

Authors response to the reviewer's reports.

We would like to thank both reviewers once again for the careful reading of the revised manuscript (revision 1) and provided feedback. Below we provide our responses (italic blue) to the issues addressed by the reviewers, and indicate the changes made in the manuscript. These changes are also highlighted in blue font in the revised manuscript (revision 2).

Report # 1. Suggestions for revision or reasons for rejection

The authors did a very good job improving the quality and significance of the paper. However, there are three points which should be addressed before the paper is ready for publication:

1. I don't understand why ' s_{site} ' has been replaced with ' $S_p \cdot n_{\text{site}}^{-1}$ ' in Equation (3). On the one hand if ' n_{site} ' is smaller than 1 (like in the ISO experiments of FS04), ' $S_p \cdot n_{\text{site}}^{-1}$ ' becomes larger than the total particle surface area available which doesn't make sense. On the other hand, ' n_{site} ' is also included in Equation (4) where the probability of having an active site is multiplied with the probability that the site induces freezing. So it looks like that the usages of ' n_{site} ' in both equations somehow compensate each other as with increasing ' n_{site} ' the nucleation rate ' $J_{\text{het}} = j_{\text{het}} \cdot S_p \cdot n_{\text{site}}^{-1}$ ' for given contact angle decreases while the probability of having an active site increases.

In the original publication of Niedermeier et al., (2014) the active site surface area s_{site} was set equal to S_p/n_{site} under assumption that the total surface available for ice nucleation can be subdivided into n_{site} patches, each of the patches characterized by single value of contact angle (the original SBM setup). The classical "active site" hypothesis, as introduced by Fletcher, does not require the knowledge of s_{site} , rather suggesting a Poisson distribution of active sites over the total particle surface. The scaling of number of sites with total surface area still holds in this case, $n_{\text{site}} \sim S_p$. The total particle surface area per droplet S_p is the only variable here that we know prior to experiments, but neither s_{site} nor n_{site} is known a priori, and therefore n_{site} has been used as a fitting parameter. We have chosen to use S_p/n_{site} instead of s_{site} in a hope to achieve some understanding of how the fit value of n_{site} would behave for different samples and concentration (see also discussion of reviewer #2 comments below). This is a substantial difference from the work of Niedermeier et al., (2015), where the average number of all ice active sites per droplet, λ_{INS} , was measured independently from the plateau values on the freezing curves.

What concerns S_p/n_{site} becoming larger than average total particle surface if $n_{\text{site}} < 1$, that does makes sense from a statistical point of view because a population of droplets is considered, so that s_{site} is an average active site surface area. This is the case where average probability of droplet freezing is below 1.

We have adjusted the relevant sentences in the manuscript to make this clear, as detailed in the responses to the second reviewers' comments.

2. It is mentioned in the text that care should be taken when interpreting the SBM parameters - ' n_{site} ', ' μ ', and ' σ ' - due to the ambiguity of having three adjustable parameters. I agree with this statement in that direction that experimental results as shown in part in your manuscript as well as in others (e.g., Niedermeier et al., 2011) can be represented by different sets of ' n_{site} ', ' μ ', and ' σ '. However, the immersion freezing results of e.g., Augustin et al. (2013) for pollen and Niedermeier et al. (2015) for K-feldspar show that this ambiguity can be reduced because ' n_{site} ' could be directly determined in those experiments and only ' μ ',

and 'sigma' were left for fitting. And for those cases I would say that the values of 'n_{site}' can be interpreted as the average number of active sites per droplet being activated.

Yes, we agree with that (see our response above and the discussion of the second reviewer's comments). In our experiments, however, no plateau has been observed due to the higher amount of ice nucleating material even in the least concentrated suspension droplets. In the limit of low temperatures and low concentrations the n_{site} value becomes n_s^ which can be interpreted as the average number of active sites per droplet.*

3. I don't understand why "a bimodal SBM fit of the entire curve set [...] is clearly outside the scope of this paper"? I agree that the presence of a second active site mode is pretty clear even without a bimodal fit. But reading the manuscript again I would think that such a fit would strengthen the discussion about the bimodal population of active sites. The determined 'mu', and 'sigma' values for the FS04 0.8 wt% concentration should also be valid (or at least be very similar within the range of uncertainty) for the high nucleation efficacy mode of the other, lower concentrations. The only thing that would change, I think, is 'n_{site}' for the high nucleation efficacy mode. However, if the authors still think this topic to be not critical for the paper I would at least suggest to change the FS04 notification in the text and tables by distinguishing between e.g., FS04a (high nucleation efficacy) and FS04b (low nucleation efficacy) or something similar.

We don't see how the fitting of $n_s(T)$ should strengthen the discussion of the bimodal population of active sites, apart of introducing additional numerical uncertainty. With respect to the suggested change of sample naming, we have labeled the physical samples (powders) prior to investigation and we would like to keep the labels conform with the other studies made with the same sample (FS04). The presence of high temperature population of IN active sites become obvious only after conducting isothermal experiments at certain temperature, but of course the sample was still the same.

To make it more clear, we use different labels for the low temperature (FS04L) and the high temperature (FS04H) active sites populations starting from section 5.6.

References:

Augustin, S., Wex, H., Niedermeier, D., Pummer, B., Grothe, H., Hartmann, S., Tomsche, L., Clauss, T., Voigtländer, J., Ignatius, K. and Stratmann, F.: Immersion freezing of birch pollen washing water, Atmos. Chem. Phys., 13, 10989–11003, doi:10.5194/acp-13-10989-2013, 2013.

Niedermeier, D., Shaw, R. A., Hartmann, S., Wex, H., Clauss, T., Voigtländer, J. and Stratmann, F.: Heterogeneous ice nucleation: Exploring the transition from stochastic to singular freezing behavior, Atmos. Chem. Phys., 11(16), 8767–8775, doi:10.5194/acp-11-8767-2011, 2011.

Niedermeier, D., Ervens, B., Clauss, T., Voigtländer, J., Wex, H., Hartmann, S. and Stratmann, F.: A computationally efficient description of heterogeneous freezing: A simplified version of the Soccer ball model, Geophys. Res. Lett., 41(2), 736–741, doi:10.1002/2013gl058684, 2014.

Niedermeier, D., Augustin-Bauditz, S., Hartmann, S., Wex, H., Ignatius, K. and Stratmann, F.: Can we define an asymptotic value for the ice active surface site density for heterogeneous ice nucleation?, J. Geophys. Res. Atmos., 2014JD0228, 2015

Report #2. Suggestions for revision or reasons for rejection

Review of “A comparative study of K-rich and Na/Ca-rich feldspar ice nucleating particles in a nanoliter droplet freezing assay” by A. Peckhaus and Co-authors

The revised version of the manuscript under review here has improved a lot. The language now is fluent, most mistakes have been corrected (the few I stumbled across are given at the end), and that is also true for other technical issues I raised in the first round.

There are, however, still two main topics on which I want to comment, denoted 1) and 2), and the few technical remarks below. After this will have been addressed, this work definitely merits publication in ACP.

1) Concerning the fitting procedures and related conclusions

I respect your choice to not use a single set of values derived for your fitting parameters and test all obtained data against that. But there are still points I want to raise related to the fitting procedure and conclusions you draw from that. This might in parts be similar to some of my original remarks in those cases where I feel there is still room for improvement.

1. - p3, line 7-8: “This behavior was interpreted in terms of a specific average number of ice nucleating sites per particle reaching unity inside the temperature range where the freezing curve starts to level off.” - This is not correctly said here - this NUMBER (!) (of sites) does not reach a value of 1 here (which is what the text says). This needs to be reformulated.

We agree with the reviewer; this statement is incorrect. It now reads: “In the measurements of size-selected K-feldspar (microcline) aerosol particles carried out in the Leipzig aerosol cloud interaction simulator (LACIS) the frozen fraction of droplets containing individual feldspar aerosol particles has been shown to reach a plateau at a value below one well above -38°C (Niedermeier et al., 2015, NIED2015 in the following text). This behavior was explained in a way that some of the droplets contained feldspar particles without a single ice nucleating site.”

2. p3, line 4-5: “... we show that the observed temperature dependence of the INAS surface density is an inherent feature of the experimental method.” - Later in your work you argue that the fit values you obtain are more widely usable and you even use them to draw conclusions for your own work (see below, the two last quotes I took from your paper, before my point 2) starts). This is inconsistent with what you say here, where the impression arises that obtained results will differ for different experimental methods used. As I will discuss below, there is a difference in what you did and how things were done in Niedermeier et al. (2015) which might explain some of your results concerning n_s^* and n_{site} , and your statement here might not be valid if the fit procedure was done as in Niedermeier et al. (2015). Check for that and then be consistent throughout the text when you argue for or against using the values derived from fitting.

According to the reviewer's request we reduce the degree of generalization. The sentence now reads: “We show that the observed temperature dependence of the INAS surface density can be reproduced in the SBM framework using the fit parameters obtained for various feldspar samples.”

3. -p13, line 25-26: “... SBM ... cannot be effectively used to constrain the fitting routine. [new paragraph] The allowed variability of fit parameters can be reduced if we consider that the same IN material has been used in CR experiments with different weight concentrations W .” - The first here mentioned

sentence needs to be reformulated, as it is not the SBM that cannot be effectively used, but instead it is the fact that you did not use as much of the available information as possible, as you then explain in the second sentence quoted here. Instead of “SBM” it would rather be “the subset of input parameters used here”, or something along that line.

Done as requested. The sentence now reads “We conclude therefore that the subset of input parameters used here does capture the observed trend (the less active suspensions exhibit a stronger shift of median freezing temperature) but cannot be effectively used to constrain the fitting routine”.

4. -p14, line 11-14 and p14, line 23-24: “This observation, however, hints that n_{site} should not be treated blindly as a number of active sites activated during the cooling ramp or isothermal freezing, but rather as a number of active sites required by the numerical algorithm to reproduce the freezing curve. Thus, caution should be exercised when interpreting the fit results, as numerical features can be mistaken for physical relationships.” and “... fitting the freezing curves with a three adjustable parameter fit without providing additional constraint does not necessarily lead to a better understanding of IN nature.” - To my understanding, there is a big difference in your data set and that by Niedermeier et al. (2015), a paper you relate to quite a bit. While frozen fractions you measure always reach 1, this is not the case in Niedermeier et al. (2015). There, the amount of material (or better surface area) per droplet is so small, that (statistically) droplets exist that contain a particle that does not have an ice active site at all. This leads to a temperature region where measured frozen fractions do not increase with decreasing temperature and a plateau forms at values for frozen fractions < 1 . *From this region and the assumption of a Poisson distribution, an average number of ice nucleating sites per droplet (λ) is derived.* This is not a fit factor but a value that could be determined, but it cannot be determined from your data set, as your droplets contained so much material that a plateau in frozen fractions < 1 was not seen. Niedermeier et al. (2015) then relate λ to n_{s}^* (see their equation 7), and n_{s}^* therewith is a particle property, the way it was defined. You vary n_{s}^* (maybe because you cannot constrain it from a plateau?) and then, based on that, obtain varying n_{site} values which you then judge non-meaningful in a physical sense. To my understanding, this originates in the fact that you cannot see a plateau in frozen fractions < 1 , and hence you have one constrain less than Niedermeier et al. (2015). *So your judgements I quoted above and related remarks in your manuscript are valid for your data set (and similar ones which do not observe the plateau), but not in general.* This needs to be rephrased throughout your text, including the two sentences I quoted here.

The reviewer is absolutely correct here and we want to thank the reviewer for pointing this out so clearly. The droplet assay methods do not allow direct measurements of λ_{INS} in a plateau region. We therefore have to use n_{site} as an adjustable parameter instead (compare equation 3 in Niedermeier 2015 and our equation 3). The variation of n_{s}^ is provided via the relationship $n_{\text{s}}^* = n_{\text{site}}/S_{\text{p}}$ in the limit of $P_{\text{unfr}} = 0$.*

Our $n_{\text{s}}^ = n_{\text{site}}/S_{\text{p}}$ becomes analogue of $n_{\text{s}}^* = \lambda_{\text{INS}}/S_{\text{p}}$ of Niedermeier 2015 in the limit of low particle surface per droplet (low concentration and small particle size). Indeed, our apparent value of n_{s}^* is equal to $\lambda_{\text{INS}}/S_{\text{p}}$ if surface area of 500 nm particle is used for S_{p} (the blue broken line in the figure 9). That actually means that it might be possible to predict where a plateau would appear on the freezing curve in the single particle-per-droplet-experiment (as in LACIS instrument) using the fit parameters obtained in our droplet freezing assay study.*

We therefore have removed the first sentence mentioned in this comment and modified the second one to make it clear why in our case the n_{site} cannot be set equal to the average number of site per droplet at any temperature and concentration.

We have added the following paragraph to the theoretical section (2), page 5 lines 21 to 29: “It has to be pointed out that there is a substantial difference between the parameterization scheme of Niedermeier et. al., (2014, 2015) and the one used in this work. In the study of Niedermeier et al., (2015) the feldspar particles in the droplets were so small, that some droplets contained no ice active sites at all. This leads to a temperature region where measured frozen fractions do not increase with decreasing temperature and a plateau forms at values for frozen fractions below one. From this region and assuming the Poisson distribution of the number of ice active sites per droplet, the average number of ice nucleating sites λ_{INS} could be directly determined (Hartmann et. al., 2013, Niedermeier et. al., 2015). This value was then used in place of the n_{site} in equation (3), thus reducing the number of fitting parameters from three to two. In our case, the value of λ_{INS} could not be determined from the experimental data and therefore n_{site} had to be used as an additional fitting parameter.

5. -p16, line 13ff: Again, as I understand, n_{s^*} at least as defined in Niedermeier et al. (2015) is a particle property, which, however, you cannot obtain from your data set and need to use as an additional free parameter. n_{s^*} in Niedermeier et al. (2015) was obtained for the lowest temperatures at which frozen fractions were observed to not increase further upon further cooling. But you say here “further increase of the IN active site efficiency ... would not result in the further increase of the freezing probability”. This makes sense as the freezing probability is already 1, as you nicely explain in the beginning of this paragraph. So I do not see how you can judge from that that n_{s^*} is a suspension property, as suspensions with higher concentrations will cause all droplets to freeze above the temperature range where the plateau is observed. However, there is an effect of time (as you observed yourself), and the short time for LACIS (1.6 seconds is what you used) is much faster than your own cooling rate, so would this not explain some of the discrepancy observed in Fig. 9?

You are right, the correct statement would be that n_{s^} is the “suspension droplet property”, because it depends on the asymptotic n_{site} and on the size of the droplet (for a given concentration). But keeping both droplet size and the number of IN active sites per droplet constant, the variation of contact angle would not change the value of n_{s^*} .*

6. -p17, line 24ff: Starting with “Multiplying the n_{s^*} ...” - here you do use the plateau seen for the highly active fraction to derive that ~ 30% of all droplets contained one of the high temperature active sites, using this to draw further conclusions. I totally agree with you doing it this way, but to do this, you have to trust the derived n_{s^*} value, which, it seems, you repeatedly recommend not to do (see quotes from your text above).

We have modified the preceding discussion in attempt to avoid this contradiction.

7. p21, line 23-24: “The asymptotic active site density n_{s^*} , achieved by $n_s(T)$ as the freezing probability of every droplet in the ensemble approaches unity, can be interpreted as a method independent property, inherent to the suspension only. Together with the mean value of contact angle, this asymptotic value provides a basis for the parametrization of IN properties that is required within the atmospheric modeling.” - Again, I agree with this, but this does not fit to what you said on that topic in your manuscript (see the quotes from your text above).

See previous comment.

2) Concerning the presence of organic contaminations

First of all, I wonder about the number you give for the mass concentration of active sites you estimate for you sample: if 1/3 or all droplets contain such a site, and the mass of feldspar per droplet is $1.2 \cdot 10^{-8}$ g, wouldn't it be that there is one site in $\sim 1/3 \cdot 1.2 \cdot 10^{-8}$ g = $7 \cdot 10^{-8}$ g, the reciprocal of which is $1.4 \cdot 10^7$ /g. This latter

value, to my understanding, is the mass concentration of active sites, or am I wrong? Your value is a factor of 50 higher, and I wonder where the discrepancy comes from.

Well, the reciprocal of $0.29 \cdot 1.2 \cdot 10^{-8} \text{ g}$ is equal to $2.874 \cdot 10^8 \text{ g}^{-1}$, please check your calculations.

