

1 **Quantifying the effect of aerosol on vertical velocity and effective terminal**
2 **velocity in warm convective clouds**

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10 **Abstract**

11 Better representation of cloud–aerosol interactions is crucial for an improved
12 understanding of natural and anthropogenic effects on climate. Recent studies have
13 shown that the overall aerosol effect on warm convective clouds is non-monotonic.
14 Here, we reduce the system’s dimensions to its center of gravity (COG), enabling
15 distillation and simplification of the overall trend and its temporal evolution. Within
16 the COG framework, we show that the aerosol effects are nicely reflected by the
17 interplay of the system's characteristic vertical velocities, namely the updraft (w) and
18 the effective terminal velocity (η). The system's vertical velocities can be regarded as
19 a sensitive measure for the evolution of the overall trends with time. Using bin-
20 microphysics cloud-scale model, we analyze and follow the trends of the aerosol
21 effect on the magnitude and timing of w and η , and therefore the overall vertical COG
22 velocity. Large eddy simulation model runs are used to upscale the analyzed trends to
23 the cloud-field scale and study how the aerosol effects on temporal evolution of the
24 field’s thermodynamic properties are reflected by the interplay between the two
25 velocities. Our results suggest that aerosol effects on air vertical motion and droplet
26 mobility imply an effect on the way in which water is distributed along the
27 atmospheric column. Moreover, the interplay between w and η predicts the overall
28 trend of the field's thermodynamic instability. These factors have an important effect
29 on the local energy balance.

30

31 **1. Introduction**

32 Clouds are key players in the Earth's climate system via their influence on the energy
33 balance (Baker and Peter, 2008;Trenberth et al., 2009) and hydrological cycle. Of all
34 of the anthropogenic effects on climate, aerosol's effect on clouds remains one of the
35 most uncertain (Boucher et al., 2013). In warm clouds, aerosol act as cloud
36 condensation nuclei (CCN) around which droplets can form, and therefore aerosol
37 amount and properties determine the initial number of droplets and their size
38 distribution (Squires, 1958;Rosenfeld and Lensky, 1998;Andreae et al., 2004;Koren et
39 al., 2005). The initial droplet concentration affects cloud dynamics via microphysical
40 and dynamical feedback throughout their lifetime. For example, the onset of
41 significant collision events between droplets in polluted clouds (which are initially
42 smaller and more numerous than in clean clouds (Squires, 1958)) is delayed (Gunn
43 and Phillips, 1957;Rosenfeld, 1999, 2000;Squires, 1958;Warner, 1968). This delay
44 can have opposing effects on cloud development by increasing both the water loading
45 (which reduces cloud buoyancy and vertical development) and the latent heat release
46 resulting from the longer and more efficient condensation (increasing cloud buoyancy
47 and vertical development) (Dagan et al., 2015a;Dagan et al., 2015b;Pinsky et al.,
48 2013;Koren et al., 2014). We note that often, these opposing effects act at different
49 stages of the cloud's lifetime, further complicating the prediction of overall trends.

50 Vertical velocities (w) are among the key processes driving convective clouds. The
51 intensity, duration and characteristic size of the updrafts determine the convective
52 clouds' properties. In addition, the clouds' vertical velocity affects the distribution of
53 water along the atmospheric column, thereby having a strong effect on radiation
54 (Koren et al., 2010) and heat balance (Khain et al., 2005). Although previous studies
55 have focused on deep convective clouds, these effects are expected to be significant in
56 warm convective clouds as well. Moreover, warm processes serve as the initial and
57 boundary conditions for mixed-phase processes in deep convective clouds, and
58 therefore gaining a better process understanding of the warm phase is essential for
59 understanding the deeper systems (Chen et al., 2017).

60 The system has another characteristic velocity that measures droplet mobility. This
61 velocity, defined as the effective terminal velocity (η), measures the weighted-by-
62 mass terminal velocity of all hydrometeors within a given volume and therefore

63 defines the falling velocity of the volume's center of gravity (COG) (Koren et al.,
64 2009;Koren et al., 2015) compared to the air vertical velocity. Smaller droplets imply
65 smaller $|\eta|$ (higher mobility) and therefore less deviation from the surrounding air
66 movement. Since η is always negative, smaller $|\eta|$ implies that per a given air updraft,
67 the collective liquid water mass will be carried up higher in the atmosphere. The
68 movement of the COG compared to the surface, defined as V_{COG} , is the vector sum of
69 the two velocities: $V_{\text{COG}} = w - |\eta|$.

