

6 April 2018

Response to Dr George Kiladis (Reviewer 1) comments on

“Multivariate analysis of Kelvin wave seasonal variability in ECMWF L91 analyses”

by Marten Blaauw and Nedjeljka Žagar

Dear Dr Kiladis,

Thank you very much for your detailed and constructive comments on the paper.

We have taken them into account in the revised paper.

We hope that the revised paper better highlights analysis possibilities offered by the MODES package i.e. by the multivariate analysis of the Kelvin wave and other equatorial waves on the sphere.

Enclosed please find our responses to your comments using the same organisation as in the review. Your comments are coloured blue whereas our responses are in black.

Yours sincerely,

Marten Blaauw and Nedjeljka Žagar

GENERAL COMMENT:

This is a fine paper on Kelvin activity that utilizes the normal mode function decomposition method pioneered by Kasahara and Puri and further refined by Zagar and others. The paper essentially represents a “proof of concept” of the technique as applied to Kelvin waves, although a lot of interesting information is included. The paper succeeds in demonstrating the utility of NMF decomposition and should provide a good starting point for those interesting in pursuing this approach, especially given the fact that software has been conveniently set up for others to apply as described in Zagar et al. 2015.

SPECIFIC COMMENTS:

The paper appears to be in good shape overall, although there are some lingering questions in this reviewer’s mind about interpretation, as discussed below. This mainly has to do with lumping all of the vertical modes together, which does not necessarily seem physical to me for all the cases considered. Perhaps not for this study, but it would be very instructive and add a lot of value to come up with some associated relationships between the subseasonal variability in Kelvin energy discussed here and some indices of tropical convection. The authors have made an initial attempt of this for the seasonal cycle and interannual timescale and their interpretation seems reasonable there. As far as higher frequencies go, for instance, cross spectra between the timeseries shown in Fig. 5 and geographically distributed OLR or brightness temperature could be very revealing. Ultimately, this could also be done for other modes isolated by this technique too. Figure captions could be improved overall, especially at the locations noted below. Also the text is not as clear as it could be in places.

Response: Thank you very much for the comments and suggestions. Indeed, the first goal of the paper is to introduce a novel methodology to analyze linear Kelvin waves on the sphere. As shown by Boyd and Zhou (J. Atmos. Sci., 2008), the degree of the Kelvin wave equatorial confinement on the sphere is controlled not only by the equivalent depth (i.e. by the equatorial Rossby radius of deformation) as on the equatorial beta plane but also by the zonal wavenumber. Therefore, even barotropic Kelvin waves with equivalent depth around 10 km are on the sphere trapped to the equator. This is a strong reason to use the spherical Kelvin wave solution for the projection.

We demonstrate the method by examples and diagnostics of seasonal variability that leads to results that are in agreement with previous studies, but also provide new understanding. As the first paper using this method for the Kelvin wave analysis, it takes space to present how the modal decomposition works and what kind of outputs it provides. As you pointed out, there are numerous research questions where this method may add insight and complement existing diagnostics. We find it hard to expand the paper beyond what has been already included. One of the topics left for future work is the suggested cross spectra.

Technical corrections

32: do you mean “modulate the TTL”?

Response: Yes. Corrected.

49: nomenclature here is slightly confusing: hkw has not been defined. If you are indeed following Holton then this is a perturbation term, otherwise it might be mistaken for the equivalent depth.

Response: The paragraph has been reformulated. We clarify that h_{kw} is the geopotential height perturbation associated with the Kelvin wave.

58: this statement is misleading, actually the tropical “cloud activity” really refers to the mean cloudiness (Tindall et al. were citing Zhang 1993) which is a maximum in January and minimum in July near the equator.

Response: The sentence has been changed as follows:

Such analysis was carried out by \cite{Tindall2006b} for the lower stratosphere for the ERA-15 data in 1981-93 period. Their results suggested that KWs contributes approximately 1 K² of the temperature variance on the equator with peak activity occurring during solstice seasons at 100 hPa, during December-February at 70 hPa and at 50 hPa it occurs during the easterly to westerly quasi-biennial oscillation (QBO) phase transition.

79: the horizontal and temporal resolution from line 106 should also be included here.

Response: Changed as suggested.

93: not sure what “denotedm” means here, should this be in parentheses (denoted m)?

Response: We are sorry for the typo. It has been corrected.

126: I am confused by one aspect of this procedure: As nicely discussed in detail by Zagar et al. (2015) and references therein, each vertical mode is characterized by an equivalent depth and associated horizontal structure function. Here it appears that all of the vertical modes are summed. For the sake of discussion, suppose we have a stratospheric “free” Kelvin mode which is present at the same time as an independent “convectively coupled” Kelvin mode that has maximum amplitude in the troposphere. These could be either collocated in lat-lon space or present at the same time in different regions of the globe. I think it would be profitable to make clear that it would still be possible to separate these modes by this procedure if one had enough additional information on the associated equivalent depths of each mode, which could be much different from each other. Stratospheric Kelvin waves at 50hPa follow dispersion related to a 120 m equivalent, whereas this is more like 25 m for convectively coupled waves. Acknowledging this fact seems appropriate, along with perhaps some words on how it could be dealt with in practice. I wonder, for instance, if investigating time series of KW energy for individual vertical modes could be done in a systematic way, using an extension of the approach in Zagar and Franzke (2015)? I think it would add considerable value to add a short discussion on these points.

Response: We deliberately use all vertical modes summed up their sum provides the total Kelvin wave signal in physical space. We do use a smaller number of vertical

modes ($M=60$) then the number of levels with data (91) but the decomposition provides the complete information about the waves in the studied layer of upper troposphere and above. Because the majority of the results concerns the total KW signal in physical space we do not make specific references to equivalent depths in the discussion.

In the revised paper, we add some more discussion about the role of equivalent depth in the construction process of the projection. It is not straightforward to discuss results on any level in terms of equivalent depths as for this we would need information on the amount of the Kelvin wave signal projecting to various equivalent depths. This can be obtained by filtering to physical space each vertical mode separately that increases the computational demand by factor m . In this study we limited the discussion to the basic concept of the method and seasonal features of the complete Kelvin wave signal.

It would be possible to split the Kelvin wave filtering in terms of vertical modes and discuss how (if) the KW signal in terms of m is grouped in various ranges of m (as indicated for MJO-related variance in Žagar and Franzke (GRL, 2015)). Such diagnosis is less trivial in the case with the high model lid such as here (1 Pa). The top model levels in this period also had some artificial damping and wave reflections. One way to solve this would be to limit the NMF projection to the troposphere only or the troposphere+lower stratosphere as for example done by Žagar et al (2017, JAS) using the ERA Interim data. The ongoing work on the KW properties in reanalysis datasets should provide further insight which we hope to report soon.

137: As in the previous comment, you are including the projection onto the vertical mode that corresponds to, say, the 10 km equivalent depth, which I would assume be more representative of an external Kelvin mode. Perhaps one way to look at this is to assume that there would be a “spectrum” of vertical modes for each situation depending on how much the data projects onto each individual mode. I think it would be worth elaborating on this point here, especially for those who may be less familiar with the idea that you are discretizing the vertical and associated horizontal structures for a reason, but that in reality a given atmospheric disturbance will be composed of a potentially different combination of these from case to case.

Response: The revised paper includes some more discussion of the role of vertical decomposition i.e. the equivalent depth. We do not filter any vertical mode separately as it would broaden presentation beyond the scope of this paper. Earlier paper by Žagar et al (Mon. Wea. Rev., 2009b) showed that presentation in terms of vertical modes in time can be very useful to represent the vertical Kelvin wave propagation. It is another topic left for future studies.

Our preliminary results on how the KW energy projects indeed among a “spectrum” of vertical modes, divides the vertical modes into roughly two groups: the vertical modes with equivalent depths ranging from 10 to 0.1 km that represent a part of the signal characterized by a strong (semi)annual periodicity. The second group contains signal that project to waves with equivalent depths ranging from 100 to 10 m and are observed throughout the year. The physical signature of these waves, decomposed based on their numerically discretized vertical structure functions, is not well understood yet in relation to the free stratospheric and the convectively coupled KWs that you mentioned in the comment. As for the previous comment, a dataset with a lower lid such as reanalysis data would make the interpretation task easier.

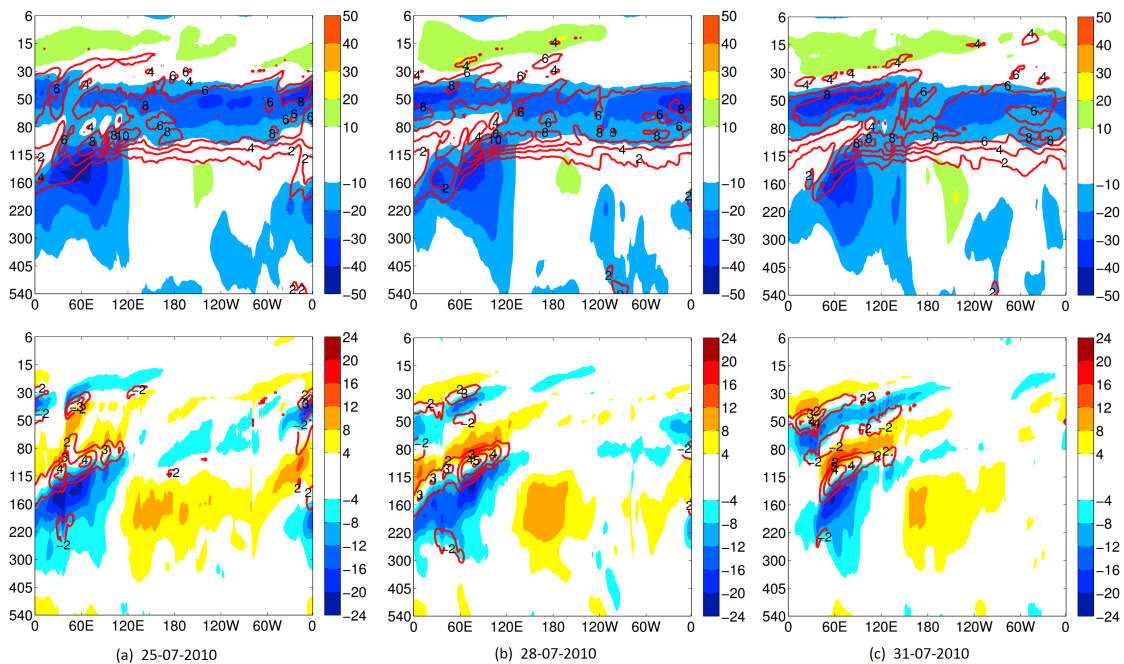
138: probably should describe the figure in more detail first, such as the tilted structures of what fields are shown, etc., before launching into the implications.

Response: We changed section 2.2 to provide more clarity on the Kelvin wave examples. In Fig. 2 different July days in 2010 have been chosen (25, 28, 31 July) with a shorter time interval of three days in order to visualize the stratospheric KW propagation more clearly. The chronological order of explanation has changed in section 2.2 such that Figures 1 and 2 are described in more detail first with respect to the free stratospheric waves as well as quasi-stationary tropopause structures, followed by the implications.

145: “strong KW activity was present” I guess you are referring to the case discussed in Fig. 2? Are you saying that the entire pattern shown represents a free Kelvin mode? This is where some information on the associated convective activity might be very useful.

Response: Yes. In Fig. 2 we refer in particular to 28 and 31 July when the wave package is located in the Eastern Hemisphere. It is hard to argue that the whole stratospheric pattern represents a free Kelvin mode. We rewritten the discussion. There are clear signs of eastward and downward KW propagation above 80 hPa. It is hard to see visually where coupled Kelvin modes in the TTL end and where the free Kelvin modes start to dominate.

To clarify the relationship between the observed Kelvin wave activity in relation to the background wind and stratification conditions, we illustrate below the background fields as well:



The bottom three panels are as in revised Fig. 2 in the paper. The top three panels illustrate from the ECMWF zonal wind (blue-to-red shades, for $|U| > 10 \text{ ms}^{-1}$) and the static stability (red contours, for $N^2 > 2 \times 10^{-4} \text{ s}^{-2}$) fields. The easterly winds in the TTL (160 hPa) create a “window” through which the Kelvin wave energy can “escape” into the stratosphere. A double-folding structure in the static stability fields (up to $8 \times 10^{-4} \text{ s}^{-2}$) coincides with large amplitude Kelvin wave temperature perturbations (up to 4 K).

154: Another very useful bit of information would relate the activity of KWs (such as measured by the energy spectrum) to the QBO, perhaps in a future study.

Response: We agree and the Kelvin wave-QBO relation is one of the couplings we hope to address using a longer time series of data from reanalyses.

161: “climatological zonal structure” at first, I thought this was only for the period of Fig. 2 and the figure caption does not help.

Response: The caption has been re-written. Figure 3 shows the six-year average of full zonal wind in the analyses and static stability.

191: “resonates” => “fluctuates” might be a better choice of words.

Response: Changed as suggested.

244: I’m unsure what the tidal effect would look like, but could the tide itself be projecting onto the Kelvin structure in some way? It doesn’t seem that a Kelvin wave structure should be impacted by the tide, especially if you consider that these are both orthogonal “normal modes”. This may deserve a few more words and could emphasize one potential drawback of the approach.

Response: Rewritten as “The spectrum contains a peak at 1-day period associated with the diurnal tide partially projecting on the Kelvin waves.” without further elaboration which is beyond the scope of present study. An unpublished master thesis used MODES to analyze what large-scale wave the tides in the same dataset project on.

259: Probably should use a bit more care when discussing the impact of the QBO since this is highly dependent on the level you are referring to. One way to put it might be to point out that vertical penetration of Kelvin wave energy into the stratosphere depends on the state of the QBO in the lower layers of the stratosphere.

Response: Corrected as: “Moreover, KW activity is enhanced whenever easterly QBO winds are present down into the lower stratosphere \citep{Baldwin2001, Alexander2010} or during El Niño \citep{Yang2013}.”

269: It turns out the the QBO was easterly at 50 hPa in July 2007, but only just beginning the easterly phase at that level.

Response: Thank you. We have added this comment.

291: What is the advantage of using “absolute amplitude” over say, variances? This should be discussed and justified.

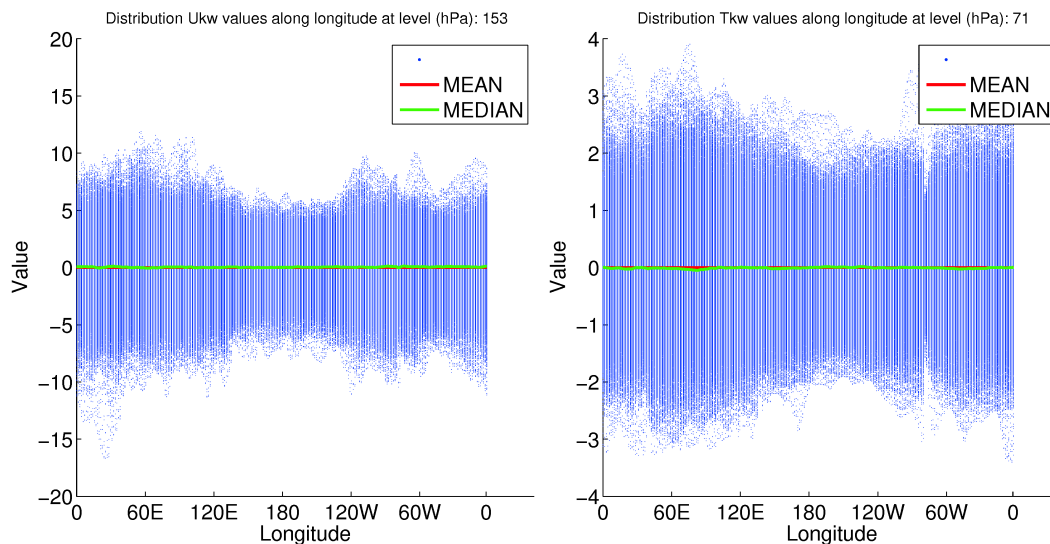
Response: The explanation has been added as the following footnote in the revised manuscript: “Most previous studies define KW activity as square amplitude rather than absolute amplitude. In our high resolution dataset we observe highly localized patterns of the KW activity in the Eastern hemisphere due to ongoing wave amplification. By using absolute amplitudes we better visualize the longitudinal structure of the KW activity in comparison to its local maxima.”

287: I wouldn't insist on it, but it may also be of interest to examine whether there is significant skewness in the distributions of the raw filtered data on the subseasonal timescales, and whether they are approximately normal. In other words, does it matter what the phase of the Kelvin component is at a given level, or are negative perturbations approximately the opposite of positive ones?

Response: To answer your question, we checked the distribution of raw filtered data with applied low-pass filter over periods of 3-20 days for the KW zonal wind and temperature components at several levels. Enclosed are examples for (left panel) KW zonal wind at ~153 hPa (in ms^{-1}) and (right panel) KW temperature at ~71 hPa (in K). All scatter point values over 6-year period are plotted as a function of longitude. The 6-year mean (red line) and median (green line) are computed for each longitude.

It follows that the distribution is well-described as normal on subseasonal timescales. Mean and median values are approximately zero.

The same applies for filtered data for periods 20-90 days and for other levels.



292: caption and discussion of Fig. 7 is confusing. When describing 7a the caption says “mean” when you really mean “(semi)annual” as discussed above. Isn't 7c for the high frequency? If so the caption should say so.

Response: Figure caption has been rewritten. The word “mean” has been removed. All three panels represented 6-year mean Kelvin wave zonal wind and temperature fields that are filtered over three different specific ranges of periods.

297: “quadrupole” is more commonly used, but perhaps not in Europe.

Response: Changed as suggested.

310: There is decent agreement between the results here and those of Flannaghan and Fueglistaler as to where the Kelvin activity is maximized and I think this should be discussed at this point as well as below (e.g. Fig. 6 of Flannaghan and Fueglistaler 2013).

Response: This is discussed in details in section 4.4 where seasonal decomposition similar to Figure 6 of Flannaghan and Fueglistaler (2013) is presented.

333: This is a very interesting analysis and the link between the low frequency Kelvin component to the “Gill-type response” is very insightful. However, the pure Gill response is only Kelvin-like to the east and includes Rossby gyres to the west of the heating, so at least part of the easterlies would not necessarily be due to a projection on Kelvin waves. This should at least be mentioned, if not discussed in more detail.

Response: The Gill-type response results from the steady-state, long-wave approximation without background wind that leads to an idealized view with Kelvin waves represented only by westerlies east of the Maritime continent. Real data is more complex and we have been more careful in the revised paper in using the “Gill-type KW” term following Salby and Garcia (1987). We emphasize that we discuss the low-frequency Kelvin wave response to large-scale tropical heating that has strong easterly zonal wind component as well.

356: This is a clever way of getting at the impact of the quasi-stationary Kelvin wave forcing.

Response: Thank you

384: It would indeed be interesting to see what the relationship between intraseasonal Kelvin activity isolated here might be to the convective activity on the same timescale.

Response: We recognize this as an interesting question but beyond the scope of the present paper.

416: It seems that the right panels refer to a specific longitude only but this is never identified in the text or caption.

Response: Figure caption has been re-written and discussion improved. The amplitude of the KW zonal wind wave are maximal amplitudes occurring anywhere along the equator averaged over the 6-year period for each calendar month.

431: Now it seems that these numbers are somehow zonal averages? Rather confusing, and once again the figure caption does not help either.

Response: Corrected. These numbers are maximal values found along the equator.

437: I guess this is not shown? That should be noted.

Response: Added as suggested.

Multivariate analysis of Kelvin wave seasonal variability in ECMWF L91 analyses

Marten Blaauw¹ and Nedjeljka Žagar¹

¹University of Ljubljana, Faculty of mathematics and physics, Ljubljana, Slovenia

Correspondence to: Marten Blaauw (marten.blaauw@fmf.uni-lj.si)

1 **Abstract.**

2 The paper performs multivariate analysis of the linear Kelvin waves (KWs) represented by the operational 91-level ECMWF
3 analyses in 2007-2013 period, with focus on seasonal variability. The applied method simultaneously filters Kelvin wave
4 wind and temperature perturbations in the continuously stratified atmosphere on the sphere. The spatial filtering of the three-
5 dimensional Kelvin wave structure in the upper troposphere and lower stratosphere is based on the Hough harmonics using
6 several tens of linearized shallow-water equation systems on the sphere with equivalent depths ranging from 10 km to a few
7 meters.

8 Results provide the global Kelvin wave energy spectrum. It shows a clear seasonal cycle with the Kelvin wave activity
9 predominantly in zonal wavenumbers 1–2 where up to 50% more energy is observed during the solstice seasons in comparison
10 with boreal spring and autumn.

11 Seasonal variability of Kelvin waves in the upper troposphere and lower stratosphere is examined in relation to the back-
12 ground wind and stability. A spectral bandpass filtering is used to decompose variability into three period ranges: seasonal,
13 intraseasonal and intramonthly variability component. Results reveal a slow seasonal KW component with a robust dipole
14 structure in the upper troposphere with its position determined by the location of the dominant convective outflow throughout
15 the seasons. Its maximal strength occurs during boreal summer when easterlies in the Eastern hemisphere are strongest. Other
16 two components represent vertically propagating Kelvin waves and are observed throughout the year with seasonal variability
17 mostly found in the wave amplitudes being dependent on the seasonality of the background easterly winds and static stability.

18 1 Introduction

19 Atmospheric equatorial Kelvin waves (hereafter KWs), first discovered in the stratosphere (Wallace and Kousky, 1968), are
20 nowadays observed and studied over a broad range of spatial and temporal scales. A broad wavenumber-frequency spectrum
21 can be traced to the spatiotemporal nature of tropical convection which generates KWs along with a spectrum of other equatorial
22 waves. Atmospheric wave response to the stochastic nature of convection was studied by Garcia and Salby (1987) and Salby
23 and Garcia (1987) who made a distinction between (i) projection or vertical response to short-term heating fluctuations (e.g.
24 daily convection) and (ii) barotropic or horizontal response to seasonal convective heating. For KWs, the vertical response
25 gives rise to a broad frequency spectrum of vertically propagating KWs that radiate outward into the stratosphere where
26 they drive zonal-mean quasi-periodic flows such as the quasi-biennial oscillation (QBO, Holton and Lindzen, 1972). The
27 horizontal response to seasonal transitions in convective heating gives rise to planetary-scale disturbances with a half-sinusoidal
28 vertical structure confined to the troposphere. A part of this response remains stationary over the convective hotspot; its shape
29 resembling a classic "Gill-type" KW solution (Gill, 1980). The other part of the response intensifies and advances over the
30 Pacific, representing a transient component of the Walker circulation (Salby and Garcia, 1987).

31 Both components of the KW response received increased attention in the scientific community over the last decades in terms
32 of the role they play in the (intra)seasonal variability of the Tropical Tropopause Layer (hereafter TTL), defined as a transition
33 layer between the typical level of convective outflow at ~ 12 km where the Brunt-Väisälä frequency is at its minimum, and the
34 cold point tropopause at ~ 16 - 17 km (Highwood and Hoskins, 1998; Fueglistaler et al., 2009). Within the TTL, temperature
35 variations play an important role in controlling the stratosphere-troposphere exchange of various species such as ozone and
36 water vapour thereby aiding in the dehydration process of air entering the stratosphere. The two parts of the KW response
37 modulate the TTL differently on different time scales (Highwood and Hoskins, 1998; Randel and Wu, 2005; Ryu et al.,
38 2008; Flannaghan and Fueglistaler, 2013); their relative contribution to TTL dynamics varies with season and is not yet fully
39 understood. The present study contributes to this topic by applying a novel multivariate analysis of Kelvin wave seasonal
40 variability in model-level analysis data.

