Thanks to the referee for very helpful comments, which have allowed us to clarify and improve the manuscript. Below we address the reviewer' comments, with the original comments in black, and our response in blue. We have revised the manuscript accordingly. All changes made to the manuscript have been marked with Track-Change tool in one of submitted files.

Anonymous Referee #1

Review of "H2SO4-H2O-NH3 ternary ion-mediated nucleation (TIMN): Kinetic-based model and comparison with CLOUD measurements" by F. Yu et al. The manuscript presents a kinetic, quasi-unary molecular cluster and aerosol particle

model to simulate ternary ion-mediated nucleation (TIMN) from sulfuric acid (H₂SO₄), water (H₂O) and ammonia (NH₃). This work extends the previously developed binary H₂SO₄-H₂O (BIMN) model (Yu, 2006b) to include also ammonia. This is done by using quantum chemical data for some H₂SO₄-H₂O-NH₃ molecular clusters (some of which have been previously published by the authors, and some of which are new but not yet published) and previously measured experimental thermodynamic data for bulk solutions, and implementing them in the model. Model results for the formation rate J_{1.7} of nanoparticles of 1.7 nm are compared to rates derived from particle measurements at the CLOUD aerosol chamber.

The manuscript is fairly clearly written and suits in the scope of ACP. However, the model details need further clarification, and some assumptions and approximations made in the model require justification and/or more discussion. Also, discussion of the results with respect to experiments and other nucleation parameterizations or models needs to be more balanced. After the authors have addressed these issues (as listed in detail below), the study can be considered for publication in ACP.

We appreciate the time and effort of the referee in providing the detailed comments. Please see below for our point-to-point replies and clarifications.

Specific comments:

The most important issues regarding the model can be summarized as follows: The authors claim to present "the first comprehensive kinetically-based H₂SO₄-H₂O-NH₃ ternary ion-mediated nucleation (TIMN) model that is based on the thermodynamic data derived from both quantum-chemical calculations and laboratory measurements."

However, it turns out that the model is in fact quasi-unary, i.e. approximates the multicompound chemical system as a one-compound system. Also, the quantum-chemical data is rather sparse, liquid thermodynamic data is used from quite small nanoparticle sizes onward, and the rest of the thermodynamics is in practice guessed by connecting quantum chemical and bulk data by an exponential function.

These facts and the related uncertainties should be clearly brought up and discussed. Considering the roughness of some approximations, the suggestion that the model is in excellent agreement with CLOUD data needs much more comparisons and more than a few data points from CLOUD.

We feel that the referee probably misunderstood the TIMN model. As shown in Figures 1 and 3 and discussed in the text, the model is multicomponent and does not approximate multicomponent systems by one-component system. First of all, the distributions of small clusters of variable chemical composition were explicitly calculated (Figure 3) as a function of T, RH, and [NH₃]. Secondly, the compositions of neutral, positively charged and negatively charged clusters studied here are different. Thirdly, the model explicitly accounts for the formation and properties of both binary and ternary clusters and the interactions between neutral and charged clusters.

As for the amount of quantum-chemical data used to constrain the model, the TIMN model is constrained by largest amount of QC data available at the present time that was obtained using PW91PW91/6-311++G(3df,3pd) method. We have pointed out clearly in the manuscript that since the formation of small clusters is the limiting step for nucleation, improving nucleation thermodynamics by applying QC data is critically important. While extrapolation may lead to possible uncertainties which has been clearly acknowledged in the original manuscript, this approach provides nucleation thermochemistry of much better quality than conventional bulk liquid/capillarity approximation, which fails to predict free energies and formation rates of small molecular clusters, and is innovative in terms of connecting thermochemical properties of QC data for small binary and ternary clusters that cannot be adequately described by the capillarity approximation. In order to address the Reviewer's concern, additional discussion on uncertainties associated with the interpolation has been added to the revised manuscript.

As for the comparison with CLOUD data, Figures 6 & 7 show clearly that we have compared our model predictions with 48 data points from CLOUD measurement in the original manuscript. The comparisons include the dependences of nucleation rates on all the key parameters controlling nucleation rates: [NH₃], ion production rate, [H₂SO₄], temperature, and RH. In order to address the Reviewer's concern, we have made additional comparisons with CLOUD data and included them in the revised manuscript.

Thermodynamic data

The thermodynamic input data includes quantum chemical (QC) data for the very smallest clusters of a few molecules. Particles containing more than at least ten sulfuric acid molecules are assumed to behave according to the electrically neutral macroscopic liquid droplet model. For the intermediate sizes below ten H₂SO₄ molecules, QC data and liquid data are connected together by a type of exponential function.

(1) In general, it would be extremely helpful to explain the thermodynamic data in the form of a table which lists the different cluster / particle compositions and sizes, and the approaches used for their Gibbs free energies. It's much easier and faster for the reader than finding the information in the text.

Agreed. QC data are already in the form of a table (see Tables 2-4).

Quantum chemical (QC) data for small molecular clusters

The QC data has been obtained using the PW91PW91/6-311++G(3df,3pd) density functional theory (DFT) method. PW91 is a commonly used DFT method in atmospheric cluster calculations, and it has been shown to yield mean errors similar to (although somewhat higher than) other common DFT methods in QC benchmarking studies (e.g. Elm and Kristensen, 2017).

In terms of the number of sulfuric acid molecules, which is the principal building block of the clusters and particles in the presented kinetic model, the used QC data covers cluster sizes up to (a) 1 sulfuric acid molecule for positively charged, (b) 4 for negatively charged (5 if the bisulfate ion is counted in), and (c) 4 for electrically neutral clusters. (2) Page 5, line 152: "The thermodynamic data sets used for binary clusters were also updated." For which clusters were the data updated: All or just some of them? What kind of differences are there compared to the previously published data for these clusters?