Also, when you then turn to polysaccharides and argue that your sample would have had to be comprised of 10% polysaccharides, you are still “comparing apples with oranges”. Of the ~10% of biological material that was estimated to be present in the new publication you consult here now (Augustin-Bauditz et al., 2016), only a VERY minor fraction of all organic material makes up the ice active polysaccharides (and that fraction might strongly depend on the sample). To cite Augustin-Bauditz et al., 2016: “The size of a single INM was estimated to be 10 nm”. From this (assuming a spherical shape and a density of 2 g/cm^3), one ice active polysaccharide has a mass of $\sim 10^{-18} \text{ g}$. This, together with the concentration of ice active molecules you derived (n_m of $5 \cdot 10^7 / \text{g}$) leads to $\sim 5 \cdot 10^{-11} \text{ g}$ polysaccharides per gram of your sample. This is clearly not 10%, and I would even argue that such a contamination is not visibly detectable.

Admittedly, these ice nucleating polysaccharides might not occur on their own but be related to some additional (organic) material, but there is room for quite some more organic material that could be there before it would become visible.

To summarize this: please check/ correct the values you give in the text and rewrite the text accordingly (some of your arguments won't hold, unless I miscalculated something above). And I understand that you do not want to rule out the possibility that there might be a VERY active mineral dust site on the feldspar, but I still recommend to tune down the statements concerning the possibility of biological contamination. (E.g.: Abstract, page 2, line 1: replace “has been ruled out” by “might be unlikely”; page 22, line 10: Replace “found to be too high to be explained by surface contamination ...” with something more suitable (see my estimates above); and check for other occurrences and rewrite where necessary).

We agree that the argument concerning 10% of organic contamination does not strictly hold and it has been removed from the discussion. The comparison with fertile soil and Illite – BPWW mixtures is at very least illustrative, as both systems have been shown to exhibit enhancement of the IN efficacy due to the presence of organic components, but have lower mass concentration of high temperature active sites compared to FS04. Additionally, the value of contact angle obtained from the SBM fit for the high temperature active sites is also significantly lower than the value obtained for BPWW (0.56 for FS04H vs 0.83 for BPWW).

Since our calculations of mass concentration of active site are correct, we prefer to keep the numbers as a basis for future discussions. As suggested, we tune down the statements concerning the possibility of biological contamination.

The sentence in the abstracts now reads: “Given a high mass concentration of these high temperature active sites ($2.9 \times 10^8 \text{ g}^{-1}$) and a very low value of contact angle (0.56 rad) the possibility of biological contamination of the sample was concluded to be unlikely but could not be completely ruled out.”

The conclusion section has been modified accordingly: “The number of high temperature active sites per mass of feldspar ($n_m = 2.9 \times 10^8 \text{ g}^{-1}$) was found to be two orders of magnitude higher than the mass concentration of ice active sites in fertile soil (O’Sullivan et al., 2014), and almost an order of magnitude higher than the mass concentration of ice active sites in mixture of illite NX with birch pollen washing water (BPWW, Augustin-Bauditz et al., 2016). Based on this comparison and values of μ_θ , we argue that biological nature of high temperature active sites is unlikely but their nature could not be uncovered in this study.”

Technical comments

Abstract line 20-21: This sentence seems to have a “copy-paste-error”: “..., the parameter space can be constrained the unique sets of model parameters for specific feldspar suspensions can be derived.” – Rephrase

Done as requested

page 4, line 15: Replace “In this framework, of this” with “In the framework of this”

Done as requested

page 11, line 8: Add “a” between “occurred at” and “lower temperature”.

Done as requested

page 11, line 25: Replace “... suspension. The ...” by “suspensions, the ...”

Done as requested

page 15, line 4: I wonder to what the curves were identical. I assume you mean “The fit parameters that provided the best fit of THE DIFFERENT liquid fraction decay curves were identical.”? If yes, please add “the different”.

Done as requested

page 18, line 3: You say “... these sites will be detectable only in concentrated suspensions and setups.” - This is in contradiction with the fact that multiple types of sites were seen for size segregated measurements for some samples in the past (you cited some respective papers in the sentence before), so your statement is only true if the sites occur only very infrequently. I suggest starting this sentence with: “When some types of sites occur only very infrequently, their presence will be detectable only”

Agreed, the sentence modified accordingly.

A comparative study of K-rich and Na/Ca-rich feldspar ice nucleating particles in a nanoliter droplet freezing assay

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Abstract. A recently designed droplet freezing assay was used to study the freezing of up to 1500 identical 0.2 nL water droplets containing suspensions of one Na/Ca-rich feldspar and three K-rich and one Na/Ca-rich feldspar particles. Three types of experiments have been conducted: cooling ramp, isothermal freezing at a constant temperature, and freeze-thaw cycles. The observed freezing behavior has been interpreted with the help of a model based on the classical nucleation theory (Soccer Ball Model, SBM, Niedermeier, 2015). By applying the model to the different freezing experiments conducted with the same ice nucleating (IN) material, the unique sets of model parameters for specific feldspar suspensions could be derived. The SBM was shown to adequately describe the observed cooling rate dependence, the ice nucleating active sites (INAS) surface density $n_s(T)$ in a wide temperature range, and the shift of the freezing curves towards lower temperature with dilution. Moreover, the SBM was capable of reproducing the variation of INAS surface density $n_s(T)$ with concentration of ice nucleating particles in the suspension droplets and correctly predicting the leveling-off of $n_s(T)$ at low temperature. The freeze-thaw experiments have clearly shown that the heterogeneous freezing induced even by very active ice nucleating species still possesses a stochastic nature, with the degree of randomness increasing towards homogeneous nucleation.

A population of the high temperature INAS has been identified in one of the K-rich feldspar samples. The freezing of 0.8 wt % suspension droplets of this particular feldspar was observed already at -5°C . These high temperature active sites could be deactivated by treating the sample with hydrogen peroxide but survived heating up to 90°C . Given a high mass concentration of these high temperature active sites ($2.9 \times 10^8 \text{ g}^{-1}$) and a very low value of contact angle (0.56 rad) the possibility of biological contamination of the sample was concluded to be unlikely but could not be completely ruled out. The freezing efficacy of all feldspar samples has been shown to reduce only slightly after suspension in water for over 5 months.

1 Introduction

Atmospheric aerosol particles influence the radiation budget of the Earth due to their absorption and scattering properties, they act as cloud condensation nuclei (CCN) due to the aerosol-cloud-interaction and promote ice formation in precipitation processes (Pruppacher and Klett, 2004). It is assumed that the formation of precipitation at mid-latitudes proceeds predominantly via the ice phase (Baltensperger, 2010). A solid ice nucleating particle (INP) is needed to trigger heterogeneous ice nucleation. For a quantitative description of heterogeneous ice nucleation, the concept of ice nucleation active site (INAS) surface density was introduced in order to assess the ice nucleating (IN) efficiency of aerosol particles, regardless of the experimental measurement conditions (Connolly et al., 2009). The ability of aerosol particles to act as INP strongly depends on the material and the freezing mode (Hoose and Möhler, 2012). Especially mineral dust particles like kaolinite (Wex et al., 2014), illite (Hiranuma et al., 2014) and feldspar (Atkinson et al., 2013, denoted ATK2013 from now on) were identified as efficient INP showing high INAS surface density in a particular temperature range.

Although a large amount of the earth's crust consists of feldspar mineral (~51%, Ronov and Yaroshevsky, 1969) only a minor fraction (~13% according to B. J. Murray et al., 2012) of this primary mineral contributes to the mineral-containing atmospheric aerosol particles. In particular, field campaigns showed that the mass fraction of K-feldspar collected on filter substrates in Taifou (Morocco) was 10 wt% in dust storm and 25 wt% in low-dust conditions (Kandler et al., 2009). Similar results were observed at Cape Verde with 20 wt% ("dust period") and 25 wt% ("maritime period"). These field campaigns have been carried out in the vicinity of the Sahara Desert and may exhibit strong gradients of particle concentration with distance from the source (Nickovic et al., 2012). Mineral dust particles collected in Asia contained 11 wt% Na/Ca-rich feldspar and 8 wt% of K-rich feldspar (Jeong, 2008).

Despite their low mass abundance feldspar particles could play a crucial role in ice nucleation due to the fact that the freezing properties of a particle ensemble can be dominated by INPs exhibiting the highest ability to initiate ice formation. Up to now, feldspar was studied with various experimental methods and in different freezing modes.

Deposition ice nucleation experiments carried out in an environmental scanning electron microscope (ESEM) have shown that K-rich feldspar (microcline) had the lowest onset freezing temperature and supersaturation with respect to RH_{ice} (onset RH_{ice} : 105% at $-12^{\circ}C$, Zimmermann et al., 2008). In contrast, RH_{ice} for Na/Ca-rich feldspar (albite) showed only a weak temperature dependence, whereas K-feldspar exhibited an increase of onset RH_{ice} with decreasing temperature. Diffusion chamber experiments have led to the conclusion that K-feldspar (orthoclase) is an effective deposition INP at a temperature of $-40^{\circ}C$ (ice nucleation onset observed at $135.0\% \pm 3.6\%$ at the threshold of 0.1% of ice activated particles, Yakobi-Hancock et al., 2013).

In a number of droplet freezing assay experiments (ATK2013; Whale et al., 2015; Zolles et al., 2015), K-feldspar particles have been investigated in the immersion freezing mode. It was found that K-feldspar particles initiate freezing at higher temperatures than any other mineral dust particles. It was hypothesized that the fraction of K-feldspar in natural mineral dusts samples correlates with the ice nucleation efficiency (ATK2013). [In the measurements of size-selected K-feldspar](#)

(microcline) aerosol particles carried out in the Leipzig aerosol cloud interaction simulator (LACIS) the frozen fraction of droplets containing individual feldspar aerosol particles has been shown to reach a plateau at a value below one and at a temperature well above -38°C (Niedermeier et al., 2015, NIED2015 in the following text). This behavior was explained in a way that some of the droplets contained feldspar particles without a single ice nucleating site.

Na/Ca-feldspar particles studied with a Cold Stage/Raman microscope setup featured high ice activity in both deposition and immersion freezing modes, presumably due to the presence of K-feldspar impurities (Schill et al., 2015).

Several experiments addressed the influence of ageing on the ice nucleation efficiency of feldspar particles. Chemical treatment with sulfuric acid was shown to cause a reduction of ice activity of K-feldspar particles depending on the coating conditions (Augustin-Bauditz et al., 2014; Kulkarni et al., 2014). The ice activity of aged K-feldspar was similar to other chemically treated minerals, i.e., Arizona test dust (ATD), kaolinite and illite NX. Mechanical milling of K-feldspar particles caused a slight increase in their ice activity, while enzymatic treatment significantly reduced their ice activity probably due to blocking of ice active sites (Zolles et al., 2015). Subsequent heating led to a restoration of the ice nucleation efficiency. Zolles et al. (2015) found indications “that the higher IN efficiency of the K-feldspar sample is an intrinsic property and not a result of adsorbed organic/biological material”.

Laboratory studies of ice nucleation of feldspar in condensation and contact freezing mode are scarce. In particular, condensation freezing experiments conducted in the Manchester ice cloud chamber (MICC, Emersic et al., 2015) fall tube have shown the temperature dependence of n_s values being less steep compared to the immersion freezing experiments reported in ATK2013. In contact freezing experiments, K-feldspar particles have shown IN efficiency comparable to that of ATD and rhyolitic ash in the same temperature range (Niehaus et al., 2014). Note that in this study the particle size distribution was rather broad and therefore the results should be interpreted with caution.

In spite of accumulating evidence of the importance of K-feldspar for the atmospheric ice nucleation, systematic studies of natural feldspars are yet rare. Recently we have developed an apparatus capable of measuring freezing of several hundred identical nanoliter droplets of mineral dust suspensions in both steady cooling and constant temperature regimes. This work is the first attempt to use this apparatus for a comprehensive characterization of several feldspar samples and assessment of stochastic vs. singular nature of ice nucleation induced by a highly effective ice nucleator. As will be shown below, a low variability of droplet size and concentration, a large number of individual droplets, an automatic control of individual droplet freezing time and temperature used in our instrument improves the experimental statistics and allows for parameterization of freezing efficiency of feldspar based on the classical nucleation theory.

This manuscript is organized as follows: In the methods section, the experimental setup and the model approach based on a so- called Soccer Ball Model (SBM, Niedermeier et al., 2011b, 2014, 2015) are described, followed by characterization of four feldspar samples (K-rich and Na/Ca-rich feldspar). In section 5 we present the results of cooling ramp experiments (CR), isothermal freezing experiments (ISO), and freeze-thaw cycle experiments. We show that both temperature and time dependent freezing behavior of selected feldspar samples can be described with the unique sets of fit parameters within the

SBM approach. We show that the observed temperature dependence of the INAS surface density can be reproduced in the SBM framework using the fit parameters obtained for various feldspar samples. Section 6 discusses the influence of aging and chemical treatment of feldspar. The concluding section is focused on the concentration and cooling rate/time dependence of immersion freezing of feldspar suspension droplets, discussed from the point of view of both singular and stochastic ice nucleation active sites hypotheses.

2 Theoretical background

The parametric description of heterogeneous ice nucleation is based either on the stochastic or singular hypothesis (Niedermeier et al., 2011b; Vali, 2014). The stochastic approach assumes that a critical ice cluster needs to be formed before the freezing of the entire droplet can proceed. The heterogeneous IN causes a lowering of the ice germ formation energy and therefore enhances the probability of ice nucleation. For a given supercooling temperature, the probability of freezing event is a function of nucleation rate and time. In contrast, the singular approach assumes that the ice nucleation occurs on the specific active sites of the IN immediately as soon as a characteristic temperature has been reached (Fletcher, 1969). In the framework of this approach the ice nucleation probability is independent of time. Besides these two extremes, there exist several approaches that try to bridge the gap. In more detail, the time-dependent freezing rate (TDFR) model combines assumptions of the singular approach with a cooling rate dependence (Vali, 2014), multicomponent stochastic models make use of a simple linear expression of the temperature dependence of nucleation rate coefficient (Broadley et al., 2012) and classical nucleation theory (CNT) based approaches use a distribution of active sites or contact angles to represent the variability in ice nucleation behavior (Marcolli et al., 2007; Niedermeier et al., 2011b).

Assuming the singular hypothesis, the ice nucleation active site (INAS) surface density as a function of temperature $n_s(T)$ can be expressed via the fraction of frozen droplets $f_{ice}(T)$ and the surface area S_p of INPs per droplet (Connolly et al., 2009; Niemand et al., 2012):

$$n_s(T) = -\frac{\ln(1-f_{ice}(T))}{S_p} \quad (1)$$

The total particle surface area is either derived from surface area distributions or calculated from the mass of particles per droplet multiplied by the Specific Surface Area measured with BET approach (BET-SSA, Brunauer et al., 1938).

In this work we use the simplified version of SBM (Niedermeier et al., 2014, 2015) to show that both cooling ramp and isothermal experiments can be parameterized with a single set of CNT-based fit parameters. The approach is based on the assumption, that each droplet contains *on average* a number n_{site} of IN active sites, their IN efficiency being characterized by the normally distributed contact angles θ . The distribution $p(\theta)$ is described by a mean contact angle μ_θ and standard deviation σ_θ . In this case, the probability P_{unfr} of a single suspension droplet to remain liquid after time t at given supercooling temperature T is given by

$$P_{unfr}(T, \mu_\theta, \sigma_\theta, t) = \int_{-\infty}^{+\infty} p(\theta) \exp(-J_{het}(T, \theta) S_p n_{site}^{-1} t) d\theta \quad (2)$$

Where $J_{het}(T, \theta)$ is the freezing rate coefficient at given temperature T and contact angle θ , and S_p is the total particle surface area per droplet (Pruppacher and Klett, 2004; Vali, 1999). Note that although $\theta \in [0, \pi]$ the integration is carried out on the interval $[-\infty, +\infty]$ to account for the continuity of a Gaussian probability distribution function $p(\theta)$. Outside of the $[0, \pi]$ interval, θ is set to either 0 or π . Assuming the Poisson distribution of active sites between the droplets, the fraction of frozen droplets f_{ice} after time t can be calculated:

$$f_{ice} = 1 - \exp \left[-n_{site} \left(1 - P_{unfr}(T, \mu_\theta, \sigma_\theta, t) \right) \right] \quad (3)$$

In case of CR experiments, the cooling rate $c = dT/dt$ has to be introduced to relate the temperature and time: $T = T_{start} + ct$, where T_{start} is the start temperature of the cooling ramp (typically 273 K). The parameters n_{site} , μ_θ and σ_θ can be obtained by fitting the Eq. (3) to the experimentally measured fraction of frozen droplets as a function of freezing temperature (in CR experiments) or freezing times in ISO experiments. As in Niedermeier et al., (2014), the parameterization of relevant thermodynamic quantities has been adopted from (Zobrist et al., 2007). The goodness of fit is described by the correlation coefficient r^2 .

