



## High-resolution ( $0.05^\circ \times 0.05^\circ$ ) $\text{NO}_x$ emissions in the Yangtze River Delta inferred from OMI

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### Abstract

Emission datasets of nitrogen oxides ( $\text{NO}_x$ ) at high horizontal resolutions (e.g.,  $0.05^\circ \times 0.05^\circ$ ) are crucial for understanding human influences at fine scales, air quality studies, and pollution control. Yet high-resolution emission data are often lacking or contain large uncertainties especially for the developing  
15 regions. Taking advantage of long-term satellite measurements of nitrogen dioxide ( $\text{NO}_2$ ), here we develop a computationally efficient method to inverting  $\text{NO}_x$  emissions in major urban areas at the  $0.05^\circ \times 0.05^\circ$  resolution. The inversion accounts for the nonlinear effects of horizontal transport, chemical loss, and deposition. We construct a 2-dimensional Peking University High-resolution Lifetime-Emission-Transport (PHLET) model, its adjoint model (PHLET-A), and a Satellite Conversion Matrix  
20 approach to relate emissions, simulated  $\text{NO}_2$ , and satellite  $\text{NO}_2$  data. The inversion method is applied to summer months of 2012–2016 in the Yangtze River Delta area (YRD,  $118^\circ\text{E}$ – $123^\circ\text{E}$ ,  $29^\circ\text{N}$ – $34^\circ\text{N}$ ), a major



polluted region of China, using the POMINO NO<sub>2</sub> vertical column density product retrieved from the Ozone Monitoring Instrument. A systematic analysis of inversion errors is performed, including using an Observing System Simulation Experiment-like test. Across the YRD area, the inverted summer average emission ranges from 0 to 12.0 kg km<sup>-2</sup> h<sup>-1</sup>, and the lifetime (due to chemical loss and deposition) from 1.4 to 3.6 h. Our inverted emission dataset reveals fine-scale spatial information tied to nighttime light, population density, road network, and maritime shipping. Many of the inverted fine-scale emission features are not well represented or not included in the widely used Multi-scale Emissions Inventory of China. Our inversion method can be applied to other regions and other satellite sensors such as the TROPOspheric Monitoring Instrument.

## 10 1. Introduction

Nitrogen oxides (NO<sub>x</sub> = NO + NO<sub>2</sub>) are a main precursor of particulate matter, ozone, and other atmospheric pollutants. NO<sub>x</sub> strongly influence the atmospheric oxidative capacity, affect the climate, and are toxic to many organisms. NO<sub>x</sub> are emitted from natural (soil, biomass burning, and lightning) and anthropogenic (transportation, energy, industry, and residential) sources (Lin, 2012). Over the past decade, China has experienced rapid growth in the Gross Domestic Product (GDP, by 8.3% a<sup>-1</sup> on average from 2008 to 2017), fossil fuel consumption (by 5.5% a<sup>-1</sup> from 2007 to 2015), and urbanization (National Bureau of Statistics of China, <http://data.stats.gov.cn/>). These socioeconomic changes have been accompanied by a rapid change in NO<sub>x</sub> emissions in the urban and surrounding areas. With the large and continuously increasing urban population and motor vehicles, NO<sub>x</sub> pollution is particularly severe in large cities such as Beijing and Shanghai (Barnes and Rudziński, 2013; Lin et al., 2016). Many coastal cities like Shanghai have also experienced enormous growth in the shipping business and resulting pollution along with the growing volume of global economic trade. Emissions from seaborne transport play an increasingly important role in the global air pollution (Fu et al., 2017). Understanding the urban pollution and its environmental impacts requires accurate quantitative knowledge on NO<sub>x</sub> emissions at a very high horizontal resolution, which is still lacking especially for the developing countries.



Gridded bottom-up emission inventories typically use spatial proxies (like population and GDP) to allocate provincial-level emission values to individual locations (Zhao et al., 2011; Janssens-Maenhout et al., 2015), which may lead to large uncertainties at high resolutions (Zhao et al., 2011; Zheng et al., 2017; Geng et al., 2017). Top-down inversion using satellite retrieval products of tropospheric vertical column densities (VCDs) of nitrogen dioxide (NO<sub>2</sub>) is a widely used independent estimate of NO<sub>x</sub> emissions (Martin et al., 2003; Stavrou et al., 2008; Lin et al., 2010; Mijling and R., 2012; Gu et al., 2014; Beirle et al., 2015; Miyazaki et al., 2016; Ding et al., 2017a). The traditional top-down methods based on local mass balance (LMB) or its variants assume a weak effect of horizontal transport (Martin et al., 2003; Lamsal et al., 2011; Lin, 2012; Gu et al., 2014; Boersma et al., 2015). These algorithms work relatively well at low resolutions (> 50 km) given the relatively short lifetime of NO<sub>x</sub> (hours to 1 day), but may introduce large uncertainties when applied to higher resolutions – for example, emissions in the rural-urban fringe zone cannot be identified accurately. The Adjoint Model and Kaman Filter methods better account for horizontal transport, although their applicability is limited by expensive computational costs (Stavrou et al., 2008; Mijling and R., 2012; Miyazaki et al., 2016; Qu et al., 2017; Ding et al., 2017a). These more sophisticated methods are typically applied to limited time periods, limited spatial domains, and/or low horizontal resolutions (Gu et al., 2014; Ding et al., 2017b; Miyazaki et al., 2012; Stavrou et al., 2008; Qu et al., 2017; Huang et al., 2014). The LMB, Adjoint Model and Kaman Filter approaches normally use 3-dimensional chemical transport models (CTMs) to relate emissions to VCDs. With a few exceptions (Lin et al., 2012; Stavrou et al., 2013), the uncertainties in CTMs are not often assessed comprehensively due to expensive computational costs. A computationally low-cost method for space-based high-resolution NO<sub>x</sub> emission inversion will be helpful for understanding the urban pollution and its trends and variability. This is particularly true with the advent of fine spatial resolution satellite sensors such as the TROPOspheric Monitoring Instrument (TROPOMI).

This study presents a computationally low-cost space-based top-down approach to constructing high-resolution NO<sub>x</sub> emission inventory for the urban and surrounding areas. The approach is applied to the Yangtze River Delta (YRD) area (118°E-123°E, 29°N-34°N, which includes Shanghai, Nanjing,



Hangzhou and other 13 cities) on a  $0.05^\circ \times 0.05^\circ$  grid, using the POMINO NO<sub>2</sub> VCD data retrieved from the Ozone Monitoring Instrument (OMI). We derive the average NO<sub>x</sub> emissions for the summer months (June, July, and August) of 2012–2016. We construct a 2-dimensional (2-D) Peking University High-resolution Lifetime-Emission-Transport (PHLET) model and its adjoint model (PHLET-A) to facilitate  
5 the emission inversion. The concentration-dependent lifetime of NO<sub>x</sub> is estimated as well in order to account for the nonlinear NO<sub>x</sub> chemistry.

Section 2 presents the data and method for high-resolution NO<sub>x</sub> emission inversion. Inversion uncertainties are analyzed explicitly. We also test the inversion method by applying it to the NO<sub>2</sub> VCDs simulated by the GEOS-Chem CTM, in a manner similar to the Observing System Simulation Experiment  
10 (OSSE). Section 3 presents the top-down estimate of NO<sub>x</sub> emissions, lifetimes, and their uncertainties. Comparison with the Multi-scale Emissions Inventory of China (MEIC) is also provided. Section 4 concludes the study.

## 2. Data and Method

### 2.1. A general framework to retrieve NO<sub>x</sub> emissions at a high resolution

15 The high-resolution NO<sub>x</sub> emission retrieval framework consists of multiple steps. First, the POMINO NO<sub>2</sub> VCD data over summer 2012–2016 are averaged on a  $0.05^\circ \times 0.05^\circ$  grid, using a special oversampling technique that preserves the finest spatial information possible. Second, the PHLET model is constructed to simulate the local net source (emission – loss) and horizontal transport of NO<sub>2</sub> VCD on the  $0.05^\circ \times 0.05^\circ$  grid. A Satellite Conversion Matrix (SCM) approach is used for spatial conversion between the PHLET  
20 grid space and the satellite pixel space. Third, the PHLET-A adjoint model is constructed to, together with PHLET, invert the local net source from satellite NO<sub>2</sub> VCD data. Finally, the emission and lifetime of NO<sub>x</sub> at each grid cell is derived from the inverted local net source term, by assuming a fixed formula within the small study domain for the nonlinear relationship between lifetime and VCD. A rigorous error analysis for the framework and models is also conducted, including using an OSSE-like test.



Our inversion method explicitly accounts for horizontal transport and the nonlinear relationship between  $\text{NO}_x$  emissions, lifetimes, and  $\text{NO}_2$  VCDs. With a few reasonable assumptions, the method is computationally efficient, suitable for speedily conducting high-resolution emission inversion in multiple areas and across a long time period. In the case of YRD here, with one computational core (Intel<sup>®</sup> Xeon<sup>®</sup> Gold 6130 CPU @ 2.10GHz), the inversion calculation takes about 36 hours after necessary input data are prepared.

## 2.2. Tropospheric $\text{NO}_2$ VCDs retrieved from OMI

OMI is a UV/VIS nadir solar backscatter spectrometer on board the Aura satellite. OMI provides daily global coverage. Each complete swath of OMI consists of 60 ground pixels, the sizes of which increase from  $13 \text{ km} \times 24 \text{ km}$  at nadir to about  $40 \text{ km} \times 150 \text{ km}$  at the swath edge in accordance to the view zenith angle (VZA) from  $0^\circ$  to  $57^\circ$  (de Graaf et al., 2016).

We use Level-2 tropospheric  $\text{NO}_2$  VCD data from the POMINO product (Lin et al., 2014; Lin et al., 2015). As described in detail in Lin et al. (2014; 2015), POMINO is an OMI-based regional  $\text{NO}_2$  product that includes a number of important features. Briefly, POMINO adopts the tropospheric slant column density (SCD) data from DONIMO v2 and conducts an improved calculation of tropospheric air mass factors (AMFs) and VCDs (i.e.,  $\text{VCD} = \text{SCD} / \text{AMF}$ ) (Boersma et al., 2011). Key features of the POMINO algorithm include explicit representation of aerosol scattering and absorption (by combining aerosol data from daily nested GEOS-Chem (at  $0.3125^\circ \text{ long.} \times 0.25^\circ \text{ lat.}$ ) simulations and monthly MODIS/Aqua aerosol optical depth (AOD) data), explicit representation of the angular dependence of surface reflection, high-resolution  $\text{NO}_2$  profiles from GEOS-Chem (at  $0.3125^\circ \text{ long.} \times 0.25^\circ \text{ lat.}$ ), consistent retrievals of clouds (a prerequisite for the  $\text{NO}_2$  retrieval) and  $\text{NO}_2$ , and use of a parallelized, LIDORT-driven AMFv6 package. POMINO  $\text{NO}_2$  VCDs are consistent with ground-based MAX-DOAS data (Liu et al., 2018b).

