



# First tomographic observations of gravity waves by the infrared limb imager GLORIA

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**Abstract.** Atmospheric gravity waves are a major cause of uncertainty in global atmospheric models. This uncertainty affects regional climate projections and seasonal weather predictions. Improving the representation of gravity waves in global atmospheric models, is therefore of primary interest. In this regard, measurements providing an accurate 3D characterization of gravity waves are needed. Using the Gimballing Limb Observer for Radiance Imaging of the Atmosphere (GLORIA), the first airborne implementation of a novel infrared limb imaging technique, a gravity wave event over Iceland was measured. An air volume disturbed by this gravity wave, was investigated from different angles by encircling the volume with a closed flight pattern. Using a tomographic retrieval approach the measurements of this air mass under different angles allowed for a 3D reconstruction of the temperature and trace gas structure. The temperature measurements were used to derive gravity wave amplitudes, 3D wave vectors, and direction-resolved momentum fluxes. These parameters facilitated the backtracing of the waves to their sources on the south coast of Iceland. Two wave packets are distinguished, one stemming from the main mountain ridge in the South of Iceland, a second one from the smaller mountains in the North. The total, area-integrated fluxes of these two wave packets are determined. Following the waves forward with a ray-tracing model highlighted the importance of 3D propagation, an effect generally neglected in global atmospheric models.

## 1 Introduction

Gravity waves (GWs) are oscillations in wind velocity and temperature with buoyancy as restoring force (Fritts and Alexander, 2003). They are the main driver of prominent circulation patterns in the mesosphere, such as the wind reversal in the upper mesosphere – lower thermosphere region. Thereby, they are responsible for the cold summer mesopause and the warm winter stratopause (Holton, 1982, 1983; McLandress, 1998; Siskind, 2014).

GWs not only have a strong influence on the mesosphere but also on the stratosphere. There, they influence the circumpolar jet and its varying degrees of strength (McLandress et al., 2012; Ern et al., 2016); the tropical quasi-biennial-oscillation of



stratospheric tropical winds and its teleconnections into the extratropical troposphere (Dunkerton, 1997; Kawatani et al., 2010; Ern et al., 2014); and the variability in the strength of the meridional Brewer Dobson circulation (Alexander and Rosenlof, 2003; Butchart, 2014). These stratospheric circulations then have an impact on near-surface seasonal weather and regional climate via dynamical couplings with the troposphere (Scaife et al., 2016; Kidston et al., 2015).

5 Considering their small scales, GWs cannot be resolved in global atmospheric circulation models (GCMs) due to computational issues. Hence, they are simplified in form of parameterizations. Consequences of these GW parameterizations are for example surface temperature uncertainties of up to 2 K (Sigmond and Scinocca, 2010) and pressure discrepancies of several hPa at polar latitudes (Sandu et al., 2016) in climate projections. Improved weather predictions and climate projections therefore require more advanced parameterization schemes as proposed by various studies (Kim et al., 2013; Bushell et al., 2015; 10 de la Camara and Lott, 2015; Amemiya and Sato, 2016).

One of the strongest simplifications, used for parameterizations, is to assume solely vertical propagation of GWs. However, several modelling studies, have highlighted the importance of 3D propagation of GWs to correctly reproduce the above mentioned circulation patterns (Sato et al., 2009; Preusse et al., 2009; McLandress et al., 2012; Kalisch et al., 2014; Ribstein and Achatz, 2016). Further, GW source distributions are often over-simplified in parameterizations and need validation by 15 observations (Geller et al., 2013).

To underline the importance of 3D propagation and validate GW source distributions, measurements are needed, which allow for a full 3D wave characterization including the propagation direction (Alexander et al., 2010). Such a characterization is, in principle, possible from various in-situ techniques. Several methods were developed to evaluate data from close-to-vertical profiles taken by radiosondes, dropsondes or falling spheres. These methods include hodograph analysis (Guest et al., 20 2000), Stokes method (Eckermann and Vincent, 1989) or a combination of wind and temperature measurements in a common approach (Wang and Geller, 2003; Zhang et al., 2014). Furthermore, there are multiple techniques based on horizontal traces for example from airplane measurements (Alexander and Pfister, 1995; Fritts et al., 2016; Smith et al., 2016; Wagner et al., 2017) and observations by superpressure balloons (Boccara et al., 2008; Hertzog et al., 2008). All these methods have in common that they infer the wave direction via polarisation and dispersion relations and do not reveal the 3D wave structure 25 directly.

First 3D wave structures from satellite measurements in the stratosphere are presented by Ern et al. (2017) and Wright et al. (2017). However, these studies are based on nadir observations of the Atmospheric Infrared Sounder (AIRS) satellite instrument and are limited by the coarse vertical resolution. This implies that GWs with vertical wavelengths below 15 km are invisible to the instrument. In the mesosphere, a full wave characterization of short scale GWs has been achieved with the 30 Middle Atmosphere Alomar Radar System (MAARSY; Stober et al., 2013). Such observations are limited to a few ground based stations. Further, it is difficult to link observations at altitudes as high as the mesopause region to specific GW sources, which are usually located at much lower altitudes in the troposphere and lower stratosphere. So far no measurement technique existed to measure the 3D structure of mesoscale GWs in the lower stratosphere.

A novel technique to measure GWs in the upper troposphere – lower stratosphere, i.e. close to the GW sources, is limb 35 imaging. Limb imaging allows for a 3D reconstruction of the atmospheric temperature and consequently a full characterization



of mesoscale GWs. The development of the Gimballed Limb Observer for Radiance Imaging of the Atmosphere (GLORIA) is the first implementation of such an airborne infrared limb imager (Friedl-Vallon et al., 2014; Riese et al., 2014).

This technique was applied for the exploration of a GW for the first time in a research flight on 25 January 2016 above Iceland. The results of this research flight are presented in this paper. Section 2.1 describes the instrument and the retrieval technique. The measurement results are presented in section 2.2 and subsequently analysed for GWs in section 3.1. The obtained GW parameters are used for a wave propagation study in section 3.2.