70 V_{COG} has recently been shown to be a good measure for the temporal evolution of
71 thermodynamic instability in cloud fields (Dagan et al., 2016). V_{COG} represents the
72 vertical movement of liquid water, which is downward gradient of the net
73 condensation-less-evaporation profile. A negative V_{COG} implies net transport of the
74 liquid water from the cloudy layer to the sub-cloud layer. This holds true for clean
75 (low aerosol concentration) precipitating cases (Dagan et al., 2016), in which the
76 water that condenses in the cloudy layer sediments down to the sub-cloud layer where
77 it partially evaporates. The net condensation in the cloudy layer and the net
78 evaporation in the sub-cloud layer produce a decrease in the thermodynamic
79 instability with time. On the other hand, for the polluted non-precipitating cases, V_{COG}
80 is positive; indicating that the net liquid water movement is upward. The water that is
81 being condensed in the lower part of the cloudy layer is transported upward and
82 evaporates in the upper cloudy and inversion layers (Dagan et al., 2016). The end
83 result of this vertical condensation–evaporation profile is an increase in
84 thermodynamic instability with time.

85 Khain et al. (2005) used a two-dimensional cloud model with spectral (bin)
86 microphysics to study the aerosol effect on deep convective cloud dynamics. They
87 concluded that one of the reasons for comparatively low w in clean maritime
88 convective clouds compared to polluted continental ones is the rapid creation of
89 raindrops. This increases the liquid water loading in the lower part of the cloud,
90 thereby reducing buoyancy. They also claimed that the delayed raindrop production in
91 the continental cloud increases the duration of the diffusion droplet growth stage,
92 which in turn, increases the latent heat release by condensation.

93 Seigel (2014) showed an increase in w with increasing aerosol loading in the cloud
94 core in numerical simulations of a warm convective cloud field. He also showed a

95 decrease in cloud size under polluted conditions due to increased mixing between the
96 clouds and their dry environment driven by stronger evaporation of smaller droplets in
97 polluted cases.

98 It has been recently shown (Dagan et al., 2015a;Dagan et al., 2015b;Dagan et al.,
99 2017) that under given environmental conditions, warm convective clouds have an
100 optimal aerosol concentration (N_{op}) with respect to their macrophysical properties
101 (such as total mass and cloud top height) and total surface rain yield. For
102 concentrations smaller than N_{op} , the cloud can be considered as aerosol-limited
103 (Koren et al., 2014;Reutter et al., 2009), and an increase in the mean cloud properties
104 with aerosol loading can be expected due to an increase in the condensation efficiency
105 and droplet mobility (Koren et al., 2015;Dagan et al., 2015a;Dagan et al., 2017).
106 Suppressive processes such as enhanced entrainment and water loading take over
107 when the concentrations are higher than N_{op} and reverse the trend. It has also been
108 shown that the value of N_{op} depends heavily on the environmental conditions
109 (thermodynamic conditions that support deeper clouds would have a larger N_{op}).

110 In this work, a bin-microphysics cloud model and large eddy simulation (LES) of a
111 cloud field were used to explore how changes in aerosol concentration affect w and η ,
112 the interplay between them and, as a result, the height of the COG in warm convective
113 clouds (Koren et al., 2009).

114

115 **2. Methodology**

116 **2.1 Single-cloud model**

117 The Tel Aviv University axisymmetric nonhydrostatic cloud model (TAU-CM) with
118 detailed treatment of cloud microphysics (Reisin et al., 1996;Tzivion et al., 1994) was
119 used. The included warm microphysical processes were nucleation of droplets,
120 condensation and evaporation, collision–coalescence, breakup, and sedimentation.
121 The microphysical processes were formulated and solved using the method of
122 moments (Tzivion et al., 1987).

123 The background aerosol size distribution used here represents a clean maritime
124 environment (Jaenicke, 1988). The aerosols are assumed to be composed of NaCl.

125 The different aerosol concentrations (25, 500 and 10,000 cm⁻³, denoted hereafter as
126 25CCN, 500CCN and 10000CCN, respectively) and size distributions are identical to
127 those used in Dagan et al. (2015a). To study the involved processes, we used a wide
128 range of aerosol loading conditions, from extremely pristine to extremely polluted.
129 These specified three aerosol concentrations represent conditions which are below,
130 around and above the optimal aerosol concentration (N_{op}). To avoid giant CCN
131 effects, the aerosol size distribution was cut at 1 μm (Feingold et al., 1999; Yin et al.,
132 2000; Dagan et al., 2015b).

133 The model resolution was set to 50 m, in both the vertical and horizontal directions,
134 and the time step to 1 s. The initial conditions were based on theoretical atmospheric
135 profiles that describe a tropical environment (Malkus, 1958) (see profile T1RH2 in
136 Fig. 1 in Dagan et al., 2015a). They consisted of a well-mixed sub-cloud layer
137 between 0 and 1000 m, a conditionally unstable cloudy layer (6.5°C/km) between
138 1000 and 4000 m, and an overlying inversion layer (temperature gradient of 2°C over
139 50 m). The relative humidity (RH) in the cloudy (inversion) layer was 90% (30%).
140 The results presented here were examined for a few different sets of initial conditions
141 (different inversion-base heights and cloudy layer RH). Although for different initial
142 atmospheric conditions the transition between aerosol invigoration to suppression
143 occurs at different aerosol concentration (Dagan et al., 2015a), the conclusions were
144 found to be general for different sets of initial conditions.

