Response to Anonymous Referee #1

The manuscript discusses the process of activation of cloud droplets on big aerosol particles. It checks for what aerosol size range the process of activation of cloud droplets can be explained by collisions between aerosol particles. It also checks the importance of the process of activation via collection compared to activation via diffusion of water vapor. The study is done using an LES setup combined with Lagrangian (i.e. particle tracking) representation of cloud microphysics. In the discussed simulations both aerosol particles and cloud droplets are represented using the Lagrangian approach, which allows to numerically resolve the activation process.

As shown in the manuscript, the studied process of activation by collection is very rare and affects mostly big aerosol particles entrained above the cloud base. As discussed in the summary of the manuscript, the studied process can be safely neglected, or even more, it might already be implicitly covered in some of the activation parametrization schemes. The presented study is therefore more theoretical and shows, in my understanding, in what aerosol size range the term *activation* as understood by the Köhler theory has any meaning.

The manuscript is well written and my further comments are both few and minor.

Thank you very much for your comments which helped to clarify the manuscript.

General comments

The manuscript defines three scenarios of activation of an aerosol particle by collision (lines 135-143):

- 1. coalescence of two inactivated aerosol particles resulting directly or after some diffusional growth in activated particle,
- 2. coalescence of an inactivated aerosol particle and activated aerosol particle that leads to an inactivated particle that activates due to diffusion,
- 3. coalescence of an inactivated aerosol particle and activated aerosol particle that leads to an activated particle. This scenario is considered an activation via collection only when the critical radius of the created particle is bigger than the initial wet radius of the colliding activated aerosol.

The first scenario is straightforward, but in my opinion the second and the third scenario deserve more explanation why they are considered an activation via collection. Indeed, from the point of view of the colliding inactivated aerosol particle, it can be said that the activated aerosol particle with which it collided got annihilated and in turn the aerosol in question got activated after some additional diffusional growth.

However, from the point of view of the colliding activated particle it can be said that the activated aerosol particle scavenged the inactivated particle and thanks to diffusion of water vapor remained activated (i.e. the activated particle remains activated and the inactivated particle is annihilated).

In general, counting and labeling activation events that happen due to collision is more difficult because there are two initial particles and one resulting activated aerosol particle, whereas the traditional Köhler theory activation results in one-to-one correspondence between an activated aerosol particle and the created cloud droplet. Could you clarify which colliding particles are considered activated and which annihilated?

Could you consider adding some sketch or maybe a plot using Köhler curves that exemplifies how the considered scenarios work? It could help to clarify which particles are labeled as annihilated, activated and inactivated and to showcase the typical dry and wet radius sizes of the particles colliding in all scenarios.

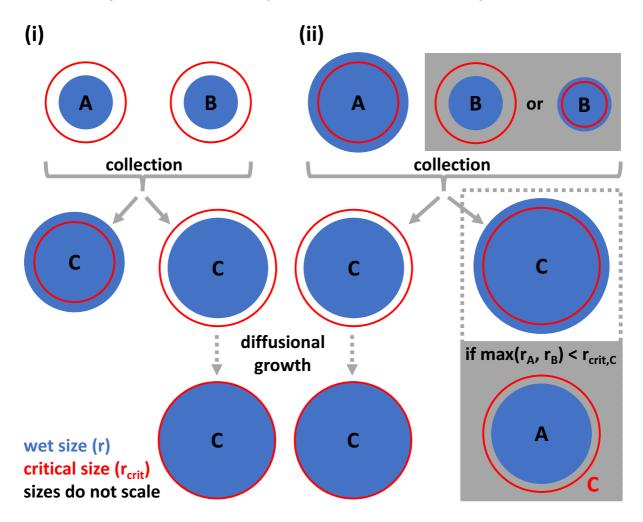
The identification of collectional mass growth is based on the comparison of the collectional mass growth $\Delta m|_{coll}$ to the diffusional $\Delta m|_{diff}$. The scenarios exemplify how this $\Delta m|_{coll}$ is able to exceed $\Delta m|_{diff}$. Accordingly, they are scenarios defined, they result from the collections I observed. And indeed, the first scenario is straight forward, but the other scenario might also lead to $\Delta m|_{coll}>\Delta m|_{diff}$, and need to be considered. I added a sketch to the manuscript (Fig. 3) which illustrates each scenario. The sketch displays the critical radius (red) as well as the wet radius (blue) of each particle during the process of collectional activation. A more in depth discussion of the relevant processes have been added to the text (line 149-166):

"To identify a collectional activation, the integrated collectional mass growth $\Delta m|_{coll}$ is compared to the diffusional $\Delta m|_{diff}$ in the moment the particle grows beyond its critical radius. If the former exceeds the latter, $\Delta m|_{coll} > \Delta m|_{diff}$, this activation is considered as collectional. There are various microphysical interactions resulting in $\Delta m|_{coll} > \Delta m|_{diff}$, and its basic types are illustrated in Fig. 3. Note that also a combination or a repetition of these types is possible, i.e., multiple subsequent collections. In a collectional activation of type (i), the water mass growth by collection dominates, i.e., the coalescence of two previously inactivated aerosols A and B results directly or after some diffusional growth in an activated particle C. In a collectional activations of type (ii), the critical radius increases faster than wet radius, i.e., the coalescence of an already activated particle A with another activated or an inactivated particle B results in inactivated particle C, which activates after some diffusional growth. If the resulting particle is directly activated, this process is only considered a collectional activation if the largest wet radius of the two coalescing particles A and B is smaller than the critical radius of the newly produced particle C:

$$max(r_A, r_B) < r_{crit.C}$$

This ensures that the combined water of particles A and B is necessary to activate particle C. If this is not the case, i.e., the water of particle A or B is able to activate particle C on its own, the latter process is considered a regular collection of cloud droplets or as scavenging and neglected in the following analysis. Moreover, the coalescence of two activated

particles resulting in a collectional activation is mathematically possible but not found to play a role in the analyzed simulations. Note that only collectional activations of the first type are able to increase the number of activated aerosols, while the second type might have no or a negative impact on the total number of activated aerosols since the coalescence of at least one activated particle results in one activated particle."



Specific comments

• **line 26**: As discussed in the Summary when referring to the work by Nenes et al. 2001, it is not necessary for a cloud droplet to become formally activated (i.e. reach its critical radius as defined by the Köhler theory) in order to grow in the cloudy environment and behave similar to the formally activated droplets. Could you consider adding such comment also in the introduction?

Yes (line 25 - 27): "Due to their large size, however, these particles may behave like regular cloud droplets inside the environment of a cloud although they are not formally activated (Nenes et al., 2001). Accordingly, Köhler activation theory is usually considered a weak concept for these particles."

• line 32: I think the question this article addresses is about "limits of traditional Köhler

activation theory". As discussed in the Summary and in the referred work of Chuang et al. 1997 and Nenes et al. 2001, the Köhler theory can be used to calculate the equilibrium saturation for big aerosol particles. The problem is that the big aerosol particles will not reach their equilibrium in the necessary time and therefore will not become formally activated.

You are perfectly right. I added the word "activation" to clarify this (line 34).

• **line 103**: Does it mean that the weighting factors for all super-droplets are constant? Does it affect the representation of collisions (compared to the tests presented in Unterstrasser et al. 2016)?

Initially, the weighting factors are the same, which might impede collections in a zero-dimensional setup as tested in Unterstrasser et al. (2017). Accordingly, the results should be considered as a lower estimate of the impact of collectional activation. However, as super-droplets experience collections, their weighting factor reduces resulting in a wide range of different weighting factors during the simulation. As discussed in Unterstrasser et al. (2017), this might facilitate collisions if more than one grid box is simulated, i.e., if super-droplets are allowed to interact with another ensemble of droplets when they move from one grid box to the next. The following addition has been made (line 314 - 315): "Additionally, the collection algorithm itself might underestimate collisions due to the initial distribution of weighting factors (Unterstrasser et al., 2017), and the determined influence of collectional activation should be considered as a lower estimate."

• **Figure 4**: I think the panels should be bigger (at least as big as those in Fig. 3). What is causing the spikes for maximum diffusion radius for the simulation with the lowest aerosol concentration? For convenience, would you consider adding a panel that shows the diffusional activation rate calculated basing on the simulations discussed here?

The size of the panels has been increased (Fig. 5). A panel of the diffusional activation has been added (Fig. 5 d), which caused some subsequent changes in the text (line 198 - 200).

Thank you for the hint regarding the spikes in the $100 \, \mathrm{cm}^3$ simulation. They result from the recirculation of large particles (see Naumann and Seifert, 2016, doi: 10.1002/2016MS000631), which have grown by collection inside the cloud, then detrained from the cloud, evaporated smaller than their critical radius outside the cloud (i.e., deactivated), entrained into the cloud again, where they grew larger than the critical radius by diffusion (i.e., activated by diffusion). Since the algorithm for distinguishing between diffusional and collectional activation only considered the growth between deactivation and activation, they have been spuriously considered as diffusional activations. In total, only 2×10^{-4} % of all diffusional activation have been affected by this process. I was able to remove these false diffusional activations from the analysis of the $100 \, \mathrm{cm}^{-3}$ simulation. No influence of recirculations has been found for simulations with a

higher aerosol concentration. The new profile for the 100 cm⁻³ simulation has been added to Fig. 5. The conclusions did not change.

• Figure 7a and lines 207-214: Figure 7a is difficult for me to read and understand. First, the lines are plotted on top of each other making it difficult to see the behavior of each simulation. Second, the description of what is on the axes and what is actually plotted is unclear to me. For example, in the simulation with 4000 aerosols in cm $^{-3}$ for dry radius of 0.1 μ m there are 0.2 collisions with inactivated aerosol particles and 0.8 collisions with activated aerosol particles to activate the aerosol particle. In the same time in the description it is stated that only one collision is needed to cause activation and that the collision occurs between an activated and inactivated particle. Could you clarify, or maybe provide some example? Third, are all aerosol particles counted twice in this plot? — Once as the aerosol particle that is going to be activated (i.e. the location on the x-axis) and once as colliding particles (i.e. the different lines shown on the plot)?