## 2 Measurements

### 2.1 Measurement technique

This paper is based on tomographic measurements taken by the infrared limb imager GLORIA on board the German high altitude – long range research aircraft (HALO). The aircraft campaign took place from December 2015 to March 2016 with campaign bases in Kiruna, Sweden, and Oberpfaffenhofen, Germany. In total there were 21 research flights performed covering 20°N to 90°N and 80°W to 30°E. The scientific targets of this campaign were to demonstrate the use of infrared limb imaging for gravity wave studies (GWEX), to study the full life cycle of a gravity wave (GW-LCYCLE), to investigate the Seasonality of Air mass transport and origin in the Lowermost Stratosphere (SALSA), and to observe the Polar Stratosphere in a Changing Climate (POLSTRACC).

GLORIA combines a Michelson interferometer with a two-dimensional infrared detector and measures molecular thermal emissions in the spectral range between  $780\text{ cm}^{-1}$  and  $1400\text{ cm}^{-1}$  ( $7.1$  to  $12.8\text{ }\mu\text{m}$ ). It has a  $256\times 256$  pixels detector. However, to increase the read-out time, only a subset of  $48\times 128$  pixels is used recording 6144 spectra simultaneously. GLORIA's line-of-sight aims towards the horizon on the right side of the aircraft and measures infrared radiation emitted by molecules in the atmosphere. The point of the line-of-sight which is closest to the earth surface is called tangent point. Due to the curvature of the earth surface and the atmospheric density profile, the weighting function of the measurement signal has its maximum around this tangent point (Riese et al., 1999). This means that typically most of the measured radiation is emitted around the tangent points, which are located between 5 km and aircraft flight altitude. The horizontal observation angle can be adjusted from  $45^\circ$  (right-forward) to  $135^\circ$  (right-backward) in respect to the aircraft's flight direction. In this way, the instrument can investigate the same air volume from different directions, which allows for a tomographic retrieval scheme (Ungermaun et al., 2010; Kaufmann et al., 2015).

The basis of a tomographic retrieval scheme is a fast radiative transfer model. For the retrievals presented in this paper the Juelich Rapid Spectral Simulation Code Version 2 (JURASSIC2; Ungermaun et al., 2010) is used. With this radiative transfer model  $F(x)$  infrared radiances can be calculated directly from an atmospheric state  $x \in \mathbb{R}^n$ . Reconstructing the atmospheric state  $x$  from the infrared measurements  $y \in \mathbb{R}^m$  (the so called retrieval or inverse modelling) in contrast presents a non-linear inverse problem, which is solved with an iterative minimization approach (Ungermaun et al., 2011, 2015). For this, the cost-



**Table 1.** Spectral windows used for the retrieval presented in this paper. The last column indicates which window is used for which retrieval quantity.

	spectral range / $\text{cm}^{-1}$			used for
1	790.625	–	792.500	temperature
2	793.125	–	795.000	$\text{CCl}_4$
3	796.875	–	799.375	$\text{CCl}_4$
4	883.750	–	888.125	$\text{HNO}_3$
5	892.500	–	896.250	$\text{HNO}_3$
6	900.000	–	903.125	$\text{HNO}_3$
7	918.750	–	923.125	$\text{HNO}_3$
8	956.875	–	962.500	temperature
9	980.000	–	984.375	temperature, $\text{O}_3$
10	992.500	–	997.500	temperature, $\text{O}_3$
11	1000.625	–	1006.250	temperature, $\text{O}_3$
12	1010.000	–	1014.375	temperature, $\text{O}_3$

function

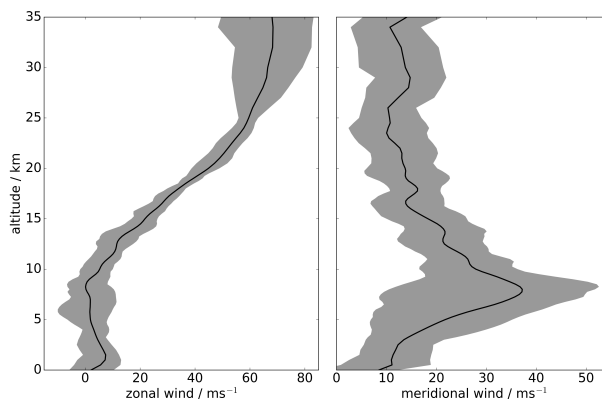
$$J(\mathbf{x}) = (\mathbf{F}(\mathbf{x}) - \mathbf{y})^T \mathbf{S}_\epsilon^{-1} (\mathbf{F}(\mathbf{x}) - \mathbf{y}) \quad (1)$$

has to be minimized. Here  $\mathbf{S}_\epsilon \in \mathbb{R}^{m \times m}$  represents the covariance matrix of the measurement error  $\epsilon$ . To get a unique and well-constrained solution to this minimization problem, a regularization term is added to the cost-function. This term ensures that the solution is physically reasonable.

As a-priori field  $\mathbf{x}_a$  a temperature field from the European Centre for Medium-Range Weather Forecasts (ECMWF) operational analyses at resolution T1279/L137 was used, which was smoothed in all spatial directions to remove GW signatures. In this way, on the one hand, the convergence speed of the iterative minimization is improved, as the temperature background structure is close to the true values due to the high quality of the ECMWF model. On the other hand, the smoothing ensures that any GW structure in the retrieval result does not stem from the used a priori data. If the a-priori data exerts any influence, it would dampen the GW structure.