41 Seasonal variations of Kelvin wave dynamics in the TTL have been previously studied using temperature data derived from
42 satellites such as SABER (Sounding of the Atmosphere using Broadband Emission Radiometry, Garcia et al., 2005; Ern et al.,
43 2008; Ern and Preusse, 2009), HIRDLS (High Resolution Dynamics Limb Sounder, Alexander and Ortland, 2010), and GPS-
44 RO (Global Positioning System Radio Occultation, Tsai et al., 2004; Randel and Wu, 2005; Ratnam et al., 2006). For example,
45 Alexander and Ortland (2010) reported a clear seasonal cycle around 16-17 km (~ 100 hPa) in KW temperature observed by
46 HIRDLS, coinciding closely with variations in background stability. A widely used method for the KW filtering from gridded
47 data is the space-time spectral analysis introduced by Hayashi (1982). Space-time spectral filtering assumes that the linear
48 adiabatic theory for equatorial waves on a resting atmosphere is applicable (Gill, 1982). Filtering operates on single variable
49 data and it has been widely used to diagnose equatorial waves in the outgoing longwave radiation (OLR, e.g. Wheeler and
50 Kiladis, 1999) and climate model outputs (e.g. Lin and Coauthors, 2006). Based on 40-year ECMWF reanalysis (ERA-40)

51 data, Suzuki and Shiotani (2008) found that the temperature component of Kelvin waves tends to peak at 70 hPa while the
 52 zonal wind peaks at lower altitudes, i.e. at 100 hPa and 150 hPa in Eastern and Western hemisphere, respectively.

53 On the equatorial β -plane, shallow-water linear wave theory describes the Kelvin wave geopotential height (h_{kw}) and zonal
 54 wind (u_{kw}) perturbations propagating zonally with phase speed c as (Matsuno, 1966):

$$55 \quad h_{kw}(x, y) = \frac{c}{g} u_{kw} \quad \text{where} \quad u_{kw}(x, y) = u_0 \exp\left(-\frac{\beta y^2}{2c}\right) \cos k(x - ct). \quad (1)$$

56 Here, u_0 is the zonal wind amplitude at the equator, g is gravity, y is the distance from the equator and $\beta = df/dy$, f being
 57 the Coriolis parameter. The dispersion relationship between the wave frequency ν and the zonal wavenumber k is $\nu = kc$. The
 58 gravity wave speed in a layer of homogeneous fluid with mean depth D is given by $c = \sqrt{gD}$ (Gill, 1982).

59 The KW e -folding decay width a_e , known as the equatorial radius of deformation, is given by $a_e = (c/2\beta)^{1/2}$. By pre-
 60 scribing D , the horizontal structure of KW is defined by (1) for any k and can be used to simultaneously analyze wind and
 61 geopotential height perturbations due to KW waves on a single horizontal level. Such analysis was carried out by Tindall et al.
 62 (2006) for the lower stratosphere for the ERA-15 data in 1981-93 period. Their results suggested that KWs contributes ap-
 63 proximately 1 K² of the temperature variance on the equator with peak activity occurring during solstice seasons at 100 hPa,
 64 during December–February at 70 hPa and at 50 hPa it occurs during the easterly to westerly quasi-biennial oscillation (QBO)
 65 phase transition. Yang et al. (2003) used a_e as the fitting parameter for the projection of the ERA-15 data on the meridional
 66 structure of the KW and other equatorial waves. They found that the best fit trapping scale within 20°N–20°S is around 6°.
 67 The multivariate projection of data on the horizontal structures of equatorial waves including KWs on the equatorial β -plane
 68 was performed also for the short-range forecast errors of the ECMWF model (Žagar et al., 2005, 2007). For example, Žagar
 69 et al. (2007) found that forecast errors within 20°N–20°S belt project on KWs significantly more in the easterly QBO phase
 70 than in the westerly phase.

71 In this paper we extend the linear Kelvin wave analysis based on the shallow-water equation theory on the equatorial β -plane
 72 to the sphere. Second, we extend the KW filtering on individual horizontal levels or vertical planes to the three-dimensional
 73 (3D) KW analysis simultaneously in wind and temperature fields. This study thus explores seasonal variability of KWs in the
 74 TTL layer in a multivariate fashion using most of the information on the vertical wave structure available in recent operational
 75 ECMWF analyses.

76 On the sphere, the Kelvin mode is the slowest eastward-propagating eigensolution of the shallow-water equations (or Laplace
 77 tidal equations) linearized around a state of rest (e.g. Kasahara, 1976). In the continuously stratified atmosphere, the depth D
 78 becomes the "equivalent depth" of a given baroclinic mode and we need to solve Laplace tidal equations for a range of D from
 79 large (corresponding to the barotropic structure) to rather small (for high baroclinic modes) in order to consider the spectrum
 80 of Kelvin waves (e.g. Boyd, 2018). In contrast to the Kelvin wave trapping on the equatorial β -plane, which is controlled by a_e
 81 i.e. by the equivalent depth, the degree of the KW equatorial confinement on the sphere is in addition controlled by the zonal
 82 wavenumber (Boyd and Zhou, 2008). As shown by Boyd and Zhou (2008), even barotropic KW with D around 10 km are on
 83 the sphere confined within the tropical belt.

84 In section 2 we present a methodology which diagnosis 3D Kelvin waves in spherical datasets. Section 3 presents the KW
 85 energetics in wavenumber space focusing on the seasonal cycle. Section 4 presents seasonal KW variability in several frequency
 86 bands both for the horizontal as well as for the vertical projection KW response. Conclusions and outlook are given in section
 87 5.

88 2 Data and methodology

89 The Kelvin waves are filtered using the normal-mode function (NMF) decomposition derived by Kasahara and Puri (1981) and
 90 formulated as the *MODES* software package by Žagar et al. (2015). Here the methodology is briefly summarized followed by
 91 the method for the computation of the KW temperature perturbations and by examples of the 3D KW structure in global data.

92 Input ECMWF operational analyses covers approximately 6.5 years from January 2007 until June 2013. The dataset starts
 93 after two important updates in the ECMWF assimilation cycle: a resolution update on 1 February 2006 and the introduction of
 94 GPS-RO temperature profiles in the assimilation on 12 December 2006. The data ends at the next update in vertical resolution
 95 from L91 to L137 on 25 June 2013. The data horizontal resolution is 256×128 points in the zonal and meridional directions
 96 (regular Gaussian grid N64), respectively, on 91 irregularly spaced hybrid model levels up to around 0.01 hPa (around 80 km).
 97 The temporal resolution is 6 hours, i.e. 4 times per day, at 00, 06, 12 and 18 UTC. A case study of the large-scale KW in July
 98 2007 in this dataset by Žagar et al. (2009) showed that the NMF method provides information on the 3D wave structure and its
 99 vertical propagation in the stratosphere. Another case study from the same month demonstrated how the vertical KW structure
 100 improves as the number of vertical levels increased (Žagar et al., 2012).

101 2.1 Filtering of Kelvin waves by 3D normal-mode function expansion

102 The basic assumption behind the NMF expansion is that a global state of the atmosphere described by its mass and wind
 103 variables at any time can be considered as a superposition of the linear wave solutions upon a predefined background state.
 104 The NMF decomposition derived by Kasahara and Puri (1981) uses the σ vertical coordinate and linearization around the state
 105 of rest and realistic vertical temperature and stability stratification. 3D wave solutions of linearized primitive equations are
 106 represented as a truncated time series of the Hough harmonic oscillations and the vertical structure functions. The assump-
 107 tion of separability leads to separate equations for the vertical structure and horizontal oscillations. The latter are known as
 108 shallow-water equations on the sphere or Laplace tidal equations without forcing. The two systems are coupled by a separation
 109 parameter D which is called the equivalent height (Boyd, 2018). Eigenmodes of the global shallow-water equations are known
 110 as Hough harmonics. They describe two types of wave motions: Rossby waves and inertia-gravity waves which obey their
 111 corresponding dispersion relationships on the sphere.

112 The expansion of a global input data vector $\mathbf{X}(\lambda, \varphi, \sigma) = (u, v, h)^T$ can be represented by a discrete finite series as:

$$113 \begin{pmatrix} u(\lambda, \varphi, \sigma) \\ v(\lambda, \varphi, \sigma) \\ h(\lambda, \varphi, \sigma) \end{pmatrix} = \sum_{m=1}^M \mathbf{S}_m \left[\sum_{n=1}^R \sum_{k=-K}^K \chi_n^k(m) \mathbf{H}_n^k(\lambda, \varphi; m) \right] G_m(\sigma) \quad (2)$$

114 The input data vector contains wind components u, v and the transformed geopotential height h defined as $h = g^{-1}P$ where
 115 g is the gravity and P is defined as: $P = \Phi + RT_0 \ln(p_s)$; that is, it is the sum of geopotential Φ and a surface pressure, p_s ,
 116 term. Other two variables represent the specific gas constant for dry air (R) and the globally-averaged vertical temperature
 117 profile ($T_0(\sigma)$). The zonal and vertical truncations (K and M , respectively) define maximal numbers of zonal waves at a
 118 single latitude (wavenumber k) and a maximal number of vertical modes (denoted m) respectively. For every vertical structure
 119 eigenfunctions $G_m(\sigma)$, Hough harmonic functions, $\mathbf{H}_n^k(\lambda, \varphi)$ describe non-dimensional oscillations in the horizontal plane of
 120 the fluid with the mean depth equal the equivalent depth D_m . The parameter D_m appears in Eq. (2) in the diagonal matrix \mathbf{S}_m
 121 with elements $(gD_m)^{1/2}$, $(gD_m)^{1/2}$ and D_m which normalizes the input data vector after the vertical projection and thereby
 122 removes dimensions. Parameter R is the total number of meridional modes which is a sum of the eastward inertio-gravity waves
 123 (EIG), westward inertio-gravity waves (WIG) and Rossby waves. Linearization about the state of rest is not a drawback of the
 124 method as wave frequencies are used solely for the formulation of the projection basis and not for studying wave propagation
 125 properties. As shown by Kasahara (1980) (see also its Corrigendum) the meridional structures of the Hough functions for
 126 large scales are not significantly different if the linearization is performed around the non-zero mean zonal flow. The impact of
 127 latitudinal shear on the Kelvin waves was shown negligible by Boyd (1978). Further details of the NMF projection procedure
 128 are given in Žagar et al. (2015).

129 For each zonal wavenumber, the Kelvin mode is the lowest eastward-propagating latitudinal Hough function. In (2), the
 130 Kelvin wave is represented by the nondimensional complex expansion coefficients $\chi_n^k(m)$ with the meridional index $n = 1$.
 131 However, to follow often used notation, we shall denote the Kelvin wave in the remainder of this study as the $n = 0$ EIG mode,
 132 i.e. the Kelvin wave wind and geopotential height are represented by coefficients $\chi_{kw} = \chi_0^k(m)$. The truncation values are
 133 $K = 85$ and $M = 60$. This means that KW signal in 3D circulation at a single time instant consists of 5100 waves, 85 waves
 134 in every shallow-water equation system. Higher vertical modes were left out as their equivalent depth is smaller than 2 meters
 135 and their contribution to the total KW signal is negligible in the outputs in the TTL and the stratosphere. The relation between
 136 the truncation parameters and the normal-mode projection quality is discussed in Žagar et al. (2015) and references therein.

137 Once the forward projection is carried out and coefficients $\chi_n^k(m)$ are produced, filtering of KWs in physical space can be
 138 performed through (2) after setting all χ , except those representing the KWs, to zero. The result of filtering are fields u_{kw} ,
 139 v_{kw} and h_{kw} which provide the KW zonal wind, meridional wind and geopotential height perturbations. Notice here that in
 140 contrast to the equatorial β -plane, KWs on the sphere have a small meridional wind component which is thus left out from
 141 the discussion (Boyd, 2018).

142 The KW temperature perturbation, T_{kw} can be derived from the h_{kw} fields on σ levels using the hydrostatic relation in σ
 143 coordinates:

$$144 \quad T_{kw} = -\frac{g\sigma}{R} \frac{\partial h_{kw}}{\partial \sigma}. \quad (3)$$

145 The orthogonality of the normal-mode basis functions provides KW energy as a function of the zonal wavenumber and
 146 vertical mode. After the forward projection, the energy spectrum of total (potential and kinetic) energy for each Kelvin wave

147 can be computed using the energy product for the k th and m th normal modes (Žagar et al., 2015) as:

$$148 \quad I_{kw}(k, m) = \frac{1}{2} g D_m \chi_{kw} [\chi_{kw}]^* . \quad (4)$$

149 The units are J kg^{-1} . The KW global energy spectrum as a function of the zonal wavenumber is obtained by summing energy
150 in all vertical modes:

$$151 \quad I_{kw}(k) = \frac{1}{2} \sum_{m=1}^M g D_m \chi_{kw} [\chi_{kw}]^* . \quad (5)$$

152 2.2 Examples of 3D structure of Kelvin waves in L91 analyses

153 Kelvin waves are shown in Fig. 1-2 for a few days in July 2010 to introduce and illustrate their properties as filtered by the
154 NMF methodology.

155 Figure 1 illustrates the meridional structure of Kelvin waves on 25 July 2010 on 2 levels. KW activity was found largest in
156 the zonal wind component at 150 hPa over the Indian Ocean. The geopotential dipole structure is centred over the convective
157 hotspot over the Maritime continent. At 100 hPa, we find largest amplitude of KW temperature perturbations up to 4 K
158 positioned above the zonal wind maxima at 150 hPa. The meridional wind component of the KW is nonzero in spherical
159 coordinates, but is at most 0.22 ms^{-1} at 100 hPa which is negligible compared to the zonal wind component (maximum 12.5
160 ms^{-1}) making the KW wind field primarily zonal. Note that the presented horizontal structure at a single level is a superposition
161 of 60 vertical modes, i.e. 60 shallow water models with equivalent depths from about 10 km to a couple of meters.

162 Figure 2 illustrates day-to-day filtered KW fields along the equator on three separate July days in 2010, namely 25, 28 and
163 31. Both zonal wind (blue-to-red shades) and temperature fields (red contours) are shown. Without any predefined constrains
164 on the KW propagation, one can observe a rich variety of KW behaviour occurring in time: from the quasi-stationary dipole
165 patterns centred at 160 hPa to a wave package of free propagating wave structures in the stratosphere transiting from the
166 western into the eastern hemisphere.

167 In the stratosphere, the uppermost easterly wind component in blue shades around 30 – 50 hPa moves in eastward and
168 downward direction, demonstrating the upward transport of KW energy (Andrews et al., 1987). KW amplitudes were largest
169 over Eastern hemisphere with temperatures up to 4 K and zonal winds up to 12 ms^{-1} . The large amount of KW activity
170 occurred during the easterly phase of the QBO with strong easterly winds present between 30 and 80 hPa (not shown), providing
171 favourable conditions for strong KW activity.

172 Between 100 and 200 hPa during the second half of July, there was low-frequency KW activity present in the form of a
173 stationary and robust "wave-1" pattern with strong KW easterly winds up to 24 ms^{-1} in Eastern Hemisphere and KW westerly
174 winds up to 10 ms^{-1} in the Western Hemisphere. The high vertical resolution within the TTL resolves shallow KW structures
175 and a typical slanted structure towards the east in KW easterlies as well. The appearance and strength of horizontal KW
176 response coincides with the presence of strong easterly winds in the TTL in the Eastern Hemisphere during this period (not
177 shown). Figure 2 also shows that below 300 hPa the KW activity decreases and we shall not discuss levels under 300 hPa in
178 the paper.

179 The zonal wind and temperature components are coupled through Eq. (3) which states that the amplitude of the negative
 180 KW temperature perturbation is proportional to the negative vertical gradient in geopotential (and vice versa), as well as in the
 181 zonal wind since the zonal wind and geopotential are in phase. Horizontally, the cold anomaly is always located between the
 182 westerly and the easterly phase of the zonal wind component. Vertically, maximal positive temperatures are observed between
 183 easterly winds below and westerly winds above. An estimate of the vertical wavelength can be made based on alternating zonal
 184 wind minima and maxima. For example, on 25th July a well-developed KW package extending into the stratosphere moved
 185 from the Western into the Eastern hemisphere. A quasi-stationary component of the wave package is observed around 60°E
 186 with easterly winds located at 50 hPa (~ 21.5 km) and 150 hPa (~ 13.5 km), implying a vertical wavelength of around 8 km.
 187 More examples based on daily basis filtered from the 10-day deterministic forecast of the ECMWF can be found on the
 188 MODES website¹.

189 2.3 Other data and impact of the background state

190 In addition to the outputs from modal decomposition, full zonal wind and temperature fields from ECMWF analyses are used
 191 to compute the background fields based on the same N64 grid and over the same period (Jan 2007 - Jun 2013). Zonal wind U
 192 and static stability N are latitudinally averaged in the belt 5°S-5°N on all model levels to produce their zonal structure.

193 Static stability profiles are estimated through

$$194 \quad N^2 = \frac{g^2}{\Theta} \frac{\partial \Theta}{\partial \phi} \quad (6)$$

195 in units of s^{-2} and are defined on hybrid model levels on which the geopotential field ϕ and the potential temperature field Θ
 196 are derived a priori from the input data. Both fields are shown in Fig. 3.

197 The zonal wind field has the largest values on average in the TTL around 150 hPa with westerly winds peaking in the
 198 Western Hemisphere over the Pacific Ocean and easterly winds peaking in the Eastern hemisphere over the Indian Ocean
 199 and Indonesia. It represents a typical time-averaged outflow pattern in response to tropical convection (e.g. Fueglistaler et al.,
 200 2009). Throughout the seasons there is a longitudinal shift of this pattern following the convective source which is most clearly
 201 observed at 150 hPa. Such seasonal shift is visible up to 100 hPa in Fig. 3(b) where winds are weaker compared to 150 hPa.
 202 In northern winter, zonal winds are strongest over Indonesia and the Eastern Pacific with the zonal wind maxima position and
 203 strength similar compared to the longer ERA-40 dataset used by Suzuki and Shiotani (2008). During boreal summer easterly
 204 winds mainly prevail over the Indian Ocean, which is linked to the Indian Monsoon season.

205 At 100 hPa, the static stability illustrates the strongest seasonal cycle with values ranging from near-tropospheric values of
 206 $3 \times 10^{-4} \text{ ms}^{-2}$ during northern winter towards stratospheric values of $5 - 6 \times 10^{-4} \text{ ms}^{-2}$ during boreal summer. Note also
 207 the resolved local maxima in static stability at 80 hPa above the warm pools, known as the Tropical Inversion Layer (TIL)
 208 and which is possibly wave-driven (Grise et al., 2010; Kedzierski et al., 2016). Figure 3(b) suggests that the TIL descends
 209 down to 100 hPa during boreal summer months peaking over Western Pacific, in agreement with the cycle found in GPS-RO
 210 observations by Grise et al. (2010).

¹<http://meteo.fmf.uni-lj.si/MODES/>

211 Kelvin waves are subject to wave modulation in changing background environments. Along its trajectory, the potential
212 energy of the KW changes with varying background winds and stability which can be largely described by linear wave theory
213 as long as waves are not near their critical level involving breaking and dissipation (Andrews et al., 1987). For simplification,
214 KW modulation can be examined for the case of pure zonal as well as pure vertical wave propagation based on the wave
215 modulation analysis performed by Ryu et al. (2008). A few key points on their local wave action conservation principle are
216 summarised in the following.

217 In the tropical atmosphere, zonal modulation is the dominant process for KWs propagating in the stratosphere and in all non-
218 easterly winds in the TTL. Vertical modulation becomes important in the presence of easterly winds within the TTL. Zonal
219 modulation is found to affect both u_{kw} and T_{kw} components and their amplitudes are proportional to the Doppler-shifted phase
220 speed by $(c - U)^{1/2}$ in case of pure zonal propagation direction. This means that Kelvin waves diminish in amplitude over
221 regions with westerly winds and become more prone to dissipative processes, while amplify over regions with easterly winds².
222 In case of pure vertical modulation, the change in wave potential energy mainly fluctuates with the temperature component of
223 the Kelvin wave. Along the rays' vertical path, the waves amplitude is proportional to the Brunt-Väisälä frequency as $\propto N^{3/2}$,
224 and to the Doppler-shifted phase speed as $\propto (c - U)^{-1/2}$, such that N is expected to play a primary role above 120 hPa where
225 its value starts increasing rapidly (see Fig. 3).

226 Alexander and Orland (2010) showed through wave modulation principles that temporal variations in zonal-mean N indeed
227 are correlated with observed KW amplitudes at 16 km (approx. 100 hPa). A more extensive wave modulation analysis was
228 described by Flannaghan and Fueglistaler (2013) using the full ray tracing equations to demonstrate that zonal winds in the TTL
229 not only modulate Kelvin waves locally, but also create a lasting modulating effect on wave activity through ray convergence
230 in the stratosphere. In particular, the seasonal cycle of the upper tropospheric easterlies (on average located over the western
231 Pacific), that acts as an escape window for Kelvin waves throughout the year and largely explains the longitudinal structure of
232 Kelvin wave zonal wind and temperature climatology.

233 We shall present the seasonal variability of tropical convection by using the Outgoing Longwave Radiation (OLR) dataset
234 with daily outputs from the NOAA Interpolated OLR product (Liebmann and Smith, 1996). The OLR product, often used as a
235 proxy for convection, is extracted on a $2.5^\circ \times 2.5^\circ$ grid and interpolated on a N64 grid. Latitudinal averages are derived over
236 larger domain, namely over 15°S - 15°N since organized convection tend to happen more remote from the equator, especially
237 during the summer monsoon season over the Asian continent.

238 3 Kelvin wave energetics

239 We start with a discussion of the KW energy distribution among zonal wavenumbers as given by (5), followed by seasonal
240 differences.

²Keeping in mind that vertical wave propagation and consequently modulation becomes increasingly important as well wherever easterly winds are strong.

241 3.1 Energy distribution of Kelvin wave

242 The seasonal cycle in the energy-zonal wavenumber spectra is shown in Fig. 4 after summing up over all vertical modes. On
243 average, energy decreases as the zonal wavenumber increases as typical for atmospheric energy spectra. As we deal with the
244 large scales, we show only the first six zonal wavenumbers with energy values shown separately for the annual mean and the
245 four seasons separately.

246 Figure 4 shows that largest seasonal variations in KW energy are found at the largest zonal scales. For all zonal wavenumbers,
247 above annual-mean energy values are observed during DJF and JJA seasons while SON and MAM are below annual-mean
248 energy. In the zonal wavenumber 1, total KW energy varies between 200 Jkg^{-1} in MAM season and somewhat over 300 Jkg^{-1}
249 in JJA. In wavenumber 2, values do not exceed 100 Jkg^{-1} and JJA still contains the largest energy. At higher wavenumbers,
250 DJF season becomes the most energetic. In $k > 4$, total KW energy is under 20 Jkg^{-1} and continue to reduce with k . The slope
251 of the KW energy spectrum is between $-5/3$ and -1 at planetary scales (not shown), similar to the spectra presented in Žagar
252 et al. (2009) for July 2007 data. The JJA spectra has on average the steepest slope compared to other seasons, in particular the
253 DJF spectra. The energy distribution on planetary scales is mainly associated with large-scale tropical circulation established
254 in response to ongoing tropical convection. Therefore, the zonal distribution of tropical convection may likely play a crucial
255 role in explaining DJF and JJA season differences of KW energy, which will be explored in next section.

256 3.2 Seasonal cycle of KW energy

257 Figure 5 illustrates more details on the seasonal cycle by showing KW energy time series at the largest scales represented by
258 zonal wavenumbers $k = 1$, $k = 2$ and remaining scales $k > 2$. During most JJA seasons and occasionally in DJF (e.g. 2008)
259 the total amount of KW energy in $k = 1$ can reach up to 600 Jkg^{-1} , or twice the JJA average. The minimum in $k = 1$ KW
260 energy mainly occurs during October followed by April with values dropping towards 100 Jkg^{-1} , or half the SON average. The
261 temporal pattern in $k = 2$ is similar to the $k = 1$ pattern, but with a less pronounced semiannual cycle with maximum values up
262 to 200 Jkg^{-1} and minimum values towards 30 Jkg^{-1} . On zonal scales $k > 2$, KWs still show a semiannual cycle with highest
263 vertically-integrated values of energy in DJF.

