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Impact of vertical wind shear on roll structure in idealized hurricane boundary layers

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Abstract. Quasi two-dimensional roll vortices are frequently observed in hurricane boundary layers. It is believed that this highly coherent structure, likely caused by the inflection point instability, plays an important role in organizing turbulent transport. Large-eddy simulations are conducted to investigate the impact of wind shear characteristics such as the shear strength and inflection-point level on the roll structure in terms of its spectral characteristics and turbulence organization. A mean wind profile nudging approach is used in the simulations to maintain the specified mean wind shear without directly affecting turbulent motions. Enhancing the radial wind shear expands the roll horizontal scale and strengthens the roll's kinetic energy. Increasing the inflection-point level tends to produce a narrow and sharp peak in the power spectrum at the wavelength consistent with the roll spacing indicated by the instantaneous turbulent fields. The spectral tangential momentum flux, in particular, reaches a strong peak value at the roll wavelength. In contrast, the spectral radial momentum flux obtains its maximum at the wavelength that is usually shorter than the roll's, suggesting that the roll radial momentum transport is less efficient than the tangential. The most robust rolls are produced in a simulation with the highest inflection-point level and relatively strong radial wind shear. Based on the spectral analysis, the roll-scale contribution to the turbulent momentum flux can reach 40% in the middle of the boundary layer.

1 Introduction

The hurricane boundary layer (HBL) is well known for its critical role in evolutions of tropical cyclones (TCs) as the air-sea interaction represents both the most important source and sink of the moist available energy and the kinetic energy, respectively. One of the frequently occurring features in the HBL is horizontal roll vortices, which have quasi-two dimensional coherent and banded structure extending from the surface to the top of the HBL. The observed horizontal roll scale, i.e., the average distance between two neighbouring rolls, ranges from sub-kilometre to ~10 km (Wurman and Winslow 1998; Lorsolo et al. 2008; Foster 2013). Observational and modelling studies suggest that these roll vortices make significant contribution to the vertical heat and momentum transport (Zhang et al. 2008; Zhu 2008) and thus provide a critical control of the wind, temperature and moisture profiles.

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Previous studies have attributed the prevalence of the roll structure to the existence of an inflection point in the mean HBL radial wind profile and attempted to establish the link between the HBL environment and the roll statistical characteristics (e.g. Foster, 2005; Nolan, 2005). These analyses are generally consistent with observations: 1) the rolls are oriented at 0-10° to the left of the tangential wind; 2) the roll aspect ratio (ratio of the horizontal scale to the vertical) ranges from 2 to 4; and 3) the roll generated momentum fluxes are nonlocal. A recent study by Foster (2013) differentiates the standard boundary layer roll vortices, as those highlighted above, from the observed large roll vortices from Synthetic Aperture Radar images, whose horizontal scale reaches to 10-20 km. His results from a two-dimensional nonlinear resonant triad interaction model further suggest that the observed unusually large roll aspect ratio result from the up-scale energy transport through the nonlinear wave-wave interaction. Gao and Ginis (2014, hereafter GG14; 2016) investigated the formation of HBL rolls by solving a two-dimensional perturbation system driven by the mean wind profiles that are solutions of an axisymmetric HBL model. They concluded that the mean wind shear intensity affects the roll growth rate and the inflection-point level (IPL hereafter) impacts the roll wavelength. One of the strengths of these two-dimensional models lies in their use of the basic wind profiles that are either from observations or dynamically consistent with the TC environment. While these twodimensional quasi-analytical models have significantly advanced our understanding of HBL roll dynamics, they cannot accurately represent three dimensional stochastic turbulent flows. These work and conclusions are worth revisiting using a large-eddy simulation (LES) approach.

There have been a few LES studies of the HBL rolls. Zhu (2008) configured a nested WRF (Weather Research Forecast) model to include an LES domain with a horizontal resolution of 100 m and a vertical grid spacing varying from 5 to 65m below 1.6km. The WRF-LES was used to simulate a real case of hurricane landfall. Organized large-eddy circulations with horizontal scales ranging from 1 to 10 kilometres were found to intensely enhance the vertical momentum, heat and moisture transport. He further proposed a framework of the turbulent transport parameterization based on the conceptual model of convective up- and down-draft representation for shallow cumulus convection. While this mesoscale-LES grid nesting framework represents a highly realistic and sophisticated numerical approach, it does not allow for idealized sensitivity studies to examine impact of various mean conditions, such as wind profiles, on the roll structure. In an idealized study of HBL rolls, Nakanishi and Nino (2012, hereafter NN12) adopted a traditional LES approach, which uses a $20 \times 20 \times 4 \text{ km}^3$ domain with periodic lateral boundary conditions. They concluded that the inflection point instability in the radial wind profile leads to the formation of the quasi-linear roll structure with wavelengths between 1.5 and 2.4 km. The LES study by Green and Zhang (2015) also confirmed many of these findings and further suggested that the turbulence diffusivity varies considerably among different simulations, an indication that the downgradient transfer model breaks down for the momentum fluxes associated with the rolls.

Among these LES studies, only the WRF-LES nesting approach used by Zhu (2008) explicitly simulates mesoscale circulations and thus includes their effects on the roll structure. Others neglect the effects by assuming a local balance

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among the turbulent mixing, gradient wind, Coriolis force, and hurricane induced centripetal force. Consequently, the wind profile based on the local force balance may not represent the most relevant features with respect to the roll development in the HBL in the LES studies. For example, Morrison and Bussinger (2005) provided both observed radial and tangential winds from WSR-88D radar data, and the inflection point levels (IPLs) estimated from these observations are about 300 m to 800 m for the winds at the tropical cyclone radius 29km to 122km, respectively. These IPLs are generally higher than those of the LES simulations by Nakanishi and Nino (2012), which are 100 m and 300 m at the radius 40 and 100km, respectively. Therefore, there is a need to use more realistic wind profiles in the LES studies. The latest study of Bryan et al (2016) provided an improved HBL LES framework that accounts for the influence of mesoscale advections on the wind profiles. The current work introduces an empirical approach as discussed in next sections.

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Boundary layer rolls have been a subject of many studies since 1960s as reviewed by Atkinson and Zhang (1996) and Young et al (2002). Several physical mechanisms have been proposed for different environments, including the combined surface shear-buoyancy instability (Moeng and Sullivan 1994, Glendening 1996), the surface shear-cloud convection-radiation instability (Chlond 1992), the parallel instability (Lilly 1966), and the inflection point instability (Brown 1970, Brown 1972, Foster 2005). As discussed at the beginning of the paper, the most relevant mechanism for the HBL rolls is the inflection point instability. This work aims to gain new understanding of the impact of the mean wind profile characteristics that are directly associated with the inflection point instability, the shear strength and IPL, on the roll structure. We use a different LES modelling approach, featuring a mean nudging method which is applied to the momentum equations to strongly regulate the mean wind profile. This approach enables us to conduct a systematic study of the roll response, including the growth of the HBL, turbulence intensity, and the spectral distribution, to changes in the mean wind profiles. The remainder of the paper is organized as follows. Section 2 describes the LES model and simulation setups. Section 3 and 4 provide general description of the simulation results and spectral analysis, respectively. Further discussions on the wind shear are given in section 5. Section 6 summarizes the work.

