



1 **Evaluate autoconversion and accretion enhancement factors in GCM warm-rain**
2 **parameterizations using ground-based measurements at the Azores**

3 Peng Wu¹, *Baiké Xi¹, Xiquan Dong¹, and Zhibo Zhang²

4¹ Department of Hydrology and Atmospheric Sciences, The University of Arizona, Tucson,
5 Arizona, USA

6² Physics Department, The University of Maryland, Baltimore County, Maryland, USA

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18* Corresponding author address: Dr. Baiké Xi, Department of Hydrology and Atmospheric
19 Sciences, University of Arizona, 1133 E. James E. Rogers Way, Tucson, AZ 85721-0011.

20 baikexi@email.arizona.edu;

Phone:

520-626-8945



21 Abstract

22 A great challenge in climate modelling is how to parametrize sub-grid cloud processes, such
23 as autoconversion and accretion in warm rain formation. In this study, we use ground-based
24 observations and retrievals over the Azores to investigate the so-called enhancement factors,
25 E_{auto} and E_{accr} , which are often used in climate models to account for the influences of sub-
26 grid variances of cloud and precipitation water on the autoconversion and accretion
27 processes. E_{auto} and E_{accr} are computed at a variety of tempo-spatial scales corresponding to
28 different model resolutions. The calculated E_{auto} increase from 1.79 (0.5-hr/36 km) to 3.15
29 (3.5-hr/126 km), and the calculated E_{accr} increases from 1.25 (0.5-hr/36 km) to 1.6 (5-hr/180
30 km). Comparing the prescribed enhancement factors to the values from observations shows
31 that GCMs are using a much higher E_{auto} (3.2) and lower E_{accr} (1.07). This helps to explain
32 why most of the GCMs produce too frequent precipitation events but with too light
33 precipitation intensity. The ratios of rain to cloud liquid water at $E_{accr}=1.07$ and $E_{accr}=2.0$ are
34 0.048 and 0.119, respectively, further proving that the prescribed value of $E_{accr}=1.07$ used in
35 GCMs is too small to simulate correct precipitation intensity. Both E_{auto} and E_{accr} increase
36 when the boundary layer becomes less stable, and the values are larger in precipitating clouds
37 ($CLWP > 75 \text{ gm}^{-2}$) than those in nonprecipitating clouds ($CLWP < 75 \text{ gm}^{-2}$). Therefore, the
38 selection of E_{auto} and E_{accr} values in GCMs should be regime-dependent.

39



40 **1. Introduction**

41 Due to their vast areal coverage (Warren et al., 1986, 1988; Hahn and Warren, 2007) and
42 strong radiative cooling effect (Hartmann et al., 1992; Chen et al., 2000), small changes in the
43 coverage or thickness of marine boundary layer (MBL) clouds could change the radiative
44 energy budget significantly (Hartmann and Short, 1980; Randall et al., 1984) or even offset
45 the radiative effects produced by increasing greenhouse gases (Slingo, 1990). The lifetime of
46 MBL clouds remains an issue in climate models (Yoo and Li, 2012; Jiang et al., 2012; Yoo et
47 al., 2013; Stanfield et al., 2014) and represents one of the largest uncertainties in predicting
48 future climate (Wielicki et al., 1995; Houghton et al., 2001; Bony and Dufresne, 2005).

49 MBL clouds frequently produce precipitation, mostly in the form of drizzle (Austin et al.,
50 1995; Wood, 2005a; Leon et al., 2008; Wood, 2012). A significant amount of drizzle are
51 evaporated before reaching the surface, for example, about ~76% over the Azores region in
52 Northeast Atlantic (Wu et al., 2015), which provides another water vapour source for MBL
53 clouds. Due to their pristine environment and their close vicinity to the surface, MBL clouds
54 are especially sensitive to aerosol perturbations and constitute the central piece of global
55 aerosol indirect effects in climate models (Quaas et al., 2009; Kooperman et al., 2012). Most
56 aerosol indirect effects are associated with precipitation suppression (Albrecht, 1989;
57 Ackerman et al., 2004; Lohmann and Feichter, 2005; Wood, 2007). Thus, accurate prediction



58 of precipitation is essential in simulating the global energy budget and in constraining aerosol
59 indirect effects in climate projections.

60 Due to the coarse spatial resolutions of the general circulation model (GCM) grid, many
61 cloud processes cannot be adequately resolved and must be parameterized (Morrison and
62 Gettleman, 2008). For Example, warm rain parameterizations in most GCMs treat the
63 condensed water as either cloud or rain in the processes of autoconversion and accretion
64 (Kessler, 1969; Khairoutdinov and Kogan, 2000; Morrison and Gettleman, 2008).
65 Autoconversion is the process that drizzle drops being formed through the collision-
66 coalescence of cloud droplets and accretion is the process where rain drops grow by the
67 coalescence of drizzle-sized drops with cloud droplets. Autoconversion mainly accounts for
68 precipitation initiation while accretion primarily contributes to precipitation intensity.
69 Autoconversion is often parameterized as functions of cloud droplet number concentration
70 (N_c) and cloud water mixing ratio (q_c), while accretion depends on both cloud and rain water
71 mixing ratios (q_c and q_r) (Kessler, 1969; Tripoli and Cotton, 1980; Beheng, 1994;
72 Khairoutdinov and Kogan, 2000; Liu and Daum, 2004; Wood, 2005b; Morrison and
73 Gettleman, 2008; Larson and Griffin, 2013). All the previous studies proposed that these two
74 processes as power law functions of cloud and precipitation properties (See section 2 for
75 details).



76 In conventional GCMs, the lack of information on the sub-grid variances of cloud and
77 precipitation leads to the unavoidable use of the grid-mean quantities (N'_c , q'_c , and q'_r , where
78 prime denotes grid mean, same below) in calculating autoconversion and accretion rates.
79 However, due to the nonlinear nature of the relationships and positive skewness of MBL
80 cloud liquid water path (CLWP) distributions from measurements (Wood and Hartmann,
81 2006), the two processes depend significantly on the sub-grid scale variability and co-
82 variability of cloud and precipitation microphysical properties (Weber and Quass, 2012;
83 Boutle et al., 2014). In GCMs, sub-grid scale variability is often ignored or hard coded using
84 constants to represent the variabilities under all meteorological conditions and across the
85 entire globe (Pincus and Klein, 2000; Morrison and Gettleman, 2008; Lebsock et al. 2013).
86 This could lead to systematic errors in precipitation rate simulations (Wood et al., 2002;
87 Larson et al., 2011; Lebsock et al. 2013; Boutle et al., 2014; Song et al. 2018), where GCMs
88 are found to produce too frequent but too light precipitation compared to observations (Zhang
89 et al., 2002; Jess, 2010; Stephens et al., 2010; Nam and Quaas, 2012; Song et al. 2018). The
90 bias is found to be smaller by using a probability density function (PDF) of cloud water to
91 represent the sub-grid scale variability in autoconversion parameterization (Beheng, 1994;
92 Zhang et al., 2002; Jess, 2010), or more complexly, by integrating the autoconversion rate
93 over a joint PDF of liquid water potential temperature, vertical velocity, total water mixing
94 ratio and rain water mixing ratio (Cheng and Xu, 2009).