To better relate  $\text{NO}_x$  emissions to  $\text{NO}_2$  VCDs at the  $0.05^\circ \times 0.05^\circ$  resolution, we only employ the  $\text{NO}_2$  data in summer (June, July, and August), in which season the lifetime of  $\text{NO}_2$  is the shortest (a few hours). We combine data over 2012–2016 to increase the sample size. The change in  $\text{NO}_2$  VCD from June to August



is relatively small, reducing the effect of intra-seasonal variability when inverting  $\text{NO}_x$  emissions from summer mean  $\text{NO}_2$  VCDs. We screen out the 30 outer pixels with VZA larger than  $30^\circ$  (cross-track width larger than 36 km) that greatly smear the spatial gradient of  $\text{NO}_2$ , pixels with cloud radiance fraction exceeding 50%, and pixels with AOD larger than 3 (i.e., when the aerosol data used in the  $\text{NO}_2$  retrieval are unreliable). We also exclude data with raw anomaly problems (<http://projects.knmi.nl/omi/research/product/rowanomaly-background.php>). We then convert the pixel-specific Level-2 data to the  $0.05^\circ \times 0.05^\circ$  grid.

To convert from the satellite pixel space to the  $0.05^\circ \times 0.05^\circ$  grid space, we use an oversampling method that employ satellite data on multiple days to enhance the horizontal resolution (Zhang et al., 2014). For each  $0.05^\circ \times 0.05^\circ$  grid cell, we average all pixels covering the grid cell from all valid days, using area-based weighting. The oversampling approach takes advantage of the fact that the exact footprint of the OMI instrument slightly changes from one day to another, so does the exact footprint of a satellite pixel at a given VZA. Thus, sampling from multiple days increases the horizontal resolution of data. Our oversampling approach is different from Fioletov et al., who filled a grid cell with data from pixels within a certain distance (e.g., 30 km), which implied a spatial smoothing (Fioletov et al., 2011; Krotkov et al., 2016; Sun et al., 2018).

For purpose of emission inversion, we assume that the error of VCD at a satellite pixel ( $\sigma_p$ ) contains an absolute error of  $0.5 \times 10^{15}$  molecules  $\text{cm}^{-2}$  and a relative error of 30% (Lin et al., 2010; Boersma et al., 2011; Lin et al., 2015; Beirle et al., 2011). We further add in quadrature an additional error ( $\sigma_g$ ) when a satellite pixel is projected to the grid cells at a finer resolution; this error is important in the urban-rural fringe zone. For a given grid cell,  $\sigma_g$  is set to be 15% of the standard deviation of VCDs at its surrounding eight grid cells. Sampling over multiple days reduces the random error by a factor of  $s = \left(\sqrt{(1-c)/n + c}\right)$ , where  $c$  represents the fraction of systematic error (assumed to be 50%) and  $n$  the number of days with valid data (Eskes et al., 2003; Miyazaki et al., 2012). Thus, the total error for the temporally averaged VCD at a given grid cell is  $\sigma_s = \sqrt{(\sigma_p^2 + \sigma_g^2)} \cdot s$ .



### 2.3. The PHLET model simulation

We construct the PHLET model on the  $0.05^\circ \times 0.05^\circ$  grid to interpret the relationship between local net source (emissions – loss), horizontal transport, and VCD of  $\text{NO}_2$  in a 2-D gridded space (Eq. (1)) in the sense of long-time average. PHLET simulates the horizontal transport of  $\text{NO}_x$  through a time averaged advection process and an “effective” diffusion process, which represents the residual from the temporally averaged advection. The model assumes a horizontally homogeneous vertical shape of  $\text{NO}_2$  concentrations, and that  $\text{NO}_2$  is concentrated near the surface (Beirle et al., 2011). The assumption is implicitly used in many previous studies for polluted areas (Liu et al., 2016; Beirle et al., 2011). The corresponding uncertainty in the modeled  $\text{NO}_2$  VCDs is set as 15% (Lin et al., 2014; Boersma et al., 2011).

Although lightning emissions, biomass burning emissions, aircraft emissions, and the vertical transport can lead to  $\text{NO}_2$  at higher altitudes over the YRD area, the amount of  $\text{NO}_2$  aloft is much smaller than  $\text{NO}_2$  near the ground due to large anthropogenic pollution emitted from the ground (Lin, 2012). We regard  $\text{NO}_2$  aloft as the regional background, and do not include it in Eq. 1 – as such, PHLET accounts for anthropogenic and soil  $\text{NO}_x$  emitted from the surface but not other types of emission sources. [For  $\text{NO}_x$  near the ground in the YRD area, the contribution of lightning, biomass burning, and aircraft emissions is negligible compared to the major anthropogenic (energy, industry, transportation, residential) sources.] To ensure the consistency between PHLET and OMI  $\text{NO}_2$  data, we assume the background value to be half of the minimum OMI  $\text{NO}_2$  VCD among all grid cells (i.e.  $0.54 \times 10^{15}$  molecules  $\text{cm}^{-2}$ ), and then subtract the background value from the gridded OMI data when comparing with PHLET simulations. The corresponding uncertainty in the modeled  $\text{NO}_2$  VCDs is set as 5%.

Equation (1) presents the governing equation in PHLET:

$$\frac{\partial C(x,y)}{\partial t} = r \cdot L(x,y) - \mathbf{V}(x,y) \cdot \nabla C(x,y) + \nabla \cdot (\mathbf{K}(x,y) \cdot \nabla C(x,y)) \quad (1)$$

$C(x,y)$  represents the tropospheric  $\text{NO}_2$  VCD (in molecules  $\text{cm}^{-2}$ ) with the regional background removed.

The value of  $C(x,y)$  after the model reaches equilibrium ( $\frac{\partial C(x,y)}{\partial t} = 0$  for every  $x$  and  $y$ ) gives the



distribution of NO<sub>2</sub> VCDs to be compared with the gridded, background value excluded OMI data. As such, we assume steady state of NO<sub>2</sub> in the PHLET model, and assign an uncertainty of 15% to simulated  $C(x, y)$  to account for the possibility that NO<sub>2</sub> may not be fully in steady state. Also, combining data from multiple years to derive an averaged NO<sub>2</sub> distribution for simulation (rather than conducting the  
5 simulations for individual years and months) leads to an additional uncertainty, which is set to be 10%.

$L(x, y)$  represents the local net source term (in molecules cm<sup>-2</sup> s<sup>-1</sup>, equivalent to  $2.63 \times 10^{-12}$  kg km<sup>-2</sup> h<sup>-1</sup>) combining the effects of emissions (anthropogenic + soil), deposition, and chemistry of NO<sub>x</sub>, and  $r$  the ratio of NO<sub>2</sub> over NO<sub>x</sub> concentration. The daytime NO<sub>x</sub> chemical system reaches equilibrium rapidly and  $r$  varies little (Beirle et al., 2011; Valin et al., 2013). We set  $r$  to be 0.76 with an uncertainty of 10%  
10 (Seinfeld et al., 2006; Beirle et al., 2011).  $L(x, y)$  can be separated into an emission term and a loss term:

$$L(x, y) = E(x, y) - \frac{C(x, y)}{r \cdot \tau(x, y)} \quad (2)$$

where  $E(x, y)$  denotes the gridded emission of NO<sub>x</sub>, and  $\tau(x, y)$  the lifetime of NO<sub>2</sub> associated with deposition and chemical loss.

$\mathbf{V}(x, y) \cdot \nabla C(x, y)$  represents the time averaged advection term.  $\mathbf{V}(x, y)$  denotes the mean wind vector  
15 (in m s<sup>-1</sup>) averaged over summer 2012–2016. To solve the advection process, we follow the Walcek scheme (Walcek, 2000); the SHASTA scheme (Schere, 1983) leads to similar results.

$\nabla \cdot (\mathbf{K}(x, y) \cdot \nabla C(x, y))$  represents the diffusion term, where  $\mathbf{K}(x, y)$  denotes the “effective” diffusion coefficient tensor (in m<sup>2</sup> s<sup>-1</sup>). The diffusion term accounts for transport by the residual winds deviating from the temporally averaged wind vector  $\mathbf{V}(x, y)$ . Appendix A shows how to determine the diffusion  
20 coefficient and solve the diffusion process.

The discrete form of PHLET is set on the  $0.05^\circ \times 0.05^\circ$  grid. To run PHLET, the NO<sub>2</sub> VCDs at the domain edges, as the lateral boundary conditions (LBCs), are set as the corresponding OMI NO<sub>2</sub> VCDs. For initial conditions, the VCD at each grid cell inside the domain boundaries is set to be zero, and the



local net source term is assigned to be a low value ( $0.02 \text{ kg km}^{-2} \text{ h}^{-1}$ , or  $7.60 \times 10^9 \text{ molecules cm}^{-2} \text{ s}^{-1}$ ). The horizontal distribution of modeled  $\text{NO}_2$  VCDs at equilibrium does not depend on the initial conditions. At equilibrium, the domain average of modeled  $L(x, y)$  reaches zero, because there are no horizontal fluxes into or out of the domain boundaries.

5 For horizontal transport, we use 3-hourly wind fields from the European Centre for Medium-range  
Weather Forecasts (ECMWF) ERA5 dataset  
(<https://confluence.ecmwf.int/display/CKB/ERA5+data+documentation>; last access: 2018/7/2). The  
resolution of raw ERA5 data is  $0.28125^\circ$  on the reduced Gaussian grid, which is regridded to  $0.05^\circ \times$   
10  $0.05^\circ$  by using the online program offered by ECMWF (see Fig. A1). We adopt the mean wind field of  
the lowest 14 vertical levels (out of 157 levels in total); these 14 levels represent the altitudes from surface  
to about 500 m (Hersbach and Dee, 2016; Beirle et al., 2011). Over the study period, the prevailing wind  
is northwesterly, and the wind speed is small over land (Fig. A1). For both zonal and meridional wind  
speeds, the uncertainty in the average wind speed is set to be 10%, which is similar to the temporal  
standard deviation of the wind speed. We assess the model errors introduced by the uncertainties in the  
15 wind field and effective diffusion coefficients by Monte Carlo simulations; the resulting relative  
uncertainty in the modeled  $\text{NO}_2$  VCDs is about 5%.

Re-mapping of PHLET simulated  $\text{NO}_2$  VCDs in accordance to satellite pixels is important. Given the size  
of OMI pixels, the OMI  $\text{NO}_2$  data smooth to some extent the actual horizontal distribution of  $\text{NO}_2$ . To  
ensure consistent spatial sampling between PHLET and OMI data, for each day we project the PHLET  
20 modelled  $\text{NO}_2$  VCD data (in the original  $0.05^\circ \times 0.05^\circ$  grid space) to the satellite pixel space to mimic  
how OMI “sees” the ground, remove the pixels with invalid OMI data, and then project the model data  
back to the  $0.05^\circ \times 0.05^\circ$  grid. The last two procedures are the same as done for OMI data. The whole  
process of grid conversion is done through the SCM approach (Appendix B). Although PHLET simulates  
summer average  $\text{NO}_2$  VCDs (rather than daily values), we repeat the grid conversion process for as many  
25 days as there are valid OMI data.



The model error  $\sigma_m$  is set to be the sum in quadrature of errors contributed by the steady state assumption (15%), the time averaging over multiple years and months (10%), the assumption of horizontally constant vertical shape of  $\text{NO}_2$  (15%), the treatment of background  $\text{NO}_2$  concentration (5%), and the error in the wind data and the calculation of effective diffusion coefficients (5%).