2 Approach

25 **2.1 COAMPS-LES**

The Naval Research Laboratory Coupled Ocean/Atmosphere Mesoscale Prediction System-Large-Eddy Simulation (COAMPS-LES) is used in this study. The LES model was first introduced by Golaz et al. (2005) for the study of boundary layer cloud systems. It has been applied to investigate various types of boundary layer turbulence, including topographic flows, and stratocumulus dynamics (Golaz et al. 2007, Wang et al. 2012, and Jiang and Wang 2013). Readers are referred to these papers for detailed description as well as its various applications. Briefly, the model applies the anelastic approximation for efficient numerical computation and uses the Deardorff's prognostic turbulence kinetic energy approach for the subgrid-scale model (Deardorff 1980). For this study, the model coordinate is configured such that x is directed

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away from the centre of a TC in the radial direction, y is in the direction 90° counter-clockwise from x (azimuthal or longitudinal direction), and z the vertical axis. Because our simulations are focused on the dynamics and structure of the rolls, moisture is not included. The predictive variables are radial wind u, tangential wind v, potential temperature θ , and subgrid-scale turbulence kinetic energy. The model uses the horizontal resolution $\Delta x = \Delta y = 50$ m and a variable vertical grid with $\Delta z = 30$ m below 3km and gradually increasing to 200 m. This grid system covers a $25.2 \times 25.2 \times 4.9$ km³ domain. The Rayleigh damping technique is applied near the model top to reduce downward reflection of internal gravity waves. The surface momentum flux is calculated using the Charnock relationship linking the surface roughness length to the friction velocity under the neutral condition. To accelerate the LES spin-up process, a moderate constant surface heat flux $F_h = 20$ W m² is applied. Because of the strong near-surface winds (~ 30 m s¹), the application of the heat flux does not change the dominance of the shear production of turbulence. All the simulations start with the same initial conditions: a specified gradient wind (v = 45.5 m s¹ and u = 0 m s¹) for horizontal winds and a linear θ profile with a gradient of 0.00475 K m¹ and a value of 298.5 K at the first vertical level. The model is integrated for 10 h with a time step of 0.5 s.

2.2 Mean wind nudging

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As discussed in the introduction, the mean wind profiles resulting from the LES studies that do not include the mesoscale circulations (e.g., HBL inflow) may not adequately represent the wind characteristics in a hurricane environment. It is highly desirable that observationally based wind profiles be used and approximately maintained throughout the simulations. For these purposes, we adopt a modelling approach that can strongly regulate the mean wind profile according to our specifications. A special nudging term is added to each horizontal momentum equation to force the mean wind to approach a specified target wind profile. A unique feature of these nudging terms is that they only nudge the horizontally averaged wind. That is, at each time step, the horizontal mean wind profile, which is dependent only on z, is calculated from the predicted winds and used as the budged variable in the nudging term. Because the target profile is only a function of z, the nudging tendency is exactly the same at every horizontal grid point for the same level at each time step. Consequently, the LES predicted turbulent perturbations, which are defined as deviates from a horizontal mean, are not directly affected by the nudging terms. Both the turbulent perturbations and statistics are, of course, regulated by the mean wind profiles. This nudging approach was used to spin up LES simulations of stratocumulus clouds by Kazil et al (2016).

The momentum equations with the nudging terms can be written as

$$\frac{\partial u}{\partial t} = -\vec{v} \cdot \nabla u - \frac{1}{\rho_0} \frac{\partial p}{\partial x} + SGS - \left[\frac{v_g^2 - v^2}{R} - f(v_g - v) \right] + \left\{ \frac{U_T(z) - \langle u \rangle(z)}{\tau} \right\}$$
(1)

and

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$$\frac{\partial v}{\partial t} = -\vec{v} \cdot \nabla v - \frac{1}{\rho_0} \frac{\partial p}{\partial y} + SGS - \left[\frac{u \cdot v}{R} + fu \right] + \left\{ \frac{V_T(z) - \langle v \rangle(z)}{\tau} \right\},\tag{2}$$

where R is the radius from the LES domain to the centre of the TC, U_T and V_T are the prescribed target radial and tangential wind profiles, respectively, v_g represents the gradient wind, SGS the effect of subgrid scale motions, $\langle \ \rangle$ a horizontally averaged variable at each time step, and τ a relaxation time scale. Other symbols in Eq. (1) and Eq. (2) have their generally accepted meaning. These equations are the same as those used by NN12 except the nudging terms represented by the curly bracket in each equation. The square bracket is the gradient wind imbalance term associated with the centripetal force, the Coriolis force, and the large-scale radial pressure gradient. This term represents a major forcing that is responsible for the mean wind shear characteristics; it is designated as the rotational term hereafter for simplicity. Sensitivity simulations have been conducted to evaluate how well the mean wind profiles can be controlled by the nudging term. We have found that the mean wind profiles are better regulated by the nudging if the rotational terms are removed and its removal has little impact on the turbulence statistics. This is consistent with the previous results showing negligible effects from the curvature terms on the roll structure as well as the turbulence generation in general (Foster, 2005; NN12). Thus the square bracket terms are set zero in Eq. (1) and Eq. (2) for all the simulations presented in this paper. Therefore, the nudging terms are used to represent all the major processes that control the mean wind profiles, except turbulence terms. It is noteworthy that this new approach has a number of attractive advantages. Firstly, it maintains the mean wind profiles, which are derived from observations, and accordingly, are more realistic. Secondly, it offers a convenient way to systematically change the mean wind profile and therefore, allows us to examine the roll's response to these changes. At last, because the actual rotational terms are not explicit in the momentum equations, the horizontal winds no longer rotate with time and LES simulations may reach non-oscillatory quasi-equilibrium solutions. A comparison of three test simulations is presented in the Appendix.

20 2.3 Target wind profiles

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We are interested in two sets of LES quasi-equilibrium solutions corresponding to different mean wind characteristics with regard to both the wind shear strength and IPL. These two parameters are chosen because according to previous studies, they are key parameters related to inflection-point instability. The former is the main source of turbulence and the latter is linked to the roll scales (e.g. Chlond, 1992; GG14). The radial wind shear above the surface layer is a main focus of this study. The shear layer, where the inflection point is located, usually extends from ~ 100 m to the top of the HBL. To avoid

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confusion, we will use the term "surface wind shear" to describe the wind shear that is concentrated in the lowest 100 m. For the purpose of comparisons between simulations, we require that all the simulations approximately have the same wind speed. Therefore, the same gradient wind speed 45.5 m s⁻¹ is used.

To specify the target wind profiles, we experiment with LES simulations using variations of the observed winds (e.g., Foster, 2005 and Morrison and Bussinger, 2005). We choose two groups of the target winds as shown in Fig. 1. Group L simulations are forced with the target radial wind profiles (U_T) that have three shear strengths with IPLs approximately at 200 m (Fig. 1a). Similarly, group H simulations also have three shear strengths with IPLs between 400 m–500 m in the radial wind. The target tangential wind profile (V_T) is specified in Fig. 1b. The V_T profile with the shear occurring below 700 m (dash-dotted) is used for group L simulations, the other (solid) for group H. The constant value of 45.5 m s⁻¹ of V_T above 1.5 km represents the gradient wind speed. These simulations and relevant parameters are listed in Table 1.

3 Overall turbulence structure

This section is centred on a comparison of turbulence fields and statistics between group L and H simulations (see Table 1). A special attention is given to the coherent and organized turbulent flow manifested by the roll structure. All the profiles presented here are obtained from ensemble averaging, which is applied over the entire horizontal domain and between 8 and 10 h with a sample rate of 30 s. A time series of an average variable is constructed by taking the horizontal mean every minute.

