Response to referee #1

The authors used idealized simulations to illustrate the importance of thermal compression waves in the total energy transport at the speed of sound (in those simulations). This part is convincing.

The authors also used these results to question the traditional view of energy transport by transient eddy, stationary eddy, and mean meridional circulations. However, their argument is not convincing.

If their claim can be quantified (see the suggestion below), it would represent an important contribution.

Major comments:

"Conceptually, eddies in traditional view include waves (e.g., gravity and Rossby waves). Therefore the authors' claim (that the traditional view considers the total energy transfer solely in an advective-like manner by the winds) seems incorrect."

As far as we know, total energy has not been considered to be transported with the phase speed or group velocity of large-scale waves, such as Rossby waves. Rather the meridional component of velocity associated with these waves have been considered to cause a meridional transfer of total energy. Large wavelength Rossby waves have westward group velocity and so will transfer energy westward, but this is energy associated with the kinetic energy and potential energy of the wave, rather than the quantity total energy.

There are however, many quotes that can be found in the literature alluding to total energy transfer in an advective-like manner by the winds. For example:

1) When discussing heat in sensible form and in latent form exchanged between one latitude and another Priestley (1949) states: "The main agents of meridional transport have been assumed to be the broad and deep northward and southward flowing currents of air whose dimensions are comparable in size to the cyclonic and anti-cyclonic pressure systems." This suggests transport at the speed of the air currents.

2) Shaw and Pauluis (2012) state: "Advection by the Eulerian mean meridional circulation dominates the total energy transport in the tropics" and "In the region of the Ferrel cell, a poleward energy transport is achieved by atmospheric eddies, which transport both sensible and latent heat poleward".

3) Liang et al. (2018) state: "In the time mean, the atmosphere carries heat meridionally by moving poleward air parcels with high moist static energy and moving equatorward air parcels with low moist static energy". Carrying heat meridionally by moving air parcels equatorwards and polewards suggests an advective-like process.

We think "soley in an advective-like manner' isn't unreasonable, but we have changed the text in most places so as not to use soley.

"Quantitatively, the authors should show the corresponding results based on the traditional view (i.e., using equations 1-3) in the figures and actually demonstrate the differences of these results versus their results. This would help address the relative

#### importance of thermal compression waves."

Our simulations are quite simple in that we prescribe a local heat source and examine a short time later the perturbed energy and mass fields. To examine the traditional view we would have to simulate the Hadley cell, Rossby waves and baroclinic eddies etc. That is a good idea, but goes beyond the scope of this work. We agree with the referee that in questioning the traditional view we are hypothesizing and in this revised manuscript we have been more cautious in our statements. However, we do need to say something about how these results may be relevant to the traditional view.

The situation is complicated since observational studies and many modeling studies enforce mass balance when computing poleward total energy transport (Trenberth 1991; Masuda 1988; Keith 1995; Magnusdottir and Saravanan 1999; Graversen et al. 2007; Yang et al. 2015; Liang et al. 2018). This typically involves adding a correction to the meridional velocity (e.g. Yang et al. 2015; see appendix). Our line of thinking is that the larger latent heat release at low latitudes than at high latitudes is causing expansion at low latitudes and compression at higher latitudes, which leads to a poleward mass transfer, and that the resultant buoyancy driven circulations and horizontal eddies are bringing mass back from the high latitudes to the low latitudes to give a mass balance. For instance, an eddy that has warm air moving poleward and cold air equatorward may result in an equatorward mass transfer since the warm air tends to be less dense and the cold air more dense. Both thermal expansion/compression and buoyancy driven circulations are all taking place at the same time, which makes the situation complicated. While there must be a mass balance in the long term mean, transfer of total energy by expansion and compression fundamentally involves mass transfer, so this process might not be accounted for properly if a mass balance condition is imposed. However, this is a hypothesis and at this stage we cannot say much about this issue.

As we stated above the decomposition of Eq. 3 will still include the contribution of expansion and compression to the dry static energy flux. Whether the traditional methodology accurately assesses the contribution due to eddies is unclear to us, particularly since studies typically employ a mass balance constraint. To assess the relative contribution of eddies versus the expansion/compression mechanism would require carefully designed experiments preferably with a fully compressible global model. The referee is correct that we are not able to say how important thermal compression waves are to the total energy transport based on our results. However, given that we find considerable transport of total energy at the speed of sound in our idealized simulations we think the current traditional view is incomplete.

Interestingly a recent paper by Liang et al. (2018) seems to be trying to remove a component involving poleward mass transfer in the total energy transport to come up with a new definition of heat transport. Recognition that considerable mass and total energy transport might be occurring at the speed of sound could provide a different perspective on this problem.

In order to make the limitations of the idealized experiments clearer in the introduction (page 2, line 23) it is now stated:

"For simplicity this study does not consider water substance. It utilizes an idealized framework, by looking at the transfers of energy and mass that occur in response to imposed heat sources in an initially quiescent atmosphere. Therefore it is difficult to draw definitive conclusions about how much energy and mass might be transferred by this mechanism in a more realistic large scale atmospheric circulation that includes for instance the Hadley circulation, Rossby waves and baroclinic eddies."

Also in section 6 the discussion from page 15, line 28 to page 16, line 20, has been significantly modified to address these issues.

## The presentation is clear. However, for the key points in the manuscript, the use of 28 figures is not justified. The authors could make good use of supplementary material by moving most of the figures there. This would also increase the readability.

We agree that it is a good idea to make use of supplementary material to reduce the number of figures. We have moved eight figures to the Supplement. These are the figures showing the solution for the 1D linearized thermal compression wave, the thought experiment figure, the figures showing the results of the convective-scale heat source with compression waves, and the results for the continent-scale heat source without the Coriolis term.

#### Minor comments:

## Equation 2: there should be square brackets on the right hand side, to be consistent with equation 3.

Eq. 2 has the factor  $2\pi R_e \cos\phi$  which is the distance around the earth at the latitude  $\phi$ . So that expression on the right hand side is the flux across a circle of latitude. This equation is however usually written as a time average (Starr and White 1954; Oort and Piexóto 1983), although the derivation doesn't require an average in time to be taken. When an average in time is taken there is an approximate mass balance, so the mechanism we are seeing for meridional transfer of total energy that occurs on very short time scales (hours), will not be able to be resolved given the time averaging in observational studies is quite large (days or months). It is possible that by considering time-averaged fluxes this is causing a misinterpretation of how a considerable portion of the energy transport is physically accomplished. However, this is a hypothesis and would have to be subject to a rigorous study.

It is now stated "Note that Eqs. 1 and 2 are often expressed as a time average."

## Figures 1 and 2: when u' is as large as 5-10 m/s, should a nonlinear model (rather than a linearized model) be used? How does it affect the results?

The units are cm/s so the velocity perturbation is quite small.

#### Figure 9: is the exponent (-5) in "kg m<sup>-3</sup> 10<sup>-5</sup>" correct in the figure 9 caption?

Yes the exponent is correct.

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#### Response to referee #2

The manuscript discusses the role of gravity waves and especially acoustic waves in transporting mass and energy in response to atmospheric disturbances caused by diabatic heating. It makes use of physical arguments, didactic examples, and numerical experiments. These are important ideas, and, given the increasing use of fully compressible equation sets in operational and research models, it is timely to reemphasize hem. That said, the key ideas involve basic, well-understood fluid dynamics, though they may be obscured by the acoustically filtered equation sets often used in meteorology. Moreover, much of the present manuscript seems to be reiterating points made in previous work (Nicholls and Pielke 1994a,b, 2000). One of my main points is that the manuscript should be revised to minimize this repetition and to emphasize the new ideas and results.

#### Main points

## "1. As mentioned above, repetition of previous work should be minimized and the new results emphasized."

In the introduction it is now stated more explicitly what is new about this study:

"Previous work is extended to larger scales and the effects of including the Coriolis force are examined. Comparison is made between simulations with and without thermally generated compression waves and it is demonstrated that differences start to become noticeable when the horizontal scale of the diabatic forcing is very large. Fields of vertically summed energies and mass are constructed to give a clear perspective of the lateral transports. Furthermore, the total heat input is calculated and compared to the total energy perturbation in the model domain to check energy conservation."

Furthermore, it is now worded more clearly in section 2.2 that the 1D linear solution was derived in NP94a and in section 2.3 that the thought experiment was presented in NP94b. Additionally, sections 2.2 and 2.3 have been shortened and the figures moved to the Supplement as well as some of the discussion. We do think it is important to include this material as background material covering the main ideas, since this does not appear a topic that many are familiar with.

# 2. It would be useful to relate the ideas and experiments discussed here to the ideas of hydrostatic and geostrophic adjustment, e.g., Gill A. E. (1982), pp 191-, Bannon, P. R., (1995) J. Atmos. Sci., 1743-1752. In particular, Gill (p194) discusses the energy carried away by Poincare waves in the (shallow water) geostrophic adjustment process.

This is an interesting suggestion. There are similarities between the analytical thermal compression wave solution and shallow water solutions. The energy discussion by Gill (p194) is based on wave energetics. For the linearized compressible equations a wave energy equation can be derived (e.g. Nicholls and Pielke 1994a, Eq. 36). In that manuscript it was shown in equations (37) and (38) that the wave potential energy is far smaller than the perturbation internal energy in a thermal compression wave. So two energy conservation equations can be derived, one that is wave energy (wave potential energy plus kinetic) and one that is total energy (internal plus kinetic), and the wave energy is far smaller in magnitude. It would be interesting to consider the geostrophic adjustment process for thermally generated compression waves in a more simplified theoretical framework.

In the Supplement we now include a comparison of the total energy and wave energy (Supplement Eq. S6 and S7, and Figure S3), and these are mentioned in the main manuscript

(page 4, lines 8-10, and lines 18-20).

"3. The full version of equation (15) involves the initial profiles \bar{\rho} and \bar{\theta}\_v, so some approximation to the full fluid dynamical equations seems to be involved. This then raises the question of whether the full version of (15) has exact, or only approximate, mass and energy conservation properties. These properties seem to be crucial to the whole exercise, but I wasn't able to quickly track this information down by looking at the references given."

Equation (15, now Eq. 10) does indeed use approximations. These are appropriate for regional atmospheric modeling simulations as long as the departure from the basic state is small. For the simulations in this paper these approximations are reasonable and energy conservation is not compromised too much. However if this model was used to simulate large-scale baroclinic eddies then modifications to the model equations would probably need to be made to obtain accurate mass and energy conservation. For instance, there are large meridional potential temperature differences from equator to pole and for a horizontally homogeneous basic state the potential temperature perturbations would be large and the departure from the basic state would not be small.

This issue is now discussed on page 16, line 16-20.

"4. The full version of (15) is compared with one that omits the first three terms on the RHS. This omission eliminates the thermal compression waves under study, but at the cost of sacrificing mass and energy conservation. Strong arguments have been made that numerical models, should solve 'dynamically consistent' equation sets, retaining appropriate conservation laws, including mass and energy, even when those equation sets are approximate. For example, the hydrostatic equations and at least some versions of anelastic and pseudo-incompressible equations are dynamically consistent in this sense, and they are widely used. It would therefore be of great interest to under-stand how such equation sets respond to a local diabatic heating, and how the energy budget is to be interpreted in such models. (It is conceivable that a similar adjustment process occurs to that in the fully compressible case, but instantaneously rather than at the speed of sound.) I believe that a comparison of the full equation set with hydrostatic and/or anelastic equations would be of much wider interest than the artificial system that involves dropping the RHS of (15)."