## 5 2.4. PHLET-A: The adjoint model of PHLET

We construct the PHLET-A adjoint model to obtain an optimized horizontal distribution of the local net source term ( $L$  in Eq. (1)) under the given OMI  $\text{NO}_2$  VCDs, wind field, and other parameters. PHLET-A accounts for the complex nonlinear effects of 2-dimensional transport and loss processes. We define a scalar cost function (Eq. (3)) to quantify the difference between OMI  $\text{NO}_2$  VCDs and PHLET simulated  
10  $\text{NO}_2$  VCDs.

$$J = (\mathbf{C}^{OMI} - \mathbf{C}^{PHLET})^T \mathbf{S}_0^{-1} (\mathbf{C}^{OMI} - \mathbf{C}^{PHLET}) \quad (3)$$

Because PHLET does not require a priori knowledge about the local net source, the cost function does not include the a priori term either. The vector  $\mathbf{C}$  denotes gridded  $\text{NO}_2$  VCDs.  $\mathbf{S}_0$  denotes the observational error covariance matrix, as derived in Appendix C.

15 Applying Lagrange identity and integrating by parts, we derive PHLET-A and its initial and lateral boundary conditions (Marchuk, 1994; Sandu et al., 2005; Martien et al., 2006; Hakami et al., 2007):

$$\frac{\partial \lambda(x, y)}{\partial t} + \nabla(\mathbf{V}(x, y) \cdot \lambda(x, y)) + \nabla \cdot (\mathbf{K}(x, y) \cdot \nabla \lambda(x, y)) = 0 \quad (4)$$

$$\lambda(x, y)|_{t=T} = \frac{\delta J}{\delta C(x, y)}|_{t=T} \quad (5)$$

$$\lambda(x, y)|_{boundary} = 0 \quad (6)$$



Here,  $T$  stands for the time when the domain-wide  $\text{NO}_2$  VCDs come to equilibrium, i.e., the start time of the adjoint simulation. By discrete adjoint sensitivity analysis, the gradient of cost function to emission is obtained:

$$\frac{\delta J}{\delta L_{i,j}} = r \cdot \Delta x \cdot \Delta y \cdot \Delta t \cdot \sum_k \lambda_{i,j,k} \quad (7)$$

5 where the indices  $i, j, k$  denote zonal, meridional, and time, respectively. The gradient is then used in an iterative optimization algorithm (Appendix C) to minimize the cost function  $J$ , i.e., to minimize the weighted difference between model simulated and OMI  $\text{NO}_2$ . The iteration stops when  $J$  is reduced from an initial value of 7937 to a stabilized value below 390 (Fig. C1).

## 2.5. Deriving emission and loss from the local net source term

10 The optimized local net source term combines the contributions of emission (anthropogenic + soil) and loss (chemical loss + deposition). We further separate emission from loss by assuming a fixed formula within our small study domain for the nonlinear relationship between lifetime and VCD of  $\text{NO}_2$ .

In the summertime daytime, the dominant sink of  $\text{NO}_x$  is reactions with the radicals to produce nitric acid and organic nitrogen species. The  $\text{NO}_x$  chemistry quickly reaches a steady state under high solar radiation and air temperature in the early afternoon (Murphy et al., 2006; Valin et al., 2013) when OMI passes over the YRD. The chemical lifetime of  $\text{NO}_x$  depends on the concentrations of  $\text{NO}_x$  and non-methane volatile organic compounds (NMVOC), radiation, temperature, and other factors. Within our small study domain, we assume all factors except  $\text{NO}_x$  concentrations to be spatially homogeneous. As such, the chemical lifetime of  $\text{NO}_x$  at steady state is a sole function of  $\text{NO}_x$  concentration (and thus  $\text{NO}_2$  VCD, given the  
15 constant  $\text{NO}_2/\text{NO}_x$  ratio). Appendix D shows in detail how to deduce the chemical lifetime of  $\text{NO}_x$  from  $\text{NO}_2$  VCD, to account for the effect of dry deposition, to separate emission and lifetime from the local net source term, and to quantify the errors involved using Monte Carlo simulations.



## 2.6. Uncertainty estimate for inverted emissions

For a particular grid cell, our inverted emission is affected by the error involved in the inversion of  $L$  (embedded in satellite data and model simulations) and the error in the separation of emission and lifetime from  $L$ . The satellite data error  $\sigma_s$  is analyzed in Sect. 2.2. The model induced error  $\sigma_m$  is analyzed in  
5 Sect. 2.3. The error of  $L$ ,  $\sigma_L$ , is connected with  $\sigma_s$  and  $\sigma_m$  through the adjoint simulation (Sect. 2.4), and is given by Hessian of the cost function  $J$  (Appendix C).

The error involved in the separation of emission and lifetime,  $\sigma_f$ , is contributed by the assumption on the  $\text{NO}_2/\text{NO}_x$  ratio  $r$  (Sect. 2.3), the simplified treatment of deposition and chemical processes of  $\text{NO}_x$  (Appendix D), and the assumed relationship between lifetime and VCD (Appendix D).  $\sigma_f$  is estimated by  
10 500 times of data fitting of  $L$  at individual grid cells (Appendix D).

Thus, the error in inverted emission,  $\sigma_e$ , is equal to the sum in quadrature of  $\sigma_L$  and  $\sigma_f$ , i.e.,  $\sigma_e = \sqrt{\sigma_L^2 + \sigma_f^2}$ . The error in the inverted lifetime is derived in a similar way.

Appendix E further presents an OSSE-like test to estimate the reliability of our emission inversion method, by examining to what extent the method can invert the emissions used in a nested GEOS-Chem simulation  
15 (0.3125° long. × 0.25° lat.) for summer 2014. Overall, the inverted emission data capture the mean value and spatial variability of the GEOS-Chem emissions, with a linear regression slope of 0.98, a correlation of 0.93, and a mean bias of 0.25 kg km<sup>-2</sup> h<sup>-1</sup> (16%). This test suggests the high reliability of our inversion method.

## 3. High-resolution spatial distributions of $\text{NO}_2$ VCDs, local net sources, and lifetimes over the YRD

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Figure 1a shows the number of days with valid OMI data in summer 2012–2016 over the YRD area on the 0.05°×0.05° grid. The number of days varies from about 14 to 113 (56 on average). There is a “band” pattern in the spatial distribution, due to the difference in the number of satellite orbits covering each grid



cell (not shown). This band pattern is not obvious in the distribution of OMI NO<sub>2</sub> VCDs (Fig. 1b), suggesting that the temporally averaged VCD values are less sensitive to the number of days (14 or more) used for temporal averaging. There are fewer valid data in severely polluted locations. The effect of sampling size on the uncertainty in OMI NO<sub>2</sub> is accounted for in our study (Sect. 2.2).

5 Figure 1b shows the gridded horizontal distribution of OMI NO<sub>2</sub> VCDs. The background value has not been removed. NO<sub>2</sub> VCDs are high over the major urban centers along the Yangtze River and the coastal line, especially Shanghai, Nanjing (Capital of Jiangsu Province), Hangzhou (Capital of Zhejiang Province), and the Ningbo-Zhoushan area (with intensive maritime shipping activities). The maximum VCD value exceeds  $14 \times 10^{15}$  molecules cm<sup>-2</sup> in north Shanghai. NO<sub>2</sub> VCDs are larger than  $1 \times 10^{15}$  molecules cm<sup>-2</sup> at all grid cells, reflecting the influence of local anthropogenic sources and/or pollution transported from nearby cities (Cui et al., 2016). NO<sub>2</sub> VCDs are lower than  $3 \times 10^{15}$  molecules cm<sup>-2</sup> along the boundaries of our study domain.

Across the grid cells, the absolute errors in OMI NO<sub>2</sub> VCDs are about  $0.58\text{--}3.4 \times 10^{15}$  molecules cm<sup>-2</sup> (Fig. 2a), and the relative errors are about 24%–54% (Fig. 2b). In general, the grid cells with larger NO<sub>2</sub> VCDs have larger absolute errors but smaller relative errors. Over the eastern sea and the southwestern corner of the domain, NO<sub>2</sub> VCDs are relatively small (Fig. 1b), thus their absolute errors are small (Fig. 2a), but their relative errors are large (Fig. 2b).

Figure 1c shows the spatial distribution of the inverted local net source  $L$  (emission – loss). The values of  $L$  are greatest ( $8.9 \text{ kg km}^{-2} \text{ h}^{-1}$ ) over the major urban areas with high NO<sub>2</sub> VCDs, and are low ( $< -3.2 \text{ kg km}^{-2} \text{ h}^{-1}$ ) in many areas with low NO<sub>2</sub> loadings. However, the values of  $L$  are the lowest ( $(-7.2)\text{--}(-3.2) \text{ kg km}^{-2} \text{ h}^{-1}$ ) at places in the urban-rural fringe zones with NO<sub>2</sub> hotspots nearby; this feature reflects that NO<sub>2</sub> is transported from the urban centers and destroyed in the fringe zones. The absolute errors of  $L$  (Fig. 2c) are highly consistent with those of the NO<sub>2</sub> VCD (Fig. 2a), with a spatial correlation of 0.95. The absolute errors of  $L$  are notable in the urban-rural fringe zones, because the deviation of  $L$  at these areas is very sensitive to errors in the assumed transport and loss process.



Figure 1d shows the inverted lifetime of  $\text{NO}_2$  on the  $0.05^\circ \times 0.05^\circ$  grid. The lifetime ranges from 1.4 to 3.6 h across the study domain. The lifetime is below 1.5 h at grid cells with  $\text{NO}_2$  VCDs of about  $2 \times 10^{15}$  molecules  $\text{cm}^{-2}$ , increasing to 2.2 h at grid cells with the lowest VCDs ( $< 2 \times 10^{15}$  molecules  $\text{cm}^{-2}$ ), and exceeding 3 h at many polluted grid cells, i.e., the urban centers. The mean lifetime over the study domain is about 2.0 h. Appendix D further shows the chemical lifetime to be 1.7–6.6 h and the deposition lifetime to be constantly at 7.8 h across all grid cells. The nonlinear dependence of lifetime on VCD is expected from our inversion method (Appendix D). The absolute uncertainty in the inverted lifetime is greater than 1.0 h at the  $\text{NO}_2$  hotspot locations, between 0.75 and 1.0 h over the eastern sea and the southwest of the study domain, and about 0.7 h at many other locations (Fig. 2d).

## 10 4. High-resolution spatial distribution of $\text{NO}_x$ emissions over the YRD

### 4.1. Spatial distribution of inverted emissions

Figure 1e shows the inverted horizontal distribution of summer 2012–2016 average  $\text{NO}_x$  emissions on the  $0.05^\circ \times 0.05^\circ$  grid. The inverted emissions include the contributions of anthropogenic and soil sources. As discussed in Sect. 4.3, soil emissions contribute little (0.9%) to the total emission over the study domain.

15 Figure 1e shows that  $\text{NO}_x$  emissions vary from 0 to  $12.0 \text{ kg km}^{-2} \text{ h}^{-1}$  across the grid cells. The highest emission value occurs in north Shanghai, close to Wusongkou where Shanghai Port is located, which has become the largest container terminal all over the world in 2010 (Fu et al., 2012). High emission values also occur places along the Yangtze River and the coastal line. Along the Yangtze River, the highest emission value occurs in Nanjing City. Along the coastal line, there is an emission hotspot in the Ningbo-  
20 Zhoushan area. The general spatial distribution of inverted  $\text{NO}_x$  emissions is consistent with that of OMI  $\text{NO}_2$  VCDs (correlation = 0.82), reflecting the short lifetime of  $\text{NO}_x$  and thus a modest effect of horizontal transport. Nonetheless, emissions are much more concentrated at a few sparse locations than  $\text{NO}_2$  VCDs are, and many locations near the emission hotspots have very low emissions but relatively large  $\text{NO}_2$  VCDs, suggesting that the effect of horizontal transport cannot be ignored at such a high resolution.



