



Quantification of the enhanced effectiveness of NO_x control from simultaneous reductions of VOC and NH₃ for reducing air pollution in Beijing-Tianjin-Hebei region, China

Jia Xing^{1,2}, Dian Ding¹, Shuxiao Wang^{1,2}, Bin Zhao^{1,2,5}, Carey Jang³, Wenjing Wu¹, Fenfen Zhang¹, Yun
5 Zhu⁴, Jiming Hao^{1,2}

¹State Key Joint Laboratory of Environmental Simulation and Pollution Control, School of Environment, Tsinghua University, Beijing 100084, China

²State Environmental Protection Key Laboratory of Sources and Control of Air Pollution Complex, Beijing 100084, China

³The U.S. Environmental Protection Agency, Research Triangle Park, NC 27711, USA

10 ⁴College of Environmental Science & Engineering, South China University of Technology, Guangzhou Higher Education Mega Center, Guangzhou, China

⁵Joint Institute for Regional Earth System Science and Engineering and Department of Atmospheric and Oceanic Sciences, University of California, Los Angeles, CA 90095, USA

Correspondence to: Shuxiao Wang (shxwang@tsinghua.edu.cn)

15 **Abstract.** As one common precursor for both PM_{2.5} and O₃ pollution, NO_x gains great attention because its controls can be beneficial for reducing both PM_{2.5} and O₃. However, the effectiveness of NO_x controls for reducing PM_{2.5} and O₃ are largely influenced by the ambient levels of NH₃ and VOC, exhibiting strong nonlinearities characterized as NH₃-limited/-poor and NO_x-/VOC-limited conditions, respectively. Quantification of such nonlinearities is prerequisite to making suitable policy decisions but limitations of existing methods were recognized. In this study, a new method was developed by fitting multiple simulations of a
20 chemical transport model (i.e., Community Multi-scale Air Quality Modeling System (CMAQ)) with a set of polynomial functions (denoted as “pf-RSM”) to quantify responses of ambient PM_{2.5} and O₃ concentrations to changes in precursor emissions. The accuracy of the pf-RSM is carefully examined to meet the criteria of a mean normalized error within 2% and a maximal normalized error within 10% by using forty training samples with marginal processing. An advantage of the pf-RSM method is that the nonlinearity in PM_{2.5} and O₃ responses to precursor emission changes can be characterized by quantitative indicators, including
25 (1) peak ratio (denoted as PR) representing VOC-limited or NO_x-limited condition, (2) suggested reduction ratio of VOC to NO_x (denoted as VNr) to avoid increasing O₃ under VOC-limited condition, (3) flex ratio (denoted as FR) representing NH₃-poor or NH₃-rich condition, and (4) enhanced benefits in PM_{2.5} reductions from simultaneous reduction of NH₃ with the same reduction rate of NO_x. A case study in Beijing-Tianjin-Hebei region suggested that most urban areas present strong VOC-limited condition with PR from 0.4 to 0.8 in July, implying that the NO_x emission reduction rate need be greater than 20%-60% to pass the transition
30 from VOC-limited to NO_x-limited. A simultaneous VOC control (VNr is about 0.5-1.2) can avoid increasing O₃ during the transition. For PM_{2.5}, most urban areas present strong NH₃-rich condition with PR from 0.75-0.95, implying the NH₃ is sufficiently abundant to neutralize extra nitric acid produced by an additional 5%-35% of NO_x emissions. Enhanced benefits in PM_{2.5} reductions from simultaneous reduction of NH₃ were estimated to be 0.04-0.15 μg m⁻³ PM_{2.5} per 1% reduction of NH₃ along with NO_x, with greater benefits in July when the NH₃-rich condition is not as strong as in January. Thus, simultaneously reducing NH₃ and VOC
35 emission along with NO_x reduction is recommended to assure the control effectiveness of PM_{2.5} and O₃.



1. Introduction

Tropospheric ozone (O_3) and fine particulate matter ($PM_{2.5}$) are two major air pollutants that exert significant effects on human health (Forouzanfar et al., 2015; GBD-MAPS, 2016; Cohen et al., 2017) and the global climate (Myhre et al., 2013). Effective controls on the anthropogenic sources of O_3 and $PM_{2.5}$ are necessary to reduce their harmful effects on health and climate. As one common precursor for both O_3 and $PM_{2.5}$, NO_x significantly influences on the ambient concentrations of O_3 and $PM_{2.5}$. Previous studies suggested that the deterioration of air quality in China over past two decades is highly associated with the increasing trend of national NO_x emissions (Wang et al., 2011) which are estimated to be increased from 11.0 Mt in 1995 to 26.1 Mt in 2010 (Zhao et al., 2013). Since early 2010s, strict regulations have been implemented on power plants and vehicle emissions, leading to a considerable NO_2 reduction witnessed by the declining trend in satellite-retrieved NO_2 column densities (i.e., reduced by 32% from 2011 to 2015, Liu et al., 2016). However, the reduction in $PM_{2.5}$ is not as much significant as that in NO_2 or SO_2 (Fu et al., 2017). The reason might be associated with the increases of NH_3 which has not been well-controlled to date in China and exhibits an increasing trend by nearly 20% from 2011 to 2014 observed from satellite-retrievals (Fu et al., 2017). Such increases of NH_3 weakened the control effectiveness of SO_2 and NO_2 in $PM_{2.5}$ reduction (Wang et al., 2011; Fu et al., 2017). Worse still, recently O_3 concentrations exhibit an increasing trend in some cities in Yangtze River Delta and Pearl River Delta (Li et al., 2014). The number of days on which O_3 concentration exceeded the national standard (i.e., 8-hour maxima level less than $160 \mu g m^{-3}$) was increased from 7.2% in 2010 to 12.7% in 2015 in Shanghai. The annual averaged O_3 was increased by 0.86 ppb/year from 2006 to 2011 in Guangdong, accompanied by a correspondingly NO_2 reduction of 0.61 ppb/year (Li et al., 2014). Such increase of O_3 is likely to be associated with the NO_x reductions in the area that located at the VOC-limited condition (i.e., decreased NO_x leads to increased O_3), implying the disbenefit of NO_x controls for O_3 reduction under VOC-limited condition. How to assure the effectiveness of NO_x controls for reducing O_3 and $PM_{2.5}$ becomes a difficult challenge for policy design (Cohan et al., 2005; Tsimpidi et al., 2008). To address that challenge, studies on investigating the relationship between the responses of O_3 and $PM_{2.5}$ to precursor emission changes have been conducted. Indicators such as NO_y , H_2O_2/HNO_3 and $H_2O_2/(O_3+NO_2)$ as well as the degree of sulfate neutralization, gas ratio, and adjusted gas ratio are used to define the O_3 and $PM_{2.5}$ chemistry respectively in many studies (Sillman et al., 1995; Tonnesen et al., 2000; Zhang et al., 2009; Liu et al., 2010; Ye et al., 2016). The aforementioned indicators can provide rapid assumptions for the baseline status of pollution sensitivities to precursor emissions. Modeling studies with chemistry transport models (CTMs) have been conducted to investigate the responses of O_3 and $PM_{2.5}$ to emission perturbation through sensitivity analyses, such as decoupled direct methods (DDMs) and high-order DDMs (Hakami et al., 2003; Cohan et al., 2005), and source apportionment technology such as ozone source apportionment technology (Dunker et al., 2002), particulate matter source apportioning technology (Wagstrom et al., 2008), integrated source apportionment method (Kwok et al., 2013; 2015). A statistical response surface model (RSM) has been developed and successfully used in O_3 and $PM_{2.5}$ response simulations in our previous studies (Wang et al., 2011; Xing et al., 2011; 2017; Zhao et al., 2015a; 2017). In contrast to sensitivity and source apportionment techniques, the RSM provides real-time response to a wide range of emission perturbation, from -100% totally controlled to +20% (Zhao et al., 2017) or even +100% doubled baseline level (Xing et al., 2011), thus is able to quantify the strong nonlinear responsiveness of O_3 and $PM_{2.5}$ to reduction in their precursor emissions, manifested as the volatile organic compound (VOC)-limited or NO_x -limited O_3 chemistry (Seinfeld et al., 2006) and NH_3 -rich or NH_3 -poor for inorganic PM chemistry (Zhang et al., 2009). The RSM model is based on regression from thousands of “brute-force” simulations with chemical transport model (CTM) by using a maximum likelihood estimation - experimental best linear unbiased predictors (hereafter referred as “regression-based RSM”). However, such a large amount of CTM simulations required by RSM results in heavy computing burden (usually one CTM scenario for a month simulation needs 400 CPU-hour, depending on the simulated domain size and selected mechanism) which largely limits the application of RSM. Moreover, the regression-based RSM model is treated as a black box which is not



easy to investigate the nonlinearity (e.g., peak value, derivative) of the predicted system.

To address the issue in regression-based RSM, this study aims to develop a polynomial family of functions in RSM model to represent the responsive behavior of O_3 and $PM_{2.5}$ concentrations to precursor emissions. The RSM with polynomial functions is referred to as “pf-RSM” in the remainder of this paper. Effectiveness of air pollution controls by NO_x and other precursor emission reductions was investigated by the newly developed pf-RSM.

2. Methods

2.1. Model setup and data

The data used in this study were obtained from a recent regression-based RSM study conducted in the Beijing–Tianjin–Hebei (BTH) region in China. One baseline scenario and 1100 “brute-force” controlled scenarios were performed using the Community Multi-scale Air Quality (CMAQ) Modeling System (version 5.0.1) in a 12×12 -km domain over the BTH region. The details of the Weather Research and Forecasting–CMAQ model and emissions were described in a previous study (Zhao et al., 2016). We used the SAPRC99 gas-phase chemistry module (Carter, 2003) and the sixth-generation CMAQ aerosol model (AERO6) (Appel et al., 2013) with the treatment of organic aerosols replaced with the 2D-VBS (two-dimensional volatility basis set) framework (Zhao et al., 2015b; 2017). The simulation period is January and July in 2014 to represent winter and summer respectively. The emission data was developed by Tsinghua University based on a bottom-up method with a high spatial and temporal resolution (Zhao et al., 2016).

The responses of O_3 (daily 1-hour maxima) and $PM_{2.5}$ (daily 24-hour average) to the emissions of five group of precursors, namely NO_x , SO_2 , NH_3 , VOC + intermediate VOC (denoted as “VOCs”), and primary organic aerosol (POA) from five regions, namely Beijing, Tianjin, northern Hebei (denoted as “HebeiN”), eastern Hebei (denoted as “HebeiE”), and southern Hebei (denoted as “HebeiS”) were analyzed. The O_3 and $PM_{2.5}$ concentrations were analyzed in urban areas of prefecture-level cities in the five target regions (Zhao et al., 2017). The performance of the model system was evaluated in our previous paper (Zhao et al., 2017; Xing et al., 2017) which suggested acceptable CMAQ model performance that meets the recommended benchmark in the comparison with ground-observed concentrations, as well as acceptable performance of regression-based RSM model with mean normalized errors within 3%.