We agree it would be of great interest to compare the full equation set with other approximate equation sets and understand how the energy budget is to be interpreted. As Klemp and Wilhelmson (1978) point out there are similarities of the system Eq. (15, now Eq. 10)) without the terms on the RHS with the anelastic system. There has been considerable interest in the applicability of soundproof models to large-scale motions (e.g. Benacchio et al. 2015). It is not clear to us how other models that are not fully compressible and do not simulate Lamb waves that propagate at the speed of sound would respond to localized heat sources and whether the redistribution of total energy and mass would occur in a realistic manner. We hypothesize that a hydrostatic large-scale model that includes Lamb waves as solutions that are not slowed down would probably be conserving total energy and mass and in a similar way to a fully compressible large-scale model. This is certainly an area that should be investigated further.

5. P3 lines 16-17: 'This decomposition tacitly makes the assumption...' Actually the decomposition (3) is correct, but the tacit assumption is often made when interpreting (3). I think part of the problem is imprecise use of terminology in the community: the 'transients'

### in (3) morph into 'eddies' (a bit ambiguous) which morph into 'turbulence' (definitely wrong for the compression waves discussed here). See also section 2.4.

Yes this is correct and we have reworded this sentence (page 3, line 25):

"A tacit assumption that is commonly made in interpreting Eq. 3 is that total energy is a quantity that is advected solely with the wind"

We have also added on page 3, line 31-34.

"There is nothing intrinsically wrong with the decomposition in Eq. 3 and the transfer of energy by compression waves would be included. However, the assumption that total energy is transported in an advective manner may have led to practical methodologies for computing the contributions in Eq. 3 that do not account for the possibility of energy transport at the speed of sound. This issue will be discussed further in section 6."

Also in section 6 the discussion from page 15, line 28 to page 16, line 20, has been significantly modified.

"6. Section 2.4. I think part of the problem is that, because of the historical use of acoustically filtered equation sets such as anelastic, or hydrostatic in pressure coordinates, the term 'heat flux' has become identified with the potential temperature flux, which in turn is closely related to the entropy flux. Thus the energy and entropy budgets have become confounded in our thinking. But, while entropy is carried along with the fluid, to a good approximation, energy is not. See also the discussion in Nicholls and Pielke 1994b. If the paper can help to clarify these issues then that would be a useful service to the community."

We agree that this is part of problem. It would be interesting to examine the entropy transports. We are not sure that there wouldn't be some entropy transport with the propagation of thermal compression waves. However it appears that a quantity more related to the usual view of "heat flux" can be derived from the equation for entropy, which is basically a potential temperature flux. We took this approach in deriving an approximate conservation equation in Nicholls and Pielke (1994b, Eq. 21). Maybe there is some wider applicability of this approach to large-scale circulations but we have not examined this issue. We don't think we can address the issue of entropy flux in this paper unfortunately.

## "7. I found the results section hard work. I think it could be better organized to emphasize the points the authors wish to make, and to help the reader to make comparisons between different experiments."

We have moved eight figures to the Supplement. These are the figures showing the solution for the 1D linearized thermal compression wave, the thought experiment figure, the figures showing the results of the convective-scale heat source with compression waves, and the results for the continent-scale heat source without the Coriolis term. These results have been summarized in the main paper.

#### **Minor points**

#### "P6 line 14: frequency should be period (or change 5 min to 2 pi / 5 min)."

We have corrected this.

"P7 line 16: greater than 0?"

Thank you for noticing this error.

## "Section 2.7: I am perfectly happy with the idea that these disturbances are waves, and for me this section is unnecessary (though perhaps the authors have met some resistance to the idea and so feel that the section is necessary)."

We think that while these disturbances have wave-like characteristics, there are aspects that are not normally associated with waves so that it is worth keeping this section.

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## On the role of thermal expansion and compression in large scale atmospheric energy and mass transports

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Abstract. There are currently two views of how atmospheric total energy transport is accomplished. One view considers total energy as a quantity that is transported in an advective-like manner by the wind. The other considers that thermal expansion and the resultant compression of the surrounding air causes a transport of total energy in a wave-like manner at

- 10 the speed of sound. This latter view emerged as the result of detailed analysis of fully compressible mesoscale model simulations that demonstrated considerable transfer of internal and gravitational potential energy at the speed of sound by Lamb waves. In this study, results are presented of idealized experiments with a fully compressible model designed to examine the large-scale transfers of total energy and mass when local heat sources are prescribed. For simplicity a Cartesian grid was used, there was a horizontally homogeneous basic state, and the simulations did not include moisture.
- 15 Three main experimental designs were employed: The first has a convective storm scale heat source. This experiment illustrates the basic process of expansion in the heated region leading to compression of the adjacent air and the subsequent formation of a Lamb wave that propagates laterally at the speed of sound. The second experiment has a continent scale heat source prescribed near the surface to represent surface heating and which includes a constant Coriolis parameter. Results indicate that after several hours considerable amounts of total energy and mass are transferred offshore at the speed of sound.
- 20 This simulation is compared to one with the term in the governing equations responsible for forcing thermal compression waves omitted. There is a fairly small but nevertheless significant difference of the wind field compared to the fully compressible results. A comparison of the fully compressible simulation with a simulation without the Coriolis force illustrates the role of geostrophic adjustment in significantly influencing the total energy distribution. The third experiment has a cloud cluster scale heat source prescribed at the equator and which includes a latitude dependent Coriolis parameter.
- 25 Results show considerable amounts of meridional total energy and mass transfer at the speed of the sound.
  <u>If as the results of this idealized study suggests there is significant transport of total energy at the speed of sound taking place in the atmosphere then the current theory of total energy transport would be incomplete. This could bring into question the methodology commonly used to attribute the total energy transports to transient eddy, stationary eddy, and mean meridional circulations.</u>
- 30 Based on these results the conceptual differences between the terms "total energy transport" and "heat transport" in a fluid are discussed. Fast moving compression waves are unlikely to be accurately simulated by most climate models since they utilize semi-implicit time differencing techniques, and this could potentially be a source of error that has yet to be evaluated.

#### **1** Introduction

Satellite studies of the zonally averaged top of atmosphere (TOA) radiative fluxes show that there is a net input of energy at low latitudes and output at high latitudes (e.g., Vonder Haar and Suomi 1971). For a heat balance, there must be a poleward transfer of total energy, and fluid motions of both the atmosphere and oceans are considered to play major roles. It has been generally understood that the atmosphere and ocean carries, heat from one area to another in an advective-like manner by the winds and ocean currents. However for the atmosphere this was brought into question by numerical modelling studies conducted with a fully compressible numerical model (Nicholls and Pielke 1994a and b; hereafter NP94a and NP94b, Melville Nicholls 8/24/18 10:34 AM Formatted: Not Highlight

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Melville Nicholls 8/25/18 4:52 PM Deleted: can Melville Nicholls 8/25/18 4:52 PM Deleted: y respectively). It was found that large quantities of internal and gravitational potential energies could be transferred in a wave-like manner at the speed of sound. The basic idea is relatively straightforward: Consider for instance that as an air parcel is heated it causes the temperature and pressure of the parcel to increase (a hot air balloon would be another way to think about this). The resultant pressure gradient between the heated air and its immediate environment then drives a

5 divergent outflow causing the heated air parcel to expand. What is usually considered the salient point is that the expansion leads to a density decrease, and therefore makes the air parcel (or hot air balloon) more buoyant. However, at the same time, the expansion of the air parcel must also cause the air in the immediate surroundings to become compressed, and that means the pressure must increase in this surrounding air. The pressure gradient therefore works outwards, continually accelerating air in an expanding radius. The result is the generation of a compression wave, that we have termed a "thermal compression 10 wave", which has some clear similarities to a mechanically forced sound wave.

Thermal compression waves produced in this manner are not high frequency sinusoidal waves so in this respect they differ from typical sound waves. There is a wave front that propagates at the speed of sound and behind this a region of compressed air. It is at this point that it can be seen that a transfer of energy and mass might be occurring since compressed air has more molecules per unit volume and in the mean the molecules are moving slightly faster. The perturbations of

- 15 pressure, temperature and density in the large volume of compressed air surrounding the heated air parcel are extremely small compared to those occurring in the immediate vicinity of the air parcel where relatively strong buoyancy circulations develop. Nevertheless this rapidly widening envelope of compressed air with small internal energy and density anomalies adds up over a very large volume to constitute a major reservoir of total energy and mass, and this reservoir does not stay in place once the heating ends, but propagates away rapidly at the speed of sound.
- 20 While this theory of total energy transport has been known for some time it has not yet had any significant impact on the global scale view of how total energy transport is occurring. In this manuscript the main objective is to show that this mechanism of total energy transfer is likely to be important for large scales, and moreover to point out that this mechanism is probably not simulated very well in current global scale models. For simplicity this study does not consider water substance. It utilizes an idealized framework, by looking at the transfers of energy and mass that occur in response to imposed heat
- 25 sources in an initially quiescent atmosphere. Therefore it is difficult to draw definitive conclusions about how much energy and mass might be transferred by this mechanism in a more realistic large scale atmospheric circulation that includes for instance the Hadley circulation, Rossby waves and baroclinic eddies. Previous work is extended to larger scales and the effects of including the Coriolis force are examined. Comparison is made between simulations with and without thermally generated compression waves and it is demonstrated that differences start to become noticeable when the horizontal scale of
- 30 the diabatic forcing is very large. Fields of vertically summed energies and mass are constructed to give a clear perspective of the lateral transports. Furthermore, the total heat input is calculated and compared to the total energy perturbation in the model domain to check energy conservation. Since the perturbations associated with thermally generated compression waves are typically extremely small it might seem at first sight that their effects can be safely neglected. The case is made that inaccuracies will be produced when they are not simulated correctly on the large scale, which might not be negligible.
- 35 The manuscript is organized in the following manner: Section 2 gives an overview of the two theories. Section 3 discusses the numerical model and the design of the three experiment configurations, which consist of convective scale, continent scale, and cloud cluster scale simulations. Section 4 presents results for the three main experiments and several auxiliary experiments. In section 5 the significance of these results for understanding total energy and mass transfers are discussed as well as potential implications for climate modelling. Finally in section 6 conclusions are summarized.

