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Title: Estimating the size of a methane emission point-source at different scales: from local to landscape

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Dear Editor,

We would like to thank the referee and editor for their comments. As suggested, we have amended the manuscript to incorporate all of the reviewers' comments.

Please find our detailed responses below.

Yours sincerely,

Stuart Riddick (corresponding author)

and co-authors: Sarah Connors, Andrew Robinson, Alistair Manning, Pippa Jones, David Lowry, Euan Nisbet, Robert Skelton, Grant Allen, Joseph Pitt and Neil Harris

Reviewer 1
Comment3

In section 2.3.3: Why was a Gaussian plume model used for the middle-distance analysis when NAME LPDM particle trajectories were available for Haddenham Church (and were used in the landscape analysis)?	The NAME model can calculate concentrations as well so I guess the two methods could have been used and cross-compared. However, given the short distance from the landfill to the monitoring station and the availability of observed meteorology it was decided that the Gaussian Plume model would be better suited for our purposes.	The following was added at P6 L2: “The particle trajectories were calculated in the NAME model and could have been used to calculate emissions, however given the short distance from the landfill to the monitoring station and the availability of observed meteorology it was decided that a Gaussian Plume model would be better suited for our purposes.”
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Comment 4

Is auto-correlation of error accounted for in the uncertainty analyses? Can the uncertainties be evaluated somehow (reduced chi-square statistic, cross-validation)?	Uncertainty correlation is not considered in InTEM, errors are considered independent of each other. This is a weakness of the setup employed and further analysis is needed using other cost functions can help with this (i.e. the Bayesian cost function).	Added at P7 L30: “Uncertainty correlation was not considered in the modelling, errors are considered independent of each other. This is a weaknesses and further analysis is needed using other cost functions (e.g. the Bayesian cost function).”
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Comment P9 L14

Have you removed the hyphen as requested for "eight-time series"? I agree with the reviewer, this should read "eight timeseries".	Changes as suggested at P9 L27.	P9 L27: “eight-time series” changed to "eight timeseries"
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Reviewer 2
Comment 2

P6, L9-10: “The standard deviation of the lateral (σ_y , m) and vertical (σ_z , m)	The values used can be found in the Supplementary Material Section 1.	Text added at P6 L13:
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mixing ratio distribution are calculated from the stability class of the air (Pasquill, 1974).” So what are the values for the standard deviation used in this paper?		“the values used in our analyses are presented in Supplementary Material Section 1 (Pasquill, 1974).”
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Comment 3

P7, L19: “This allows for any potential bias due to highly uncertain observations to be accounted for.” I don’t see how the bias would be accounted for.	High methane concentration values seen at Haddenham are usually short lived and appear as peaks lasting only a few hours (max). They usually occur at night time and, as the isotopic analysis shows, probably come from a landfill, which is an intermittent of methane. These are therefore more uncertain. The values would have a relatively high cost score at these times. So, by including the hourly SD into the uncertainty calculation this helps to de-weight the large concentrations, which have higher uncertainty, from increasing the overall cost score.	Text added at P7 L22: “High CH ₄ concentration values seen at Haddenham are usually short lived and only appear as peaks lasting a maximum of only a few hours. These usually occur at night time and, as the isotopic analysis shows, probably come from a landfill, which is an intermittent of CH ₄ . These are therefore more uncertain. The values would have a relatively high cost score at these times. So, including an hourly standard deviation into the uncertainty calculation helps to de-weight the large concentrations, which have higher uncertainty, from increasing the overall cost score.”
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Comment 4

P9, L14-15: “A statistical filtering technique separated methane mixing ratios at each site into. . .” What is this statistical filtering?	See comment above.	A new paragraph is included (P9 L12) to make the link to the Connors et al paper, Sarah Connors’ thesis and the new information in the supplementary material clearer. “The results presented here are taken from a study developing a method to estimate regional CH ₄
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		emissions in East Anglia (Connors et al., in prep.). More details on the measurements sites, the inversion set-up used for InTEM, the diagnostics used and the emission uncertainties can be found there and in Connors (2015). The main points for the purposes of this paper are summarised below and in the Supplementary Material Section 2.”
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Comment 5

P9, L16: Why “18th percentile”? Why not 10th or 25th?	This percentile is used as a result of sensitivity analysis showing that the resulting InTEM inversion results produced the lowest cost scores. Therefore, the emissions produced are closer to the measured observations than any of the other percentiles tested. We tested from the 5 th to the 45 th . Sensitivity analysis shows this baseline produces emission results with consistently stable emissions with the lowest cost score of all baselines tested.	Text added at P9 L29: “This percentile was chosen as a result of a sensitivity analysis which showed that InTEM inversion results using the 18 th percentile produced the lowest cost scores, i.e. the calculated emissions are closer to the measured observations compared to any of the other percentiles tested (percentiles from the 5 th to the 45 th were tested).”
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<p>- Both reviewers suggest OSSEs to strengthen support for the landscape scale approach. Are the authors sure they do not wish to add this at this stage?</p> <p>- Following on from this: In the current state, I think you need to remove the last sentence of the abstract. Both reviewers agree you cannot</p>	Unfortunately, due to a lack of resources we are unable to perform OSSEs. As suggested the last sentence of the abstract has been removed.	
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"suggest the landscape inverse modelling approach described in this paper can be used to identify point-sources within an emission landscape" without additional support.		
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<p>My issue is that the authors included a plot that shows troubling results. This is the plot under “Supplementary Material Section 2: Scatterplot of posterior enhancements vs. observed enhancements”.</p> <p>First: these are not enhancements, they are concentrations. In the inverse modeling literature an enhancement is the concentration of the constituent at the observation site <i>minus the background</i>. In my review I asked for a plot of modeled vs observed enhancements in order to separate the variability in the background from the variability in the influence of emissions. When one plots modeled vs. observed concentrations, a well modeled background will hide problems with the model of the emissions.</p> <p>Second: the points in this plot are so dense that they are indistinguishable. There are plotting strategies that can ameliorate this.</p>	<p>The reviewer has raised an interesting point, but we disagree as to its importance. Before going into detail, we think there are two options: (a) remove the NAME InTEM material and put it in a later paper which describes the method in more detail; and (b) leaving the material in with more explanation and context as to the message we are trying to make with that material. We strongly prefer the latter as there is a real need to start addressing the issue of the consistency of GHG emission estimates across scales which is currently lacking.</p> <p>The first point we would like to clarify is that the calculation in NAME InTEM does subtract out a baseline before the emissions are estimated. The procedure for baseline estimation is summarised in section 3.2.2 with more information given in Sarah Connors’s thesis (now referenced) as well as in the Connors et al paper (in prep). In the inversion, NAME InTEM only calculates enhancements. The</p>	<p>Text added to manuscript before P13 L17, i.e. as a new penultimate paragraph: “Even though the annual emission estimate calculated using the InTEM inversion model is close to that calculated by the Gaussian Plume model, the uncertainty associated with the InTEM inversion estimate is large. Comparison of the measurements with the CH₄ time series produced by NAME InTEM (Supplementary Figures 1 and 2) shows the model to consistently underestimate the larger and sharper observed peaks. This arises as a result of the smaller weighting given to the peaks in the observed atmospheric concentrations in the NAME InTEM analysis (which uses all data) than in the WindTrax and Gaussian plume analyses which focus on these peaks. In particular, high peaks are underweighted because they are small scale features not easily delineated in the regional inversions and the boundary layer is harder to model accurately at night when the highest peaks tend</p>
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<p>Third, and most importantly, I think this plot indicates a problem in the model. There is a clear heteroscedasticity in the residuals. This is likely due to the fact that the background was not subtracted. The variation in the model and observed <i>background</i> is likely falling along the 1-1 line, and the enhancements are likely falling off of it, and are likely heteroscedastic.</p> <p>A plot of modeled vs observed enhancements is generally considered the most basic diagnostic plot for this type of analysis. I would actually like to see this type of plot for every site and every model. It isn't clear for which model this plot is showing.</p>	<p>baseline values have been added back in to that figure.</p> <p>The second point we are trying to make is that we are not trying to hide anything. While the data points are dense in that figure, they are much clearer in the accompanying time series showing the measurements and the calculated values. We have changed the order of those two figures in order to make the point more clearly. The figures could be redrawn, but it would take a few weeks.</p> <p>Thirdly, we are not sure why this behaviour should be expected for a large-scale inversion model attempting to estimate point source emissions:</p> <p>(a) The different models give different weightings to the large peaks observed in the concentrations. The emissions calculated by WindTrax and the Gaussian Plume model use those peaks as their major source of information. The NAME InTEM approach, on the other hand, tends to give them low statistical weighting because (i) it is hard to model such small-scale signals in the regional inversion and (ii) the</p>	<p>to occur due to their containment within the shallow nocturnal boundary layer. The heteroscedasticity seen in Supplementary Figure 2 is therefore to be expected as NAME InTEM reproduces the lower values better than the high ones.</p> <p>The inherent challenges in inversion modelling, such as assuming a constant monthly emission (Supplementary Material Section 2 Figure SM2.3) and the atmospheric variability at night which is poorly resolved by the model, result in the emission estimates calculated in this research having an uncertainty of $\pm 91\%$. This research is presented as an example of inversion modelling: a work in progress and, while the emission estimates are currently uncertain, the location of the emissions are well represented.”</p>
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	<p>events occur most strongly at night when the meteorological description is poorer.</p> <p>(b) There is a large variability in emissions (as shown in several Figures) while NAME InTEM is producing an annual estimate. Further, the emissions are not normally distributed (see new Figure in Supplementary info).</p> <p>The discrepancies shown in the figure are entirely consistent with these factors as the ‘outliers’ are nearly all occasions when the measurements are higher than the modelled values. The point of including the analysis in the paper (and it is not a major part) is to examine the consistency between the 3 approaches. We are not trying to exaggerate its importance, but we are trying to highlight its potential for (a) identification of point source emissions, and (b), in time, their quantification. On-going work is underway to improve baseline estimation and error analysis.</p> <p>Finally, similar anomaly plots cannot be straightforwardly produced for the WindTrax and Gaussian Plume approaches because they solve for the emissions values which match the</p>	
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	observations. (In terms of the 3 rd point above, they use all the information contained in each peak studied.) We are therefore unclear as to why putting these back into concentrations is meaningful.	
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Estimating the size of a methane emission point-source at different scales: from local to landscape