In the regression-based RSM developed previously, the system supports to investigate different emission changes for 5 precursors in 5 regions (i.e., extended RSM, ERSM described in Zhao et al., 2015a and Xing et al., 2017). In this study, for simplification, the pf-RSM was built on the simultaneous change in one or all regions (i.e., controls separately in individual region, or jointly controls in all 5 regions with same control ratio). However, the pf-RSM can be extended to pf-ERSM following the same structure as regression-based ERSM but using polynomial functions for $PM_{2.5}$, O_3 and precursors.

2.2. Development of the pf-RSM

In general, tropospheric O_3 and $PM_{2.5}$ concentrations are contributed by its sources and sinks through a series of atmospheric processes, such as horizontal or vertical advection and diffusion, gas phase chemistry, and deposition. The nonlinear behavior in each of these processes contributes to the nonlinearity in the responses of concentrations to precursor emissions. Similar responsive functions can be expected across regions and time; for example, a universal ozone isopleth diagrams developed using the empirical kinetic modeling approach of the U.S. Environmental Protection Agency (Gipson et al., 1981) represents the general O_3 responsiveness to NO , and VOC concentrations. A fitting-based model was developed to simplify the O_3 responsiveness to precursor emissions by using a general formulation (Heyes, et al., 1996). The simplified formulation of concentrations to emissions



can be easily applied to optimize control strategies (Heyes et al., 1997), which is a great advantage over the regression-based model. Moreover, with the fitting-based RSM, the inclusion of a prior knowledge of pollutant responses to emissions might substantially reduce the case number required to build the RSM (see Figure 1).

In this study, the prior knowledge of pollutant responses to emissions was characterized as a series polynomial functions by the previous developed regression-based RSM. The coefficients of the function was estimated by fitting the function with training samples selected “brute-force” cases to match with the regression-based RSM prediction (i.e., isopleth validation) and the CMAQ simulations (i.e., out-of-sample validation). The flow scheme of the development of the pf-RSM is displayed in Figure 2. The structure of the polynomial function to be fitted is expressed as follows:

$$\Delta Conc = \sum_{i=1}^n X_i \cdot (E_{NO_x})^{a_i} \cdot (E_{SO_2})^{b_i} \cdot (E_{NH_3})^{c_i} \cdot (E_{VOCs})^{d_i} \cdot (E_{POA})^{e_i} \quad (E1)$$

where:

$\Delta Conc$ is the response of O_3 and $PM_{2.5}$ concentrations (i.e., change to the baseline concentration), the concentration value can be hourly, monthly or annual averages at either single grid cell or aggregated grids in target region;

E_{NO_x} , E_{SO_2} , E_{NH_3} , E_{VOCs} , and E_{POA} is the change ratio of NO_x , SO_2 , NH_3 , $VOCs$, and POA emissions, respectively, related to baseline (i.e., baseline = 0);

a_i , b_i , c_i , d_i , and e_i represent the nonnegative integer powers of E_{NO_x} , E_{SO_2} , E_{NH_3} , E_{VOCs} , and E_{POA} , respectively; and X_i is the coefficient of term i .

$\Delta Conc$ is calculated from a polynomial function of five variables (E_{NO_x} , E_{SO_2} , E_{NH_3} , E_{VOCs} , E_{POA}). The number of terms (n), coefficients (X_i) and degree (a_i , b_i , c_i , d_i , e_i) of each term were determined using the following steps.

2.2.1. Degree examination

First, the degrees of the five variables were determined individually by fitting the responsive function with a polynomial of a single indeterminate plot (Figure 3). The $PM_{2.5}$ responses to the change in each precursor emission estimated using the RSM were fitted by a series of polynomials of a single indeterminate plot with different orders from the first (linear) to the fifth degree, as shown in following functions (similar to E1):

$$\Delta Conc = \sum_{i=1}^a A_i \cdot (E_p)^i \quad (E2)$$

where:

$\Delta Conc$ is the response of O_3 and $PM_{2.5}$ concentrations to changes in individual precursor emissions;
 E_p is the change ratio of one precursor (the subscript P can represent NO_x , SO_2 , NH_3 , $VOCs$, or POA) emission related to baseline;

A_i is the coefficient of term i ; and

the superscript a is the degree of precursor P , which determined the order of the best fitting polynomials.

Figure 3(a) presents $PM_{2.5}$ responses to changes in NO_x , shows that $PM_{2.5}$ responses cannot be well fitted with polynomials of order lower than 3. Thus the degree of NO_x to $PM_{2.5}$ should be 4. By contrast, $PM_{2.5}$ responses to changes in SO_2 (Figure 3a) can be well fitted linearly; thus, the degree of SO_2 to $PM_{2.5}$ is 1. The degrees of five precursors to O_3 and other pollutants were also examined, and the results are summarized in Table 1. Highly nonlinear responses were found for both O_3 and $PM_{2.5}$ to the NO_x , VOC and NH_3 emissions. That might be associated with the strong nonlinearity in the atmospheric oxidation reactions and aerosol thermodynamics which are parameterized with SAPRC99 gas-phase chemistry module and the AERO6 with 2D-VBS module, respectively in CMAQ used in this study.



2.2.2. Term selection

The correlation among variables (i.e., product term) was determined in pairs by fitting the responsive function with a polynomial of a two-indeterminate isopleth, expressed as follows:

$$\Delta Conc = \sum_{i=1}^b B_i \cdot (E_{P1})^{a_i^1} \cdot (E_{P2})^{a_i^2} \quad (E3)$$

5 where:

$\Delta Conc$ is the response of O_3 and $PM_{2.5}$ concentrations to changes in individual precursor emissions;
 E_{P1} and E_{P2} are the change ratios of two precursor ($P1$ and $P2$ can represent any two of NO_x , SO_2 , NH_3 , VOCs, or POA) emission related to baseline;

B_i is the coefficient of product term i ;

10 a_i^1 and a_i^2 are the degrees of precursors $P1$ and $P2$, respectively; and

the superscript b is the number of total interaction terms between $P1$ and $P2$ (i.e., a_i^1 multiplied by a_i^2).

The product term $E_{P1}E_{P2}$ represents the interaction between $P1$ and $P2$. If no such interaction occurs, the product term $E_{P1}E_{P2}$ is 0. The interaction examination was conducted by comparing predicted responses to joint changes in two precursor emissions between with-interaction (E4) and no-interaction (E5).

$$15 \quad \Delta Conc = \sum_{i=1}^a A_i \cdot (E_{P1})^i + \sum_{j=1}^{a'} A'_j \cdot (E_{P2})^j + \sum_{i=1}^b B_i \cdot (E_{P1})^{a_i^1} \cdot (E_{P2})^{a_i^2} \quad (E4)$$

$$\Delta Conc = \sum_{i=1}^a A_i \cdot (E_{P1})^i + \sum_{j=1}^{a'} A'_j \cdot (E_{P2})^j \quad (E5)$$

If responses calculated using eq (E5) are equal or approximate to those calculated using eq (E4), no interactions between $P1$ and $P2$ would occur (i.e., the product term $E_{P1}E_{P2}$ is 0). If responses are not equal or approximate to each other, interactions between $P1$ and $P2$ cannot be overlooked. However, we wanted to limit the number of terms in the polynomial function; thus, we did not
20 include all interaction terms between $P1$ and $P2$ in the function. Instead, we gradually selected interaction terms between $P1$ and $P2$ from eq (E3), until the responses matched with those calculated using eq (E4).

An example was shown in Figure S1 which presents $PM_{2.5}$ responses to joint changes in NO_x and NH_3 emissions in July. The $PM_{2.5}$ response calculated using eq (E4) (with all interaction terms) was consistent with that estimated using the regression-based RSM. The $PM_{2.5}$ response calculated using eq (E5) (with no interaction terms) exhibited a noticeable discrepancy compared with those
25 calculated using eq (E4) and estimated using the regression-based RSM. With one selected interaction term, the $PM_{2.5}$ response exhibited a substantial improvement compared with that calculated using eq (E4), thereby indicating interactions between NO_x and NH_3 emissions for $PM_{2.5}$.

The results of term selections for both O_3 and $PM_{2.5}$ are summarized in Figure 4. The interaction terms of NO_x and VOCs are included for both pollutants. SO_2 and POA did not interact with other species.

30 2.2.3 Sampling optimization

Training samples were generated to fit the polynomial function for each pollutant. The number of training samples needed to be as small as possible, but greater than the number of terms (i.e., unknown coefficients) in the polynomial function. Our previous study (Xing et al., 2011) suggested that samples generated through uniform methods, such as Latin hypercube sampling (LHS), and a Hammersley quasi-random sequence sample (HSS), could provide even distributions for individual sources. However, additional
35 marginal processing is recommended for its ability to improve the performance of prediction at margins.

Sensitivity analysis of the number and distributions of training samples was conducted in this study. Groups of 22, 30, 40, 50 training samples were sampled using uniform-distributed HSS. Additional marginal processing was conducted using a power function ($n = 2$) from uniform-distributed HSS on the samples, expressed as follows:



$$TX = \begin{cases} \left(\frac{x-a}{b-a}\right)^2 \times 2 \times (b-a) + a, & X \leq a + \frac{b-a}{2} \\ \left[1 - \left(\frac{b-x}{b-a}\right)^2 \times 2\right] \times (b-a) + a, & X > a + \frac{b-a}{2} \end{cases} \quad (\text{E6})$$

where:

X is sampled from a uniform-distributed HSS in section [a, b] (in this study we selected [0, 1.2], which denotes that emission changes were from all- controlled to a 20% increase); and

5 TX represents the samples after the marginal processing.

The training samples were predicted using the regression-based RSM and subsequently used to fit the polynomial function for all pollutants. We selected two datasets as out-of-samples to validate the fitting polynomial function, i.e., jointly controls in 5 regions (denoted as “OOS100”) and single regional controls (denoted as “OOS15”) (see Table 2). The control matrixes of these two datasets are provided in supplementary information (Table S1).

10 The predictive performance of the pf-RSM was evaluated using five statistical indices, namely the mean normalized error (MeanNE), maximal normalized error (MaxNE), mean fractional error (MeanFE), maximal fractional error (MaxFE) and correlation coefficient (R), each calculated as follows:

$$\text{MeanNE} = \frac{1}{N} \sum_{i=1}^N \frac{|M_i - O_i|}{O_i} \quad (\text{E7})$$

$$\text{MaxNE} = \max\left(\frac{|M_i - O_i|}{O_i}\right) \quad (\text{E8})$$

$$15 \quad \text{MeanFE} = \frac{1}{N} \sum_{i=1}^N \frac{|M_i - O_i|}{M_i + O_i} \times 2 \quad (\text{E9})$$

$$\text{MaxFE} = \max\left(\frac{|M_i - O_i|}{M_i + O_i} \times 2\right) \quad (\text{E10})$$

$$R = \sqrt{\frac{[\sum_{i=1}^N (M_i - \bar{M})(O_i - \bar{O})]}{\sum_{i=1}^N (M_i - \bar{M})^2 \sum_{i=1}^N (O_i - \bar{O})^2}} \quad (\text{E11})$$

where:

20 M_i and O_i are the pf-RSM -predicted and CMAQ-simulated value of the i^{th} data in the series which can be a series of days, grid cells or control cases; and

\bar{M} and \bar{O} are the average pf-RSM-predicted and CMAQ-simulated value over the series.