95 Process rate enhancement factors (E) are introduced when considering sub-grid scale
96 variability in parameterizing grid-mean processes and they should be parameterized as
97 functions of the PDFs of cloud and precipitation properties within a grid box (Morrison and
98 Gettleman, 2008; Lebsock et al. 2013; Boutle et al., 2014). However, these values in GCMs
99 are prescribed as constants regardless of underlying surface or meteorological conditions (Xie
100 and Zhang, 2015). Previous studies used aircraft *in situ* measurements (Boutle et al., 2014)
101 and satellite observations (Lebsock et al. 2013) to evaluate the dependence of E on sub-grid
102 scale variability over oceans. These studies found that sub-grid scale variability and
103 covariance between cloud and precipitation properties significantly affect autoconversion and
104 accretion parameterizations. Using ground-based observations and retrievals, Xie and Zhang
105 (2015) proposed a scale-aware cloud inhomogeneity parameterization that they applied to the
106 Community Earth System Model (CESM) and found that it can recognize spatial scales
107 without manual tuning. The inhomogeneity parameter is essential in calculating enhancement
108 factors and affect the conversion rate from cloud to rain liquid. Xie and Zhang (2015),
109 however, did not evaluate the validity of CESM simulations from their parameterization; the
110 effect of N_c variability, or the effect of covariance of cloud and rain on accretion process was
111 not assessed.

112 Dong et al. (2014a and 2014b) and Wu et al. (2015) reported MBL cloud and drizzle
113 properties over the Azores and provided the possibility of calculating the enhancement



114 factors using ground-based observations and retrievals. This manuscript is organized as
115 follows: section 2 will include a summary of the mathematical formulas from previous
116 studies that can be used to calculate grid-mean process enhancement factors. Ground-based
117 observations and retrievals are introduced in Section 3. Section 4 presents results and
118 discussion, followed by summary and conclusions in Section 5.

119 2. Mathematical Background

120 Autoconversion and accretion rates in GCMs are usually parameterized as power law
121 equations (Tripoli and Cotton, 1980; Beheng, 1994; Khairoutdinov and Kogan, 2000; Liu and
122 Daum, 2004; Morrison and Gettleman, 2008):

$$123 \left(\frac{\partial q_r}{\partial t}\right)_{auto} = A q_c'^{a1} N_c'^{a2}, \quad (1)$$

$$124 \left(\frac{\partial q_r}{\partial t}\right)_{accr} = B (q_c' q_r')^b, \quad (2)$$

125 where A , $a1$, $a2$, B , and b are constants that change value depending on which scheme is
126 being used. Table 1 provides a list of the schemes and their associated constants. q_c' , q_r' , and
127 N_c' are grid-mean cloud water mixing ratio, rain water mixing ratio, and droplet number
128 concentration, respectively. Because it is widely used in model parameterizations, the
129 detailed results from Khairoutdinov and Kogan (2000) and Morrison and Gettleman (2008)
130 scheme will be shown in Section 4 while a summary will be given for other schemes.



131 Ideally, the covariance between physical quantities should be considered in the
132 calculation of both processes. However, q_c' and N_c' in Eq. (1) are arguably not independently
133 retrieved in our retrieval method which will be introduced in the section below. We only
134 assess the individual roles of q_c and N_c sub-grid variations in determining autoconversion rate.
135 q_c and q_r , on the other hand, are retrieved from two independent algorithms as shown in Dong
136 et al. (2014a and 2014b) and Wu et al. (2015), thus we will assess the effect of cloud and rain
137 property covariance on accretion rate calculations.

138 In the sub-grid scale, the PDFs of q_c and N_c are assumed to follow a gamma distribution
139 based on observational studies of optical depth in MBL clouds (Barker et al., 1996; Pincus et
140 al., 1999; Wood and Hartmann, 2006):

$$141 \quad P(x) = \frac{\alpha^\nu}{\Gamma(\nu)} x^{\nu-1} e^{-\alpha x}, \quad (3)$$

142 where x represents q_c or N_c with grid-mean quantity q_c' or N_c' , represented by μ , $\alpha = \nu/\mu$ is
143 the scale parameter, σ^2 is the relative variance of x (= variance divided by μ^2), $\nu = 1/\sigma^2$ is
144 the shape parameter. ν is an indicator of cloud field homogeneity, with large values
145 representing homogeneous and small values indicating inhomogeneous cloud fields.

146 By integrating autoconversion rate, Eq. (1), over the grid-mean rate, Eq. (3), with respect
147 to sub-grid scale variation of q_c and N_c , the autoconversion rate can be expressed as:

$$148 \quad \left(\frac{\partial q_r}{\partial t}\right)_{auto} = A \mu_{q_c}^{2.47} \mu_{N_c}^{-1.79} \frac{\Gamma(\nu+a)}{\Gamma(2.47)\nu^a}, \quad (4)$$



149 where $a = a1$ or $a2$. Comparing Eq. (4) to Eq. (1) gives the the autoconversion enhancement
 150 factors (E_{auto}) with respect to q_c and N_c :

$$151 \quad E_{auto} = \frac{\Gamma(v+a)}{\Gamma(a)v^a}. \quad (5)$$

152 In addition to fitting the distributions of q_c and N_c , we also tried two other methods to
 153 calculate E_{auto} . The first is to integrate Eq. (1) over the actual PDFs from observed or
 154 retrieved parameters and the second is to fit a lognormal distribution for sub-grid variability
 155 like what has been done in other studies (e.g., Lebsock et al., 2013; Larson and Griffin,
 156 2013). It is found that all three methods get similar results. In this study, we use a gamma
 157 distribution that is consistent with the widely used GCM parameterization (Morrison and
 158 Gettleman, 2008). Also note that, in the calculation of E_{auto} from N_c , the negative exponent (-
 159 1.79) may cause singularity problems in Eq. (5). When this situation occurs, we do direct
 160 calculations by integrating the N_c PDF rather than using Eq. (5).

161 To account for the covariance of microphysical quantities in a model grid, it is hard to
 162 apply bivariate gamma distribution due to its complex nature. In this study, the bivariate
 163 lognormal distribution of q_c and q_r is used (Lebsock et al., 2013; Boutle et al., 2014) and can
 164 be written as:

$$165 \quad P(q_c', q_r') = \frac{1}{2\pi q_c' q_r' \sigma_{q_c} \sigma_{q_r} \sqrt{1-\rho^2}} \exp \left\{ -\frac{1}{2} \frac{1}{1-\rho^2} \left[\left(\frac{\ln q_c' - \mu_{q_c}}{\sigma_{q_c}} \right)^2 - 2\rho \left(\frac{\ln q_c' - \mu_{q_c}}{\sigma_{q_c}} \right) \left(\frac{\ln q_r' - \mu_{q_r}}{\sigma_{q_r}} \right) + \right. \right. \\ 166 \quad \left. \left. \left(\frac{\ln q_r' - \mu_{q_r}}{\sigma_{q_r}} \right)^2 \right] \right\}, \quad (6)$$



167 where σ is standard deviation and ρ is the correlation coefficient of q_c and q_r .