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Abstract. High methane (CH₄) mixing ratios (up to 4 ppm) have occurred sporadically at our measurement site in Haddenham, Cambridgeshire since July 2012. Isotopic measurements and back trajectories show that the source is the Waterbeach Waste management park 7 km SE of Haddenham. To investigate this further, measurements were made on June 30th and July 1st 2015 at other locations nearer to the source. Landfill emissions have been estimated using three different approaches at different scales; near-source using the WindTrax inversion dispersion model, middle-distance using a Gaussian plume model and at the landscape scale using the NAME InTEM inversion. The emission estimates derived using the WindTrax and Gaussian plume approaches agree well for the period of intense observations. Applying the Gaussian plume approach to all periods of elevated measurements seen at Haddenham produces year-round and monthly landfill emission estimates with an estimated annual emission of 11.6 Gg CH₄ yr⁻¹. The monthly emission estimates are highest in winter (2160 kg hr⁻¹ in February) and lowest in summer (620 kg hr⁻¹ in July). These data identify the effects of environmental conditions on landfill CH₄ production and highlight the importance of year-round measurement to capture seasonal variability in CH₄ emission.

1 Introduction

Atmospheric methane (CH₄) gas is both a greenhouse gas and partially responsible for modulating tropospheric ozone production and loss. As such, changes in atmospheric CH₄ mixing ratios can cause significant shifts in local and regional atmospheric chemistry and global climate. Current research suggests the most significant CH₄ sources are natural wetlands (top-down, 142–208 Tg CH₄ yr⁻¹; and bottom-up, 177–284 Tg CH₄ yr⁻¹) and agriculture and waste emissions (top-down, 180–241 Tg CH₄ yr⁻¹; and bottom-up, 187–224 Tg CH₄ yr⁻¹), with further contributions from fugitive emission due to the use of fossil fuels, natural emissions and biomass burning (IPCC., 2013; Kirschke et al., 2013). Anthropogenic sources contribute ~60% of modern-day emissions (Saunois et al. 2016). Included in these estimates, decomposition of organic matter at landfills is estimated to comprise between 3% and 19% of global anthropogenic emissions (Chen & Prinn, 2006). Given this large and important uncertainty, the aim of this study is to estimate CH₄ mass flux from an operational landfill in Cambridgeshire using a variety of methods.

Approximately 60% of gas emitted from typical landfills is CH₄, 40% is carbon dioxide and trace amounts are given off as nitrogen, oxygen and water vapour (Hegde et al., 2003). At the surface, anoxic microbial processes form CH₄, whereas oxidation forms both carbon dioxide and water. Deeper below the surface anaerobic processes dictate gas formation due to the oxygen-poor environment. Simple organic acids (e.g. carboxylic acid), carbon dioxide (CO₂) and hydrogen (H₂) are formed from the hydrolysis of organic matter. Methanogenic bacteria then convert carboxylic acid (RCOOH) to CH₄ which can diffuse through the refuse to be emitted to the atmosphere (Xu et al., 2012). Riddick et al. (2016) suggest that instead of heterogeneous emission across the landscape landfill, CH₄ is emitted in discrete hot-spots which may be caused by variability in the materials that can degrade to form CH₄ throughout the landfill and the nature of physical transmission pathways to the surface. Modern landfills in the UK have extensive reticulations of gas pipes to extract methane, and fractures or leaks in the pipes create potent point sources of methane to escape past the soil oxidation barrier.

The emitted CH₄ can be identified by measuring its $\delta^{13}\text{C}$ isotopic signature. Typically, biogenic methane has a $\delta^{13}\text{C}$ isotopic signature of between -55 and -70‰ (Dlugokencky et al., 2011). However, landfill methane emissions, which comprise the residual gas after the methane flux has passed through the oxidation barrier in the soil cover, tend to fall at the isotopically heavier end of this range as oxidative methanotrophy is selective for the lighter carbon. Typically, the $\delta^{13}\text{C}$ isotopic signature for landfill CH₄ in the south east of the UK has been measured at $-58 \pm 3\text{‰}$ (Zazzeri et al., 2015).

Although landfill interiors are well-isolated from day-to-day weather, and even seasonality, emissions from the landfill surface can be strongly affected by environmental conditions. Xu et al. (2012) and Riddick et al. (2016) observed decreasing landfill CH₄ emission as surface atmospheric pressure increased at landfill sites in Lincoln, USA and Ipswich, UK, respectively. Emission of landfill CH₄ may be suppressed as atmospheric pressure increases; conversely, the passage of depressions may pneumatically draw gas out from the landfill. Landfill CH₄ emissions decrease with increased ground temperature in dry soil conditions (Scheutz et al., 2004; Riddick et al., 2016). This is consistent with the hypothesis that bacterial methanotrophic oxidation of methane in the aerobic cover soil has an Arrhenius relationship with temperature, increasing exponentially with ground temperature between 2 and 25 °C (Maurice & Lagerkvist, 2004; Scheutz et al., 2004).

A variety of methods have been used to estimate CH₄ emission estimates from landfill sites using on-site and near-site measurements. These include chamber methods, tracer plume and eddy covariance. Tracer release (TR) methods have been used to good effect, where pollutant mixing ratios are estimated using the co-release of a tracer at a known rate. However, this methodology needs the spatial distribution of tracer emissions to be configured so that it approximately matches the landfill CH₄ emissions (Mønster et al., 2014), presenting logistical challenges when operating on active landfill sites. Landfill CH₄ emissions have been measured using eddy covariance techniques, which use the covariance between vertical wind speed and gas mixing ratio to estimate emissions at a high sampling rate (Xu et al., 2012). However, the assumption of homogeneity by eddy covariance calculations is invalidated by the heterogeneous nature of landfill CH₄ emissions. Furthermore, these estimates strictly apply to the area and time where the measurements are made. Estimates produced in a heterogeneous environment such as a landfill can thus be hard to interpret or extrapolate to the whole landfill and to other times of year.

Riddick et al. (2016) treated a landfill site in Suffolk, UK as a point source and estimated a mean CH₄ emission of 709 $\mu\text{g m}^{-2} \text{s}^{-1}$ using CH₄ concentration data, collected 800 m from the landfill, and meteorological data in an inverse dispersion model. At a farther distance, 2 km, Hensen and Scharff (2001) used a Gaussian plume model to estimate emissions of between 66 and 292 $\mu\text{g m}^{-2} \text{s}^{-1}$ from three landfill sites near Amsterdam in the Netherlands. To our knowledge no research has been conducted on using a Gaussian plume approach at more than 2 km. Also, we believe that no other study has attempted to use an inversion model to identify emission hotspots within a landscape. In this study we use methane measurements made at Haddenham, Cambridgeshire in which we record intermittently high values of up to 4 ppm when the wind is from the southeast. Methane emissions from the Waterbeach Landfill site, 7 km to the SE of our measurement site at Haddenham, are a likely source of these enhancements. To aid identification of this CH₄ source, we collected air samples during a south-easterly air flow and measured the relative abundance of $\delta^{13}\text{C}$ isotopes. These are compared with additional measurements made nearer the landfill. Short time series of CH₄ measurements taken near the landfill are used to estimate emissions using the inverse dispersion model WindTrax (www.thunderbeachscientific.com). The emissions are compared with a Gaussian plume estimate made using the Haddenham data for the same period. The Gaussian plume calculations are extended to cover the whole of the first two years of measurements at Haddenham in order to investigate how the emissions vary over time. Finally, we aim to compare the annual emission estimate found using the Gaussian model with the estimate from the NAME InTEM inversion model that uses two years' CH₄ measurement data from a network throughout East Anglia to estimate the regional annual emission.