2.3 Indicators for representing nonlinearity in responses to precursor emissions

In our previous RSM studies, indicators representing the nonlinearity of O_3 and $PM_{2.5}$ responses to precursor emissions have been defined as the peak ratio (PR) for O_3 (Xing et al., 2011) and flex ratio (FR) for $PM_{2.5}$ (Wang et al., 2011), respectively.

25 For O_3 , the PR is the NO_x emissions that produce maximum O_3 concentrations under baseline VOC emissions (see in Figure 5a). A PR lower than 1 (i.e., baseline) indicates that the baseline condition is VOC -limited; in all other cases, the baseline condition is NO_x -limited.

The previous calculations for the PR were performed through a looping procedure in the RSM statistical system, which is not straightforward. One advantage of the pf-RSM is that the PR can be directly calculated from the polynomial function as follows:

$$30 \quad PR = 1 + E_{NO_x} \left| \frac{\partial \Delta Conc_{O_3}}{\partial E_{NO_x}} \right|_{\Delta Conc_{O_3}=0} E_{NO_x} \in [a, b] \quad (\text{E12})$$

where

$\frac{\partial \Delta Conc_{O_3}}{\partial E_{NO_x}}$ is the first derivation of the $Conc_{O_3}$ response to E_{NO_x} .

In addition, we can further quantify how much simultaneous control of VOC is required to avoid increasing O_3 from the NO_x controls under VOC-limited condition (see in Figure 5b). The suggested VOC controls can be represented as the ratio of VOC to



NO_x (denoted VNr) which can be calculated as follows:

$$VNr = X \left| \frac{\partial \Delta Conc_{O_3}}{\partial E_{NO_x}} \right|_{\partial \Delta Conc_{O_3} = 0} \quad \text{when } PR < 1, \quad X = E_{VOC} / E_{NO_x} \quad (E13)$$

where

$\frac{\partial \Delta Conc_{O_3}}{\partial E_{NO_x}}$ is the first derivation of the $Conc_{O_3}$ response to E_{NO_x} when $E_{VOC} = X \times E_{NO_x}$

5 For PM_{2.5}, here we defined the FR as the NH₃ emission ratio at the flex nitrate (or PM_{2.5}) concentrations (i.e., when the second derivation of the function of concentration sensitivities to NH₃ emissions is zero) under baseline NO_x emissions (see in Figure 6a). A FR greater than 1 indicates that the baseline condition is NH₃-poor (i.e., large sensitivity of PM_{2.5} to NH₃); in all other cases, the baseline condition is NH₃-rich (small sensitivity of PM_{2.5} to NH₃). The values of FR also suggest the transition point between two schemes.

10 Similarly, the FR can be directly calculated from the polynomial function as follows:

$$FR = 1 + E_{NH_3} \left| \frac{\partial^2 \Delta Conc_{PM}}{\partial E_{NH_3}^2} \right|_{\partial^2 \Delta Conc_{PM} = 0} E_{NH_3} \in [a, b] \quad (E14)$$

where

$\frac{\partial^2 \Delta Conc_{PM}}{\partial E_{NH_3}^2}$ is the second derivation of the $Conc_{PM}$ response to E_{NH_3} .

15 Further, we can quantify the extra benefit in PM_{2.5} reductions (denoted as ΔC) from simultaneous reduction of NH₃ along with the control of NO_x (see in Figure 6b), which can be calculated as follows:

$$\Delta C = \left(\frac{\partial \Delta Conc_{PM_{2.5}}}{\partial E_{NO_x}} \right) \Big|_{E_{NH_3} = E_{NO_x}} - \left(\frac{\partial \Delta Conc_{PM_{2.5}}}{\partial E_{NO_x}} \right) \Big|_{E_{NH_3} = 0} \quad (E15)$$

where

$\frac{\partial \Delta Conc_{PM_{2.5}}}{\partial E_{NO_x}} \Big|_{E_{NH_3} = E_{NO_x}}$ is the first derivation of the $Conc_{PM_{2.5}}$ response to E_{NO_x} when $E_{NH_3} = E_{NO_x}$;

$\frac{\partial \Delta Conc_{PM_{2.5}}}{\partial E_{NO_x}} \Big|_{E_{NH_3} = 0}$ is the first derivation of the $Conc_{PM_{2.5}}$ response to E_{NO_x} when $E_{NH_3} = 0$

20 The PR and FR are the results of $1 + E_{NO_x}$ and $1 + E_{NH_3}$, respectively, corresponding to the extreme value point and inflexion point of $Conc_{O_3}$ and $Conc_{PM}$, respectively, in section [a, b] (i.e., [0, 1.2] in this study). The VNr and ΔC were estimated for the five regions in BTH.

3. Results

3.1 Sensitivity analysis on training sample number and distribution

25 Table 3 summarizes the performance of the pf-RSM with different training samples for predicting PM_{2.5} and O₃. Generally, good agreement was observed in all cases. Even with 20 training samples (only five more than the number of terms in the polynomial function), the MeanNE and MeanFE were lower than 3.1% and 1.5% respectively, and the MaxNE and MaxFE were lower than 15.1% and 7.0%, respectively. The R values were greater than 0.8. The performance improved with an increase in training sample number. When 50 training samples were selected, the MeanNE and MeanFE were lower than 1.7% and 0.8% respectively, and the
 30 MaxNE and MaxFE were lower than 8.7% and 4.2%, respectively. The R values were greater than 0.94. Additional marginal processing improved the performance of PM_{2.5} and O₃ prediction by reducing the maximal errors rather than the mean errors. In all cases, the MaxNE and MaxFE in O₃ decreased from 12.4% and 5.8%, to 5.5% and 2.7%, respectively. The MaxNE and MaxFE in PM_{2.5} slightly decreased from 15.1% and 6.98%, to 15.0% and 6.97% respectively. To meet the criteria of MeanNE within 2% and MaxNE within 10% (which is comparable to the performance of previous
 35 regression-based RSM), use of 40 training samples with marginal processing (to improve boundary conditions) is recommended.



One kind of visual comparison, i.e., isopleth validation of the pf-RSM with different training samples was conducted, and its details are shown in supplementary information (Figures S2–S9). The performance of the pf-RSM with less than 40 training samples exhibited a noticeable discrepancy (i.e., spatial pattern of the response under the controls) compared with that of the regression-based RSM. The 40 training samples presented good agreement with the predictions of the regression-based RSM. Additional marginal processing also improved the performance of the pf-RSM.

3.2 Application of the polynomial function at different locations and times

First, we applied the pf-RSM in each grid cell in the simulated domain. The base case and 40 controlled scenarios simulated by the CMAQ model (41 training samples in total) were used to fit the function of each grid cell. Two out-of-sample CMAQ cases (i.e., Case 1: moderate control with E_{NO_x} , E_{SO_2} , E_{NH_3} , E_{VOCs} and $E_{\text{POA}} = -49\%$, -45% , -20% , -64% , and -20% respectively; Case 2: strict control with E_{NO_x} , E_{SO_2} , E_{NH_3} , E_{VOCs} and $E_{\text{POA}} = -76\%$, -79% , -81% , -83% , and -73% , respectively) were used to validate the performance of the pf-RSM.

Figures 7 and 8 presents the spatial distribution of CMAQ-simulated and pf-RSM-predicted $\text{PM}_{2.5}$ and O_3 in baseline and their responses in two control scenarios. $\text{PM}_{2.5}$ predictions by the pf-RSM exhibited the same values in the baseline scenario as those simulated by the CMAQ model because the ΔConc is 0 with no perturbations in emissions (E1). With the reduction of emissions in the two control cases, the $\text{PM}_{2.5}$ and O_3 concentrations were reduced substantially in the CMAQ and pf-RSM predictions. The pf-RSM and CMAQ made very similar predictions for both cases, with normalized errors all within 5.6% for $\text{PM}_{2.5}$ and 2.0% for O_3 across the domain.

The performance of $\text{PM}_{2.5}$ and O_3 prediction in the pf-RSM across grid cells was summarized in Table S2. Larger errors were shown in Case 2 than in Case 1 because of relatively poor performance at the margin areas, where emissions were greatly controlled (Xing et al., 2011). Under moderate control condition (i.e., Case 1), smaller errors were observed in polluted regions for $\text{PM}_{2.5}$ and O_3 because of larger denominators (i.e., a high concentration). However, under strict control conditions (i.e., Case 2), larger errors were evident in more polluted regions, particularly for $\text{PM}_{2.5}$, indicating that the biases due to marginal effects were more prevalent in polluted regions.

Second, we applied the pf-RSM on each day in 2 simulated months (i.e., January and July, 2014). The same 41 training samples and 2 additional CMAQ cases were used to fit and validate the pf-RSM on each day.

The daily series of the CMAQ-simulated and pf-RSM-predicted 24-hour averaged $\text{PM}_{2.5}$ and 1-hour maxima O_3 in baseline and two control scenarios are shown in Figure 9. Generally, the pf-RSM-predicted daily $\text{PM}_{2.5}$ and O_3 concentrations fairly well matched with CMAQ model simulations, with normalized errors within 12.7% and 6.5% for $\text{PM}_{2.5}$ and O_3 , respectively. Substantial reductions in $\text{PM}_{2.5}$ were observed in Case 2, where strict controls were applied. Noticeable biases were observed on January 23rd when $\text{PM}_{2.5}$ levels were high in Beijing and HebeiS. Reductions in O_3 were noticeable in both control cases, particularly on days when O_3 levels were high. However, increases in O_3 were observed on July 21–23, after the controls were applied and when O_3 levels were low. This can be explained by the O_3 chemistry scheme being in a strong VOC-limited condition on days with low O_3 levels, resulting in enhanced O_3 from NO_x controls (Xing et al., 2011). The pf-RSM also reproduced increases in O_3 on those days. The performance of $\text{PM}_{2.5}$ and O_3 prediction in the pf-RSM throughout the simulation period was summarized in Table S3. The MeanNEs for $\text{PM}_{2.5}$ and O_3 were within 3.7% and 1.3% respectively. Larger errors were evident in Case 2 than in Case 1 because of poor performance at margin areas, where emissions are greatly controlled (Xing et al., 2011). These biases in Case 2 became larger on more polluted days, particularly for $\text{PM}_{2.5}$, suggesting that marginal biases were more evident during polluted period.