145

146 To examine the effect of aerosols on the entire cloud, the properties presented in this
147 work are cloud mean values weighted by the liquid water mass in each grid cell.
148 Cloudy grid cells were defined as cells with liquid water content larger than 0.01 g/kg.
149 The cloud's COG (Koren et al., 2009) was calculated as:

$$COG = \frac{\sum m_i z_i}{\sum m_i} \quad (1)$$

150

151 where m_i and z_i are the mass [kg] and height [m] of voxel i , respectively.

152 The η (effective terminal velocity) was calculated according to Koren et al. (2015):

$$\eta = \frac{\sum V_{t_j} m_j n_j}{\sum m_j n_j} \quad (2)$$

153

154 where V_{t_j} , m_j and n_j are the terminal velocity [m/s], mass [kg] and concentration [cm^{-3}]
155 of droplets in bin j , respectively. This was calculated for all cloudy grid cells.

156 For being consistent with the COG point of view, the mean air vertical (w) was
157 calculated as a mean weighted by the liquid mass:

$$w = \frac{\sum m_i w_i}{\sum m_i} \quad (3)$$

158

159 The axisymmetric model uses a geometry that is only a simplification and idealization
160 of a full 3D flow and does not account, for example, for wind shear and processes
161 acting on larger scales like clouds effect on the environmental conditions with time.
162 For accounting for these processes, we used 3D cloud field scale simulations as well
163 (see Sec. 2.2 below).

164

165 **2.2 Cloud field simulations**

166 We used the System for Atmospheric Modeling (SAM) LES model (Khairoutdinov
167 and Randall, 2003) with a bin-microphysics scheme (Khain and Pokrovsky, 2004) to
168 simulate the BOMEX (Barbados Oceanographic and Meteorological EXperiment)
169 warm cumulus case study (Holland and Rasmusson, 1973; Siebesma et al., 2003). The
170 horizontal resolution was set to 100 m, the vertical resolution to 40 m. The domain
171 size was $12.8 \times 12.8 \times 4.0 \text{ km}^3$ and the time step was 1 s. We ran the model for 16 h,
172 but the statistical analysis included only the last 14 h of the simulation. We used 8
173 different aerosol concentrations: 5, 25, 50, 100, 250, 500, 2000 and 5000 cm^{-3} . Again,
174 we used a marine background aerosol size distribution (Jaenicke, 1988). Further
175 details about the simulations can be found in Dagan et al. (2017).

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180 **3. Results and discussion**

181 **3.1 Single cloud: vertical velocity and effective terminal velocity**

182 Starting from the single-cloud scale, we first followed the entire cloud mean w (eq. 3),
183 mean η (eq. 2), mean V_{COG} , and COG height (eq. 1) as a function of time for the three
184 different levels of aerosol loading (25, 500, and 10,000 cm^{-3}). From an early stage of
185 the cloud's evolution, the cleanest cloud (25CCN) had the lowest COG. This was a
186 result of the lower w (Fig. 1a) and larger absolute value of the negative η (caused by
187 the initially larger droplets – Fig. 1b), which together cause a lower V_{COG} (Fig. 1c). At
188 the early stages of the polluted clouds, the 500CCN and 10000CCN COG moved
189 upward at the same rate. After about 60 min of simulation, the 500CCN's COG started
190 to decrease while the 10000CCN's COG remained relatively high. This trend could
191 not be explained by the cloud's mean w (Fig. 1a). The 500CCN's w was higher than
192 that of the 10000CCN during the period between 50 and 63 min of simulation.
193 Without considering the effect of η on the COG, one would expect that the 500CCN's
194 COG would be higher than that of the 10000CCN. The 500CCN had lower (more
195 negative) values of η than the 10000CCN, which decreased the height of its COG
196 compared to the 10000CCN. These larger negative values of η in the 500CCN were
197 due to the rain that developed from this cloud (the rain from the 10000CCN is
198 negligible), which led to lower mobility (lower ability to move with the ambient air
199 (Koren et al., 2015)).

200 We note that the vertical change in the COG height is determined by changes in the
201 vertical distribution of water mass due to microphysical processes like condensation,
202 evaporation and removal of mass by rain (in addition to movement according to
203 V_{COG}). Hence, in some parts of the simulations the V_{COG} was not a perfect predictor of
204 the COG evolution. This is especially true when rain and evaporation are strong i.e.
205 toward the end of the clouds' lifetime.