3.1 Time evolution and mean state

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To gain a general impression of the HBL development and differences among the simulations, the time series of the HBL heights (z_i) and mean profiles are examined. As shown in Fig. 2, z_i increases rapidly with time for most simulations during the first 5 hours, after which the growth rate slows down considerably, implying a quasi-equilibrium state being reached. H2 behaves slightly differently in that z_i becomes slowly varying only after 8 h. There is a clear tendency of a stronger radial wind shear resulting in higher z_i for each group (L or H) of simulations. It is worth noting that H3 predicts the highest z_i among all the simulations, suggesting that it produces the strongest turbulence intensity even though it does not have the strongest radial shear (Table 1). It does have, however, the highest IPL and a relatively strong shear (Fig. 2b). The lowest z_i is obtained by L1 and H1, whose turbulence intensities are low because of the weak radial wind shear for both cases. For all the simulations, the parameter, $-z_i/L_{mo}$, where L_{mo} is the Monin-Obukhov length, is between 0.075 and 0.12 (Table 1). These values are considerably smaller than the values (0.5–0.65) that represent the shear-buoyancy regime transition found by Moeng and Sullivan (1994) in their study of the shear and buoyancy driven boundary layers, implying that the shear production of turbulence is dominant in all the simulations. The maximum value of $-z_i/L_{mo}$ among all the simulations is 0.13, which is considerably less than the lower criterion $-z_i/L_{mo} = 1.5$ for the formation of buoyancy-shear driven roll

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structures (Glendening, 1996). Therefore, any roll structure resulting from these simulations should not be explained by the buoyancy-shear mechanism.

Because the mean wind profiles are nudged toward the target winds, the last hour average winds exhibit the characteristics that bear resemblance to the target wind profiles (Fig. 1 and Fig. 2). For instance, the radial shear intensity increases with the radial wind speed within each group. It is noticed that group L has stronger wind shears and lower IPLs than group H and the shear reaches maximum at IPL for every radial wind profile. Group L has a stronger radial shear for the same maximum wind speed than group H simulations, which have higher IPLs around 480m than group L (\sim 240 m). The mean tangential winds are also very similar within each group. The mean potential temperature ($\bar{\theta}$) profiles show considerable variations because of different entrainment rates primarily determined by the shear generated turbulence as well as the surface heat flux.

3.2 Roll visualization

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Two major differences in the wind forcing among the simulations are associated with the radial wind shear strength and the IPLs. How do these differences affect the roll structure as well as turbulence in general? The link between the wind shear profiles and flow pattern is evident in horizontal cross sections of w' at three levels, $z/z_i \in (0.2, 0.4, 0.9)$, from the two groups of simulations shown in Fig. 3. These plan views demonstrate quasi-linear patterns defined by up and down motions for all the simulations except H1 for which the pattern is not clearly recognizable at $z/z_i=0.4$ and 0.9, although a narrowly spaced and weak quasi-linear pattern is present at $z/z_i=0.2$. The absence of the coherent structure from H1 is likely due to the weakest wind shear associated with the inflection point, which fails to generate strong turbulence to support the roll growth. The quasi-linear structures from the other 5 simulations have strong vertical coherence shown at three levels. Therefore, these flow patterns can be recognized as "roll structure".

It is evident that the rolls appear stronger, in terms of the maximum||w'||, with the increases in the radial wind shear intensity within each group, i.e., from L1 to L3 or H1 to H3. For example, $||w'||_{max}$ at $z/z_i = 0.2$ from L1 is about 5 ms⁻¹ compared with 7 m s⁻¹ from L2 and 10 m s⁻¹ from L3. The increasing shear also leads to an increase in the roll horizontal scale within each group. The scale can be roughly estimated based on the number of the rolls. It is about 1 km, 2 km, and 2.5 km for L1, L2 and L3, respectively, and 3 km and 3. 6 km for H2 and H3, respectively. Different IPLs in the radial wind profiles have crucial impact on the roll structure. A comparison of w' between the simulations of these two groups (i.e. L2 vs. H2 or L3 vs. H3) in Fig. 3 indicates that the horizontal scales of the rolls tend to be larger for group H (3 km for H2 and 3.6 km for H3) than group L (2 km for L2 and 2.5 km for L3) due to the higher IPLs in the former. It is noteworthy that H3, which has the highest IPL and moderately strong wind shear (Table 1), is characterized by the most vigorous rolls that have the largest horizontal scale, implying the importance of the IPL in regulating the roll intensity as well as the scale. The roll expansion

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from these simulations is consistent with the general increase in the HBL heights with the enhanced wind shear and rising IPLs (Fig. 2).

These simulations also show strong signature of gravity waves. For example, the linear roll patterns are well defined near the top of the HBL at z/z=0.9, where stable stratification is present (Fig. 2d). The pattern is particularly robust in H3. The similar patterns also occur above the HBL (not shown here). Strong evidence of gravity waves also comes from the turbulent statistics discussed in the next section. It is likely that this roll-like pattern within the inversion is connected to both the gravity waves and the roll structure in the HBL. The fact that H3 produces the strongest rolls as well as the largest gravity wave amplitude hints the possibility of an interaction between these two processes. This implication supports the previous results that internal gravity waves may be excited by the roll motion in the HBL and they interact with the rolls to enhance the associated turbulent transport (GG14, NN12).

Many of the above discussed aspects of the roll structure are also evident in the horizontal cross sections of other perturbation variables. Fig. 4 shows the wind component perturbations (u' and v') and their vertical fluxes (w'u' and w'v') at z/z_i =0.2 from H3. The negative v' tends to correlate with positive w' along each narrow quasi-linear band. These negative v' bands are caused by the upward motion transporting lower speed upward, directly resulting in a very similar roll pattern in the w'v' field (Fig. 4b). These patterns suggest that the roll-scale tangential momentum flux is dominated by the downward transport driven by the vigorous upward motion. The radial wind perturbations (u') also show the similar roll feature with the black line indicating a convergence line with $u' \sim 0$, corresponding to the positive w' in H3 (Fig. 4a). It is interesting that the roll patterns are barely distinguishable in w'u' (Fig. 4d), in contrast to w'v' (Fig. 4b), although they are evident in both w' and u' fields (Fig. 4d). The poor correlation between u' and w' near the surface is likely due to the alignment of the roll axis, namely, nearly along the tangential direction. This can be seen by assuming the rolls are strictly two-dimensional and ignoring the small angle between the roll axis and the tangential direction. The continuity equation reduces to $u'_x + w'_z = 0$ and w' can be written as $w' = -\int\limits_0^z \partial u' / \partial x \cdot dz$, which implies that the vertical velocity near the surface is mainly

driven by the low-level convergence of the radial flow. The above expression also implies that u' and w' are approximately 90^0 out of phase: when u' reaches a maximum or minimum, $\partial u'/\partial x \sim 0$ and, therefore, $w' \sim 0$. Similarly, when w' reaches a maximum or minimum, $u' \sim 0$.

This argument is supported by more quantitative analysis. For this purpose, a coordinate transformation is performed on the instantaneous fields so that the resulted u velocity is perpendicular to the longitudinal roll alignment while v is along the longitudinal direction. Then all the turbulent perturbations can be averaged over a distance (5 km in this case) along the roll direction to provide a snap shot of mean roll circulations at an x-z cross section. Figure 5 shows the roll velocity

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perturbations and the layer averaged radial convergence $(\frac{1}{z}\int_{0}^{z}\partial u'/\partial x\,dz)$ at z=90 m and z=500 m. It is evident that $u'\cong 0$

at 90 m coincides with the strong convergence and positive w' values near $x \sim 6.4$ km, 9.8 km, and 13.5 km indicated by the open circles, making positive w' correlate with both positive and negative u'. At 500m, however, the locations with $u' \cong 0$ move toward the rotation centre (i.e., toward the left), thus enabling a better correlation of positive w' with negative u'. The cross section of the roll circulation from Fig. 6 shows that updrafts are originated along the convergence slope where $u' \cong 0$ and tend to coincide with negative u' above the slope, leading to a stronger downward cross-roll momentum transport aloft. It is noteworthy that the maximum convergence of the lowest 500 m occurs at similar locations as that of the 90 m despite the titling of the convergence zone, implying that the main forcing of the updrafts is the radial convergence near the surface. It also explains that the updrafts expand in the cross-roll direction with height without significant tilting.