3.3 Quantification of nonlinearities in control effectiveness for reducing PM_{2.5} and O₃

The nonlinear effectiveness of emission control for reducing PM_{2.5} and O₃ can be quantified by the indicators defined in Section 2.3. The FR values across grid cells were calculated using eq (E14) for PM_{2.5} chemistry in January (Figure 10a). Most of the study regions exhibited FR values lower than 1, suggesting a strong NH₃-rich condition. These results are consistent with those of previous studies (Liu et al., 2010; Wang et al., 2011). Larger FR values (slightly lower than 1.0) were observed in the central and southern regions (i.e., Beijing, Tianjin and HebeiS) than in other regions, suggesting that the PM_{2.5} concentrations were sensitive to both NO_x and NH₃ controls, possibly because of the high SO₂ and NO_x emissions in Beijing, Tianjin and HebeiS (Zhao et al., 2016), which led to the high consumption of NH₃ neutralized with H₂SO₄ and HNO₃, as well as high PM_{2.5} concentrations (Figure 5).

Table 4 summarized the indicators at urban areas of prefecture-level cities in the five target regions. In both January and July, most of the urban areas present NH₃-rich condition with FR from 0.75-0.95 (Table 4), implying the NH₃ is sufficiently abundant to neutralize extra nitric acid produced by an additional 5%-35% (i.e., =1/FR-1) of NO_x emissions, which is consistent with our previous study (Wang et al., 2011). The extra benefit in PM_{2.5} reductions from simultaneous reduction of NH₃ along with the control of NO_x was estimated to be 0.04-0.15 μg m⁻³ PM_{2.5} per 1% reduction of NH₃. Larger benefit in PM_{2.5} reductions by simultaneous reduction of NH₃ was found in July when the NH₃-rich condition is not as strong as in January.

The PR values for O₃ chemistry in July were calculated using eq (E12), as shown in Figure 10b. Different PR values were observed in urban and downwind areas, which is consistent with the findings of previous studies (Xing et al., 2011). Smaller PRs (0.4–0.8, see Table 4) were evident in urban areas (i.e., megacities such as Beijing, Tianjin, Shijiazhuang, and Tangshan), where NO_x emissions are saturated, resulting in a strong VOC-limited condition. This indicates that the control of NO_x could result in an increase of O₃; however, O₃ would decrease with 20%–60% (i.e., =1-PR) control of NO_x. To avoid increasing O₃ during the transition from VOC-limited to NO_x-limited condition, a simultaneous VOC reduction by 0.5-1.2 times as the rate of NO_x reduction is recommended. Stronger VOC-limited condition is found in January, while O₃ concentration is considerably lower than in July. However, the strong VOC-limited condition in January will also lead to a considerable disbenefit of NO_x reduction for PM_{2.5} controls (see the isopleth plot of PM_{2.5} response to NO_x and NH₃ emission changes in Figure S6, also found in Zhao et al., 2017) because the enhanced atmospheric oxidation ability by reducing NO_x under VOC-limited condition will facilitate the formation of secondary aerosols. Therefore simultaneous VOC reduction can help avoid such increase of PM_{2.5} associated with NO_x controls under strong VOC-limited condition in January. Notably, the O₃ discussed in this paper refers to the monthly averages of daily 1-hour maximum values. The PR values varied considerably between the clean and polluted days, suggesting a mostly NO_x-limited condition during polluted periods which are usually subject to a more severe O₃ burden (Xing et al., 2011). Nevertheless, the control of NO_x emissions is critical for reducing regional O₃ and PM_{2.5}, however, it is recommended to simultaneously reduce VOC and NH₃ emission along with NO_x reduction to avoid the risk of increasing O₃ and gain extra benefit in PM_{2.5} reduction.

4. Summary and Conclusion

Quantification of the effectiveness of air pollution controls by emission mitigations needs an accurate representation of the nonlinear responses of ambient O₃ and PM_{2.5} concentrations to precursor emission changes. To address this challenge, this study proposed a new method by fitting multiple simulations of a chemical transport model with a set of polynomial functions, called “pf-RSM”. The pf-RSM method was successfully applied in a study of BTH region in China. The pf-RSM method characterizes the nonlinearity in the air quality response to emission changes. In the polynomial functions developed in this study, high degrees were found for the responses to the emissions of NO_x, VOC and NH₃ which exhibit stronger nonlinear behavior than SO₂ and POA.



The interaction terms of NO_x and VOC are included for both $\text{PM}_{2.5}$ and O_3 , indicating that atmospheric oxidations play significant role in the nonlinearity of air quality responses. The interaction term of NO_x and NH_3 emissions is also considered for $\text{PM}_{2.5}$, suggesting the nonlinearity in nitrate formation and aerosol thermodynamics.

5 After the application of a prior knowledge of the pollutant responsiveness to emissions in the RSM system, the cases required for single regional pf-RSM development were substantially decreased to 40 samples, compared with the previous requirement of over 100 samples, imply that the fitting-based RSM (i.e., pf-RSM) is three time faster than previous regression-based RSM. The pf-RSM system in this study operates rapidly, and thus can quickly generate responses with high spatial and temporal resolutions, thereby further facilitating cost-benefit optimization and enabling further assessment studies to be conducted. The polynomial functions developed in this study have been successfully applied in all grid cells across the simulated domain and all days across 10 the simulated periods for both January and July, indicating the combination of terms selected in this study is spatially / temporally independent as it mainly depends on the nonlinearity in the atmospheric processes. It means that only the “coefficients” of terms need to be fitted with training samples in another case (Step 3 in Figure 2), as seen in Table S4 which provides the coefficients of 15 terms for $\text{PM}_{2.5}$ and O_3 in BTH region. The degrees and selected terms (Step 1-2 in Figure 2) do not need to be recalculated unless there have significant updates in chemistry mechanism in the CTM. However, it might need further confirmed by more 15 applications in other regions outside BTH.

Based on the pf-RSM, a series of indicators were calculated from the polynomial function to represent the nonlinearity in control effectiveness for reducing $\text{PM}_{2.5}$ and O_3 , including Peak Ratio (i.e., PR), suggested VOC/ NO_x Ratio to avoid increasing O_3 (i.e., VNr), Flex Ratio (i.e., FR) and the extra benefit from simultaneous reduction of NH_3 ($\mu\text{g m}^{-3}$ $\text{PM}_{2.5}$ per 1% reduced NH_3). We found a strong VOC-limited condition and NH_3 -rich condition for O_3 and $\text{PM}_{2.5}$ respectively, in most of urban areas of BTH. 20 Results suggest that NO_x emission reduction rate need be greater than 20%-60% to pass the transition from VOC-limited to NO_x -limited, and a simultaneous VOC reduction by 0.5-1.2 times as the rate of NO_x reduction is recommended to avoid increasing O_3 during the transition in July. Along with the control of NO_x , the simultaneous reduction of NH_3 can provide a considerable benefit in $\text{PM}_{2.5}$ reduction by 0.04-0.15 $\mu\text{g m}^{-3}$ per 1% reduction of NH_3 . Our results demonstrate the importance of simultaneous reductions of VOC and NH_3 emissions to enhance the effectiveness of air pollution controls by NO_x emission reductions in Beijing- 25 Tianjin-Hebei region in China.

5. Data availability

Model outputs and pf-RSM code package are available upon request from the corresponding author.

Acknowledgements

30 This work was supported in part by National Key R & D program of China (2016YFC0207601), National Science Foundation of China (21625701 & 21521064) and Shanghai Environmental Protection Bureau (2016-12). This work was completed on the “Explorer 100” cluster system of Tsinghua National Laboratory for Information Science and Technology. The authors also acknowledge the contributions of Dr. Xiaoyue Niu, Qi Li, Kui Hua, Nayang Shan from Center for Statistical Science at Tsinghua University.

35



Reference

- Appel, K. W., Pouliot, G. A., Simon, H., Sarwar, G., Pye, H. O. T., Napelenok, S. L., Akhtar, F., and Roselle, S. J.: Evaluation of dust and trace metal estimates from the Community Multiscale Air Quality (CMAQ) model version 5.0, *Geosci. Model Dev.*, 6, 883–899, <https://doi.org/10.5194/gmd-6-883-2013>, 2013.
- 5 Carter, W.P.: The SAPRC-99 chemical mechanism and updated VOC reactivity scales. California Air Resources Board, 2003.
- Cohan, D.S., Hakami, A., Hu, Y., Russell, A.G. Nonlinear response of ozone to emissions: source apportionment and sensitivity analysis. *Environ. Sci. Technol.* 39, 6739-6748, 2005.
- Cohen, A.J., Brauer, M., Burnett, R., Anderson, H.R., Frostad, J., Estep, K., Balakrishnan, K., Brunekreef, B., Dandona, L., Dandona, R., Feigin, V.: Estimates and 25-year trends of the global burden of disease attributable to ambient air pollution: an analysis of data from the Global Burden of Diseases Study 2015. *The Lancet*, 389 (10082), 1907-1918, 2017.
- 10 Dunker, A. M., Yarwood, G., Ortman, J.P., Wilson, G.M.: Comparison of source apportionment and source sensitivity of ozone in a three-dimensional air quality model, *Environmental Science and Technology*, 36, 2953-2964, 2002.
- Foley, K.M., Napelenok, S.L., Jang, C., Phillips, S., Hubbell, B.J., Fulcher, C.M.: Two reduced form air quality modeling techniques for rapidly calculating pollutant mitigation potential across many sources, locations and precursor emission types. *Atmospheric environment*, 98, 283-289, 2014.
- 15 Forouzanfar, M.H., Alexander, L., Anderson, H.R., Bachman, V.F., Biryukov, S., Brauer, M., Burnett, R., Casey, D., Coates, M.M., Cohen, A., Delwiche, K.: Global, regional, and national comparative risk assessment of 79 behavioural, environmental and occupational, and metabolic risks or clusters of risks in 188 countries, 1990–2013: a systematic analysis for the Global Burden of Disease Study 2013. *The Lancet*, 386 (10010), 2287–2323, 2015.
- 20 Fu, X., Wang, S., Xing, J., Zhang, X., Wang, T. and Hao, J.: Increasing Ammonia Concentrations Reduce the Effectiveness of Particle Pollution Control Achieved via SO₂ and NO_x Emissions Reduction in East China. *Environmental Science & Technology Letters*, 2017.
- GBD-MAPS project report, New Study: Air pollution from coal a major source of health burden in China, 2016, available at <https://www.healtheffects.org/system/files/HEI-GBD-MAPS-China-Press-Release.pdf>
- 25 Gipson, G.L., Freas, W.P., Kelly, R.F., Meyer, E.L.: Guideline for use of city-specific EKMA in preparing ozone SIPs. EPA-450/4-80-027, US Environmental Protection Agency, Research Triangle Park, North Carolina, USA, 1981.
- Hakami, A., Odman, M.T., Russell, A.G.: High-order, direct sensitivity analysis of multidimensional air quality models, *Environmental Science and Technology*, 37, 2442-2452, 2003.
- Heyes, C., Schöpp, W., Amann, M., Unger, S.: A Reduced-Form Model to Predict Long-Term Ozone Concentrations in Europe. Interim Report WP-96-12, 1996.
- 30 Heyes, C., Schöpp, W., Amann, M., Bertok, I., Cofala, J., Gyarmas, F., Klimont, Z., Makowski, M., Shibayev, S.: A model for optimizing strategies for controlling ground-level ozone in Europe. Interim Report IR-97-002, 1997.
- Kwok, R. H. F., Napelenok, S.L., Baker, K.R.: Implementation and evaluation of PM_{2.5} source contribution analysis in a photochemical model, *Atmos. Environ.*, 80, 398–407, 2013.
- 35 Kwok, R. H. F., Baker, K.R., Napelenok, S.L., Tonnesen, G.S.: Photochemical grid model implementation and application of VOC, NO_x, and O₃ source apportionment, *Geosci. Model Dev.*, 8, 99-114, 2015.
- Li, J., Lu, K., Lv, W., Li, J., Zhong, L., Ou, Y., Chen, D., Huang, X. and Zhang, Y.: Fast increasing of surface ozone concentrations in Pearl River Delta characterized by a regional air quality monitoring network during 2006–2011. *Journal of Environmental Sciences*, 26(1), 23-36, 2014.



