

## Response to the Reviewer.

In most cases, the responses of the authors have been acceptable. Specifically with the raising of the mast over the desert on the 23rd, most of the comments and analyses have been modified to reflect this more objectively and correctly. Some of the other weaknesses have also been appropriately addressed, e.g. justifying the constant flux layer hypothesis. The authors also interpret results more cautiously when attributing the observed differences in the imbalance term between the forest and the desert, to a secondary circulation.

However, the manuscript still feels incomplete, particularly because of the heavily underutilized Doppler wind lidars. As it currently stands, these lidars are only mentioned in Appendix B - which is not even referenced in the main text at all. As such, Figure 7 contradicts the time series of  $\langle W \rangle$  from the sonics - but this is not explained or even mentioned at all in the present version of the manuscript.

I propose another major revision of the manuscript, by incorporating more analyses involving the two Doppler wind lidars. In doing so, the authors have a unique opportunity to provide another view of the secondary circulations which hasn't been explored so far. I believe that such analyses will substantially increase the value of this study.

[We thank the reviewer for the constructive comments and suggestions.](#)

## Major comments

**Page 4, line 20:** Although you apply planar fit now, you still don't incorporate the directional shear  $v'w'$ , in the definition of the friction velocity. It's likely it won't alter the current  $u^*$  values that much, but it should still be included for completeness;

[It is included in the computations. The text is updated to reflect this.](#)

**page 5, line 28:** how was  $\delta$  obtained?

[The boundary-layer was detected from a decrease in the backscatter coefficient between the aerosol-laden boundary layer and the clean free atmosphere following the method outline in M \$\ddot{u}\$ nk \$\ddot{u}\$ l et al. \(2007\). However, the boundary-layer height is not used in manuscript anymore and we didn't include this to the methods for this reason. We have now removed the mention of the boundary layer height since it is not relevant to the discussion anymore.](#)

[M \$\ddot{u}\$ nk \$\ddot{u}\$ l C., Eresmaa N., R \$\ddot{a}\$ s \$\ddot{a}\$ nen J., Karp \$\ddot{p}\$ inen A. \(2007\): Retrieval of mixing height and dust concentration with lidar ceilometer. Boundary-Layer Meteorology 124\(1\):117-128](#)

**page 7, line 1:** Is the mean vertical velocity that is plotted in Fig. 2, the vertical velocity that is rotated with the planar fit procedure?

[It is the rotated vertical velocity. The text is updated to reflect this.](#)

**Fig. 2 and Fig. 7:** This is where the major drawback of this study lies: In addition to these two figures contradicting each other, it remains unclear why that would be so since the authors do not address it at

**all. First, the authors do not compare Fig. 7 with Fig. 4a,b in Eder et al (2015, AFM). Their LES results and your lidar results are in agreement (at least in terms of the sign of average vertical velocity).**

The results of Fig. 7 are in qualitative agreement with Fig. 4 of Eder et al. (2015), but it should be noted that their Fig. 4 shows a spatial and temporal average for a 30 min interval, while our results are a temporal average over multiple days. Because of this discussion, we realize that figure 2 and 7 should not be compared with each other as they represent different scales in space and time. Figure 2 shows the nature of fine scale turbulence, while figure 7 shows more of the large scale motions spanning the whole boundary layer. However, we have updated figure 7 with the figure attached in this letter.

**Second, it's obvious from Fig. 7 that at the lowest range gates of both lidars, the vertical velocities converge to zero, perhaps maybe even changing signs very near the surface - which would then be in accordance with Fig. 2. However, this area is under the influence of the dead zone from the lidars, so only speculation is allowed. Even so, it remains clear from Fig. 7 that, throughout the CBL, it is the desert that experiences a downdraft and the forest is the one associated with an updraft. This is in contradiction with the general conclusion of the study, i.e. with the orientation of such a secondary circulation that the authors suggest exists (based on Imb and triple-order moments analyses).**

We want to structure our reply in four parts: first, we discuss the quality of  $w$  from the Doppler lidar, then further indicators for a change of sign in  $w$  near the surface are discussed and, lastly, our thinking about the contradiction.

(1) The  $w$  from the Doppler lidars is uncorrelated with the horizontal wind speed and direction, which indicates that the measured  $w$  is not a projection of the horizontal wind speed into the vertical component due to bad instrument leveling. Further, the measured profiles agree with results of highly detailed LES simulations of Yatir forest by Kröniger et al. (accepted and in production).

Kröniger, K., De Roo, F., Brugger, P., Huq, S., Banerjee, T., Zinsser, J., Rotenberg, E., Yakir, D., Rohatyn, S., and Mauder, M. (2018). Effect of secondary circulations on surface-atmosphere exchange of energy at an isolated semi-arid forest. *Boundary-Layer Meteorol.*, Accepted, doi: 10.1007/s10546-018-0370-6.

(2) Averaged  $w$ -profiles from the Doppler lidars for different times of the day show that during the night the desert has larger  $w$  compared to the forest up to 500 m a.g.l. But this phenomenon sinks towards the surface during the day and was partly masked in previous version of Fig. 7 of the manuscript by the height averaging bins of  $z/\delta$ . Figure 1 below shows separate  $w$ -profiles for different times of the day without normalization by  $\delta$ , where the described phenomena can be seen. As the reviewer has mentioned, the profiles above the desert and forest do actually cross over, as seen from figure 1 below. Especially during noon time, the forest is associated with downdrafts and the desert is associated with updrafts. From figure 1, noon and daytime profiles show this cross over at the lowest levels. This phenomenon is observed from the lidars up to a height of about 100m. So we have updated figure 7 with this figure.

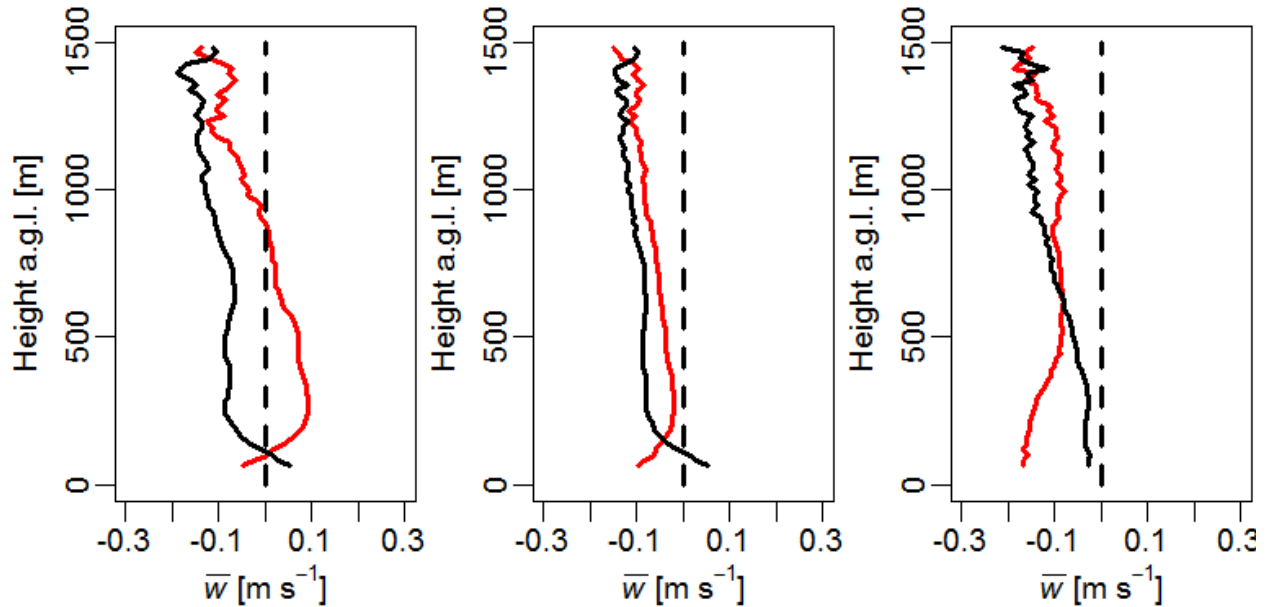


Figure 1: Vertical mean velocity profile averaged from 18 – 29 August (only times with both instruments simultaneously online and the nearest three range gates are discarded). Left to right: Four hour window centered on noon (this corresponds to the old Fig. 7 of the manuscript), day time (sunrise to sundown) and night time (sundown to sunrise). The forest is shown as a solid red line, the desert as solid black line, and a vertical line at  $\bar{w} = 0$  as black dashed line. Note that near the surface the desert has always larger  $w$ , but only during the noontime with the updrafts of the forest is a change of sign.

(3) We have yet to understand this phenomenon, but we believe it is connected to the particular topographical surroundings of the measurement sites. This educated guess is supported by positive  $w$  near the surface in LES of Yatir forest without topography (Eder et al., 2015 or Kröniger et al., accepted and in production). Also in terms of foot-prints, the  $w$  of the EC station only account for the very near surrounding of the measurement sites, while mid boundary-layer measurements of the Doppler lidars are more representative of the forest as a whole.