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#### 2 Overview of total energy transfer mechanisms

#### 2.1 The current paradigm of total energy transport

The derivation of the total energy equation can be found in many standard texts (e.g. Gill 1982; Peixoto and Oort 1992). It can be written in the following form:

$$5 \quad \frac{\partial}{\partial t} \Big( c_{\nu} \rho T + \rho g z + \rho L q + \rho \frac{u^2}{2} \Big) + \nabla \cdot \Big\{ \Big( c_{\nu} \rho T + \rho g z + \rho L q + \rho \frac{u^2}{2} \Big) u + p u + F - \kappa \nabla T - \mu \nabla \Big( \frac{u^2}{2} \Big) \Big\} = 0 \tag{1}$$

where  $c_{\nu}$  is the specific heat at constant volume,  $\rho$  the density, *T* the temperature, *g* the acceleration due to gravity, *L* the latent heat of condensation, *q* the specific humidity *u* the velocity vector, *p* the pressure, *F* the radiative flux density,  $\kappa$  the thermal conductivity, and  $\mu$  the viscosity. The total energy is comprised of internal energy, gravitational potential energy, latent heat energy, and kinetic energy. Note that this Eulerian conservation equation concerns the energy per unit volume.

In large-scale energy budget studies the hydrostatic approximation is made and the flux across a vertical latitudinal wall is rewritten in the (x, y, p) coordinate system (Priestley 1949; White 1951a, b; Starr and White 1954), The following expression can be derived for the flux across a circle of latitude (e.g. Oort and Peixoto (1983):

$$\int_{z=0}^{\infty} \oint \rho \left( c_p T + gz + Lq \right) v dx dz = 2\pi R_e \cos\phi \int_0^{p_0} \left( c_p T + gz + Lq \right) v \frac{dp}{g}$$
(2)

where the enthalpy has been introduced  $(c_pT = c_vT + p/\rho)$ ,  $c_p$  is the specific heat at constant pressure,  $R_e$  the radius of the 15 earth,  $\phi$  the latitude, v the meridional velocity and  $p_0$  the surface pressure. To derive this equation the terms involving kinetic energy, thermal diffusion and viscosity have been neglected. Note that Eqs. 1 and 2 are often expressed as a time average. Out and Peixoto (1983) make the following statement regarding the time average of the term on the right side of Eq. 2: "Further, the integrand can be decomposed into the contributions by transient eddies, stationary eddies and mean meridional circulations in order to get a better understanding of the physical mechanisms involved in the fluxes:"

 $20 \left| \begin{array}{c} \int (c_p T + gz + Lq)v \end{bmatrix} = c_p [\overline{v'T'}] + c_p [\overline{v}^*\overline{T}^*] + c_p [\overline{v}][\overline{T}] \\ + g [\overline{v'z'}] + g [\overline{v}^*\overline{z}^*] + g [\overline{v}][\overline{z}] \\ + L [\overline{v'q'}] + L [\overline{v}^*\overline{q}^*] + L [\overline{v}][\overline{q}] \end{array} \right|$ 

(3)

where over-bars represent a time average and square brackets a zonal average. The prime symbol represents the departure of the variable from the time average, and the asterisk the departure from the zonal average. A tacit assumption that is commonly made in interpreting Eq. 3 is that total energy is a quantity that is advected solely with the wind. For instance, the

term  $c_p[\overline{v'T'}]$  is considered a transient eddy flux of enthalpy, implying that a large-scale eddy that moved warm air poleward and cold air equatorward would be physically accomplishing a meridional total energy transport. However, studies that have conducted detailed analyses of total energy transfer using fully compressible models demonstrate that total energy can be transferred in a wave-like manner at the speed of sound, which challenges this assumption (NP94a and b; Nicholls and

30 Pielke 2000). There is nothing intrinsically wrong with the decomposition in Eq. 3 and the transfer of energy by compression waves would be included. However, the assumption that total energy is transported in an advective manner may have led to practical methodologies for computing the contributions in Eq. 3 that do not account for the possibility of energy transport at the speed of sound. This issue will be discussed further in section 6.

#### 2.2 A linearized one-dimensional solution for a thermal compression wave

35 When an air parcel is heated the temperature and pressure increases and the resulting pressure gradient causes it to expand. During its expansion, the air surrounding the parcel is compressed. This compression does not simply remain in situ; a wave front propagates away from the heated air parcel at the speed of sound leading to weak positive pressure, temperature, and

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<b>Deleted:</b> Note that this decomposition tacitly makes the assumption that total energy is a quantity that is advected solely with the win	
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density anomalies over an increasingly large volume surrounding the heated air parcel. The internal energy per unit volume given by  $c_v \rho T$  can be rewritten using the ideal gas law  $p = \rho RT$ , where R the gas constant for dry air, as  $c_v p/R$ . Therefore a positive pressure anomaly in the region of compressed air means that the internal energy is increased in this region. In addition, the increased density means that the gravitational potential energy  $\rho gz$  is increased. Therefore this mechanism can

- 5 quickly lead to an increase of total energy over a very large volume surrounding the air parcel and constitutes a total energy transfer at the speed of sound. <u>NP94a derived a</u> simple mathematical solution illustrating the basic process in the absence of the gravitational force for the one-dimensional linearized momentum, thermodynamic and continuity equations which allow thermal compression waves. This solution, which has been expanded to include the temperature perturbation, is given in the Supplement (Section S1 and Figures S1 and S2). Furthermore, expressions for the total energy and wave energy are given in
- 10 section S1 Eq. S6 and S7, respectively. Figure S3 compares the internal energy in a wave produced by a heat pulse with the wave energy.

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The solution for a heat pulse having duration of 600 s shows anomalies moving in opposite directions from the source region at the speed of sound (Fig. S2). The positive pressure perturbations indicate that these are regions with enhanced internal energy as shown in Fig. S3. While the central heated region has warmed considerably there is no significant change

- 15 in internal energy per unit volume.  $(c_v \rho T)$  since there has been a large density decrease in the narrow heated region. Mass can be seen to be conserved since the density has increased slightly in the two wide compressed regions which are propagating away at the speed of sound. Therefore, this simple 1D solution shows a significant redistribution of internal energy and mass occurring at the speed of sound.
- <u>The magnitude of the wave energy in the fast moving anomaly for the heat pulse solution is four orders of magnitude less</u>
   than the internal energy perturbation (Fig. S3). It is important not to confuse these two energy forms that can both be derived from the linearized equations.

#### 2.3 A thought experiment demonstrating internal energy transfer is different than convective heat transfer

Another perspective on total energy transfer was presented in NP94b based on a thought experiment. A detailed description is provided in the Supplement (Section 2 and Figure S4). An ideal gas in a container was considered that was divided by a

- 25 movable frictionless partition. Heating the gas on one side of the container would cause it to expand and the gas on the other side to be compressed (Fig. S4). Considering a control volume within the unheated side the compression would have resulted in an increase in internal energy. This increase would be identical to the increase in internal energy in a similar sized control volume within the heated side since the pressure on both sides of the container would be identical and the internal energy per unit volume only depends on pressure. If the partition was removed and the gas stirred so that the warmer air was mixed with
- 30 the relatively colder unheated air this would not result in a transfer of internal energy into the control volume on the right side of the container since the pressure would remain virtually unchanged.

Convective heat transfer is considered to be the transfer of heat from one place to another by the movement of fluids. It is common in meteorology to describe heat as being advected from one place to another, whereby it is meant that when relatively warm air moves into a region it constitutes a "heat transfer". This interpretation is at the heart of the decomposition

35 made in Eq. 3. From this perspective the heat transport in the thought experiment depicted in Fig. S4 took place in the second stage when air was mixed and the air in the control volume became notably warmer. However, this did not constitute a total energy transfer, which occurred earlier in the first stage during the compression of the unheated gas.

The idea that convective heat transfer is not the same thing as internal energy transfer is a very simple idea as shown by this thought experiment and shouldn't raise any red flags. Now take this one step further and propose a similar thing is actually happening in the atmosphere and that internal energy is being transferred at the speed of sound. This apparently is one step too far and this hypothesis becomes subject to incredulity.

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#### 2.4 Different meanings of heat transfer

It is pertinent at this stage to review three uses of the term heat transfer:

1) In thermodynamics, heat is defined as energy in transit across the boundary of a system, which does not involve work or the transfer of matter. Since heat is the flow of energy across the boundary of a system it is not correct to say it is stored in

5 the system. However, the transfer of heat does lead to an increase of the internal energy of the system equal to the heat transferred.

2) Convective heat transfer within the body of a fluid is often defined as the transfer of heat from one place to another by the movement of fluid elements. A moving fluid element is said to carry energy with it. This energy is often described as thermal energy, or internal energy. However, there is a problem with this interpretation as made clear by the thought

10 experiment discussed in section 2.3, Transport of relatively warm air into the control volume during the mixing stage did not result in a change of the internal energy within the control volume. It led to a change in temperature, such that the mean kinetic energy of the molecules in the control volume increased, but their number decreased (corresponding to the density decreasing) so that overall there was no net change in internal energy.

3) The expression for the change of total energy (Eq. 1) involves fluxes of enthalpy, gravitational potential energy, and latent
 heat energy. These summed have also been called a "heat flux".

Clearly the term "heat" is being used for different physical quantities, and this is one reason there is confusion on this issue. Consider the <u>thought experiment discussed in section 2.3</u> and suppose that the warm and cold air in a thin region at their interface started to be mixed after removal of the partition. The turbulent eddies produced by the stirring shouldn't result in a horizontal transfer of internal energy as we have maintained. Now consider putting a brief heat source at the far left side of

- 20 the container, which produced a transient compression wave that proceeded to propagate through the interface between the warm and cold air that is being stirred. As the compression wave passes from left to right through the region of eddies there would for a brief instant of time be an enthalpy flux and internal energy would consequently increase on the far right side of the container. It would not be accurate to say that the turbulent eddies are physically responsible for that enthalpy flux just because they occupy the same space as the compression wave.
- 25 Obviously the <u>exchange of warm and cold air masses in the container is of major physical importance as are the</u> meridional transports of warm and cold air by eddies in the atmosphere. This meridional transport in the atmosphere is playing a significant role in the overall energy balance. For instance, TOA radiative fluxes would be different without these warm and cold air advections. However the simple thought experiment discussed above suggests that the quantity total energy in Eq. 1 is not necessarily being transferred when there is advection of warm or cold air masses. The transfer of the
- 30 quantity total energy is complicated to understand because the atmosphere to a reasonable approximation behaves like an ideal gas so that heat input results in expansion and work being done on the surrounding air. This work done compressing the surrounding air is fundamental to understanding why energy is quickly redistributed at the speed of sound.