168 Similarly, by integrating the accretion rate in Eq. (2) from Eq. (6), we get the accretion
169 enhancement factor (E_{accr}) of:

$$170 \quad E_{accr} = \left(1 + \frac{1}{v_{qc}}\right)^{\frac{1.15^2 - 1.15}{2}} \left(1 + \frac{1}{v_{qr}}\right)^{\frac{1.15^2 - 1.15}{2}} \exp(\rho 1.15^2 \sqrt{\ln\left(1 + \frac{1}{v_{qc}}\right) \ln\left(1 + \frac{1}{v_{qr}}\right)}). \quad (7)$$

171 3. Ground-based observations and retrievals

172 The datasets used in this study were collected at the Department of Energy (DOE)
173 Atmospheric Radiation Measurement (ARM) Mobile Facility (AMF), which was deployed
174 on the northern coast of Graciosa Island (39.09°N, 28.03°W) from June 2009 to December
175 2010 (for more details, please refer to Rémillard et al. 2012; Dong et al. 2014a and Wood et
176 al. 2015). The detailed operational status of the remote sensing instruments on AMF was
177 summarized in Figure 1 of Rémillard et al. (2012) and discussed in Wood et al. (2015). The
178 ARM Eastern North Atlantic (ENA) site was established on the same island in 2013 and
179 provides long-term continuous observations.

180 The cloud-top heights (Z_{top}) were determined from W-band ARM cloud radar (WACR)
181 reflectivity and only single-layered low-level clouds with $Z_{top} \leq 3$ km are selected. Cloud-
182 base heights (Z_{base}) were detected by a laser ceilometer (CEIL) and the cloud thickness was
183 simply the difference between cloud top and base heights. The cloud liquid water path
184 (CLWP) was retrieved from microwave radiometer (MWR) brightness temperatures



185 measured at 23.8 and 31.4 GHz using a statistical retrieval method with an uncertainty of 20
186 g m^{-2} for $\text{CLWP} < 200 \text{ g m}^{-2}$, and 10% for $\text{CLWP} > 200 \text{ g m}^{-2}$ (Liljegren et al., 2001; Dong et
187 al., 2000). Drizzling status is identified through a combination of WACR reflectivity and
188 Z_{base} . As in Wu et al. (2015), we label the status of a specific time as “drizzling” if the
189 WACR reflectivity below the cloud base exceeds -37 dBZ.

190 Cloud microphysical properties (CLWC and N_c) are retrieved using the methods
191 presented in Dong et al. (2014a and 2014b). The CLWC values are transformed to q_c when
192 calculating autoconversion and accretion rates by dividing by air density. Drizzle property, or
193 rain LWP, (RLWP), below Z_{base} is retrieved using the method proposed in O’Connor et al.
194 (2005) and used by Wu et al. (2015). Similarly, drizzle LWC (DLWC) is transformed to q_r
195 when calculating the accretion rate.

196 The ARM merged sounding data (Trojan, 2012) are used to calculate lower tropospheric
197 stability (LTS), which is used to infer the boundary layer stability. In this study, unstable and
198 stable boundary layers are defined as LTS less than 13.5 K and greater than 18 K,
199 respectively, and environment with an LTS between 13.5 K and 18 K is defined as mid-stable
200 (Wang et al. 2012; Bai et al. 2018). Enhancement factors in different boundary layers are
201 summarized in Section 4.2 and may be used as references for model simulations. Further, two
202 regimes are classified: CLWP greater than 75 g m^{-2} as precipitating and CLWP less than 75 g
203 m^{-2} as nonprecipitating (Rémillard et al., 2012).



204 To evaluate the dependence of autoconversion and accretion rates on sub-grid scale
205 variabilities for different model spatial resolutions, we use a variety of time-intervals to
206 mimic different grid sizes. For example, a 2-hour interval corresponds to a 72-km grid box if
207 assuming 10 m s^{-1} horizontal wind and a 5-hour interval corresponds to a 180-km grid box.
208 We used 10 time-intervals (0.5-, 1-, 1.5-, 2-, 2.5-, 3-, 3.5-, 4-, 4.5-, 5-hour) and mainly show
209 the results from 2-hour and 5-hour intervals in Section 4.

210 **4. Results and discussions**

211 In this section, we first show the data and methods using a selected case, followed by
212 statistical analysis based on 19-month of data and multiple time-intervals.

213 **4.1 Case study**

214 The selected case occurred at the Azores on July 27, 2010 (Figure 1a). This case was
215 characterized by a long time of non-drizzling or light drizzling cloud development (00:00-
216 14:00 UTC) before intense drizzling occurs (14:00-20:00 UTC). Wu et al. (2017) studied this
217 case in detail to demonstrate the effect of wind shear on drizzle initiation. Here, we choose
218 two periods with similar mean CLWPs: 81 g m^{-2} for 7:00 – 12:00 UTC (period c) and 85 g m^{-2}
219 for 13:00 – 18:00 UTC (period d) but with different distributions (Figures 1c and 1d). The
220 PDFs of CLWP are then fitted using gamma distributions to get shape parameters (ν) as
221 shown in Figures 1c and 1d. Smaller ν is usually associated with more inhomogeneous cloud
222 field, which allows more rapid drizzle production and more efficient liquid transformation



223 from cloud to rain (Xie and Zhang, 2015) in regions that satisfy precipitation criteria, which
224 is usually controlled using threshold q_r , droplet size or relative humidity (Kessler, 1969; Liu
225 and Daum, 2004). The period d has a wider CLWP distribution than the period c, resulting in
226 a smaller ν and thus larger E_{auto} . Using the fitted ν , the E_{auto} from CLWP is calculated from
227 Eq. (5) and the period d is larger (1.81 vs. 1.33). The E_{auto} values for the periods d and c can
228 also be calculated from N_c using the same procedure as CLWP with similar result (2.1 vs.
229 1.51). The E_{accr} values for the periods d and c can be calculated from the covariance of
230 CLWP and RLWP and Eq. (7). Not surprisingly, the period d has larger E_{auto} than the period
231 c. The combination of larger E_{auto} and E_{accr} in the period d contribute to the rapid drizzle
232 production and high rain rate as seen from WACR reflectivity and RLWP.

233 It is important to clarify the meaning of enhancement factors in precipitation
234 parameterization. If we assume two scenarios for CLWPs with a model grid having the same
235 mean values but different distributions: (1) The distribution is extremely homogeneous, there
236 will be no sub-grid variability because the cloud has the same chance to precipitate and the
237 enhancement factors would be unity (this is true for arbitrary grid-mean CLWP amount as
238 well). (2) The cloud field gets more and more inhomogeneous with a broad range of CLWPs
239 within the model grid box, which results in a greater enhancement factor and increases the
240 possibility of precipitation. That is, a large enhancement factor can make the part of cloud



241 with higher CLWPs within the grid box become more efficient in generating precipitation,
242 rather than the entire model grid.