Another insight from this discussion is that the secondary circulation cannot be thought of as a single large rotational system spanning from the desert and forest, rather a much more complex and three dimensional structure. *Close to the surface layer and the canopy sublayer, the transport of energy is indeed from the desert to the forest (Fig. 5 in the manuscript draft). Further, we observe that the desert has more updrafts and the forest has more downdrafts close to the surface (Fig. 1 and 7 (new) in the manuscript draft). However, as we go up above roughly 100m, this behavior flips (new Fig. 7 in the manuscript draft). Lastly, Kröniger et al. (accepted and in production) found in his simulations that large rotational systems developed at specific locations connected to surface features. Therefore, we conclude that the bulk transport in the convective mixed layer by a secondary circulation is from the forest to the desert, but advected with the mean wind and heavily influenced by surface features on a smaller scale than the forest itself. This is highlighted more in the text.*

**This raises another question: does the secondary circulation extend all the way to the top of the CBL or just to a certain  $z/\delta$  The discrepancy explained in the previous paragraph would suggest the latter. As pointed out by the authors, an answer may lie in the vertical velocity skewness  $Skw$ . A simple analysis to do would be to, for available times that the lidars were working, obtain vertical profiles of  $Skw$  and inspect their temporal evolution over both the desert and the forest. E.g. plotting a time-height Howmoller diagram for the whole 12 days of the campaign comes to mind. Since the forest experiences negative  $Skw$ , it would be interesting to see how far up this persists. Of course, because a third-order**

**moment is involved, a longer averaging period is required - for instance 1 (maybe even 2) hour (thus skipping the single VAD scan that was performed in between vertical stares).**

We believe the secondary-circulation does extend all the way up the boundary-layer top based on two results from other studies (below a short summary):

- 1) Brugger et al. (2018) observed that the boundary-layer height can be increased by Yatir, if not suppressed by very stable stratification of the free atmosphere or high wind speeds in the boundary-layer. This requires, that the forests effects have already reached the boundary-layer top at the forest site and was in line with an assumed rising of the forest's effects with the convective velocity scale.
- 2) LES simulations of Yatir forest by Kröniger et al. (accepted and in production) showed the horizontal circulations spanning the atmospheric boundary-layer.

The proposed approach with time-height series of the vertical velocity skewness (shown in Fig. 2 below) was not followed, because the skewness is typically positive throughout a convective mixed layer with narrow, intense updrafts and broader, weaker downdrafts (Hogan et al., 2009). The skewness differences due to turbulence production of a canopy are restricted to the canopy sublayer and therefore not visible in the skewness profile of the Doppler lidar at the forest.

Kröniger, K., De Roo, F., Brugger, P., Huq, S., Banerjee, T., Zinsser, J., Rotenberg, E., Yakir, D., Rohatyn, S., and Mauder, M. (2018). Effect of secondary circulations on surface–atmosphere exchange of energy at an isolated semi-arid forest. *Boundary-Layer Meteorol.*, Accepted, doi: 10.1007/s10546-018-0370-6.

Brugger, P., Banerjee, T., De Roo, F., Kröniger, K., Qubaja, R., Rohatyn, S., Rotenberg, E., Tatarinov, F., Yakir, D., Yang, F. and Mauder, M. (2018): Effect of surface heterogeneity on the boundary-layer height: a case study at a semi-arid forest. *Boundary-Layer Meteorology*. DOI: <https://doi.org/10.1007/s10546-018-0371-5>.

Hogan R.J., Grant A. L. M., Illingworth, A. J., Pearson G. N. and O'Connor E. J. (2009): Vertical velocity variance and skewness in clear and cloud-topped boundary layers as revealed by Doppler lidar. *Q. J. R. Meteorol. Soc.* 135: 635–643 (2009), DOI: 10.1002/qj.413

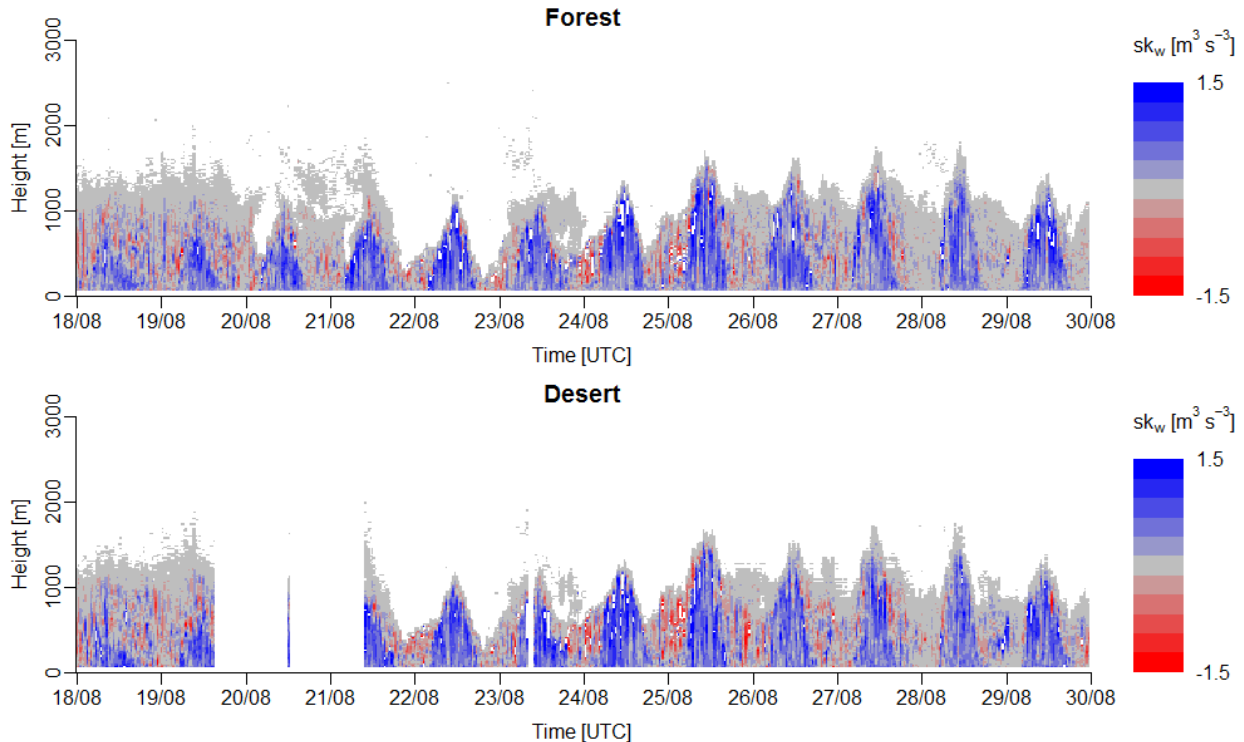


Figure 2: Time-height series of the vertical velocity skewness for the forest (top) and desert (bottom) from the Doppler lidar measurements.

Another useful avenue that would go along the 'eddy size distribution' line-of-thinking that the authors mention in the beginning of the Conclusion, would be to spectrally decompose the lidar-derived Skw. This has been done on several occasions (Hogan et al, 2009, their Fig. 7). By doing this for each range gate, a height-frequency Howmoller diagram could be designed (for a single representative case study, not all 12 days). Such a diagram would then elucidate how each scale of motion contributes to overall Skw. I'm certain some interesting differences between the forest and the desert would become apparent.

As noted above, the LIDAR data can show the skewness only for the convective mixed layer so we are not proceeding forward with this analysis. However, our team is conducting detailed LES studies of the forest-desert system and we will incorporate this analysis with the LES data in a future publication.

page 11, line 6: I'm still not comfortable with bringing ejections and sweeps into the mix here (as I've pointed out in my first response). I agree that they are contributors to third-order moments, but the way you describe it currently makes it seem like ejections and sweeps are related to secondary circulations - which is not true. A word of caution would help here, disclosing the fact that ejections/sweeps are a much finer-scale, smaller-scale motions than secondary circulations.

We have added a note mentioning that all structures visible here are due to the impact of fine scale turbulence.

In line with the spectral decomposition of lidar-derived Skw I mentioned earlier, I wonder if decomposing the mixed third-order moments would reveal some aspects at the low-frequency part of those cospectra? Significant deviations should be expected there, considering the different ranges of signs (between desert and forest) that you obtained in Fig. 6.

Again, this study will be conducted in future with detailed LES analysis.

Also, the fact that higher-order moments require longer averaging times than means and variances, makes me question how reliable the different signs between the forests and desert actually are. Sensitivity analyses of  $\langle w'w'u' \rangle$ ,  $\langle w'w'w' \rangle$  and  $\langle w'w'T' \rangle$  as a function of increasing the averaging time with increments of 30 minutes, would make the results more bulletproof.

Since all the statistics are reported for 30 min periods, we have retained the 30 min averaging, in order to study and compare the same dynamics from different statistics. Changing the length and time scale of the observation, as observed from the difference of LIDAR/EC data in terms of the circulation might tell us about a different dynamics which we might not be studying.

### Minor Comments

page 2, line 5: having both or and etc. is redundant, keep just one of them;

Corrected

page 4, line 16: it's usually referenced as Monin-Obukhov Similarity Theory (instead of Stability);

Corrected

page 8, line 7: 23rd instead of 23th;

Corrected

page 8, line 12: 23rd instead of 23th;

Corrected

page 9, line 1: in the constant flux layer;

Corrected

page 9, line 12: replace summation with sum

Corrected

page 10, line 3: 23rd instead of 23th;

Corrected

page 10, line 12: 23rd instead of 23th;

Corrected

**page 11, line 9: I don't find  $Skw$  being positive over the desert surprising - it is expected to be positive throughout the CBL. It may be surprising because LES typically give negative values of  $Skw$  near the surface, which is an artificial result usually due to SGS motions. What is surprising is the difference in sign between the forest and desert, but you've already attributed that to the presence of the canopy;**

[Noted now in the text](#)

**page 11, line 10: State here as well that the increase in  $Skw$  is likely due to the height change;**

[Stated](#)

**page 11, line 10: 23rd instead of 23th;**

[Corrected](#)

**page 12, line 9: 23rd instead of 23th;**

[Corrected](#)

**page 13, line 4: 23rd instead of 23th;**

[Corrected](#)

**page 13, line 23: This last part is a remnant from the previous version - it should also be removed;**

[Corrected](#)

**Appendix C: Usually it is considered enough to simply cite the relevant literature when mentioning how the coordinate systems were rotated. No need to completely describe the workings of planar fit, since it just lengthens the manuscript unnecessarily;**

[Just mentioned the reference now.](#)

# Turbulent transport of energy across a forest and a semi-arid shrubland.

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**Abstract.** The role of secondary circulations has recently been studied in the context of well defined surface heterogeneity in a semi-arid ecosystem where it was found that energy balance closure over a desert-forest system and the structure of the boundary layer was impacted by advection and flux divergence. As a part of the CliFF (Climate Feedbacks and benefits of semi-arid forests, a collaboration between KIT, Germany and the Weizmann Institute, Israel) campaign, we studied the boundary layer dynamics and turbulent transport of energy corresponding to this effect in the Yatir forest situated in the Negev desert in Israel. The forest surrounded by small shrubs presents a distinct feature of surface heterogeneity, allowing us to study the differences between their interactions with the atmosphere above by conducting measurements with two EC stations and two Doppler LiDARs. As expected, the turbulence intensity and vertical fluxes of momentum and sensible heat are found to be higher above the forest compared to the shrubland. Turbulent statistics indicative of nonlocal motions are also found to differ over the forest and shrubland and also display a strong diurnal cycle. The production of turbulent kinetic energy (TKE) over the forest is strongly mechanical, while buoyancy effects generate most of the TKE over the shrubland. Overall TKE production is much higher above the forest compared to the shrubland. The forest is also found to be more efficient in dissipating TKE. The TKE budget appears to be balanced on average both for the forest and shrubland, although the imbalance of the TKE budget, which contains the role of TKE transport, is found to be quite different in terms of diurnal cycles for the forest and shrubland. The difference of turbulent quantities and the relationships between the components of TKE budget are used to infer the characteristics of turbulent transport of energy between the desert and the forest.