206 Figure 1 demonstrates the importance of the aerosol effect on both w and η in
207 determining the COG height. Figure 2 presents the evolution of the clouds on the
208 phase space span by w vs. V_{COG} . All clouds began their evolution on the 1:1 line. This
209 means that at the early stages of the cloud's evolution, $\eta \sim 0$ and hence $V_{\text{COG}} \sim w$.
210 After about 40 min of simulation, the cleanest cloud's (25CCN) trajectory began to
211 deviate from the 1:1 line to the left, demonstrating an increase in $|\eta|$ and hence lower

212 droplet mobility. The deviation from the 1:1 line occurred later (at about $t = 55$ min of
213 simulation) in the more polluted simulation (500CCN), whereas for the most polluted
214 clouds (10000CCN), the lack of significant collision–coalescence and rain production
215 resulted in evolution on the 1:1 line throughout the cloud's lifetime. This delay in the
216 deviation from the 1:1 line (increasing the time for which $\eta \sim 0$) demonstrates the
217 increase in droplet mobility with aerosol loading. The longer period for which $\eta \sim 0$ in
218 the polluted cases enables the water mass to be pushed higher into the atmosphere and
219 hence (together with the increase in the air vertical velocity – Fig. 1a) to produce
220 cloud invigoration by the aerosol (Koren et al., 2015).

221

222 **3.2 LES results: aerosol effect on the vertical velocity and effective terminal** 223 **velocity in cloud fields**

224 Shifting our view from the single-cloud scale to the cloud-field scale adds another
225 layer of complexity as clouds affect the way in which the whole field's
226 thermodynamics evolve with time. Moreover, 3D simulations account for the effect of
227 wind shear. Aerosol concentration has recently been shown to determine the trend of
228 this evolution (Dagan et al., 2016;Dagan et al., 2017). Clean precipitating clouds act
229 to consume the initial instability that created them by warming the cloudy layer (in
230 which there is net condensation) and cooling the sub-cloud layer (by rain
231 evaporation). On the other hand, polluted non-precipitating clouds act to increase the
232 field's instability by cooling and moistening the upper cloudy and inversion layers.

233 Figure 3 presents the domain's mean w (in both space and time, weighted by the liquid
234 water mass to be consistent with the COG view – see eq. 3 above) vs. the domain
235 mean η . The color-coding in Fig. 3 denotes the different aerosol concentrations. In
236 agreement with previous studies (Saleeby et al., 2015;Seigel, 2014), an increase in
237 aerosol loading yielded an increase in w . In our simulations, this increase is driven by
238 larger latent heat contribution to the cloud's buoyancy due to the increased
239 condensation efficiency (Dagan et al., 2015a;Dagan et al., 2017;Koren et al.,
240 2014;Pinsky et al., 2013;Seiki and Nakajima, 2014) and thermodynamic instability
241 (Dagan et al., 2016;Dagan et al., 2017). In parallel, aerosol shifts to smaller droplets
242 (Squires, 1958) and reduces the magnitude of η , indicating better mobility of the
243 smaller droplets (Koren et al., 2015). The outcome of these two effects (that work

244 together to push the water mass higher in the atmosphere) is an increase in COG
245 height with aerosol loading (Heiblum et al., 2016b;Dagan et al., 2017).

246 In the single-cloud-scale analysis (section 3.1), we showed how the timing of the
247 evolution of the two velocities dictates the aerosol effect. Here, having many clouds in
248 the field in different stages of their lifetimes, we first analyzed the bulk properties of
249 the two velocities. With the intention of quantifying the relative contribution of the
250 aerosol effect on the mean COG height by modulating w and η , we plotted them one
251 against the other for all of the simulations that differed in aerosol loading and for all
252 clouds in the domain (Fig. 3a). For the entire simulation period, the η vs. w scatter
253 plot resulted in an almost a straight line ($R^2 = 0.96$) which was sorted by aerosol
254 concentration with a slope of 0.69. This means that an increase in aerosol
255 concentration that will result in a 1 m/s increase in mean w will drive a decrease in the
256 magnitude of $|\eta|$ by 0.69 m/s. In other words, the relative contribution to the changes
257 in the mean COG height in the domain caused by the increase in aerosol loading
258 (Heiblum et al., 2016b;Dagan et al., 2017) during the entire simulation is ~60% due to
259 changes in w and ~40% due to changes in η .

260 To include the aerosol effect on the cloud-field thermodynamic properties, we divided
261 the simulation period into three equal thirds (excluding the first 2 h, each third of a
262 period covered 4 h and 40 min). The x and * markers in Fig. 3a represent the first
263 third (2 h to 6 h 40 min into the simulation) and last third (11 h 20 min to 16 h into the
264 simulation), respectively. During the first third, the slope of w vs. η was steeper than
265 the mean over the entire simulation (slope of 0.92 with $R^2 = 0.96$); during the last
266 third, it was more gradual (slope of 0.47 with $R^2 = 0.87$). The almost 1:1 relation
267 between w and η in the first third of the simulation period suggests a comparable
268 contribution in determining the aerosol effect on mean COG height. However, the
269 relative contribution of η decreases as the simulation progresses, to about 1/3 during
270 the last third of the simulation period (compared with 2/3 of w).