264 In particular, for zonal wavenumber $k = 1$ one can distinguish intermonthly in addition to semiannual variability. Inter-
265 monthly variability is most clearly observed during JJA, for example in July 2011 where one can distinguish six separate
266 peaks of over 400 Jkg^{-1} energy over a period of approximately 90 days resembling an average wave period of about 18 days.
267 These are typical periods for free propagating Kelvin waves as observed in the TTL and lower stratosphere (e.g. Randel and
268 Wu, 2005). Note here again that our KW energy is vertically integrated over the whole model depth. This means that the ob-
269 served intermonthly variability of KWs appears dominated by the cyclic process of free propagating KWs entering the TTL,
270 amplifying due to changing environmental conditions, followed by wave breaking or dissipation.

271 The dominant scales of temporal variability in KWs are illustrated by a frequency spectrum of $k = 1$ in Fig. 6. The spectrum
272 is produced by the Fourier transform of energy time series of 6.5 years. The resulting power spectrum has been smoothed by
273 taking the Gaussian-shaped moving averages over the raw spectrum by using the Daniell kernel three times (Shumway and

274 Stoffer, 2010). The spectrum contains a peak at 1-day period associated with the diurnal tide projecting to the Kelvin waves.
275 After that, a gradual increase of energy is seen towards the 16-day period with multiple individual periods standing out. For
276 periods longer than 20 days, individual peaks are found close to 25, 43 and 59 days. After that, most KW energy is contained
277 by far in the semiannual cycle. The frequency spectrum provides a useful starting point for the discussion in the next section
278 when the spatiotemporal patterns of KWs shall be examined in several spectral domains.

279 Returning to Fig. 5, a low-pass filter with 90 day cut-off has been applied on KW energy in order to keep only the two
280 main spectral peaks in Fig. 6. The result is visible as the thicker black line in Fig.5 for all three zonal wavenumber groups. A
281 semiannual cycle for all zonal wavenumbers is evident with most energy observed around January and July, while least energy
282 is observed approximately one month after the equinoxes. During the years 2007, 2010, 2011, and 2012, more $k = 1$ KW
283 energy is observed during JJA compared to the follow-up DJF season. The DJF of 2009-2010 was for example above average
284 with energy values for $k = 1$ above 350 Jkg^{-1} .

285 The year to year differences can be explained by many coupled factors. In general, one expects the vertically-integrated KW
286 activity to increase when background wind conditions become favorable, i.e. in the presence of easterly winds. This occurs
287 in the TTL in relation to strong convective outflow (Garcia and Salby, 1987; Suzuki and Shiotani, 2008; Ryu et al., 2008;
288 Flannaghan and Fueglistaler, 2013) during DJF and JJA seasons mainly. Moreover, KW activity is enhanced whenever easterly
289 QBO winds are present down into the lower stratosphere (Baldwin and Coauthors, 2001; Alexander and Ortland, 2010) or
290 during El Niño (Yang and Hoskins, 2013). The latter factor may partly explain a large difference in the KW energy during the
291 El Niño DJF of 2009-2010 and the below-average energy level a year after, during the strong La Niña DJF period of 2010-
292 2011. However, during the La Niña DJF of 2007-2008, the amount of KW energy is above normal. That season was however
293 characterized by above-normal MJO activity which often occurs during favourable easterly QBO conditions in the stratosphere
294 (Son et al., 2017). During 2010-2011 DJF season stratospheric winds were largely westerly thereby prohibiting KW activity.
295 The role of these low-frequency atmospheric phenomena on KW seasonal variability is a topic of further research.

296 Finally, Fig. 5 also shows that KW activity in July 2007, previously examined by Žagar et al. (2009), was exceptionally
297 strong. A large part of that energy, (somewhat more than half) belonged to zonal wavenumber 1. In spatiotemporal terms, it is
298 associated with the presence of a strong dipole structure in the TTL (as in Fig.2), which is colocated with favourable easterly
299 wind conditions in the TTL as well as in the stratosphere (not shown). In fact, at 50 hPa the QBO was just at the beginning of
300 its westerly phase in July 2007.

301 **4 A spatiotemporal view on Kelvin wave seasonal variability**

302 **4.1 Kelvin wave decomposition among wave periods**

303 In this section, the spatiotemporal view of KWs shall be presented over three dominant ranges of wave periods in Fig. 6,
304 namely: (i) the (semi)annual cycle using a low-pass filter with cut-off period at 90 days, (ii) the intraseasonal period using
305 a bandpass filter over periods between 20-90 days, and finally (iii) the intramonthly period with bandpass filtered periods

306 between 3-20 days. The chosen periods, especially the intramonthly periods, are similar to those used in previous studies. In
307 each case, mean 6-year fields as well as seasonal means shall be presented.

308 Note that our temporal filtering operates on time series of KW signals at every grid point. This is different from the commonly
309 applied space-time filtering following Hayashi (1982) that applies KW dispersion relations. Our filtered KWs can appear
310 stationary or even westward shifted due to westward-moving sources of the KW amplification (e.g. easterly winds, high static
311 stability in the TTL).

312 Both KW components u_{kw} and T_{kw} are Fourier-transformed to frequency space where the spectral expansion coefficients
313 χ_{kw} in domains outside the desired frequency ranges are put to zero. Case (i) results in KW components $u_{kw,l}$ and $T_{kw,l}$ where
314 l indicates the low-frequency component. Case (ii) results in $u_{kw,m}$ and $T_{kw,m}$ where m indicates the intramonthly period.
315 Case (iii) results in fields $u_{kw,h}$ and $T_{kw,h}$ where h stands for the high-frequency component. Previous studies have defined
316 free propagating Kelvin waves over similar ranges (3-20 days, Alexander and Ortland (2010); 4-23 days, Suzuki and Shiotani
317 (2008)) and similarly for intraseasonal periods (23-92 days, Suzuki and Shiotani (2008)). Next, seasonal averages will be taken
318 over the four seasons, resulting in variables $\overline{u_{kw,l}}^s$, $\overline{T_{kw,l}}^s$ for the low-frequency component and similarly for the other two
319 cases. The superscript s represents one of the four seasons: northern winter ($s = DJF$), spring ($s = MAM$), summer ($s = JJA$),
320 and autumn ($s = SON$).

321 Cases (ii) and (iii) contain purely subseasonal variability and therefore one can expect their 6-year means to be zero-valued
322 since variability beyond 90 days has been put to zero. Similarly, mean fields for each of the four seasons results in $\overline{u_{kw,h}}^s \ll$
323 $\overline{u_{kw,l}}^s$ and $\overline{u_{kw,m}}^s \ll \overline{u_{kw,l}}^s$ and the same for the temperature component. This reflects the fact that positive and negative
324 phases of the fast KW responses average out to approximately zero on seasonal timescales (figure not shown). Therefore, the
325 seasonal mean of the absolute amplitudes of the zonal wind and temperature are examined instead, i.e. $|\overline{u_{kw,h}}^s|$, $|\overline{u_{kw,m}}^s|$ and
326 similarly for temperature. This describes seasonal fluctuations in subseasonal KW amplitudes³.

327 Figure 7 shows results for all three cases after taking mean over the whole period. The left panel resembles a dominant
328 "wave-1" structure with zonal wind maximized around 140 hPa. Easterly KW winds are strongest around 60°E and westerly
329 winds around the Date Line. Note that two stationary perturbations over African (30°E) and South American (80°W) orography
330 are the result of our terrain-following NMF analysis. If one compares the KW zonal wind pattern with the climatological zonal
331 wind pattern in Fig. 3(a) it can be observed that the zonal wind pattern is located around 20° west of the climatological pattern.
332 Wave temperature perturbations are largest where the vertical gradients in zonal wind are largest which explains the quadrupole
333 structure. Warm and cold KW anomalies are located at 100 hPa in the Eastern and Western hemisphere, respectively, and vice
334 versa at 200-300 hPa.

335 The average low-frequency or seasonal KW structure has a significant resemblance with the classical Gill-type KW solution
336 (Gill, 1980) describing a steady-state linear wave response to convective forcing. The Gill-type KW solution is characterized
337 by westerly upper-troposphere winds east of the large-scale convective source. In responds to the seasonal cycle of convection,

³Most previous studies define KW activity as square amplitude rather than absolute amplitude. In our high resolution dataset we observe highly localized patterns of the KW activity in the Eastern hemisphere due to ongoing wave amplification. By using absolute amplitudes we better visualize the longitudinal structure of the KW activity in comparison to its local maxima.

338 the solution in Fig. 7a illustrates, in addition to a low-frequency KW variability in westerly winds, also a considerable low-
339 frequency variability west of the convective outflow. This part of the signal represents the wave modulation effect of the
340 propagating KWs on seasonal timescales.

341 The middle panel of Fig. 7 shows the average distribution of KW activity on intraseasonal timescales. The activity is largest
342 in the Eastern hemisphere with average zonal wind maxima up to 3 ms^{-1} and temperature maxima up to 0.7 K. Zonal wind
343 activity is largest over a broad area between 90 and 150 hPa over the Indian Ocean and the Maritime Continent. Temperature
344 activity occurs slightly higher around 90-100 hPa. Intraseasonal activity is locally somewhat increased also around 120°W ,
345 west of the Andes mountain range.

346 Finally, Fig. 7c illustrates the average distribution of intramonthly KWs. The Eastern hemisphere again makes up for the
347 larger KW activity than the Western hemisphere, but the maximum is located more upward in comparison to the intraseasonal
348 scales, around 80 hPa. Zonal wind activity peaks up to 3 ms^{-1} over a broad range of 70-110 hPa and temperature peaks over
349 a more narrow area around 76 hPa (up to 0.75 K). The main area for KW activity is found over Indian Ocean region, while
350 least wave activity is above central Pacific. Towards the stratosphere KW activity reduces and becomes more uniform along in
351 longitudinal direction.

352 4.2 Low-frequency Kelvin wave variability

353 The seasonal patterns of the low-frequency components of the KW is presented as pressure-longitudinal cross-sections along
354 the equator (at 0.7°N) of the KW seasonal means, given by $\overline{[u_{kw,l}]^s}$ and $\overline{[T_{kw,l}]^s}$ in Fig. 8.

355 The largest amplitudes are found during the JJA months. A strong dipole "wave-1" pattern is evident in the TTL. The
356 strongest zonal winds are found close to 150 hPa with easterlies up to -12 ms^{-1} centered over Indian Ocean and westerlies
357 up to 6 ms^{-1} over the Western Pacific. Negative temperature KW anomalies at 110 hPa are strongest as well during JJA with
358 values up to 1.5 K over Indian Ocean and annually averaged value of -0.5 K over Western Pacific.

359 During DJF, the dipole pattern has shifted more eastward and upward compared to JJA and has a more slanted structure.
360 Easterly (westerly) KW winds are located more east over the Maritime continent (central Pacific) and are centered at 130 hPa.
361 The upper temperature dipole pattern is found higher up at 90 hPa approximately. Values are somewhat weaker compared to
362 NH summer with easterlies up to -6 ms^{-1} and westerlies up to 5 ms^{-1} .

363 Finally, SON and MAM season months are transition seasons with respect to the strength and position of the KW dipole as
364 it moves west- and downward towards JJA and east- and upward towards DJF. MAM has the weakest KW dipole with slightly
365 stronger westerly winds up to 5 ms^{-1} .

366 The longitudinal position and the strength of the low-frequency KWs have been linked to the seasonal patterns of the back-
367 ground winds in the TTL representing the upper level monsoon and Walker circulations (Flannaghan and Fueglistaler, 2013).
368 The average background winds maximize at 150 hPa as shown in Fig. 3(a). In Fig. 8, one can see how the KW easterlies in the
369 Eastern hemisphere are strongest during JJA in relation to the Indian-South Asian monsoon circulation. Background easterlies
370 as strong as -30 ms^{-1} are located approximately 10° east of the KW maximum easterlies. DJF has the strongest background

371 westerlies in relation to the upper-level circulation of the Western Pacific anticyclones. MAM shows similar background wind
 372 patterns compared to DJF but with weaker circulation. SON shows similar patterns with JJA but with weaker winds.

373 Further details on longitudinal position and interannual variability of the low-frequency KW response at its maximum value
 374 at 150 hPa are illustrated by the Hovmoller diagram in Fig. 9. For comparison, tropical convection is represented as well through
 375 the OLR proxy variable averaged over 15°S-15°N latitudes. All fields have been filtered with a 90 day cut-off low-pass filter
 376 in order to highlight the seasonality. As a result, one can observe enhanced/reduced KW activity during the same individual
 377 seasons as seen from the timeseries in Fig. 5. Above average seasonal KW activity with stronger dipole structures occurred
 378 during the summer of 2007 (mainly through its easterlies at 60°E) and during the winters of 2006-2007 and 2009-2010. In
 379 these winters, El-Nino was active and a clear longitudinal eastward shift is observed in OLR, in the background circulation
 380 (not shown), as well as in the dipole KW structure. The El-Nino winter of 2009-2010 was followed by a strong La Nina winter
 381 with an increase in tropical convection over the Maritime continent (note: OLR values below 195 Wm⁻²).

382 The vertical seasonal movement of the KW dipole has been linked with the seasonal movement of the tropical tropopause
 383 height (Flannaghan and Fueglistaler, 2013; Ryu et al., 2008). The position of the tropical tropopause height (represented by a
 384 static stability value of $5 \times 10^{-4} \text{ s}^{-2}$ in Fig. 8) is found at approximately 85 hPa during DJF and descends towards 100 hPa in
 385 JJA, similar to values obtained from GPS-RO observations by Grise et al. (2010). In particular, during JJA, one can notice how
 386 the asymmetry in the tropical tropopause height over Indian Ocean around 60°E coincides with increasing temperatures by the
 387 KW dipole up to 1.5 K. Such deformation of the tropical tropopause is also evident during DJF and SON seasons.

388 Figures 10a and 10b illustrate seasonal-mean KW temperatures $\overline{T_{kw,l}}^s$ in relation to the tropical tropopause layer defined
 389 by static stability N^2 . Seasonal variations in KW temperatures are colocated with the position of the tropopause, descending
 390 down from its highest position during DJF to its lowest position during JJA. Temperature amplitudes are observed to decline
 391 roughly above $N^2 = 5 - 6 \times 10^{-4} \text{ s}^{-2}$. Within this zonal-mean seasonal picture, zonal asymmetries in N^2 exist and are found:
 392 (i) near the Date Line with values of $8 \times 10^{-4} \text{ s}^{-2}$ at 80 hPa during DJF and $7 \times 10^{-4} \text{ s}^{-2}$ at 90 hPa during JJA and (ii) lower
 393 at 100 hPa over the Indian Ocean during JJA. Particularly during JJA, the deformation of the zonal-mean static stability field
 394 colocates strongly with the position of a strong KW temperature anomaly over Indian Ocean. A rough estimation is made on
 395 the contribution of the KW anomaly to the zonal deformation of the tropopause layer by removing zonal-mean parts of both
 396 fields. First, static stability zonal anomalies, $\overline{N'^2}^s$, are derived by subtracting zonal-mean values of N^2 from the full N^2 field
 397 per timestep and at every pressure level, followed by seasonal averaging. Next, we can estimate the static stability change
 398 associated with the KW anomaly, using the relation: $N_{kw}^2 = \frac{g}{\theta} \frac{\partial \theta_{kw}}{\partial z}$, followed by seasonal averaging as well, i.e. $\overline{N_{kw}^2}^s$.

399 As a result, Fig. 10c and 10d show how both static stability anomalies are overlapping. During DJF, the structure of the
 400 zonal anomaly $\overline{N'^2}^s$ has a positively-valued tilt eastward which stretches up to 80 hPa, while during JJA a strong static stability
 401 anomaly is found more localized over Indian ocean region with values in the TTL up to $\overline{N'^2}^{JJA} = \pm 0.8 \times 10^{-4} \text{ s}^{-2}$. The
 402 anomaly associated with the KW temperature anomaly is found to peak up to $+0.6 \times 10^{-4} \text{ s}^{-2}$ during JJA and up to $+0.4 \times 10^{-4}$
 403 s^{-2} during DJF. Finally, by dividing both fields with each other, the resulting contribution of the quasi-stationary Kelvin wave
 404 to the observed deformation of the tropical tropopause layer is estimated up to 60% during JJA and 80% during DJF.

405 4.3 Intraseasonal Kelvin wave variability

406 The seasonality of intraseasonal Kelvin wave variability is shown in Fig. 11 and shall be briefly discussed here. The DJF stands
407 out as the most active season for KW activity, located mainly in the Eastern hemisphere centred at 100°E and with maximum
408 activity at 110 hPa for zonal wind and temperature with a second maximum in temperature at 90 hPa. Values observed are up
409 to 0.8 K for KW temperature and 5 ms⁻¹ for KW zonal wind. During MAM season, the KW activity fields are weaker but
410 spread over a larger area in the Eastern hemisphere and in the TTL with maximum activity centered at 120 hPa (90 hPa) for
411 the zonal wind (temperature) component. Both JJA and SON seasons have KW activity positioned at lower altitudes and more
412 westward. In both seasons, KW zonal wind activity is split up between two structures with an eastward tilt with height; one
413 with a maximum around 110°E and one pattern starting from 100 hPa and extending towards 60°E. Note also the increase
414 in KW activity in the Western hemisphere below 150 hPa in the East Pacific. The maximum KW activity in the temperature
415 component for both seasons is positioned near 100 hPa approximately on the tropical tropopause contour with value 5×10^{-4}
416 s⁻².

417 The eastward tilted structure is observed throughout all seasons except MAM when background easterly winds are nearly
418 absent in the Eastern hemisphere. In all other seasons one can observe how the tilted structure is locked to the background
419 easterlies with maximum amplitudes located slightly above and west of it. Such eastward tilt with height has been frequently
420 observed, for example over radiosonde station Medan at 100°E during the early stage of MJO development (Kiladis et al.,
421 2005).

422 4.4 Intramonthly Kelvin waves

423 The seasonal variability of intramonthly Kelvin waves, represented by their absolute amplitudes $\overline{|u'_{kw,h}|^s}$ and $\overline{|T'_{kw,h}|^s}$, shall
424 be examined in relation to the background conditions. Figure 12 illustrates favorable regions for KW activity. In general, KW
425 activity increases upward from around 120 hPa towards its zonal-mean peak value at 76 hPa. The largest values are observed
426 in the Eastern hemisphere in region from 30°E till 150°E. The temperature component in particular has a constant maximum
427 peak (up to 0.8 K) located around 76 hPa throughout the year, where also the largest increase in N^2 occurs as shown in Fig. 3.
428 Above 70 hPa, KW activity continuously decreases in the stratosphere.

429 The longitudinal structure of the KW zonal wind shows two distinct peaks in the TTL, one consistently located at 76 hPa and
430 another around 100-110 hPa in the Eastern hemisphere which is mainly present during solstice seasons. The first maximum co-
431 incides with the temperature distribution which can be explained by their balance relationships and free horizontal propagation
432 in the stratosphere. Below the tropopause, KW activity is coupled to convective processes alternating the tropospheric vertical
433 wave structures as discussed by Flannaghan and Fueglistaler (2012).

434 The secondary maximum around 110 hPa in Fig. 12 is present mainly during solstice seasons in the Eastern hemisphere and
435 it is associated with the seasonal movement of the background wind. The maximum of KW wind and the background wind
436 maximum move eastward from DJF to JJA season similar to the low-frequency variability. A day-by-day comparison of the
437 KW activity and background wind confirms that propagating KWs amplify while approaching a region of strong easterlies,

438 forming a folding structure around it while the individual KWs dissipate towards the center of easterly winds. One can notice
439 in Fig. 12 a fast reduction of KW amplitudes eastward of its maximum towards the center of the background easterlies. It is
440 likely related to dissipation and wave breaking processes as observed over Indonesia (120°E) by Fujiwara et al. (2003). Within
441 such regions, the KW-background wind interaction becomes complex and the linearity assumption breaks (Ryu et al., 2008;
442 Flannaghan and Fueglistaler, 2013).

443 A comparison with the previous study by Suzuki and Shiotani (2008) using ERA-40 data shows that the L91 data contain
444 stronger KW activity in the vicinity of the background easterlies in the Eastern hemisphere, and more fine-scale details which
445 can be explained by better analyses based on more observations and improved models including increased resolution. For
446 example, Suzuki and Shiotani (2008) used 5 levels of ERA-40 data between 50 and 200 hPa whereas the present study considers
447 25 model levels between 50 – 200 hPa. Maxima of the KW temperature signal appear in similar locations and strength except
448 for a small offset in vertical position (70 hPa in Suzuki and Shiotani (2008) versus 80 hPa in Fig. 12) and a larger zonal
449 asymmetry in our results.

450 Another view of the seasonal cycle of free propagating KWs is illustrated in Fig. 13 which focuses on the spatiotemporal
451 distribution of individual KW tracks. Hovmoller diagrams are illustrated of KW zonal wind and temperature at levels 110 and
452 200 hPa cumulated from different years into a single calendar year along with the background zonal wind. In addition, the
453 monthly-mean values of daily maximum KW amplitudes occurring in longitude are added on the rightside of each diagram. It
454 represents seasonality in the KW maximum amplitudes in a similar fashion to Fig. 6 in Alexander and Ortland (2010) which is
455 based on HIRDLS satellite data.

456 The individual wave tracks at 110 hPa illustrate KWs with amplitudes exceeding 3 ms^{-1} and 0.6 K which are propagating
457 throughout the year in the Eastern hemisphere, during June-October months only over the Pacific, and all except DJF months in
458 most of the Western Hemisphere. Typical wave tracks start east of the 0° (30°W) meridian during winter (summer) and largely
459 disappear west of 120°E . The largest wave amplitudes are observed between 50°E and 100°E prior to regions of easterly winds
460 in agreement with Fig. 12. Here presented details show that most notable waves appear during the Asian monsoon period with
461 upper-level easterlies prevailing from June into September. The largest KW amplitudes appear confined to the June and July
462 months followed by a rapid drop in August. In fact, a local minimum in the number of KWs as well as in wave amplitudes
463 occurs in August before the KW activity increases slightly during autumn.

464 At 200 hPa, the favorable area for KW propagation shifts to the Western Hemisphere and large KW activity is observed west
465 of the South American continent throughout the year (west of 80°W) with a westward extension over the Pacific during JJA.
466 Another set of wave tracks starts over equatorial South America around 30°W and continues till 60°E during JJA. During DJF
467 these wave tracks shift more east and start at 5°W and continue till 90°E . The seasonal shifts of approximately 30° in KW
468 tracks collocate with similar shifts in the prevailing TTL winds.

469 The amplitude of KWs undergoes a clear annual cycle with a small secondary peak present during DJF, as represented by the
470 monthly-means of daily maximum amplitudes on the rightside of Fig. 13. The largest amplitudes are found at 110 hPa during
471 JJA with monthly-mean zonal wind (temperature) values up to 8.5 ms^{-1} (1.8 K) in June. During the DJF months Kelvin
472 waves amplify more eastward with monthly-mean zonal wind (temperature) values up to 7.8 ms^{-1} (1.6 K) in December.

473 Our result matches well with the observed seasonal pattern in maximum KW temperatures at 16km (~ 100 hPa) from the
474 HIRDLS satellite observations (Alexander and Ortland, 2010, Fig. 6). At 200 hPa, KW amplitudes are on average lower with
475 a yearly-averaged amplitude reduction around 55% in temperature and 35% in zonal wind.