## 1 Introduction

Understanding the interaction between vegetation canopies and atmosphere is a crucial component in quantification of biosphere-atmosphere exchange of heat, carbon dioxide, water and trace gas fluxes. It is also important for the development of numerical weather and climate models where the fluxes in the canopy surface layer (CSL) and the atmospheric surface layer (ASL) are parameterized through bulk exchange coefficients of momentum and scalar. However, idealizations of the forest canopies



as horizontally homogeneous momentum sinks and scalar sources introduces uncertainties in flux estimations and estimating diffusion coefficients. Presence of heterogeneities such as roughness transitions, complex topography, mesoscale circulations etc. are common sources of such uncertainties that give rise to nonlocal motions and secondary circulations. These secondary circulations can occur not only in forests but are generic characteristics of boundary layer flows over natural and man made landscapes with discongruity of land use types, surface moisture, temperature etc. (Higgins et al., 2013; Eder et al., 2015). Different types of land covers such as agricultural lands or urban areas can affect local energy balance closure and the structure of the overlying boundary layer as well as cloud formation and regional weather (Eder et al., 2015; Fuentes et al., 2016). Strong difference of surface properties and large swaths of such surface patches are known to induce secondary circulations (Mahfouf et al., 1987; Dalu and Pielke, 1993; Raupach and Finnigan, 1995; Courault et al., 2007; van Heerwaarden and Guerau de Arellano, 2008; Garcia-Carreras et al., 2010; Banerjee et al., 2013; Dixon et al., 2013; Sühling and Raasch, 2013; Kang and Lenschow, 2014; Van Heerwaarden et al., 2014). Recent works by Mauder et al. (2007), Stoy et al. (2013) and Eder et al. (2014) have suggested that non-closure of energy balance is also related to advection and flux divergence due to secondary circulations (Kanda et al., 2004; Foken, 2008). The non-closure of the energy balance refers to the fact that the available energy  $R_n - G$  is often higher than the turbulent energy  $H + LE$  in micrometeorological sites, where  $R_n$  is net radiation,  $G$  is soil heat flux,  $H$  is sensible heat flux and  $LE$  is latent heat flux. Thus it is established that studies involving surface heterogeneities such as difference of roughness characteristics and albedo are crucial for the advancements of our understanding into biosphere-atmosphere interaction since the quasi-universal scaling laws of turbulent moments and simple parametrizations of exchange coefficients are disturbed and rendered non-operational.

Several studies have attempted to study the nature of turbulence across a roughness transition such as a grassland and a forest canopy by means of experimental and numerical methods (Li et al., 1990; Peltola, 1996; Irvine et al., 1997; Belcher et al., 2003; Yang et al., 2006; Cassiani et al., 2008; Detto et al., 2008; Dupont and Brunet, 2009; Dalpe and Masson, 2009; Fesquet et al., 2009; Gavrilov et al., 2010, 2011; Huang et al., 2011; Rominger and Nepf, 2011; Schlegel et al., 2012; Banerjee et al., 2013; Chatziefstratiou et al., 2014; Markfort et al., 2014; Kanani-Sühling and Raasch, 2015; Queck et al., 2016; Kröniger et al., 2017) and documented several length scales associated with the roughness transitions, recirculation zones and as well as the nature of the turbulent momentum budget. However, all of these studies are concerned with the flow adjustment in the immediate vicinity of the roughness transition (edges or gaps). Eder et al. (2015) have studied the dynamics of the convective boundary layer over a well defined surface heterogeneity- namely the Yatir forest and the shrubland surrounding it which are located in the northern part of the Negev desert in Israel. Eddy covariance (EC) and Doppler LiDAR measurements were conducted by Eder et al. (2015) in two sites, one in the forest and one in the desert approximately 6.5 km apart. The forest has a darker surface and consequently lower albedo (12.5%) than the desert (33.7 %). Moreover, the higher surface roughness of the forest results in higher turbulence intensity, which leads to more efficient heat transfer above the forest, a phenomenon called canopy convector effect (Rotenberg and Yakir, 2011; Banerjee et al., 2017a). The region being very dry, there is very little latent heat flux (Bowen ratio  $> 10$  over the summer), resulting in spatial difference of surface buoyancy flux of  $220-290 \text{ Wm}^{-2}$  between the desert and forest. Furthermore, the length scale of surface heterogeneities (6-10 km) is larger than the minimal length scale needed for development of secondary circulations  $L_{rau} = C_{Rau}U/w_* \approx 2 - 5 \text{ km}$  (Raupach and Finnigan, 1995; Eder et al.,

2015), where  $U$  is mean wind speed,  $w_*$  is the convective velocity scale and  $C_{Rau} = 0.8$ , an empirical parameter, so that it is possible for secondary circulations to develop.

The present work is an attempt to examine this hypothesis of secondary circulations in more detail. We use eddy covariance and Doppler LiDAR measurements at two sites over the shrubland and the Yatir forest 4.3 km apart, where the shrubland is upwind of the forest in the path of the principal wind direction (during the summer, there exists a heat induced low pressure system to the east, resulting in the main wind direction from the north west). We investigate the individual components of the turbulent kinetic energy budget, as well as the nature of advection and turbulent transport over the forest and desert and determine if there is a relationship between them. Not many instances were found in the literature where the nature of turbulent transport was studied across large scale surface roughness heterogeneities, except for Nadeau et al. (2011) and Yue et al. (2015). However, Yue et al. (2015) only studied turbulent production and the turbulent velocity fluctuations in presence of a complex topography - so the nature of turbulent transport via secondary circulations was not highlighted. Nadeau et al. (2011) studied the decay of turbulence over different land surface types. Hence the difference of turbulence production and simultaneous transport across different land use types were not studied, which determines the scope of the current work.

## 2 Method

### 2.1 Theory

The turbulent kinetic energy (TKE) budget without invoking any special assumption is given by (Stull, 2012)

$$\frac{\partial e}{\partial t} + U_j \frac{\partial e}{\partial x_j} = \delta_{i3} \frac{g}{T} \left( \overline{u'_i T'} \right) - \overline{u'_i u'_j} \frac{\partial U_i}{\partial x_j} - \frac{\partial \left( \overline{u'_j e} \right)}{\partial x_j} - \frac{1}{\rho} \frac{\partial \left( \overline{u'_i p'} \right)}{\partial x_i} - \epsilon, \quad (1)$$

where  $i$  and  $j$  are usual tensor indices which can take the values of 1, 2 and 3, to indicate  $x$ ,  $y$  and  $z$  directions respectively and  $\delta_{i3}$  is the Kronecker delta.  $e = (1/2)(\sigma_u^2 + \sigma_v^2 + \sigma_w^2) = (1/2)(\overline{u'^2} + \overline{v'^2} + \overline{w'^2})$  is the TKE,  $U$  denotes mean longitudinal velocity,  $u'$ ,  $v'$  and  $w'$  denote the fluctuations from mean for the longitudinal, transverse and vertical velocity components,  $g$  is acceleration due to gravity,  $T$  denotes mean potential temperature,  $T'$  is the potential temperature fluctuation,  $p'$  is the dynamic pressure perturbation,  $\rho$  is density of air. The first term on the left hand side (LHS) denotes storage or TKE tendency. The second term on the LHS indicates advection of TKE by mean wind flow. The first term on the right hand side (RHS) denotes buoyant production/destruction of TKE. The second term on the RHS denotes mechanical/shear production of TKE. The third term on RHS denotes turbulent transport of TKE and can also be called turbulent flux divergence. The fourth term on RHS denotes transport of TKE by pressure velocity correlation.  $\epsilon$  is the dissipation of TKE.

Expanding the equations in terms of  $x$ ,  $y$  and  $z$  coordinates, the full TKE budget can be written as equation A1 as shown in appendix A. Since it is difficult to keep track of the full equation due to the large number of terms, it would be easier to use a simple form of the TKE budget (Stull, 2012)

$$0 = -\overline{u'w'} \frac{dU}{dz} + \frac{g}{T} \overline{w'T'} - \epsilon - Imbalance. \quad (2)$$

where the *Imbalance* is defined in equation A2. Note that  $\overline{u'w'}$  and  $\overline{w'T'}$  denote vertical momentum flux and sensible heat flux respectively. Also notice that if the term *Imbalance* is set to zero, one recovers the TKE budget for an idealized surface layer where the coordinate system is aligned with the mean wind, and a planar, homogeneous flow with zero subsidence is assumed. Since our objective in the current problem is to study the effect of heterogeneity, we cannot make these assumptions.

5 Moreover, we are also constrained by being able to measure only at two single points in space quite far apart. Single point eddy covariance measurements cannot compute spatial gradients, and the pressure perturbations are not measured either. Thus explicit computations of the imbalance terms are not possible. Due to the three dimensional nature of the problem, it is also difficult to anticipate what degrees of assumptions are sufficient so that some of the terms can be ignored safely.