271 The decrease in the w vs. η slopes toward the end of the simulations is driven by the
272 changes in the thermodynamic instability. The increase in instability under polluted
273 conditions produces an increase in mean w (Dagan et al., 2016). Nevertheless,
274 increased instability and deepening of the cloud layer are not sufficient to produce a
275 significant amount of rain under the most polluted simulations and hence, there is no

276 increase in the magnitude of η . An increase in w with no change in η is manifested as
277 a horizontal shift to the right on the η vs. w phase space (red arrow in Fig. 3a). On the
278 other hand, the decreased instability under clean conditions produces a decrease in
279 both mean w and the rain amount (Dagan et al., 2017), and therefore in $|\eta|$ (blue arrow
280 in Fig. 3a). The end result of the different changes in w and η under clean and polluted
281 conditions is a decrease in the slope of η vs. w and therefore, a decrease in the relative
282 contribution of η to the aerosol effect on the mean COG.

283

284 In Fig. 3a, the presented quantities are domain and time averages. Figure 1 showed
285 that the relative contribution of w and η to the aerosol effect on COG height strongly
286 depends on the stage of the cloud's evolution. The averaging in Fig. 3a mixes many
287 clouds at different stages in their evolution and represents the effect on the mean COG
288 in the domain. To further explore the relative contribution of the aerosol effect on w
289 and η as a function of cloud-evolution stage, we used a cloud-tracking algorithm
290 (Heiblum et al., 2016a). We identified the growing stage of the clouds as the stage for
291 which the cloud top ascends. Figure 3b presents the η vs. w phase space only for
292 clouds in their growing stage. Table 1 presents the slopes of the linear regression lines
293 for the entire simulation time and for the different thirds of the simulation period. The
294 decrease with time in the relative contribution of η compared to w to the aerosol effect
295 on COG height was also seen for the growing clouds (see the decrease in the slope
296 with time). This, again, was due to the changes in thermodynamic conditions.

297 As shown for the cloud scale, one of the most notable aerosol effects can be viewed as
298 delaying the onset of significant collection processes in the polluted clouds (Koren et
299 al., 2015), and therefore delaying the increase in $|\eta|$ values early in the cloud's
300 lifetime. Therefore, during the growing stage, the relative contribution of η was higher
301 (Fig. 3b) as compared to "all clouds" (Fig. 3a). This was demonstrated by the
302 increasing slope of the η vs. w phase space during the growing stage (Table 1).

303

304 To quantify the evolution of the thermodynamic instability with time as a function of
305 aerosol loading (on a cloud field scale), we looked at the time trends in the η vs. w
306 phase space. We defined the angle 'A' as the angle between the time trend points on

307 the η vs. w phase space per given aerosol loading (the line that connects the first and
308 last thirds of the simulation and the x-axis on the η vs. w phase space —see schematic
309 definition of A in Fig. 3b). We note that A rotates counter-clockwise with increasing
310 aerosol loading (Fig. 3a). It starts as $\sim 100^\circ$ for the cleanest simulation and
311 monotonically increases with aerosol loading to $\sim 360^\circ$ for the most polluted
312 simulations (Fig. 4b). A between 90° and 180° (as shown for clean cases—Fig. 4b)
313 represents a decrease in both w and $|\eta|$ and hence a decrease in the thermodynamic
314 instability with time. A between 270° and 360° , on the other hand (as shown for the
315 most polluted cases—Fig. 4b), represents an increase in both w and $|\eta|$ and hence an
316 increase in the thermodynamic instability with time.

317 The sign of V_{COG} has been shown to predict the evolution of thermodynamic
318 instability (Dagan et al., 2016). Thus, correlations between A and V_{COG} are expected.
319 Figure 4 presents V_{COG} (Fig. 4a) and A (Fig. 4b) as a function of the aerosol loading,
320 and V_{COG} vs. A (Fig. 4c). Figure 4a and b demonstrates that both the V_{COG} and A
321 increase monotonically with aerosol loading following a similar trend. V_{COG} and A
322 cross the 0 and 180° lines, respectively, at similar aerosol concentrations, representing
323 the transition between consumption and production of the thermodynamic instability
324 (Dagan et al., 2016). Figure 4c further demonstrates an almost perfect linear
325 correlation ($R^2 = 0.99$) between V_{COG} and A sorted by aerosol concentration.

326

327 **3.3 Summary**

328 Clouds form a complex system in which microphysical and dynamical processes are
329 tightly linked and modulated by the thermodynamic properties of the environment. In
330 turn, on the cloud-field scale, clouds affect the field's thermodynamic conditions. The
331 aerosol effect on the droplet size distribution therefore affects all of the above. Better
332 process-level understanding of aerosol effect on cloud and rain properties in the case
333 of warm convective clouds is essential for improving our understanding of the climate
334 system. In this study, our aim was to better understand and quantify the aerosol effect
335 on the air vertical velocity and droplet terminal velocity. Both characteristic vertical
336 velocities quantities modulate the distribution of water along the atmospheric column,
337 and hence affect the radiation (Koren et al., 2010) and heat balance (Khain et al.,
338 2005). The findings presented here for the single cloud and cloud field scales could be

339 used in future works to better represent cloud-aerosol interactions in coarser
340 resolution models (like climate models) as it provides a compact way to represent
341 aerosol effect on the liquid water vertical mass flux and clouds effect on the
342 thermodynamic conditions.