0 3.3 Turbulence statistics

Turbulence statistics respond strongly to the different wind profiles as demonstrated in Fig. 7. The negative radial momentum flux $(\overline{w'u'})$ is significantly enhanced with the increase in the radial shear intensity for group L or H, particularly near the levels of the inflection points, where the shear reaches its local maximum as pointed out by GG14. The higher IPLs from group H enhance $\overline{w'u'}$ in the upper portion of the HBL because of the increased shear layer depth (Fig. 2). The stronger turbulence aloft in group H simulations further intensifies the entrainment across the inversion, leading to a deeper HBL. Both H3 and L3 have similar $\overline{w'u'}$ maxima in spite of the large difference in their shear shown in Table 1. The tangential momentum flux $(\overline{w'v'})$ also strengthens from group L to H responding, in part, to the enhanced tangential wind shear above 300 m (Fig. 2). The $\overline{w'v'}$ in H3 increases the most since the turbulence (e.g. $\overline{w'^2}$) is considerably stronger in the upper part of the HBL than in other simulations. One consequence of the $\overline{w'v'}$ increase is to reduce the surface "friction" effect on the tangential wind speed because the overall HBL flux gradient is decreased as a result of the enhanced downward $\overline{w'v'}$ in the mid- and upper HBL. Recalling the robust roll structure from H3 (Fig. 3), we interpret the strengthening of turbulence as resulting from the highly organized and effective roll transport. This reasoning is supported by the spectral analysis presented in section 4.

The buoyancy flux $(C_p\rho_0 \ \overline{w'\theta_v'})$ decreases from the fixed value, 20 Wm⁻², at the surface to the maximum negative entrainment flux at the inversion base (Fig. 7f). It is well documented that the ratio between the entrainment and surface heat flux is -0.2 for free convection generated by the surface heat flux (Deardorff 1982, Conzemius and Fedorovich 2006). Thus, the effect of wind shear on $C_p\rho_0 \ \overline{w'\theta_v'}$ is evident as the magnitude of this ratio can be as large as ~ -1.5 for H3. Variance of each wind component (i.e., $\overline{u'^2}$, $\overline{v'^2}$ or $\overline{w'^2}$) increases with the shear strength for both group H and L (Figs. 7 c-

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e). H3, which has the highest inflection point and moderately intense shear, produces the strongest turbulence. It is noticed

that, above the HBL, both $\overline{w'^2}$ and $\overline{\theta'^2}$ are not negligible, or even very large for some of the simulations (e.g., H3 and H2)

while the $\overline{w'\theta_{v'}}$ values are close to zero as shown in Figs. 7e-g. This strongly suggests the presence of internal gravity

waves above the HBL, which are presumably generated by mesoscale perturbations associated with the HBL rolls.

According to linear wave theory, there is a 90° phase lag between the wave-induced vertical velocity and potential

temperature perturbations, and therefore, vertical heat flux associated with wave-induced perturbation is zero, although the

vertical velocity and potential temperature variances can be large. The presence of gravity waves above boundary layer rolls

is consistent with results from many studies including both LES (e.g., NN12) and 2-D model studies (e.g., GG14).

The skewness of the HBL flow, defined by $S_w = \overline{w'^3} / \overline{w'^2}^{3/2}$ (Figs. 7h and 7i), represents the symmetry, or lack thereof, in the

turbulence structure. That all the S_w values above 150m are positive points to a positively skewed structure, that is, the flow

is characterized with narrower/stronger updrafts and broader/weaker downdrafts (Zhu 2008; Foster 2005). In general, a high

degree of the flow asymmetry is reached in the upper portion of the HBL.

Some important features emerging from the above diagnosis are worthy of emphasis: 1) most simulations (except H1)

produce well-defined roll structure manifested by a quasi-linear pattern through the depth of the HBLs; 2) increasing radial

wind shear results in enhanced turbulence, higher HBL height, and larger roll spatial scales; 3) rising IPL also leads to a

larger roll spatial scale in spite of the weakened radial shear; 4) the vertical tilting (in the radial direction) of the low-level

convergence zone enhances the radial momentum flux associated with HBL roll circulations; and 5) the presence of internal

gravity waves is strongly suggested by the "roll-like" pattern above the HBL and the 90 degree lag between w' and θ'

implied by the turbulence statistics. Some of these features are further confirmed by the spectrum analysis described in the

next section.

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4 Spectrum analysis

To understand how the turbulent flow at various scales respond to the changes in the wind forcing and how effective rolls

are in vertical momentum transfer, we examine 2D power density spectra of the simulated w' and its co-spectra with u', v',

and w'^2 at $z/z_i = 0.4$ where the rolls are most robust. The focus on 2D spectra instead of 1D is due to the fact that the former

represents spectral peaks and associated spatial information more reliably than the latter as discussed by Kelly and

Wyngaard (2006).

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4.1 Turbulence spectra

All the spectra are calculated using data collected between 8-10 h with a sampling interval of 5 min. They are functions of the magnitude of the horizontal wavenumber vector $k_h = \sqrt{k_x^2 + k_y^2}$, where k_x and k_y are the wavenumber in the radial and tangential direction, respectively. Figures 8 and 9 compare various turbulence spectra at $z/z_i = 0.4$ among simulations within each group as well as between the two groups. For each group, the power of w' increases with the enhancing shear at all wave numbers (Fig. 8a). This increase, however, is more significant for the wave numbers less than 0.01 m⁻¹, i.e., the spatial scales larger than 600 m, which is particularly true for group H. The changes in the spectral distribution from group L to H are more complicated because the higher IPLs are associated with weaker wind shear (Fig. 2). The major difference between the two groups occurs at the wavenumbers between 10^{-3} m⁻¹ and 5×10^{-3} m⁻¹. The H2 spectrum remains essentially the same as the L2 for the wavenumber $k_h \ge 0.008 \text{ m}^{-1}$, below which the H2 power becomes lower than the L2 before it reaches the narrow peak at $k_h = 0.002$ m⁻¹. For L3 and H3, their spectra are very close to each other except that the latter (H3) exhibits a peak at a smaller wavenumber (i.e., $k_h = 0.0017 \text{ m}^{-1}$, or the longer wavelength ~ 3.6 km) than the former (L3) (i.e., $k_h = 0.0017 \text{ m}^{-1}$) 0.0027 m⁻¹, or the wavelength ~ 2.3 km). The spectral peak from H3 is the strongest and its wavenumber is the smallest among all the simulations (Table 1). This is consistent with the instantaneous roll features that the H3 rolls are the strongest and the horizontal scale is the largest (Fig. 3). In contrast to the relatively smooth shape of the group L spectra, the spectra of both H2 and H3, which have higher IPLs than group L, exhibit a narrow peak (Fig. 8a), indicating the presence of a highly energetic and single-mode structure. This qualitative difference suggests that IPL plays a critical role in determining the roll strength and the effectiveness of the turbulent transport.

Many of the essential features discussed for the w' power spectrum are also evident in the cospectrum of $w' - w'^2$, w' - v', and w' - u' in Fig. 8b and Fig. 9. Note that the covariance of w' and w'^2 gives $\overline{w'^3}$, which is related to the skewness. The cospectrum of $w' - w'^2$ from each of the simulations L2, L3, H2 and H3 is consistent with the corresponding w' power spectrum in that both have the same peak wavelength. The cospectrum peak from H3 is the most prominent in that it is both large and narrow, implying that the roll vertical motion is strongly and positively skewed.