The whole figure has been changed to clarify the manuscript. Figure 8 shows the average number of collections necessary for activation irrespective of the number of collected activated or inactivated particles. All necessary information on how many activated aerosols have been involved in a collectional activation was already contained in Fig. 9 (the former Fig. 7b).

• **line 258-259**: "collectional activation affects predominantly particles that have been entrained above cloud base, i.e., activates aerosols that have not been able to activate by diffusion at cloud base (...)" Does this sentence mean that the aerosols in question were not activated at cloud base because they were never at the cloud base? If yes, then I think saying that those aerosols have not been able to activate at cloud base is misleading, because they were never there.

You are right. The sentence has been clarified to: "Moreover, collectional activation affects predominantly particles that have been entrained above cloud base, i.e., above the region of the cloud where the highest supersaturations occur. Accordingly, these particles experience systematically lower supersaturations which prevents diffusional activation." (line 280 - 282)

• line 353: Could you clarify what values of dissipation rate were used for the collision efficiency from the Wang and Grabowski 2009 paper? The efficiencies in this paper are provided for two dissipation rates (either 100 cm2/s3 or 400 cm2/s3). Was the closer one chosen? Or was a constant dissipation rate assumed when choosing the collision efficiency?

The kinetic energy has been determined in the sub-grid scale model of the LES and the efficiencies of Wang and Grabowski (2009) have been interpolated to that value (using the given data for $100 \text{ cm}^2 \text{ s}^{-3}$, $400 \text{ cm}^2 \text{ s}^{-3}$, as well as unity for a zero dissipation rate). This has been clarified to: "These turbulence effects are steered by the kinetic energy dissipation rate ϵ calculated in the LES subgrid-scale model (Riechelmann et al., 2012). The

parameterizations by Ayala et al. (2008) are a direct function of ϵ , while the tabulated values of the enhancement factor for the collision efficiency by Wang and Grabowski (2009) are interpolated to the present value of ϵ ." (line 384 - 386)

• **line 356**: Would you consider Brownian motion of aerosol particles as another possibility for activation due to collisions? Would a collision kernel representing both Brownian motion of aerosol particles and turbulence effects be an interesting extension of this study?

Indeed, a collision kernel with Brownian motions and turbulence would be an interesting extension of this study. Especially for very small collected particles, the consideration of additional processes affecting the collection process might result into a larger fraction of collected particles (e.g., Ardon-Dryer et al., 2015, doi: 10.5194/acp-15-9159-2015). However, I would expect that Brownian motions would rather have no impact on collisional activation by facilitating the collection of aerosols with a negligible amount of liquid water but a comparably large fraction of aerosol mass. This would result in a faster increase of the critical radius than the wet radius and therefore inhibit collisional activation (as discussed in Section 2 of the manuscript). I added a short discussion to Section 6 (line 309 - 312): "Moreover, the collection kernel might not incorporate all processes relevant for collections among aerosols and droplets. For instance, Brownian diffusion might increase the collection of smaller particles (e.g., Ardon-Dryer et al., 2015) but might not lead to collectional activation since it will add predominantly aerosol mass and only a small amount of water (cf. Section 2)"

Technical corrections

• line 23 and 39: I would not use the word even when describing opposite behavior(?).

Ok. The word "even" is not necessary there.

 line 195: When saying activation you mean collectional activation? Maybe it should be explicitly stated?

Done.

 line 326: I think that the paper by Shima et al. 2009 should be referred here again when introducing the "all-or-nothing" representation of collisions for the Lagrangian microphysics.

Good point. Done.

Response to Shin-ichiro Shima

I would like to recommend this paper to be published but after major revisions.

This is an interesting paper introducing a new mechanism of cloud droplet activation named "collectional activation". The author investigated its contribution theoretically, then numerically using an LCM. Note also that this analysis could only be possible if using an LCM. One of the conclusion is that the impact is small because it seldom occurs compared to conventional "diffusional activation", but I think the community still needs to be aware of such possibility.

However, there exist at least one major issue in this manuscript. Unfortunately, the determination criterion of "collectional activation" the author introduced is not appropriate. Please see the attached note "Possible_collectional_activation_scenario.pdf". You can see that r>r_crit is not a rigorous criterion to determine "collectional activation". I strongly suggest the author to examine all the materials minutely, keeping the above fact in mind, I am still not fully sure how big the revision could be, but because all the analyses are based on the above criterion, this correction could affect the paper substantially, though it probably do not change the main conclusion significantly.

Please also see other major/minor comments annotated in the attached pdf.

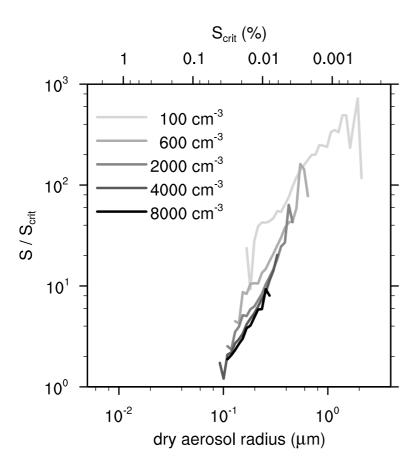
I am very thankful for the reviewer's comments which helped to clarify the paper in various aspects. However, I do not agree with his major comment on the appropriateness of the applied criterion for the detection of collectional activations, which will be outlined in this general response. More detailed answers will follow below.

The reviewer argues that the applied criterion to determine if an aerosol is activated or not, i.e., to distinguish between aerosols and cloud droplets, by comparing their radius against their respective critical radius (r vs. r_{crit}), is not adequate. In the present manuscript, I consider a particle as activated if it has grown beyond its critical radius ($r > r_{crit}$), a criterion which has been used and applied by various authors before (e.g., Rogers and Yau, 1989; Chuang et al., 1997; Khain et al., 2000; Boucher 2015; Hoffmann et al., 2015). Additionally, I request that the supersaturation enables further diffusional growth in the moment of activation to establish equivalence of diffusional and collisional activation (see line 119 - 123). Accordingly, the reviewer's collectional activation scenarios (ii) to (iv) are already considered in this study, which has been clarified and explained in more detail in the revised version of the manuscript (line 119 - 135 and comment 8 below). I only disagree with the reviewer's scenario (i). The reviewer argues that all particles which experience a supersaturation that exceeds the critical supersaturation ($S > S_{crit}$) should be considered as activated irrespective of their radius.

Of course, a supersaturation which exceeds the critical supersaturation ($S > S_{crit}$) will result in a radius which exceeds the critical radius ($r > r_{crit}$) at some point in time. And indeed, if the temporal dimension of particle growth and hence activation is neglected, both criterions are identical (see lines 20 - 27). But the time necessary for activation increases significantly for larger aerosols due to the kinetically limited transport of water molecules to the particle (Chuang et al. 1997; Hoffmann 2016). And if the supersaturation varies, as it

is the case in a real cloud due to entrainment/turbulence or simply due to the cloud's limited lifetime, the considered particle might not grow beyond its critical radius although the critical supersaturation has been exceeded for a certain period of time. Accordingly, the criterion of $r > r_{crit}$ is essential to decide if an activation has been completed or not.

Moreover, the critical supersaturations of the aerosols affected by collectional activation are so low that they are easily exceeded anywhere inside the cloud (cf. Fig. 5b). For the smallest aerosols affected by collectional activation (0.1 μ m dry radius), the critical supersaturation is 0.03 % and decreases significantly for larger ones (e.g., 0.005 % for a radius of 0.4 μ m, i.e., where the collectional fraction of activations becomes significant). The following figure shows the average supersaturation at the moment of collectional activation. Accordingly, the critical supersaturation is not restricting activation; it is exceeded several times by the supersaturations found in the simulated clouds.



Accordingly, the reviewer's criterion to consider all aerosols with $S > S_{crit}$ as activated makes no sense for the analysis carried out in this study. It would probably consider all aerosols larger than 0.1 μ m as activated. And we would have no information if these aerosols succeed to grow beyond the critical radius for activation. (Which is probably not the case due to the kinetically limited transport of water vapor to the particle (e.g., Chuang et al., 1997; Nenes et al., 2001; Hoffmann et al. 2015).) Anyhow, the reviewer's questions shows perfectly the problems associated with Köhler activation theory at these large aerosol radii: It is simply not valid anymore. The critical supersaturation is easily exceeded, but the growth beyond the critical radius can be impeded by the naturally occurring variations of the supersaturation.

Further reviewer comments (I copied them in a chronological order from the reviewer's PDF annotations):

1. Major request.

This is not true for "collectional activation". Modify it appropriately. **See main response above.**

2. Major request.

The discussion here is interesting and helpful to understand "collectional activation". However, r>r_crit is not a rigorous criterion for "collectional activation". Consider how to revise or justify the analysis.

See main response above.

3. Minor request.

To avoid confusion, you should explicitly mention that condensation/evaporation process is ignored in the theoretical analysis in this section.

Good point: "Moreover, all other microphysical processes, specifically diffusional growth, are neglected." (line 50)

4. Minor suggestion

To avoid confusion, you should clearly mention that those two red lines represent the critical radii, not the particle radius.

Good point: "For scenario B, an initially inactivated particle and an initially activated particle are examined (the critical radii are displayed in red by a continuous or dashed line, respectively)." (line 73 - 74)

5. Major question

Isn't this too big for calculating collision coalescence? Maybe it is okay for your method but have you checked the sensitivity to dt?

I didn't check the sensitivity to dt in this study, but a general study on the sensitivity of the collection algorithm to dt can be found in Unterstrasser et al. (2017). For a timestep of 1.0 s the results are reasonable. Accordingly, they should also be reasonable for a timestep of less or equal to 0.5 s. A reference to the study of Unterstrasser et al. (2017) is already given in line 356.

6. Major request

Please make it clear how you decide the initial dry aerosol radius. Uniform random sampling in log(dry r) space? or any other?

Yes, as already stated two sentences above: "The dry aerosol radius is assigned to each super-droplet using a random generator which obeys a typical maritime aerosol distribution represented by the sum of three lognormal distributions (Jaenicke, 1993) (Fig. 2)." (line 109 - 110)

7. Major request

Not true for "collectional activation"

See main response above.