- Liu, X.-H., Zhang, Y., Xing, J., Zhang, Q., Streets, D. G., Jang, C. J., Wang, W.-X., Hao, J.-M.: Understanding of Regional Air Pollution over China using CMAQ - Part II. Process Analysis and Ozone Sensitivity to Precursor Emissions, *Atmos. Environ.*, 44, 3719-3727, 2010.
- Liu, F., Zhang, Q., Zheng, B., Tong, D., Yan, L., Zheng, Y. and He, K.: Recent reduction in NO_x emissions over China: synthesis of satellite observations and emission inventories. *Environmental Research Letters*, 11(11), 114002, 2016.
- Myhre, G., Shindell, D., Bréon, F.M., Collins, W., Fuglested, J., Huang, J., Koch, D., Lamarque, J.F., Lee, D., Mendoza, B., Nakajima, T.: Anthropogenic and Natural Radiative Forcing. In: *Climate Change 2013: The Physical Science Basis. Contribution of Working Group I to the Fifth Assessment Report of the Intergovernmental Panel on Climate Change*, T.F. Stocker et al, Eds. Cambridge Univ. Press, 659-740, 2013.
- 10 Santner, T.J., Williams, B.J., Notz, W.: *The Design and Analysis of Computer Experiments*, Springer Verlag, New York, 2003.
- Seinfeld, J. H. and Pandis, S.N.: *Atmospheric chemistry and physics: From air pollution to climate change*, John Wiley and Sons, Inc., 241 pp, 2006.
- Sillman, S.: The use of NO_y, H₂O₂, and HNO₃ as indicators for ozone-NO_x-hydrocarbon sensitivity in urban locations. *J. Geophys. Res.*, 100 (D7), 4175-4188, 1995.
- 15 Tonnesen, G.S. and Dennis, R.L.: Analysis of radical propagation efficiency to assess ozone sensitivity to hydrocarbons and NO_x 1. Local indicators of instantaneous odd oxygen production sensitivity. *Journal of Geophysical Research*, 105 (D7), 9213-9225, 2000.
- Tsimpidi, A.P., Karydis, V.A., Pandis, S.N.: Response of Fine Particulate Matter to Emission Changes of Oxides of Nitrogen and Anthropogenic Volatile Organic Compounds in the Eastern United States, *J. Air & Waste Manage. Assoc.*, 58:1463-1473, 2008, DOI: 10.3155/1047-3289.58.11.1463
- 20 Wagstrom, K. M., Pandis, S.N., Yarwood, G., Wilson, G.M., Morris, R.E.: Development and application of a computationally efficient particulate matter apportionment algorithm in a three-dimensional chemical transport model. *Atmospheric Environment*, 42, 5650-5659, 2008.
- Wang, S. X., Xing, J., Jang, C., Zhu, Y., Fu, J.S., Hao, J.: Impact assessment of ammonia emissions on inorganic aerosols in east 25 China using response surface modeling technique. *Environ. Sci. Technol.*, 45, 9293-9300, 2011.
- Xing, J., Wang, S.X., Jang, C., Zhu, Y., Hao, J.M.: Nonlinear response of ozone to precursor emission changes in China: a modeling study using response surface methodology. *Atmos. Chem. Phys.*, 11, 5027-5044, 2011.
- Xing, J., Wang, S., Zhao, B., Wu, W., Ding, D., Jang, C., Zhu, Y., Chang, X., Wang, J., Zhang, F. and Hao, J.: Quantifying Nonlinear Multiregional Contributions to Ozone and Fine Particles Using an Updated Response Surface Modeling 30 Technique. *Environmental science & technology*, 51(20),11788-11798, 2017.
- Ye, L., Wang, X., Fan, S., Chen, W., Chang, M., Zhou, S., Wu, Z., Fan, Q.: Photochemical indicators of ozone sensitivity: application in the Pearl River Delta, China. *Frontiers of Environmental Science & Engineering*, 10(6), 15, 2016.
- Zhang, Y., Wen, X.-Y., Wang, K., Vijayaraghavan, K., Jacobson, M.Z.: Probing into Regional O₃ and PM Pollution in the U.S., Part II. An Examination of Formation Mechanisms through a Process Analysis Technique and Sensitivity Study. *Journal of 35 Geophysical Research*, 114(D22305), 2009, doi:10.1029/2009JD011900.
- Zhao, B., Wang, S. X., Liu, H., Xu, J. Y., Fu, K., Klimont, Z., Hao, J. M., He, K. B., Cofala, J., and Amann, M.: NO_x emissions in China: historical trends and future perspectives, *Atmos. Chem. Phys.*, 13, 9869-9897, <https://doi.org/10.5194/acp-13-9869-2013>, 2013.



- Zhao, B., Wang, S.X., Xing, J., Fu, K., Fu, J.S., Jang, C., Zhu, Y., Dong, X.Y., Gao, Y., Wu, W.J., Wang, J.D.: Assessing the nonlinear response of fine particles to precursor emissions: development and application of an extended response surface modeling technique v1.0. *Geosci. Model Dev.*, 8, 115-128, 2015a.
- 5 Zhao, B., Wang, S., Donahue, N.M., Chuang, W., Hildebrandt Ruiz, L., Ng, N.L., Wang, Y., Hao, J.: Evaluation of one-dimensional and two-dimensional volatility basis sets in simulating the aging of secondary organic aerosols with smog-chamber experiments, *Environ. Sci. Technol.* 49, 2245-2254, DOI 10.1021/es5048914, 2015b.
- Zhao, B., Wang, S., Donahue, N.M., Jathar, S.H., Huang, X., Wu, W., Hao, J., Robinson, A.L.: Quantifying the effect of organic aerosol aging and intermediate-volatility emissions on regional-scale aerosol pollution in China, *Sci. Rep.*, 6, 10.1038/srep28815, 2016.
- 10 Zhao, B., Wu, W., Wang, S., Xing, J., Chang, X., Liou, K.N., Jiang, J.H., Gu, Y., Jang, C., Fu, J.S. and Zhu, Y.: A modeling study of the nonlinear response of fine particles to air pollutant emissions in the Beijing–Tianjin–Hebei region. *Atmospheric Chemistry and Physics*, 17(19), 12031-12050, 2017.



Table 1. Degree of variables in the polynomial function of response to emission changes

pollutant	E_{NO_x}	E_{SO_2}	E_{NH_3}	E_{VOCs}	E_{POA}
PM _{2.5}	4	1	3	2	1
O ₃	5	1	1	3	1

* E_{NO_x} , E_{SO_2} , E_{NH_3} , E_{VOCs} , and E_{POA} is the change ratio of NO_x, SO₂, NH₃, VOCs, and POA emissions, respectively.



Table 2. Out of sample dataset for validation

Description	Control factor	Number of cases
Jointly controls in 5 regions (OOS100)	5 precursors including NO _x , SO ₂ , NH ₃ , VOCs and POA in all regions	100, Latin Hypercube Sampling between 0.0 to 1.2 (baseline =1.0)
Single regional controls (OOS15)	5 precursors including NO _x , SO ₂ , NH ₃ , VOCs and POA in individual region	15, 3 samples in each region by 0.1, 0.5 and 1.15 (baseline =1.0)



Table 3. Performance of PM_{2.5} and O₃ prediction using pf-RSM with different training samples

Num. Dataset	Dist.	PM _{2.5}										O ₃									
		Jan					Jul					Jan					Jul				
		MeanNE	MaxNE	MeanFE	MaxFE	R	MeanNE	MaxNE	MeanFE	MaxFE	R	MeanNE	MaxNE	MeanFE	MaxFE	R	MeanNE	MaxNE	MeanFE	MaxFE	R
20	OOS100 Even	2.50%	15.09%	1.24%	6.98%	0.94	1.03%	5.56%	0.52%	2.77%	0.99	2.04%	10.33%	1.01%	4.90%	0.99	0.23%	1.50%	0.12%	0.74%	1.00
	OOS100 Margin	3.07%	15.02%	1.52%	6.97%	0.93	1.66%	6.89%	0.83%	3.59%	0.98	1.73%	5.53%	0.87%	2.74%	1.00	0.22%	0.86%	0.11%	0.43%	1.00
	OOS15 Even	0.76%	1.86%	0.38%	0.93%	0.99	1.79%	3.33%	0.91%	1.69%	0.97	2.48%	4.84%	1.23%	2.38%	0.96	1.08%	3.29%	0.54%	1.69%	0.92
	OOS15 Margin	1.61%	3.38%	0.80%	1.66%	0.96	2.59%	5.23%	1.27%	2.53%	0.95	2.83%	4.69%	1.39%	2.27%	0.96	1.13%	2.49%	0.56%	1.23%	0.84
30	OOS100 Even	1.89%	9.90%	0.94%	4.71%	0.97	1.14%	4.34%	0.57%	2.12%	0.99	1.25%	12.41%	0.64%	5.77%	0.99	0.19%	1.46%	0.09%	0.73%	1.00
	OOS100 Margin	2.19%	11.96%	1.09%	5.63%	0.97	1.07%	4.11%	0.53%	2.03%	0.99	1.65%	4.87%	0.82%	2.39%	1.00	0.24%	0.89%	0.12%	0.44%	1.00
	OOS15 Even	1.13%	2.32%	0.57%	1.18%	0.99	1.49%	2.64%	0.75%	1.34%	0.98	1.52%	2.82%	0.77%	1.44%	0.99	0.59%	2.48%	0.29%	1.22%	0.92
	OOS15 Margin	0.74%	1.77%	0.37%	0.89%	0.99	1.21%	2.35%	0.60%	1.17%	0.99	1.61%	2.73%	0.80%	1.35%	0.99	0.70%	2.10%	0.35%	1.04%	0.90
40	OOS100 Even	1.79%	8.60%	0.89%	4.12%	0.98	0.81%	5.37%	0.40%	2.61%	0.99	1.54%	10.11%	0.79%	5.46%	0.99	0.19%	1.34%	0.09%	0.67%	1.00
	OOS100 Margin	1.88%	8.25%	0.93%	3.95%	0.98	1.00%	4.28%	0.50%	2.17%	0.99	1.19%	3.96%	0.60%	2.03%	1.00	0.19%	0.78%	0.09%	0.39%	1.00
	OOS15 Even	0.35%	0.79%	0.18%	0.39%	1.00	1.12%	2.05%	0.56%	1.03%	0.99	1.04%	2.34%	0.53%	1.19%	0.99	0.66%	2.03%	0.33%	1.00%	0.92
	OOS15 Margin	0.85%	1.80%	0.43%	0.91%	0.99	1.07%	2.08%	0.54%	1.05%	0.99	0.99%	2.34%	0.49%	1.16%	0.99	0.58%	1.93%	0.29%	0.96%	0.93
50	OOS100 Even	1.53%	8.17%	0.76%	3.92%	0.98	0.74%	3.77%	0.37%	1.88%	1.00	0.98%	6.50%	0.49%	3.10%	1.00	0.15%	1.07%	0.08%	0.54%	1.00
	OOS100 Margin	1.71%	8.66%	0.84%	4.15%	0.98	0.86%	3.81%	0.43%	1.89%	0.99	1.39%	4.71%	0.70%	2.30%	1.00	0.18%	0.66%	0.09%	0.33%	1.00
	OOS15 Even	0.88%	1.39%	0.44%	0.70%	0.99	0.72%	1.92%	0.36%	0.97%	0.99	1.10%	2.42%	0.55%	1.22%	0.99	0.54%	1.96%	0.27%	0.97%	0.96
	OOS15 Margin	0.93%	2.48%	0.47%	1.26%	0.99	0.81%	1.70%	0.41%	0.86%	0.99	1.20%	2.33%	0.59%	1.15%	0.99	0.45%	1.90%	0.23%	0.94%	0.94

