

1 **New particle formation from sulfuric acid and ammonia: nucleation and**  
2 **growth model based on thermodynamics derived from CLOUD**  
3 **measurements for a wide range of conditions**

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15 **Abstract**

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17 Understanding new particle formation and growth is important because of the strong impact  
18 of these processes on climate and air quality. Measurements to elucidate the main new particle  
19 formation mechanisms are essential; however, these mechanisms have to be implemented in  
20 models to estimate their impact on the regional and global scale. Parameterizations are  
21 computationally cheap ways of implementing nucleation schemes in models but they have their  
22 limitations, as they do not necessarily include all relevant parameters. Process models using  
23 sophisticated nucleation schemes can be useful for the generation of look-up tables in large-  
24 scale models or for the analysis of individual new particle formation events. In addition, some  
25 other important properties can be derived from a process model that implicitly calculates the  
26 evolution of the full aerosol size distribution, e.g., the particle growth rates. Within this study,  
27 a model (SANTIAGO, Sulfuric acid Ammonia NucleaTIon And GrOwth model) is constructed  
28 that simulates new particle formation starting from the monomer of sulfuric acid up to a particle  
29 size of several hundred nanometers. The smallest sulfuric acid clusters containing one to four  
30 acid molecules and varying amount of base (ammonia) are allowed to evaporate in the model,  
31 whereas growth beyond the pentamer (5 sulfuric acid molecules) is assumed to be entirely  
32 collision-controlled. The main goal of the present study is to derive appropriate thermodynamic  
33 data needed to calculate the cluster evaporation rates as a function of temperature. These data  
34 are derived numerically from CLOUD (Cosmics Leaving OUtdoor Droplets) chamber new  
35 particle formation rates for neutral sulfuric acid-water-ammonia nucleation at temperatures  
36 between 208 K and 292 K. The numeric methods include an optimization scheme to derive the  
37 best estimates for the thermodynamic data ( $dH$  and  $dS$ ) and a Monte Carlo method to derive  
38 their probability density functions. The derived data are compared to literature values. Using  
39 different data sets for  $dH$  and  $dS$  in SANTIAGO detailed comparison between model results  
40 and measured CLOUD new particle formation rates is discussed.

## 41 1. INTRODUCTION

42  
43 The formation of new aerosol particles from the gas phase (nucleation) is the most important  
44 source of cloud condensation nuclei (CCN) in the free and upper troposphere (Dunne et al.,  
45 2016; Gordon et al., 2017). Binary new particle formation (NPF) from sulfuric acid and water  
46 is thought to be an important mechanism at cold conditions that can be enhanced by ions (Lee  
47 et al., 2003; Kirkby et al., 2011; Duplissy et al., 2016). The ternary system involving ammonia  
48 besides sulfuric acid and water can yield significantly enhanced NPF rates (Ball et al., 1999;  
49 Benson et al., 2009; Glasoe et al., 2015; Kirkby et al., 2011; Kürten et al., 2016). The addition  
50 of only a few pptv of ammonia can increase NPF rates by several orders of magnitude compared  
51 with the pure binary system (Kürten et al., 2016). The importance of ammonia in terms of NPF  
52 is highlighted by recent modeling studies, where a large fraction of CCN originates from ternary  
53  $\text{H}_2\text{SO}_4\text{-H}_2\text{O-NH}_3$  nucleation (Dunne et al., 2016; Gordon et al., 2017). The detection of  
54 ammonia above several pptv in the upper troposphere by recent satellite measurements supports  
55 these findings (Höpfner et al., 2016). Furthermore, an aircraft campaign up to ~5 km altitude  
56 measured elevated  $\text{NH}_3$  concentrations over Texas (Nowak et al., 2010). Therefore, it is likely  
57 that ammonia plays an important role in new particle formation in the free troposphere. An  
58 expected future increase in the anthropogenic ammonia emissions could even increase the  
59 significance of ammonia in terms of NPF (Clarisse et al., 2009).

60 At cold conditions, NPF from  $\text{H}_2\text{SO}_4\text{-H}_2\text{O-NH}_3$  is efficient enough to explain NPF at  
61 atmospherically relevant concentrations of sulfuric acid and ammonia (Kirkby et al., 2011;  
62 Dunne et al., 2016; Kürten et al., 2016). However, the involvement of ammonia in the formation  
63 of new particles at the relatively warm conditions close to the surface is not clear yet. A recent  
64 study indicates that ion-induced ternary nucleation can explain some new particle formation  
65 events in the boreal forest in Finland (Yan et al., 2018); evidence that  $\text{NH}_3$  is important in  
66 polluted boundary layer environments has been presented earlier (Chen et al., 2012). Most  
67 recently, Jokinen et al., (2018) showed that ion-induced ternary nucleation is important in  
68 coastal Antarctica. The importance of ammonia in enhancing boundary layer nucleation in the  
69 presence of highly-oxygenated molecules (HOM) from monoterpenes and sulfuric acid has  
70 recently been described (Lehtipalo et al., 2018).

71 In order to model nucleation, knowledge about cluster evaporation rates is required. This can  
72 either be gained by measurements in a flow tube (Hanson and Eisele, 2002; Jen et al., 2014; Jen  
73 et al., 2016; Hanson et al., 2017) or in a chamber such as CLOUD (Cosmics Leaving Outdoor  
74 Droplets, Kürten et al., 2015a). Another possibility is to apply quantum chemical (QC)  
75 calculations (Kurtén et al., 2007; Nadykto and Yu, 2007; Ortega et al., 2012; Elm et al., 2013;  
76 Elm and Kristensen, 2017; Yu et al., 2018). Comparison between experimental data measured  
77 at the CLOUD chamber and modeled formation rates using the ACDC (Atmospheric Cluster  
78 Dynamics Code) model (McGrath et al., 2012) with evaporation rates from quantum chemistry  
79 (Ortega et al., 2012) yielded good agreement for some conditions (208 and 223 K). For higher  
80 temperatures ( $\geq 248$  K) the model generally overestimated the formation rates up to several  
81 orders of magnitude. A more recently developed nucleation model, also relying on evaporation  
82 rates from QC calculations, yields good agreement with the CLOUD data for some conditions  
83 (Yu et al., 2018).

84 For the global modeling studies by Dunne et al. (2016) and Gordon et al. (2017) CLOUD  
85 data have been parameterized to yield nucleation rates for four different channels (binary  
86 neutral and ion-induced, and ternary neutral and ion-induced). The parameterization works well  
87 and describes the nucleation rates over a wide range of conditions (Dunne et al., 2016) but it  
88 also has its limitations. First, it does not give any insights on the stability of individual sulfuric  
89 acid-ammonia clusters. Second, the influence of other parameters on nucleation (e.g., the  
90 condensation sink) cannot be tested, while the model by Yu et al. (2018) considers the effect of  
91 the condensation sink on the nucleation rate. Third, the parameterization provides only the  
92 nucleation rate, while a full nucleation model utilizing size bins over a wide diameter range can  
93 also yield the particle growth rates (Li and McMurry, 2018).

94 In the present study a model covering the aerosol size distribution over a wide size range,  
95 i.e., from the monomer of sulfuric acid up to several hundred nanometers, is constructed. The  
96 model simulates acid-base nucleation and considers evaporation rates for the clusters containing  
97 one to four sulfuric acid molecules and variable number of base molecules. The model allows  
98 calculating new particle formation and growth rates at different sizes and considers sinks like  
99 wall loss, dilution and coagulation. SANTIAGO (Sulfuric acid Ammonia NucleaTion And  
100 GrOwth model) is an extension of a previous simpler model version used to simulate acid-base  
101 nucleation involving dimethylamine (Kürten et al., 2014; Kürten et al., 2018). The model  
102 extension in the present study is a prerequisite for the main goal to derive the thermochemical  
103 parameters ( $dH$  and  $dS$ ) for the sulfuric acid-ammonia system from CLOUD chamber data  
104 (Dunne et al., 2016; Kürten et al., 2016). The data cover electrically neutral conditions for the  
105 clusters up to the tetramer (containing four sulfuric acid molecules and up to four ammonia  
106 molecules). First, a model has been developed that uses molecular and geometric size bins to  
107 cover a wide particle size range (starting with the monomer of sulfuric acid). Second, two  
108 numeric algorithms yield a best fit for the  $dH$  and  $dS$  values and their probability density  
109 functions (pdf). The pdf are obtained by using a Monte Carlo method introduced by Kupiainen-  
110 Määttä (2016). In total, CLOUD data from 125 experiments are considered; these cover the  
111 range from 208 K to 292 K and a wide range of atmospherically relevant sulfuric acid and  
112 ammonia concentrations. The results of the model are compared to the measured CLOUD data  
113 and further comparison regarding the thermochemical data from literature (Ortega et al., 2012;  
114 Hanson et al., 2017; Yu et al., 2018) is presented.

## 117 2. METHODS

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119 The aim of the present study is to find values for  $dH$  and  $dS$  of selected clusters (11 different  
120 clusters) such that modeled new particle formation (NPF) rates represent measured NPF rates  
121 from the CLOUD experiment with a small error. In order to perform this task, a model has been  
122 developed that calculates the NPF rates based on given concentrations of sulfuric acid and  
123 ammonia, relative humidity,  $RH$ , and temperature,  $T$  (Section 2.2). The data set from Kürten et  
124 al. (2016) for 125 neutral NPF rates is used to derive  $dH$  and  $dS$ . A best-fit thermodynamic data  
125 set is obtained by using an optimization method (Section 2.4). Moreover, the distributions of  
126 the probability density functions for each cluster are explored with a Monte Carlo method  
127 (Kupiainen-Määttä, 2016 and Section 2.5). The thermodynamic parameters (enthalpy change

128  $dH$  and entropy change  $dS$  due to the addition or removal of a molecule) are required in order  
129 to obtain the evaporation rate of a cluster. The mathematical relationship between  $dH$ ,  $dS$  and  
130 the evaporation rate are provided in the supplementary information (SI Text S2).

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## 132 **2.1 Experimental data from the CLOUD experiment**

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134 The experimental data used to develop the model were taken at the CLOUD (Cosmics  
135 Leaving OUtdoor Droplets) chamber at CERN (European Organization for Nuclear Research).  
136 The 26.1 m<sup>3</sup> stainless steel chamber allows conducting nucleation and growth experiments  
137 under atmospherically relevant conditions regarding the trace gas concentrations, temperature,  
138 relative humidity and ion concentrations (Kirkby et al., 2011). The chamber and the results for  
139 different chemical systems have been described elsewhere in the literature (e.g., Kirkby et al.  
140 2011; Almeida et al., 2013; Duplissy et al., 2016). In the present study no new data are presented  
141 from CLOUD; instead the data from the Dunne et al. (2016) and Kürten et al. (2016) studies  
142 are used. Whereas in the previous publications the influence of the ion concentration on  
143 nucleation was also discussed, this study focuses on neutral nucleation only. The parameter  
144 space covers temperatures between 208 K and 292 K (five different temperatures) and a wide  
145 range of atmospherically relevant sulfuric acid and ammonia concentrations. No systematic  
146 investigation of the relative humidity was carried out; for most experiments, the relative  
147 humidity was at 38%. The new particle formation rates are reported for a mobility diameter of  
148 1.7 nm (1.4 nm geometric diameter, see Ku and Fernandez de la Mora, 2009).