8. Major request.

Not true for "collectional activation". They can grow even when 0<S<S_crit if r>r_s. This is covered in the study. The corresponding text has been clarified: "In this section, the applied methodology for untangling the contributions of diffusion and collection to the activation of aerosols is introduced. An aerosol becomes activated when it grows beyond its critical radius ($r>r_{crit}$). Moreover, activation requires the particle to be located in a volume of air with a sufficient supersaturation to enable unhindered diffusional growth. Depending on the microphysical process responsible for the final crossing of r_{crit} , different supersaturation allow unhindered diffusional growth.

Due to the continuous character of diffusional growth, the supersaturation has to be larger than the critical supersaturation in the moment in which the critical radius is exceeded:

$$S > S_{crit} = S_{eq}(r_{crit}),$$

where S_{eq} is the equilibrium supersaturation calculated according to Köhler theory (see Eq. (A3)). This condition is automatically fulfilled in the case of diffusional growth due to the constraints of Köhler theory on the equilibrium supersaturation. If the critical radius is exceeded by collection, the radius after collection might be immediately larger than r_{crit} and, hence, the necessary supersaturation is allowed to be smaller to enable unhindered diffusional growth:

$$S > S_{eq}(r_{ac}),$$

where $r_{ac} > r_{crit}$ is the wet radius after collection. This criterion is not automatically fulfilled and checked additionally to establish the formal equivalence of both processes, i.e., enabling unhindered diffusional growth after activation. Note that the process of activation, i.e., the entire growth beyond r_{crit} , can be driven by diffusional growth or by accumulating liquid water due to collection or by a combination of both." (line 119 - 135)

9. Major question and suggestion.

In my point of view, the definition of the collectional activation employed here is too complicated and unnatural.

Is it really necessary to include

inact + inact -> inact -> act

inact + act -> inact -> act

inact + act -> act (exclude scavenging)

as collectional activation?

Aren't these very rare events that can be negligible?

Further, I think collectional deactivation should be also interesting.

This is just an idea, but in my opinion, it is better to separate the instantaneous activation/deactivation analysis and history analysis, to clarify the structure of the paper.

It sounds natural to me to define the activation/deactivation categories using only instantaneous information:

diffusional activation inact -> act diffusional deactivation act -> inact collectional activation: inact + inact -> act (only direct one) collectional deactivation:

inact + act -> inact

act + act -> inact

For the first step, analyzing the instantaneous activation/deactivation characteristics, should be sufficient.

Then, in the next step, you can carry out history analysis, and indeed it is interesting and important,

However, doing both at once complicate the discussion.

Please consider my proposal.

Actually, there is only one way to cause a collectional activation in the current study: In the moment a particle grows larger than the critical radius, the integrated collectional mass growth needs to exceed the integrated diffusional mass growth ($\Delta m|_{coll} > \Delta m|_{diff}$.). The various types of interactions have been added to exemplify the naturally occurring microphysical processes that lead to $\Delta m|_{coll} > \Delta m|_{diff}$. They have been illustrated in Fig. 3 and need to be considered in the interpretation of the results. The only unnatural intervention is the exclusion of scavenging or the collection of drops if $\max(r_A, r_B) > r_{crit,C}$. This has been clarified by rewriting the whole paragraph (line 149-166):

"To identify a collectional activation, the integrated collectional mass growth $\Delta m|_{coll}$ is compared to the diffusional $\Delta m|_{diff}$ in the moment the particle grows beyond its critical radius. If the former exceeds the latter, $\Delta m|_{coll} > \Delta m|_{diff}$, this activation is considered as collectional. There are various microphysical interactions resulting in $\Delta m|_{coll} > \Delta m|_{diff}$, and its basic types are illustrated in Fig. 3. Note that also a combination or a repetition of these types is possible, i.e., multiple subsequent collections. In a collectional activation of type (i), the water mass growth by collection dominates, i.e., the coalescence of two previously inactivated aerosols A and B results directly or after some diffusional growth in an activated particle C. In a collectional activations of type (ii), the critical radius increases faster than wet radius, i.e., the coalescence of an already activated particle A with another activated or an inactivated particle B results in inactivated particle C, which activates after some diffusional growth. If the resulting particle is directly activated, this process is only considered a collectional activation if the largest wet radius of the two coalescing particles A and B is smaller than the critical radius of the newly produced particle C:

$$max(r_A, r_B) < r_{crit,C}$$
.

This ensures that the combined water of particles A and B is necessary to activate particle C. If this is not the case, i.e., the water of particle A or B is able to activate particle C on its own, the latter process is considered a regular collection of cloud droplets or as scavenging and neglected in the following analysis. Moreover, the coalescence of two activated particles resulting in a collectional activation is mathematically possible but not found to play a role in the analyzed simulations. Note that only collectional activations of the first type are able to increase the number of activated aerosols, while the second type might have no or a negative impact on the total number of activated aerosols since the coalescence of at least one activated particle results in one activated particle."

10. Typo d -> Delta **Done.**

11. Typo

Done.

12. Minor request.

This is ambiguous. Do you mean when it will be activated by diffusion without further coalescence?

This has been clarified. See answer to comment 9.

13. Minor request.

Same as above

This has been clarified. See answer to comment 9.

14. Typo

Done.

15. Typo

Done.

16. Minor suggestion.

Do diffusional activations also occur at high altitude? If so, wouldn't it be informative for readers to show also the vertical profile of the diffusional activation?

Yes, partly because of newly entrained aerosols or due to the kinetically limited activation of aerosols within the central updraft (see, e.g., Slawinska et al. 2012; Hoffmann et al. 2015 as stated in line 200). A vertical profile of the diffusional activation rate has been added (Fig. 5d).

17. Major question.

This is not trivial. Do you have any clear explanation why this does not happen? Is this just caused by the lack of aerosol particles of this size or is there any other mechanism to inhibit both diffusional and collectional activation?

For both activation types, the large critical radius inhibits activation for larger aerosols within the typical lifetime of the simulated clouds (about 15 min). The kinetically limited flow of water molecules slows down the diffusional activation at larger radii, e.g., more than 1000 s are necessary for the activation of an aerosol of 1 μ m dry radius at 1 % supersaturation (Hoffmann 2016). Similarly, collectional activation is not able to produce the necessary radii in the available time since the droplets might be too small to cause intense collisions. Moreover, the critical radii might be too big for the simulated clouds to sustain them and they might fall out of the cloud before activation (the largest activated aerosol is 200 μ m in wet radius, Fig. 7).

The questioned sentence has been extended (line 214-215): "Larger aerosols do not activate at all since their critical radius is too large to be exceeded by diffusion or collection."

18. Minor question.

If red is 0.8 and blue is 0.2, and 100 collectional activations occur, I understand that 80 activated and 20 inactivated aerosols are involved in these

100 collectional activation events. Is this correct?

If so, in Fig.7, red is always larger than blue, but this is puzzling.

At the section starting from L.135, it is declared that the following two processes are considered a collectional activation:

inact + inact -> act

inact + act -> act

It means, the number of activated aerosols involved in collectional activations must be always smaller than the number of inactivated aerosols involved.

However, this is not the case in Fig.7.

Please make this point clear.

Maybe just the legend is opposite? That is, red is inactivated and blue is activated? or maybe you count

inact + inact -> act as blue and inact + act -> act as red?

The whole figure has been changed to clarify the manuscript. Figure 8 shows the average number of collections necessary for the collectional activation of one aerosol. The number of collected activated or inactivated particles has been neglegated in this figure. All necessary information on how many activated aerosols have been involved in the analyzed collectional activations was contained in the former Fig. 7b (now Fig. 9).

19. Minor question.

Same question as above. How do you calculate the red and blue line for this case? **See last comment.**

20. Minor request

It is difficult to follow the meaning of this sentence. In particular the last half. Do you mean "average entrainment height of all particles inside the cloud is the cloud base"?? Please give a clear and detailed explanation.

Yes. The sentence has been clarified to: "Since multiple collections are necessary for their activation (see Fig. 8), the lower average entrainment height is representative for the average entrainment height of all particles inside the cloud, which is the cloud base through which most particles enter the cloud (e.g., Hoffmann et al. 2015)." (line 263 - 265)

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On the Limits of Köhler Activation Theory: How do Collision and Coalescence Affect the Activation of Aerosols?

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- Abstract. Activation is necessary to form a cloud droplet from an aerosol, and it occurs as soon as a wetted aerosol grows
- 2 beyond its critical radius. Traditional Köhler theory assumes that this growth is driven by the diffusion of water vapor. However,
- 3 if the wetted aerosols are large enough, the coalescence of two or more particles is an additional process for accumulating
- 4 sufficient water for activation. This transition from diffusional to collectional growth marks the limit of traditional Köhler
- 5 theory and it is studied using a Lagrangian cloud model in which aerosols and cloud droplets are represented by individually
- 6 simulated particles within large-eddy simulations of shallow cumuli. It is shown that the activation of aerosols larger than
- 7 $0.1 \,\mu\mathrm{m}$ in dry radius can be affected by collision and coalescence, and its contribution increases with a power-law relation
- 8 toward larger radii and becomes the only process for the activation of aerosols larger than $0.4-0.8\,\mu\mathrm{m}$ depending on aerosol
- 9 concentration. Due to the natural scarcity of the affected aerosols, the amount of aerosols that are activated by collection is
- small with a maximum of 1 in 10000 activations. The fraction increases as the aerosol concentration increases, but decreases
- 11 again as the number of aerosols becomes too high and the particles too small to cause collections. Moreover, activation by
- 12 collection is found to affect primarily aerosols that have been entrained above the cloud base.

