

1 **On the Freezing Time of Supercooled Drops in Developing**
2 **Convective Clouds**

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12 **Abstract**

13 Ice generation and evolution in convective clouds are still poorly understood and challenging to
14 model. Aircraft measurements during the Ice in Clouds-Tropical (ICE-T) project suggest that the
15 observed ice particles in intense convective clouds are primarily small at relatively warm
16 temperature (between -7 °C and -10 °C), and large frozen drops are detected at a colder
17 temperature than -10 °C. However, the ice particle size distributions (PSDs) between -7 °C and -
18 10°C modelled using a parcel model containing a spectral bin microphysics scheme are much

- Deleted: In this study, the particle size distributions (PSDs) measured in fresh developing maritime convective clouds sampled during the Ice in Clouds-Tropical (ICE-T) project are shown and compared with the PSDs modeled using a parcel model containing a spectral bin microphysics scheme.
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40 ~~broader than the observations~~. To interpret the ~~difference in the temperature-dependent ice PSD~~
41 ~~evolution between the model simulations and the observations~~, the freezing times and
42 temperatures of supercooled drops are ~~modeled and interpreted~~. The results indicate that the
43 freezing time (~~from the initial nucleation to fully frozen~~) ~~must be considered; it is not~~
44 ~~instantaneous, and is~~ longer for large drops than for small drops. ~~In strong updrafts, such as that~~
45 ~~sampled by the Learjet during ICE-T~~, large freezing drops can be carried upwards to a lower
46 temperature than their nucleation temperature before ~~they are fully frozen. This offers a feasible~~
47 ~~explanation for the temperature-dependent ice particle size evolution in strong updrafts observed~~
48 ~~during ICE-T~~. In models, drop freezing is ~~normally~~ assumed to be instantaneous, which is not
49 realistic; the models yields broader ~~ice PSDs between -7 °C and -10 °C~~ than is observed. The
50 ~~results highlight the importance to consider the freezing time of supercooled drops in interpreting~~
51 the observed ~~and modelled~~ ice PSDs in fresh developing convective clouds ~~and in modelling ice~~
52 ~~generation in cloud resolving models~~. To better understand the mechanisms of drop freezing and
53 ice initiation in convective clouds, more laboratory experiments and in situ measurements are
54 needed.

55 1. Introduction

56 Ice initiation in convective clouds is still not well understood (Cantrell and Heymsfield, 2005;
57 Lawson et al., 2015; Yang et al., 2016), and it remains one of the main sources of uncertainties in
58 numerical models (Khain et al., 2015). Observations suggest that ice initiation in convective
59 clouds is strongly related to the freezing of supercooled drops ~~and the size of the freezing drops~~
60 (Rangno and Hobbs, 2005; Lawson et al., 2015; Yang et al., 2016; Field et al., 2017).
61 Supercooled drops do not fully freeze instantaneously, and ~~drops at the early stage of freezing~~
62 ~~usually have little if any deformation (Johnson and Hallett, 1968; Murray and List, 1972;~~

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96 [Hindmarsh et al., 2003](#), The freezing rate of supercooled drops depends on the rate of heat
97 transfer between the drop and ambient air (Pruppacher and Klett, [2010](#)). Typically, the freezing
98 process comprises four stages (Hindmarch et al., 2003): 1) the supercooling stage, during which
99 a drop is supercooled to its nucleation temperature; 2) the recruescence stage, during which rapid
100 kinetic ice nucleation occurs, which results in a rapid [rise](#) in temperature that is terminated when
101 the drop temperature reaches 0 °C; 3) the freezing stage, during which the liquid part of a drop
102 continuously freezes and the drop temperature remains at 0 °C; and 4) the cooling stage, during
103 which the frozen drop cools to the ambient temperature.

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104 A number of laboratory experiments have been performed to study the freezing of supercooled
105 drops. For example, Johnson and Hallett (1968) showed that the freezing time of supercooled
106 drops decreases with decreasing ambient temperature. They also showed that the freezing rate of
107 supercooled drops is related to the composition of [the](#) air and that the freezing time of a
108 millimeter-sized drop in helium and hydrogen is only one-fifth of that in air. Hindmarsh et al.
109 (2003) showed that the freezing time increases with increasing drop size. In addition, Hindmarsh
110 et al. (2003) used experimental results to discuss the accuracy of three drop freezing models: the
111 uniform temperature model, the inward freezing model and the outward freezing model. All
112 three of these models have fairly good accuracy in modeling drop temperatures and freezing
113 times, and there are only minor differences between them.

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114 In most numerical weather prediction models (NWPMs) and global climate models (GCMs), the
115 freezing of supercooled drops is assumed to be instantaneous, because it is difficult to track the
116 freezing stage of every particle in models and because there are no good observations with which
117 to evaluate the modeled ice microphysics in detail. Phillips et al. (2015) implemented time-
118 dependent freezing for raindrops in a cloud model using spectral bin microphysics (SBM). Their

127 sensitivity tests showed that time-dependent drop freezing delays the formation of hail in
128 convective clouds; however, their model was unable to track the freezing stage of every particle.
129 Using a simplified cloud parcel model and an electromagnetic scattering model, Kumjian et al.
130 (2012) showed that the modeled radar polarimetric variables for convective clouds are more
131 consistent with observations if time-dependent drop freezing is considered. However, drop
132 freezing [in fresh developing convective clouds, such as the freezing time and the temperature of](#)
133 [supercooled drops](#), has rarely been discussed.

134 Aircraft in situ measurements are [vital for improving](#) our current understanding of ice [generation](#)
135 in convective clouds and to evaluate model simulations. Traditional in situ measurements can
136 rarely identify ice that is smaller than [100 μm](#) in diameter. The 3-View Cloud Particle Imager
137 (3V-CPI) is a good tool with which to record [images of](#) small particles, and it can be used to
138 identify [the shapes of the](#) small ice (Lawson et al., 2015). During the Ice in Clouds-Topical (ICE-
139 T) project, the 3V-CPI that was operated on the SPEC Learjet yielded high-resolution particle
140 images and particle size distributions (PSDs). The 3V-CPI measurements suggest that the

141 observed [ice at relatively warm temperature \(about -8 °C\)](#) in fresh developing convective clouds
142 are [primarily](#) small (Lawson et al., 2015); however, the results of some other studies have
143 suggested that larger supercooled drops may freeze before smaller drops (Bigg, 1953;

144 Heymsfield, 2013). This raises the question: [are models able to capture the characteristics of the](#)
145 [ice PSDs observed in developing convective clouds?](#) Understanding the freezing time of
146 supercooled drops is helpful for interpreting the [difference between the observed and the](#)
147 [modeled](#) ice PSDs in developing convective clouds. In addition, [the aircraft observations are](#)
148 [useful for evaluating the impact of instantaneous drop freezing on the modeled PSDs.](#)

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Deleted: Thus, to better understand ice initiation in convective clouds and to evaluate the modeled microphysics, more observations are needed.