The measurement and modelling techniques used are described in Sect. 2. The modelling studies performed are described in Sect. 3. The results are then presented in Sect. 4. The paper concludes with a short discussion and the conclusions of the results and the broader applicability of the approach.

2 Methods

This paper presents methane emission estimates from a landfill made by three methods at different scales: near-source, middle-distance and landscape, a summary of each method is presented in Table 1. Waterbeach Waste Management Park (52.302 N, 0.180 E) is used to deposit unrecyclable waste on an open active area approximately 700 m by 300 m. Surrounding the active area is an area of decomposing waste capped with a welded high-density polyethylene (HDPE) geo-membrane and covered with at least two meters of top soil. Landfill gas is extracted from this capped area under suction using a network of pipes and wells and is used as fuel for the on-site electricity generators. The various measurement techniques are now described in turn.

2.1 Isotopic methane measurements

Whole air samples were collected in 3L Teflon bags at Haddenham Church (Fig. 1). These samples were taken over the 11th February 2015 when the wind was from the south/south-east, i.e. from the direction of the landfill. Air samples were taken at Haddenham in the early morning in order to capture the elevated mixing ratio of landfill emissions within the nocturnal boundary layer. The carbon isotopic ratio, expressed in ‰, was measured in triplicate to high

precision ($\pm 0.05\%$) by continuous flow gas chromatography isotope ratio mass spectrometry (CF GC-IRMS) (Fisher et al., 2006), at Royal Holloway, University of London (RHUL).

2.2 Near-Source

2.2.1 Measurements – Los Gatos UGGA

The Los Gatos Research Ultra-portable Greenhouse Gas Analyser (UGGA; www.lgrinc.com) is a laser absorption spectrometer that measures CH_4 and CO_2 concentration in air using off-axis integrated cavity output spectroscopy (Paul et al., 2001). The UGGA reports CO_2 mixing ratio and CH_4 mixing ratio every second, with a stated precision of < 2 ppb (1σ @ 1 Hz) over an operating range of 0.1 to 100 ppm. Calibration of the UGGA was done before and after deployment using low (1.93 ppm), target (2.03 ppm) and high (2.74 ppm) gases calibrated on the WMO scale.

The UGGA was deployed on a farm road on Mitchell Hill Farm, Cottenham (52.304 N, 0.170 E) where it measured the mixing ratio of CH_4 downwind of the landfill. The measurement site was 300 m NW of the landfill site. The inlet line was attached to a mast 2.5 m above the ground, protected from water incursion using an aluminium funnel and filtered using a $2\ \mu\text{m}$ filter. 15-minute averaged background methane concentration was measured background CH_4 mixing ratios were measured using the Los Gatos UGGA downwind of the landfill site before, at 12 pm and after each day's measurements.

2.2.2 Meteorological Data

In situ meteorological data were collected using a wireless weather station (Maplin, UK) attached to a mast at 2 m from the ground at the measurement site on Mitchell Hill Farm. Meteorological data were sampled and recorded at five-minute intervals and include: wind speed (u , m s^{-1}), wind direction (WD , $^\circ$ to North), air temperature at 2 m (T_a , K), relative humidity (RH , %), rain rate (R , mm hr^{-1}) and air pressure (P , Pa).

Micrometeorological parameters used for subsequent modelling were calculated from data collected at the same measurement site on Mitchell Hill Farm. Roughness height (z_0 , m) and Monin-Obukhov length (L , m) are calculated from the wind speeds measured at three heights. The roughness length is calculated as the exponential of the intercept, with the natural logarithm of wind measurement heights plotted against wind speeds. The Monin-Obukhov length is calculated (Eq. 1) from the density of air (ρ , kg m^{-3}), the specific heat capacity of air at constant pressure (c_p , $\text{J kg}^{-1} \text{K}^{-1}$), the absolute temperature of air at $z = 0$ (T_0 , K), the acceleration due to gravity (g , m s^{-2}), and the sensible heat flux (H , W m^{-2}). The sensible heat flux (H , W m^{-2}) is calculated (Eq. 2) from the transfer coefficient for heat flux (CH , 1×10^{-3}) (Pan et al., 2003).

$$L = -\frac{\rho c_p T_0 u^3}{K g H} \quad (1)$$

$$H = \rho c_p CH (T_a - T_0) u \quad (2)$$

2.2.3 Model used – WindTrax Inverse Dispersion Model

The inversion function of the WindTrax atmospheric dispersion model version 2.0 (Flesch et al., 1995) is used to infer the CH_4 emissions from the landfill. Methane emissions are calculated using measured CH_4 mixing ratios downwind,

measured background CH₄ mixing ratios upwind and the simulated ratio of CH₄ mixing ratio enhancement to emission (Flesch et al., 2004; 2005). WindTrax calculates the ratio of CH₄ mixing ratio to emission by back-calculating the movement of many CH₄ particles from the detector to the landfill emission area and estimating the vertical velocity as they leave the emission area. Following the method of Laubach et al. (2008) and Flesch et al. (2009), CH₄ mixing ratios and meteorological data were averaged over 15 minutes to preserve real changes to CH₄ emission caused by changing environmental or atmospheric factors. Each 15-minute-averaged measurement is used as an input to back-calculate the CH₄ emission using 50,000 particle trajectories.

2.3 Middle-Distance

2.3.1 Measurements – GC-FID

Methane mixing ratios were measured every 75 seconds from July 2012 to July 2015 at the Holy Trinity church, Haddenham (52.359° N, 0.148° E) since July 2012 (see Fig. 1) using a 200 series Ellutia GC-FID (www.ellutia.com). The site elevation is 40 metres above sea level and the inlet is on the tower, 25 m above the ground. The GC-FID takes air to be assayed for CH₄ mixing ratio mixed with a carrier gas which passes through a column of alumina coated tubing heated in an oven at 90°C. As the gases exit the column they are pyrolyzed by a hydrogen/air mixture within the flame ionization detector. Ions formed during the combustion are measured to indicate the mixing ratio of the gas species. The Ellutia GC-FID, as used here, has a detection limit of approximately 1.5 ppb, a range of 1.5 to 3 ppm and measures mixing ratios every 75 s. The instrument is calibrated every 30 minutes using a gas standard. The Teflon inlet line is attached to the church roof 30 m above the ground and is protected from water incursion using an aluminium funnel and a 2 µm particle filter.

The data are transmitted back to the laboratory for processing. Data processing of individual chromatograms is done using IGOR Pro (Wavemetrics, USA) to determine peak height. Measurements from all sites are calibrated to the WMO (World Meteorological Office) calibration scale (Dlugokencky et al., 2005). Hourly WMO calibrated mixing ratios are then calculated using Openair in R.

2.3.2 Meteorological Data

Data were taken from UK Met Office's Numerical Atmospheric Modelling Environment (NAME) model, as described later in Sect. 2.4.2.

2.3.3 Model used – Gaussian Plume

The Gaussian Plume (GP) model describes the mixing ratio of a gas as a function of distance downwind from a point source (Seinfeld and Pandis, 2006). *The particle trajectories were calculated in the NAME model and could have been used to calculate emissions, however given the short distance from the landfill to the monitoring station and the availability of observed meteorology it was decided that a Gaussian Plume model would be better suited for our purposes.* As a gas is emitted, it is entrained in the prevailing ambient air flow and disperses in the y and z directions (relative to a mean horizontal flow in the x direction) with time, forming a cone. The gas is considered to be well mixed within the volume of the cone, such that the mixing ratio of the gas as a function of distance downwind depends

on the emission flux at source, the advective wind speed (u , m s^{-1}), and the rate of dispersion (governed by boundary layer micrometeorological factors described in Sect. 2.2). The mixing ratio of the gas (X , $\mu\text{g m}^{-3}$), at any point x metres downwind of the source, y metres laterally from the centre line of the plume, and z metres above ground level can be calculated (Eq. 3) using the source strength (Q , g s^{-1}), the height of the source (h_s , m) and the air stability. The standard deviation of the lateral (σ_y , m) and vertical (σ_z , m) mixing ratio distribution are calculated from the stability class of the air, **the values used in our analyses are presented in Supplementary Material Section 1 (Pasquill, 1974)**. The Gaussian plume approach assumes that the vertical eddy diffusivity and wind speed are constant and there is total reflection of methane at the surface (e.g. Zannetti, 1990; Hensen and Scharff, 2001; Hensen et al., 2009).