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## 150 **2.2 Acid base model**

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152 The model used in the present study solves a set of differential equations describing the  
153 concentrations of clusters and particles (McMurry, 1980; Kürten et al., 2014; Kürten et al.,  
154 2015a; McMurry and Li, 2017; Kürten et al., 2018). The model from Kürten et al. (2018)  
155 describes nucleation for the system of sulfuric acid and dimethylamine, where the formed  
156 clusters are stable against evaporation at a temperature of 278 K. For this reason, the **sulfuric**  
157 **acid-dimethylamine** system can be treated as quasi-unary and the kinetic approach (all cluster  
158 evaporation rates equal zero) yields very good agreement between modeled and measured  
159 particle concentrations and formation rates over a wide range of particle diameters. The model  
160 treats the smallest clusters in molecular size bins, based on the number of sulfuric acid  
161 molecules in a cluster, while geometric size bins are used for the larger clusters/particles  
162 (Kürten et al., 2018). In the present study 12 molecular bins and 25 geometric bins with a  
163 geometric growth factor of 1.25 result in a maximum particle diameter of 295 nm. **Choosing a**  
164 **larger number of bins and/or geometric factor would result in a larger upper size limit, which**  
165 **was, however, not necessary in the present study.** Compared with the earlier study by Kürten et  
166 al. (2018) the number of bins is reduced in order to reduce computation time; **the simulation of**  
167 **one new particle formation event (several hours of nucleation) takes ~0.1 s on a personal**  
168 **computer with a 3.4 GHz processor.**

169 While the approach of using a quasi-unary system with zero evaporation worked well for  
170 sulfuric acid-dimethylamine, this assumption cannot be used for sulfuric acid and ammonia  
171 because some small clusters evaporate rapidly (Nadykto and Yu, 2007; Ortega et al., 2012; Jen

172 et al., 2014). In the following, the number of sulfuric acid molecules denotes the clusters as  
173 monomers (1 sulfuric acid), dimers (2 sulfuric acids), trimers (3 sulfuric acids), etc. The clusters  
174 from the monomer to the tetramer can contain different numbers of ammonia molecules, where  
175 the maximum number of ammonia molecules is not allowed to exceed the number of acid  
176 molecules. The assumption that no clusters are allowed that contain more base than acid is  
177 based on fast evaporation rates that have been found for such clusters from quantum chemical  
178 calculations (Schobesberger et al., 2015; Elm et al 2017; Yu et al., 2018); the assumption is  
179 further supported by mass spectrometric measurements that could not identify such clusters  
180 (Kirkby et al., 2011; Schobesberger et al., 2015). This results in the acid-base reaction scheme  
181 shown in Figure 1, where  $A_1$  denotes the sulfuric acid monomer concentration and  $B_1$  the  
182 ammonia concentration. For the larger clusters and particles (starting with the pentamer), no  
183 differentiation regarding the base content is applied. The full set of differential equations used  
184 in SANTIAGO (Sulfuric acid Ammonia NucleaTion And GrOwth model) is listed in SI Text1.  
185 Compared with its previous version SANTIAGO can more accurately describe nucleation from  
186 sulfuric acid and ammonia because of the consideration of clusters with different amounts of  
187 acid and base that are allowed to evaporate.

188 While a mixed acid-base cluster can in principle loose either acid or base, the following rule  
189 was implemented in the model: clusters containing more acid than base can only evaporate an  
190 acid molecule, while clusters containing equal numbers of acid and base can loose a base  
191 molecule only. While this is a simplification of the reality, quantum chemical calculations  
192 support that this assumption generally considers the dominant evaporation processes (Yu et al.,  
193 2018). In principle, acid and base evaporation could be implemented for each cluster in the  
194 model but this would increase the number of free parameters from 22 (with the simplification)  
195 to 40 (with all possible evaporations) which would probably not lead to better results but  
196 increase the computation time significantly. The existence of clusters containing more base than  
197 acid is excluded in SANTIAGO, which is also supported by quantum chemical calculations  
198 (Ortega et al., 2012; Yu et al., 2018).

199 The thermodynamic parameters for the two smallest pure acid clusters ( $A_2$  and  $A_3$ ) are taken  
200 from a study where the parameters were derived from flow tube measurements (Hanson and  
201 Lovejoy, 2006). Ehrhart et al. (2016) showed that a numeric model for sulfuric acid-water  
202 binary nucleation using those data can well replicate new particle formation rates measured at  
203 CLOUD. In their study, Hanson and Lovejoy report dependencies of the dimer and trimer  
204 evaporation rates regarding the relative humidity, which are also adopted in the present study  
205 (evaporation rate proportional to  $(20\%/RH)^{0.5}$  for the dimer and  $(20\%/RH)^{1.5}$  for the trimer).  
206 The same dependency was used here and the evaporation rate for the pure tetramer ( $A_4$ ) was  
207 scaled by the same  $RH$ -dependent factor as for the pure acid trimer. Further humidity effects  
208 are not applied; therefore, the results for the thermodynamic data can be interpreted as a  
209 weighted average over the range of the different water contents for each cluster. The equations  
210 for calculating an evaporation rate from  $dH$  and  $dS$  are given in SI Text2 (see also Ortega et al.,  
211 2012). In general, slower evaporation rates result from more negative values of  $dH$  and from  
212 less negative values of  $dS$ ; the evaporation rate varies exponentially with  $dH$  and  $dS$ . How strong  
213 the evaporation rate varies with temperature, is determined by the value of  $dH$ .

214 Forward reaction rates are calculated based on the equations for the collision frequency  
215 function by Chan and Mozurkewich (2001) with a value of  $6.4 \times 10^{-20}$  J for the Hamaker constant

216 (Hamaker, 1937). An enhanced collision-rate between small clusters and particles due to van  
 217 der Waals forces was reported in recent CLOUD publications (Kürten et al., 2014; Lehtipalo et  
 218 al., 2016; Kürten et al., 2018). SANTIAGO takes into account dilution and wall loss, which are  
 219 relevant loss processes in the CLOUD chamber (Kirkby et al., 2011; Kürten et al., 2015a; SI  
 220 Text1). The value of the modeled new particle formation rate,  $J_{model}$ , is taken for the nonamer  
 221 (Kürten et al., 2015b):

$$J_{model} = \sum_{i+j \geq m} K_{i,j} \cdot N_i \cdot N_j. \quad (1)$$

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 225 The nonamer ( $m = 9$ ) has approximately a mobility diameter of 1.7 nm for which CLOUD new  
 226 particle formation rates are derived (Kirkby et al., 2011; Dunne et al., 2016). The formation rate  
 227 calculation takes into account that the collision of two smaller clusters with concentrations  $N_i$   
 228 and  $N_j$  yield a particle equal or larger than the nonamer. The differential equations are integrated  
 229 over the same time that each of the 125 individual CLOUD runs lasted; this time varied between  
 230 roughly half an hour and several hours dependent on the gas concentrations. The latest value of  
 231 the calculated nucleation rate defines the modeled NPF rate. Further details regarding the model  
 232 can be found in Kürten et al. (2015a, 2018) and in SI Text1.

233 The particle growth rates,  $GR$ , can be calculated using the monomer and cluster concentrations  
 234 in SANTIAGO:

$$GR_m = \sum_{i=1}^{m-1} \frac{\pi/6 \cdot d_{p,i}^3}{\pi/2 \cdot d_{p,m}^2} \cdot K_{m,i} \cdot N_i. \quad (2)$$

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 238 The increase in diameter depends on the particle diameter for which the growth rate is  
 239 determined,  $d_{p,m}$ , and the colliding cluster/particle diameter,  $d_{p,i}$  (Nieminen et al., 2010). Note  
 240 that equation (2) does not only consider the growth due to monomer additions ( $i = 1$ ) but also  
 241 the gain due to collisions with all clusters/particles smaller than the considered diameter.  
 242 Lehtipalo et al. (2016) have highlighted the importance of such cluster-cluster or cluster-particle  
 243 collisions, especially for systems containing high cluster concentrations like the sulfuric acid-  
 244 dimethylamine system. In the present study  $GR$  is calculated for  $m = 9$ , which corresponds to a  
 245 mobility diameter of 1.7 nm.

### 246 2.3 Metric for average error of the model

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 249 In order to optimize the thermodynamic parameters it is necessary to define a criterion that  
 250 describes the overall deviation between the 125 measured and modeled new particle formation  
 251 rates. Since the NPF rates span a large range (from roughly  $10^{-3}$  to  $10^2 \text{ cm}^{-3} \text{ s}^{-1}$ ) it is reasonable  
 252 to compare the ratios between modeled and measured rates rather than the absolute differences.  
 253 In this way, it is avoided that mainly the high values of the NPF rates are brought into  
 254 agreement. In addition, it is taken into account that the data covers five different temperatures  
 255 (208, 223, 248, 278 and 292 K) with different numbers of experiments conducted at each of the  
 256 temperatures. In order to weigh each of the temperatures equally and not to bias the error  
 257 calculation towards the temperature where most of the experiments were conducted at the  
 258 following error function,  $f$ , was defined:

259

$$\begin{aligned}
 260 \quad f &= \log \left( \frac{1}{5} \cdot \left( \frac{1}{n_1} \cdot \sum_{i=1}^{n_1} 10^{|\log(J_{model,i}) - \log(J_{exp,i})|} + \frac{1}{n_2} \cdot \sum_{i=1}^{n_2} 10^{|\log(J_{model,i}) - \log(J_{exp,i})|} + \right. \right. \\
 261 \quad &\left. \frac{1}{n_3} \cdot \sum_{i=1}^{n_3} 10^{|\log(J_{model,i}) - \log(J_{exp,i})|} + \frac{1}{n_4} \cdot \sum_{i=1}^{n_4} 10^{|\log(J_{model,i}) - \log(J_{exp,i})|} + \frac{1}{n_5} \cdot \right. \\
 262 \quad &\left. \left. \sum_{i=1}^{n_5} 10^{|\log(J_{model,i}) - \log(J_{exp,i})|} \right) \right) \quad (3)
 \end{aligned}$$

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264 In this equation the values  $n_1$  to  $n_5$  indicate the number of experiments at each temperature.