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166 This study aims to [better understand the impact of the freezing time and temperature of large](#)
167 [supercooled drops on ice PSDs evolution in developing convective clouds](#). [Observed PSDs in](#)
168 [developing convective clouds during the ICE-T project are used to evaluate the PSDs modelled](#)
169 [by a parcel model, and the deficiency of instantaneous drop freezing in the model simulations are](#)
170 [discussed based on the aircraft observation and quantitative calculations of the freezing time and](#)
171 [temperature](#) of supercooled drops. This paper is organized as follows: Section 2 introduces the
172 dataset and the analytical method; Section 3 discusses the results; and a summary is given in
173 Section 4.

174 2. Dataset and Analysis Method

175 2.1 Calculation of the freezing time of supercooled drops

176 The calculation of the freezing time and temperature of supercooled drops is governed by a
177 series of heat transfer and phase change equations. These detailed equations have been described
178 in previous studies (e.g., Dye and Hobbs et al., 1968; [Heymsfield, 1982](#); Hindmarsh et al., 2003).

179 The drop temperature [increase](#) is balanced by convective heat transfer (i.e., ventilation), radiation
180 and latent heat terms. In this calculation, a supercooled drop is assumed to be carried upward by
181 an updraft, which ascends adiabatically. The terminal velocity of the drop follows that defined by
182 Foote and Du Toit (1969). [Diffusional growth is included but coalescence is neglected.](#)

183 [Coalescence is the key process by which large supercooled drops develop in convective clouds.](#)
184 [However, it is not necessary to include the coalescence process during the freezing of the drop in](#)
185 [the calculation of the freezing time of a single supercooled drop, because the freezing time is the](#)
186 [shortest assuming that drop size doesn't increase due to coalescence after freezing begins. The](#)
187 [drop size increase due to coalescence process results in a longer freezing time. In this study, we](#)

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201 [prefer to examine the shortest freezing time of supercooled drop for a given size](#). The initial drop
202 temperature is the same as the ambient air temperature. The temperature inside the drop is
203 assumed to be uniform; this is a reasonable assumption because water and ice have a larger
204 thermal conductivity than air and because of the internal mixing of liquid within the drop (Yao
205 and Schrock, 1976). Hindmarsh et al. (2003) showed that including temperature variations inside
206 the drop has a minor impact on the results. The freezing time is defined as the time period from
207 the start to the end of the drop freezing.

208 2.2 Aircraft measurements during ICE-T

209 The ICE-T project was conducted in July 2011 over the Caribbean Sea, near the U.S. Virgin
210 Islands; its goal was to study ice generation in tropical maritime convective clouds. Both the
211 National Center for Atmospheric Research (NCAR) C-130 aircraft and the SPEC Incorporated
212 Learjet were deployed during ICE-T.

213 The SPEC Learjet was equipped with [the state-of-art instruments that were used to study the](#)
214 microphysics in convective clouds during ICE-T. The primary [objective of the Learjet was to](#)
215 [make rapid, repeated penetrations in the updrafts of growing turrets](#). The instruments included a
216 fast forward-scattering spectrometer probe (FFSSP); a CPI; a two-dimensional stereo (2D-S)
217 probe; a high-volume precipitation spectrometer (HVPS-3), and a Rosemount temperature probe.
218 The measurements obtained using the FFSSP, CPI, 2D-S, and HVPS were combined to generate
219 the PSDs. CPI images were used to identify liquid drops and ice particles that were smaller than
220 500 μm in diameter, and these percentages of drops and ice particles were applied to the 2D-S
221 PSDs. The 2D-S and HVPS images were used to identify drops and ice particles that were larger
222 than 500 μm in diameter. More information about the processing of the Learjet data can be found

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227 in Lawson et al. (2015).

228 The NCAR C-130 was not used to repeatedly penetrate fresh developing convective clouds
229 during ICE-T; instead, it penetrated convective clouds at different stages of their development.

230 Most of these penetrations occurred far below the cloud top, although some were near the cloud

231 top (Heymsfield et al., 2014; [Yang et al., 2016](#)). The [C-130](#) instruments included [a Forward](#)

232 [Scattering Spectrometer Probe \(FSSP\)](#), a two-dimensional cloud (2D-C) probe, a two-

233 dimensional precipitation (2D-P) probe, and a Rosemount temperature probe. The Wyoming

234 Cloud Radar (WCR; Wang et al. 2012) was operated on the C-130 to obtain 2D reflectivity

235 structures, and the Wyoming Cloud Lidar (WCL; Wang et al. 2009) was used to identify liquid-

236 dominated and ice-dominated clouds.

237 2.3 Parcel model simulation

238 In this study, we compare the PSDs modeled using a parcel model containing SBM to those

239 observed [by](#) the aircraft. The SBM was developed by Hebrew University (Khain et al., 2000) and

240 has been implemented in the Weather Forecast and Research model (WRF; Lynn et al., 2005).

241 Time-dependent drop freezing is not included in this scheme. The purpose of this simulation is

242 not to evaluate the modeled [ice concentration](#) using observations, but instead to [identify the](#)

243 [extent of the](#) deficiency of instantaneous drop freezing in SBM. The modeled parcel has a depth

244 of 500 m. The observed drop size distribution at -6 °C is used as an input. [The observed mean](#)

245 [vertical velocity in the updrafts sampled by the Learjet is used in the simulation](#). The

246 hydrometeor types include cloud drop/rain, ice/snow, and graupel; the PSD of each hydrometeor

247 type has 33 mass bins. The ice nucleation mechanisms include immersion freezing using [the](#)

248 [Bigg](#) parameterization (1953), deposition/condensation nucleation (Meyer et al., 1992), contact

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260 nucleation (Meyer et al., 1992), and the Hallett-Mossop process (Hallett and Mossop, 1974).
261 Other ice microphysics processes include riming, coalescence and diffusional growth. During
262 every time step, 1% of the aerosols in the ambient air are assumed to become entrained into the
263 cloud parcel. The ambient aerosol size distribution is observed using a high-flow dual-channel
264 differential mobility analyzer (HDDMA; DeMott et al., 2016) and a Passive Cavity Aerosol
265 Spectrometer Probe (PCASP; Baumgardner et al., 2011) operated on the C-130.