Under these constraints, a strategy is needed to evaluate the TKE budget. The dominant mechanical production term, the  
 10 buoyant production/destruction term and the dissipation term will be evaluated directly from the data. The residual of the TKE budget will be described as the imbalance as per equation 3 which would contain the effects of advection and transport terms. The advantage of using this strategy is that since the original TKE budget equation has to be closed, the errors in computing the production and dissipation terms can also be assumed to be inside the *Imbalance* term.

$$Imbalance = -\overline{u'w'} \frac{dU}{dz} + \frac{g}{T} \overline{w'T'} - \epsilon. \quad (3)$$

15 To compute the mechanical production term, we momentarily assume that the TKE budget is well balanced and Monin Obukhov ~~Stability~~-Similarity Theory (MOST) (Monin and Obukhov, 1954) is valid (Kaimal and Finnigan, 1994; Banerjee et al., 2016; Li et al., 2016). This allows us to write

$$\frac{dU}{dz} = \phi_m(\zeta) \frac{u_*}{\kappa z}, \quad (4)$$

where  $\phi_m$  is the stability correction function for momentum which varies with the stability parameter  $\zeta = (z - d)/L$  and  
 20  $\kappa = 0.4$ , the von Kármán constant.  ~~$u_* = \sqrt{|\overline{u'w'}|}$~~   $u_* = \sqrt{|\overline{u'w'}|^2 + |\overline{v'w'}|^2}$  is the friction velocity,  $z$  is the measurement height and  $L = -u_*^3 / (\kappa(g/T)\overline{w'T'})$  is the Obukhov length,  $d$  is zero plane displacement height, taken as 2/3 of canopy height. The standard MOST scaling relations for  $\phi_m$  are used, i.e.,  $\phi_m = 0.74 + 4.7\zeta$  for stable ( $\zeta > 0$ ) and  $\phi_m = (1 - 16\zeta)^{-1/4}$  for unstable ( $\zeta < 0$ ) stratification (Businger et al., 1971; Dyer, 1974).

Equation 4 allows us to compute the mechanical production term in equation 2 as:

$$25 \quad -\overline{u'w'} \frac{dU}{dz} = \phi_m \frac{u_*^3}{(\kappa z)}. \quad (5)$$

The buoyancy term can directly be computed from the EC measurements as well. To compute the dissipation term  $\epsilon$ , we use the scaling relation of second order structure function  $D_{uu} = \overline{[u(x+r) - u(x)]^2}$  in the inertial subrange (Salesky et al., 2013; Banerjee et al., 2015, 2016; Li et al., 2016)

$$D_{uu}(r) = C_u \epsilon^{2/3} r^{2/3}, \quad (6)$$

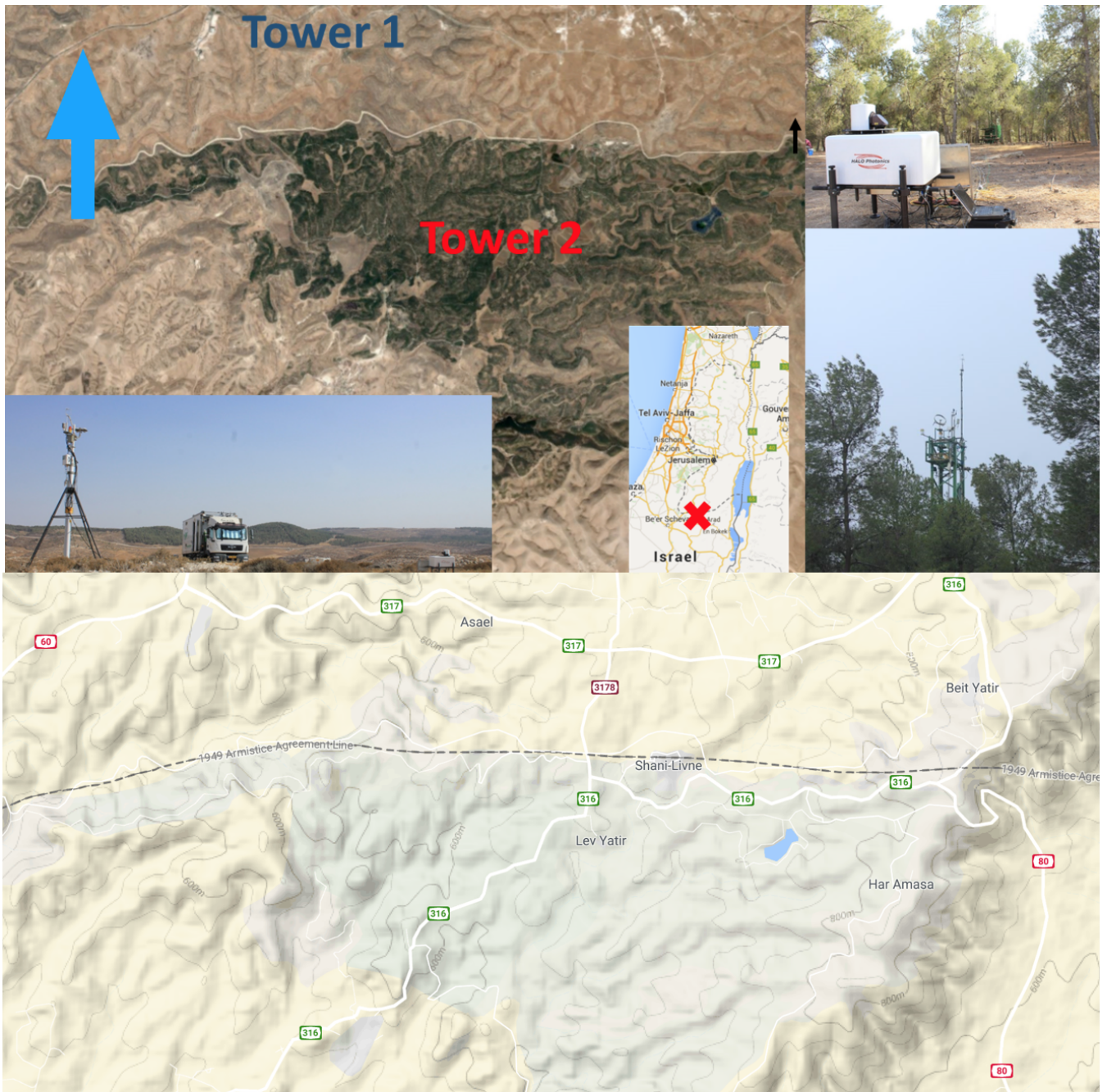
30 where  $C_u \approx 2$  (Stull, 2012), and  $r$  is the spatial lag in the longitudinal direction which can be computed by multiplying the sampling time interval with the mean longitudinal velocity, assuming that Taylor's frozen turbulence hypothesis is valid

( $r = |u| \Delta t$ ). The range of  $r$  where this relation is valid is found to be between 0.2 to 2 m and  $\epsilon$  is found by regression of equation 6. Note that the computation of  $\epsilon$  is independent from any assumptions used to compute the production terms.

## 2.2 Research site

The measurements were conducted in the Yatir forest and the surrounding shrubland in Israel between 18th August and 30th August, 2015 as part of the “Climate feedbacks and benefits of semi-arid forests” (CliFF) campaign, a joint collaboration between Karlsruhe Institute of Technology (KIT), Germany and the Weizmann Institute, Israel. Fig 1 gives an idea about the locations of the EC towers. Tower 1 (Latitude 31.375728, Longitude 35.024262) was located at the semi-arid shrubland 620 m above sea level and tower 2 (Latitude 31.345315, Longitude 35.052224) was located inside the forest 660 m above sea level. The linear distance between the two locations was measured to be 4.3 km and as can be observed from figure 1, there is a distinct surface heterogeneity between the two sites. The climate of the area is in between Mediterranean and semi-arid, with a mean annual precipitation of about 285 mm (Eder et al., 2015). Note that the measurement sites reported in this work are different from those in Eder et al. (2015). The trees in the forest were mostly Aleppo Pine (*Pinus halepensis*), average 10 m in height with negligible height variation. The surrounding land was sparsely populated by small shrubs and in the dry season where the measurements were conducted, was mostly free of vegetation. Thus it is referred to as ‘desert’ for easy distinction (Eder et al., 2015). The measurement height for the forest was 19 m above ground (9 m above the canopy height). Note that with this height selection, the measurements were conducted above the roughness sublayer, which ends at approximately 2 times the canopy height (Harman and Finnigan, 2007). A mast was used over the desert and the measurement height was 9 m until 23rd August, after which it was changed to 15 m for the remaining period. In this zone of the atmospheric surface layer, the longitudinal and crosswise velocity variances decrease logarithmically with height and the vertical velocity variance shows an independence with height (Townsend, 1976; Perry and Chong, 1982; Marusic et al., 2013; Banerjee and Katul, 2013a). High frequency turbulent data were collected at 20 Hz and 30 minutes averaging periods were used for both sites. After conducting quality control of the data following Eder et al. (2015), a planar fit coordinate rotation is applied on the velocity components since the data is collected on a sloped ground. The coordinate rotation following Wilczak et al. (2001) ensures that the cross stream velocity component  $v$  is zero and corrects the tilting of the anemometer with respect to the local streamlines. Moreover, a different set of coordinate rotation is applied for the desert data after 23rd August. ~~More details of the coordinate rotation technique can be found in appendix ??.~~

In addition, two Doppler LiDARs were used at the two locations ~~to measure the boundary layer height as well~~which measured vertical velocities (Brugger et al., 2018; Kroeniger et al., 2018). The Doppler LiDARs used were StreamLine systems from HaloPhotonics. They were operated in a vertical stare mode most of the time (interrupted every half hour for less than 90 seconds). Technical specifications and instrument settings of the Doppler LiDARs are given in Table 1. The Doppler LiDAR at tower 1 was not working from 19.08.2015 - 15:00 UTC until 21.08.2015 - 10:30 UTC and very shortly on the 23.08.2015 around 10:00 UTC due to power cuts.