A major feature of the cospectrum of w' and v' from both H2 and H3 of Fig. 9 is its sharp negative maximum at the same peak wavenumber as that from the w' spectrum, suggesting significant roll contributions to the longitudinal momentum flux. Compared with H2 and H3, the group L cospectra show a much smaller maximum even though their peak wavenumbers are the same as those of the rolls derived from the w' spectrum. For w' - u' cospectra, only H3 results in the same peak wavenumber as the rolls defined by the w' spectrum, while other simulations produce the peak wavenumbers that are larger than the corresponding rolls. Therefore, the roll structure from H3 is arguably the most robust as it has the strongest spectral

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peaks, among all the simulations, at the same roll wavelength in the w' power spectrum and the cospectra of $w' - w'^2$, w' - v', and w' - u'.

It is also noteworthy that the presence of a significant narrow peak in the momentum flux spectra is consistent with the observational analysis by Zhang et al (2008), which shows sharp peaks in all the cospectra of w' and the horizontal wind and temperature perturbations (their Fig. 9). A main difference is that their observed peak occurs at 900 m with an aspect ratio ~ 2 and our LES modelled is at 3.5km with the ratio 2.7.

4.2 Spectral decomposition of turbulent fluxes

How significant are the contributions from the HBL rolls compared to other turbulent eddies to turbulent fluxes in the LES simulations? This issue has been addressed previously with a decomposition method that is based on the roll coherence feature. For example, the updraft-downdraft roll circulation can be defined based on the quasi-linear longitudinal coherence of the roll structure (Glendening 1996); the roll-scale characteristics may also be represented as conditional means of the turbulent flow (Zhu 2008). Because a key feature of the rolls is that turbulence is organized in such a way that various flux spectral distributions reach the respective maximum at the roll wavelength. Therefore, a decomposition method that is based on spectral analysis provides a more fundamental representation of roll characteristics. This approach is also consistent with the observational analyses of HBL rolls by Zhang et al (2008).

To compute the contributions from different wavenumbers, we integrate each flux over three spectral bands to yield the subtotals at each model level. The spectral bands are chosen, in principle, to represent turbulent fluxes from the small scale, the large-eddy scale, and the roll scale based on the H3 spectra (Figs. 8 and 9). The small scale (L_S) ranges from 100m to 1km; the large-eddy scale (L_E) 1km to 2.5 km; the roll scale (L_R) 2.5 km to 12km. The calculation is carried out from the surface to 2 km.

To emphasize the relative importance of the fluxes at different spectral ranges we calculate both the fluxes and the flux fractions defined by the ratio of a specific flux to the total, as shown in Fig. 10. The small-scale contribution to $\overline{w'^2}$ dominates in most of the HBL; the large roll variance increases significantly with height to the top of the HBL above which it carries more than 70% of the total variance (Fig. 10a). This is consistent with the characteristics of the flux profiles implying the presence of gravity waves above the HBL (Fig. 7e, f and g). These gravity waves have the wavelengths comparable to the horizontal scales of the rolls, implying that the rolls are the most likely wave source.

The longitudinal momentum fluxes ($\overline{w'v'}$) from different spectral ranges exhibit different vertical distribution with the small-scale reaching the maximum near the surface and the larger scale near the mid-HBL (Fig. 10b). This difference

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reflects different nature of the turbulence at different scales. The small-scale turbulence is largely produced by the near surface shear of tangential wind shear, thus the flux maximum is naturally close to the surface. The roll circulation, caused by the inflection point instability, generates the momentum flux that depends on the wind shear in both the tangential and radial direction in the mid-HBL. The momentum flux $\overline{w'v'}$ obtains the largest roll fractional contribution 43% at the mid-HBL among all fluxes (Fig. 10f). The combined roll and large-eddy fluxes account for 65% of the total. The roll contribution to $\overline{w'u'}$ is only 25%; it is considerably weaker than the contribution to $\overline{w'v'}$, a result in accordance with the previous discussion that the radial flux has less roll coherence than the longitudinal one. The roll contribution to $\overline{w'}$ reaches the maximum at $0.7z_i$, accounting for about 20% of the total (Fig. 10d and h), while the combined roll and large-eddy contribution is about 45%.

4.3 Roll characteristics: correlation coefficients and skewness

We have argued that the correlation between the roll-scale w' and u' is weaker than that between w' and v' because the low-level convergence is mainly driven by the radial wind component, thus leading to the diminished u' in the area where the roll w' reaches the maximum values. This reasoning is based on both the instantaneous perturbation fields (Figs. 4-6) and the momentum related cospectra (Fig. 9). It is also supported by quantifying correlations of w' - v' and w' - u' from the roll contributions shown in Fig. 10. These correlation coefficients are shown in Fig. 11. The absolute value of the coefficient C_{wv}^R , defined by $C_{wv}^R = [w'v']^R / \{[w'^2]^R \cdot [v'^2]^R\}^{0.5}$ where superscript R represents the roll contribution, is around 0.45 from 30 m to 500 m, then decrease to near zero at 1 km. In contrast, $|C_{wv}^R|$ increases from 0 near surface to 0.3 at 200 m, keeps nearly constant up to 900 m, and then gradually decreases to 0.2 at 1.5 km. The values of $|C_{wv}^R|$ are smaller than those of $|C_{wv}^R|$ below 600 m, indicating a weaker roll correlation of w' with u' than with v'. The increasing value of $|C_{wv}^R|$ with height in the lowest 300 m is also in an agreement with the understanding of the tilted convergence zone allowing for more efficient radial momentum flux away from the surface (Fig. 6).

The results of the roll contribution to the third moment $\overline{w'^3}$ may be used to characterize the roll structure such as the roll skewness (S_w^R). For this purpose, the skewness is computed in the same fashion as the correlation coefficients from the roll contributions to $\overline{w'^2}$ and $\overline{w'^3}$. Because the simulated skewness is likely problematic near the surface due to the coarse resolution (Sullivan and Pattern 2011), only the profile above 200 m is plotted in Fig. 11. The skewness S_w^R decreases from 1.6 at 200 m to 0.7 at 600 m and to 0 above the HBL, where gravity waves are likely present. This decreasing-with-height tendency agrees with the calculation of Zhu (2008, Fig. 9a), although our skewness values are larger than his result. Therefore, the roll updraft fraction is generally less than 50% and increases with height. In addition, the roll-scale skewness

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is close to zero above the HBL, indicating that the flow at these scales is symmetric. This characteristic is consistent with the linear theory of internal gravity waves. For a linear wave at a given level, the updrafts and downdrafts in a horizontal domain with period boundary conditions applied along the side walls should occupy approximately the same amount of the fractional coverage.

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The spectral analysis in this section confirms that both the roll's horizontal scale and intensity are highly dependent on the shear and IPL in the radial wind profile. The stronger the radial wind shear is and the higher the IPL is, the stronger and larger the rolls are. More importantly, increasing IPL tends to produce a robust roll structure in the sense that a narrow and sharp peak is present in the w' power spectrum and its wavelength is the same as the peak wavelengths from the co-spectra of $w'-w'^2$, w'-v', and w'-u'. This is in contrast to the weaker rolls (e.g. H2) for which the peak wavelength from the w'-u' is shorter than the others because of the weaker coherency between the roll-scale w' and u'.

5 Impact of tangential wind shear

We have so far emphasized the impact of the radial wind shear on both turbulence intensity and spectral distribution. However, both the radial and tangential winds may have significant shear above the surface layer (Fig. 2b and 2c). What roles does the tangential wind shear play in regulating the roll structure? This section attempts to address this issue by comparing the simulations H3, L3, L3H, and H3L, which are forced with different radial and tangential wind shear in the target profiles (Table 1). The simulation L3H uses the same target radial wind profile as the L3, but the same target tangential wind as the group H simulations (i.e. the profile H in Fig. 1). Correspondingly, the H3L adopts the same target radial wind profile as the H3, but the target tangential wind of the group L (i.e. the profile L in Fig. 1). This target wind specification is designed to examine how the roll structure responds to a change in one wind component while the other remains the same.