It has to be pointed out that there is a substantial difference between the parameterization scheme of Niedermeier et al., (2014, 2015) and the one used in this work. In the study of NIED2015 the individual feldspar particles in the droplets were so small (500 nm and below), that some droplets contained no ice active sites at all. This leads to a temperature region where measured frozen fractions do not increase with decreasing temperature and a plateau forms at values for frozen fractions below one. From this region and assuming the Poisson distribution of the number of ice active sites per droplet, the average number of ice nucleating sites λ_{INS} could be directly determined (Hartmann et. al., 2013, NIED2015). This value was then used in place of the n_{site} in equation (3), thus reducing the number of fitting parameters from three to two. In this study, the value of λ_{INS} could not be determined from the experimental data and therefore n_{site} was used as a fitting parameter together with μ_θ and σ_θ .

Equation 3 can be used to explore the relationships between the apparent fraction of frozen droplets and material properties, the later described as a combination of μ_θ and σ_θ . Since the experimental parameter (particle number or mass per droplet) is represented by n_{site} , this equation provides also a basis for comparison between experiments conducted with the same material but under different experimental conditions (different droplet size and particle concentration). Moreover, it can be used to explore the relationship between the median freezing temperature and the cooling rate, which is often referred to as an indicator of either the stochastic or singular description of ice nucleation.

The INAS surface density can be derived from the CNT-based parameterization by substituting Eq. (3) into (1):

$$n_s(T) = \frac{n_{site}}{s_p} \left(1 - P_{unfr}(T, \mu_\theta, \sigma_\theta, t) \right) \quad (4)$$

5 This relationship is very helpful to understand the apparent behavior of the $n_s(T)$ curves obtained directly from the measurements via Eq. (1), as discussed below.

3 Methods

3.1 Experimental setup

10 The central part of the experimental setup is a cold stage (Linkham, Model MDBCS-196), which was used to carry out the cooling ramp and isothermal experiments (Fig. 1). Cooling is achieved by pumping liquid nitrogen from a reservoir through the copper sample holder. The cold stage can operate in the temperature range from 77 K to 400 K. Controlled heating and cooling ramps can be performed at rates between 0.01 K/min to 100 K/min. The temperature stability is better than 0.1 K.

15 A single crystal silicon substrate (Plano GmbH, 10×10 mm) was first cleaned with high grade acetone (p.a.), then rinsed several times with NanoPure water (Barnstead Thermolyne Corporation, Infinity Base Unit, 18.2 MΩ/cm). Finally, the silicon wafer was purged with nitrogen to remove residual water. This silicon wafer was then mounted into a square depression in the sample holder. A surface prepared in this way induces freezing of pure water droplets only at temperatures very close to the temperature of homogeneous freezing of water, as discussed below in section 5.2.

20 The feldspar suspensions were prepared by adding the feldspar powder into 25 mL of NanoPure water and stirred for an hour. A piezo-driven drop-on-demand generator (GeSIM, Model A010-006 SPIP, cylindrical case) was used to print individual suspension droplets in a regular array onto the silicon substrate. Before dispensing, the substrate was cooled to the ambient dew point to reduce the evaporation of droplets. Up to 1500 suspension droplets of (215 ± 70) pL volume were deposited onto the silicon wafer resulting in droplets with (107 ± 14) μm diameter in spherical cap geometry with contact angle of $74^\circ \pm 10^\circ$. After printing, the droplet array was covered with silicone oil (VWR, Rhodorsil 47 V 1000) to prevent evaporation
25 and any eventual interaction between the supercooled and frozen droplets. Measurements of the droplet geometry and volume are described in the Supplement.

The temperature of the droplets was measured with a calibrated thin film platinum resistance sensor (Pt-100) that was fixed directly on the surface of the silicon substrate by a small amount of heat conducting paste (vacuum grade) as shown on the inset of Fig. 1. The Pt-100 sensor was calibrated against a reference sensor in the temperature range from -40°C to +30°C
30 prior to the experiment. The single point temperature measurement error was estimated to be ± 0.1 K.

A charge-coupled device (CCD)-camera (EO progressive) with a wide field objective (DiCon fiberoptics Inc.) was used to record the freezing of the suspension droplets. The substrate is illuminated by a ring light source mounted around the objective lens. Two polarizers (one in front of the light source and one in front of the objective) were used to enhance the brightness of the frozen droplets compared to the liquid ones. Video- and temperature recordings of the cooling and freezing process were taken at a frame rate of 1 to 8 frames per second (fps), allowing for identification of individual freezing events with time resolution of 0.125 to 1 s and 0.1 K temperature accuracy. Freezing of individual droplets can be recognized by a pronounced increase of the light scattered from the frozen droplets (detected through the crossed polarizer in front of the objective lens). An automated video analysis routine allows for extraction of the fraction of frozen droplets as a function of temperature from the raw data. Subsequent data processing with a LabView routine allowed for calculation of a fraction frozen vs. temperature curve.

3.1.1 Cooling ramp experiments

Two types of freezing experiments have been performed with this experimental setup: In cooling ramp (CR) experiments, the temperature is linearly reduced with a constant cooling rate. Cooling ramp experiments from 273K to 233K were performed at three different cooling rates $c = dT/dt$ (-1 K/min, -5 K/min and -10 K/min) and the fraction of frozen droplets f_{ice} was recorded as a function of temperature with 0.1 K resolution. After each CR experiment, the substrate was heated to 274 K until every droplet has melted. In this way, the same sample can be used for several repeated CR experiments, allowing correlation analysis of subsequent freezing runs.

3.1.2 Isothermal experiments

In isothermal (ISO) experiments (also known as temperature jump experiments), the temperature is reduced rapidly via initial ramp (cooling rate from -5 K/min to -10 K/min) to a pre-set value and then held constant for about an hour, during which the individual droplet freezing times are recorded continuously. The set point temperature was chosen such that a maximum of 25% of the droplets froze during the initial cooling ramp. These types of experiments addresses both the influence of temperature and time on the ice nucleation process of feldspar particles immersed in water droplets.

4 Materials

4.1 Feldspar samples

The feldspar samples FS01, FS04 and FS05 were provided by the Institute of Applied Geosciences, Technical University of Darmstadt (Germany) and the feldspar sample FS02 was provided by the University of Leeds (UK). Samples FS01, FS04 and

FS05 have been prepared by ball milling of single crystal mineral specimens. FS02 is the standard BCS 376 from the Bureau of Analysed Samples, UK. All samples were studied during the Fifth International Ice Nucleation (FIN) measuring campaigns at AIDA cloud chamber in the framework of the Ice Nucleation Research Unit (INUIT) project of German Research Foundation (DFG, see Acknowledgements) and the name convention has been preserved for consistency with the future publications. Table 1 gives an overview of the investigated feldspar samples.

4.1.1 Sample preparation for chemical ageing experiments

To assess the effect of ageing on the IN activity, the feldspar particles (FS01 und FS05) were left in water for over five months and the supernatant water was exchanged several times. Extreme care has been taken to avoid any contamination as a consequence of water exchange. The concentration of exchanged cations (K^+ , Na^+ , Ca^{2+} , Mg^{2+}) have been measured regularly during the first month (see Supplement). For the cooling ramp experiments, the feldspar particles were centrifuged (Thermo scientific, 2000rpm for 20min), dried and re-suspended in 25 mL NanoPure water. Alternatively, fresh suspensions of feldspar (FS04) particles were heated to approximately $+90^{\circ}C$ for over an hour. Additionally, the FS04 feldspar sample has been suspended in 100 mL hydrogen peroxide aqueous solution (AppliChem GmbH, 30% p.a.) at $+65^{\circ}C$ and stirred for an hour or kept in hydrogen peroxide solution at room temperature overnight.

4.2 Morphology and particle surface area

An environmental scanning electron microscope (ESEM FEI, Quanta 650 FEG) was used to record images and energy dispersive X-ray (EDX) spectra of individual feldspar particles deposited on graphite and silicon substrates. For each sample, over one hundred individual spectra have been recorded for the individual particles separated by at least $10\text{ }\mu m$ from other particles or agglomerates. The program Esprit 1.9 (Bruker) was used to quantify the chemical composition of the feldspar samples. SEM images of feldspar particles showed agglomerates consisting of several large rocky particles with the smaller particle fragments on their surface (Fig. 2). With respect to their morphology, both individual feldspar particles within a single sample, and those particles from different feldspar samples were very similar. The wide field images have been used to assess the size of the individual particles and to derive the average total particle surface area S_p contained by a single suspension droplet (see supplementary Fig. S1). An example of the size distribution of FS02 residual particles deposited on silicon substrate is given in the Supplement (Fig. S2), and is in good agreement with the size distribution determined by laser diffraction method for the sample FS02 (ATK2013).

The specific surface area (also often referred to as BET surface area, S_{BET}) has been measured with N_2 gas adsorption technique following the Brunauer-Emmett-Teller method (BET, Brunauer et al., 1938). The S_{BET} of feldspar samples ranged from 1.79 to $2.94\text{ m}^2/g$ (Table 1) which is lower than the BET surface areas reported by ATK2013, ($3.2\text{ m}^2/g$ for FS02 and $5.8\text{ m}^2/g$ for Na/Ca feldspar particles respectively) and slightly higher than the BET surface area reported by (Schill et al., 2015) ($1.219\text{ m}^2/g$ for Na/Ca feldspar particles). The BET surface area was then used to calculate the

“gravimetric” particle total surface area using the relationship $S_p = W \cdot V_{drop} \cdot S_{BET}$, which accounts for the weight concentration of feldspar, W . Both methods delivered similar values of S_p , as demonstrated in Fig. S2.

4.3 Mineral composition

5 The mineralogical composition of the bulk samples FS01, FS04, and FS05 was determined by X-ray powder diffraction analysis (XRD). Relevant measurement parameters are shown in Table 1. Identification of the mineral phases was performed using the ICDD Database (ICDD, 2002).

The ternary phase diagram derived from EDX measurements of individual feldspar particles shows that particles of FS01, FS02 and FS04 have a similar chemical composition close to the end member microcline/orthoclase (Klein and Philpotts, 2013) (Fig. 3a). The compositional distributions of FS01 and FS02 are nearly overlapping, but some particles richer in sodium and calcium were observed. The composition of FS04 was slightly closer to the end member microcline/orthoclase. Iron as a trace component was found in individual EDX spectra of FS02 and FS04, which can probably originate from trace impurities of aegirine (member of sodium pyroxene group) known to form in the alkaline igneous rocks also responsible for the formation of alkali feldspars (Deer et al., 1978), as in the region of Mount Malosa in Malawi. Note that the EDX spectra were measured on a single particle basis and therefore do not represent the weight average composition of the entire sample. The composition of the agglomerates may differ from that of the individual particles. In accordance with the solid solution series of plagioclase, the majority of FS05 particles are situated in the region of andesine (intermediate plagioclase, 30-50% anorthite, Klein and Philpotts, 2013) (Fig. 3b). However, individual particles were richer in sodium and closer to the end member albite. Based on the analysis of individual EDX spectra, the Al:Si ratio was found to be very close to 1:3. This ratio varies from 1:3 for albite to 2:2 for anorthite (end member of the plagioclase solution series). The EDX spectra of size selected FS05 particles (300 nm mobility diameter) do not significantly differ in their composition from larger coarse-grained particles. We therefore suggest that the FS05 sample predominantly consists of albite with minor heterogeneous inclusions of andesine. The observed steady rise of Ca^{2+} and Na^{+} concentration measured in the suspension over the period of four weeks supports this conclusion (see Supplement). In the following, we refer to FS05 as a “Na/Ca-rich feldspar” and to FS01, FS02 and FS04 samples as “K-rich feldspar”. Overall, the EDX results mainly confirmed the composition of feldspar samples derived from XRD analysis (see Table 1).

5 Results and discussion

5.1 Freeze-thaw cycle experiments

To investigate the repeatability of droplet freezing, freeze-thaw cycle experiments with identical cooling rates have been performed. Every individual droplet has been assigned a rank number according to its freezing time in two successive CR

experiments, with rank number 1 corresponding to the first droplet frozen and so on. The pairs of rank numbers of the individual droplets have been plotted on a 2D coordinate grid as shown in the Fig. 4. Droplets that have evaporated in the second temperature ramp experiment or could not be detected automatically were excluded from consideration. A perfect correlation between rank orders in two cycle experiments would imply that every droplet froze exactly at the same temperature in both CR runs. On the other hand, no correlation between the freezing rank numbers would imply statistically independent freezing events or very steep temperature dependence of the heterogeneous nucleation rate coefficient (if the freezing times of individual droplets could not be distinguished within the time resolution of the video camera).

For NanoPure water droplets on a cleaned silicon wafer substrate, no correlation between the ranking order of freezing events could be observed, as shown by Pearson's r coefficient equal to 0.14. However, a small fraction of droplet population near the beginning of a cooling cycle (Fig. 4a) showed local increase of correlation, which could probably be associated with contamination of the silicon wafer or impurities in the water or in the silicon oil. The freezing of these contaminated droplets is also visible as a flat shoulder on the warm side of the frozen fraction curve for NanoPure water in the Fig. 5.

For concentrated FS01 suspensions, a higher correlation of freezing events was observed ($r = 0.89$, Fig. 4c). FS05 suspensions showed a lower correlation coefficient ($r = 0.8$, Fig. 4b). The highest correlation coefficient was obtained for concentrated FS04 suspensions ($r = 0.92$, Fig. 4d).

We have also performed freeze-thaw experiments with FS01 and FS02 samples in four different concentrations (0.8 wt%, 0.1 wt%, 0.025 wt%, and 0.01 wt%), but have not observed a clear relationship between the correlation coefficient and concentration.

These results suggest that the correlation coefficient is related to the IN efficiency of the suspension material. INPs initiating freezing at a lower temperature also showed a lower correlation coefficient, while more efficient INPs initiating freezing at a higher temperature, and in a narrower temperature range, showed higher correlation coefficients. A similar conclusion was drawn for the ice nucleation of collected rainwater samples (Wright et al., 2013). Therein, a slight decrease of standard deviations of the median freezing temperatures at higher temperatures (i.e. reduced cooling rate dependence) has been reported. In the work of Campbell et al., (2015) a correlation plot was used for the characterization of silicon substrates roughened with diamond powder. It could be demonstrated that there was a strong correlation between freezing ranks of droplets in successive cooling runs on the scratched silicon substrates. Similar experiments, investigating the repeatability of freezing temperatures of single droplets of distilled water and two soil dust samples were carried out with a microliter droplet freezing assay (Vali, 2008). The derived Spearman rank correlation coefficients for pairs of runs were higher than 0.9, indicating a high repeatability of freezing temperatures. The standard deviation of the mean freezing temperature, evaluated from the freeze/thaw cycle experiments on individual droplets containing ATD (Wright et al., 2013), soil dust (Vali, 2008) and Nonadecanol (Zobrist et al., 2007) was found to be less than 1 K. For volcanic ash (Fornea et al., 2009) and black carbon (Wright et al., 2013), this value was larger by a few degrees. These experiments corroborated the small variability in freezing temperatures of individual droplets. Our correlation plots demonstrate both the randomness of freezing temperatures in

successive cycle experiments, as well as the variability of surface properties across the population of feldspar particles. In contrast, for the cycle experiments with individual droplets, the variability of surface properties could be neglected (Niedermeier et al., 2011b). The strong correlation between freezing events observed in our freeze-thaw cycles confirms the idea that the heterogeneous nucleation of ice is stochastic in nature, but its average observable characteristics (like fraction of frozen droplets) are governed by temperature dependent efficiency of individual IN active sites.