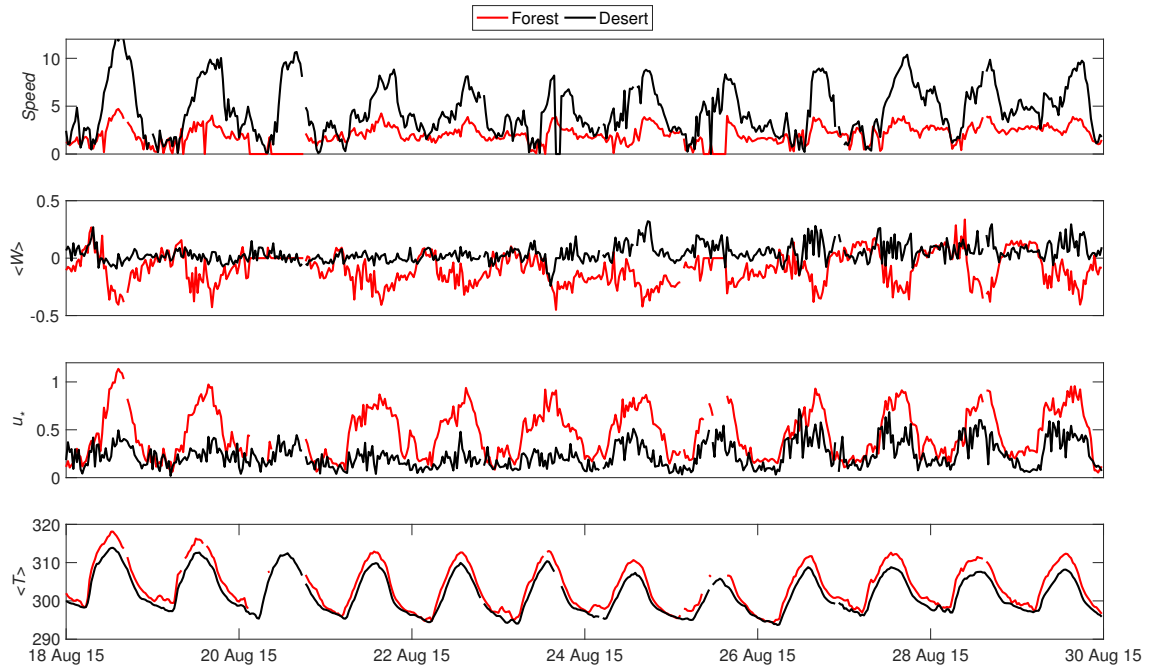


**Figure 1.** Map of Yatir forest in Israel and locations of the measurement stations. Insets: snapshots of measurement set-ups. Bottom panel: topography map of the Yatir forest, from Google maps.



**Table 1.** Instrument specification and settings of the Doppler LiDARs. From top to bottom: Serial number of the forest and desert LiDAR, pulse length of the laser pulse at full width at half maximum, range gate length, pulse repetition frequency, number of averaged pulses for a backscatter coefficient profile and the wavelength of the emitted laser pulse (short wavelength infrared).

Serial numbers	0114-74 and 0114-75
Pulse length	60 m
Range gate length	18 m
Pulse repetition frequency	15 kHz
Averaged pulses per estimate	15000
Wavelength of laser light	1.5 $\mu\text{m}$

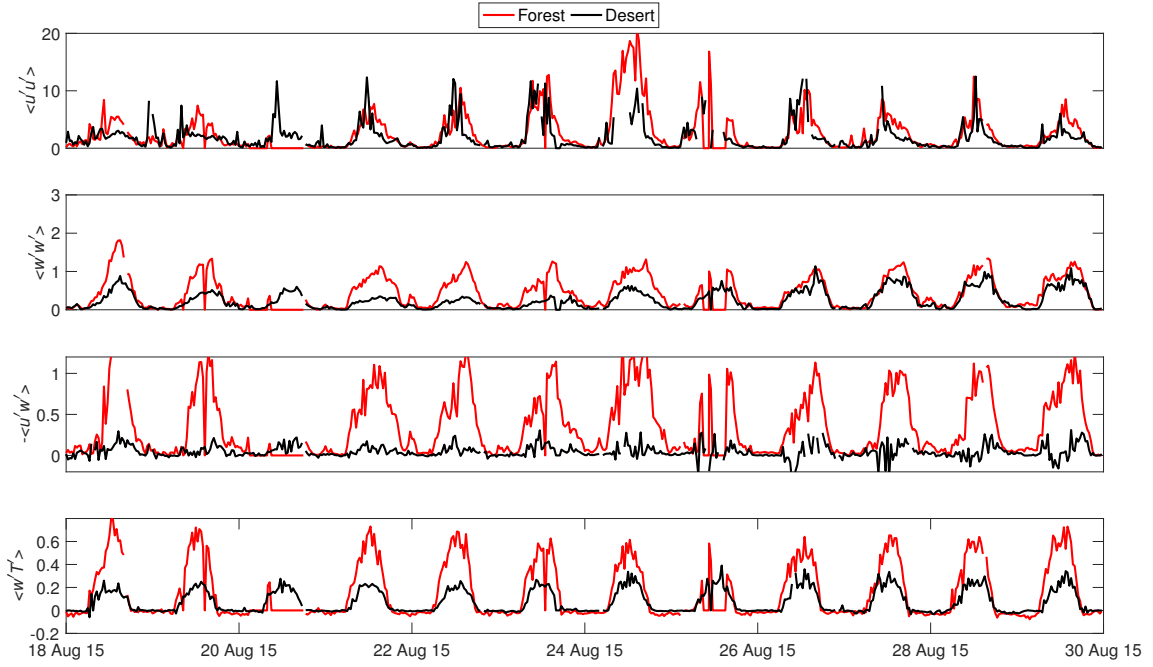


**Figure 2.** Time series of half hourly averages of mean speed ( $\text{ms}^{-1}$ ), mean vertical velocity ( $\text{ms}^{-1}$ ), friction velocity ( $\text{ms}^{-1}$ ) and mean potential temperature (K) for the measurement period. Black line indicates desert and red line indicates forest.

### 3 Results and Discussion

#### 3.1 Time series of turbulence statistics

Time series of mean speed ( $\text{ms}^{-1}$ ), mean vertical velocity ( $W$ ,  $\text{ms}^{-1}$ ) (after applying coordinate rotation) friction velocity ( $u_*$ ,  $\text{ms}^{-1}$ ), mean near surface air (potential) temperature ( $T$ , K), for the measurement period are shown in figure 2. Figure 3 shows

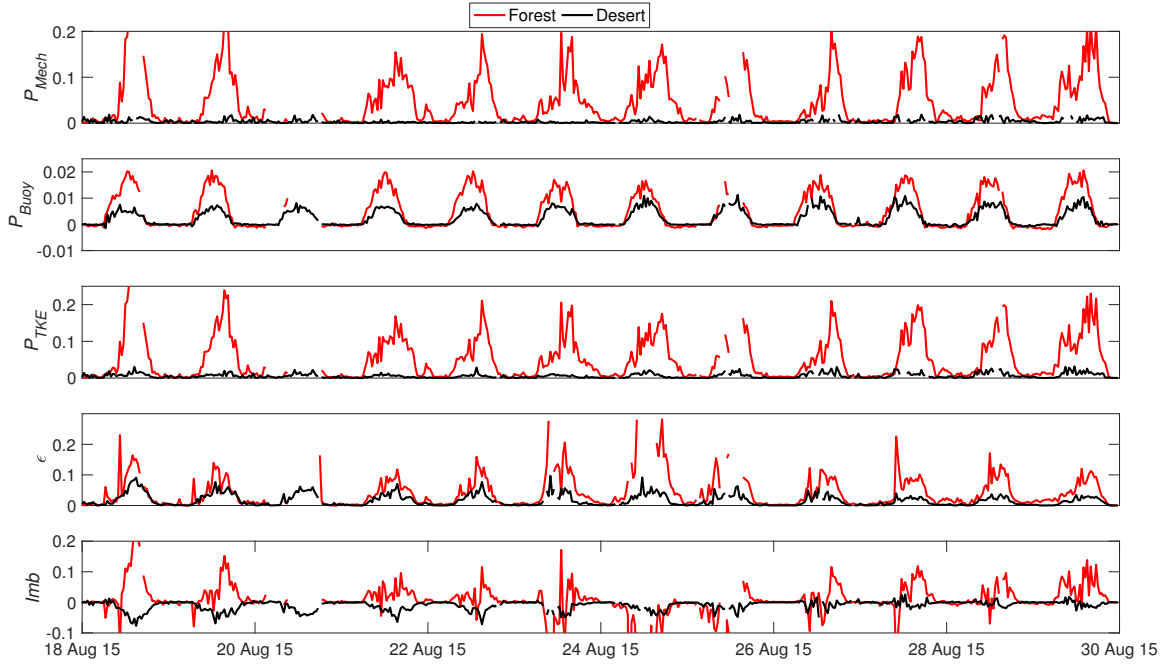


**Figure 3.** Time series of longitudinal velocity variance ( $\text{m}^2\text{s}^{-2}$ ), vertical velocity variance ( $\text{m}^2\text{s}^{-2}$ ), momentum flux ( $\text{m}^2\text{s}^{-2}$ ) and sensible heat flux ( $\text{Kms}^{-1}$ ) for the measurement period. Black line indicates desert and red line indicates forest.

time series of longitudinal velocity variance ( $\overline{u'u'}$ ,  $\text{m}^2\text{s}^{-2}$ ), vertical velocity variance ( $\overline{w'w'}$ ,  $\text{m}^2\text{s}^{-2}$ ), momentum flux ( $\overline{u'w'}$ ,  $\text{m}^2\text{s}^{-2}$ ) and sensible heat flux ( $\overline{w'T'}$ ,  $\text{Kms}^{-1}$ ). Black line indicates desert and red line indicates forest. As noticed, the desert is associated with a higher wind speed because of a lower amount of friction on the desert surface. The higher vertical velocity over the desert indicates the presence of stronger updrafts which would be explained by higher buoyancy driven turbulence.