476 The semiannual cycle in maximum amplitudes remains visible up till 70 hPa. Above 70 hPa, where the KW activity remains
477 large in Eastern hemisphere (Fig. 12), the semiannual cycle is replaced by an interannual cycle in line with the dominant impact
478 of the QBO.

479 5 Discussion and Conclusions

480 We have applied the multivariate decomposition of the ECMWF operational analyses during the period 2007-2013 when
481 the operational data assimilation and forecasting were performed on 91 model levels. The applied normal-mode function
482 decomposition provides simultaneously the wind components, geopotential height and temperature perturbations of Kelvin
483 waves for many scale without any prior data filtering. The three-dimensional Kelvin wave structure in the upper troposphere
484 and lower stratosphere is composed of Kelvin wave solutions of 60 linearized shallow-water equation systems on the sphere
485 with equivalent depths from 10 km up to about 3 meters. As the KW meridional wind component is very small it is not discussed
486 here. We showed that large-scale KWs readily persist in the data despite analyzing selected processing times independently.

487 The KW is a normal mode of the global atmosphere and our 3D-orthogonal decomposition allows quantification of its
488 contribution to the global energy spectrum and variability. We have presented the total (kinetic+potential) energy of KWs in
489 the L91 data as a function of the zonal wavenumber in different seasons. The zonal wavenumber $k = 1$ contains the largest
490 portion of KW energy in all seasons. There is almost one third more energy in JJA than in MAM in $k = 1$. In $k = 2$ there is
491 50% less energy than in $k = 1$ but JJA still contains most energy. In all larger zonal wavenumbers, the most energetic season is
492 DJF.

493 We focused on the spatiotemporal features of the KW temperature and zonal wind components in the four seasons. The
494 Kelvin wave seasonal cycle in the tropical tropopause layer (TTL) was compared with seasonal variability of the Outgoing
495 Longwave Radiation (OLR), and the background wind and stability fields, which are believed to play an important role for
496 the KW variability. Our results of the seasonal KW variability complement previous studies which applied different methods
497 for the KW filtering and different datasets. The frequency spectrum has revealed a semiannual cycle as well as intraseasonal
498 and intramonthly variability. Three ranges of wave periods were analyzed: 3-20 days, 20-90 days and longer than 90 days.
499 This choice was partly deliberate in order to compare our results with several previous studies of KW variability. First we
500 demonstrated that the low-frequency KW dipole pattern in the TTL, with westerly winds in the Western hemisphere and
501 with easterly winds in the Eastern hemisphere, partly resembles a seasonal-averaged Gill-type "wave-1" pattern and contains
502 partly low-frequency modulation of vertically-propagating KWs. The quadrature-shaped temperature component represents a
503 thermally adjusted pattern with respect to the zonal wind component, and contributes to seasonal warming above 100 hPa in the
504 Western and cooling in the Eastern hemisphere. The largest KW amplitudes are observed during JJA and DJF seasons. From
505 boreal summer towards winter, KW perturbations moves eastward (from Indian Ocean basin towards Maritime Continent) and

506 upward (e.g. zonal wind component moves up from 150 hPa towards 120 hPa). The KW zonal wind amplitude varies between
507 12 m/s strong easterlies over Indian ocean near 150 hPa in JJA to 6 m/s over Western Pacific. Over Indian Ocean in JJA, the
508 KW easterlies thus make almost half of the total wind vector. The associated KW temperature perturbations are from 1.5 K
509 over Indian ocean in JJA to -0.5 K over West Pacific. The zonal modulation of Kelvin waves is found to be locked with respect
510 to the seasonal movement of convection and the convective outflow in the TTL. The modulation effect is strongest for the
511 low-frequency Kelvin waves during the summer monsoon season, when strong easterly winds are present at 150 hPa, resulting
512 in the largest KW zonal wind and temperature anomalies, of which the latter results in deformation of the tropical tropopause
513 over Indian Ocean.

514 Intraseasonal (periods 20-90 days) activity is strongest in DJF with maxima up to 0.8 K for KW temperature and up to 5 m/s
515 for KW zonal wind centred at 120°E. Both temperature and zonal wind activities have eastward tilt with height. In comparison
516 to previous study by Suzuki and Shiotani (2008) using ERA-40 data, the slanted structure in the present data continues to
517 extend more upward and eastward which is likely due to the increased number of vertical model levels compared to ERA-40.
518 The importance of vertical model resolution for the KW structure and amplitude was demonstrated in Žagar et al. (2012) and
519 Podglajen et al. (2014).

520 For periods 3 – 20 days, the seasonal cycle of KWs is clearly seen in the wave amplitude. In the zonal-mean perspective, the
521 largest amplitudes are located between 70 and 100 hPa for both zonal wind and temperature but it is modulated by the seasonal
522 movement of the TTL. A major zonal asymmetry was found in KW activity: around 110 hPa the Kelvin wave undergoes
523 amplification mainly in the Eastern hemisphere during the solstice seasons, while at 200 hPa a secondary region of the KW
524 amplification occurs in the Western hemisphere during boreal summer. The intermonthly KWs show largest amplitudes in the
525 vicinity of the strongest easterlies preferably west and above the centre of easterlies. The applied novel methodology makes it
526 possible to observe such dynamics on daily basis whenever easterlies are strong in the TTL. Nearly real-time representation of
527 the KW activity is available on <http://modes.fmf.uni-lj.si>.

528 In summary, our seasonal variability analysis shows that the background wind in the TTL linked with convective outflows,
529 play a dominant role in the longitudinal position where the zonal modulation of Kelvin waves is preferred, while the tropical
530 tropopause and its seasonal vertical movement determine the vertical extent of the KW modulation processes.

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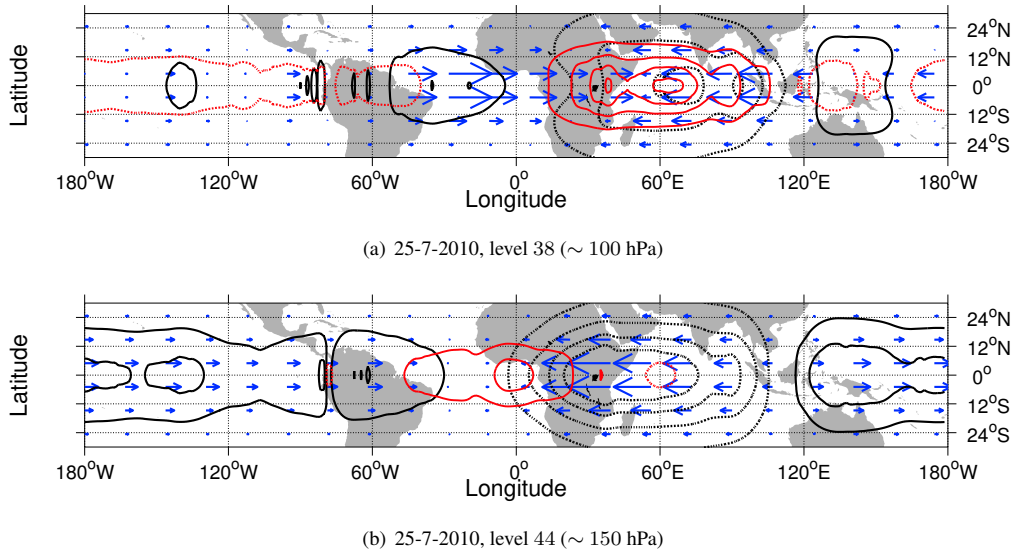


Figure 1. The horizontal structure of Kelvin waves in the ECMWF analysis data on 25 July 2010 at (a) 100 hPa and (b) 150 hPa. The geopotential height perturbations (h_{kw}) are shown by black contours, every 20 m, whereas temperature perturbations (T_{kw}) are in coloured red, every 1 K). Dashed contours represent negative and full line positive perturbations. Zero lines are omitted.

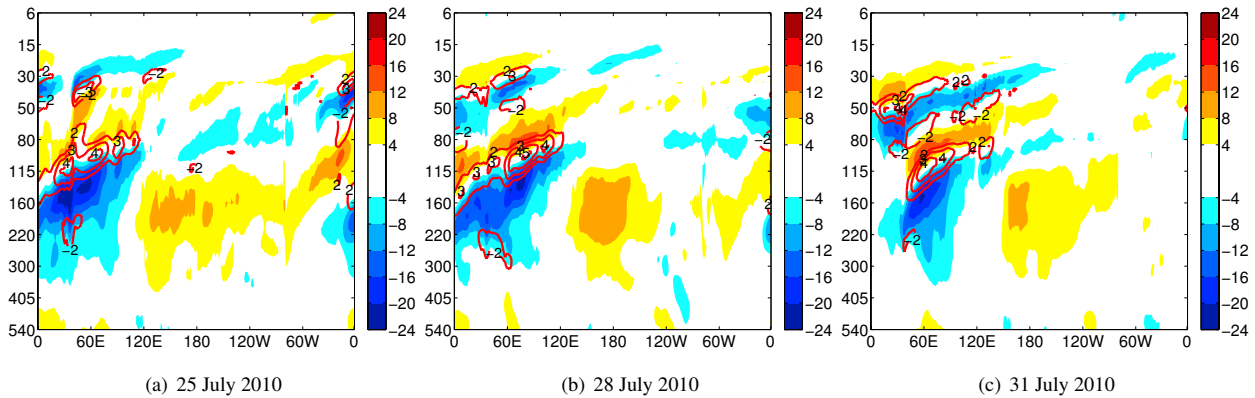


Figure 2. Longitude-pressure cross-section of the Kelvin wave zonal wind (red-blue shaded contours) and temperature (red contours) perturbations along 0.7°N on (a) 25 July, (b) 28 July and (c) 31 July 2010. Temperature is shown every 1 K, starting at 2 K. Zonal winds are drawn every 4 ms^{-1} . Zero lines are omitted.

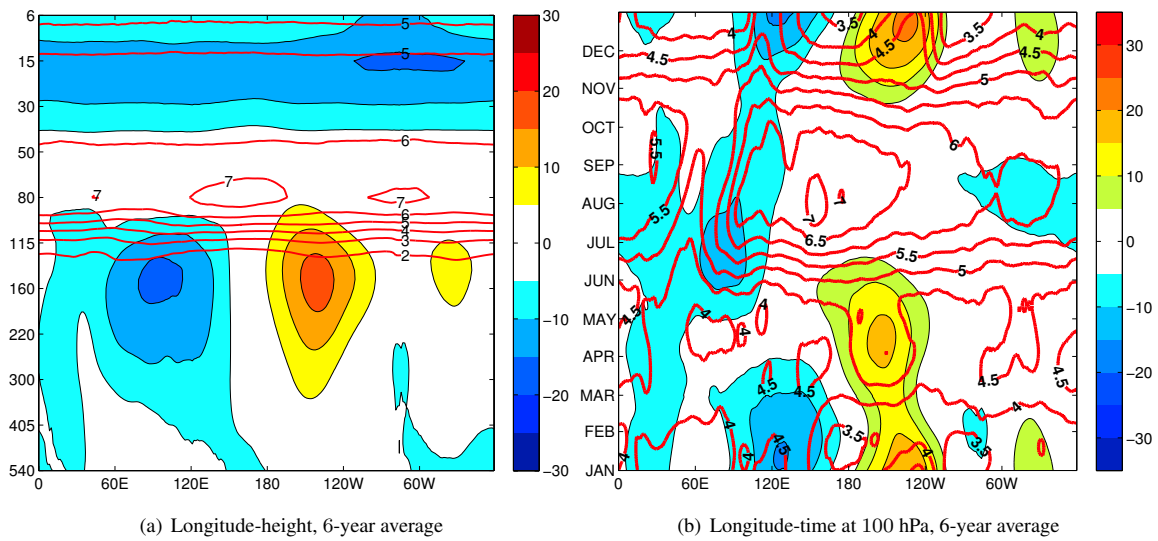


Figure 3. Six-year average of the zonal wind and static stability fields of the ECMWF operational analyses. Both fields are latitudinally averaged over 5°S - 5°N , and have been low-pass filtered a priori with a cut-off period of 90 days to highlight seasonal variability. (a) Longitude-height section and (b) Longitude-time section at 100 hPa. Zonal winds are coloured by blue-to-red contours, each 5 ms^{-1} whereas static stability is shown in red contours, each (a) $1 \times 10^{-4} \text{ s}^{-2}$ and (b) $0.5 \times 10^{-4} \text{ s}^{-2}$. Zero lines are omitted.

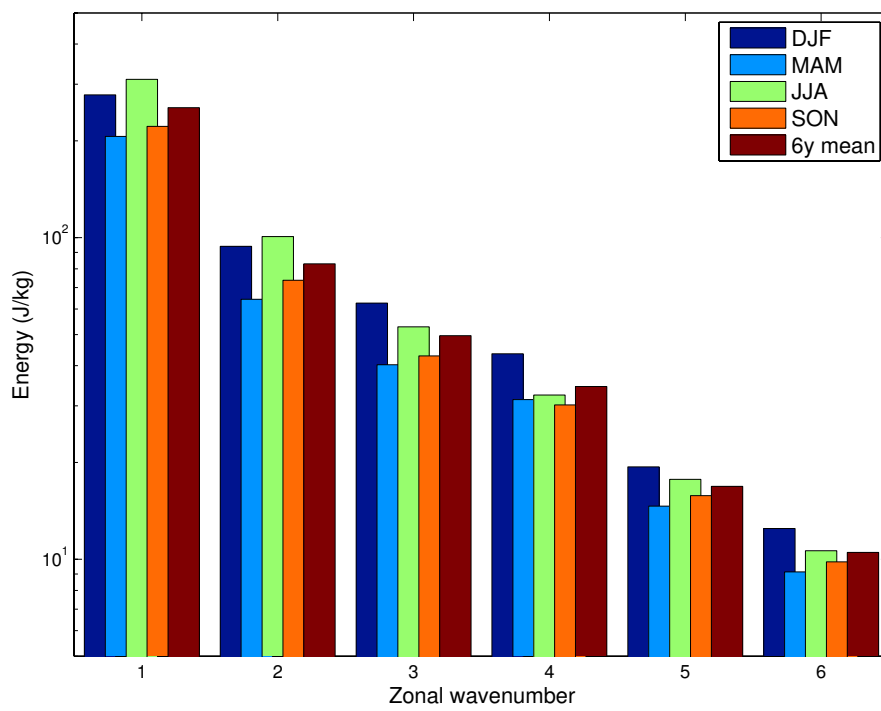
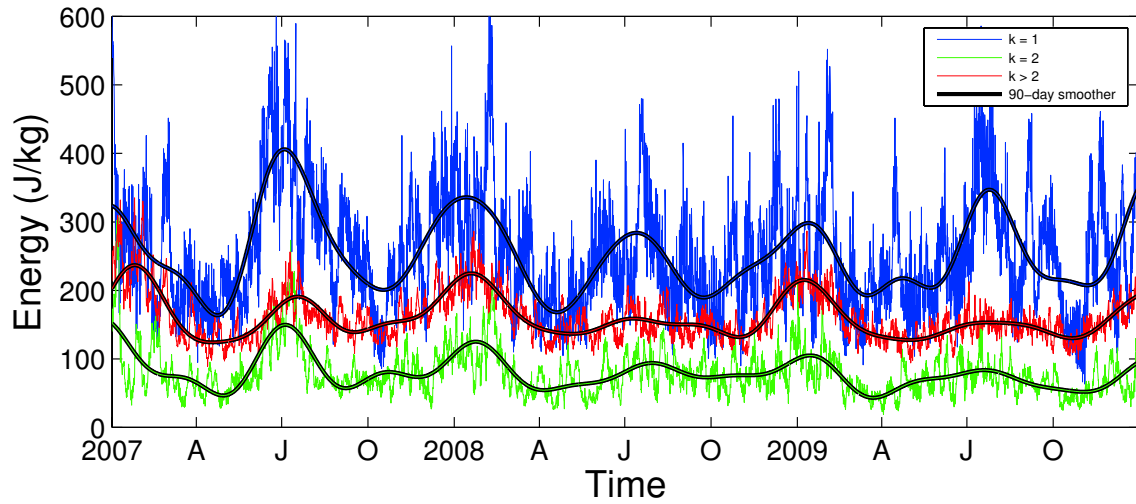
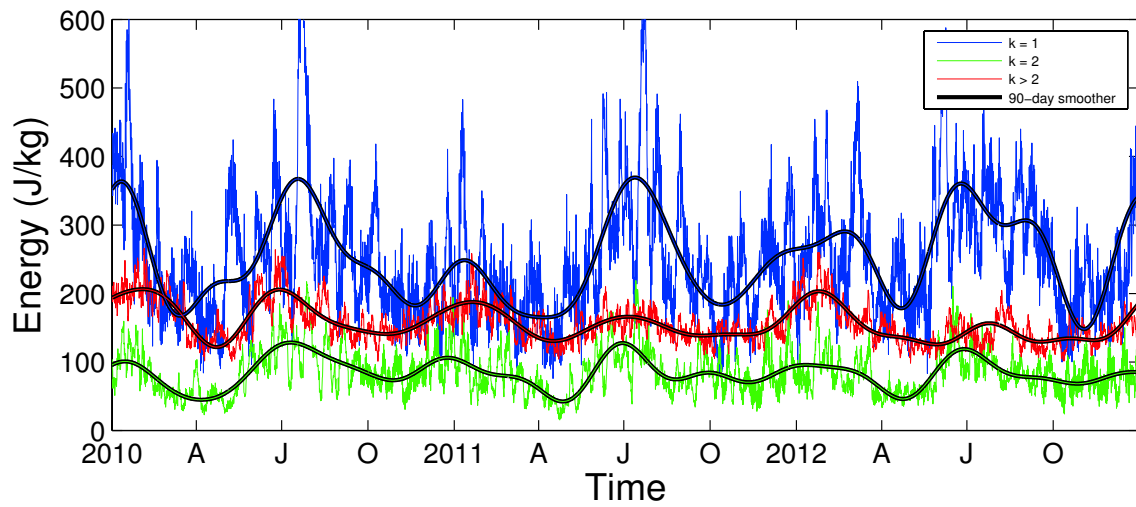


Figure 4. Kelvin wave energy (in Jkg^{-1}) as function of the zonal wavenumber k for $k = 1 - 6$. For each k , seasonal averages are shown along with the total average as described by the legend. Energy is vertically integrated over 60 vertical modes. Further details are in the text.



(a) 2007 – 2009



(b) 2010 – 2012

Figure 5. Timeseries of the global total KW energy for various zonal wavenumbers over the following periods: (a) 2007 – 2009 and (b) 2010 – 2012. Labels on the x-axis 'A', 'J' and 'O' refer to the first days of April, July and October, respectively. Presented are the zonal wavenumbers $k = 1$ (blue line), $k = 2$ (green line) and all smaller zonal scales, $k > 2$ (red line). A 90-day low-pass filter has been applied (black lines) for each time series in order to filter out high-frequency variability and to highlight seasonal variability.

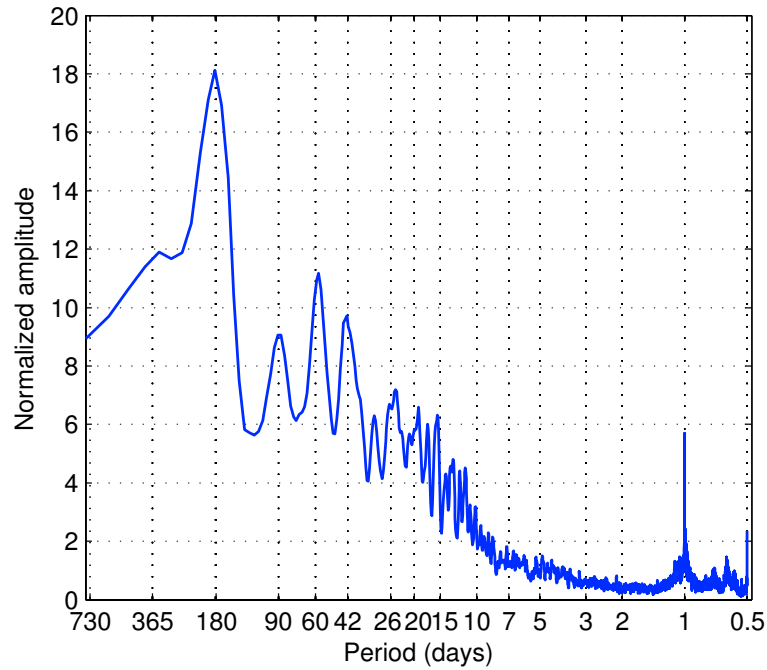


Figure 6. Kelvin wave frequency spectrum for the zonal wavenumber $k = 1$. The 1-2-1 filter with a Daniell kernel has been used to smooth the initial raw power spectra.

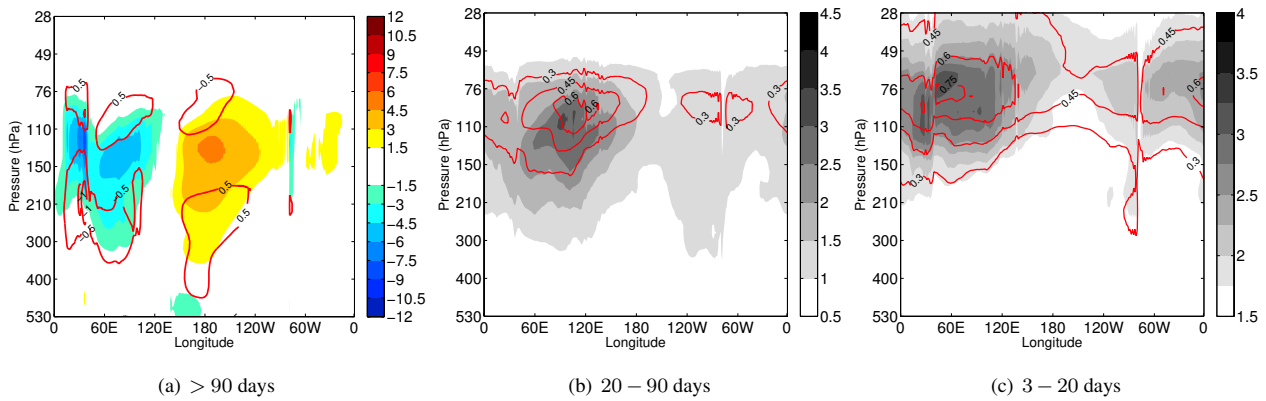


Figure 7. Longitude-pressure sections along 0.7°N of the KW zonal wind and temperature averaged over the 6-year period for: (a) low-frequency, (b) intraseasonal, and (c) intramonthly periods. The contouring is as follows: (a) zonal wind is coloured each 1.5 ms^{-1} and temperature is shown by red contours each 0.5 K , with zero lines omitted, (b) absolute amplitudes of the zonal wind and temperature are shown in grey shades each 0.5 ms^{-1} and red contours, each 0.15 K , respectively, and (c) absolute amplitudes of the zonal wind are in grey shades each 0.25 ms^{-1} and of temperature in red contours each 0.15 K .