5.2 Cooling ramp experiments

Suspensions of FS01, FS02, FS04 and FS05 were investigated in the concentration range from 0.8wt% to 0.01wt% (Fig. 5A-5D) at three different cooling rates: 1, 5 and 10 K/min. Supercooled water droplets containing feldspar particles froze well above the homogeneous freezing limit (which was found to be 237 K for 100 μ m droplets on a pure silicon substrate, see Figure 5). The concentrated suspensions (0.8wt%, dark coloured curves) have shown in general steeper freezing curves as compared to less concentrated suspensions. The freezing behavior of FS01 and FS02 were nearly identical. The freezing of Na/Ca-rich feldspar suspensions (FS05, Fig. 5C) occurred at a lower temperature range (from 255.5K to 248K) as compared to K-rich feldspar suspensions. The concentrated (0.8wt%) suspension of FS04 was quite outstanding relative to other samples, as the droplets started to freeze already at 268K (Fig. 5D). All suspension droplets of FS04 were frozen at 255K. The effect of concentration was similar for all investigated feldspar sample suspensions. With decreasing concentration of feldspar suspensions, the frozen fraction curves covered a broader temperature range and the frozen fraction curves are shifted to lower temperatures. Note that the freezing curves of less concentrated FS04 suspensions (0.01 wt% to 0.1wt%) are very similar to those of FS01 and FS02 feldspar suspensions. The raw measurement data have been averaged within the 0.5K temperature intervals (Fig. 6 shows the case of FS02 and FS04).

5.3. Isothermal experiments

For a droplet population containing single component INPs kept at constant temperature, the classical nucleation theory (CNT) predicts an exponential decay of the number of *liquid* droplets with time. To see if such behavior can be observed under realistic experimental conditions, we have conducted a series of isothermal experiments where droplets were cooled down rapidly (typically at rate of 10 K/min) and then kept at constant temperature T_{ISO} for an hour. These experiments have been conducted for concentrated (0.8 wt%) suspensions of FS02 at $T_{ISO} = 253K, 254K, 255K,$ and $256K,$ and FS04 at $T_{ISO} = 266K$ and $267K$. The resulting unfrozen decay curves are shown in Fig. 7 together with the SBM simulations that are discussed in the next section.

For the FS04 suspensions, the $f_{liq}(t)$ curve shows a nearly linear (in log-log scale) decrease with time (Fig. 7B), with the decay rate becoming less steep at lower temperatures. A linear decrease is usually attributed to a single component IN

population with a uniform and narrow distribution of active sites and/or contact angles on the particle surface: AgI (Murray et al., 2012), kaolinite (Murray et al., 2011) and illite NX (Diehl et al., 2014). In addition, biological IN were found to exhibit a constant nucleation rate indicating a narrower distribution of active sites and/or contact angles on the IN species (Yankofsky et al., 1981).

For droplets of FS02 suspensions, decay of the fraction of liquid droplets $f_{liq}(t)$ clearly deviates from the linearity (in log-log space) indicating a broad distribution of the active sites responsible for ice nucleation (Fig. 7A). The deviation from linearity is more pronounced for lower temperatures, as more and more ice nucleating sites become engaged.

Such non-linear time dependence has been reported for a number of mineral dust particles immersed in water droplets. In droplet freezing assay experiments, suspensions of feldspar identical to our FS02 sample (Herbert et al., 2014), ATD suspensions (Wright et al., 2013) and less concentrated illite NX suspensions (Broadley et al., 2012) featured a non-linear time behavior. Studies in the Zurich Ice Nucleation Chamber (ZINC) have also found that size-selected kaolinite particles (Fluka, 400nm and 800nm) showed also a non-exponential decay with increasing residence time and temperature (Welti et al., 2012). Non-exponential time dependence was associated with a heterogeneous system featuring a high degree of interparticle variability. Other authors ascribe the deviation from the single-exponent to the diversity of active sites and the finite number of droplets (Wright et al., 2013).

5.4. Cooling rate dependence

For all investigated concentrated feldspar suspensions, a weak cooling rate dependence of the median freezing temperature ($T_{0.5}$) was observed (Fig. 8). For FS01, FS02 and FS05 the median freezing temperature was shifted by $\Delta T = 0.6 - 0.7$ K toward lower temperature, as cooling rate $c = dT/dt$ increased from -1K/min to -10K/min. However, for concentrated FS04 suspensions (0.8 wt%), the $T_{0.5}$ decreased by only 0.2 K.

The experimental and numerical studies of the cooling rate effect on the median freezing temperature $T_{0.5}$ have been reviewed recently by Wright et al., (2013) and Herbert et al., (2014). For mineral dusts (ATD, montmorillonite) the median freezing temperature becomes lower by 0.5 K to 1.5 K per ten-fold increase in the cooling rate. For kaolinite suspensions (Clay Minerals Society, CMS) a temperature shift of 8 K (three orders of magnitude change in cooling rate) has been predicted based on the parameterization of experimental data (Murray et al., 2011), but the measured temperature shift revealed only 3 K temperature shift when decreasing cooling rate by two orders of magnitude (Wright et al., 2013).

Unlike mineral dusts, biological INP showed a weaker cooling rate dependence. For Snomax®, a weak increase of the $T_{0.5}$ value with decreasing cooling rate was found by Wright et al., (2013) and Budke and Koop, (2015). The increase in cooling rate by two orders of magnitude led to a temperature shift of 0.55K and 0.64K for highly concentrated (Class A type) and less concentrated (Class C type) Snomax® suspensions, respectively. This is consistent with our observation of reduced cooling rate dependence for droplets containing highly effective IN particles.

5.5 SBM-based fit of experimental data

To demonstrate the common features and differences in freezing behavior of all feldspar suspensions, we have applied the SBM-based fit to the experimental freezing curves of all feldspar samples obtained for various concentrations. The binned data have been fitted with Eq. (3) with adjustable fit parameters n_{site} , μ_θ , and σ_θ (Fig. 6). Binning improves the efficiency of minimization algorithm that has been programmed in Matlab. The fit parameter values are given in Table 2A.

For isothermal experiments, the fit routine has been modified to fit the entire decay curve of the liquid droplet fraction. This was achieved by setting the cooling ramp relationship to $T = T_{start} + ct$ in the time interval $t_{start} \leq t \leq t_{ISO}$. Once $T_{ISO} = T(t_{ISO})$ has been reached, the relationship is set to $T(t) = T_{ISO}$. In this way, the fit routine was forced to find the set of fit parameters capable of reproducing both frozen fraction at the end of the cooling ramp $f_{liq}(t_{ISO})$ and time evolution of the decay curve at constant temperature $f_{liq}(t)$, $t > t_{ISO}$. The resulting “composite” fit curves are shown in Fig. 7A and 7B for FS02 and FS04, respectively, and resulting fit parameters are given in Table 2B.

Ideally, a single set of SBM parameters should represent the freezing behavior of a given INP obtained in different experiments (CR with different cooling rates, CR with various concentrations, and ISO freezing experiments) equally well. If this is not the case, a constraining condition is required to obtain a meaningful set of fitting parameters. A suitable constraint can be found in different ways: by analyzing the cooling rate dependence of $f_{ice}(T)$ or by finding the unique set of fit parameters adequately describing both CR and ISO experiments.

First, we compare the observed shift of the median temperature with the theoretical values calculated with Eq. (3), with $T_{0.5}$ being the temperature where $f_{ice} = 0.5$ and $\Delta T_{0.5}(c) = T_{0.5}(c) - T_{0.5}(-1 K/min)$ (solid lines in Fig. 8). The values of n_{site} , μ_θ and σ_θ have been taken from the SBM fit of the CR freezing curves, as described above in this section. The absolute values of $\Delta T_{0.5}(c)$ are satisfactory reproduced by the model for FS01 and FS02 at $c = -5 K/min$ and for FS04 at $c = -10 K/min$ but are 0.2K off for FS01, FS02, and FS05 at $c = -10 K/min$. The shift of the median temperature is less pronounced for better ice nuclei (compare $\Delta T_{0.5}(-10 K/min) = -0.2K$ for FS04 vs. $\Delta T_{0.5}(-10 K/min) = -0.5K$ for “generic” feldspars FS01, FS02, and FS05 and this feature is clearly captured by the SBM (Fig. 8). Although the trend in the cooling rate dependence is adequately predicted, we note that the $\Delta T_{0.5}(c)$ calculated with Eq. (3) cannot predict more than $\Delta T_{0.5} = -0.5K$ for a ten-fold change in the cooling rate without relaxing the constraint on μ_θ and σ_θ (see also the discussion in Herbert et al., 2014). However, a slightly better agreement with the measurements of $\Delta T_{0.5}$ at $c = -10 K/min$ could be achieved by assuming the log-normal $p(\theta)$, but otherwise preserving all model parameters (dashed line in Fig. 8). We conclude therefore that the subset of input parameters used in this study does capture the observed trend (the less active suspensions exhibit a stronger shift of median freezing temperature) but cannot be effectively used to constrain the fitting routine.

The allowed variability of fit parameters can be reduced if we consider that the same IN material has been used in CR experiments with different weight concentrations W . In this case, the values of μ_θ and σ_θ can be kept constant in the

simulation of the freezing curves, and only n_{site} should be varied. The initial pair of μ_θ and σ_θ can be determined either by fitting the freezing curve measured for the lowest concentration or by assuming the fit parameters obtained from the ISO experiments (if available), as it has been done here for FS02.

The same approach has been used to constrain the fit of isothermal data for FS02 and FS04, obtained for different values of T_{ISO} . For FS02, the initial values of $\mu_\theta = 1.32 \text{ rad}$ and $\sigma_\theta = 0.1 \text{ rad}$ have been obtained from the fit of composite liquid fraction decay curve at 256 K. This pair of parameters has then been used to fit the other ISO decay curves and the freezing curves measured in the CR experiments with various concentrations. Within this approach, a high quality fit ($r^2 > 0.95$) of all frozen fraction curves (Fig. 6A) and liquid fraction decay curves (Fig. 7A) could be achieved. Note that the pair of fit parameters for FS02 is very close to the values $\mu_\theta = 1.29 \text{ rad}$ and $\sigma_\theta = 0.1 \text{ rad}$ obtained in (NIED2015) by fitting the frozen fraction curves measured in the diffusion channel LACIS for the similar feldspar specimen (FS01).

The fit of the ISO measurements of FS02 has yielded a higher number of IN active sites n_{site} for higher T_{ISO} (Table 2B). This counterintuitive observation could be possibly explained by the relationship between T_{ISO} and the final fraction of frozen droplets achieved at the end of the ISO run. For higher T_{ISO} , the final fraction of frozen droplets is lower, and the fit algorithm “compensates” for the reduction of available sites by increasing their total number. This effect was not very pronounced in case of FS04 (see Table 2B), probably because the final fraction of frozen droplets for both used T_{ISO} values used was very similar.

Almost the same distribution of contact angle ($\mu_\theta = 1.33 \text{ rad}$, $\sigma_\theta = 0.1 \text{ rad}$) as for FS02 was obtained by fitting the concentrated FS05 suspensions. This is a somewhat unexpected result since freezing curves are visibly shifted towards the lower temperature (by at least 2K, see Fig. 4A and 4C). Straightforward interpretation of fitting parameters would mean that the difference between K-rich feldspar (FS01, FS02) and Na/Ca-rich feldspar (FS05) is not in the activity of IN sites but in their number per unit particle surface (compare $n_{site} = 47$ for FS05 against $n_{site} = 181$ for FS02, with only 20% difference between total particle surface S_p). On the other hand, the same difference in median freezing temperature can be compensated by increasing the standard deviation from $\sigma_\theta = 0.1 \text{ rad}$ for FS02 to $\sigma_\theta = 0.14 \text{ rad}$ for FS01 (compare $n_{site} = 30$ for FS01 and $n_{site} = 181$ for FS02, which have a very similar freezing behavior). In our opinion, such analysis clearly demonstrates that if the freezing curves are fitted with all three parameters made adjustable, the n_{site} should not be interpreted as the average number of ice active sites per particle. Such interpretation would only make sense if a plateau on the freezing curve can be observed for very small concentration of IN particles, allowing the independent determination of the average number of ice active sites per droplet, λ_{INS} . Therefore, the intercomparison of the freezing behavior, either of different specimens or observed within different experimental setups, based on such a fit, should be done with extreme caution.

The sample FS04 stands out clearly within the analyzed group of feldspars in several respects. For this specimen, it was not possible to fit all freezing curves obtained at various concentrations with a fixed pair of fit parameters μ_θ and σ_θ . The $\mu_\theta = 0.75 \text{ rad}$ found for freezing curve measured for the 0.8 wt% suspension indicates a very high IN efficiency. However, for the diluted suspensions (0.1 wt% to 0.01 wt%) the fit parameters that secured the best fit appeared to be close to the values

obtained for three other feldspar specimens (see Table 2A). Such behavior could only be interpreted in terms of bimodal population of active sites in the FS04 sample, with the sites belonging to the very active second mode present in scarce numbers and thus visibly dominating the freezing curve of concentrated suspension droplets. In diluted suspensions, the presence of the second mode is visible as a shoulder on warmer side of the freezing curves for 0.1 wt% and 0.05 wt% suspensions (see Fig. 6B).

5 This shoulder, however, does not affect the fit algorithm. Note that we have not constrained the fitting parameters in any way here, applying the fit algorithm to every freezing curve independently, which caused a slight variation of μ_θ and σ_θ .

The two-component hypothesis of FS04 freezing behavior is strongly supported by the data of isothermal decay experiments and corresponding fit. The fit parameters that provided the best fit of the different liquid fraction decay curves were identical, apart from the 15% difference in the n_{site} value, so that the only experimental value actually different in the simulation is the T_{ISO} (266K and 265K). The value of $\mu_\theta = 0.56 \text{ rad}$ is even lower than the mean contact angle obtained from the fit of the freezing curve $\mu_\theta = 0.75 \text{ rad}$, and the standard deviation $\sigma_\theta = 0.04$ indicates a very homogeneous population of IN active sites. The difference in μ_θ between the CR and the ISO fits should be attributed to the fact that in the CR experiment the whole distribution of freezing sites is involved in ice nucleation, and therefore the contact angle obtained in the fit represents the whole distribution of active sites. In contrast, in the ISO experiments only the most efficient sites are activated so that the less efficient sites are excluded from the freezing process. The homogeneity of the active sites distribution is consistent with the linearity of the decay curve in the log-log scale (Fig. 7B).

Such low values and narrow distributions of contact angles (and hence, high IN activity) have been previously obtained in SBM fits for freezing curves of biological INPs. For example, the INPs generated from Czech and Swedish birch pollen washing water (BPWW) have been characterized by $\mu_\theta = 1.01 \text{ rad}$, $\sigma_\theta = 0.08 \text{ rad}$, and $\mu_\theta = 0.83 \text{ rad}$, $\sigma_\theta = 0.0005 \text{ rad}$, respectively (Augustin et al., 2013). For Snomax® particles, the best INP known up to date (Wex et al., 2015), SBM parameters of $\mu_\theta = 0.595 \text{ rad}$, $\sigma_\theta = 0.04 \text{ rad}$ have been calculated based on the same approach (Hartmann et al., 2013). Within this reference framework, the IN efficiency of the highly active mode of FS04 is higher than that of the BPWW and at least as high as that of the Snomax®.

Overall, the IN activity of feldspars investigated in this study is situated at the upper end of ice activity scale. For ATD, the range of SBM parameters was found between $\mu_\theta = 2.13 \text{ rad}$, $\sigma_\theta = 0.33 \text{ rad}$, and $\mu_\theta = 2.48 \text{ rad}$, $\sigma_\theta = 0.39 \text{ rad}$ (Niedermeier et al., 2011b). The mean and standard deviation of the contact angle distribution of Illite NX was found to be $\mu_\theta = 1.9 \text{ rad}$ and $\sigma_\theta = 0.29 \text{ rad}$, respectively (Hiranuma et al., 2015). This comparison suggests that the SBM framework correctly reproduces the relative ice nucleation efficiency of natural and artificial mineral dust aerosols.