For the present retrieval we used the spectral ranges listed in Tab. 1. In these spectral ranges the main emitters are  $\text{CO}_2$ ,  $\text{CCl}_4$ ,  $\text{HNO}_3$ , and  $\text{O}_3$ . The volume mixing ratio of  $\text{CO}_2$  is well known in this part of the atmosphere. Therefore, spectral lines of  $\text{CO}_2$  are used effectively for the retrieval of temperature. Tomographic reconstructions of the 3D temperature distribution and the mixing ratios of  $\text{CCl}_4$ ,  $\text{HNO}_3$ , and  $\text{O}_3$  in the upper troposphere and lower stratosphere were achieved. However, a discussion of the trace gas distributions exceeds the scope of this paper.





**Figure 1.** Mean zonal and meridional wind profiles from ECMWF operational analyses T1279/L137 above Iceland and the measurement region at 12 UTC on January 25, 2016. The grey area marks the spread of the wind profiles in this area.

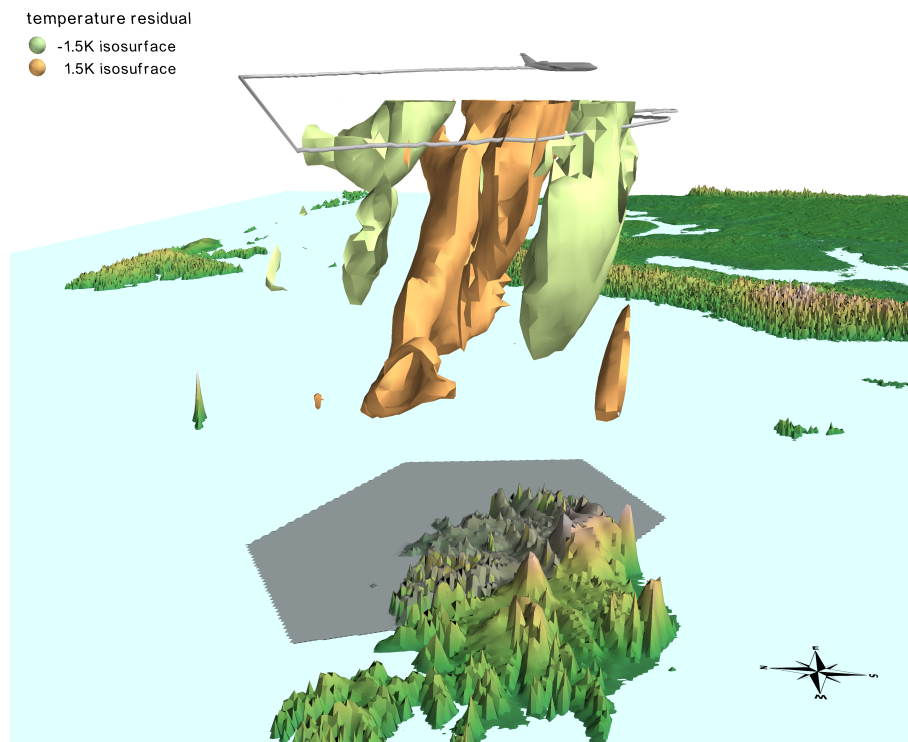
An error analysis of the retrieval has been performed following the methods described in Ungermann et al. (2015). The precision (noise error) is below 0.05 K and the accuracy, which includes misrepresented background gases, uncertainties in spectral line characterisation, uncertainties in instrument attitude, and calibration errors, is in the order of 0.5 K.

The vertical resolution can be defined as the full width at half maximum of the averaging kernel matrix and is around 200 m at an altitude of 11.5 km. The diameter of the smallest sphere containing all elements of the averaging kernel larger than half the maximum, which is a measure for the horizontal resolution (Ungermann et al., 2011), is around 20 km inside the performed hexagonal flight path.

## 2.2 Research flight above Iceland

On the measurement day 25 January 2016, a southerly wind made landfall on the south coast of Iceland (Fig. 1), thus exciting mountain waves. Above 10 km altitude the zonal wind increased drastically with height and turned from southerly to south-westerly direction. This created a strong vertical wind shear, which influenced the propagation of the excited mountain waves as discussed in Sec. 3.2. The wave structure over eastern Iceland was encircled by a hexagonal flight pattern with 460 km diameter between 10 and 12 UTC (Fig. 2). Before the hexagon a linear flight through the wave field has been performed to collect in-situ data at flight altitude and to release dropsondes.

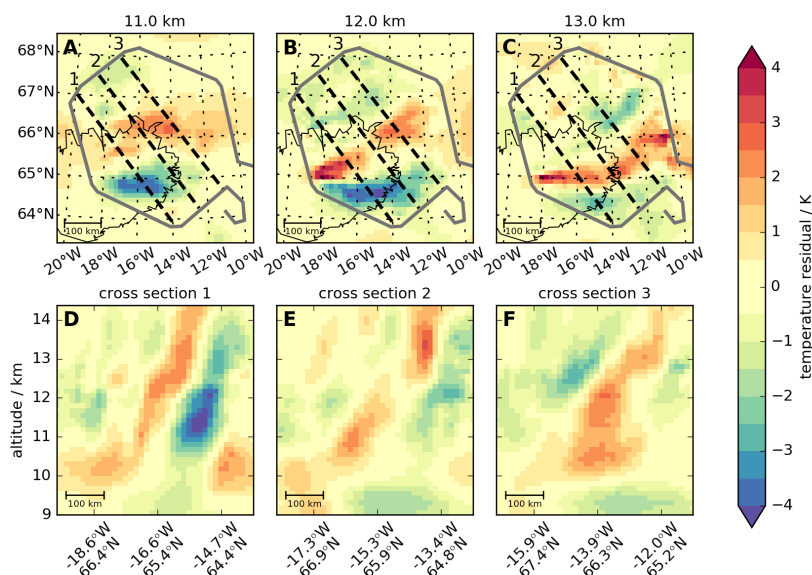
For the GLORIA retrieval only the measurements taken between 10 and 12 UTC have been taken into account. To identify GWs in the retrieved 3D temperature field, the large scale temperature background, which is caused by the balanced flow and the stratification of the atmosphere, has to be separated from the smaller scale temperature variations caused by the GW. This was done through applying a Savitzky-Golay filter (Savitzky and Golay, 1964) to the GLORIA temperature data in all three dimensions. Therefore 3rd order polynomials were fitted to 25, 60, and 60 neighbouring points in the vertical, zonal,



**Figure 2.** Tomographic retrieval of the temperature field for the research flight on January 25, 2016, over Iceland. The grey line above the retrieved 3D pattern indicates the flightpath. The shadow corresponds to the projection of the observation area on the Earth surface.

and meridional direction. The values of these polynomials at the respective points are taken as temperature background. The remaining temperature residuals clearly reveal the complex structure of the wave field, which can be seen in 3D in Fig. 2.