We have meant that the scheme to calculate the evaporation rates of binary clusters has been updated. In the previous IMN model (Yu, ACP, 2006), the evaporation rates of binary clusters were calculated with an equation considering the Thomson effect and dipole-charge interaction

(Eq. 14 in Yu (2006)). The present TIMN uses quite different approach to calculate the evaporation rates, as detailed in the text. In order to avoid confusion, this sentence has been deleted.

(3) Page 9, line 250: "We have extended the earlier QC studies of binary and ternary clusters to larger sizes."

Which sizes? Please indicate clearly which clusters are new, and which have been studied in previous publications. Also, list clearly the clusters for which QC data is applied (instead of other type of thermodynamic data). Are these the clusters listed in Tables 2-4?

Yes, these are clusters listed in Tables 2-4. The data from earlier studies and experimental data are properly marked, and notes describing their origin are given below the tables.

(4) Page 9, lines 254-255: The authors have used also a "locally developed sampling code, which creates a 'mesh' around the cluster, in which molecules being attached to the cluster are the mesh nodes", but this sentence is all that is said about the code. Please elaborate what this code exactly does, and give a reference, if possible.

The code is based on the following principle: mesh, with molecule to be added to the cluster placed in the mesh nodes, is created around the cluster, and blind search algorithm is used to generate the guess geometries. The mesh density and orientation of molecules are variable, as well as the minimum distance between molecules and cluster. We have added this elaboration to the revised manuscript.

(5) Page 10, lines 289-292: "Both the absolute values and trends in _G0+w derived from calculations are in agreement with the laboratory measurements within the uncertainty range of _1-2 kcal mol-1 for both QC calculations and measurements. This confirms the efficiency and precision of QC methods in calculating thermodynamic data needed for the development of nucleation models." _1-2 kcal mol-1 can be expected to be the general uncertainty of quantum chemical methods. However, as the Gibbs free energies are incorporated in the exponential factor of the evaporation rate (Eq. (7)), this uncertainty may propagate to an uncertainty of up to orders of magnitude in the particle formation rates and concentrations. This is discussed and demonstrated e.g. by Kürten at al. (2016), who estimated the uncertainties in the modeled particle formation rates by increasing or decreasing all Gibbs free energies by 1 kcal mol-1. Depending on the conditions, this changes the formation rate by less than an order of magnitude, or even by up to several orders of magnitude. Please discuss also the sensitivity of the particle kinetics to the evaporation rates, and

the impact of the uncertainties in _G on the formation rate.

We agree with the referee that the uncertainties in computed free energies of 1-2 kcal mol⁻¹ may lead to large uncertainties in particle formation rates under some conditions. However, uncertainties estimated by Kürten at al. (2016) represent the upper limit because estimates of Kürten at al. (2016) do not consider the error cancellation. In reality there probably does not exist such a thing as a systematic error of plus or minus 1 kcal mol⁻¹ assigned to each step of the cluster formation, because computed free energies may be overestimated for some clusters and underpredicted for others that leads to partial or, in some case, full error cancelation. In order to make it clear, we have added discussion on these matters in the revised manuscript.

(6) Page 11, lines 321-322: "Since positively charged H₂SO₄ dimers are expected to contain large number of water molecules, no quantum chemical data for these clusters are available."

What does this mean? Does it mean that the data cannot be computed at all, or that

the authors haven't computed such data in these studies?

This means that neither the authors nor other groups have computed these clusters. While it is hypothetically possible to compute them, no one has it done so far. Here the most difficult part is the adequate configurational sampling because the number of conformers is growing quickly with increasing hydration number and cluster size. We have modified the sentence to make it clear.

(7) Page 12, lines 348-351: "Table 3 shows that the presence of NH₃ in H₂SO₄ clusters suppress hydration and that _G₀₊w for S₂A₂ falls below -2.0 kcal mol-1. This is consistent with earlier studies by our group and others showing that large S_nA_n clusters (n>2) are not hydrated under typical atmospheric conditions." Please give references for these studies, especially for those conducted by other groups. Does this mean that all clusters and nanoparticles larger than (H₂SO₄)₂(NH₃)₂ are generally not hydrated, or do the particles become hydrated again at some larger size? At which size? What is assumed about the hydration of electrically neutral H₂SO₄-NH₃ clusters beyond the quantum chemistry data set, i.e. larger than (H₂SO₄)₄(NH₃)₅?

Generally, the hydration of a specific cluster (S₂A₂) tells nothing about the hydration of other clusters with different numbers of acid and base molecules. Therefore, it should be stated here that neglecting water in the larger clusters is just an assumption that has to be made due to the lack of thermodynamic data (as the authors have actually done later on line 454).

We have added references to the relevant studies in the revised manuscript:

- Henschel, H., Navarro, J. C. A., Yli-Juuti, T., Kupiainen-Määttä, O., Olenius, T., Ortega, I. K., ... & Vehkamäki, H. (2014). Hydration of atmospherically relevant molecular clusters: Computational chemistry and classical thermodynamics. *The Journal of Physical Chemistry* A, *118*(14), 2599-2611.
- Henschel, H., Kurtén, T., & Vehkamäki, H. (2016). Computational study on the effect of hydration on new particle formation in the sulfuric acid/ammonia and sulfuric acid/dimethylamine systems. *The Journal of Physical Chemistry A*, *120*(11), 1886-1896.
- Herb, J., Nadykto, A. B., & Yu, F. (2011). Large ternary hydrogen-bonded pre-nucleation clusters in the Earth's atmosphere. *Chemical Physics Letters*, *518*, 7-14.