5.6 Surface density of IN active sites

30 The CR experiments performed with varying concentration allowed us to calculate the INAS surface density via Eq. (1). Both $n_s(T)$ curves for FS01 and FS02 are very similar and are therefore shown together in Fig. 9. In the temperature range between 252K and 260K (occupied by the 0.8 wt% suspension data) our $n_s(T)$ values are only slightly lower than those reported for

FS02 in ATK2013. The data of ATK2013 is shown in the form of an exponential parameterization and is used as a reference for all other $n_s(T)$ plots (black solid line in Fig. 9 to Fig. 11). Size-selected measurements of FS01 particles in LACIS also showed a similar slope of $n_s(T)$ curve but the values are shifted towards higher n_s , located at lower temperatures (orange open triangles, NIED2015). Both our $n_s(T)$ curves for FS01 and FS02 suspensions and the data from NIED2015 showed a leveling-off of $n_s(T)$ values with decreasing temperature. A qualitative explanation that was suggested in NIED2015 is that at lower temperature the surface density of INAS is approaching asymptotic value n_s^* , equal to the maximum surface density of *all possible* INAS for the given particle population. The leveling off has not been reported in ATK2013, obviously because the suspension was not diluted sufficiently to reach the temperature range where the leveling-off would be expected.

The $n_s(T)$ can be easily related to the SBM fit parameters obtained from the CR and ISO experiments via Eq. (4). The shaded area in the Fig. 9 shows the range of $n_s(T)$ that we obtain by assuming the fit parameters from Table 2A: $\mu_\theta = 1.32 \text{ rad}$, $\sigma_\theta = 0.1 \text{ rad}$, $c = -1 \text{ K/min}$, $n_{site} = 2$, and varying weight concentration of feldspar in the droplet suspension from 0.01 wt% to 0.8 wt% (and therefore varying the total particle surface area since $S_p = W \cdot V_{drop} \cdot S_{BET}$). Note that varying S_p has essentially the same effect on $n_s(T)$ as varying n_{site} since these two quantities appear as a ratio in the Eq. 4. The fact that all experimental data fall inside the shaded area demonstrates that the range covered by n_{site} variation corresponds to the variation range of total particle surface at different weight concentrations. One can immediately see that the SBM simulation captures the leveling-off of $n_s(T)$ at lower temperature.

As pointed out in NIED2015, the asymptotic value n_s^* is the limit of $n_s(T)$ when the probability of the suspension droplet to freeze at T , $P_{freeze} = 1 - P_{unfr}(T, \mu_\theta, \sigma_\theta, t)$, approaches 1 (recall Eq. (4)). It is therefore clear that the suspension droplet is bound to freeze when $n_s(T)$ reaches the value n_s^* , and further increase of the IN active site efficiency (described in the model by decreasing the value of contact angle) would not result in the further increase of the freezing probability (or the fraction of frozen droplets). **The value of n_s^* is therefore a true property of the system for a given suspension concentration and droplet size.** For combined FS02 and FS01, the upper bound of n_s^* was found to be $2.1 \times 10^7 \text{ cm}^{-2}$, corresponding to the surface area occupied by a single IN active site $S_{site} \approx 5 \mu\text{m}^2$, a square patch with the side length of $2.2 \mu\text{m}$, which is at least 6 orders of magnitude larger than the cross-sectional area of a critical ice nucleus at low temperature (Pruppacher and Klett, 2004).

We observe that the data of NIED2015 lie outside the shaded area in Fig. 9. The values of $n_s(T)$ reported in NIED2015 have been obtained for single, size selected feldspar particles, with the modal electrical mobility diameters ranging from $0.2 \mu\text{m}$ to $0.5 \mu\text{m}$. If we use the geometric surface area (based on the aerodynamic diameter, as specified in NIED2015) of a $0.5 \mu\text{m}$ particle as for S_p in Eq. (4), and assume the constant temperature and a residence time of 1.6 s (as in LACIS), we obtain the blue broken line that agrees with the data of NIED2015 quite well. The ratio of n_s^* values is evidently equal to the ratio of S_p values in NIED2015 and in this study (red broken curve in Fig. 9). Thus, we arrive at the conclusion that the apparent INAS surface density in the plateau region is a function of the particle surface area per droplet, which is not obvious considering that per definition the INAS surface density is defined as a number of frozen droplets *normalized* by the particle surface.

For the INAS surface density asymptote with NIED2015 data, we calculate $n_s^* = 4.7 \times 10^8 \text{ cm}^{-2}$, and the corresponding surface area occupied by a single IN in this case is reduced to $\approx 0.21 \mu\text{m}^2$, a square patch with the side length of $\approx 460 \text{ nm}$, still “oversized” compared to a single critical ice germ. The fact that the asymptotic “surface area per active site” is much larger than the cross-sectional area of a critical ice germ supports the idea that “ice active sites” are local features (of morphological or chemical nature) and not the homogeneous patches on the particle surface.

The $n_s(T)$ curves of FS05 suspensions are shifted toward the lower temperatures compared to FS01 and FS02 (Fig. 10) but otherwise showed the same behavior (exponential growth in the range from 250 K to 257 K and gradual leveling-off at lower temperature). Together with our values, both measurements reported recently in ATK203 and (Schill et al., 2015) fall nicely into the range of n_s values predicted by Eq. (4), by assuming the fit parameters of: $\mu_\theta = 1.33 \text{ rad}$, $\sigma_\theta = 0.1 \text{ rad}$, $c = -1 \text{ K/min}$, and $n_{\text{site}} = 5$, and varying weight concentration of feldspar in the droplet suspension from 0.01 wt% to 0.8 wt%. The upper bound of n_s^* was found to be $1.8 \times 10^7 \text{ cm}^{-2}$, very close to that of FS01 and FS02.

The outstanding nature of FS04 becomes more evident on the $n_s(T)$ plot (Fig. 11). The bimodal behavior is clearly visible with the first mode (labeled FS04H) being active already at 268K, 5K below the melting point. The second mode (labeled FS04L) is located at lower temperature and almost coincides with the $n_s(T)$ curve of FS01 and FS02 (shown as red broken line in Fig. 11). Both modes show the leveling-off starting below 266 K for the FS04H and below 248 K for FS04L.

The coexistence of two independent sets of IN active sites can be reproduced by Eq. (4) by using two separate sets of fitting parameters (Table 2A) for calculation of $n_s(T)$. The $n_s(T)$ range covering the low-temperature mode FS04L is obtained by assuming the fit parameters: $\mu_\theta = 1.3 \text{ rad}$, $\sigma_\theta = 0.12 \text{ rad}$, $n_{\text{site}} = 10$, and varying the weight concentration of feldspar in the droplet suspension from 0.01 wt% to 0.1 wt%, whereas the high temperature mode FS04H is represented by fit parameters: $\mu_\theta = 0.75 \text{ rad}$, $\sigma_\theta = 0.12 \text{ rad}$, and varying the n_{site} from 0.2 to 10. Note that the $n_s(T)$ curve calculated with the fit parameters obtained from the isothermal freezing experiments ($\mu_\theta = 0.56 \text{ rad}$, $\sigma_\theta = 0.04 \text{ rad}$, Table 2B) is only reproducing the rising slope of the measured curve. This means that the overall shape of the high-temperature part of the curve (above 255K) is influenced both by IN active sites from both active and less active modes FS04H and FS04L, and is responsible for the higher value of μ_θ than the one obtained from the isothermal freezing experiment.

A formal comparison of the asymptotic INAS surface densities n_s^* for two modes -- $2.4 \times 10^7 \text{ cm}^{-2}$ for the low temperature mode versus $1.0 \times 10^4 \text{ cm}^{-2}$ for the high temperature mode -- suggests that the highly active sites constitute roughly 0.1% of all sites in our suspension droplets. Multiplying the n_s^* for the high temperature mode with the total particle surface area per droplet, we obtain $n_s^* \times S_p = 0.29$, implying that only 30% of all suspension droplets of the most highly concentrated suspension contain at least one high temperature active site at all. One can obtain approximately the same number by noting that only 75% of all droplets froze in the ISO experiment after cooling the droplet assay down to 266 K and waiting for an hour (see Fig. 7B). Since the amount of feldspar in our suspension droplets (0.8 wt%) corresponds roughly to 3.7×10^3 individual feldspar particles of 0.5 μm diameter, one could estimate that only one in ≈ 12000 feldspar aerosol particles of this

size would contain a single, highly active IN site. This estimation might be helpful in understanding the nature of these sites, as discussed below.

A two-step ice nucleation behavior was previously observed for pure, size-selected ATD particles (Niedermeier et al., 2011a), for residual particles of birch pollen washing water (Augustin et al., 2013) in LACIS, for soil dust particles (O'Sullivan et al., 2015), and for Snomax® (Budke and Koop, 2015; Wex et al., 2015) particles in droplet freezing assay experiments. These measurements highlight that there could be multiple, distinct populations of INPs present in a particular material. When such active sites occur only very infrequently, their presence will be detectable only in concentrated suspensions and setups, allowing measurements at high supercooling temperature. To our knowledge, multiple ice nucleating species in a single-component mineral dust aerosol (like illite, kaolinite, montmorillonite, etc.) have not been observed before.

10 6 Influence of ageing

6.1 Aging in aqueous suspension

To examine the influence of aging on the ice activity of feldspars, K-feldspar (FS01) and Na/Ca-feldspar (FS05) particles were soaked in water for over five months and the supernatant water was exchanged twice. Soaking in water resulted in a decrease of the median freezing temperature by 2 K for FS01 and by 3 K for FS05 0.8 wt% suspensions. (Fig. 12). The reduction of IN efficiency is thought to be correlated with the release of soluble components from the framework of the mineral (e.g. alkali metal ions, hydrated aluminum and silicon species), which might be repartitioned as amorphous material on the surface of feldspar particles (Zhu and Lu, 2009; Zhu, 2005) and inhibit ice active sites. The stronger reduction in T_{50} values observed for FS05 might be a consequence of a higher dissolution rate of the Na/Ca-feldspar particles (Parsons et al., 1994; Zhu, 2005). The time evolution of the leaked cation concentration (K^+ , Na^+ , Ca^{2+} , and Mg^{2+}) have was measured during the first month by liquid ion chromatography and is shown in the supplementary Fig. S6. We have observed a steady rise of cation concentrations, during the whole period of observation, according to the $\sim t^{0.5}$ law, well known in petrology for the dissolution rates of tectosilicates as they are weathered to become clays (Parsons, 1994). This behavior clearly differs from the cation release from illite clay mineral in aqueous suspension, where no further increase of the cation concentration was observed after initial fast release occurring on the order of several minutes (Hiranuma et al., 2015). The depletion of framework cations in the surface crystalline layers of feldspar might be another explanation for the observed reduction of ice nucleation efficiency. Due to the constant release of the framework cations, the IN activity of the ageing feldspar should gradually reduce over long time periods, as the feldspar is weathered to become clay.

6.2 Treatment with heat and hydrogen peroxide

We have attempted to shed some light onto the anomalously high IN efficiency of concentrated FS04 by treating it both thermally and chemically. Our primary suspect was contamination with biological IN particles, known to be the most active

INP in immersion mode. To this end, we have conducted the CR experiments with the 0.8wt% suspensions heated up to 90°C for an hour. Heating is a common procedure to test for proteinaceous ice nuclei that are expected to degrade progressively with increasing temperature (Pouleur et al., 1992; Pummer et al., 2012). Heat-treated FS04 showed a slight decrease of the T_{50} value from 264.7K to 263.9K in 1K/min CR experiment, but the $n_s(T)$ curve preserved its bimodal shape and position (Fig. 13). This clearly demonstrates that proteinaceous IN could not be responsible for the high ice activity of FS04 particles. Another test is the removal of thermally stable, carbonaceous IN by digestion with hydrogen peroxide solution (O’Sullivan et al., 2014; O’Sullivan et al., 2015). This treatment, performed at 65°C for one hour, has indeed resulted in the significant reduction of the ice activity of FS04. Keeping the freshly prepared FS04 sample in hydrogen peroxide over night at room temperature lowered the T_{50} even further (Fig. 12C and Fig. 13). A weak cooling rate dependence of chemically treated FS04 particles was observed, with the 10-fold change in responsible for $\Delta T \approx 0.5K$. This is more than ΔT observed for untreated suspensions by a factor of 2 (open symbols in Fig. 12 and Fig. 5) and is characteristic for generic feldspars FS01 and FS02. By looking at $n_s(T)$ curves of thermally and chemically treated FS04, it becomes clear that the treatment has reduced its IN activity down to that of the generic K-feldspar (FS01 and FS02). A further reduction was not observed and is not expected since the generic K-feldspar particles showed no detectable change in ice activity after a thermal treatment (O’Sullivan et al., 2014; Zolles et al., 2015). Based on these results alone, organic IN cannot be ruled out as a reason for the anomalously high freezing efficiency of FS04.

Let us estimate the amount of “contamination” required to produce the observed enhancement of INAS surface density at high temperature. The feldspar powder used for preparation of FS04 suspension was produced by ball milling of a single crystal specimen. Due to the usual precautionary measures taken to avoid the contamination during and after the preparation, it is logical to assume that the contamination could have been introduced on the surface of the specimen prior to milling, and the amount of contamination should be proportional to the surface area of the original specimen. In the previous section, we came to the conclusion that only every third droplet in our experiment contained a highly active ice nucleating “entity”, FS04H. Since the mass of feldspar per 0.2 nL droplet at 0.8 wt% concentration is $V_d \times 0.008 \times \rho_{FS} = 1.2 \times 10^{-8} g$, we can estimate the mass concentration of active sites $n_m = 2.9 \times 10^8 g^{-1}$, which is, for example, two orders of magnitude higher than the mass concentration of ice active sites in untreated fertile soil (see Fig. 7 in O’Sullivan et al., 2014). Soil particles contain up to 40% organic matter which is thought to be responsible for their IN properties (Tobo et al., 2014). Augustin-Bauditz et al., (2016) has measured the freezing behavior of illite NX mixed with birch pollen washing water (BPWW) extract. BPWW contains resuspendable IN active macromolecules, most probably polysaccharides (Pummer et al., 2012), which, unlike ice nucleating proteins, preserve their IN efficiency upon heating. Although no freezing events above -17°C have been detected in Augustin-Bauditz et al., (2016), extrapolating their fraction of frozen droplets curve to -10°C and calculating the mass concentration of IN active sites as $n_m(263 K) = -\frac{6 \cdot \ln(1-f_{ice}(263 K))}{\pi \rho_p d_p^3}$, we obtain concentration of macromolecules $n_m \approx 5 \times 10^7 g^{-1}$. This value is close (within an order of magnitude) to what we obtained for high-temperature active sites FS04H at 266 K. *Note, however, that in the study of Augustin-Bauditz et al., (2016), the illite NX powder was deliberately*

mixed with BPWW extract. Additionally, to accept the biogenic contamination as the explanation for the high-temperature IN sites, we have to assume that the feldspar crystal used for the sample preparation was contaminated with INM with very homogeneous IN properties, as implied by a narrow distribution of contact angles established by fitting the isothermal freezing experiments at 266 K and 267 K. Finally, the modal value of contact angle distribution obtained with SBM fitting of immersion freezing curves for pure BPWW particles yielded a value 0.83 rad (Augustin et al., 2013), which is larger than any of our values for the high-temperature fraction of IN active sites in FS04 feldspar. These arguments bring us to the conclusion that at a realistic contamination level polysaccharides are not efficient enough to be responsible for the high-temperature nucleation of ice in FS04 suspension droplets. Since BPWW-like macromolecules are the only “likely” candidates for such contamination (capable of preserving the IN activity after heating but degrading after H₂O₂ treatment), the biogenic nature of high-temperature active sites seems to be unlikely. The origin of these sites, however, remains uncertain.

Several studies addressed the influence of ageing processes on the IN activity of feldspar particles. In more detail, diffusion chamber studies showed no statistically significant change in ice nucleation ability of unwashed and washed feldspar (orthoclase) particles in deposition mode freezing experiments (Yakobi-Hancock et al., 2013). Enzyme-treated K-feldspar nucleated ice at much lower temperatures, but after heating, the ice activity has been restored to the original level. For Na/Ca-feldspar particles (albite and andesine), no distinct change after thermal and chemical treatment was noticed (Zolles et al., 2015). A strong reduction of ice activity of K-feldspar particles (microcline) immersed in water droplets was achieved by treatment with sulfuric acid (Augustin-Bauditz et al., 2014). It was suggested that the treatment with sulfuric acid irreversibly modified the lattice structure of K-feldspar, as was also suggested by the ice nucleation experiments with bare and sulfuric acid coated K-feldspar particles (Kulkarni et al., 2012). To be more specific, in the deposition freezing experiments a reduced ice activity for coated feldspar particles was found, while no significant difference between bare and coated K-feldspar particles was observed in immersion freezing experiments. This behavior was explained in terms of dissolution of coating material under water-supersaturated conditions. These results, however, cannot be directly compared with our observations since coatings have not been applied in our study.