243 It is clear that CLWP and N_c in Figure 1b are correlated with each other. In addition to
244 their natural relationships, CLWP and N_c in our retrieval method are also correlated (Dong et
245 al. 2014a and 2014b). Thus, the effect of CLWP and N_c covariance on E_{auto} is not included in
246 this study. In Figures 1c and 1d, the results are calculated using a time-interval of 5-hour for
247 the selected case on 27 July 2010. In Section 4.2, we will use these approaches to calculate
248 their statistical results for multiple time-intervals using the 19-month ARM ground-based
249 observations and retrievals.

250 4.2 Statistical result

251 For a specific time-interval, e.g. 2-hour, we estimate the shape parameter (ν) and
252 calculate E_{auto} through Eqns. (5) and (7). The PDFs of E_{auto} for both 2-hour and 5-hour
253 intervals are shown in Figures 2a-2d. The distributions of E_{auto} values calculated from
254 CLWPs with 2-hour and 5-hour intervals (Figures 2a and 2b) are similar to each other with
255 nearly the same mean values (2.95 vs. 3.16). The calculated E_{auto} values range from 1 to 10,
256 and most are less than 4 with bi-modal distributions. The average value for the 2-hour
257 interval (2.95) is smaller than that for the 5-hour window (3.16), indicating a possible
258 dependence of E_{auto} on model grid size. Because drizzle-sized drops are initiated from
259 autoconversion process, we investigate the relationship of E_{auto} and precipitation frequency,



260 which we define as the average percentage of drizzling occurrence based on radar reflectivity
261 below cloud base. The precipitation frequency (black lines in Figures 2a and 2b) within each
262 PDF bin shows an increasing trend for E_{auto} from 0 to ~ 4 , then stays relatively constant when
263 $E_{auto} > 4$, indicating that in precipitation initiation process, E_{auto} keeps increasing to a certain
264 value (~ 4) until the precipitation frequency reaches a near-steady state. Larger E_{auto} values do
265 not necessarily result in higher precipitation frequency but instead may produce more drizzle-
266 sized drops from autoconversion process when the cloud is precipitating. Therefore, the E_{auto}
267 value of 4 is a critical threshold for converting cloud droplets into drizzle drops within MBL
268 clouds.

269 The PDFs of E_{auto} calculated from N_c also share similar patterns of positive skewness and
270 peaks at ~ 1.5 - 2.0 for the 2-hour and 5-hour intervals (Figures 2c and 2d). Although the
271 average values are close to their CLWP counterparts (2.69 vs. 2.95 for 2-hr and 3.45 vs. 3.16
272 for 5-hr), the difference between 2-hour and 5-hour intervals becomes large. The precipitation
273 frequencies within each bin do not show similar slightly decreasing trend like what is shown
274 in Figures 2a and 2b. This suggests complicated effects of droplet number concentration on
275 precipitation initiation and warrants more explorations of aerosol-cloud-precipitation
276 interactions. This is very intriguing result, which suggests the existence of significant sub-
277 grid variation of N_c and this variation can significantly influence the warm rain process. As
278 mentioned in Section 2, we also fit CLWP and N_c using lognormal distributions. The



279 distributions of E_{auto} are close to Figure 2 (not shown here) with average values of 3.33 and
280 3.67, respectively, for 2-hour and 5-hour intervals.

281 The covariance of CLWP and RLWP (equivalently, q_c and q_r) is included in calculating
282 E_{accr} and the results are shown in Figures 2e and 2f. The calculated E_{accr} values range from 1
283 to 4 with mean values of 1.48 and 1.60 for 2-hour and 5-hour intervals, respectively. These
284 two mean values are much greater than the prescribed value used in GCMs (1.07 for example
285 from Morrison and Gettleman, 2008). Since accretion is the process where rain drops collect
286 cloud droplets, we superimpose the ratio of RLWP to CLWP within each bin (black lines in
287 Figures 2e and 2f) to represent the portion of rain water in the atmospheric column. This ratio
288 increases from $E_{accr}=0$ to ~ 2 , and then decreases, suggesting a possible optimal state for
289 collision-coalescence process to achieve maximum efficiency for converting cloud water into
290 rain water at $E_{accr}=2$. In other words, the conversion efficiency cannot be infinitely increased
291 with E_{accr} under fixed available cloud water. The ratios of RLWP to CLWP at $E_{accr}=1.07$ and
292 $E_{accr}=2.0$ are 0.048 and 0.119, further proving that the prescribed value of $E_{accr}=1.07$ used in
293 GCMs is too small to simulate correct precipitation intensity in the models. Therefore, we
294 suggest increasing E_{accr} from 1.07 to 1.5-2.0 in GCMs.

295 To illustrate the impact of using prescribed enhancement factors, autoconversion and
296 accretion rates are calculated using the prescribed values in GCMs (e.g., 3.2 for E_{auto} and 1.07
297 for E_{accr} , Morrison and Gettleman, 2008; Xie and Zhang, 2015) and the newly calculated ones



298 in Figure 2 that use observations and retrievals. The q_c and q_r are calculated by dividing cloud
299 or rain water content by air density from the merged sounding. Figure 3 shows the joint
300 density of autoconversion (Figures 3a and 3b) and accretion rates (Figures 3c and 3d) from
301 observations (x-axis) and model parameterizations (y-axis) for 2-hour and 5-hour intervals.
302 Despite the spread, the peaks of the joint density of autoconversion rate appear slightly above
303 the one-to-one line, suggesting that cloud droplets in the model are more easily to be
304 converted into drizzle/rain drops than observations. On the other hand, the peaks of accretion
305 rate appear slightly below the one-to-one line which indicates that simulated precipitation
306 intensities are lower than observed ones. The magnitudes of the two rates are consistent with
307 Khairoutdinov and Kogan (2000), Liu and Daum (2004), and Wood (2005b).

308 Compared to the observations, the precipitation in GCMs occurs at higher frequencies
309 with lower intensities, which might explain why the total precipitation amounts are close to
310 surface measurements over an entire grid-box. This ‘promising’ result, however, fails to
311 simulate precipitation on the right time scale and cannot capture the correct rain water
312 amount, thus providing limited information in severe weather warnings such as flash
313 flooding.

314 Clouds in an unstable boundary layer have a better chance of getting moisture supply
315 from the surface by upward motion than clouds in a stable boundary layer. Precipitation
316 frequencies are thus different in the two boundary layer regimes. For example, clouds in a



317 relatively unstable boundary layer seem easier to produce drizzle than those in a stable
318 boundary layer (Wu et al., 2017). Provided the same boundary layer condition, CLWP is an
319 important factor in determining the precipitation status of clouds. At the Azores, drizzling
320 clouds are more likely to have CLWP greater than 75 g m^{-2} than their nondrizzling
321 counterparts (Rémillard et al., 2012). To further investigate what conditions and parameters
322 can significantly influence the enhancement factors, we classify low-level clouds according
323 to their boundary layer conditions and CLWPs.