We agree with the Referee that the hydration of a specific cluster (S2A2) tells nothing about the hydration of other clusters with different numbers of acid and base molecules, and that neglecting water in the larger clusters is just an assumption that has to be made due to the lack of thermodynamic data. We have pointed this out in the revised manuscript. However, it is also important to note that the recent study by Henschel, H., Kurtén, T., & Vehkamäki, H. (2016) confirms our conclusion. In particular, Fig. 3 in their study shows clearly that in the case of fairly large cluster consisting of $3 H_2SO_4$ and $3 NH_3$ molecules, the average hydration number is less than 0.7 even if RH=100%.

(8) Page 12, lines 365-367: "This finding is fully consistent with the laboratory measurements showing that growth of neutral S_sA_a clusters follows s = a pathway (Schobesberger et al., 2015)."

The study by Schobesberger et al. (2015) does not present any measurement data for neutral clusters. (Instead, they are modeled by the ACDC program in that study.) Please correct the sentence.

Corrected.

(9) Page 13, lines 389-393: "_Go +s values for S-S₃₋₄W_w are consistently 1.5-3

kcal mol-1 less negative than the corresponding semi-experimental estimates (Table 4). The possible reasons behind the observed systematic difference are yet to be identified and include the use of low-level ab initio HF method to compute reaction enthalpies and uncertainties in experimental enthalpies in studies by Froyd and Lovejoy (2003)."

The computed values for $_G_{0+W}$ (as well as for $_G_{0+W}$ for some positive clusters), on the other hand, are more negative than those determined by Froyd and Lovejoy (2003). Why doesn't the discussed systematic difference apply to these values?

Yes, it's applicable to all the relevant comparisons. Another important issue is that there exist multiple sources of uncertainties in the data sets of Froyd and Lovejoy (2003). First of all, the data sets for both positively and negatively charged clusters are not strictly experimental. While in the case of negative clusters, the low level ab initio is used to get the final semi-experimental energy values, in the case of positive ions, a theoretical thermochemical cycle is applied. The accuracy of these "experimental" data are pretty much unknown; however, these data sets are currently the only ones that report some sort of experimental values for negative and positive clusters of sulfuric acid with water and, thus, we had no choice other than to compare computed data with these particular data sets.

(10) Page 15, lines 471-472: "In the TIMN model, the equilibrium distributions are used to calculate number concentrations weighted stepwise Gibbs free energy change" Where is this averaged _G used in the model? Doesn't the model use averaged evaporation frequencies (Eq. (10)), which are calculated over the individual evaporation rates and thus do not correspond to the averaged _G?

The mode actually uses the averaged $\overline{\Delta G_{s-1,s}}$ to calculate averaged evaporation rates. To avoid confusion, we have modified Eq. (10) (Eq. 12 in the revised manuscript).

(11) Page 15, lines 477-479: "In the atmosphere, where substantial nucleation is observed, the sizes of critical clusters are generally small (s <_ 5-10) and nucleation rates are largely controlled by the stability (or) of small clusters with s <_ 5 - 10." Please give references for this.

The number of H_2SO_4 molecules in critical clusters has been estimated from $d(\ln J)/d(\ln[H_2SO_4])$. A reference (Sipilä et al., Science, 2010) is now added.

(12) Table 2 and discussion on pages 17-19: For positively charged clusters, there is QC data only up to clusters containing one H₂SO₄ molecule and two NH₃ molecules. That is, not even the first growth step with respect to H₂SO₄ clustering (i.e. the formation of a H₂SO₄ dimer) is covered, and in practice all the data for positive clusters is guessed by using Eq. (11) (except for clusters containing more than 10 acid molecules, starting from which data for electrically neutral bulk solutions is used also for the positive clusters).

This is an extremely crude approximation. Please bring up this fact, and explain what new "insights" we can learn about the thermodynamics of these clusters by using these type of data.

We agree with the referee that the QC data for positively charged clusters are very limited and the interpolation approximation is subject to large uncertainty. In order for the nucleation on

positive ions to occur, the first step is for H₂SO₄ to attach to a positive ion that does not contain H₂SO₄. Unlike negative ions, the effect of charge on the bonding of H₂SO₄ with positive ions is much weaker and thus the stepwise Gibbs free energy change for the addition of one H₂SO₄ molecule to form a positively charged cluster is likely to be similar to that of neutral clusters, i.e., decreasing with cluster size. Therefore, the QC data for positively charged clusters containing one H₂SO₄ molecule provides a critical constrain. The success of the model in predicting the [NH₃] needed for nucleation on positive ions to occur (Fig. 6) show the usefulness of the first step data and approximation. Nevertheless, we agree with the referee about the uncertainty and bring up the fact of the lack of thermodynamic data for positive ions in the revised manuscript.

(13) Page 17, lines 536-538: Similarly to positive clusters, the results for the thermodynamics of negative clusters raise some questions: "The effect of NH₃ on negative ions becomes important at s _____4, when bonding between the clusters and NH₃ becomes strong enough to contaminate a large fraction of binary clusters with ammonia (Fig.3)." No QC data or experimental bulk data is used for the clusters around sizes s _____4 – 9. Considering that this behavior is deduced by interpolating between QC data for small clusters that take up ammonia rather weakly, and macroscopic solution data for an electrically neutral H₂SO4-H₂O-NH₃ liquid, it is difficult to see this result as very reliable. Please state that the thermodynamics of these clusters are highly uncertain (or explain why they would not be).

The interpolation is more than likely a reasonable approximation for negatively charged clusters with s=4-9, as indirectly confirmed by the success of our model in predicting the observed dependence of nucleation rates on [H₂SO₄] and [NH₃] (Figs. 6 and7). Please note that in many conditions where nucleation is significant, $s<=\sim4$ and the uncertainty associated with the interpolation is small. We agree that further experimental or QC study will be helpful to reduce the uncertainty and have empathized this in the revised manuscript.

