the wind, the*  
 1025 *background represents the condensation (red) and evaporation rate (blue) [ $g\ kg^{-1}\ s^{-1}$ ],*  
 1026 *and the black asterisks indicate the vertical location of the cloud centroid. Note that in*  
 1027 *some cases the lines indicating core boundaries overlap (mainly seen for RH and W*  
 1028 *cores).*

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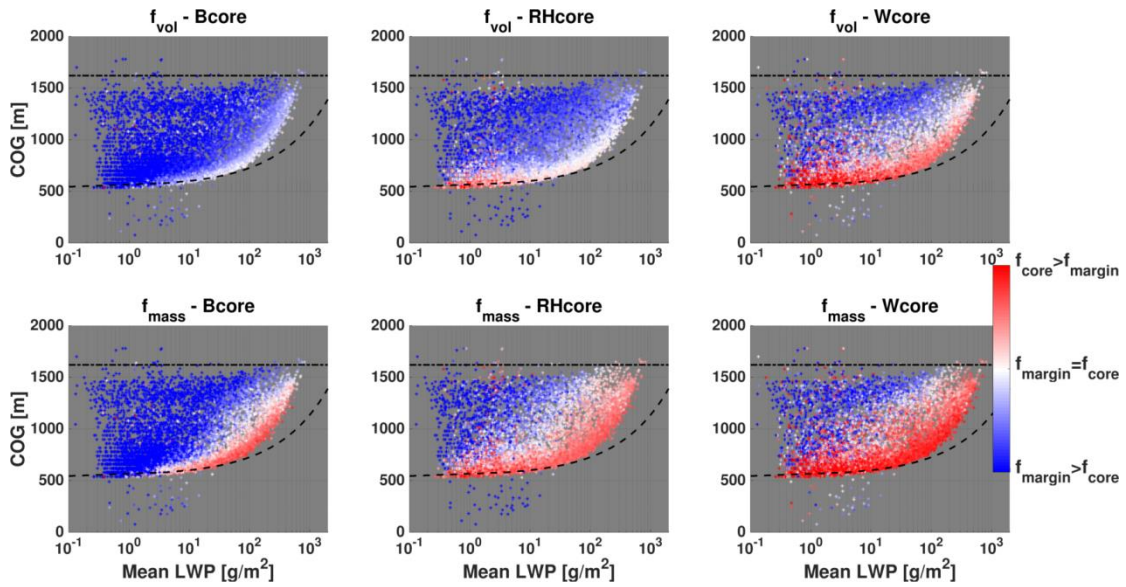


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1032 *Figure 3. Temporal evolution of selected core properties, including: (a) The fraction of*  
 1033 *the cores' mass from the total cloud mass ( $f_{mass}$ ), (b) the fraction of the cores' volume*  
 1034 *from the total cloud volume ( $f_{vol}$ ), (c) the normalized distance between cloud centroid*  
 1035 *and core centroid ( $D_{norm}$ ), and (d) the fraction of cores' pixels contained within another*  
 1036 *core ( $f_{pixel}$ ), including all six permutations. See panel legends for descriptions of line*  
 1037 *colors.*

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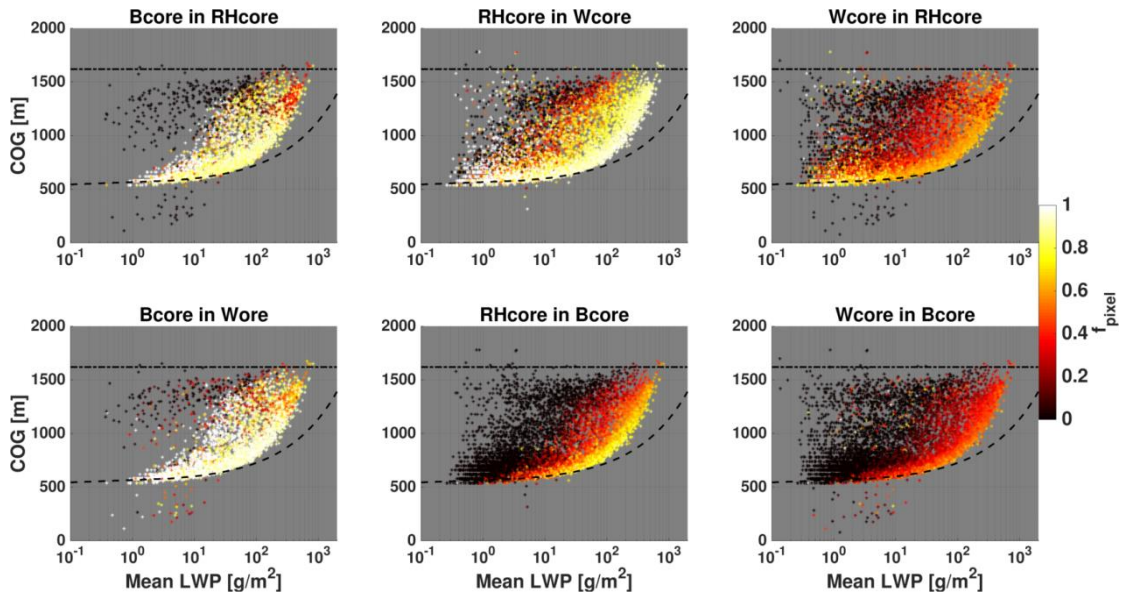