In Fig. 3, horizontal and vertical cross sections through the measurement volume are presented. They show how the wave structure varies with height and horizontal location. For instance, the wave fronts directly above Iceland ( $64^{\circ}\text{N}$  to  $65.5^{\circ}\text{N}$  and  $14^{\circ}\text{W}$  to  $18^{\circ}\text{W}$ ) are aligned east-west and tilted southwards against the prevailing southerly wind (Fig. 1). Further to the north-east ( $65^{\circ}\text{N}$  to  $67^{\circ}\text{N}$  and  $10^{\circ}\text{W}$  to  $14^{\circ}\text{W}$ ), the horizontal orientation of the wave fronts turns more into south-west to north-east. The horizontal wavelength varies inside the hexagon from 100 km up to 350 km. The vertical wavelength of the waves is between 3 km and 6 km. The temperature residuals range from  $\pm 4$  K (in the south-west of the hexagon at an altitude of 12 km,  $64^{\circ}\text{N}$  to  $65.5^{\circ}\text{N}$ , and  $14^{\circ}\text{W}$  to  $18^{\circ}\text{W}$ ) down to  $\pm 1$  K (in the smaller scale waves in the north-western part of the hexagon at  $66^{\circ}\text{N}$  to  $68^{\circ}\text{N}$  and  $16^{\circ}\text{W}$  to  $20^{\circ}\text{W}$ ).



**Figure 3.** Horizontal (A-C) and vertical (D-F) cross sections through the 3D volume shown in Fig. 2. The grey line marks the flightpath. The locations of the vertical cross sections are indicated by numbered dashed lines.

### 3 Analysis

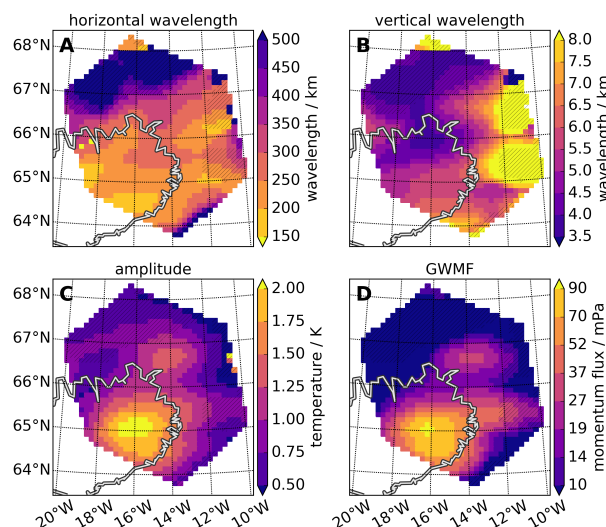
#### 3.1 Sinusoidal wave fits

In order to further interpret the GW structure and fully characterize it, wave parameters are derived using a small-volume few-wave decomposition technique (Lehmann et al., 2012). The algorithm performs 3D sinusoidal fits in small data cubes. In such a way, the wave amplitude, horizontal and vertical wavelengths, and 3D wave direction can be derived. In contrast to a Fourier transform, this technique allows for the characterization of waves with wavelengths larger than the cube size (up to a factor of 2.5 times the cube size). Due to the prevailing wavelength range in our measurements (cf. Fig. 2), a cube size of 160 km x 160 km x 3.6 km, containing 4900 data points, was chosen. The fitted parameters are the horizontal (Fig. 4A) and vertical (Fig. 4B) wavelengths, including the 3D direction of the wave vector and the amplitudes (Fig. 4C) of the waves.

A key quantity of GWs is the vector of vertical flux of horizontal pseudo-momentum (short GW momentum flux, GWMF)

$$F_{ph} = \frac{1}{2} \rho \frac{k_h}{m} \left( \frac{g}{N} \right)^2 \left( \frac{\hat{T}}{T} \right)^2 \quad (2)$$

where  $\rho$  represents the air density,  $k_h$  and  $m$  the horizontal and vertical wavenumbers,  $g$  the standard gravity,  $N$  the buoyancy,  $T$  the background temperature, and  $\hat{T}$  the temperature amplitude (Ern et al., 2004). The GWMF is a measure for the momentum carried by a GW and determines the strength of the coupling of a GW with the background and how much drag a GW can exert on the atmosphere.



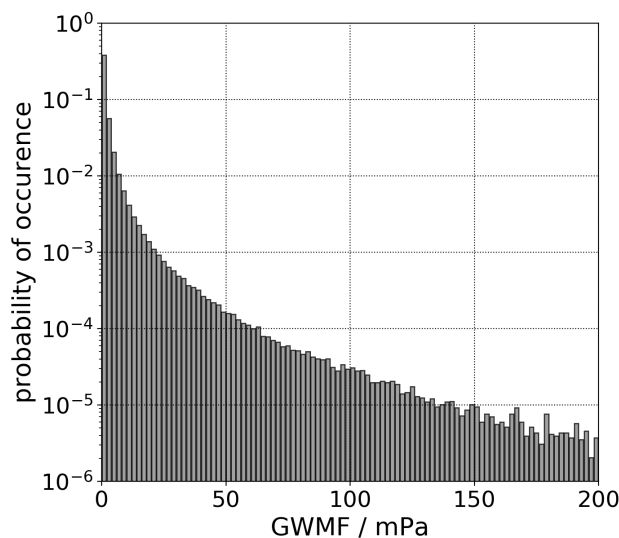
**Figure 4.** 3D sinusoidal wave fit of the GLORIA measurements in fitting cubes of 160 km x 160 km x 3.6 km at a center height of 11.5 km. Non-significant fitting results with wavelengths above 2.5 times the cube size are hashed. These parameters are used to drive the GROGRAT model, the results of which are shown in Fig. 6