7 Conclusions

A newly developed Cold Stage apparatus was used to study the freezing behavior of up to 1000 identical feldspar suspension droplets, each with a volume of 0.2 nL. The setup features a motorized droplet injector positioning stage, liquid N₂ temperature control, and automated freezing detection system based on a wide field video camera equipped with polarization optics. Suspensions of three K-rich feldspars (microcline) and one Na/Ca-rich feldspar (albite with andesine inclusions) have been examined with different concentrations ranging from 0.01 wt% to 0.8 wt% and cooling rates from -1 K/min to -10 K/min. All concentrated feldspar suspensions have shown a steep temperature dependence of the INAS density, whereas diluted suspensions showed a flattening with decreasing temperature approaching asymptotically a limiting value n_s^* . The K-rich feldspar samples, FS01 and FS02, and Na/Ca-rich feldspar, FS05, showed a weak cooling rate dependence: median freezing

temperature decrease on the order of 0.6K over a ten-fold increase in the cooling rate. In contrast, the median freezing temperature of the FS04 suspension increased by only 0.2K, when accelerating the cooling from -1K/min to -10K/min.

The setup has proven to be perfectly suited for isothermal freezing experiments, which we have conducted with FS02 at four constant temperatures from 253K to 256K, and with FS04 at two constant temperatures of 266 K and 267 K. The liquid fraction decay curves were found to be clearly nonlinear in the log-log coordinates for the FS02 and quite linear for FS04. Since the non-linearity of the decay curves is normally associated with the heterogeneity of the sample, one would expect stronger heterogeneity of FS02 as compared to FS04.

To explore the relationship between stochastic and singular nature of ice nucleation, several freeze-thaw experiments with cooling rate of -5 K/min have been conducted. The degree of correlation between two subsequent freezing runs expressed as Pearson's correlation coefficient, have been shown to increase gradually from 0.14 in the case of pure water droplets on a silicon substrate to 0.92 for the best IN material in this study (FS04) observed at the highest examined concentration. The fact that the correlation does not become ideal, even for the best IN, clearly demonstrates the stochastic nature of ice nucleation.

We have used a CNT-based theoretical framework (the so-called Soccer Ball Model, SBM, Niedermeier et. al., 2015) to provide a consistent interpretation of the observed freezing behavior. This framework is based on the assumption that the active sites are randomly distributed over the surface of all INPs inside a single suspension droplet. The IN efficiency of these sites is characterized by a Gaussian distribution of contact angle θ with mean value μ_θ and standard deviation σ_θ . We show that it is possible to adequately describe the freezing curves obtained for different concentration and cooling rates in the CR experiments, and the isothermal decay of fraction of liquid droplets with time using a unique set of SBM parameters μ_θ and σ_θ and varying n_{site} according to the weight concentration of feldspar in suspension. Moreover, it was possible to use the same parameters to reproduce the experimental data obtained for the same feldspar specimen by different methods: LACIS, droplet freezing assay from ATK2013, and the data of Schill et al., (2015). Most noteworthy, however, is the observation that this approach seems to be capable of reproducing the variation of INAS surface density $n_s(T)$ with concentration of IN in the suspension droplets and correctly predicts the leveling-off of the $n_s(T)$ at low temperatures. The asymptotic active site density n_s^* , achieved by $n_s(T)$ as the freezing probability of every droplet in the ensemble approaches unity, can be interpreted as a true property of the system for a given suspension concentration and droplet size. Together with the mean value of contact angle, this asymptotic value provides a basis for the parametrization of IN properties that is required within the atmospheric modeling.

It should be stressed, however, that a consistent interpretation of the freezing behavior for a particular INP type is only possible through a combination of different experiments (cooling ramp, isothermal decay, freeze-thaw cycles) and thorough characterization of particle morphology (BET SSA, chemical composition, and size distribution). The fit parameters obtained by fitting the temperature jump and subsequent isothermal decay experiments allowed us to constrain the variability of fit parameters describing the CR freezing curves and therefore the $n_s(T)$ curves. Further improvement of the CNT-based parametrizations, beyond what was done in here, can be achieved by accounting for the contact angle variability and the particle

surface variability separately, and by assuming asymmetry of the contact angle distribution. Although the mechanistic understanding of IN active sites is still missing, this framework is worth developing further to be prepared for the future when the nature of the IN active sites will be characterized quantitatively via nanoscale measurements or ab-initio calculations.

One of the K-rich feldspar specimens (FS04) has shown an anomalously high IN efficacy, initiating the freezing already at -5°C. The INAS surface density of this feldspar clearly demonstrated a bimodal distribution of active sites, with a high temperature mode occupying the temperature range from 255K to 268K, and a low temperature mode in the range below 255 K, identical to the generic feldspar suspensions (FS01 and FS02). A proteinaceous origin for these highly active IN entities could be ruled out, since heating the suspension to 95°C yielded no observable change in the IN efficacy. Treatment of 0.8 wt% suspension of FS04 with 30% hydrogen peroxide (H₂O₂) solution resulted in the deactivation of the high-temperature IN mode (FS04H) and reduction of ice nucleation activity down to that of the generic K-rich feldspar (FS01, FS02). Applying the SBM fit to the temperature jump – isothermal decay experiments, a value of $\mu_\theta = 0.56 \text{ rad}$ was obtained, which was previously found for proteinaceous INP (Snomax), but is lower compared to $\mu_\theta = 0.83 \text{ rad}$ measured for the polysaccharides washed down from birch pollen grains. The number of high temperature active sites per mass of feldspar ($n_m = 2.9 \times 10^8 \text{ g}^{-1}$) was found to be two orders of magnitude higher than the mass concentration of ice active sites in fertile soil (O’Sullivan et al., 2014), and almost an order of magnitude higher than the mass concentration of ice active sites in mixture of illite NX with birch pollen washing water (BPWW, Augustin-Bauditz et al., 2016). Based on this comparison and values of μ_θ , we argue that biological nature of high temperature active sites is unlikely but their nature could not be uncovered in this study.

We conclude by suggesting that the droplet freezing assay presented in this paper is a useful tool for studying immersion freezing induced by a wide range of IN active materials, due to the low variability of droplet volume, a large number of individual droplets that can be observed simultaneously, and possibility to conduct different types of freezing experiments with the same sample. Such an instrument, when complemented by a careful surface and chemical characterization of an INP sample, provides a fast and comparatively cheap method for INP characterization.

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Table 1: The mineral composition and specific surface area (N₂ BET SSA) of feldspar samples.

Sample	Source	Mineral composition (XRD)	BET SSA [m ² /g]
FS01	Minas Gerais, Brazil, supplied by IAG TU Darmstadt	76% K-feldspar (microcline) 24% Na/Ca-feldspar (albite)	1.79
FS02	Bureau of Analyzed Samples, UK, standard BCS 376 (provided by University of Leeds, UK)	80% K-feldspar* 16% Na/Ca-feldspar* 4% quartz	2.64
FS04	Mt. Maloso area (Malawi), supplied by IAG TU Darmstadt	80% K-feldspar (microcline) 18% Na/Ca-feldspar (albite) 2% quartz	2.94
FS05	IAG TU Darmstadt, in-house collection	>90% Na/Ca-feldspar (albite)	1.92

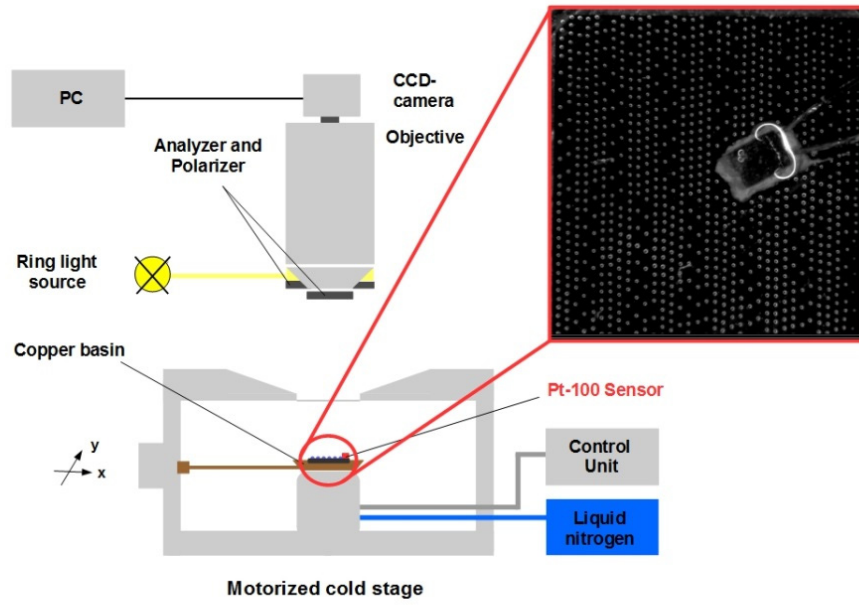
*mineral phase was not specified

Table 2A. SBM parameters obtained by fitting the CR freezing curves. The total particle surface area per droplet S_p is given for 0.8 wt% concentration and could be recalculated for all other mass concentrations. Pearson's r correlation coefficient was calculated from the freeze – thaw experiments. Note that n_s^* given here represents the upper bound value for the suspension series.

	FS01	FS02			FS05	FS04			
W [wt%]	0.8	0.8	0.05	0.01	0.8	0.8	0.1	0.05	0.01
S_p [cm ²]	2.5×10^{-5}	3.7×10^{-5}			2.7×10^{-5}	4.2×10^{-5}			
n_s^* [cm ⁻²]	2.1×10^7				1.8×10^7	1×10^4	2.4×10^7		
n_{site} [#]	30	181	8	2	47	3.5	63	25	6.8
μ_θ [rad]	1.3	1.32			1.33	0.75	1.32	1.3	1.35
σ_θ [rad]	0.14	0.1			0.102	0.12	0.15	0.12	0.1
r^2	0.99	0.96	0.99	0.95	> 0.95	0.99	0.95	0.98	> 0.99
Pearson's r	0.89	-	-	-	0.8	0.92	-	-	-

Table 2B: SBM parameters obtained by fitting the ISO decay curves.

	FS02				FS04	
$T_{ISO} [K]$	256	255	254	253	267	266
$S_p [cm^2]$	3.7×10^{-5}				4.2×10^{-5}	
$n_s^* [cm^{-2}]$	1.1×10^8	4.0×10^7	1.8×10^7	1.1×10^7	1.0×10^4	8.6×10^3
$n_{site} [\#]$	4400	1565	705	410	0.42	0.36
$\mu_\theta [rad]$	1.32				0.56	
$\sigma_\theta [rad]$	0.1				0.04	
r^2	0.99	0.98	0.98	0.94	0.99	0.98



5 **Figure 1:** Schematic drawing of the nanoliter droplet freezing assay setup (side view). The inset shows the top view of 10×10 mm Si-wafer with ≈ 1200 droplets immersed in silicon oil. The square shape near the center of the wafer is the Pt-100 temperature sensor.

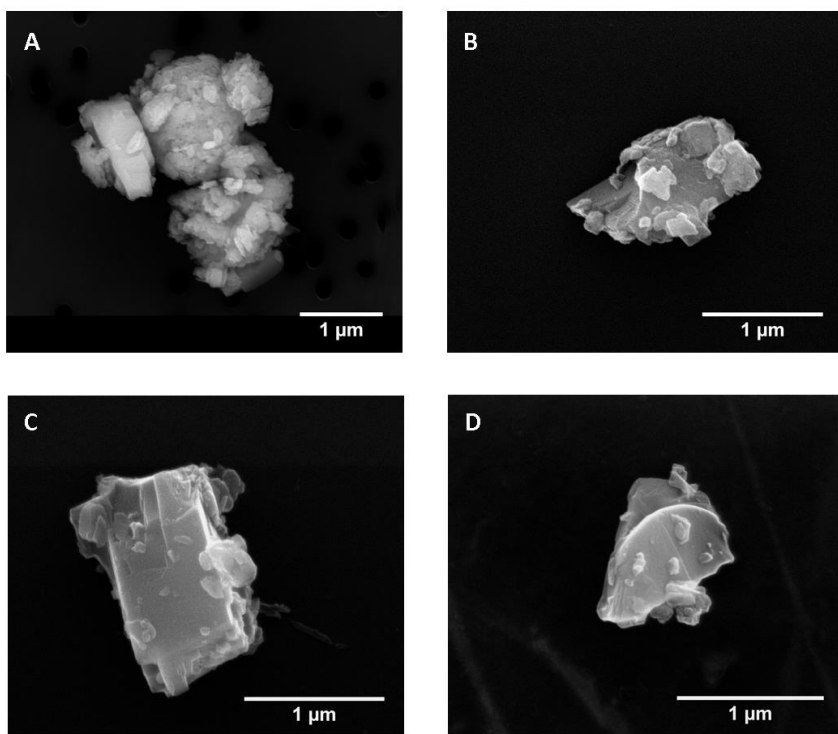


Figure 2: SEM images of A) FS01, B) FS02, C) FS04 and D) FS05 particles.

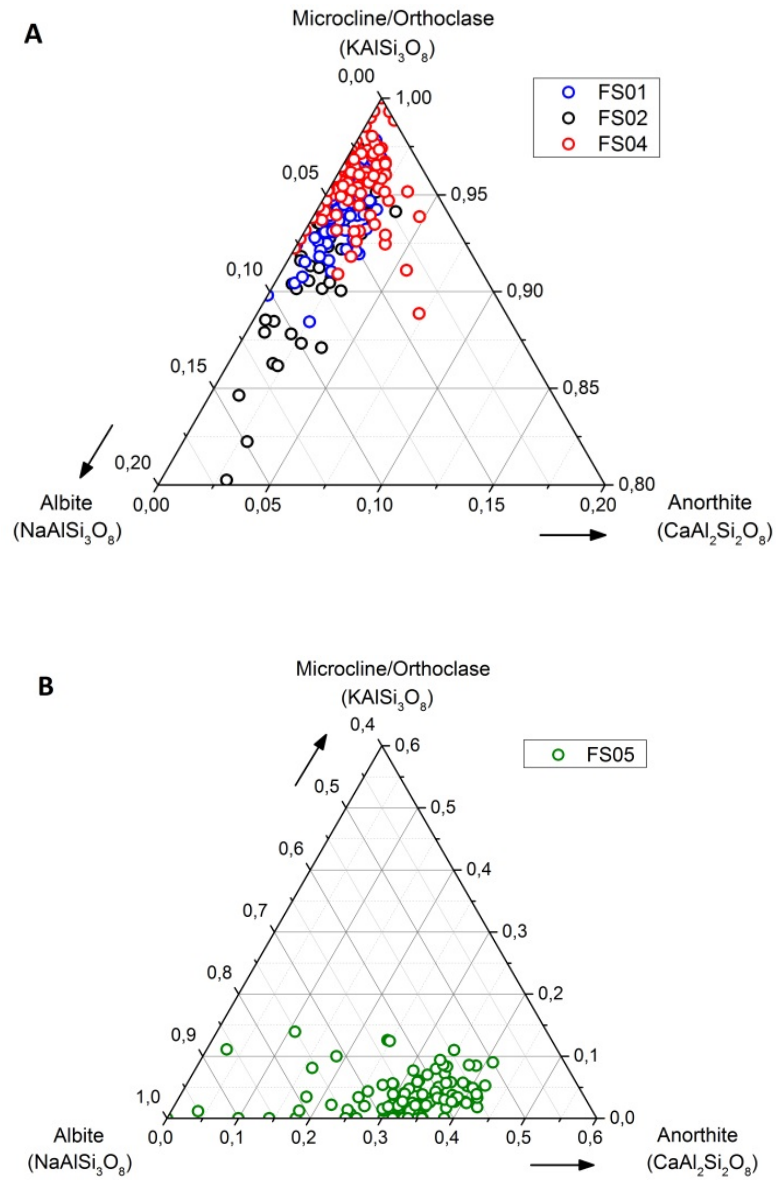
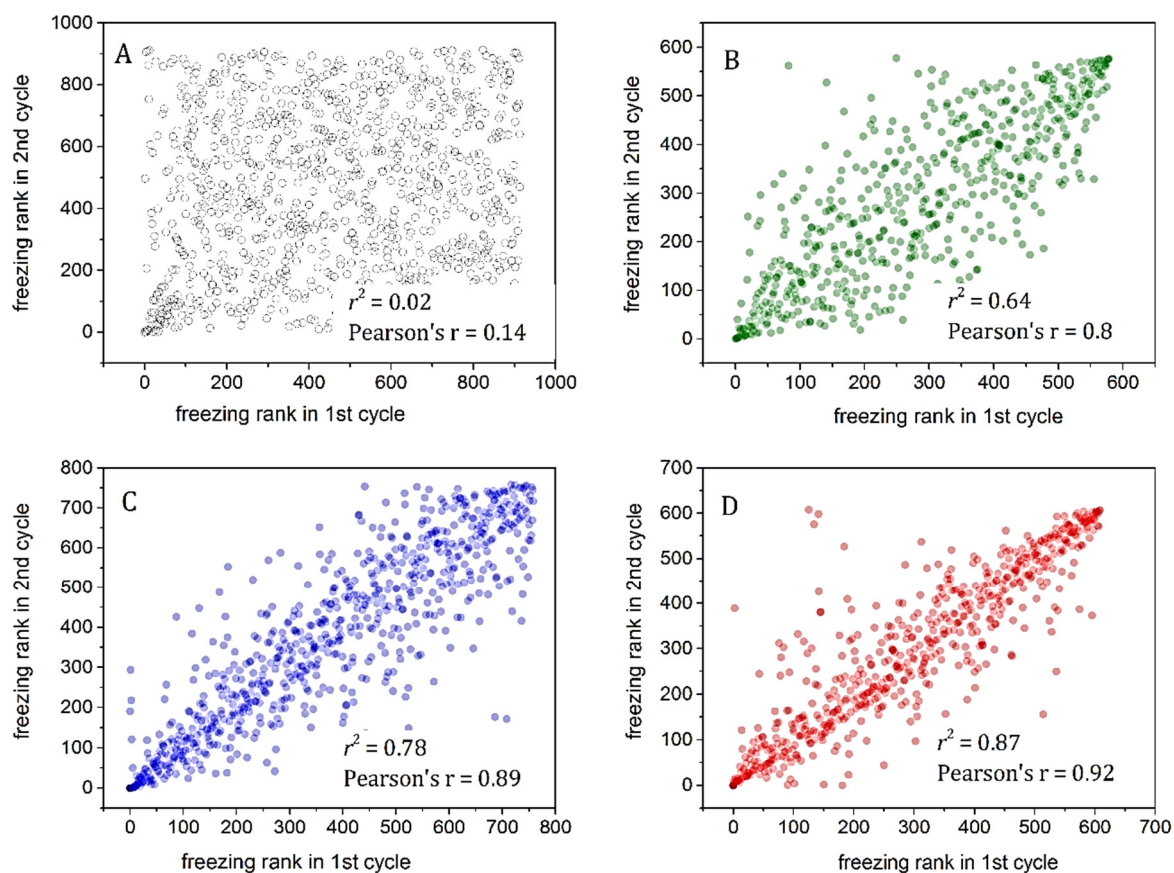