265

## 266 2.4 Optimization method

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268 The optimization method used was introduced by Steihaug (1983) and uses an  
 269 approximation for the function,  $f$ , that should be minimized. A quadratic model (second order  
 270 Taylor expansion) approximates the function:

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$$272 \quad M(x_k + s_k) = f(x_k) + g_k^T \cdot s_k + \frac{1}{2} \cdot s_k^T H_k s_k. \quad (4)$$

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274 In this study, the point  $x_k$  is the current set of thermodynamic parameters (11 dH and 11 dS  
 275 values, i.e., 22 parameters in total) and  $s_k$  is the vector that moves the point to a new position  
 276 that ideally yields a smaller error (i.e., a smaller value for  $f$ ). The gradient vector is denoted by  
 277  $g_k$  and the Hessian matrix by  $H_k$ . Steihaug's conjugated gradient method finds  $s_k$  that minimizes  
 278  $M$  (Steihaug, 1983; Nocedal and Wright, 2006). The algorithm takes into account that the length  
 279 of the vector  $s_k$  stays within a certain trust region,  $\Delta_k$  (i.e.,  $\|s_k\| \leq \Delta_k$ ). The value of

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$$281 \quad \rho_k = \frac{f(x_k) - f(x_k + s_k)}{M(x_k) - M(x_k + s_k)} \quad (5)$$

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283 is used to decide whether  $\Delta_k$  can be increased, stays unchanged or should be reduced after each  
 284 iteration,  $k$ . The empirical factor  $\eta_1$  is used to determine after each iteration whether a step  
 285 should be taken or not:

286

$$287 \quad x_{k+1} = \begin{cases} x_k + s_k & \rho_k \geq \eta_1 \\ x_k & \rho_k < \eta_1 \end{cases} \quad (6)$$

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289 The trust region radius is updated by using the following rules:

290

$$291 \quad \Delta_{k+1} = \begin{cases} t_1 \cdot \Delta_k & \rho_k < \eta_2 \\ \min(t_2 \cdot \Delta_k, \Delta_{max}) & \rho_k \geq \eta_3 \\ \Delta_k & \eta_2 \leq \rho_k < \eta_3 \end{cases}, \quad (7)$$

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293 where the empirical parameters  $\eta_2$ ,  $\eta_3$ ,  $t_1$  and  $t_2$  are used. The algorithm in this study was run  
 294 with parameters  $\Delta_0 = 0.5$ ,  $\Delta_{max} = 2$ ,  $t_1 = 0.25$ ,  $t_2 = 2.0$ ,  $\eta_1 = 0.20$ ,  $\eta_2 = 0.25$ ,  $\eta_3 = 0.75$  and  
 295 converged approximately after 20 steps. The values for  $x_0$  (initialization) are the dH and dS  
 296 values from Ortega et al. (2012).

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## 2.5 Monte Carlo method

With the Monte Carlo method (Differential Evolution-Markov Chain algorithm, DE-MC, see Ter Braak, 2006; Ter Braak and Vrugt, 2008; Kupiainen-Määttä, 2016) the probability density functions (pdf) of the thermodynamic parameters are explored. The pdf give information on the uncertainties of the parameters found by the optimization algorithm, as it is very likely that the optimized values represent a local minimum in the parameter space that is just one possible solution out of many others. The DE-MC algorithm aims at finding the most probable values for the parameters instead of finding the optimal values (Kupiainen-Määttä, 2016). Therefore, the Monte Carlo solutions can be used to evaluate if the optimized values are within the range of the most probable solutions.

### 2.5.1 Initialization for generating the prior distributions

At the start of the Monte Carlo simulation, the parameters  $dH$  and  $dS$  are initialized, where each value is randomly selected from a range of possible values. In this study, this range was defined by the values from Ortega et al. (2012)  $\pm 10$  kcal mol<sup>-1</sup> for  $dH$  and  $\pm 10$  cal mol<sup>-1</sup> K<sup>-1</sup> for  $dS$ . For these randomly selected thermodynamic parameters, the initial error (equation (3)) is calculated.

### 2.5.2 Main loop

Within the main loop (iterated 5000 times), the first step involves the random variation of the parameters. The value for each  $dH$  and  $dS$  is updated with a probability of 0.2. Given that 22 parameters are used, this means that on average 4.4 parameters changed during each iteration. If, however, the situation occurs that no update for any of the parameters is requested, the selection process is repeated until at least one thermodynamic parameter is updated (Kupiainen-Määttä, 2016). If a value should be updated its step width is chosen from a normal distribution with a standard deviation of 0.05 times the width of the allowed range (i.e., 20 kcal mol<sup>-1</sup> for  $dH$  and 20 cal mol<sup>-1</sup> K<sup>-1</sup> for  $dS$ ). If a step would lead to the crossing of the upper or lower bound for any of the parameters, a new random value is chosen until the updated value stays within its allowed range. With the new set of parameters, the new error,  $f(x_k + s_k)$ , is calculated. If  $f(x_k + s_k) < f(x_k)$ , then the new set of parameters is accepted. However, even if  $f(x_k + s_k)$  is larger than  $f(x_k)$  the step might still be accepted with the probability

$$P = \exp\left(-\frac{1}{2\sigma^2} \cdot (f(x_k + s_k) - f(x_k))\right), \quad (8)$$

where a  $\sigma$  of 0.2 has been chosen (same as by Kupiainen-Määttä, 2016). This means that even steps in the “wrong” direction (making the error larger) have a chance of being taken. This can avoid that the parameters might become trapped in a local minimum, which can, e.g., be the case with minimization methods. In any case,  $x_{k+1}$  is set to  $x_k + s_k$  if a step is taken before a new iteration starts. The error as well as the full set of parameters are recorded after each iteration.



### 340 2.5.3 Generation of the prior distribution

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342 In total 20 data sets (each containing 5000 steps) are generated with the methods described  
343 in Section 2.5.1 and 2.5.2. From each of the 20 data sets the average error was determined from  
344 the last 2500 points. Whenever the error for one data set is smaller than the geometric mean  
345 from all 20 errors, the data set was selected (Kupiainen-Määttä, 2016). All selected data sets  
346 combined and thinned to 5000 data points represent the prior distribution,  $Z_0$ . For each  
347 parameter the standard deviation  $\sigma_{ini}$  is determined.

348

### 349 2.5.4 DE-MC algorithm

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351 In the DE-MC (Differential Evolution-Markov Chain) algorithm, five Markov chains are run  
352 in parallel, where each of the chain starts from a random point of the joint history,  $Z_0$  (Ter Braak,  
353 2006; Ter Braak and Vrugt, 2008; Kupiainen-Määttä, 2016). In the algorithm, the probability  
354 to jump from an old point,  $x_{old}$ , to a new point,  $x_{new}$ , should be the same as moving from  $x_{new}$  to  
355  $x_{old}$ . This is achieved, by calculating the new position vector according to

356

$$357 \quad x_{new} = x_{old} + \gamma \cdot (x_1 - x_2) + \delta, \quad (9)$$

358

359 where  $x_1$  and  $x_2$  are randomly selected points from the joint history,  $Z_0$ . The factor  $\gamma$  is taken as  
360 (Ter Braak, 2006)

361

$$362 \quad \gamma = \frac{2.38}{\sqrt{2 \cdot n_{coefs}}} = \frac{2.38}{\sqrt{2 \cdot 22}} = 0.359 \quad (10)$$

363

364 or 0.98 (at every fifth step). Each individual  $dH$  and  $dS$  value for the new point is updated with  
365 a probability of 0.2 (see Section 2.3.2).  $\delta$  is drawn from a normal distribution with  $\sigma = 0.05 \times \sigma_{ini}$   
366 (calculated from the prior distribution, see above). The decision process whether a step should  
367 be accepted or not is the same as in Section 2.5.2 (equation (8)).

368

369 The points from the five chains are appended to the joint history,  $Z_0$ , and the new points in  
370 the following iterations are drawn from the updated history. This way, eventually convergence  
371 should be reached after many iterations resulting in the posterior distributions (probability  
372 density functions) for all parameters. The metric indicating convergence is given by  
(Kupiainen-Määttä, 2016):

373

$$374 \quad \hat{R} = \frac{k-1}{k} + \frac{c+1}{c} \cdot \frac{b}{W}, \quad (11)$$

375

376 with the parameter  $k$  indicating the step index; the number of chains is  $c = 5$ . The variance of  
377 the means for each parameter,  $b$ , is calculated from

378

$$379 \quad b = \frac{1}{c} \cdot \sum_{l=1}^c (\bar{\mu} - \mu_l)^2, \quad (12)$$

380

381 where  $\bar{\mu}$  is the average of a parameter over all chains and  $\mu_l$  is the average for each of the chains,  
382  $l$ . The mean of the variances,  $W$ , is calculated from

383

$$W = \frac{1}{c} \cdot \sum_{l=1}^c Var_l, \quad (13)$$

385

386 where  $Var_l$  is the variance for each parameter in one of the chains. Convergence is assumed  
387 when  $\hat{R}$  (for each of the 22 parameters) reaches a value of  $< 1.1$ . In the present study, this was  
388 the case after more than  $10^5$  iterations.

389

390

### 391 3. RESULTS

392

#### 393 3.1 Thermodynamic data

394

395 The results for the thermodynamic parameters are shown in Figure 2. This figure indicates  
396 the results from the optimization method (dashed lines) and the probability density functions  
397 (pdf, solid lines) along with their medians (dotted lines) for the 11 different clusters. A  
398 comparison between the pdf and the values from Ortega et al. (2012) and Hanson et al. (2017)  
399 is shown in Figure S1. The pdf result from generating histograms of the values from  $Z_0$ , where  
400 the first 5000 points are neglected (see Section 2.5.4). Discussion on the thermodynamic data  
401 follows in Section 4.

402 An overall comparison between modeled and measured NPF rates is shown in Figure 3.  
403 SANTIAGO uses the thermodynamic data from Steihaug's optimization method. The  
404 maximum ratio for the deviation between the modeled and measured nucleation rates is below  
405 a factor of 10 with only a few exceptions. The average deviation is a factor of  $\sim 4$ . Some of the  
406 cases where the ratio deviates by more than a factor of 10 correspond to the lowest temperature  
407 (208 K) binary experiments where the model overestimates the measured NPF rates (Section  
408 3.2). As intended (Section 2.3) the data in Figure 3 do not indicate an apparent bias.