324 The averaged E_{auto} and E_{accr} values for each category are listed in Table 2. Both E_{auto} and
325 E_{accr} increase when the boundary layer becomes less stable, and these values become larger in
326 precipitating clouds ($\text{CLWP} > 75 \text{ gm}^{-2}$) than those in nonprecipitating clouds ($\text{CLWP} < 75 \text{ gm}^{-2}$).
327 In real applications, autoconversion process only occurs when q_c or cloud droplet size reaches
328 a certain threshold (e.g., Kessler, 1969 and Liu and Daum, 2004). Thus, it will not affect
329 model simulations if a valid E_{auto} is assigned to Eq. (1) in a nonprecipitating cloud. The E_{auto}
330 values in both stable and mid-stable boundary layer conditions are smaller than the prescribed
331 value of 3.2 in GCMs, while the values in unstable boundary layers are significantly larger
332 than 3.2 regardless of if they are precipitating or not. All E_{accr} values are greater than 1.07,
333 the constant used in GCMs. The E_{auto} values in Table 2 range from 2.31 to 6.17 and the E_{accr}
334 values vary from 1.4 to 1.7, depending on different boundary layer conditions and CLWPs.
335 Therefore, the selection of E_{auto} and E_{accr} values in GCMs should be regime-dependent.



336 Although the difference of E_{auto} and E_{accr} between the model and the observations exist, it
337 is difficult to vary enhancement factors for each grid box at each time step in GCM
338 simulations. Proper adjustments, however, can be made according to the model grid size,
339 boundary layer conditions, and precipitating status. As stated in the methodology, we used a
340 variety of time intervals, by assuming a 10 m s^{-1} horizontal wind, those intervals would
341 correspond to different spatial scales implying different model resolutions. Figure 4
342 demonstrates the dependence of both enhancement factors on different time intervals and
343 model grid sizes. The E_{auto} values increase from 1.79 at a grid box of $18 \times 18 \text{ km}$ to 3.11 at a
344 grid box of $108 \times 108 \text{ km}$, which are 44% and 3% percent lower than the value used in GCMs
345 (3.2, upper dashed line). After that, the E_{auto} values remain relatively constant, at around 3.15,
346 which is close to the prescribed value used in GCMs. The E_{accr} values increase from 1.25 at a
347 grid box of $18 \times 18 \text{ km}$ to 1.53 at a grid box of $108 \times 108 \text{ km}$, those are 17% and 43%,
348 respectively, larger than the value used in GCMs (1.07, lower dashed line). These results
349 suggest that the current GCMs should increase their prescribed E_{accr} value by 43% in their
350 simulations of precipitation within a grid box of $1^\circ \times 1^\circ$.

351 It is noted that E_{auto} and E_{accr} depart from GCM prescribed values at opposite directions as
352 model grid size increases. For models with finer resolutions (e.g., 18 km or 54 km), both E_{auto}
353 and E_{accr} are significantly different from the values in GCMs, which can partially explain the
354 issue of ‘too frequent’ and ‘too light’ precipitation. Under both conditions, the accuracy of



355 precipitation estimation is degraded. For models with coarser resolutions (e.g., 144 km or 180
356 km), E_{auto} is close to 3.2 while E_{accr} is much larger than 1.07 when compared to finer
357 resolution simulations. In such situations, the simulated precipitation will be dominated by
358 the ‘too light’ problem, in addition to regime-dependent (Table 2), E_{auto} and E_{accr} should be
359 also scale-dependent.

360 Also note that the location we choose to collect ground-based observations and retrievals
361 is on the remote ocean where the MBL clouds mainly form in a relatively stable boundary
362 layer and are characterized by high precipitation frequency. Even in such environments,
363 however, the GCMs overestimate the precipitation frequency (Ahlgriim and Forbes, 2014).
364 In an environment where boundary layer structures are more complicated and precipitation
365 events occur less often, the continental US for example, using the fixed E_{auto} value would
366 cause much larger errors than those that occur over the Azores. Therefore, for simulations
367 over continents we suggest using E_{auto} values that are even smaller than what is suggested in
368 Figure 4.

369 To further investigate how enhancement factors affect precipitation simulations, we use
370 E_{auto} as a fixed value of 3.2 in Eq. (4), and then calculate the CLWPs needed for models to
371 reach the same autoconversion rate as observations. The CLWP differences between models
372 and observations are representing the amount of liquid water needed by models to adjust for
373 getting a realistic autoconversion rate in the simulations. Similar to Figure 1, the PDFs of



374 CLWP differences (model – observation) are plotted in Figures 5a and 5b for 2-hour and 5-
375 hour intervals. Figure 5c shows the average percentages of model CLWP adjustments for all
376 time intervals, which corresponds to different model grid sizes. The mode and average values
377 for both time intervals are negative, suggesting that models need to simulate lower CLWPs in
378 general to get reasonable autoconversion rates. Lower CLWPs are usually associate with
379 smaller E_{auto} values that induce lower simulated precipitation frequency. On average, the
380 percentage of CLWP adjustments decrease with increasing model grid size. For example, the
381 adjustments for finer resolutions (e.g., 18 – 54 km) can be more than 20% of the cloud water,
382 whereas adjustments in coarse resolution models (e.g., 144 – 180 km) are relatively small
383 because the prescribed E_{auto} (=3.2) is close to the values from observations (Figure 4). The
384 adjustment method presented in Figure 5 however, changes cloud water substantially and
385 may cause variety of subsequent issues, such as altering cloud radiative effects and disrupting
386 the hydrological cycle. The assessment we do in Figure 5 only provides a reference to the
387 equivalent effect on cloud water by using the prescribed E_{auto} value in GCMs as compared to
388 those from observations.

389 All above discussions are based on the prescribed E_{auto} and E_{acccr} values (3.2 and 1.07) in
390 GCMs and WRF from Morrison and Gettelman (2008). Whereas there are quite a few
391 parameterizations that have been published so far, in this study, we list E_{auto} and E_{acccr} for
392 three widely used parameterization schemes in Table 3, which are given only for 2-hour and



393 5-hour intervals. The values of the exponent in each scheme directly affect the values of the
394 enhancement factors. For example, the Beheng (1994) scheme has highest degree of
395 nonlinearity and hence has the largest enhancement factors. The Liu and Daum (2004)
396 scheme is very similar to the Khairoutdinov and Kogan (2000) scheme because both schemes
397 have a physically realistic dependence on cloud water content and number concentration
398 (Wood, 2005b). For a detailed overview and discussion of various existing parameterizations,
399 please refer to Liu and Daum (2004), Liu et al. (2006a), Liu et al. (2004b) and Wood (2005b).

400 **5. Summary**

401 To better understand the influence of sub-grid cloud variations on the warm-rain process
402 simulations in GCMs, we investigated the warm-rain parameterizations of autoconversion
403 (E_{auto}) and accretion (E_{accr}) enhancement factors. These two factors represent the effects of
404 sub-grid cloud and precipitation variabilities when parameterizing autoconversion and
405 accretion rates as functions of grid-mean quantities. In current GCMs, E_{auto} and E_{accr} are
406 prescribed as 3.2 and 1.07, respectively, in the widely used Morrison and Gettleman (2008)
407 scheme. To assess the dependence of the two parameters on sub-grid scale variabilities, we
408 used ground-based observations and retrievals collected at DOE ARM Azores site to
409 reconstruct the two enhancement factors in a variety of time intervals and different model
410 grid sizes.