$$\text{Concentration}(x, y, z) = \frac{Q}{2\pi u \sigma_y \sigma_z} e^{-\frac{y^2}{(2\sigma_y)^2}} \left(e^{-\frac{(z-h_s)^2}{(2\sigma_z)^2}} + e^{-\frac{(z+h_s)^2}{(2\sigma_z)^2}} \right) \quad (3)$$

2.4 Landscape

2.4.1 Measurements – East Anglia Network

Methane mixing ratios were measured by a network of four sites throughout East Anglia: Tilney-All-Saints Church, Haddenham Church, Weybourne and Tacolneston (Fig. 1). Ellutia GC-FIDs, as described in Sect 2.3.1, were used at Tilney-All-Saints Church, Haddenham Church and Weybourne. Measurement at Haddenham church is described in Sect. 2.3.1, similar systems were arranged at Tilney-All-Saints and Weybourne where inlet were positioned at 25 and 15 m from the ground, respectively. A Picarro CRDS measured the CH_4 mixing ratios in air at Tacolneston at 50 m and 100 m from the ground. Calibration of the Picarro CRDS was done daily for 10 minutes using low (1.93 ppm), target (2.03 ppm) and high (2.74 ppm) CH_4 gases calibrated on the World Meteorological Organization (WMO) scale.

2.4.2 Model used - InTEM Inversion Modelling

The dispersion model used to represent air flow from potential methane sources to the measurement site is the UK Met Office's Numerical Atmospheric Modelling Environment (NAME) model (Jones et al., 2007). This is a Lagrangian dispersion model which runs using 3D meteorological fields produced by the UK Met Office's numerical weather prediction model, the Unified Model (UM) (Cullen, 1993). These meteorological fields are available on two resolutions: global (three hourly, 25 km) and UK (hourly, 1.5 km). NAME was run using a combination of both resolutions with the 1.5 km UK fields nested within the global data.

NAME produces a modelled representation of the contributing surface influence (defined as the 100 m above ground level in NAME) to a particular source location over a defined period of time. This is done by releasing chemically-inert particles ($10,000 \text{ hr}^{-1}$) from the x , y , z coordinate of a measurement site location. Their movements and geolocation are tracked backwards in time every minute for five days. NAME produces a time-integrated particle density map for each source (units g s m^{-3}), which shows, on a gridded output, what relative contribution each grid square has had over the five day period (Manning et al., 2011). The resolution of this air history map is equal to $1.5 \times 1.5 \text{ km}$.

Emissions are inferred in InTEM by using an iterative best fit technique, simulated annealing, which compares the hourly-measured observations with derived modelled observations, based on the NAME InTEM method described in

Manning (2003) and Manning et al. (2011). These modelled, or ‘pseudo’, observations are created by multiplying a simulated emissions field ($\text{g s}^{-1} \text{m}^{-3}$) with a representation of the physical atmospheric processes for each measurement (Eq. 4).

$$\text{emissions } (\text{g s}^{-1} \text{m}^{-2}) \times \text{dilution } (\text{s m}^{-1}) = \text{concentration } (\text{g m}^{-3}) \quad (4)$$

The dilution matrix (units s m^{-1}), which links the simulated emission field (g s m^{-3}) with the observations (g m^{-2}) is produced from the hourly NAME air history maps by dividing by the mass released (g) and then multiplying by a surface area matrix (m^2). This dilution matrix is multiplied by the InTEM generated emissions field (both are gridded to the solution grid resolution).

The two observation time series are quantitatively assessed using a ‘least squares’ cost function, shown in Eq. 5. For each time step, the difference between the measured (y_i) and the pseudo observations ($(kx)_i$) is weighted by the total uncertainty ($(\sigma_\epsilon^2)_i$), where the uncertainty is defined as the total error estimated in measurement observations, modelling and baselines (Connors et al., in prep). This allows for any potential bias due to highly uncertain observations to be accounted for. High CH_4 concentration values seen at Haddenham are usually short lived and only appear as peaks lasting a maximum of only a few hours. These usually occur at night time and, as the isotopic analysis shows, probably come from a landfill, which is an intermittent of CH_4 . These are therefore more uncertain. The values would have a relatively high cost score at these times. So, including an hourly standard deviation into the uncertainty calculation helps to de-weight the large concentrations, which have higher uncertainty, from increasing the overall cost score.

InTEM then iterates for thousands of potential emission fields through the simulated annealing technique to find an optimum result with the lowest cost score (Eq. 5). Uncertainty correlation was not considered in the modelling, errors are considered independent of each other. This is a weaknesses and further analysis is needed using other cost functions (e.g. the Bayesian cost function).

$$J(X) = \sum_{i=1}^m \frac{(y_i - (kx)_i)^2}{(\sigma_\epsilon)_i^2} \quad (5)$$

3. Model runs

3.1 Instantaneous methane emissions – Summer 2015 case study

3.1.1 Near-source - Inverse dispersion modelling

The inversion function of the WindTrax atmospheric dispersion model version 2.0 (Flesch et al., 1995) is used to infer the CH_4 emissions from the Waterbeach landfill using the mixing ratio data collected at Mitchell Hill Farm on the 30th June 2015 and 1st July 2015. Data used as input to WindTrax are: wind speed (u , m s^{-1}), wind direction (WD , $^\circ$), temperature (T , $^\circ\text{C}$), CH_4 mixing ratio at 4 m (X , $\mu\text{g m}^{-3}$), background CH_4 mixing ratio (X_b , $\mu\text{g m}^{-3}$), the Monin-Obukhov Length and the surface roughness. 15-minute-averaged CH_4 mixing ratio data are screened for erroneous values, and data are removed for any periods where wind did not come from the landfill or for high atmospheric stability events, i.e. wind speed, $u < 0.15 \text{ ms}^{-1}$.

An uncertainty analysis is conducted, where potential variant input values are used in re-run WindTrax scenarios to calculate the resultant change in calculated CH₄ emission. These uncertainties are then combined as the square root of the sum of the squares of the individual uncertainties to give an overall uncertainty in emission estimate. The main sources of error are the size of the emission area, as it changed daily, wind speed, the roughness length, and Monin-Obukhov length. The values used to estimate the uncertainty are from published data.

3.1.2 Emissions from middle-distance – Gaussian Plume model

A Gaussian Plume (GP) approach, was used to infer the CH₄ emissions from the Waterbeach landfill using the mixing ratio data collected at Haddenham Church on the 30th June 2015 and 1st July 2015. Data used as input to the GP model are: wind speed, wind direction, temperature, CH₄ mixing ratio at 4 m, background CH₄ mixing ratio and the Pasquill-Gifford atmospheric stability class. The Pasquill-Gifford stability classes are estimated from calculated values of the Monin-Obukhov length as measured at Mitchell Hill Farm. As with the inverse dispersion modelling approach, 15-minute-averaged data are used and screened for erroneous values, any periods where the prevailing wind did not come from the direction of the landfill or for high atmospheric stability events.

The main uncertainty using the GP approach is in estimating the Pasquill-Gifford atmospheric stability class. The Monin-Obukhov length is used to assign this value and an uncertainty of $\pm 7\%$ was used here because L is calculated using two anemometers each with 5 % uncertainty. Other sources of uncertainty were in the instruments used to measure CH₄ mixing ratio and temperature, with uncertainty ranges discussed in Sect. 2. In addition to these sources, a potentially important, yet unquantifiable uncertainty could be off-site sources of emission; unlike the inverse dispersion approach, the GP used in the configuration assumes the landfill is the only point source emitter situated 6 km to the south east of the measurement location and does not take into account other nearby sources, such as emissions from the on-site generator or other sources upwind. However, any significant difference between the emission estimates calculated using the inversion and the GP approaches may usefully serve to indicate the size of emission from the rest of the Waterbeach Waste Management Park and beyond

3.2 Annual and seasonal emission estimates

3.2.1 Middle-distance – Gaussian Plume model

The GP approach is described above. Data used as input to GP model are: wind speed, wind direction, temperature, CH₄ mixing ratio, background CH₄ mixing ratio and the Pasquill atmospheric stability class. Hourly data are used and screened for erroneous values, any periods where wind did not come from the landfill or for high atmospheric stability events.

As with the case study in 3.1.1, the main source of error used as input for the GP approach is the size of the uncertainty in estimating the Pasquill-Gifford atmospheric stability class. The study also includes the instrument precision and wind speed and temperature uncertainties as derived from the NAME model. Also, we assume the landfill is the only point source emitter 6 km to the south east and does not take into account other nearby sources, such as emissions from the on-site generator and further upwind.