13 1 Introduction

- 14 Activation is necessary for the formation of droplets from aerosols. Accordingly, activation controls the number and size of
- 15 cloud droplets and hence so-called aerosol-cloud interactions, e.g., cloud albedo (Twomey, 1974) or cloud lifetime (Albrecht,
- 16 1989). In contrast to cloud droplets, which behave like bulk water, the understanding of unactivated aerosols and their activa-
- 17 tion depends fundamentally on the aerosol's physicochemical properties, which cause the so-called solute and curvature effects
- 18 (Köhler, 1936). These effects enable, on the one hand, the stable existence of haze particles (also termed wetted aerosols) in
- 19 subsaturated environments and inhibit, on the other hand, diffusional growth if the supersaturation does not exceed a certain
- 20 threshold. This so-called critical supersaturation is associated with a critical radius, to which a wetted aerosol must grow to be
- 21 considered as activated. Small aerosols activate almost immediately when the supersaturation exceeds the critical supersatura-
- 22 tion, as it is assumed in many parameterizations of the activation process (e.g., Twomey, 1959). For larger aerosols, however,
- 23 the critical radius becomes so large that the time needed for activation can be substantially increased (or even prevented un-
- 24 der certain conditions) due to the kinetically limited transport of water vapor to the particle's surface (Chuang et al., 1997).
- 25 Therefore, Due to their large size, however, these particles may behave like regular cloud droplets inside the environment of a

cloud although they are not formally activated (Nenes et al., 2001). Accordingly, Köhler activation theory is usually considered 26 a weak concept for these particles. But where are the limits of Köhler activation theory located? An upper limit of the appli-27 28 cability of Köhler activation theory can be identified by the switch from predominantly diffusional to collectional (collision 29 followed by coalescence) mass growth if the involved particles become large enough. Indeed, inactivated aerosols triggering collisions is closely related to the impact of giant and ultra-giant aerosols (dry radius $> 1 \,\mu m$) on clouds, which are able to 30 31 initiate precipitation due to their large wet radii (> $20 \,\mu m$) (e.g., Johnson, 1982). Recent Moreover, recent studies indicate that collection might even affect smaller particles: by considering the effects of turbulence, the collection kernel for the interaction 33 of small particles can be significantly increased (e.g., Devenish et al., 2012). Accordingly, the main questions of this study are: Where are the limits of traditional Köhler activation theory? At which aerosol size will collection dominate the activa-34 tion process? And how much does collectional activation contribute to the activation of aerosols? To answer these questions, theoretical arguments and large-eddy simulations (LES) with particle-based cloud physics are applied. Particle-based cloud 36 physics, so-called Lagrangian cloud models (LCMs), are especially suitable for this study because they explicitly resolve the 37 38 activation process and do not rely on a parameterization of it (e.g., Andrejczuk et al., 2008; Hoffmann et al., 2015; Hoffmann, 2016). Therefore, the results will give insights on the physical processes usually not covered (or missed) by those activation 39 parameterizations typically implemented in other cloud models. 40 This paper is designed as follows. The subsequent Section 2 will illuminate how collections can cause (or even inhibit)

This paper is designed as follows. The subsequent Section 2 will illuminate how collections can cause (or even-inhibit) activation by simple theoretical arguments. In Section 3, the LES-LCM simulation setup is introduced. Results will be presented in the Sections 4 and 5, where the former section exemplifies the applied methodology used to untangle diffusional from collectional activation and the latter section presents the results from a shallow cumulus test case. The study is summarized and discussed in Section 6. Appendix A introduces the governing equations of the applied LCM and necessary extensions carried out for this study.

47 2 Theoretical considerations

- 48 In this section, the general effects of coalescence on the activation of aerosols will be addressed. To simplify the argumentation
- 49 in this part of the study, it is assumed that collections take place regardless of the physics that enable or inhibit them in reality.
- 50 Moreover, all other microphysical processes, specifically diffusional growth, are neglected.
- We consider one particle which grows by coalescing with other particles. Accordingly, the particle's water mass after n
- 52 collections is given by

53
$$m_n = m_0 + \sum_{i=1}^n m_i = m_0 + n \cdot \langle m \rangle,$$
 (1)

54 where m_0 terms the particle's initial water mass and m_i (i > 0) the mass of water added by each collection. The second equals

55 sign introduces the assumption of a monodisperse ensemble of collected particles.

Based on Köhler theory, it can be shown that the critical radius for activation is given by

$$7r_{\text{crit}} = \sqrt{3\frac{b \cdot m_s}{A}},$$

where m_s is the dry aerosol mass. Curvature effects are considered by $A = 2\sigma/(\rho_1 R_v T)$, depending on the surface tension of water σ , mass density of water ρ_l , specific gas constant of water vapor R_v , and temperature T. The physicochemical aerosol properties responsible for the solute effect are represented by $b = 3\nu_s \rho_s \mu_l/(4\pi \rho_l \mu_s)$, with the van't Hoff factor ν_s , the mass density of the aerosol ρ_s , and the molecular masses of water μ_l and aerosol μ_s , respectively. Accordingly, the critical mass for activation after n collections yields

63
$$m_{\text{crit},n} = \frac{4}{3}\pi\rho_{\text{l}} \cdot r_{\text{crit},n}^3 = \frac{4}{3}\pi\rho_{\text{l}} \cdot \left[3\frac{b}{A} \cdot \left(m_{\text{s},0} + \sum_{i=1}^n m_{\text{s},i} \right) \right]^{3/2},$$
 (3)

where $m_{s,0}$ terms the initial aerosol mass and $m_{s,i}$ (i>0) the aerosol mass added by each collection. Approximating the summation in (3) demands further assumptions on the distribution of aerosol mass within the particle spectrum. Two scenarios are defined. Scenario A: the collected particles contain a negligible amount of aerosols. Accordingly, the aerosol mass does not change $(\sum_{i=1}^{n} m_{s,i} = 0)$. Scenario B: each particle contains the same mass of aerosol. Correspondingly, the aerosol mass increases proportionally to the number of collections $(\sum_{i=1}^{n} m_{s,i} = n \cdot \langle m_s \rangle)$.

In Fig. 1, the evolving particle radius and critical radius are displayed as a function of the number of collections (details on the particle properties are given in the figure's caption). The simultaneous examination of particle radius and critical radius reveals if a particle is activated (particle radius larger than critical radius) or deactivated (particle radius smaller than critical radius). For scenario A, the initially inactivated particle (black line) grows faster than the critical radius (blue line), and the aerosol activates after 3 collections. For scenario B, an initially inactivated particle (continuous red line) and an initially activated particle (dashed red line) are examined are examined (the critical radii are displayed in red by a continuous or dashed line, respectively). Since the critical radius for activation increases faster than the particle radius, activation is inhibited or the deactivation of previously activated particle is caused.

These considerations suggest that only the collection of particles with a large amount of water and a comparably small amount of aerosol mass (i.e., highly dilute solution droplets) might lead to activation (as shown in scenario A). This, however, indicates that the collected particles are probably activated already. Therefore, the process of collectional activation will not increase the total number of activated aerosols since one ore or more already activated aerosols need to be collected (or and hence annihilated) in the process of one collectional activation. By contrast, the collection of particles with a comparably large amount of aerosol (i.e., less dilute solutions, as shown in scenario B) might inhibit activation since the increase of the critical radius exceeds the increase of the wet radius.

The following part of the study is investigating how coalescence is able to cause aerosol activation in shallow cumulus clouds using a detailed cloud model considering diffusional growth as well as detailed physics of collision and coalescence.

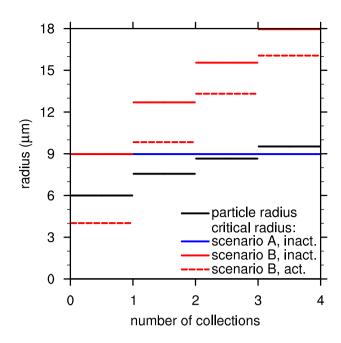


Figure 1. Change of particle radius (black line) and critical radius (colored lines) as a function of the number of collections for the growth scenarios A (negligible increase of aerosol mass, blue line) and B (aerosol mass increases proportional to the number of collections, red lines) as well as an initially inactivated (continuous lines) and an activated particles particle (dashed line). The initial wet particle radius and the wet radii of the collected particles are assumed to be $6\,\mu\text{m}$. The initial dry aerosol mass (sodium chloride) is $2.2 \times 10^{-16}\,\text{kg}$ ($0.29\,\mu\text{m}$ dry radius) (continuous lines) and $4.4 \times 10^{-17}\,\text{kg}$ ($0.17\,\mu\text{m}$ dry radius) (dashed line). For scenario B, the collected particles contain $2.2 \times 10^{-16}\,\text{kg}$ dry aerosol mass ($0.29\,\mu\text{m}$ dry radius).

3 Simulation setup

 The following results are derived from LES simulations applying an LCM for representing cloud microphysics. The LCM is based on a recently developed approach which simulates individual particles that represent an ensemble of identical particles and maintains, as an inherent part of this approach, the identity of droplets and their aerosols throughout the simulation (Andrejczuk et al., 2008; Shima et al., 2009; Sölch and Kärcher, 2010; Riechelmann et al., 2012; Naumann and Seifert, 2015). A summary of the governing equations and the extensions carried out for this study to treat aerosol mass change during collision and coalescence is given in the Appendix A. The underlying dynamics model, the LES model PALM (Maronga et al., 2015), solves the non-hydrostatic incompressible Boussinesq-approximated Navier-Stokes equations, and prognostic equations for water vapor mixing ratio, potential temperature, and subgrid-scale turbulence kinetic energy. For scalars, a monotonic advection scheme (Chlond, 1994) is applied to avoid spurious oscillations at the cloud edge (e.g., Grabowski and Smolarkiewicz, 1990).

The initial profiles and other forcings of the simulation follow the shallow trade wind cumuli intercomparison case by Siebesma et al. (2003), which itself is based on the measurement campaign BOMEX (Holland and Rasmusson, 1973). A

cyclic model domain of $3.2 \times 3.2 \times 3.2 \,\mathrm{km}^3$ is simulated. (In comparison to Siebesma et al. (2003), the horizontal extent has been halved in each direction due to limited computational resources.) The grid spacing is $20\,\mathrm{m}$ isotropically. Depending on the prescribed aerosol concentration, a constant time step of $\Delta t = 0.2 - 0.5\,\mathrm{s}$ had to be used for the correct representation of condensation and evaporation, but it is also applied to all other processes. The first 1.5 hours of simulated time are regarded as model spin-up; only the following four hours are analyzed.