*PM_{2.5} and O₃ responses are calculated based on monthly averaged concentrations in averages of urban sites



Table 4. Estimation of indicators that representing the nonlinear control effectiveness for reducing PM_{2.5} and O₃ in Beijing-Tianjin-Hebei region

indicator	Month	Beijing	Tianjin	HebeiN	HebeiE	HebeiS
Peak Ratio (PR)	January	0.11	0.10	0.19	0.15	0.13
	July	0.76	0.45	>1.2	0.74	0.59
suggested reduction ratio of VOC to NO _x to avoid increasing O ₃ (VNr)	January	3.8	3.5	2.5	2.8	3.0
	July	0.6	1.2	-	0.5	1.1
Flex Ratio (FR)	January	0.77	0.73	0.76	0.77	0.79
	July	0.91	0.92	-	0.77	0.94
extra benefit from simultaneous reduction of NH ₃ (μg m ⁻³ PM _{2.5} per 1% reduced NH ₃)	January	0.064	0.128	0.041	0.077	0.064
	July	0.148	0.145	-	0.138	0.126

*Indicators are calculated based on monthly averaged concentrations at urban areas of prefecture-level cities in the five target regions

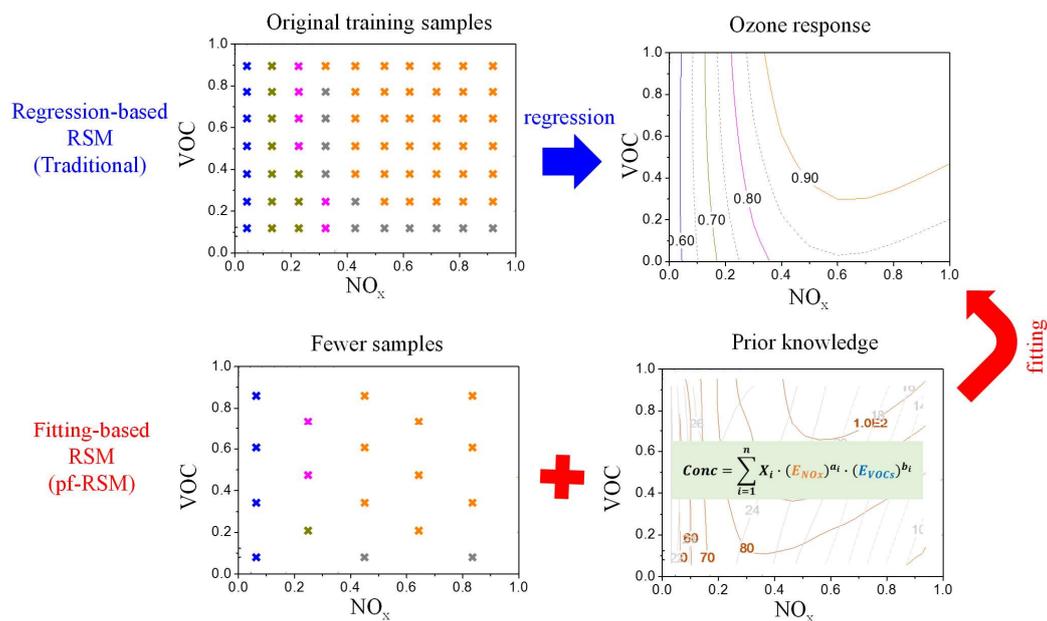


Figure 1. Schematic plot of comparison between traditional RSM (regression-based) and RSM with polynomial function (denoted as “pf-RSM”, fitting-based)

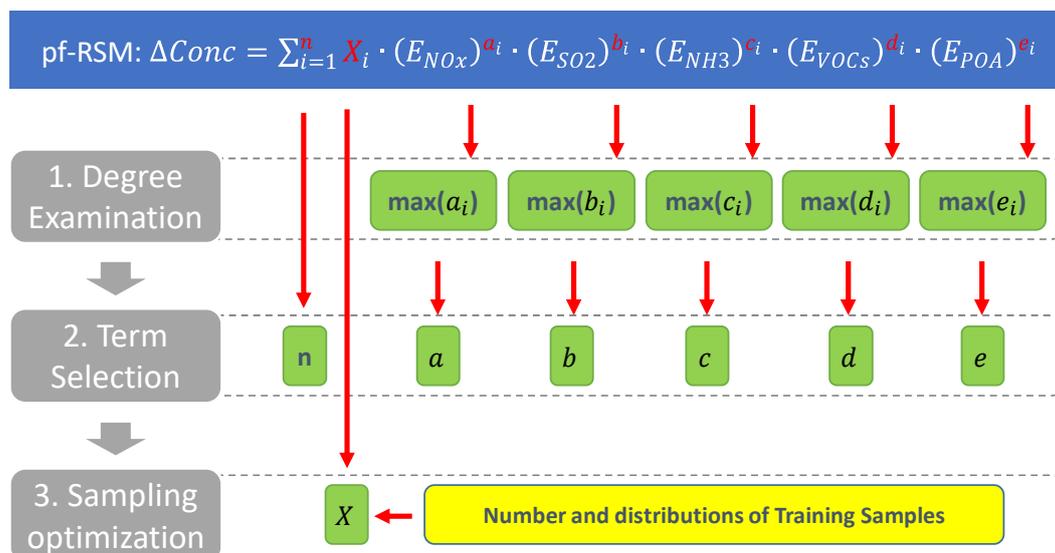


Figure 2. Flow scheme of pf-RSM development

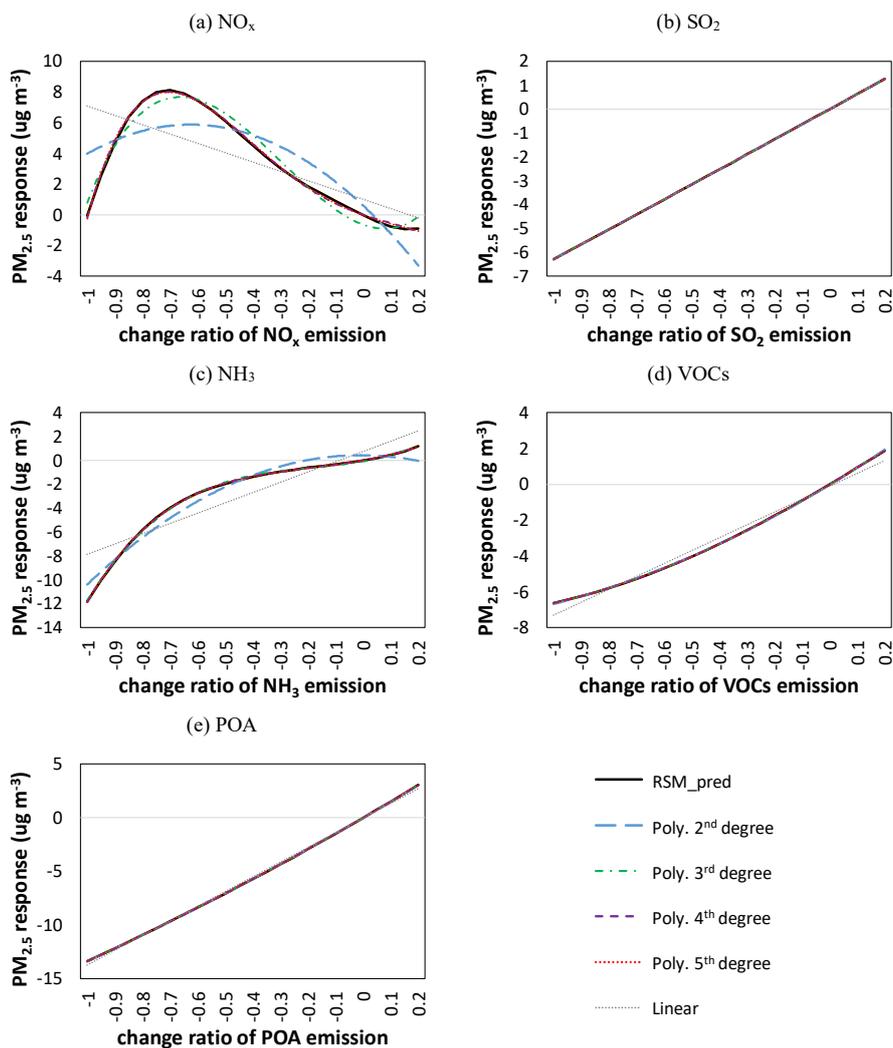


Figure 3. Fitting the $\text{PM}_{2.5}$ responsive function with a polynomial of a single indeterminate plots