(14) Table 4: The hydrate data for the negatively charged clusters is quite sparse for some clusters. Why are not hydrates with more water molecules considered for, for example, $S-S_1$ or $S-S_2$?

The hydration of these clusters is weak and, thus, does not impact the cluster formation because none of them are hydrated under typical atmospheric conditions (see refs. below).

Herb, J., Xu, Y., Yu, F., & Nadykto, A. B. (2012). Large hydrogen-bonded pre-nucleation (HSO₄⁻)(H₂SO₄)_m(H₂O)_k and (HSO₄⁻)(NH₃)(H₂SO₄)_m(H₂O)_k clusters in the Earth's atmosphere. The Journal of Physical Chemistry A, 117(1), 133-152.

Nadykto, A. B., Yu, F., & Herb, J. (2008). Towards understanding the sign preference in binary atmospheric nucleation. Physical Chemistry Chemical Physics, 10(47), 7073-7078.

(15) Tables 2-4: Why isn't all QC data that is used in the model given in the tables? For example, binary electrically neutral clusters are not included in Table 3. Please indicate clearly where these data can be found.

To keep the manuscript concise, we choose not to repeat results already published unless really necessary. We have provided references for the binary neutral clusters.

Nadykto, A. B., Al Natsheh, A., Yu, F., Mikkelsen, K. V., & Herb, J. (2008). Computational quantum chemistry: A new approach to atmospheric nucleation. Advances in quantum chemistry, 55, 449-478.

Herb, Jason, Alexey B. Nadykto, and Fangqun Yu. "Large ternary hydrogen-bonded prenucleation clusters in the Earth's atmosphere." Chemical Physics Letters 518 (2011): 7-14.

(16) Figure 3: Why are some hydrates with different numbers of water molecules grouped together? For instance, (H₂SO₄)₂(H₂O)₁₋₇ is presented as one bar; this doesn't tell much about the hydration as 1 and 7 are quite different numbers. Also, in panel (d), please clarify that there is no hydrate data for these clusters; otherwise the figure panel might be understood so that the clusters don't take up water at all.

We group together some clusters with different numbers of water molecules to make the figure more clear and neat. We have clarified it in the figure caption for panel (d) as suggested by the Reviewer.

(17) Figure 4: Why is the cumulative Gibbs free energy zero for the first growth steps of the negative clusters in panel (b)? In panel (a), it does not look like these values add up to zero, but should be negative instead.

 $\Delta G_{s-1,s}$ for small negatively charged clusters are strongly negative, implying that their formation is barrierless. However, these small clusters cannot be considered as nucleated particles because $\overline{\Delta G}_{s-1,s}$ can become positive for larger clusters due to the charge effect decreasing quickly as the clusters are growing The negative $\overline{\Delta G}_{s-1,s}$ for small clusters is not able to cancel the positive $\overline{\Delta G}_{s-1,s}$ for larger clusters and thus $\overline{\Delta G}_{s-1,s}$ for small clusters are set to zero when they are negative in the cumulative Gibbs free energy calculation.

(18) Caption of Figure 4: "Calculations were carried out at T=292 K, RH=38%, $[H_2SO_4]=3x108$ cm-3 and $[NH_3]= 0.3$ ppb." How were the vapor concentrations, e.g. $[H_2SO_4]$, used in the calculations?

P in Eq. (12) (Eq. 11 in the revised manuscript).

Experimental bulk data for larger nanoparticles

Bulk thermodynamic data is assumed for particles of all charging states containing at least ten H₂SO₄ molecules. While this is in practice the only available option due to the lack of other type of data, the approximation calls for some discussion about the related uncertainties.

(19) At which conditions (temperature, partial pressures of the H₂SO₄, NH₃, H₂O vapors) were the measurements (Marti et al., 1997; Hyvärinen et al., 2005) performed? How reliably can it be extrapolated to different conditions outside the measurement range?

The conditions of the measurements are given and possible uncertainties are discussed in the revised manuscript.

(20) Page 16, lines 487-491: "Based on experimental data (Kebarle et al., 1967; Davidson et al., 1977; Wlodek et al., 1980; Holland and Castleman, 1982; Froyd and Lovejoy, 2003), the stepwise _G values for clusters decreases exponentially as the cluster sizes increase and approaches to the bulk values when clusters containing more than _8-10 molecules (Yu, 2005)."

Is possible size-dependent chemical composition, i.e. acid:base molar ratio, considered here (e.g. Chen et al., 2018)? How does it affect the model results?

This is a general statement about the decrease of stepwise ΔG with the size of charged clusters. The possible size-dependent chemical position may be taken into account implicitly through the interpolation as the compositions of small clusters are different from those of large (s>10) clusters. Please see reply to comment #13 for the discussion concerning impacts of on our model results.

(21) Page 16, lines 491-494: "Cluster compositions measured with an atmospheric pressure interface time-of-flight (APi-TOF) mass spectrometer during CLOUD experiments also show that the chemical effect of charge-carrying becomes unimportant when the cluster contains more than 9 H₂SO₄ molecules (Schobesberger et al., 2015)." In the study by Schobesberger et al. (2015), it looks like the different charges approach similar composition somewhere in the size range where the H₂SO₄ content is _20-100 molecules (Figure 9 in the study). At 10 H₂SO₄ molecules, the composition of negative and positive particles is still different. Please comment.

Figure 9 of Schobesberger et al. (2015) shows that the difference in the composition of positively and negatively charged clusters quickly decreases as number of H_2SO_4 molecules increases from 1 to ~ 10 and exhibits little further changes. It is true that at 10 H_2SO_4 molecules, the composition of negative and positive particles is still different but the difference is much smaller than that in the case of small clusters. We have pointed this out in the revised manuscript.