#### 2.5 Vertical transport of total energy

Consider a horizontally homogeneous atmosphere and low-level heat source. The heated air will expand in the vertical and work will be done not only against the atmospheric pressure as in the example discussed in section 2.2, but also against gravity. The acoustic cut-off period, for a non-isothermal atmosphere is approximately 5 min in the troposphere and stratosphere (Beer 1974; Walterscheid et al. 2003). Shortly after the low-level heat source is turned on in a simulation an upward propagating pulse of vertical velocity develops. This pulse propagates upwards at the speed of sound and increases in amplitude as it reaches higher levels (e.g. NP94b). When it reaches 100 km above the surface after traveling for approximately 5 min, a trailing lobe with negative vertical velocity becomes evident. If there is a Rayleigh friction layer at

upper levels then the wave will not reflect off the top of the model. As the simulation continues further wave-like activity of the vertical velocity occurs, but its amplitude is relatively small in the troposphere and lower stratosphere, where persistent

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Deleted: Another perspective on internal energy transfer is gained by considering the thought experiment shown in Figure 3. An ideal gas in an insulated container is separated into two parts, gas 1 and gas 2, by a movable frictionless partition Consider uniformly heating gas 1 on the left side of the container. This will cause the temperature and pressure to increase. Gas 1 will expand and the movable partition will move to the right compressing gas 2. If the heating is discontinued the partit come to an equilibrium position, as shown in Fig. 3b. such that the pressure in gas 2 equals the pressure in gas 1. The temperature of gas 2 will have increased due to compression, but will be considerably less than that of gas 1. Since the internal energy per unit volume  $(c_v p/R)$  is only a function of pressure, it will be the same in gas 2 as in gas 1. Obviously, since gas 1 now occupies a larger volume than gas 2 it will have a larger net internal energy. ... [3] ville Nicholls 8/15/18 3:58 PM

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**Deleted:** In this situation the fluxes of enthalpy would not be properly represented by a decomposition into terms like Eq. 3, which would physically be attributing the transport to turbulent eddies. It is possible that an analogous situation could occur in the atmosphere and this point will be returned to in section 5, after results of the numerical simulations are presented.

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**Deleted:** movement of warmer air to the right side of the container and colder air to the left side

Melville Nicholls 8/8/18 4:30 PM Deleted: frequency weak upward motion prevails. Walterscheid et al. (2003) discuss results of a model simulation of acoustic waves in the mesosphere and lower thermosphere generated by deep tropical convection. They found quite a complicated behaviour with a trapped oscillation below about 80 km altitude with a period of ~5 min and a nearly vertically propagating wave with about a 3 min period above this height.

5 NP94b showed a low-level horizontally homogeneous heat source results in compression of the air aloft throughout a deep layer. Associated with the mean upward motion in the troposphere and lower stratosphere are a mass flux and an energy flux. From Eq. 1 the rate of change of total energy to a good approximation for a dry atmosphere is given by the convergence of the energy flux:

$$\frac{\partial}{\partial t} \left( \frac{c_p}{R} p + \rho g z + \rho \frac{w^2}{2} \right) = -\frac{\partial}{\partial z} \left\{ \left( \frac{c_p}{R} p + \rho g z + \rho \frac{w^2}{2} \right) w \right\}$$

10 where *w* is the vertical velocity. The simulation by NP94b showed the pressure perturbation rapidly increasing with height to the top of the thin heated layer adjacent to the surface and then falling off exponentially above (Fig. 7 of that paper). Also the density decreased significantly in the heated layer and increased very slightly above but throughout a much deeper layer. These positive pressure and density perturbations aloft represent significant increases of internal and gravitational potential energy throughout a deep region above the low level heat source, and a net convergence of the energy flux given by Eq. (9) 15 must have occurred at each level.

Later on in the simulation a turbulent boundary layer developed. The turbulent sensible heat flux was calculated and shown at low levels to a very good approximation equal to the upward total energy flux. This is an expected result since after all this is the way the enthalpy flux from the surface is in practice calculated. However, prior to the turbulent boundary layer thermals developing there was still an upward enthalpy flux. This flux didn't depend on the presence of thermals, only on the vertical expansion of the low level air.

As part of this current modelling study we have conducted a simulation with a model top at 140 km with a 20 km deep Rayleigh friction layer. The results remain similar to NP94b showing a significant increase of the total energy up to the lower stratosphere in response to a low-level heat source. Therefore if one wanted to calculate the net heat input, and also calculate the increase of the perturbation energy field in response to this net heat input, then the calculation would have to

25 integrate vertically through a large depth, into the stratosphere, to get a reasonable agreement between them.

#### 2.6 Lamb waves

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Solutions to the linearized equations for a stratified fluid show the existence of three types of waves known as acoustic waves, Lamb waves, and gravity waves (e.g. Gill 1982). The restoring force for acoustic and Lamb waves is compression, and for gravity waves is buoyancy. The properties of Lamb waves have been discussed by numerous researchers (e.g. Lamb 1910, 1932; Taylor 1936; Lindzen and Blake 1972). A feature of this wave is that for an isothermal atmosphere their

velocities are parallel to the surface, so the vertical velocity is zero.

The vertical structure of Lamb waves for an isothermal atmosphere is given by:

$$u' \propto exp\left(\frac{(\gamma-1)z}{\gamma H_s}\right)$$
$$p' \propto exp\left(\frac{-z}{\gamma H_s}\right)$$

35  $\rho' \propto exp\left(\frac{-z}{vH_c}\right)$ 

where  $H_s = R_{f_0}^T/g$  is the scale height with  $T_0$  the basic state temperature and  $\gamma = c_p/c_{vz}$ . Since  $\gamma - 1$  is greater than 0 it can be seen that the perturbation horizontal velocity u' increases with height, whereas the perturbation pressure p' and density  $\rho'$  decrease with height. NP94b modelled a two-dimensional sea-breeze circulation produced by a surface heat source that was

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### turned off after an hour. The solution at two hours showed Lamb waves had moved off shore on either side of the land surface.

\_Nicholls and Pielke (2000) using a fully compressible version of the Regional Atmospheric Modelling System (RAMS)

#### modified to include sources and sinks of water vapour simulated an isolated convective storm. They found a Lamb wave emerged from the storm, which was trailed by slower moving gravity wave modes. An analysis of internal and gravitational potential energies showed that the net total energy within the Lamb wave, propagating away at the speed of sound, was approximately equal to the net latent heat release that had taken place in the convective storm. It was noted that because the Lamb wave propagated in the horizontal plane it had a two-dimensional character. For instance, whereas a heat source in one dimension creates a compression wave with only a positive pressure perturbation as in Fig. <u>\$2</u>, in two dimensions a leading

10 positive pressure anomaly is trailed by a negative pressure anomaly (Fig. 2 of Nicholls and Pielke 2000). This geometric effect on the shape of sound waves is well known (e.g. Lighthill 1978).

These results suggest that thermally generated Lamb waves are likely to be ubiquitous in the atmosphere, and moreover that they play a significant role in horizontal transfers of total energy and mass. Unlike for acoustic waves there is no cut-off frequency, so very low-frequency Lamb waves can be produced by convective forcing. Nishida et al. (2014) studied

15 background Lamb waves in the Earth's atmosphere. They found evidence of Lamb waves from 0.2-10 mHz based on array analysis of microbarometer data with root mean square amplitude (rms) of about 0.15 Pa. In their assessment of excitation mechanisms they emphasized turbulence as the probable source for the background Lamb waves. However, it is possible that thermally generated Lamb waves caused by latent heat release in storms could have contributed based on the results of Nicholls and Pielke (2000).

#### 20 2.7 To what extent can these thermally generated disturbances be considered waves?

While we use the term thermal compression waves to refer to large regions of compressed air moving at the speed of sound that are generated by heat sources it is important to recognize that they don't satisfy every criterion usually associated with waves. For instance, waves are often considered a periodic disturbance of the particles of a substance and that after their passage there is no resultant movement of the particles. Sometimes a wave is defined as a process that transports energy without transporting mass. In contrast, the pressure pulse in Fig. 2 is not periodic and its passage leads to a net movement of

the fluid particles. There is clearly a mass transfer in this process.

While it might be considered stretching the definition of a wave to refer to these thermally generated disturbances as waves, there is little doubt that a thermally generated disturbance like the one that propagated at the speed of sound in the simulation of a convective storm by Nicholls and Pielke (2000) would be regarded as a wave-like feature if it was detected by a microbarometer array.

#### 2.8 Thermally generated gravity waves

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In the numerical experiments discussed later in this paper the prescribed heat sources also generate gravity waves as well as compression waves, so in order to get a better understanding of these simulations a brief review is given in this section. Bretherton and Smolarkiewicz (1988) drew attention to the link between gravity waves and compensating subsidence in the environment surrounding a convective cloud. The spreading gravity wave response to a developing cloud was investigated using a two-dimensional simulation. They found that a buoyancy source caused vertical displacements in the air in a

- widening region around the cloud which for this two dimensional framework made the buoyancy of the environment approximately equal to the buoyancy in the cloud.
- Nicholls et al. (1991) derived simple analytical two-dimensional solutions to the linear hydrostatic Boussinesq equations for an atmosphere at rest with prescribed heat sources and sinks. For a case with an idealized rigid lid and a deep heat source, represented by a half-sine wave in the vertical, the thermally generated buoyancy circulation was characterized by upward



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motion in the heated region with outflow aloft and inflow at low levels. The outflow and inflow expanded rapidly on either side of the heat source. The leading edges of these expanding circulations were deep fast-moving wave-like pulses of subsidence. Therefore, the subsidence compensating the central upward motion did not occur continually over broad regions on either side of the heat source, but had a distinct horizontally propagating character. The propagating subsidence regions

- caused adiabatic warming, adjusting the environmental potential temperature towards the perturbed values at the heated 5 centre for this two-dimensional framework. Response to a thermal forcing profile more typical of a mesoscale convective system (MCS) having a stratiform region was also examined for a rigid lid. In this case a deep rapidly propagating circulation like the one previously discussed was superimposed on a slower propagating circulation characterized by a midlevel inflow and upper- and lower-level outflows. This second slower moving mode had a cool potential temperature
- 10 anomaly at low levels and a warm potential temperature anomaly aloft. The leading pulses of vertical motion had upward motion at low levels and downward motion aloft. The speed of the modes is given by

 $c_n = \frac{NH}{n\pi}$ 

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where N is the Brunt-Väisälä frequency, H the height of the rigid lid, and n the wave number of the vertical heating with a vertical structure sin  $(n\pi z/H)$ , where z is height.

- The two-dimensional solution for a semi-infinite region, without a troposphere/stratosphere interface, shows considerable 15 differences of the low-level fields in some respects (Pandya et al. 1993). In particular, the magnitude of the subsidence is substantially reduced, and occurs over a much broader region. Moreover, the axis of the peak vertical velocity in the lowlevel subsidence region is no longer vertically aligned, but strongly tilted. Nevertheless, adiabatic warming behind the broader wave front still gradually approaches the values at the heated centre. Another factor to consider is that in the real
- atmosphere there is increased stability above the tropopause, which partially reflects waves and to some extent increases the 20 similarity with the rigid lid solution. A two-dimensional squall line simulation by Nicholls (1987) showed a structure similar to the analytic solution for the first mode during the early stage of development. The deep convective heating extending to the top of the troposphere produced a deep overturning circulation with surface mesolows growing laterally away from the centre of the convection at a rapid pace. For the first deep convective mode that extends throughout the depth of the tropical
- 25 troposphere, H is approximately 15 km and taking N=0.01 s<sup>-1</sup> gives a horizontal propagation speed of 48 m s<sup>-1</sup>. For the second mode, the speed is 24 m s<sup>-1</sup>. These speeds are much faster than typical atmospheric motions.