The simulated particles, called super-droplets following the terminology of Shima et al. (2009), are released at the beginning of the simulation, and are randomly distributed within the model domain up to a height of $2800\,\mathrm{m}$. The average distance between the super-droplets is $4.3\,\mathrm{m}$, yielding a total number of about 360×10^6 simulated particles and about $100\,\mathrm{super}$ -droplets per grid box. Initial weighting factors, i.e., the number of real particles represented by each super-droplet, are $8\times10^9, 48\times10^9, 160\times10^9, 320\times10^9, 320\times10^9$, and 640×10^9 for each particle, representing aerosol concentrations of 100, 600, 2000, 4000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 3000, 30

The dry aerosol radius is assigned to each super-droplet using a random generator which obeys a typical maritime aerosol distribution represented by the sum of three lognormal distributions (Jaenicke, 1993) (Fig. 2). However, only aerosols larger than $0.005\,\mu\text{m}$ are initialized since smaller aerosols do not activate in the current setup. The different aerosol concentrations are created by scaling the weighting factor of each simulated particle to attain the desired concentration. The aerosols are assumed to consist of sodium chloride (NaCl, mass density $\rho_{\rm s} = 2165\,\mathrm{kg\,m^{-3}}$, van't Hoff factor $\nu_{\rm s} = 2$, molecular weight $\mu_{\rm s} = 58.44\,\mathrm{g\,mol^{-1}}$). The initial wet radius of each super-droplet is set to its approximate equilibrium radius depending on aerosol mass and ambient supersaturation (Eq. (14) in Khvorostyanov and Curry, 2007). The applied collection kernel includes effects of turbulence, which have been shown to increase the collection probability of small particles significantly (e.g., Devenish et al., 2012). See Appendix A for more details on the applied LCM.

119 4 Methodology

In this section, the applied methodology for untangling the contributions of diffusion and collection to the activation of aerosols is introduced. An aerosol becomes activated when it grows beyond its critical radius ($r > r_{crit}$). This process can be driven by the diffusion of water vapor or by accumulating liquid water due to collection or by a combination of both. To Moreover, activation requires the particle to be located in a volume of air with a sufficient supersaturation to enable unhindered diffusional growth after activation, Depending on the microphysical process responsible for the final crossing of r_{crit} , different supersaturation allow unhindered diffusional growth.

Due to the continuous character of diffusional growth, the supersaturation has to be larger than the activated particle is required to be located in a volume of air which exceeds the critical supersaturation at the moment of activation $(S > S_{crit})$ at 128 $r = r_{crit}$. This is always in the moment in which the critical radius is exceeded:

$$129 S > S_{\text{crit}} = S_{\text{eq}}(r_{\text{crit}}), (4)$$

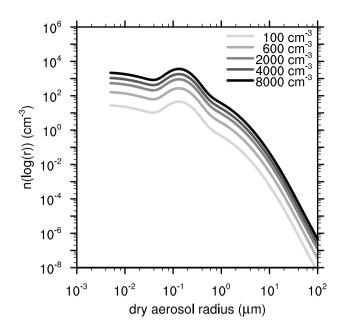


Figure 2. The number density distribution of dry aerosol radii for different aerosol concentrations (line brightness).

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where $S_{\rm eq}$ is the equilibrium supersaturation calculated according to Köhler theory (see Eq. (A3)). This condition is automatically fulfilled in the case of diffusional growth, but it is checked additionally in the case of collectional activation to ensure equivalence of collectional and diffusional activation. due to the constraints of Köhler theory on the equilibrium supersaturation. If the critical radius is exceeded by collection, the radius after collection might be immediately larger than $r_{\rm crit}$ and, hence, the necessary supersaturation is allowed to be smaller to enable unhindered diffusional growth:

$$135 \quad S \ge S_{\text{eq}}(r_{\text{ac}}), \tag{5}$$

where $r_{\rm ac} \ge r_{\rm crit}$ is the wet radius after collection. This criterion is not automatically fulfilled and checked additionally to establish the formal equivalence of both processes, i.e., enabling unhindered diffusional growth after activation. Note that the process of activation, i.e., the entire growth beyond $r_{\rm crit}$, can be driven by diffusional growth or by accumulating liquid water due to collection or by a combination of both.

To decide if an activation is primarily driven by diffusion or collection, all simulated particles have been tracked throughout the simulation and their mass growth has been integrated from their minimum mass before activation, $\min(m)$, to the critical activation mass, m_{crit} :

143
$$\Delta m|_{\text{diff}} = \int_{\min(m)}^{m_{\text{crit}}} dm|_{\text{diff}},$$
 (6)

144
$$\Delta m|_{\text{coll}} = \int_{\min(m)}^{m_{\text{crit}}} dm|_{\text{coll}},$$
 (7)

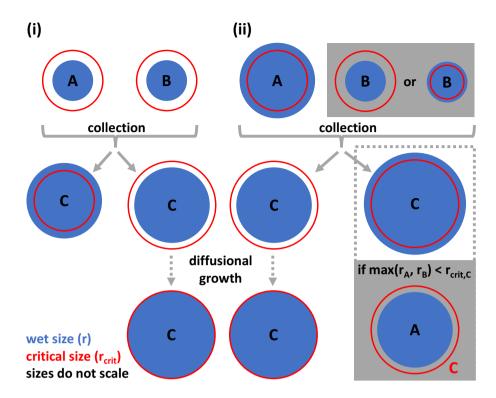


Figure 3. Time series Possible microphysical processes leading to the collectional activation of a particle which is activated by collection. Panel Scenario (ai) shows its radius contains only inactivated aerosols, scenario (blackii) and critical radius (red) and panel (b) depicts contains at least one activated aerosol aerosol. The blue circle displays the ambient supersaturation experienced by that wet size of the particle (black) and its critical supersaturation (, the red) circle the critical size, which has to be exceeded for activation. The displayed sizes do not scale.

where $\mathrm{d}m|_{\mathrm{diff}}$ and $\mathrm{d}m|_{\mathrm{coll}}$ are directly derived from the LCM's model equations (A2) and (A6) – (A7), respectively. Note the following procedures for determining $\min(m)$, $\Delta m|_{\mathrm{diff}}$, and $\Delta m|_{\mathrm{coll}}$ during the simulation: (i) If a particle shrinks below $\min(m)$ before activation, $\Delta m|_{\mathrm{diff}}$ and $\Delta m|_{\mathrm{coll}}$ are set to zero and are re-calculated starting from this new minimum mass. (ii) If a particle becomes deactivated, i.e., evaporates smaller than its critical radius after being activated, the current mass is considered the new $\min(m)$ and $\Delta m|_{\mathrm{diff}}$ and $\Delta m|_{\mathrm{coll}}$ are set to zero. (iii) If a collection does not result in an activation and the particle evaporates back to its equilibrium radius afterwards, $\Delta m|_{\mathrm{diff}}$ will be negative and $\Delta m|_{\mathrm{coll}}$ positive. To avoid the potentially incorrect classification of a following activation, $\Delta m|_{\mathrm{diff}}$ and $\Delta m|_{\mathrm{coll}}$ are set to zero if $\Delta m|_{\mathrm{diff}}$ becomes negative and the current mass is considered as $\min(m)$.

The following two processes are considered. To identify a collectional activationif the, the integrated collectional mass growth exceeds the diffusional $(dm|_{coll} > dm|_{diff})$: first, the $\Delta m|_{coll}$ is compared to the diffusional $\Delta m|_{diff}$ in the moment the particle grows beyond its critical radius. If the former exceeds the latter, $\Delta m|_{coll} > \Delta m|_{diff}$, this activation is considered as collectional. There are various microphysical interactions resulting in $\Delta m|_{coll} > \Delta m|_{diff}$, and its basic types are illustrated

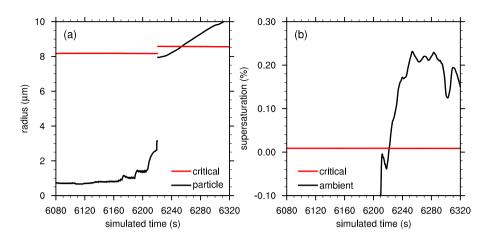


Figure 4. Time series of a particle which is activated by collection. Panel (a) shows its radius (black) and critical radius (red) and panel (b) depicts the ambient supersaturation experienced by that particle (black) and its critical supersaturation (red).

in Fig. 3. Note that also a combination or a repetition of these types is possible, i.e., multiple subsequent collections. In a collectional activation of type (i), the water mass growth by collection dominates, i.e., the coalescence of two inactivated aerosols resulting previously inactivated aerosols A and B results directly or after some diffusional growth in an activation; second, the activated particle C. In a collectional activations of type (ii), the critical radius increases faster than wet radius, i.e., the coalescence of an inactivated aerosol with an activated aerosol resulting in an inactivated aerosolalready activated particle A with another activated or an inactivated particle B results in inactivated particle C, which activates after some diffusional growth. If the latter process results directly in an activated aerosol, this collection resulting particle is directly activated, this process is only considered a collectional activation if the largest wet radius of initially activated particle the two coalescing particles A and B is smaller than the critical radius of the newly formed activated particle. The latter restriction produced particle C:

$$167 \quad \max(r_A, r_B) < r_{\text{crit}, C}. \tag{8}$$

This ensures that the coalescence of both particles combined water of particles A and B is necessary to aggregate the required amount of water for activation and excludes scavenging by large activated particles collecting smaller ones while precipitating activate particle C. If this is not the case, i.e., the water of particle A or B is able to activate particle C on its own, the latter process is considered a regular collection of cloud droplets or as scavenging and neglected in the following analysis. Moreover, the coalescence of two activated particles resulting in a collectional activation is mathematically possible but not found to play a role in the analyzed simulations. Note that only collections collectional activations of the first type are able to increase the number of activated aerosols, while the second type might have no or a negative impact on the total number of activated aerosols as discussed in Section 2 since the coalescence of at least one activated particle results in one activated particle.