(22) Page 17, line 524: "consistent with the laboratory measurements (Marti et al., 1997)" Isn't the discussed _G data derived from these measurements (i.e. naturally, it is consistent)? Please clarify.

Yes. The sentence has been modified to make it clear.

Page 24, lines 774-776: Is this the correct reference?

This is a wrong reference. Thank you for pointing this out. The correct one is: Hyvärinen, A., T. Raatikainen, A. Laaksonen, Y. Viisanen, and H. Lihavainen, Surface tensions and densities of H₂SO₄ + NH₃ + water solutions, Geophy. Res. Lett., 32, L16806, doi:10.1029/2005GL023268, 2005.

Approximated values for intermediate sizes with < 10 H₂SO₄ molecules

(23) Eq. (11): What is this "extrapolation" formula based on? It is not clear why this functional form would be suitable for connecting QC and bulk measurements. Please explain clearly how the formula is derived, and discuss the related uncertainties.

Linear and exponential extrapolations are two common methods for this type of application. We choose exponential extrapolation as it fits better the stepwise ΔG change of neutral clusters that QC data are available. The related uncertainties are discussed in the revised manuscript.

(24) Page 16, lines 503-506: "c in Eq. (11) is the exponential coefficient that determines how fast _Gs-1,s approaches to bulk values as s increases. In the present study, c is estimated from _Gs-1,s at s=2 and s=3 for neutral binary and ternary cluster for which experimental (Hanson and Lovejoy, 2006; Kazil et al., 2007) or quantum-chemical data (Table 3) are available."
What can the data for clusters that contain 2 or 3 H2SO4 molecules possibly tell about how fast _G approaches bulk values?
Is c estimated based on QC data, experimental data, or both? How is this done exactly? Is it only for neutral clusters, or also for charged clusters?

It's an approximation. See our reply to comment 23 above. In the present model, we estimated *c* based on QC data of neutral clusters. We acknowledge that the extrapolation approximation is subject to uncertainty but this is the best approach we can come up with at this point in order to develop a model that can be applied to all conditions. Further QC and experimental studies of the thermodynamics of larger clusters can help to reduce the uncertainty.

(25) Finally, the most important issue regarding the thermodynamics is the fact that the "critical sizes", i.e. the barriers for nucleation, are located around cluster sizes for which there is no reliable thermodynamic data (Figure 4). For all different types of clusters (binary, ternary, all charging states), the maximum of the free energy curve is beyond the QC data (or just at the upper limit of the QC data in the case of negative ternary clusters). That is, the critical stage of nucleation is based on Eq. (11), which in turn does not seem to be based on an actual physical model. Considering this, can the model really give important new information on H₂SO₄-H₂O-NH₃ particle formation mechanisms?

The maximum of the free energy curve shown in Fig. 4b is the accumulative free energy change and the maximum value (or nucleation barrier) is dominated by smaller clusters (Fig. 4a). In other words, the formation of small clusters are limiting steps and the uncertainty of stepwise ΔG for larger clusters where QC data are not available has limited impact on the predicted nucleation rate. As demonstrated in the paper, the model reveals the general favor of nucleation of negative ions, followed by nucleation on positive ions and neutral nucleation, for which higher NH₃ concentrations are needed, in excellent agreement with CLOUD measurements. The usefulness of the model can be seen from its success in reproducing the observed dependence of nucleation rates on various parameters and its ability to calculate nucleation rates under conditions for which measurements are not available.

Kinetic model

(26) In the kinetic model, the clusters are assumed to be in equilibrium with respect to both water and ammonia. Such equilibriation assumption can be made if the time scales of the attachment and evaporation processes of some compound are substantially shorter than those of other compounds. This is the case for water, as (a) its concentration (to which the attachment, i.e. molecular collision, frequency is directly proportional) is around _10 orders of magnitude higher than that of H2SO4 or NH3, and (b) its binding to the clusters is so much weaker that its evaporation rate is _ several orders of magnitude higher than that of other compounds (except for some charged clusters in e.g. Table 2).

This is, however, generally not the case for ammonia. The binding of NH₃ depends strongly on the cluster composition: Depending on the acid:base ratio, either NH₃ or H₂SO₄ evaporates much faster than the other. Within the set of small clusters, the weakest and strongest bindings of NH₃ are of the same order as those of H₂SO₄ (e.g. Table 3). The collision rates of NH₃ are not necessarily multiple times higher than those of H₂SO₄, either: While ammonia is generally more abundant than H₂SO₄ in the atmosphere, there are environments where [H₂SO₄] and [NH₃] are around the same order (such as some of those simulated in this study).

Due to these reasons, the explanation for assuming equilibrium with respect to NH₃ is not justifiable (pages 13-14, lines 414-418): "In the lower troposphere, where most of the nucleation events were observed, [H₂SO₄] is typically at sub-ppt to ppt level, while [NH₃] is in the range of sub-ppb to ppb levels. This means that small ternary clusters can be considered to be in equilibrium with H₂O and NH₃ vapors."

(a) Doesn't ammonia need to also evaporate much faster from the clusters for the equilibrium assumption to be justified? (b) At the simulated conditions, [H₂SO₄] and [NH₃] are in many cases of the same order. For instance, in Figure 6 at the lower end of the [NH₃] axis, [NH₃] is of the same order or even lower than [H₂SO₄]. In Figure

7a, [NH3] is around 10 ppt, i.e. _ 108 cm-3, and [H2SO4] is around 107. . . 109 cm-3.

Please show that the equilibrium with respect to NH_3 really is a valid assumption for these simulation systems.