266 3. Results and Discussion

267 3.1 Comparison of observed and modeled particle size distributions

268 Fig. 1 shows the PSDs measured by the Learjet and those modeled using a parcel model with
269 SBM. The observed mean vertical velocity and averaged maximum vertical velocity are shown
270 in Fig. 1a-e. The averaged maximum vertical velocity is the mean value of the maximum vertical
271 velocities in all penetrations for a given temperature range; each penetration has one value of
272 maximum vertical velocity. The simulation data on the left panels include all of the ice physics
273 implemented in the SBM, while drop-ice collision is turned off for the right panels. The
274 modelled ice concentration is much lower than that observed by the Learjet, this may be because
275 there are ice generation mechanisms not implemented in the model, such as ice multiplication
276 due to large drop freezing (Lawson et al., 2015). Here we do not focus on the ice concentration
277 but the size of ice. The Learjet measurements suggest that the ice particles observed in fresh
278 developing convective clouds are relatively small (20-300 μm in diameter) between -7°C and -
279 10°C and that the ice PSD broadens as the temperature decreases. If drop-ice collisions are
280 excluded, most of the modeled ice is small at warm temperatures, consistent with observation
281 (Fig. 1h and i), only a very low concentration of large ice is found, which is from immersion

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288 [freezing](#). The deposition/condensation nucleation exhibits the largest contribution to the
 289 modelled ice (Fig. 1f-i). Immersion freezing and contact freezing contribute less to the modeled
 290 ice PSDs. If drop-ice collision is implemented, the concentration of large ice suddenly increases
 291 by 2 orders of magnitude at temperature between -7 °C and -10 °C (Fig. 1c and d), results in
 292 much broader ice PSDs than observed, indicating these large ice are from the drop-ice collision
 293 process, and are added to the ice PSDs as soon as the large drops collide with small ice
 294 assuming instantaneous freezing.

295 In real convective clouds, large drops do not freeze instantaneously after they are nucleated. At
 296 the early stage of freezing, large drops remain spherical or quasi-spherical (Johnson and Hallett,
 297 1968; Murray and List, 1972; Hindmarsh et al., 2003), and probably contain more liquid mass
 298 than ice mass, so they may be regarded as liquid in the observations. Previous studies suggest it
 299 may take tens of seconds for a millimeter supercooled drop to complete freezing (Hindmarsh et
 300 al., 2003). Therefore, in strong updrafts, such as those sampled by the Learjet during ICE-T,
 301 large drops that start to freeze at warm temperatures may be fully frozen at temperatures colder
 302 than the initial nucleation temperature. However, in models, drop freezing is assumed
 303 instantaneous, so the modeled ice PSDs are much broader than observed between -7 °C and -
 304 10 °C (Fig. 1).

305 Examples of [ice \(and freezing drop\)](#) images collected by the 2D-C on the C-130 and the CPI on
 306 the Learjet are shown in Fig. 2. Both the 2D-C and CPI images were measured near the cloud top
 307 in the updraft cores of developing convective clouds. As noted in the figure, the observed
 308 particles are mostly small between -8 °C and -10 °C (Fig. 2c). Some particles may be small drops
 309 at the early stage of freezing because they exhibit slight shape deformation, as shown by the
 310 particle images in the red box in Fig. 2c; however, we have no other evidence with which to

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365 confirm this. Between -10 °C and -13 °C, we observe more ice particles, including both large
366 [frozen drops](#) and small [ice](#), as well as rimed graupel (Fig. 2a and b). Columns and plates were
367 also observed. Considering the time that is needed for columns and plates to grow [and the](#)
368 [freezing time of large frozen drops](#), they were probably [nucleated](#) at a warmer temperature than
369 is observed. Due to the relatively low resolution of the 2D-S, 2D-C, HVPS and 2D-P images,
370 large drops [at the early stage of freezing](#) that exhibit no obvious shape deformation are regarded
371 as drops [rather than ice](#).

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372 3.2 Freezing time of supercooled drops

373 To better [interpret the freezing of large supercooled drops in strong updrafts](#), we analyze the
374 freezing time [and temperature](#) of supercooled drops in this section. Fig. 3 shows the changes in
375 drop temperature and ice mass fraction [as functions of time and ambient temperature](#). The
376 updraft velocity [used in the calculation](#) is [the observed temperature-dependent mean vertical](#)
377 [velocity that shown in Fig. 1a-e](#). Drops and air parcels ascend from -6 °C (~520 mb, ~5600 m).
378 The nucleation temperature, which is the temperature at which drops begin to freeze, is assumed
379 to be -8 °C. The figure demonstrates that a drop with a radius of 100 µm cools from -6 °C to -
380 8 °C and begins to freeze at approximately [22 s](#). The latent heat released due to freezing leads to
381 a sudden [rise](#) in temperature from -8 °C to 0 °C (Fig. 3a), and the ice mass fraction increases
382 from 0 to 0.1 (Fig. 3b). It takes approximately [5](#) seconds for the drop to fully freeze; during
383 freezing, the drop temperature remains at 0 °C (Fig. 3a), and the ice mass fraction continuously
384 increases (Fig. 3b). After completely freezing, the frozen drop rapidly cools due to the large
385 difference between the ambient temperature and the drop surface temperature. The cooling rate
386 slows down when the frozen drop temperature approaches the ambient temperature. According

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411 to ~~the~~ equations, the cooling rate for a drop in the updraft is largely controlled by convective heat
412 transfer, rather than radiation or diffusional growth. If significant riming occurs on the freezing
413 (frozen) drop surface, the cooling rate could be slower, and the freezing time could thus be
414 longer due to the latent heat release that occurs during riming (Heymsfield, 1982; Phillips et al.,
415 2015). The drop temperature changes in a similar way for larger drops as it does for small drops.
416 However, due to their higher terminal velocity, it takes longer for larger drops to reach their
417 nucleation temperature (-8 °C). Drops with radii of 250 μm and 500 μm begin to freeze at 28 s
418 and 41 s, respectively (Fig. 3a), and ~~the~~ ambient temperatures are approximately -8.1 °C and -
419 8.2 °C (Fig. 3c), respectively, ~~which is slightly colder than the drop temperature because of the~~
420 ~~gradual heat transfer from drop to air~~. In addition, it takes longer for larger drops to completely
421 freeze. Drops with radii of 250 μm and 500 μm require approximately 15 s and 34 s,
422 respectively, to fully freeze (Fig. 3a); these frozen drops are found at temperatures of -9.4 °C and
423 -10.18 °C, respectively (Fig. 3c).