To exemplify this methodology, Fig. 4 shows, for an aerosol selected from the LCM simulations discussed below, the time series of its radius and critical radius (panel a) and the ambient supersaturation and critical supersaturation (panel b). Note

that this aerosol is actually one super-droplet, representing a larger ensemble of identical aerosols, which is, however, inter-preted as one aerosol here. The initial dry radius of the aerosol is 0.27 µm. On its way to activation, the particle experiences diffusional growth, which can be easily identified by the continuous change of radius. One collection event, characterized by a distinct increase in radius, is visible at 6220s simulated time. At this point in time, the inactivated aerosol (wet radius $3.1\,\mu\mathrm{m}$) coalesces with an activated particle (wet radius $7.8\,\mu\mathrm{m}$, aerosol dry radius $0.13\,\mu\mathrm{m}$), but the product of coalescence (wet radius $7.9 \,\mu\text{m}$, aerosol dry radius $0.28 \,\mu\text{m}$) remains inactivated. Due to the increased amount of aerosol mass, the critical radius (and to a lesser extent the critical supersaturation) increases (decreases) after the coalescence. Afterwards, the particle grows by diffusion and exceeds the critical radius at 6253s simulated time, which can be identified as the time of activation. All in all, this activation is considered a collectional activation since $\frac{dm}{coll} = 1.9 \times 10^{-12} \text{ kg} > \frac{dm}{diff} = 6.2 \times 10^{-13} \text{ kg}$. $\Delta m|_{\rm coll} = 1.9 \times 10^{-12} \,\mathrm{kg} > \Delta m|_{\rm diff} = 6.2 \times 10^{-13} \,\mathrm{kg}$. Moreover, this is a collectional activation of type (ii) since it involves the collection of an already activated aerosol.

5 Results

The last section showed that collection can contribute significantly to the mass growth leading to the activation of a single aerosol. But how does collection contribute to the activation of aerosols in general? Figure 5 shows the vertical profiles of (a) the collectional activation ratemaximum diffusion radius, i.e., the number of aerosols activated by collection per unit volume and unit timelargest critical radius of an aerosol activated exclusively by diffusion at a certain height, (b) the maximum diffusion radius, supersaturation, (c) the collectional activation rate, i.e., the maximum critical radius of aerosols exclusively activated by diffusion at a certain heightnumber of aerosols activated by collection per unit volume and unit time, and (e) the supersaturationd) the corresponding diffusional activation rate. Profiles (a) and (eb) to (d) are conditionally averaged over all supersaturated grid cells. Only data of the last 4 simulated hours is considered. Values above the average cloud top height (at 1500 m) are not displayed due to insufficient statistics.

The maximum diffusion radius (Fig. 5 b) increases (neglecting outliers) a) increases almost monotonically with height reaching maxima between $40 \,\mu\text{m}$ 30 $\,\mu\text{m}$ and $9 \,\mu\text{m}$ for aerosol concentrations of $100 \,\text{cm}^{-3}$ to $8000 \,\text{cm}^{-3}$, respectively. The supersaturation (Fig. 5 eb) exhibits a distinct peak at the cloud base and relaxes toward its equilibrium value determined by the number of activated aerosols and vertical velocity above (e.g., Rogers and Yau, 1989, Chap. 7). Due to the larger number of water vapor absorbers, the supersaturation as well as the maximum diffusion radius are generally smaller in the more aerosol-laden simulations.

The collectional activation rate (Fig. 5 ac) increases almost linearly with height. This increase can be related to the longer lasting diffusional growth resulting in potentially larger particles at higher levels, which increases the collection kernel and therefore the collection probability. The slope is larger in aerosol-laden environments, where more aerosols are available for activation. Additionally, the height above cloud base, where the collectional activation starts, increases with the aerosol concentration since the average particle radius is too small to enable collisions at lower levels. Accordingly, the collectional activation rate in the 8000 cm⁻³ simulation exhibits smaller to similar values than in the 4000 cm⁻³ simulation although the slope in the

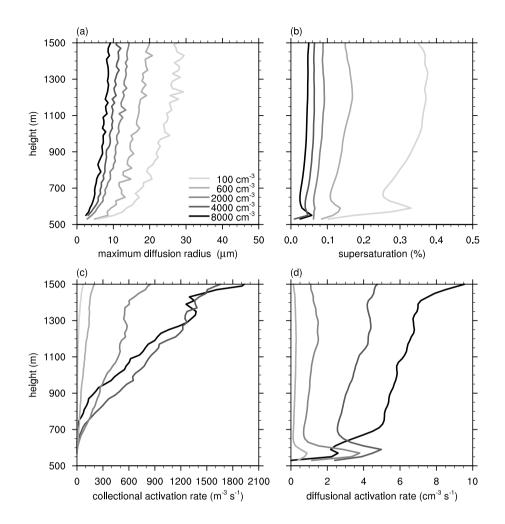


Figure 5. Vertical profiles of the collectional activation rate maximum diffusion radius (a), and the maximum diffusion radius supersaturation (b), and the supersaturation collectional activation rate (c), and the diffusional activation rate (d) for the analyzed aerosol concentrations (line brightness).

8000 cm⁻³ simulation is larger. Note that the general The shape of the collectional activation rate differs significantly from the typical profile of diffusional activation the diffusional activation rate (Fig. 5 d), which exhibits as a distinct peak at cloud base where the majority of aerosols activates by diffusion (not shown, see, e.g., Slawinska et al., 2012; Hoffmann et al., 2015) after the entrainment through the cloud base (Slawinska et al., 2012; Hoffmann et al., 2015).

Generally, The comparison of Fig. 5c and d indicates already that the contribution of collectional activation to the number of activated aerosols is significantly smaller than the contribution of diffusional activation (Fig. 6): Figure 6 shows that only 1 activation in 10 000 to 35 000 is caused by collection, with a greater contribution of collectional activation in moderately aerosol-laden environments up to 4000 cm⁻³. As it will be outlined below, this increase can be attributed to a shift of col-

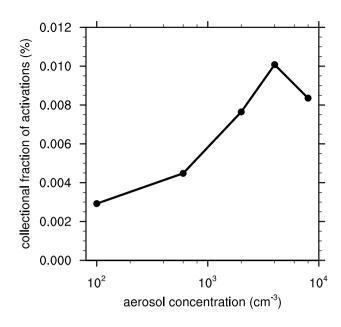


Figure 6. The collectional fraction of all activations as a function of the aerosol concentration.

lectional activation to smaller, but more numerous aerosols. For 8000 cm⁻³, however, the fraction decreases again since the particles are too small to trigger a larger amount of collisions.

Figure 7 shows the collectional and diffusional fraction of activations as a function of the dry aerosol radius on the lower abscissa and the corresponding critical radius (calculated for the cloud base temperature of approximately 294.5 K) on the upper abscissa. As expected, diffusional activation is the dominant process for small aerosols (dry radius $< 0.1 \,\mu\text{m}$) as long as the dry aerosol radius is not too small and the corresponding critical supersaturation not too high to inhibit activation. Accordingly, the left boundary of diffusional activation is shifted toward larger radii as the maximum supersaturations decrease in more aerosol-laden environments (see Fig. 5 eb). For aerosols larger than $0.1 \,\mu\text{m}$, collectional activation becomes increasingly important affecting aerosols in the range of $0.16 - 2.5 \,\mu\text{m}$, $0.13 - 0.65 \,\mu\text{m}$, $0.11 - 0.46 \,\mu\text{m}$, $0.092 - 0.33 \,\mu\text{m}$, $0.11 - 0.28 \,\mu\text{m}$ for aerosol concentrations of 100, 600, 2000, 4000, and $8000 \,\text{cm}^{-3}$, respectively. Larger aerosols do not activate at all since their critical radius is too large to be exceeded by diffusion or collection.

The collectional fraction of activations increases following a power-law relation toward larger radii, reflecting the higher collision probability of larger particles. The collectional fraction reaches up to 100% for the 100, 600, and $2000\,\mathrm{cm^{-3}}$ simulations at about 0.83, 0.54, and $0.42\,\mu\mathrm{m}$ dry aerosol radius, respectively, indicating a significant effect of collectional activation on this part of the aerosol spectrum. For higher aerosol concentrations, collectional activation does not dominate, but still contributes noteworthy with fractions up to 20% and 10% for aerosol concentrations of 4000 and $8000\,\mathrm{cm^{-3}}$, respectively. The dry aerosol radius at which collectional activation reaches 100% can be clearly assigned to matches the maximum radii that can be produced by diffusion. To create any larger particles, existing particles need to be merged. Accordingly, to activate aerosols with a larger critical radius, collection must be inherently involved. For the $100\,\mathrm{cm^{-3}}$ simulation, the largest radii

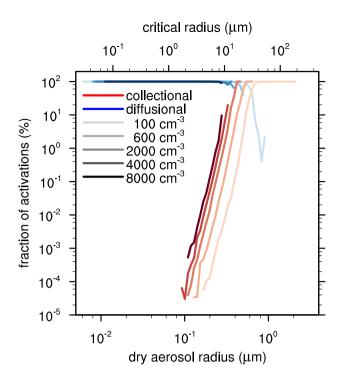


Figure 7. The collectional (red lines) and diffusional (blue lines) fraction of activations as a function of the dry aerosol radius (lower abscissa) and critical radius (at cloud base temperature of 294.5 K, upper abscissa) for the analyzed aerosol concentrations (line brightness).

produced by diffusion are about $40 \,\mu\text{m}$ (neglecting the outliers in $30 \,\mu\text{m}$ (Fig. 5 ba), corresponding to a dry aerosol radius of $0.76 \,\mu\text{m}0.63 \,\mu\text{m}$, which is close to the dry aerosols first dry aerosol radii exhibiting a $100 \,\%$ collectional fraction of activations. A similar agreement can be found for the simulations initialized with aerosol concentrations of 600 and $2000 \,\text{cm}^{-3}$.

In general, the range of aerosols affected by collectional activation shifts toward smaller radii as the aerosols concentration increases. This is primarily a result of the decreasing maximum radii that can be reached by diffusion alone (Fig. 5 ba). Additionally, the supersaturation decreases too (Fig. 5 cb), which decelerates diffusional activation and therefore favors collectional activation. Since small aerosols are significantly more abundant than larger ones (Fig. 2), the number of aerosols that are potentially activated by collection increases as a result of this shift, resulting in the larger collectional fraction of all activations shown in Fig. 6.

In Section 2, it has been argued that the collection of particles with a large fraction of liquid water (and accordingly less acrosol) are more beneficial to collectional activation than particles with a large amount of acrosol mass.