Figure 2e shows the absolute uncertainties of  $\text{NO}_x$  emissions at individual grid cells. The emission uncertainty varies from 0.1 to  $1.4 \text{ kg km}^{-2} \text{ h}^{-1}$  across all grid cells. The largest uncertainty occurs in north Shanghai, corresponding to the highest VCD (Fig. 1b) and emission (Fig. 1e) values. The spatial pattern of emission uncertainties (Fig. 2e) is closer to the pattern of  $\text{NO}_2$  VCDs (Fig. 1b, correlation = 0.91) than to the pattern of emissions (Fig. 1e, correlation = 0.75). The emission uncertainties are spatially more homogeneous than VCDs and emissions are, because the emission uncertainties can be high at locations with low VCDs and emissions. The spatial pattern of emission uncertainties is consistent with that of  $L$  uncertainties (Fig. 2c, correlation = 0.85).

The scatter plot in Fig. 2f shows the emission uncertainty as a function of emission at each grid cell. Although the emission uncertainty tends to be higher when the inverted emission value increases, the relationship is highly nonlinear, and there is large data spread. The data spread reaches its maximum value when emissions are the lowest, declines with increasing emissions, and is relatively small when emissions exceed  $3 \text{ kg km}^{-2} \text{ h}^{-1}$ . The data points in Fig. 2f are further colored to indicate the VCDs at individual grid cells. It is clear that the grid cells with low emissions but high emission uncertainties have large  $\text{NO}_2$  VCDs. These grid cells are located in the urban-rural fringe zones with significant  $\text{NO}_2$  pollution transported from nearby urban centers.

#### 4.2. Comparing our inverted emissions with nighttime light, population density, and road network

This section compares our inverted  $\text{NO}_x$  emission dataset with several spatial proxies widely used in bottom-up inventories, including nighttime light brightness ( $0.5' \times 0.5'$ , Fig. 3a), population density ( $0.1^\circ \times 0.1^\circ$ , Fig. 3b), and road network (Fig. 3c). These proxies broadly represent the intensity of human activities and are highly related to  $\text{NO}_x$  emissions (Geng et al., 2017).

Figure 3a shows the spatial distribution of nighttime light brightness in 2012. The data are taken from Version 4 DMSP-OLS Nighttime Lights Time Series (<https://www.ngdc.noaa.gov/eog/dmsp/downloadV4composites.html>; last access: 2018/08/19). The brightness is represented digitally from 0 to 63 bits. The nighttime light reflects the intensity of household



- activity, commercial activity, and resource consumption (Elvidge et al., 2013). When regridded to  $0.05^\circ \times 0.05^\circ$ , the spatial correlation between nighttime light brightness and  $\text{NO}_x$  emissions is about 0.70, i.e., the nighttime light brightness can explain 49% of the spatial variability in  $\text{NO}_x$  emissions in the YRD area.
- 5 Figure 3b shows the population density data, which are taken from the Gridded Population of the World v4 (GPWv4) (<http://sedac.ciesin.columbia.edu/data/collection/gpw-v4/sets/browse>; last access: 2018/08/19) (Center for International Earth Science Information Network - CIESIN - Columbia University, 2016). This dataset provides population density data for every five years (2000, 2005, 2010, 2015, etc.). Data in 2012, 2013 and 2014 are estimated by fitting a natural spline to the 2000, 2005, 2010, and 2015 values. Data in 2016 are estimated by fitting a natural spline to the 2005, 2010, 2015, and 2020 values. The population density varies greatly from the urban centers to the countryside. In north Shanghai, the population density exceeds  $5 \times 10^3 \text{ km}^{-2}$ . The  $\text{NO}_x$  emission hotspots match the population hotspots, and the lowest-emission locations have little population. When regridded to  $0.05^\circ \times 0.05^\circ$ , the spatial correlation between population densities and  $\text{NO}_x$  emissions is 0.52.
- 10
- 15 Figure 3c shows our  $\text{NO}_x$  emissions overlaid with the OpenStreetMap road network data (<http://download.geofabrik.de>; last access: 2018/6/27). The network includes both highways and local roads. In the southern areas (between  $29^\circ\text{N}$  and  $31^\circ\text{N}$ ), the spatial distribution of  $\text{NO}_x$  emissions largely coincides with the road network. The spatial coincidence is less obvious in the north because of the influence of non-mobile sources.  $\text{NO}_x$  emissions are notable along the three major national highways connecting Jinhua City (one of the largest hubs of light industry products in China), Hangzhou City, and Ningbo City.  $\text{NO}_x$  emissions are also identifiable along the national highway from Hangzhou City to Huangshan City. Pairs of  $\text{NO}_x$  emissions and traffic hubs are located to the west of the Taihu Lake and in the urban centers. These results suggest the capability of our inverted emission dataset in capturing the contribution of traffic sources.
- 20



### 4.3. Comparing our inverted emission dataset to the MEIC inventory

This section compares our inverted emission data to the widely used MEIC anthropogenic bottom-up inventory over summer 2012–2016 ([www.meicmodel.org](http://www.meicmodel.org); last access: 2018/7/2). The MEIC data are available at the  $0.25^\circ \times 0.25^\circ$  resolution. Because our emission data include the slight contribution of soil sources, we use the nested GEOS-Chem to calculate soil emissions (Fig. 3d), and then subtract these soil emissions from our data. Figure 3 shows the resulting “anthropogenic” portion of our inverted emissions. Summed over the study domain, the soil sources contribute 0.9% of our inverted emissions.

Figures 3e and 3f show that compared to MEIC, our high-resolution anthropogenic emission dataset provides much more detailed spatial information. Our dataset identifies the emission hotspots and their contrast with nearby low-emission areas (e.g., in the urban-rural fringe zones) better than MEIC does. The contribution of mobile sources along the road network is clearer in our dataset. Our emission data contain sources over the nearby sea (i.e., from shipping), along the coastal line, and in the southwest of the domain, which are not included in MEIC. In Hangzhou City, our dataset suggests the highest emissions to be to the south of Qiantang River (marked in purple line in Fig. 1b), whereas the MEIC inventory suggests north. The total emission in MEIC is smaller than ours by 28.3% over the entire study domain and by 10.4% over land.

Figure 4 compares emissions in several cities between our and MEIC inventory. A total of 14 cities within the domain are selected, and for each city the  $\text{NO}_x$  emissions are summed over the grid cells within the municipal administrative boundaries. The MEIC inventory is re-gridded to  $0.05^\circ \times 0.05^\circ$  for this purpose. Among the cities, emission values differ from -51.4% to +61.3% between the two datasets. In Shanghai, Suzhou and Wuxi, our dataset is lower than MEIC by 27.1%, 43.7%, and 51.4%, respectively. MEIC uses the industrial GDP as a spatial proxy to attribute provincial-level industrial emissions to individual counties and grid cells (Geng et al., 2017). This may overestimate the emissions in Suzhou and Wuxi, since much of the industrial GDP in the two cities is contributed by high-tech industries with low emissions.



Figure 4 also shows that in Zhoushan, Huai'an and Yancheng, our dataset is higher than MEIC by 61.3%, 55.5%, and 55.1%, respectively. Zhoushan (around 30°N, 122°E) has many isles and marine ports, as identifiable on the nighttime light map (Fig. 3a). The marine ports in the Ningbo-Zhoushan area contribute about 10% of the total shipping emissions in China (Endresen et al., 2003;Fu et al., 2017). Our dataset  
5 accounts for emissions from marine shipping and ports, whereas MEIC does not.

Section 4.2 shows the spatial correlation at the  $0.05^\circ \times 0.05^\circ$  resolution between our inverted  $\text{NO}_x$  emissions and the proxies to be 0.70 for nighttime light and 0.52 for population density. When regridded to  $0.25^\circ \times 0.25^\circ$ , the correlation becomes higher: 0.79 for nighttime light and 0.63 for population density. As the spatial resolution gets finer, the chance that  $\text{NO}_x$  emissions are collocated with population or  
10 nighttime light becomes smaller (Zheng et al., 2017), because of the influences of  $\text{NO}_x$ -emitting factories, power plants, and mobile sources. By comparison, the correlation between the MEIC inventory and these proxies on the  $0.25^\circ \times 0.25^\circ$  grid is 0.83 for nighttime light and 0.71 for population density, higher than for our emission dataset. This difference is in part because our dataset better accounts for the influences of land mobile and offshore shipping sources which are spatially not tied closely to nighttime light and  
15 population at this resolution.

## 5. Concluding remarks

This study presents a satellite-based  $\text{NO}_x$  emission inversion method for urban and surrounding areas at very high horizontal resolution. As a demonstration, the method is applied to the YRD area at the  $0.05^\circ \times 0.05^\circ$  resolution in summer 2012–2016, based on the POMINO  $\text{NO}_2$  product. We construct a simplified,  
20 computationally efficient 2-D lifetime-emission-transport model (PHLET) and its adjoint model (PHLET-A) to, together with other procedures, facilitate the emission inversion. The reliability of our inversion method is supported by 1) a rigorous step-by-step derivation of models, assumptions, and parameters used, 2) a comprehensive uncertainty analysis, and 3) an OSSE-like test with GEOS-Chem simulated  $\text{NO}_2$  data. Our inverted emission dataset in the YRD area on the  $0.05^\circ \times 0.05^\circ$  grid shows fine-  
25 scale spatial information that is tied to nighttime light, population density, road network, and maritime



shipping. Our dataset reveals many fine-scale spatial characteristics not well represented or not included in the widely used MEIC inventory.

Our emission inversion method is useful for understanding how human activities have altered the atmospheric environment at fine resolutions. Many crucial human activities, such as urbanization, are conducted at very fine spatial scales. How the resulting emissions affect air quality, public health, and geo-health are still poorly understood due to lack of high-resolution emission data. This problem is particularly severe in the developing countries, because of their rapid paces of urbanization and great inadequacies in emission-related information such as economic statistics and emission factors. This poses a grand challenge for emission control and environmental management. Thus, our inversion method and resulting emission data offer useful independent high-resolution information to monitor the fine-scale emission sources, to improve the bottom-up inventory, to model the urban pollution chemistry and the effect of urbanization, and to conduct spatially targeted emission control.

Our emission inversion method and models have a few important features enabling their global applications. The PHLET model offers computationally efficient simulations of the  $\text{NO}_x$  chemistry, deposition, and transport. At a low computational cost, our inversion method is able to account for the nonlinear relationship between  $\text{NO}_x$  concentration, chemical loss, deposition, and transport. With the advent of TROPOMI and other satellite sensors with unprecedented spatial resolutions, our inversion approach can be applied to these measurements for continuous inference of emissions at finer and finer resolutions. As a final point, PHLET and PHLET-A are written in the Python language, which can be readily used with low financial costs.

### **Data availability**

Observational data are obtained from individual sources (see links in the text and acknowledgments). Model results are available upon request. Model codes are available on a collaborative basis.