424 Fig. 4 shows the freezing time and frozen temperature as functions of the drop radius for
425 different vertical air velocities and nucleation temperatures. The freezing time represents the
426 time period from the start of drop freezing to the end of drop freezing. The figure shows that the
427 freezing time increases as the radius increases. For the same nucleation temperature, drops freeze
428 faster in stronger updrafts than they do in weaker ones ~~because of the greater difference between~~
429 ~~the particle and air temperatures~~ (Fig. 4a); however, their frozen temperatures are colder in
430 stronger updrafts (Fig. 4b). In addition, for the same updraft strength, a drop freezes faster when
431 its nucleation temperature is lower, and it fully freezes at colder temperatures. Moreover, for the
432 same drop radius, the effect of the updraft strength on the freezing time is smaller if a drop
433 nucleates at a lower temperature, as is indicated by the smaller differences between the solid,

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446 dashed and dotted lines for colder nucleation temperatures (Fig. 4a); however, its impact on
447 frozen temperature does not vary substantially with different nucleation temperatures (Fig. 4b).
448 Calculations of the freezing time and frozen temperature based on the observed temperature-
449 dependent mean vertical velocity and the averaged maximum vertical velocity provide similar
450 information (Fig. 4c and d). Between -7 °C and -10 °C, the observed vertical velocity is strong,
451 so for drops larger than 400 μm in radius which start freezing at -6 °C or -8 °C, the frozen
452 temperature is 2–3 degrees colder than the nucleation temperature. The mean vertical velocity at
453 temperature colder than -10 °C is weaker than that between -7 °C and -10 °C, so for drops that
454 start freezing at -10 °C, the freezing temperature is similar to the nucleation temperature (solid
455 green line in Fig. 4d). This suggests the large frozen drops observed at -10 °C may start freezing
456 at a temperature either warmer than or similar to -10 °C. While for the averaged maximum
457 vertical velocity, the frozen temperature is about 1–2 degrees colder than the nucleation
458 temperature (-10 °C) for drops with radius of 500–1000 μm.
459 According to Bigg (1953), large drops may begin to freeze at warmer temperatures than small
460 drops because large drops have higher probability of containing immersion ice nuclei for a given
461 temperature (Khain et al., 2000). Fig. 5 shows the nucleation temperature and frozen temperature
462 as functions of the drop radius. The nucleation temperature is the temperature at which drops
463 have a 10⁻⁴% probability of freezing, as determined based on Bigg’s parametrization for
464 immersion freezing. This probability is low because of the low concentration of immersion ice
465 nuclei that are present at warm temperatures. The figure shows that large drops may begin to
466 freeze at warmer temperatures than small drops; however, due to their longer freezing times,
467 large drops may fully freeze at colder temperatures than small drops if the updraft is strong
468 enough. Immersion freezing is not the only ice nucleation mechanism. In convective clouds,

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474 small ice can be generated at warmer temperatures by other mechanisms (e.g.,
475 condensation/deposition nucleation). [The ice PSDs measured by the Learjet indicates that ice](#)
476 [observed between -7 °C and -10 °C are small, and larger frozen drops were observed at](#)
477 [temperatures colder than -10 °C](#), but it is not known whether these large drops started to freeze
478 before or after the small droplets, and the mechanisms that lead to drop freezing are not well
479 understood. [In models, drop freezing is assumed instantaneous, which is not realistic, would](#)
480 [result in warmer frozen temperatures than in real clouds, as indicated by the large temperature](#)
481 [difference between the dashed and solid lines shown in Fig. 5.](#)

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482 3.3 Discussion

483 The above analysis indicates that [in strong updrafts, such as that sampled by the Learjet during](#)
484 [the ICE-T project, large drops may be fully frozen at temperatures colder than their nucleation](#)
485 [temperature. However, if the vertical air velocity is not strong enough, large drops may descend](#)
486 or remain at the same level for long periods of time, and they may freeze if their temperature
487 reaches the nucleation temperature. [To illustrate this, data from a C-130 penetration](#) is shown in
488 Fig. 6. In this case, [the](#) penetration occurred approximately 500 m below the cloud top, as is
489 indicated by the WCR reflectivity (Fig. 6a). The WCL power (Fig. 6c) quickly attenuated and the
490 WCL depolarization ratio (Fig. 6d) is relatively low, which indicates that this cloud was
491 dominated by liquid drops. At the flight level, the temperature (Fig. 6e) ranges from -4 °C to -
492 4.5 °C in the updraft and is approximately -5 °C near the cloud edge. The maximum updraft
493 velocity is 7 m/s, and the mean updraft velocity is approximately 3 m/s. The Doppler velocity
494 (Fig. 6b) is negative in most areas of the clouds, [indicating large particles falling through the](#)
495 [updrafts in most areas](#), and its maximum value is approximately 4 m/s, [indicating ascending](#)
496 [large particles in the strongest updraft core](#). The 2D-C images clearly show the existence of ice

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512 (Fig. 6f). Most of the ice particles are frozen drops and graupel, and some are needles and
 513 columns. Considering the time that is needed for the drops to freeze and for the needles and
 514 columns to grow through vapor diffusion, the [observed ice \(graupel, needles and columns\)](#) may
 515 have [been](#) nucleated when the cloud top was lower than observed. [A previous statistical study](#)
 516 [also support that large ice present at warm temperatures in developing convective clouds with](#)
 517 [relatively weak updraft \(Yang et al., 2016\).](#)

518 The freezing of supercooled drops may be associated with some corresponding processes. For
 519 example, drops may break up or shatter during freezing, which can produce multiple ice
 520 fragments and splinters ([Lawson et al., 2015](#)). Mason and Maybank (1960) showed that the
 521 freezing of a millimeter-sized drop may produce more than a hundred splinters. These ice
 522 splinters can enhance ice initiation in convective clouds. [The Hallett-Mossop process appears to](#)
 523 [be inefficient in the strong ICE-T convective updrafts \(Lawson et al., 2015\), but is evidently](#)
 524 [more important in mature convective clouds with relatively weak updrafts \(Heymsfield and](#)
 525 [Willis, 2014\).](#) [In addition](#), time-dependent freezing can have an impact on the dynamics in
 526 developing clouds. The instantaneous freezing of a supercooled drop results in the sudden release
 527 of a large amount of latent heat, which may lead to an overestimation of the vertical velocity in
 528 modeled convective clouds ([Fan et al., 2015](#)). In contrast, time-dependent drop freezing can
 529 affect the cloud dynamics in a different way because its latent heat is gradually released. This
 530 study [points out the need to understand](#) drop freezing in convective clouds and allows us to
 531 interpret the [deficiency of instantaneous drop freezing in cloud model up to now](#); however, it
 532 also raises some specific questions about ice initiation [and the possible consequences of time-](#)
 533 [dependent drop freezing on cloud evolution](#). Answering these questions requires a better
 534 understanding of the [drop freezing mechanisms in convective clouds, which in turn requires](#)

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Deleted: In addition, the change in drop temperature during freezing may exert impacts on the Hallett-Mossop process. Heymsfield and Mossop (1984) showed that the Hallett-Mossop process is not only related to the ambient temperature but is also related to the graupel surface temperature. In the SBM used in this study, the Hallett-Mossop process is only parameterized for ambient temperatures between -3 °C and -8 °C. However, the Hallett-Mossop process may occur at colder ambient temperatures if the frozen drop (or graupel) surface temperature is appropriate (Heymsfield and Mossop, 1984). Fig. 3 shows that the drop temperature cools from 0 °C to its ambient temperature after being fully frozen and that the cooling rate may be even slower if there is significant riming on the surface of the particle (Phillips et al. 2015). During this process, if the drop surface temperature and other ambient conditions are suitable, the Hallett-Mossop process may occur at an air temperature that is colder than -8 °C, which could also enhance the initiation of ice in developing convective clouds. For example, a millimeter-sized frozen drop can collect approximately 600 droplets in five seconds, assuming that the droplet concentration is 50 cm⁻³ and its diameter is 20 μm. Thus, two or three ice splinters may be produced if the ambient conditions are suitable. Moreover

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579 more laboratory experiments to be performed and more in situ measurements to be obtained in
580 the future.