409

#### 410 3.2 Comparison between modeled and experimental data: $J_{1.7\text{nm}}$ vs. $[\text{H}_2\text{SO}_4]$

411

412 To further evaluate the performance of SANTIAGO the calculated NPF rates are shown  
413 together with the measured rates as a function of the sulfuric acid concentration for the five  
414 different temperatures (Figure 4). The color code represents the ammonia mixing ratio, while  
415 grey symbols indicate pure binary nucleation (see Kürten et al., 2016; Duplissy et al., 2016).  
416 Again, as in Figure 3 the agreement between modeled and measured data is good. The same  
417 applies to the parameterization; in some cases, the parameterization yields even better  
418 agreement compared with the model. This is the case, e.g., for the binary nucleation at 208 K  
419 and the data at 278 K and 292 K for the lowest ammonia mixing ratios. However, one clear  
420 advantage of SANTIAGO is that it describes the functional behavior of the system more  
421 accurately. At a temperature of 208 K for the high ammonia mixing ratio the model line shows  
422 a pronounced curvature, whereas the parameterization yields a straight line on the log-log-plot.  
423 The curvature is due to the fact that the survival probability of subcritical clusters (i.e., clusters  
424 below the nonamer) can be strongly affected by losses to walls or pre-existing particles (Ehrhart and  
425 Curtius, 2013). This effect is most strongly pronounced when the concentration of the  
426 nucleating vapor is relatively low, which results in slow cluster/particle growth rates. Other

427 thermodynamic data sets can be used to generate model curves similar to the ones in Figure 4.  
428 Using the data from Ortega et al. (2012) and Hanson et al. (2017) generates Figure S3 and  
429 Figure S4. Figure S2 shows the model curves using  $dH$  and  $dS$  from the medians of the Monte  
430 Carlo simulation. The medians also give good results, except for an overestimation at 248 K  
431 and 278 K at the lowest  $\text{NH}_3$  concentration. This is probably due to comparatively low  $dG$   
432 values for the sulfuric acid tetramer (Table 1). Unfortunately, Yu et al. (2018) did not provide  
433  $dH$  and  $dS$  values but only  $dG$  values at 298 K; therefore, their data set could not be tested.

434

### 435 **3.3 Comparison between modeled and experimental data: $J_{1.7\text{nm}}$ vs. $[\text{NH}_3]$**

436

437 SANTIAGO can yield the dependency of the NPF rates for varying ammonia concentrations  
438 at fixed sulfuric acid concentration. Figure 5 shows these data for five different temperatures  
439 over a wide range of  $\text{NH}_3$  concentrations. The modeled data agree overall very good with the  
440 experimental CLOUD data. The data points indicated in Figure 5 are obtained by normalizing  
441 the CLOUD data to one sulfuric acid concentration for each of the temperatures (see Kürten et  
442 al., 2016); the sulfuric acid concentrations for the normalization are indicated in the figure  
443 annotation.

444 For the lowest temperature (208 K) the new particle formation rates show almost no increase  
445 with  $[\text{NH}_3]$  when ammonia is present at low concentrations ( $\leq 10^6 \text{ cm}^{-3}$ ); this indicates that NPF  
446 is dominated by the pure binary channel. The data points for pure binary conditions are placed  
447 at the estimated  $\text{NH}_3$  background concentrations for 208 K and 223 K in Figure 5 (Kürten et  
448 al., 2016). However, in the model for generating the lines at pure binary conditions (Figure 4),  
449 zero  $\text{NH}_3$  is assumed. For larger  $[\text{NH}_3]$  the NPF rates increase until they reach a plateau at ( $\geq$   
450  $10^9 \text{ cm}^{-3}$ ). In this case new particle formation is only limited by the availability of sulfuric acid;  
451 evaporating ammonia molecules from clusters are, however, rapidly replaced because the  
452 arrival rate of ammonia is similar or faster than the ammonia evaporation rate. For the data at  
453 223 K the situation is very similar. The plateau values agree very well with the calculated values  
454 for collision-controlled new particle formation (Kürten et al., 2018), which can be seen as a  
455 validation of SANTIAGO.

456 For both temperatures (208 K and 223 K) the experimental pure binary new particle  
457 formation rates are well represented by the model. At 248 K and above, the modeled rates at  
458 low  $[\text{NH}_3]$  very likely overestimate the NPF rates (dashed sections of the curves, see discussion  
459 in Section 4) because the model considers only evaporation up to the sulfuric acid tetramer,  
460 which is not sufficient to accurately model binary nucleation at these conditions. **However, the**  
461 **slow rates of  $<1 \times 10^{-3}$  or  $1 \times 10^{-4} \text{ s}^{-1}$  are not atmospherically relevant near the ground in most cases.**  
462 Beyond the regions where binary nucleation dominates, the rates increase steeply with  $[\text{NH}_3]$ .  
463 Although the slopes of the curves flatten somewhat towards high ammonia concentrations, no  
464 plateau is reached even at concentrations of  $10^{11} \text{ cm}^{-3}$  (approximately 4 ppbv).

465

### 466 **3.4 Particle growth rates**

467

468 Figure 6 shows calculated growth rates as a function of the sulfuric acid concentration  
469 according to equation (2). Additionally, a curve from the equations given by Nieminen et al.  
470 (2010) is included. The model results from the present study show a linear increase in  $GR$  as a

471 function of the sulfuric acid monomer concentration as expected (Nieminen et al., 2010). The  
472 higher values from SANTIAGO can be explained by the different methods for calculating the  
473 collision rate constant that includes van der Waals enhancement for the model of the present  
474 study (c.f. Kürten et al., 2018). The increase in  $GR$  at low temperature (208 K) is not intuitive  
475 as the collision rates decrease somewhat with temperature, which should lead to slower  $GR$ .  
476 However, the clusters are more stable at low temperature and their elevated concentrations can  
477 contribute to particle growth (Lehtipalo et al., 2016). This effect is pronounced at 208 K with  
478 some ammonia, which indicates that considering only the condensation of monomers is not  
479 sufficient for some conditions. Not only growth can be effected by coagulation but also new  
480 particle formation rates; therefore, the implementation of a full coagulation scheme (SI Text  
481 S1) is important for the present study. The possibility of deriving growth rates with the model  
482 is an important feature that is not included in the parameterization for the CLOUD new particle  
483 formation rates by Dunne et al. (2016). The modeled growth rates enable further comparison to  
484 experimental data and the future study of particle growth to climatically relevant diameters.

485

486

## 487 4. DISCUSSION

488

### 489 4.1 General discussion on the thermodynamic values

490

#### 491 4.1.1 Results from the optimization and Monte Carlo method

492

493 The posterior distributions with the median values for  $dH$  and  $dS$  for all clusters are shown  
494 in Figure 2. For comparison, the values from Steihaug's optimization method are also shown.  
495 For the  $dS$  values, the medians and the optimized values agree very well. However, the  
496 distributions are rather flat indicating that there is a wide possible range of entropies that lead  
497 to reasonable agreement between modeled and measured NPF rates. This is also reflected in  
498 Table 1 when comparing the  $dS$  to the Ortega et al. (2012) data. These were used to initialize  
499 the optimization method. However, no large differences can be found between the initialized  
500 and optimized values, which can be interpreted such that the quantum chemical calculations  
501 yield accurate results for  $dS$ .

502 The distributions for the  $dH$  values show more structure. However, the only cluster where a  
503 clear peak can be found is the  $A_2B_2$  cluster (for the B evaporation). The median value of the  
504 distribution is somewhat lower (by  $\sim 2$  kcal mol<sup>-1</sup>) compared with the optimized value but it is  
505 well within the half-width of the distribution. For most  $dH$  values there exist flat regions of the  
506 probability density function, e.g., for the  $A_2B_1$  cluster (A evaporation) between  $-28$  kcal mol<sup>-1</sup>  
507 and  $-39$  kcal mol<sup>-1</sup>. In this range the evaporation rate varies between  $5 \times 10^{-3}$  s<sup>-1</sup> and  $1 \times 10^{-11}$  s<sup>-1</sup>  
508 (at 278 K and  $dS = -43$  cal mol<sup>-1</sup> K<sup>-1</sup>, SI Text2). In practice, it does not matter which one of  
509 these evaporation rates is used; the magnitude of the evaporation rate in this range has  
510 essentially no effect on the outcome because the cluster is stable on the considered time-scale  
511 (Kupiainen-Määttä, 2016).

512 For some clusters, limits seem to exist for  $dH$ . For example, the  $dH$  value for the  $A_4$  is below  
513  $-15$  kcal mol<sup>-1</sup> and for the  $A_4B_3$  clusters (A evaporation) the upper limit is approximately  $-19$

514 kcal mol<sup>-1</sup>. The pdf for the A<sub>1</sub>B<sub>1</sub> and the A<sub>2</sub>B<sub>1</sub> clusters show local maxima, which indicate  
515 elevated probability densities around -16.5 kcal mol<sup>-1</sup> and -23 kcal mol<sup>-1</sup>.

516

#### 517 **4.1.2 Comparison of $dH$ and $dS$ to literature data**

518

519 For most of the clusters, the agreement between the Ortega et al. (2012) data and the data  
520 from the present study is quite good. One exception, is the A<sub>4</sub> cluster, where the pdf indicates  
521 a median value of -23.1 kcal mol<sup>-1</sup> for  $dH$  (-19.7 kcal mol<sup>-1</sup> from the optimization method) in  
522 contrast to -16.78 kcal mol<sup>-1</sup> by the Ortega et al. (2012) study. The much lower value found in  
523 the present study is reasonable since Ortega et al. (2012) did not include water vapor in their  
524 calculations. The available water in the CLOUD experiment can lead to significant slower  
525 evaporation rates indicated by the lower  $dH$  value. The difference to the Hanson et al. (2017)  
526 data is generally much larger. Especially, the trimer and tetramer with one ammonia (A<sub>3</sub>B<sub>1</sub> and  
527 A<sub>4</sub>B<sub>1</sub>) evaporate significantly slower for the Hanson et al. (2017) data. This might explain the  
528 much higher NPF rates observed at the warm temperatures for the Hanson et al. (2017)  
529 predictions compared with the CLOUD data (Figure S4). Yu et al. (2018) report  $dG$  values  
530 (Table 1) in their study. While the agreement between their model and CLOUD data is generally  
531 good for ion-induced conditions, the agreement for neutral conditions is only good for low  
532 temperature conditions. At temperatures  $\geq 248$  K the Yu et al. (2018) model underestimates the  
533 measurements by up to many orders of magnitude. This can at least partly be explained by the  
534 significantly higher  $dG$  values for some clusters (e.g., A<sub>2</sub>B<sub>1</sub> and A<sub>4</sub>B<sub>1</sub>) in comparison to the  
535 other literature data and the values from the present study.