The fitted wave parameters in Fig. 4A - C are used to calculate the GWMF (Fig. 4D). The horizontal distribution of the GWMF clearly highlights two distinct wave packets: one with local GWMF of up to 50 mPa around 66.5°N, 14°W and one with local GWMF of up to 100 mPa south of 66°N and between 14°W and 18°W. This distribution of GWMF allows for the estimation of the total momentum contained in these GW packets, if we integrate over their respective area. The wave packet further south has a total momentum of 2.7 GN, the second wave packet further north only 0.4 GN. The total momentum of all the measured GWs above Iceland is 3.1 GN.

To classify this event, a comparison of all GW events in January 2016 has been performed in the operational analyses of ECMWF (Fig. 5). This indicates our event as very strong as only 0.14% of all GW occurrences during this period have a higher GWMF. This occurrence frequency is in good agreement with Alexander et al. (2010), Hertzog et al. (2012), and Podglajen et al. (2016) who present satellite and super-pressure balloon measurements at slightly higher altitudes.

### 3.2 Wave propagation with GROGRAT

In order to identify the GW source, we used the Gravity wave Regional Or Global RAY Tracer (GROGRAT; Marks and Eckermann, 1995). GROGRAT describes the propagation of wave packets based on linear wave theory. Backward ray-tracing has been used in previous studies to characterize GW sources (Preusse et al., 2014; Pramitha et al., 2015). In order to initialize a ray-tracer, the wave must be fully characterized. This capability is the main advance of the GLORIA observations to previous remote sensing observations of temperature. GW parameters obtained from single vertical temperature profiles, lead to a cone of potential source regions instead of a precise source location (Gerrard et al., 2004). This is the reason why GWMF data from



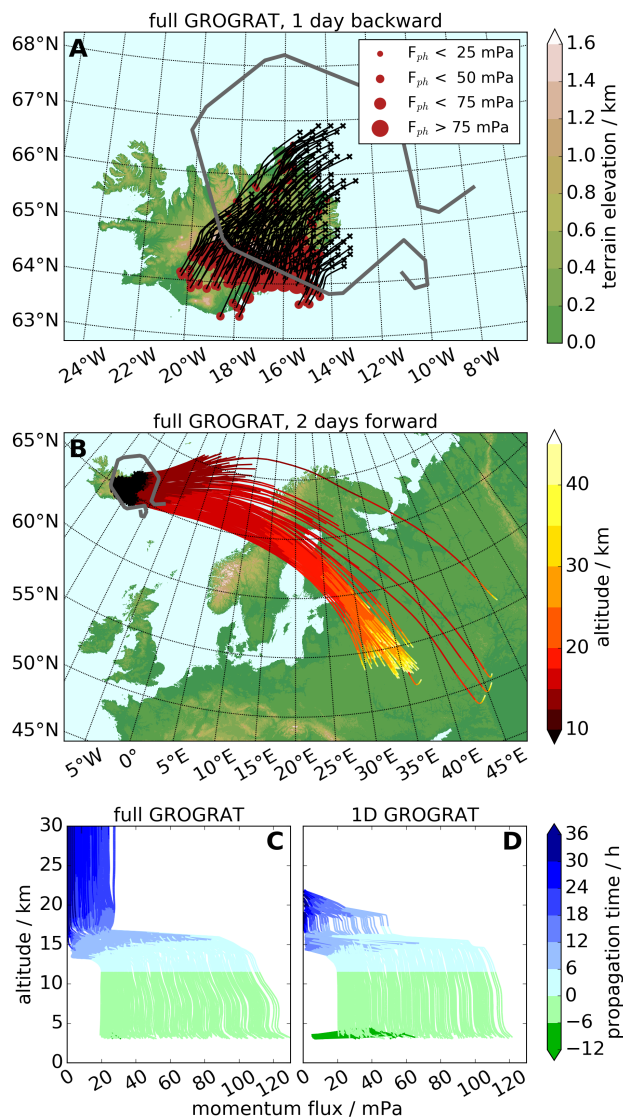
**Figure 5.** Probability of occurrence for GWs with specific momentum flux at 11.5 km altitude in a latitude band between 60°N and 70°N in January 2016 calculated from 6-hourly ECMWF operational analyses fields.

conventional limb scanners has not been interpreted in terms of backward ray-tracing. Only the 3D nature and accuracy of the GLORIA measurements allows backtracing to the precise source location. This is further highlighted by the error analysis presented in appendix A.

In the error analysis, a systematic low bias of the vertical wavelengths was found, which is caused by the sinusoidal fit (appendix A). Therefore, the vertical wavelengths from the sinusoidal fits were scaled by a factor 1.1, according to the determined bias, before being used for the ray-tracing. For the propagation of GWs in a ray-tracing model temporally and spatially varying background temperature and wind fields are needed, which were obtained from ECMWF operational analyses.

Fig. 6 shows the backward ray-traces of the measured GWs from their measurement position (black crosses) down to the source location (red dots). The measurement position has been defined as the center point of the sinusoidal fitting cube. The strength of the GW is expressed by the size of the red dots, which has been chosen according to the GWMF at the source location. The source locations of the GWs, and in particular those of the highest GWMF, gather around the main mountain ridge of Iceland. The GWs are, thus, likely to have been excited by the southerly wind approaching these mountains about 6 hours before the measurements. The ray-traces from the wave packet measured further in the north partly also stop in the north of the island at single mountain peaks.