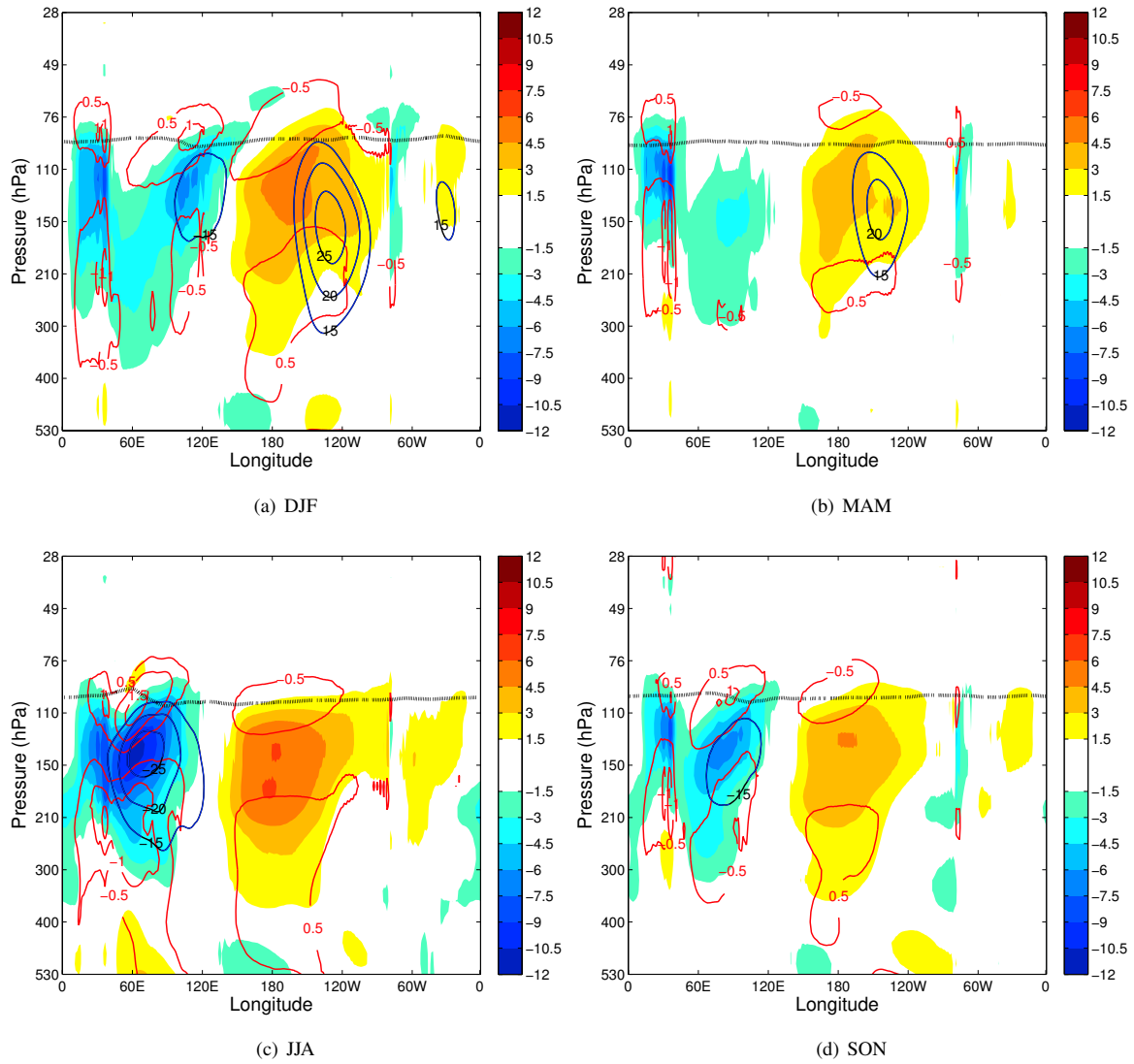


Figure 8. Seasonally averaged longitude-pressure sections of the Kelvin wave zonal wind (blue-to-red colour-filled contours) and temperature (red contours) along 0.7°N . (a) DJF, (b) MAM, (c) JJA and (d) SON. Contouring of the KW signal is the same as in Fig. 7(a). A single static stability contour with value $5 \times 10^{-4} \text{ s}^{-2}$ is shown as a thick dotted black line to represent the seasonal movement of the tropical tropopause height. The average background zonal wind is shown by blue contours (each 5 ms^{-1} , starting from 15 ms^{-1}). The background zonal wind and stability fields are latitudinally-averaged over 5°S - 5°N . All fields are smoothed using a low-pass filter with the cut-off period of 90 days.

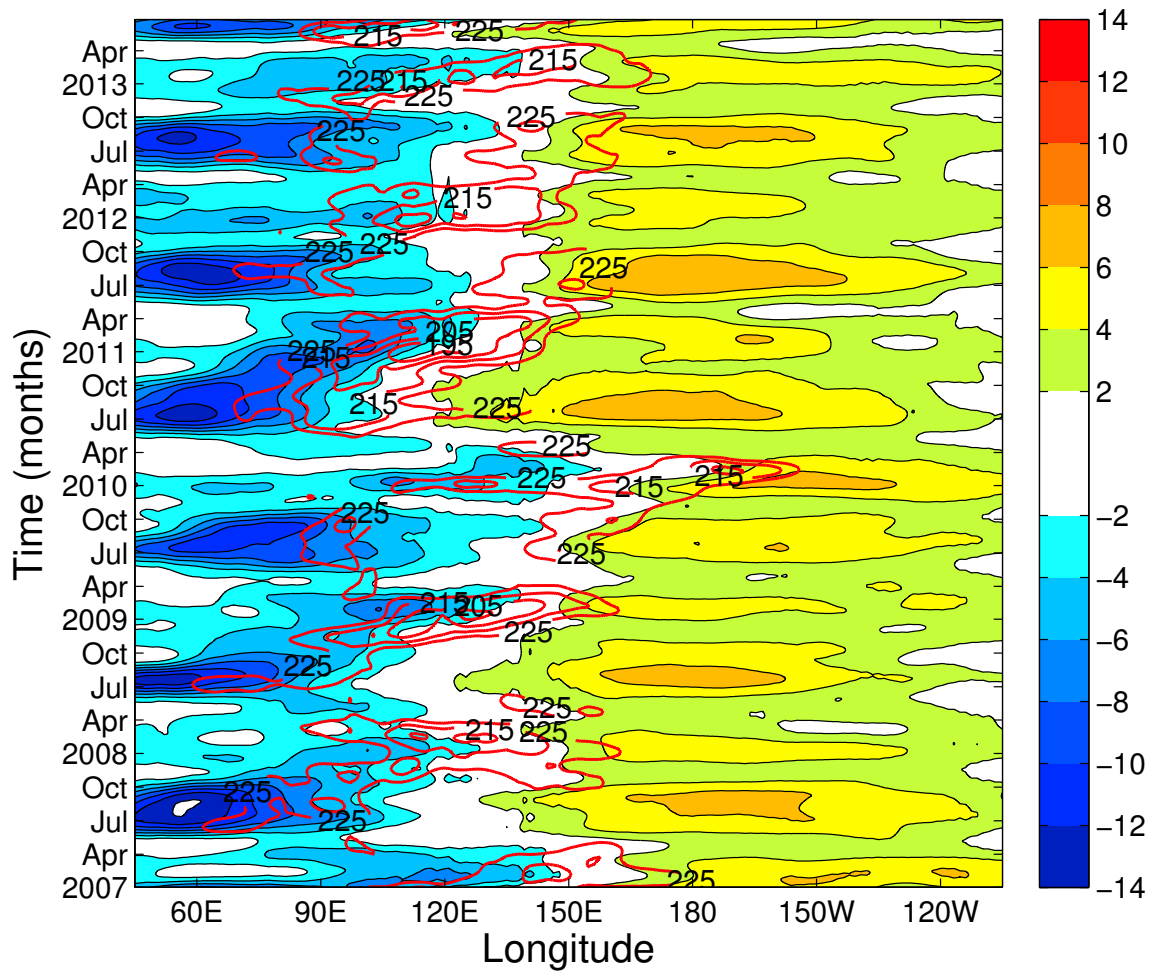


Figure 9. Longitude-time section at model level 45 (~ 153 hPa) of the Kelvin wave zonal wind along 0.7°N (blue to red shaded contours every 2 ms^{-1} with zero line omitted) and the Outgoing Longwave Radiation averaged over the latitude belt 15°S - 15°N (red contours each 10 Wm^{-2} starting at 225 Wm^{-2}). Both fields have been filtered a priori using a low-pass filter with the cut-off period of 90 days.

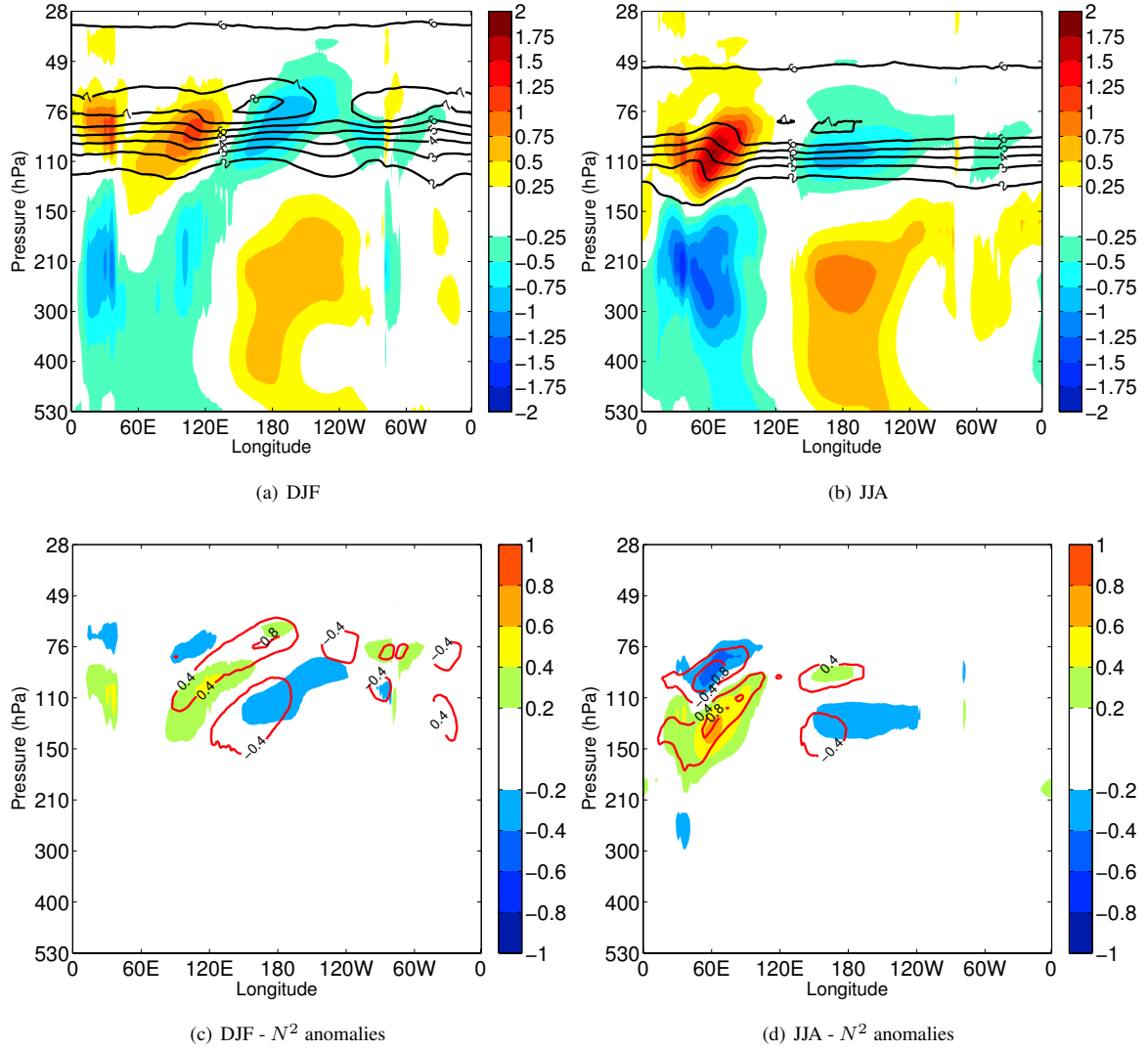


Figure 10. Seasonally averaged longitude-pressure sections for (a and c) DJF and (b and d) JJA. (a-b) KW temperature, $\overline{T_{kw}}^s$, (blue-to-red shades every 0.25 K) and static stability field, $\overline{N^2}^s$ (black contours, each $1 \times 10^{-4} \text{ s}^{-2}$, starting at $2 \times 10^{-4} \text{ s}^{-2}$). (c-d) KW static stability anomaly, $\overline{N_{kw}^2}^s$ (blue-to-red, each $0.2 \times 10^{-4} \text{ s}^{-2}$), and static stability anomaly with respect to the zonal mean, $\overline{N^2}^s$ (red contours, each $0.4 \times 10^{-4} \text{ s}^{-2}$).

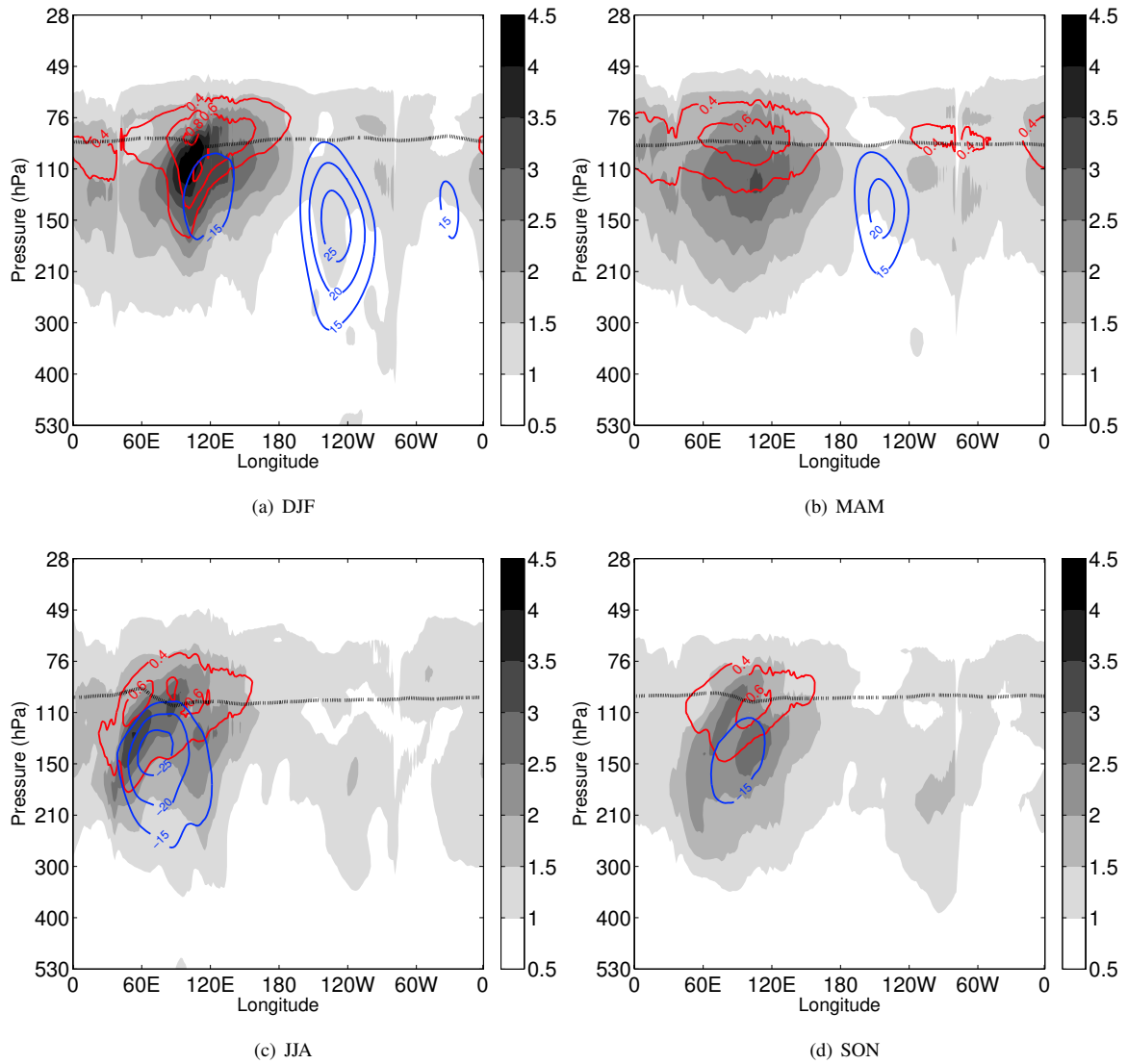


Figure 11. Seasonally averaged longitude-pressure sections along 0.7°N of the intraseasonal Kelvin wave zonal wind (white-to-black shades, each 0.5 ms^{-1}) and temperature (red contours, each 0.2 K). (a) DJF, (b) MAM, (c) JJA and (d) SON. The averaging is performed for the absolute values of both zonal wind and temperature perturbations. The background zonal wind (shown by blue contours) and the tropical tropopause height (single thick dotted contour) are defined as in Fig. 8.

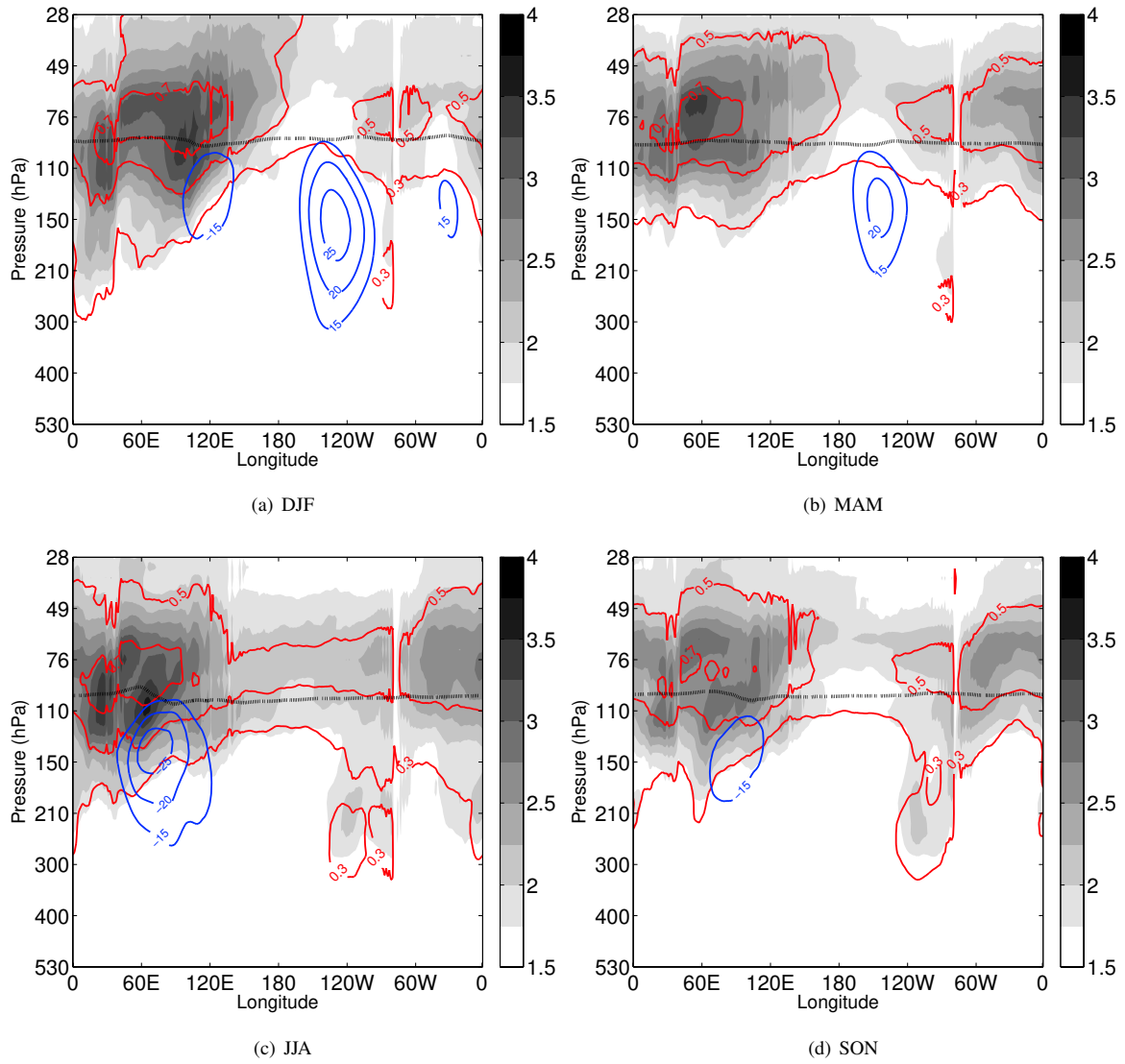


Figure 12. As in Fig. 11 but for the intramonthly Kelvin waves. The zonal wind (white-to-black shades) is drawn every 0.25 ms^{-1} .

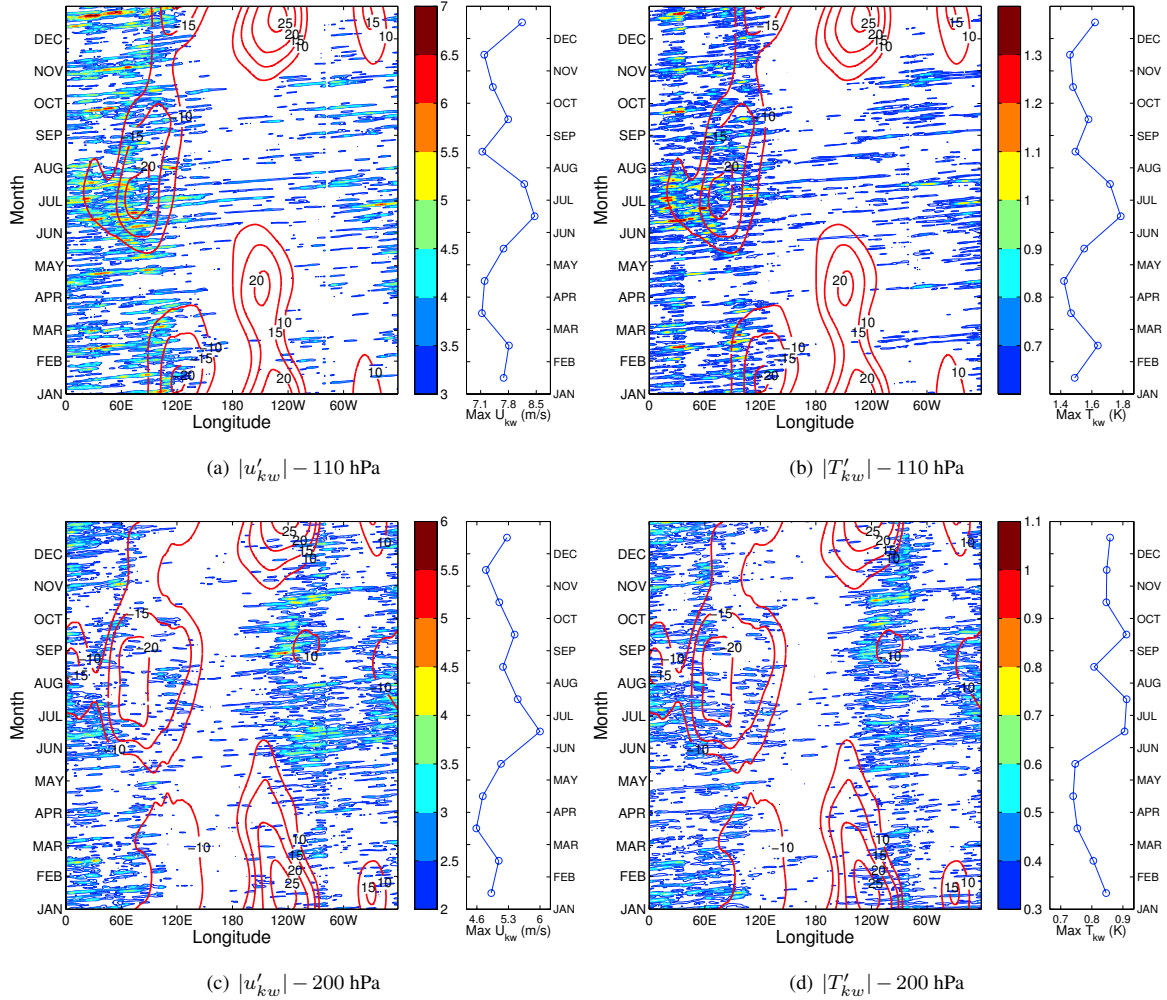


Figure 13. Intramonthly Kelvin wave zonal wind and temperature composites as a function of longitude and month in a calendar year at (a-b) model level 40 (~ 110 hPa) and (c-d) model level 49 (~ 200 hPa) along 0.7°N . The waves are accumulated from different years onto a single calendar year to highlight seasonal behaviour. Only the most energetic signals are shown: (a and c) zonal wind, $|u'_{kw}|$, each 0.5 ms^{-1} , and (b and d) temperature $|T'_{kw}|$, each 0.1 K . For comparison, the background zonal wind field is presented by red contours, each 5 ms^{-1} . On the right side of each panel, blue lines with circles denote maximal amplitude of the KW zonal wind occurring anywhere along the equator averaged over the 6-year period for each calendar month. This highlights seasonality in the maximum amplification of propagating KWs.