3.2.2 Landscape - InTEM Inversion Model

The results presented here are taken from a study developing a method to estimate regional CH₄ emissions in East Anglia (Connors et al., in prep.). More details on the measurements sites, the inversion set-up used for InTEM, the diagnostics used and the emission uncertainties can be found there and in Connors (2015). The main points for the purposes of this paper are summarised below and in the Supplementary Material Section 2.

InTEM was run using data from all four measurement sites (Fig. 1) between 1st June 2013 and 31st May 2014. Repeating the inversion method gives slightly different cost scores and emission totals due to the stochastic nature of the changes made during the simulated annealing process (Manning et al., 2011). For this study, InTEM was repeated 25 times as this resulting in consistent methane emission estimates, standard deviations and cost score.

Methane emissions are produced on a solution grid of varying spatial resolution. This resolution is determined using the NAME air history maps and the National Atmospheric Emissions Inventory (NAEI) for methane. Surface regions which have a larger influence on the observation sites and have a large emission in the NAEI produce boxes at a higher spatial resolution. The smallest resolution allowed for the emission grid is set equal to the NAME grid resolution (1.5 x 1.5 km). The box which contains the Cottenham landfill site is roughly 9 x 4.5 km.

An estimated methane baseline mixing ratio is calculated to represent the methane mixing ratio that would have been measured at a given site in the absence of emissions from within the dispersion domain. A statistical filtering technique separated methane mixing ratios at each site into **eight timeseries** using the NAME air history maps by wind direction. A rolling 18th percentile spanning one week is then passed through each time series. Sensitivity analysis shows this baseline produces emission results with consistently stable emissions with the lowest cost score of all baselines tested. **This percentile was chosen as a result of a sensitivity analysis which showed that InTEM inversion results using the 18th percentile produced the lowest cost scores, i.e. the calculated emissions are closer to the measured observations compared to any of the other percentiles tested (percentiles from the 5th to the 45th were tested).**

The uncertainty estimates used within InTEM reflect the variability of the resulting emission estimates. Uncertainty is defined as the total of the calibration gas uncertainty range, the GC instrument precision and the standard deviation within the hourly observation, plus a default mixing ratio of 5 ppb to represent uncertainty with the baseline and dispersion modelling. For a more detailed description of the measurement sites and the InTEM setup please refer to Connors et al. (in prep).

4. Results

4.1 Isotopic methane measurements

Several large CH₄ plumes were measured by the GC-FID in Haddenham Church on the 11th February 2015 (Fig. 2) during a wind event from the south east ranging from background, c. 1900 ppb, to a maximum mixing ratio of 2460 ppb. Air samples collected in Tedlar bags at the same time at the same location and analysed later for CH₄ mixing ratio using a Picarro CRDS at RHUL show good agreement in measurement between the GC-FID and Picarro CRDS. The $\delta^{13}\text{C}$ isotopic signature of the source contributing to excess methane over background can be calculated using the Keeling plot approach (e.g. Zazzeri et al., 2015). This is a plot of $1/\text{CH}_4$ (ppm) vs measured isotopic signature for

each sample. The intercept of the correlation line fit where $1/\text{CH}_4 = 0$ closely approximates the source signature. The Keeling plot of the air samples taken at Haddenham Church between 0600 and 1400 hours on 11th February 2015 estimates the $\delta^{13}\text{C}$ isotopic signature at -58.3 ‰ (Fig. 3). The typical $\delta^{13}\text{C}$ isotopic signature value for a landfill in the south east of the UK has been estimated to be $-58 \pm 3 \text{ ‰}$ (Zazzeri et al., 2015), which is very different from other possible local source signatures such as fossil fuels or combustion. This strongly suggests that the air measured at the church has come from a landfill. Air samples were taken closer to the landfill, 10 m from the active site.

4.2 Estimating methane emissions – Case study June 2015

The average CH_4 emission for the Waterbeach landfill in July based on near source CH_4 measurements used in WindTrax is estimated at $565 \mu\text{g m}^{-2} \text{ s}^{-1}$ (453 kg hr^{-1}). In general, emissions on the 30th June (average = $256 \mu\text{g m}^{-2} \text{ s}^{-1}$) are ten times lower than those on the 1st July (average = $2840 \mu\text{g m}^{-2} \text{ s}^{-1}$), corresponding to less stable conditions and lower atmospheric pressure on the 1st (Fig. 4). The maximum emission is estimated at $18700 \mu\text{g m}^{-2} \text{ s}^{-1}$ at 1215 UTC on the 1st July.

A range of scenarios were run in WindTrax to investigate the uncertainty in CH_4 emissions caused by the CH_4 measurement, the wind speed measurement, estimating the roughness length and estimating the Monin-Obukhov length. Realistic uncertainty in the Monin-Obukhov length and instrument uncertainty for the CH_4 measurement have little effect on the emission estimate. Uncertainty in estimating the emission area and roughness length have a noticeable effect on CH_4 emission, resulting in an uncertainty of $\pm 3 \text{ ‰}$ and $\pm 4 \text{ ‰}$ on modelled CH_4 emissions, respectively. WindTrax has the greatest response to the uncertainty in estimating wind speed, resulting in an emission uncertainty of $\pm 19 \text{ ‰}$. The overall uncertainty in CH_4 emission, calculated as the root of the sum of each component squared, is estimated at $\pm 20 \text{ ‰}$ (Table 2).

The methane emissions calculated using the WindTrax model can be compared with those calculated by a Gaussian plume model using the same measurements. As with WindTrax, the emissions on the 30th June (average = $408 \mu\text{g m}^{-2} \text{ s}^{-1}$) are lower than those on the 1st July (average = $1270 \mu\text{g m}^{-2} \text{ s}^{-1}$). However, the difference in emissions is not as large (Fig. 5). The maximum emission is estimated at $2590 \mu\text{g m}^{-2} \text{ s}^{-1}$ at 1215 UTC on the 1st July, which suggests that the Gaussian plume approach measures a more mixed emission than the inversion dispersion model.

A range of scenarios were also configured using the Gaussian plume approach to reflect uncertainty in CH_4 measurement, wind speed measurement, temperature measurement and the Monin-Obukhov length (Table 3). Changing the Monin-Obukhov length had no detectable effect on the emission estimate because the change in L is not enough to vary the assigned Pasquill-Gifford Stability class used in the emission calculation. Varying the temperature and wind speed had little effect on CH_4 emission and resulted in an uncertainty of $\pm 1 \text{ ‰}$ and $\pm 5 \text{ ‰}$ on modelled CH_4 emissions, respectively. The uncertainty in estimating CH_4 emissions caused by the instrument precision is the greatest source of uncertainty and results in an uncertainty of the emission estimate of $\pm 22 \text{ ‰}$. The overall uncertainty in CH_4 emission, calculated as the root of sum of each component squared, is estimated to be $\pm 23 \text{ ‰}$.

4.3 Annual and seasonal emission estimates

Methane emissions from the landfill at the Waterbeach Waste Management Park were calculated using 1171 hourly averaged CH₄ mixing ratio data measured at Haddenham Church between July 2012 and June 2015. The GP model can only be used to calculate the emission when the wind is blowing from the SE (i.e. from the landfill). For this particular time series, the wind was only from the SE for 1171 hours. Meteorological data from the Unified Model analyses are used to calculate the Pasquill-Gifford stability class. When applied in the Gaussian Plume model, the monthly average CH₄ emission for July is estimated at 616 kg hr⁻¹, in reasonable agreement with the estimates of 453 and 641 kg hr⁻¹ of the WindTrax inverse dispersion and Gaussian Plume models using measured meteorological data. Emissions for all months are shown in Table 4.

In general, CH₄ emission rates are higher during the winter months and lower during the summer months (Fig. 6). During the winter months (December, January, February) CH₄ emission from the landfill is estimated at 1860 kg hr⁻¹ (441 μg m⁻² s⁻¹), whereas in the summer months (June, July, August) the CH₄ emission drops to more than half to 930 kg hr⁻¹ (207 μg m⁻² s⁻¹). Variability in emissions is also larger in winter than in summer. The mean annual emission, calculated as the sum of the monthly mean emissions, is estimated at 11.6 Gg yr⁻¹.

As before scenarios were ran using the GP approach to reflect variability in instrument precision, wind speed, temperature and the Pasquill-Gifford stability class (Table 5). Changing the temperature had no effect on the emission estimate, and instrument precision was a larger source of uncertainty, ± 9 %. However, the effect of instrument precision was smaller than the uncertainty in the case study possibly because the measured mixing ratios are at their lowest during the summer. The calculation of the PGSC and the uncertainty in wind speed were the highest source of uncertainty resulting in variability in CH₄ emission of ± 24 % and ± 20 %, respectively. The overall uncertainty in CH₄ emission is estimated to be ± 32 %.