For the equilibrium assumption to be justified, the collision rate of clusters with NH₃ should be substantially higher than that with H₂SO₄. The evaporation rate of NH₃ depends on the composition of the cluster and can be very fast when NH₃:H₂SO₄ ratio are above one for small clusters. In many atmospheric conditions, especially in lower troposphere, [NH₃] is generally a few orders of magnitude higher than [H₂SO₄] and equilibrium assumption should be reasonable. For practical applications, nucleation rates are generally predicted based on the assumption that the clusters are in equilibrium and nucleation rates reach the steady state. Please note that the nucleation rates measured in CLOUD are also steady state values.

We agree with the Referee that the system may deviate from equilibrium if $[NH_3]$ is less than or close to $[H_2SO_4]$. Under such cases, the equilibrium assumption may overestimate nucleation rates. We have added discussion on these matters in the revised manuscript.

(27) Some other aspects of the model also need clarification. The kinetic equations (Eqs.(1-6)) seem to include also collisions between charged clusters / particles of the same polarity. How high are the rate constants for such processes? Doesn't electrostatic repulsion prevent these attachments? Further, if multiply charged particles can form in these collisions, how are these different charge numbers treated in the model? Shouldn't there be separate equations for particles that contain a single charge, two charges, three, and so on?

Yes, the electrostatic repulsion is too strong for small clusters to gain more than one charge. However, small charged clusters can be scavenged by large pre-existing particles of same polarity. Large pre-existing particles serve as the sink for small clusters in the model and the effect of multiple charge is small and thus is not tracked.

(28) Page 5, lines 162-166: "The initial negative ions, which are normally assumed to be NO-3, are converted into HSO-4 core ions (i.e., S-) and, then, to larger H2SO4 clusters in the presence of gaseous H2SO4. The initial positive ions H+Ww are converted into H+A1-2Ww in the presence of NH3, H+SsWw in the presence of H2SO4, or H+AaSsWw in the case, when both NH3 and H2SO4 are present in the nucleating vapors." What are the rate constants for the conversions of NO-3 and H+Ww?

This is a general statement of ion clustering process in the atmosphere when nucleation occurs. In the model we assume the starting negative ion is HSO_4^- . The rate constant for the conversion of initial positive ions to the one containing H_2SO_4 is ~ $2x10^{-9}$ cm³s⁻¹.

What does $H_{+}A_{1-2}W_w$ (or $H_{+}S_sW_w$ and $H_{+}A_aS_sW_w$) mean, i.e. how many ammonia and water molecules does it contain?

It's a general expression of cluster formula. As given in the Figure 1 caption, S, W, and A represent sulfuric acid (H_2SO_4), water (H_2O), and ammonia (NH_3) respectively, while *s*, *w*, and *a* refer to the number of S, W, and A molecules in the clusters/droplets, respectively.

In the equations (page 7, lines 192-193), " $N_{+,-0}$ and Q are the concentration of initial ions not containing H₂SO₄ and the ionization rate, respectively" What do the "initial ions" refer to, e.g. H+Ww or H+A1-2Ww? NO-3 or HSO-4?

Initial positive ions include both H^+W_w and $H^+A_{1-2}W_w$ (in equilibrium). Negative initial ion is HSO_4^- .

(29) Eq. (3): Why does the evaporation term for creating H₂SO₄ monomers from a dimer includes a factor of two (_j,2), but the corresponding collision term, removing monomers in the collision creating a dimer, does not?

Evaporation of one dimer generates two monomers. For the corresponding collision term (monomer with monomer), a factor of two (in loss) cancels the double count of collisions among monomers.

(30) Page 8, lines 212-213: "The methods for calculating _, , _, and _ for binary H2SO4-H2O clusters have been described in detail in Yu (2006b)." I was not able to find the descriptions for _, _, and _ in the given reference; the paper only seems to re-direct the reader to discussion in 3 other papers. Please briefly summarize how these parameters are obtained.

We have added additional references and a brief description.

(31) Page 8, lines 221-222: "No is the number concentration of H₂SO₄ at a given T under the reference vapor pressure P of 1 atm." Isn't No simply the number concentration corresponding to the reference pressure P of the QC calculations? What does it have to do with any [H₂SO₄]? In general, the evaporation rate should not be related to the concentration of any compound, as it does not depend on the composition of surrounding vapor (only on the temperature, i.e. the inert gas).

The referee is correct that the evaporation rate should not be related to the concentration of any compound. N° in the equation will be cancelled out with the N° in $\Delta G_{i-1,i}$. Details of the

derivation and relationship can be found in the reference given (i.e., Yu, 2007). Please note that we have corrected a missed term in Eq. (8).

(32) Page 8, lines 223-225: "The temperature dependence of $_H_o$ and $_S_o$, which is generally small and typically negligible over the temperature range of interest, was not considered." Can you give a reference for the negligible temperature dependence?

The conclusion is based on typical calculated ΔC_p , which largely controls the temperature dependence of ΔH and ΔS (see A.B. Nadykto et al. / Chemical Physics 360 (2009) 67–73 and references therein) and does not exceed a few tens of cal/mol/K in most cases studied here. The reference is added to the revised text.

(33) Page 19, lines 572-573: "mean evaporation rate (⁻) of an H₂SO₄ molecule" Is it assumed that only a single H₂SO₄ molecule evaporates, i.e. no water ligands, for instance, are attached to it? If so, please discuss the validity of this assumption, or even better, average the evaporation rates over all evaporation pathways with different numbers of other compounds attached to the acid molecule.

Yes, the present model assumes only a single H_2SO_4 molecule evaporates. This is likely the dominant evaporation pathway. We have pointed this out in the revised manuscript.