### Author contributions

JL conceived the research. HK, RZ and JL designed the research. HK and RZ performed the data processing, model development, and simulations. ML, HW, LC, RN and JW contributed to data processing, model simulations, and data analyses. QZ provided MEIC data. HK and JL analyzed the results and wrote the paper with input from all authors.

### Competing interests

The authors declare that they have no conflict of interest.

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### Appendix A. Solving the diffusion process

The diffusion term can be simplified as follows:

$$\nabla \cdot (\mathbf{K}(x, y) \cdot \nabla C(x, y)) = \frac{\partial}{\partial x} (K_x \cdot \frac{\partial C}{\partial x}) + \frac{\partial}{\partial y} (K_y \cdot \frac{\partial C}{\partial y}) \quad (\text{A1})$$

$K_x$  and  $K_y$  are the diffusion coefficients in the zonal and meridional directions, respectively. Given these coefficients, we solve the equation with the algorithm described in (Brasseur and Jacob, 2017).

We derive the diffusion coefficients based on a random walk assumption (Schirmacher, 2015):

$$K_{x \text{ or } y} = \frac{1}{2} \overline{V_{x \text{ or } y}^2} t_0, \quad (\text{A4})$$



$\overline{V_{x \text{ or } y}'}$  is the deviation of wind speed in the zonal or meridional direction.  $t_0$  is 3 hours, the sampling interval of ERA5 wind data. Figure A1 shows the time averaged wind vector and the distribution of  $K_x$  and  $K_y$ . The relative uncertainty in wind speed is assumed to be 10%, close to the temporal standard deviation of wind speed. The uncertainties of  $K_x$  and  $K_y$  are set to be 20%, about twice of the relative uncertainty in wind speed. The calculated  $K_x$  ranges from  $30397 \text{ m}^2\text{s}^{-2}$  over land to  $203783 \text{ m}^2\text{s}^{-2}$  over sea. The  $K_y$  ranges from  $25811 \text{ m}^2\text{s}^{-2}$  over land to  $297053 \text{ m}^2\text{s}^{-2}$  over sea. These diffusion coefficients tend to be slightly underestimated, because the variabilities of wind speed at higher frequencies (than 3-hourly) are not accounted for. This means that PHLET may underestimate the horizontal transport slightly.

## 10 Appendix B. Satellite Conversion Matrix to account for the smoothing effect of satellite pixels

The SCM is essentially a tool to preform quick conversion between grids, regular or not. In the YRD area, there are  $100 \times 100 = 10000$  grid cells on the  $0.05^\circ \times 0.05^\circ$  grid. We use the SCM ( $\mathbf{A}$  matrix: [10000, 10000]) to convert from its original grid ( $\mathbf{X}$  vector: [10000, 1]) to the final grid ( $\mathbf{Y}$  vector: [10000, 1]), i.e.,  $\mathbf{Y} = \mathbf{A}\mathbf{X}$ . The 10000 elements in one specific row of  $\mathbf{A}$  represent the weights of the 10000 elements of  $\mathbf{X}$  to an element in  $\mathbf{Y}$ . Apparently,  $\mathbf{A}$  is a sparse matrix. The following description shows how  $\mathbf{A}$  is constructed.

First, the VCDs specific to satellite pixels are reconstructed from the model grid cells. Each model grid cell (MGC) is divided into  $10 \times 10 = 100$  finer grid cells (FGCs), each having the same area. Suppose the number of MGCs fully or partially covered by a given pixel  $p$  is  $N_c$ , and the number of FGCs in a given MGC  $i$  covered by  $p$  is  $g_i^p$ , then the total number of FGCs covered by  $p$  is:

$$G^p = \sum_{i=1}^{N_c} g_i^p \quad (\text{B1})$$

Thus, the average VCD for the pixel  $p$  can be reconstructed as follows:



$$\text{VCD}^p = \sum_{i=1}^{N_c} \frac{g_i^p}{G^p} \cdot \text{VCD}_i \quad (\text{B2})$$

Equation (B2) essentially means how a satellite pixel smooths the VCD. The blue portion of Fig. B1 denotes the projection from MGC  $i$  to pixel  $p$ .

The next step represents how the oversampling approach is applied to satellite-smoothed VCD data.

- 5 Suppose the number of satellite pixels fully or partially covering a MGC  $j$  is  $N_p$ , then the total number of FGCs being part of the intersection of the  $N_p$  pixels and MGC  $j$  is:

$$G_j = \sum_{p=1}^{N_p} g_j^p \quad (\text{B3})$$

Finally, the average VCD for the MGC  $j$  converted from the  $N_p$  pixels is:

$$\text{VCD}'_j = \sum_{p=1}^{N_p} \frac{g_j^p}{G_j} \cdot \text{VCD}^p \quad (\text{B4})$$

- 10 The pink portion of Fig. B1 denotes the projection from pixel  $p$  to MGC  $j$ . Thus, the element of SCM converting from MGC  $i$  to MGC  $j$  can be derived as follows:

$$A_{j,i} = \sum_{p=1}^{N_p} \frac{g_j^p}{G_j} \cdot \frac{g_i^p}{G^p} \quad (\text{B5})$$

### Appendix C. Solving the observation error covariance matrix and the adjoint model

- The observation error covariance matrix ( $\mathbf{S}_o$ ) consists of a satellite data error covariance matrix ( $\mathbf{S}_s$ ) and  
 15 a PHLET model error covariance matrix ( $\mathbf{S}_m$ ):

$$\mathbf{S}_o = \mathbf{S}_s + \mathbf{S}_m \quad (\text{C1})$$

Both  $\mathbf{S}_s$  and  $\mathbf{S}_m$  are assumed to be diagonal, with the diagonal elements set to be  $\sigma_s^2$  and  $\sigma_m^2$ , respectively.



As shown in Eq. (7), PHLET-A represents the sensitivity of cost function ( $J$ ) to local net source ( $L$ ) (Marchuk, 1994; Sandu et al., 2005). Given a starting point of  $L$ , we can derive a search direction by the Cautious Broyden-Fletcher-Goldfarb-Shanno (CBFGS) method (Li and Fukushima, 2001; Boussez et al., 2015). Then, by practicing backtracking line search based on the Armijo–Goldstein condition (Armijo, 1966), we can evaluate an optimized  $L$ . The uncertainty of  $L$  is given by the Hessian of the cost function, which is approximated by the CBFGS method (Brasseur and Jacob, 2017):

$$S = 2 \cdot (\nabla_L^2 J)^{-1} \quad (C2)$$

#### Appendix D. Deriving $\text{NO}_2$ lifetime from VCD

We assume a steady state of radicals ( $\text{HO}_x$ ), where the production rate of  $\text{HO}_x$  is equal to the loss rate through three types of termination reactions: between the hydroxyl radical (OH) and  $\text{NO}_2$ , between NO and peroxy radicals to form organic nitrates, and between peroxy radicals (Murphy et al., 2006; Valin et al., 2011):

$$P(\text{HO}_x) = k_1 C_{\text{OH}} C_{\text{NO}_2} + \alpha k_{2\text{eff}} \frac{k_1 C_{\text{NMVOC}} C_{\text{OH}}}{k_{2\text{eff}} C_{\text{NO}}} C_{\text{NO}} + 6k_{3\text{eff}} \left( \frac{k_1 C_{\text{NMVOC}} C_{\text{OH}}}{k_{2\text{eff}} C_{\text{NO}}} \right)^2 \quad (D1)$$

Here  $P(\text{HO}_x)$  is the production rate, and the right hand side of Eq. (D1) is the loss rate.  $C_{\text{NO}_2}$  and  $C_{\text{OH}}$  denote the concentrations of  $\text{NO}_2$  and OH, respectively. Since the conversion between the peroxy radicals ( $\text{HO}_2 + \text{RO}_2$ ) and OH is in steady state, the term  $\frac{k_1 C_{\text{NMVOC}} C_{\text{OH}}}{k_{2\text{eff}} C_{\text{NO}}}$  expresses the “effective” total concentration of peroxy radicals in terms of the concentrations of NMVOC, OH and NO. Assuming  $P(\text{HO}_x)$ ,  $C_{\text{NMVOC}}$  and all reaction constants to be constant (Valin et al., 2011), and given that  $C_{\text{NO}} = C_{\text{NO}_2} \cdot \frac{1-r}{r}$ , Eq. (D1) can be simplified as Eq. (D2):

$$a C_{\text{OH}} C_{\text{NO}_2} + b C_{\text{OH}} + c \left( \frac{C_{\text{OH}}}{C_{\text{NO}_2}} \right)^2 = 1 \quad (D2)$$



Here  $a$ ,  $b$ ,  $c$  are the coefficients. Because the chemical lifetime of  $\text{NO}_2$  is determined by  $C_{\text{OH}}$  ( $\tau_c = \frac{1}{k_1 C_{\text{OH}}}$ ), we can deduce the relationship between  $C_{\text{NO}_2}$  and  $\tau_c$ :

$$\frac{a'}{\tau_c} + \frac{b'}{\tau_c \cdot C_{\text{NO}_2}} + c' \left( \frac{1}{\tau_c \cdot C_{\text{NO}_2}} \right)^2 = -1 \quad (\text{D3})$$

$\text{NO}_2$  is lost primarily through reaction with OH and secondarily through dry deposit ( $\frac{C_{\text{NO}_2}}{\tau_d}$ ), thus its lifetime ( $\tau$ ) is also determined by these two loss processes. Therefore,

$$\tau_c = \frac{1}{\frac{1}{\tau} - \frac{1}{\tau_d}} \quad (\text{D4})$$

In the areas of low emissions, the emission term can be neglected in Eq. 2, thus the local net source  $L = -\frac{C_{\text{NO}_2}}{r \cdot \tau}$ . Therefore Eq. D3 becomes Eq. D5, which connects  $L$  and  $C_{\text{NO}_2}$ .

$$a' \frac{r(L+kC_{\text{NO}_2})}{C_{\text{NO}_2}} + b' \frac{r(L+kC_{\text{NO}_2})}{C_{\text{NO}_2}^2} + c' \left( \frac{r(L+kC_{\text{NO}_2})}{C_{\text{NO}_2}^3} \right)^2 = 1 \quad (\text{D5})$$

where  $k = \frac{1}{\tau_d}$ . We determine the coefficients  $a'$ ,  $b'$ ,  $c'$ , and  $k$  in Eq. D5 by conducting nonlinear fitting of OMI  $\text{NO}_2$  VCD data and  $L$  values in the low emission areas (see below). This procedure establishes the nonlinear relationship between  $\tau$  and VCD, which is then applied to the entire study domain.

The low-emission areas have small values of VCD and large negative values of  $L$ . Figure D1a shows a scatter plot for the inverted local net source  $L$  and VCD at each individual grid cell of the study domain. The data scatter reflects the combined effect of emission, loss, and horizontal transport. We then fit the quantiles of  $L$  where the VCD is relatively low ( $< 5 \times 10^{15}$  molecules  $\text{cm}^{-2}$ ) into Eq. 6 through a nonlinear quantile fitter based on Tensor flow. Using the quantile fitting also means that the low-emission grid cells do not need to be explicitly identified prior to the fitting. The quantile fitting gives  $L$  as a function of VCD (when emissions are neglected), through which the relationship between lifetime and VCD is derived. We



conduct the fitting by 500 times, each by linearly changing the assumed percentile threshold of  $L$  from 0.01% to 10%, to determine the fitted median value (red line in Fig. D1a) and uncertainty (gray shaded areas, 95% CI). The uncertainty is caused by the assumption on the  $\text{NO}_2/\text{NO}_x$  ratio  $r$ , the simplification of the relationship between lifetime and VCD, and possible misjudgment of low-emission areas.