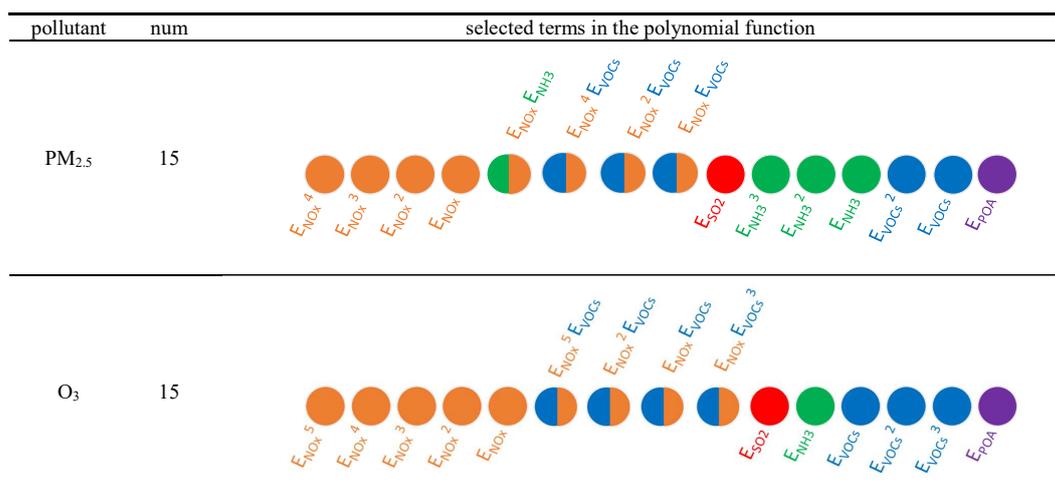


Figure 4. Term selections for PM_{2.5} and O₃ in the polynomial function

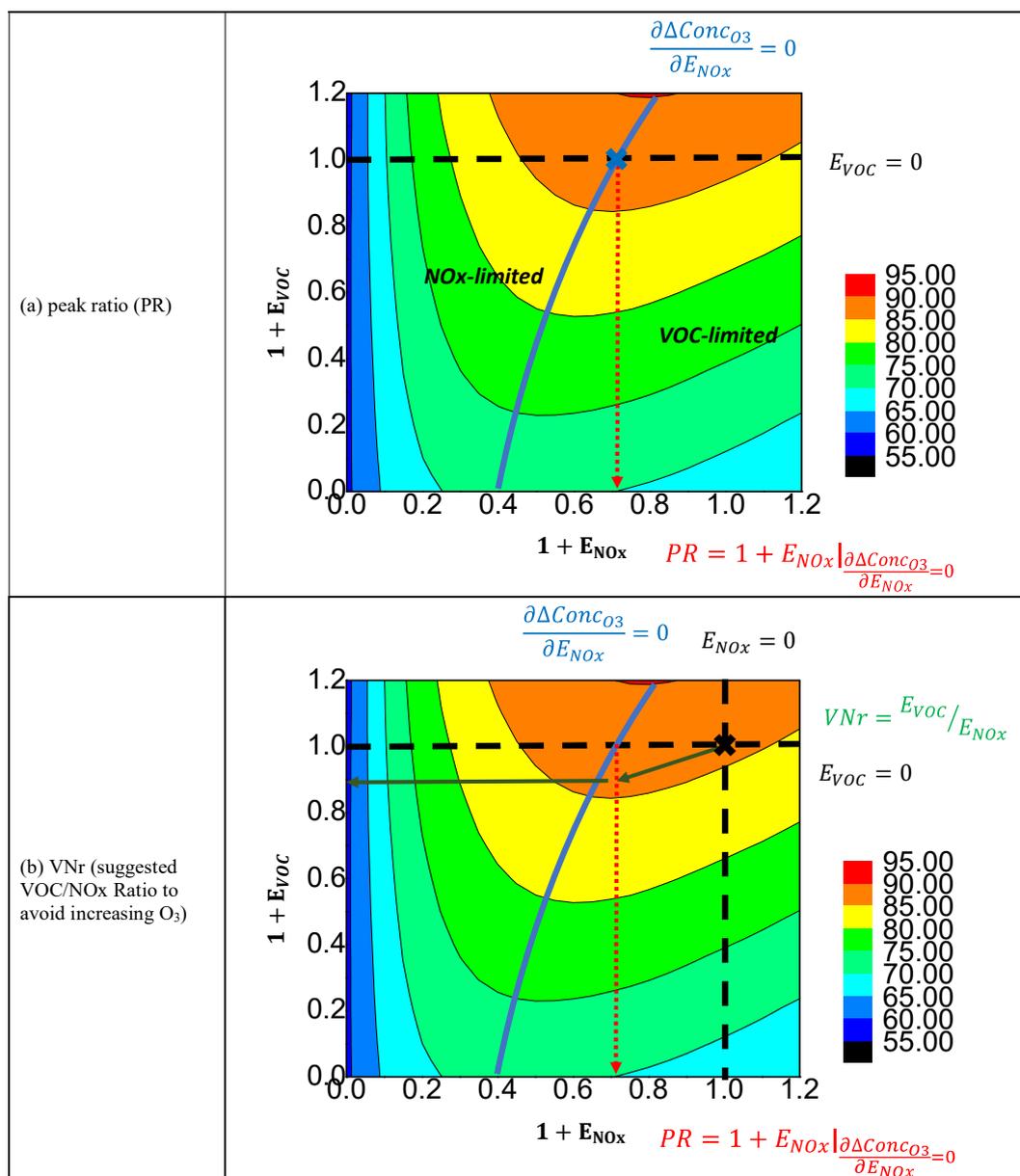


Figure 5. Definition of Peak Ratio (PR) and suggested VOC/NO_x Ratio (VNr) basing on the 2-D isopleths of O₃ sensitivity to NO_x and VOC emission changes (an example in Beijing in July)

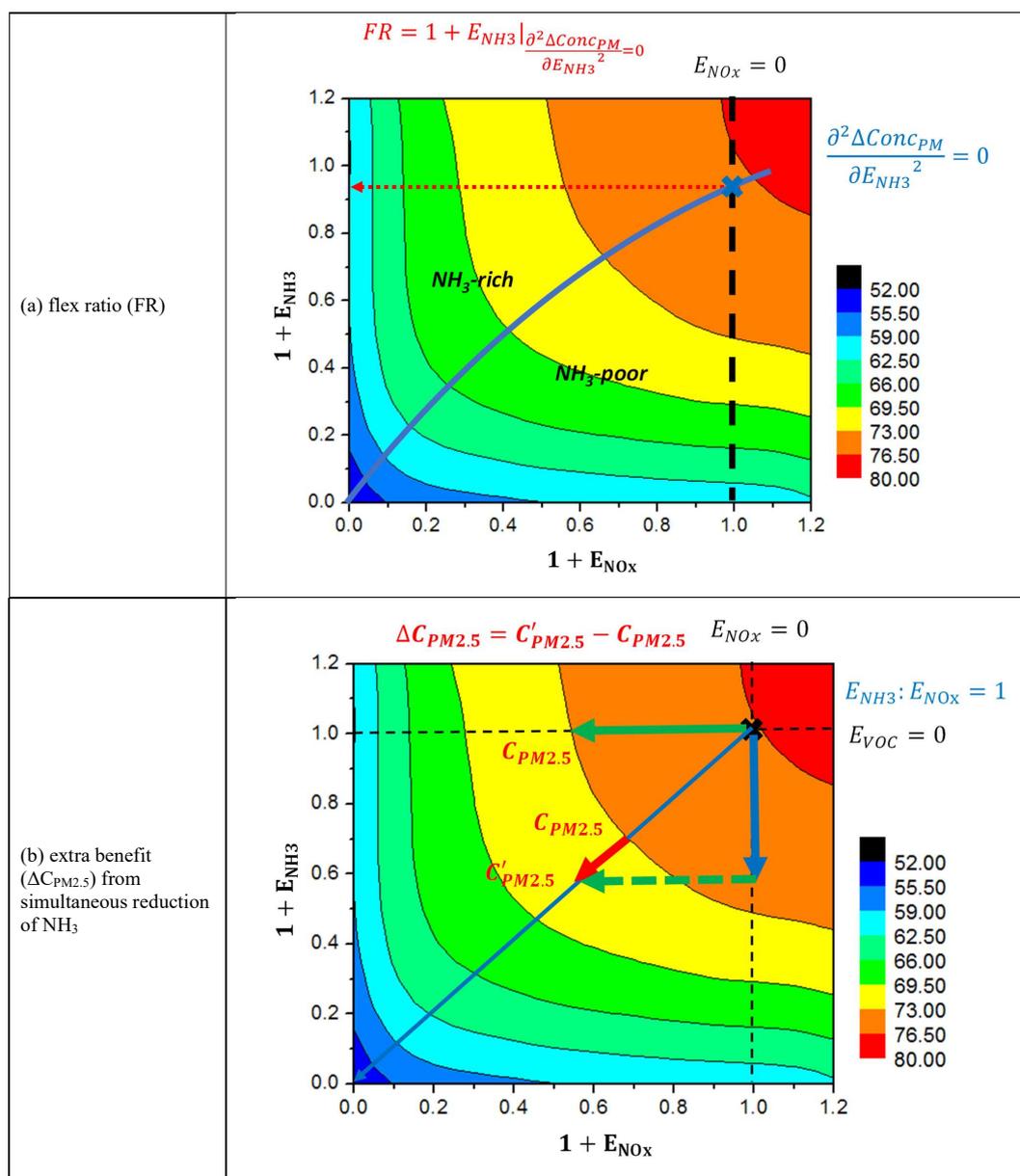


Figure 6. Definition of Flex Ratio (FR) and extra benefit from simultaneous reduction of NH_3 basing on the 2-D isopleths of $PM_{2.5}$ sensitivity to NO_x and NH_3 emission changes (an example in Beijing in July)

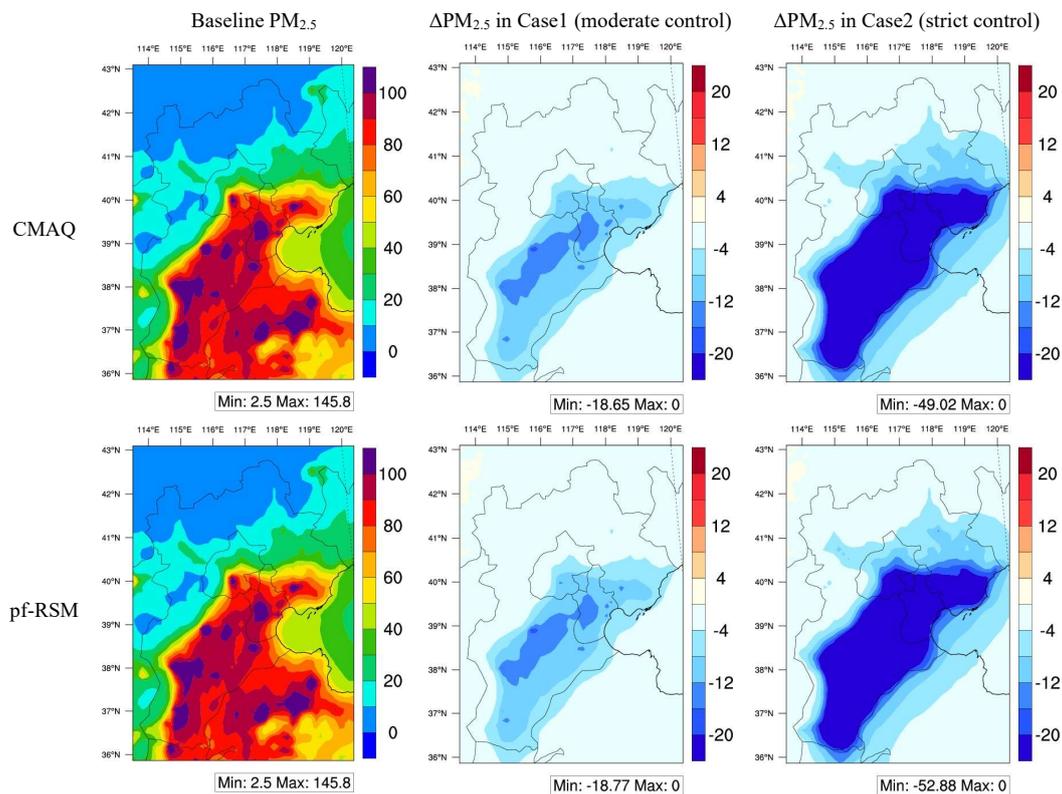


Figure 7. Spatial distribution of CMAQ-simulated and pf-RSM-predicted PM_{2.5} in baseline and PM_{2.5} responses in two control scenarios (monthly averages in January 2014, unit: μg m⁻³, the E_{NO_x}, E_{SO₂}, E_{NH₃}, E_{VOCs} and E_{POA} in case1 and case2 are -49%, -45%, -20%, -64%, -20% and -76%, -79%, -81%, -83%, -73% respectively)