(34) Page 19, lines 573-574: "The shapes of $\bar{}$ curves are similar to those of $\bar{}_{Gs-1,s}$ (Fig. 4a) as $\bar{}$ values are largely controlled by $\bar{}_{Gs-1,s}$." How is $\bar{}$ related to the averaged values $\bar{}_{Gs-1,s}$? Isn't $\bar{}$ calculated based on individual values $\bar{}_{Gs-1,s}$ (Eq. (10)), i.e. not exactly equivalent to $\bar{}_{Gs-1,s}$?

Please see our reply to comment #10.

(35) The discussion on page 19, lines 575-584, feels somewhat confusing: First it's said that the effect of ammonia is significant for larger clusters and of less importance for small clusters (e.g. "the binding of NH₃ to small neutral and charged clusters are weaker compared to that for larger clusters"), but after this it's concluded that "The nucleation rates, limited by formation of small clusters (s <_ 5), depend strongly on the stability or evaporation rate of these small clusters and, thus, on [NH₃]."

While the binding of NH₃ to small neutral and charged clusters is weaker compared to that to larger clusters, small clusters containing NH₃ are much more stable than those without (Fig. 4) and thus ammonia is important for nucleation. We have clarified this in the revised manuscript.

(36) Page 19, line 588: "the concentrations of clusters of all sizes are explicitly predicted" A quasi-unary model cannot be called "explicit"; please re-formulate.

Please see our reply to the general comments in the beginning. To address the Reviewer's concern, we have deleted the word "explicitly" from the sentence.

(37) Eq. (13): Is it so that only growth through H_2SO_4 vapor is taken into account in the calculation of the particle formation rate? What about the effects of coagulation and recombination?

The quantity J that can be deduced from measurements -and that also is the relevant quantity for atmospheric modeling- includes all processes through which particles form, not only monomer condensation and evaporation. Therefore, these should be included also in the model-based formation rate.

For the chemical system considered in the present study, generally $N_1 >> N_2 >> N_3 \dots$ As a result, H_2SO_4 vapor growth dominates the steady state flux crossing 1.7 nm.

(38) Figure 1: The figure is confusing, and using patterns to fill the lines or spheres makes it somewhat difficult to read. For instance, it looks like "Condensation" means that electrically neutral clusters are ionized into charged particles (the arrows lead only to the charged blocks), and that "Coagulation / Scavenging" means that positively charged particles attached to each other or neutral particles. What is the difference between "Coagulation / Scavenging" and "Coagulation"?

We were trying to use "Scavenging" to represent the removal of small clusters by large preexisting particles, also through coagulation. Condensation is actually implied in the green arrows. To avoid the confusion, we have deleted words "Condensation" and "Scavenging".

Results and discussion

(39) As a general comment, the description of the model should be a bit less ambitious. As one-compound discrete-sectional kinetic models have existed at least since the 1970s, the model cannot be considered "first", nor is it exactly "comprehensive" or "accurate" due to the quasi-unary assumption.

The addition of NH₃ to the previous BIMN model does not make the model very new, either, as it means simply using different thermodynamic data in an existing model - and the main author has also previously published a modeling study entitled "Effect of ammonia on new particle formation: A kinetic H₂SO₄-H₂O-NH₃ nucleation model constrained by laboratory measurements" (Yu, 2006a). Besides, as the authors themselves also bring up, the kinetics of H₂SO₄-H₂O-NH₃ molecular clusters including the different charging states have been previously modeled e.g. by the ACDC program

(which the authors quite extensively criticize).

To address the Reviewer's concern, we have removed "first" and "accurate". For the reasons we gave in our reply to the general comments in the beginning, we think the present model is quite comprehensive.

(40) As previously (e.g. Nadykto et al., 2011; Nadykto et al., 2014), the main criticism is targeted at the modeling work by University of Helsinki (and this time also at the particle formation rate parameterization CLOUDpara based on the experimental data from the CLOUD chamber). In general, the authors criticize the ACDC model; however, the output of a clustering model is determined by the input parameters, namely the thermodynamic data. The ACDC program does not use any specific QC data, but the data is instead given by the user.

The ACDC data presented by Kürten et al. (2016) results from QC thermochemistry calculated with the RI-CC2/aug-cc-pV(T+d)Z//B3LYP/CBSB7 method. Therefore, the authors should call this rather e.g. "RI-CC2//B3LYP" data than "ACDC" data. The RI-CC2//B3LYP method is known to have a tendency to over-predict cluster stability, as has been discussed for example by the Helsinki group (e.g. Kupiainen-Määttä et al., 2015; Myllys et al., 2016), and thus it is not much used anymore in QC calculations.

The over-predictions of the thermochemical stability of nucleating clusters by RI-CC2//B3LYP used in ACDC code was actually first pointed out by Nadykto et al. (2014) and discussed by Nadykto et al. (2015) and Kupiainen-Määttä et al. (2015). We agree with the Reviewer that ACDC program can use other types of QC data, however, the data obtained using ACDC we were referring to in the paper are based on RI-CC2//B3LYP thermochemistry. In order to address the Reviewer's concern, we have replace "ACDC data" with "ACDC predictions based on nucleation thermochemistry obtained using RI-CC2//B3LYP method".

(41) Page 4, lines 122-123: "ACDC is also an acid–base reaction model, with the largest clusters containing 4-5 acid and 4-5 base molecules (no water molecules)": This is not the case, as ACDC is simply a program that solves the kinetic equations (similar to Eqs. (1-6)) for a given set of molecular clusters using given thermodynamic input data, which does not need to involve acids or bases. It is not limited to some fixed specific largest cluster sizes; in the cited studies, the largest sizes were determined by the availability of QC data for the systems of interest.

We have deleted this sentence.