- 5 The orange line in Fig. D1b presents the relationship between  $\text{NO}_2$  VCD and chemical lifetime ( $\tau_c$ ) derived based on the mean value of the fitting. The value of  $\tau_c$  varies from 1.7 to 6.6 h with an average of 2.8 h. The lifetime declines rapidly with increasing VCD from 0 to  $2 \times 10^{15}$  molecules  $\text{cm}^{-2}$ , and then grows gradually with increasing VCD. This result is consistent with Valin et al. (2011). By comparison, the value of  $\tau_d$  is 7.8 h and is spatially homogeneous under the assumption here. The total lifetime ( $\tau$ )  
10 varies from 1.4 to 3.6 h (Fig. D1b, blue line) across the study domain.

### Appendix E. Testing our emission inversion method using GEOS-Chem simulated $\text{NO}_2$ data

We apply our emission inversion method to the  $\text{NO}_2$  VCD data simulated by the nested GEOS-Chem CTM. Specifically, we use GEOS-Chem v9-02 (Liu et al., 2018a; Ni et al., 2018; Yan et al., 2016) to simulate the  $\text{NO}_2$  VCDs in the early afternoon (around the overpass time of OMI) in summer 2014 on the  
15  $0.3125^\circ \times 0.25^\circ$  grid. The simulated  $\text{NO}_2$  data are shown in Fig. E1a. Next, we convert the GEOS-Chem  $\text{NO}_2$  VCDs into the  $0.05^\circ \times 0.05^\circ$  grid, and parameterize PHLET with the wind field adopted by GEOS-Chem, following the procedures in Sect. 2.3. Then we use PHLET, PHLET-A, and the lifetime-emission separation method to estimate the  $\text{NO}_x$  emissions. Finally, we compare the inverted emissions (re-mapped to the  $0.25^\circ \times 0.3125^\circ$  grid) to those used in GEOS-Chem.

- 20 Figure E1c and E1d shows the horizontal distributions of our inverted “anthropogenic” emissions and emission uncertainties, respectively. The contribution of soil emissions (as simulated by GEOS-Chem) is subtracted from the inverted dataset. Figure E1e shows the differences between the inverted anthropogenic emissions and the GEOS-Chem anthropogenic emissions. The emission difference at each grid cell varies from  $-4.5$  to  $5.8 \text{ kg km}^{-2} \text{ h}^{-1}$ , which is attributed to the limitation of our inversion method.



The domain average difference is  $0.25 \text{ kg km}^{-2} \text{ h}^{-1}$ , or 16% (with respect to GEOS-Chem emission value). The scatter plot in Fig. E1f suggests excellent consistency between the inverted and the GEOS-Chem emissions, with a linear regression slope of 0.98 and correlation of 0.93. The inverted emissions tend to be overestimated in the low-emission areas, but the differences are within the uncertainties of the inverted  
5 emissions (shaded area).

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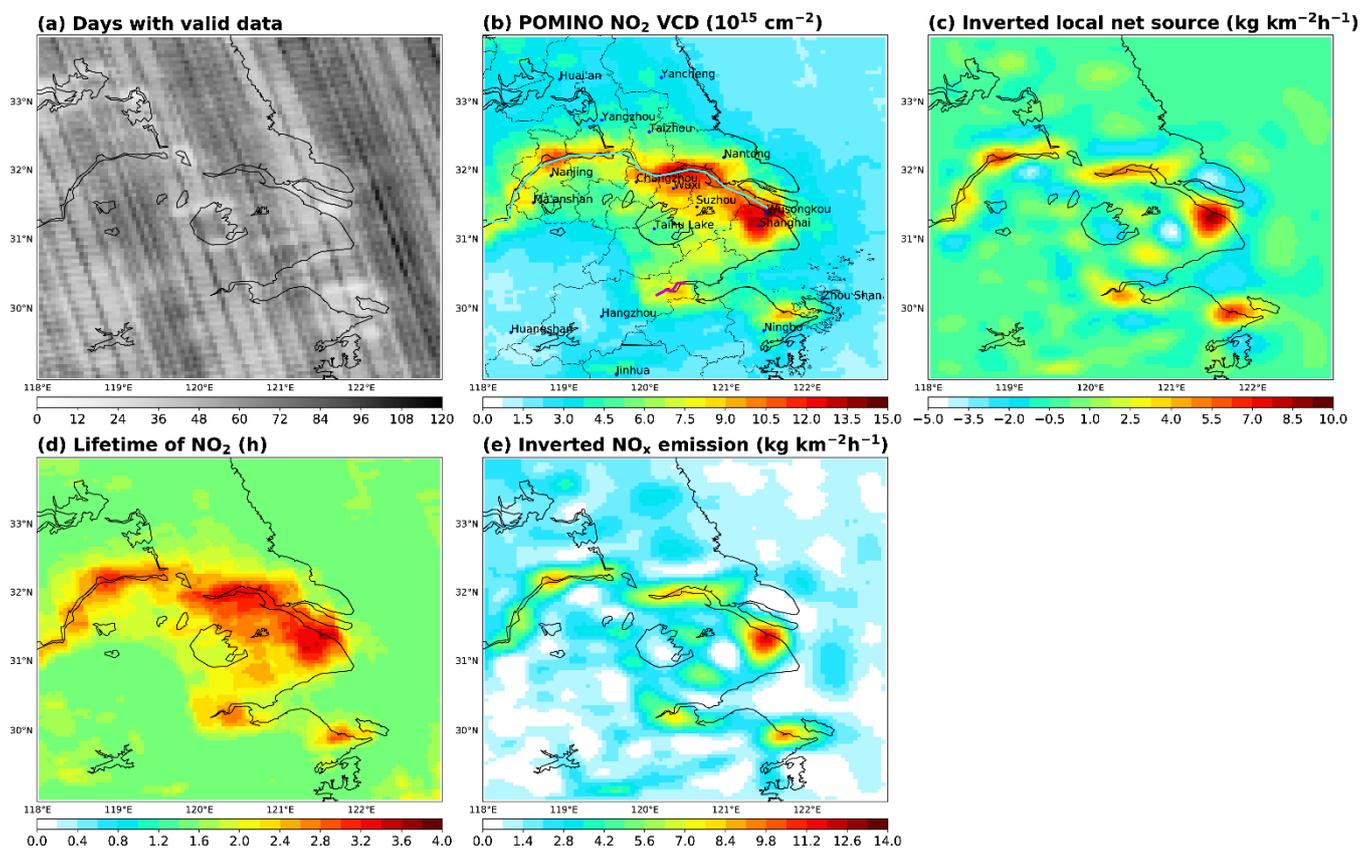
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5 Figure 1. (a) Number of days with valid data in each grid cell over summer months of 2012–2016. (b) POMINO NO<sub>2</sub> VCDs averaged over summer 2012–2016. Cities and locations mentioned in this paper are denoted. The Yangtze River is marked as a blue line, and the Qiantang River (passing Hangzhou) a purple line. (c) Inverted local net source. (d) Inverted NO<sub>x</sub> lifetime due to both chemical loss and deposition. (e) Inverted NO<sub>x</sub> emissions from anthropogenic and soil sources.

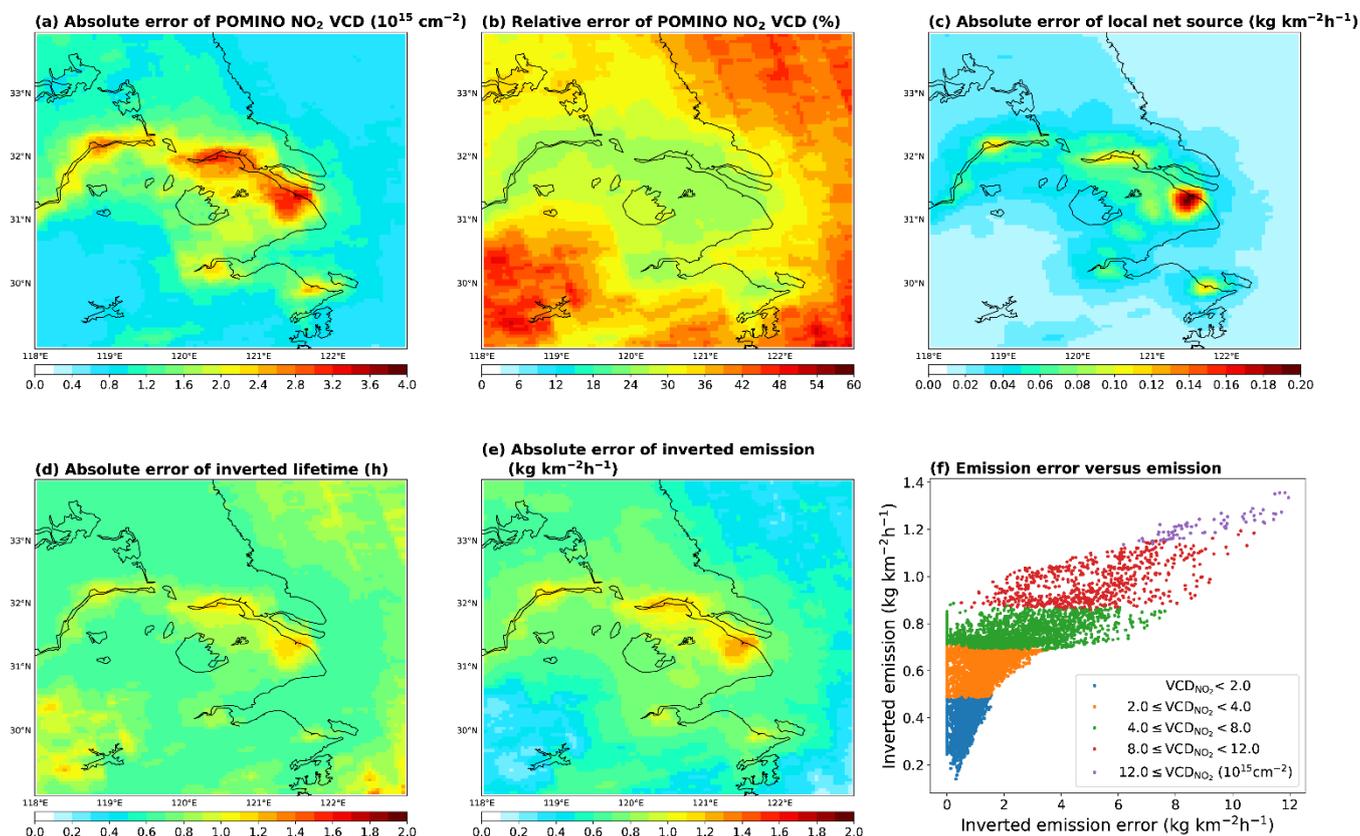


Figure 2. (a) Absolute error ( $1\sigma$ ) of POMINO NO<sub>2</sub> VCD at each grid cell at  $0.05^\circ \times 0.05^\circ$  resolution. (b) Relative error ( $1\sigma$ ) of POMINO NO<sub>2</sub> VCD. (c) Absolute error ( $1\sigma$ ) of the inverted local net source. (d) Absolute error ( $1\sigma$ ) of the inverted NO<sub>x</sub> lifetime due to chemical loss and deposition. (e) Absolute error ( $1\sigma$ ) of inverted NO<sub>x</sub> emission. (f) Absolute error ( $1\sigma$ ) of inverted NO<sub>x</sub> emission as a function of inverted NO<sub>x</sub> emission at each grid cell. Data points are coloured according to the magnitudes of POMINO NO<sub>2</sub> VCDs.