343 Analyzing the two characteristic velocities on the cloud scale allows separation, as a
344 first approximation, between the aerosol effects on condensation/evaporation
345 efficiencies (reflected by the magnitude of w) and those on droplet mobility (reflected
346 by the inverse magnitude of η). The magnitudes of w and η act in opposite ways, i.e.,
347 stronger w and smaller $|\eta|$ imply more efficient transport of liquid water to the upper
348 atmosphere. We use their sum, defined as V_{COG} , to estimate the overall effect on the
349 COG's vertical movement. Single-cloud analysis showed the timing of this interplay
350 and how each velocity affects the COG elevation. It showed that the invigorating
351 aerosol effect can be viewed mostly at the early stages of cloud development, when an
352 increase in aerosol loading enhances the condensation efficiency (reflected as higher
353 w levels) and delays the onset of significant collection processes (reflected as a delay
354 in the sharp increase in η). Both act to transfer liquid water higher into the atmosphere
355 (Koren et al., 2015). Later, as the cloud dissipates, the “payment” is viewed as
356 enhanced evaporation, and if the cloud manages to reach the significant collection-
357 process stage, then the surface rain is stronger (expressed as a sharp increase in $|\eta|$).

358 Similar to the single-cloud case, the cloud field (LES) results (that unlink the single
359 clouds simulations, account for 3D processes such as wind shear) demonstrated an
360 increase in w and decrease in the magnitude of η (less negative η) with aerosol
361 loading, both yielding a higher COG. We analyzed the bulk properties of the two
362 velocities for the entire simulation time (14 h) and for all clouds in the domain and
363 showed that the relative contribution of the aerosol effect on w and η in determining
364 COG evolution is comparable (60% and 40%, respectively). However, at the
365 beginning of the simulation, this ratio was almost 1:1, and the relative contribution of
366 η decreased with time. Such temporal changes in the w vs. η slope indicate changes in
367 the thermodynamic properties of the field (Dagan et al., 2016). Increasing
368 thermodynamic instability under polluted conditions results in an increase in mean w ,
369 while the decreasing instability under clean condition results in a decrease in rain
370 amount and hence, in η . Both trends act to reduce the slope. We have defined the
371 angle A , which represents the evolution of the thermodynamic conditions with time. A

372 can serve as a compact measure of the thermodynamic instability evolution in future
373 observational or numerical studies that quantify w and η .

374 Using a cloud-tracking algorithm, we identified the growing stage of the clouds and
375 examined the relative contribution of the aerosol effect on COG height by modulating
376 w and η during this stage. We showed that the relative contribution of the aerosol
377 effect on η is larger during the growing stage (for which aerosol loading acts to
378 maintain lower $|\eta|$ for a longer time) compared to the mature and dissipating stages,
379 thereby strengthening the argument that most of the aerosol invigoration effect occurs
380 early in the cloud's evolution (Koren et al., 2015).

381

382 *Data availability.* Information about the model and initialization files are available
383 upon request to the contact author.

384

385 *Competing interests.* The authors declare that they have no conflict of interest.