The comparison of the turbulence statistics profiles from H3 and H3L with those from L3 and L3H shown in Fig. 12 suggests that the radial wind plays a dominant role in determining the turbulence intensity. The target radial wind with a high IPL from H3 and H3L leads to both the stronger $\overline{w'u'}$ and higher HBL tops than the wind profile with a low IPL from L3 and L3H, regardless of different target tangential wind used. The tangential momentum flux $\overline{w'v'}$ is, however, predominately determined by the tangential wind shear (Fig. 12a). Both L3 and H3L result in similar weak momentum fluxes $(\overline{w'v'})$, which can be attributed to the same target tangential wind profile L in Fig. 1b. The stronger momentum fluxes are obtained from H3 and L3H, which have the same extended higher-level tangential shear profile H in Fig. 1b.

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The spectral response of the turbulence is displayed in Fig. 13. A dominant feature is that there is a strong peak in the power spectrum of w' as well as the two co-spectra of w'-v' and w'-u' at the same wave number from H3 and H3L, which have the same radial wind with the higher IPLs (Fig. 1a). This is particularly true for the co-spectra of w'-u'. In contrast, the peak values of the spectra from L3 and L3H are more broadly distributed at higher wave numbers. It is worth noting that the peak in the w'-v' co-spectrum of H3L is considerably weaker than that of H3 because of the tangential wind shear reduction at upper levels in the target wind profile L (Fig. 1b).

The above results suggest that the radial wind shear plays a more dominant role in determining the roll characteristics with regard to the scale selection, while the tangential wind shear strongly influences the tangential momentum flux $\overline{w'v'}$, which affects the turbulence intensity. This result is largely consistent with the analysis of GG14 who found that the radial wind shear and IPL defines the roll characteristics regarding the mode selection and turbulence intensity. Their analysis, however, does not include contributions from the tangential wind shear to the roll energetics because of the two-dimensional nature of their dynamic model.

6 Summary and conclusion

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A series of LES simulations have been conducted to examine the response of the roll structure to different mean wind shear conditions in terms of the radial wind shear strength and the IPL in the idealized HBL. A unique feature in our approach is that a mean wind nudging technique with specified target wind profiles is used to maintain the horizontal-domain average wind profiles without directly affecting turbulent perturbations. Two groups of simulations (*L* and *H*) are conducted. Each group uses the same target tangential wind profile, but the three radial wind profiles with different shear. Group H are designed to have higher IPLs (~ 430m) in the radial wind than group L (~ 200 m).

All simulations except H1, which has the weakest radial wind shear, produce the rolls manifested by a quasi-linear structure with the horizontal scale ranging from 1 km to 3.6 km. The roll structure extends from the near-surface level $(z/z_i \sim 0.1)$ to the HBL top $(z/z_i \sim 0.9)$. Within each group of simulations (L or H), increasing radial wind shear tends to enhance overall turbulence and increase the HBL height. Both the w' spectral peak and its wavelength increase with the enhanced radial wind shear, indicating that the shear regulates both the roll's intensity and horizontal scale. Increasing IPLs, from group L to H, results in more vigorous rolls with distinctly narrow and sharp peaks in their power spectra. The most robust rolls are produced in H3, which is forced with the highest IPL and moderately strong shear in the radial wind. A unique and important feature of this roll structure is that the peak wavelength is the same among the power spectrum of w' and the cospectra of $w' - w'^2$, w' - v', and w' - u', implying that a consistent large roll contribution to the relevant turbulent fluxes.

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This feature is also in contrast to all other simulations in which the peak wavelength from the w'-u' is shorter than the others because of the less coherent aspect between the roll-scale w' and u'.

One of the important features regarding the roll contribution to the vertical momentum flux is that the tangential wind is better correlated with the vertical motion than the radial wind in the lower half HBL. It is because the low-level convergence mainly comes from the radial wind, whose roll-scale perturbation is close to zero where the upward motion is maximized. The convergence zone is tilted with height toward the rotation centre to generate broader updrafts in the area of negative radial wind perturbations. Consequently, the negative correlation of upward motion and radial wind perturbation increases with height. This view is supported by the roll momentum correlation coefficients calculated based on the spectral analysis.

Effects of tangential wind shear are also investigated. A sensitivity simulation, in which the upper level tangential wind shear is reduced, shows that the basic roll structure is not significantly impacted in the sense that both the power spectrum and the momentum flux co-spectra generally maintain their distributions. The tangential momentum flux, however, changes significantly with the tangential wind shear, which feedbacks to the turbulence generation and leads to some difference in the overall turbulence intensity. This effect is also reflected in the w' power spectrum and tangential momentum flux cospectrum in which the peak values are reduced. Therefore, the radial wind characteristics critically determine the roll's presence, intensity, and scale, while the tangential wind shear has considerable impact on the tangential momentum transport.

The results of the spectral analysis are also used to compute the roll contributions to various turbulent fluxes if the roll scale motions are defined in terms of the wavelength in the w' spectrum, i.e., $2.5 \ km \le L_R \le 6 \ km$ for H3. Our calculation shows the following roll contributions for various turbulent flux variables at the mid-HBL: 15% for $\overline{w'}^2$, 40% $\overline{w'v'}$, 20% $\overline{w'u'}$, and 20% $\overline{w'}^3$. The large-eddy contribution, defined by $1.0 \ km \le L_E \le 2.5 \ km$, is $25\% \ (\overline{w'}^2)$, $30\% \ (\overline{w'v'})$, $30\% \ (\overline{w'u'})$, and $20\% \ (\overline{w'}^3)$. These values are, in general, consistent with previous studies (e.g. Zhu 2008; Zhang et al 2008). Because the magnitude of the negative roll tangential flux increases from almost zero to the maximum near the mid-HBL, the roll circulations tend to enhance the lower-level mean tangential wind by upward transport of the weaker wind.

This study highlights the critical roles of the radial wind shear in regulating the roll structure. As discussed in the introduction, the mean wind shear should be a strong function of both the local rotational forcing and the mesoscale tendencies. The mean nudging approach used in this work is intended to bridge the gap between the commonly used LES configuration and the need for including the mesoscale effects, and to facilitate sensitivity simulations. Because of the strong nudging it is difficult to fully analyse the impact of the rolls on the mean wind profile in this study. A more comprehensive study of the roll structure requires incorporating effects of the hurricane mesoscale environment such as

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radial wind advection. The LES approach recently proposed by Bryan et al (2016) and the nested LES in a mesoscale model of Zhu (2008) provide attractive the modelling frameworks that can be used to address issues related to the feedback of the rolls to the mean wind profiles in HBLs.

5 **Appendix:** Mean wind nudging

The mean wind nudging method introduced in section 3 is used to maintain LES predicted mean wind profiles and to make systematic changes in the mean wind for sensitivity simulations; it has no direct influence on the resolved turbulence. Three LES simulations are presented here to evaluate these statements. The first simulation (RN1) uses the horizontal momentum equations with the rotation terms (i.e., the square bracket terms) and without the nudging terms in Eq. (1) and Eq. (2). The second (RN2) keeps both the rotation and the nudging terms for which the target wind profiles are the same as the 9-10 h averaged wind from RN1. The third (RN3) removes the rotation term and keeps the nudging, and the target profiles are the same as those from RN2 except the target radial wind is enhanced to -16.5 m s⁻¹ at 90 m as shown in Fig. A1a. The relaxation time scale is 10 minutes.