Multivariate analysis of Kelvin wave seasonal variability in ECMWF L91 analyses

Marten Blaauw ¹ and Nedjeljka Žagar ¹

¹University of Ljubljana, Faculty of mathematics and physics, Ljubljana, Slovenia

Correspondence to: Marten Blaauw (marten.blaauw@fmf.uni-lj.si)

1 **Abstract.** ~~The paper presents the seasonal variability of~~

2 ~~The paper performs multivariate analysis of the linear~~ Kelvin waves (KWs) ~~represented by the operational 91-level ECMWF~~
3 ~~analyses in 2007-2013 ECMWF analyses on 91 model levels. The waves are filtered using the normal-mode function decomposition~~
4 ~~which simultaneously analyses wind and mass field based on their relationships from linear wave theory. Both spectral as well~~
5 ~~as spatiotemporal features of the KWs are examined in terms of their seasonal variability in comparison with background wind~~
6 ~~and stability. Furthermore, a differentiation is made using spectral bandpass filtering between the slow horizontal barotropic~~
7 ~~KW response and the fast vertical projection response observed as vertically-propagating KWs~~ 2007-2013 period, with focus
8 ~~on seasonal variability. The applied method simultaneously filters Kelvin wave wind and temperature perturbations in the~~
9 ~~continuously stratified atmosphere on the sphere. The spatial filtering of the three-dimensional Kelvin wave structure in the~~
10 ~~upper troposphere and lower stratosphere is based on the Hough harmonics using several tens of linearized shallow-water~~
11 ~~equation systems on the sphere with equivalent depths ranging from 10 km to a few meters.~~

12 Results ~~show~~ provide the global Kelvin wave energy spectrum. It shows a clear seasonal cycle in KW activity which is
13 ~~predominantly at the largest zonal scales (wavenumber 1-2) with the Kelvin wave activity predominantly in zonal wavenumbers~~
14 ~~1 – 2~~ where up to 50% more energy is observed during the solstice seasons in comparison with boreal spring and autumn. ~~The~~
15 ~~spatiotemporal structure of the KW reveals the slow response as a robust "Gill-type" structure~~

16 ~~Seasonal variability of Kelvin waves in the upper troposphere and lower stratosphere is examined in relation to the background~~
17 ~~wind and stability. A spectral bandpass filtering is used to decompose variability into three period ranges: seasonal, intraseasonal~~
18 ~~and intramonthly variability component. Results reveal a slow seasonal KW component with a robust dipole structure in the~~
19 ~~upper troposphere~~ with its position determined by the location of the dominant convective outflow winds throughout the
20 seasons. Its ~~maximum~~ maximal strength occurs during northern boreal summer when easterlies in the Eastern Hemisphere
21 ~~hemisphere~~ are strongest. ~~The fast response in the form of free traveling KWs occur~~ Other two components represent vertically
22 ~~propagating Kelvin waves and are observed~~ throughout the year with seasonal variability mostly found in the wave amplitudes
23 being dependent on ~~the seasonality of the~~ background easterly winds and static stability.

24 1 Introduction

25 Atmospheric equatorial Kelvin waves (hereafter KWs), first discovered in the stratosphere (Wallace and Kousky, 1968), are
26 nowadays observed and studied over a broad range of spatial and temporal scales. A broad wavenumber-frequency spectrum
27 can be traced to the spatiotemporal nature of tropical convection which generates KWs along with a spectrum of other equa-
28 torial waves. Atmospheric wave response to the stochastic nature of convection was studied by Garcia and Salby (1987) and
29 Salby and Garcia (1987) who made a distinction between (i) projection or vertical response to short-term heating fluctuations
30 (e.g. daily convection) and (ii) barotropic or horizontal response to seasonal convective heating. For KWs, the vertical response
31 gives rise to a broad frequency spectrum of vertically propagating KWs that radiate outward into the stratosphere where they
32 drive zonal-mean quasi-periodic flows such as the quasi-biennial oscillation (QBO, Holton and Lindzen, 1972). The horizontal
33 response to seasonal transitions in convective heating gives rise to planetary-scale disturbances with a half-sinusoidal vertical
34 structure confined to the troposphere. A part of this response remains stationary over the convective hotspot; its shape resem-
35 bling a classic "Gill-type" KW solution (Gill, 1980). The other part of the response intensifies and advances over the Pacific,
36 representing a transient component of the Walker circulation (Salby and Garcia, 1987).

37 Both components of the KW response received increased attention in the scientific community over the last decades in terms
38 of the role they play in the (intra)seasonal variability of the Tropical Tropopause Layer (hereafter TTL), defined as a transition
39 layer between the typical level of convective outflow at ~ 12 km where the Brunt-Väisälä frequency is at its minimum, and the
40 cold point tropopause at ~ 16 - 17 km (Highwood and Hoskins, 1998; Fueglistaler et al., 2009)(Highwood and Hoskins, 1998; Fueglistaler e
41 Within the TTL, temperature variations play an important role in controlling the stratosphere-troposphere exchange of vari-
42 ous species such as ozone and water vapour thereby aiding in the dehydration process of air entering the stratosphere. The
43 two parts of the KW response ~~alternate~~ modulate the TTL differently on different time scales (Highwood and Hoskins, 1998;
44 Randel and Wu, 2005; Ryu et al., 2008; Flannaghan and Fueglistaler, 2013); their relative contribution to TTL dynamics varies
45 with season and is not yet fully understood. The present study contributes to this topic by applying a novel multivariate analysis
46 of Kelvin wave seasonal variability in model-level analysis data.

47 Seasonal variations of Kelvin wave dynamics in the TTL have been previously studied using temperature data derived
48 from satellites such as SABER (Sounding of the Atmosphere using Broadband Emission Radiometry, Garcia et al., 2005;
49 Ern et al., 2008; Ern and Preusse, 2009), HIRDLS (High Resolution Dynamics Limb Sounder, Alexander and Ortland, 2010),
50 and GPS-RO (Global Positioning System Radio Occultation, Tsai et al., 2004; Randel and Wu, 2005; Ratnam et al., 2006).
51 For example, Alexander and Ortland (2010) reported a clear seasonal cycle around 16-17 km (~ 100 hPa) in KW temperature
52 observed by HIRDLS, coinciding closely with variations in background stability. A widely used method for the KW filtering
53 from gridded data is the space-time spectral analysis introduced by Hayashi (1982). ~~It~~ Space-time spectral filtering assumes
54 that the linear adiabatic theory for equatorial waves on a resting atmosphere is applicable (Gill, 1982). Filtering operates on
55 single variable data and it has been widely used to diagnose equatorial waves in the outgoing longwave radiation (OLR, e.g.
56 Wheeler and Kiladis, 1999) and climate model outputs (e.g. Lin and Coauthors, 2006). Based on 40-year ECMWF reanalysis
57 (ERA-40) data, Suzuki and Shiotani (2008) found that the temperature component of Kelvin waves tends to peak at 70 hPa

58 while the zonal wind peaks at lower altitudes, i.e. at 100 hPa (and 150 hPa) in Eastern (Western) hemisphere in Eastern and
 59 Western hemisphere, respectively.

60 The zonal wind and geopotential height of the KW are closely related. For a single zonal wavenumber k , the geopotential,
 61 Φ_{kw} , and the zonal wind U_{kw} of a zonally propagating KW are related according to the following equation: On the equatorial
 62 β -plane, shallow-water linear wave theory describes the Kelvin wave geopotential height (h_{kw}) and zonal wind (u_{kw}) perturbations
 63 propagating zonally with phase speed c as (Matsumo, 1966):

$$64 \quad \Phi_{kw} = g h_{kw}(x, y) = \frac{\nu}{k} \frac{c}{g} U_{kw}, \quad \text{where} \quad U_{kw}(x, y) = U_0 \exp\left(-\frac{\beta k y^2}{2\nu} - \frac{\beta y^2}{2c}\right) \cos k(x - ct). \quad (1)$$

65 Here, U_0 is the KW amplitude in zonal wind on u_0 is the zonal wind amplitude at the equator, $\beta = 2\Omega/a$ (Ω being the
 66 rotation rate and a the radius of Earth), ν is the wave frequency, g is gravity and y is the distance from the equator.
 67 These expressions are obtained as a special solution of the linearized shallow-water equations on the equatorial β -plane
 68 (e.g. Holton, 2004, Chapter 11). The $\beta = df/dy$, f being the Coriolis parameter. The dispersion relationship between the
 69 wave frequency ν and the zonal wavenumber k is $\nu = kc$. The gravity wave speed in a layer of homogeneous fluid with mean
 70 depth D is given by $c = \sqrt{gD}$ (Gill, 1982).

71 The KW e -folding decay width, a_e , known as the equatorial radius of deformation, is given by $a_e = (c/2\beta)^{1/2}$, where
 72 the KW phase speed c is determined from the dispersion relation $\nu = kc$. By prescribing the value of KW phase speed c (i.e.
 73 the equivalent depth of the shallow-water equation system), analytical solutions from linear wave theory D , the horizontal
 74 structure of KW is defined by (1) for any k and can be used to simultaneously analyze wind and height data of the KW wave
 75 geopotential height perturbations due to KW waves on a single horizontal level. Such multivariate analysis was carried out
 76 by Tindall et al. (2006) who analyzed several levels the ECMWF 15-year reanalysis dataset (for the lower stratosphere for
 77 the ERA-15) in the lower stratosphere. They reported a maximum of Kelvin wave activity at 100 hPa around the solstices
 78 when tropical cloud activity maximizes. For the ERA-15 data in 1981-93 period, their Kelvin wave analysis explained. Their
 79 results suggested that KWs contributes approximately 1 K² of the temperature variance on the equator with peak activity
 80 occurring during solstice seasons at 100 hPa, during December-February at 70 hPa and at 50 hPa it occurs during the
 81 easterly to westerly quasi-biennial oscillation (QBO) phase transition. Yang et al. (2003) used a_e as the fitting parameter for
 82 the projection of the ERA-15 data on the meridional structure of the KW and other equatorial waves. They found that the best
 83 fit trapping scale within 20°N-20°S is around 6°. The multivariate projection of data on the horizontal structures of equatorial
 84 waves including KWs on the equatorial β -plane was performed also for the short-range forecast errors of the ECWMF model
 85 (Žagar et al., 2005, 2007). For example, Žagar et al. (2007) found that forecast errors within 20°N-20°S belt project on KWs
 86 significantly more in the easterly QBO phase than in the westerly phase.

87 The present paper extends the use of linear wave theory from In this paper we extend the linear Kelvin wave analysis based
 88 on the shallow-water equation theory on the equatorial β -plane to the sphere. Second, we extend the KW filtering on individual
 89 horizontal levels or vertical planes to the three-dimensional (3D) spherical coordinates in order to analyze KW analysis
 90 simultaneously in wind and temperature fields in recent ECMWF operational analyses. We focus on. This study thus explores
 91 seasonal variability of KWs in the TTL layer in the ECMWF operational analyses during a period when the model employed

92 91-vertical level (L91) between the surface and 1 Pa. The L91 model was in operations between 2006 and early summer 2013
93 when it was replaced by 137 levels. This study thus explores most of a multivariate fashion using most of the information
94 on the vertical structure of KWs available in the L91 analysis data. We present a methodology for the simultaneous analysis
95 of wind and temperature perturbations associated with KWs with respect to the background state and apply it to quantify
96 scale-dependent seasonal KW variability in several frequency bands. wave structure available in recent operational ECMWF
97 analyses.

98 The paper consists of five sections. Methodology On the sphere, the Kelvin mode is the slowest eastward-propagating
99 eigensolution of the shallow-water equations (or Laplace tidal equations) linearized around a state of rest (e.g. Kasahara, 1976).
100 In the continuously stratified atmosphere, the depth D becomes the "equivalent depth" of a given baroclinic mode and we need
101 to solve Laplace tidal equations for a range of D from large (corresponding to the barotropic structure) to rather small (for
102 high baroclinic modes) in order to consider the spectrum of Kelvin waves (e.g. Boyd, 2018). In contrast to the Kelvin wave
103 trapping on the equatorial β -plane, which is controlled by a_e i.e. by the equivalent depth, the degree of the KW diagnosis
104 and the data are presented in section 2 equatorial confinement on the sphere is in addition controlled by the zonal wavenumber
105 (Boyd and Zhou, 2008). As shown by Boyd and Zhou (2008), even barotropic KW with D around 10 km are on the sphere
106 confined within the tropical belt.

107 In section 2 we present a methodology which diagnosis 3D Kelvin waves in spherical datasets. Section 3 presents the
108 KW energetics in wavenumber space focusing on the seasonal cycle. Section 4 presents a 3D view on KWs in L91 dataset,
109 seasonal KW variability in several frequency bands both for the horizontal as well as for the vertical projection KW response.
110 Conclusions and outlook are given in section 5.

111 2 Data and methodology

112 The Kelvin waves are filtered using the Normal-Mode-Function-normal-mode function (NMF) decomposition derived by
113 Kasahara and Puri (1981) and briefly summarized below, formulated as the *MODES* software package by Žagar et al. (2015).
114 Here the methodology is briefly summarized followed by the method for the computation of the KW temperature perturbations
115 and by examples of the 3D KW structure in global data.

116 Input ECMWF operational analyses cover 6 covers approximately 6.5 years from January 2007 till June 2013, approximately
117 6.5 years, untill June 2013. The dataset starts after two important updates in the ECMWF assimilation cycle: a resolution update
118 on 1 February 2006 and the introduction of GPS-RO temperature profiles in the assimilation on 12 December 2006. The data
119 ends at the next update in vertical resolution from L91 to L137 on 25 June 2013. The data horizontal resolution is 256×128
120 points in the zonal and meridional directions (regular Gaussian grid N64), respectively, on 91 irregularly spaced hybrid model
121 levels up to around 0.01 hPa (around 80 km). The temporal resolution is 6 hours, i.e. 4 times per day, at 00, 06, 12 and 18 UTC.
122 A case study of the large-scale KW in July 2007 (Žagar et al., 2009) showed how in this dataset by Žagar et al. (2009) showed
123 that the NMF method provides information on the horizontal and vertical 3D wave structure and its vertical propagation in the

124 stratosphere. [Another case study from the same month demonstrated how the vertical KW structure improves as the number of](#)
 125 [vertical levels increased \(Žagar et al., 2012\).](#)

126 2.1 Filtering of Kelvin waves by 3D normal-mode function expansion

127 The basic assumption behind the NMF expansion is that a global state of the atmosphere described by its mass and wind vari-
 128 ables at any time can be considered as a superposition of the linear wave solutions upon a predefined background state. ~~These~~
 129 ~~linear solutions describe two types of wave motions: Rossby waves and inertio-gravity waves which obey their corresponding~~
 130 ~~dispersion relationships. The associated eigensolutions in terms of the Hough harmonics define both mass and wind fields of~~
 131 ~~the waves. The linear wave theory approach has been successfully employed in many studies, especially for the large-scale~~
 132 ~~tropical circulation features (e.g. Gill, 1980; Salby and Garcia, 1987; Garcia and Salby, 1987)-~~

133 The NMF decomposition derived by Kasahara and Puri (1981) uses the σ ~~coordinates and a vertical coordinate and linearization~~
 134 ~~around the state of rest and~~ realistic vertical temperature and stability stratification. 3D wave solutions of ~~primitive equations~~
 135 ~~linearized around the state of rest~~ [linearized primitive equations](#) are represented as a truncated time ~~serie series~~
 136 harmonic oscillations and the vertical structure functions. The [assumption of separability leads to separate equations for the](#)
 137 [vertical structure and horizontal oscillations. The latter are known as shallow-water equations on the sphere or Laplace tidal](#)
 138 [equations without forcing. The two systems are coupled by a separation parameter \$D\$ which is called the equivalent height](#)
 139 [\(Boyd, 2018\). Eigenmodes of the global shallow-water equations are known as Hough harmonics. They describe two types of](#)
 140 [wave motions: Rossby waves and inertio-gravity waves which obey their corresponding dispersion relationships on the sphere.](#)

141
 142 [The expansion of a global input data vector \$\mathbf{X}\(\lambda, \varphi, \sigma\) = \(u, v, h\)^T\$ can be represented by a discrete finite series as:](#)

$$143 \begin{pmatrix} u(\lambda, \varphi, \sigma) \\ v(\lambda, \varphi, \sigma) \\ h(\lambda, \varphi, \sigma) \end{pmatrix} = \sum_{m=1}^M \mathbf{S}_m \left[\sum_{n=1}^R \sum_{k=-K}^K \chi_n^k(m) \mathbf{H}_n^k(\lambda, \varphi; m) \right] G_m(\sigma) \quad (2)$$

144 The [input data vector contains wind components \$u, v\$ and the transformed geopotential height \$h\$ defined as \$h = g^{-1}P\$ where](#)
 145 [\$g\$ is the gravity and \$P\$ is defined as: \$P = \Phi + RT_0 \ln\(p_s\)\$; that it, it is the sum of geopotential \$\Phi\$ and a surface pressure, \$p_s\$, term.](#)
 146 [Other two variables represent the specific gas constant for dry air \(\$R\$ \) and the globally-averaged vertical temperature profile](#)
 147 [\(\$T_0\(\sigma\)\$ \). The zonal and vertical truncations \(\$K\$ and \$M\$, respectively\) define ~~maximum maximal~~ numbers of zonal waves at a
 148 single latitude \(wavenumber \$k\$ \) and a maximal number of vertical modes ~~denoted \$m\$ respectively.~~ \(denoted \$m\$ \) respectively. For
 149 \[every vertical structure eigenfunctions \\$G_m\\(\sigma\\)\\$, Hough harmonic functions, \\$\mathbf{H}_n^k\\(\lambda, \varphi\\)\\$ describe non-dimensional oscillations in\]\(#\)
 150 \[the horizontal plane of the fluid with the mean depth equal the equivalent depth \\$D_m\\$. The parameter \\$D_m\\$ appears in Eq. \\(2\\) in\]\(#\)
 151 \[the diagonal matrix \\$\mathbf{S}_m\\$ with elements \\$\\(gD_m\\)^{1/2}\\$, \\$\\(gD_m\\)^{1/2}\\$ and \\$D_m\\$ which normalizes the input data vector after the vertical\]\(#\)
 152 \[projection and thereby removes dimensions.\]\(#\) Parameter \$R\$ is the total number of meridional modes which is a sum of the
 153 eastward inertio-gravity waves \(EIG\), westward inertio-gravity waves \(WIG\) and Rossby waves. ~~Oscillations in the horizontal~~
 154 ~~plane are given in terms of Hough harmonic functions, \$\mathbf{H}_n^k\(\lambda, \varphi\)\$ for every vertical structure eigenfunctions \$G_m\(\sigma\)\$. The~~](#)

155 horizontal and vertical solutions are connected by the equivalent depth parameter D_m , which appears in Eq. (2) in the diagonal
 156 matrix \mathbf{S}_m with elements $(gD_m)^{1/2}$, $(gD_m)^{1/2}$ and D_m . Linearization about the state of rest is not a drawback of the method as
 157 wave frequencies are used solely for the formulation of the projection basis and not for studying wave propagation properties.
 158 As shown by Kasahara (1980) (see also its Corrigendum) the meridional structures of the Hough functions for large scales are
 159 not significantly different if the linearization is performed around the non-zero mean zonal flow. The impact of latitudinal shear
 160 on the Kelvin waves was shown negligible by Boyd (1978). Further details of the applied NMF representation NMF projection
 161 procedure are given in Žagar et al. (2015).

162 The input data vector contains wind components u, v and the geopotential height h defined as $h = g^{-1}P$ where g is the
 163 gravity and P is a modified geopotential given by: $P = \Phi + RT_0 \ln(p_s)$, i. e. the sum of the geopotential field Φ and a
 164 surface pressure p_s term. Other two variables represent the specific gas constant for dry air (R) and the globally-averaged
 165 vertical temperature profile (T_0). The For each zonal wavenumber, the Kelvin mode is the lowest eastward-propagating
 166 latitudinal Hough function. In (2), the Kelvin wave is represented by the nondimensional complex expansion coefficients
 167 $\chi_n^k(m)$ represent both geopotential height and wind perturbations due to waves. The Kelvin mode is represented in (2) by
 168 the first eastward-propagating IG mode. Although our meridional index starts from 1 (to follow otherwise used notation) with
 169 the meridional index $n = 1$. However, to follow often used notation, we shall denote KW in the remainder the Kelvin wave
 170 in the remainder of this study as the $n = 0$ EIG mode, i.e. the KWs are given Kelvin wave wind and geopotential height are
 171 represented by coefficients $\chi_{kw} = \chi_0^k(m)$.

172 In our application to the L91 ECMWF dataset, we used data on the N64 Gaussian grid and 91 model levels with model
 173 top located at 0.01 hPa (around 80 km). Data are analyzed 4 times per day, at 00, 06, 12 and 18 UTC. The pre-processing
 174 step consists of the interpolation of winds and geopotential from the hybrid ($\sigma-p$) levels to σ levels after geopotential Φ
 175 is computed on the hybrid levels. The The truncation values are $K = 55$ $K = 85$ and $M = 60$. This means that KW signal
 176 in 3D circulation at a single time instant consists of 5100 waves, 85 waves in every shallow-water equation system. Higher
 177 vertical modes were left out as their contribution equivalent depth is smaller than 2 meters and their contribution to the total
 178 KW signal is negligible in the outputs in the TTL and the stratosphere. The relation between the truncation parameters and the
 179 normal-mode projection quality is discussed in Žagar et al. (2015) and references therein.

180 Once the forward projection is carried out and coefficients $\chi_n^k(m)$ are produced, filtering of KWs in physical space can be
 181 performed through (2) after setting all χ , except those representing the KWs, to zero. The result of filtering are fields u_{kw} ,
 182 v_{kw} and h_{kw} which provide the KW zonal wind, meridional wind and geopotential height perturbations. Notice here that in
 183 contrast to the equatorial β -plane, KWs on the sphere have a very small meridional wind component which is thus left out
 184 from the discussion (Boyd, 2018).