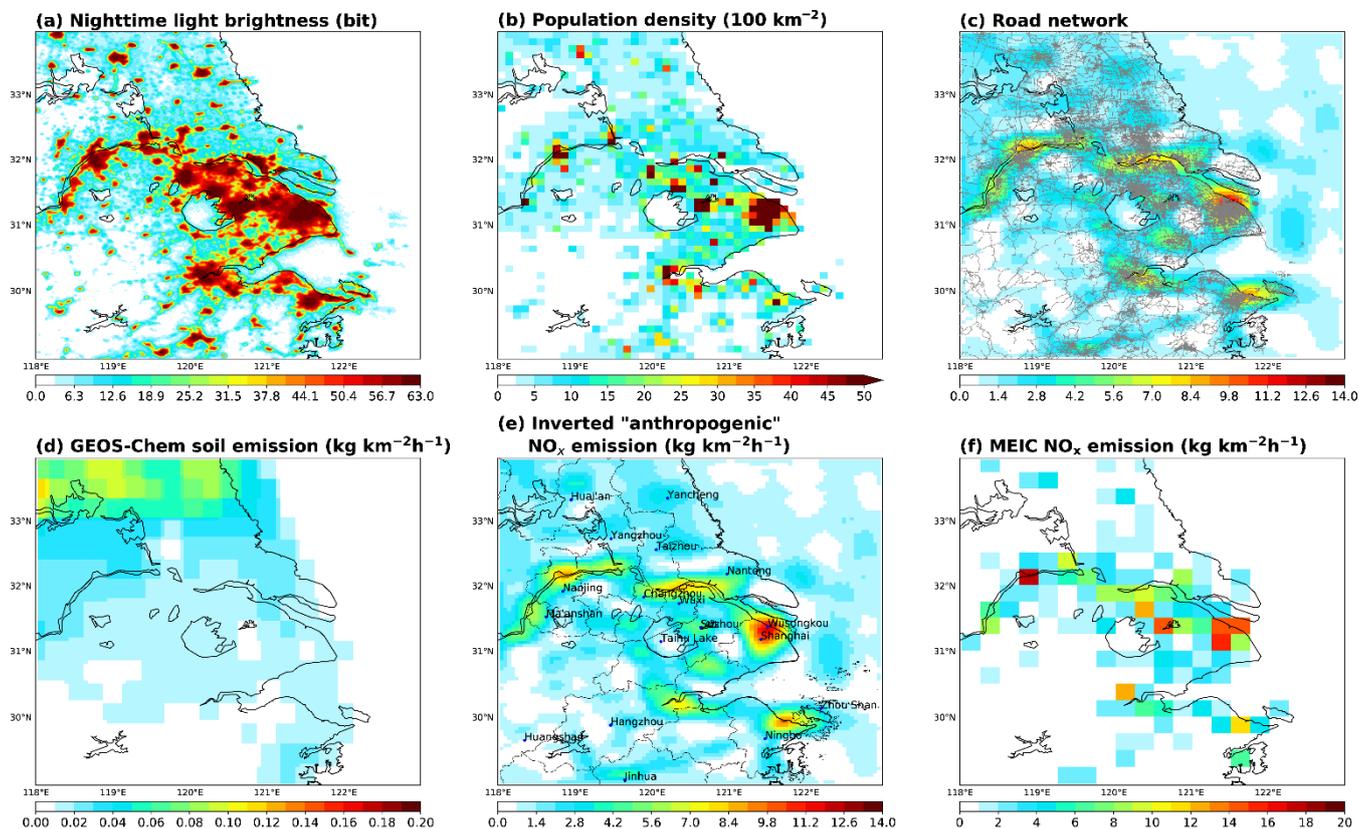


Figure 3. (a) Nighttime light brightness on a  $0.5' \times 0.5'$  grid in 2012. (b) Population density averaged over 2012–2016 on a  $0.1^\circ \times 0.1^\circ$  grid. (c) Road network (grey lines) superimposed upon the inverted  $\text{NO}_x$  emissions. (d) Soil  $\text{NO}_x$  emissions calculated by a nested GEOS-Chem simulation ( $0.25^\circ \times 0.3125^\circ$ ) and regraded to the  $0.05^\circ \times 0.05^\circ$  grid. (e) Inverted “anthropogenic”  $\text{NO}_x$  emissions on a  $0.05^\circ \times 0.05^\circ$  grid. City names and boundaries are given. (f) MEIC  $\text{NO}_x$  emissions on a  $0.25^\circ \times 0.25^\circ$  grid.

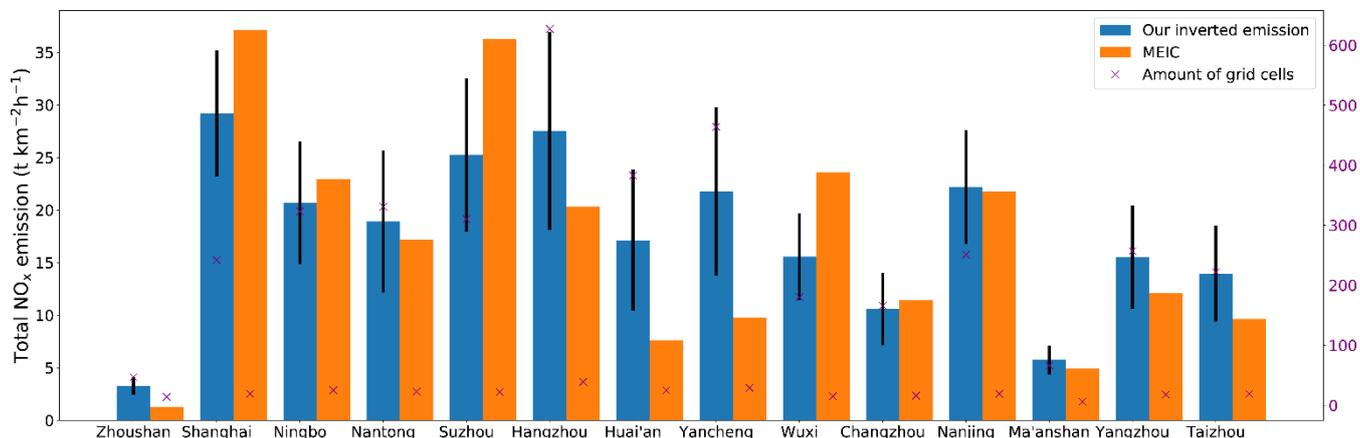


Figure 4. Total anthropogenic NO<sub>x</sub> emission in each city for summer 2012–2016 inverted here versus from the MEIC inventory. Soil NO<sub>x</sub> emissions calculated by nested GEOS-Chem have been subtracted from our inverted emission data. Black vertical lines denote the uncertainty (1σ). Red points denote the numbers of grid cells covered by each city at different resolutions (0.05° × 0.05° in our inverted dataset and 0.25° × 0.25° in MEIC).

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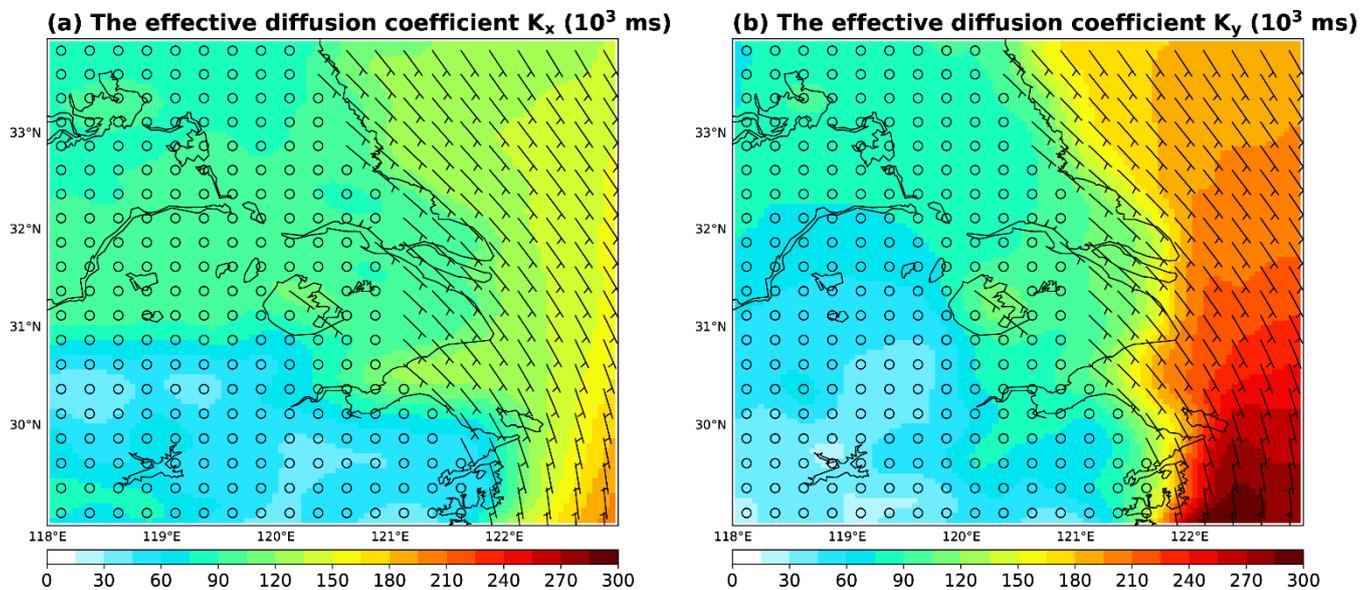


Figure A1. The effective diffusion coefficients for summer 2012–2016 on a  $0.05^\circ \times 0.05^\circ$  grid. Overlaid is the temporal mean wind vector, which is plotted for every  $5 \times 5 = 25$  grid cells to enhance the readability.

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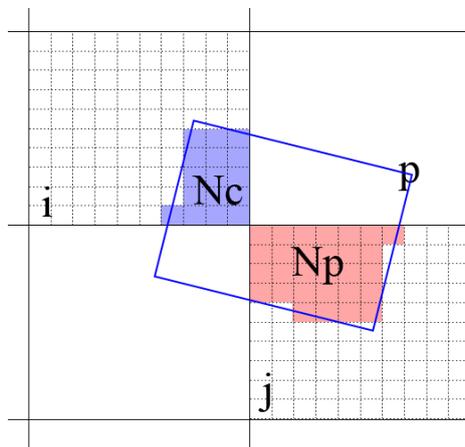


Figure B1. Illustration of how the original PHLET model grid cell  $i$  is projected to the satellite pixel  $p$  and then to the final grid cell  $j$  through the SCM approach. The size of the satellite pixel is scaled down to be comparable with the size of a model grid cell, for illustration purpose.