In general, all the variables are in excellent agreement among the three simulations as shown in Figs. A1-A2. The simulation RN1 and RN2 have very consistent z_i after 4 simulation hours, while the RN3 predicts z_i that is 50 m lower than the others. The radial wind velocity at 60 m from RN1 oscillates around the mean value -9.5 ms^{-1} after 1 h, which is consistent with that from RN2 and only 0.6 ms⁻¹ stronger than RN3 that excludes the rotation term. The significantly reduced oscillation in RN2 is due to the strong nudging, and the absence of the oscillation in RN3 reflects the removal of the rotation term. Despite these differences, all the mean and turbulence profiles compare well among these simulations. RN1 and RN2 almost have identical results as seen from Fig. A2. RN3 predicts slightly weaker turbulence in the upper HBL, being consistent with the weaker shear in both \bar{u} and \bar{v} at these levels. These results confirm the previous two-dimensional model simulations and LES analyses that the rotation terms do not have major influence on the turbulence structure (Foster 2005, NN12). They also demonstrate that the mean wind nudging method can be used to examine the response of turbulence to a specific mean wind profile that is strongly regulated by the nudging process. All the simulations made in the paper exclude the rotation terms and include the nudging terms in Eq. (1) and (2) with the relaxation time scale 10 min.

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Table 1: Simulation conditions and results with the following parameters: Maximum radial wind shear (RSH_{max}), inflection-point level (IPL), target radial wind (U_T), target tangential wind(V_T), wavelength at the peak of w' power spectrum (Lp), HBL height (z_i), aspect ratio (L_p/z_i), and the ratio $-z_i/L_{mo}$, where L_{mo} is the Monin-Obukhov length.

	Exp	RSH_{max}	IPL	U_T	V_{T}	L_p	z_i	L_p/z_i	- z_i/L_{mo}
10		s ⁻¹	m	Fig. 1a	Fig. 1b	km	km		
	L1	0.0139	210	L1	L	1.20	0.88	1.4	0.07
15	L2	0.0216	210	L2	L	1.94	1.05	1.8	0.08
	L3	0.0273	180	L3	L	2.29	1.14	2	0.08
	H1	0.0053	480	H1	Н	1.01	0.91	1.1	0.08
	H2	0.0110	360	H2	Н	3.15	1.12	2.8	0.1
20	Н3	0.0142	450	Н3	Н	3.60	1.35	2.7	0.13
	L3H	0.0276	210	L3	Н	2.3	1.22	1.9	0.08
	H3L	0.0147	420	Н3	L	3.1	1.25	2.5	0.1
	113L	0.0147	420	113	L	3.1	1.23	۷.3	0.1

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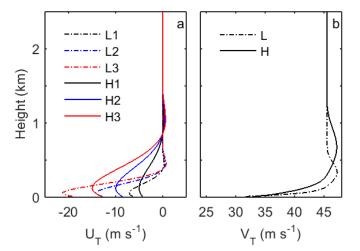


Figure 1: Target wind profiles used in group L (dash-dotted) and H (solid) simulations. (a) Target radial wind profiles; (b) target tangential wind profiles. Note that only one target tangential profile V_T is used for either group.





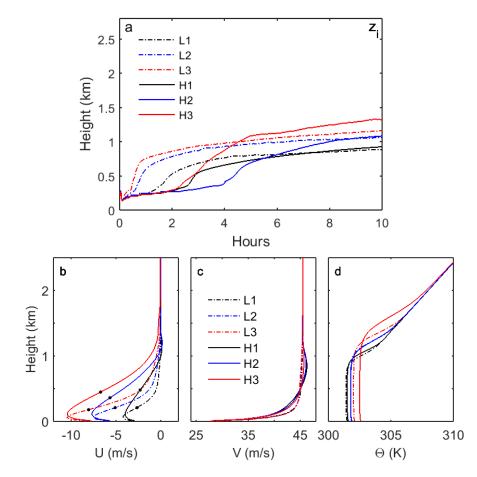


Figure 2: HBL height evolution and mean vertical profiles. (a) BL height z_i from group L and H simulations; (b) mean radial wind \overline{u} ; (c) mean tangential wind \overline{v} ; and (d) mean potential temperature $\overline{\theta}$. The black dots in Fig. 2b denote the inflection point levels (IPLs).





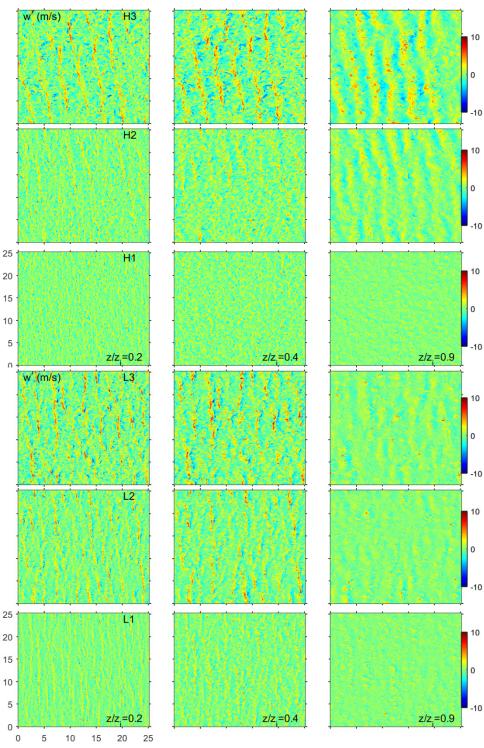


Figure 3: Horizontal cross sections of vertical velocity \mathbf{w}' at three different levels (i.e., z/zi = 0.2, 0.4, and 0.9, respectively) from group L and H simulations.





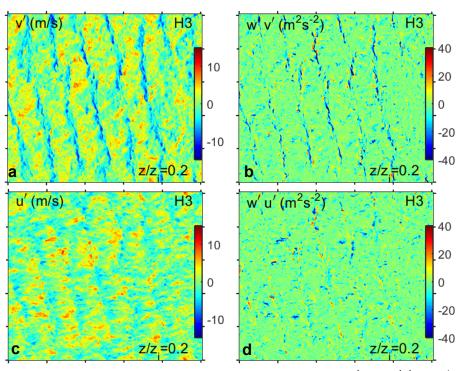


Figure 4: Plan views of turbulent perturbations from H3 at z/z_i =0.2. The fields are (a) v', (b) w'v', (c) u', and (d) w'v'. An "eye-fit" black line is drawn in (c) to show an example of convergence zone induced by the radial wind.

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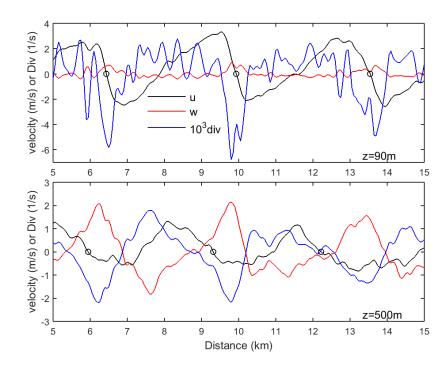


Figure 5: Phase differences between roll perturbation u' (black), \mathbf{w}' (red), and vertically integrated divergence, $div = \frac{1}{z} \int_{0}^{z} \partial u' / \partial x \, dz$ (blue) at z = 90 m (top) and z = 500 m (bottom) for H3. The open circles denote the locations where u' = 0 and $\partial u' / \partial x < 0$. Note the different vertical scales between the top and bottom panels.

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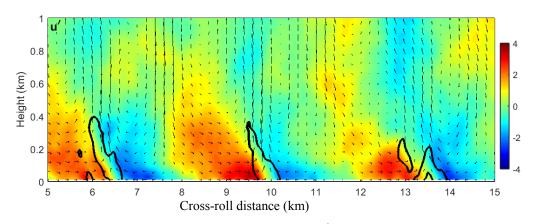


Figure 6: Vertical cross section of the along-roll averaged perturbation u' from H3 along the cross-roll direction $\partial u'/\partial x = -5 \times 10^{-3} \text{ s}^{-1}$ is contoured by thick black lines. The flow vectors are also shown.