185 The KW temperature perturbation, T_{kw} can be derived from the h_{kw} fields on σ levels using the hydrostatic relation in σ
 186 coordinates:

$$187 \quad T_{kw} = -\frac{g\sigma}{R} \frac{\partial h_{kw}}{\partial \sigma}. \quad (3)$$

188 The orthogonality of the normal-mode basis functions provides KW energy as a function of the zonal wavenumber and
 189 vertical mode. After the forward projection, the energy spectrum of total (potential and kinetic) energy for each Kelvin wave
 190 can be computed using the energy product for the k th and m th normal modes (Žagar et al., 2015) as:

$$191 \quad I_{\text{kw}}(k, m) = \frac{1}{2} g D_m \chi_{kw} [\chi_{kw}]^* . \quad (4)$$

192 The units are J kg^{-1} . The KW global energy spectrum as a function of the zonal wavenumber is obtained by summing energy
 193 in all vertical modes:

$$194 \quad I_{\text{kw}}(k) = \frac{1}{2} \sum_{m=1}^M g D_m \chi_{kw} [\chi_{kw}]^* . \quad (5)$$

195 2.2 Examples of 3D structure of Kelvin waves in L91 analyses

196 Kelvin waves are shown in Fig. 1-2 for a few days in July 2010 to introduce and illustrate their properties as filtered by the
 197 NMF methodology. ~~The second part of July 2010 was characterized by an abundance in both vertically propagating as well as~~
 198 ~~quasi-stationary KW structures throughout the atmosphere.~~

199 Figure 1 illustrates the meridional structure of Kelvin waves on 25 July 2010 on 2 levels. KW activity was found largest in
 200 the zonal wind component at 150 hPa over the Indian Ocean. The geopotential dipole structure is ~~centered-centred~~ over the
 201 convective hotspot over the Maritime continent. At 100 hPa, we find largest amplitude of KW temperature perturbations up to
 202 4 K positioned above the zonal wind maxima at 150 hPa. The meridional wind component of the KW is nonzero in spherical
 203 coordinates, but is at most 0.22 ms^{-1} at 100 hPa which is negligible compared to the zonal wind component (maximum 12.5
 204 ms^{-1}) making the KW wind field primarily zonal. Note that the presented horizontal structure at a single level is a superposition
 205 of 60 vertical modes, i.e. 60 shallow water models with equivalent ~~depts-depths~~ from about 10 km to a couple of meters.

206 Figure 2 ~~can be discussed in relation to Eq. . It states that the amplitude of the cold (warm) KW temperature perturbation~~
 207 ~~is proportional to the negative (positive) vertical gradient in geopotential, as well as in zonal wind since zonal wind and~~
 208 ~~geopotential components are in phase. Horizontally, the cold anomaly is always located between the westerly and the easterly~~
 209 ~~phase of the zonal wave component. Vertically, maximum positive temperatures are observed between easterly winds below and~~
 210 ~~westerly winds above. A rough estimation can be made of the vertical wavelength based on alternating zonal wind minima and~~
 211 ~~maxima. For example, on 31 July a quasi-stationary vertical wave structure with extension in the stratosphere located around~~
 212 ~~60°E has easterly winds located at 50 hPa illustrates day-to-day filtered KW fields along the equator on three separate July days~~
 213 ~~in 2010, namely 25, 28 and 31. Both zonal wind (~ 21.5 km) and 150 hPa (~ 13.5 km), which makes a vertical wavelength~~
 214 ~~of around 8 km. blue-to-red shades) and temperature fields (red contours) are shown. Without any predefined constrains on the~~
 215 ~~KW propagation, one can observe a rich variety of KW behaviour occurring in time: from the quasi-stationary dipole patterns~~
 216 ~~centred at 160 hPa to a wave package of free propagating wave structures in the stratosphere transiting from the western into~~
 217 ~~the eastern hemisphere.~~

218 In the stratosphere, ~~above 80 hPa, strong KW activity was present in the form of free waves propagating the uppermost~~
 219 ~~easterly wind component in blue shades around $30 - 50$ hPa moves in~~ eastward and downward ~~, therefore with direction,~~

220 demonstrating the upward transport of KW energy (Andrews et al., 1987). KW amplitudes were largest over Eastern hemi-
221 sphere with temperatures up to 4 K and zonal winds up to 12 ms⁻¹. The large amount of KW activity occurred during the
222 easterly phase of the QBO with strong easterly winds present between 30 and 80 hPa (not shown), providing favourable con-
223 ditions for ~~the waves to propagate upward~~strong KW activity.

224 Between 100 and 200 hPa during the second half of July, there was low-frequency KW activity present in the form of a
225 stationary and robust "wave-1" pattern with strong KW easterly winds up to 24 ms⁻¹ in Eastern Hemisphere and KW westerly
226 winds up to 10 ms⁻¹ in the Western Hemisphere. The high vertical resolution within the TTL resolves shallow KW structures
227 and a typical slanted structure towards the east in KW easterlies as well. The appearance and strength of horizontal KW
228 response coincides with the presence of strong easterly winds in the TTL in the Eastern Hemisphere during this period (not
229 shown). Figure 2 also shows that below 300 hPa the KW activity decreases and we shall not discuss levels under 300 hPa in
230 the paper.

231 The zonal wind and temperature components are coupled through Eq. (3) which states that the amplitude of the negative
232 KW temperature perturbation is proportional to the negative vertical gradient in geopotential (and vice versa), as well as in the
233 zonal wind since the zonal wind and geopotential are in phase. Horizontally, the cold anomaly is always located between the
234 westerly and the easterly phase of the zonal wind component. Vertically, maximal positive temperatures are observed between
235 easterly winds below and westerly winds above. An estimate of the vertical wavelength can be made based on alternating zonal
236 wind minima and maxima. For example, on 25th July a well-developed KW package extending into the stratosphere moved
237 from the Western into the Eastern hemisphere. A quasi-stationary component of the wave package is observed around 60°E
238 with easterly winds located at 50 hPa (~ 21.5 km) and 150 hPa (~ 13.5 km), implying a vertical wavelength of around 8 km.

239 More examples based on daily basis filtered from the 10-day deterministic forecast of the ECMWF can be found on the
240 MODES website¹.

241 2.3 Other data and impact of the background state

242 In addition to the outputs from modal decomposition, full zonal wind and temperature fields from ECMWF analyses are used
243 to compute the background fields based on the same N64 grid and over the same period (Jan 2007 - Jun 2013). Zonal wind U
244 and static stability N are latitudinally averaged in the belt 5°S-5°N on all model levels to produce their zonal structure.

245 Static stability profiles are estimated through

$$246 N^2 = \frac{g^2}{\Theta} \frac{\partial \Theta}{\partial \phi} \quad (6)$$

247 in units of s⁻² and are defined on hybrid model levels on which the geopotential field ϕ and the potential temperature field Θ
248 are derived a priori from the input data. Both fields are shown in Fig. 3.

249 The zonal wind field has the largest values on average in the TTL around 150 hPa with westerly winds peaking in the Western
250 Hemisphere over the Pacific Ocean and easterly winds peaking in the Eastern ~~Hemisphere~~ hemisphere over the Indian Ocean
251 and Indonesia. It represents a typical time-averaged outflow pattern in response to tropical convection (e.g. Fueglistaler et al.,

¹<http://meteo.fmf.uni-lj.si/MODES/>

252 2009). Throughout the seasons there is a longitudinal shift of this pattern following the convective source which is most clearly
253 observed at 150 hPa. Such seasonal shift is visible up to 100 hPa in Fig. 3(b) where winds are weaker compared to 150 hPa.
254 In northern winter, zonal winds are strongest over Indonesia and [the](#) Eastern Pacific with the zonal wind maxima position and
255 strength similar compared to the longer ERA-40 dataset used by Suzuki and Shiotani (2008). During [northern-boreal](#) summer
256 easterly winds mainly prevail over the Indian Ocean, which is linked to the Indian Monsoon season.

257 At 100 hPa, the static stability illustrates the strongest seasonal cycle with values ranging from near-tropospheric values
258 of $3 \times 10^{-4} \text{ ms}^{-2}$ during northern winter towards stratospheric values of $5 - 6 \times 10^{-4} \text{ ms}^{-2}$ during [northern-boreal](#) summer.
259 Note also the resolved local maxima in static stability at 80 hPa above the warm pools, known as the Tropical Inversion
260 Layer (TIL) and which is possibly wave-driven (Grise et al., 2010; Kedzierski et al., 2016). Figure 3(b) suggests that the TIL
261 descends down to 100 hPa during [the-boreal](#) summer months peaking over Western Pacific, in agreement with the cycle found
262 in GPS-RO observations by Grise et al. (2010).

263 Kelvin waves are subject to wave modulation in changing background environments. Along its trajectory, the potential
264 energy of the KW changes with varying background winds and stability which can be largely described by linear wave theory
265 as long as waves are not near their critical level involving breaking and dissipation (Andrews et al., 1987). For simplification,
266 KW modulation can be examined for the case of pure zonal as well as pure vertical wave propagation based on the wave
267 modulation analysis performed by Ryu et al. (2008). A few key points on their local wave action conservation principle are
268 [summarized-summarised](#) in the following.

269 In the tropical atmosphere, zonal modulation is the dominant process for KWs propagating in the stratosphere and in all
270 non-easterly winds in the TTL. Vertical modulation becomes important in the presence of easterly winds within the TTL.
271 Zonal modulation is found to affect both u_{kw} and T_{kw} components and their amplitudes are proportional to the Doppler-
272 shifted phase speed by $(c - U)^{1/2}$ in case of pure zonal propagation direction. This means that Kelvin waves diminish in
273 amplitude over regions with westerly winds and become more prone to dissipative processes, while amplify over regions with
274 easterly winds². In case of pure vertical modulation, the change in wave potential energy mainly [resonates-fluctuates](#) with the
275 temperature component of the Kelvin wave. Along the rays' vertical path, the waves amplitude is proportional to the Brunt-
276 Väisälä frequency as $\propto N^{3/2}$, and to the Doppler-shifted phase speed as $\propto (c - U)^{-1/2}$, such that N is expected to play a
277 primary role above 120 hPa where its value starts increasing rapidly (see Fig. 3).

278 Alexander and Ortland (2010) showed through wave modulation principles that temporal variations in zonal-mean N indeed
279 are correlated with observed KW amplitudes at 16 km (approx. 100 hPa). A more extensive wave modulation analysis was
280 described by Flannaghan and Fueglistaler (2013) using the full ray tracing equations to demonstrate that zonal winds in the TTL
281 not only modulate Kelvin waves locally, but also create a lasting modulating effect on wave activity through ray convergence
282 in the stratosphere. In particular, the seasonal cycle of the upper tropospheric easterlies (on average located over the western
283 Pacific), that acts as an escape window for Kelvin waves throughout the year and largely explains the longitudinal structure of
284 Kelvin wave zonal wind and temperature climatology.

²Keeping in mind that vertical wave propagation and consequently modulation becomes increasingly important as well wherever easterly winds are strong.

285 We shall present the seasonal variability of tropical convection by using the Outgoing Longwave Radiation (OLR) dataset
286 with daily outputs from the NOAA Interpolated OLR product (Liebmann and Smith, 1996). The OLR product, often used as
287 a proxy for convection, is extracted on a $2.5^\circ \times 2.5^\circ$ grid and interpolated on a N64 grid. Latitudal-Latitudinal averages are
288 derived over larger domain, namely over 15°S - 15°N since organized convection tend to happen more remote from the equator,
289 especially during the summer monsoon season over the Asian continent.

290 3 Kelvin wave energetics

291 We start with ~~an overview of a discussion of the~~ KW energy distribution among ~~the~~ zonal wavenumbers as given by (5),
292 followed by ~~the seasonal cycle of KW energy as a function of zonal wavenumber.~~ seasonal differences.

293 3.1 Energy distribution of Kelvin wave

294 The seasonal cycle in the energy-zonal wavenumber spectra is shown in Fig. 4 after summing up over all vertical modes. On
295 average, energy decreases as the zonal wavenumber increases as typical for atmospheric energy spectra. As we deal with the
296 large scales, we show only the first six zonal wavenumbers with energy values shown separately for the annual mean and the
297 four seasons separately.

298 Figure 4 shows that largest seasonal variations in KW energy are found at the largest zonal scales. For all zonal wavenumbers,
299 above annual-mean energy values are observed during ~~winter and summer seasons while autumn and spring~~ DJF and JJA
300 seasons while SON and MAM are below annual-mean energy. In the zonal wavenumber 1, total KW energy varies between
301 200 Jkg^{-1} in MAM season and somewhat over 300 Jkg^{-1} in JJA. In wavenumber 2, values do not exceed 100 Jkg^{-1} and
302 JJA still contains the largest energy. At higher wavenumbers, DJF season becomes the most energetic. In $k > 4$, total KW
303 energy is under 20 Jkg^{-1} and continue to reduce with k . The slope of the KW energy spectrum is between $-5/3$ and -1 at
304 planetary scales (not shown), similar to the spectra presented in Žagar et al. (2009) for July 2007 data. The ~~summer-JJA~~ summer-JJA spectra
305 has on average the steepest slope compared to other seasons, in particular the ~~winter-DJF~~ winter-DJF spectra. The energy distribution on
306 planetary scales is mainly associated with large-scale tropical circulation established in response to ongoing tropical convection.
307 Therefore, the zonal distribution of tropical convection may likely play a crucial role in explaining ~~winter and summer~~ DJF
308 and JJA season differences of KW energy, which will be explored in next section.

309 3.2 Seasonal cycle of KW energy

310 Figure 5 illustrates more details on the seasonal cycle by showing KW energy time series at the largest scales represented by
311 zonal wavenumbers $k = 1$, $k = 2$ and remaining scales $k > 2$. During most ~~summers~~ JJA seasons and occasionally in ~~winter~~
312 DJF (e.g. 2008) the total amount of KW energy in $k = 1$ can reach up to 600 Jkg^{-1} , or twice the ~~summer-JJA~~ summer-JJA average.
313 The minimum in $k = 1$ KW energy mainly occurs during October ~~month~~ followed by April with values dropping towards
314 100 Jkg^{-1} , or half the ~~autumn-SON~~ autumn-SON average. The temporal pattern in $k = 2$ is similar to the $k = 1$ pattern, but with a less

315 pronounced semiannual cycle with maximum values up to 200 Jkg^{-1} and minimum values towards 30 Jkg^{-1} . On zonal scales
316 $k > 2$, KWs still show a semiannual cycle with highest vertically-integrated values of energy ~~over winter seasons~~ in DJF.

317 In particular, for zonal wavenumber $k = 1$ one can distinguish ~~inter-monthly~~ intermonthly in addition to semiannual vari-
318 ability. ~~Inter-monthly~~ Intermonthly variability is most clearly observed during ~~northern summer~~ JJA, for example in July 2011
319 where one can distinguish six separate peaks of over 400 Jkg^{-1} energy over a period of approximately 90 days resembling
320 an average wave period of about 18 days. These are typical periods for free propagating Kelvin waves as observed in the
321 TTL and lower stratosphere (e.g. Randel and Wu, 2005). Note here again that our KW energy is vertically integrated over the
322 whole model depth. This means that the observed intermonthly variability of KWs appears dominated by the cyclic process of
323 free propagating KWs entering the TTL, amplifying due to changing environmental conditions, followed by wave breaking or
324 dissipation.

325 The dominant scales of temporal variability in KWs are illustrated by a frequency spectrum of $k = 1$ in Fig. 6. The spectrum
326 is produced by ~~a the~~ Fourier transform of energy data time series of 6.5 years ~~to frequency space~~. The resulting power
327 spectrum has been smoothed by taking the Gaussian-shaped moving averages over the raw spectrum by using ~~a the~~ Daniell
328 kernel three times (Shumway and Stoffer, 2010). The spectrum ~~shows a clear~~ contains a peak at 1-day period ~~representing~~
329 ~~tidal variability in KWs~~ associated with the diurnal tide partially projecting on the Kelvin waves. After that, a gradual increase
330 of energy is seen towards the 16-day period with multiple individual periods standing out. For periods longer than 20 days,
331 individual peaks are found close to 25, 43 and 59 days. After that, most KW energy is contained by far in the semiannual cycle.
332 The frequency spectrum provides ~~an a~~ useful starting point for the discussion in the next section when the spatiotemporal
333 patterns of KWs shall be examined in several spectral domains.

334 Returning to Fig. 5, a low-pass filter with 90 day cut-off has been applied on KW energy in order to keep only the two
335 main spectral peaks in Fig. 6. The result is visible as the thicker black line in Fig.5 for all three zonal wavenumber groups. A
336 semiannual cycle for all zonal wavenumbers is evident with most energy observed around January and July, while least energy
337 is observed approximately one month after the equinoxes. During the years 2007, 2010, 2011, and 2012, more $k = 1$ KW
338 energy is observed during ~~summer~~ JJA compared to the follow-up ~~winter~~. ~~The winter~~ DJF season. ~~The DJF~~ of 2009-2010 was
339 for example above average with energy values for $k = 1$ above 350 Jkg^{-1} .

340 The year to year differences can be explained by many coupled factors: ~~-,~~ In general, one expects ~~the~~ vertically-integrated
341 KW activity to increase when background wind conditions become favorable, i.e. in the presence of easterly winds. This
342 occurs in the TTL in relation to strong convective outflow (Garcia and Salby, 1987; Suzuki and Shiotani, 2008; Ryu et al.,
343 2008; Flannaghan and Fueglistaler, 2013) during ~~winter and summer~~ DJF and JJA seasons mainly. Moreover, ~~one can expect~~
344 ~~enhanced KW activity whenever the easterly QBO cycle is present in the~~ KW activity is enhanced whenever easterly QBO
345 winds are present down into the lower stratosphere (Baldwin and Coauthors, 2001; Alexander and Ortland, 2010) or ~~when the~~
346 ~~ENSO index is positive during El Niño~~ (Yang and Hoskins, 2013). The latter factor ~~might explain partly the~~ may partly explain
347 a large difference in the ~~abundant amount of~~ KW energy during the El Niño ~~winter~~ DJF of 2009-2010 and the below-average
348 ~~amount of KW energy~~ energy level a year after, during the strong La Niña ~~winter~~ DJF period of 2010-2011. However, during
349 the La Niña ~~winter~~ DJF of 2007-2008, the amount of KW energy is ~~observed to be~~ above normal. That ~~winter~~ season was

350 however characterized by ~~favorable~~ above-normal MJO activity which often occurs during favourable easterly QBO conditions
351 in the stratosphere ~~while during the winter of~~ (Son et al., 2017). During 2010-2011 DJF season stratospheric winds were largely
352 westerly ~~of nature~~ thereby prohibiting KW activity. The role of these low-frequency atmospheric phenomena on KW seasonal
353 variability is a topic of further research.

354 Finally, Fig. 5 also shows that KW activity in July 2007, previously examined by Žagar et al. (2009), was ~~an exceptionally~~
355 ~~energetic month~~ exceptionally strong. A large part of that energy, ~~approximately 400 Jkg⁻¹ (52.7% of total KW energy), was~~
356 ~~projected on~~ (somewhat more than half) belonged to zonal wavenumber 1. In spatiotemporal terms, it ~~represented~~ is associated
357 with the presence of a strong dipole structure in the TTL (as in Fig.2), which is colocated with favourable easterly wind
358 conditions in the TTL as well as in the stratosphere (not shown). In fact, at 50 hPa the QBO was just at the beginning of its
359 easterly phase in July 2007.

360 4 A spatiotemporal view on Kelvin wave seasonal variability

361 4.1 Kelvin wave decomposition among wave periods

362 In this section, the spatiotemporal view of KWs shall be presented over three dominant ranges of wave periods in Fig. 6,
363 namely: (i) the (semi)annual cycle using a low-pass filter with cut-off period at 90 days, (ii) the intraseasonal period using
364 a bandpass filter over periods between 20-90 days, and finally (iii) the intramonthly period with bandpass filtered periods
365 between 3-20 days. The ~~choice of ranges chosen periods~~, especially the intramonthly periods ~~is related to previous studies using~~
366 ~~observations. For all three cases, mean 6-year,~~ are similar to those used in previous studies. In each case, mean 6-year fields as
367 well as seasonal means shall be presented.

368 Note that our temporal filtering operates on time series of KW signals at every grid point. This is different from the
369 commonly applied space-time filtering following Hayashi (1982) that applies KW dispersion relations. Our filtered KWs can
370 appear stationary or even westward shifted due to westward-moving sources of the KW amplification (e.g. easterly winds, high
371 static stability in the TTL).

372 Both KW components u_{kw} and T_{kw} are Fourier-transformed to frequency space where the spectral expansion coefficients
373 χ_{kw} in domains outside the desired frequency ranges are put to zero. Case (i) results in KW components $u_{kw,l}$ and $T_{kw,l}$ where
374 l indicates the low-frequency component. Case (ii) results in $u_{kw,m}$ and $T_{kw,m}$ where m indicates the intramonthly period.
375 Case (iii) results in fields $u_{kw,h}$ and $T_{kw,h}$ where h stands for the high-frequency component. Previous studies have defined
376 free propagating Kelvin waves over similar ranges (3-20 days, Alexander and Ortland (2010); 4-23 days, Suzuki and Shiotani
377 (2008)) and similarly for intraseasonal periods (23-92 days, Suzuki and Shiotani (2008)). Next, seasonal averages will be taken
378 over the four seasons, resulting in variables $\overline{u_{kw,l}}^s$, $\overline{T_{kw,l}}^s$ for the low-frequency component and similarly for the other two
379 cases. The superscript s represents one of the four seasons: northern winter ($s = DJF$), spring ($s = MAM$), summer ($s = JJA$),
380 and autumn ($s = SON$).

381 Cases (ii) and (iii) contain purely subseasonal variability and therefore one can expect their ~~mean 6-year~~ fields means to be
382 zero-valued since variability beyond 90 days has been put to zero. Similarly, mean fields for each of the four seasons results

383 in $\overline{u_{kw,h}}^s \ll \overline{u_{kw,l}}^s$ and $\overline{u_{kw,m}}^s \ll \overline{u_{kw,l}}^s$ and the same for the temperature component. This reflects the fact that positive
384 and negative phases of the fast KW responses average out to approximately zero on seasonal timescales (figure not shown).
385 Therefore, the seasonal mean ~~over-of~~ the absolute amplitudes ~~for-of-the~~ zonal wind and temperature are examined instead,
386 i.e. $|\overline{u_{kw,h}}^s|$, $|\overline{u_{kw,m}}^s|$ and similarly for temperature ~~component, in-order-to-study~~. This describes seasonal fluctuations in
387 subseasonal KW amplitudes³.

388 Figure 7 shows results for all three cases after taking mean over the whole period. The left panel resembles a dominant
389 "wave-1" structure with zonal wind maximized around 140 hPa. Easterly KW winds are strongest around 60°E and westerly
390 winds around the Date Line. Note that two stationary perturbations over African (30°E) and South American (80°W) orography
391 are the result of our terrain-following NMF analysis. If one compares the KW zonal wind pattern with the climatological zonal
392 wind pattern in Fig. 3(a) it can be observed that the zonal wind pattern is located around 20° west of the climatological pattern.
393 Wave temperature perturbations are largest where the vertical gradients in zonal wind are largest which explains the ~~quadripole~~
394 ~~structure. Heating (cooling) by KWs is quadrupole structure. Warm and cold KW anomalies are~~ located at 100 hPa in ~~Eastern~~
395 ~~(Western) Hemisphere and the other way around~~ the Eastern and Western hemisphere, respectively, and vice versa at 200-300
396 hPa.

397 The average low-frequency or seasonal KW structure has a significant resemblance with the classical Gill-type KW solution
398 (Gill, 1980) describing a steady-state linear wave response to convective forcing. The Gill-type KW solution is characterized
399 by westerly upper-troposphere winds east of the large-scale convective source. In responds to the seasonal cycle of convection,
400 the solution in Fig. 7a illustrates, in addition to a low-frequency KW variability in westerly winds, also a considerable
401 low-frequency variability west of the convective outflow. This part of the signal represents the wave modulation effect of
402 the propagating KWs on seasonal timescales.

403 The middle panel of Fig. 7 shows the average distribution of KW activity on intraseasonal timescales. The activity is largest
404 in the Eastern Hemisphere hemisphere with average zonal wind maxima up to 3 ms⁻¹ and temperature maxima up to 0.7 K.
405 Zonal wind activity is largest over a broad area between 90 and 150 hPa over the Indian Ocean and the Maritime Continent.
406 Temperature activity occurs slightly higher around 90-100 hPa. Intraseasonal activity is locally somewhat increased also around
407 120°W, west of the Andes mountain range.