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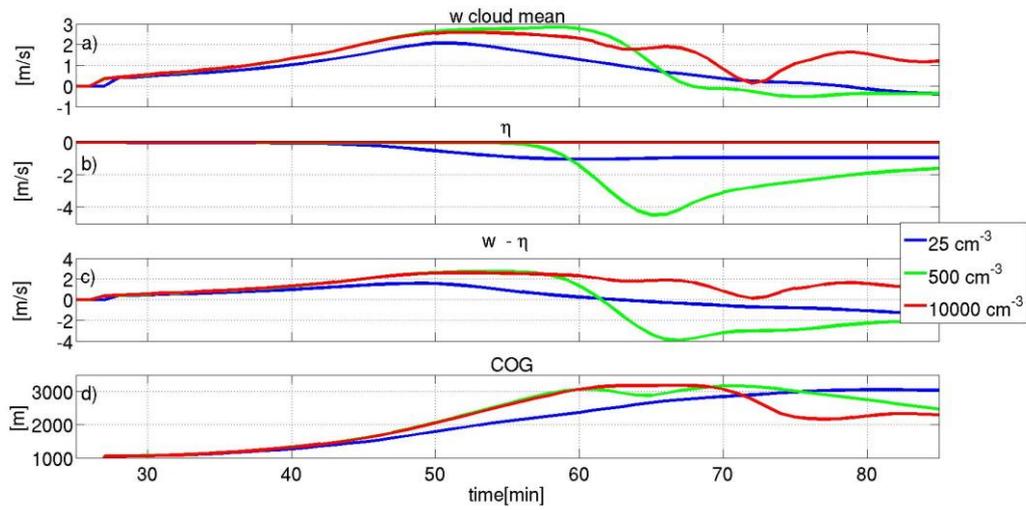
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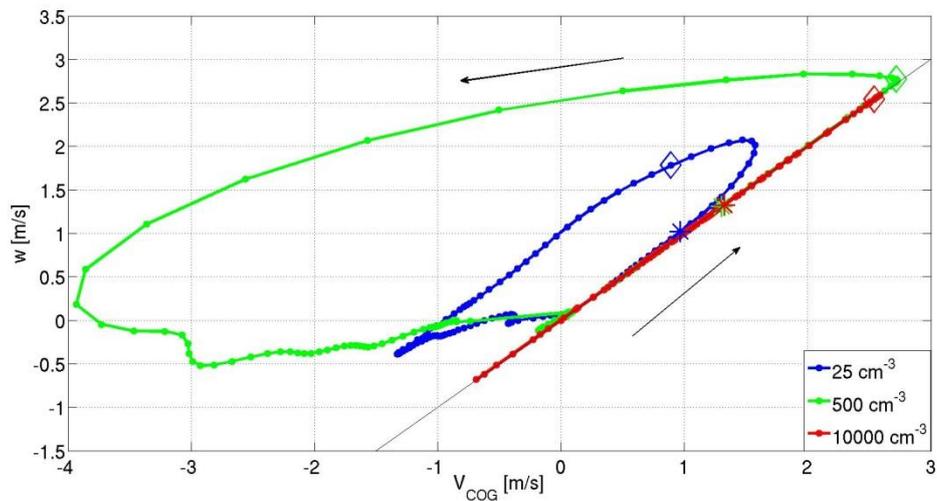
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509 **Figure 1. (a) Mean vertical velocity (w), (b) mean effective terminal velocity (η),**
510 **(c) mean vertical velocity plus effective terminal velocity, and (d) cloud center of**
511 **gravity (COG) as a function of time for three different aerosol concentrations.**

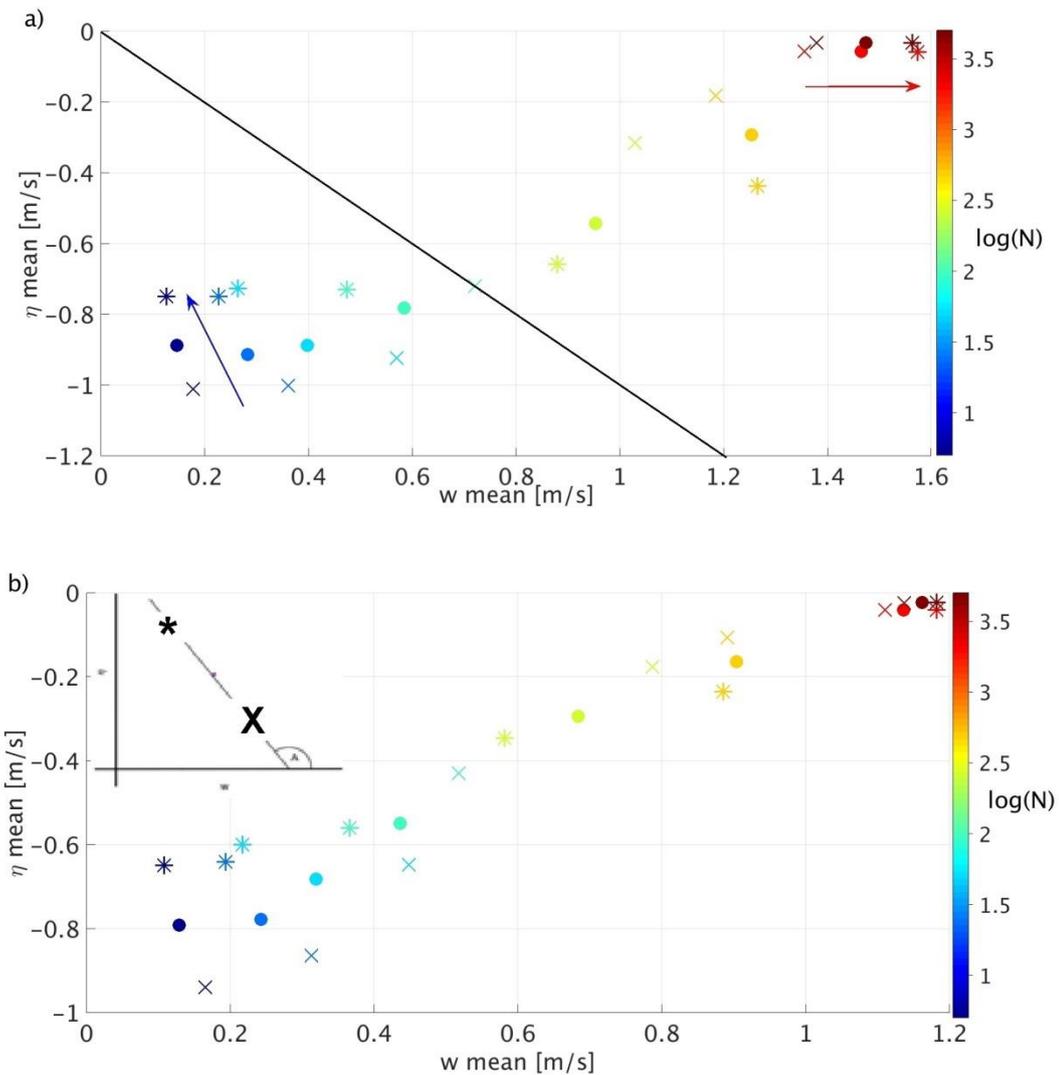
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514 **Figure 2. Cloud evolution on the phase space span by w vs. V_{COG} . The arrows**
515 **mark the direction of the trajectories and the thin black line is the 1:1 line. Stars**
516 **and diamonds denote $t = 40$ min and 55 min of the simulation, respectively.**