1040

1041 *Figure 4. CvM phase space diagrams of  $B_{core}$  (left column),  $RH_{core}$  (middle column),*  
1042 *and  $W_{core}$  (right column) fractions for all clouds between 3 h and 8 h in the BOMEX*  
1043 *simulation. Both volume fractions ( $f_{vol}$ , upper panels) and mass fractions ( $f_{mass}$  lower*  
1044 *panels) are shown. The red (blue) colors indicate a core fraction above (below) 0.5.*  
1045 *For a general description of CvM space characteristics the reader is referred to Sect.*  
1046 *2.4.*

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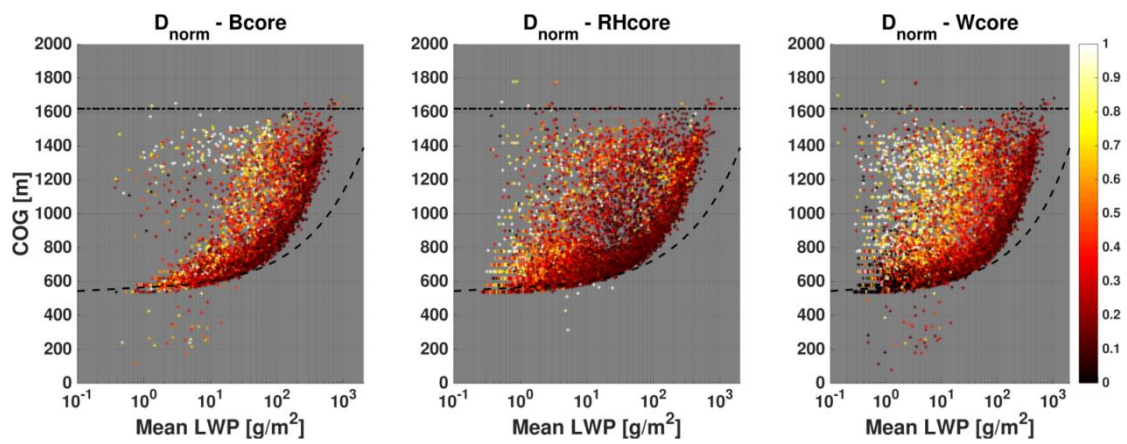


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1050 *Figure 5. CvM phase space diagrams of pixel fractions ( $f_{\text{pixel}}$ ) of each of the three*  
1051 *cores within another core, including six different permutations (as indicated in the*  
1052 *panel titles). Bright colors indicate high pixel fractions (large overlap between two core*  
1053 *types) while dark colors indicate low pixel fraction (little overlap between two core*  
1054 *types). The differences in the scatter density and location for different panels are due*  
1055 *to the fact that only clouds which contain a core fraction above zero (for the core in*  
1056 *question) are considered. For example, for the Buoy in RH panel (upper left), only*  
1057 *cloud that contain some pixels with positive buoyancy are considered.*