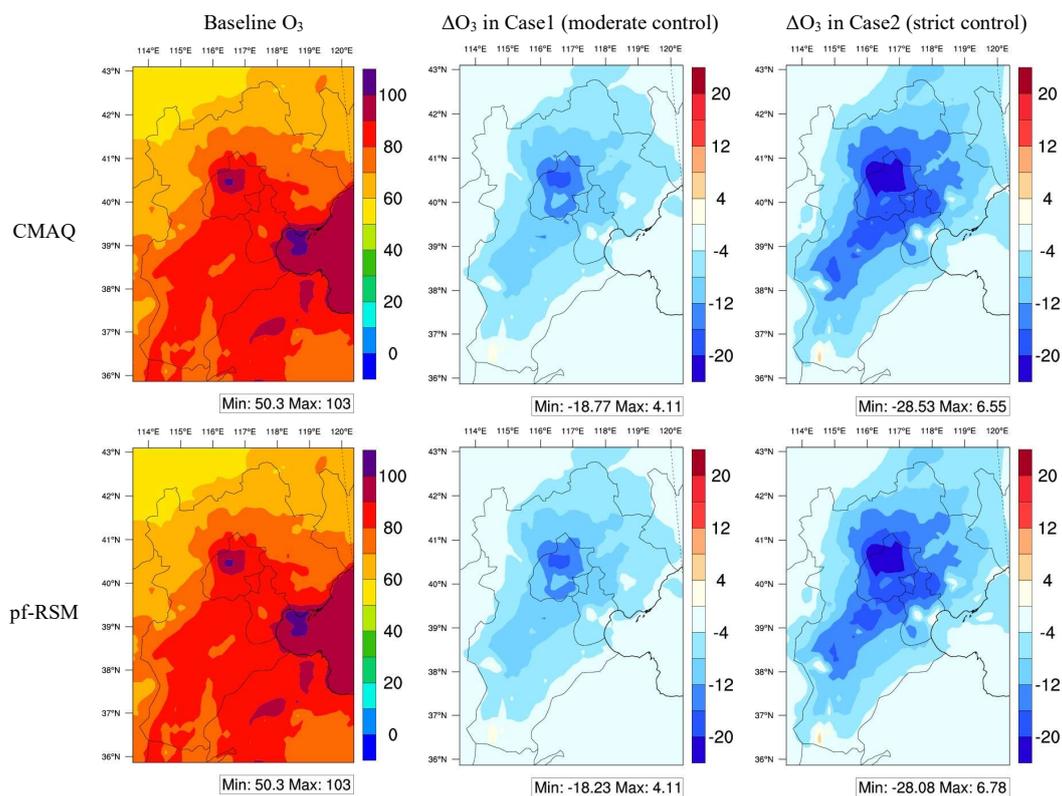


Figure 8. Spatial distribution of CMAQ-simulated and pf-RSM-predicted O₃ in baseline and O₃ responses in two control scenarios (monthly averages of daily 1-hour maxima O₃ in July 2014, unit: ppb, the E_{NOx}, E_{SO₂}, E_{NH₃}, E_{VOCs} and E_{POA} in case1 and case2 are -49%, -45%, -20%, -64%, -20% and -76%, -79%, -81%, -83%, -73% respectively)

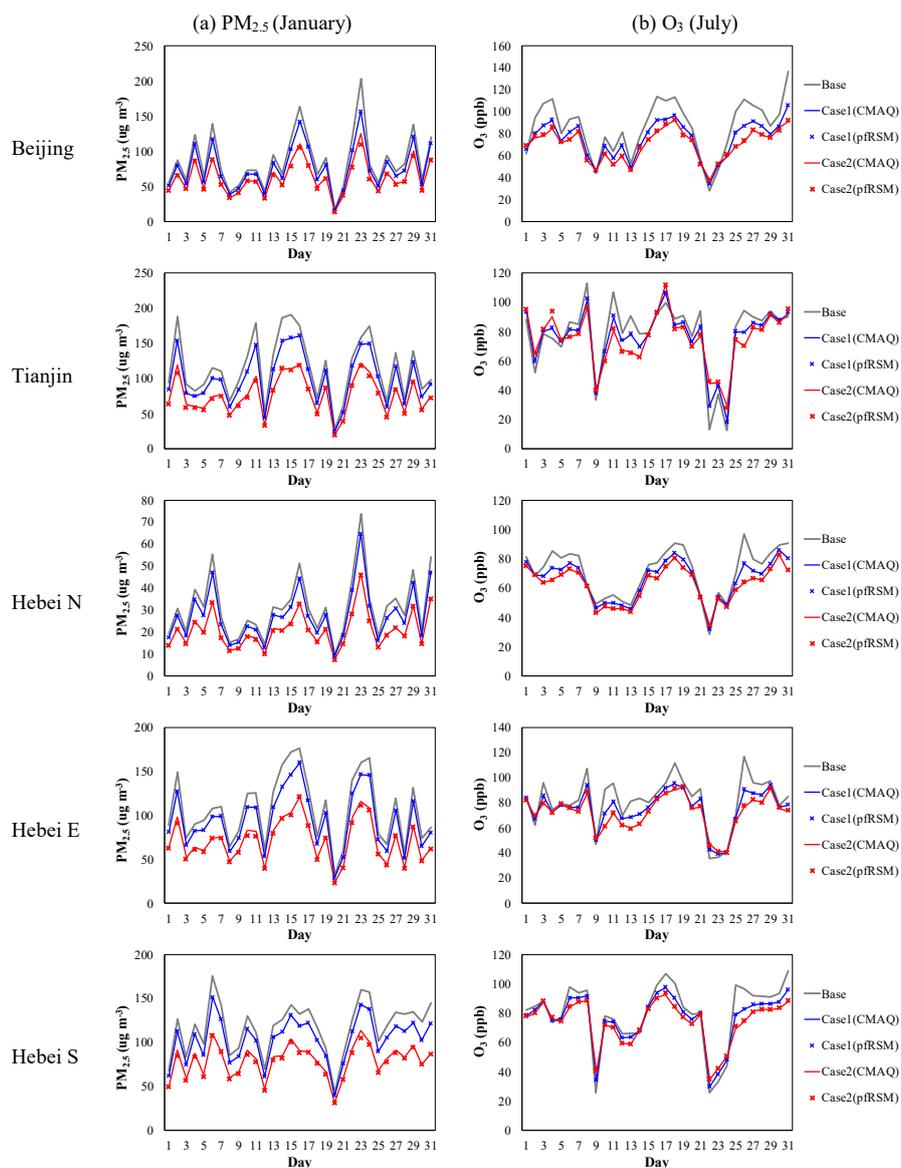


Figure 9. Daily series of CMAQ-simulated and pf-RSM-predicted daily averaged $PM_{2.5}$ in January and daily 1-hour maxima O_3 in July 2014 in baseline and two control scenarios (the E_{NOx} , E_{SO2} , E_{NH3} , E_{VOC5} and E_{POA} in case1 and case2 are -49%, -45%, -20%, -64%, -20% and -76%, -79%, -81%, -83%, -73% respectively)

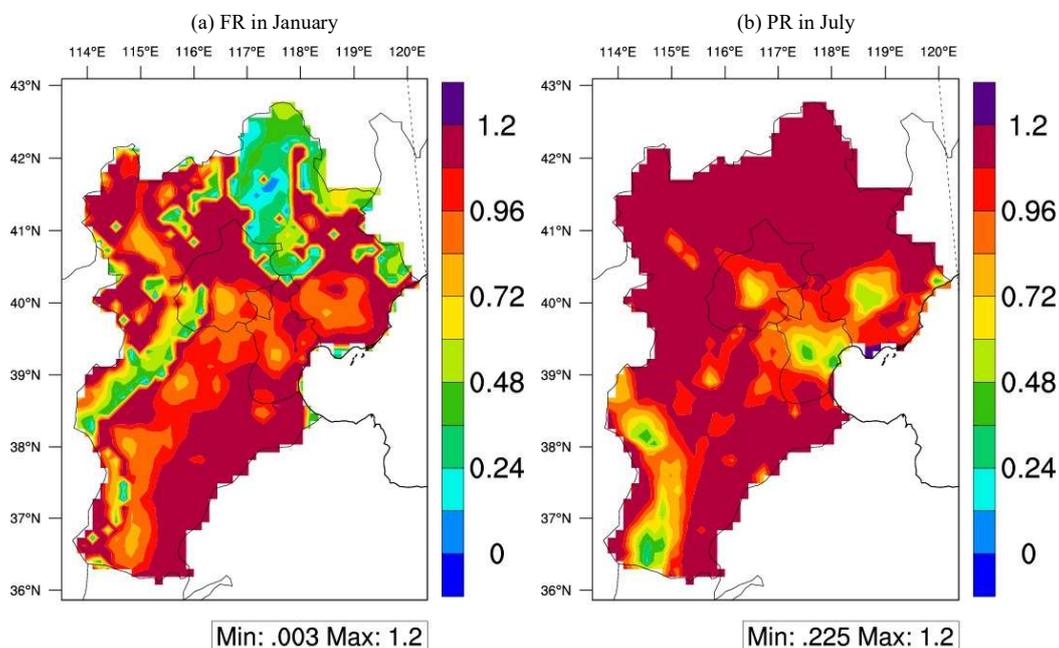


Figure 10. Spatial distribution of the indicators for $\text{PM}_{2.5}$ (flex ratio, FR) in January and O_3 chemistry (peak ratio, PR) in July, 2014