581 This study focuses on relatively warm temperatures in tropical maritime developing convective
582 clouds, with 14 penetrations between -7 °C and -10 °C, and 6 penetrations between -10 °C and -
583 12 °C. The sample size is relatively small, but the observations are helpful for studying the ice
584 PSDs in tropical maritime convective clouds, at least for the clouds sampled by the Learjet
585 during the ICE-T project. Currently, there are not many measurements of PSDs in tropical
586 maritime developing convective clouds with strong updraft cores using the state-of-art cloud
587 probes, especially for small ice PSDs. Clearly, more field measurements are needed in the future.

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588 4. Summary

589 In this study, the PSDs measured in fresh developing maritime convective clouds sampled during
590 ICE-T are shown, and the deficiency of assuming instantaneous drop freezing in models is
591 discussed. The observations in strong convective cores presented here suggest that the observed
592 ice is primarily small at relatively warm temperature (between -7 °C and -10 °C), but the
593 modelled ice PSDs are much broader than observed. To interpret the difference between the
594 modelled and the observed ice PSDs, the freezing times and temperatures of supercooled drops
595 are calculated. This analysis indicates that the freezing time is longer for large drops than it is for
596 small drops. In strong updrafts, such as that sampled by the Learjet during ICE-T, large freezing
597 drops may be transported to a colder temperature than their nucleation temperature before they
598 are fully frozen. However, in models, drop freezing is assumed instantaneous, which is not
599 realistic, and results in much broader ice PSDs at warm temperatures. Instantaneous freezing is a
600 reasonable assumption in models if the freezing time of supercooled drops is shorter than the

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613 [time step, but for simulations of convective clouds using models with relatively high temporal](#)
614 [resolution, the time step may be shorter than the freezing time of supercooled drops, especially](#)
615 [the large supercooled drops.](#) This study [aids in interpreting the modeled and](#) observed ice PSDs
616 in fresh developing convective clouds, [drawing on the the perspective of the time required for](#)
617 [drops to freeze.](#) However, the mechanisms of drop freezing and ice initiation are still not well
618 known. Future studies are required to evaluate model simulations using time-dependent drop
619 freezing, to understand the impact of time-dependent drop freezing on the microphysics and
620 dynamics of convective clouds, and to further explore the mechanisms of drop freezing and ice
621 initiation.

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627 products. [We](#) thank Drs. Paul Lawson and Sarah Woods for processing and sharing the data of
628 particle size distributions measured by Learjet.

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635 **References**

- 636 Baumgardner, D. and co-authors: Airborne instruments to measure atmospheric aerosol particles,
637 clouds and radiation: A cook's tour of mature and emerging technology. *Atmospheric*
638 *Research*, 102, 10-29, 2011.
- 639 Bigg, E. K.: The formation of atmospheric ice crystals by the freezing of droplets. *Quarterly*
640 *Journal of the Royal Meteorological Society*, 79, 510-519, 1953.
- 641 Cantrell, W., and Heymsfield, A.: Production of ice in tropospheric clouds: A review. *Bulletin of*
642 *the American Meteorological Society*, 86(6), 795-807, 2005.
- 643 DeMott, P. J. and co-authors: Sea spray aerosol as a unique source of ice nucleating
644 particles. *Proceedings of the National Academy of Sciences*, 113, 5797-5803, 2016.
- 645 Dye, J. E., and Hobbs, P. V.: The influence of environmental parameters on the freezing and
646 fragmentation of suspended water drops. *Journal of the Atmospheric Sciences*, 25, 82-96, 1968.
- 647 Foote, G. B., and Du Toit, P. S.: Terminal velocity of raindrops aloft. *Journal of Applied*
648 *Meteorology*, 8, 249-253, 1969.
- 649 Hallett, J. and Mossop, S. C.: Production of secondary ice particles during the riming
650 process. *Nature*, 249, 26-28, 1974.
- 651 Fan, J., Liu, Y. C., Xu, K. M., North, K., Collis, S., Dong, X., Zhang, G. J., Chen, Q., Kollias, P.
652 and Ghan, S. J., Improving representation of convective transport for scale-aware
653 parameterization: 1. Convection and cloud properties simulated with spectral bin and bulk
654 microphysics. *Journal of Geophysical Research: Atmospheres*, 120, 3485-3509, 2015.

Deleted: Alkezweeny, A. J.: Freezing of supercooled water droplets due to collision. *Journal of Applied Meteorology*, 8, 994-995, 1969. .

658 [Heymsfield, A. J.: A comparative study of the rates of development of potential graupel and hail](#)
659 [embryos in High Plains storms. Journal of the Atmospheric Sciences, 39, 2867-2897, 1982](#)

660 Heymsfield, A., and Willis, P.: Development of first ice hydrometeors and secondary ice in a
661 tropical oceanic deep convective cloud system near Africa. AIP Conference Proceedings, 1527,
662 972-975, 2013.

663 Heymsfield, A. J., and Willis, P.: Cloud conditions favoring secondary ice particle production in
664 tropical maritime convection. J. Atmos. Sci., 71, 4500–4526, 2014.

665 Hindmarsh, J. P., Russell, A. B., and Chen, X. D.: Experimental and numerical analysis of the
666 temperature transition of a suspended freezing water droplet. International Journal of Heat and
667 Mass Transfer, 46, 1199-1213, 2003.

668 Johnson, D. A., and Hallett, J.: Freezing and shattering of supercooled water drops. Quarterly
669 Journal of the Royal Meteorological Society, 94, 468-482, 1968.

670 Khain, A., Ovtchinnikov, M., Pinsky, M., Pokrovsky, A., and Krugliak, H.: Notes on the state-
671 of-the-art numerical modeling of cloud microphysics. Atmospheric Research, 55, 159-224, 2000.

672 Khain, A. P. and co-authors: Representation of microphysical processes in cloud-resolving
673 models: Spectral (bin) microphysics versus bulk parameterization. Reviews of Geophysics, 53,
674 247-322, 2015.