411 The calculated E_{auto} values from observations and retrievals increase from 1.79 at a grid
412 box of 18×18 km to 3.15 at a grid box of 108×108 km. These values are 44% and 3% lower
413 than the prescribed value of 3.2 in Morrison and Gettleman (2008) scheme. On the other
414 hand, the E_{accr} values increase from 1.25 at a grid box of 18×18 km to 1.53 at a grid box of
415 108×108 km, which are 17% and 43% higher than the prescribed value (1.07). The much
416 higher E_{auto} and lower E_{accr} prescribed in GCMs help to explain why most produce too
417 frequent precipitation events with a precipitation intensity that is too light. The ratios of rain
418 to cloud liquid water increase with increasing E_{accr} from 0 to 2, and then decrease after that,
419 suggesting a possible optimal state for the collision-coalescence process to achieve maximum
420 efficiency for converting cloud water into rain water at $E_{accr}=2$. The ratios of RLWP to
421 CLWP at $E_{accr}=1.07$ and $E_{accr}=2.0$ are 0.048 and 0.119, further proving that the prescribed
422 value of $E_{accr}=1.07$ used in GCMs is too small to simulate correct precipitation intensity in
423 models.

424 To further investigate what conditions and parameters can significantly influence the
425 enhancement factors, we classified low-level clouds according to their boundary layer
426 conditions and CLWPs. Both E_{auto} and E_{accr} increase when the boundary layer conditions
427 become less stable, and the values are larger in precipitating clouds ($CLWP > 75 \text{ gm}^{-2}$) than
428 those in nonprecipitating clouds ($CLWP < 75 \text{ gm}^{-2}$). The E_{auto} values in both stable and mid-
429 stable boundary layer conditions are smaller than the prescribed value of 3.2 used in GCMs,



430 while those values in unstable boundary layers conditions are significantly larger than 3.2
431 regardless of whether or not the cloud is precipitating. All E_{accr} values are greater than the
432 prescribed value of 1.07 used in GCMs. Therefore, the selection of E_{auto} and E_{accr} values in
433 GCMs should be regime-dependent.

434 This study, however, did not include the effect of uncertainties in GCM simulated cloud
435 and precipitation properties on sub-grid scale variations. For example, we did not consider
436 the behavior of the two enhancement factors under different aerosol regimes, a condition
437 which may affect precipitation formation process. In addition, other factors may also affect
438 precipitation frequency and intensity even under the same aerosol regimes and even if the
439 clouds have similar cloud water contents. Wind shear, for example as presented in Wu et al.
440 (2017), is an external variable that can affect precipitation formation. Further studies are
441 needed to evaluate the role of the covariance of q_c and N_c in sub-grid scales on E_{auto}
442 determinations, which is beyond the scope of this study and requires independent retrieval
443 techniques.

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454

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647 **Table 1. The parameters of autoconversion and accretion formulations for four**
 648 **parameterizations.**
 649

	A	a_1	a_2	B	b
Khairoutdinov and Kogan (2000)	1350	2.47	-1.79	67	1.15
	$1.3 \times 10\beta_6^6$,				
	where $\beta_6^6 = [(r_v + 3)/r_v]^2$,				
Liu and Daum (2004)	r_v is mean volume radius.	3	-1	N/A	N/A
	modification was made by Wood (2005b)				
Tripoli and Cotton (1980)	3268	7/3	-1/3	1	1
Beheng (1994)	3×10^{34} for $N_c < 200 \text{ cm}^{-3}$ 9.9 for $N_c > 200 \text{ cm}^{-3}$	4.7	-3.3	1	1

650



651 **Table 2. Autoconversion (left) and accretion (right) enhancement factors in different**
652 **boundary layer conditions (LTS > 18 K for stable, LTS < 13.5 K for unstable and LTS**
653 **within 13.5 and 18 K for mid-stable) and in different LWP regimes (LWP ≤ 75 g m⁻² for**
654 **non-precipitating and LWP > 75 g m⁻² for precipitating).**

655

LTS (K)	LWP ≤ 75 g m ⁻²	LWP > 75 g m ⁻²
> 18	2.31/1.40	2.58/1.49
(13.5, 18)	2.56/1.43	2.98/1.63
< 13.5	4.15/1.51	6.17/1.70

656

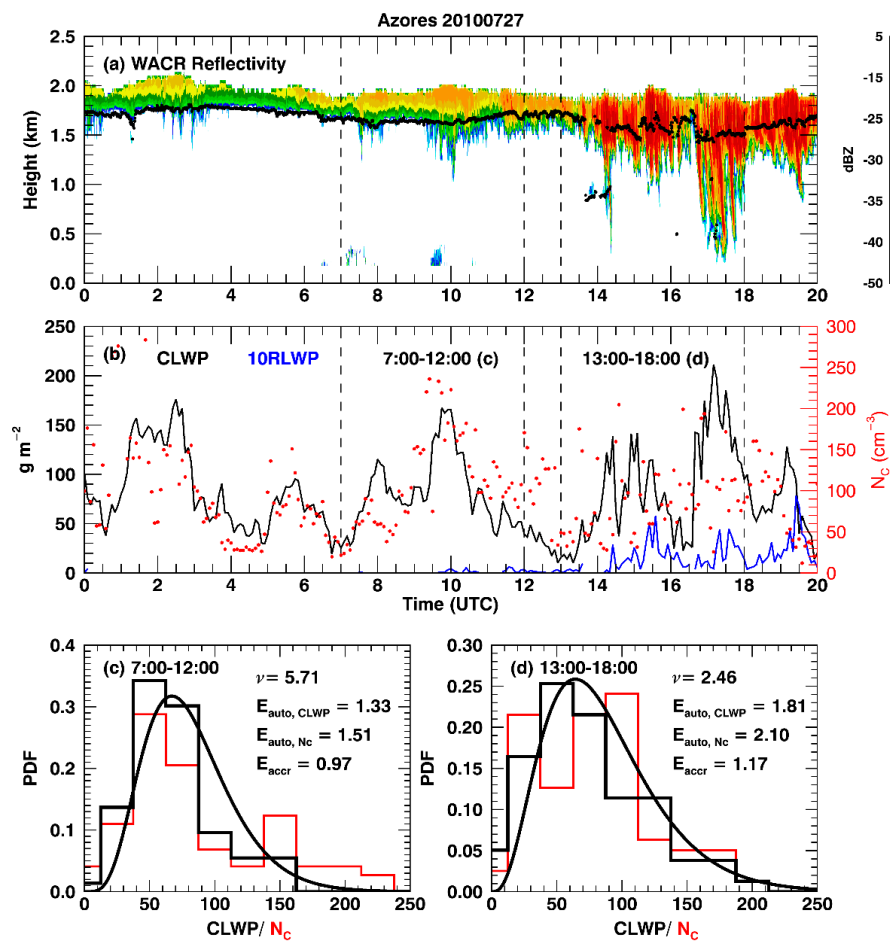


657 **Table 3. Autoconversion and accretion enhancement factors (E_{auto} and E_{accr}) for the**
658 **parameterizations in Table 1 except the Khairoutdinov and Kogan (2000) scheme. The**
659 **values 2-hr and 5-hr interval averages.**