536

#### 537 **4.2 Uncertainties and limitations of SANTIAGO**

538

539 One limitation of the model from the present study is that the effect of water vapor is not  
540 taken into account explicitly, i.e., no clusters containing different amounts of water molecules  
541 are considered. However, for the clusters containing no ammonia to some extent humidity  
542 effects are included. This is achieved by scaling the evaporation rates of the sulfuric acid dimer,  
543 trimer and tetramer by a factor  $(20\% / RH)^p$  with  $p = 0.5$  for the dimer and  $1.5$  for the trimer  
544 and tetramer. The first two values for the parameter  $p$  are from Hanson and Lovejoy (2006).  
545 For the tetramer the same dependency as for the trimer is assumed, which introduces  
546 uncertainty. The reported  $dH$  and  $dS$  values for the sulfuric acid tetramer are therefore derived  
547 for a relative humidity of 20% in order to be consistent with the Hanson and Lovejoy (2006)  
548 data. In Figure 4 the agreement between the modeled and measured pure binary data (at 208 K  
549 and 223 K) is relatively good, especially for the 223 K data. For the 208 K data SANTIAGO  
550 overestimates the measured data. It has to be noted, that the model calculations assume an  
551 average  $RH$  (33% at 208 K and 28% at 223 K), whereas the measurement conditions cover  
552 varying relative humidities (12% to 57% at 208 K and 11% to 52% at 223 K). This can explain  
553 some of the scatter in the measured data but not the systematic overestimation for the 208 K  
554 data by the model. However, the general agreement between model and measurement at  $\leq 223$   
555 K is considered good for both ternary and binary conditions. For the warmer temperatures ( $\geq$   
556 248 K) the pure binary conditions can currently not be accurately represented by the model.  
557 This can be seen in Figure 5 for the dashed sections of the curves, which approximately mark

558 the limit of the parameter space regarding the allowed  $\text{NH}_3$  concentrations. For the very low  
559  $\text{NH}_3$  concentrations, the modeled NPF rates approach the “pure” binary conditions. However,  
560 comparison with the data by Ehrhart et al. (2016) who simulated pure binary nucleation for the  
561 CLOUD chamber with the SAWNUC (Sulfuric Acid Water NUCleation) model indicate that  
562 the apparent binary data in Figure 5 are significantly overestimating the true binary NPF rates.  
563 For 248 K the overestimation seems to be within a factor of 10 but for 278 K and 292 K the  
564 overestimation amounts to many orders of magnitude (Ehrhart et al., 2016). For this reason, the  
565 solid line sections for 248 K and warmer have been defined such that the contribution from the  
566 overestimated binary conditions is in any case less than 10%. This means that SANTIAGO can  
567 be applied, e.g., at 292 K for  $\text{NH}_3$  concentrations above ca.  $1 \times 10^7 \text{ cm}^{-3}$  ( $\approx 0.4 \text{ pptv}$  at 292 K and  
568 1 bar). It can be seen that  $\text{NH}_3$  has a large effect even at these tiny concentrations, which are  
569 below the measurable range of ammonia in the atmosphere.

570 The effect of water vapor on particle growth rates needs to be studied in the future.  
571 Comparison between measured and modeled growth rates at small diameters (2 nm) in the acid  
572 base system (sulfuric acid-dimethylamine and sulfuric acid-ammonia) indicates that water has  
573 no significant effect on particle growth (Lehtipalo et al., 2016). The same can be concluded for  
574 the sulfuric acid-ammonia system at larger diameters ( $\sim 10 \text{ nm}$ , see Chen et al., 2018).

575 The fact that no larger clusters than the tetramers can evaporate in SANTIAGO apparently  
576 leads to truncation errors as discussed before for the binary conditions. This truncation leads to  
577 the overestimation of new particle formation rates for the pure binary conditions at the warm  
578 temperatures. To what extent truncation affects the ternary new particle formation can be  
579 discussed based on the cluster evaporation rates for the tetramers at the warmest temperature  
580 (292 K). The evaporation rates are  $\sim 3000 \text{ s}^{-1}$  ( $\text{A}_4\text{B}_1$ ),  $\sim 75 \text{ s}^{-1}$  ( $\text{A}_4\text{B}_2$ ) and  $\sim 0.02 \text{ s}^{-1}$  ( $\text{A}_4\text{B}_3$ ) using  
581 the thermodynamic parameters from Table 1 (first columns) and the equations to convert  $dH$   
582 and  $dS$  to an evaporation rate (see SI Text2). This indicates that new particle formation proceeds  
583 most efficiently via the clusters containing at least three base molecules. For this cluster the  
584 forward reaction rate is larger than the evaporation rate when the total sulfuric acid  
585 concentration is larger than  $\sim 2 \times 10^7 \text{ cm}^{-3}$ . If the  $\text{A}_4\text{B}_3$  and  $\text{A}_4\text{B}_4$  clusters are the dominant ones,  
586 this indicates that even if a pentamer with a small number of base molecules evaporates rapidly  
587 it is probably not very important in terms of contributing to the new particle formation rates as  
588 the main nucleation pathway will follow the clusters with high ammonia content. If truncation  
589 nevertheless plays a role, it can lead to an overestimation of evaporation for a smaller cluster,  
590 thereby compensating for the missing evaporation of the larger clusters. Therefore, it is possible  
591 that some evaporation rates in the present study could be overestimated. However, the data that  
592 are shown in Table 1 for a comparison have been derived from similar methods, where the  
593 effect of evaporation is also considered only up to a certain cluster size limit. Truncation effects  
594 are discussed in detail by Hanson et al. (2017).

595 Similarly, to truncation the negligence of evaporation of either acid or base for all considered  
596 clusters can potentially lead to errors (see Section 2.2). The model includes only the cluster  
597 evaporation rates, which seem to be most relevant (see Figure 1 and cf. Ortega et al., 2012; Yu  
598 et al., 2018). For each cluster, one evaporation rate is included (either acid or base). This means,  
599 that the negligence of the second evaporation channel can lead to an overestimation of the  
600 cluster concentration. However, in case the omitted evaporation rate is smaller than the  
601 considered one, this effect is very likely small. The selection of the considered evaporation rates

602 are guided by the literature data on QC calculations (Ortega et al., 2012; Yu et al., 2018). This  
603 does, however, not rule out that important evaporation channels could be neglected. On the  
604 other hand, increasing the number of free parameters does not necessarily improve the accuracy  
605 of the model but only its complexity and the computational demands for the optimization and  
606 Monte Carlo calculations.

607

### 608 **4.3 Implementation of literature data in SANTIAGO**

609

610 The previous study by Kürten et al. (2016) compares the CLOUD data with ACDC  
611 (Atmospheric Cluster Dynamics Code, McGrath et al., 2012) model calculations using the  
612 thermodynamic data from Ortega et al. (2012). Using the same data Figure S3 shows this  
613 comparison using the model from the present study. Surprisingly the agreement between model  
614 and measurement is better than in the study by Kürten et al. (2016). One difference between the  
615 two studies is that the ACDC model used the formation rate for neutral clusters containing six  
616 sulfuric acid molecules instead of nine in the present study. This difference was tested with the  
617 present model but it does only lead to a very small change in the simulated formation rates. An  
618 effect that can, however, explain the discrepancy is that the ACDC model calculations did not  
619 consider a wide range of particle sizes. This could lead to inaccuracies regarding the coagulation  
620 sink for the formed clusters. Especially at high acid concentrations when growth and nucleation  
621 rates are large, the particles can create a significant sink that can reach similar magnitude as the  
622 wall loss rate in the CLOUD chamber (Kürten et al., 2015b). Neglecting the full size distribution  
623 can lead to an overestimation of cluster concentrations and formation rates (SI Text1). This  
624 effect needs to be studied in more detail in the future. In any case, taking into account particles  
625 over a wide size range should improve the accuracy of a model due to the described effect.

626 The comparison between the CLOUD data and SANTIAGO using the Hanson et al. (2017)  
627 data is shown in Figure S4. Hanson et al. base their data on flow tube measurements performed  
628 at rather warm temperatures (~295 K). The agreement between the modeled and measured data  
629 is good, however, mostly at the low temperatures (208 K and 223 K); for the warmer  
630 temperatures, the model using the literature data significantly overestimates the NPF rates. This  
631 can partly be due to the fact that the model does not include all possible evaporation effects  
632 (acid and base for each cluster). Hanson et al. (2017) derived their data, however, by including  
633 many more possible evaporation channels. Their negligence shifts the new particle formation  
634 rates to higher values. It is likely that this effect is stronger at warm temperatures because at  
635 very cold conditions the evaporation rates for the clusters are generally very low except for the  
636  $A_1B_1$  cluster. For this cluster only one possible evaporation channel exists that is included in  
637 the model. By including the new particle formation rates reported by Hanson et al. (2017) for  
638 278 K at CLOUD chamber conditions (additional symbols in Figure S4 at 278 K), the  
639 agreement is somewhat better but still significantly higher than the CLOUD data. Therefore,  
640 the missing evaporation channels in this study cannot explain the full extent of the discrepancy.

641

642

## 643 **5. SUMMARY AND CONCLUSIONS**

644

645 The model (SANTIAGO, Sulfuric acid Ammonia NucleaTion And GrOwth model)  
646 describes new particle formation and growth from the reactions between sulfuric acid and  
647 ammonia. The effect of water vapor is taken into account but the capability of simulating binary  
648 nucleation is limited to low temperatures ( $\leq 223$  K) because cluster evaporation rates are only  
649 considered up to the tetramer; at warmer temperatures evaporation of larger pure acid clusters  
650 becomes important.

651 SANTIAGO implements evaporation of the smallest clusters, containing one to four sulfuric  
652 acid molecules and a variable number of ammonia molecules. The thermodynamic data ( $dH$   
653 and  $dS$ ) for 11 different channels is used to calculate evaporation rates as a function of  
654 temperature. Two numeric methods have been applied to find the best set of parameters  
655 (Steihaug algorithm) and their probability density functions (Differential Evolution-Markov  
656 Chain algorithm, DE-MC). This is achieved by comparing the model output to the CLOUD  
657 data set for neutral nucleation in the ternary system of sulfuric acid-water-ammonia (Dunne et  
658 al., 2016; Kürten et al., 2016). The average ratio between modeled and measured data is found  
659 to be as small as a factor of  $\sim 4$  (mean error) for a wide range of conditions (208 K to 292 K,  
660 sulfuric acid at atmospherically relevant concentrations, e.g.,  $\geq 5 \times 10^5$  cm<sup>-3</sup> at 208 K and  $\leq 2 \times 10^9$   
661 at 292 K) when using the best fit parameters. SANTIAGO can very well represent the neutral  
662 measured CLOUD data for all tested conditions. This means that even binary neutral nucleation  
663 at the lowest temperatures (208 K and 223 K) can be well described.

664 The optimization and the Monte Carlo method were successfully applied to explore the  
665 landscape of the cluster thermodynamics for the nucleating system of sulfuric acid and  
666 ammonia. However, the probability density functions from the DE-MC algorithm do not yield  
667 a very clear picture of the most likely values for  $dH$  and  $dS$  as the derived probability density  
668 functions are rather flat and indicate a wide range of probable values. Therefore, the parameters  
669 reported in the present study have a rather high uncertainty. Future experiments and quantum  
670 chemical calculations are necessary to narrow down these uncertainties.