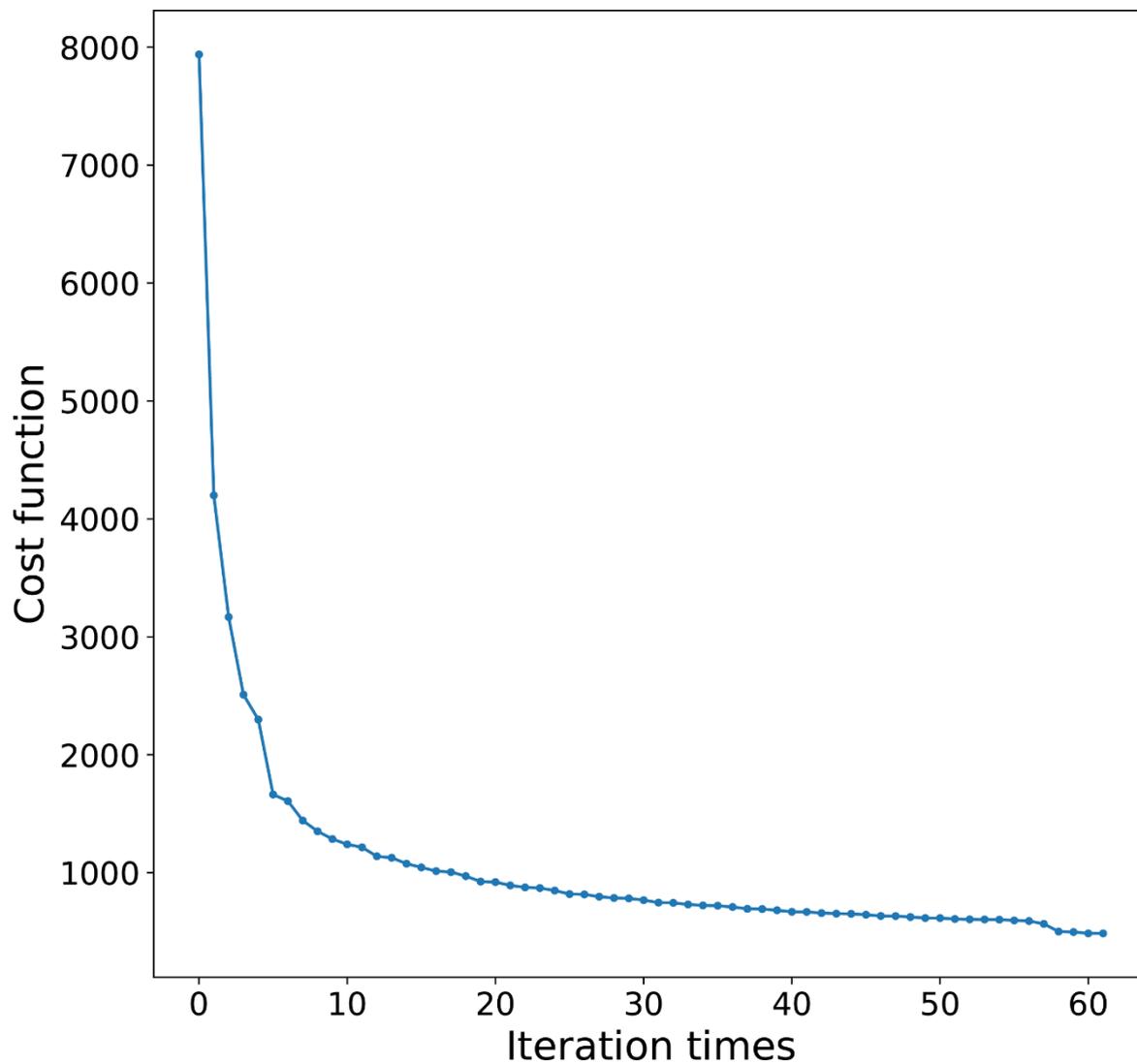
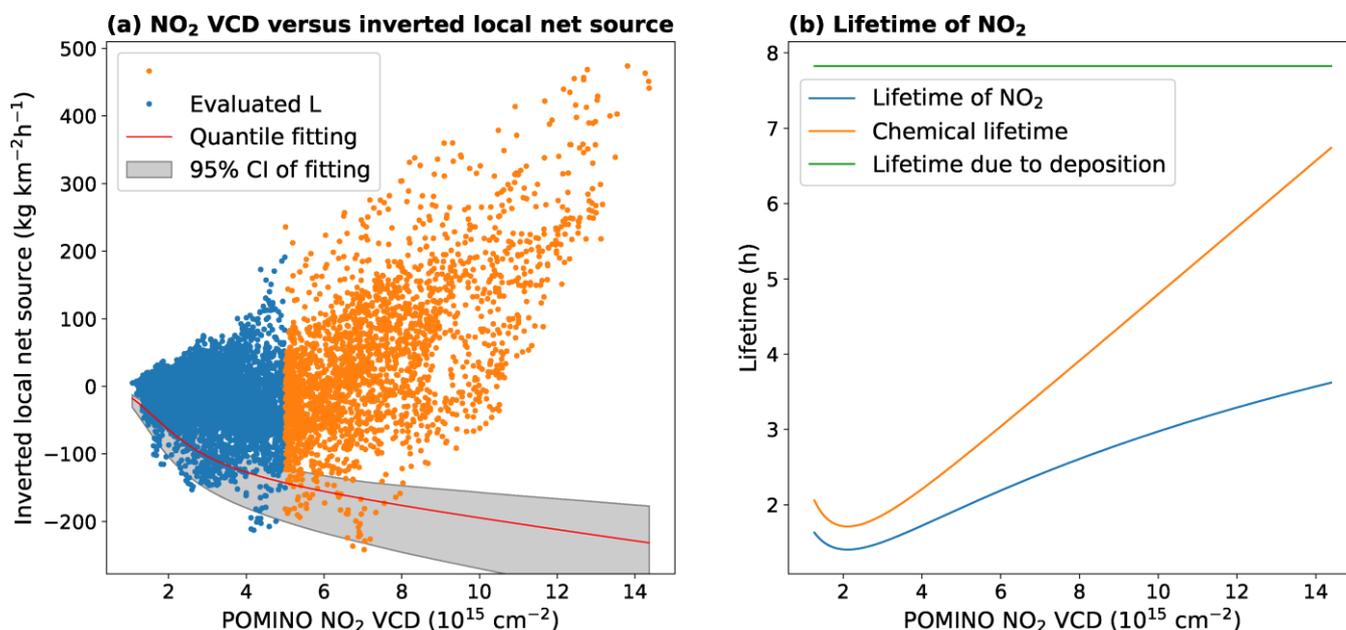


Figure C1. Variation of the cost function  $J$  with iteration times.



5 Figure D1. (a) Scatter plot for POMINO NO<sub>2</sub> VCDs (x-axis) and inverted local net sources (y-axis) across individual grid cells. Grid cells with NO<sub>2</sub> VCDs below (above)  $5 \times 10^{15}$  molecules cm<sup>-2</sup> are coloured in blue (orange). The red line and shading denote the median and uncertainty (95% CI) of the quantile fitting, respectively, to estimate the nonlinear relationship between NO<sub>2</sub> VCD and lifetime, based on data in the low-emission areas. (b) The derived relationship between NO<sub>2</sub> VCD and lifetime across the range of NO<sub>2</sub> VCDs in the YRD area.

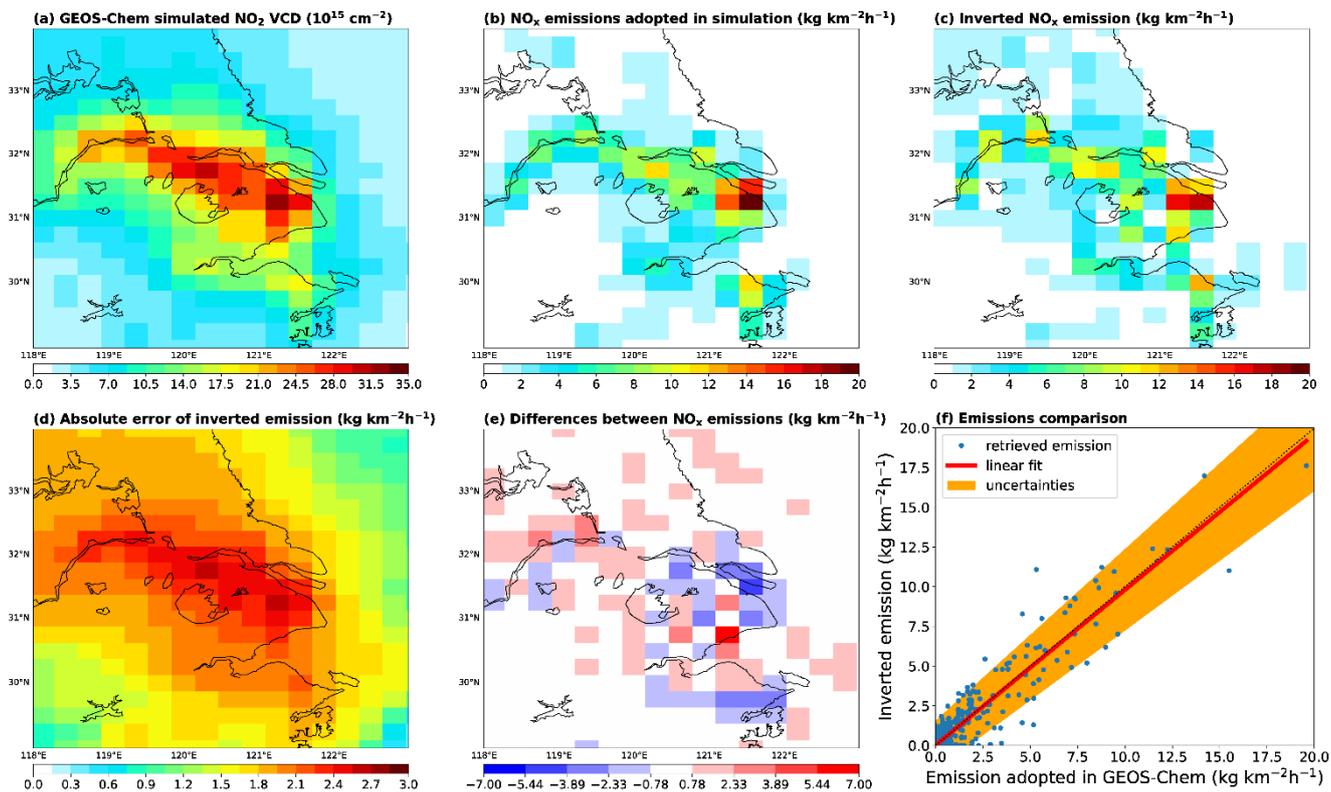


Figure E1. (a) GEOS-Chem simulated  $\text{NO}_2$  VCDs at the  $0.3125^\circ \times 0.25^\circ$  resolution for summer 2014. (b) Anthropogenic  $\text{NO}_x$  emissions used in GEOS-Chem. (c) Inverted anthropogenic emissions based on GEOS-Chem simulated  $\text{NO}_2$  VCDs. (d) Absolute errors ( $1\sigma$ ) of inverted emission data. (e) Differences between the inverted emissions and GEOS-Chem emissions (inverted minus GEOS-Chem). (f) Scatter plot for the inverted emissions (y-axis) and GEOS-Chem emissions (x-axis). The red line represents least square linear fitting. The shading represents the fitting by accounting for errors in the inverted emission data, i.e., inverted emissions +  $1\sigma$  for the upper bound, and inverted emissions -  $1\sigma$  for the lower bound. The black dotted line denotes the 1:1 line.

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