Figure 3: EDX data of individual feldspar particles plotted on the ternary phase diagram based on elemental mass percentages. A) Ternary phase diagrams of K-feldspar particles (FS01, FS02 and FS04) and B) Na/Ca-feldspar particles (FS05). Note the different scales of the ternary axis.



5 **Figure 4:** Correlations plots of freeze-thaw cycle experiments of feldspar suspensions (0.8wt%, 5 K/min). A) NanoPure water, B) FS05, C) FS01, and D) FS04. In the bottom right corner of every panel the adj. r^2 and the Pearson's r correlation coefficients describe the degree of correlation.

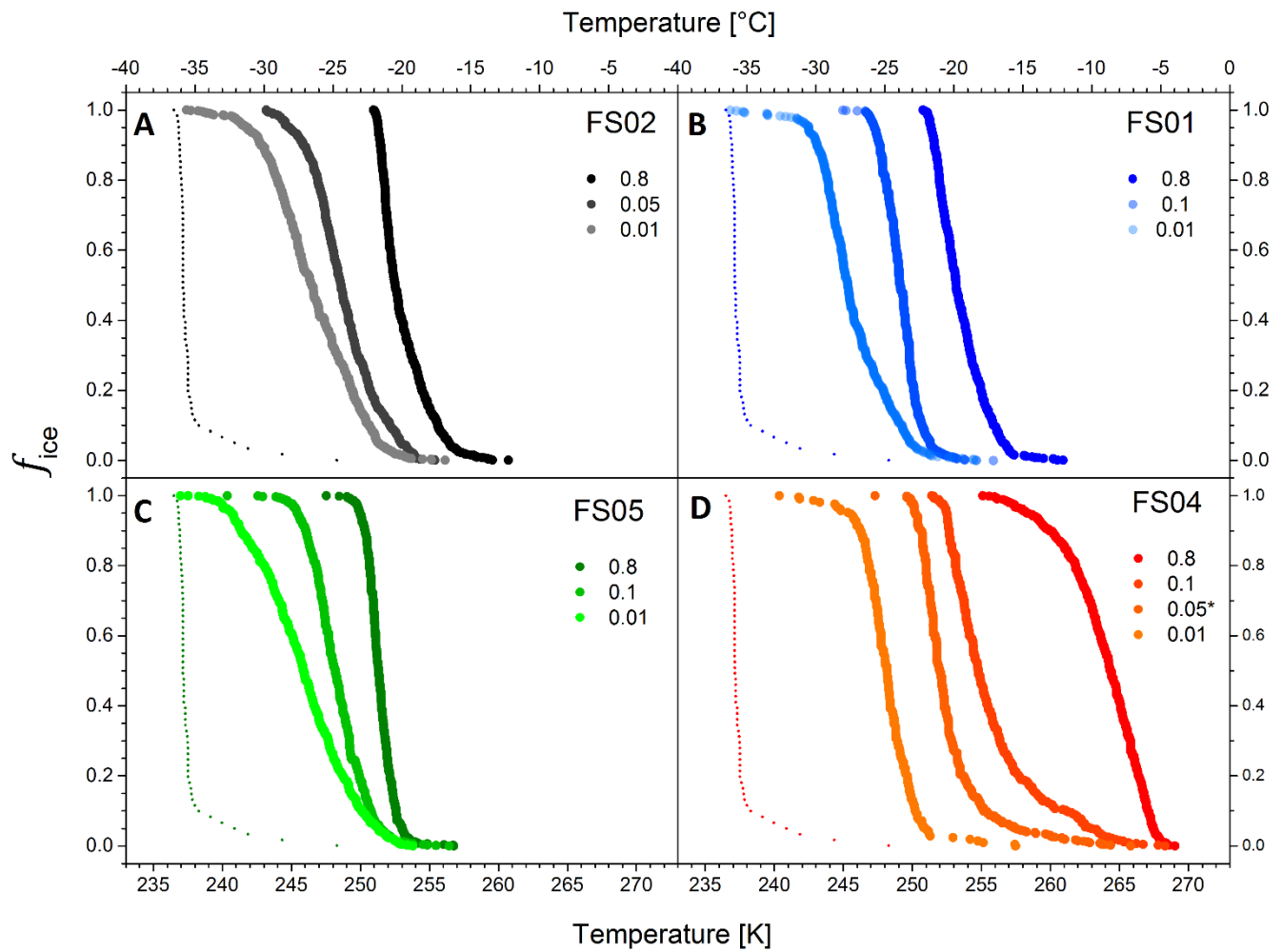


Figure 5. Frozen fraction curves of feldspar suspensions with various concentrations for A) FS02, B) FS01, C) FS05, and D) FS04 samples. Suspension concentration is given in the legend of each plot in wt %. Frozen fraction curves for Nanopure water droplets on a clean silicon wafer is given as dot line on each plot. All curves were measured with a cooling rate of -1 K/min, except for FS05 0.05 wt%, for which the cooling rate was -5 K/min (marked with an asterisk). Note the initiation of freezing at 268 K for FS04 0.8wt% suspension droplets.

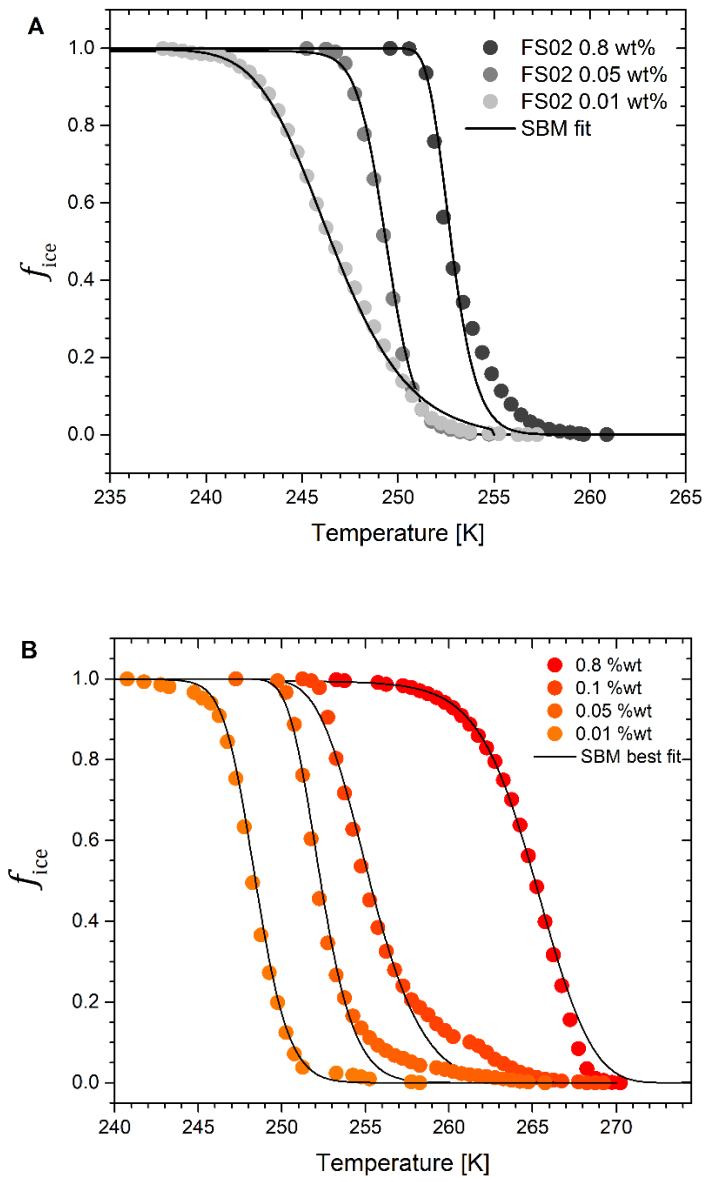


Figure 6. Freezing curves of FS02 (A) and FS04 (B) binned into 0.5K temperature intervals (filled symbols) and SBM best fit (solid curves). Fit parameters are given in Table 2A.

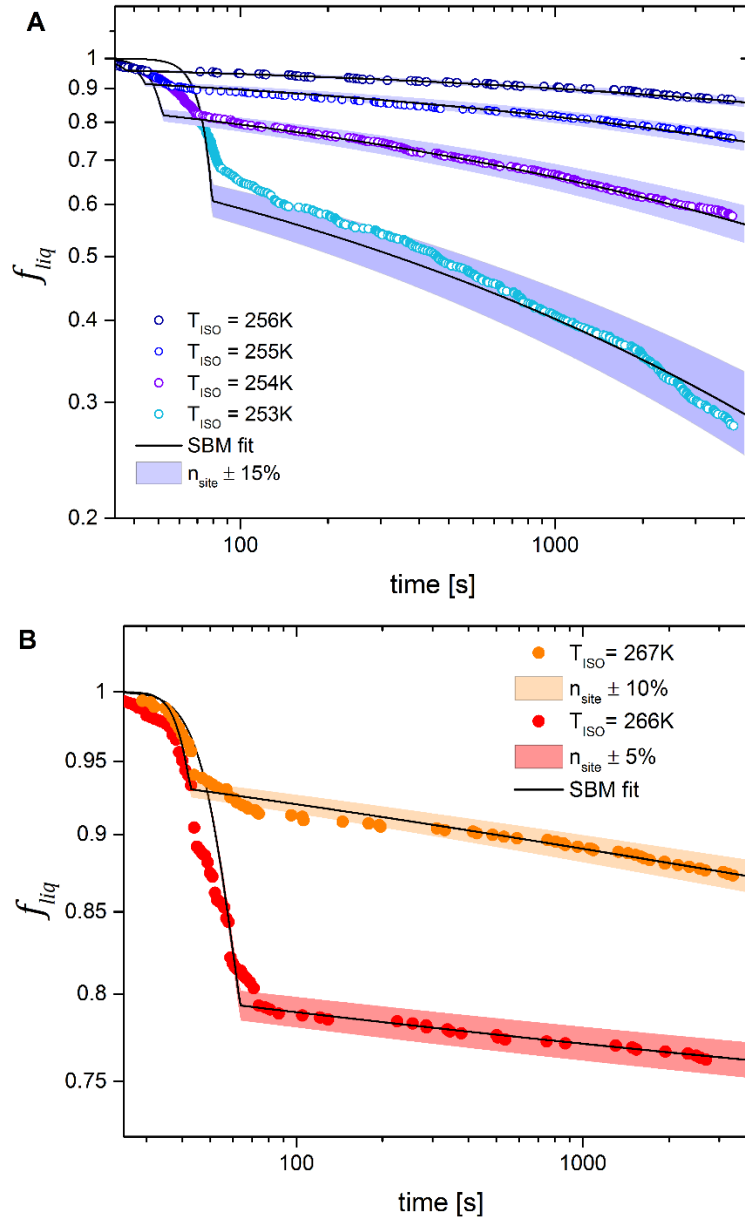
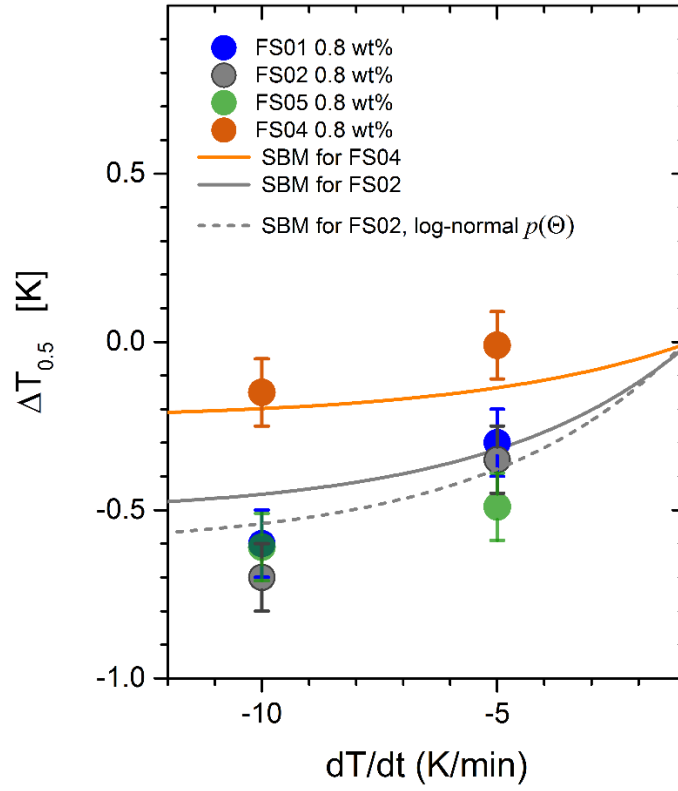


Figure 7. Decay of the fraction of liquid droplets with time for FS02 (A) and FS04 (B) for different T_{ISO} (log-log scale). Solid lines show composite SBM fit with parameters given in Table 2 (see section 7 for detailed discussion). Shaded areas indicate the variability $n_{site} \pm \Delta n_{site}$ of a best fit value, with actual Δn_{site} given in the legend.



5

Figure 8: The shift $\Delta T_{0.5}$ of the median temperature $T_{0.5}$ relative to the $T_{0.5}$ at 1 K/min for different cooling rates $c = dT/dt$. Solid lines represent expected $\Delta T_{0.5}(c)$ calculated with fit parameters given in Table 2. Dashed line is the theoretical temperature shift calculated with the same SBM parameters for FS02 but assuming the log-normal distribution of contact angles $p(\theta)$.