671 Implementation of the literature data in the model indicates that the Ortega et al. (2012)  
672 thermodynamic data describes the CLOUD data better than previously thought (Kürten et al.,  
673 2016). This could be because of the negligence of large particles in the previous study. It seems  
674 essential to include the larger nucleated particles in the model as these contribute to the sink for  
675 the small nucleating clusters and particles. The Hanson et al. (2017) data overestimate the new  
676 particle formation rates for the warm temperatures (278 K and 292 K). No direct comparison to  
677 the Yu et al. (2018) is possible as no temperature-dependent evaporation rates can be calculated  
678 from their reported  $dG$  values at 298 K.

679 SANTIAGO allows calculating new particle formation rates for a wide range of  
680 experimental conditions ( $T$ ,  $RH$ , sulfuric acid and ammonia concentration). In contrast to the  
681 parameterization from Dunne et al. (2016) for the CLOUD data it is also capable of considering  
682 different external sinks (e.g., due to chamber/flow tube walls in laboratory experiments or the  
683 presence of pre-existing particles in the atmosphere) that can affect nucleation and particle  
684 growth (Kerminen and Kulmala, 2002; Ehrhart and Curtius, 2013). With the model, growth  
685 rates can also be determined.

686 Finally, the strong dependence on  $[\text{NH}_3]$  regarding NPF even at levels below 1 pptv  
687 highlights the need for improved instrumentation when one wants to understand the impact of



688 ammonia on nucleation as no available technique can measure such low atmospheric ammonia  
689 concentrations in real-time.

690

691

#### 692 **DATA AVAILABILITY**

693

694 Data used in this study are available upon request by sending an email to the corresponding  
695 author.

696

697

#### 698 **AUTHOR CONTRIBUTION**

699

700 AK developed the numerical nucleation and growth model, implemented the optimization algorithms,  
701 performed the modeling calculations and wrote the manuscript.

702 **Nomenclature**

703

704  $b$  variance of the means for each parameter ( $dH$  or  $dS$ )

705  $B$  Hessian matrix of  $f$  regarding all  $dH$  and  $dS$  values

706  $c$  number of chains

707  $d_p$  particle diameter

708  $dH$  enthalpy for one of the reactions (see Table 1)

709  $dS$  entropy for one of the reactions (see Table 1)

710  $f$  average error for all modeled and measured particle formation rates

711  $g$  gradient vector of  $f$  regarding all  $dH$  and  $dS$  values

712  $GR$  particle growth rate

713  $i$  index

714  $j$  index

715  $J_{\text{exp}}$  experimental formation rate (from CLOUD experiment)

716  $J_{\text{model}}$  modeled formation rate

717  $k$  iteration index in numeric algorithms

718  $K$  collision rate constant for clusters/particles

719  $l$  index

720  $m$  index for critical cluster size ( $m = 9$ )

721  $M$  approximated function value in Steihaug's method

722  $n$  number of experiments ( $n_1$  for 208 K,  $n_2$  for 223 K,  $n_3$  for 248 K,  $n_4$  for 278 K,  $n_5$  for  
723 298 K)

724  $n_{\text{coefs}}$  total number of coefficients, i.e., all  $dH$  and  $dS$  values ( $n_{\text{coefs}} = 22$ )

725  $N$  cluster/particle number density

726  $p$  power dependency of an evaporation rate regarding the relative humidity

727  $P$  acceptance probability in Monte Carlo algorithm

728  $\hat{R}$  statistical metric to indicate convergence for the Monte Carlo simulation

729  $RH$  relative humidity

730  $s$  vector of step changes (all  $dH$  and  $dS$  values) in one iteration

731  $t$  empirical parameter needed in Steihaug's optimization algorithm ( $t_1, t_2$ )

732  $T$  temperature

733  $Var$  variance for a parameter in one of the chains

734  $W$  mean of the variances over all chains for one parameter

735  $x$  current vector of all  $dH$  and  $dS$  values (Monte Carlo simulation)

736  $x_1, x_2$  drawn vectors of all  $dH$  and  $dS$  values from history (Monte Carlo simulation)

737  $x_{\text{new}}$  new vector of all  $dH$  and  $dS$  values (Monte Carlo simulation)

738  $x_{\text{old}}$  old vector of all  $dH$  and  $dS$  values (Monte Carlo simulation)

739  $Z_0$  joint history for all chains in the Monte Carlo simulation

740  $\delta$  term in the calculation of the new vector in the Monte Carlo algorithm

741  $\Delta$  radius of trust region in Steihaug's method

742  $\Delta_{\text{max}}$  maximum allowed radius of trust region in Steihaug's method

743  $\gamma$  scaling factor in the calculation of the new vector in the Monte Carlo algorithm

744  $\eta$  empirical parameter needed in Steihaug's optimization algorithm ( $\eta_1, \eta_2, \eta_3$ )

745  $\mu$  mean value for one parameter

746	$\bar{\mu}$	mean value over all chains for one parameter
747	$\rho$	ratio between actual and predicted function reduction in Steihaug's method
748	$\sigma$	standard deviation
749	$\sigma_{ini}$	standard deviation of the parameters from the prior distribution

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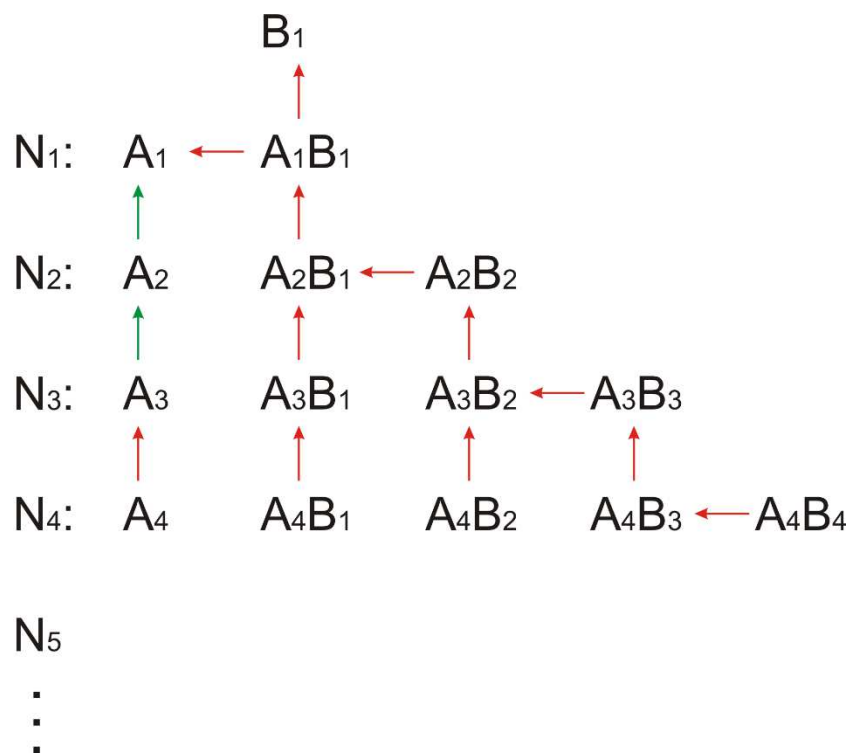
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1046 **Table 1:**  $dH$  and  $dS$  values from this study ( $^\ddagger$ optimization method,  $^*$ medians from Monte Carlo simulation) and from the literature.  $dG$  values at 298  
1047 K.  $^a$ Data from Ortega et al. (2012).  $^b$ Data from Hanson et al. (2017).  $^c$ Data from Yu et al. (2018).  $^\diamond$ Value applies for cluster without involvement of  
1048 water, with different amounts of water molecules this value varies between 11.52 and 12.59 kcal mol $^{-1}$ .  $^\circ$ Value applies for cluster without involvement  
1049 of water, with different amounts of water molecules this value varies between 5.71 and 8.37 kcal mol $^{-1}$ .  
1050

Reaction	$-dH$ (kcal mol $^{-1}$ )	$-dS$ (cal mol $^{-1}$ K $^{-1}$ )	$-dG$ (kcal mol $^{-1}$ ) at 298 K
$H_2SO_4 + NH_3 \Leftrightarrow (H_2SO_4)_1(NH_3)_1$	16.7 $^\ddagger$ , 12.8* (16.00) $^a$ (15.0) $^b$	29.8 $^\ddagger$ , 30.0* (28.14) $^a$ (21.8) $^b$	7.8 $^\ddagger$ , 3.9* (7.61) $^a$ (8.5) $^b$ (7.77) $^c$
$(H_2SO_4)_1(NH_3)_1 + H_2SO_4 \Leftrightarrow (H_2SO_4)_2(NH_3)_1$	27.8 $^\ddagger$ , 29.1* (29.00) $^a$ (29.0) $^b$	43.1 $^\ddagger$ , 42.9* (42.90) $^a$ (52.0) $^b$	15.0 $^\ddagger$ , 16.3* (16.22) $^a$ (13.5) $^b$ (11.65) $^{c,\diamond}$
$(H_2SO_4)_2(NH_3)_1 + NH_3 \Leftrightarrow (H_2SO_4)_2(NH_3)_2$	19.3 $^\ddagger$ , 21.1* (19.46) $^a$ (19.0) $^b$	34.7 $^\ddagger$ , 34.2* (33.41) $^a$ (26.8) $^b$	9.0 $^\ddagger$ , 10.9* (9.5) $^a$ (11.0) $^b$ (8.75) $^{c,\circ}$
$(H_2SO_4)_2(NH_3)_1 + H_2SO_4 \Leftrightarrow (H_2SO_4)_3(NH_3)_1$	18.3 $^\ddagger$ , 20.0* (21.06) $^a$ (26.0) $^b$	37.6 $^\ddagger$ , 37.2* (36.69) $^a$ (35.3) $^b$	7.1 $^\ddagger$ , 8.9* (10.13) $^a$ (12.5) $^b$ (7.08) $^c$
$(H_2SO_4)_2(NH_3)_2 + H_2SO_4 \Leftrightarrow (H_2SO_4)_3(NH_3)_2$	28.1 $^\ddagger$ , 30.6* (27.63) $^a$ (30.0) $^b$	38.0 $^\ddagger$ , 38.3* (38.74) $^a$ (36.9) $^b$	16.8 $^\ddagger$ , 19.1* (16.09) $^a$ (19.0) $^b$ (12.17) $^c$
$(H_2SO_4)_3(NH_3)_2 + NH_3 \Leftrightarrow (H_2SO_4)_3(NH_3)_3$	25.7 $^\ddagger$ , 27.1* (25.48) $^a$ (20.0) $^b$	37.6 $^\ddagger$ , 37.9* (38.07) $^a$ (28.5) $^b$	14.5 $^\ddagger$ , 15.8* (14.14) $^a$ (11.5) $^b$ (7.42) $^c$
$(H_2SO_4)_3 + H_2SO_4 \Leftrightarrow (H_2SO_4)_4$	19.7 $^\ddagger$ , 23.1* (16.78) $^a$ (23.0) $^b$	27.1 $^\ddagger$ , 26.7* (27.84) $^a$ (43.9) $^b$	11.6 $^\ddagger$ , 15.1* (8.48) $^a$ (9.9) $^b$ (n.a.) $^c$
$(H_2SO_4)_3(NH_3)_1 + H_2SO_4 \Leftrightarrow (H_2SO_4)_4(NH_3)_1$	21.8 $^\ddagger$ , 20.7* (21.34) $^a$ (24.5) $^b$	43.2 $^\ddagger$ , 44.2* (43.50) $^a$ (43.6) $^b$	8.9 $^\ddagger$ , 7.5* (8.38) $^a$ (11.5) $^b$ (4.16) $^c$
$(H_2SO_4)_3(NH_3)_2 + H_2SO_4 \Leftrightarrow (H_2SO_4)_4(NH_3)_2$	22.9 $^\ddagger$ , 24.1* (23.04) $^a$ (26.0) $^b$	39.6 $^\ddagger$ , 39.9* (40.15) $^a$ (36.9) $^b$	11.1 $^\ddagger$ , 12.2* (11.08) $^a$ (15.0) $^b$ (7.48) $^c$
$(H_2SO_4)_3(NH_3)_3 + H_2SO_4 \Leftrightarrow (H_2SO_4)_4(NH_3)_3$	27.9 $^\ddagger$ , 30.8* (27.60) $^a$ (30.0) $^b$	41.1 $^\ddagger$ , 40.3* (41.09) $^a$ (34.2) $^b$	15.7 $^\ddagger$ , 18.8* (15.36) $^a$ (19.8) $^b$ (12.34) $^c$
$(H_2SO_4)_4(NH_3)_3 + NH_3 \Leftrightarrow (H_2SO_4)_4(NH_3)_4$	19.2 $^\ddagger$ , 20.3 (19.18) $^a$ (21.0) $^b$	28.7 $^\ddagger$ , 29.0* (28.68) $^a$ (27.8) $^b$	10.6 $^\ddagger$ , 11.6* (10.63) $^a$ (12.7) $^b$ (11.34) $^c$