- 5 The friction velocity ( $u_*$ ) over the forest is much higher compared to the desert, especially in the daytime, which is expected because of higher surface roughness over the forest.  $u_*$  above both the forest and desert shows a strong diurnal cycle. However, there seems to be a prominent increase of  $u_*$  over the desert after ~~23th~~23rd August. This can be attributed to the raising of the tower height. Moreover, the gentle topography around the desert could result in the strong vertical updrafts above the desert. Interestingly, the near surface air temperatures over both the forest and desert show a strong diurnal cycle and their differences
- 10 are about 5K on average during daytime and almost zero at night..

The longitudinal velocity variance  $\overline{u'u'}$  over the forest and desert show similar variations over time. The vertical velocity variance  $\overline{w'w'}$  over the forest is higher than its desert counterpart, however, after ~~23th~~23rd August, the levels of  $\overline{w'w'}$  over desert increases as well and become similar to the forest. It is due to changing the tower height. As the vertical profiles of  $\overline{w'w'}$  are different between the desert and forest (due to roughness length differences), the observed differences between  $\overline{w'w'}$



**Figure 4.** Time series of mechanical production of TKE ( $\text{m}^2\text{s}^{-3}$ ), buoyant production of TKE ( $\text{m}^2\text{s}^{-3}$ ), full TKE production ( $\text{m}^2\text{s}^{-3}$ ), dissipation of TKE ( $\text{m}^2\text{s}^{-3}$ ) and imbalance of TKE ( $\text{m}^2\text{s}^{-3}$ ). Black line indicates desert and red line indicates forest.

are a function of observation height. At 15 m above the desert and 19 m above the forest floor are high enough to be ~~at~~in the “constant flux layer”, the vertical profiles of TKE ( $\overline{u'w'} + \overline{w'w'}$ ) converge. However, when observed at a lower elevation, and below the constant flux layer, the data show clear differences in  $\overline{w'w'}$ .

The vertical momentum flux  $\overline{u'w'}$  over the forest is much higher compared to the desert-which is also expected because of the higher surface roughness of the forest, making it a much more efficient momentum sink compared to the desert. Note that the shear transport of momentum flux is still much more effective over the forest compared to the desert because of roughness effects even though the mean quantities can be higher over the desert. The sensible heat flux  $\overline{w'T'}$  over the forest is also higher as discussed before due to the canopy convective effect.

### 3.2 Nature of TKE budget

Figure 4 shows the time series of the components of the TKE budget as discussed in section 2.1. The first row shows mechanical production of TKE ( $P_{Mech}$ ,  $\text{m}^2\text{s}^{-3}$ ), the second row shows buoyant production of TKE ( $P_{Buoy}$ ,  $\text{m}^2\text{s}^{-3}$ ), the third row shows full TKE production ( $P_{TKE}$ ,  $\text{m}^2\text{s}^{-3}$ ), which is the ~~summation~~sum of mechanical and buoyant TKE production. The fourth row shows dissipation of TKE ( $\epsilon$ ,  $\text{m}^2\text{s}^{-3}$ ) and the fifth row shows imbalance of TKE ( $Imb$ ,  $\text{m}^2\text{s}^{-3}$ ). Black line indicates desert



and red line indicates forest. As noticed in figure 4, the production of turbulence is mostly by mechanical or shear forcing because of the roughness of the forest, whereas mechanical production of TKE over desert is very small and does not have a strong diurnal cycle like the forest, although it increases slightly after ~~23th~~23rd August. On the other hand, TKE production over the desert is mostly carried by buoyancy. Buoyant TKE production is slightly larger over the forest. The buoyant TKE production over the desert is also higher after ~~23th~~23rd August. Given the moderate temperature difference between the desert and the forest, the difference of their corresponding buoyant TKE production is interesting. It also indicates that mechanical forcing, and not buoyancy makes a difference (mechanical production is higher by approximately an order of magnitude than buoyant production) in the turbulence generation over the desert and the forest. The diurnal cycle of the TKE dissipation  $\epsilon$  is interesting as well. The dissipation of TKE seems to be higher above the forest as well compared to the desert.

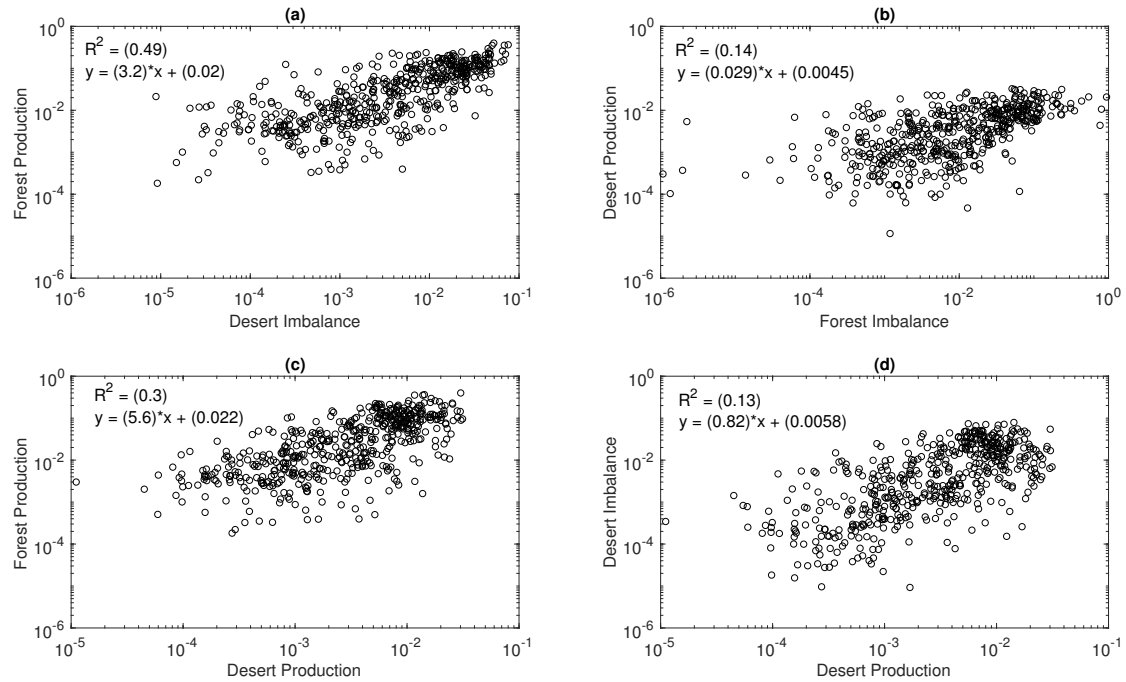
10 A smaller TKE dissipation is recorded when the measurement location is further from the ground and above the roughness sub-layer. One strong argument for observed changes after Aug 23 being tower-height effects rather than change of any large scale forcing is that changes in the desert are observed only after the ~~23th~~23rd, while the forest observations maintain a rather consistent dynamics.

The diurnal cycles of the TKE imbalance computed by equation 3 is also very interesting. The imbalance over the forest is often positive over the daytime, while over the desert it is often negative, highlighting the difference of turbulent transport and advection over the two different regimes. Also notice that the positive imbalance for forest and negative imbalance for desert almost have a phase (anti)synchronization, indicating that the turbulence above forest and desert are responsive to one another and they are part of a coupled system, indicating again towards the role of the secondary circulations.

### 3.3 Transport of TKE over desert and forest

20 Figure 5 is used to better understand the nature of turbulent transport between the desert and the forest. Panel (a) depicts the TKE imbalance over desert vs the net production of TKE over the forest. As observed, there is a significant correlation (0.5) between them, indicating that the advection and transport of TKE by flux divergence and pressure fluctuations reach downstream by means of the secondary circulations and produces TKE over the forest. On the other hand, the converse is not true, as observed in panel (b) of figure 5. There is little correlation between the Imbalance of TKE over forest and the production of TKE over desert (0.14). As observed in panel (c), the production over desert is also well correlated with the production over forest (0.3) as both the desert and forest are subjected to the same forcing. However the TKE production over desert is not that well correlated with the TKE imbalance over the desert as seen in panel (d). Thus while there should be some cross correlation in panel (a) because of desert production, that is not the only effect. The nonlocal large scale motions contribute to the transport over desert (without significantly altering TKE production over desert) which in turn cause TKE production above the forest because of the higher mechanical forcing.

30 Thus it can be stated that ~~the~~at least in the canopy sub layer and in the atmospheric surface layer, the effects of secondary circulations are transported from over the desert towards the forest following the background wind direction, and not the other way around. It is worth noting here that the term ‘secondary circulation’ has been used somewhat loosely here and contain the effects of horizontal transport as well, since partitioning the imbalance term is not possible within the scope of

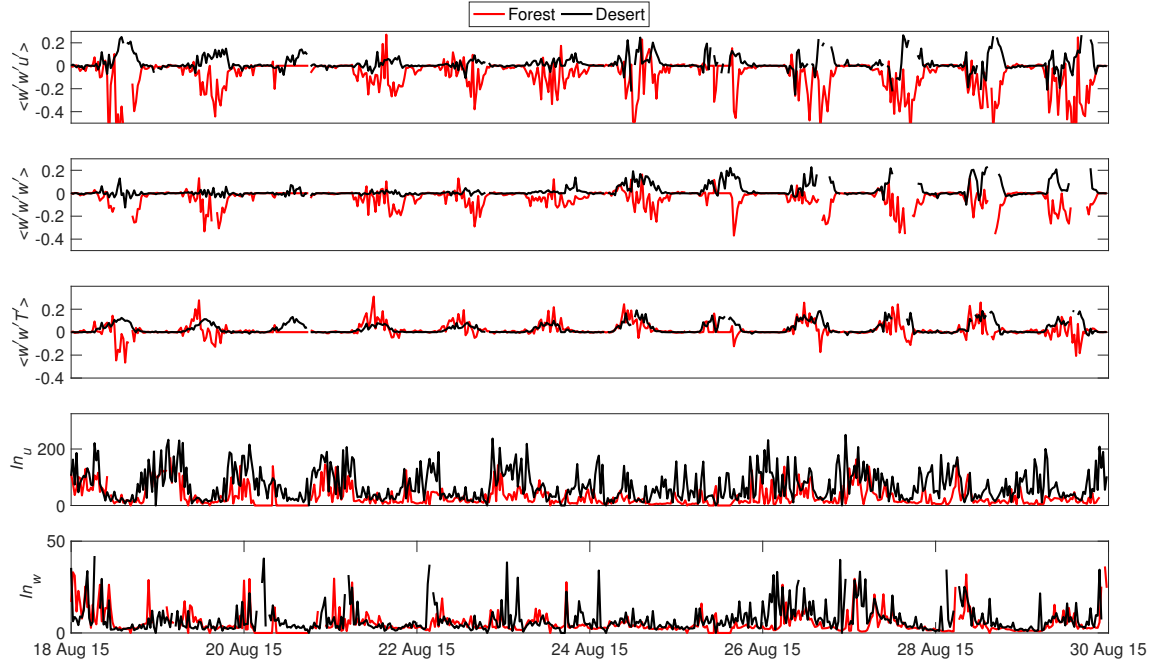


**Figure 5.** (a) TKE imbalance for desert vs TKE production for forest. (b) TKE imbalance for forest vs TKE production for desert. (c) TKE production for desert vs TKE production for forest. (d) TKE production for desert vs TKE imbalance for desert. Significance: 0.05 level.