(42) Page 4, lines 127-130: "In ACDC, the nucleation rate is calculated as the rate of clusters growing larger than the upper bounds of the simulated system (i.e., clusters containing 4 or 5 H₂SO₄ molecules) (Kurten et al., 2016) and thus may over-predict nucleation rates when critical clusters contain more than 5 H₂SO₄ molecules." It is of course not reasonable to model a system where the critical size region is outside the system boundaries. Thus, this region should be examined before simulating given conditions, as also discussed in the study by Olenius et al. (2013).

The second half of the sentence has been deleted.

(43) Page 4, lines 130-132: "All clusters simulated by the ACDC model do not contain H₂O molecules and the effect of relative humidity (RH) on nucleation thermochemistry is neglected." Page 21, lines 645-646: "an important influence of RH on nucleation rates (which is neglected in both the CLOUDpara and ACDC models)" The authors of the present manuscript are well aware of the fact that water can be included in the ACDC model: in fact, the effect of cluster hydration was recently the topic of a rather heated discussion between these authors and the researchers at University of Helsinki (Nadykto et al., 2014; Kupiainen-Määttä et al., 2015; Nadykto

et al., 2015; in this case, the question was about H2SO4-dimethylamine clusters), including i.a. ACDC simulations conducted as a function of RH. Hydration can naturally be included in a kinetic model, such as ACDC, given that there is thermodynamic input data for clusters containing water. Please correct your claims about this. The effect of water in the H2SO4-H2O-NH3 system has been studied by ACDC e.g. by Henschel et al. (2016).

In view of the information the Reviewer provided us with, we have deleted this sentence.

(44) Also the particle formation rate parameterization by Dunne et al. (2016) is criticized. It would be fair to note that the deviations of the parameterization from the CLOUD data are not a new finding, as the uncertainties and weaknesses of the parameterization are discussed rather extensively in the work by Dunne et al. (e.g. supplementary Figures S3-S6).

We don't feel it is a criticism. We meant to point out the limitation of previous results which we aim to address in the present study.

(45) Page 11, line 333-334: "most of these studies, except for Nadykto and Yu (2007), did not consider the impact of H₂O on cluster thermodynamics" The effect of H₂O on H₂SO₄-NH₃ clusters containing up to three H₂SO₄ and three NH₃ molecules has been considered by Henschel et al. (2014; 2016).

Thanks for the information. We have updated the discussion on this.

(46) Page 13, lines 396-397: The sentence "The binding of the second NH₃ to S-S₃A to form S-S₃A₂ is much weaker than that of the first NH₃ molecule. This indicates that most of S-A_a can only contain one NH₃ molecule" isn't clear: How does the binding of NH₃ to a cluster containing 3 H₂SO₄ molecules indicate something about the attachment of NH₃ to a bisulfate ion S-?

It's a typo. Should be S⁻S₃A_a. Corrected.

(47) Comparisons to CLOUD data (Figures 6 and 7): Many of the comparisons look quite nice indeed. However, more experimental data over a wider range of conditions should be shown to support the claim that the model is "in excellent agreement with CLOUD measurements".

For instance, in the work by Kürten et al. (2016) on CLOUD-based J1.7, the model used in the study (ACDC with input thermodynamics computed with the RICC2//B3LYP method) is at some conditions in excellent agreement with CLOUD data, and at some conditions there are significant differences.

Therefore, comparisons with CLOUD data should be shown for **a large set of data**, for example the figures of the study by Kürten et al. (2016), including also electrically neutral cases and a wider range of ammonia concentrations.

We have extended the comparison with CLOUD data, including the neutral cases.

(48) Figure 6: The original CLOUD data includes also J1.7 for experiments with no ions. Please add these electrically neutral experimental and model data to the figure. It looks like the slope of the modeled J1.7 is quite steep when neutral nucleation takes over; it is interesting to see how this compares with the measurements.

Neutral cases without ions are now included and discussed.

(49) Figure 7, top panel: For most lines, there are only 3 experimental data points, which doesn't make the comparison of these data to the model lines very strong. As

there is so much CLOUD data available, please pick more representative data from e.g. the work by Kürten et al. (2016). Especially low but still non-negligible ammonia mixing ratios are not shown in the current comparisons. If the model is said to cover "a wide range of atmospheric conditions", these should be included.

To be comparable, [NH₃] and T should be the same for each line, which limits the number of experimental points. We have extended the comparison with CLOUD data in separate figures.

Technical comments:

(50) Change all occurrences of "physio-chemical" to "physico-chemical"; presumably "physio" refers to physiology, not physics.

Done. Thanks for pointing these out.

(51) Page 2, line 35: Change "specie" to "species".

Done.

(52) Page 9, lines 240-245: The sentence "In earlier studies, this method has been applied to a large variety of atmospherically-relevant clusters and has been shown to be well suited to study the ones, (...)" is clumsy (i.e. what does "the ones" refer to?); please re-formulate.

Changed "the ones" to "the H2SO4-H2O and H2SO4-H2O-NH3 clusters".

(53) Page 9, line 253: Change "basin hoping" to "basin hopping".

Done.

(54) Page 11, line 332: It is misleading to list Kürten et al. (2015) as a computational study, as it doesn't present any computationally obtained thermodynamics.

We have changed Kürten et al. (2015) to Kürten et al. (2007) and added it in the reference list.

(55) Page 16, line 505: Change "cluster" to "clusters".

Done.

(56) Table 1: Please give units for the energy quantities. Please also clarify that "H" and "S" may refer to either the energetics, or the cluster composition (the first column), or use different symbols for some of the abbreviations / quantities. Also change "based" in the footnote to "based on".

That's a good point. Instead of using abbreviations, we keep the original words in the table. Units are now given in the table.

"based" in the footnote of Table 2 has been changed to "based on".

(57) The resolution and/or clarity of some figures, mainly 1 and 3, is rather poor. Please fix this.

Fixed.