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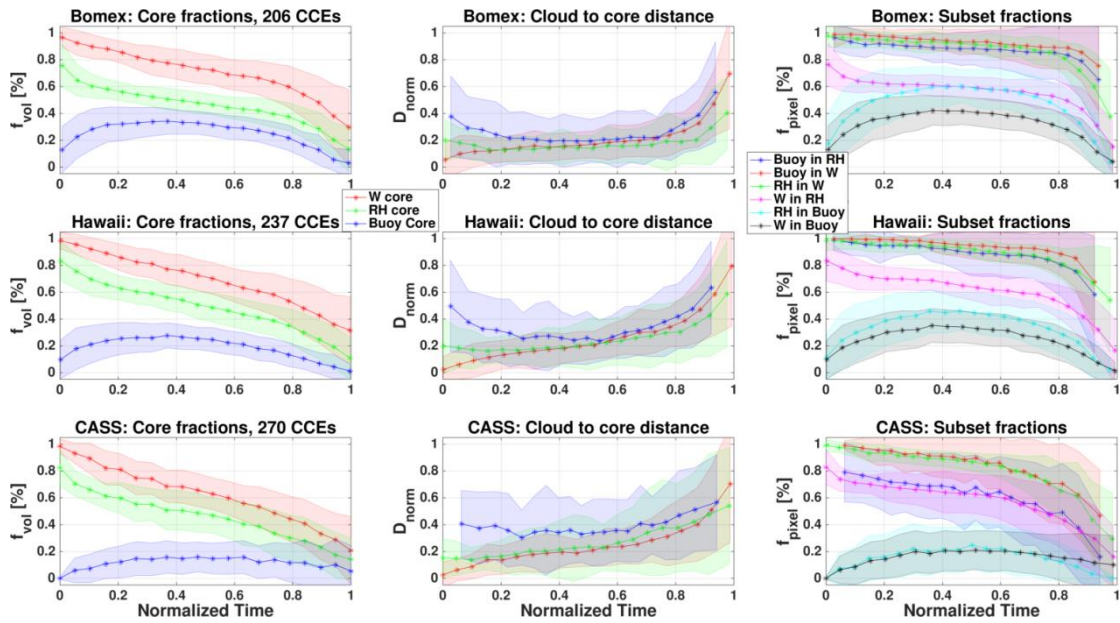
1061 *Figure 6. CvM phase space diagrams of distances between core centroid location and*  
1062 *cloud centroid location, for the three different physical core types. The distances are*  
1063 *normalized by the cloud volume radius (approximately the largest distance possible).*  
1064 *Bright (dark) colors indicates large (small) distances. As seen in Fig. 5, only clouds*  
1065 *which contain a core fraction above zero (for the core in question) are considered.*

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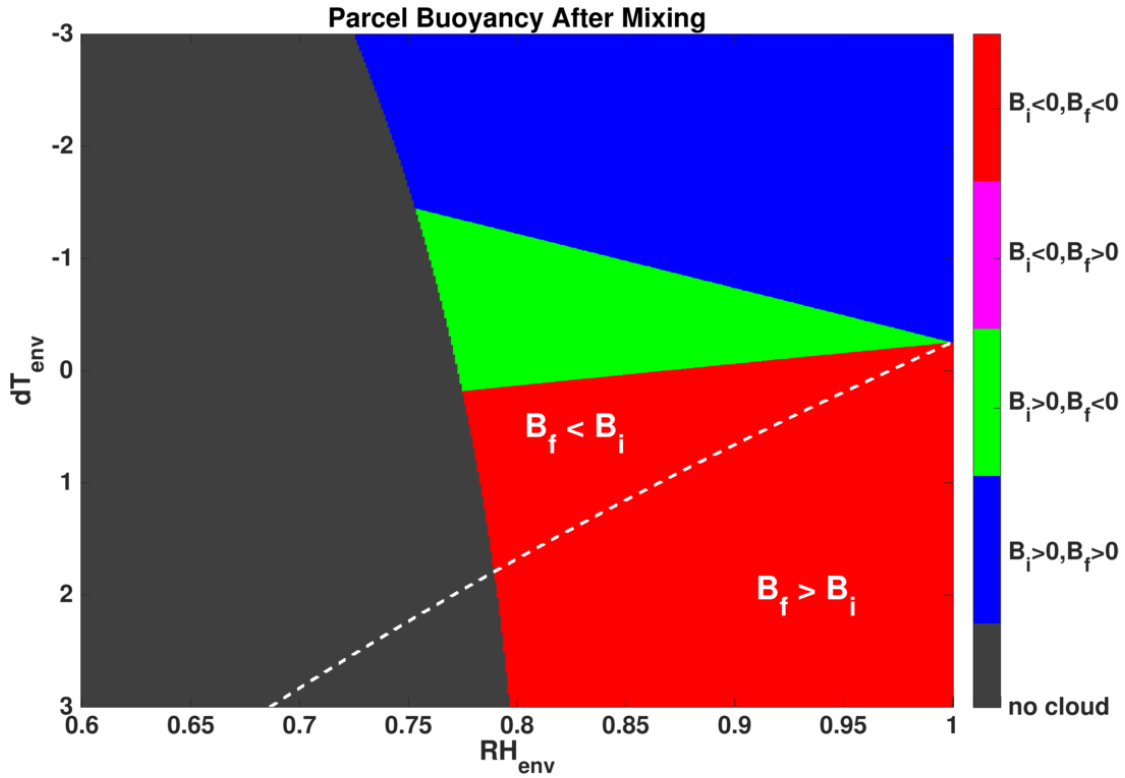
1069