Mapes (1993) postulated that higher order modes of the heating profile in a MCS may cause upward displacements at low levels in the nearby atmosphere, thus favouring the development of additional convection nearby. He also emphasized that the wave-like disturbances are not ordinary gravity waves, and pointing out their similarity to tidal bores in water, referring

- 30 to them as buoyancy bores. There has been considerable amount of research since these earlier studies that has examined their role in convective systems (e.g. Pandya et al. 2000; Nicholls and Pielke 2000; Haertel and Johnson 2001; Fovell et al. 2006; Tulich and Mapes 2008; Bryan and Parker 2010; Adams-Selin and Johnson 2013). Inclusion of planetary rotation confines the compensating subsidence and adiabatic warming caused by deep convection to a finite distance, measured by the Rossby radius of deformation (e.g. Liu and Moncrieff 2004).
- The studies by NP94a and b, were motivated by the finding that thermally generated gravity waves simulated with the 35 standard version of RAMS (without the terms on the right side of Eq. 10 discussed in the next section) were not transferring significant amounts of total energy, and moreover that there was a considerable discrepancy between the heat input and the net total energy increase within the domain. This led to the conclusion that thermally generated compression waves, which were eliminated from the RAMS model equations, might be the explanation for the missing energy.

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#### **3** Numerical model

RAMS is a nonhydrostatic numerical modelling system comprising time-dependent equations for velocity, non-dimensional pressure perturbation, ice-liquid water potential temperature (Tripoli and Cotton 1981), total water mixing ratio and cloud microphysics (Pielke et al. 1992; Cotton et al. 2003). In this study simulations are conducted without moisture. The model

5 uses a time-splitting procedure which provides numerical efficiency by treating the sound wave modes separately (Derickson 1974; Klemp and Wilhemson 1978). To obtain the most accuracy for these simulations very small time steps were used and the time splitting scheme was not employed. The model uses a similar approach to Klemp and Wilhelmson (1978) who utilize the Exner function given by

$$\pi = \left(\frac{p}{p_0}\right)^{\frac{R}{c_p}}$$

The prognostic equation for the Exner function is written in tensor form as

$$\frac{\partial \pi}{\partial t} + \frac{c^2}{c_p \,\overline{\rho} \overline{\theta}_v^2} \frac{\partial \left( \overline{\rho} \overline{\theta}_v u_j \right)}{\partial x_j} = - \, u_j \frac{\partial \pi}{\partial x_j} + \frac{R \pi}{c_v} \frac{\partial u_j}{\partial x_j} + \frac{c^2}{c_p \,\overline{\theta}_v^2} \frac{\partial \theta_v}{dt} + D_{\pi}$$

- 10 where  $u_i$  (j=1, 2, 3) are the velocities u, v, w, respectively,  $\theta_v$  is the virtual potential temperature, and  $D_{\pi}$  represents turbulent mixing. Bars over variables refer to the initial state which is a function of z only. Klemp and Wilhelmson (1978) note that the terms on the right side of this equation appear to have little influence on processes which are of physical interest in the cloud model. They coded their model so that these terms could be included or omitted. They found that omission of these terms can allow small amounts of mass to be added or removed from the domain which in turn affects the mean level of the 15 pressure. Furthermore they liken this behaviour to that occurring in the anelastic system where non-uniqueness of the
- Poisson solution requires an arbitrary specification of the mean pressure. For previous studies we have used the density instead of the Exner function (NP94a and b) and a different form of Eq. 10, which includes a moisture source or sink (Nicholls and Pielke 2000). For this study we use an equation similar to Eq. 10, which was also used by Medvigy et al. (2005) for a study with RAMS that examined mass conservation. The advantage of using this form of the equation is that inclusion or not of the third term, with the material derivative of virtual potential temperature, acts as a switch for allowing
- or not allowing thermally generated compression waves. Therefore the effects of thermally generated compression waves can be more readily evaluated.
- Preliminary experiments that examined large scale transfer of total energy showed distortions of the compression waves occurring at large distances from the source. In order to improve accuracy the model code was modified for double 25 precision.

#### 4 Description of experiments

There are three main experiments conducted for this study and several auxiliary experiments. The first shows the response to a deep convective scale heat source. The fields are portrayed in detail showing the air expanding in the heated region creating a compression wave in the surrounding air and shortly after the development of a buoyancy driven circulation. An

- 30 auxiliary experiment examines the effect of not including the first three terms on the right side of Eq. 10, which eliminates compression waves. The second main experiment has a continent scale heat source prescribed near the surface in a square region and includes a constant value of the Coriolis parameter specified for latitude of 45 degrees. The purpose is to show that there is a considerable transport of total energy and mass to large distances offshore. An auxiliary experiment examines the effect of not including compression waves. Another auxiliary experiment examines the effect of turning off the Coriolis
- 35 force. The third main experiment has a heat source located at the equator which is the size of a large cloud cluster and includes a Coriolis force that varies with latitude. The purpose of this experiment is to examine the resultant meridional transfer of total energy and mass. An auxiliary experiment examines the effect of turning the heat source off after a short

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period so that the compression wave can separate from the more slowly propagating buoyancy driven circulation. Table 1 lists the experiments.

The model is configured with 101 vertical levels and a vertical grid increment of 500 m. Below the model top which is at 50 km there is a 10 km Rayleigh friction layer in order to damp upward propagating waves. There are 161 horizontal grid points both in the x-direction and y-direction for all experiments. For the first experiment the horizontal grid increment is 4 km giving a domain width of 640 km. The heating function is

$$Q = Q_0 \sin\left(\frac{z}{H}\right) \frac{a^4}{(a^2 + x^2 + y^2)^2}$$

(1**1**)

where  $Q_0$  is the magnitude of the heat source, H=10 km, and a=12 km. The simulation is run for a 15 min period. For the continent scale heat source simulation the horizontal grid increment is 200 km giving a domain width of 32000 km. The heat source is horizontally homogeneous for a square region in the centre of the domain with sides of length 4000 km. In the vertical the heat source is a quarter cosine between the surface and 1 km. In effect this means the heating source is applied at the first thermodynamic grid point above the surface, which is at 250 m, and at the second thermodynamic grid point above the surface, which is at 250 m. For the third experiment the horizontal grid increment is 100 km giving a domain width of 16000 km. the heating function has the same form as Eq. 1 except a=500 km. The simulation is run for a period of 5 h. For Experiment 3B the heating is turned off after 2h.

15 The initial temperature profile is the mean Atlantic hurricane season sounding of Jordan (1958) up to 50 hPa, and above this level the U. S. Standard Atmosphere profile was used (e.g. Wallace and Hobbs 1977). The simulations were dry.

#### **5** Results

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#### 5.1 Convective scale heat source

Figure 1, shows x/z vertical sections through the center of the domain of the heating rate, temperature perturbation, pressure
 perturbation, x-component of velocity u, and vertical velocity w at 10 s. The heating causes the temperature and pressure to increase as would be expected and the pressure gradient is already starting to drive an outflow as can be seen in the velocity fields. Note the pressure is starting to increase at the surface as the downward propagating wave front starts to reflect off it.

Figure 2, shows vertical sections of the density perturbation and the pressure perturbation at 20 s. The density, which is not a predicted variable, is diagnosed using the equation of state. The red/blue color scheme in this figure has a non-linear scale

- 25 in order to portray very small and very large values on the same figure. It can be seen that the density has started to decrease significantly in the core of the heated region as the air expands, while in the immediate surroundings of the heated region the air is compressed. The pressure field now shows a maximum at the surface. The higher pressure can be seen to be spreading out beyond the heat source.
- Figure 3, shows vertical sections of the density perturbation, pressure perturbation and vertical velocity at 40 s. The buoyancy created by the decreased density is starting to produce a significant updraft in the troposphere. Above this the updraft extends to a height of about 18 km. For a speed of sound of 320 m s<sup>-1</sup> the distance a wave front would travel in 40 s is around 12 km. Since the heating peak is at 5 km the compression wave front reaching a height of ~18 km is reasonable. At this time the surface pressure directly beneath the heat source has started to become negative due to lateral expansion causing the vertical column of air above the surface to weigh less.
- 35 Figure 4 shows vertical sections of u at 80 s and w at 120 s. At 80 s there now an inflow at low levels and an outflow in the upper troposphere associated with the buoyancy driven circulation. At 120 s in addition to the strong updraft in the mid-troposphere there is subsidence beginning to develop in the immediate surroundings, which is again a feature of the buoyancy driven circulation.

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Figure  $\underline{S}_{4}$  are vertical sections of w at 60 s and 90 s, which extend to the top of the domain at 50 km in order to portray the vertical propagation of the compression wave. The wave front quickly propagates upwards at the speed of sound. It can be seen that the magnitude of vertical velocity in the upward propagating wave increases at it travels upwards. A second maximum is evident at 90 s, which is due to reflection of the downward propagating wave front seen at Fig. Le at the surface.

Figure 6 shows vertical sections of the density perturbation and horizontal sections of the surface pressure perturbation at 5 min and 10 min. At 5 min the positive density perturbation at the leading edge of the compression wave has reached 100 km from the center of the heat source. The density perturbation decreases with height approximately as would be expected for a Lamb wave (Eq. 7). There is a ring of high pressure at the surface. By 10 min the compression wave has propagated to approximately 200 km from the storm. Interestingly the high pressure anomaly is concentrated in a narrow ring at the

- leading edge and so has a different shape than for the 1D thermal compression wave solution, shown in Fig. <u>S</u>1. This is likely to be mainly a geometric effect since thermally generated Lamb waves have a two-dimensional character when propagating in three dimensions away from a localized heat source as discussed in section 2.6.
- The features of the buoyancy driven simulation are illustrated in Figure <u>7</u>, which shows fields at 15 min. Even for this simple constant heat source the response is quite complicated. The warm region at the centre of the heat source is surrounded by an annulus of warm air. There is a v-shaped region of cool air aloft. A low pressure anomaly occurs at the surface and a high pressure anomaly at the top of the heat source. The density perturbation is similar in shape to the potential temperature perturbation although of opposite sign. As expected there is a strong inflow at low levels and outflow at the top of the heat source. Upward motion is in the center and compensating subsidence in the surrounding air. There is a wave-like character to
- 20 the buoyancy circulation, such that the ring of subsidence is propagating away from the heat source with a speed of approximately 45 m s<sup>-1</sup>. This subsidence results in adiabatic warming. This propagating character and structure has similarities to the highly idealized solutions discussed in Nicholls et al. (1991) for the deep rapidly propagating convective mode. Fig. 7e shows that by 15 min the leading edge of the compression wave has almost propagated to 300 km and is considerably less in amplitude than at 10 min (Fig. 6d).
- 30 and there is no increase in the surrounding environment. Despite significant differences with the fully compressible case early on in the simulation by 15 min the results are virtually identical (Compare Fig. S7 with Fig. 7).

These results corroborate the conclusion by Klemp and Wilhelmson (1978) that the terms on the right side of Eq. 10 are not important for cloud modelling, at least if one is not interested in the very low amplitude compression waves that are generated. However, it shall be seen for the continent scale heat source that differences are more pronounced. Also as Klemp

35 and Wilhemson (1978) noted, for convective cloud simulations there can be a small amount of mass change within the domain, which is evident from Fig. S7b since the mean surface pressure has been reduced (assuming that the pressure field does not deviate that much from hydrostatic). As will be discussed in section 5, mass changes could be more significant if diabatic heat sources are large, or if they occur throughout the whole domain which can be the situation if radiation is included.