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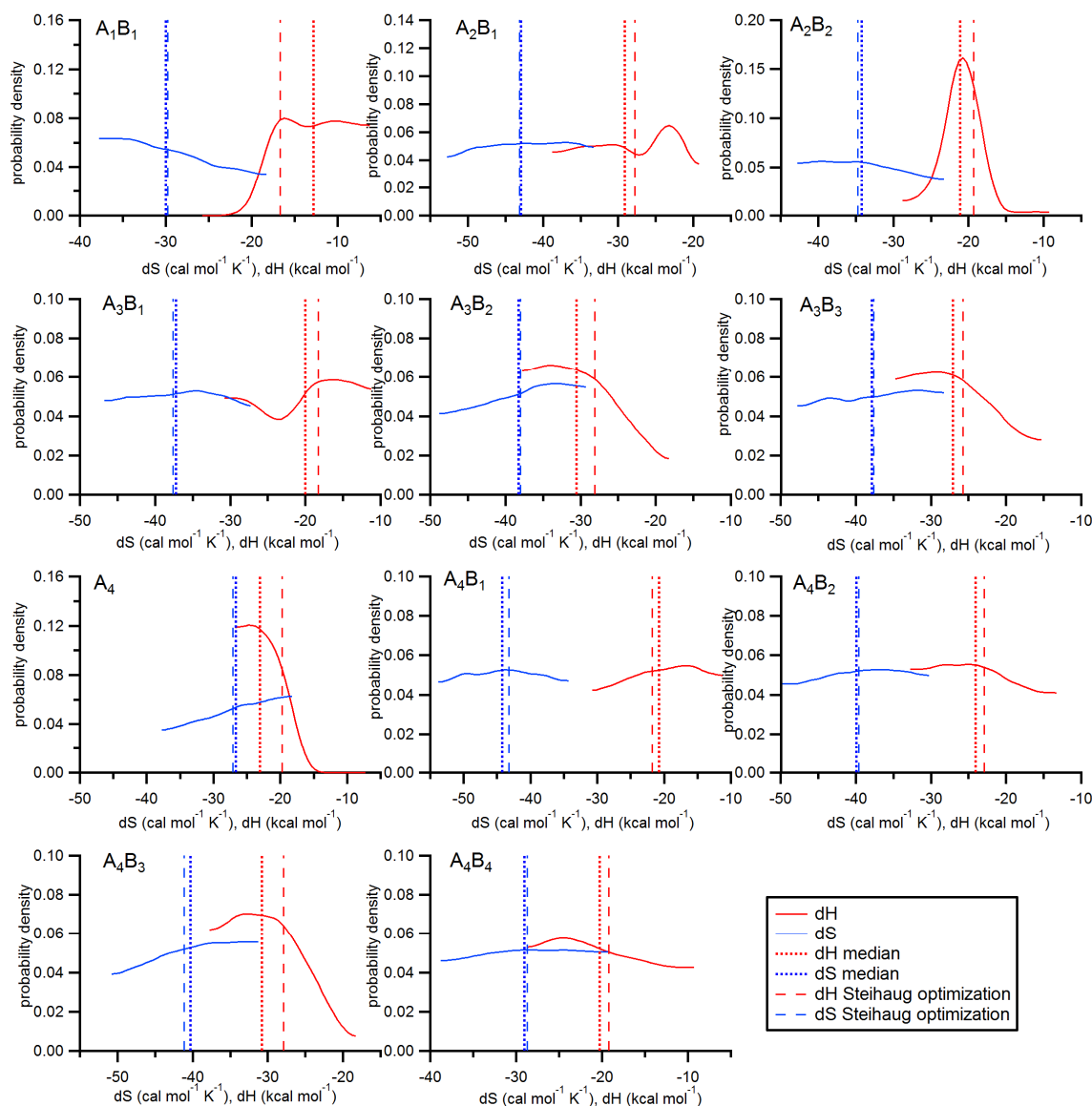
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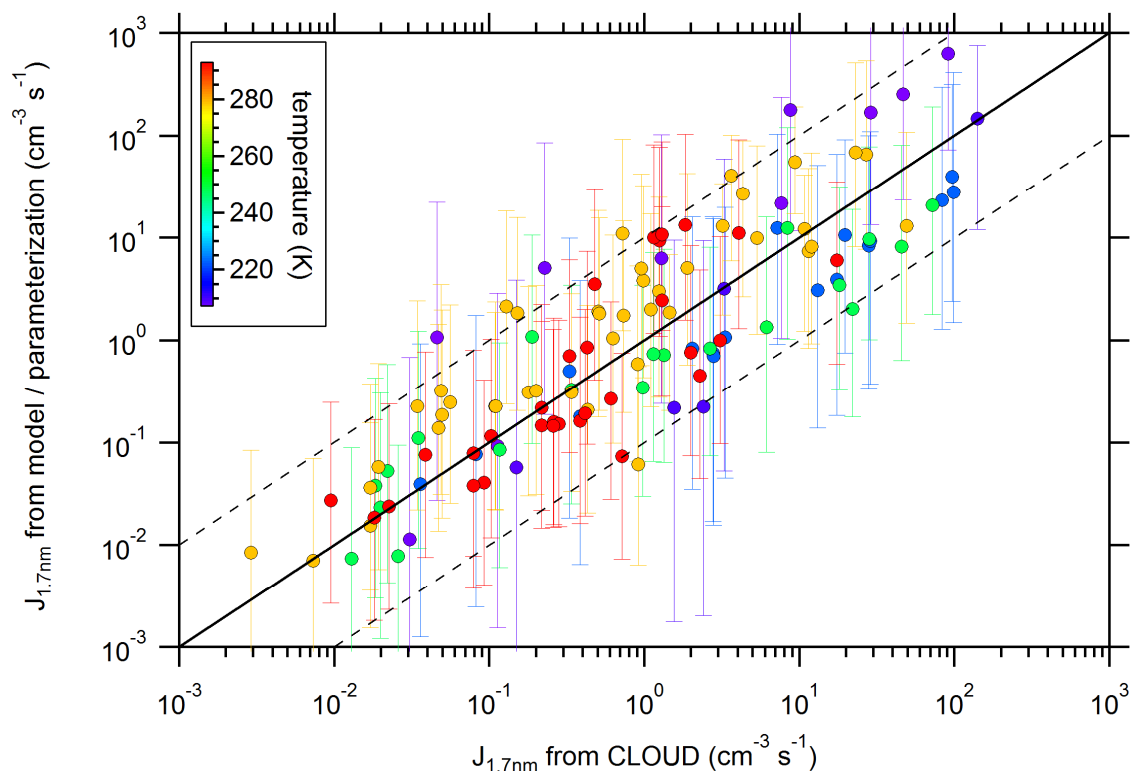
1055 **Figure 1.** Acid-base scheme implemented in SANTIAGO (Sulfuric acid Ammonia NucleaTion  
 1056 And GrOwth model).  $A_xB_y$  denotes a cluster of sulfuric acid and ammonia with  $x$  sulfuric acid  
 1057 molecules and  $y$  ammonia molecules. The arrows indicate the considered evaporation rates. Red  
 1058 colors mark the evaporation channels optimized with numeric methods in the present study.  
 1059 Evaporation rates for the channels marked with green arrows were taken from Hanson and  
 1060 Lovejoy (2006). Forward reactions are not shown but the model considers all possible  
 1061 collisions, i.e., cluster-cluster collisions and not just the additions of monomers.  
 1062 Clusters/particles beyond the pentamer (with concentration  $N_5$ ) are not allowed to evaporate;  
 1063 for these larger clusters, the base content is not considered.