Forward ray tracing is used to examine the propagation of the GWs away from the measurement location (Fig. 6B). On the measurement day, the southerly wind turned into a strong westerly direction above 10 km, creating a strong vertical wind shear. In this wind shear the GWs started to propagate eastward. This is confirmed by the measurements: at 11 km (Fig. 3A) the GWs are mainly located above the eastern part of Iceland, while at 13 km (Fig. 3C) the wave fronts already stretch far across the ocean. The waves require about one day to propagate to an altitude of 20 km (Fig. 6C). At the same time, they travel



**Figure 6.** Ray traces calculated using the GROGRAT model. The starting positions of the rays are marked with black crosses and the grey line indicates the flight path. The size of the red circles in A indicates the GWMF at the end of the ray. Panel A shows the backward ray traces and panel B the forward ray traces, all starting at the measurement locations. Panels C and D show the change of GWMF with height for a full 4D GROGRAT (C) model run and a solely vertical 1D run (D).

horizontally more than 2000 km (Fig. 6B). In the wind shear below 20 km, the horizontal wave vectors turn from southward to westward, which then allows for a quick upward propagation into the westerly wind in the mid stratosphere.

To mimic a typical GW parameterization scheme used in GCMs (McLandress, 1998), a second GROGRAT run (1D-GROGRAT) was performed with solely vertical propagation, time-independent background, and a horizontal wave direction



constant with respect to altitude. In contrast to the full GROGRAT version (Fig. 6C), where the GWs propagate into the mid stratosphere, the GWs in the simplified version dissipate below 20 km (Fig. 6D). Accordingly, the degree to which GW propagation is simplified determines the location and altitude at which GWMF is deposited. This is also very important for climate and weather prediction models, which often have difficulties in applying the drag of dissipating GWs at the correct altitude and location (McLandress et al., 2012). The importance of oblique propagation highlighted here corroborates results of several model studies (Sato et al., 2009; Preusse et al., 2009; Kalisch et al., 2014; Ribstein and Achatz, 2016) and could close gaps of GWMF in regions with sparse sources (McLandress et al., 2012).

#### 4 Conclusions

In this paper, we presented the first tomographic measurements of temperature perturbations induced by a GW event. The 3D measurements recorded by GLORIA, the first airborne implementation of a novel limb imaging technique, enabled the deduction of direction-resolved GWMF and the identification of two distinct wave packets. The retrieved 3D wave vectors were used as input in the ray-tracing model GROGRAT, which highlighted the orography of Iceland as the most likely GW source. Furthermore, upward from 11 km the wave packets propagate obliquely as is seen from the observation and reproduced by the ray-tracer. A comparison between the full GROGRAT model and a simplified 1D version indicated the relevance of oblique propagation for the GWMF deposition height. In the simplified version, all GWs deposited their momentum at an altitude of around 20 km, whereas in the full version, waves were able to vertically propagate to the top of the model at 45 km and horizontally more than 2000 km away from their source, thus redistributing GWMF significantly. Given that weather prediction and climate models routinely use 1D models of GW propagation, the present findings demonstrate that considering 3D propagation could lead to significant improvements in weather forecasting and climate prediction.

*Data availability.* The tomographic retrieval data is available on the HALO database (<https://halo-db.pa.op.dlr.de/>).

*Competing interests.* The authors declare that they have no conflict of interest.

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## Appendix A: Error analysis

In this section the effects of different errors onto the ray-tracing results presented in Section 3.2 are discussed. These errors may, in principle, be caused during each of the three main processing steps: temperature retrieval, background removal and sinusoidal wave fits (S3D). Retrieval errors can be divided into precision and accuracy (cf. Section 2.1). Due to the high number of independent data in each S3D cube, the precision error (mainly due to noise) can be neglected, in particular since in this paper only GW events with amplitudes above a threshold of 0.5 K are considered. The error sources which lead to the accuracy error are systematic and slowly varying. Thus, their impact is mostly mitigated by the background removal.

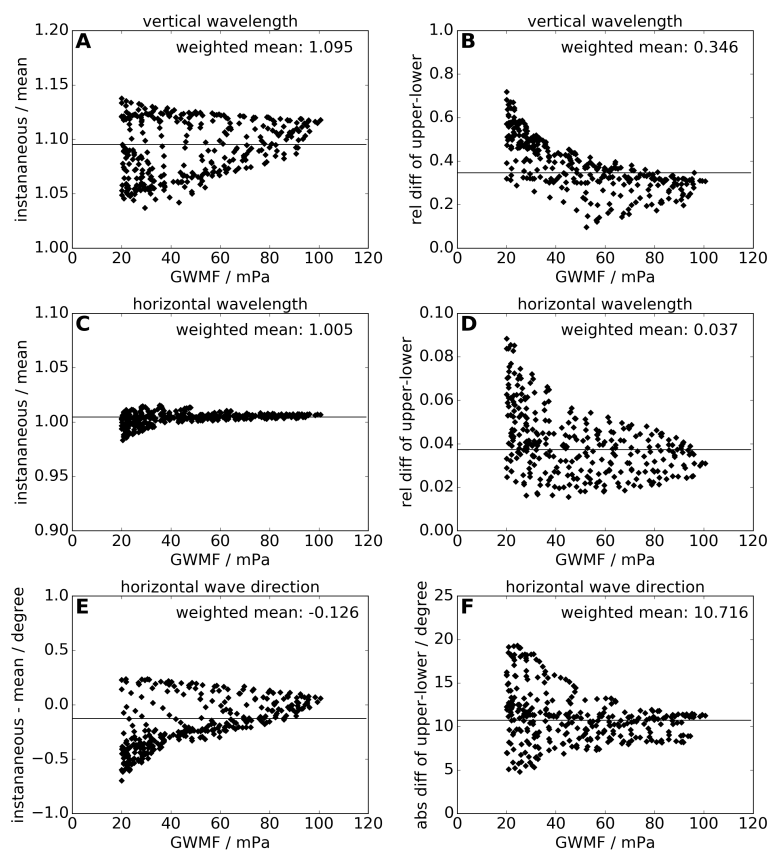
The background removal separates the data into large scale variations and short scale fluctuations, the latter interpreted as GWs. The main effect of an unfavorably tuned background removal would be to eliminate real GWs. However, it would not introduce errors in the fitted wave vectors. Thus, this has to be considered in a comparison with other data, but is not included in the further error discussion.