660

	E_{auto}		E_{accr}	
	2-hour	5-hour	2-hour	5-hour
Liu and Daum (2004)	3.76	4.20	N/A	N/A
Tripoli and Cotton (1980)	2.55	2.71	1.25	1.31
Beheng (1994)	6.73	5.00	1.25	1.31

661



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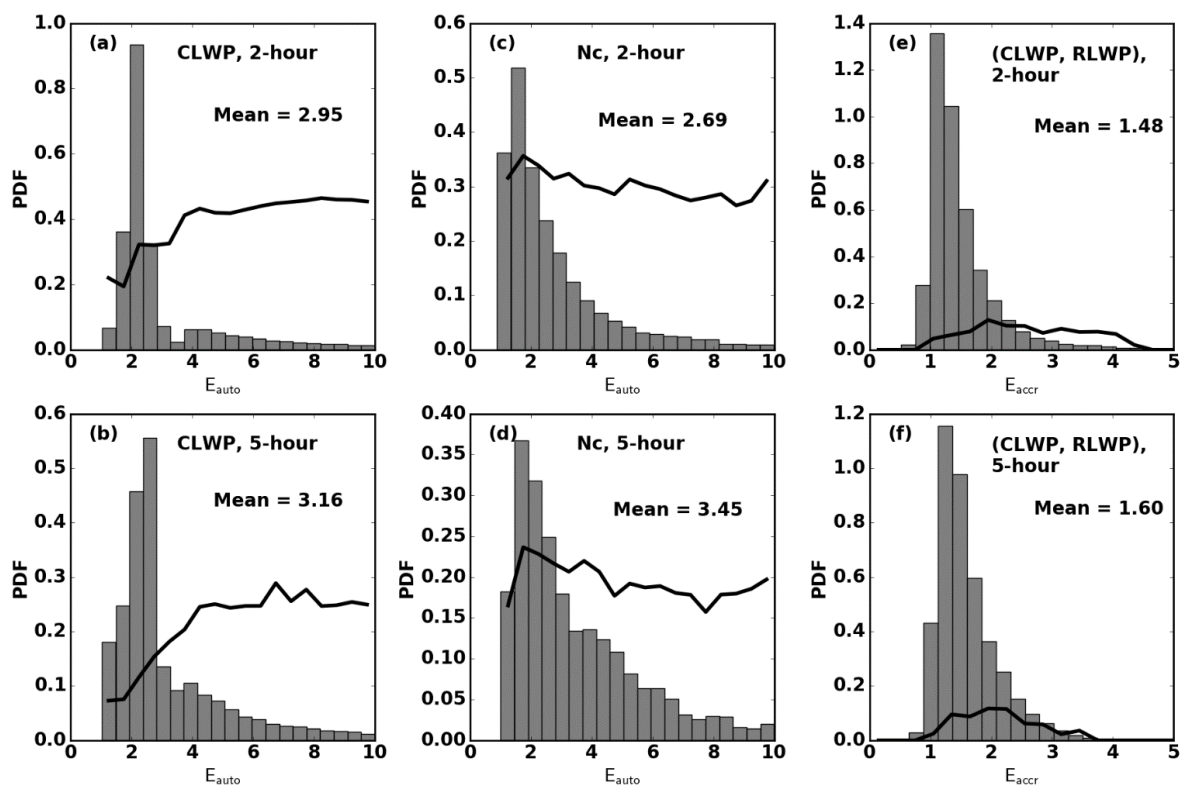
663 **Figure 1. Observations and retrievals over Azores on 27 July 2010. (a) W-band ARM**
 664 **cloud radar (WACR) reflectivity (contour) superimposed with cloud-base height (black**
 665 **dots). (b) Cloud and rain ($\times 10$) liquid water path (CLWP in black and 10RLWP in**
 666 **blue), red dots are the retrieved cloud droplet number concentration (N_c). Dashed lines**
 667 **represent two time periods with similar mean-CLWP but different distributions as**
 668 **shown by black step lines in (c) and (d). Black curved lines in (c) and (d) are fitted**
 669 **gamma distributions with the corresponding shape parameter (ν) shown on the upper**
 670 **right. Red step lines show N_c distributions. The calculated autoconversion ($E_{\text{auto, CLWP}}$**
 671 **from CLWP and $E_{\text{auto, Nc}}$ from N_c) and accretion (E_{accr}) enhancement factors are also**
 672 **shown.**

673



674

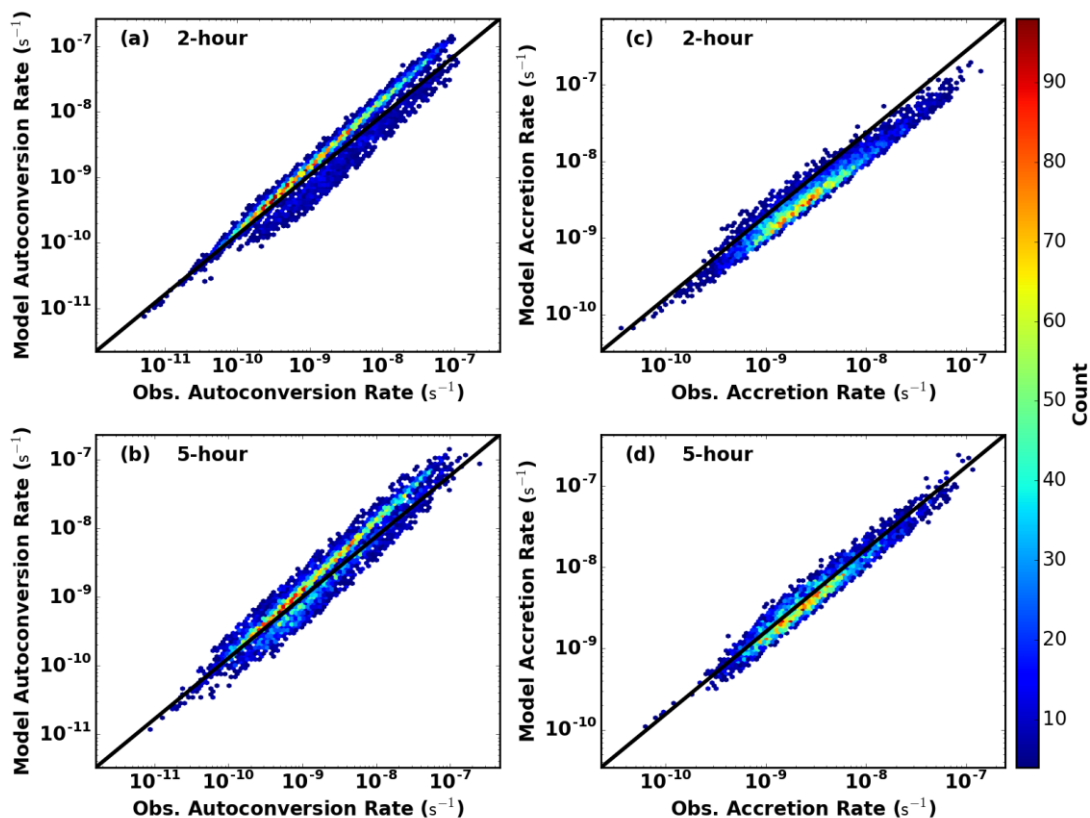
675



676

677 **Figure 2. Probability density functions (PDFs) of autoconversion (a - d) and accretion (e**
678 **- f) enhancement factors calculated from CLWP (a-b), N_c (c-d), and the covariance of**
679 **CLWP and rain LWP (RLWP) (e-f). First two rows show the results from 2-hr and 5-hr**
680 **intervals, respectively, with their average values. Black lines represent precipitation**
681 **frequency in each bin in (a)-(d) and the ratio of RLWP to CLWP in (e)-(f).**