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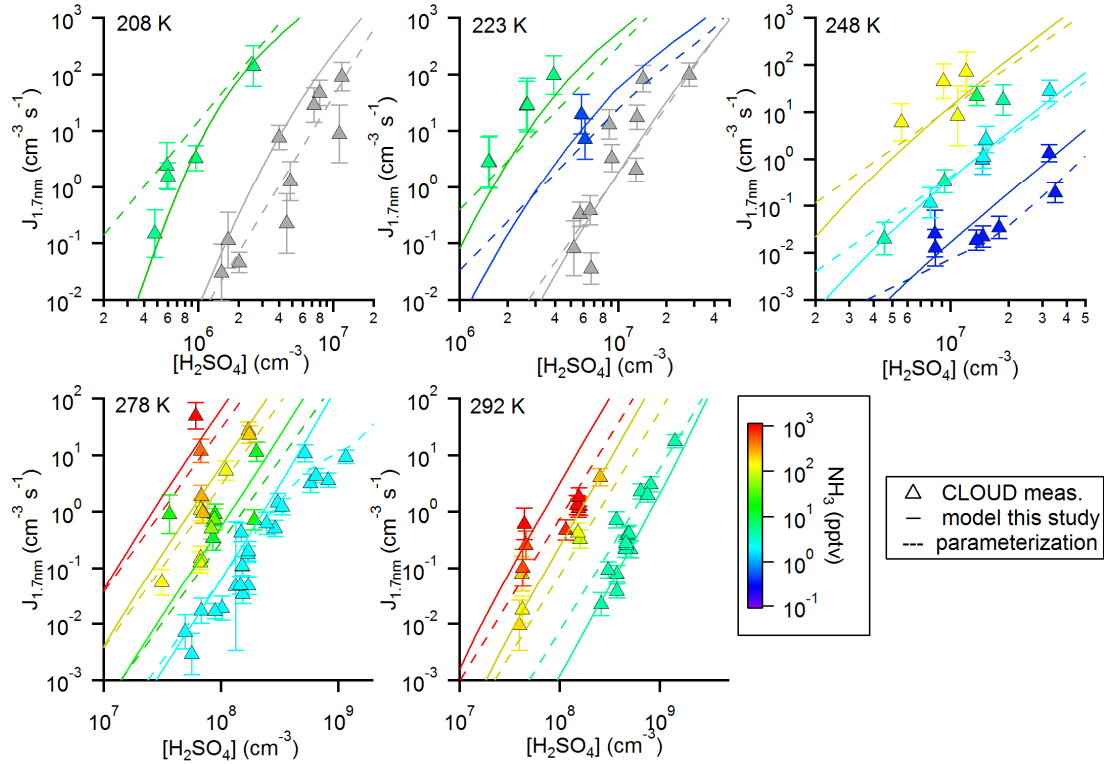
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1066 **Figure 2:** Probability density functions of  $dH$  and  $dS$  values for 11 clusters in the acid base  
 1067 system ( $A_xB_y$  = cluster of sulfuric acid and ammonia with  $x$  sulfuric acid molecules and  $y$   
 1068 ammonia molecules). The vertical lines indicate the values from the optimization method  
 1069 (dashed lines) and the medians of the probability density functions (dotted lines).



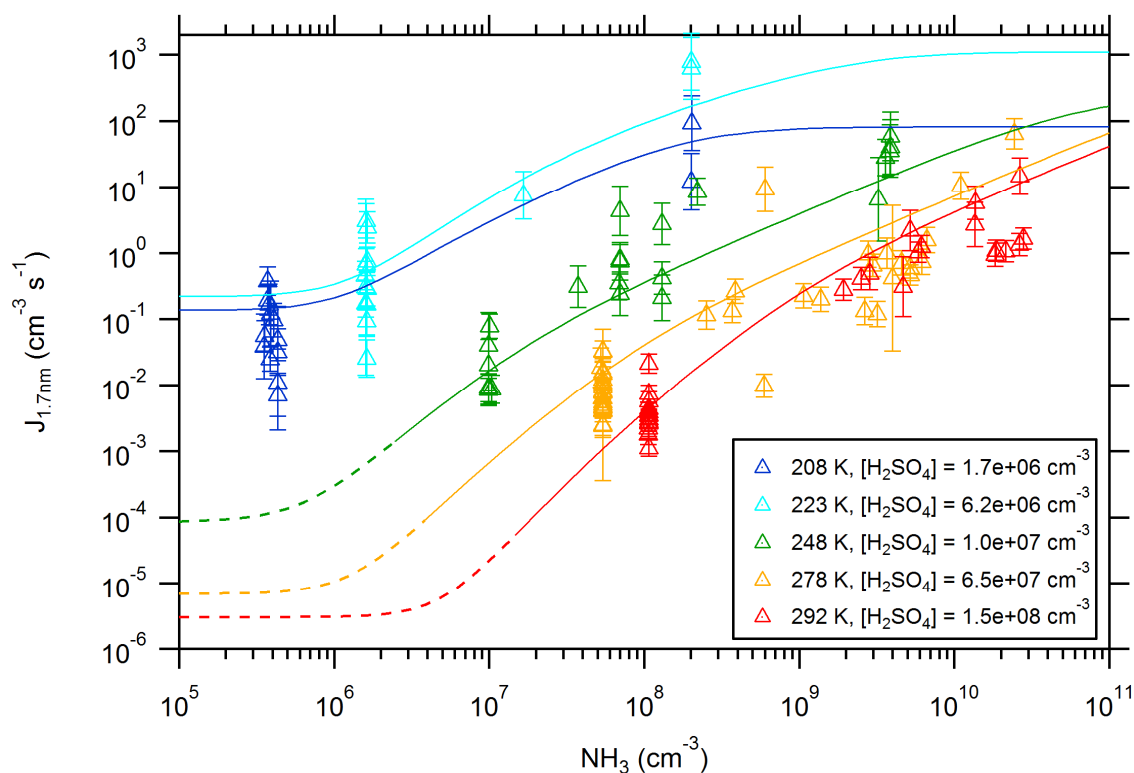
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1072 **Figure 3:** Calculated new particle formation (NPF) rates vs. measured NPF rates (from Kürten  
1073 et al., 2016). The color code indicates the temperature (between 208 K and 292 K). The  
1074 calculated values are from the model using the thermodynamic data from Steihaug's  
1075 optimization method. The solid line indicates the one-to-one correspondence, while the dashed  
1076 lines indicate a factor of ten deviation from the one-to-one line. The error bars include the  
1077 uncertainty of the  $[\text{H}_2\text{SO}_4]$  (factor of 2) and the  $[\text{NH}_3]$  (see Kürten et al., 2016).



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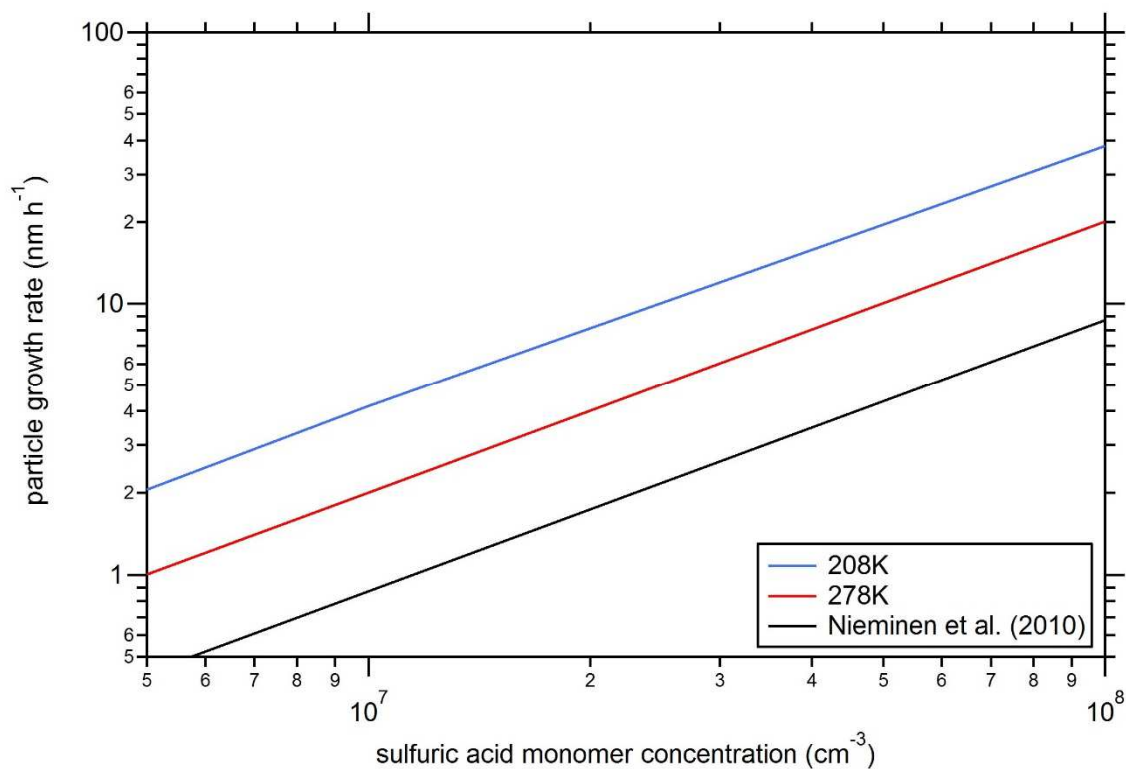
1080 **Figure 4:** Comparison between simulated and measured new particle formation rates for five  
 1081 different temperatures. The color code indicates the ammonia mixing ratio (for the respective  
 1082 temperatures indicated in the figure panels and a pressure of 1 bar); the grey symbols indicate  
 1083 pure binary conditions. The model (solid lines) uses thermodynamic data from the optimization  
 1084 scheme according to Steihaug (1983, Section 2.4). The average ratio for the deviation is  $\sim 4$ . In  
 1085 comparison, the results from the parameterization are also shown (dashed lines, Gordon et al.,  
 1086 2017).



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1089 **Figure 5:** New particle formation rates as a function of the ammonia concentration. The  
1090 triangles show the neutral formation rates from the CLOUD experiment normalized to the  
1091 indicated sulfuric acid concentration for five different temperatures (Kürten et al., 2016). The  
1092 lines show calculated NPF rates from the model using the thermodynamic data from the  
1093 optimization method (Table 1). The dashed sections (for 248 K, 278 K and 292 K) indicate  
1094 regions of the parameter space where the model does not give accurate results as the true binary  
1095 rates are expected to be lower (Ehrhart et al., 2016).





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1098 **Figure 6:** Particle growth rates as a function of the sulfuric acid monomer concentration. The  
 1099 black line indicates the theoretical curve from Nieminen et al. (2010) for a temperature of 278  
 1100 K and for sulfuric acid vapor. The other lines show the calculated particle growth rates at two  
 1101 different temperatures (indicated in the figure legend). The  $\text{NH}_3$  concentration was set to  $1 \times 10^8$   
 1102  $\text{cm}^{-3}$  (blue and red curve); for all calculations a density of  $1615 \text{ kg m}^{-3}$  and a particle mobility  
 1103 diameter of  $2.4 \text{ nm}$  was used; the diameter of the particles was calculated assuming a molecular  
 1104 mass of  $151 \text{ amu}$  (2 water and 1 ammonia molecule per sulfuric acid molecule).