The third step, the S3D method, is based on the assumption that the fitting volume is filled by a homogeneous wave with a constant wave amplitude and a constant wave vector over the fitting volume. The discussion in sections 2.2 and 3.1 demonstrates that this assumption is only valid to a certain degree. In particular, we notice that the direction of the horizontal wave vector and the vertical wavelength change with height as the wave is refracted by a changing background wind.

We use the results of the ray-tracer to estimate errors due to this change over height within the fitting volume. In Fig. A1 left column the instantaneous value  $\xi_{z=11.5}$  at the middle point of the fitting volume of each individual ray is compared to an average value  $\bar{\xi}$  over the full height range of the S3D fitting volume (comparable to the S3D fitting result); here  $\xi$  stands for either the vertical or horizontal wavelength or the horizontal wave direction. The mean vertical wavelength shows a systematic low bias of around 10% compared to the instantaneous value in the middle (Fig. A1 A). This effect is taken into account and all vertical wavelengths from the sinusoidal fit (Section 3.1) are scaled with a factor of 1.1 before being used in the ray-tracing analysis (Section 3.2). For the horizontal wavelength (Fig. A1 C) and the horizontal wave direction (Fig. A1 E) no systematic bias could be identified.

As mentioned before, the accuracy with which the input wave parameters  $\xi$  are determined is of high importance. This is highlighted through varying the values  $\xi$  by factor  $\epsilon_\xi$  and comparing the ray-tracing results with a reference run. The variations  $\epsilon_\xi$  for the vertical wavelength and the horizontal wave direction are chosen to be half the difference of the wave parameters at the upper ( $\xi_{z=max}$ ) and lower ( $\xi_{z=min}$ ) boundary of the S3D fitting volume as determined by the ray-tracing reference run (Fig. A1 B, F). The horizontal wavelength does not change much over the height of the fitting volume (Fig. A1 D). However Fig. 3 and Fig. 4 indicate a significant variation of the horizontal wavelength over the horizontal extent of the fitting volume. Hence, for the error estimate ray-tracing calculations we chose an error value of  $\pm 15\%$  as estimate for the horizontal variation of the horizontal wavelength within the S3D fitting volume. In Tab. A1 the used error estimates for the three wave parameters are summarized.

The results of the back-tracing runs with wave parameters varied by the error estimates in Tab. A1 are shown in Fig. A2. Longer vertical wavelengths (Fig. A2 C-D) lead to more northward located sources, while rays from shorter vertical wave-



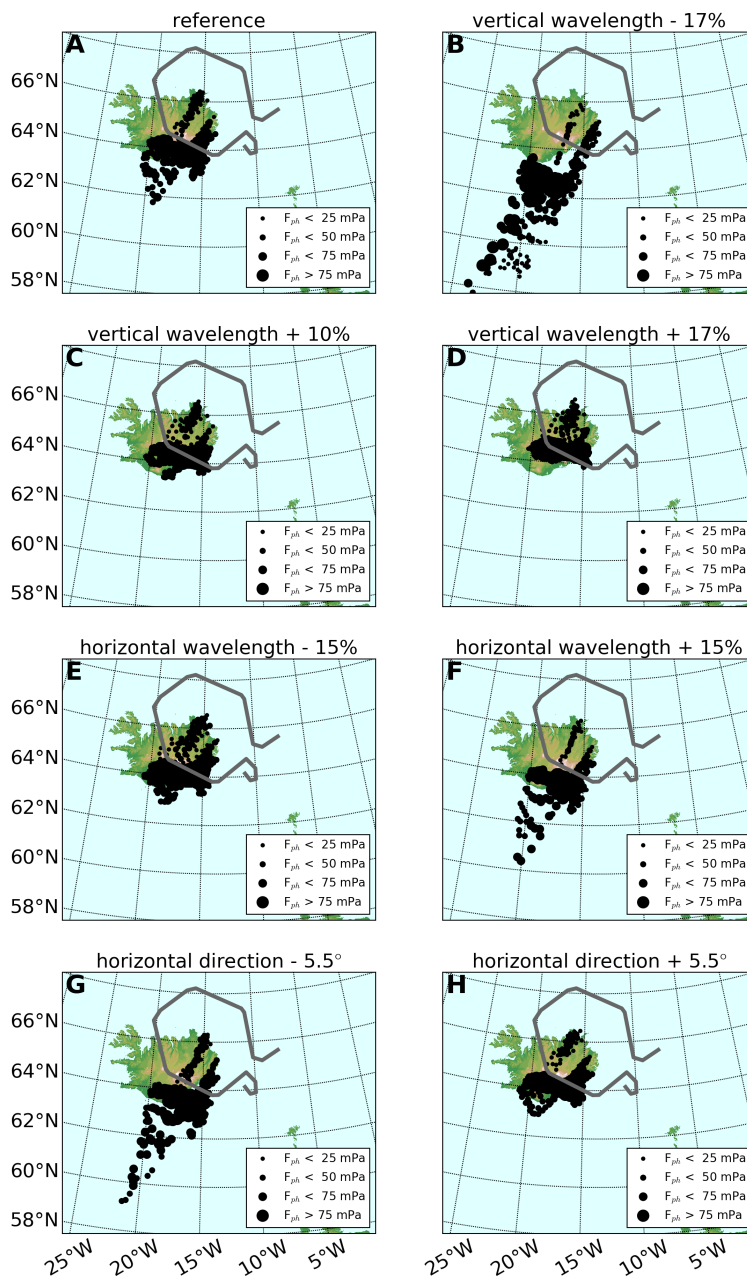
**Figure A1.** Comparison of mean values over the whole S3D fitting volume and instantaneous values in the middle for different wave parameters (left column) and variation of wave parameters from the lower to the upper boundary of the S3D fitting volume (right column). For all graphs GWMF weighted means are calculated and depicted as black lines.