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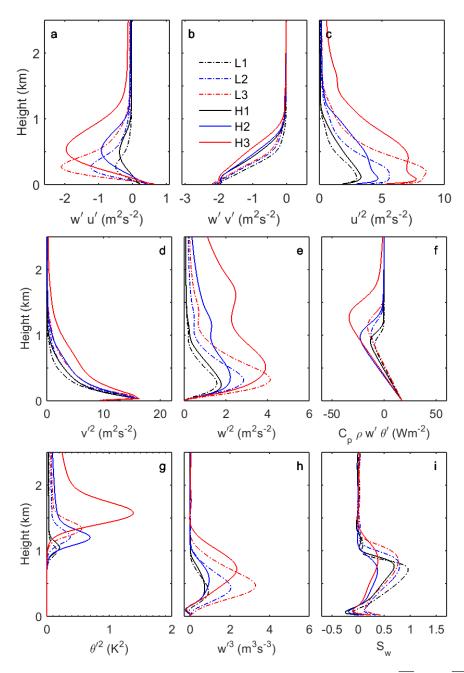


Figure 7: Profiles of LES turbulence statistics. The variables are (a) $\overline{w'u'}$, (b) $\overline{w'v'}$, (c) $\overline{u'^2}$, (d) $\overline{v'^2}$, (e) $\overline{w'^2}$, (f) $C_p \rho \overline{w'\theta'}$, (g) $\overline{\theta'^2}$, (h) $\overline{w'^3}$, and (i) $S_w = \overline{w'^3} / (\overline{w'^2})^{3/2}$.

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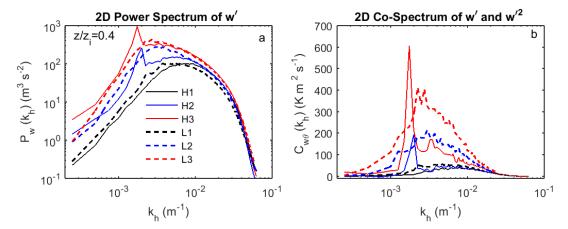


Figure 8: 2-D power spectra of w' (a) and co-spectra of $w' - {w'}^2$ (b).

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(c) (d)

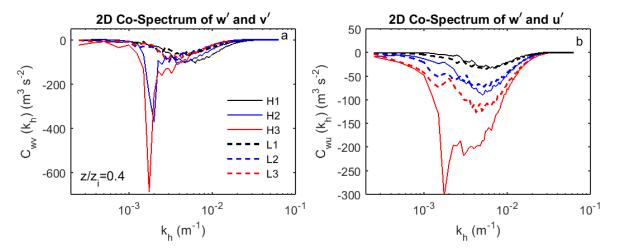


Figure 9: Co-spectra of w' and v' (a) and w' and u' (b)

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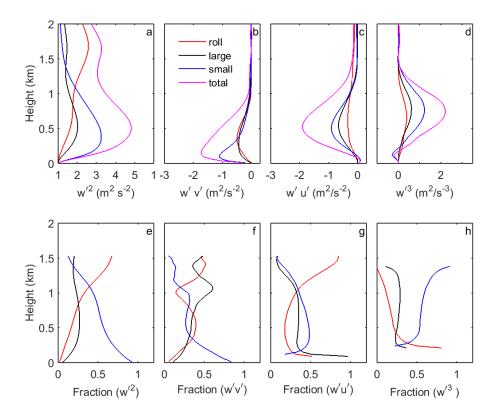


Figure 10: Decomposition of turbulent fluxes for H3. Various spectral components for turbulent flux profiles are presented in top panels; fractional contributions from the components in bottom panels. Total resolved flux is denoted by magenta, small-scale ($L_S < 1$ km) blue, large-eddy (1 km $< L_E < 2.5$ km) black, and roll ($L_R > 2.5$ km) red.

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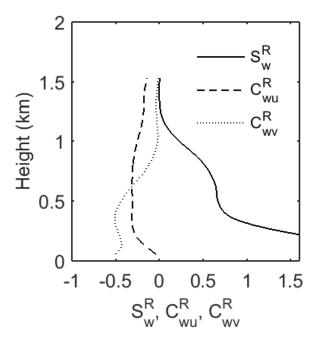


Figure 11: The vertical profiles of roll characteristics derived from H3: w skewness (solid), w' - v' correlation coefficient (dotted), and w' - u' correlation coefficient (dashed).





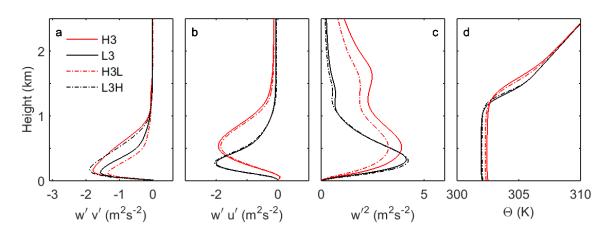


Figure 12: Comparison among simulations H3, L3, H3L and L3H with different wind shear. (a) $\overline{w'v'}$; (b) $\overline{w'u'}$; (c) $\overline{w'^2}$; and (d) $\overline{\theta}$.

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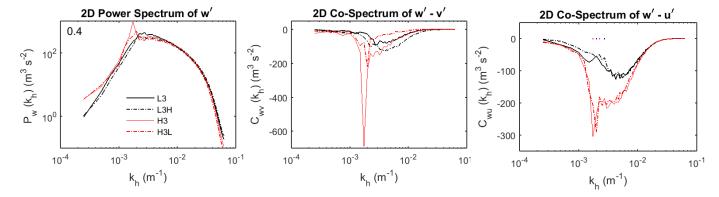


Figure 13: Comparison of the power spectra of w' (left), cospectra of w'-v' (centre), and w'-u' (right) at $z/z_i=0.4$ between L3 (black solid), L3H (black dash-dotted), H3 (red solid), and H3L (red dash-dotted).

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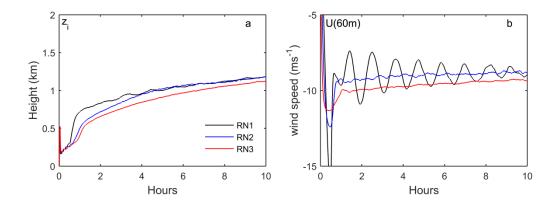


Figure A1: Comparison of the evolution of the boundary layer height z_i (a) and the radial wind component $\overline{\mathcal{U}}$ at the 60 m level (b) from three tests RN1, RN2, and RN3.





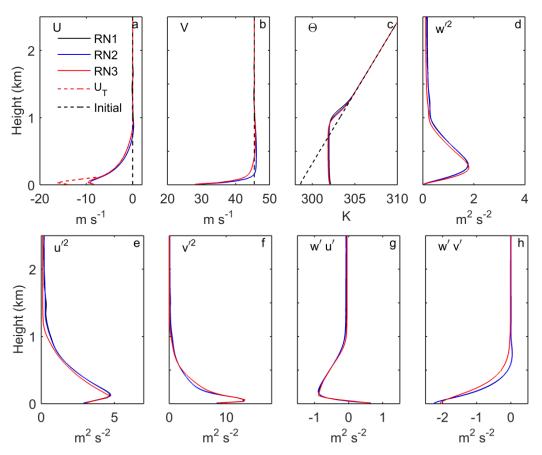


Figure A2: Comparison of test simulations for the mean nudging approach. All the profiles are averages between 9–10 h at a sampling interval 30 s. (a) Mean radial wind (the red dashed is the target radial wind used for RN3); (b) mean tangential wind; (c) $\overline{\theta}$; (d) $\overline{w'^2}$; (e) $\overline{u'^2}$; (f) $\overline{v'^2}$; (g) $\overline{w'u'}$; (h) $\overline{w'v'}$.