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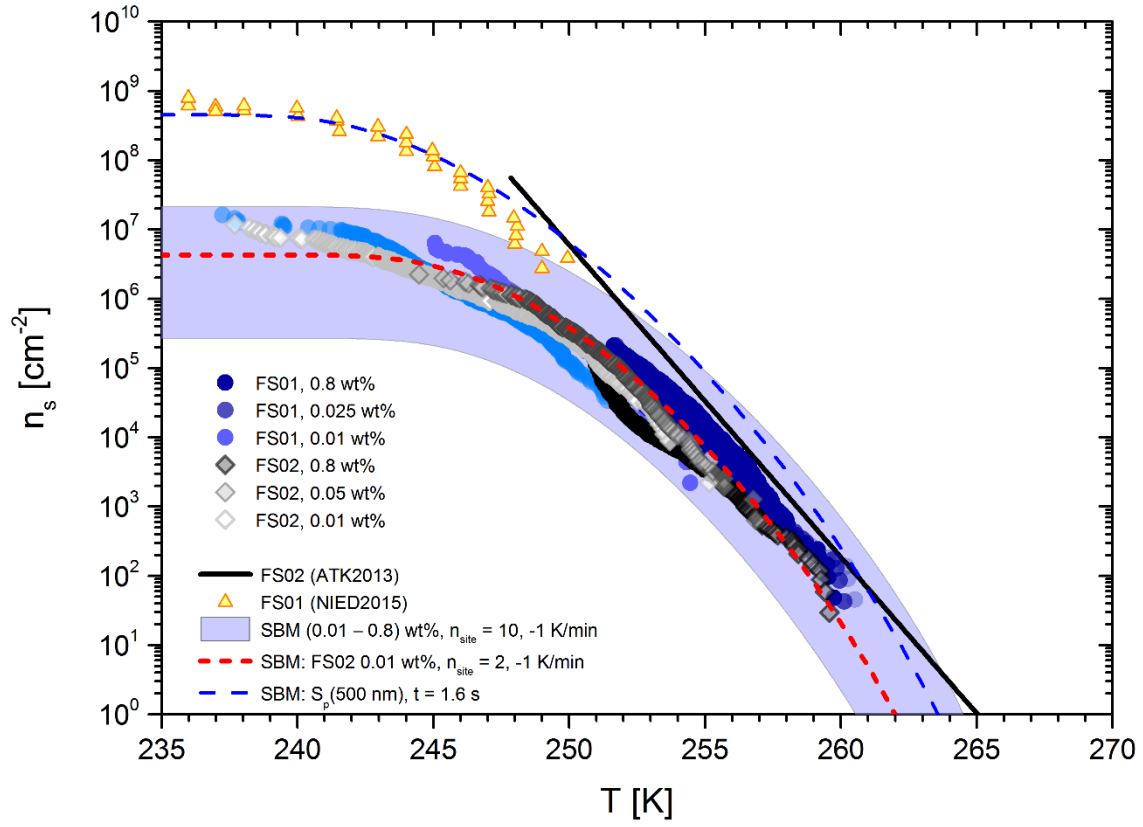
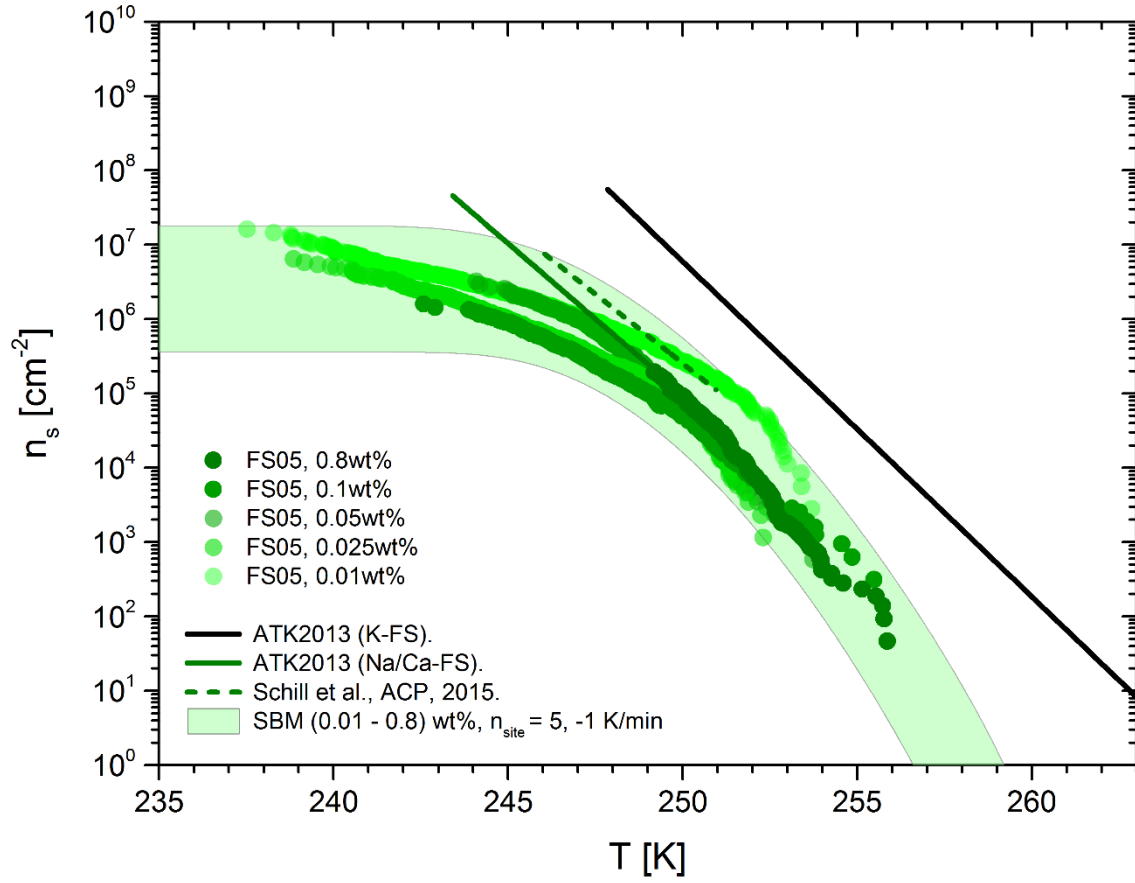


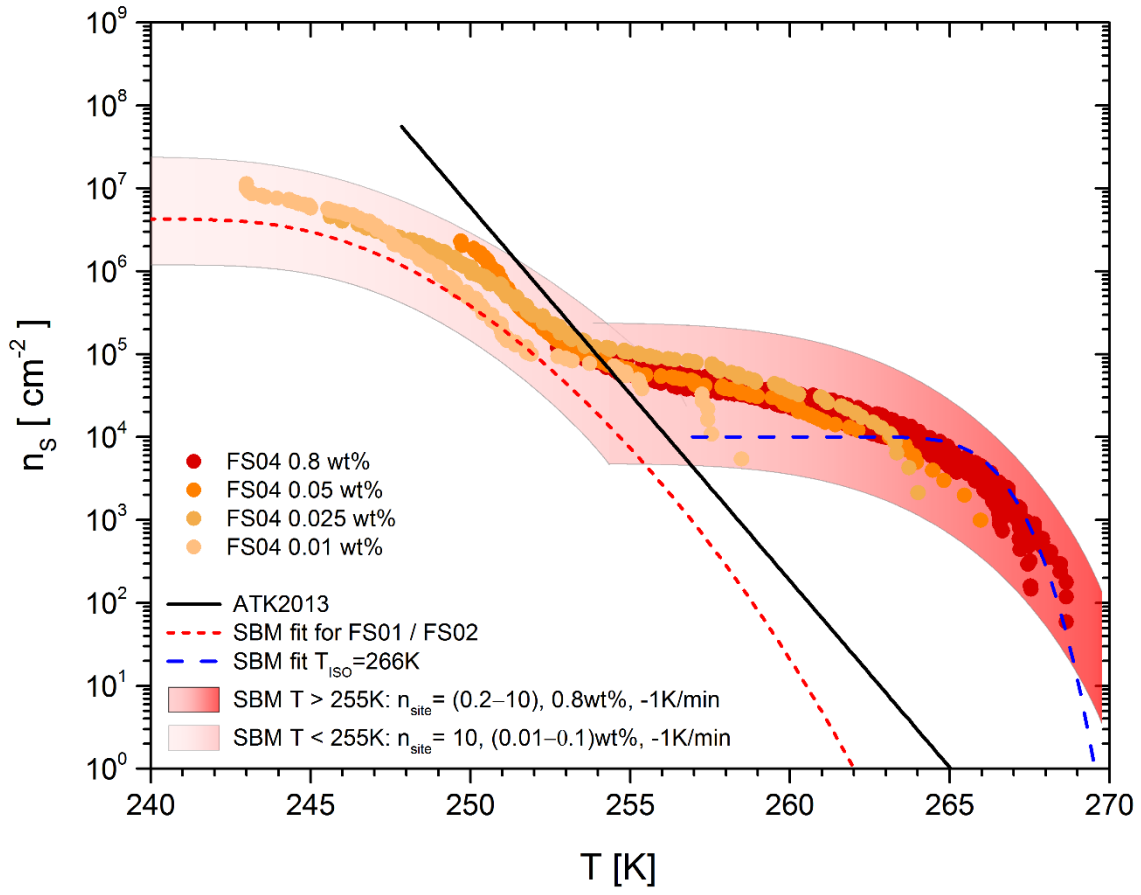
Figure 9: $n_s(T)$ curves of K-feldspar particles FS01 and FS02. Shaded area shows the range of $n_s(T)$ values predicted by equation 4 with fixed parameter set $\mu_\theta = 1.32$ rad, $\sigma_\theta = 0.1$ rad, $n_{\text{site}} = 10$, and suspension between 0.01 wt% and 0.8 wt%. Red broken line corresponds to the best fit parameter set for FS02 (Table 2A) with 0.01 wt% and $dT/dt = -1\text{K/min}$. The blue broken line is calculated with the same parameter set but assuming a single FS01 particle with Stokes diameter 500 nm per droplet and fixed temperature lasting for 1.6 sec (LACIS conditions) instead of constant cooling rate.



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Figure 10: $n_s(T)$ curves of Na/Ca-feldspar suspensions FS05. Shaded area shows the range of $n_s(T)$ values predicted by equation (4) with fixed fit parameter set $\mu_\theta = 1.33 \text{ rad}$, $\sigma_\theta = 0.102 \text{ rad}$, $n_{site} = 5$, and concentration of feldspar suspensions varied between 0.01 wt% and 0.8 wt%. Black and green solid lines are exponential fits of data from ATK2013 for K-rich and Na/Ca-rich feldspar suspension droplets, respectively.

10



5 **Figure 11:** $n_s(T)$ curves of K-feldspar particles (FS04). Shaded areas shows the range of $n_s(T)$ values (for details see text). Black solid line is a fit of data from ATK2013 for FS02. Red broken line is a fit to our FS02 data (as in Fig. 9). Blue broken line is the $n_s(T)$ curve predicted by Eq. (4) with parameters obtained from the isothermal freezing experiments (Table 2B).

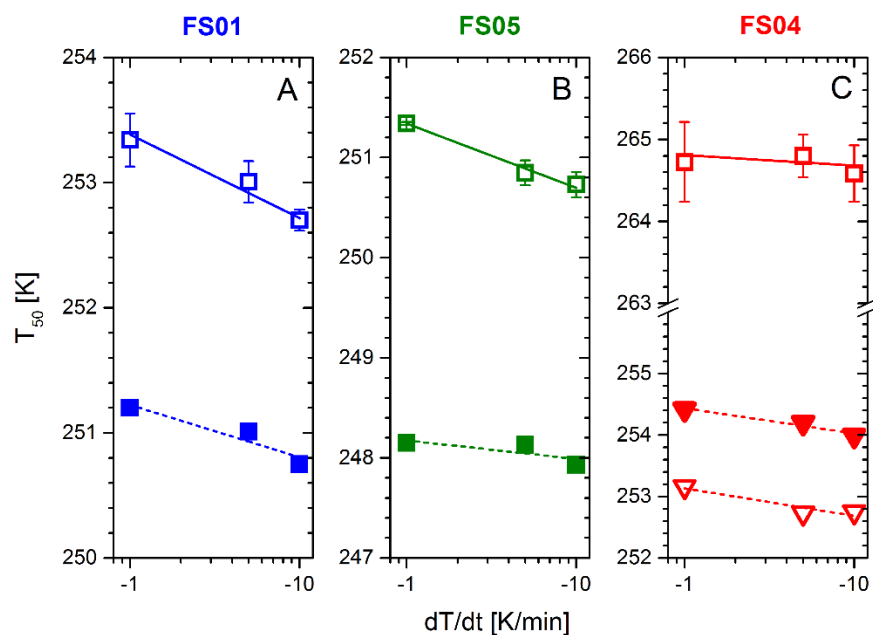
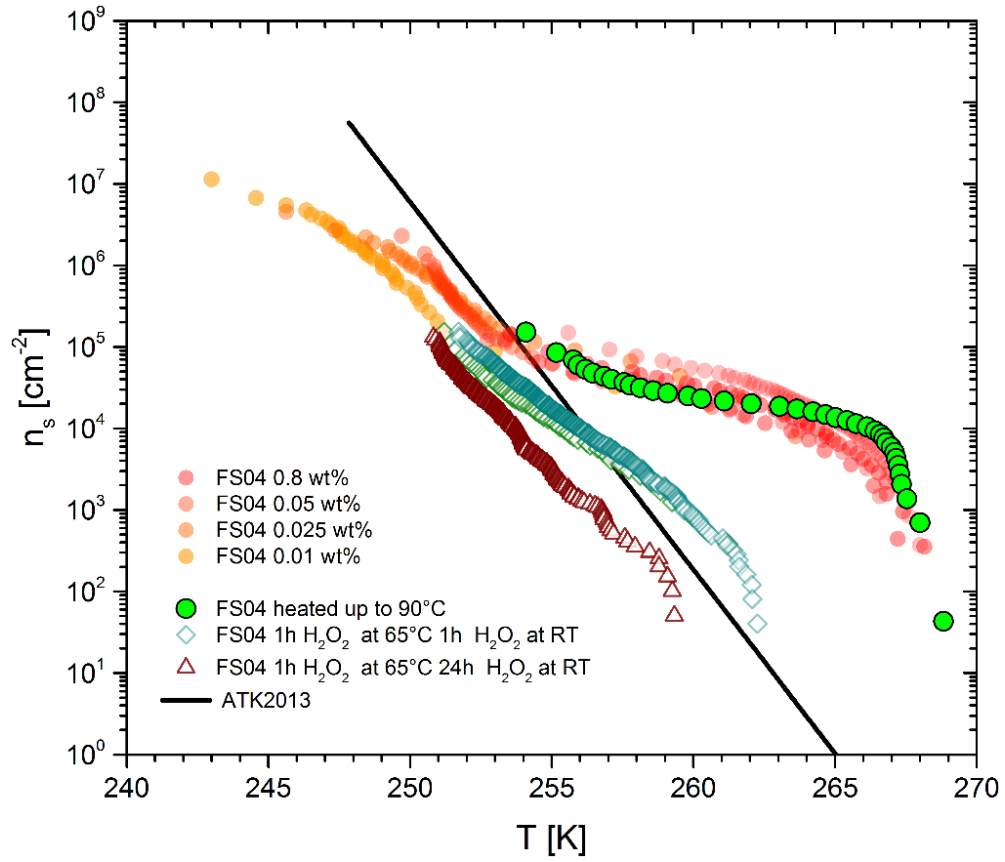


Figure 12: A, B) Median freezing temperature $T_{0.5}$ for the aqueous suspensions of FS01 und FS05 aged for over five months (blue and green filled symbols). C) Median freezing temperature $T_{0.5}$ of FS04 0.8 wt% suspension treated with 30% H_2O_2 for an hour (filled triangles) and overnight (open triangles). $T_{0.5}$ for the freshly prepared suspensions is shown as open square symbols in all three panels. Straight lines are non-weighted linear regressions of the averaged $T_{0.5}$ values for three different cooling rates.



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Figure 13: $n_s(T)$ curves of K-feldspar particles (FS04) after heating to 90°C and chemical treatment with hydrogen peroxide.