How many collections are necessary for the collectional activation of one aerosol? Figure 8 a displays the average number of collisions that take place during a collectional activation, separated into collected activated and collected inactivated particles. Accordingly, their sum yields the total number of collected particles necessary for a collectional activation. For dry aerosol radii up to $0.3-0.5\,\mu\mathrm{m}$ (depending on aerosol concentration), only one collection (activated plus inactivated) is necessary to

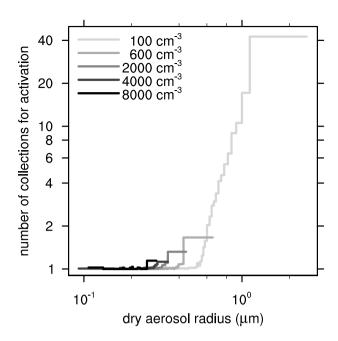


Figure 8. Panel (a) displays the The average number of collected activated (red lines) and inactivated acrosols (blue lines) collections necessary to cause a collectional activation as a function of the dry acrosol radius for the analyzed acrosol concentrations (line brightness). The data has been binned; each bin contains at least 3% of all registered collectional activations. Panel (b) shows the effective activation ratio (i.e., the net increase in the number of newly activated acrosols per collectional activation) as a function of acrosol concentration.

cause activation, while for . For larger aerosols more collections are needed. For the aerosols activated by only one collision, about 40% of all events involve two inactivated aerosols and 60% an inactivated as well as one activated aerosol, indicating the beneficial effect of highly dilute solution droplets to collectional activation as discussed above.

Accordingly, a substantial number of activated acrosolsare annihilated during collectional activation: up to 42 collections for the activation of acrosols with a dry radius of more than $1.0 \,\mu\text{m}$. As illustrated in Fig. 3, not all of these collections involve the coalescence of inactivated acrosols, which would result in a increase of the number of activated acrosols. In fact, some collections involve already activated acrosols, which results in a neutral or negative impact of collectional activation on the total number of activated particles. To quantify the influence of collectional activation on the number of activated acrosols, the *effective activation ratio* is defined: the net increase in the number of newly activated acrosols per collectional activation. Figure 8b9 displays the effective activation ratio calculated from all registered collectional activations. For an acrosol concentration of $100 \, \text{cm}^{-3}$, where a large portion of acrosols needs multiple collections for activations (Fig. 8), the effective activation ratio is -1.2, i.e., more activated acrosols are annihilated than produced $\frac{1}{2}$ But already to enable the final activation of one acrosol by collection. But for an acrosol concentration of $600 \, \text{cm}^{-3}$ and more, the effective activation ratio becomes positive and is approximately constant at 0.4, indicating that $\frac{1}{2}$ per collectional activation an average number of on average 0.4 new acti-

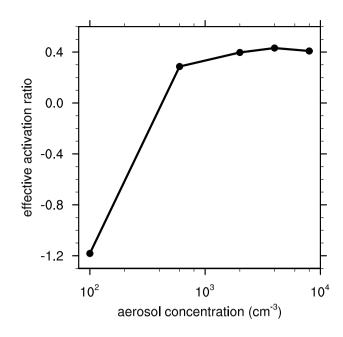


Figure 9. The effective activation ratio (i.e., the net increase in the number of newly activated aerosols per collectional activation) as a function of aerosol concentration.

vated aerosols are produced <u>per collectional activation</u>. This ratio has to be considered in the interpretation of <u>the collectional</u> fraction of all activations (Fig. 6), indicating that the net effect of collectional activation is actually smaller (or even negative).

Collectional fraction of (a) the mass growth leading to collectional activation, and (b) the average entrainment height as a function of the dry aerosol radius for the analyzed aerosol concentrations (brightness). The data has been binned; each bin contains at least 3% of all registered collectional activations.

Although activation is dominated by collectional mass growth for larger aerosols, the growth by diffusion is still essential to create sufficiently large particles to trigger collisions. Figure 10 a depicts the collectional fraction of mass growth needed to grow beyond the critical mass for activation (for aerosols activated by collection). Note that the diffusional fraction of mass growth is the remaining fraction. For the smallest affected aerosols ($\sim 0.1 \,\mu\text{m}$), the collectional fraction of mass growth is about 75% and decreases slightly to 65% for aerosols of $\sim 0.4 \,\mu\text{m}$, indicating that a large contribution of diffusional growth is necessary to produce sufficient large particles that are able to collide. The slight decrease toward larger radii is in agreement with the decrease in the number of activated aerosols collected during the activation process (Fig. 8 a): collection increase toward smaller radii indicates that collectional activation is only possible for the smallest aerosols if they encounter a substantially larger activated particle, which results in a larger collectional fraction of mass growth and a larger number of collected activated aerosols particle. For aerosols larger than $1 \,\mu\text{m}$, the collectional fraction increases rapidly to 97%, which can be attributed to the large critical radii which can be only exceeded by the collection of multiple droplets -(cf. Fig. 8).

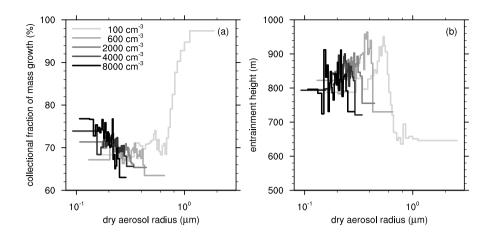


Figure 10. Collectional fraction of (a) the mass growth leading to collectional activation, and (b) the average entrainment height as a function of the dry aerosol radius for the analyzed aerosol concentrations (line brightness). The data has been binned; each bin contains at least 3% of all registered collectional activations.

Figure 10 b displays the mean entrainment height of the particles involved in each collectional activation. Despite the largest particles ($> 0.6 \,\mu\text{m}$) in the most pristine case ($100 \,\text{cm}^{-3}$), all collectional activations involve particles that have entered the cloud well above the cloud base, which is located at $500 - 600 \,\text{m}$. Accordingly, these particles miss the typical supersaturation maximum located at cloud base (see Fig. 5 eb), where a majority of these aerosols normally activates the majority of aerosols activates by diffusion. Indeed, entrainment above cloud base is generally favorable for collectional activation since these aerosols are mixed into an environment where larger particles exist, triggering collisions among them more easily. For aerosols larger than $0.6 \,\mu\text{m}$, the average entrainment height is located closer to the cloud base. Since multiple collections are necessary for their activation (see Fig. 8-a), the lower average entrainment height is more representative for the average entrainment height of all particles inside the cloud, which is the cloud base through which most particles enter the cloud (e.g., Hoffmann et al., 2015).

6 Summary and discussion

The influence of collision and coalescence on the activation of aerosols has been studied using theoretical arguments and large-eddy simulations (LES) with a coupled Lagrangian cloud model (LCM). The presented theory has shown that an unactivated aerosol can be activated by the collection of particles with a comparably small amount of aerosol mass (i.e., particles consisting almost entirely of water), while the collection of large amounts of additional aerosol mass inhibits activation or even causes the deactivation of previously activated aerosols. The LCM simulations of shallow trade wind cumuli indicated that collectional activation becomes possible for aerosols larger than approximately $0.1\,\mu{\rm m}$ in dry radius, and its contribution increases with a power-law relation toward larger aerosols. In pristine conditions, collection is the only process for the activation of aerosols

larger than $0.83\,\mu\mathrm{m}$ in dry radius at an aerosol concentration of $100\,\mathrm{cm}^{-3}$. This boundary is shifted to smaller radii in more polluted environments (down to $0.42 \,\mu m$ at $2000 \, cm^{-3}$). The highest contribution of collectional activation to the total number of activated aerosols is found at an aerosol concentration of $4000\,\mathrm{cm}^{-3}$, where 1 in $10\,000$ activations is caused by collection. If the aerosol concentration becomes higher and hence the particles too small, collectional activation is inhibited and its contri-bution decreases again. Collectional activation frequently involves the collection of already activated aerosols reducing the net increase of newly activated aerosols per collectional activation to 0.4, while the remainder (0.6 activated aerosols) is annihilated during the activation process. Moreover, collectional activation affects predominantly particles that have been entrained above cloud base, i.e., activates acrosols that have not been able to activate by diffusion at cloud base, where the largest above the region of the cloud where the highest supersaturations occur. Accordingly, these particles experience systematically lower supersaturations which prevents diffusional activation. Finally, it has been shown that the collectional activation rate increases almost linear with height, while the slope and the height, from which collectional activation starts, increase with the aerosol concentration.

In conclusion, this study revealed collision and coalescence as an additional process for the activation of aerosols. This process is not covered by commonly applied activation parameterizations (e.g., Twomey, 1959). But does this matter? First of all, with a maximum of 1 in 10 000 activations, collectional activation can be safely neglected. But one can also argue that collectional activation is already (but implicitly) covered by standard cloud models: Activation parameterizations usually activate aerosols as soon as the critical supersaturation is exceeded, i.e., they neglect kinetic effects inhibiting the immediate activation of large aerosols, which need a certain time to grow beyond their critical radius. As pointed out by Chuang et al. (1997), this might overestimate the number of activated aerosols (or cloud droplets) since a certain fraction of the larger aerosols is falsely treated as activated(or as cloud droplets). However, following. Following the argumentation of Nenes et al. (2001), these particles might act, however, as regular cloud droplets due to their large wet radii , as regular cloud droplets although they are not formally activated, and the estimated droplet number concentration is not influenced by this shortcoming of the activation parameterizationa valid measure for particles that behave like cloud droplets. And indeed, this study showed that a certain fraction of these formally inactivated particles are able to collide and coalesce, i.e., act as regular cloud droplets. Similarly, in standard cloud models, these falsely activated cloud droplets will experience the model's representation of collision and coalescence that might ultimately result in an implicit realization of collectional activation.

Accordingly, collectional activation is not of particular importance for determining the number of cloud droplets, but it indicates clearly the limits of Köhler activation theory. Without ambiguity, diffusion-based Köhler activation theory is only applicable to aerosols smaller than $0.1\,\mu\mathrm{m}$ in dry radius, while an increasing fraction of aerosols activates by collection at larger radii. Ultimately, the activation of aerosols larger than about $1.0\,\mu\mathrm{m}$ is entirely caused by collection (if it takes place at all). Therefore, the range between approximately $0.1\,\mu\mathrm{m}$ and $1.0\,\mu\mathrm{m}$ should be considered as a transition zone between (i) typical aerosols that need to experience sufficiently strong supersaturations to grow beyond the critical radius and (ii) so-called giant and ultra-giant aerosols with sufficiently large wet radii to act like cloud droplets by triggering collision and coalescence without being formally activated (e.g., Johnson, 1982).