4.3.2 InTEM Inversion Model Methane Emission Estimates

The average annual CH₄ emission from the landfill calculated using ~24,000 hourly averaged CH₄ mixing ratio data measured by the East Anglia network (Fig. 1) and NAME modelled met data in the InTEM model is estimated at 13.7 Gg yr⁻¹ (Table 4). The emission estimate was calculated from the average CH₄ emission 19.9 μg m⁻² s⁻¹ calculated for an area of 2.17x10⁷ m². The standard deviation of the CH₄ emission for 25 repeat runs of the InTEM model is 1.8 x 10⁻⁵ g s⁻¹ m⁻² (91 %).

5. Discussion and Conclusions

The data presented in this paper gives the first comparison of methane emissions from a working landfill calculated using three models at different scales: (a) near-source < 1 km (WindTrax); mid-distance 1-7 km (Gaussian Plume); and far field 7 – 70 km (InTEM). Near-source measurements were taken 300 m to the north west of the Waterbeach Waste Management Park, Cambridgeshire on the 30th June and 1st of July 2015. Mid-distance measurements were taken from Haddenham Church, 7 km north west of the landfill, between July 2012 and July 2015. Far-field

measurements were taken throughout East Anglia, ranging from 7 km to 100 km from the landfill, between July 2012 and July 2015.

After using $^{13}\text{CH}_4$ signatures to confirm that the source of the large CH_4 mixing ratios is a nearby landfill, average CH_4 emissions estimated using near-source measurements are 453 kg hr^{-1} on 30th June and 1st July 2015 and agree within associated uncertainties when compared to the mid-distance emission estimates of 641 kg hr^{-1} . From the limited observation period, we also observe greater variability in emissions using the near-source method, in accord with the finding of Riddick et al (2016) that suggest that near-source estimates can be affected by the heterogeneous nature of the landfill. We suggest that the agreement in emissions estimates between the near-source and middle-distance methods indicate that a Gaussian plume approach can be used to estimate emissions up to 7 km from a relatively large source. However, this may be an upper estimate of the distance that this approach is effective as the fetch between the source and detector was relatively flat and a more aerodynamically complex landscape may reduce the model's efficacy.

Using mid-distance measurement throughout the year we estimate the annual CH_4 emissions from the site to be 11.6 Gg yr^{-1} which is comparable to the CH_4 emission estimate as calculated using the InTEM inversion method of 13.7 Gg yr^{-1} . Our results suggest that larger emission hot-spots can be detected within the emission landscape generated by an inversion model. However, we would suggest that future sensitivity studies should be conducted to estimate the size of emission hot-spots within a landscape where the source is farther from a measurement site used as input to the inversion model.

The CH_4 emissions from this landfill site are seasonal with the largest emissions during the winter months (February 2160 kg hr^{-1}) and the lowest emissions during the summer months (616 kg hr^{-1}). This may be linked to the seasonal cycle in environmental conditions as there is an inverse relationship between CH_4 emission and temperature. The temperature relationship may be explained by the increased activity of methanotrophic bacteria in the top layers of landfill as the temperature increases.

The CH_4 emissions from this landfill site are seasonal with the largest emissions during the winter, colder months (February: 2160 kg hr^{-1}) and the lowest emissions during the summer, warmer months (616 kg hr^{-1}). This is explained by the following mechanism (Börjesson and Svensson, 1997). The temperature within the landfill is relatively stable so that the sub-surface production of CH_4 is roughly constant. In summer when the surface temperature is higher, the activity of methanotrophic bacteria in the top layers of landfill is enhanced, so that the net emission into the atmosphere is reduced. Our measurements are the first off-site measurements to demonstrate this and so are not susceptible to the sampling uncertainties associated with chamber techniques.

The CH_4 emission estimate made by this study of 11.6 Gg yr^{-1} from this site is an important contribution to the waste component (714 Gg yr^{-1}) of the 2014 total UK CH_4 emission inventory ($2,157 \text{ Gg yr}^{-1}$; NAEI, 2016). We estimate the 11.6 Gg yr^{-1} emitted is produced from the 400 Gg of total waste processed each year at the site (AMEY, 2016). The inferred CH_4 emission to waste ratio at this site is lower (0.029) than the current UK ratio (0.045), where $1.0 \text{ Tg CH}_4 \text{ yr}^{-1}$ (EC-JRC/PBL, 2010) is emitted from 22 Tg of solid waste disposed in landfill (UK Gov, 2016). This may be the result of differing environmental and management factors, such as differing mass fractions for each decomposing waste category (Jung et al., 2010), movement of landfill leachate (Attenborough et al., 2002) and site specific weather

conditions (Maurice & Lagerkvist, 2004; Scheutz et al., 2004; Xu et al., 2014). Alternatively, CH₄ emissions from new landfills which include a high component of recycling are currently overestimated.

Even though the annual emission estimate calculated using the InTEM inversion model is close to that calculated by the Gaussian Plume model, the uncertainty associated with the InTEM inversion estimate is large. Comparison of the measurements with the CH₄ time series produced by NAME InTEM (Supplementary Figures 1 and 2) shows the model to consistently underestimate the larger and sharper observed peaks. This arises as a result of the smaller weighting given to the peaks in the observed atmospheric concentrations in the NAME InTEM analysis (which uses all data) than in the WindTrax and Gaussian plume analyses which focus on these peaks. In particular, high peaks are underweighted because they are small scale features not easily delineated in the regional inversions and the boundary layer is harder to model accurately at night when the highest peaks tend to occur due to their containment within the shallow nocturnal boundary layer. The heteroscedasticity seen in Supplementary Figure 2 is therefore to be expected as NAME InTEM reproduces the lower values better than the high ones.

The inherent challenges in inversion modelling, such as assuming a constant monthly emission (Supplementary Material Section 2 Figure SM2.3) and the atmospheric variability at night which is poorly resolved by the model, result in the emission estimates calculated in this research having an uncertainty of $\pm 91\%$. This research is presented as an example of inversion modelling: a work in progress and, while the emission estimates are currently uncertain, the location of the emissions are well represented.

The output from NAME InTEM inversion model shows that reasonably dense measurement networks can be used to identify emission hotspots within an emission landscape. Once potential hotspot emission sources have been identified, year-round measurements coupled to a relatively simple Gaussian plume model could be used to estimate the annual average and any seasonality in the CH₄ emissions. As lower cost sensors become available, a cost-effective system to monitor point source emissions should become available.

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Figure 1. Location of the East Anglia Measurement Network (Tilney-All-Saints Church, Haddenham Church, Weybourne & Tacolneston), landfill at the Waterbeach Waste Management Park and the measurement site at Mitchells Hill farm, Cambridgeshire. The map was taken on 23rd July 2015 (Google Earth, 2015).

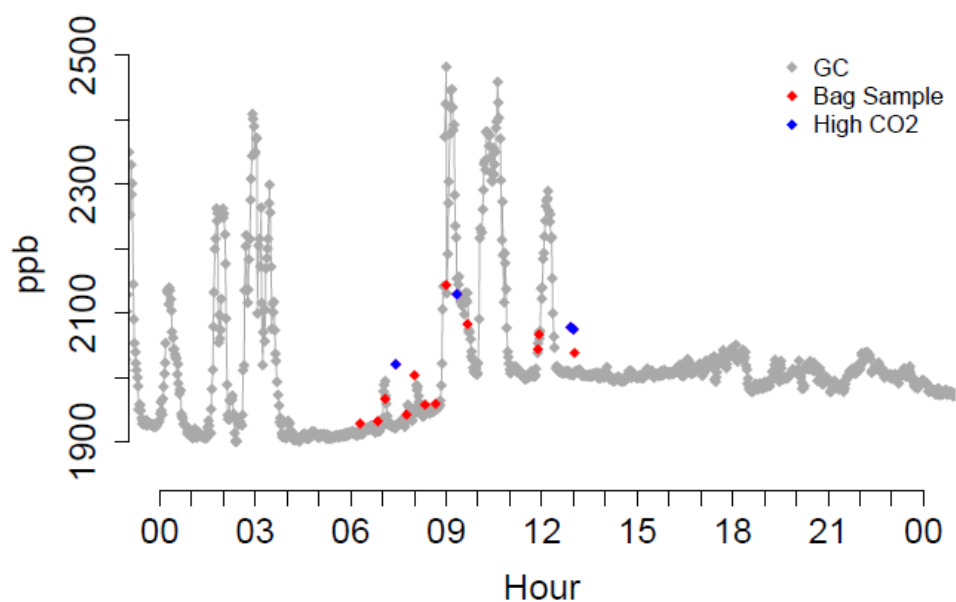


Figure 2 Methane mixing ratios measured by the GC-FID in Haddenham Church on 11th February 2015 are presented in grey. Matching methane mixing ratios collected in Tedlar bags on the 11th February 2015 and analysed on the 20th February 2015 using a Picarro CRDS at Royal Holloway University of London are presented as red points.