this campaign. In the case of transport from the forest towards the desert, it is more likely that horizontal advection is the main mechanism. The nature of the full extent of the secondary circulation are a part of much larger flow pattern and are not fully captured by the eddy covariance towers, which only capture the fine scale turbulence. To reveal the full nature of the secondary circulations, one can look at LIDAR observations as shown in appendix B (Brugger et al., 2018) as well as large eddy simulations (Kroeniger et al., 2018).

### 3.4 Effect of nonlocal motions

Figure 6 shows the time series of the triple moments  $\overline{w'w'u'}$ ,  $\overline{w'w'w'}$  and  $\overline{w'w'T'}$  in the first three rows. The vertical velocity skewness term  $\overline{w'w'w'}$  (2nd row) is of importance as it appears in the transport term of the TKE budget (equation 2) and is a measure of non-Gaussian turbulence, which indicates the presence of non-local coherent motions such as sweeps and ejections. Note that the vertical velocity skewness is often negative above the canopy which is consistent with the generic feature of canopy turbulence (Kaimal and Finnigan, 1994; Chamecki, 2013; Dias-Junior et al., 2015). What is perhaps more interesting is that the The daytime vertical velocity skewness over the desert is often positive, indicating again of the presence of nonlocal coherent structures active over the desert. The measure of skewness increases over the desert after 23th August



**Figure 6.** Top three panels: time series of triple moments  $\overline{w'u'u'}$ ,  $\overline{w'w'w'}$  ( $\text{m}^3\text{s}^{-3}$ ) and  $\overline{w'w'T'}$  ( $\text{Km}^2\text{s}^{-2}$ ). Bottom two panels show the integral time scales of horizontal ( $In_u$ ) and vertical velocities ( $In_w$ ) in seconds.

23rd August which is also due to the height change. The other two terms  $\overline{w'u'u'}$  and  $\overline{w'w'T'}$  are also associated with turbulent transport of momentum and heat by as evident from their respective budget equations (Raupach et al., 1986; Zhuang and Amiro, 1994; Cava et al., 2006; Katul et al., 2013; Banerjee et al., 2017b).

$$\frac{\partial \overline{w'u'}}{\partial t} = 0 = -\overline{w'w'} \frac{\partial \overline{U}}{\partial z} - \frac{\partial (\overline{w'u'u'})}{\partial z} + \frac{g}{\overline{T}} \overline{w'T'} - \frac{1}{\rho} \left( \overline{u' \frac{\partial p'}{\partial z}} \right); \quad (7)$$

5 and

$$\frac{\partial \overline{w'T'}}{\partial t} = 0 = -\overline{w'w'} \frac{\partial \overline{T}}{\partial z} - \frac{\partial (\overline{w'w'T'})}{\partial z} + \frac{g}{\overline{T}} \overline{T'T'} - \frac{1}{\rho} \left( \overline{T' \frac{\partial p'}{\partial z}} \right). \quad (8)$$

Moreover, the triple moments have been shown to be directly correlated with the relative contributions of nonlocal events such as sweeps and ejections as (Nakagawa and Nezu, 1977; Raupach et al., 1986; Cava et al., 2006; Katul et al., 2013; Banerjee et al., 2017b). Notice that momentum transport term  $\overline{w'u'u'}$  is also opposite in sign for the desert and forest and it shows a strong diurnal cycle. After ~~23th~~ 23rd August, increase in momentum transport is noticed for the desert. However, the diurnal cycle of the heat transport term  $\overline{w'w'T'}$  is not as strong as its momentum counterpart, but it is often found to be larger over the desert compared to the forest, consistent with the findings from the TKE budget that shows heat is transported from over the

desert towards the forest. It is however, important to note that the structures are representative of the fine scale turbulence and not directly representative of the large scale circulation structures spanning the whole boundary layer. The fourth and fifth rows of figure 6 show the timeseries of integral timescale of horizontal ( $In_u$ ) and vertical ( $In_w$ ) velocity components in seconds.  $In_u$  and  $In_w$  for every half hour time period are computed by integrating the normalized autocorrelation function of  $u$  and  $w$  until the first zero crossing (Kaimal and Finnigan, 1994). They can be interpreted as the characteristic time scale of the most energetic eddies in each direction. As noticed in figure 6, time scales in the horizontal directions are larger compared to the vertical direction. More interesting is the observation that the integral time scales for the eddies above the desert are larger than the forest- which also increase after ~~23th~~<sup>23rd</sup>. This is another indicator of buoyant production of turbulence, which generates larger eddies than shear production.

## 10 4 Conclusions

We studied the nature of turbulent transport over a well defined surface heterogeneity comprising of a desert and forest in the Yatir semi-arid area in Israel. Eddy covariance and Doppler LiDAR measurements were conducted for 12 days between 18th and 31st August, 2015 over two locations in the forest and the shrubland (referred to as ‘desert’ for the almost complete lack of vegetation during the observation period). Earlier campaigns in this area focused on energy balance closure and hypothesized about the existence of secondary circulations because of surface heterogeneity. The present work was aimed to study the nature of turbulent transport over the forest and the desert in more detail to address the following questions:

1. How does the Yatir forest affect the boundary layer dynamics such as eddy size distribution, boundary layer height and diurnal variations of turbulent statistics and fluxes compared to the surrounding desert?
2. Can the existence of secondary circulation be confirmed?
- 20 3. Is there any horizontal energy transport between the forest and the desert and how does it vary with time?

To answer the above mentioned questions, we computed half hour average turbulent statistics for both the desert and forest and looked at their diurnal variations. We also computed individual components of the turbulent kinetic energy (TKE) budget and argued that the turbulent transport of energy should be contained in the imbalance of the TKE budget, which consists of the effects of advection, transport by turbulent flux divergence and pressure velocity interactions, since we could not compute those terms explicitly. Moreover, we also computed triple moments which are associated with nonlocal motions and coherent structures and integral time scales, which are associated with the most energetic eddies. ~~We used the measured boundary layer heights to compute a first order bulk parameter which can directly quantify the presence of very large scale motions.~~ The findings to the questions are listed below:

1. The forest is found to be associated with a higher level of turbulent intensity because of higher roughness although the desert reported higher mean speeds and vertical updrafts possibly due to the presence of secondary circulations. Gentle topography around the desert might contribute to the updrafts over the desert as well. The smaller roughness of the desert
- 30

is also responsible for higher wind speeds above the desert. There is little air temperature difference between the desert and the forest, although the mean velocities and temperature have strong diurnal cycles. Momentum and heat flux are also found to be stronger above the forest. The presence of the secondary circulation enhances the turbulent fluxes as well as the turbulent intensity above the desert.

- 5      2. The role of secondary circulations can be better understood once the components of the TKE budget are studied. Over the forest the production of turbulence is mechanical, while over the desert, TKE production is mostly carried by buoyancy. The forest is more efficient in dissipating TKE as well. The imbalance of TKE is taken as the indicator of TKE transport and is found to vary diurnally almost anti synchronously over the desert and forest - confirming the role of a secondary circulation. The TKE budget is closed better over the forest compared to the desert. Turbulent triple moments which  
10      are indicators of nonlocal motions and coherent structures also show strong variability over the desert and opposite in signs, also confirming the role of secondary circulations. The integral time scales are found to be higher over the desert compared to the forest. This suggests that the secondary circulations that transport energy are more active over the desert- however, they cannot produce much turbulence over the desert since they only rely on buoyancy driven turbulence as mechanical forcing is missing over the desert. This is also highlighted by the fact that mean velocities are higher above  
15      the desert while turbulent fluctuations are higher above the forest.
3. To elucidate the role of horizontal transport between the desert and the forest, we studied the correlation between the TKE imbalance over the desert and the TKE production over the forest. The moderately high correlation suggests that the secondary circulation is transported from over the desert towards the forest, enhancing TKE production over the forest, at least in the canopy sub layer and the atmospheric surface layer. The low correlation between the TKE imbalance over  
20      the forest and TKE production over the desert confirms the directionality of this horizontal exchange, which is from the desert towards the forest and not the other way around.

To summarize, we have examined the existence and role of secondary circulations that exists because of large scale surface heterogeneities and possible due to some topography effects between the desert and forest by looking at proxy quantities computed from turbulence measurements. Although the campaign was conducted at a particular site, the conclusions drawn  
25      are fairly general and can be extended to other scenarios involving surface heterogeneities such as urban landscapes, agricultural fields etc. Future works will attempt to highlight a more spatially detailed picture of the turbulent structure under the interesting scenario of secondary circulations and horizontal energy transport.

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30      balance closure problem”, which is funded by the Helmholtz-Association through the President’s Initiative and Networking Fund, and by KIT. We suggest contacting the principal investigator Dr. Matthias Mauder (matthias.mauder@kit.edu) if one is interested in obtaining the data used in the paper.