1070 *Figure 7. Normalized time series of CCE averaged core fractions for the BOMEX*  
 1071 *(upper row), Hawaii (middle row), and CASS (bottom row) simulations. Both core*  
 1072 *volume fractions ( $f_{vol}$ , left column), normalized distances between cloud and core*  
 1073 *centroid locations ( $D_{norm}$ , middle column), and pixel fractions of one core within*  
 1074 *another ( $f_{pixel}$ , right column) are considered. Line colors indicated different core types*  
 1075 *(see legends), while corresponding shaded color regions indicate the standard*  
 1076 *deviation. Normalized time enables to average together CCEs with different lifetimes,*  
 1077 *from formation to dissipation. The number of CCEs averaged together for each*  
 1078 *simulation is included in the left column panel titles.*

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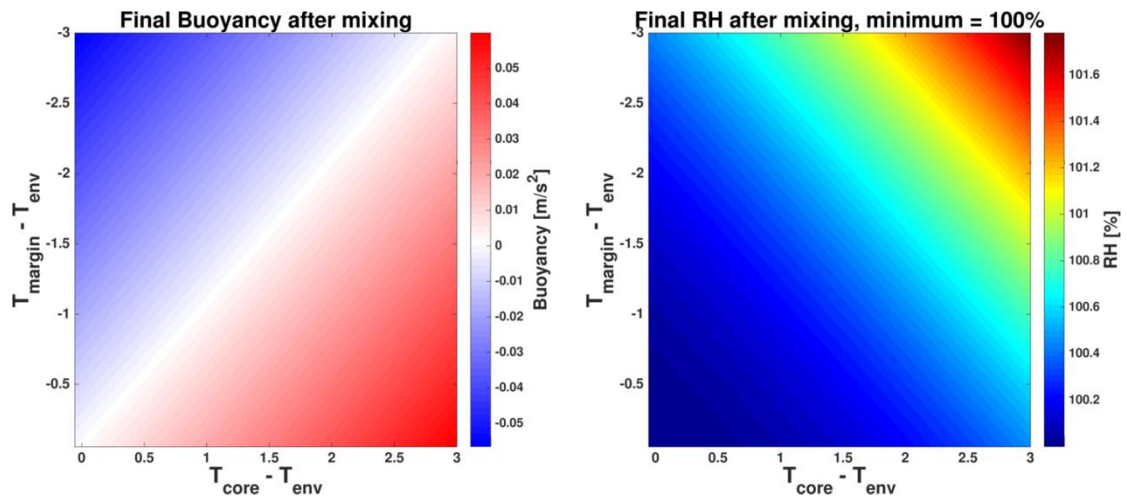




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1082 *Figure A1. Phase space presenting the effects of entrainment on cloud buoyancy, where*  
 1083 *the initial cloudy parcel buoyancy ( $B_i$ ) and final mixed parcel buoyancy ( $B_f$ ) are*  
 1084 *considered. A mixing fraction of 0.5 is chosen. The initial cloudy parcel is saturated*  
 1085 *( $S=1$ ), has a temperature of  $15^\circ\text{C}$ , pressure of 850 mb, and LWC of  $1 \text{ g kg}^{-1}$ . The X-axis*  
 1086 *spans a range of environment relative humidity values ( $RH_{env}$ ), and the Y-axis a*  
 1087 *temperature difference ( $dT_{env}=T_{env}-T_{cld}$ ) range between the cloud and the environment*  
 1088 *parcels. Red color represents  $B_i < 0$  &  $B_f < 0$  (i.e. parcel stays negatively buoyant after*  
 1089 *the mixing), magenta represents  $B_i < 0$  &  $B_f > 0$  (i.e. transition from negative to positive*  
 1090 *buoyancy), green represents  $B_i > 0$  &  $B_f < 0$  (i.e. transition from positive to negative*  
 1091 *buoyancy), and blue represents  $B_i > 0$  &  $B_f > 0$  (i.e. parcel stays positively buoyant).*  
 1092 *The grey color represents mixed parcels that were depleted from water (LWC value*  
 1093 *lower than  $0.01 \text{ g kg}^{-1}$ ) after evaporation, and are considered non-cloudy. The white*  
 1094 *line separates between areas where  $B_f > B_i$  and  $B_f < B_i$ .*

1095



1096

1097 *Figure B1. Phase space presenting the resultant buoyancy (left panel) and relative*  
 1098 *humidity (RH, right panel) when mixing  $B_{core}$  and  $B_{margin}$  parcels with equal RH but*  
 1099 *different temperatures. A mixing fraction of 0.5 is chosen. Both parcels are initially*  
 1100 *saturated (RH=100%), and have a LWC of  $0.5 \text{ g kg}^{-1}$ . The environment has a*  
 1101 *temperature of  $15^\circ\text{C}$  and pressure of  $850 \text{ mb}$ . The X(Y)-axis spans the range of*  
 1102 *temperature differences between the  $B_{core}$  ( $B_{margin}$ ) parcel and the environment.*

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