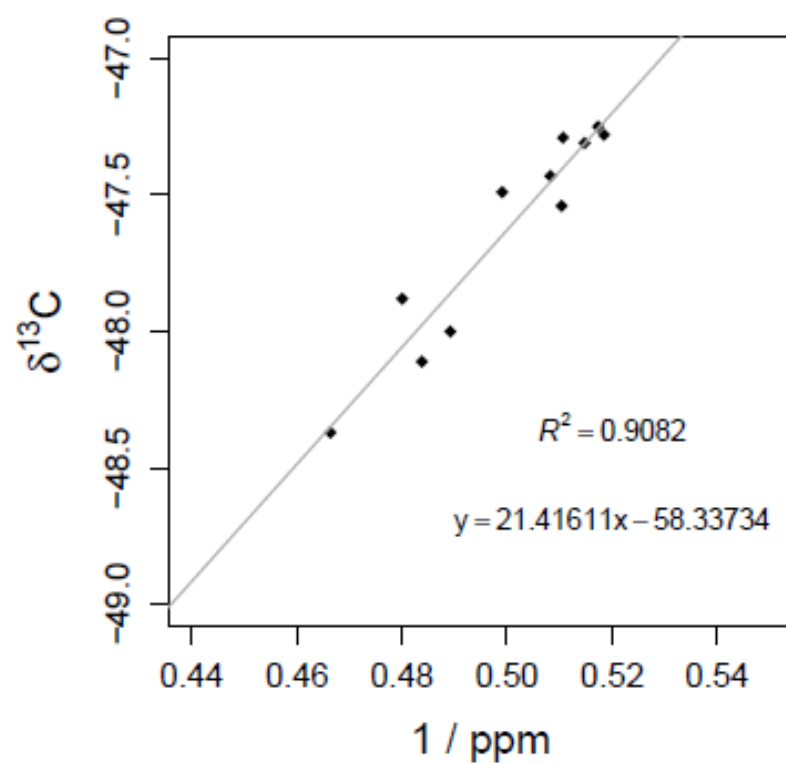


Figure 3 Keeling plot of the air samples taken at Haddenham Church between 0600 and 1400 hours on 11th February 2015.

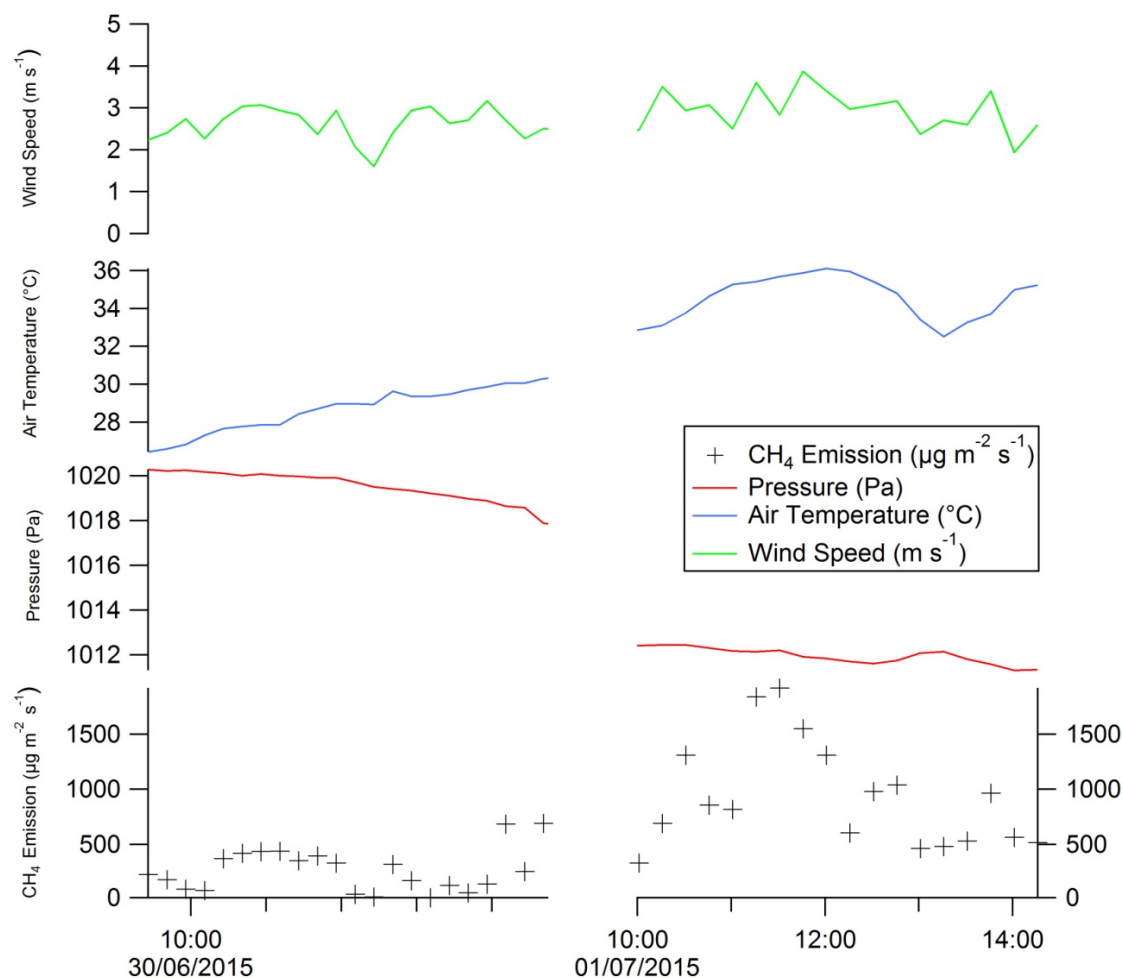


Figure 4 Measured wind Speed (top), measured temperature (middle-top), measured pressure (middle-bottom) and methane emission rate as calculated by the WindTrax atmospheric dispersion model (bottom) from data collected at Mitchell Hill Farm, Cottenham from the landfill at the Waterbeach Waste Management Park on the 30th June and 1st July 2015.