408 Finally, Fig. 7c illustrates the average distribution of ~~free-propagating-intramonthly~~ KWs. The Eastern ~~Hemisphere~~ hemisphere
409 again makes up for the larger KW activity than the Western hemisphere, but the maximum is located more upward in compar-
410 ison to the intraseasonal scales, around 80 hPa. Zonal wind activity peaks up to 3 ms⁻¹ over a broad range of 70-110 hPa and
411 temperature peaks over a more narrow area around 76 hPa (up to 0.75 K). The main area for KW activity is found over Indian
412 Ocean region, while least wave activity is above central Pacific. Towards the stratosphere KW activity reduces and becomes
413 more uniform along in ~~longitudal~~ longitudinal direction.

³Most previous studies define KW activity as square amplitude rather than absolute amplitude. In our high resolution dataset we observe highly localized patterns of the KW activity in the Eastern hemisphere due to ongoing wave amplification. By using absolute amplitudes we better visualize the longitudinal structure of the KW activity in comparison to its local maxima.

414 4.2 Low-frequency Kelvin wave variability

415 The seasonal patterns of the low-frequency components of the KW (~~from hereon referred to as the Gill-type KW response~~) is
416 presented as pressure-longitudinal cross-sections along the equator (at 0.7°N) of the KW seasonal means, given by $\overline{[u_{kw,l}]^s}$
417 and $\overline{[T_{kw,l}]^s}$ in Fig. 8.

418 The largest ~~Gill-type KW response is found during NH summer~~ amplitudes are found during the JJA months. A strong dipole
419 "wave-1" pattern is evident in the TTL. The strongest zonal winds are found close to 150 hPa with easterlies up to -12 ms^{-1}
420 centered over Indian Ocean and westerlies up to 6 ms^{-1} over the Western Pacific. Negative temperature KW anomalies at 110
421 hPa are strongest as well during JJA with values up to 1.5 K over Indian Ocean and annually averaged value of -0.5 K over
422 Western Pacific.

423 During ~~NH winter DJF~~, the dipole pattern ~~is has~~ shifted more eastward and upward compared to ~~NH summer JJA~~ and has a
424 more slanted structure. Easterly (westerly) KW winds are located more east over the Maritime continent (central Pacific) and
425 are centered at 130 hPa. The upper temperature dipole pattern is found higher up at 90 hPa approximately. Values are somewhat
426 weaker compared to NH summer with easterlies up to -6 ms^{-1} and westerlies up to 5 ms^{-1} .

427 Finally, ~~NH autumn and spring seasons SON and MAM season months~~ are transition seasons with respect to the strength
428 and position of the KW dipole as it moves west- and downward towards ~~summer JJA~~ and east- and upward towards ~~winter NH~~
429 ~~spring DJF~~. MAM has the weakest KW dipole with slightly stronger westerly winds up to 5 ms^{-1} .

430 The longitudinal position and the strength of the ~~Gill-type low-frequency~~ KWs have been linked to the seasonal patterns of
431 the background winds in the TTL representing the upper level monsoon and Walker circulations (Flannaghan and Fueglistaler,
432 2013). The average background winds maximize at 150 hPa as shown in Fig. 3(a). In Fig. 8, one can see how the KW easterlies
433 in ~~Eastern Hemisphere the Eastern hemisphere~~ are strongest during ~~NH summer JJA~~ in relation to the Indian-South Asian
434 monsoon circulation. Background easterlies as strong as -30 ms^{-1} are located approximately 10° east of the KW maximum
435 easterlies. ~~NH winter DJF~~ has the strongest background westerlies in relation to the upper-level circulation of the Western
436 Pacific anticyclones. ~~NH spring (autumn) MAM~~ shows similar background wind patterns compared to ~~NH winter (summer)~~
437 DJF but with weaker circulation. SON shows similar patterns with JJA but with weaker winds.

438 Further details on longitudinal position and interannual variability of ~~Gill-type the low-frequency~~ KW response at its max-
439 imum value at 150 hPa are illustrated by the Hovmoller diagram in Fig. 9. For comparison, tropical convection is represented
440 as well through the OLR proxy variable averaged over 15°S - 15°N latitudes. All fields have been filtered with a 90 day cut-
441 off low-pass filter in order to highlight the seasonality. As a result, one can observe enhanced/reduced ~~Gill-type~~ KW activity
442 during the same individual seasons as seen from the timeseries in Fig. 5. Above average seasonal KW activity with stronger
443 ~~Gill-type dipole~~ structures occurred during the summer of 2007 (mainly through its easterlies at 60°E) and during the winters
444 of 2006-2007 and 2009-2010. In these winters, El-Nino was active and a clear longitudinal eastward shift is observed in OLR,
445 in the background circulation (not shown), as well as in the ~~Gill-type dipole~~ KW structure. The El-Nino winter of 2009-2010
446 was followed by a strong La Nina winter with an increase in tropical convection over the Maritime continent (note: OLR values
447 below 195 Wm^{-2}).

448 The vertical seasonal movement of the KW dipole has been linked with the seasonal movement of the tropical tropopause
 449 height (Flannaghan and Fueglistaler, 2013; Ryu et al., 2008). The position of the tropical tropopause height (represented by
 450 a static stability value of $5 \times 10^{-4} \text{ s}^{-2}$ in Fig. 8) is found at approximately 85 hPa during winter-DJF and descends towards
 451 100 hPa in summer-JJA, similar to values obtained from GPS-RO observations by Grise et al. (2010). In particular, during
 452 summer-JJA, one can notice how the asymmetry in the tropical tropopause height over Indian Ocean around 60°E coincides
 453 with increasing temperatures by the KW dipole up to 1.5 K. Such deformation of the tropical tropopause is also evident during
 454 winter and autumn-DJF and SON seasons.

455 Figures 10a and 10b illustrate seasonal-mean KW temperatures $\overline{T_{kw,l}}^s$ in relation to the tropical tropopause layer defined by
 456 static stability N^2 . Seasonal variations in KW temperatures are collocated with the position of the tropopause, descending down
 457 from its highest position during winter-DJF to its lowest position during summer-JJA. Temperature amplitudes are observed to
 458 decline roughly above $N^2 = 5 - 6 \times 10^{-4} \text{ s}^{-2}$. Within this zonal-mean seasonal picture, zonal asymmetries in N^2 exist and are
 459 found: (i) near the Date Line with values of $8 \times 10^{-4} \text{ s}^{-2}$ at 80 hPa during winter-DJF and $7 \times 10^{-4} \text{ s}^{-2}$ at 90 hPa during summer
 460 JJA and (ii) lower at 100 hPa over the Indian Ocean during summer-JJA. Particularly during NH-summer-JJA, the deformation
 461 of the zonal-mean static stability field collocates strongly with the position of a strong KW temperature anomaly over Indian
 462 Ocean. A rough estimation is made on the contribution of the KW anomaly to the zonal deformation of the tropopause layer by
 463 removing zonal-mean parts of both fields. First, static stability zonal anomalies, $\overline{N'^2}^s$, are derived by subtracting zonal-mean
 464 values of N^2 from the full N^2 field per timestep and at every pressure level, followed by seasonal averaging. Next, we can
 465 estimate the static stability change associated with the KW anomaly, using the relation: $N_{kw}^2 = \frac{g}{\theta} \frac{\partial \theta_{kw}}{\partial z}$, followed by seasonal
 466 averaging as well, i.e. $\overline{N_{kw}^2}^s$.

467 As a result, Fig. 10c and 10d show how both static stability anomalies are overlapping. During winter-DJF, the structure of
 468 the zonal anomaly $\overline{N'^2}^s$ has a positively-valued tilt eastward which stretches up to 80 hPa, while during summer-JJA a strong
 469 static stability anomaly is found more localized over Indian ocean region with values in the TTL up to $\overline{N'^2}^{JJA} = \pm 0.8 \times 10^{-4}$
 470 s^{-2} . The anomaly associated with the KW temperature anomaly is found to peak up to $+0.6 \times 10^{-4} \text{ s}^{-2}$ during summer-JJA
 471 and up to $+0.4 \times 10^{-4} \text{ s}^{-2}$ during winter-DJF. Finally, by dividing both fields with each other, the resulting contribution of the
 472 quasi-stationary Kelvin wave to the observed deformation of the tropical tropopause layer is estimated up to 60% (during JJA
 473 and 80%)-during-NH-summer-(winter)during DJF.

474 4.3 Intraseasonal Kelvin wave variability

475 The seasonality of intraseasonal Kelvin wave variability is shown in Fig. 11 and shall be briefly discussed here. The NH-winter
 476 DJF stands out as the most active season for KW activity, located mainly in the Eastern hemisphere centered-centred at 100°E
 477 and with maximum activity at 110 hPa for zonal wind and temperature with a second maximum in temperature at 90 hPa.
 478 Values observed are up to 0.8 K for KW temperature and 5 ms^{-1} for KW zonal wind. During NH-spring-MAM season, the
 479 KW activity fields are weaker but spread over a larger area in the Eastern hemisphere and in the TTL with maximum activity
 480 centered at 120 hPa (90 hPa) for the zonal wind (temperature) component. Both NH-summer and autumn-JJA and SON seasons
 481 have KW activity positioned at lower altitudes and more westward. In both seasons, KW zonal wind activity is split up between

482 two structures with an eastward tilt with height; one with a maximum around 110°E and one pattern starting from 100 hPa and
483 extending towards 60°E. Note also the increase in KW activity in the Western hemisphere below 150 hPa in the East Pacific.
484 The maximum KW activity in the temperature component for both seasons is positioned near 100 hPa approximately on the
485 tropical tropopause contour with value $5 \times 10^{-4} \text{ s}^{-2}$.

486 The eastward tilted structure is observed throughout all seasons except ~~NH-spring~~-~~MAM~~ when background easterly winds
487 are nearly absent in the Eastern hemisphere. In all other seasons one can observe how the tilted structure is locked to the
488 background easterlies with maximum amplitudes located slightly above and west of it. Such eastward tilt with height has
489 been frequently observed, for example over radiosonde station Medan at 100°E during the early stage of MJO development
490 (Kiladis et al., 2005).

491 4.4 Intramonthly Kelvin waves

492 4.5 ~~Free-propagating Kelvin-waves~~

493 The seasonal variability of ~~free-traveling~~-intramonthly Kelvin waves, represented by their absolute amplitudes $\overline{|u'_{kw,h}|^s}$ and
494 $\overline{|T'_{kw,h}|^s}$, shall be examined in relation to the background conditions. Figure 12 illustrates favorable regions for KW activity. In
495 general, KW activity increases upward from around 120 hPa towards its zonal-mean peak value at 76 hPa. The largest values
496 are observed in ~~EH~~-the Eastern hemisphere in region from 30°E till 150°E. The temperature component in particular has a
497 constant maximum peak (up to 0.8 K in ~~EH~~) located around 76 hPa throughout the year, where also the largest increase in N^2
498 occurs as shown in Fig. 3. Above 70 hPa, KW activity continuously decreases in the stratosphere.

499 The longitudinal structure of the KW zonal wind shows two distinct peaks in the TTL, one consistently located at 76
500 hPa and another around 100-110 hPa in the ~~EH~~-Eastern hemisphere which is mainly present during solstice seasons. The
501 first maximum coincides with the temperature distribution which can be explained by their balance relationships and free
502 horizontal propagation in the stratosphere. Below the tropopause, KW activity is coupled to convective processes alternating
503 the tropospheric vertical wave structures as discussed by Flannaghan and Fueglistaler (2012).

504 The secondary maximum around 110 hPa in Fig. 12 is present mainly during solstice seasons in ~~EH~~-the Eastern hemisphere
505 and it is associated with the seasonal movement of the background wind. The maximum of KW wind and the background wind
506 maximum move eastward from ~~winter-to-summer~~-DJF to JJA season similar to the low-frequency variability. A day-by-day
507 comparison of the KW activity and background wind confirms that propagating KWs amplify while approaching a region of
508 strong easterlies, forming a folding structure around it while the individual KWs dissipate towards the center of easterly winds.
509 One can notice in Fig. 12 a fast reduction of KW amplitudes eastward of its maximum towards the center of the background
510 easterlies. It is likely related to dissipation and wave breaking processes as observed over Indonesia (120°E) by Fujiwara et al.
511 (2003). Within such regions, the KW-background wind interaction becomes complex and the linearity assumption breaks
512 (Ryu et al., 2008; Flannaghan and Fueglistaler, 2013).

513 A comparison with the previous study by Suzuki and Shiotani (2008) using ERA-40 data shows that the L91 data contain
514 stronger KW activity in the vicinity of the background easterlies in the Eastern ~~Hemisphere~~hemisphere, and more fine-scale

515 details which can be explained by better analyses based on more observations and improved models including increased
516 resolution. For example, Suzuki and Shiotani (2008) used 5 levels of ERA-40 data between 50 and 200 hPa whereas the present
517 study considers 25 model levels between 50 – 200 hPa. Maxima of the KW temperature signal appear in similar locations and
518 strength except for a small offset in vertical position (70 hPa in Suzuki and Shiotani (2008) versus 80 hPa in Fig. 12) and a
519 larger zonal asymmetry in our results.

520 Another view of the seasonal cycle of free propagating KWs is illustrated in Fig. 13 which focuses on the spatiotemporal
521 distribution of individual KW ~~packetstracks~~. Hovmoller diagrams ~~are illustrated~~ of KW zonal wind and temperature at levels
522 110 and 200 hPa ~~cumulated~~ from different years ~~are shown into a single calendar year~~ along with the background zonal wind.
523 In addition, the monthly-mean values of daily maximum KW amplitudes occurring ~~at a specific longitude along the equator are~~
524 ~~added next to in longitude are added on the rightside of~~ each diagram. ~~It represents seasonality in the KW maximum amplitudes~~
525 ~~in a similar fashion to Fig. 6 in Alexander and Ortland (2010) which is based on HIRDLS satellite data.~~

526 The individual wave tracks at 110 hPa illustrate KWs with amplitudes exceeding 3 ms^{-1} and 0.6 K which are propagating
527 throughout the year in the Eastern ~~Hemisphere~~~~hemisphere~~, during June–October months only over the Pacific, and all except
528 ~~winter-DJF~~ months in most of the Western Hemisphere. Typical wave tracks start east of the 0° (30°W) meridian during
529 winter (summer) and largely disappear west of 120°E . The largest wave amplitudes are observed between 50°E and 100°E
530 prior to regions of easterly winds in agreement with Fig. 12. Here presented details show that most notable waves appear
531 during the Asian monsoon period with upper-level easterlies prevailing from June into September. The largest ~~Kelvin-wave~~
532 ~~KW~~ amplitudes appear confined to the June and July months followed by a rapid drop in August. In fact, a local minimum in
533 the number of KWs as well as in wave amplitudes occurs in August before the KW activity increases slightly during autumn.

534 At 200 hPa, the favorable area for KW propagation shifts to the Western Hemisphere and large KW activity is observed
535 west of the South American continent throughout the year (west of 80°W) with a westward extension over the Pacific during
536 ~~northern-summer~~~~JJA~~. Another set of wave tracks starts over ~~equatorial~~~~equatorial~~ South America around 30°W (5°W) and
537 continues till 60°E (~~during JJA. During DJF these wave tracks shift more east and start at 5°W and continue till 90°E) during~~
538 ~~northern-summer (winter)~~. The seasonal shifts of approximately 30° in KW tracks collocate with similar shifts in the prevailing
539 TTL winds.

540 The amplitude of KWs undergoes a clear annual cycle with a small secondary peak present during ~~northern-winter~~~~DJF~~, as
541 represented by the monthly-means of daily maximum amplitudes ~~along the equator~~ on the rightside of Fig. 13. The largest
542 amplitudes are found at 110 hPa during ~~NH-summer~~~~JJA~~ with monthly-mean zonal wind (temperature) values up to 8.5 ms^{-1}
543 (1.8 K) in June. During the ~~winter-DJF~~ months Kelvin waves amplify more eastward with monthly-mean zonal wind (temper-
544 ature) values up to 7.8 ms^{-1} (1.6 K) in December. ~~Our result matches well with the observed seasonal pattern in maximum~~
545 ~~KW temperatures at 16km ($\sim 100 \text{ hPa}$) from the HIRDLS satellite observations (Alexander and Ortland, 2010, Fig. 6).~~ At 200
546 hPa, KW amplitudes are on average lower with a yearly-averaged amplitude reduction around 55% in temperature and 35% in
547 zonal wind.

548 The semiannual cycle in maximum amplitudes remains visible up till 70 hPa. Above 70 hPa, where the KW activity remains
549 large in Eastern ~~Hemisphere~~ hemisphere (Fig. 12), the semiannual cycle is replaced by an interannual cycle in line with the
550 dominant impact of the QBO.

551 **5 Discussion and Conclusions**

552 We have applied the multivariate decomposition of the ECMWF operational analyses during the period 2007-2013 when
553 the operational data assimilation ~~was and forecasting were~~ performed on 91 ~~levels. Model-level data were analyzed every 6~~
554 ~~hours. The applied model levels. The applied normal-mode function~~ decomposition provides simultaneously the wind com-
555 ponents, geopotential height and temperature perturbations of ~~the Kelvin waves on the terrain-following levels~~ Kelvin waves
556 for many scale without any prior data filtering. The three-dimensional Kelvin wave structure in the upper troposphere and
557 lower stratosphere is composed of Kelvin wave solutions of 60 linearized shallow-water equation systems on the sphere with
558 equivalent depths from 10 km up to about 3 meters. As the KW meridional wind component is very small it is not discussed -
559 here. We showed that large-scale KWs readily persist in the data despite analyzing selected processing times independently.

560 The KW is a normal mode of the global atmosphere and our 3D-orthogonal decomposition allows quantification of its
561 contribution to the global energy spectrum and variability. We have presented the total (kinetic+potential) energy of KWs in
562 the L91 data as a function of the zonal wavenumber in different seasons. The zonal wavenumber $k = 1$ contains the largest
563 portion of KW energy in all seasons. There is almost one third more energy in JJA than in MAM in $k = 1$. In $k = 2$ there is
564 50% less energy than in $k = 1$ but JJA still contains most energy. In all larger zonal wavenumbers, the most energetic season is
565 DJF.

566 We focused on the spatiotemporal features of the KW temperature and zonal wind components in the four seasons. The
567 Kelvin wave seasonal cycle in the tropical tropopause layer (TTL) was compared with seasonal variability of the Outgoing
568 Longwave Radiation (OLR), and the background wind and stability fields, which are believed to play an important role for
569 the KW variability. Our study results of the seasonal KW variability ~~complements complement~~ previous studies which applied
570 different methods for the KW filtering and different datasets. ~~As KW is a normal mode of the global atmosphere, our filtering~~
571 ~~of the KW using the 3D-orthogonal normal-mode function decomposition of global data is a useful approach to quantification~~
572 ~~of the KW variance. The KW is the most energetic inertio-gravity mode of the global atmosphere (Žagar et al., 2009) and~~
573 ~~its representation in weather and climate models is crucial for reliable simulations of the tropics and its impact on global~~
574 ~~circulation.~~

575 ~~We have presented the total energy of the KWs in the L91 data extending between the surface and 1 Pa as a function of the~~
576 ~~zonal wavenumber. Zonal wavenumber $k = 1$ contains a largest portion of KW energy in all seasons. Its energy varies between~~
577 ~~~ 300 in JJA in NH spring to over 400 J/kg in NH summer. In $k = 2$ there is 50% less energy than in $k = 1$ but the NH summer~~
578 ~~is still the most energetic season. In all greater zonal wavenumbers, DJF season contains most energy.~~

579 Frequency The frequency spectrum has revealed a semiannual cycle as well as intraseasonal and intramonthly variabil-
580 ity. Three ranges of wave periods were analyzed: 3-20 days, 20-90 days and longer than 90 days. This choice was partly

581 deliberate in order to compare our results with several previous studies of KW variability. First we demonstrated that the
582 ~~seasonal-mean KW low-frequency KW dipole~~ pattern in the TTL, with ~~(westerly-) easterly-westerly~~ winds in the ~~(Western-)~~
583 ~~Eastern hemisphere resembles a time-averaged Western hemisphere and with easterly winds in the Eastern hemisphere, partly~~
584 ~~resembles a seasonal-averaged~~ Gill-type "wave-1" pattern ~~and contains partly low-frequency modulation of vertically-propagating~~
585 ~~KWs~~. The quadrature-shaped temperature component represents a thermally adjusted pattern with respect to the zonal wind
586 component, and contributes to seasonal ~~(cooling)-warming~~ above 100 hPa in the ~~(Eastern) Western Western and cooling in the~~
587 ~~Eastern~~ hemisphere. The largest KW amplitudes are observed during ~~summer-and-winter-JJA and DJF~~ seasons. From boreal
588 summer towards winter, KW ~~perturbation-perturbations~~ moves eastward (from Indian Ocean basin towards Maritime Conti-
589 nent) and upward (e.g. zonal wind component moves up from 150 hPa towards 120 hPa). The KW zonal wind amplitude varies
590 between 12 m/s strong easterlies over Indian ocean near 150 hPa in JJA to 6 m/s over Western Pacific. Over Indian Ocean in
591 JJA, the KW easterlies thus make almost half of the total wind vector. The associated KW temperature perturbations are from
592 1.5 K over Indian ocean in JJA to -0.5 K over West Pacific. The zonal modulation of Kelvin waves is found to be locked with
593 respect to the seasonal movement of convection and the convective outflow in the TTL. The modulation effect is strongest
594 for ~~Gill-type the low-frequency~~ Kelvin waves during the summer monsoon season, when strong easterly winds are present at
595 150 hPa, resulting in the largest KW zonal wind and temperature anomalies, of which the latter results in deformation of the
596 tropical tropopause over Indian Ocean.

597 Intraseasonal (periods 20-90 days) activity is strongest in ~~NH-winter-DJF~~ with maxima up to 0.8 K for KW temperature
598 and up to 5 m/s for KW zonal wind centred at 120°E. Both temperature and zonal wind activities have eastward tilt with
599 height. In comparison to previous study by Suzuki and Shiotani (2008) using ERA-40 data, the slanted structure in the present
600 data continues to extend more upward and eastward which is likely due to the increased number of vertical model levels
601 compared to ERA-40. The importance of vertical model resolution for the KW ~~wave~~-structure and amplitude was demonstrated
602 in Žagar et al. (2012) and Podglajen et al. (2014).

603 For periods 3–20 days, the seasonal cycle of KWs is clearly seen in ~~the~~ wave amplitude. ~~The In the zonal-mean perspective,~~
604 ~~the~~ largest amplitudes are located ~~-from a zonal-mean perspective-~~ between 70 and 100 hPa for both zonal wind and tem-
605 perature ~~as expected for the free-propagating Kelvin waves~~ but it is modulated by the seasonal movement of the TTL. A
606 major zonal asymmetry was found in KW activity: around 110 hPa ~~the~~ Kelvin wave undergoes amplification mainly in ~~Eastern~~
607 ~~Hemisphere the Eastern hemisphere~~ during the solstice seasons, while at 200 hPa a secondary region of ~~the~~ KW amplifica-
608 tion occurs in ~~Western Hemisphere the Western hemisphere~~ during boreal summer. ~~Free-propagating The intermonthly~~ KWs
609 show largest amplitudes in the vicinity of the strongest easterlies preferably west and above the ~~center-centre~~ of easterlies. The
610 ~~NMF methodology has made applied novel methodology makes~~ it possible to observe such dynamics on daily basis whenever
611 easterlies are strong in the TTL. Nearly real-time representation of the KW activity is available on <http://modes.fmf.uni-lj.si>.

612 In summary, our seasonal variability analysis shows that the background wind in the TTL linked with convective outflows,
613 play a dominant role in the longitudinal position where ~~the~~ zonal modulation of Kelvin waves is preferred, while the tropical
614 tropopause and its seasonal vertical movement ~~determines determine~~ the vertical extent of ~~the~~ KW modulation processes.

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