675 Kumjian, M. R., Ganson, S. M., and Ryzhkov, A. V.: Freezing of raindrops in deep convective
676 updrafts: A microphysical and polarimetric model. Journal of the Atmospheric Sciences, 69,
677 3471-3490, 2012.

678 Lawson, P. R., Woods, S., and Morrison, H.: The microphysics of ice and precipitation
679 development in tropical cumulus clouds. *J. Atmos. Sci.*, 72, 2429-2445, 2015.

680 Lynn, B. H., Khain, A. P., Dudhia, J., Rosenfeld, D., Pokrovsky, A., and Seifert, A.: Spectral
681 (bin) microphysics coupled with a mesoscale model (MM5). Part I: Model description and first
682 results. *Monthly Weather Review*, 133, 44-58, 2005.

683 Mason, B. J. and Mayabnk, J.: The fragmentation and electrification of freezing water drops.
684 *Quarterly Journal of the Royal Meteorological Society*, 86, 176-185, 1960.

685 Meyers, M. P., DeMott, P. J., and Cotton, W. R.: New primary ice-nucleation parameterizations
686 in an explicit cloud model. *Journal of Applied Meteorology*, 31, 708-721, 1992.

687 [Murray, W. A., and List, R.: Freezing of water drops. *Journal of Glaciology*, 11, 415-429, 1972.](#)

688 Phillips, V. T., Khain, A., Benmoshe, N., Ilotoviz, E., and Ryzhkov, A.: Theory of time-
689 dependent freezing. Part II: Scheme for freezing raindrops and simulations by a cloud model
690 with spectral bin microphysics. *Journal of the Atmospheric Sciences*, 72, 262-286, 2015.

691 Pruppacher, H. R. and Klett, J. D.: *Microphysics of clouds and precipitation*. Atmospheric and
692 Oceanographic Sciences Library, 954 pp, 2010.

693 Rangno, A. L., and Hobbs, P. V.: Microstructures and precipitation development in cumulus and
694 small cumulonimbus clouds over the warm pool of the tropical Pacific Ocean. *Quarterly Journal*
695 *of the Royal Meteorological Society*, 131, 639-673, 2005.

696 Wang, Z., Wechsler, P., Kuestner, W., French, J., Rodi, A., Glover, B., Burkhart, M., and
697 Lukens, D.: Wyoming cloud lidar: Instrument description and applications. *Opt. Express*, 17,

Deleted: Pruppacher, H. R.: Electrofreezing of supercooled water. *Pure and Applied Geophysics*, 104, 623-634, 1973. .

700 13576–13587, 2009.

701 Wang, Z. and co-authors: Single aircraft integration of remote sensing and in situ sampling for
702 the study of cloud microphysics and dynamics. *Bull. Amer. Meteor. Soc.*, 93, 653–668, 2012.

703 Yang, J., Wang, Z., Heymsfield, A. J., and Luo, T.: Liquid-Ice Mass Partition in Tropical
704 Maritime Convective Clouds. *J. Atmos. Sci.*, 73, 4959-4978, 2016.

705 Yao, S. C. and Schrock, V. E.: Heat and mass transfer from freely falling drops. *Journal of Heat*
706 *Transfer*, 98, 120-126, 1976.

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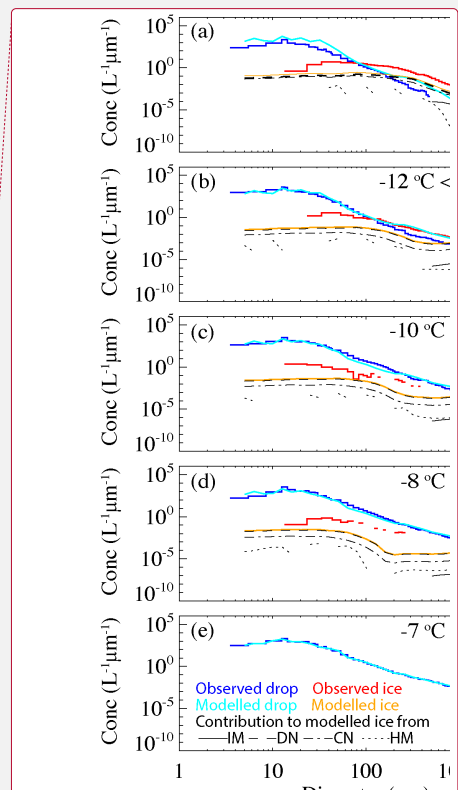
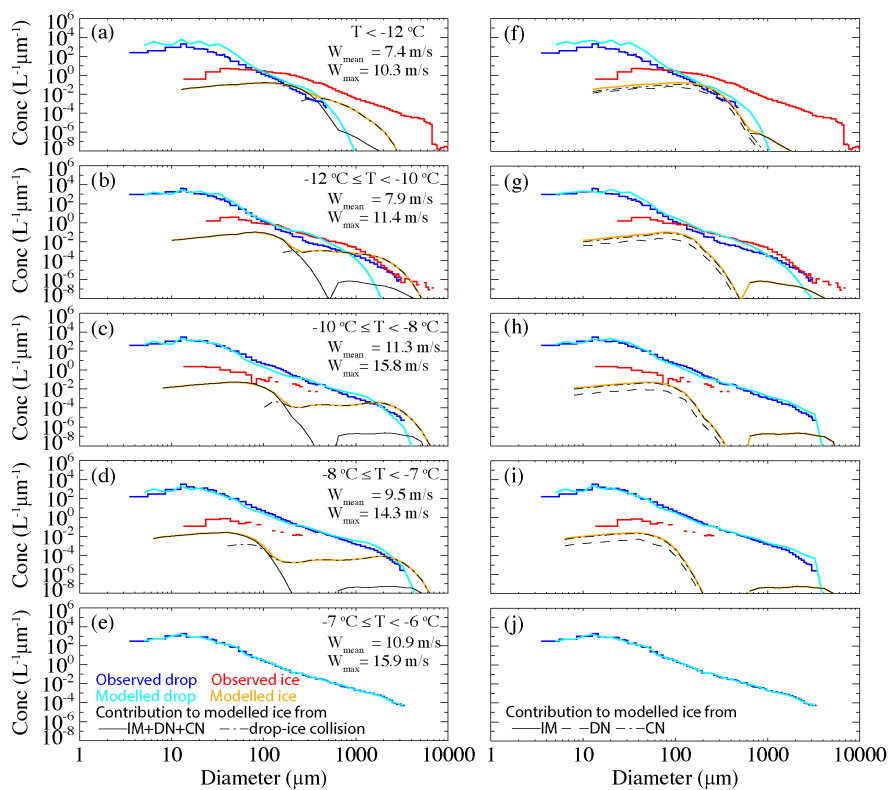
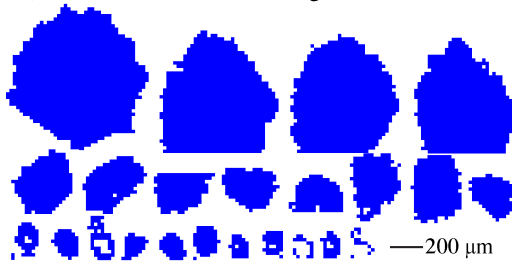