#### 40 **5.2 Continent scale heat source**

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In this section the response to horizontally homogeneous heating at the surface of a square continent is considered. Figure  $\S_{4}$  shows results at 9 h for Experiment 2A, which has the Coriolis force included. The surface potential temperature over the

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Deleted: Figure 11 shows results for the convective scale heat source with the terms on the right side of Eq. 15 omitted (Experiment 1B) at 10 s Comparing with Fig. 4 there are significant differences. The potential temperature perturbation is significantly less, which is probably due to the upward motion at the center of the heat source leading to some adiabatic cooling, which does not exist in the case of the fully compressible simulation. There is no expansion of the air and the pressure immediately starts to fall at the surface. Figure 12 shows the density perturbation at 40 s, u at 80 s, and vertical velocity at 120 s that can be compared with the corresponding frames in Fig. 6 and 7 for the compressible simulation. The density perturbation is larger in magnitude than for the fully compressible case. Also, the inflow is stronger and the outflow weaker, which is consistent with an outflow velocity associated with expansion of the heated air for the compressible case superimposed onto the buoyancy driven circulation. This simulation at 120 s has developed a more extensive subsidence region surrounding the updraft. Figure 13 at 15 min can be compared to the compressible case in Fig. 10. Despite the differences noted early in the simulations, at this time the results are virtually identical. One discernable difference is that the pressure perturbation at the top of the heat source for the compressible case (Fig. 10b) is slightly higher (Fig. 13b). These results corroborate the conclusion by Klemp and Wilhelmson (1978) that the terms on the right side of Eq. 15 are not important for cloud modeling, at least if one is not interested in the very low amplitude compression waves that are generated. However, it shall be seen for the continent scale heat source that differences are more pronounced. Also as Klemp and Wilhemson (1978) noted, for convective cloud simulations there can be a small amount of mass change within the domain, which is evident from Fig. 13b since the mea surface pressure has been reduced (assuming that the pressure field does not deviate that much fro hydrostatic). As will be discussed in section 5, mass changes could be more significant if diabatic heat sources are large, or if they occur throughout the whole domain which can be the situation for radiative forcing.

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heated land surface has increased by approximately 6 K. The surface pressure has decreased considerably over the land and has increased by  $\sim 0.16$  hPa over the adjacent ocean (note a small colour bar interval has been chosen for Fig. <u>Sp</u> so that the magnitude of the surface pressure drop over land is not shown). A vertical section through the centre of the continent of the

- density perturbation (Fig. §c) shows a large decrease near the surface (note that due to the small colour bar interval the large
  decrease over land is not coloured) and a smaller amplitude increase above and over the adjacent ocean. The total energy perturbation consisting of internal, gravitational potential and kinetic, have increased in a large dome-shaped region except for a decrease in a thin layer next to the land surface (Fig. §d). It can be seen that the total energy has increased significantly into the lower stratosphere, but not at higher levels, which is consistent with the discussion of section 2.5. Fig §e shows the field of vertically integrated total mass change (this can be considered the change in a square metre oblong column extending
- 10 from the surface to the top of the domain). The mass has decreased over the land area and has increased over the surrounding ocean area. Fig. §f shows a vertical section of the zonal velocity u. At the west and east edges of the land surface there are low-level inflows and just above are return flows. These are very crudely resolved sea breezes. There is a deep layer of weak offshore flow aloft. While some of this offshore flow is associated with the return flow of the sea-breeze, a part of this flow is due to expansion of the air occurring above the continent. Below the Rayleigh friction layer there is a wave-like structure
- 15 aloft. These are propagating at the speed of sound and the leading edge of the first anomalies have passed beyond the west and east sides of the panel at -10,000 km and 10,000 km, respectively (note the model domain size is much larger than the panel size shown in this figure). This wave-like appearance of the velocity field aloft is primarily a geometrical effect as discussed in section 2.6 and is not nearly so evident in a two dimensional simulation (not shown). It has ramifications for the fluxes of energy and mass off the continent as will be discussed shortly.
- Figure 2 zooms in on the west side of the domain to show details of the sea-breeze circulation. There is a dome of positive pressure anomaly over a surface negative pressure anomaly. The total energy perturbation field in Fig. & mainly reflects these pressure perturbations. The y-component of velocity v is negative near the surface because the Coriolis force turns the inflow winds to the right, whereas the opposite occurs in the overlying sea-breeze return flow. Fig. & shows a horizontal section of a larger portion of the domain at z=15.25 km illustrating an outflow aloft above the shoreline and a weak anti-cyclonic flow of several centimetres per second above the ocean that looks like it might be close to a gradient wind balance
- since it encircles the dome of high pressure.
- Figure 1Q shows time series of the summed energies throughout the whole domain and the heat input. The gravitational potential energy at any time is almost exactly two fifths of the internal energy as would be expected for a hydrostatically balanced circulation where they would differ by a factor of  $R/c_{\nu}$ . The total energy in the domain is the same as the heat input until seven hours, after which it becomes slightly larger. It is not clear why this small discrepancy occurs. The kinetic
  - energy is shown on a different panel because it is so much smaller in magnitude than the internal and potential energies. The summed energies shown separately for the land and ocean in Fig. 1Qd show an interesting behaviour. The internal energy initially increases quickly over land. As shown in Fig. 3 of NP94b the pressure initially increases in the heated layer adjacent to the surface, but there is an offshore mass flux as the air expands causing the surface pressure to begin to fall a
- 35 short distance inland. This outflow associated with expansion of air works its way inland at the speed of sound. It takes a little under two hours for this outflow to reach the centre of the domain, which for this simulation is 2000 km from the shoreline. There is an upward mass flux over land and an upward total energy flux (Fig. 13 of NP94b illustrates an upward sensible energy flux, or enthalpy flux, caused by a low-level heat source), which begins immediately the heating is turned on. However, at the centre of the domain the air does not expand laterally until the inward propagating outflow reaches the
- 40 centre, so to begin with there are only upward fluxes, not lateral fluxes. The offshore lateral fluxes of total energy at the shoreline while small to begin with, increase quite rapidly, such that after two hours the total energy over land no longer increases despite the heat input and actually starts to decline. This increase of the offshore flux appears to be because all the air across the whole continent is undergoing lateral expansion by two hours whereas initially it was only air near the coast.



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- Fig. §f shows a wave train in the zonal velocity field (u) at upper levels. The regions in the wave train, with a flow towards the land, started to develop over the continent at 3 h and by 5 h there was a significant onshore flow above 25 km. This coincided with the total energy over the land increasing again. By 9 h there is again a deep region of offshore flow at the shoreline (Fig. §f), but not as strong as at 2 h, and the total energy over land is continuing to increase.
- 5 The time series of the mass changes over land and ocean shown in Fig. 10d are mirror images of one another. This indicates there is reasonably good mass conservation. The rate of mass change is slow to begin with, strongest between 2-5 h, and then changes at a moderate rate. This behaviour would be expected from the evolution of the normal component of velocity (u) at the shoreline discussed in the previous paragraph.
- Figure 1\_shows results at 9 h for Experiment 2B without thermal compression waves and can be compared with Fig. §. 10 The surface potential temperature change is identical. There is a pressure decrease over land, but there no increase over the surrounding ocean. The density decreases where heating occurs, but does not show a significant increase aloft or over the ocean. The vertical section of pressure perturbation does not show a pronounced dome. There is a mass decrease over the land, but not over the ocean so that mass is not being conserved. While a sea-breeze is evident there is not a deep offshore flow at the shoreline.
- 15 Figure 12 zooms in on the west side of the domain for Experiment 2B similarly to Fig. 2 The pressure drop over the land is considerably larger for this simulation compared to the fully compressible result. For the compressible case there is a larger density increase aloft comparing Fig. Sc with Fig. 11c, so that the weight of a column of air above the surface is greater which is why the pressure fall is not so much. For this simulation the inflow is larger whereas the return flow aloft is less when compared to the compressible simulation. This can be explained by the expansion of air over the continent for the
- compressible simulation contributing an offshore component to the flow (Fig. §f), which at low levels can be thought of as superimposed on the buoyancy driven sea-breeze circulation. Since the onshore flow is larger for this simulation the Coriolis force causes the meridional component of the wind to be larger in magnitude as well. These differences of the wind speeds are approximately 15%, so while not large they are significant. Fig. 12d shows the flow aloft above the shoreline is only about one third of the strength as occurred for the fully compressible simulation (Fig. 2d). Moreover there is no anti-cyclonic
   flow at a large distance offshore.

Time series for the total energy in the domain and mass changes over the land and ocean for Experiment 2B are shown in Figure  $13_{\bullet}$  The total energy in the whole domain decreases slightly with time even though there is a large heat input showing there is not energy conservation. The mass in the domain decreases linearly with time and this is mainly over the land mass. The sea-breeze circulation is tending to bring some mass onshore, which results in a decrease over the ocean.

- 30 Results for Experiment 2C, which is fully compressible but does not include the Coriolis term is shown in the Supplement (section S4 and Figures S8 and S9). Comparing with Experiment 2A there is far more total energy and mass redistributed over the ocean and to greater distances offshore. For sea-breeze circulations the horizontal extent is comparable to the Rossby radius of deformation, which can be considered approximately the buoyancy frequency N times a height scale for the convective boundary layer divided by the Coriolis parameter, with modifications due to surface friction (e.g. Rotunno 1983;
- 35 Dalu et al. 1989; Drobinski and Dubos 2009). Without the Coriolis force the horizontal extent of the sea-breeze is considerably larger and is stronger in magnitude than for Experiment 2A at 9 h, as would be expected (not shown). The horizontal scale for geostrophic adjustment associated with the fast propagating Lamb wave shown in Fig. 9d is clearly much larger than that of the sea-breeze in Fig. 9c, since the anticyclonic flow is quite strong even at 2000-3000 km offshore. The length scale given by the speed of sound divided by the Coriolis parameter at 45 degrees latitude is approximately 3000 km.
- 40 <u>Therefore, these results are suggesting that we can consider this length scale to be a Rossby radius of deformation for these very fast moving compression waves.</u>

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#### 5.3 Equator heat source

In this section the response to a heat source with the scale of a cloud cluster and which is located at the equator is examined (Experiments  $3A_{\downarrow}$  Figure <u>14</u> shows a vertical section through the centre of the heat source and several panels of simulated fields at 1 h for Experiment <u>3A</u>. There are quite a few similarities to the convective-scale heat source. A compression wave

- 5 is generated which at this early stage is quite symmetrical as can be seen by the surface pressure perturbation. Figure 15, with vertical sections that only go to a height of 20 km, shows that by 5 h a significant asymmetry has developed as the compression wave has travelled far enough away from the equator to become influenced by the Coriolis force. The potential temperature has increased to just over one degree in the centre of the heat source. The warm region has widened due to the compensating subsidence (Fig. 15t). The compression wave front has reached about 6000 km from the source as can be seen
- in Fig. <u>15</u>b, c and d. It appears that as the wave front reaches higher latitudes the Coriolis force acts to turn the weak outflow to the right in the northern hemisphere and to the left in the southern hemisphere resulting in a convergence of mass to the east of the heat source and a divergence of mass to the west, and this results in an asymmetrical surface pressure field. For instance, Fig. <u>15</u>d shows that the meridional component of the outflow is stronger to the west of the heat source than to the east. The height-meridional vertical section of the density field shown in Fig. <u>15</u>c, which has a very small colour bar interval to portray the compression wave, indicates mass redistribution towards the polar-regions. Figs. <u>15</u>c and f indicate that the
- leading edge of the thermally generated buoyancy circulation is propagating at a speed of  $\sim$ 45 m s<sup>-1</sup> in the meridional direction.