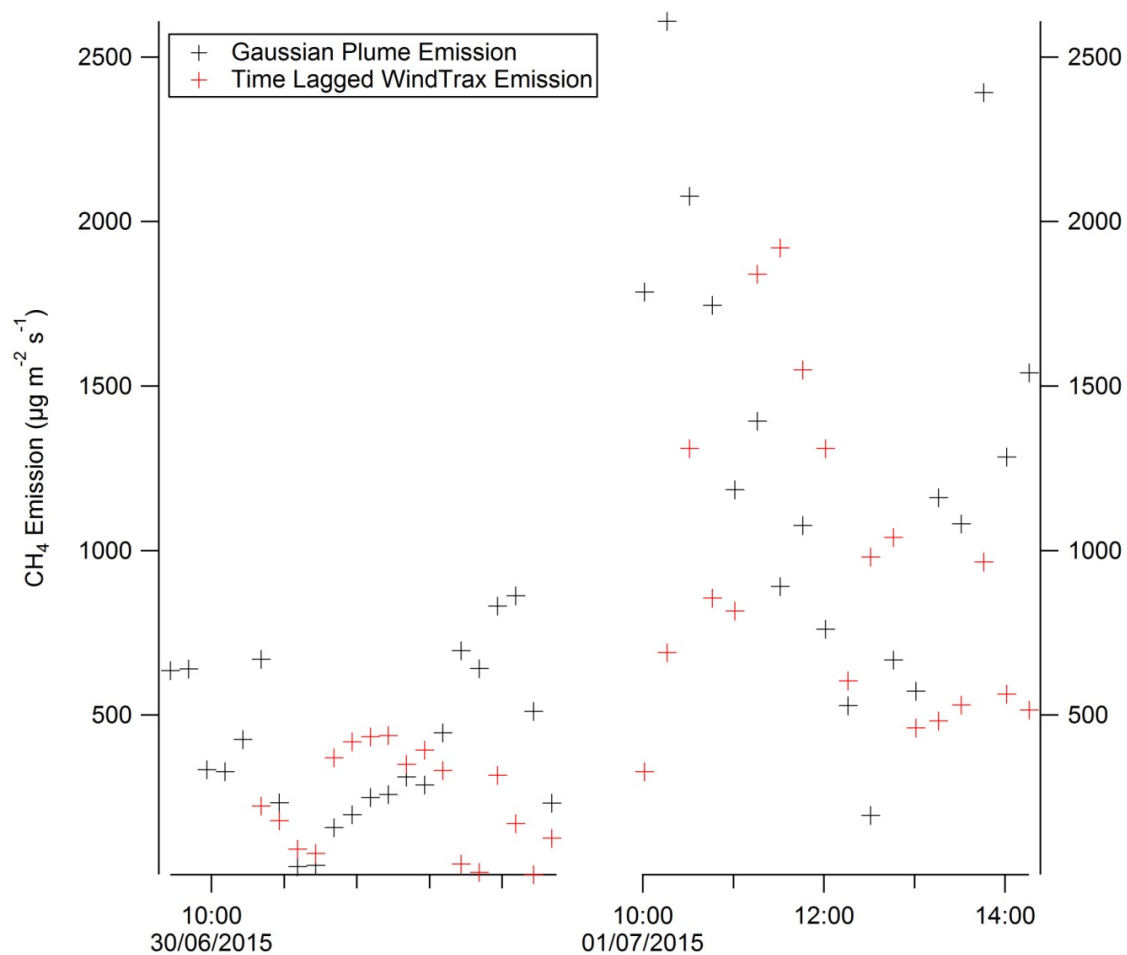


Figure 5 Methane emission rate as calculated by the Gaussian Plume modelling approach (black crosses) and the WindTrax atmospheric dispersion model (red crosses) from data collected at Mitchell Hill Farm, Cottenham from the landfill at the Waterbeach Waste Management Park on the 30th June and 1st July 2015.

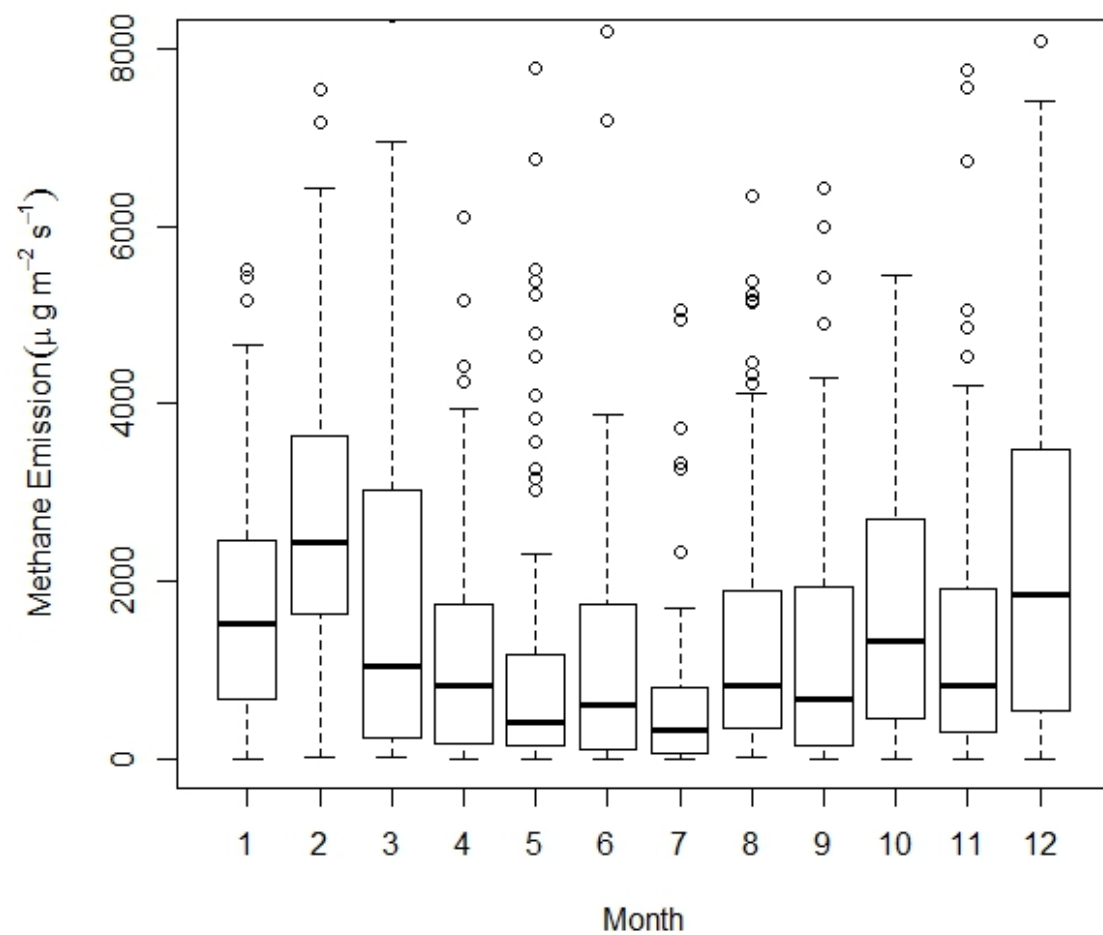


Figure 7 Box plot of hourly emissions calculated using the Gaussian Plume modelling approach showing the monthly variability in methane emissions using data from 2012 to 2014.

Table 1 Summary of methods used to calculate methane emission estimates from a landfill at different scales: near-source, middle-distance and landscape.

Scale	Measurement location (Fig. 1)	Measurement method	Meteorological data	Model used to calculate emission
Near-source	Mitchel's Farm, Cottenham, Cambridgeshire	Los Gatos UGGA (Sect. 2.2.1)	In-situ at Mitchells' Farm (Sect. 2.2.2)	WindTrax Inverse Dispersion Model (Sect. 2.2.3)
Middle-distance	Haddenham Church, Cambridgeshire	Ellutia 200 Series GC-FID (Sect. 2.3.1)	NAME Model Runs (Sect. 2.4.2)	Gaussian Plume (Sect. 2.3.3)
Landscape	East Anglia measurement Network	Ellutia 200 Series GC-FID (Sect. 2.3.1) Picarros CRDS (Sect. 2.4.1)	NAME Model Runs (Sect. 2.4.2)	InTEM Model (Sect. 2.4.2)

Table 2 Uncertainty analysis conducted on the case study (June 2015) methane emission from the landfill at the Waterbeach Waste Management Park as calculated within the WindTrax atmospheric dispersion model.

Variable	Value used	Average Emission ($\mu\text{g m}^{-2} \text{ s}^{-1}$)	Uncertainty (%)
Baseline		565	
Monin-Obukhov Length	$\pm 7\%$	563	± 0.3
Precision Roughness Length	$\pm 7\%$	588	± 4
CH ₄ Instrument	$\pm 0.01\%$	567	± 0.3
Wind Speed Measurement	$\pm 5\%$	671	± 19
Emission area	$\pm 20\%$	547	± 3
		Total	± 20

Table 3 Uncertainty analysis conducted on the case study (June 2015) methane emission from the landfill at the Waterbeach Waste Management Park as calculated within the Gaussian Plume modelling approach.

Variable	Value used	Average Emission ($\mu\text{g m}^{-2} \text{s}^{-1}$)	Average Emission (kg hr^{-1})	Uncertainty (%)
Baseline		800	641	
CH ₄ Instrument Precision	± 0.5%	973	781	22
Wind Speed Measurement	± 5%	840	674	5
Monin-Obukhov Length	± 7%	800	641	0
Temperature Measurement	± 5%	795	638	0.4
			Total	23

Table 4 Methane emission estimates from the landfill at the Waterbeach Waste Management Park as calculated by the WindTrax and Gaussian Plume approaches for the case study (June 2015) and the annual estimates for the Gaussian Plume and InTEM inversion modelling approach for 2012 – 2104.

Month	Case Study		Annual Estimate	
	Inverse dispersion (kg hr ⁻¹)	Gaussian Plume (kg hr ⁻¹)	Gaussian Plume (kg hr ⁻¹)	InTEM
January			1370	
February			2160	
March			1580	
April			1110	
May			830	
June			1070	
July	453 ± 20%	641 ± 23%	616	
August			1100	
September			1480	
October			1350	
November			1210	
December			2040	
Total Emission (Gg yr ⁻¹)			11.6 ± 32%	13.7 ± 91%

Table 5 Uncertainty analysis conducted on the annual methane emission from the landfill at the Waterbeach Waste Management Park as calculated within the Gaussian Plume modelling approach

Variable	Value used	Average Emission ($\mu\text{g m}^{-2} \text{s}^{-1}$)	Average Emission (kg hr^{-1})	Uncertainty (%)
Baseline		1650	1320	
CH ₄ Instrument Precision	± 0.5%	1790	1440	9
Wind Speed Measurement	± 20%	1980	1590	20
PGSC	± 1 SC	1490	1200	24
Temperature Measurement	± 20%	1640	1320	1
			Total	32