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518

519 **Figure 3. Temporal and spatial averages of the ambient air vertical velocity (w)**
 520 **vs. effective terminal velocity (η). Color-coding denotes the different aerosol**
 521 **concentrations. Dots represent averages of the entire simulation data (excluding**
 522 **the first 2 h spin-up time). The x and * markers represent the first third (2 h to 6**
 523 **h 40 min) and last third (11 h 20 min to 16 h) of the simulation period,**
 524 **respectively. (a) All clouds in the domain. (b) Only clouds in the growing stage.**
 525 **The black line in (a) is the zero-sum line for which $V_{COG} = 0$ (below the line V_{COG}**
 526 **< 0 and above it $V_{COG} > 0$). The angle A that measures the η vs. w time trend per**
 527 **aerosol level is illustrated in the inset in panel b.**

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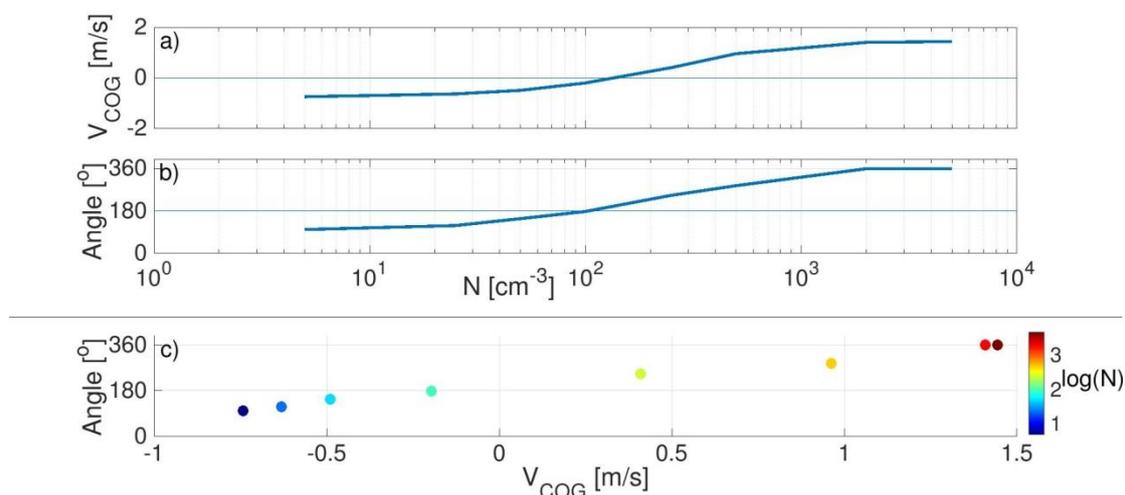
529 **Table 1. Linear regression slope on the η vs. w phase space for the different**
 530 **periods of the simulations for all clouds and growing-stage clouds in the domain.**
 531 **R^2 of the regression lines is presented in parentheses.**

	All clouds	Growing clouds
Total simulation period (2–14 h)	0.69 (0.96)	0.79 (0.98)
First period of simulation (2–6:40 h)	0.92 (0.96)	0.99 (0.93)
Last period of simulation (11:20–16 h)	0.47 (0.87)	0.59 (0.98)

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536 **Figure 4. (a) The cloud field's mean value of V_{COG} and (b) the angle A between**
 537 **the line that connect the first and last thirds of the simulation period and the x-**
 538 **axis on the η vs. w phase space for all clouds in the domain (Fig. 3a) as a function**
 539 **of aerosol loading. (c) V_{COG} vs. A . Color-coding denotes the different aerosol**
 540 **concentrations.**