Figure <u>16</u> focuses on the energy and mass changes at 5 h for Experiment 3A. The height-meridional section of the internal energy perturbation shows that the leading pulse of the compression wave is a region of enhanced internal energy. This field

- is identical to the perturbation pressure except for the multiplication factor of c<sub>v</sub> /R. There are much larger positive and negative perturbations in the region of the buoyancy driven circulation, but these tend to cancel one another. The density perturbation at the leading edge of the compression wave, shown in Fig. <u>15</u>c, results in a positive gravitational potential energy perturbations that are maximized in the upper troposphere and lower stratosphere. The fields of vertically summed internal and gravitational potential energy perturbations show maxima to the east of the source, but clearly there has been a
- 25 significant meridional transfer towards the polar-regions (Figs. 16c and d). The changes at the centre of the heat source are relatively small. Therefore the heat source has not caused a significant in situ increase of total energy when the vertical sum is considered. Figure 16e shows a height-meridional section of the total energy perturbation, which goes to the top of the domain. The largest anomaly in the compression wave occurs just over 5000 km from the heat source. The major anomalies occur in the region of the buoyancy driven circulation, but vertically integrated they tend to cancel. Fig. 16f shows the mass
- 30 has decreased in the region of the buoyancy driven circulation where there has been net lateral expansion of the air, whereas it has increased in the surrounding environment. The mass changes in the surrounding environment are much smaller in magnitude, but occur over a much larger area.

Time series of the energies and heat input for the whole domain are shown in Figure <u>17</u>, Again the potential energy can be seen to be two-fifths of the internal energy to a good approximation. For this simulation the total energy is slightly less than the heat input at the end of the five-hour simulation, demonstrating reasonable energy conservation.

Meridional fluxes that have been summed in the vertical are shown in Fig. 18. The enthalpy flux is quite strong at the leading edge of the compression wave and is towards the poles. Interestingly the flux is towards the equator in the region occupied by the buoyancy driven circulation. The strong low-level flow towards the heat source (Fig. 15e) and the higher pressure at low levels compared to aloft is causing this net equatorward flux. The potential energy flux on the other hand

40 shows the opposite behaviour in the region of the buoyancy driven circulation. Since the potential energy is small at low levels, the strong outflow in the upper troposphere dominates the transport. The total <u>energy</u> flux illustrates that a significant meridional transport away from the equator is occurring between the heat source and the leading edge of the compression

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wave. Fig. 1<sup>Sd</sup> demonstrates that there is also a broad region of meridional mass transport away from the equator, except for a small region very close to the heat source.

Results for Experiment 3B at 5 h, which is identical to Experiment 3A except the heat source is turned off after 2 h are shown in Figure <u>19</u>. There is no longer a warm potential temperature perturbation at the centre, but instead a warm air anomaly in a ring that surrounds a cool anomaly at the centre. This warm ring is propagating as subsidence causes adiabatic warming at its leading edge and ascent causes adiabatic cooling at its trailing edge. In between the downdraft and updraft the winds are towards the centre in the lower troposphere and away from the centre in the upper troposphere. So there is an overturning circulation that propagates through the environment away from where the heat source was located in a wave-like manner, which has similarities to the idealized linear two-dimensional rigid lid solution for a pulse forcing function

discussed in Nicholls et al. (1991). This thermally generated gravity wave, or buoyancy bore (Mapes 1993) propagates significantly slower than the thermally generated compression wave, so that by this time the two wave types are starting to become separated. The Lamb wave is evident in in the density perturbation field shown in Fig. 19d and it can been that it has a leading lobe with a positive anomaly and a trailing lobe with a negative anomaly, which as mentioned previously in section 2.6 is a geometric effect due to the Lamb wave having a two-dimensional character for a localized compact source in three dimensions. The idealized one-dimensional solution for a thermal compression wave shown in Fig. S2 of the Supplement on the other hand has a simpler structure and does not exhibit a leading positive lobe trailed by a negative lobe.

Energies and mass changes for Experiment 3B is shown in Fig. 2<u>0</u>. The leading lobe of the Lamb wave has positive internal and potential perturbation energies whereas as the trailing lobe has negative perturbation energies. Fig. 2<u>0</u>d shows the negative values of the vertically summed total energy perturbation in the trailing lobe are as large in amplitude as the

- 20 positive values in the leading lobe, but they occupy a much smaller area so there is still a net positive total energy in the Lamb wave. Moreover by the time the negative lobe was to reach the same distance from the source as the positive lobe it would have decreased significantly in amplitude. At the centre the vertically summed total energy perturbation is slightly negative. Positive values of vertically summed total energy perturbation are only found at over 3000 km from the centre of where the heat source was located. The vertically summed mass change has a large negative value in the area occupied by
- 25 the thermally generated gravity wave, weak negative values in the trailing lobe of the compression wave and weak positive values in the leading lobe. This indicates that a significant redistribution of mass has occurred at the speed of sound.

#### 6 Discussion

The current paradigm of large-scale meridional transport of internal and gravitational potential energies assumes it is accomplished in an advective-like manner with the winds. The results of this study suggest that significant transports could

- 30 be occurring at the speed of sound. The simulations in this study are highly idealized, but it seems unlikely that this transport mechanism wouldn't be occurring in the real atmosphere. To what degree is currently unknown. <u>The decomposition of Eq. 3</u> has been the standard procedure for many years with an interpretation that attributes the meridional fluxes to advective-like transports by transient eddy, stationary eddy, and mean meridional circulations. <u>This study has not considered energy</u> transfer in the presence of eddies that transport warm air poleward and cold air equatorward. However, it could be imagined
- 35 for the equator heat source experiment that there was a large-scale eddy at mid-latitudes transporting warm air poleward and cold air equatorward and that a Lamb wave produced by a rapidly intensifying cloud cluster or tropical cyclone near the equator propagated polewards through it. For instance, in a similar manner as portrayed by Figs. 14f and 15b that show the rapidly propagating surface pressure perturbation. This is analogous to the scenario discussed in section 2.4. Presumably the fast moving Lamb wave wouldn't be too influenced by the much slower winds of the large-scale eddy.
- 40 <u>Suppose for the sake of argument that the large-scale eddy wasn't producing meridional sensible and potential energy</u> fluxes prior to the arrival of the Lamb wave. As the Lamb wave passed through the eddy there would be poleward meridional sensible and potential energy fluxes. The flux would be associated with very small increases in the meridional

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velocity, pressure, density and temperature. If Eq. 1 was used the enthalpy flux could be either calculated using the density and temperature, or from the pressure after substitution from the ideal gas law (ignoring the effects of moisture for simplicity). It is perhaps worth mentioning that these perturbations associated with the passage of the Lamb wave are very small and would be extremely difficult to measure from atmospheric observations, although in a modelling study this would

5 be feasible. Alternatively the right side of Eq. 2 could be used to calculate the energy transport. In this case the bounds of the integral vary since the surface pressure rises as the Lamb wave propagates through the eddy. So care should be taken when attributing the fluxes just to the terms in the integrand since the bounds of the integral are changing, which affects the value of the integral.

\_\_\_\_A fundamental aspect of the transfer of total energy as the Lamb wave propagated poleward through the large scale eddy

- 10 is that it would involve a mass transfer (e.g. Fig. 16f). This raises the possibility that there might be issues with the methodologies used to calculate the contributions to total energy transport in Eq. 3 because these very rapid mass transfers at the speed of sound are not properly accounted for. Both observational and modelling studies typically enforce mass constraints when calculating meridional energy transports (e.g. Masuda 1988; Keith 1994; Magnusdottir and Saravanan 1999; Graversen et al. 2007; Yang et al. 2015; Liang et al. 2018). Perhaps this could be causing the attribution of energy
- 15 transports to be misinterpreted. This issue would need to be examined in a modelling study that simulated more realistic atmospheric circulations than in this work. The equations used by RAMS uses some approximations that are reasonable for cloud and mesoscale simulations and for the relatively small departure from the basic state in these simulations. However if this model was used to simulate large-scale baroclinic eddies, which would require significant meridional temperature gradients then modifications to the model equations would probably need to be made to obtain accurate mass and energy conservation.

Many climate models use the hydrostatic balance condition and the governing equations include Lamb waves as solutions. Therefore they may be capable of simulating some of the compressibility effects that have been investigated in fully compressible nonhydrostatic models including propagation of total energy at the speed of sound. However, the use of semiimplicit time differencing schemes, which has become common, brings this into question. Such schemes are considered of

- 25 great practical utility since they slow down fast moving modes thought to have little meteorological significance, thereby allowing the use of a much larger model time step (e.g. Robert 1969; Tapp and White 1976; Tanguay et al. 1990; Robert 1992; Simmons and Temperton 1996). Typically Lamb waves and gravity waves will be slowed down and distorted by these methods. However, thermally generated Lamb waves and gravity waves do have physically significant effects, so the use of semi-implicit schemes may be causing more inaccuracy than has been recognized in large scale global models. For instance,
- 30 if the thermally generated compression wave shown in Fig. S2 were slowed down while maintaining total energy and mass conservation then it would need to be larger in magnitude. Moreover geostrophic adjustment due to the Coriolis force acting on the horizontal velocities associated with Lamb waves would presumably occur over a smaller spatial scale. Semi-implicit methods may also have an impact on thermally generated gravity waves. A study of orographic gravity

waves was carried out by Shutts and Vosper (2011) using the Met Office Unified Model. They found that the semi-implicit off-centring parameter approach used by the model actually damped orographic waves in a global forecast if a large time-

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- step of 15 minutes was used. However, reducing the time-step to 2 minutes allowed the orographic gravity waves to be adequately simulated. The results of this study raise the possibility that the large time-steps typically used in global models may not only be significantly impacting thermally generated compression waves, but also thermally generated gravity waves. The physical importance of either of these thermally generated fast propagating wave-like disturbances was not
- 40 recognized at the time semi-implicit schemes were developed. They were designed for the purpose of eliminating the time step constraint imposed by fast moving mechanically produced sound waves, orographic gravity waves, and vertically propagating gravity waves above cloud tops, which were thought to be relatively unimportant for large scale modelling.