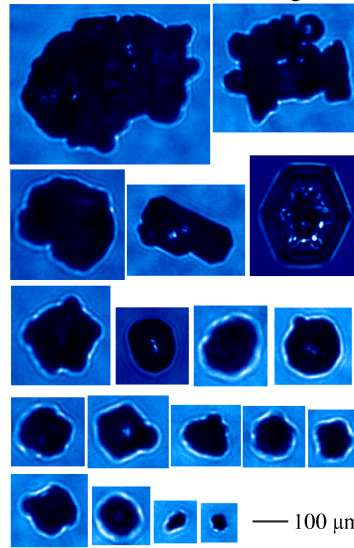
Figure 1. Particle size distributions in fresh developing convective clouds observed by the Learjet during ICE-T and those modeled using a parcel model with SBM. In (a)-(e), all of the ice physics implemented in the SBM are included; in (f)-(j), drop-ice collision is excluded. The black solid, dashed, and dashed-dotted lines in (f)-(j) represent the contributions from immersion freezing (IM), deposition/condensation nucleation (DN), and contact nucleation (CN) respectively, to the modeled ice size distributions. The black solid and dashed-dotted lines in (a)-(e) represent the contributions from primary ice nucleation (IM+DN+CN) and drop-ice collision, respectively, to the modeled ice size distributions. The observed mean vertical velocity (W_{mean}) and averaged maximum vertical velocity (W_{max}) are shown in (a)-(e).

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(a) $-10 \leq T < -13$ °C, 2D-C images



(b) $-10 \leq T < -13$ °C, CPI images



(c) $-8 < T < -10$ °C, CPI images

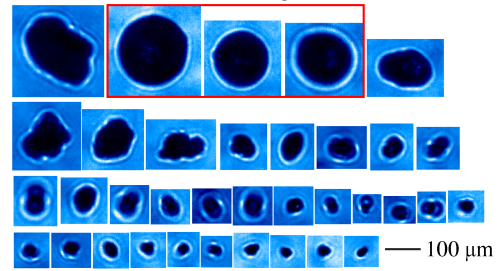


Figure 2. Examples of the 2D-C and CPI images measured in the developing convective clouds sampled during the ICE-T project.

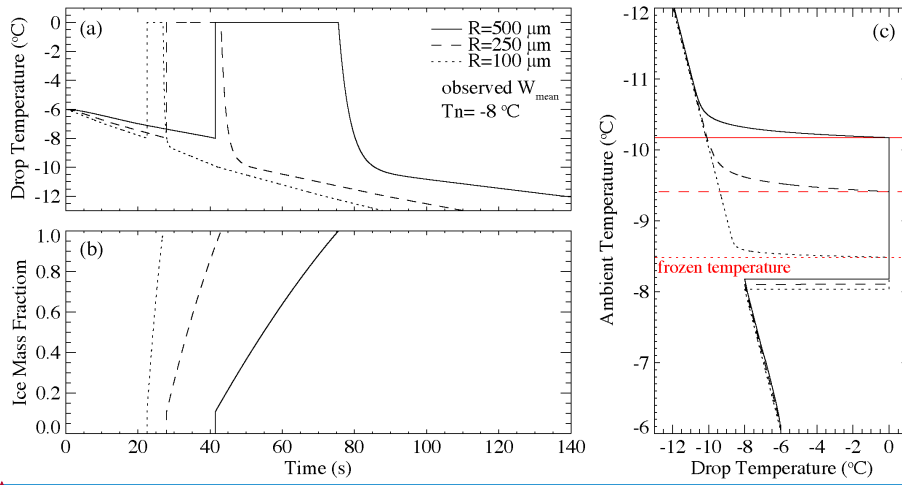
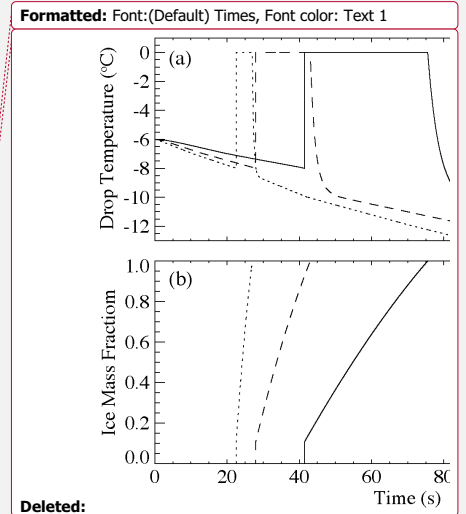


Figure 3. (a) Changes in drop temperature over time for drops with different radii based on the observed mean vertical velocity, which is temperature-dependent. Nucleation temperature (T_n) is $-8\text{ }^\circ\text{C}$; (b) same as (a) but for ice mass fraction; (c) ambient temperature versus drop temperature for drops with different radii. The red solid, dashed and dotted lines indicate the frozen temperature for drops with radius of $500\text{ }\mu\text{m}$, $250\text{ }\mu\text{m}$ and $100\text{ }\mu\text{m}$, respectively.