**Table A1.** Error estimates for the wave parameters inferred by the S3D method based on the change of the parameters over the extent of the fitting cube.

error estimate of the vertical wavelength	$\pm 17\%$
error estimate of the horizontal wavelength	$\pm 15\%$
error estimate of the horizontal wave direction	$\pm 5.5^\circ$

lengths (Fig. A2 B) end southward, i.e. upstream of Iceland over the ocean. This is due to the fact, that longer vertical wavelengths are associated with higher horizontal phase velocities and hence higher horizontal group velocities. Accordingly, in the case of shorter vertical wavelengths the waves are not able to compensate the background wind velocity and would origin from an upstream source. Actually, we find that the inferred bias (10% larger values for the vertical wavelengths), when corrected,  
 5 improves the match of the ray-positions with the topography (Fig. A2 C).





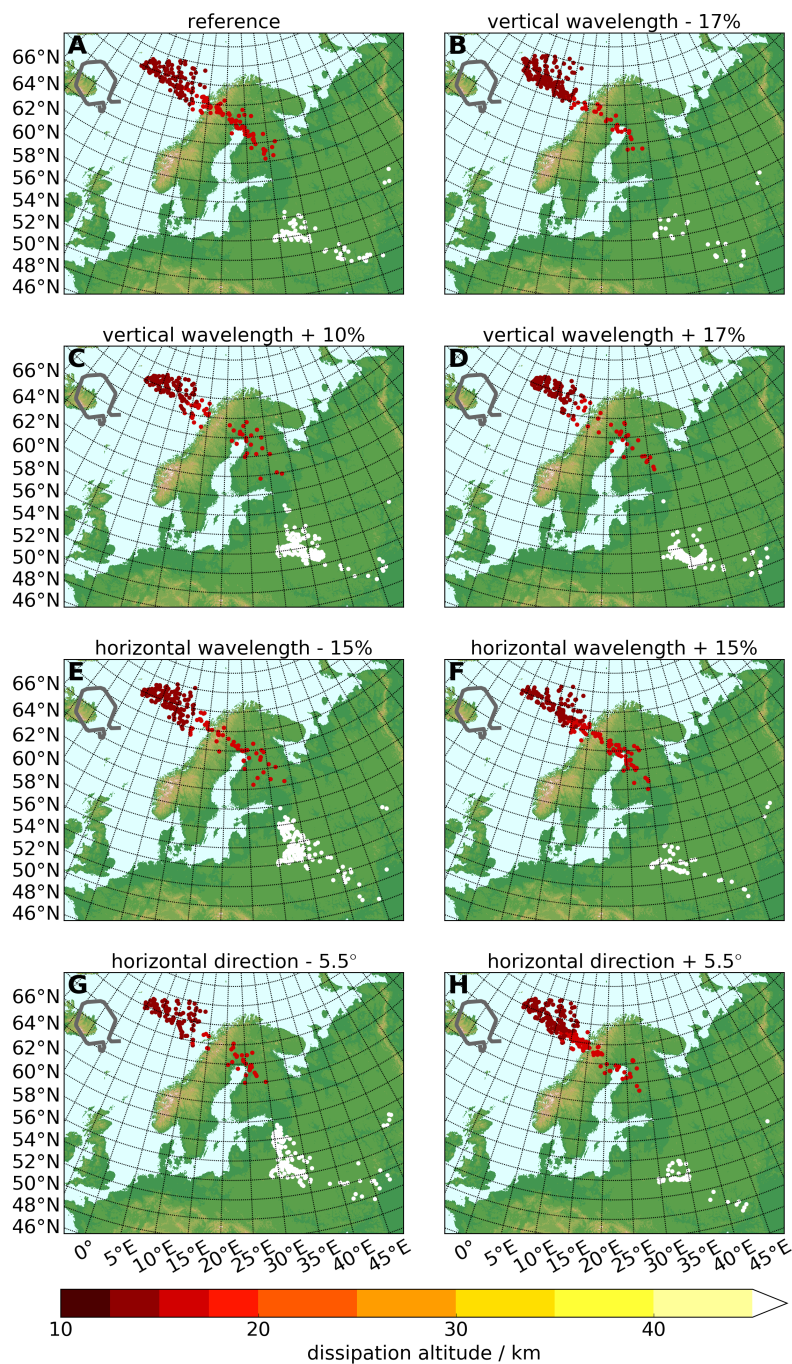
**Figure A2.** Backward ray-tracing with varying input wave parameters. The black dots mark the ray positions at 3 km altitude.



The horizontal wave direction has similar impact: When the wave is turned more into the south-easterly background flow (Fig. A2 H) the ray-paths are more vertically oriented and therefore reach the ground closer to the measurement volume. When they are turned away from the background wind (Figure A2 G), the intrinsic group velocity and the background wind are at an angle, the intrinsic group velocity does not fully compensate the background wind, and the waves cover a larger horizontal distance reaching onto the ocean upstream of Iceland.

Similar variations for the forward ray-traces are shown in Fig. A3. In all cases except for shorter vertical wavelengths, a major group of ray-traces reaches the model top at 45km altitude (white dots), i.e. our main findings presented in Sec. 3.2 are robust.

The error estimates demonstrate that a correct identification of the GW source is only feasible for highly accurate wave characterization, such as achieved here thanks to the high spatial resolution and accuracy of GLORIA 3D temperature measurements.



**Figure A3.** Forward ray-tracing with varying input wave parameters. The dots mark the dissipation point of the ray, the colour indicates the dissipation height. White dots mark waves which reach the model top at 45 km altitude.