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Melville Nicholls 8/25/18 4:35 PM Deleted: The decomposition of Eq. 3 has been the standard procedure for many years that attributes the meridional fluxes to advective-like transports by transient eddy, stationary eddy, and mean meridional circulations. This study has not considered energy transfer in the presence of eddies that transport warm air poleward and cold air equatorward. How wever, it could be imagined for the equator heat source experiment that there was a large-scale eddy at midlatitudes transporting warm air poleward and cold air equatorward and that a Lamb wave produced by a rapidly intensifying cloud cluster or tropical cyclone near the equator propagated polewards through it. For instance, in a similar manner as portrayed by Figs. 22f and 23b that show the rapidly propagating urface pressure perturbation. This is analogous to the scenario discussed in section 2.4. Presumably the fast moving Lamb wave wouldn't be too influen by the much slower winds of the large-scale  $\epsilon$  ... [6] ville Nicholls 8/19/18 5:57 PM Formatted: Highlight Melville Nicholls 8/19/18 5:57 PM Formatted: Highlight

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Omission of the term responsible for generating thermal compression waves on the right side of Eq. 10 does not always lead to small mass changes in the model domain as Klemp and Wilhelmson (1978) suggested would be the case for a cloud simulation. For instance, hurricane simulations that include radiation and initially have no clouds will show an increasing mean surface pressure due to net radiative cooling, particularly at night when there is no shortwave warming counteracting

- 5 longwave cooling, until enough latent heating occurs in the domain to counter this effect. Moreover inclusion of this term doesn't necessarily mean there will be no mass change in the domain. Fully compressible simulations with diabatic heating in clouds for instance will generate Lamb waves that propagate to the boundaries of the model domain where if there are radiative boundary conditions they may end up being partially reflected. This is because that while radiative boundary conditions are typically set up for the passage of slower moving gravity waves they may not be perfectly reflective to faster
- 10 moving waves. So some mass may start to exit the domain. Such mass changes may not be a problem as far as the accurate simulation of typical meteorological processes are concerned, but is something to be aware of.

The effects of thermally generated compression waves have yet to be fully assessed. It is likely that they are ubiquitous in the atmosphere, generated by diabatic heating variations caused by latent heat release, radiative forcing, and surface heating. Compression waves can also be caused by mass inputs and outputs due to water substance conversions such as evaporation

- 15 from the surface. Since the amplitudes of these propagating disturbances are very small it might be assumed their effects are negligible, but in this study the case has been made that this is probably incorrect. Potentially the slowing down of thermally generated compression waves and gravity waves due to the use of semi-implicit schemes could be a source of error in climate models, but just how big these errors might be has yet to be evaluated.
- Another issue that is brought up by the apparent role of Lamb waves in the transfer of total energy in the atmosphere is the 20 meaning of the term "heat transfer". It is common to think of heat as being carried from one place to another by the 20 movement of relatively warm air, sometimes referred to as convective heat transfer. As was discussed in section 2.4 this 21 usage is different from how heat is typically defined in thermodynamics as energy in transit from one system to another by 22 thermal interaction. Since the Earth's TOA radiative fluxes have a net input at low latitudes and output at high latitudes, then 23 for an energy balance to occur in the mean then there must be a poleward energy flux, given by the flux terms in equations
- 25 (1) and (2), and this has been termed a heat flux. This flux is complicated since it is comprised of fluxes of gravitational potential energy and latent heat, but it does at least have a term called the enthalpy flux, which is considered to be a convective heat flux that results in a transfer of internal energy. Now if a considerable amount of the internal energy is actually being transferred at the speed of sound and doesn't result in significant temperature perturbations as occurs in the numerical experiments in this study, then this further distances total energy transfer from what has been traditionally thought
- 30 of to a large degree as a convective heat transfer. Certainly the transfer of total energy that occurs in these experiments with a fully compressible model would not correspond to what would normally be considered a transfer of heat.

Latent heat transport (water vapour) is a quantity that is advected with the wind so that the transfers associated with expansion and compression only applies to fluxes of dry enthalpy and gravitational potential energy. However, the current view is that if energy is used to evaporate water at some location A and then the vapour is transported by air currents to

35 another location B where it condenses, then energy has been transported from A to B. This is not such a simple thing to conclude, as it may seem, if the condensation produces a Lamb wave that quickly transports the energy hundreds of kilometres away at the speed of sound.

#### **6** Conclusions

The first experimental set up in this study examined the response to a convective scale heat source. The fully compressible version of the model showed in the early stages expansion of the heated air and compression of the adjacent environment. A few minutes after the heat source had been turned on a laterally propagating Lamb wave emerged with highest pressure and density anomalies at the surface with a wave front that propagated away at the speed of sound. The reduction of density in Melville Nicholls 8/21/18 1:21 PM Deleted: 5 the heated region produced buoyancy and a strong updraft developed with compensating subsidence in the nearby environment. This subsidence also propagated in a wave-like manner, but with a slower speed of  $\sim$ 45 m s<sup>-1</sup>. Comparison with the standard version of RAMS that omits the term that involves the material rate of change of virtual potential temperature in

Eq. 10, did not show expansion of air in the heated region or compression of the adjacent air. Nevertheless the diagnosed
 density still decreased in the heated region. A comparison at 15 min showed the thermally generated buoyancy circulation was virtually identical to that of the fully compressible simulation and so for most cloud modelling purposes the terms on the
 right side of Eq. 10, can be safely neglected as found by Klemp and Wilhelmson (1978).

So far there has been no study that can be said to have definitely observed the low frequency Lamb waves generated by heat release in convective storms. Detection of thermally generated Lamb waves would bolster the conclusions from

- 10 numerical modelling studies that they exist and could be playing a role in redistribution of total energy and mass. In this study the value of the positive surface pressure perturbation associated with the Lamb wave at a distance of 300 km from the heat source was approximately 0.05 Pa. The strength of the updraft was quite weak, only  $\sim$ 4 m s<sup>-1</sup>, so this would only correspond to weak convection. For the NP2000 study, which simulated a strong convective storm, and included liquid and ice phase microphysics, the magnitude of the pressure perturbations were considerably larger having peak-to-peak values at
- 15 400 km from the storm of ~0.6 Pa. The time interval between these positive and negative peaks was ~20 min. Infrasound with periods of tens of seconds have been detected from severe weather (e.g. Bowman and Bedard 1971), however the only study to date that may possibly have detected low frequency Lamb waves generated by latent heat release in convective storms was by Nishida et al. (2014), although they hypothesized the main excitation mechanism for the background Lamb waves to be atmospheric turbulence. As mentioned in section 2.6 the rms amplitude of the Lamb waves they detected was 0.15 Pa, which falls within the range of these fully compressible simulations of convectively produced Lamb waves.
- The second experimental set up examined the response to a continent scale heat source applied near the surface. The surface pressure decreased over land and increased over the adjacent ocean. During the nine-hour simulation there was significant lateral transfer of total energy and mass offshore as far as 3000 km from the shoreline. Approximately a third of the total energy increase occurred over land, and two thirds over the ocean. A similar simulation without compression waves
- 25 showed a decrease of surface pressure over land, but no increase over the ocean. The net total energy did not increase in the domain even though there was a heat input and the net mass decreased. Comparing the horizontal velocities in the sea-breeze circulation there was approximately a 15% difference in their magnitudes. Running the fully compressible model without the Coriolis force resulted in more total energy and mass transfer off shore showing geostrophic adjustment led to significant confinement of the energy and mass. It seems reasonable to consider a horizontal length scale that is analogous to the Rossby
- 30 radius of deformation where rotational effects become as important as buoyancy effects. This would be given by the speed of sound divided by the Coriolis parameter, which at 45 degrees latitude for this experiment is approximately 3000 km. Obviously for a Coriolis parameter that depends on latitude the very large distances travelled by the compression waves makes the concept of a radius of deformation for these fast moving waves of limited utility.
- The equator heat source experiment initially created a symmetrical response, but later on as the wave front propagated to latitudes where the Coriolis force became important an interesting asymmetry developed. There was higher surface pressure to the east than the west and this was also reflected in the total energy and mass fields. The equator heat source produced significant meridional fluxes of enthalpy, potential energy and mass. Turning the heat source off at two hours allowed the thermally generated lamb wave to start to separate from the slower moving buoyancy circulation. The Lamb wave had a leading positive lobe of high pressure and a trailing negative lobe, which is a feature of a two-dimensional wave. Examining
- 40 the vertically summed total energy perturbation field it was clear that the main region of increased energy in the domain in response to the heating was concentrated in the leading lobe of the Lamb wave several thousands of kilometres from the centre of the heat source.

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These results reiterate previous results obtained many years ago that Lamb waves are able to transfer significant amounts of total energy at the speed of sound. It would be fair to say these earlier studies have had little impact on interpretations of the large scale total energy transport. This current study, which shows the vertically summed energy fields, should reinforce the hypothesis that Lamb waves could indeed play a role in the large scale transfer of total energy. There have been

- 5 numerous observational and numerical modelling studies that calculate the meridional atmospheric fluxes of total energy and find a good agreement with the net global energy inputs and outputs (e.g. Masuda 1988; Magnusdottir and Saravanan 1999; Trenberth and Stepaniak 2003; Yang et al. 2015). Therefore on the face of it there doesn't appear to be any problem with the current interpretation of atmospheric energy fluxes, or the ability of state of the art climate models to accurately simulate them. On the hand we would contend that the results of this current study and previous works are unlikely to be
- 10 fundamentally flawed, and this raises several questions: Are the studies showing considerable transfer of energy by Lamb waves too idealized and this transfer would be limited in a more realistic modelling framework? Do Lamb waves contribute significantly to the energy transport and global models are able to accurately simulate this transport, while perhaps there is a misinterpretation of the physical attribution to some degree? Is the slowing down of Lamb waves due to semi-implicit time differencing not really a substantial problem since it might be causing for the most part just a delayed response? On the other
- 15 hand is the slowing down of Lamb waves not causing just a delayed response, but also significantly changing the spatial scale of the response as suggested in section 5? Is the slowing down of Lamb waves due to semi-implicit time differencing causing them to have larger amplitude?

Another issue brought up by this study is that it has repercussions for the concept of heat transfer in a fluid. Total energy transfer is typically referred to as heat transfer, yet the mechanism of total energy transfer examined in this work doesn't have much connection to the more common notion of convective heat transfer. Finally, significant transfers of mass occurred at the speed of sound in these numerical experiments. If expansion and compression of air in response to heat sources and

- at the speed of sound in these numerical experiments. If expansion and compression of air in response to heat sources and sinks leads to large lateral redistributions of mass at the speed of sound this may have consequences for understanding the mass balance that exists in the long term mean in the atmosphere and perhaps seasonal variations.
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#### Table 1. List of Experiments

			Melville Nicholls 8/25/18 9:58 AM
Experiment	Description	•	Formatted: Font:10 pt
designation			Melville Nicholls 8/25/18 4:35 PM
1A	Convective scale heat source		Formatted Table
1B	Convective scale heat source, without compression waves		
2A	Continent scale heat source	~	
2B	Continent scale heat source, without compression waves		Melville Nicholls 8/25/18 4:28 PM
2C	Continent scale heat source, without the Coriolis force		Deleted:         Experiment         Description           1A         Convective scale heat sourc
3A	Equator heat source		
3B	Equator heat source, turned off at 2h		