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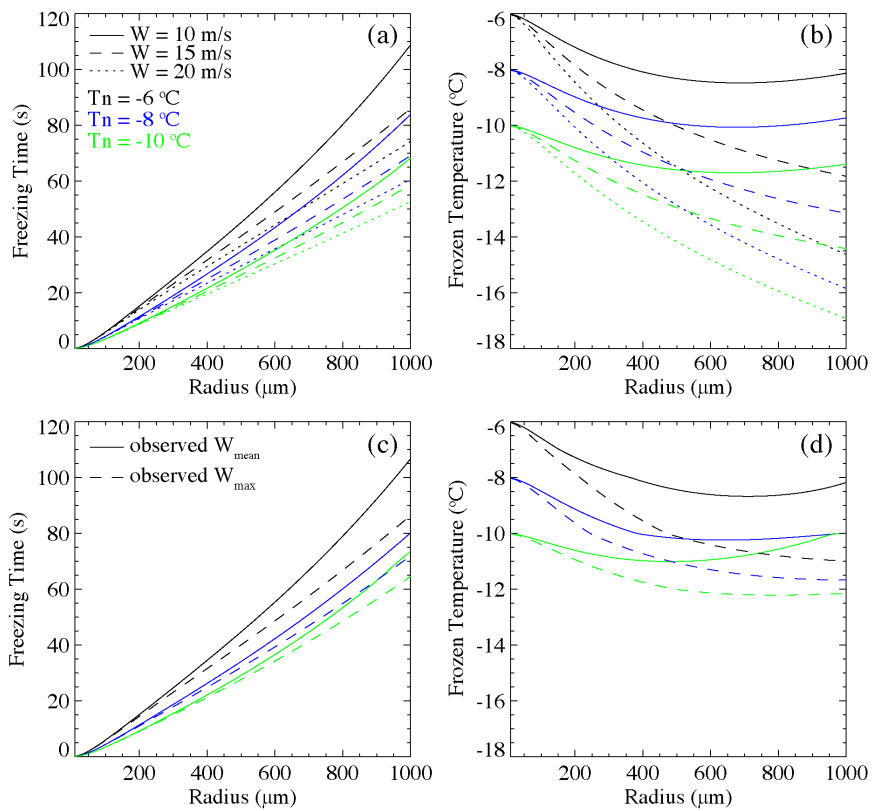
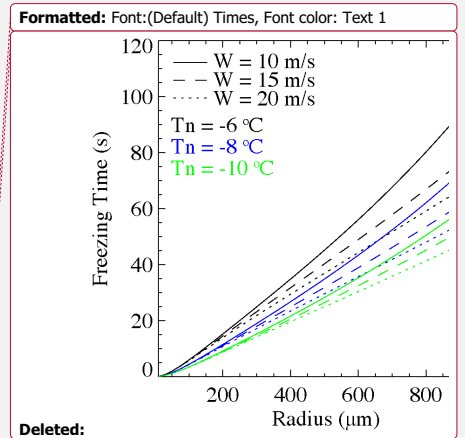


Figure 4. (a) Freezing time and (b) frozen temperature as functions of drop radius for different values of vertical air velocity (W) and nucleation temperature (T_n). (c) and (d) are the same as (a) and (b) but for the observed mean vertical velocity (W_{mean}) and averaged maximum vertical velocity (W_{max}), which are temperature-dependent.



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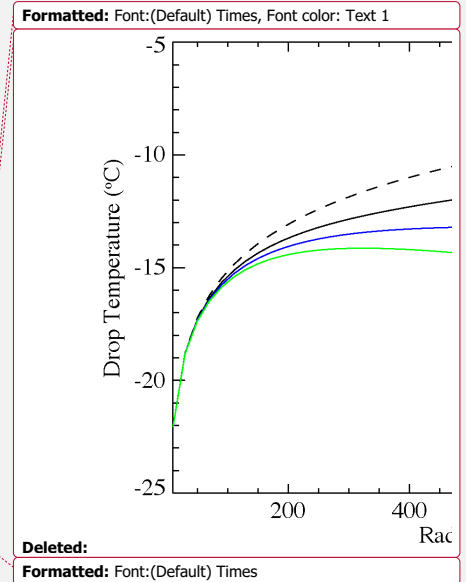
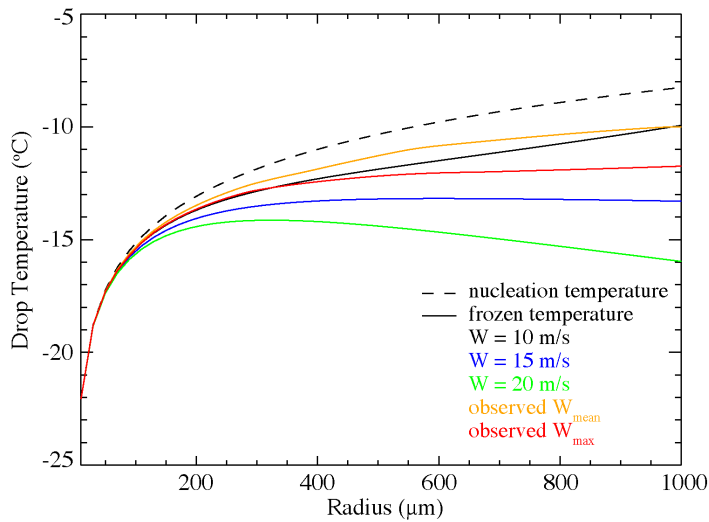


Figure 5. Drop temperature as a function of drop radius for different vertical air velocity (W) values, including the observed mean vertical velocity (W_{mean}) and averaged maximum vertical velocity (W_{max}), which are temperature-dependent. The nucleation temperature is the temperature at which drops have a $10^{-4}\%$ probability of freezing, as determined based on Bigg's parameterization for immersion freezing.

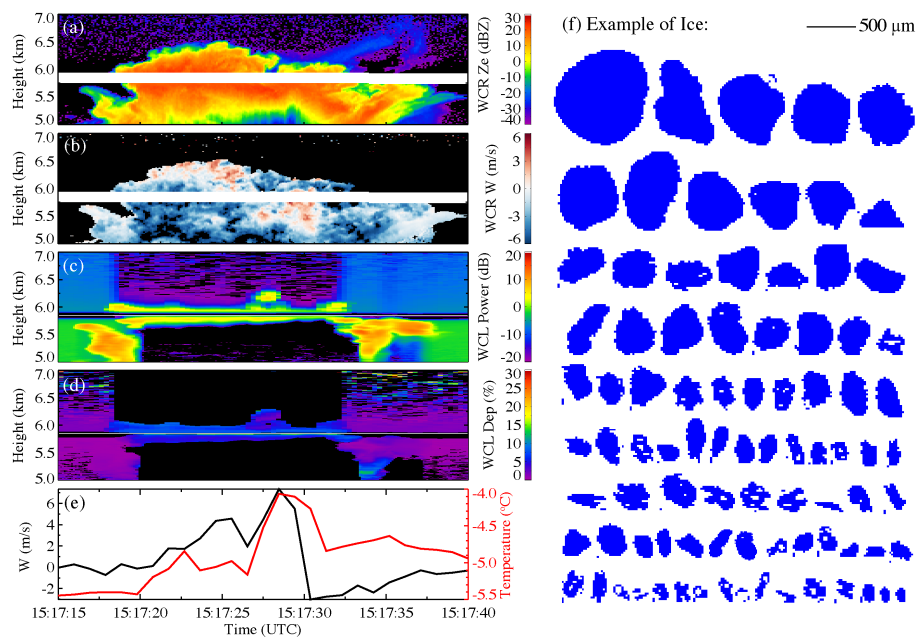


Figure 6. An example of the penetration of the C-130 in a developing cloud sampled on 23 July 2011: (a) WCR reflectivity; (b) WCR Doppler velocity; (c) WCL power; (d) WCL depolarization ratio; (e) ambient temperature and in situ vertical air velocity; and (f) examples of ice particles measured using 2D-C.