682



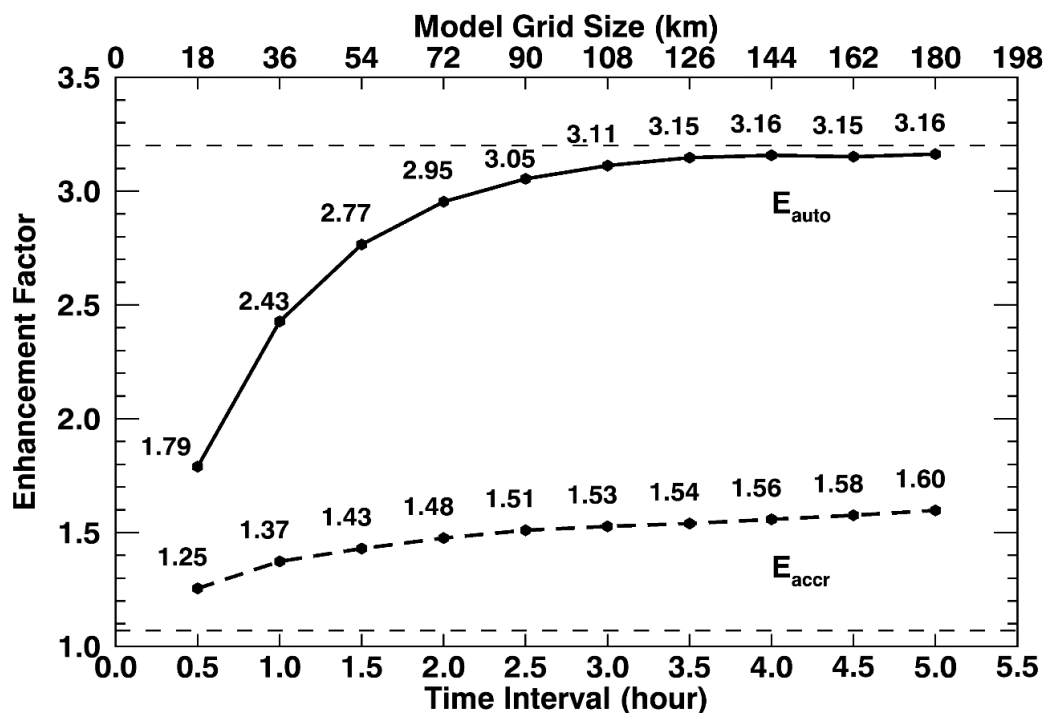
683

684 **Figure 3. Comparison of autoconversion (a-b) and accretion (c-d) rates derived from**
685 **observations (x-axis) and from model (y-axis). Results are for 2-hr (a and c) and**
686 **5-hr intervals. Colored dots represent joint number densities.**

687



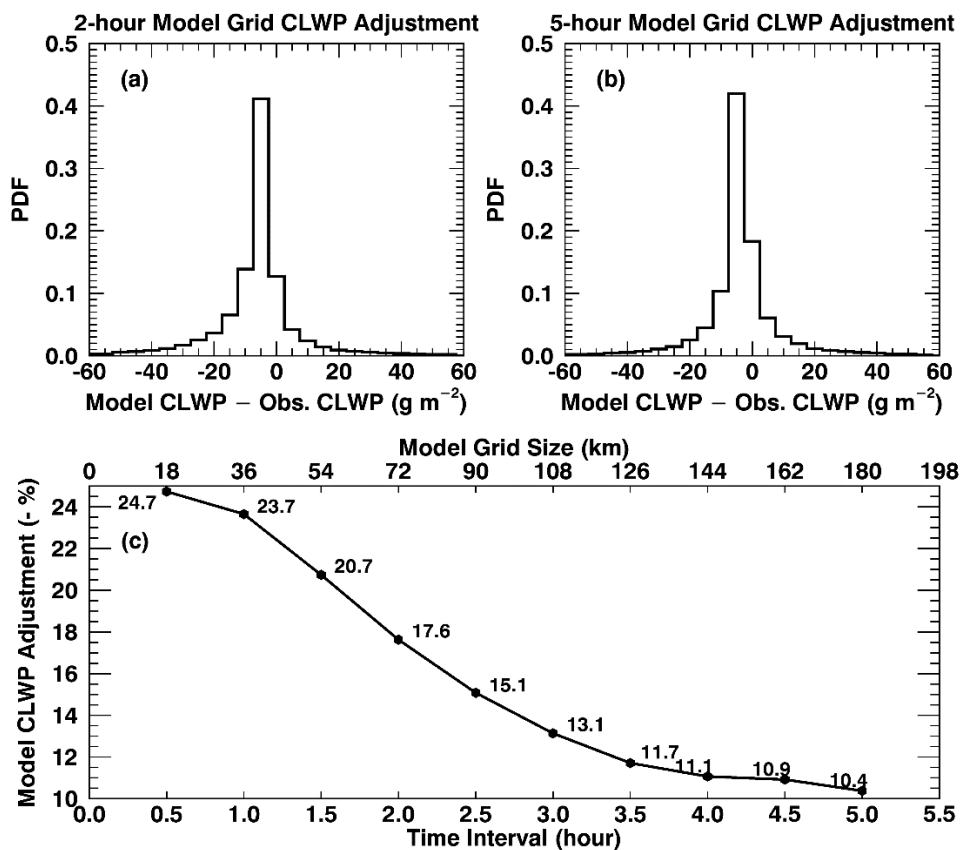
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689

690 **Figure 4.** Autoconversion (solid dot line) and accretion (dashed dot line) enhancement
691 factors as a function of time interval (of surface observations). The model grid box sizes
692 on the top X-axis are calculated using a horizontal wind of 10 m s^{-1} . The two dashed
693 lines show the constant values of autoconversion (3.2) and accretion (1.07) enhancement
694 factors used in GCMs.

695



696

697 **Figure 5. CLWPs needed for models to adjust to reach the same autoconversion rate as**
698 **observations for (a) 2-hour and (b) 5-hour intervals. Positive biases represent increased**
699 **CLWPs required in models and negative biases mean decreased CLWPs. The average**
700 **percentages of adjustments for different model grid sizes are shown in panel (c) and**
701 **note that the percentages in the vertical axis are negative.**