335 Finally, potential sources of uncertainty within this study shall be mentioned. First, the accuracy of the applied collection kernel is limited. The widely-used collision efficiencies of Hall (1980) for small particles ($\leq 20 \,\mu\text{m}$) are slightly higher 336 than other estimates (e.g., Böhm, 1992). An effect of this uncertainty is—might be the collectional activation of aerosols 337 338 that are too small to collide physically. Accordingly, collectional activation shall affect slightly larger radii than evaluated here. Further note that additional in reality. Moreover, the collection kernel might not incorporate all processes relevant for 339 collections among aerosols and droplets. For instance, Brownian diffusion might increase the collection of smaller particles 340 (e.g., Ardon-Dryer et al., 2015) but might not lead to collectional activation since it will predominantly add aerosol mass and 341 342 only a small amount of water (cf. Section 2). Additional simulations neglecting turbulence effects on the collection kernel 343 (not shown) have exhibited a similar spectral distribution of collectional activation, but indicated a smaller contribution to the total number of activated aerosols. Additionally, the collection algorithm itself might underestimate collisions due to the initial 344 distribution of weighting factors (Unterstrasser et al., 2017), and the determined influence of collectional activation should be 345 considered as a lower estimate. Second, the initialized aerosol distribution is always maritime, i.e., it includes a large fraction 346 of large aerosols which are not part of continental air masses (e.g., Jaenicke, 1993) but are primarily affected by collectional 347 348 activation as shown here. Accordingly, the collectional fraction of activations might be lower in environments which exhibit a smaller fraction of aerosols in the affected size range. Third, not all aerosols consist of (highly hygroscopic) sodium chloride 349 although the size range affected by collectional activation is usually assumed to consists of sea salt (Jaenicke, 1993). Aerosols 350 with a lower hygroscopicity would exhibit a smaller solution effect which is equivalent to a smaller dry radius of the sodium 351 chloride aerosols examined here, i.e., the wet radius of these aerosols would be smaller and they would less likely cause 352 353 collisions. Again, the range of aerosols affected by collectional activation would be shifted to larger dry radii.

Appendix A: The Lagrangian cloud model

354

364

In this section, the basic framework of the Lagrangian cloud model (LCM) applied in this study as well as the extensions made 355 to treat aerosol mass during collision and coalescence are described. One can refer to Riechelmann et al. (2012) for the original 356 357 description, Hoffmann et al. (2015) for the consideration of aerosols during diffusional growth, and Hoffmann et al. (2017) for the most recent description of the LCM. This LCM, as all other available particle-based cloud physical models (Andrejczuk 358 et al., 2008; Shima et al., 2009; Sölch and Kärcher, 2010; Naumann and Seifert, 2015), are based on the so-called super-droplet 359 approach in which each simulated particle represents an ensemble of identical, real particles, growing continuously from an 360 aerosol to a cloud droplet. The number of particles within this ensemble, the so-called weighting factor, is a unique feature 361 362 of each particle, which is considered for a physical appropriate representation of cloud microphysics within the super-droplet approach. 363

The transport of a simulated particle is described by

365
$$\frac{\mathrm{d}X_i}{\mathrm{d}t} = u_i + \widetilde{u}_i - \delta_{i3}w_s,\tag{A1}$$

where X_i is the particle location and u_i is the LES resolved-scale velocity at the particle location determined from interpolating linearly between the 8 adjacent grid points of the LES. A turbulent velocity component $\widetilde{u_i}$ is computed from a stochastic model

- based on the LES sub-grid scale turbulence kinetic energy (Sölch and Kärcher, 2010). The sedimentation velocity w_s is given
- 369 by an empirical relationship (Rogers et al., 1993). Equation (A1) is solved using a first-order Euler method.
- 370 As described in Hoffmann et al. (2015), the diffusional growth of each simulated particle is calculated from

371
$$r \frac{\mathrm{d}r}{\mathrm{d}t} = \frac{S - A/r + b \cdot m_{\rm s}/r^3}{F_{\rm k} + F_{\rm D}} \frac{S - S_{\rm eq}}{F_{\rm k} + F_{\rm D}} \cdot f(r, w_{\rm s}),$$
 (A2)

- 372 where r is the particle's radius and S terms the supersaturation within the grid box, in which the particle is located. Curvature
- 373 and solution effects are considered by the the terms A/r and $b \cdot m_s/r^3$, respectively, equilibrium supersaturation

374
$$S_{\text{eq}} = \frac{A}{r} - \frac{b \cdot m_{\text{s}}}{r^3}$$
. (A3)

- 375 The factor f parameterizes the so-called ventilation effect (Rogers and Yau, 1989). The coefficients $F_k = (L_v/(R_vT) 1)$.
- 376 $L_{\rm v}\rho_{\rm l}/(Tk)$ and $F_{\rm D}=\rho_{\rm l}R_{\rm v}T/(D_{\rm v}e_{\rm s})$ represent the effects of thermal conduction and diffusion of water vapor between the
- 377 particle and the surrounding air, respectively. Here, k is the coefficient of thermal conductivity in air, D_v is the molecular
- 378 diffusivity of water vapor in air, L_v is the latent heat of vaporization, and e_s is the saturation vapor pressure. Equation (A2) is
- 379 solved using a fourth-order Rosenbrock method.
- 380 Collision and coalescence are calculated from a statistical approach in which collections are calculated from the particle
- 381 size distribution resulting from all super-droplets currently located within a grid box(Riechelmann et al., 2012). These inter-
- 382 actions affect the weighting factor A_n (i.e., the number of all particles represented by one super-droplet), the total water
- 383 mass of a super-droplet $M_n = A_n \cdot m_n$ (where m_n is the mass of one particle represented by super-droplet n), and also
- 384 the dry aerosol mass $M_{s,n} = A_n \cdot m_{s,n}$ (where $m_{s,n}$ is the dry aerosol mass of one particle represented by super-droplet
- 385 n), which. The latter interactions has been introduced for this study. The algorithm follows the all-or-nothing principle
- 386 (Shima et al., 2009; Sölch and Kärcher, 2010), which has been rigorously evaluated by Unterstrasser et al. (2017) and has
- been recently implemented into this LCM by Hoffmann et al. (2017).
- 388 It is assumed that the super-droplet with the smaller weighting factor (index n) collects A_n particles from the super-droplet
- 389 with the larger weighting factor (index m), with commensurate changes in M_m , M_n , $M_{s,m}$, and $M_{s,n}$. Since the weighting
- 390 factor of the collecting super-droplet n does not change during this process, its wet radius

391
$$r_n = \left(\frac{M_n}{\frac{4}{3}\pi\rho_1 A_n}\right)^{1/3}$$
 (A4)

392 and the dry aerosol radius

393
$$r_{s,n} = \left(\frac{M_{s,n}}{\frac{4}{3}\pi\rho_s A_n}\right)^{1/3}$$
 (A5)

- 394 increase. Additionally, same-size collections of the particles belonging to the same super-droplet are considered. These inter-
- actions do not change M_n and $M_{s,n}$, but they decrease A_n and accordingly increase r_n and $r_{s,n}$.

These two processes yield in the following description for the temporal change of A_n (assuming that the simulated particles

397 are sorted such that $A_n > A_{n+1}$:

398
$$\frac{\mathrm{d}A_n}{\mathrm{d}t}\delta t = -\frac{1}{2}(A_n - 1)P_{nn} - \sum_{m=n+1}^{N_{\mathrm{p}}} A_m P_{mn}. \tag{A6}$$

399 The first term on the right-hand-side denotes the loss of A_n due to same-size collections; the second term the loss of A_n due

400 to collisions with particles of a smaller weighting factor. The total water mass and the total aerosol mass of a super-droplet

401 change according to

402
$$\frac{\mathrm{d}M_n}{\mathrm{d}t}\delta t = \sum_{m=1}^{n-1} A_n m_m P_{nm} - \sum_{m=n+1}^{N_p} A_m m_n P_{mn}, \tag{A7}$$

403 and

404
$$\frac{dM_{s,n}}{dt}\delta t = \sum_{m=1}^{n-1} A_n m_{s,m} P_{nm} - \sum_{m=n+1}^{N_p} A_m m_{s,n} P_{mn}, \tag{A8}$$

405 respectively. In both equations, the first term on the right-hand-side denotes the increase of M_n or $M_{s,n}$ by the collection of

406 water or dry aerosol mass from super-droplets with a larger weighting factor, while the second term describes the loss of these

407 quantities to super-droplets with a smaller weighting factor. The function P_{mn} controls if a collection takes place:

408
$$P_{mn} := P(\varphi_{mn}) = \begin{cases} 0 & \text{for } \varphi_{mn} \le \xi, \\ 1 & \text{for } \varphi_{mn} > \xi, \end{cases}$$
 (A9)

409 where ξ is a random number uniformly chosen from the interval [0,1] and

410
$$\varphi_{mn} = K(r_m, r_n, \epsilon) A_n \delta t / \Delta V$$
 (A10)

411 is the probability that a particle with the radius r_m collects one of A_n particles with the radius r_n within a volume ΔV during the

412 (collection) time step δt . The collection kernel K is calculated from the traditional collision efficiencies as given by Hall (1980),

413 and includes turbulence effects by an enhancement factor for the collision efficiencies by Wang and Grabowski (2009) and a

414 parameterization of efficiency by Wang and Grabowski (2009) as well as parameterizations for particle relative velocities and

415 changes in the particle radial distribution based on Ayala et al. (2008). These turbulence effects on K are steered by the kinetic

416 energy dissipation rate ϵ calculated by in the LES subgrid-scale model (Riechelmann et al., 2012). The parameterizations by

417 Ayala et al. (2008) are a direct function of ϵ ; the tabulated values of the enhancement factor for the collision efficiency by

418 Wang and Grabowski (2009) are interpolated to the present value of ϵ . The equations (A6) – (A8) are solved using a first-order

419 Euler method.

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- 423 freely available (revision 1954, http://palm.muk.uni-hannover.de/trac/browser/?rev=1954). Additional software developed for the LES/LCM
- 424 model as well as the analysis is available on request.

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