## Appendix A: Full form of the TKE budget

$$\begin{aligned}
 \frac{\partial e}{\partial t} + U \frac{\partial e}{\partial x} + V \frac{\partial e}{\partial y} + W \frac{\partial e}{\partial z} &= \frac{g}{T} (\overline{w'T'}) \\
 &- \overline{u'u'} \frac{\partial U}{\partial x} - \overline{v'u'} \frac{\partial V}{\partial x} - \overline{w'u'} \frac{\partial W}{\partial x} \\
 5 \quad &- \overline{u'v'} \frac{\partial U}{\partial y} - \overline{v'v'} \frac{\partial V}{\partial y} - \overline{w'v'} \frac{\partial W}{\partial y} \\
 &- \overline{u'w'} \frac{\partial U}{\partial z} - \overline{v'w'} \frac{\partial V}{\partial z} - \overline{w'w'} \frac{\partial W}{\partial z} \\
 &- \frac{\partial (\overline{u'e})}{\partial x} - \frac{\partial (\overline{v'e})}{\partial y} - \frac{\partial (\overline{w'e})}{\partial z} - \frac{1}{\rho} \frac{\partial (\overline{u'p'})}{\partial x} - \frac{1}{\rho} \frac{\partial (\overline{v'p'})}{\partial y} - \frac{1}{\rho} \frac{\partial (\overline{w'p'})}{\partial z} - \epsilon, \quad (A1)
 \end{aligned}$$

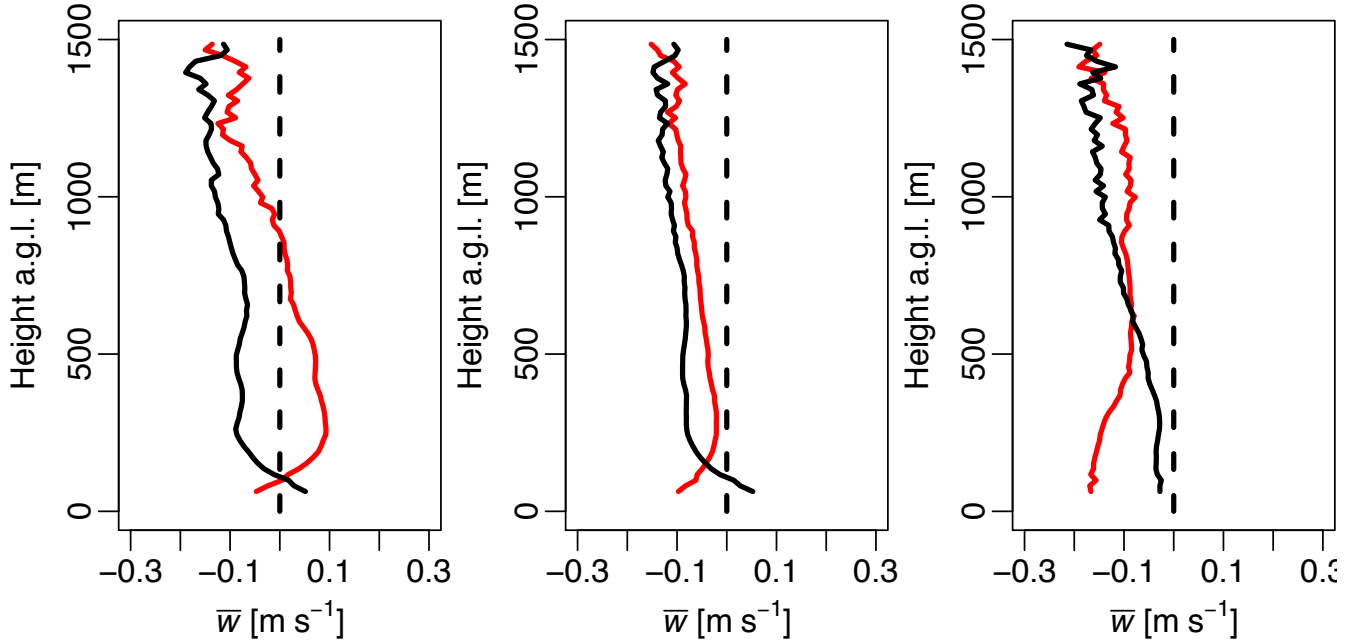
Thus to be consistent with equation 2, all the terms in equation A1 that cannot be evaluated using one point measurements can be clubbed in the imbalance term, which can be described by

$$\begin{aligned}
 Imbalance &= \frac{\partial e}{\partial t} + U \frac{\partial e}{\partial x} + V \frac{\partial e}{\partial y} + W \frac{\partial e}{\partial z} \\
 &+ \overline{u'u'} \frac{\partial U}{\partial x} + \overline{v'u'} \frac{\partial V}{\partial x} + \overline{w'u'} \frac{\partial W}{\partial x} \\
 &+ \overline{u'v'} \frac{\partial U}{\partial y} + \overline{v'v'} \frac{\partial V}{\partial y} + \overline{w'v'} \frac{\partial W}{\partial y} \\
 &+ \overline{u'w'} \frac{\partial U}{\partial z} + \overline{v'w'} \frac{\partial V}{\partial z} + \overline{w'w'} \frac{\partial W}{\partial z} \\
 15 \quad &+ \frac{\partial (\overline{u'e})}{\partial x} + \frac{\partial (\overline{v'e})}{\partial y} + \frac{\partial (\overline{w'e})}{\partial z} + \frac{1}{\rho} \frac{\partial (\overline{u'p'})}{\partial x} + \frac{1}{\rho} \frac{\partial (\overline{v'p'})}{\partial y} + \frac{1}{\rho} \frac{\partial (\overline{w'p'})}{\partial z}. \quad (A2)
 \end{aligned}$$

Thus if no assumptions or idealizations are invoked, the imbalance of the commonly used operational TKE budget (equation 2) consists of TKE tendency, advection, shear production, TKE flux divergence and pressure velocity interactions. Using an array of sonics in each direction will enable determination of all these terms. However, as evident from the myriad of terms contributing to the imbalance, it is difficult to determine what degree of assumptions of homogeneity in which direction are sufficient so that certain terms can be ignored. Thus unless all terms in equation A2 can be determined, it is easier to stick to the most idealized form of equation 2 and treat all other terms as imbalances. Future work will try to determine the partitioning of advection, flux divergence and the other shear production terms contributing to TKE budget imbalances in presence of heterogeneities.

## Appendix B: Further evidence of secondary circulation

Figure shows mean vertical velocity  $W$  above the forest and the desert averaged over all observations using the Doppler LiDARS. ~~Note that there is a mean updraft ( $W > 0$ ) above the forest and a mean downdraft above the desert ( $W < 0$ ). This suggests that there exists a mean secondary circulation and supports the findings and observations in the manuscript.~~



**Figure 7.** ~~Mean-vertical~~ Vertical mean velocity ~~ms<sup>-1</sup>-above-profile~~ averaged from 18 - 29 August (only times with both instruments simultaneously online and the ~~forest~~-nearest three range gates are discarded). Left to right: Four hour window centered on noon, day time (sunrise to sundown) and night time (sundown to sunrise). The forest is shown as a solid red line, the desert as ~~measured-by-LiDARs~~solid black line, and a vertical line at  $\bar{w} = 0$  as black dashed line. Note that near the surface the desert has always larger  $w$ , but only during the noontime with the updrafts of the forest is a change of sign.

### Appendix C: ~~Details of coordinate rotation of turbulence velocity measurements~~

A planar-fit method described by Wilezak et al. (2001) is used, which considers the tilt of the sonic anemometer with respect to local streamlines. Hence this technique is deemed to be more suitable in the presence of sloped terrain, which can be associated with a net non-zero mean vertical velocity. The hypothesis being employed is that under the condition of tilting relative to the local streamlines, a portion of the horizontal velocities will be present in the measured vertical velocity component:-

$$\bar{w}_m = b_1 \bar{u}_m + b_2 \bar{v}_m,$$

where over-bars denote half hour time averaging and the subscript  $m$  indicates measured velocity components. Note that this is a modification of the original Wilezak et al. (2001) formulation by Van Dijk et al. (2004), who noted that the equation ?? does not need an additional constant.  $b_1$  and  $b_2$  are computed using a bilinear regression using all the data points for individual sonic anemometers. Next, to orient the  $z$  axis perpendicular to the local streamlines, a rotation is performed:-

$$[\underline{u_{pf}}; \underline{v_{pf}}; \underline{w_{pf}}] \equiv [\underline{M_{pf}}][\underline{u_m}; \underline{v_m}; \underline{w_m}]$$

where the rotation matrix is defined as-

$$M_{pf} = \begin{bmatrix} \cos\alpha & 0 & -\sin\alpha \\ 0 & 1 & 0 \\ \sin\alpha & 0 & \cos\alpha \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos\beta & \sin\beta \\ 0 & -\sin\beta & \cos\beta \end{bmatrix},$$

where  $\tan\alpha = -b_1$  and  $\tan\beta = b_2$  (from which  $\sin\alpha, \cos\alpha, \sin\beta$  and  $\cos\beta$  can be computed). Finally, another rotation is applied to align the wind vector

- 5 the desert and forest, rather a much more complex and three dimensional structure. Close to the surface layer and the canopy sublayer, the transport of energy is indeed from the desert to the forest (Fig. 5). Further, we observe that the desert has more updrafts and the forest has more downdrafts close to the surface. However, as we go up above roughly 100m, this behavior flips. Lastly, Kroeniger et al. (2018) found in his simulations that large rotational systems developed at specific locations connected to surface features. Therefore, we conclude that the bulk transport in the convective mixed layer by a secondary circulation is
- 10 from the forest to the desert, but advected with the mean wind direction:-

$$u_{rot} = u_{pf} \cos\theta + v_{pf} \sin\theta; v_{rot} = -u_{pf} \sin\theta + v_{pf} \cos\theta; w_{rot} = w_{pf},$$

where  $\theta = \tan^{-1}(v_{pf}/u_{pf})$ . This also ensures that the crosswind ( $v$ ) component is zero and heavily influenced by surface features on a smaller scale than the forest itself.



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